

# Reconstruction of $\tau$ using impact parameters

*e.g.*  $e^+ e^- \rightarrow (H \rightarrow \tau \tau) (Z \rightarrow \mu \mu)$



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## Some tau decay modes:

Simplest case

$$\sim 11\% \tau^+ \rightarrow \pi^+ \nu$$

Largest BR

$$\sim 25\% \tau^+ \rightarrow \pi^+ \pi^0 \nu$$

Leptonic

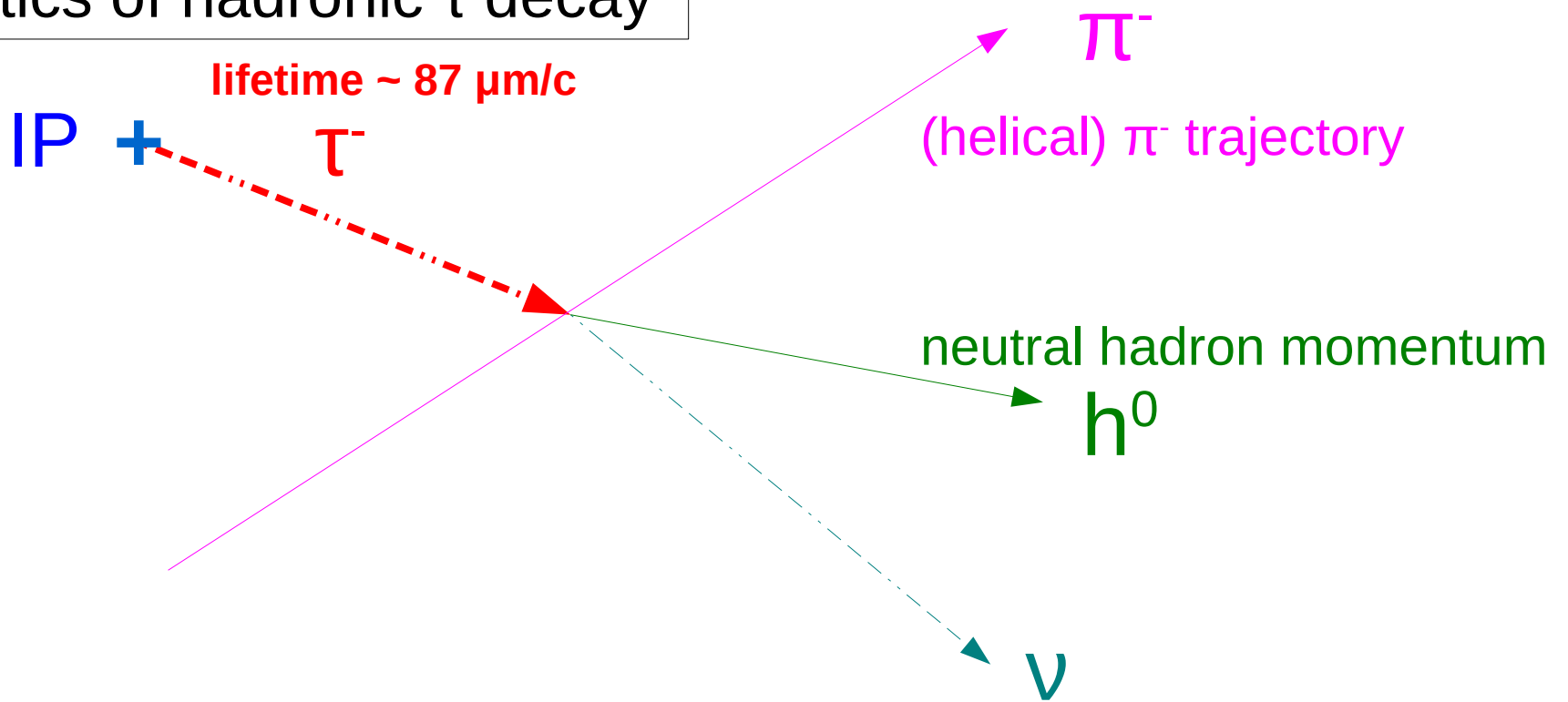
$$\sim 35\% \tau^+ \rightarrow (e/\mu)^+ \nu \nu$$

two missing neutrinos  $\leftarrow$  limited information, ignore for now

We would ideally like to fully reconstruct the  
tau momentum and its decay products

However,  $\tau$  always decays into at least one neutrino

# kinematics of hadronic $\tau$ decay



————— measured  
- - - - - un-measured

To optimally use events with taus,  
want to fully reconstruct the  $\tau$   
how to reconstruct the invisible neutrino momentum?

traditional method

e.g. LEP, BELLE, ...

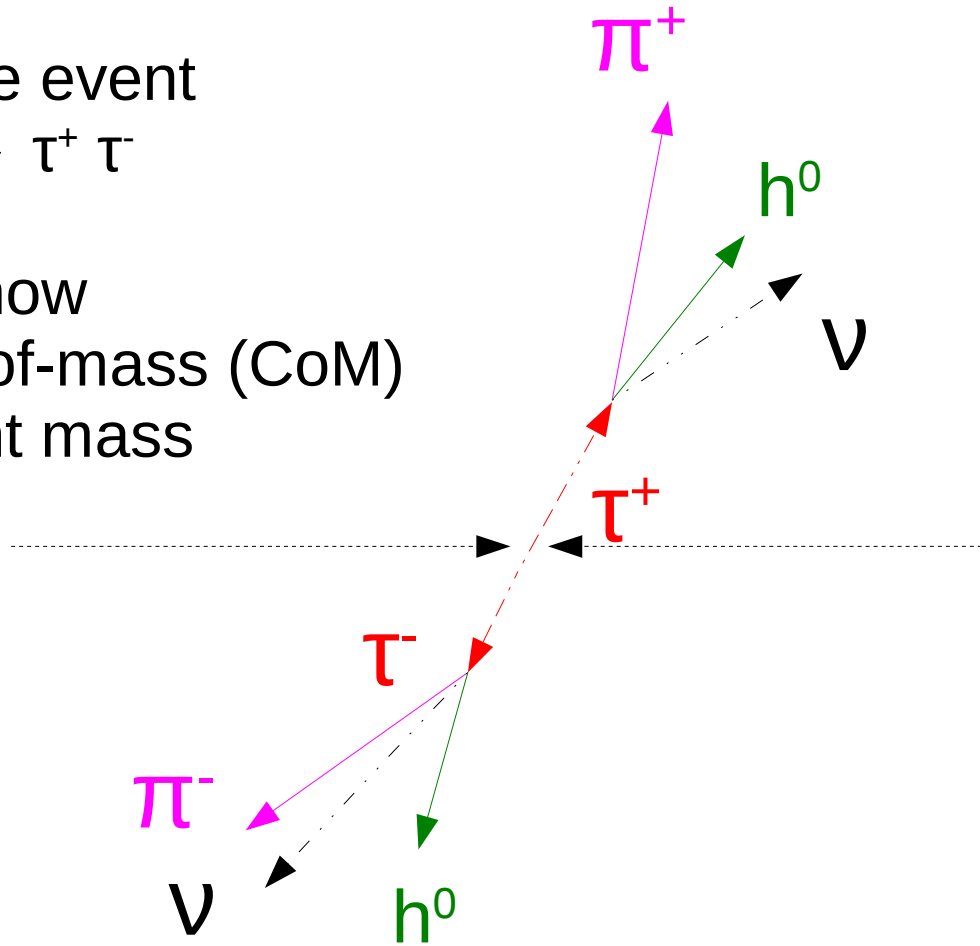
consider whole event

e.g.  $e^+ e^- \rightarrow \tau^+ \tau^-$

assume we know

$\tau$ - $\tau$  centre-of-mass (CoM)

