

# Granularity and Energy Resolution

Katja Krüger, Coralie Neubüser, Felix Sefkow, Huong Lan Tran



LINEAR COLLIDER COLLABORATION  
Designing the world's next great particle accelerator

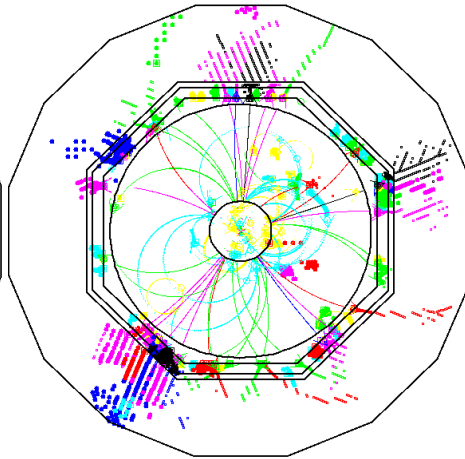
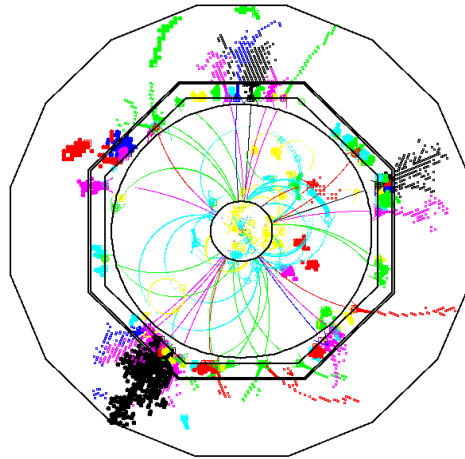
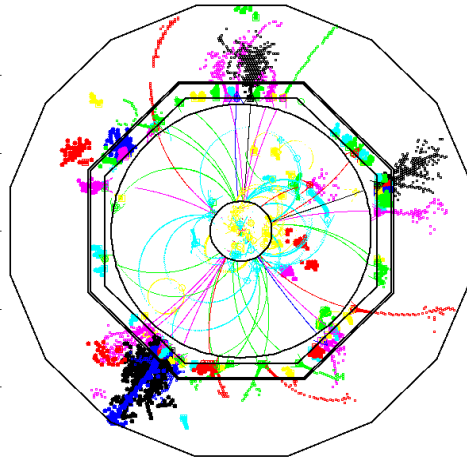
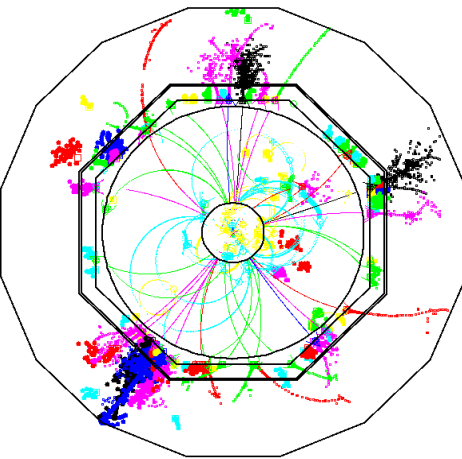


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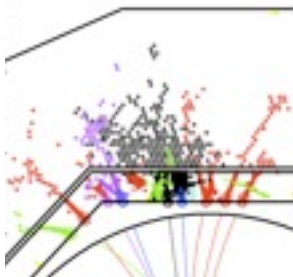
3x3

5x5

10x10



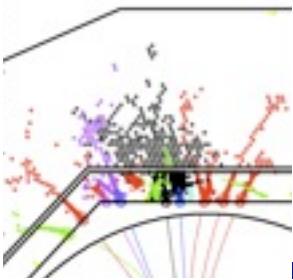
ILD software and optimisation workshop  
DESY, Feb 25, 2016



# Outline

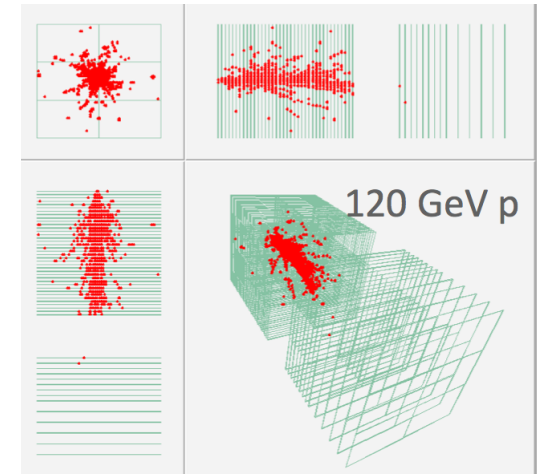
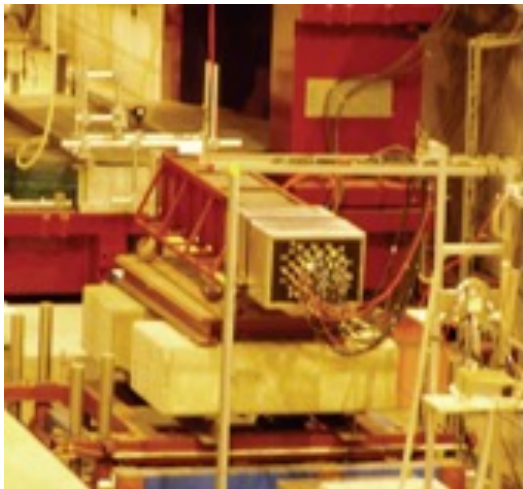
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- Introduction: effects of granularity
- Reconstruction schemes for single particles and software compensation
- Energy resolution and granularity
- AHCAL optimisation
- Studies done at DESY, in co-operation with **Argonne**, **Cambridge** and **CERN**
  - see also talks by S.Green and H.L.Tran



