

Reconstruction of τ using impact parameters

e.g. $e^+ e^- \rightarrow (H \rightarrow \tau \tau) (Z \rightarrow \mu \mu)$



Daniel Jeans
U. Tokyo

September 2015

Some tau decay modes:

Simplest case

$$\sim 11\% \tau^+ \rightarrow \pi^+ \nu$$

Largest BR

$$\sim 25\% \tau^+ \rightarrow \pi^+ \pi^0 \nu$$

Leptonic

$$\sim 35\% \tau^+ \rightarrow (e/\mu)^+ \nu \nu$$

two missing neutrinos \leftarrow limited information, ignore for now

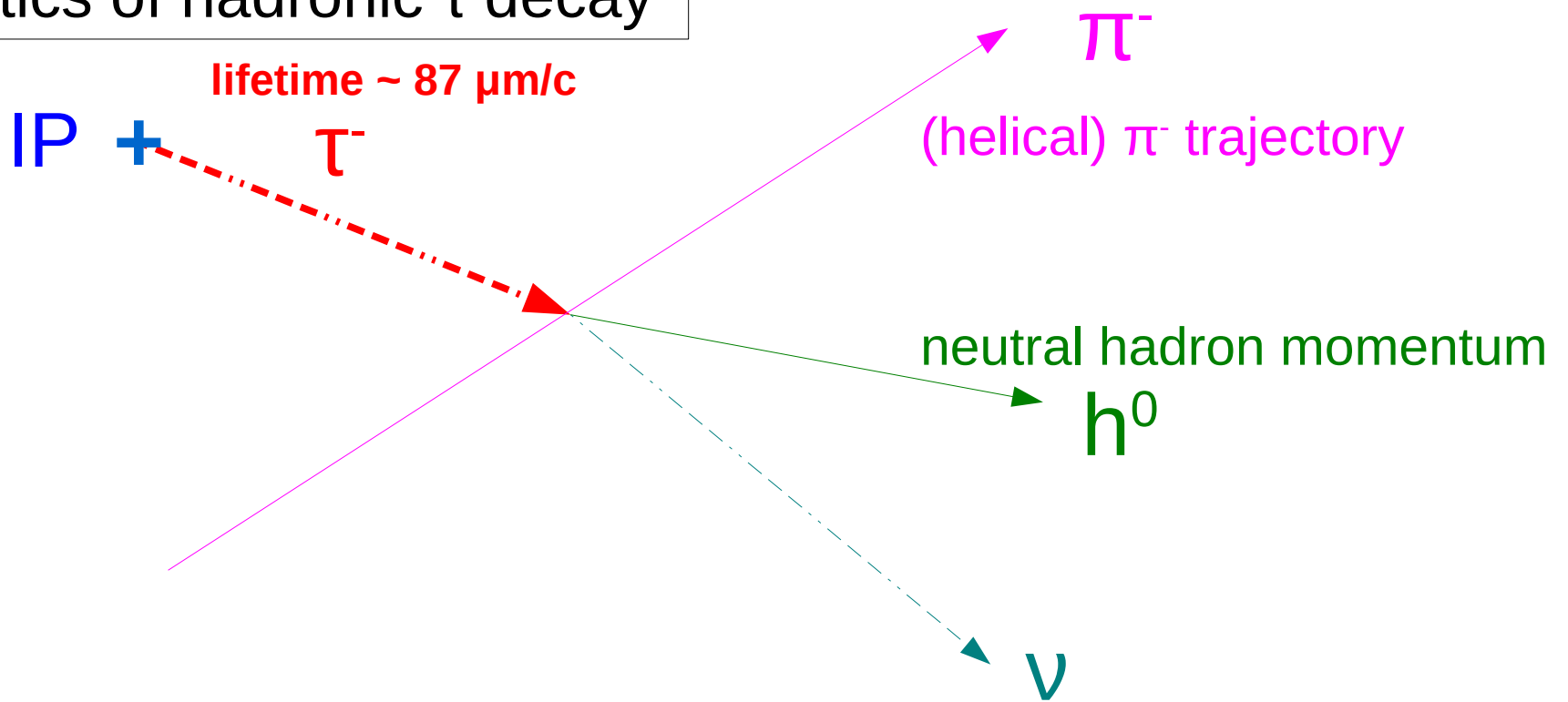
We would ideally like to fully reconstruct the momentum of tau and its decay products

- \rightarrow cleaner selection of e.g. $H \rightarrow \tau^+ \tau^-$ (better mass resolution)
- \rightarrow use of τ spin correlations

However, τ always decays into at least one neutrino

- \rightarrow lose information

kinematics of hadronic τ decay



———— measured
- - - - - un-measured

To optimally use events with taus,
want to fully reconstruct the τ
how to reconstruct the invisible neutrino momentum?

traditional method

e.g. LEP, BELLE, ...

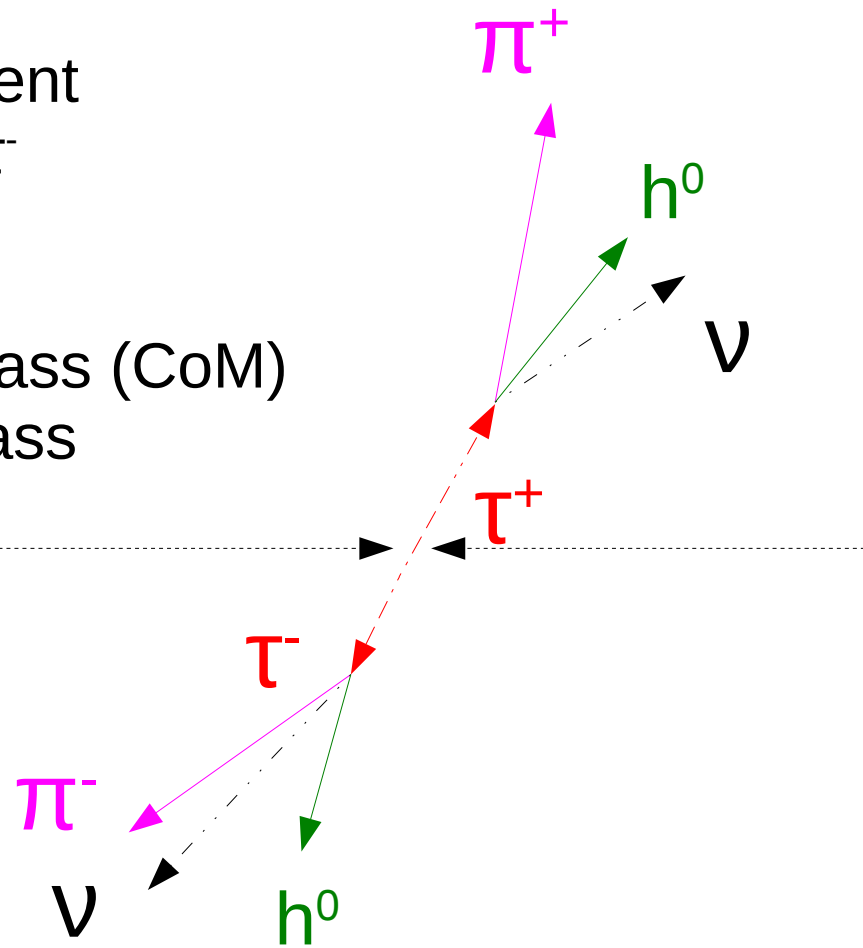
consider whole event

e.g. $e^+ e^- \rightarrow \tau^+ \tau^-$

assume we know

τ - τ centre-of-mass (CoM)

τ - τ invariant mass

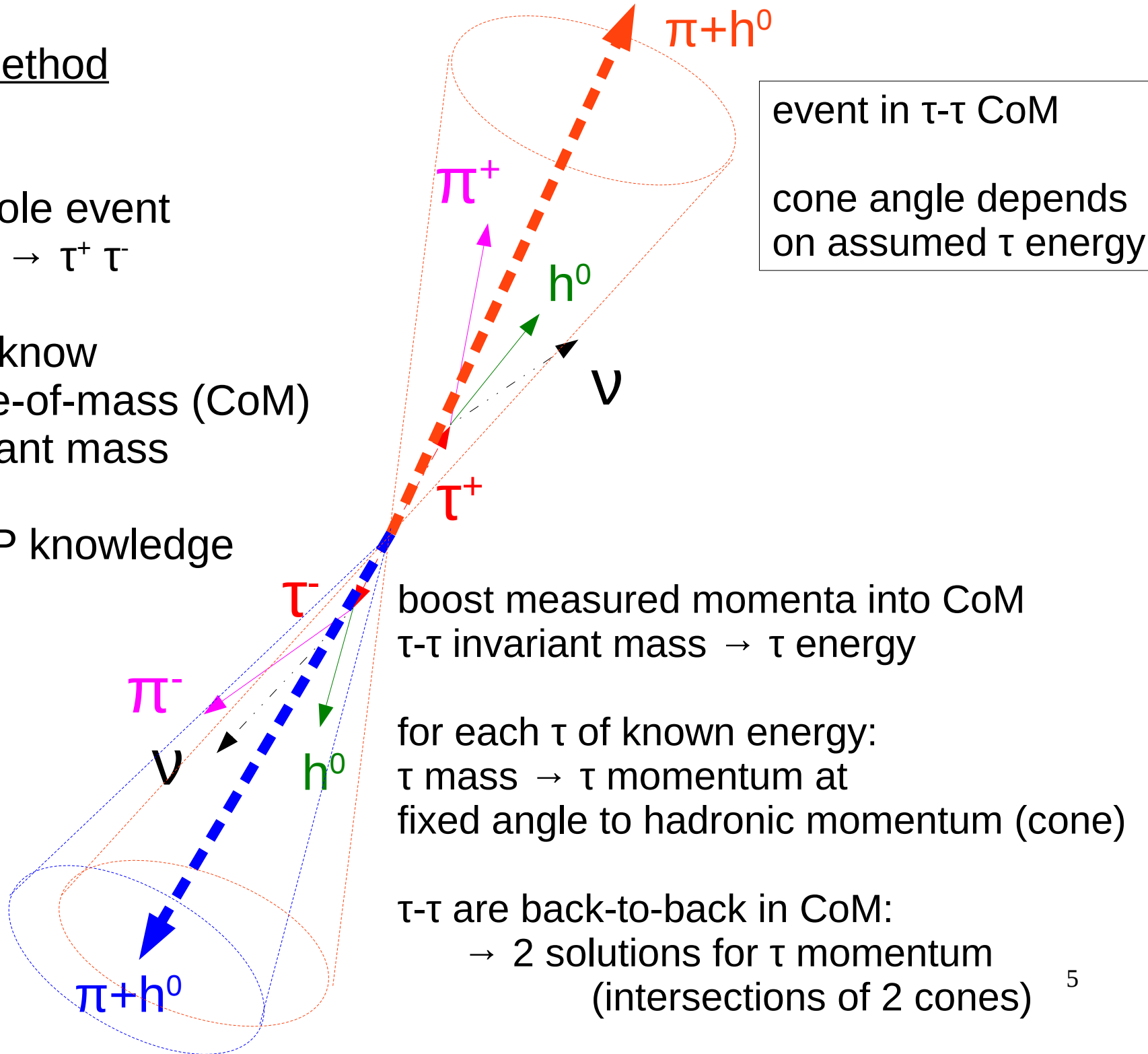


traditional method

consider whole event
e.g. $e^+ e^- \rightarrow \tau^+ \tau^-$

assume we know
 τ - τ centre-of-mass (CoM)
 τ - τ invariant mass

no precise IP knowledge



event in τ - τ CoM
cone angle depends on assumed τ energy

boost measured momenta into CoM
 τ - τ invariant mass \rightarrow τ energy

for each τ of known energy:
 τ mass \rightarrow τ momentum at fixed angle to hadronic momentum (cone)

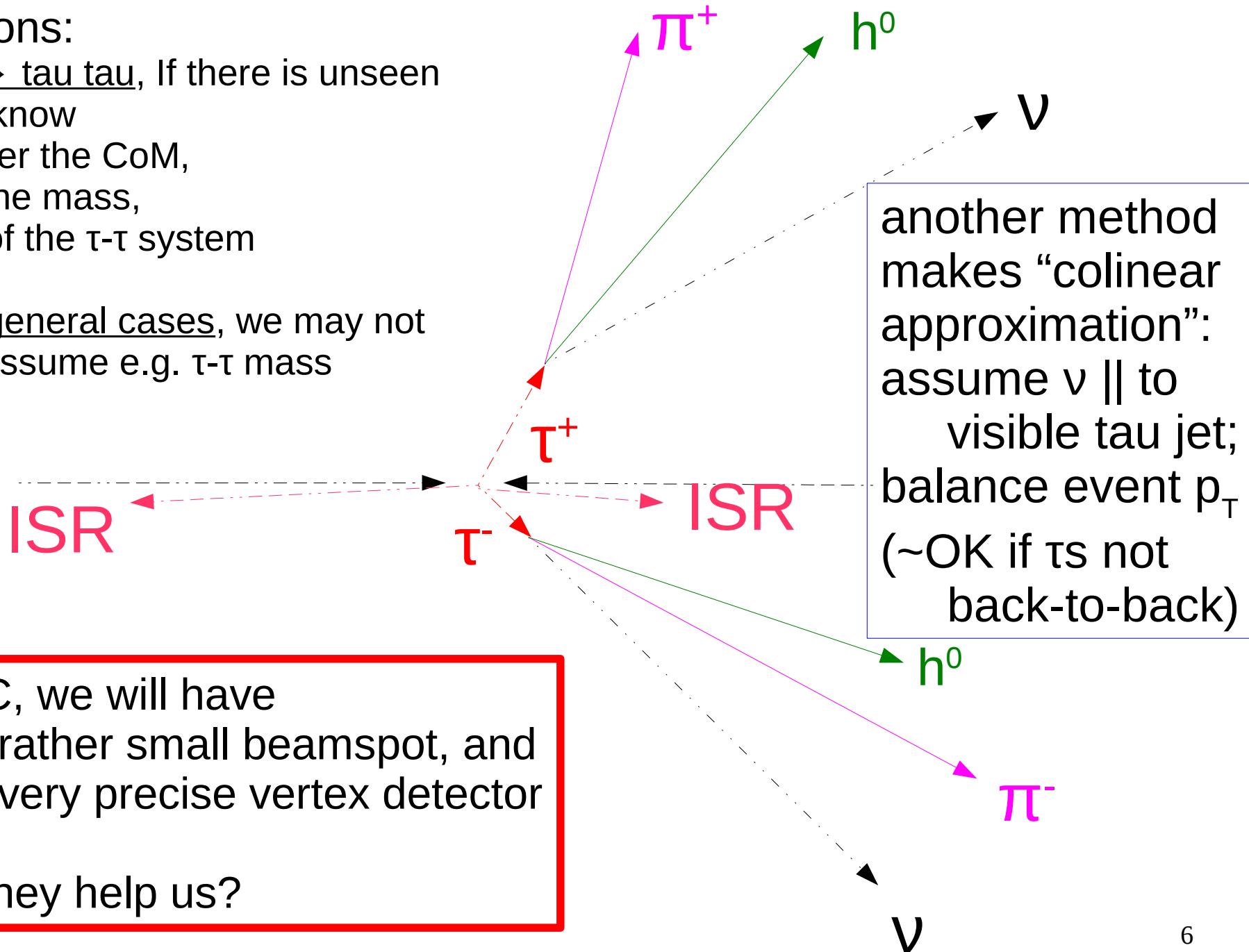
τ - τ are back-to-back in CoM:
 \rightarrow 2 solutions for τ momentum
(intersections of 2 cones)

traditional method

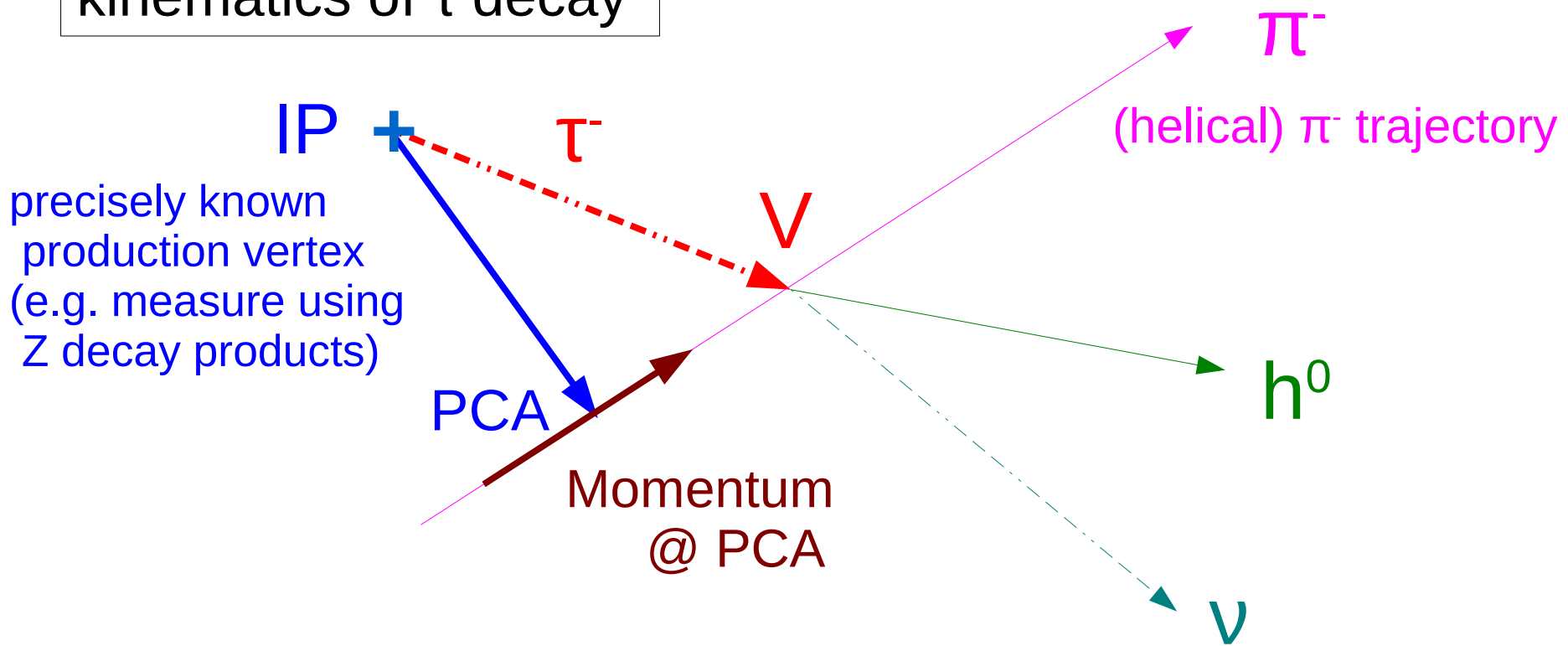
Limitations:

in $e^+e^- \rightarrow \tau\tau$, If there is unseen ISR, we know
neither the CoM,
nor the mass,
of the τ - τ system

in more general cases, we may not
want to assume e.g. τ - τ mass



kinematics of τ decay



assume that π/τ trajectory is approx linear between **PCA/IP** and **V**
 OK since typical radius of curvature \gg τ decay length

measured “track plane” defined by **IP-PCA** and **Mom@PCA**
 (these two vectors are perpendicular for 3d PCA)

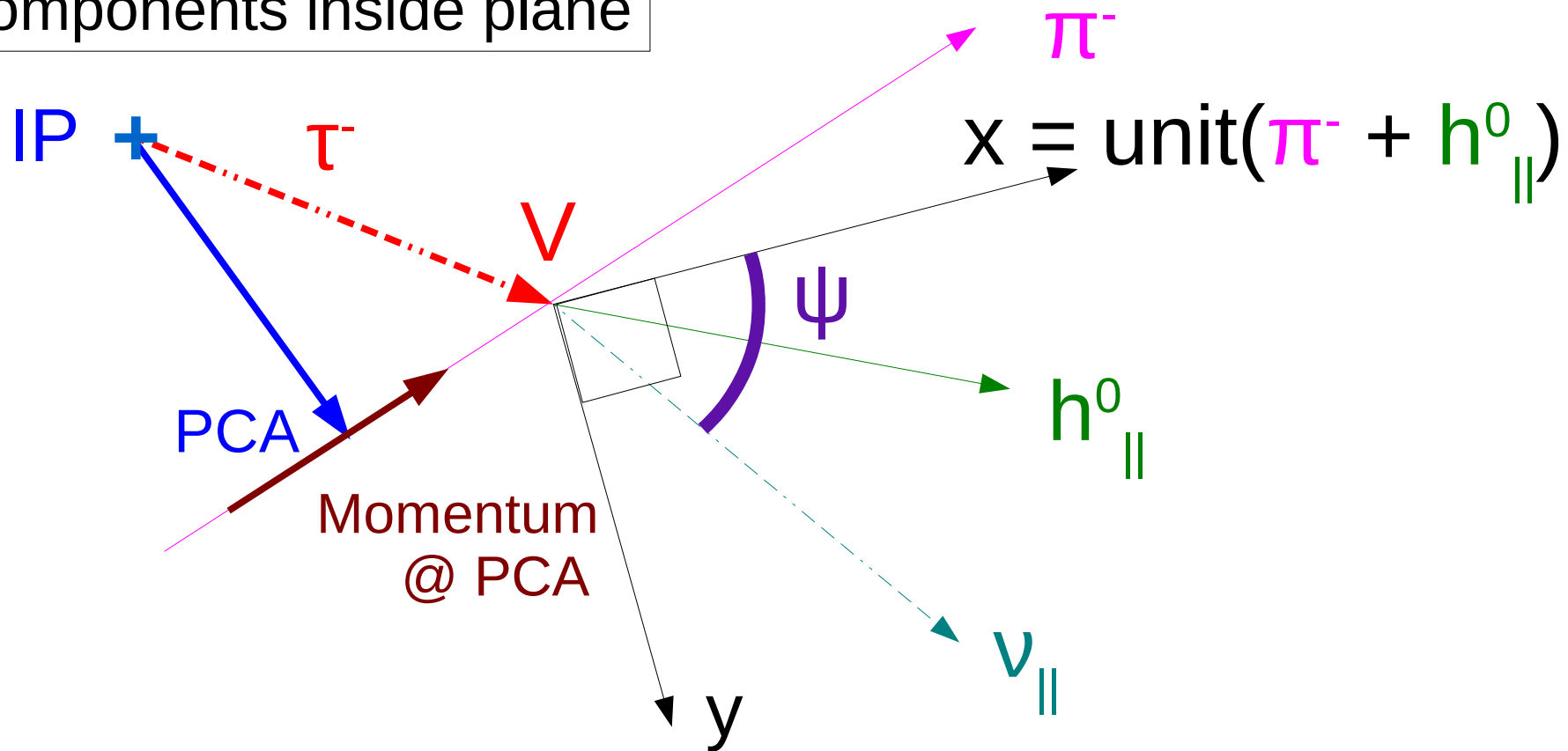
- τ momentum lies inside track plane (linear approx.)

→ $(h^0 + \nu)$ momentum lies in track plane

→ ν momentum out of plane = - h^0 momentum out of plane

$$\nu_{\text{perp}} = - h^0_{\text{perp}}$$

only components inside plane



then parameterise v momentum inside plane:

x is unit vector parallel to hadronic momentum inside plane

y is unit vector in plane, perpendicular to x

Q is magnitude of momentum in plane

$$v_{||} = Q (x \cos \psi + y \sin \psi)$$

We can then write the neutrino momentum as

$$\mathbf{v} = Q (x \cos \psi + y \sin \psi) - h_{\text{perp}}^0$$

two unknown parameters, Q and ψ

4-momentum of $\tau = \pi + h^0 + \nu$

invariant mass of τ is well-known, use to remove one param

→ for each choice of ψ can calculate Q (in general 2 solutions)

→ calculate full kinematics of τ for any assumed ψ
including decay length, lifetime

(in $\pi\nu$ decays, one Q solution gives a negative decay length,
and can be rejected)

we have reduced ν momentum to one parameter ψ

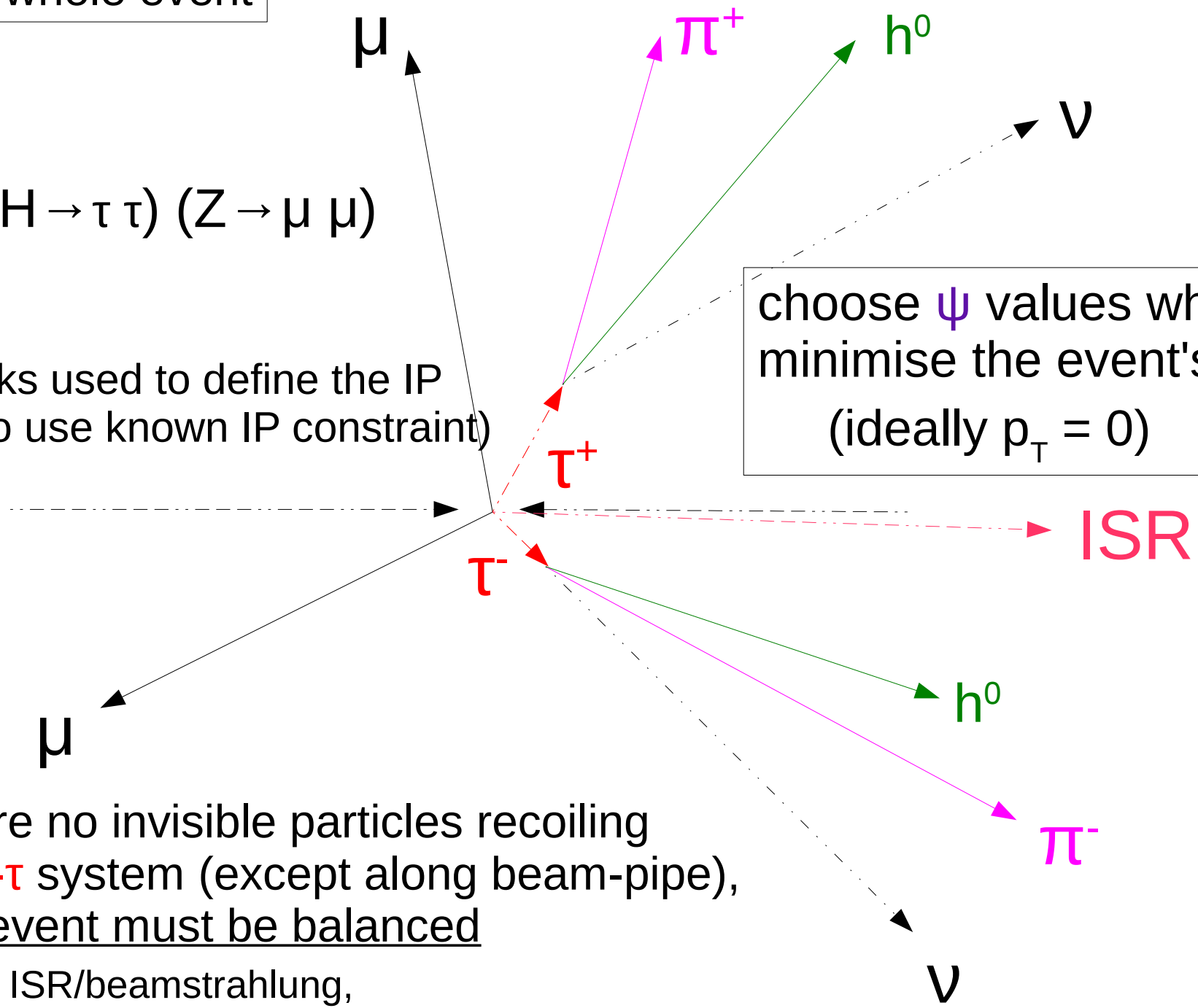
HOW TO CHOOSE ψ ?

consider whole event

e.g.
 $e^+ e^- \rightarrow (H \rightarrow \tau \tau) (Z \rightarrow \mu \mu)$

muon tracks used to define the IP
(could also use known IP constraint)

choose ψ values which
minimise the event's p_T
(ideally $p_T = 0$)



If there are no invisible particles recoiling
against τ - τ system (except along beam-pipe),
 p_T of event must be balanced

because of ISR/beamstrahlung,
don't make requirements on p_z

Test the method

$e^+ e^- \rightarrow H \mu^+ \mu^-$ events generated @ 250 GeV Whizard with CIRCE1 ISR/BS

$H \rightarrow \tau\tau$; τ decayed by TAUOLA: either both $\pi^+\nu$ or both $\pi^+\pi^0\nu$ ($\rho\nu$)

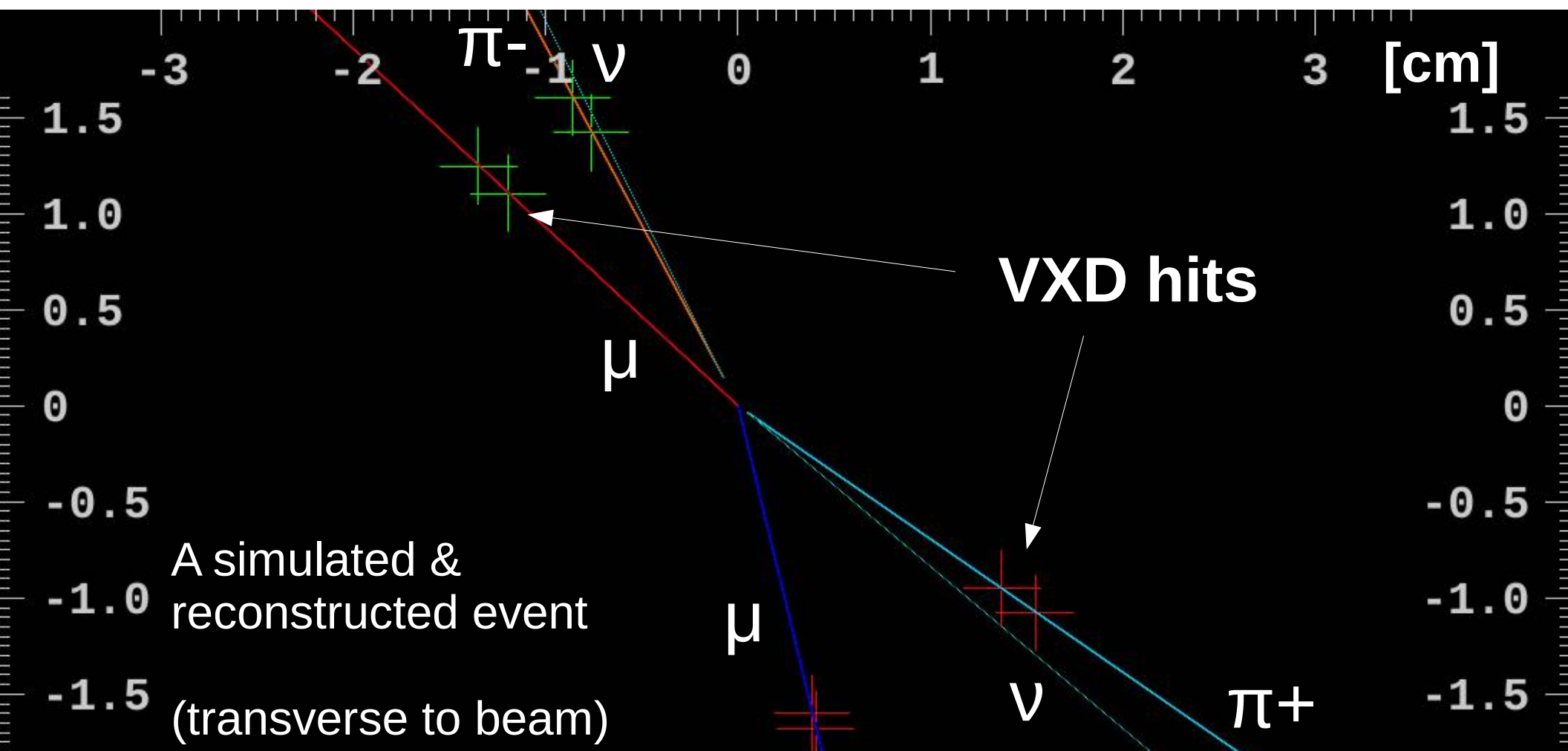
Full ILD simulation, DBD version ILD_v05_o1