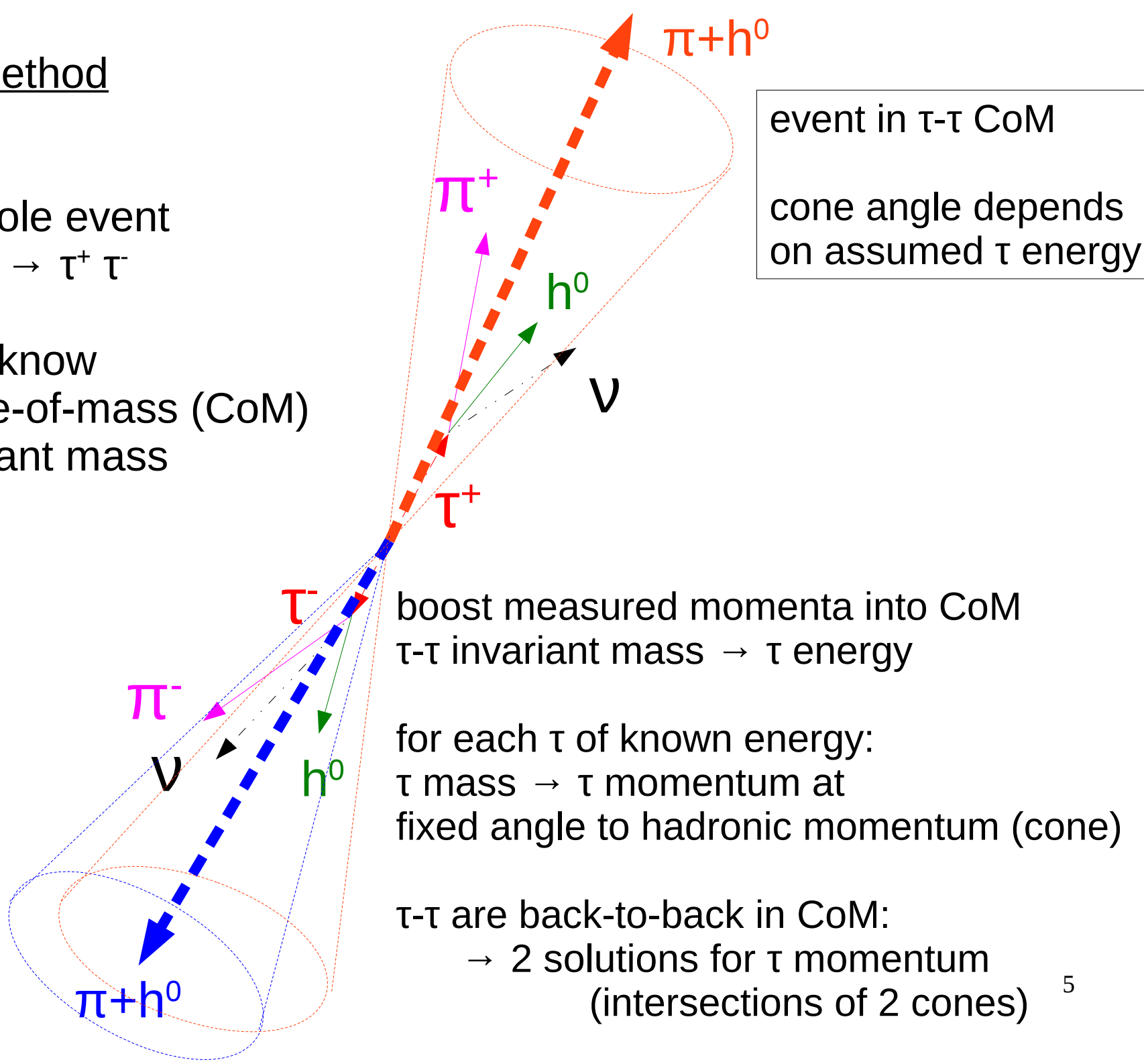
$\tau$ - $\tau$  invariant mass



traditional method

consider whole event  
e.g.  $e^+ e^- \rightarrow \tau^+ \tau^-$

assume we know  
 $\tau$ - $\tau$  centre-of-mass (CoM)  
 $\tau$ - $\tau$  invariant mass

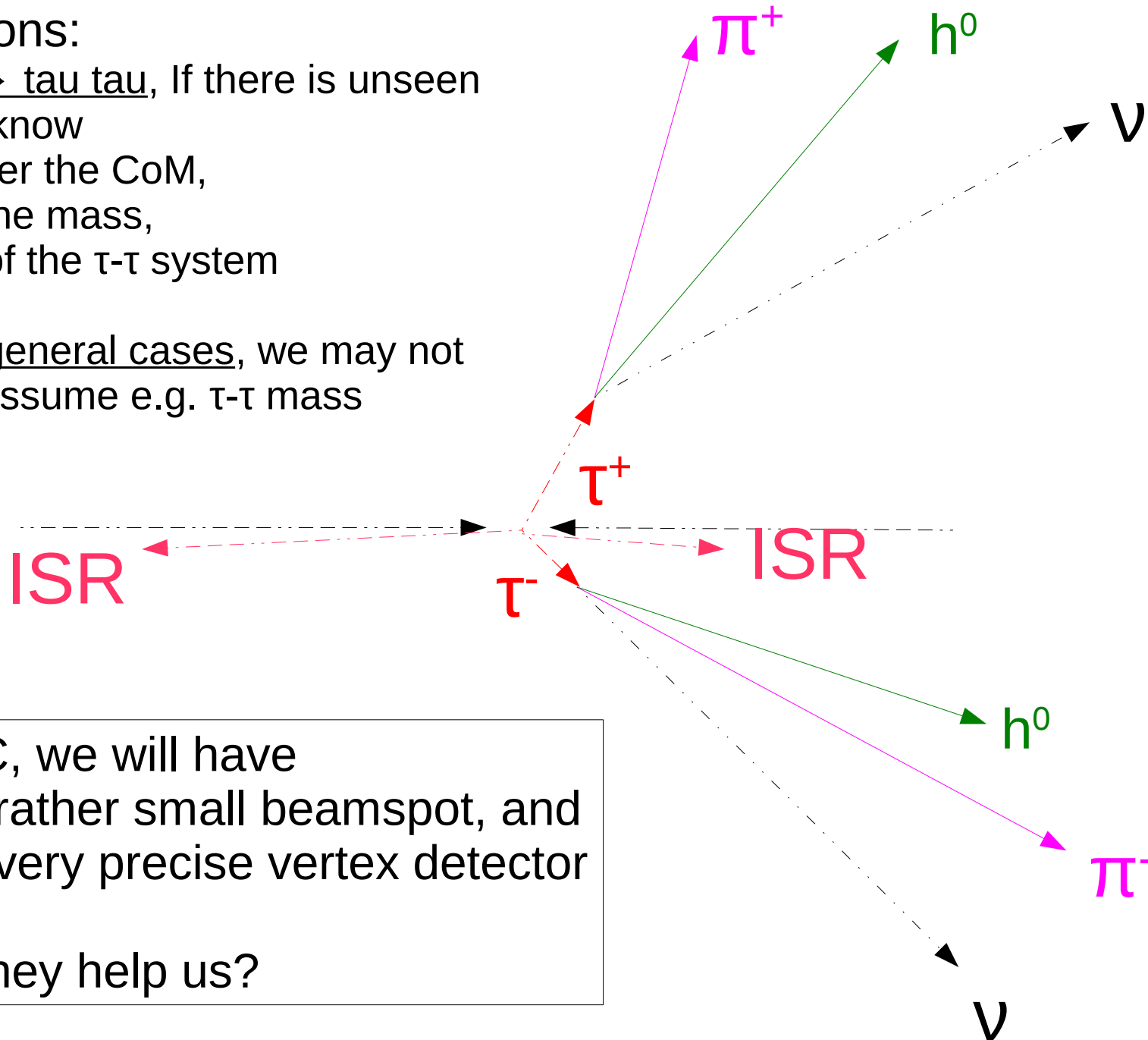


## traditional method

### Limitations:

in  $e^+e^- \rightarrow \tau\tau$ , If there is unseen ISR, we know  
neither the CoM,  
nor the mass,  
of the  $\tau$ - $\tau$  system

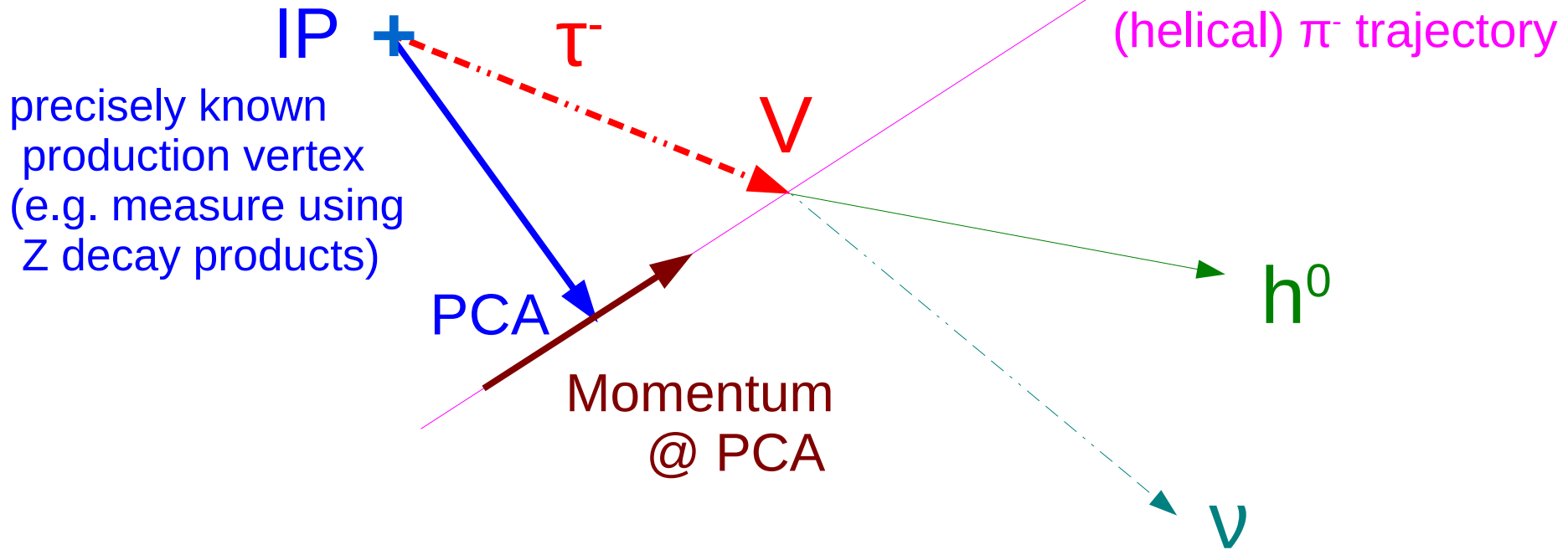
in more general cases, we may not  
want to assume e.g.  $\tau$ - $\tau$  mass



at ILC, we will have  
a rather small beamspot, and  
a very precise vertex detector

can they help us?