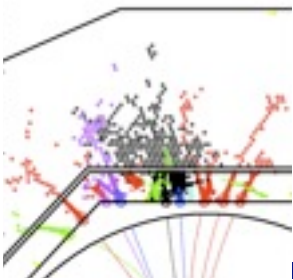
# Energy and Granularity

- A central theme in jet calorimetry since the times of H1 and ZEUS



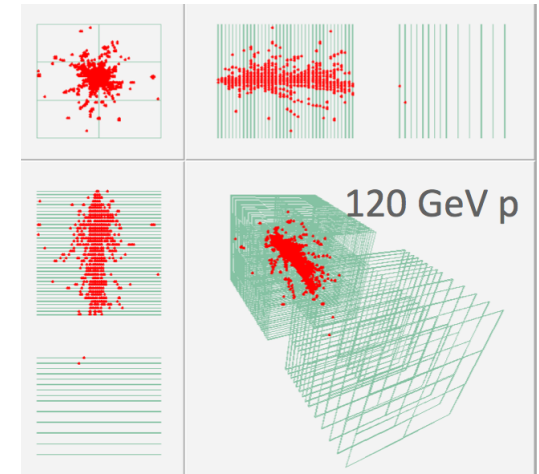
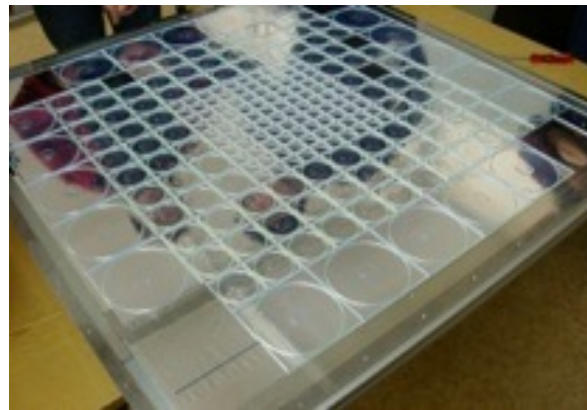
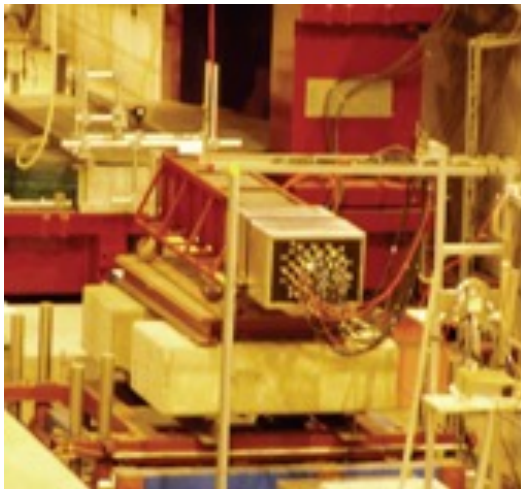
“Energy resolution  
is everything!”

“Granularity  
is everything!”



# Energy and Granularity

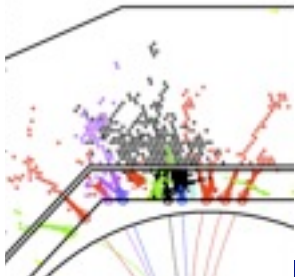
- A central theme in jet calorimetry since the times of H1 and ZEUS



“Energy resolution  
is everything!”

“We need  
enough of both!”

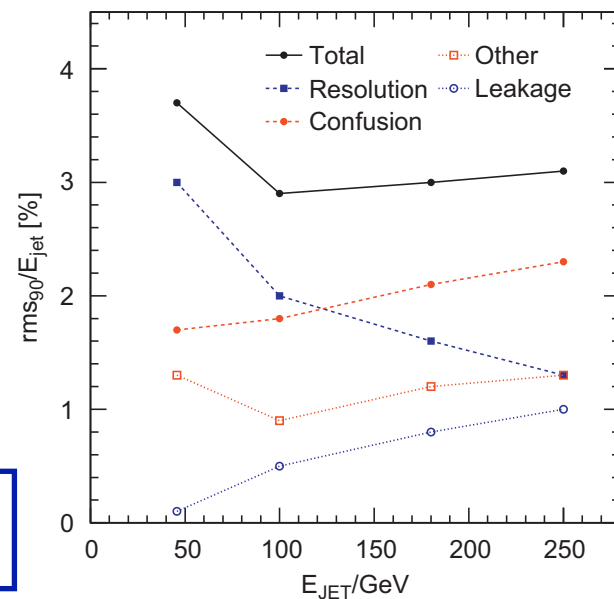
“Granularity  
is everything!”



# Particle flow performance

M.Thomson, Nucl.Instrum.Meth. A611 (2009) 25-40

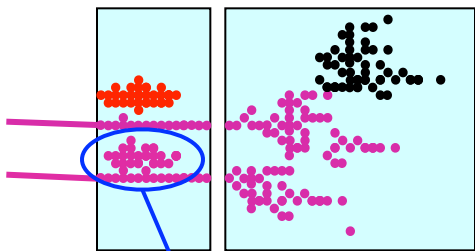
- Separating the energy depositions of individual particles requires high granularity
- Calorimeter resolution still does matter
  - dominates for jets up to  $\sim 100$  GeV
  - contributes to resolve confusion



## Types of confusion:

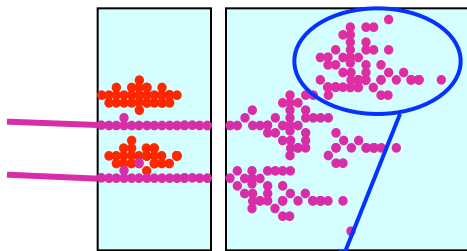
Pattern recognition based on topology and energy

### i) Photons



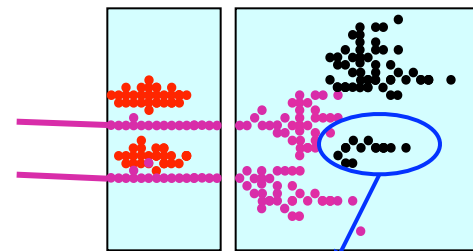
Failure to resolve photon

### ii) Neutral Hadrons



Failure to resolve neutral hadron

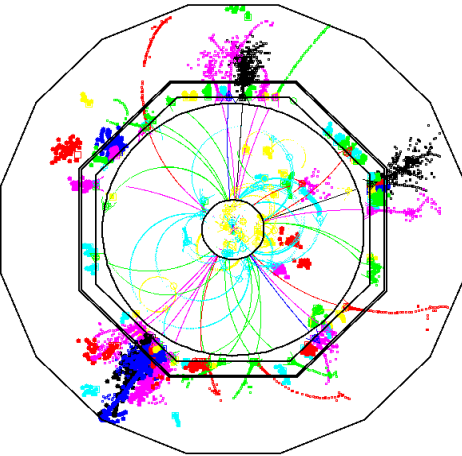
### iii) Fragments



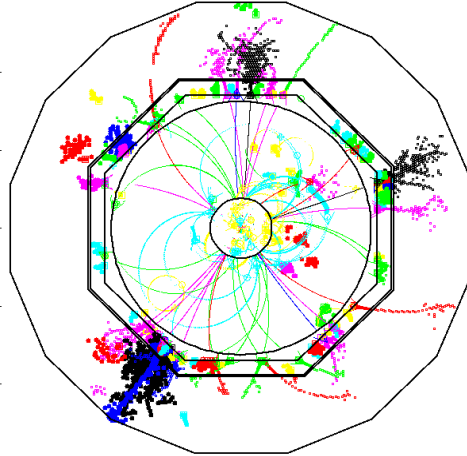
Reconstruct fragment as separate neutral hadron