Usual ILD reconstruction + GARLIC, no underlying event overlay

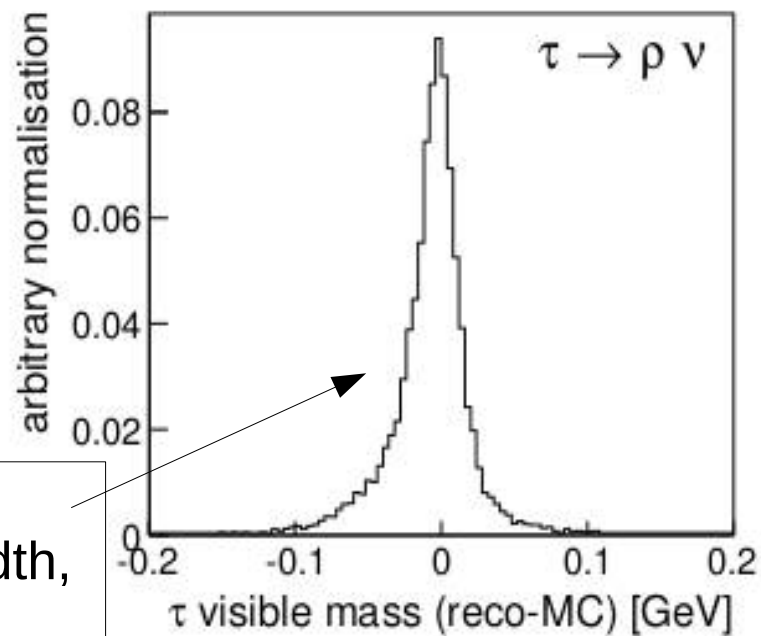
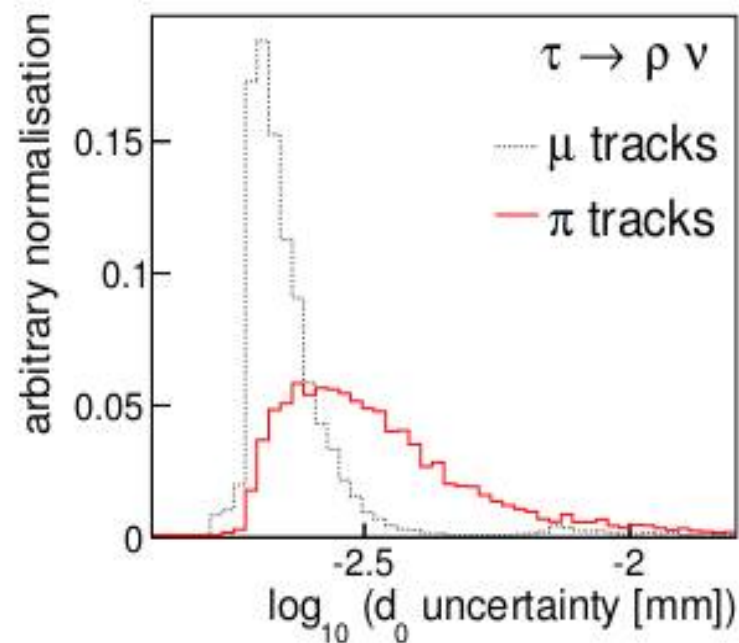
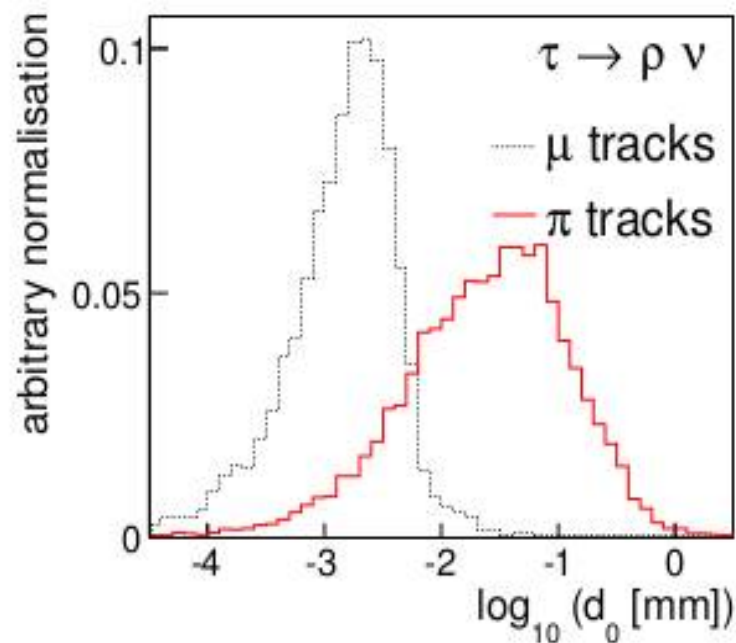
Cheat matching of GARLIC/Pandora clusters to π^0 , and of π^0 & π^+ to τ

apply π^0 mass constraint to two photon system

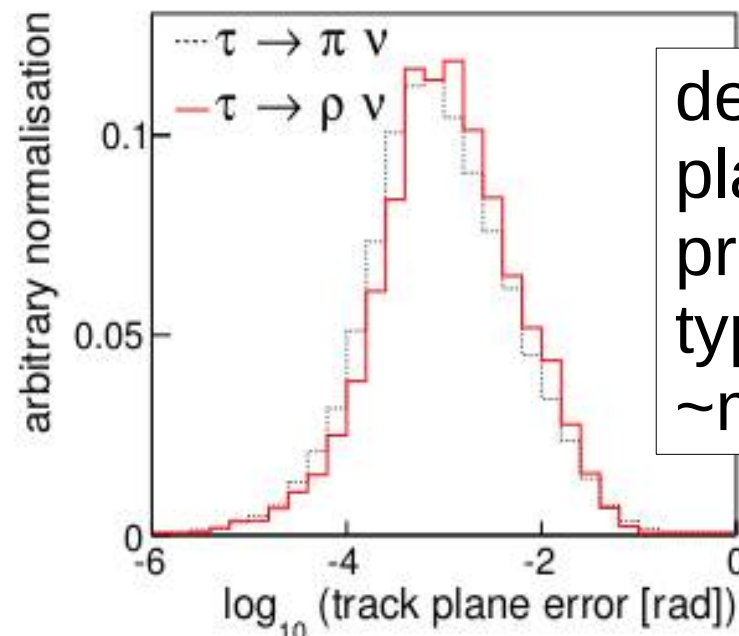
Use $\mu^+ \mu^-$ tracks to reconstruct IP: $\sim 3\mu\text{m}$ precision



Track, π^0 , ρ reconstruction

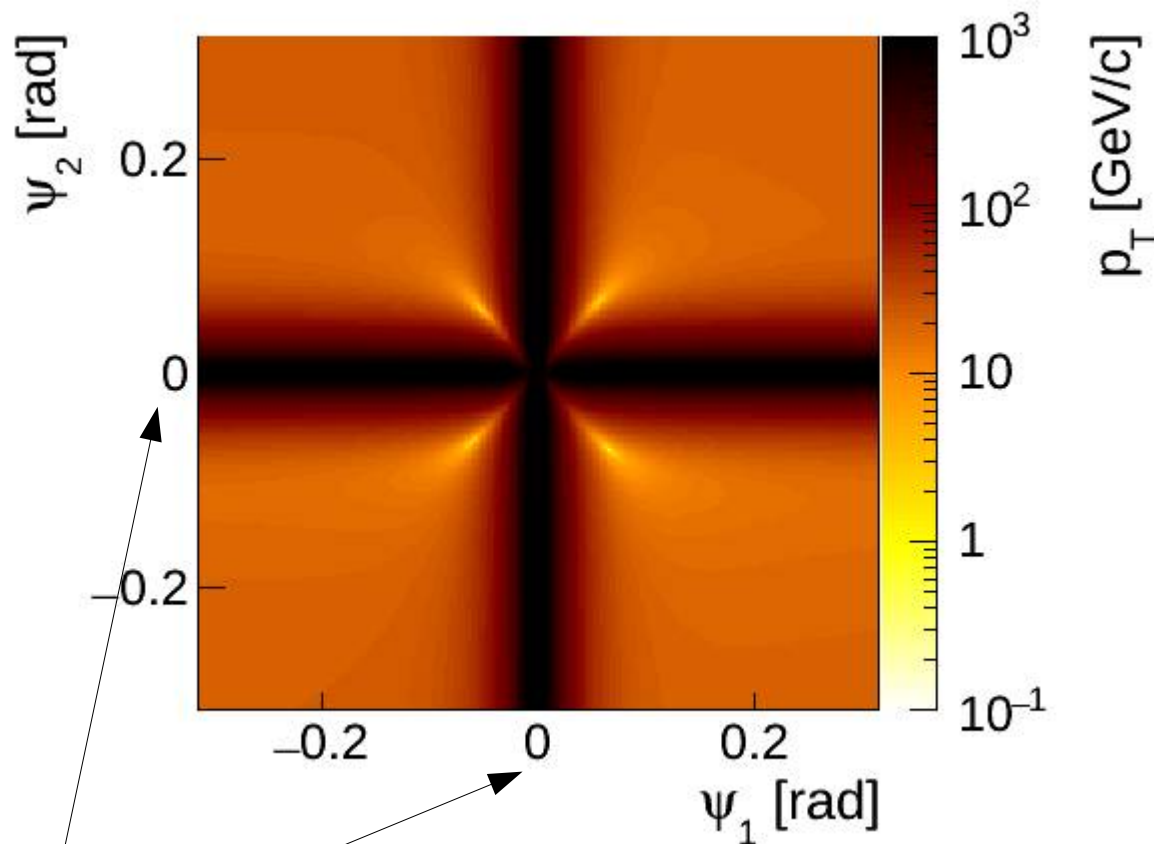


smaller than natural ρ width, small bias



decay plane precision typically \sim mrad

How does event p_T depend on neutrino angle ψ chosen for two taus?



neutrino colinear
with hadrons in
track plane

one event @ 250 GeV
 $e^+e^- \rightarrow (H \rightarrow \tau\tau) (Z \rightarrow \mu\mu)$

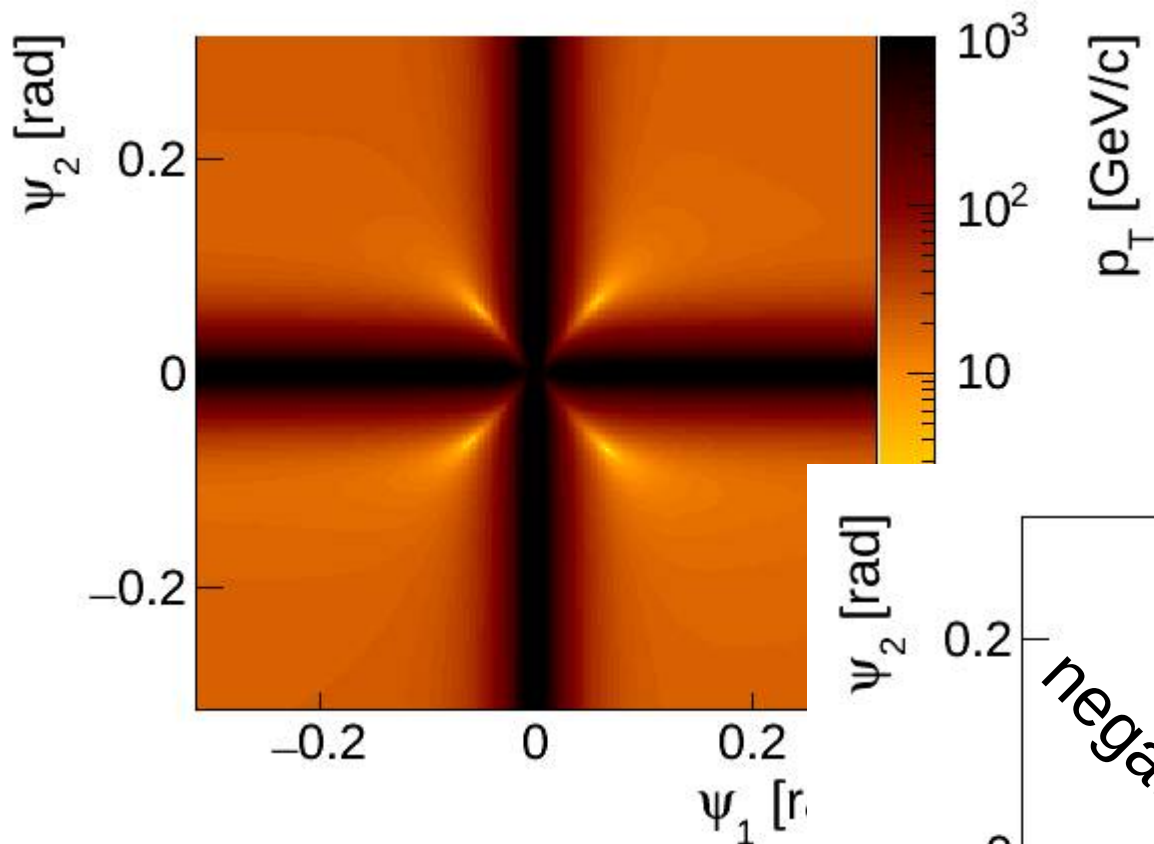
both $\tau \rightarrow \pi \nu$

**simulated and
reconstructed in ILD**

Four possible solutions with small p_T
easy to find minima using e.g. MINUIT

how to choose which one?

How does event p_T depend on neutrino angle ψ chosen for two taus?



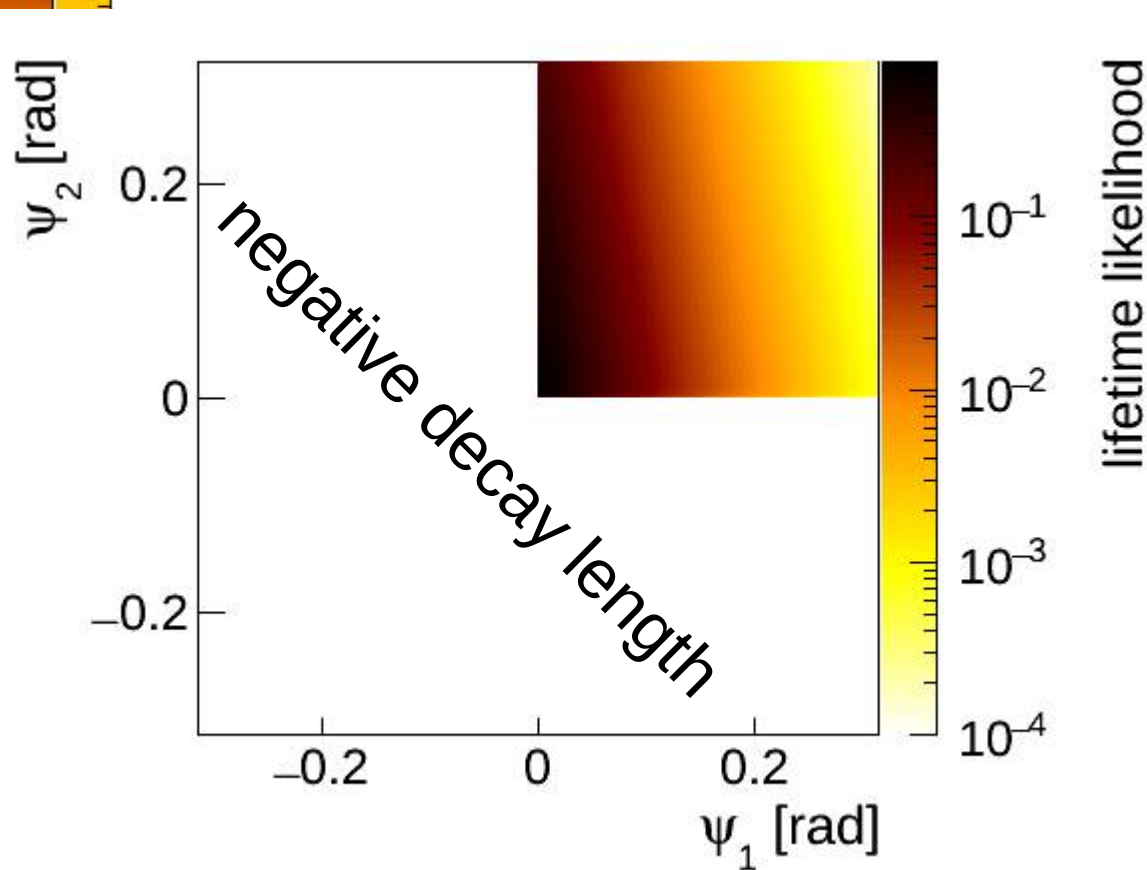
lifetime likelihood

$$\exp\left\{ - \frac{\text{candidate lifetime}}{\text{mean tau lifetime}} \right\}$$

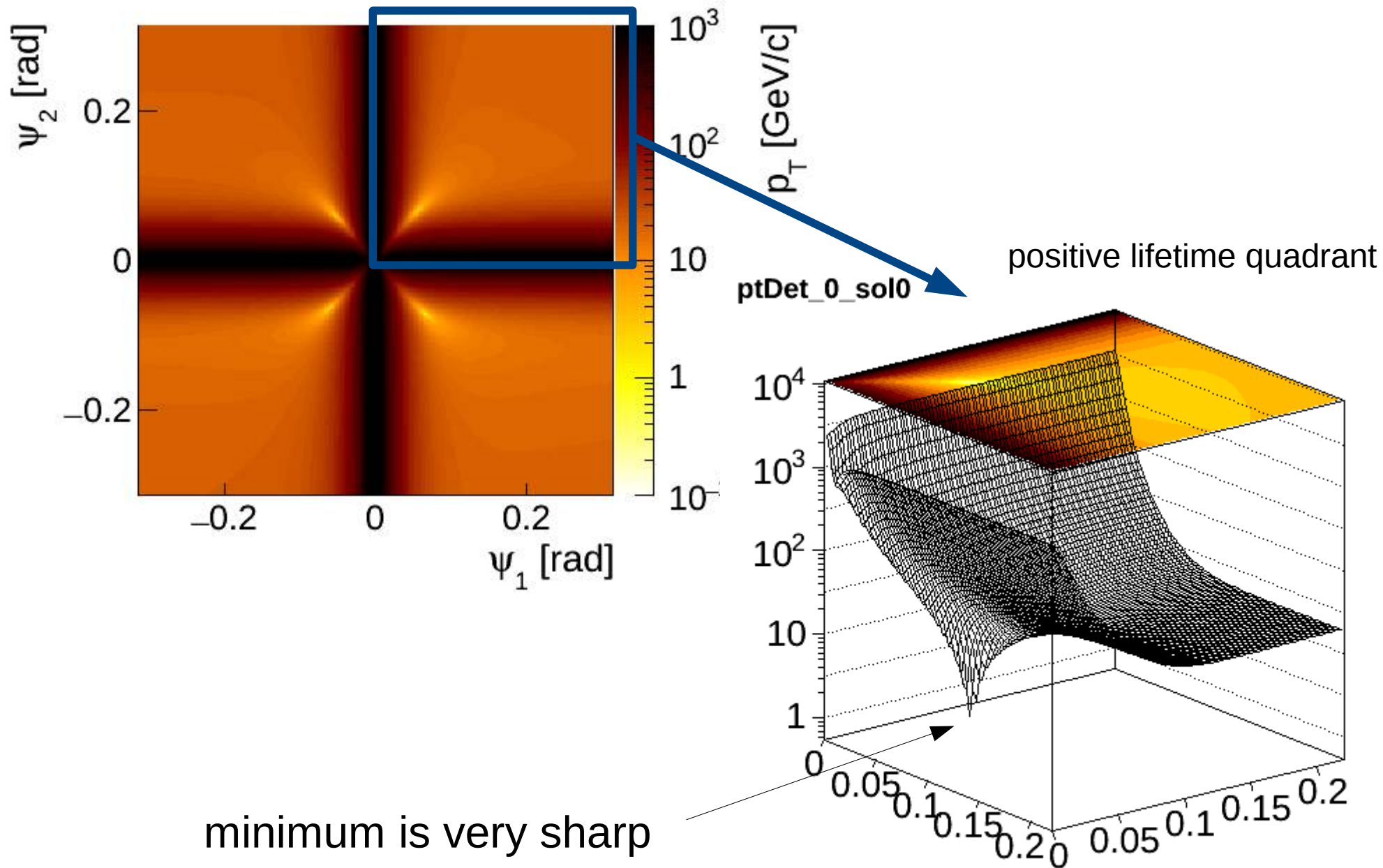
for +ve candidate decay length,

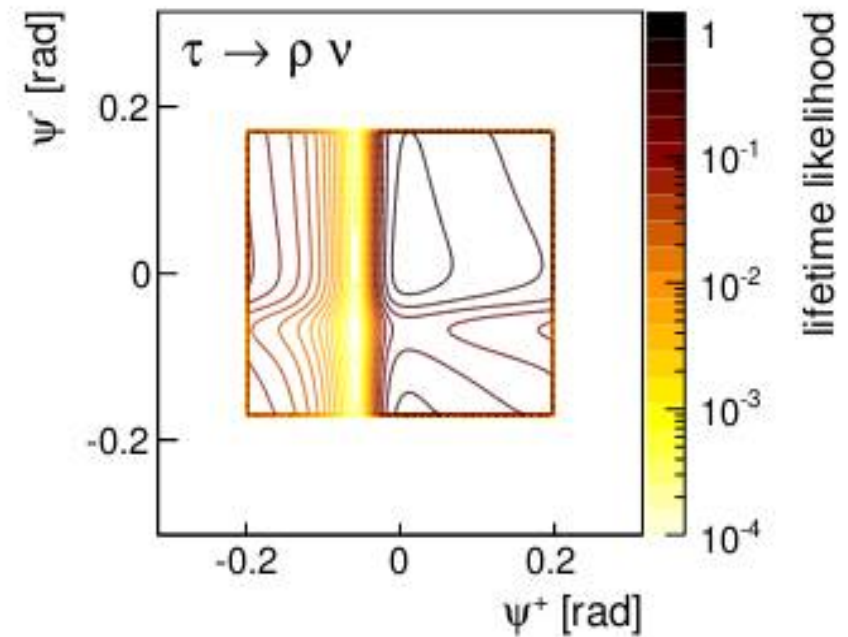
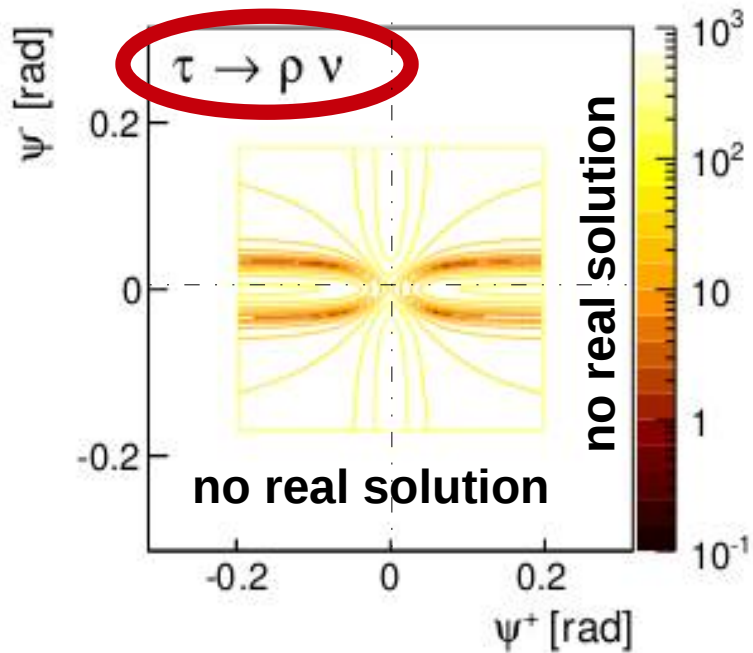
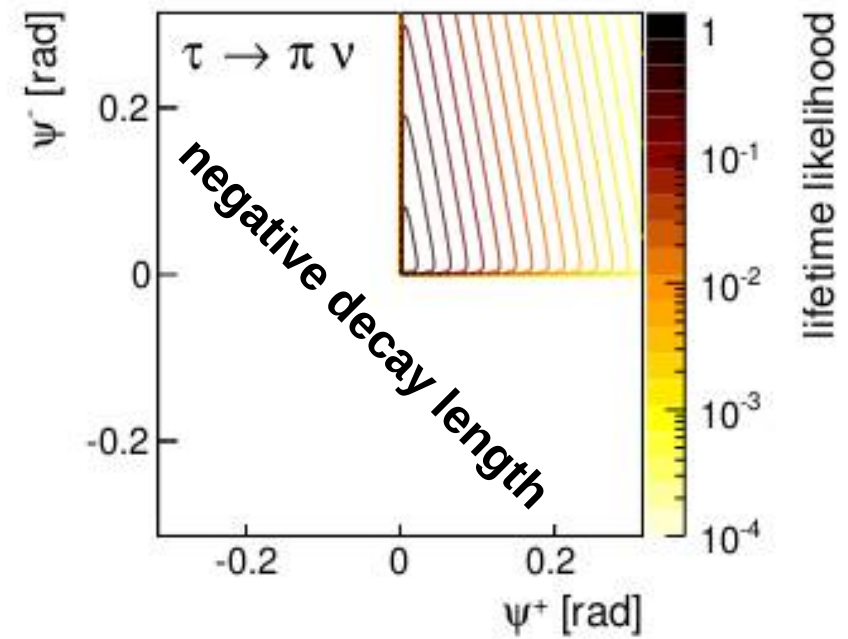
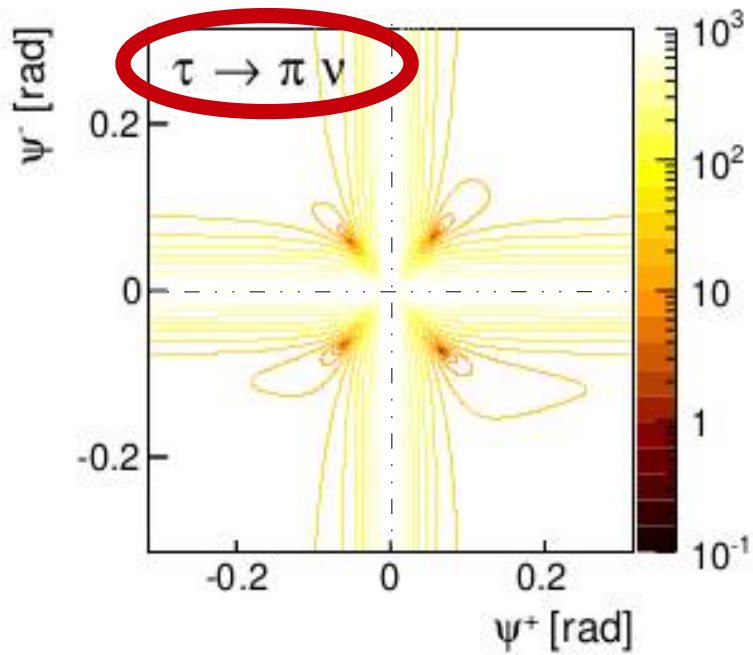
0 for -ve decay length

look at tau's reconstructed decay length / lifetime for each solution



How does event p_T depend on neutrino angle ψ chosen for two taus?