# kinematics of $\tau$ decay



assume that  $\pi/\tau$  trajectory is approx linear between PCA/IP and V  
 OK since typical radius of curvature  $\gg$   $\tau$  decay length

measured “track plane” defined by IP-PCA and Mom@PCA  
 (these two vectors are perpendicular)

-  $\tau$  momentum lies inside track plane (linear approx.)

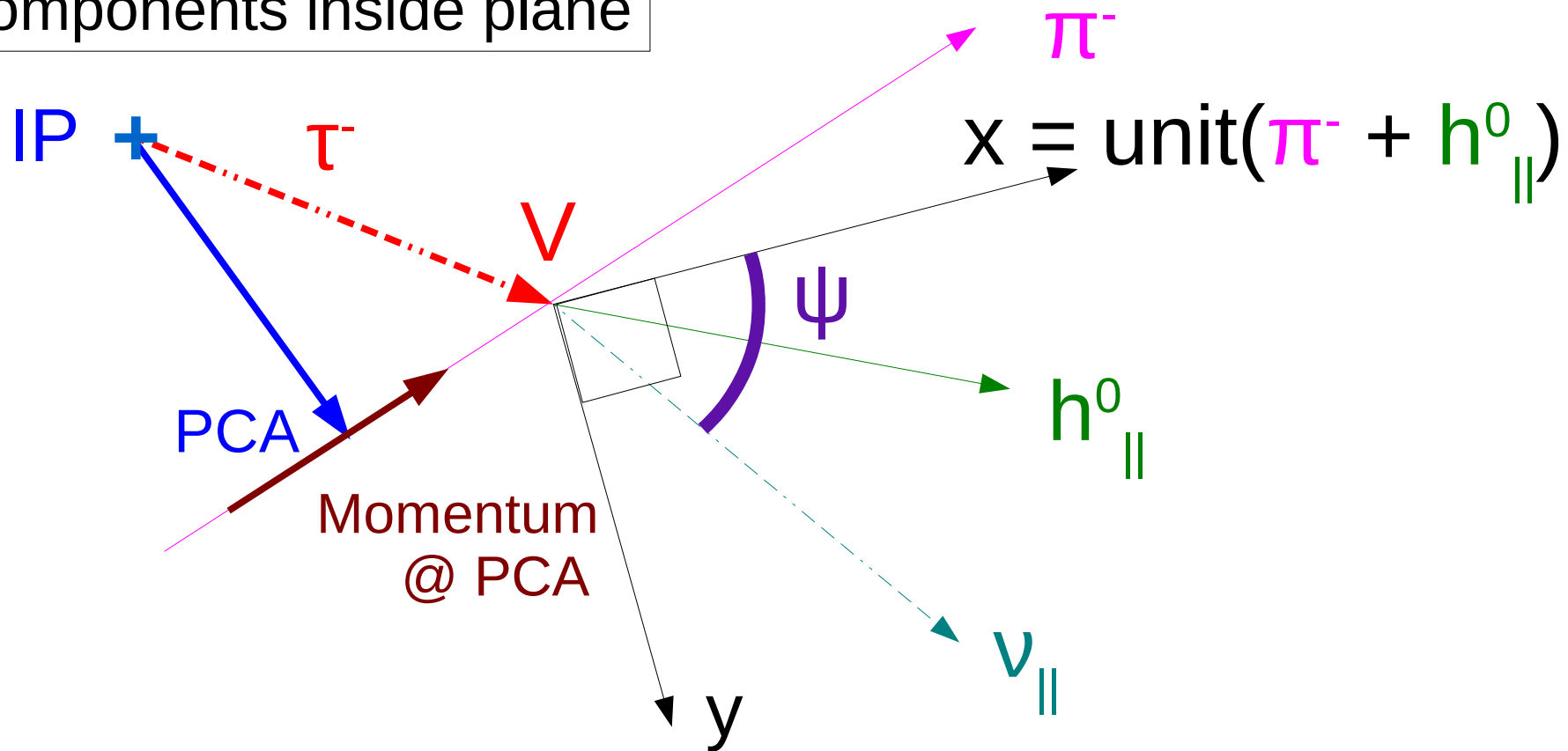
→ ( $h^0 + \nu$ ) momentum lies in track plane

→  $\nu$  momentum out of plane = -  $h^0$  momentum out of plane

$\nu_{\text{perp}}$

= -  $h^0_{\text{perp}}$

only components inside plane



parameterise  $v$  momentum inside plane

$x$  is unit vector parallel to hadronic momentum inside plane

$y$  is unit vector in plane, perpendicular to  $x$

$Q$  is magnitude of momentum in plane

$$v_{||} = Q ( x \cos \psi + y \sin \psi )$$



So we can write the neutrino momentum as

$$\mathbf{v} = Q ( x \cos \psi + y \sin \psi ) - h_{\text{perp}}^0$$

two unknown parameters,  $Q$  and  $\psi$

4-momentum of  $\tau = \pi + h^0 + \mathbf{v}$

invariant mass of  $\tau$  is well-known

→ for each choice of  $\psi$  can calculate  $Q$  (2 solutions)

→ calculate full kinematics of  $\tau$  for an assumed  $\psi$   
including lifetime

often one solution gives a negative lifetime,  
and can be rejected

we have reduced the problem of finding  $\mathbf{v}$  momentum to:

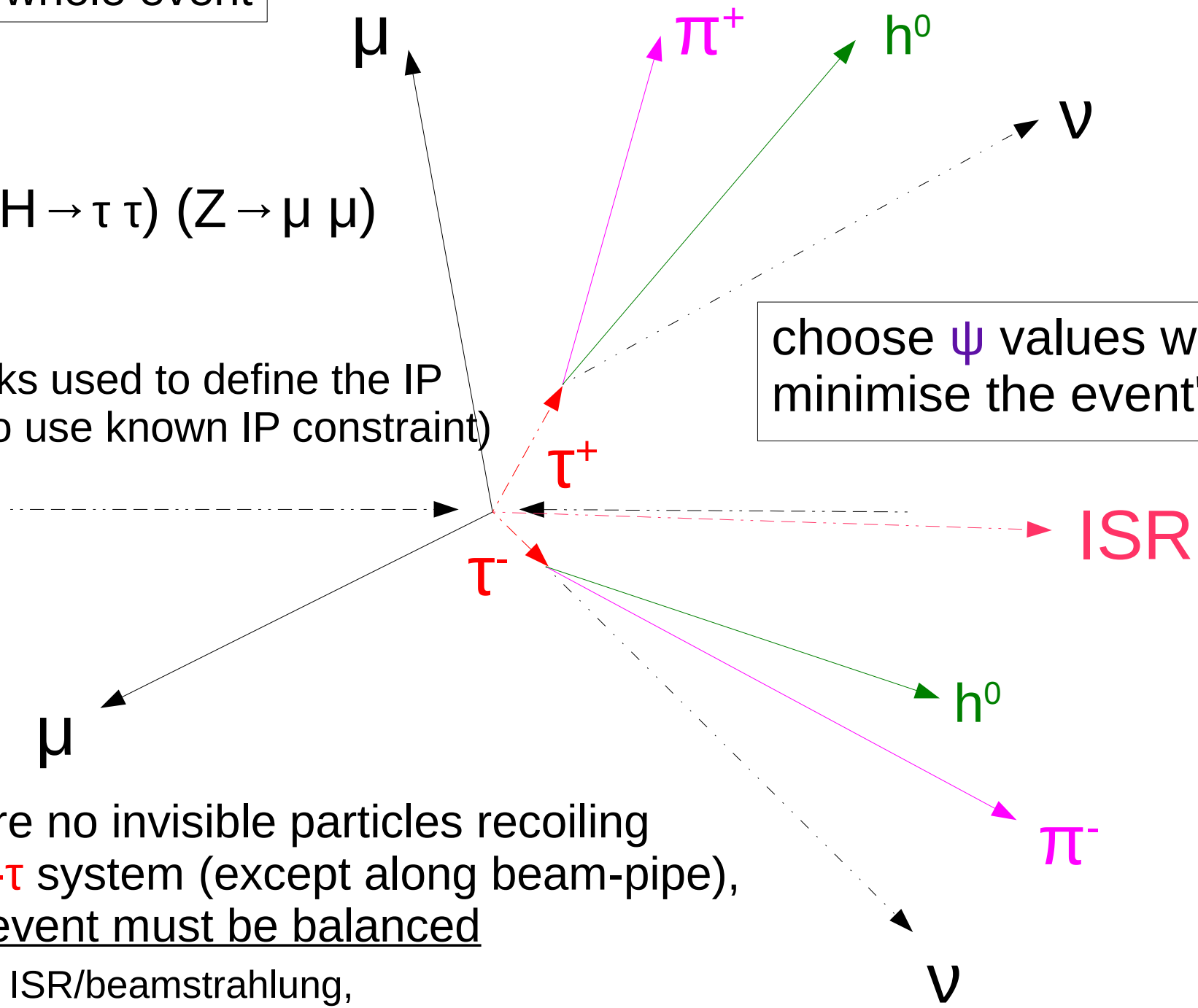
HOW TO CHOOSE  $\psi$  ?