# Make your choice...

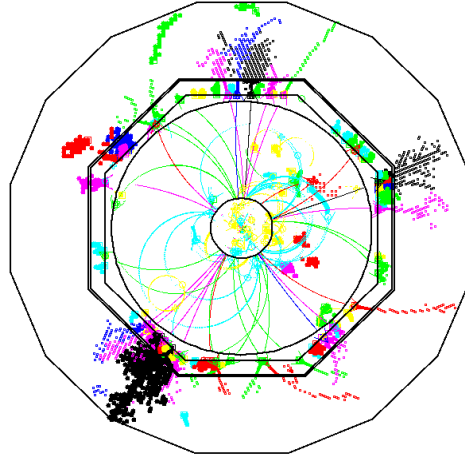
**1x1**



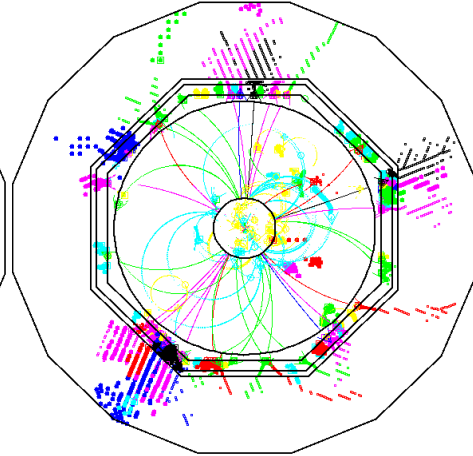
**3x3**

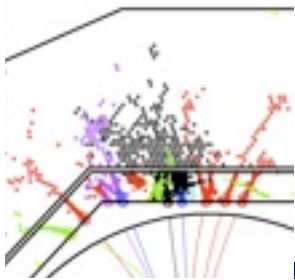


**5x5**



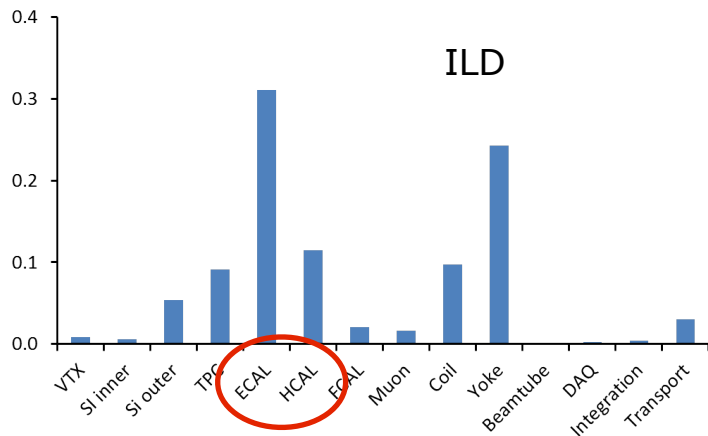
**10x10**



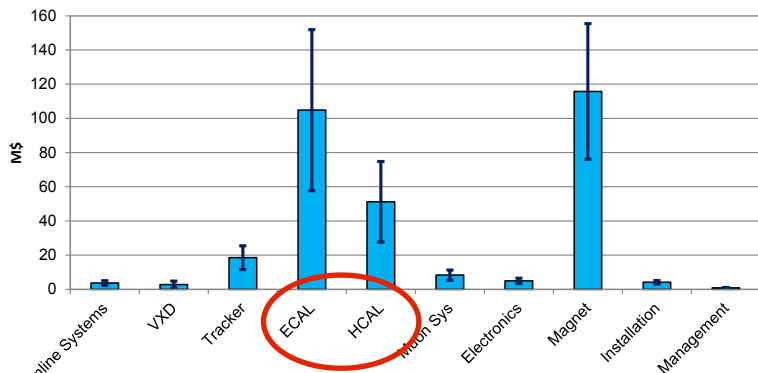


# Calorimeter cost

fraction of 392

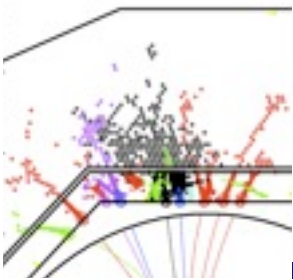


SiD M&S



sum = 315

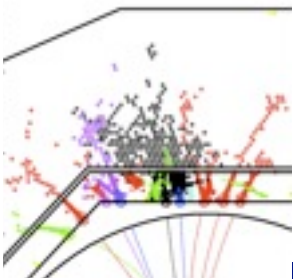
- Costing is at a very early stage
- Yet, many lessons learnt from 2nd generation prototypes
- Example ILD scint HCAL: 45M
  - 10M fix, rest ~ volume
  - 10M absorber, rest ~ area ( $n_{\text{Layer}}$ )
  - 16M PCB, scint, rest ~ channels
  - 10 M SiPMs and ASICs
- HCAL cost is rather driven by instrumented area then by cell size
- ECAL cost driver: silicon area
- Still, high granularity drives the design and needs to be justified



# Gaseous calorimeters

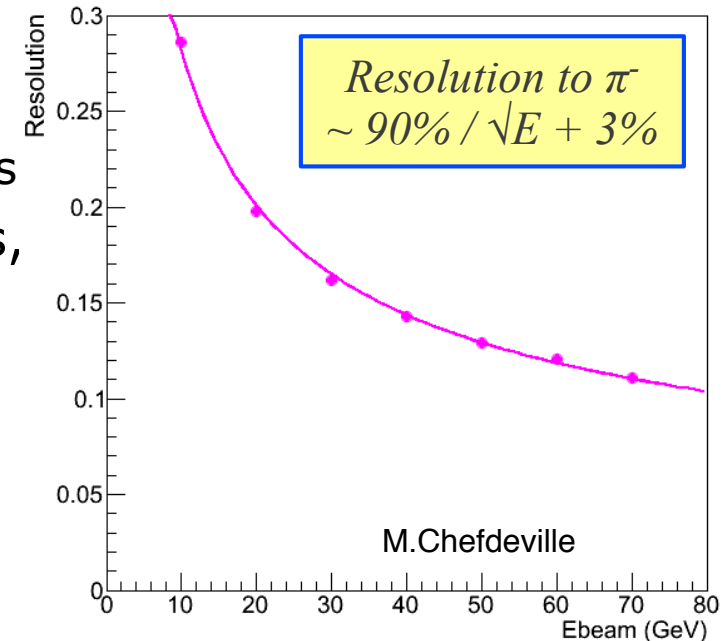
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  - small sampling, large Landau fluctuations
- **Digital** calorimeter idea: count particles, ignore fluctuations
  - $1\text{cm}^2$  cells: saturate above 30 GeV
- **Semi-digital** idea: mitigate saturation using several thresholds and weights
  - assumes signal prop. to E deposition