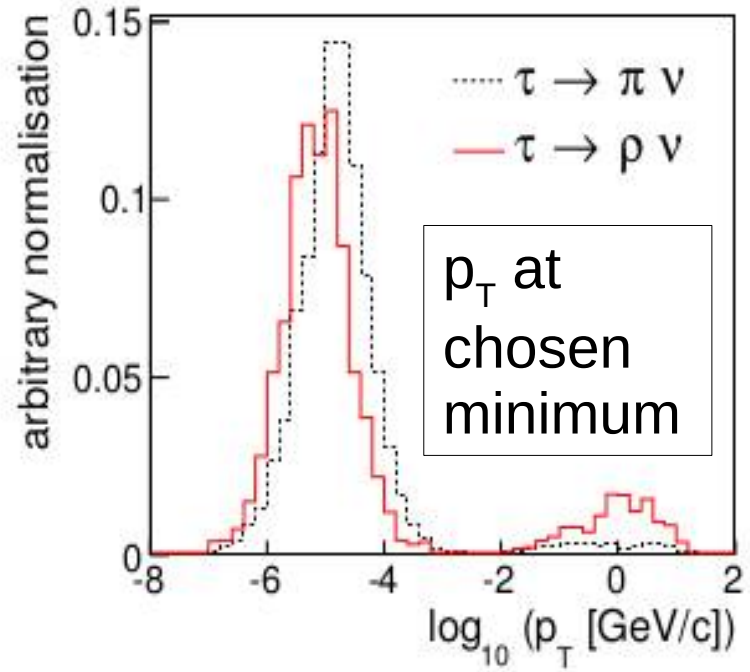




Find p_T minimum in each quadrant:

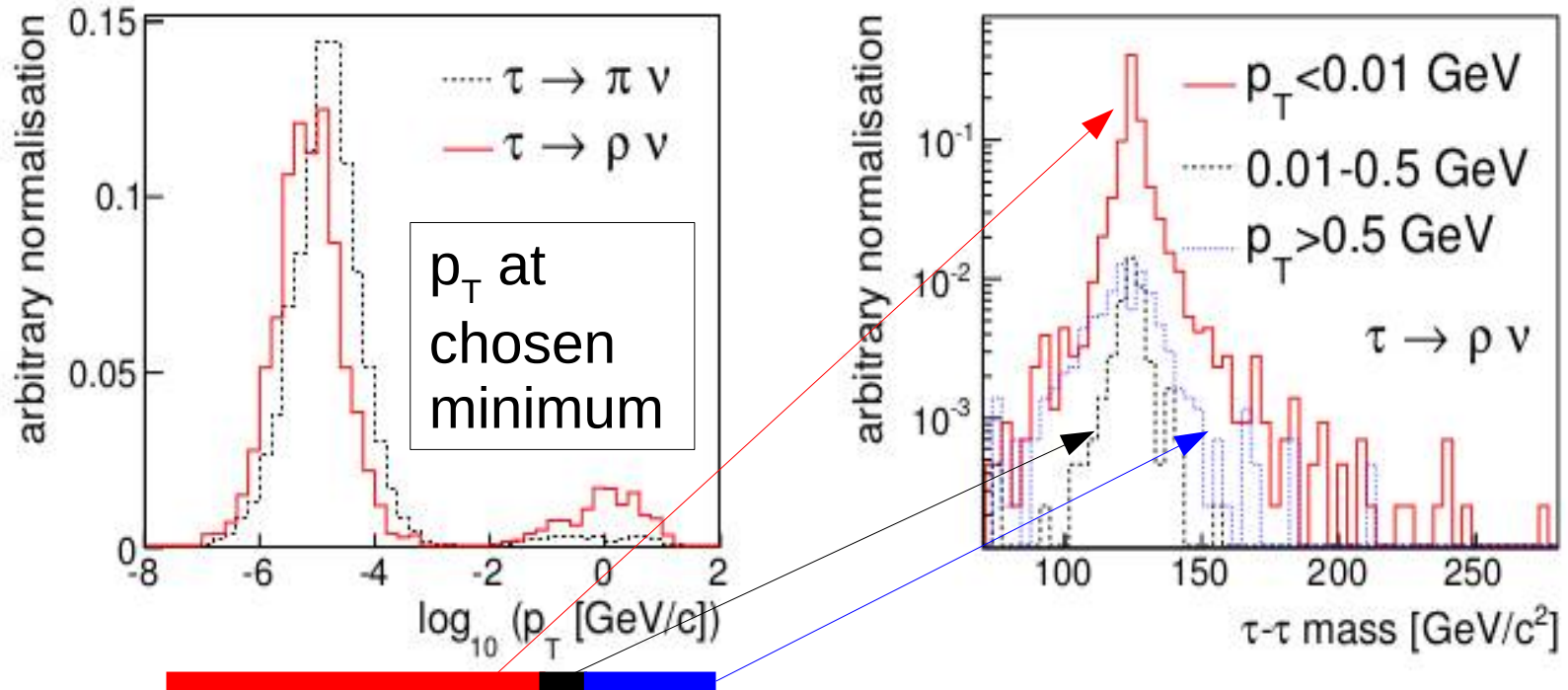
choose smallest p_T minimum with positive decay length

How well does it work?



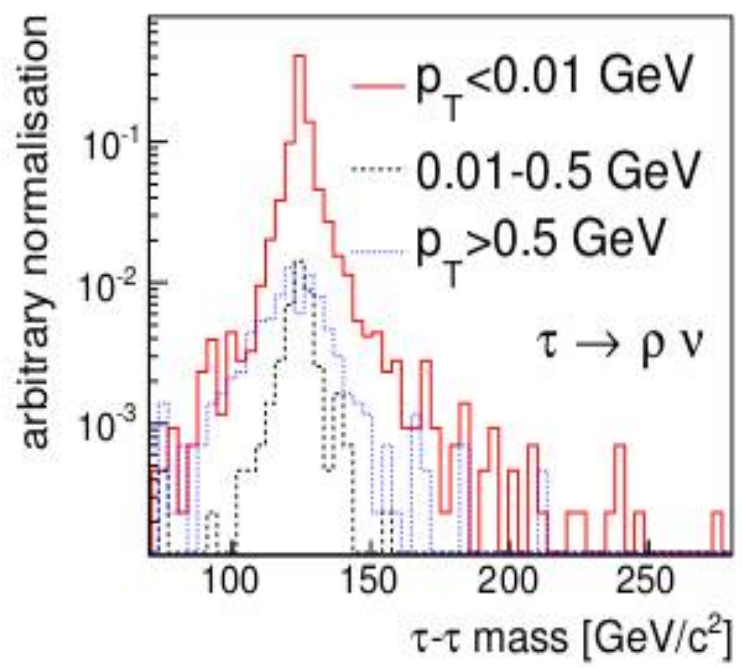
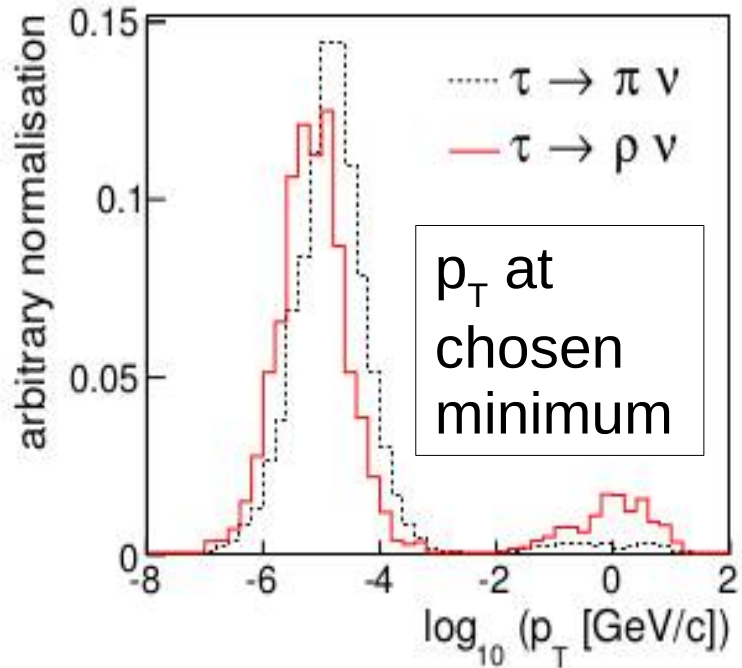
How well does it work?

Check the invariant mass of τ system: should be 125 GeV

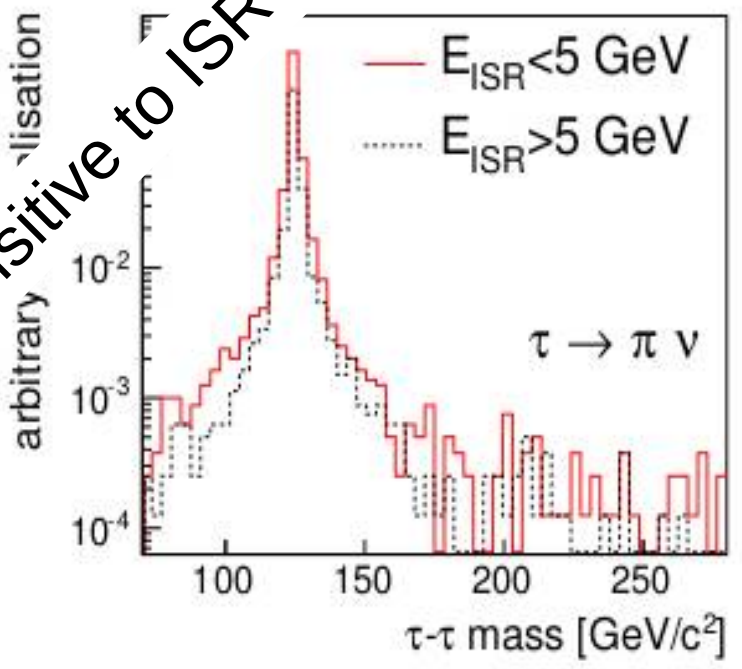


How well does it work?

Check the invariant mass of τ system: should be 125 GeV

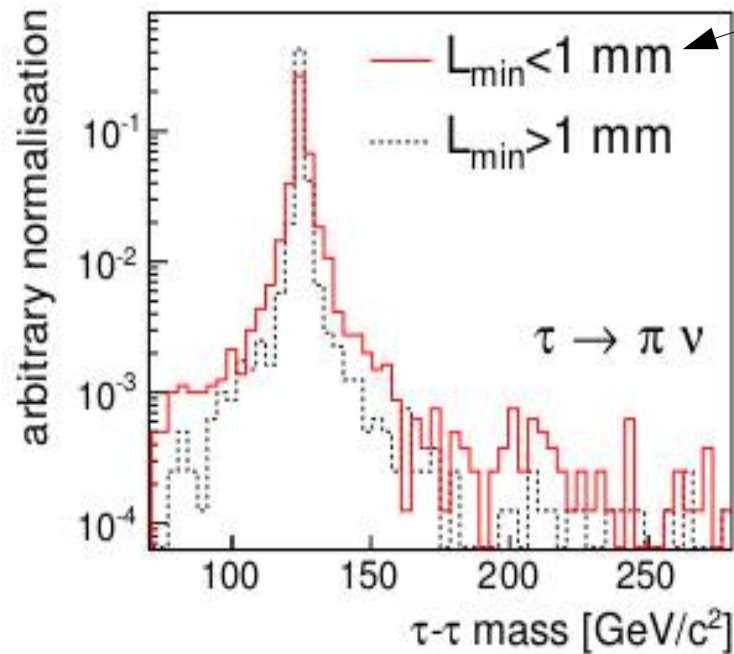
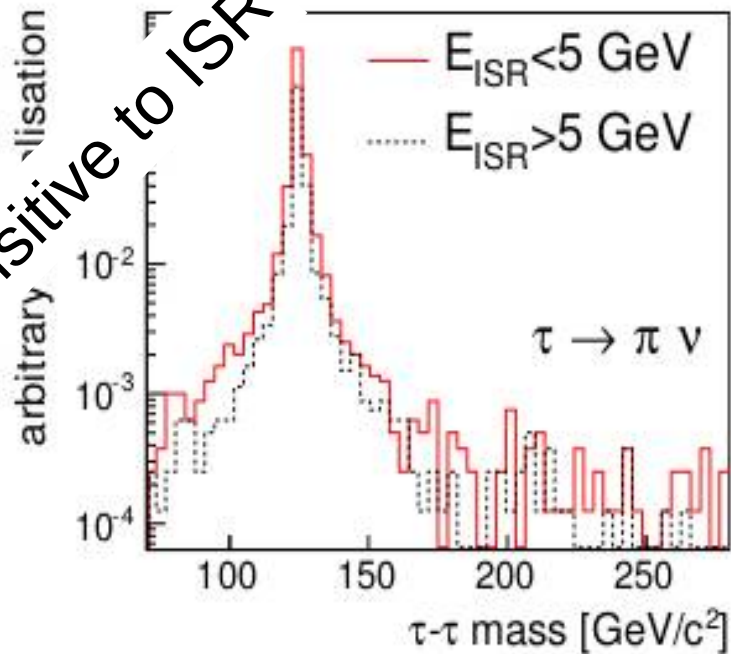
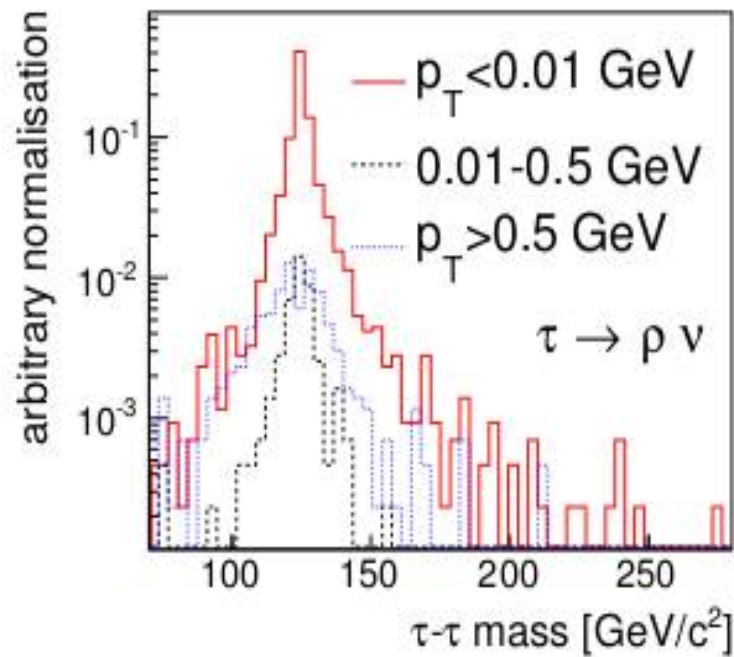
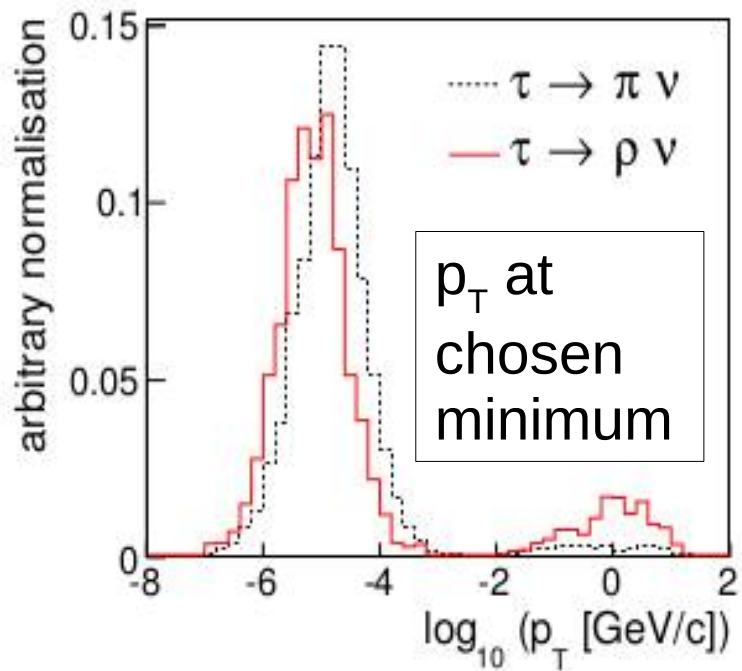


insensitive to ISR



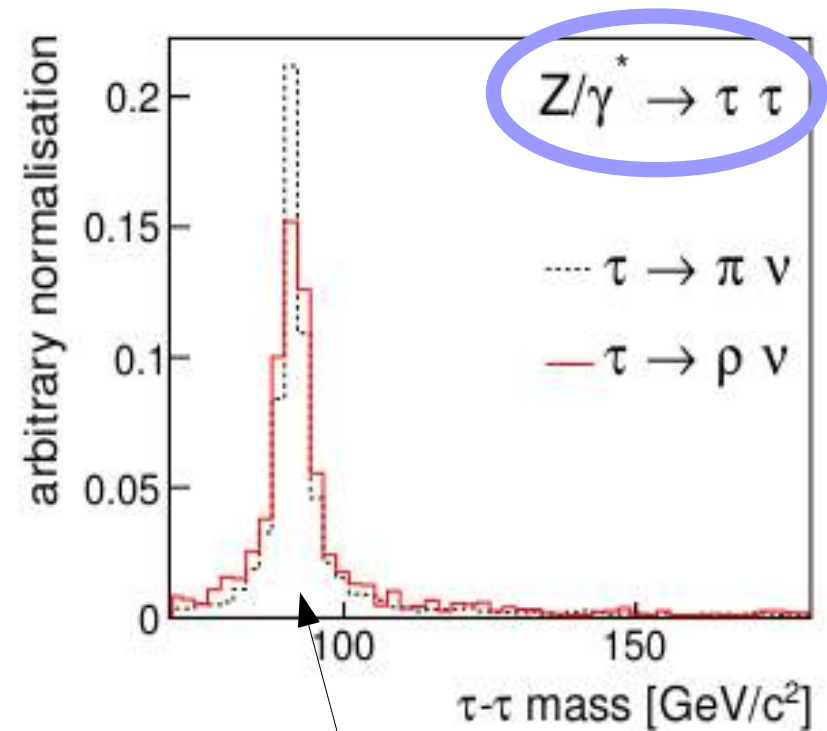
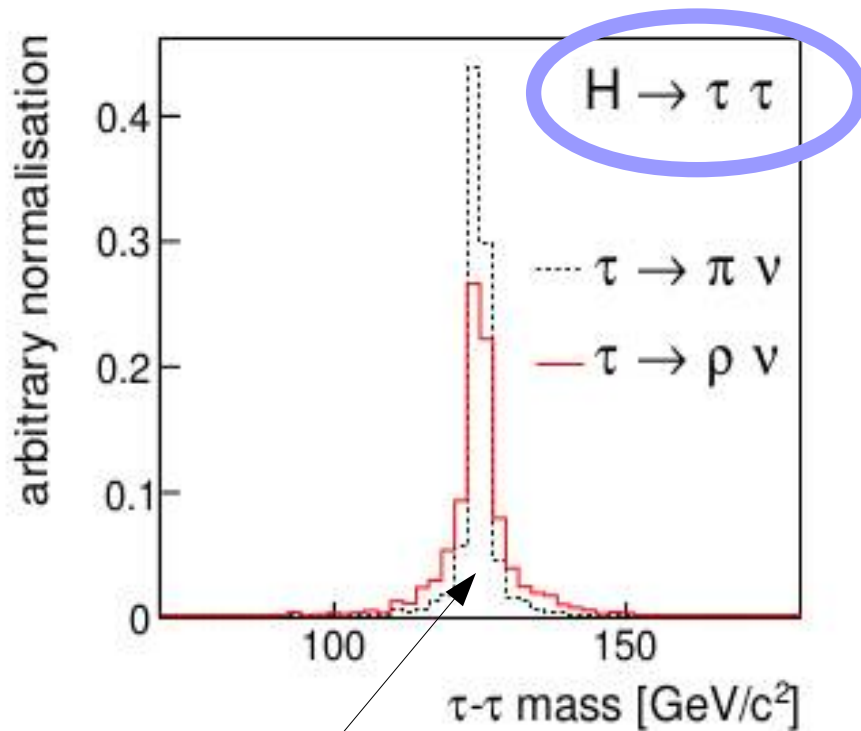
How well does it work?

Check the invariant mass of τ system: should be 125 GeV



“unlucky” short-lived taus are somewhat less-well measured

insensitive to ISR



width of central peak
 $\sim 0.6 \text{ GeV}$ for $\pi^+\nu$
 $\sim 1.1 \text{ GeV}$ for $\pi^+\pi^0\nu$

within $(125 \pm 10) \text{ GeV}$:
 $\sim 95\%$ of $\pi^+\nu$
 $\sim 89\%$ of $\pi^+\pi^0\nu$

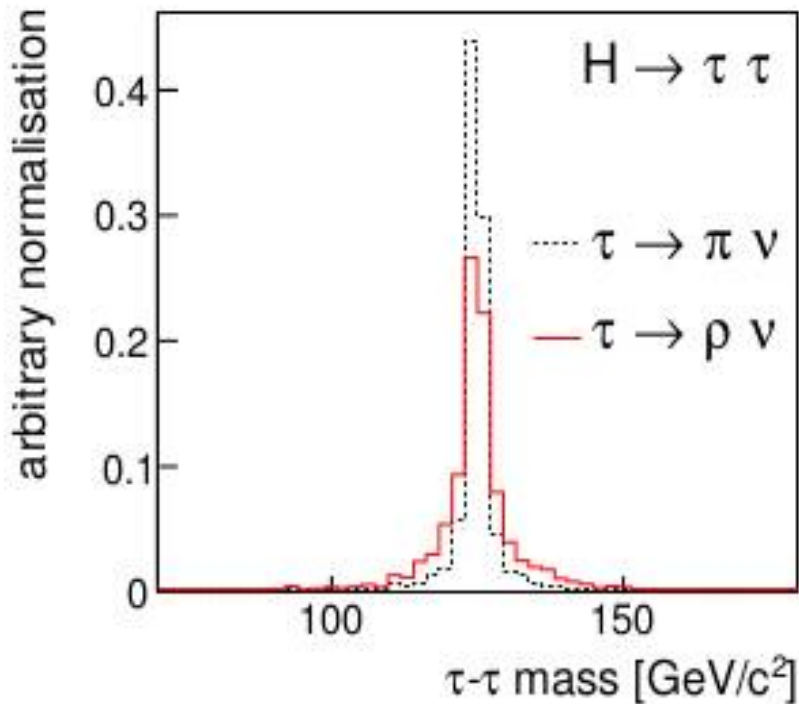
easily distinguished from Z

Compare to methods not using impact parameter

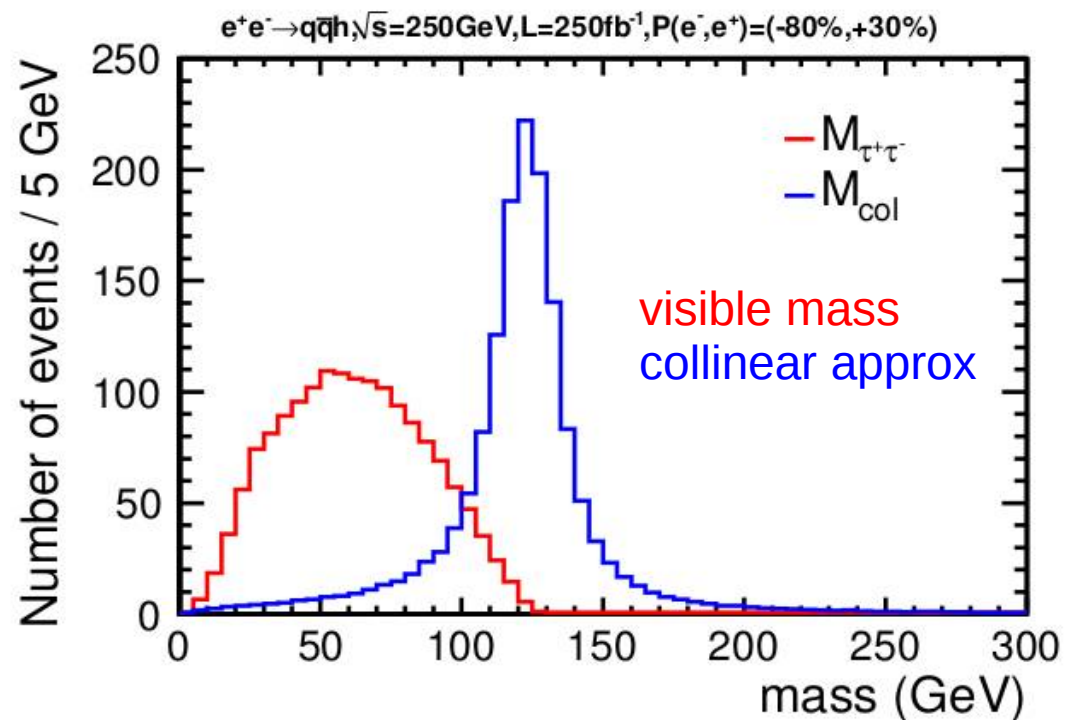
e.g. Kawada et al [arXiv:1509.01885v1]

Collinear approximation:

- assume neutrinos collinear with visible decay products
- require p_T balance in event



n.b. full ILD reco, $\mu\mu H$,
pure tau decay modes,
cheated γ, π, τ association



n.b. full ILD reco, qqH ,
all tau decay modes,
no cheating of association

Summary

reconstruction method for hadronic tau decays works well @ ILC

requires good IP reconstruction and impact parameter resolution of order 10 microns (interesting to exactly how good it needs to be)

insensitive boost along beam axis

- ISR, beamstrahlung OK → HZ @ high energy OK
- in principle, also applicable to hadron collider experiments
 - if impact parameter resolution sufficiently good
 - if IP can be measured

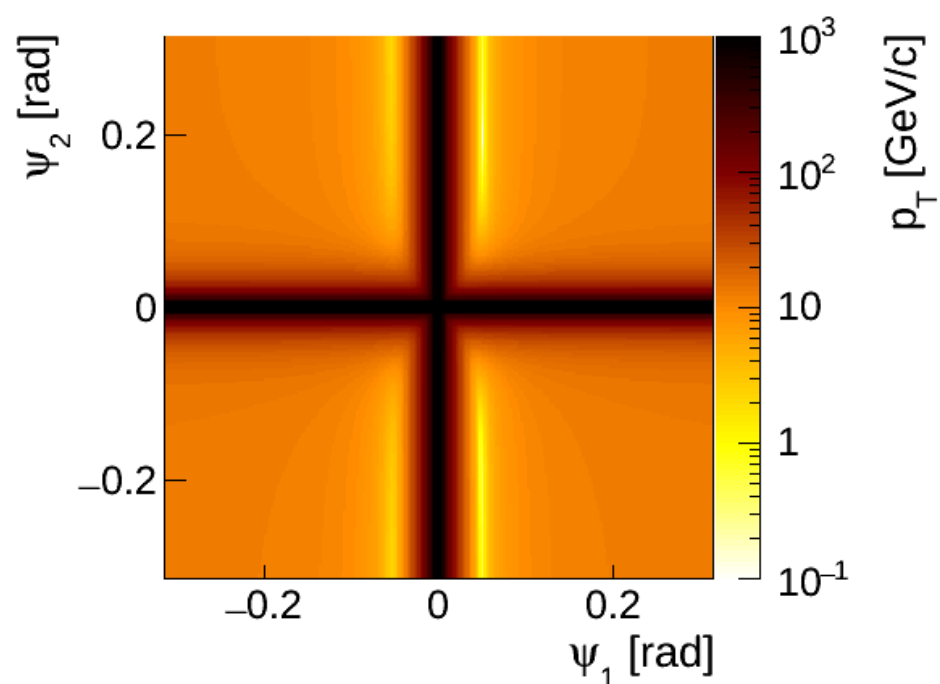
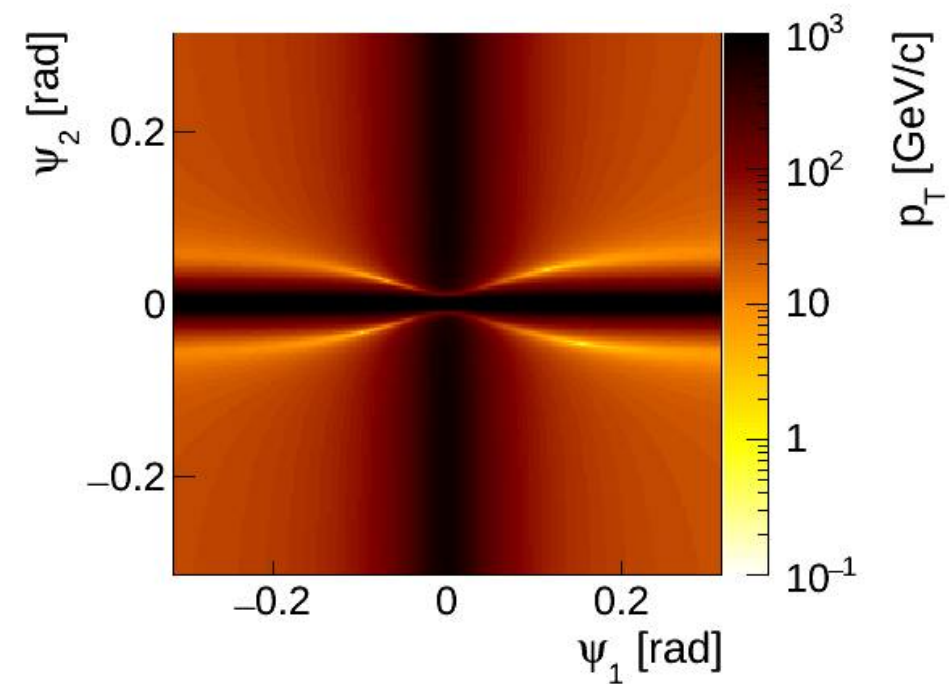
Reconstructs τ - τ mass to a precision of ~ 1 GeV

Paper submitted to NIM-A (arXiv:1507.01700)

Now working on removing cheating (associating tracks, clusters to taus)
then use tau spin correlations to measure Higgs CP