consider whole event

e.g.  
 $e^+ e^- \rightarrow (H \rightarrow \tau \tau) (Z \rightarrow \mu \mu)$

muon tracks used to define the IP  
(could also use known IP constraint)

choose  $\psi$  values which  
minimise the event's  $p_T$



If there are no invisible particles recoiling  
against  $\tau$ - $\tau$  system (except along beam-pipe),  
 $p_T$  of event must be balanced

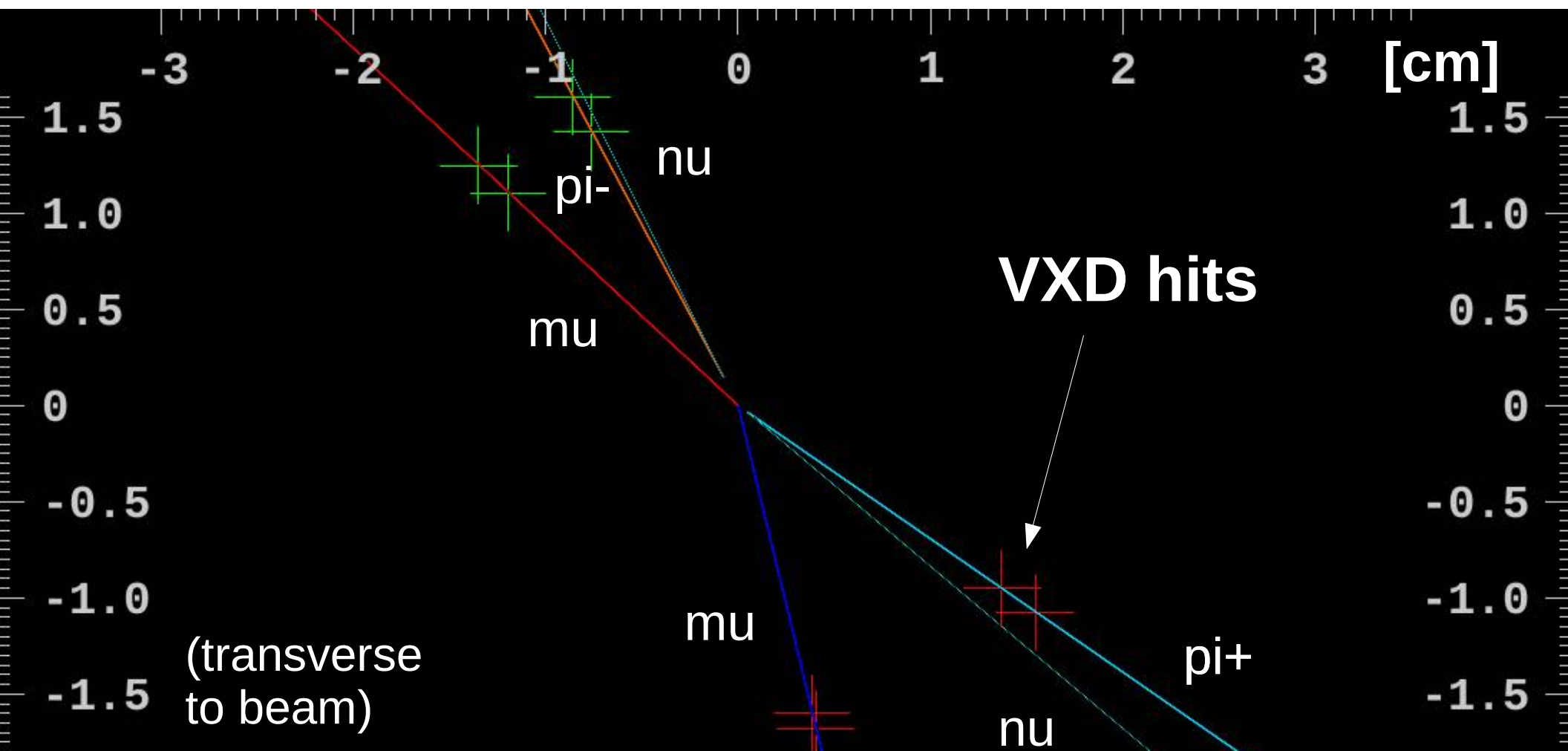
because of ISR/beamstrahlung,  
don't make requirements on  $p_z$

$e^+ e^- \rightarrow H \mu^+ \mu^-$  events generated @ 250 GeV Whizard with CIRCE1 ISR/BS  
 $H \rightarrow \tau\tau$ ;  $\tau$  decayed by TAUOLA: either both  $\pi^+\nu$  or both  $\pi^+\pi^0\nu$  ( $\rho\nu$ )

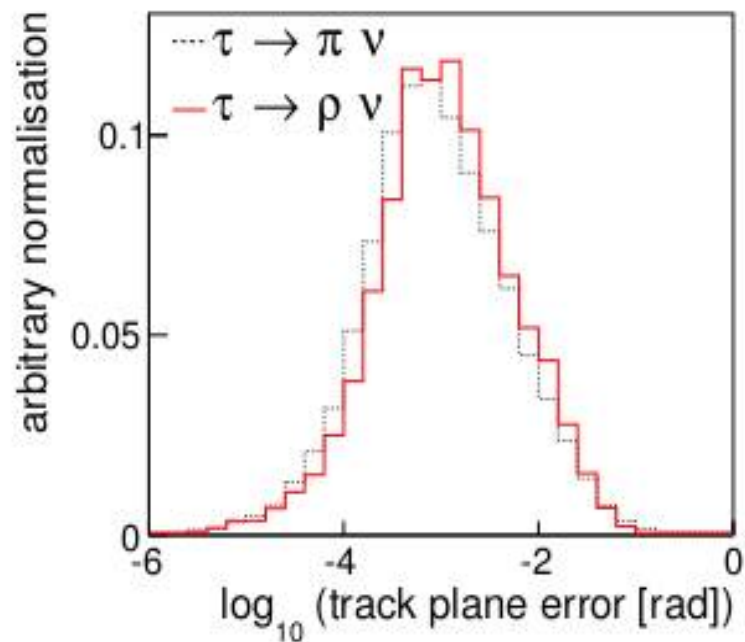
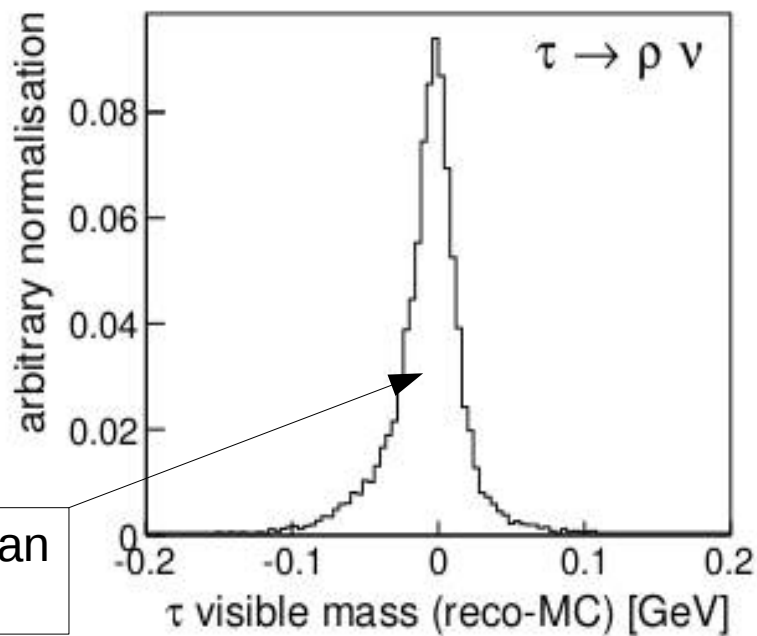
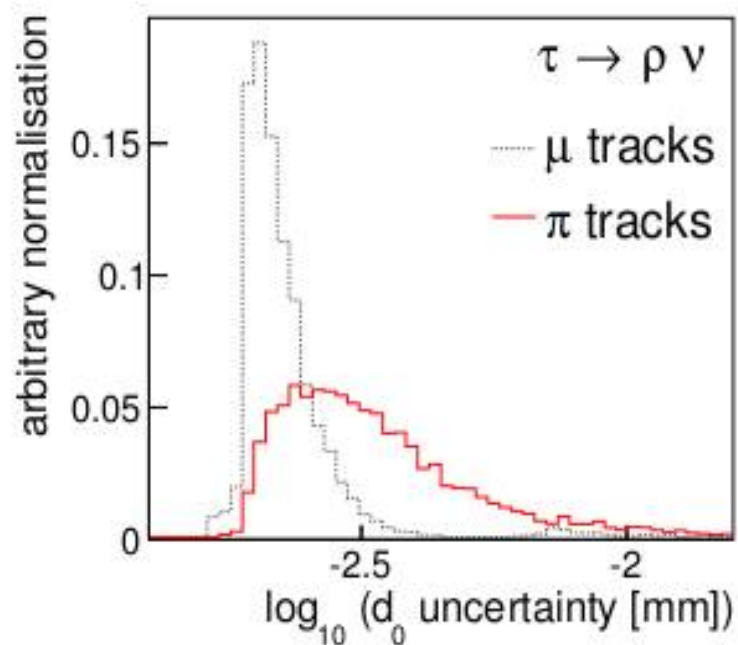
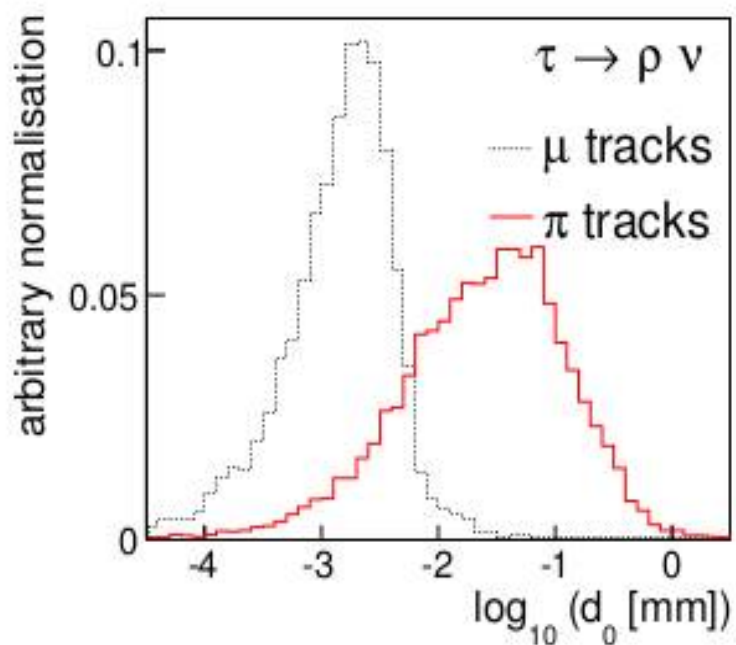
Full ILD simulation, DBD version ILD\_v05\_o1