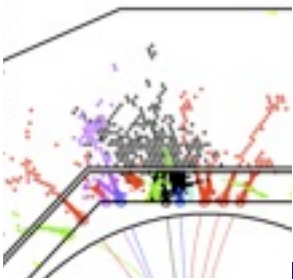




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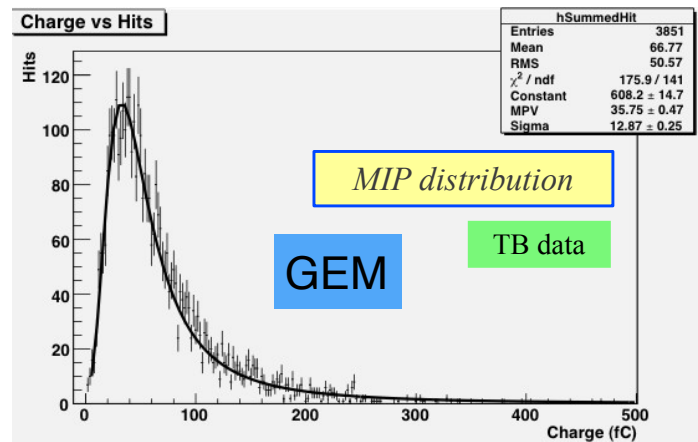
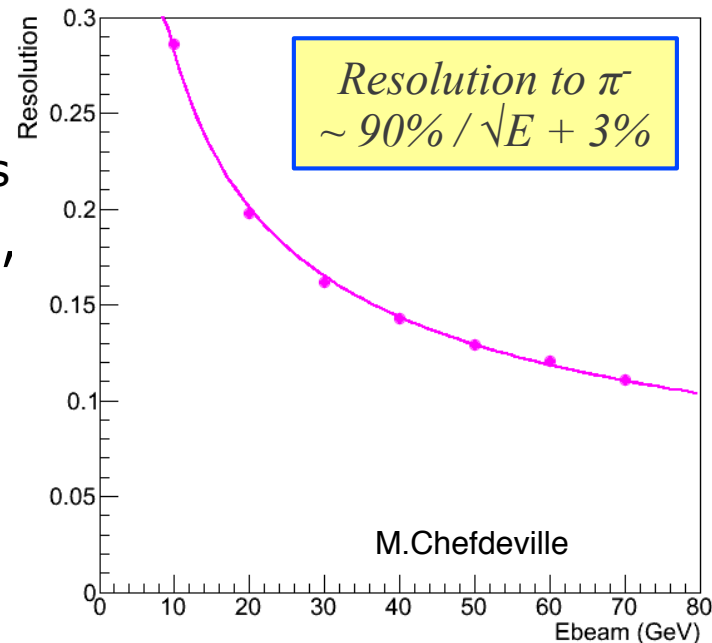
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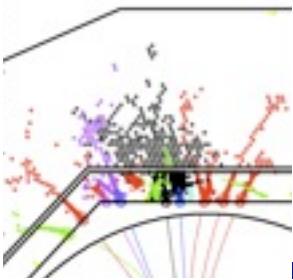




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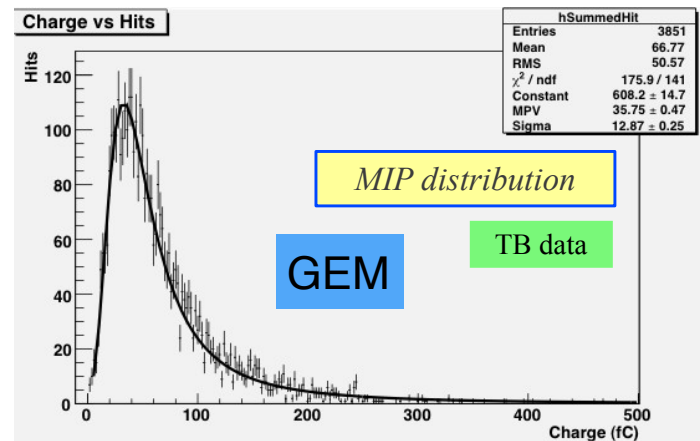
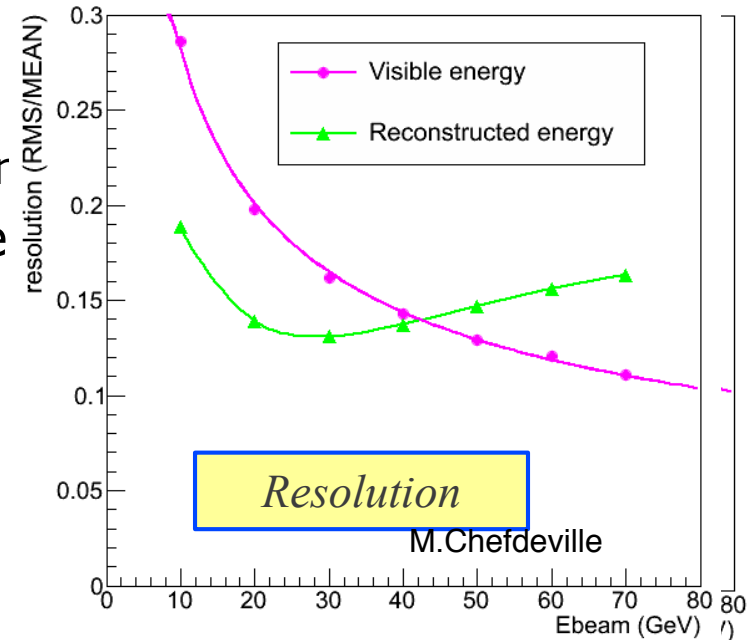
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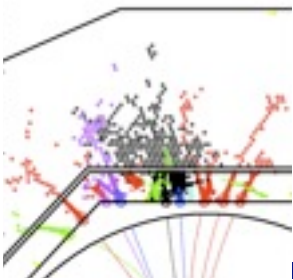




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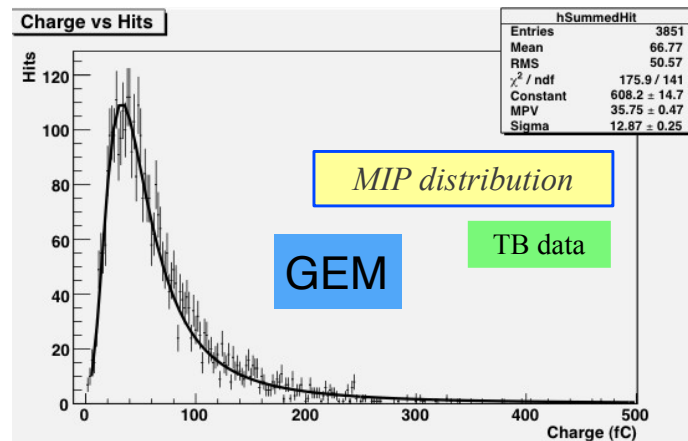
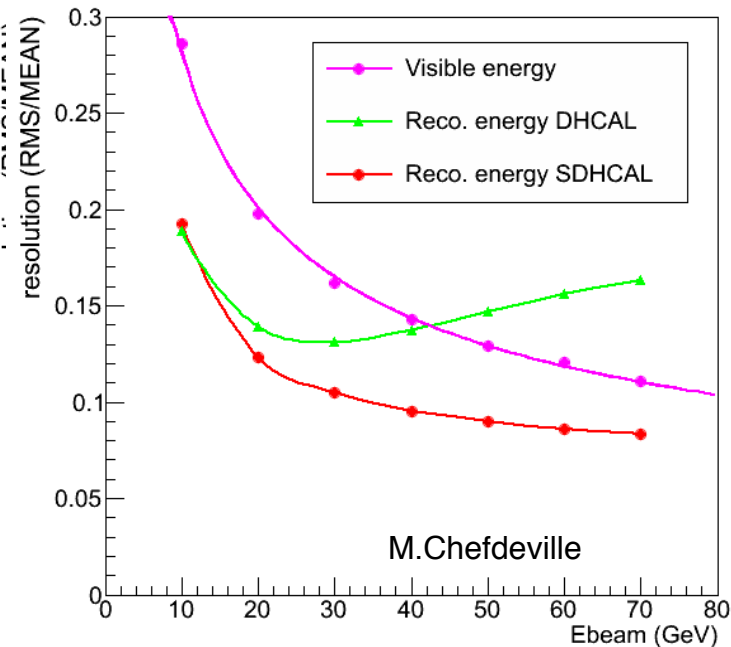
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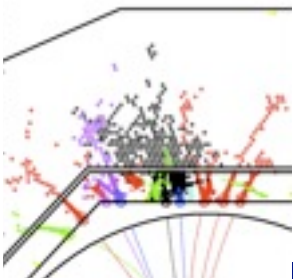