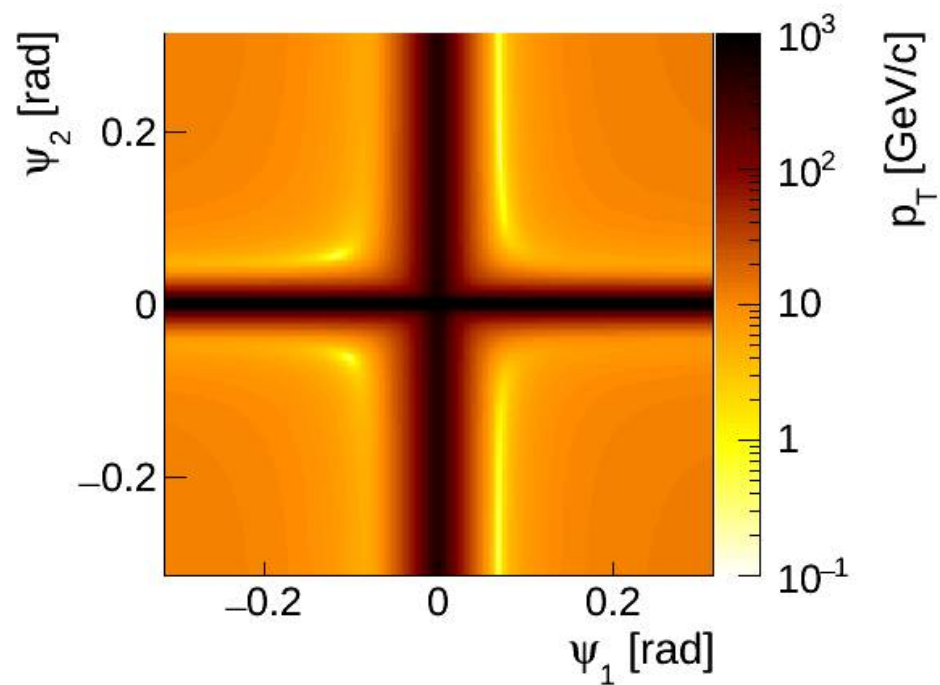
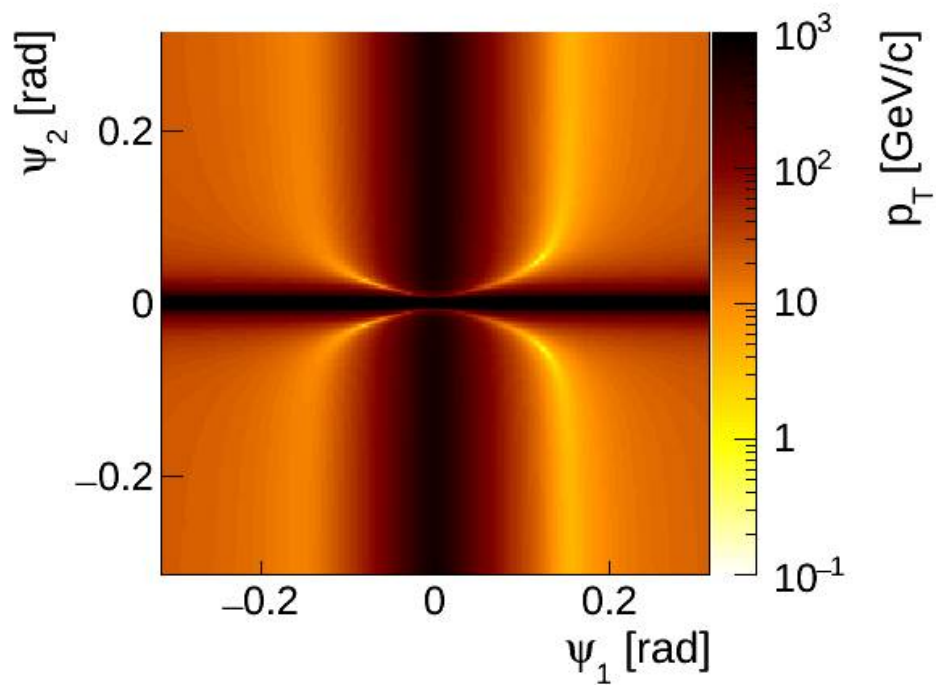
electron, hadronic Z decays: p_T less well measured

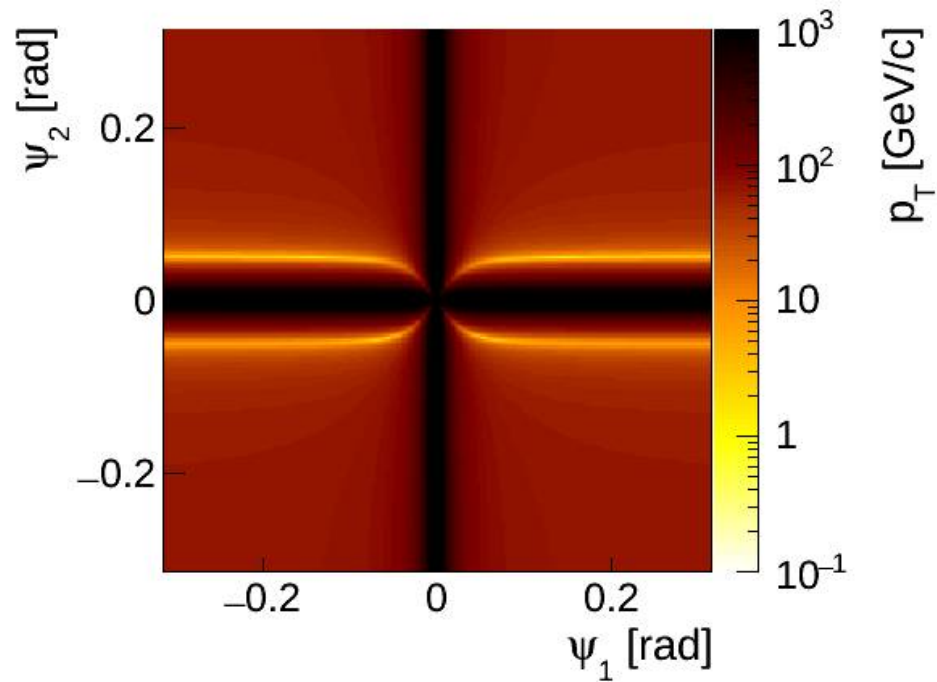
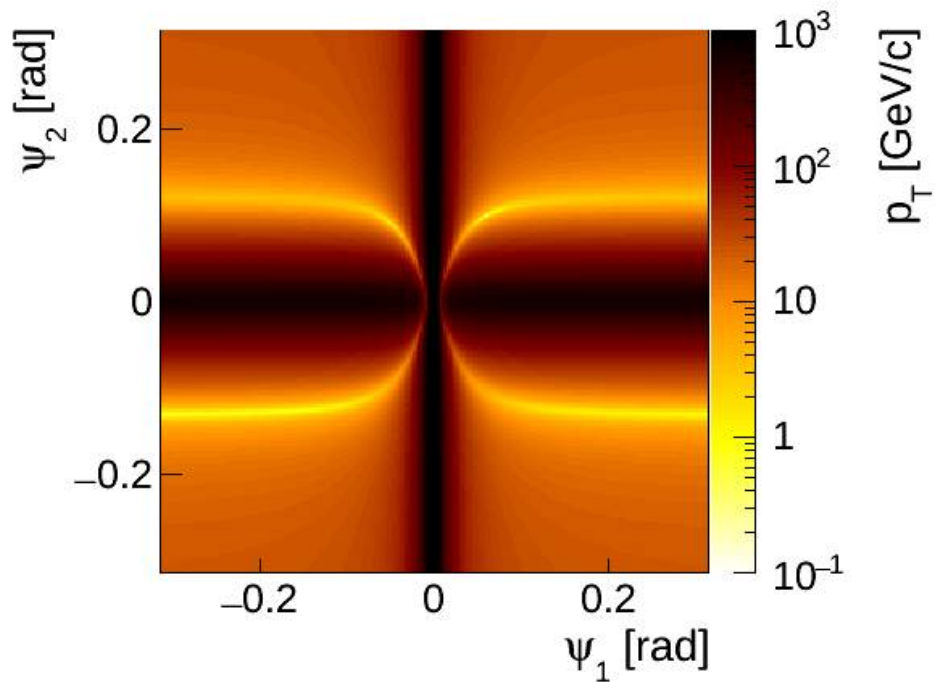
BACKUP
and old slides



a few more events

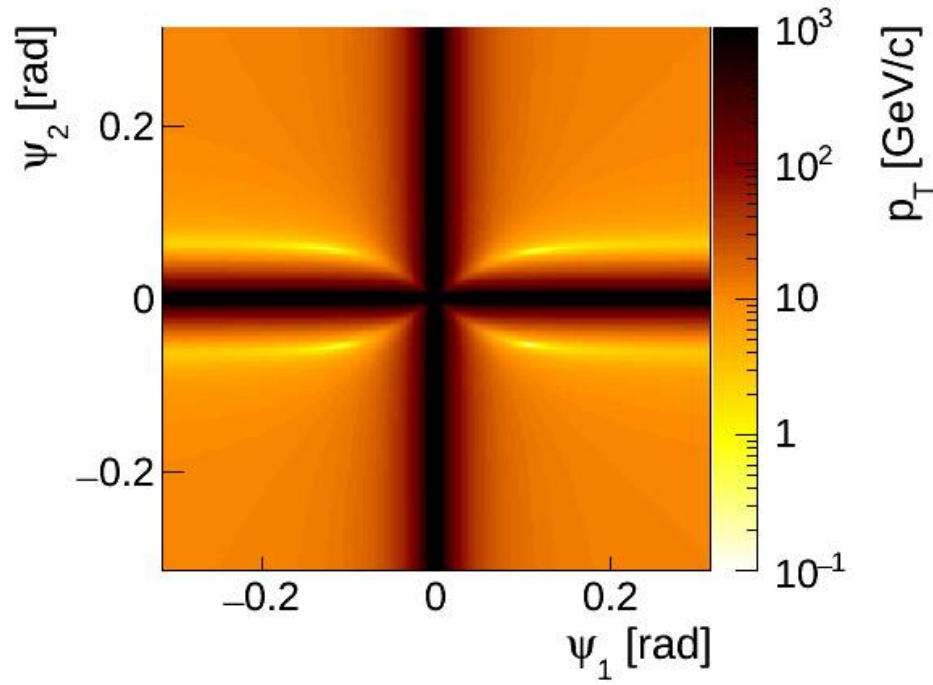
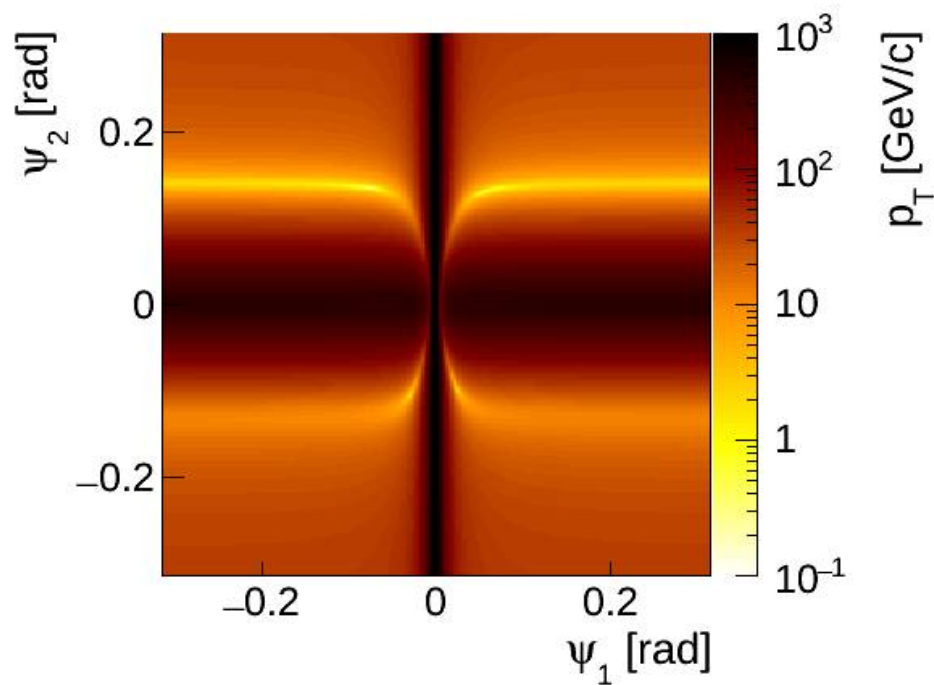
both $\tau \rightarrow \pi \nu$





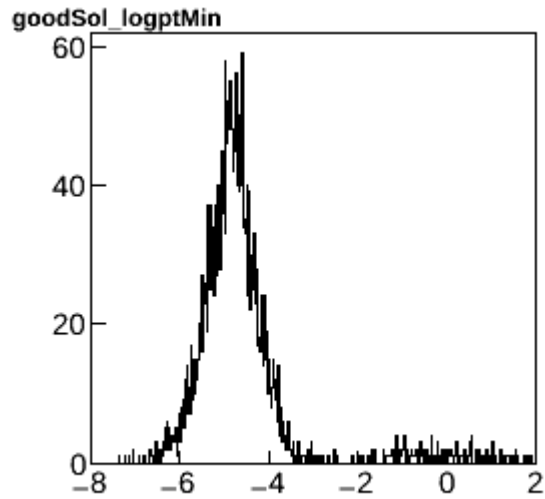
a few more events

both $\tau \rightarrow \pi \nu$

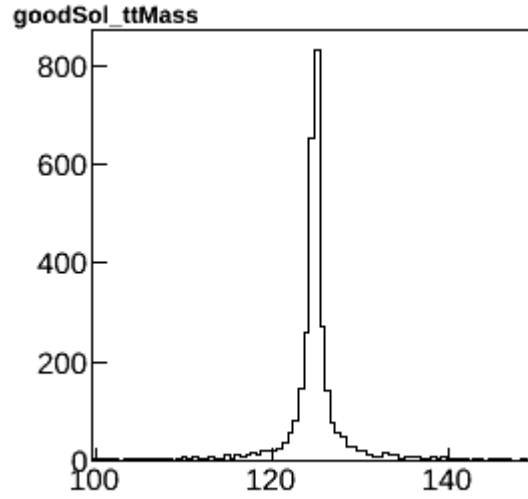


Full reconstruction

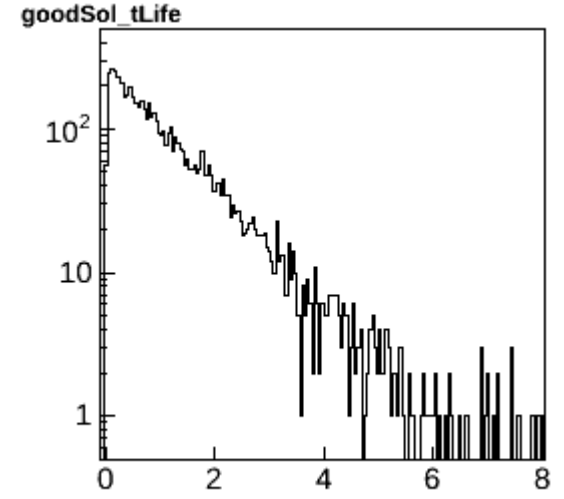
both $\tau \rightarrow \pi \nu$



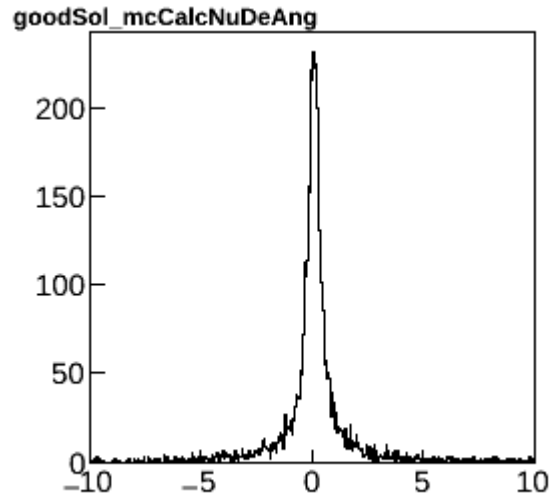
$\log_{10}(pT)$ at best solution [GeV]



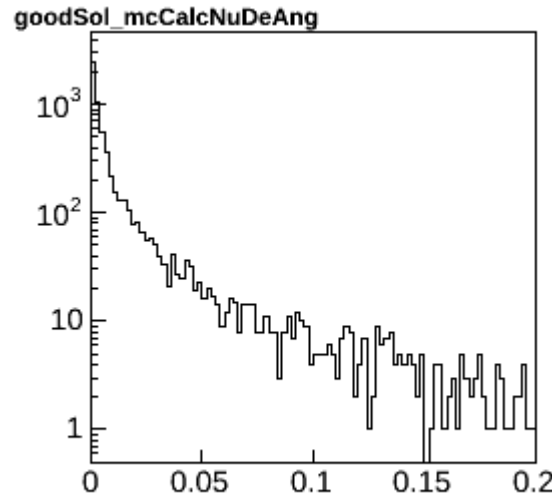
tau-tau mass [GeV]



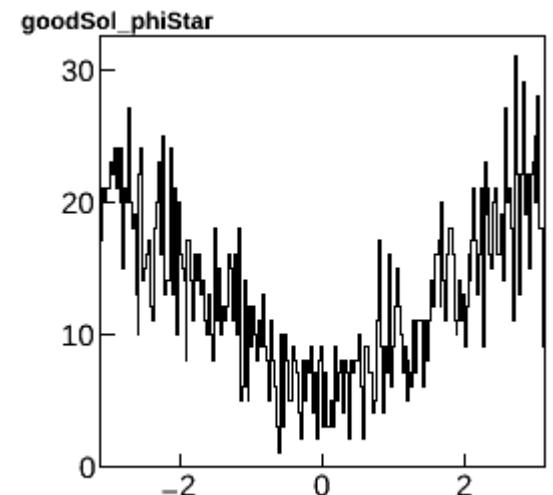
reconstructed lifetime/
87 $\mu\text{m}/c$



difference between true
and reco neutrino energy [GeV]



angle between true and
reco neutrino [rad]



angle used to
measure Higgs CP

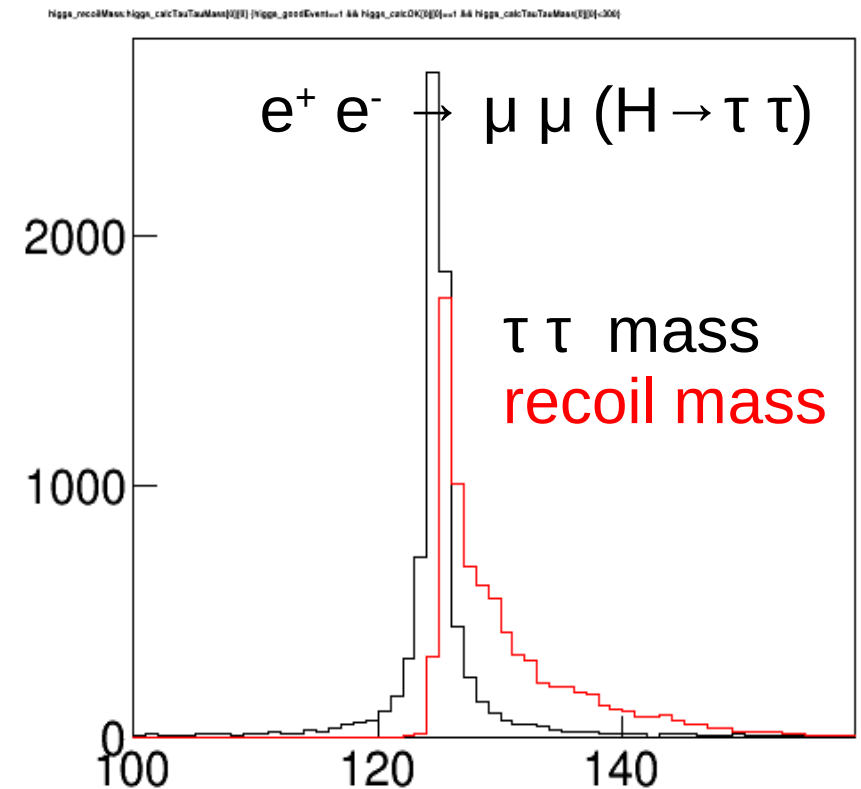
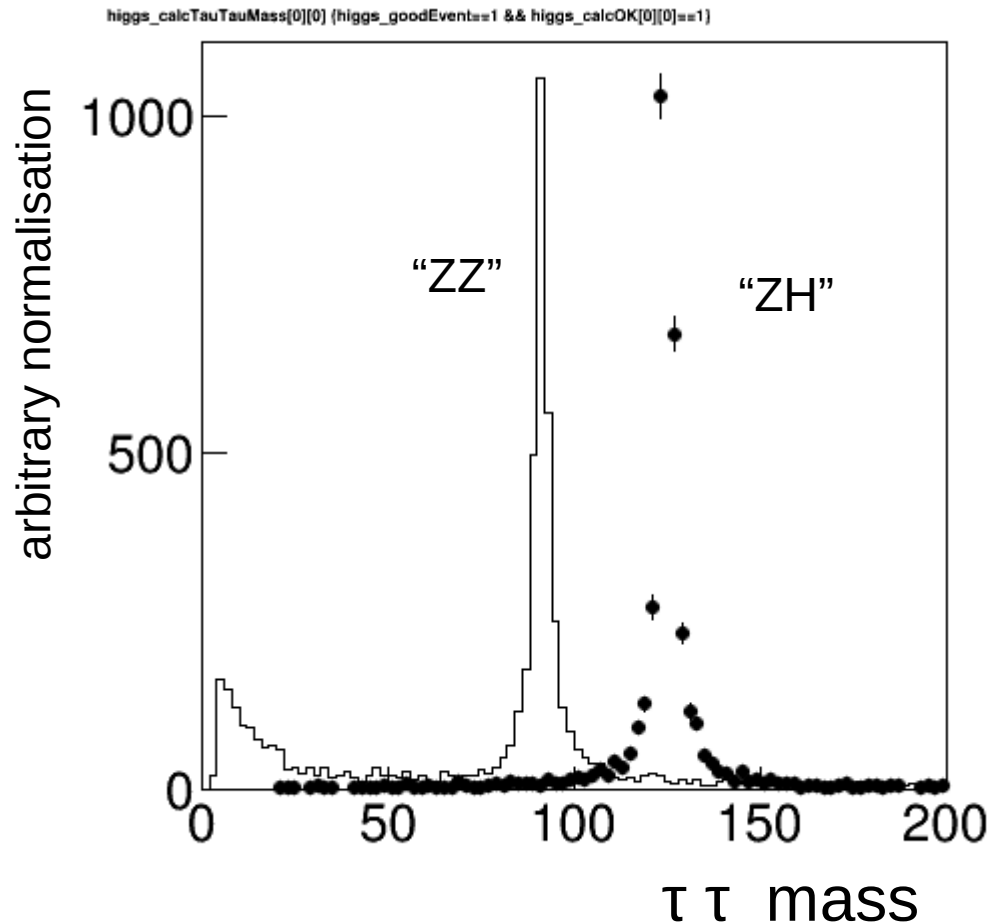
compare

$$e^+ e^- \rightarrow \mu \mu (H \rightarrow \tau \tau)$$

to its major irreducible background

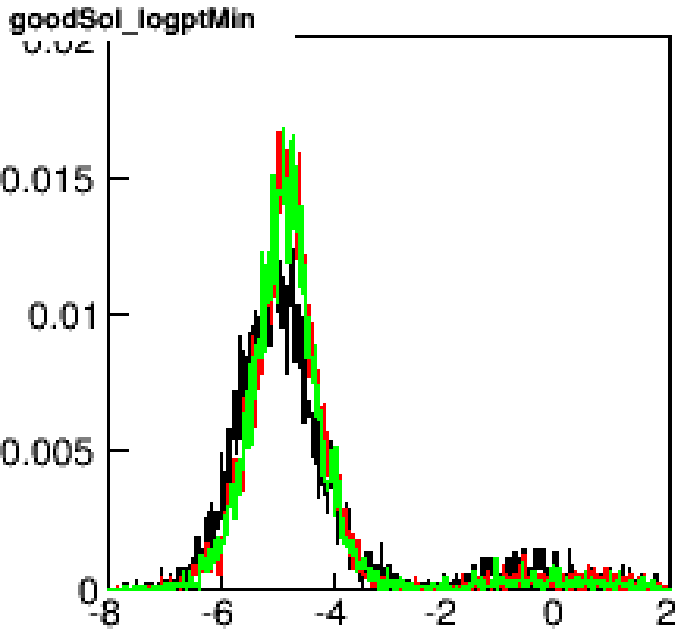
$$e^+ e^- \rightarrow \mu \mu \tau \tau$$

(without H contribution: Z, gamma*)

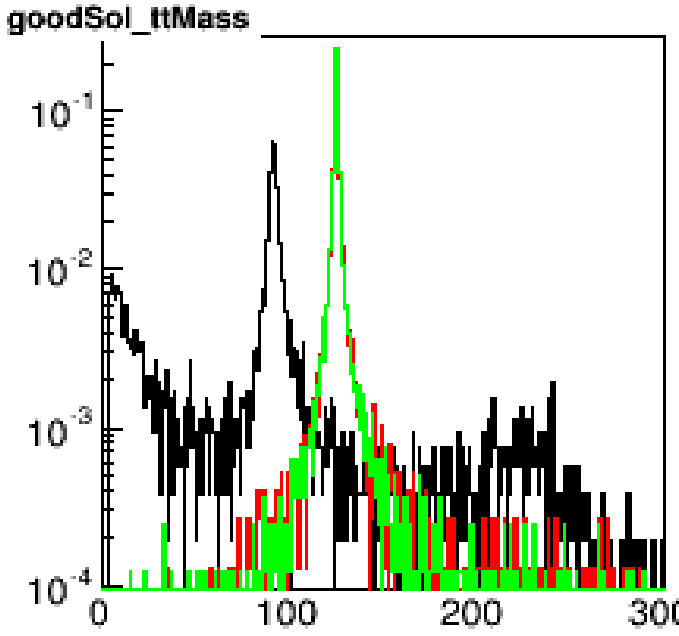


both $\tau \rightarrow \pi \nu$

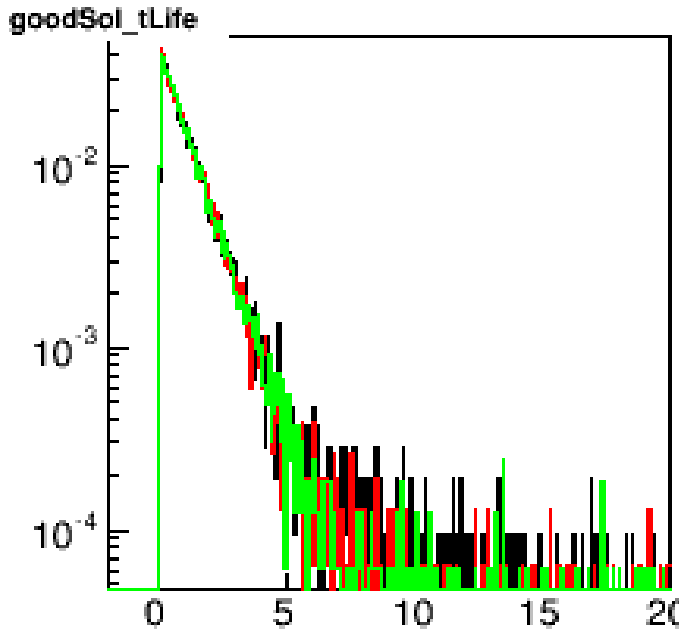
arbitrary normalisation



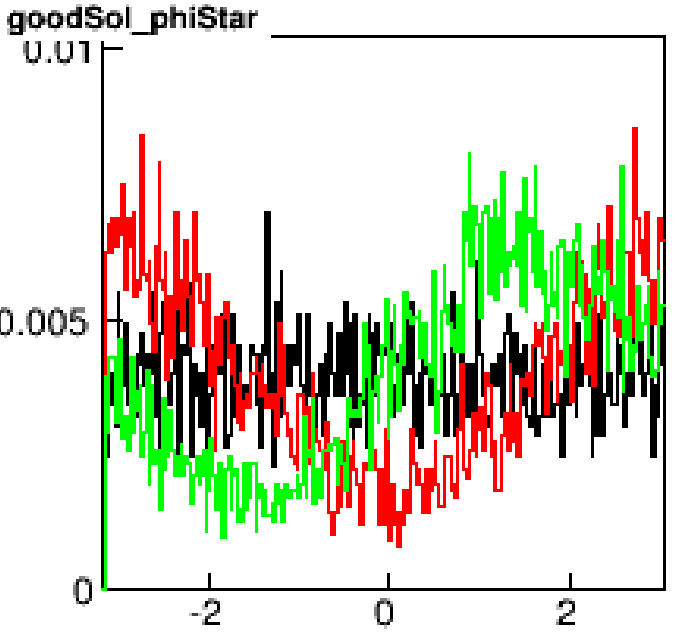
pT at minimum



tau-tau mass



reconstructed lifetime



CP-sensitive angle

CP⁺ Higgs
 $H = \cos(\pi/4) \text{CP}^+ + \sin(\pi/4) \text{CP}^-$
non-Higgs $\mu\mu\tau\tau$

Summary

method to fully reconstruct hadronic tau decays

needs:

- good vertex detector

- precise knowledge of IP

- no extra neutrinos in event

no assumption on:

- tau-tau mass

- tau-tau centre-of-mass

- ISR/beamstrahlung

Demonstrated in $\tau^+ \rightarrow \pi^+ \nu$

now working on $\tau^+ \rightarrow \pi^+ \pi^0 \nu$

Then proceed to full CP analysis

backup slides

Motivation:

the Higgs decays to

ZZ , WW , $\tau^+\tau^-$, converted photons

are particularly interesting, because spin state of W , Z , τ , photon
are reflected in the distribution of its decay products