Usual ILD reconstruction + GARLIC, no underlying event overlay

Cheat matching of GARLIC/Pandora clusters to  $\pi^0$ , and of  $\pi^0 \pi^+$  to  $\tau$   
apply  $\pi^0$  mass constraint to two photon system

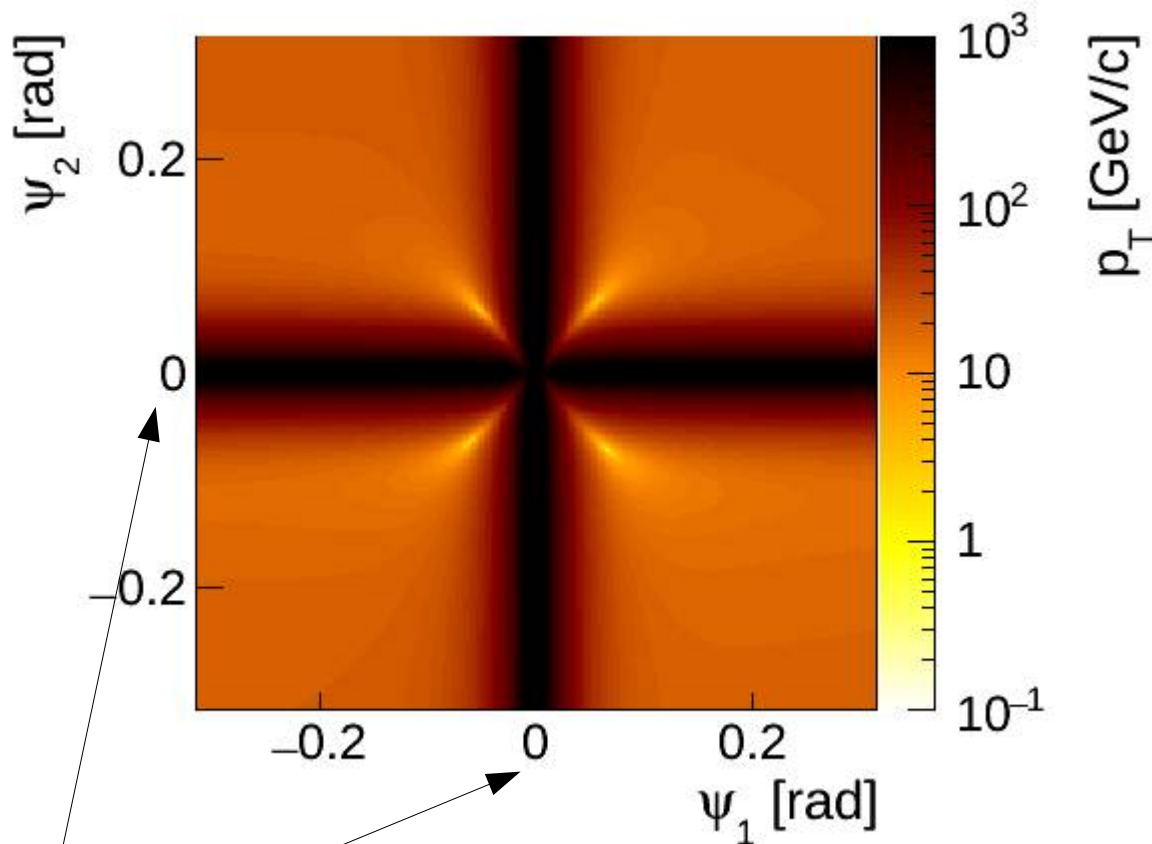


# Track and pi0 reconstruction



smaller than  $\rho$  width

How does event  $p_T$  depend on  $\psi$  chosen for two taus?



one event @ 250 GeV  
 $e^+e^- \rightarrow (H \rightarrow \tau\tau) (Z \rightarrow \mu\mu)$

both  $\tau \rightarrow \pi \nu$

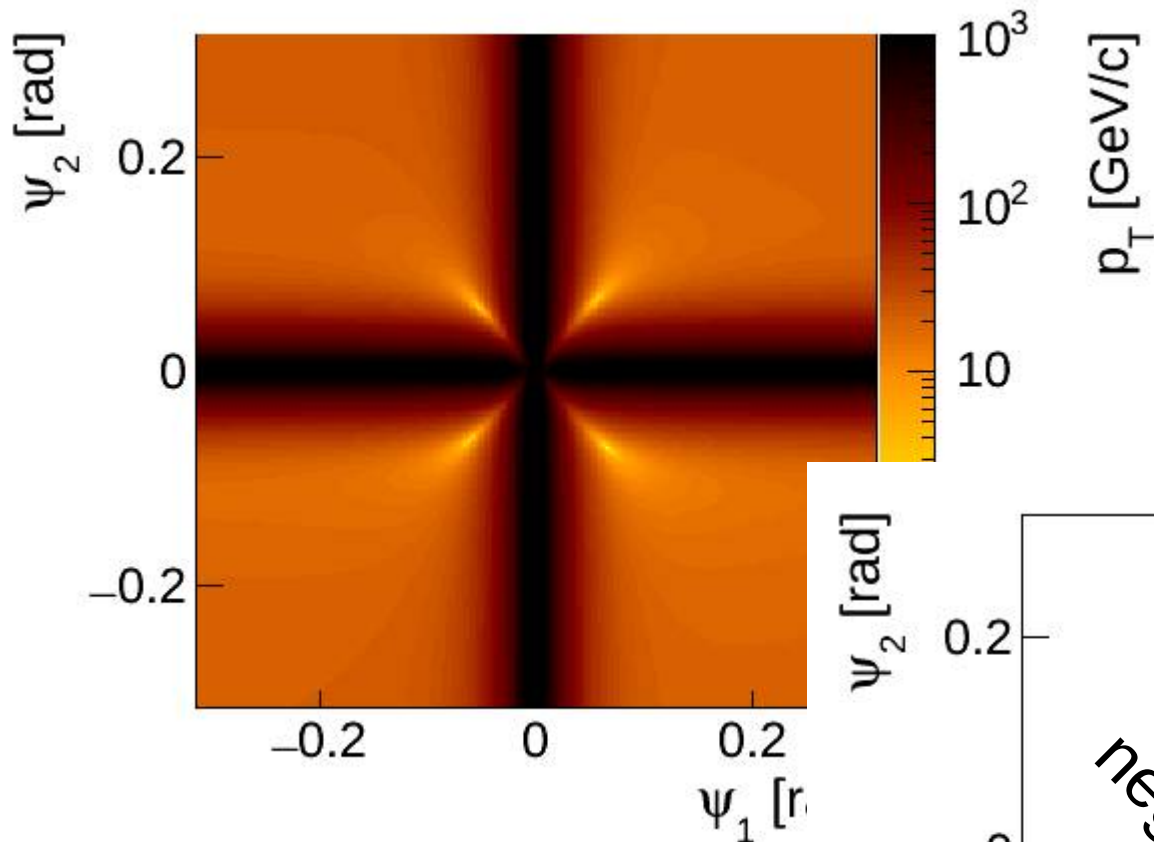
**simulated and  
reconstructed in ILD**

neutrino co-linear  
with hadrons in  
track plane

Four possible solutions with small  $p_T$   
easy to find minima using e.g. MINUIT

how to choose which one?