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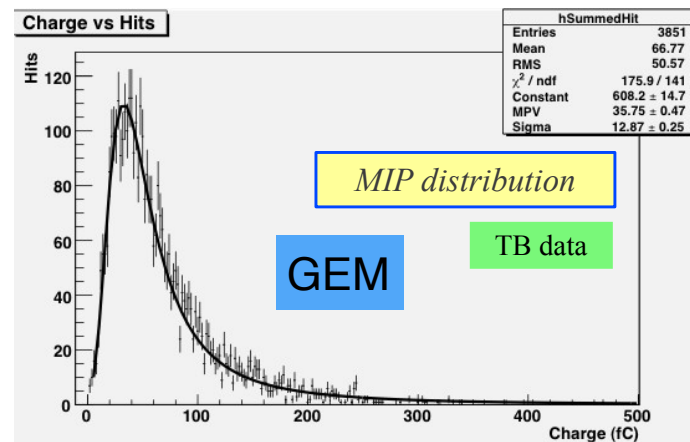
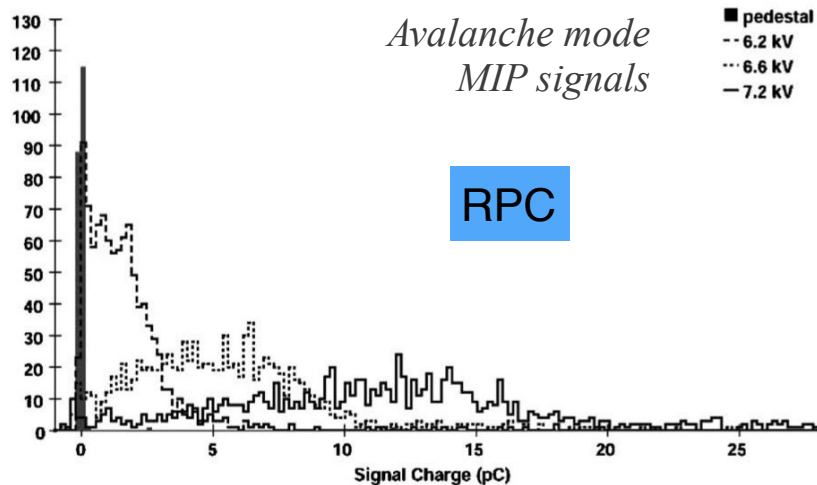
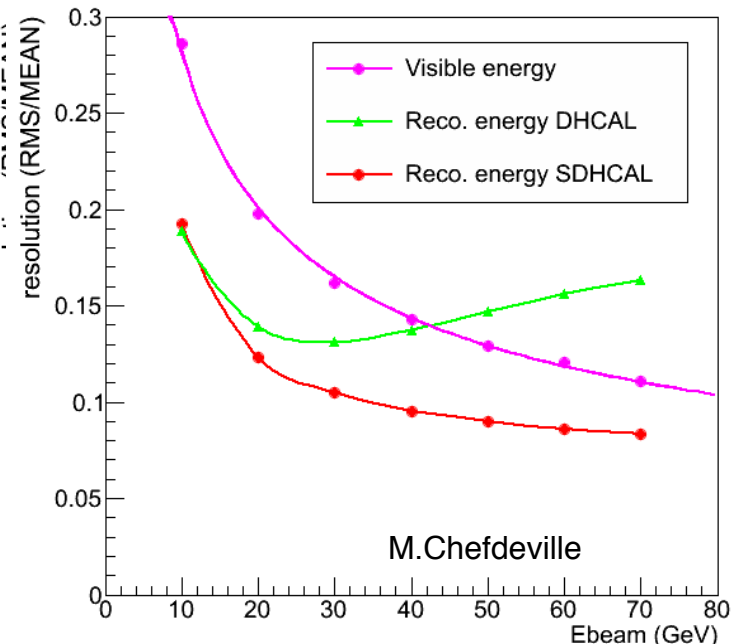
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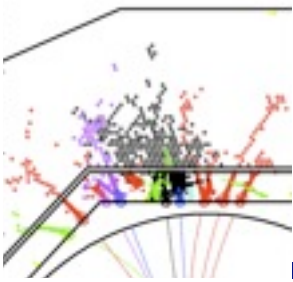


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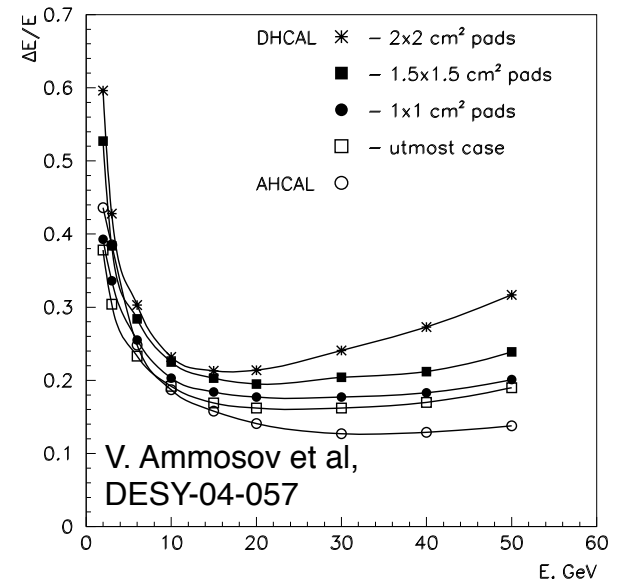
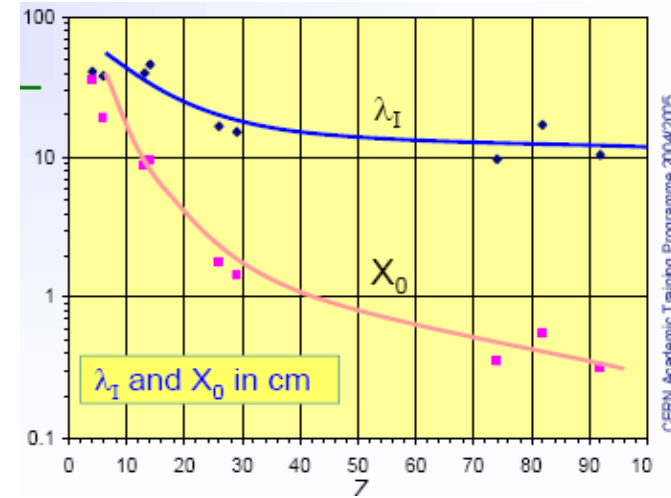
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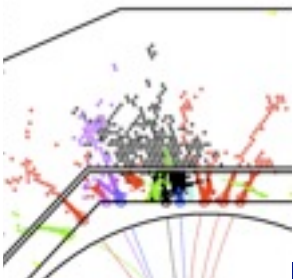