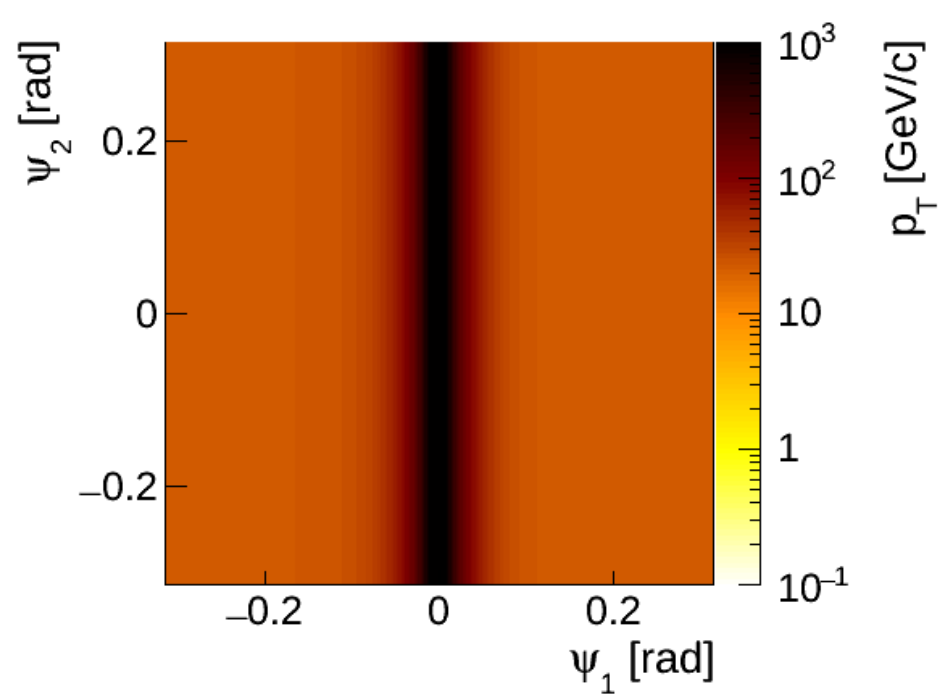
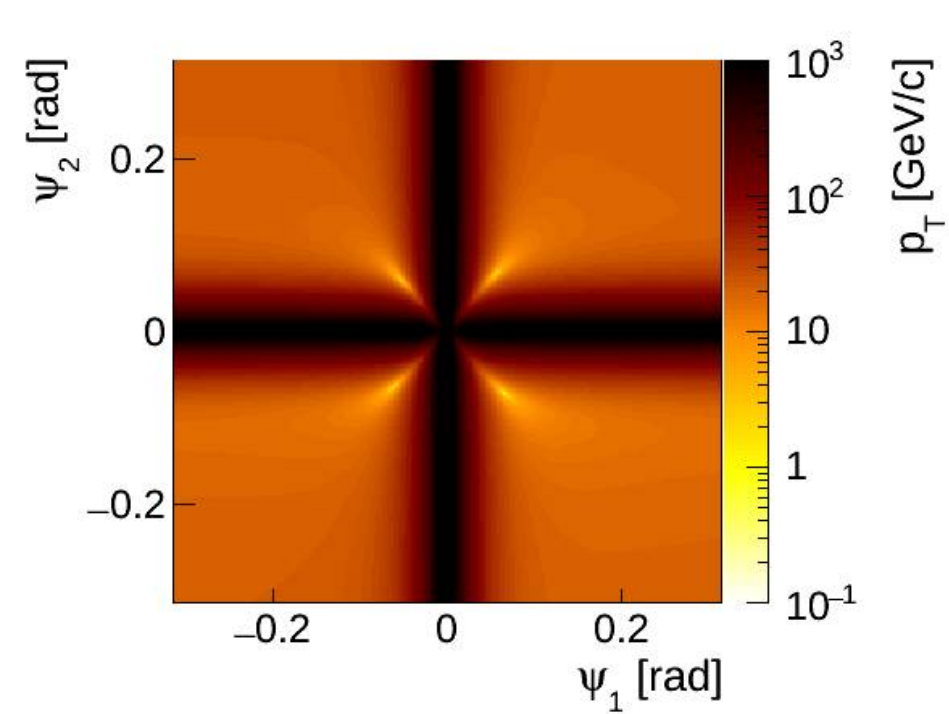
This allows measurement of *e.g.* Higgs CP properties

$$H = \cos\varphi (\text{CP}+) + \sin\varphi (\text{CP}-)$$

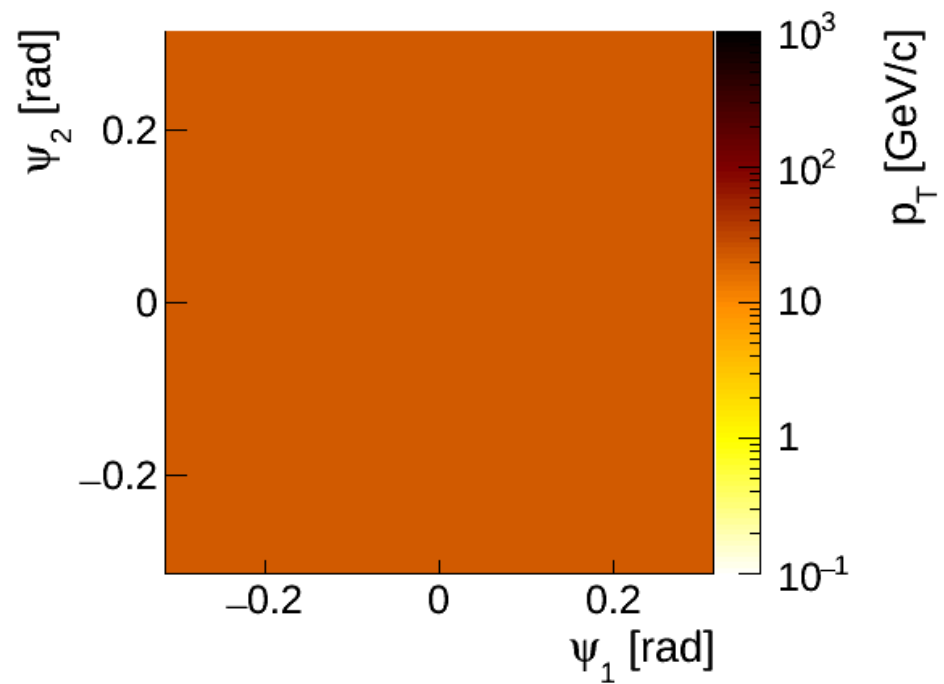
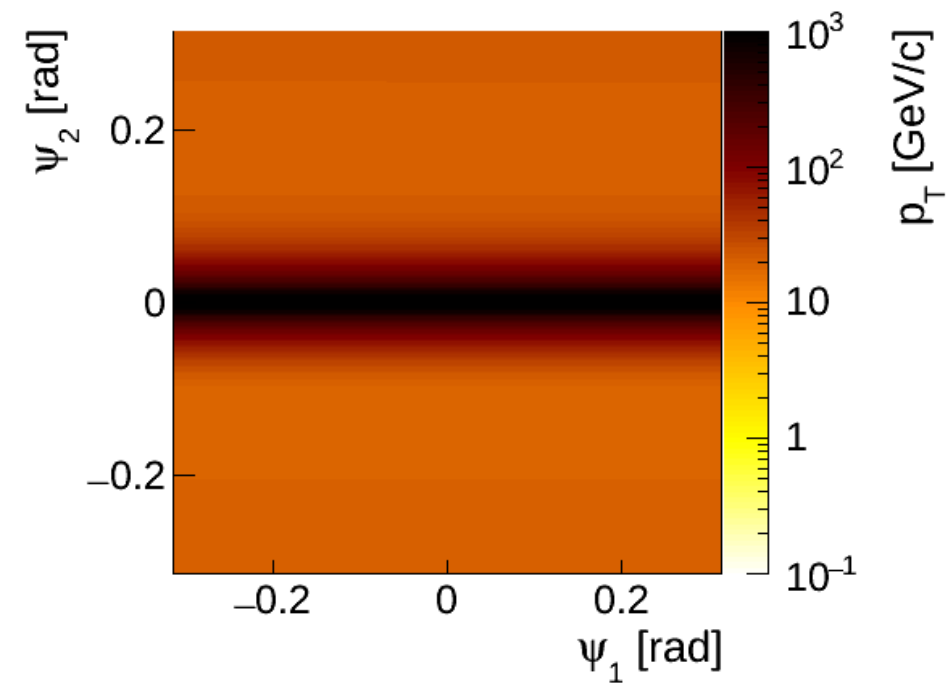
$H \rightarrow \tau^+\tau^- \sim 6\%$ for $m_H = 125 \text{ GeV}$

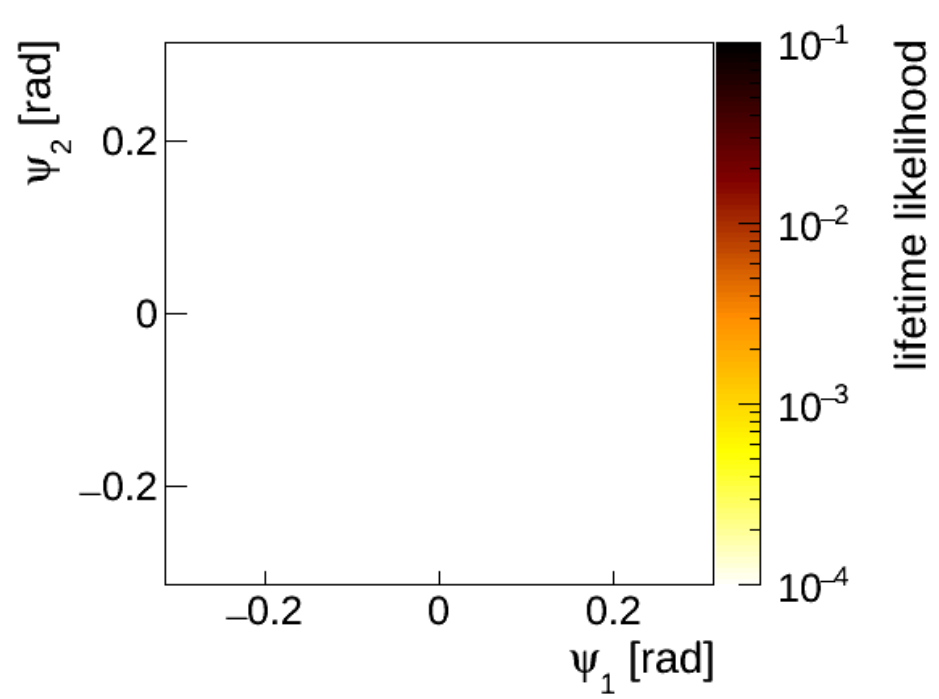
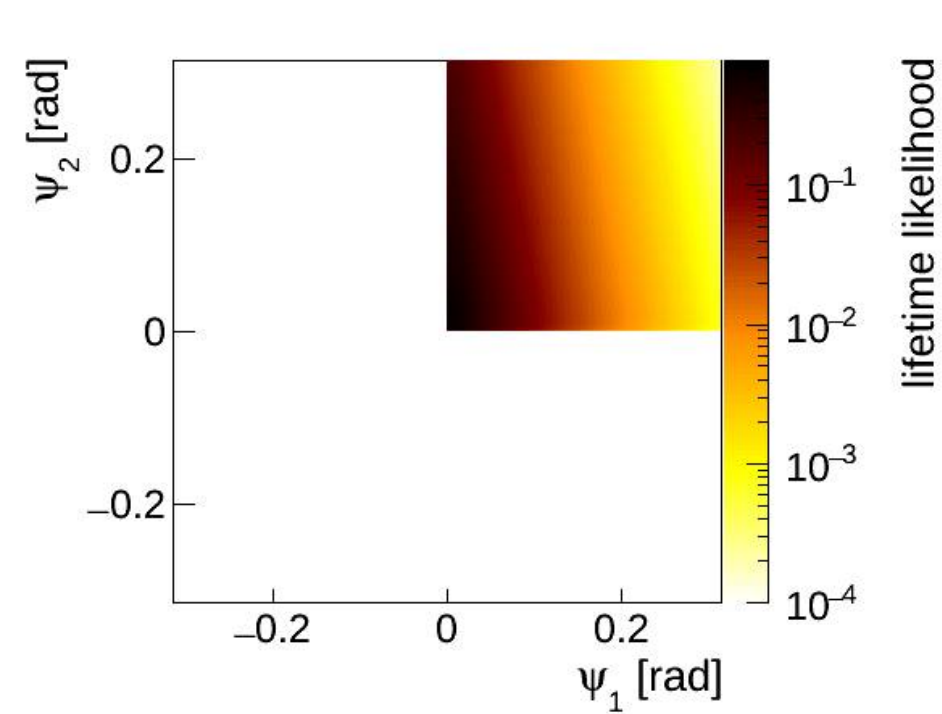
~ 2 times larger than ZZ

fermionic

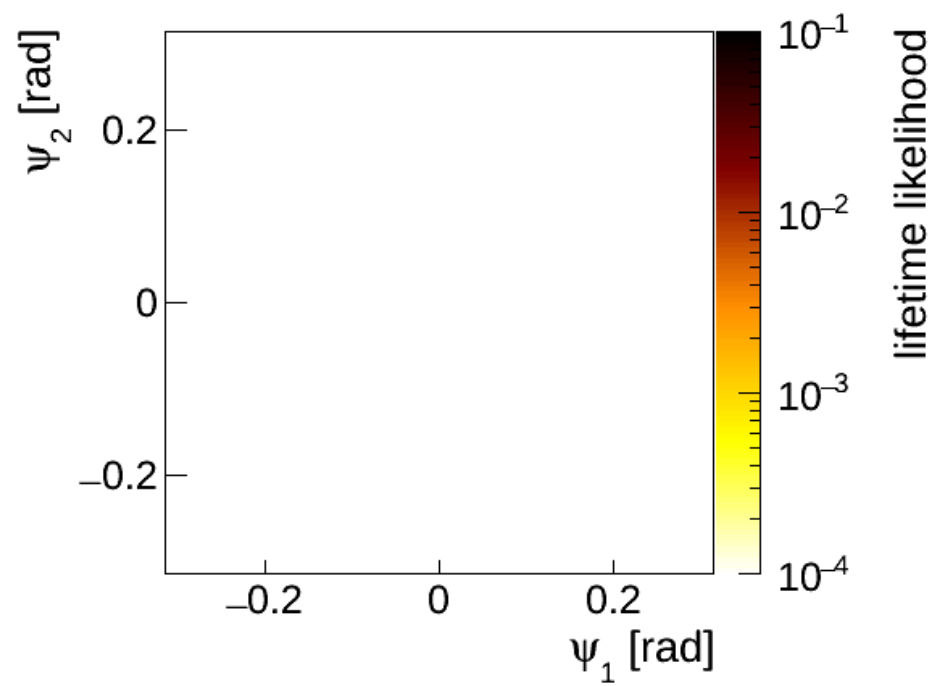
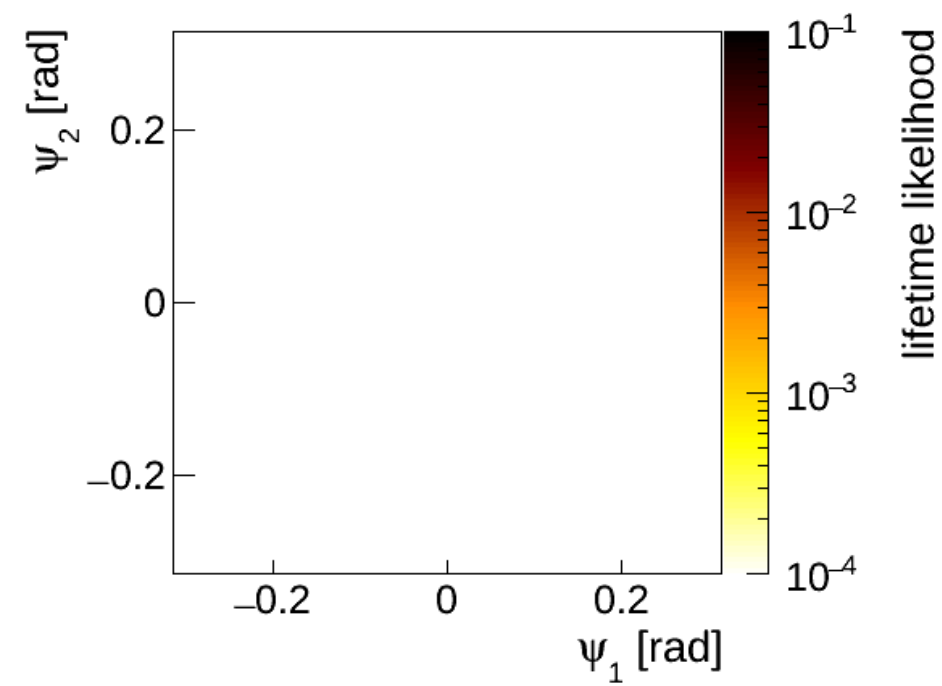


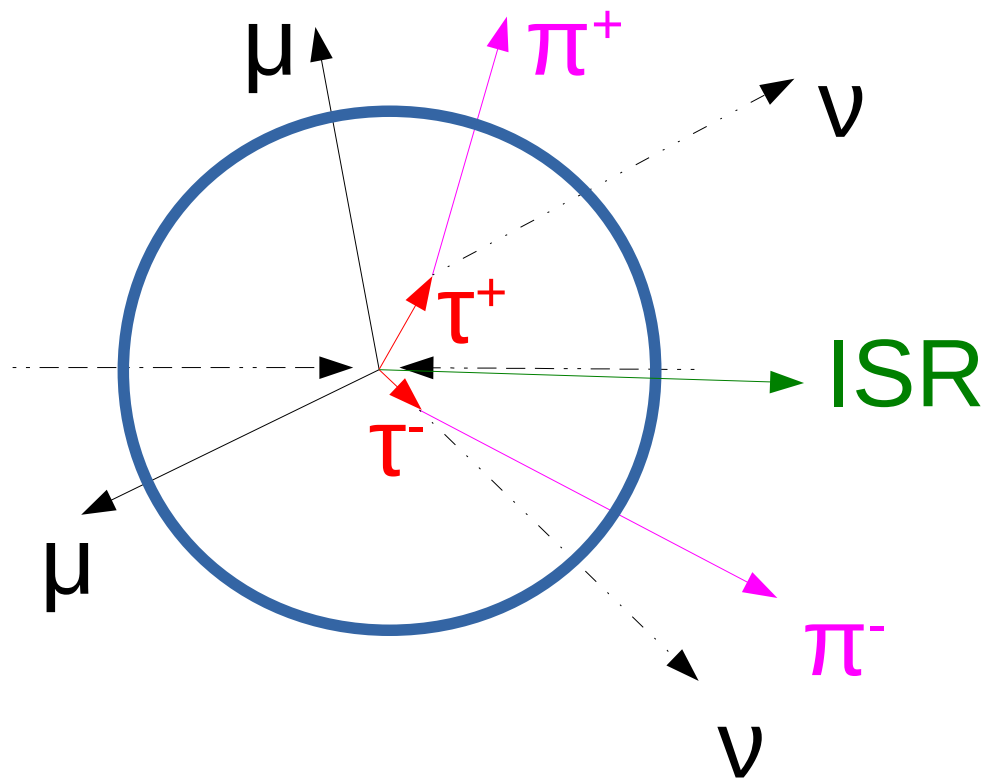
2x2 Q solution combinations for one event





2x2 Q solution combinations for one event





Unmeasured quantities

2 x neutrino 3-momenta
lost ISR photons

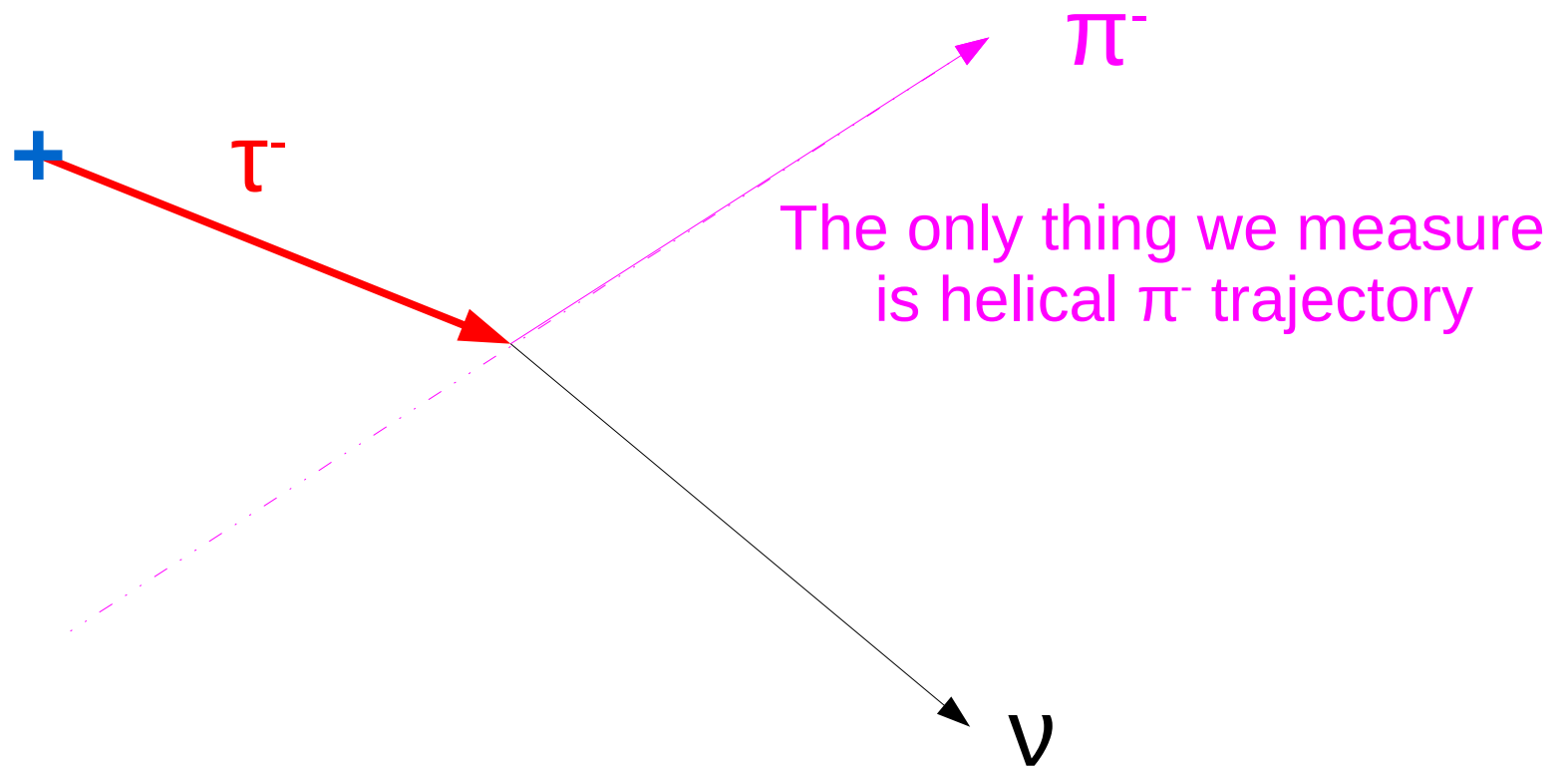
Kinematic constraints

overall 4-momentum conservation

2 x tau decay kinematics ← more details next

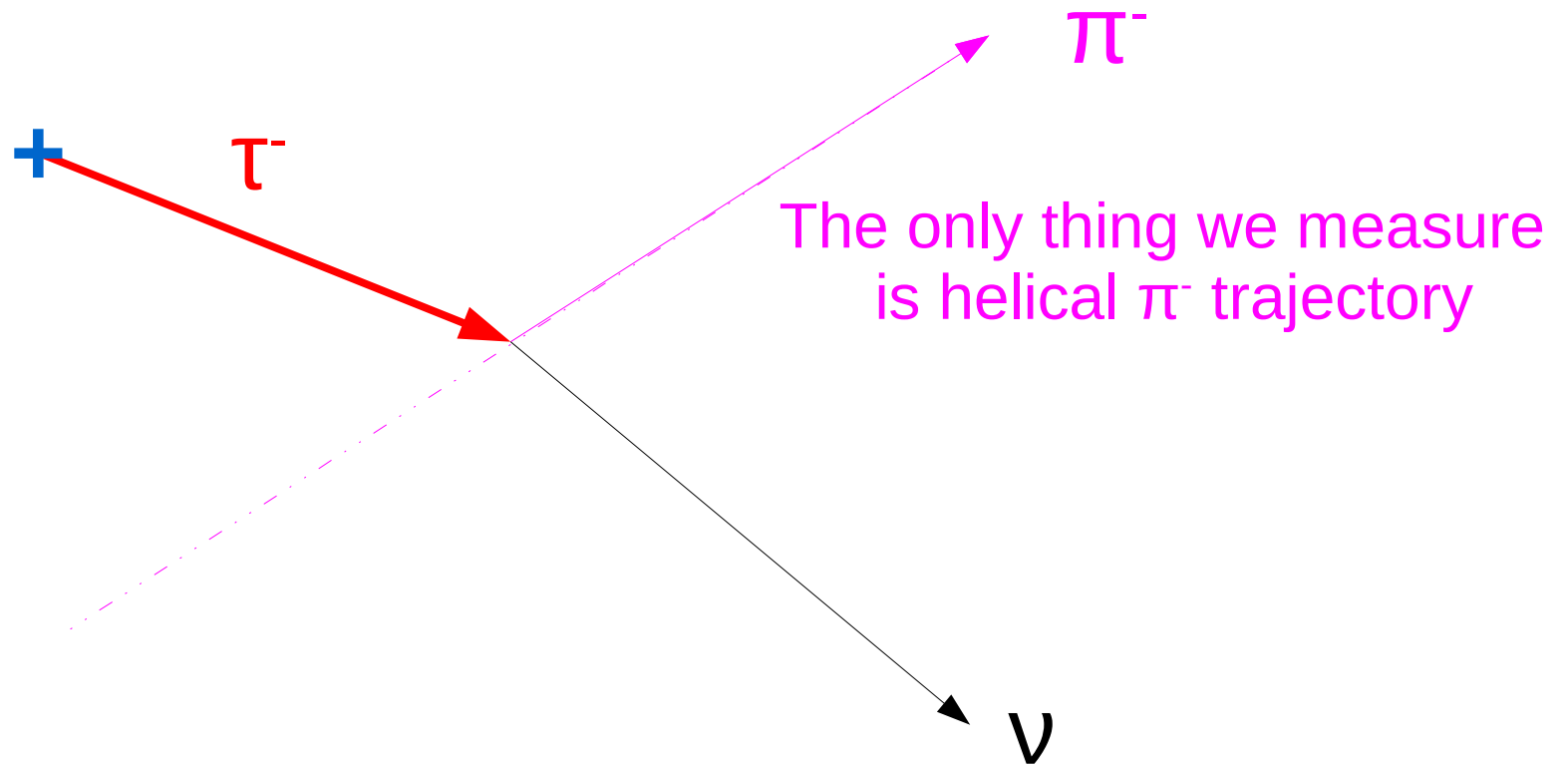
$\tau\tau$ mass (if we assume $H \rightarrow \tau\tau$)

$\mu\text{-}\mu$ mass not useful: resolution much better than Z width



We know that:

- endpoint of τ lies on pi- trajectory



We know that:

- endpoint of τ lies on π^- trajectory
- neutrino momentum lies in plane defined by τ^- and π^- momenta

Let's test these ideas:

private production of

$e^+e^- \rightarrow Z H \rightarrow \mu\mu \tau^+ \tau^-$ events

Whizard 2.2.2,

with ISR, beamstrahlung (also samples without)

250 GeV centre-of-mass

eL pR beam polarisation

τ decay to pi-neutrino only

Tauola 1.1.4,

with correct spin correlations

simulated in ILD detector (Mokka)

ILD_o1_v06 detector model

ilcsoft v01-17-04 reconstruction

use tracks from MarlinTrkTracks collection

PID by MC cheating (for now)

ISR properties

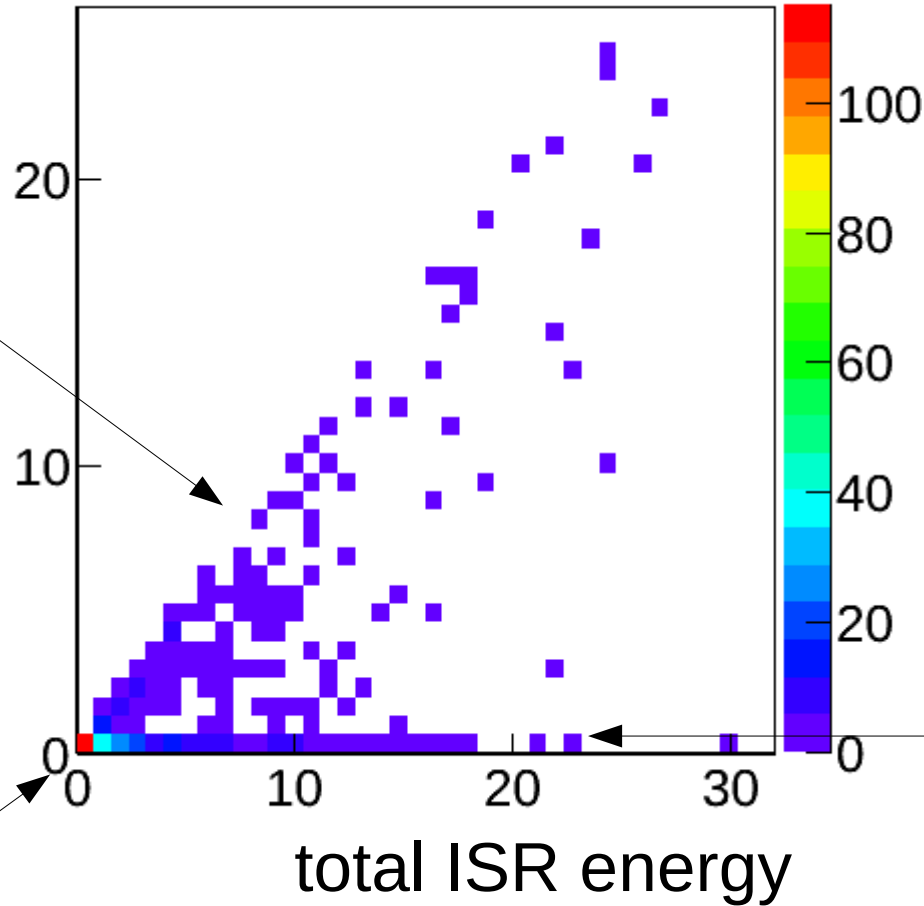
actually ISR + beamstrahlung

- total Energy
- invariant mass of sum of all ISR/BS photons ← zero if only on one side
e.g. single ISR photon