How does event  $p_T$  depend on  $\psi$  chosen for two taus?



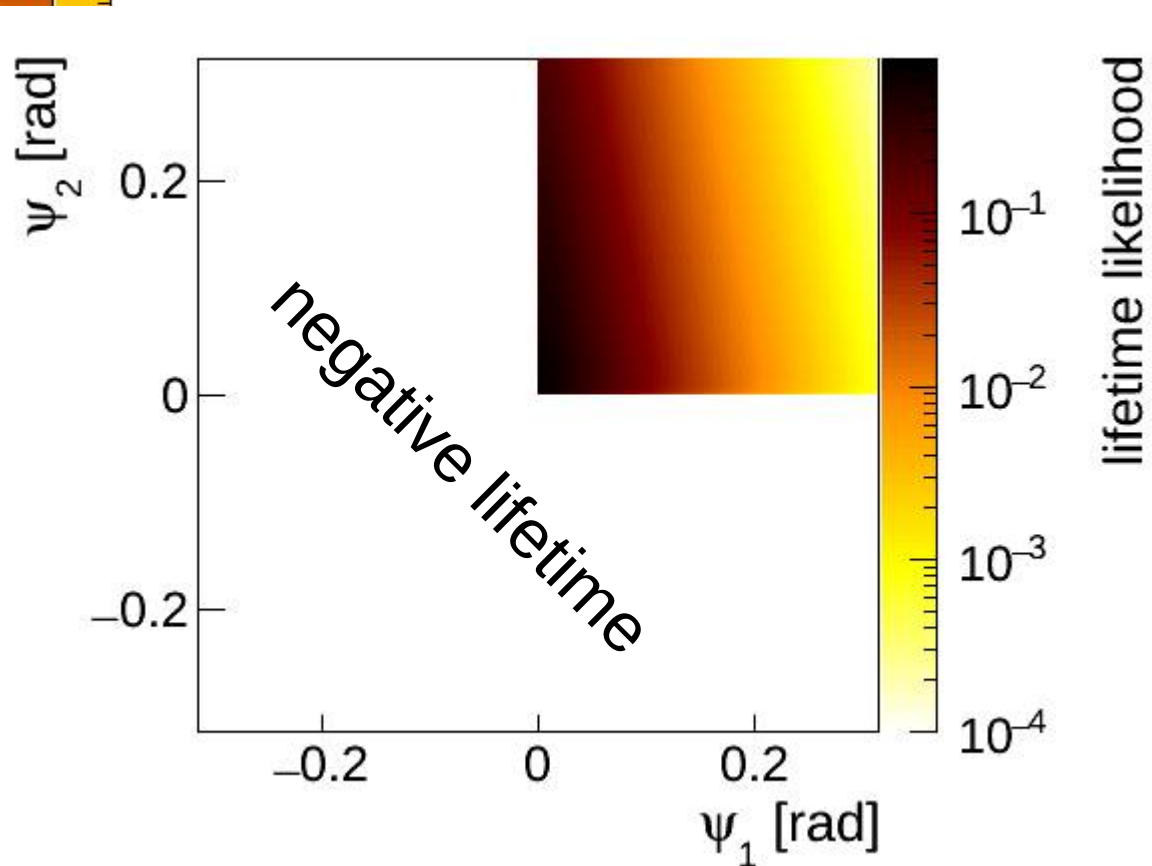
lifetime likelihood

$$\exp\left\{ - \frac{\text{candidate lifetime}}{\text{mean tau lifetime}} \right\}$$