# Initial choices

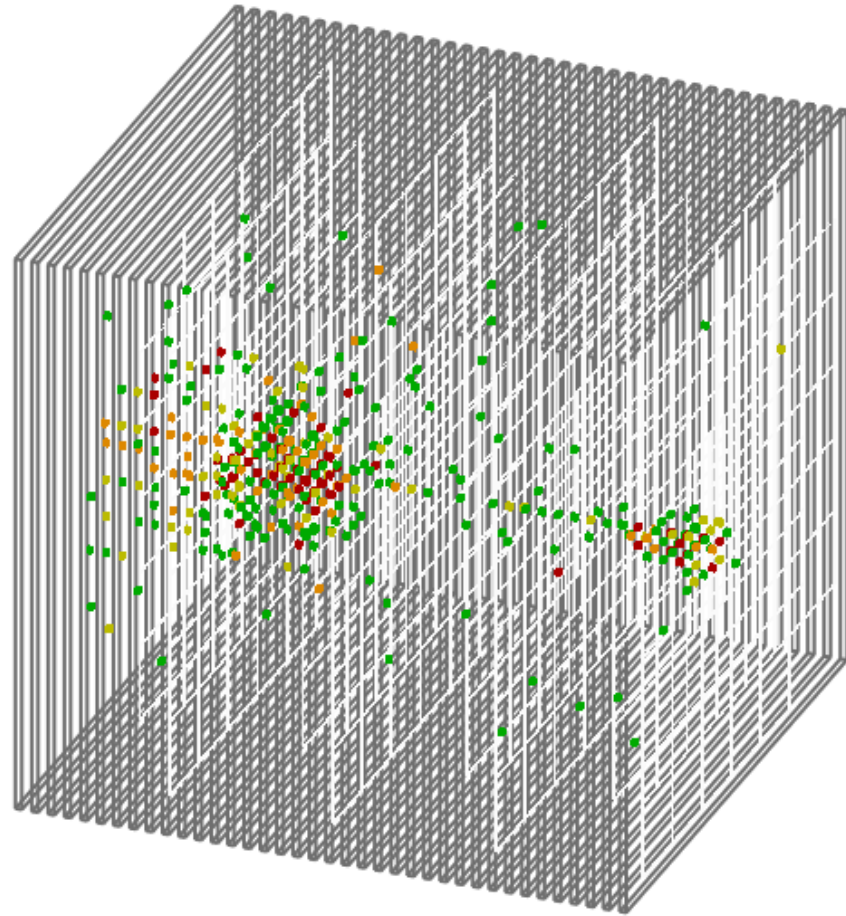


- Analogue:
  - 3cm x 3cm at  $\sim 3$ cm sampling pitch
  - corresponds to Molière radius and  $X_0$ ; hadron shower sub-structure scale
  - small effect on plain energy response and resolution, only via threshold
  - more direct effects when software compensation methods are applied
- Digital:
  - 1cm x 1cm at  $\sim 3$ cm sampling pitch
  - to limit saturation effects
  - affects single particle linearity and resolution directly