$\sqrt{(\text{higgs_isrE})^2 - (\text{higgs_isrPz})^2} : \text{higgs_isrE}$

photons on both sides

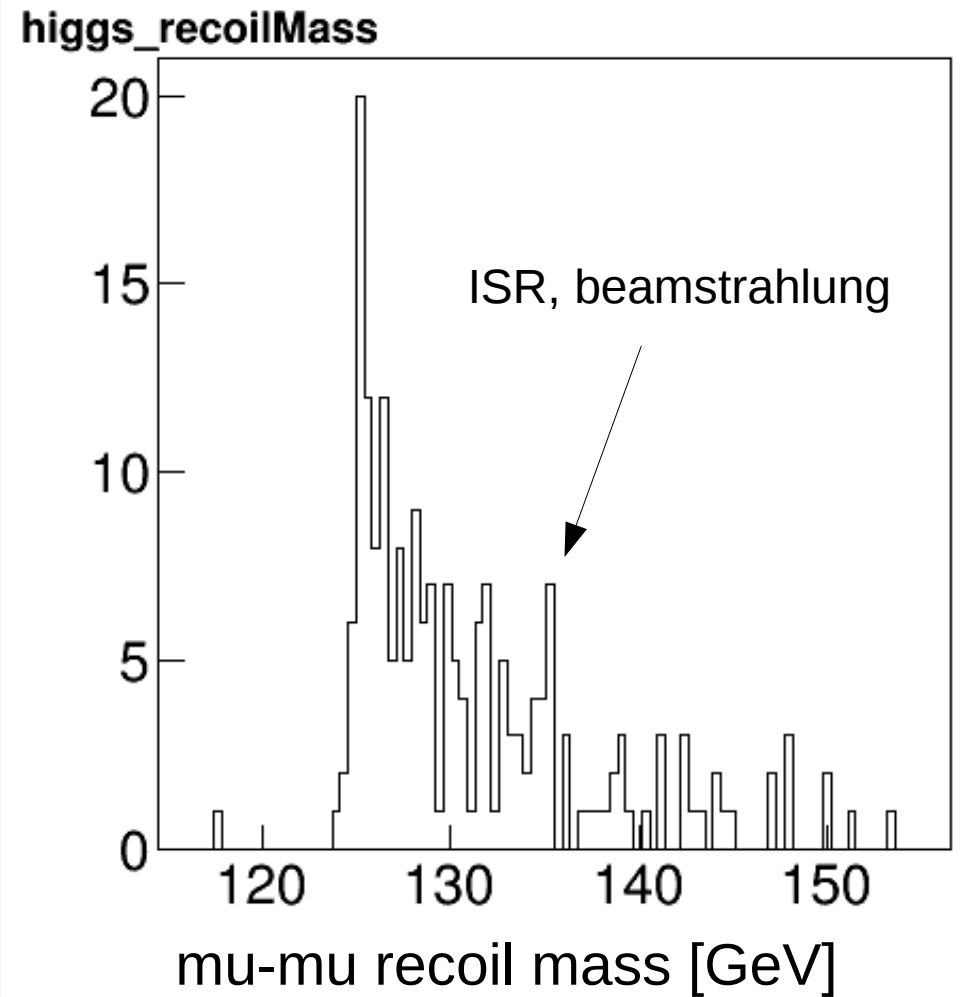
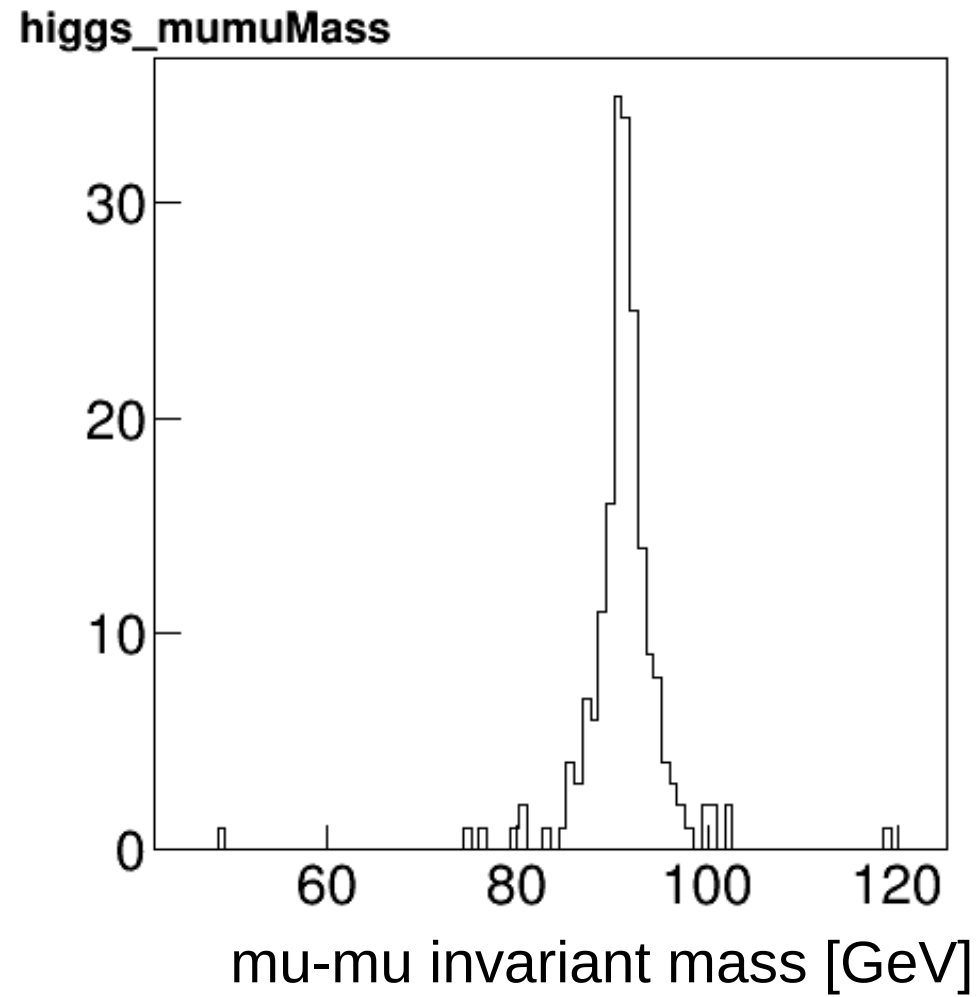
ISR invariant mass

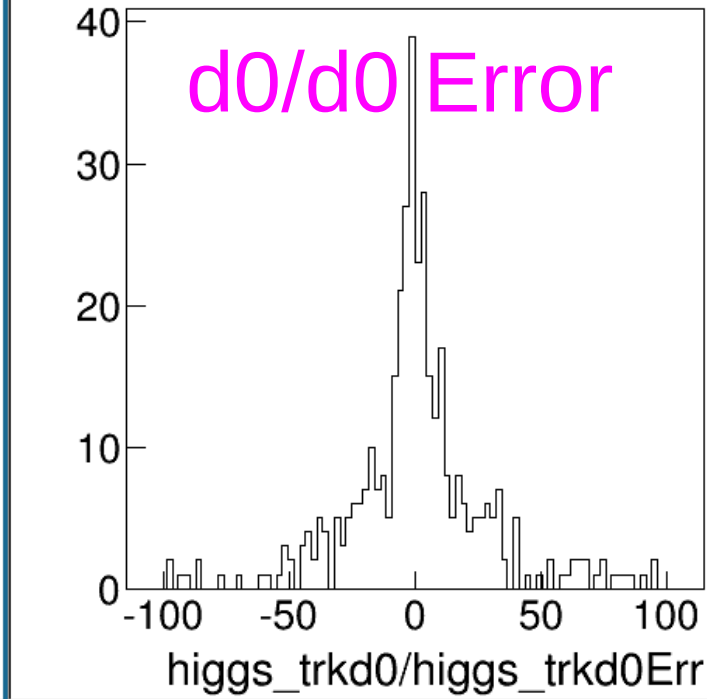
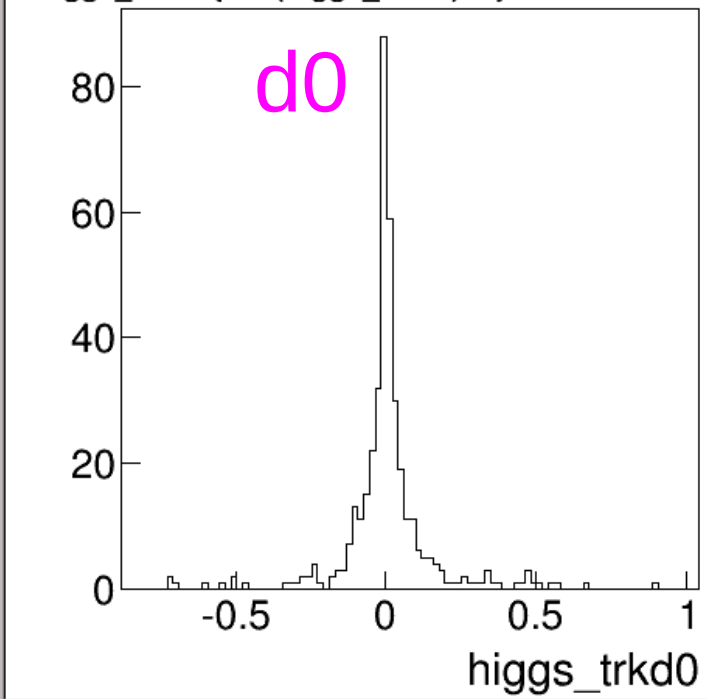
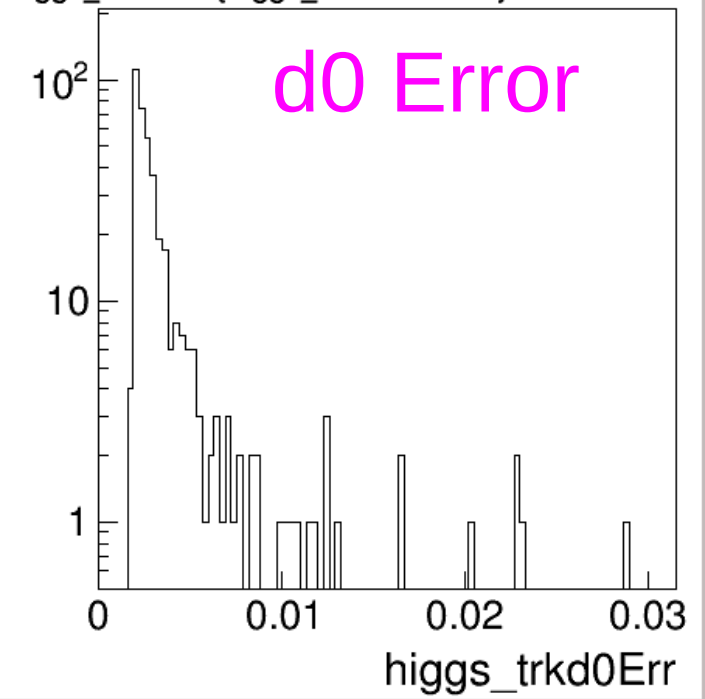


“significant”
photon(s) on
only one side

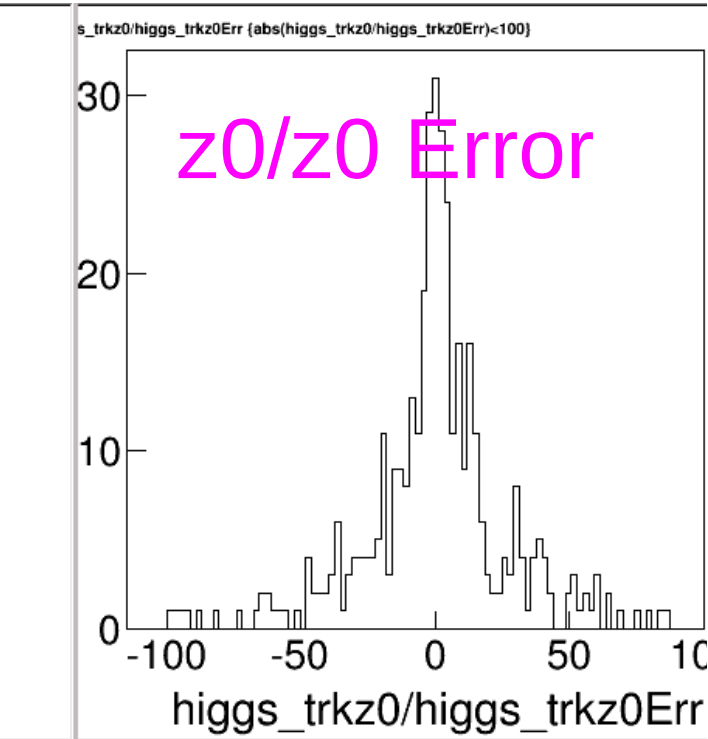
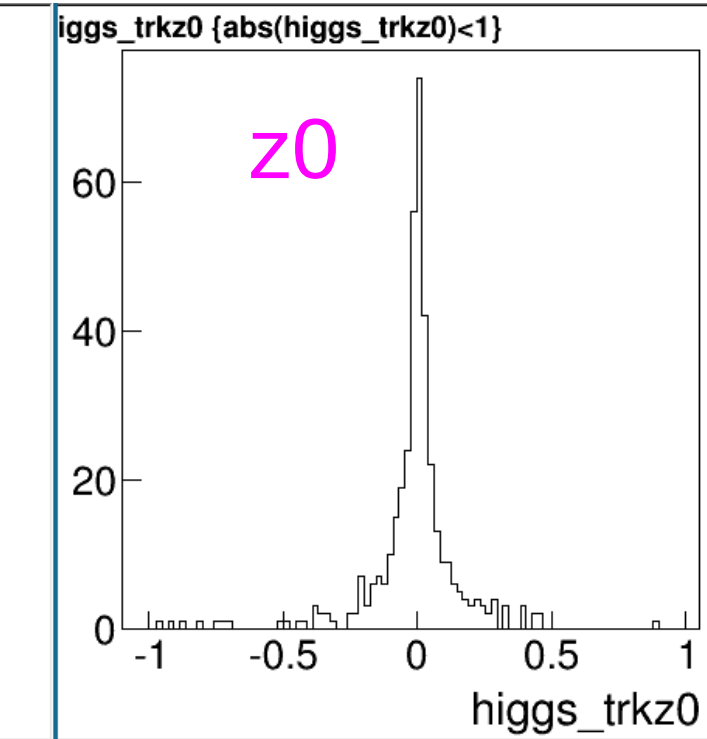
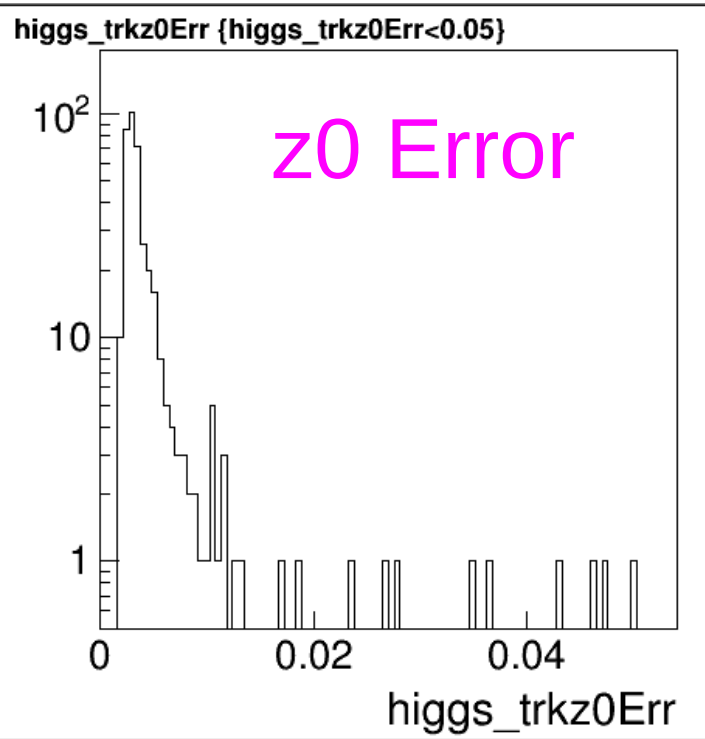
usually ISR ~ 0

the reconstructed muon tracks

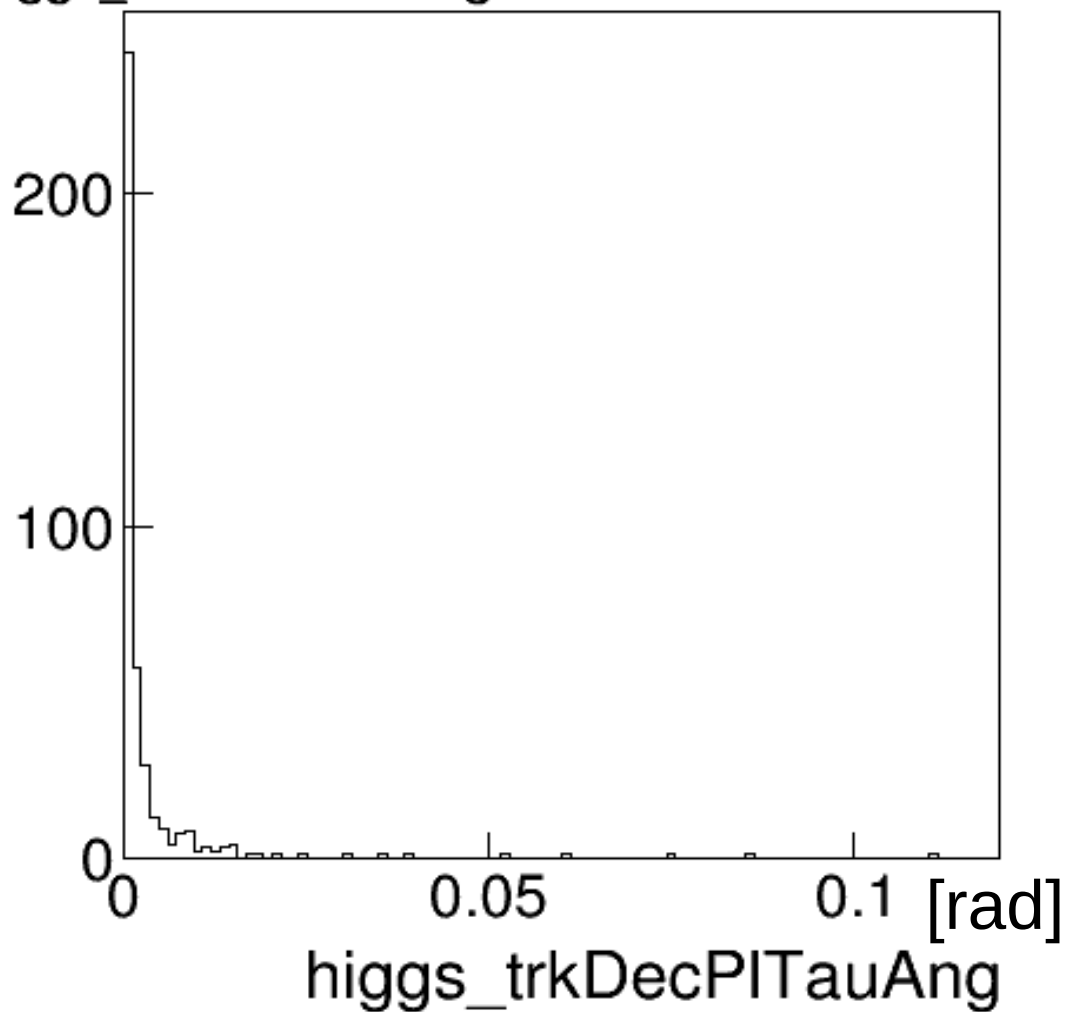




Charged pion track parameters [in mm]



higgs_trkDecPITauAng



Cross-check

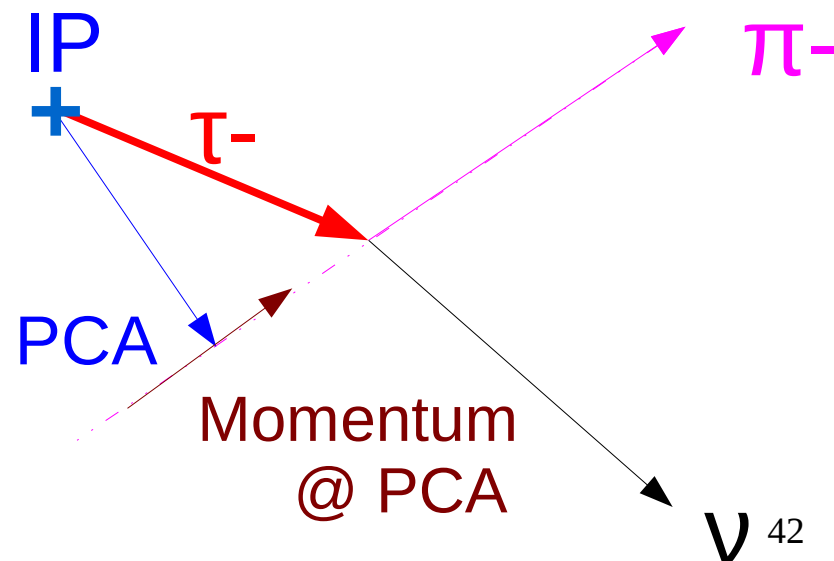
Angle between

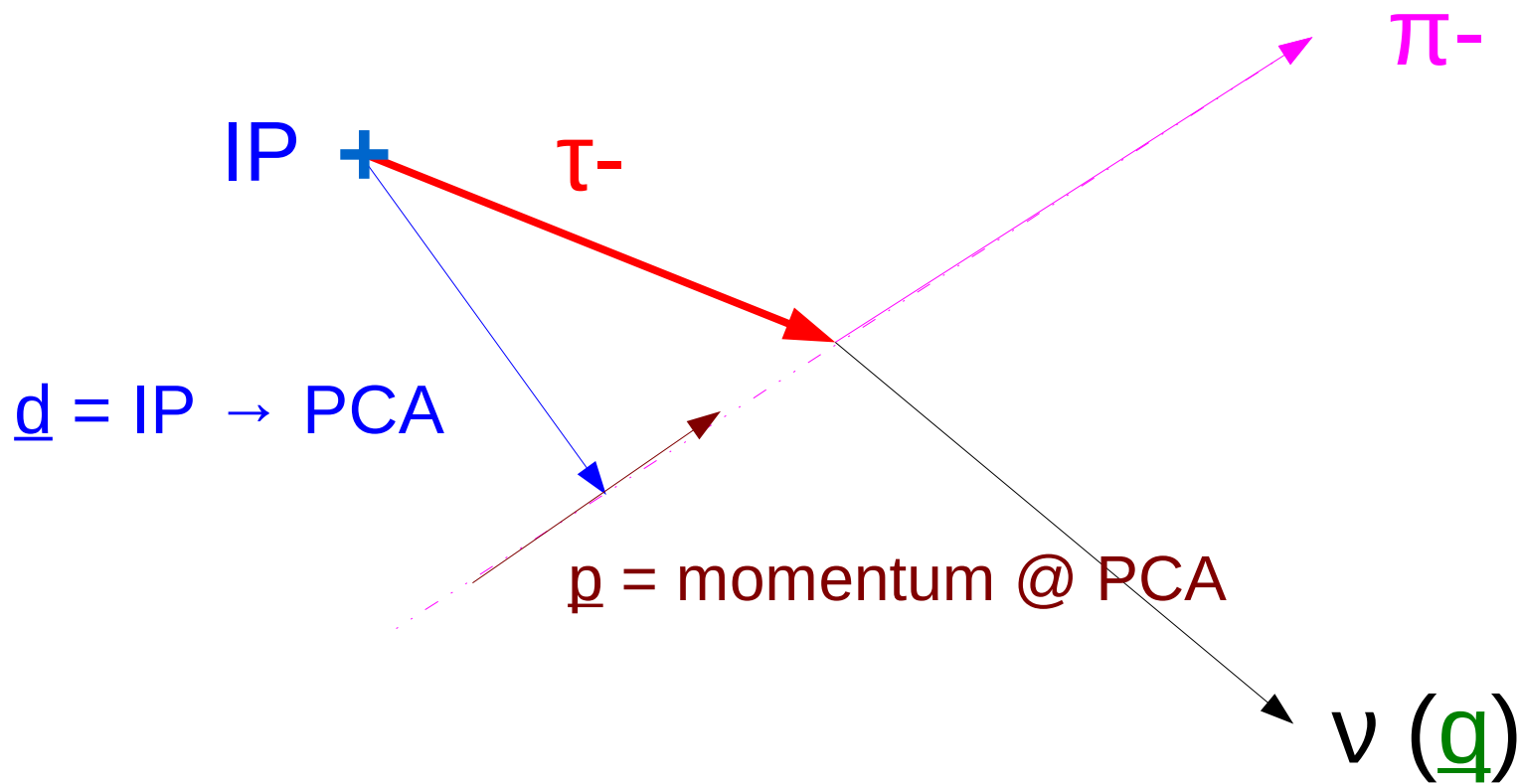
MC τ momentum

and

reconstructed plane of
pion track

(should ideally be 0)





\underline{d} and \underline{p} are perpendicular in x-y, but not in 3d

define $\underline{d}' = \underline{p} \times (\underline{d} \times \underline{p})$ ← inside p-d plane, perpendicular to p

neutrino momentum \underline{q} lies in plane of \underline{d} and \underline{p}

so we can write: $\underline{q} = |\underline{q}| (\cos\psi \underline{p}^* + \sin\psi \underline{d}'^*)$

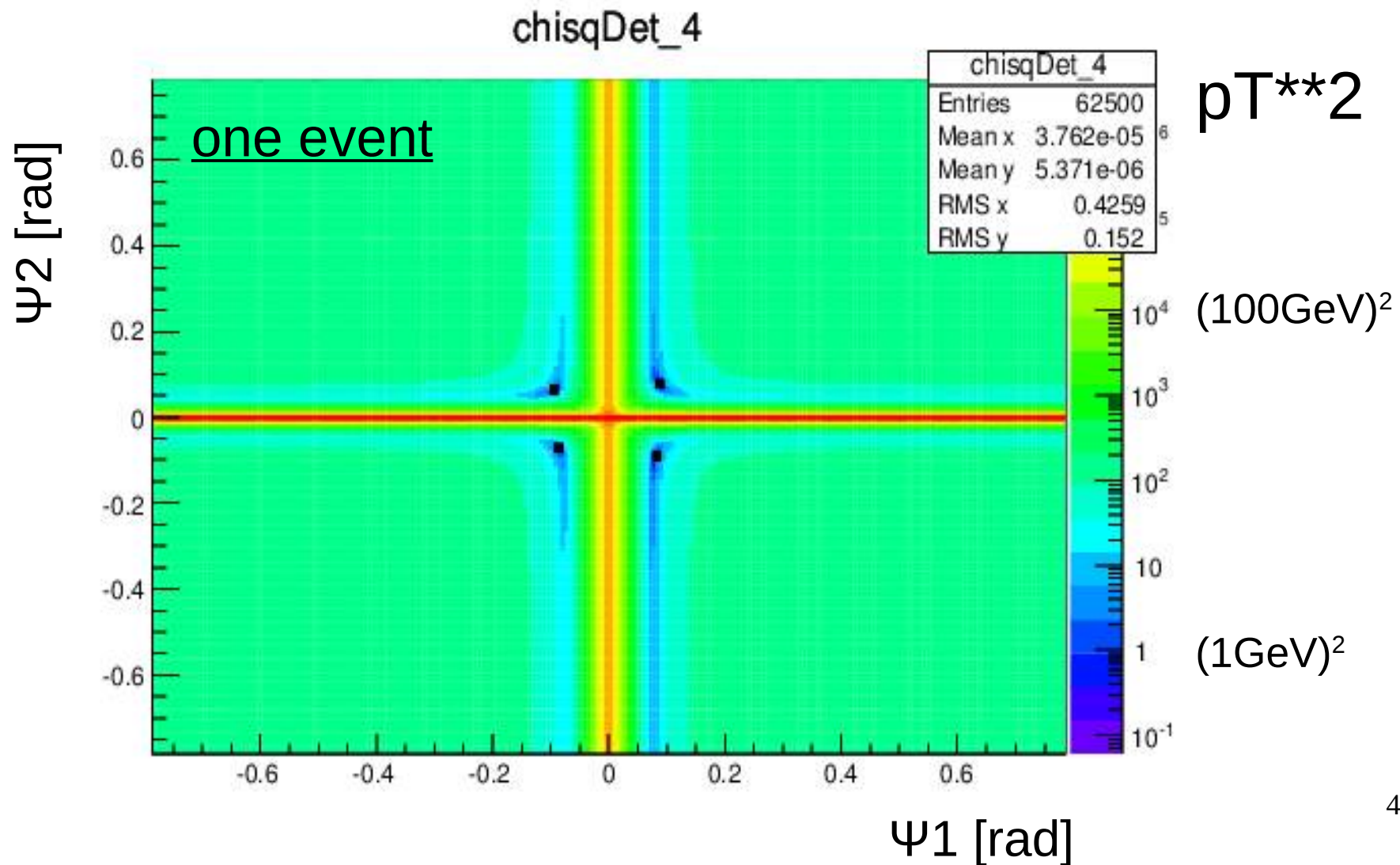
where \underline{x}^* is a unit vector: $\underline{x} / |\underline{x}|$

We know that the invariant mass of $(\underline{p} + \underline{q})$ is m_{tau}

so we can calculate the neutrino energy $|\underline{q}|$ for each value of ψ

For a given event, we can then see how the
total event p_T (muons, pions, neutrinos)
should be ~ 0 , even with lost ISR
depends on the
angles ψ_1, ψ_2 (for the 2 taus)

For a given event, we can then see how the total event p_T (muons, pions, neutrinos) should be ~ 0 , even with lost ISR depends on the angles ψ_1, ψ_2 (for the 2 taus)

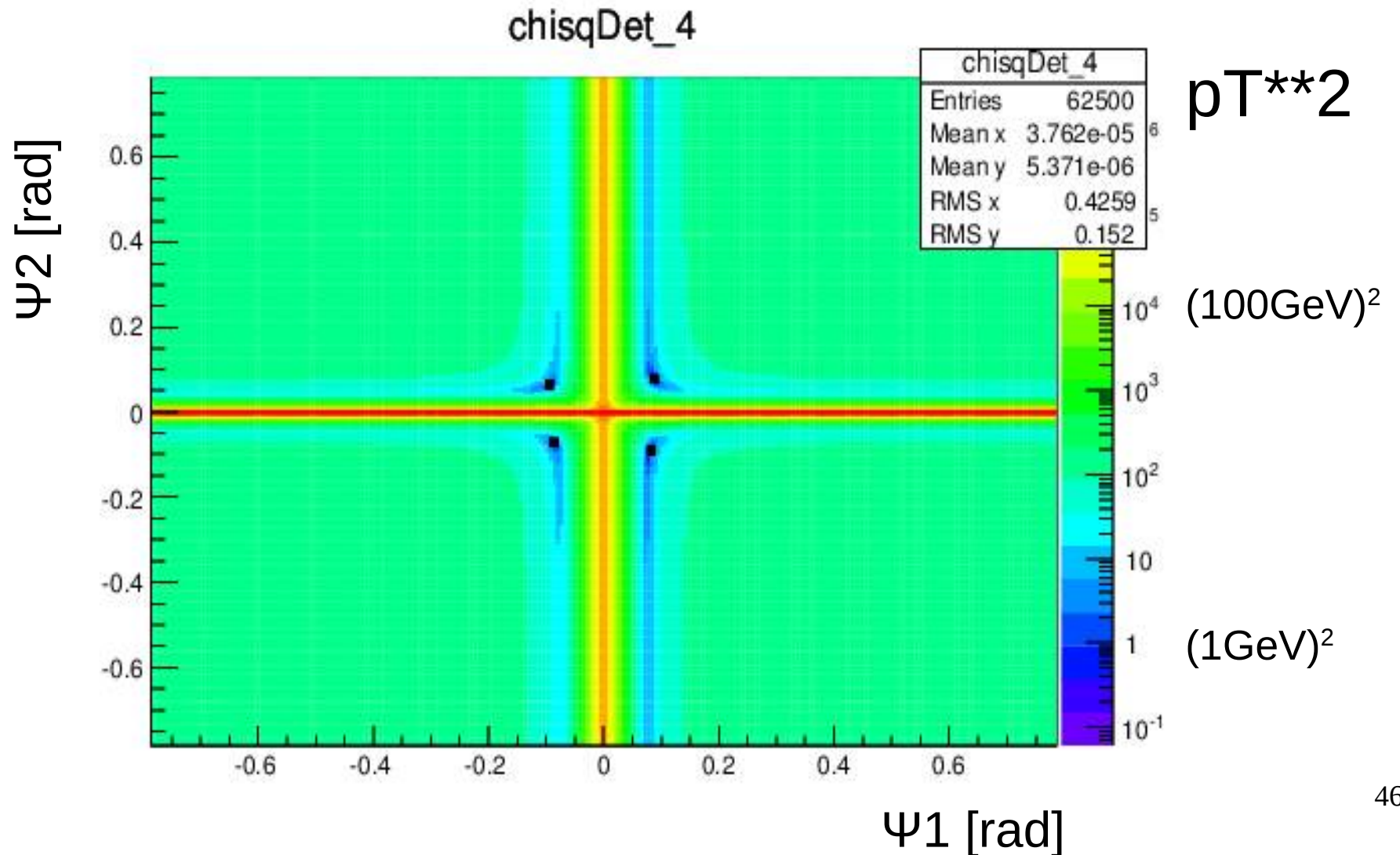


$\Psi = 0$ corresponds to neutrino colinear with pion
 needs large energy to make tau mass
 gives very large pt imbalance