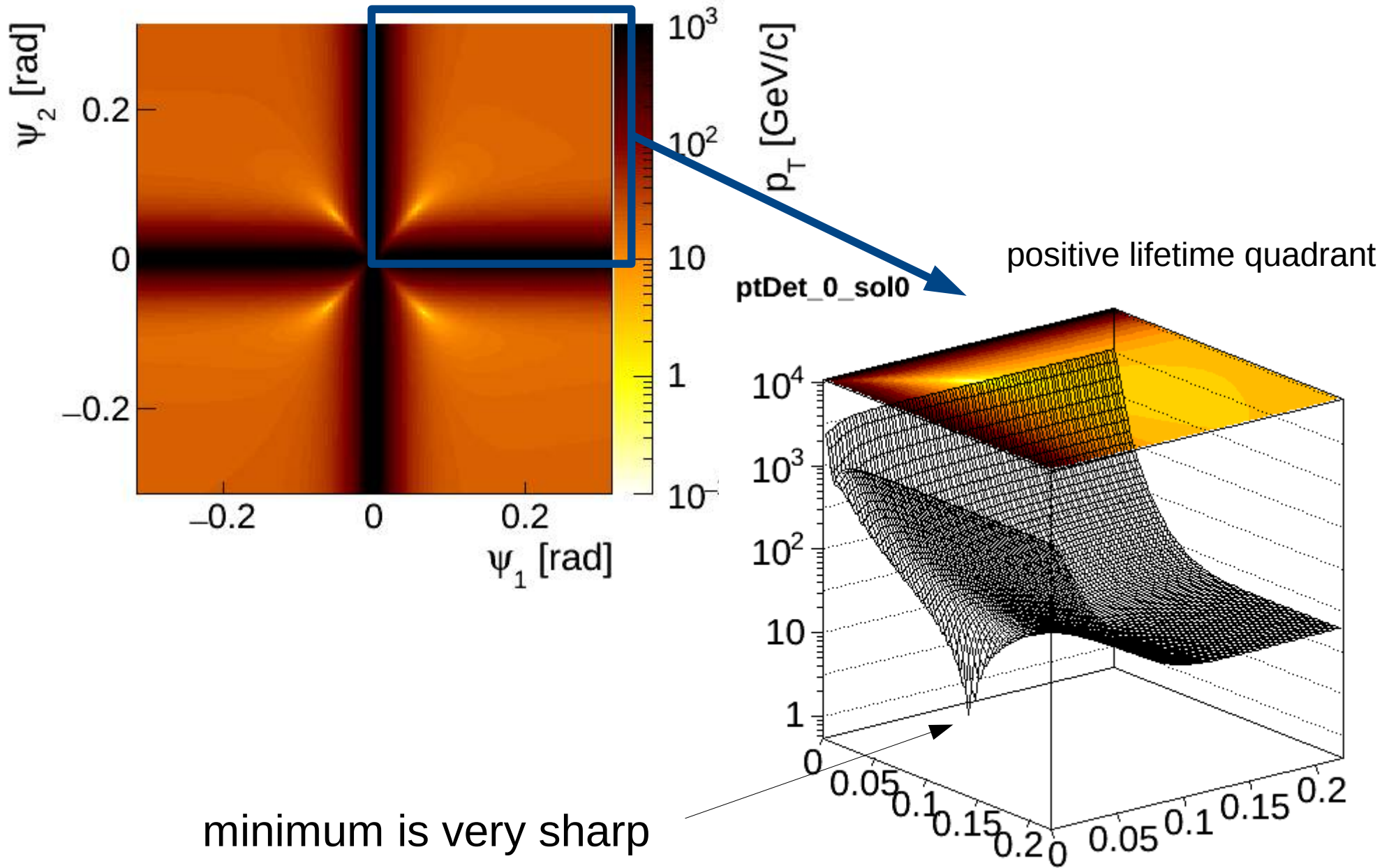
for positive candidate lifetime,

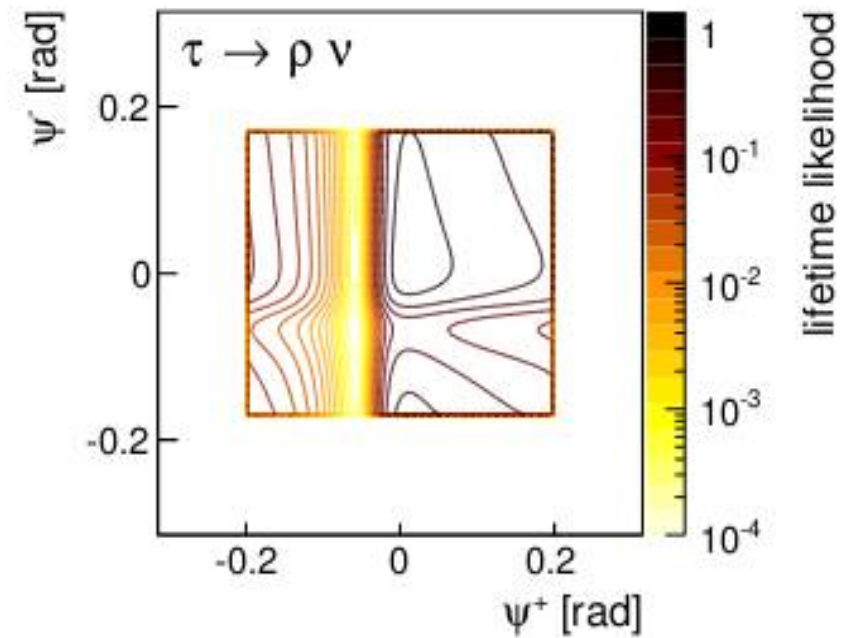
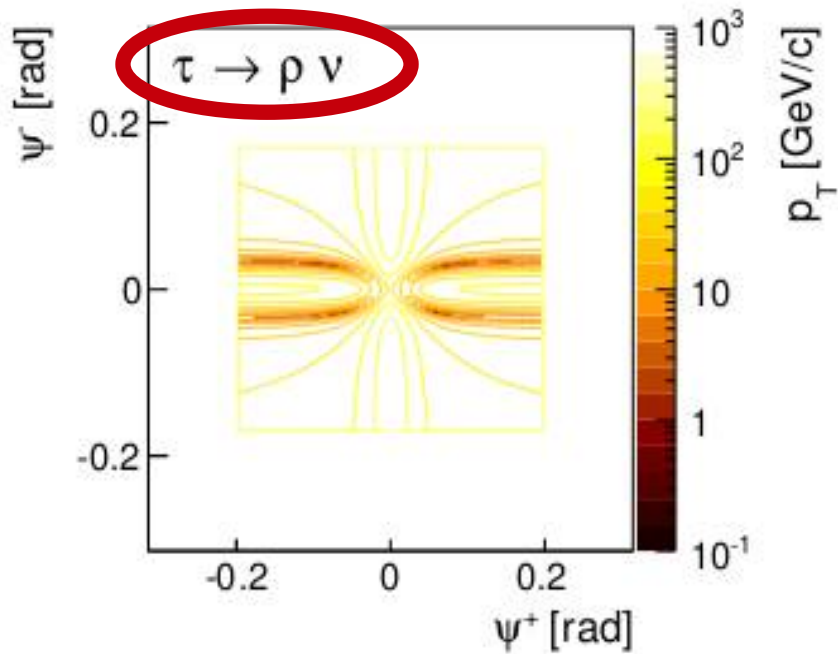
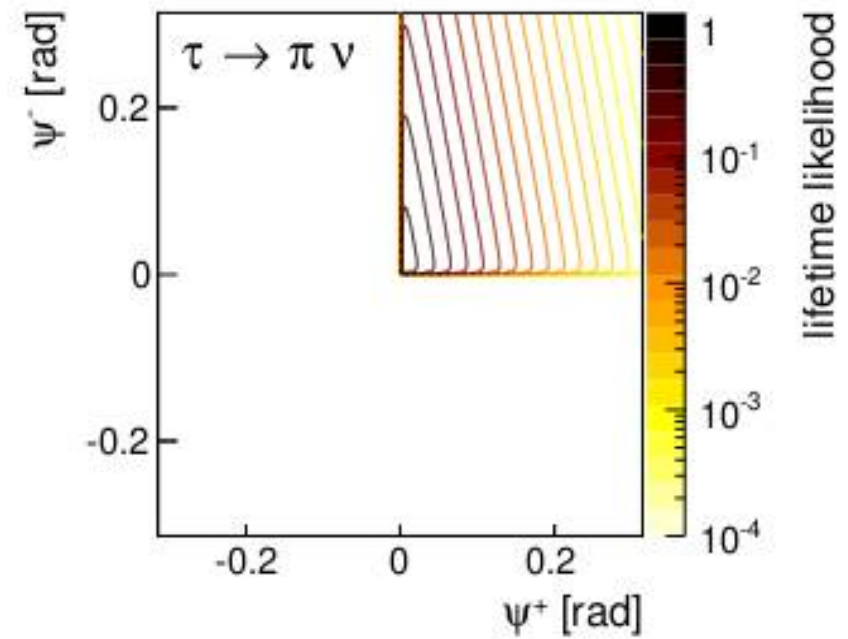
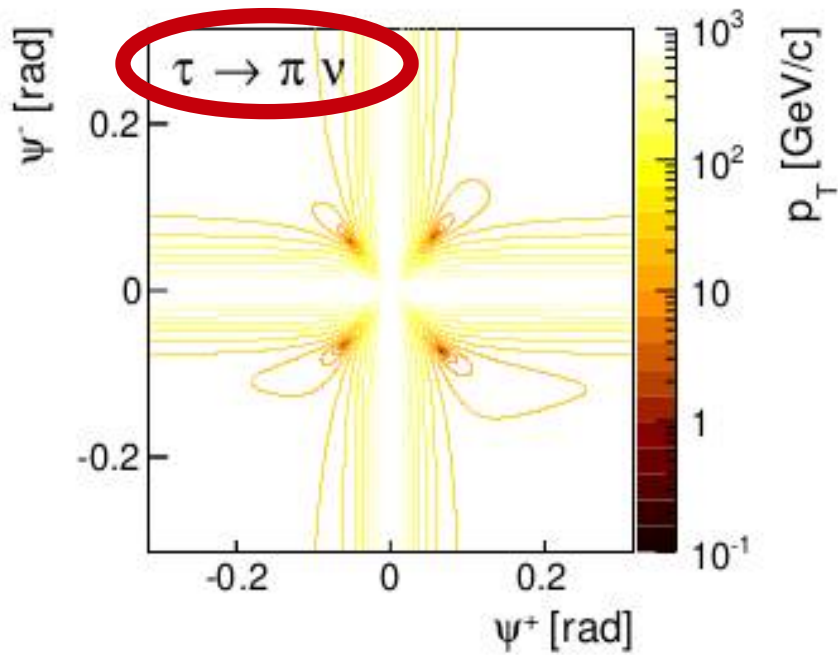
0 for negative lifetime

look at reconstructed  
tau lifetimes  
of each solution



How does event  $p_T$  depend on  $\psi$  chosen for two taus?



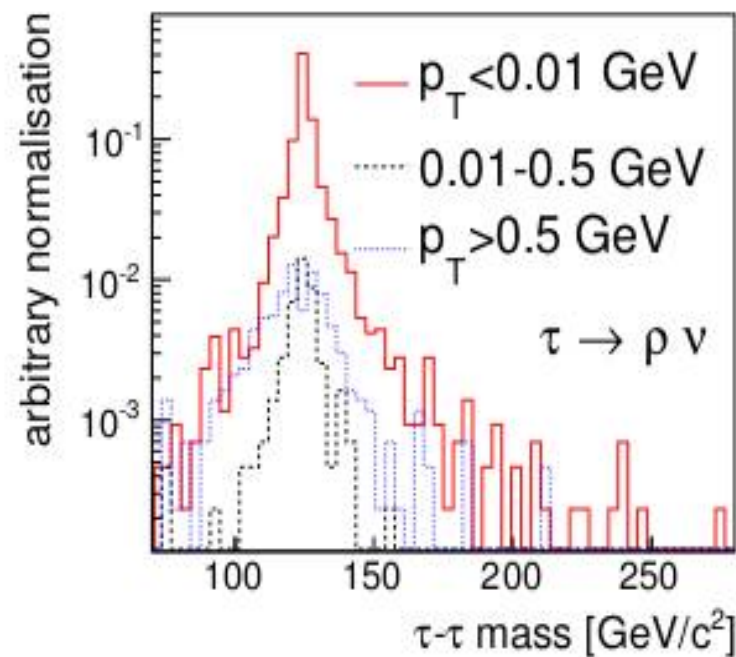
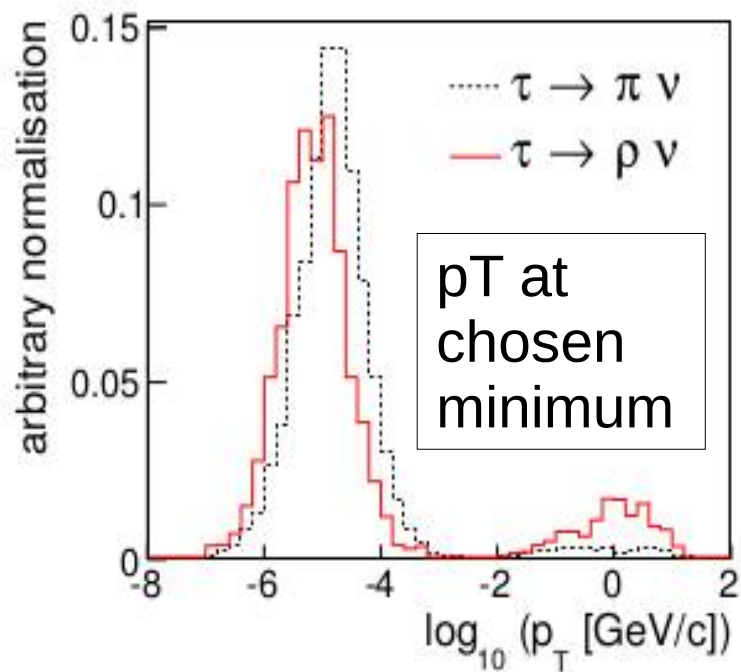