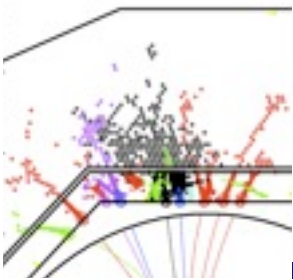




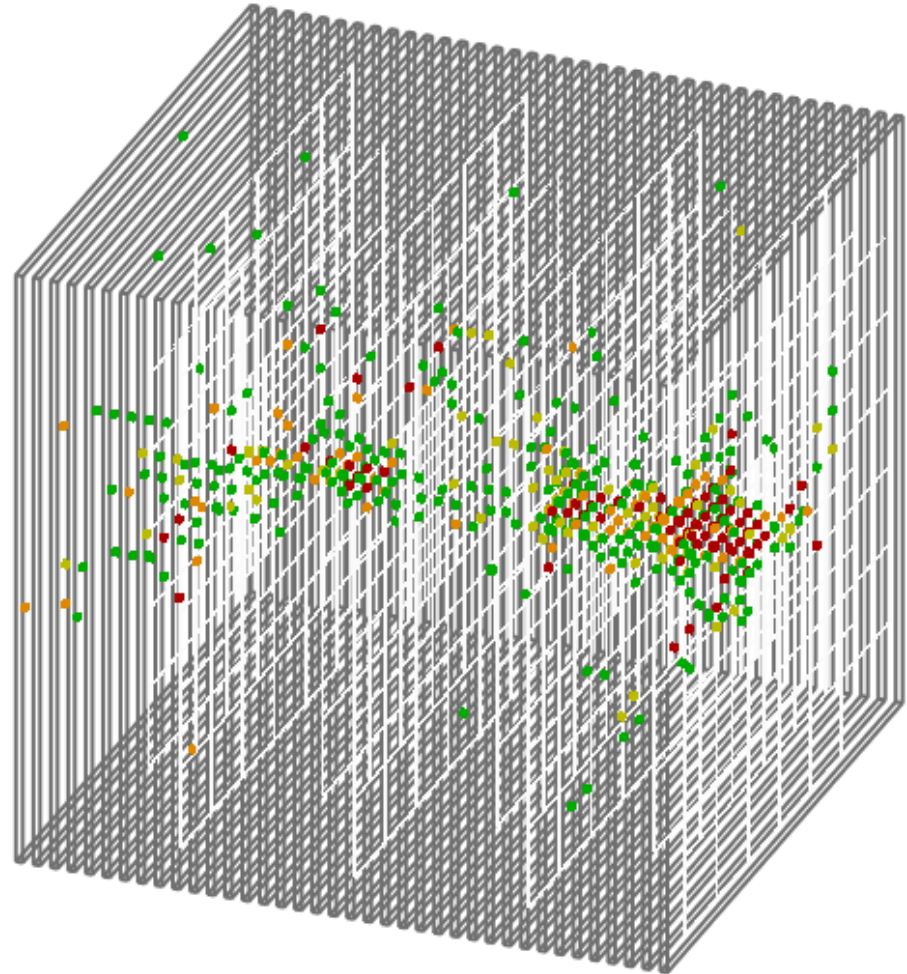
# Event displays: Analogue HCAL



- pions 80 GeV
- W absorber
- 3cm scintillator + SiPM

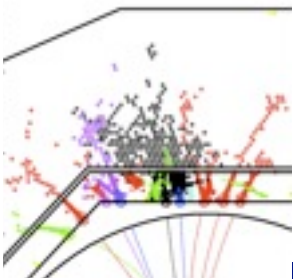


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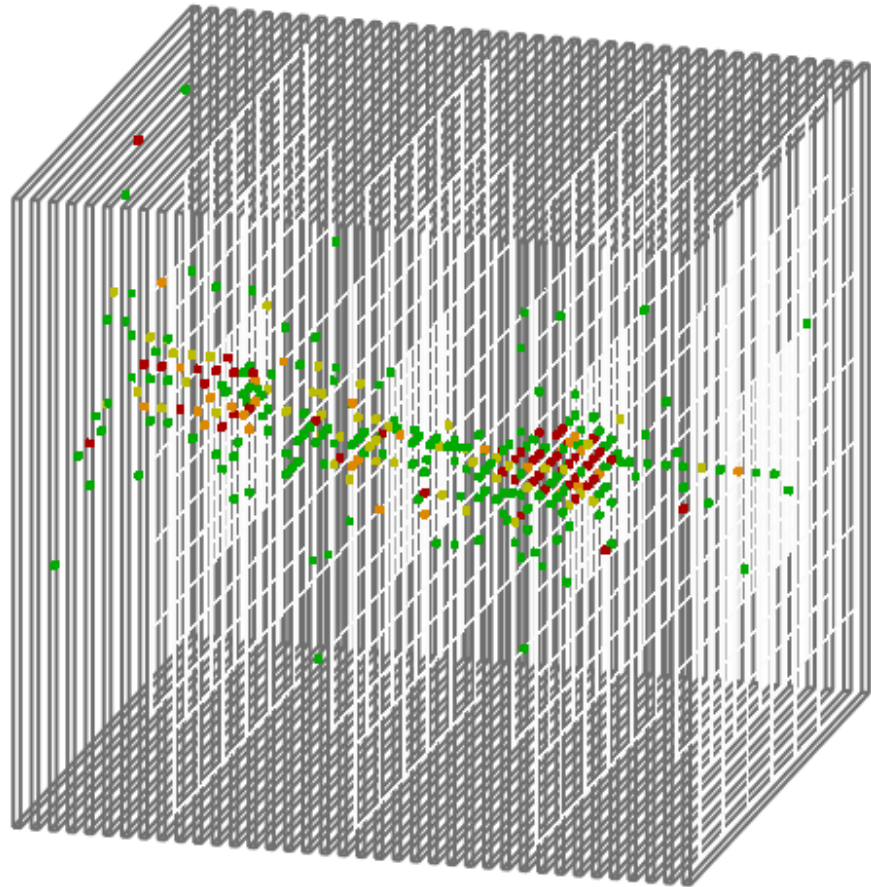


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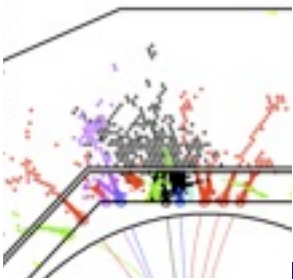




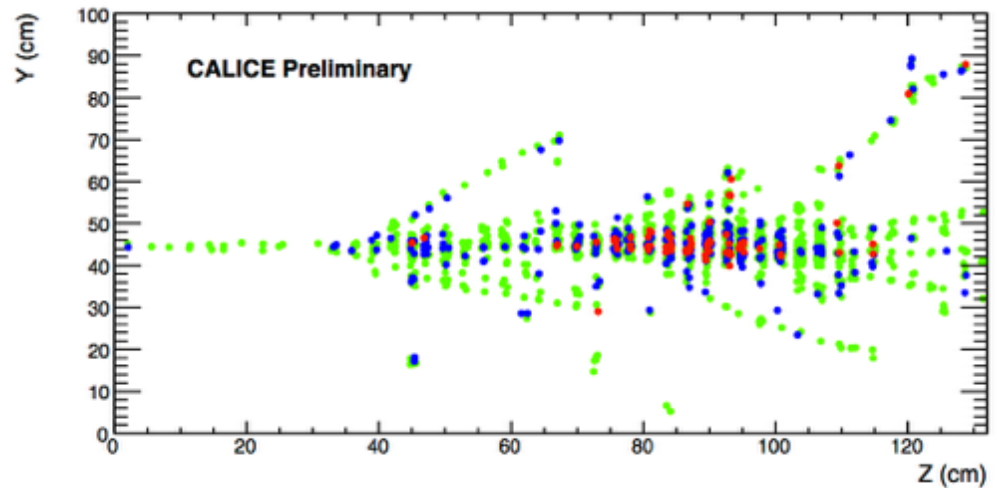
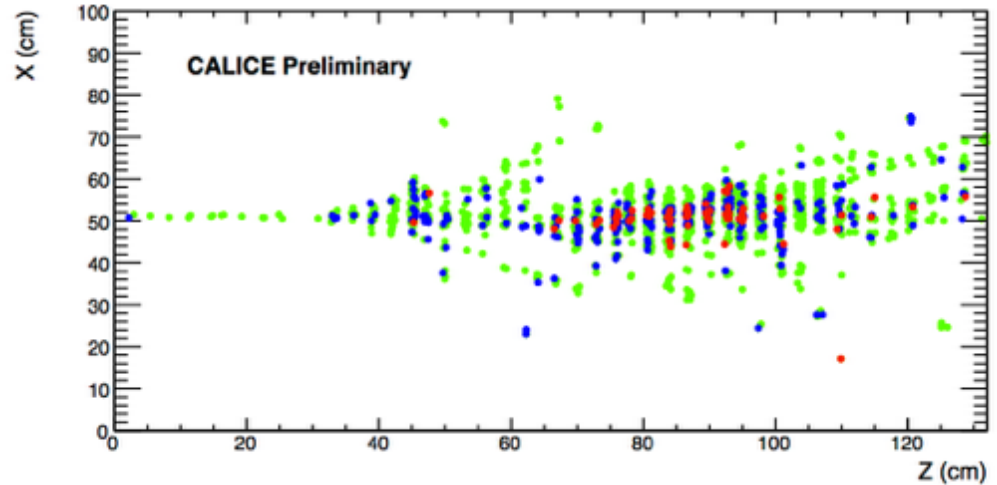
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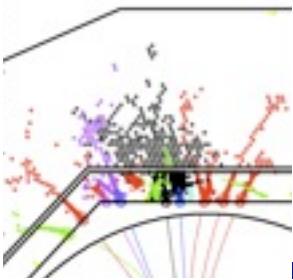
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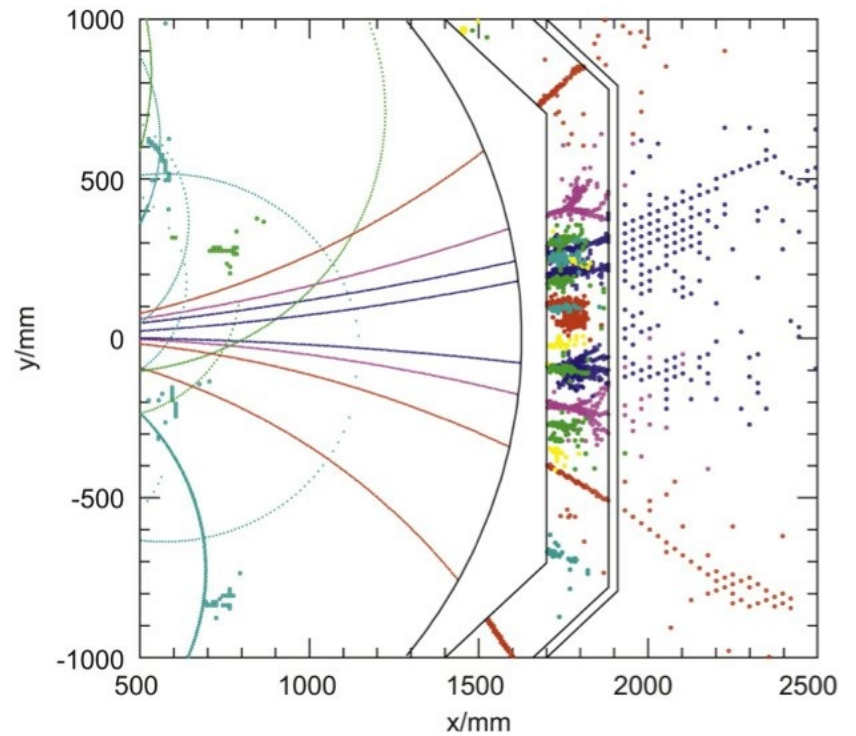
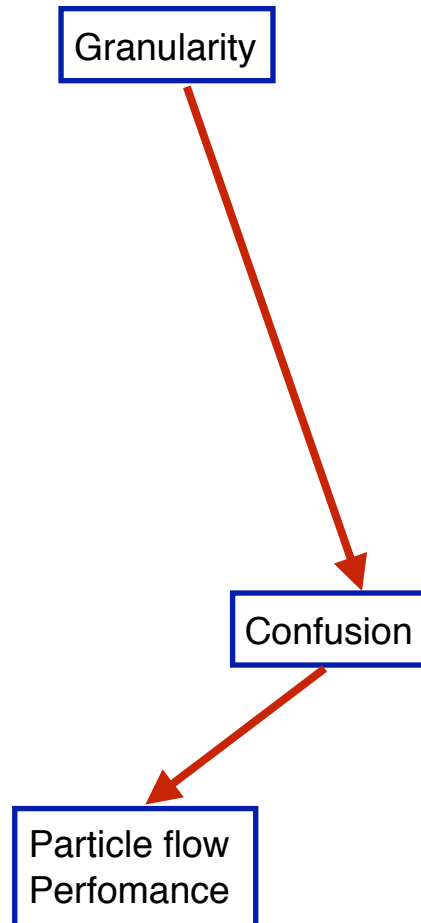
# Semi-digital RPC HCAL