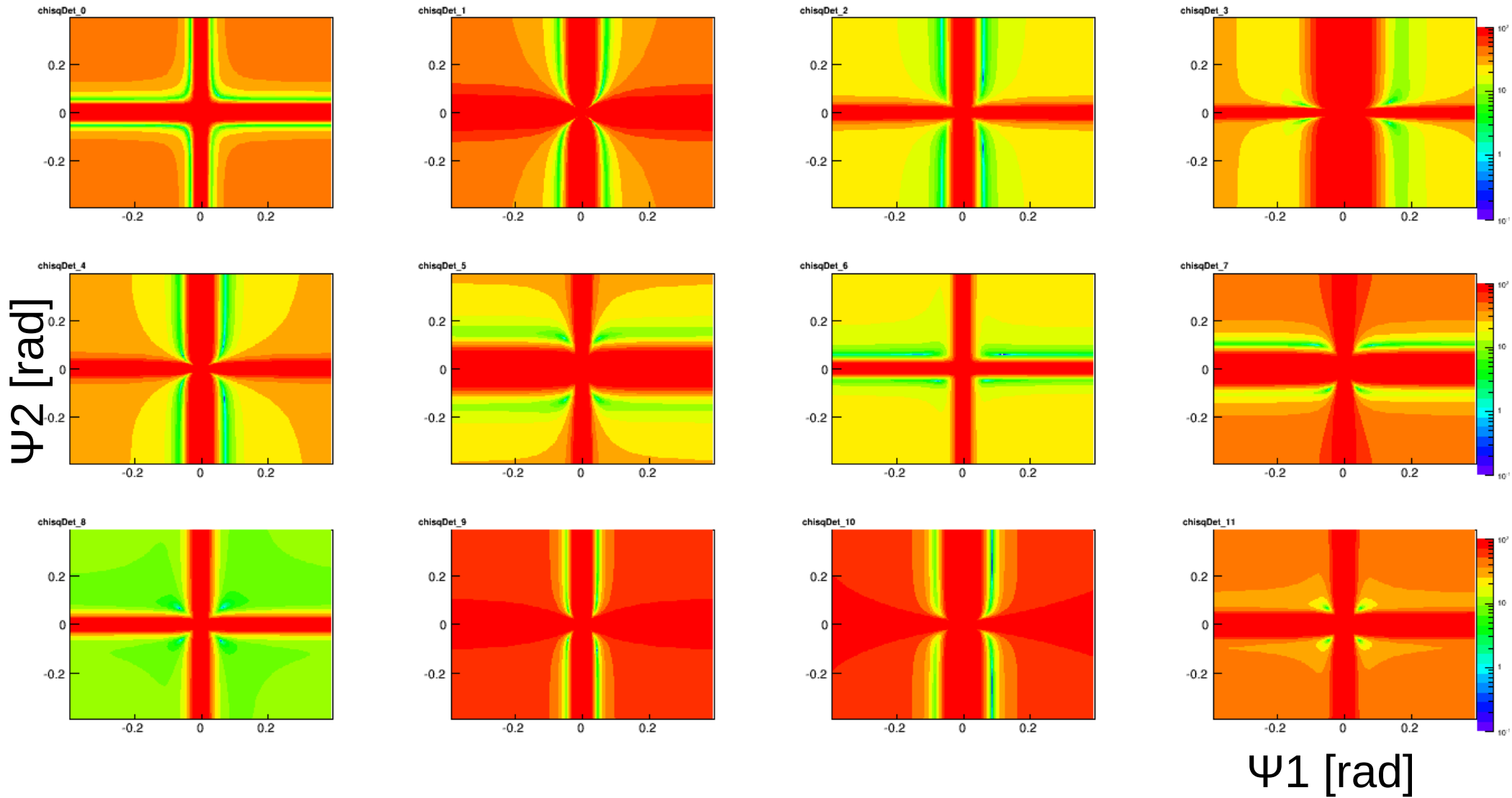
$$\underline{q} = |q| (\cos \psi \underline{p}^* + \sin \psi \underline{d}^*)$$

We can see local minima in each of the 4 quadrants

Is the nu momentum on the d = +ve or -ve side of the pion momentum

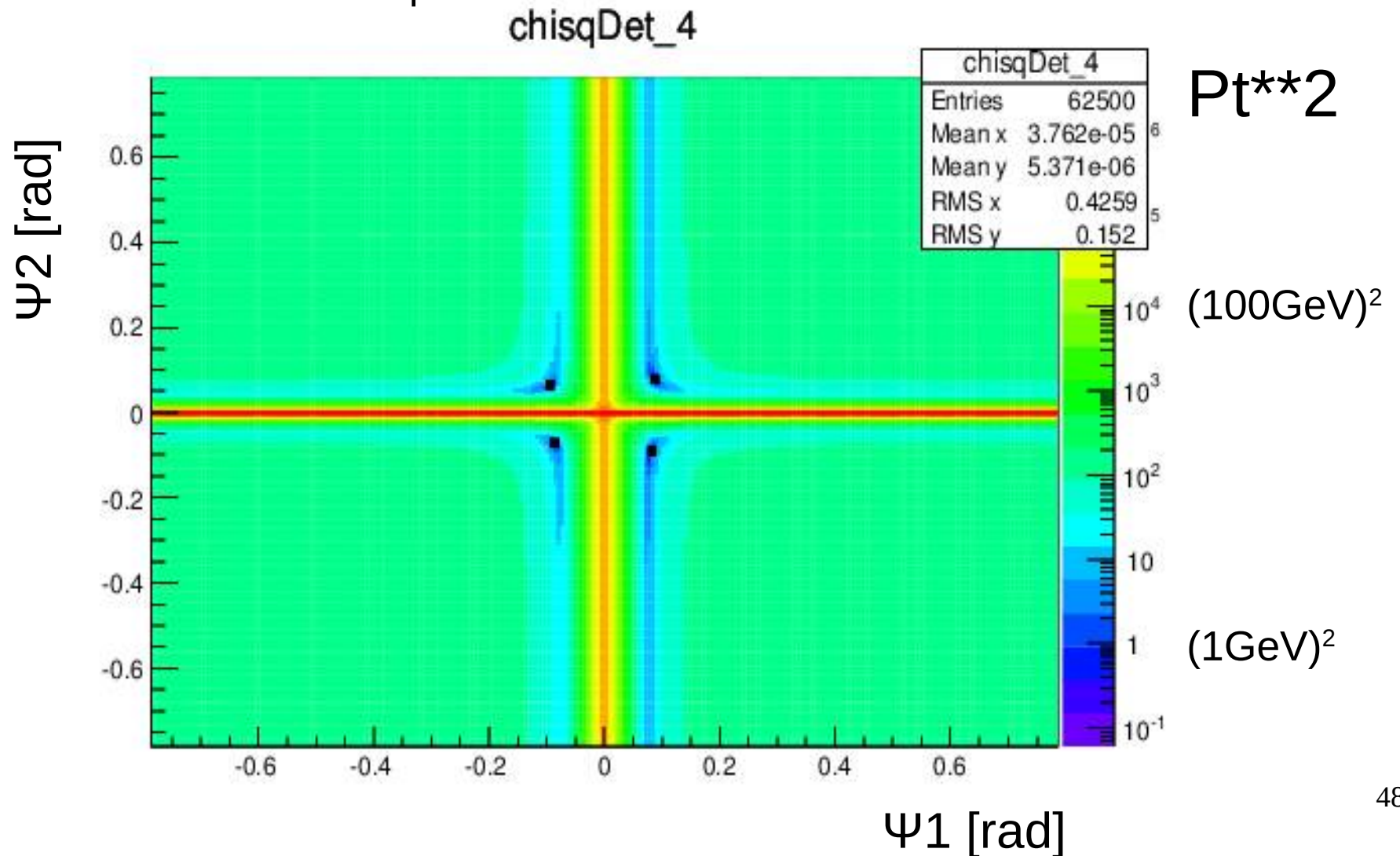


A few more events:



color = pT (0.1 1 10 100) GeV⁴⁷

by requiring pt-balance in the event [$\sum p_x = \sum p_y = 0$]
 it is possible (but somewhat messy) to calculate the angles Ψ
 due to finite resolution of measured quantities,
 a real solution is not always possible
 More robust approach is to do a
 standard minimisation [i.e. not a constrained fit]
 to minimise the event pT



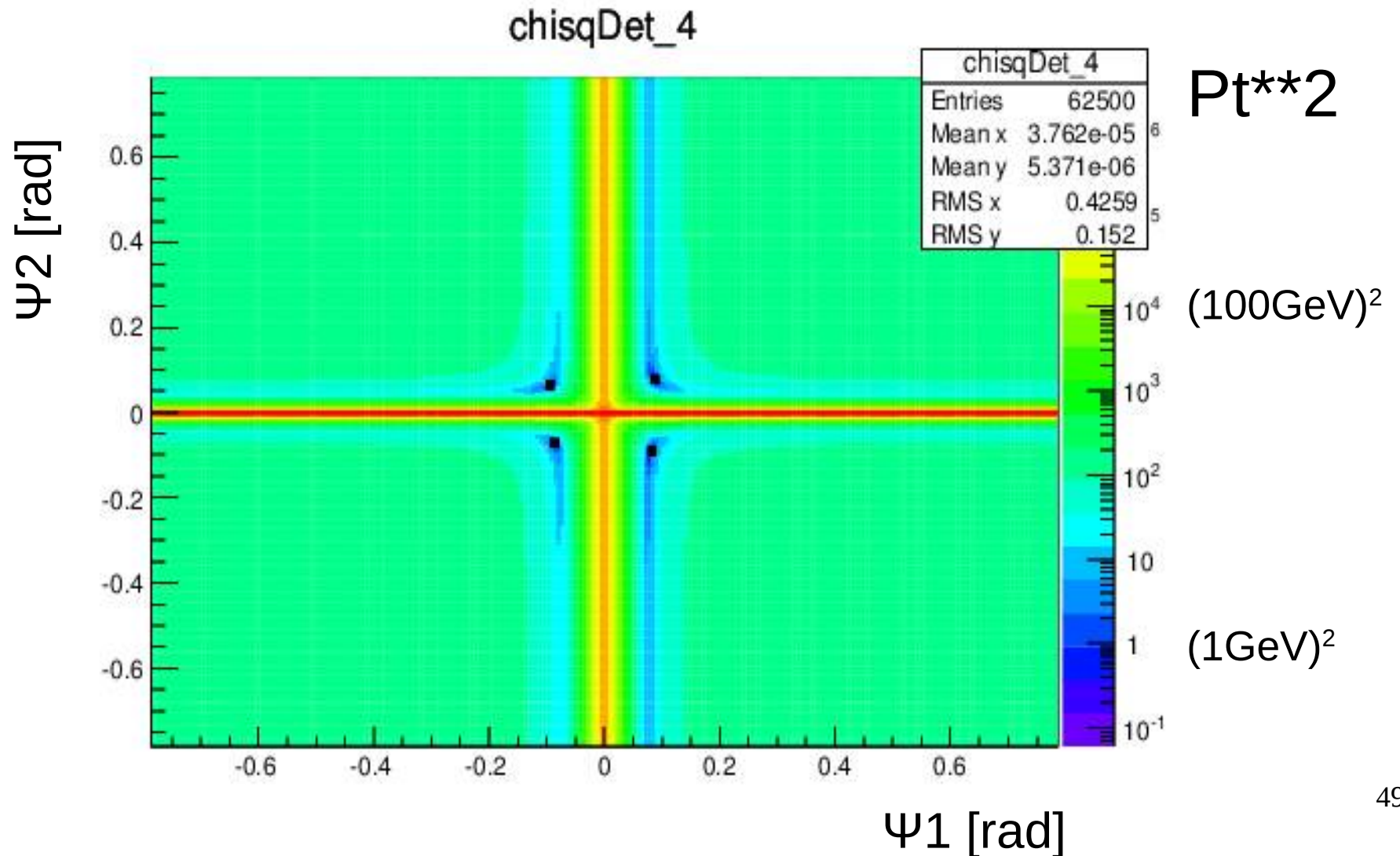
Minuit minimisation separately in each quadrant (no constraints needed)

→ Four solutions

How to choose which one is the best?

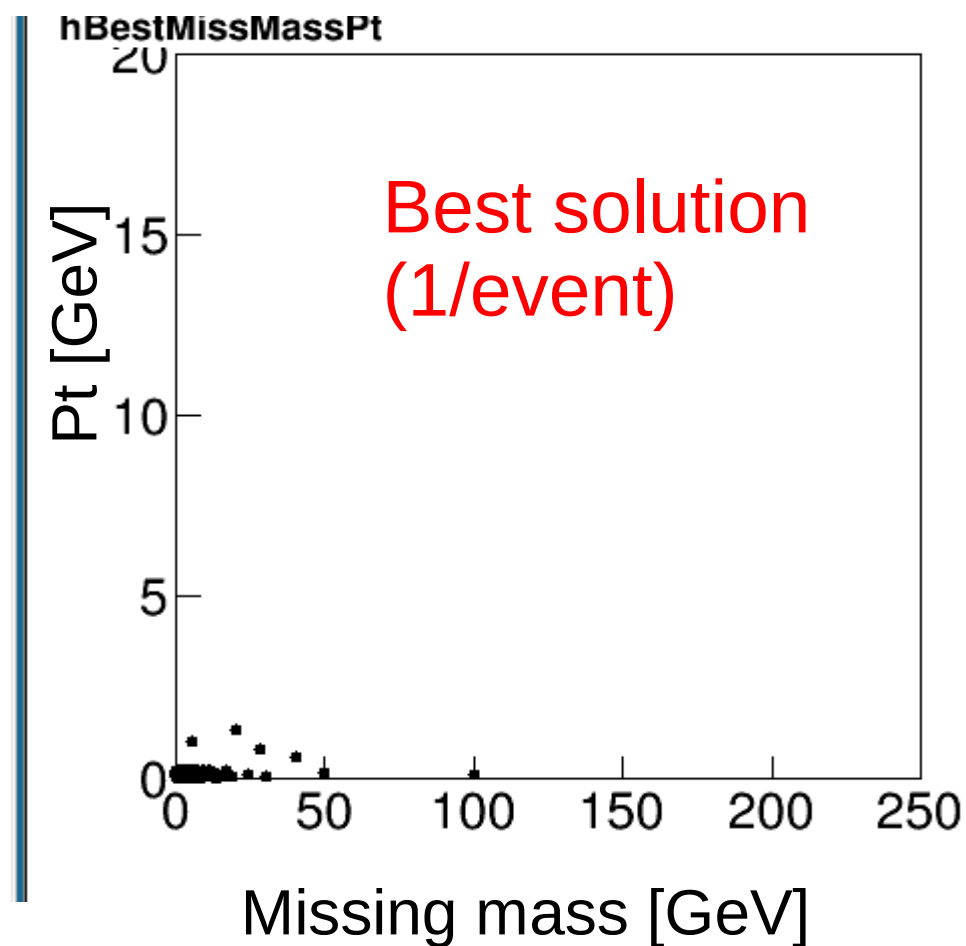
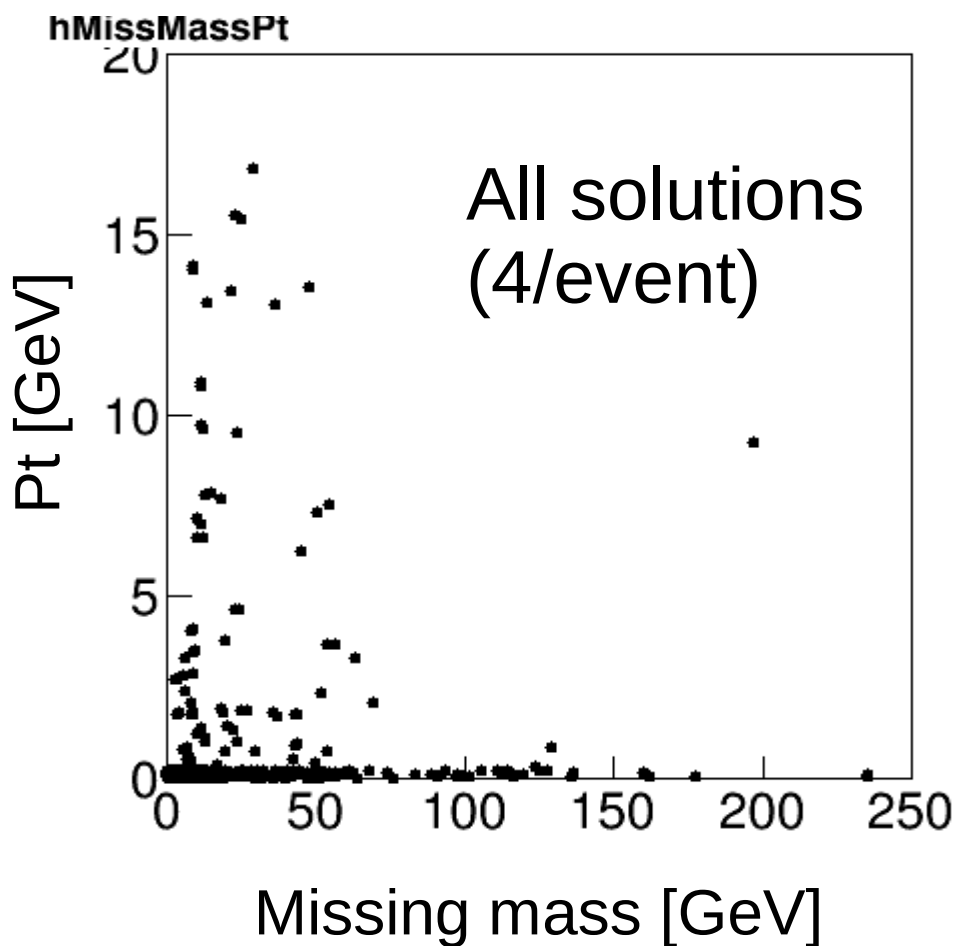
Value at minimum ← pt as small as possible

Comparison of $|p_z|$ and missing energy ← same, if 1 ISR photon
invariant mass of 2 taus (if we assume presence of Higgs)



For now, define “best” solution as one with smallest value of **pT + missing mass**

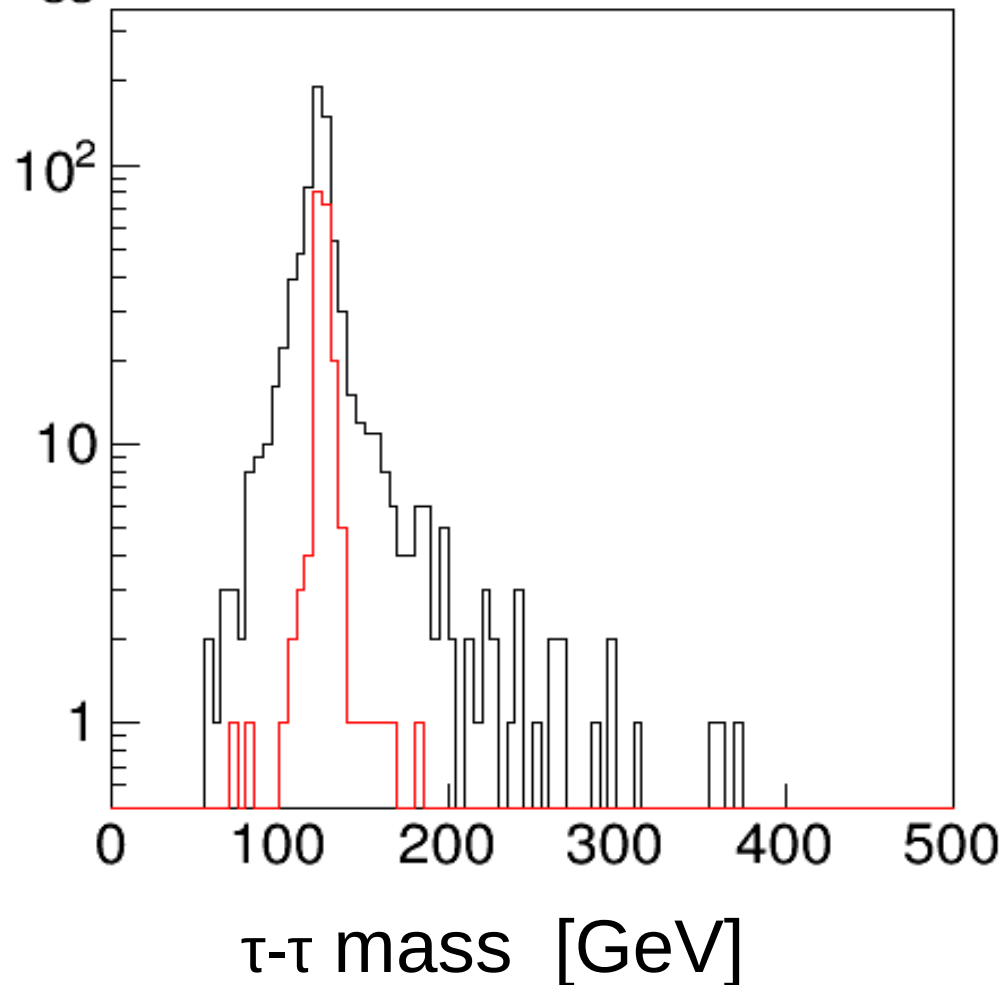
If we have zero or one ISR photon, missing mass = 0



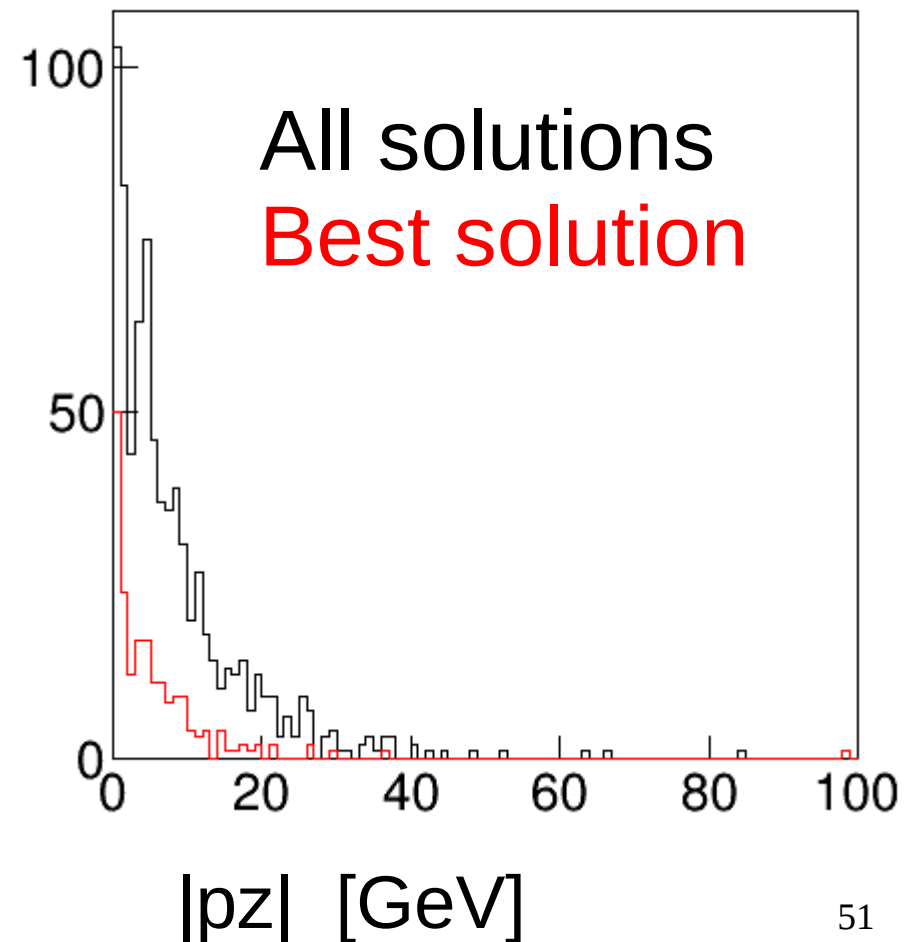
Check: Invariant mass of two τ s,
total p_z (e.g. of ISR)

n.b. we have not used these in any part of the analysis

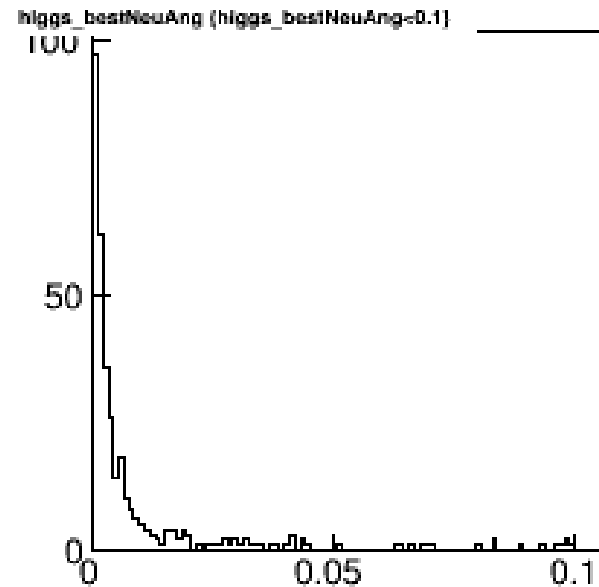
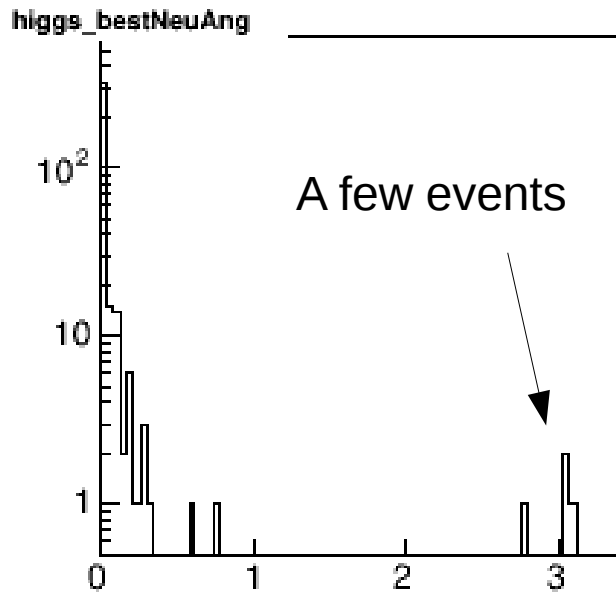
hHiggsMissMass



hMissMassPz



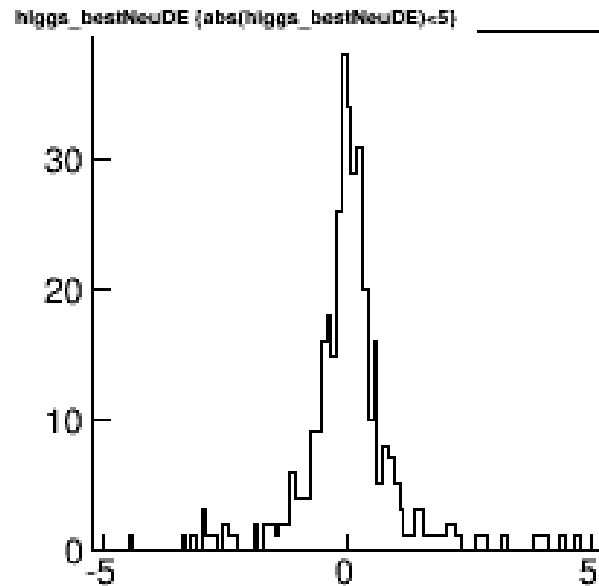
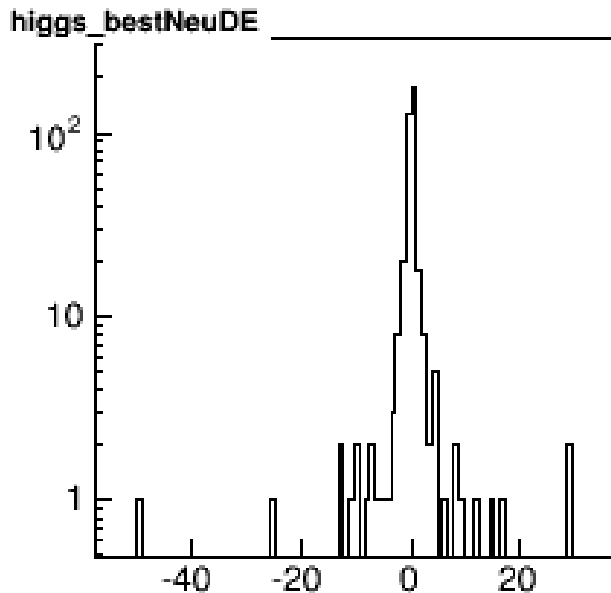
Compare fitted and true neutrino energies and directions