For now, choose smallest  $p_T$  minimum with positive decay length

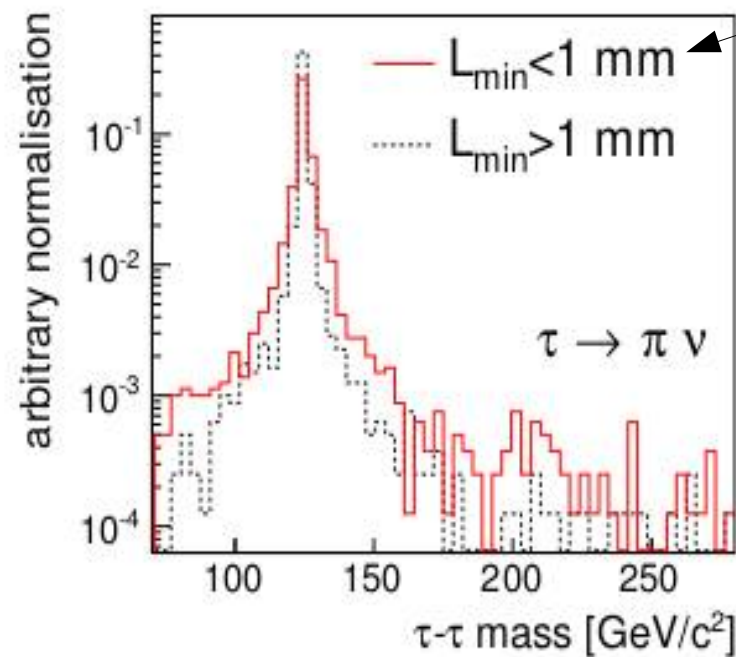
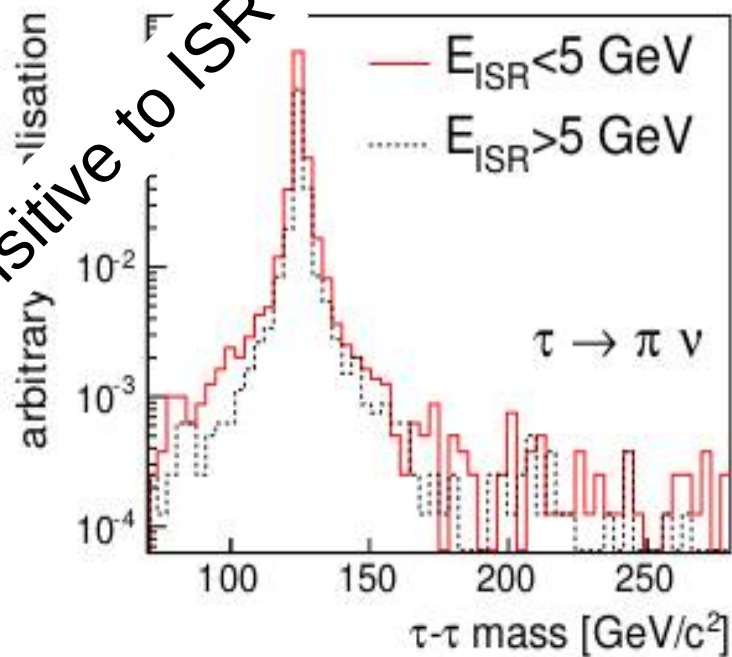


How well does it work?

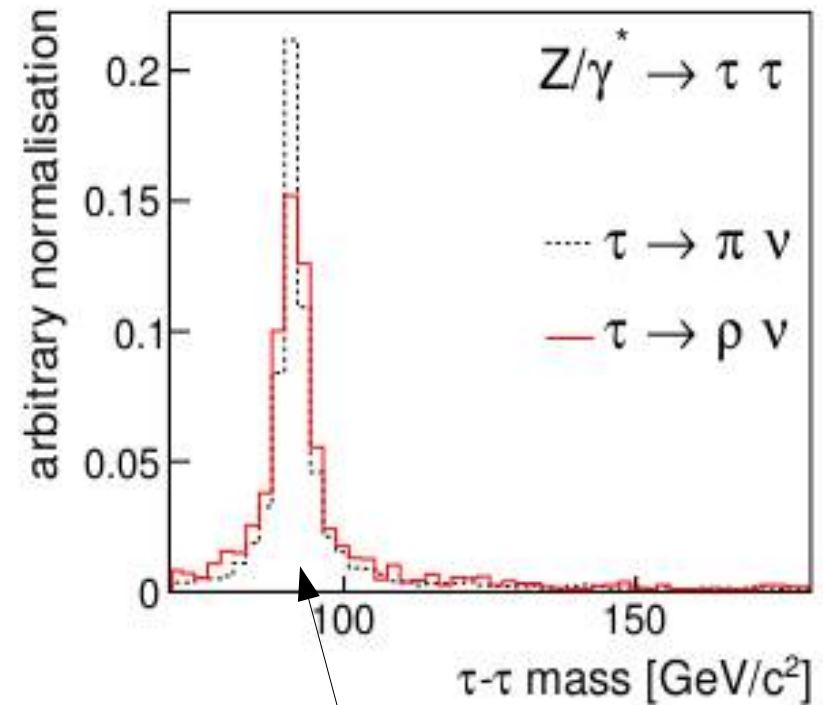
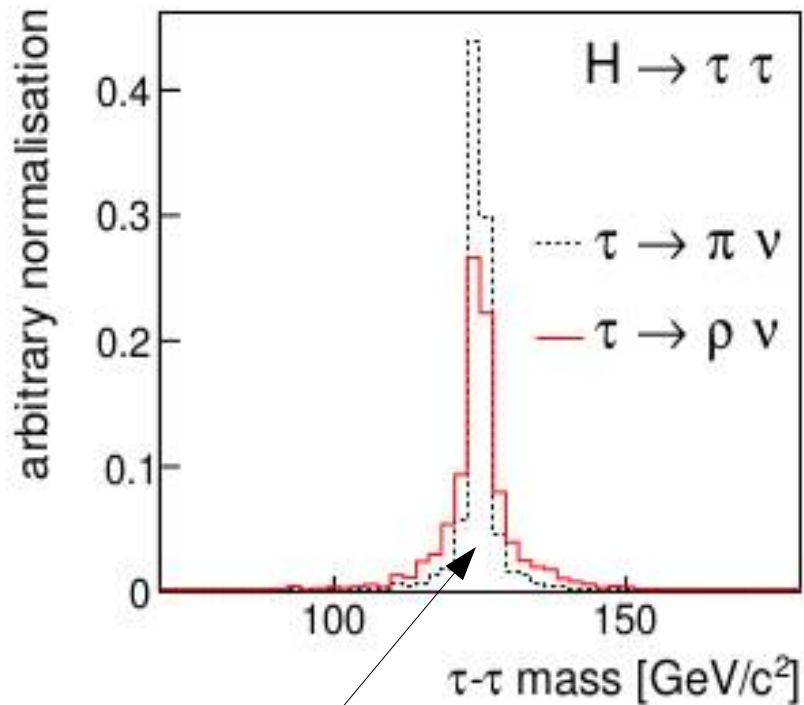
Check the invariant mass of  $\tau$  system: should be 125 GeV



insensitive to ISR



unlucky taus



width of central peak  
 $\sim 0.6 \text{ GeV}$  for  $\pi^+\nu$   
 $\sim 1.1 \text{ GeV}$  for  $\pi^+\pi^0\nu$

95% of  $\pi^+\nu$   
 89% of  $\pi^+\pi^0\nu$   
 within 10 GeV of peak

easily distinguished from Z

## Summary

reconstruction method for hadronic tau decays works well @ ILC

requires good IP reconstruction and impact parameter resolution of order 10 microns (interesting to exactly how good it needs to be)

insensitive boost along beam axis

- ISR, beamstrahlung OK, HZ above threshold OK
- in principle, also applicable to hadron collider experiments
  - if impact parameter resolution sufficiently good
  - if IP can be measured

Paper submitted to NIM-A (arXiv:1507.01700)

Now working on removing cheating (associating tracks, clusters to taus)  
then use tau spins to measure Higgs CP