Only best solution

Angle between MC and fitted neutrinos [rad]

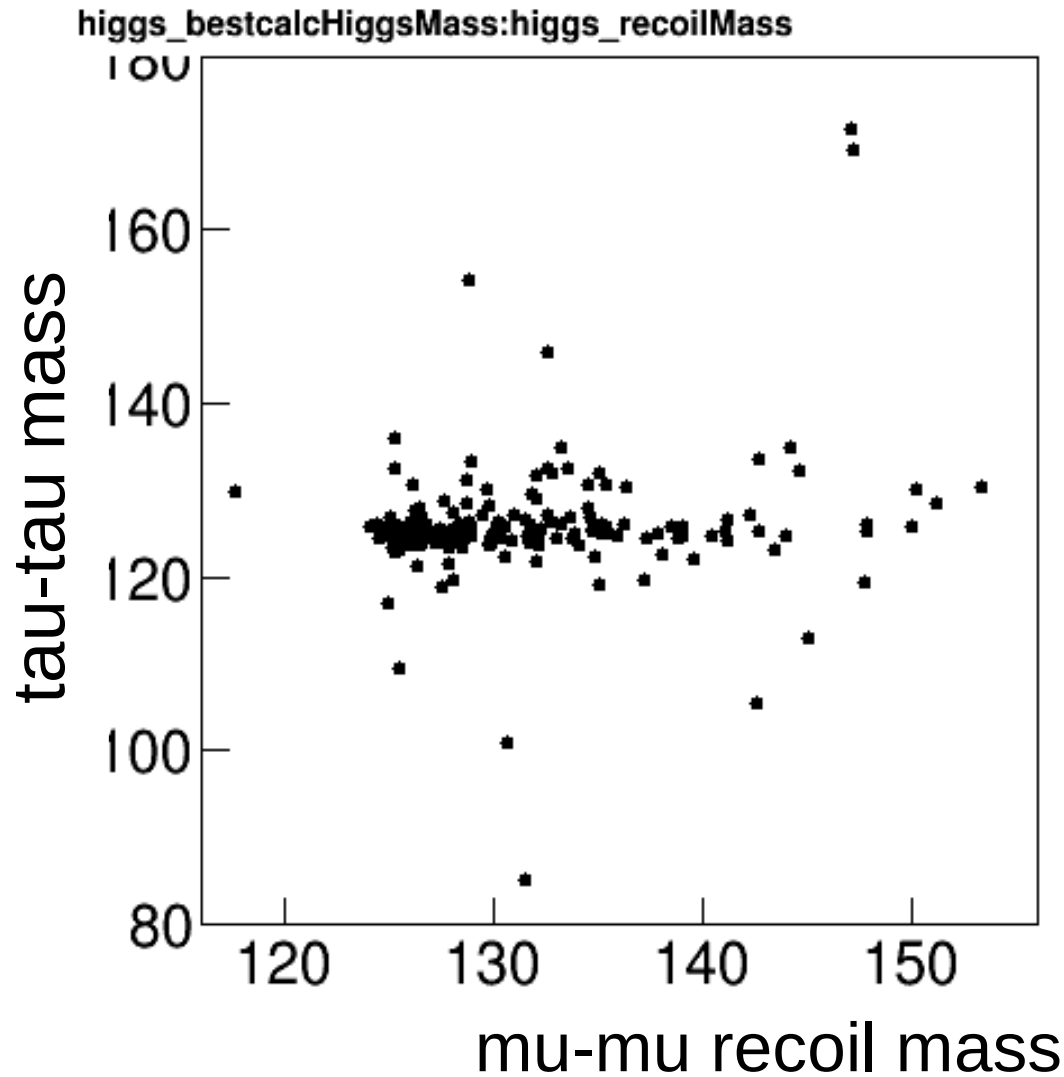
Precision typically
< ~ 10 mrad
< ~ GeV



MC – fitted neutrino energy [GeV]

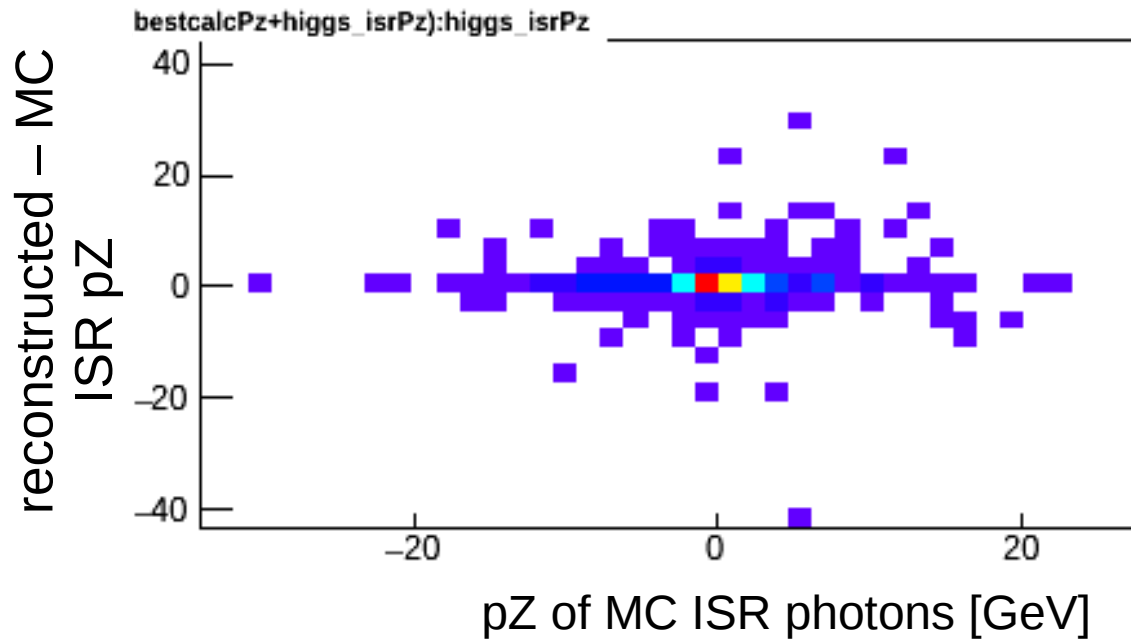
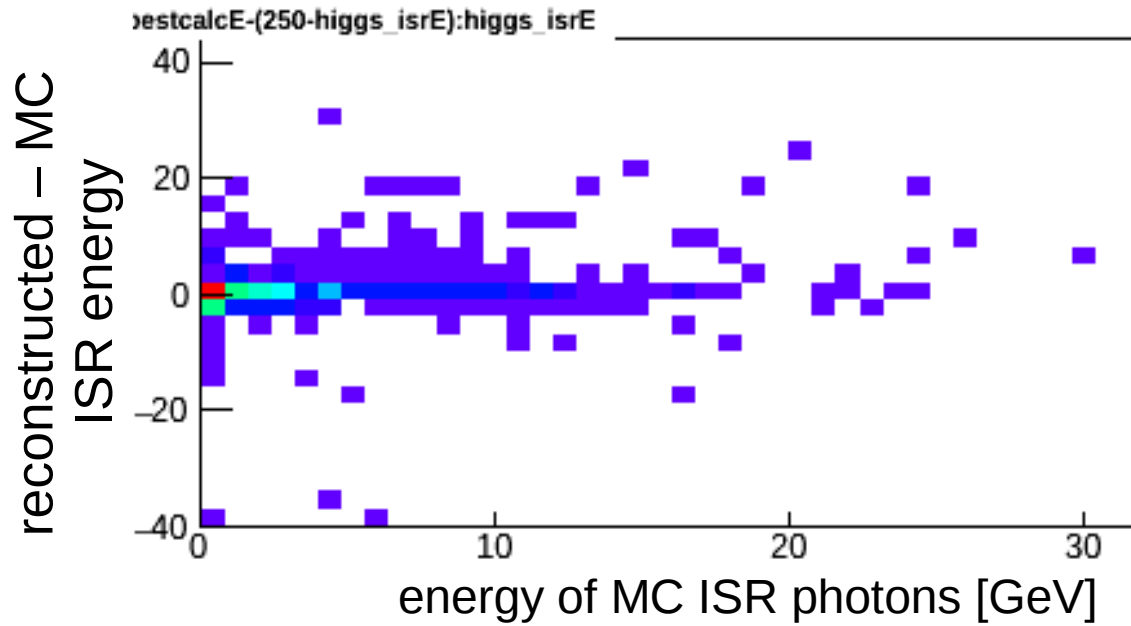
recoil mass (from muons) vs. reconstructed τ - τ mass

Only best solution



As expected, this method of mass reco not affected by ISR₅₃
unlike recoil mass

How well is ISR/BS energy and pZ reconstructed?



Summary

It's interesting to try to fully reconstruct τ s:

significant BR of Higgs

they can act as “polarimeters”

→ reconstruct their spin state by looking at their decay products

The ILC machine and detectors have great potential for tau reco:

tiny beam spot

high precision vertex detector

In hadronic tau decays of ($\tau \tau + “X”$) processes

we can calculate the tau neutrino momenta with good precision

if we can measure p_T of “X”

If this is not possible, other approaches may be possible

→ make different assumptions about event

Kinematic fitting should give some improvements in precision

take account of uncertainties in measured quantities

tools are ~in hand

Things to do next:

- apply kinematic fit on the identified (best) solutions
may improve the resolution
- apply to tau \rightarrow rho nu decay mode
I think (almost) same method can be used

Multi-prong decays should be easier

Identify vertex \rightarrow tau momentum direction

Leptonic decays need more constraints

maybe if only one tau decays leptonically,

something can still be done with some extra assumptions

- apply to Higgs CP measurement



First approach:

Constrained kinematic fitting

Using MarlinKinFit package

extended to use LCIO tracks (with full covariance matrix)

a lot of patient help from Jenny & Benno List

neutrino momenta: unknown parameters

muon & charged pion tracks: measured parameters

(ISR treatment also possible, using expected ISR distribution)

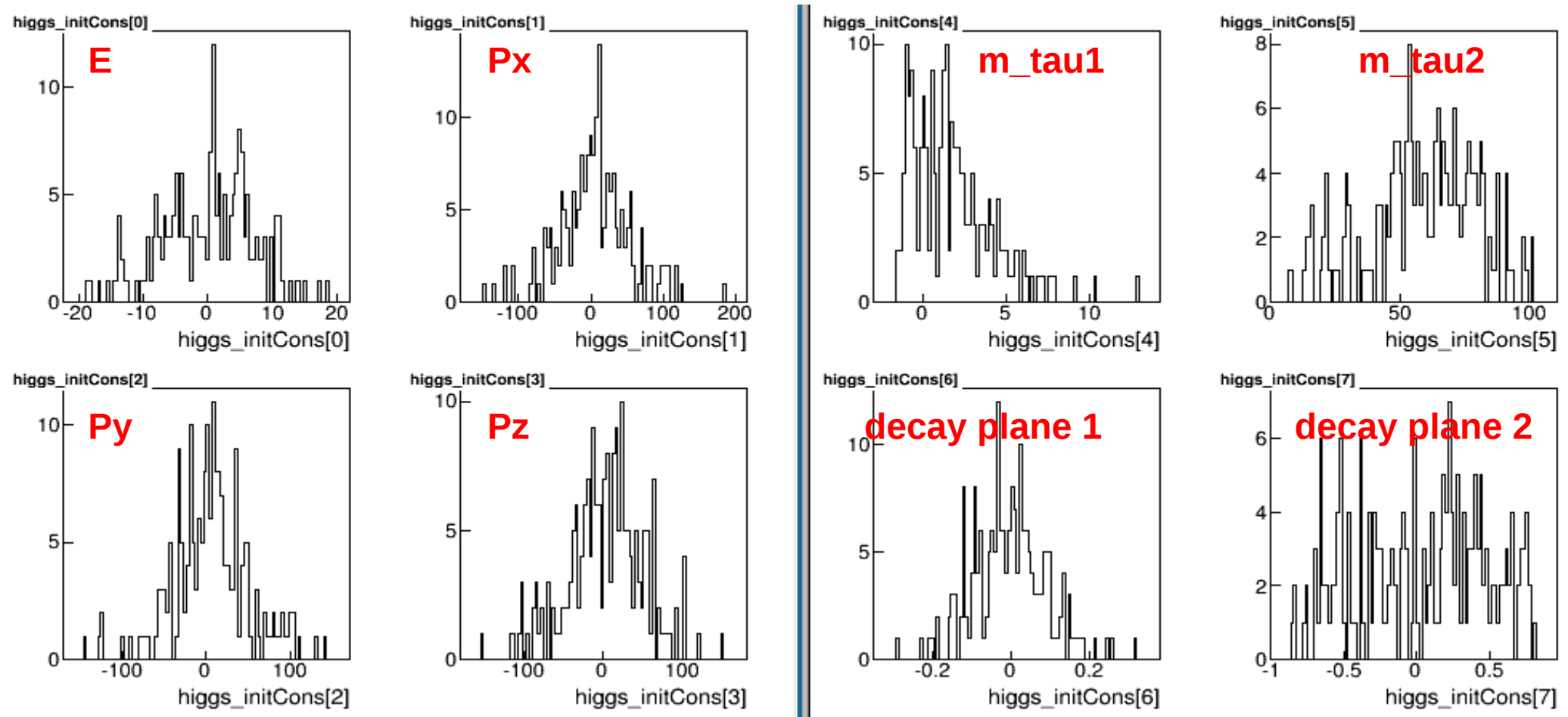
Overall 4-momentum constraint

Tau mass constraints

Tau decay plane constraints

Adjust measured and un-measured parameters to satisfy constraints,
while minimising the “chisq” (deviations from measured values)

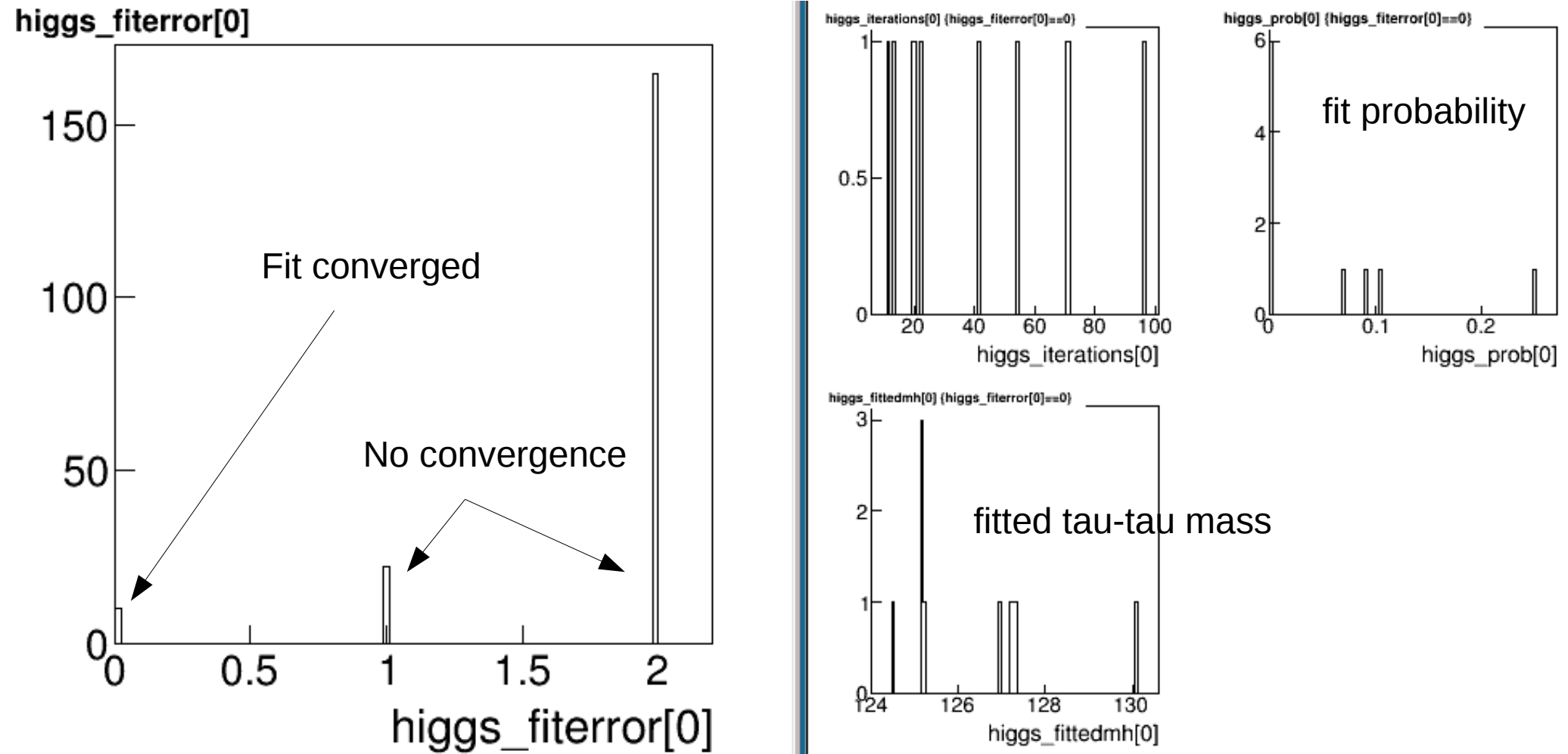
Choice of starting position for neutrino momentum
turns out to be rather important
here use randomly smeared direction around charged pion track



Value of constraints before fitting
far from being satisfied

Units are
GeV for momenta/masses₃₈
cos(angle) for decay plane

Fit results

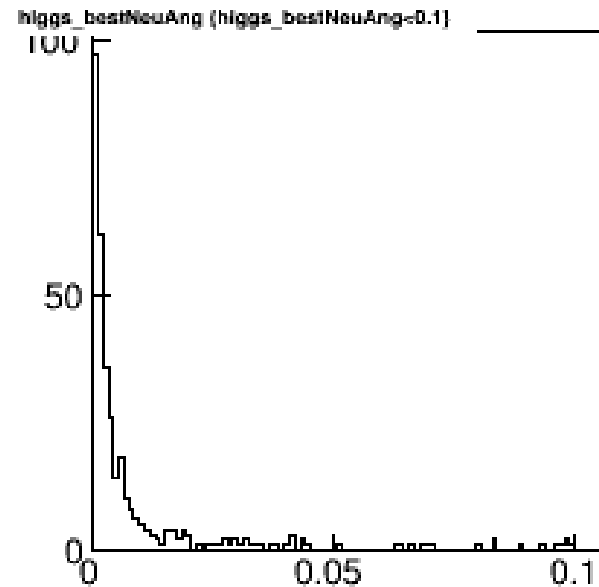
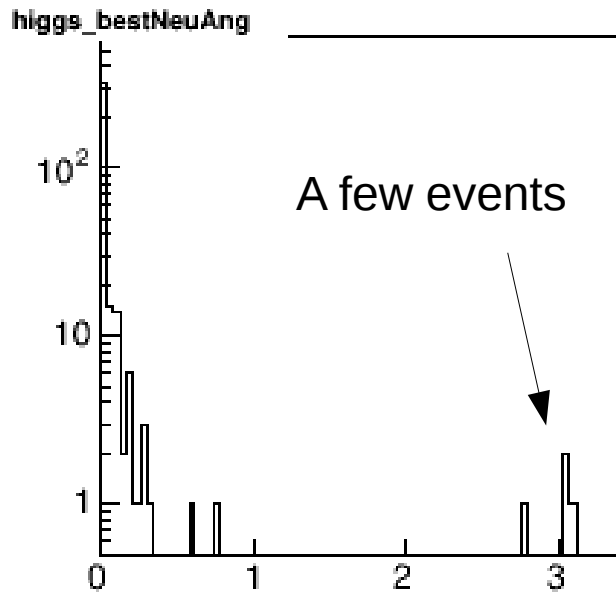


Only very small fraction of fits converge

Those that do look somewhat OK, but not great...

If initial guess for neutrino momenta are smeared around MC value, it works much better ← need better initial estimates

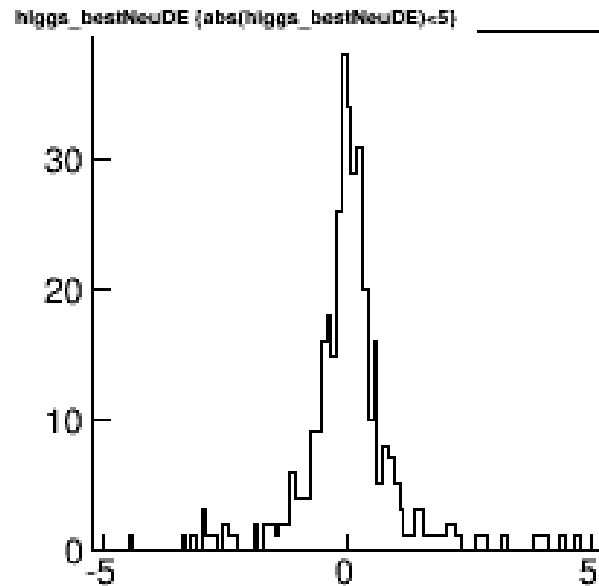
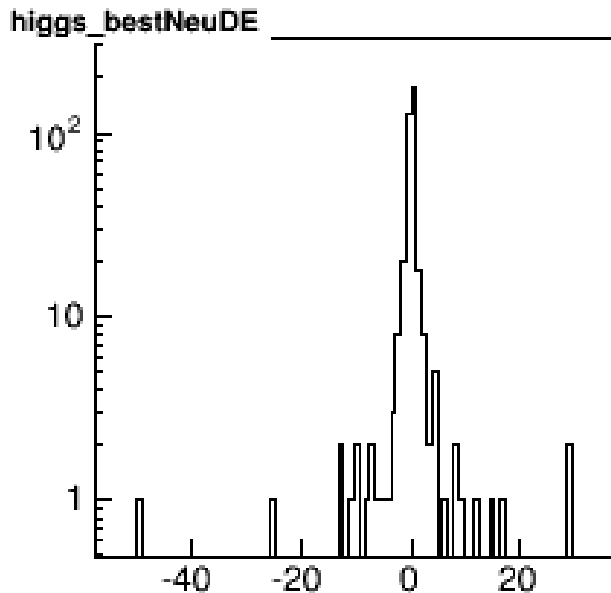
Compare fitted and true neutrino energies and directions



Only best solution

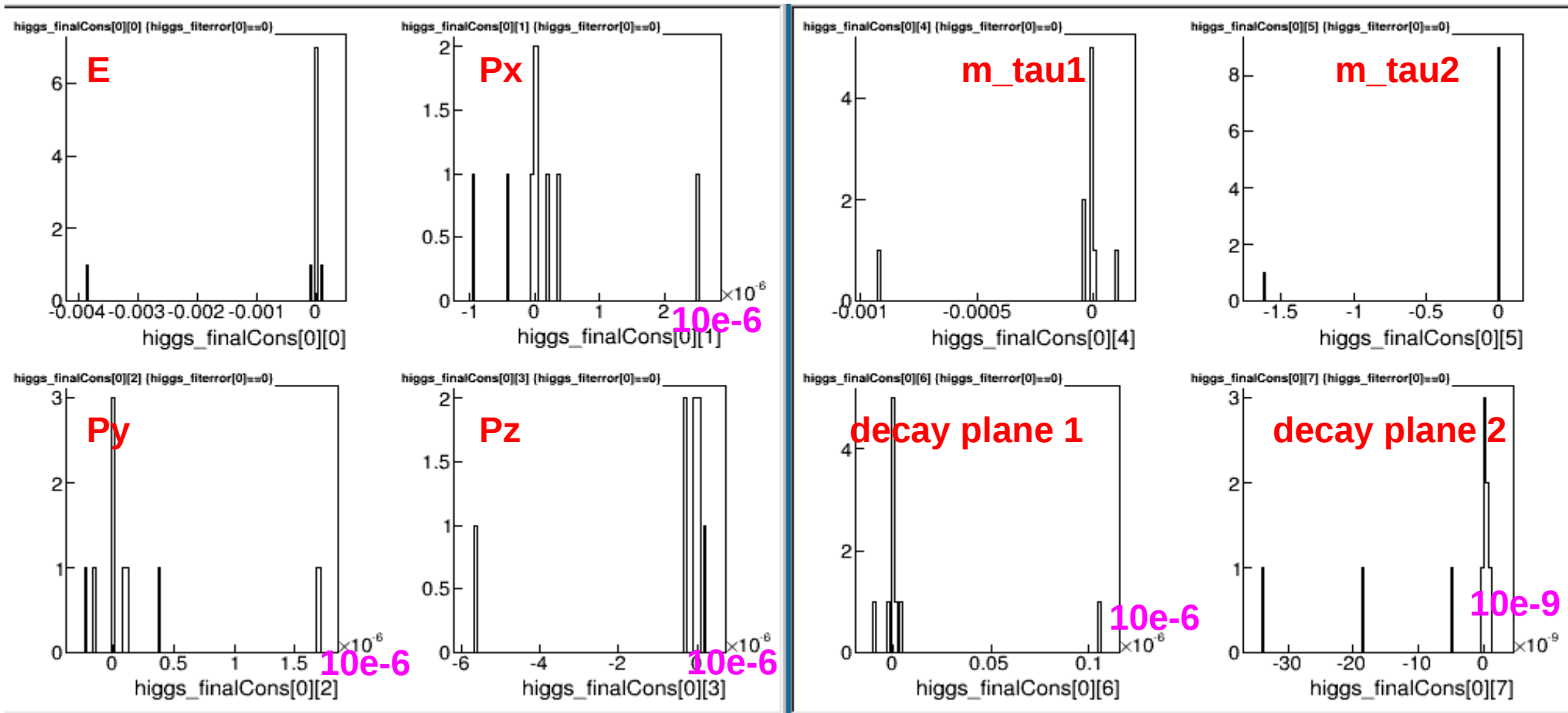
Angle between MC and fitted neutrinos [rad]

Precision typically
< ~ 10 mrad
< ~ GeV



MC – fitted neutrino energy [GeV]

Value of constraints after converged fitting



Constraints well satisfied:
Fitter itself is working ~OK

Units are
GeV for momenta/masses
cos(angle) for decay plane

It seems essential to have a good initial estimate of unknown quantities (neutrino momenta) before applying a constrained kinematic fit

Second approach:

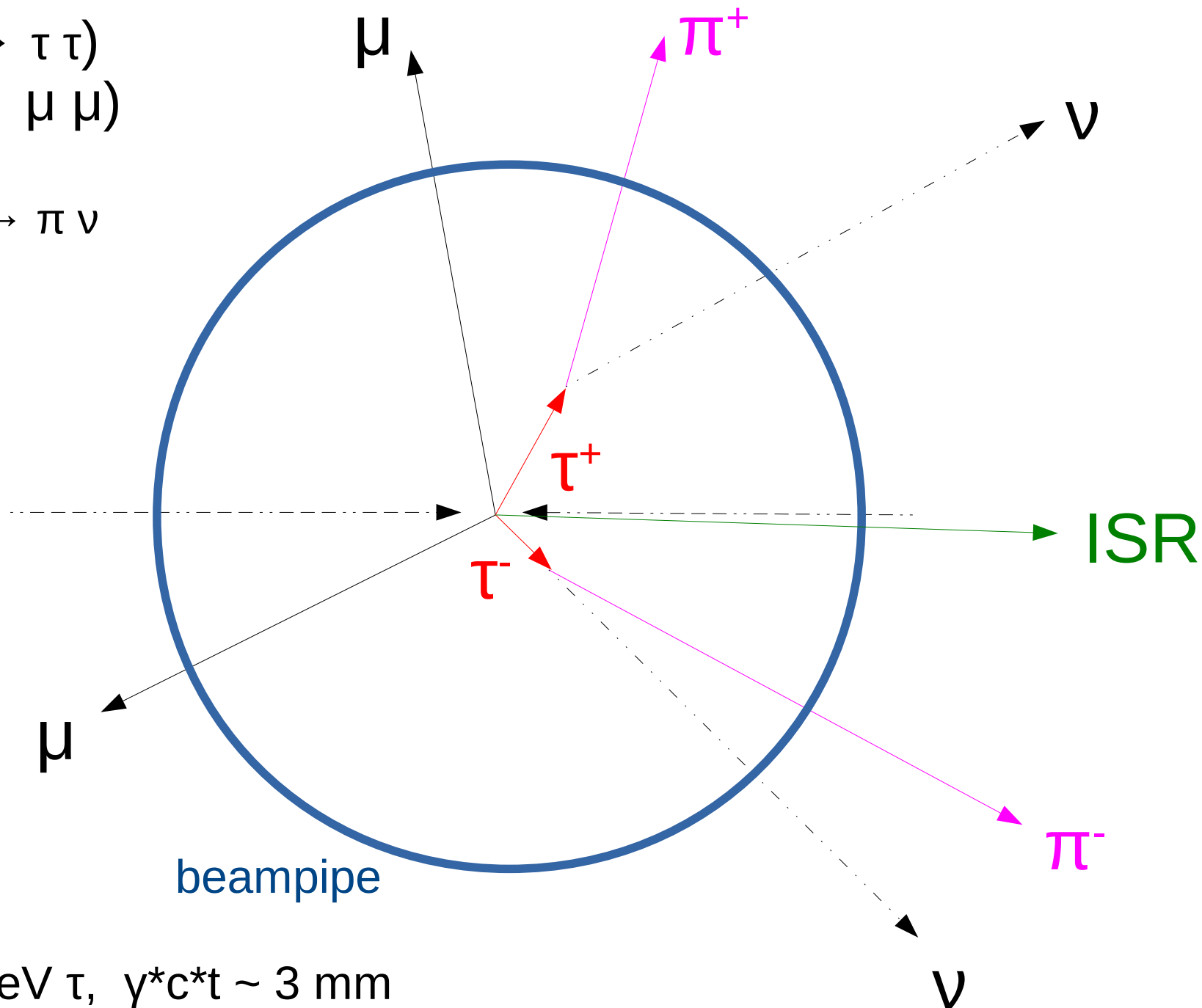
Try to calculate the unknown quantities
Ignore uncertainties on measured quantities

$e^+ e^- \rightarrow$

$(H \rightarrow \tau \tau)$

$(Z \rightarrow \mu \mu)$

both $\tau \rightarrow \pi \nu$



For 60 GeV τ , $\gamma \cdot c \cdot t \sim 3$ mm
ILD impact parameter resolution ~ 5 μ m