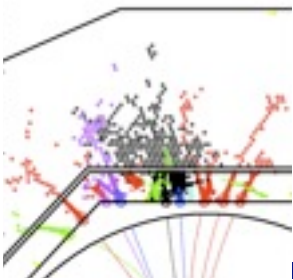


- pions 80 GeV
- Fe absorber
- 1 cm RPC, 3 thresholds

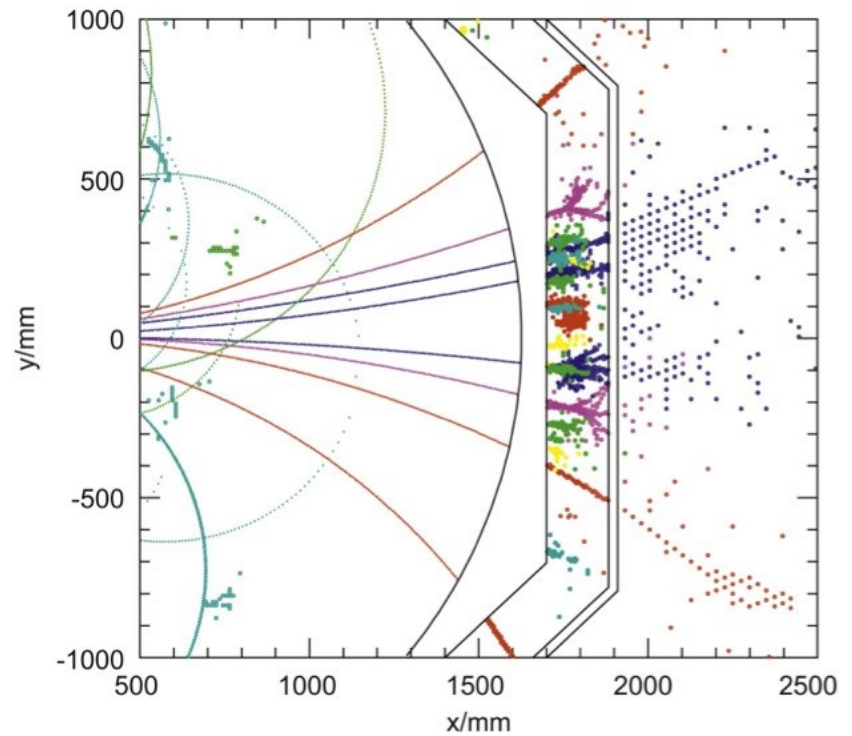
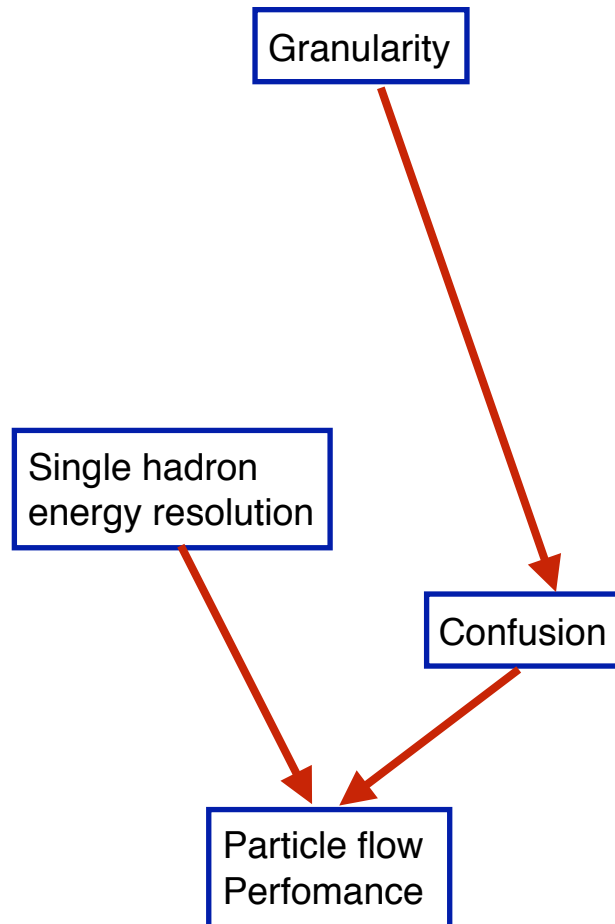


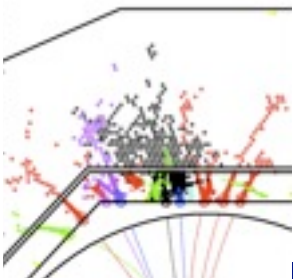
# Effects of high granularity



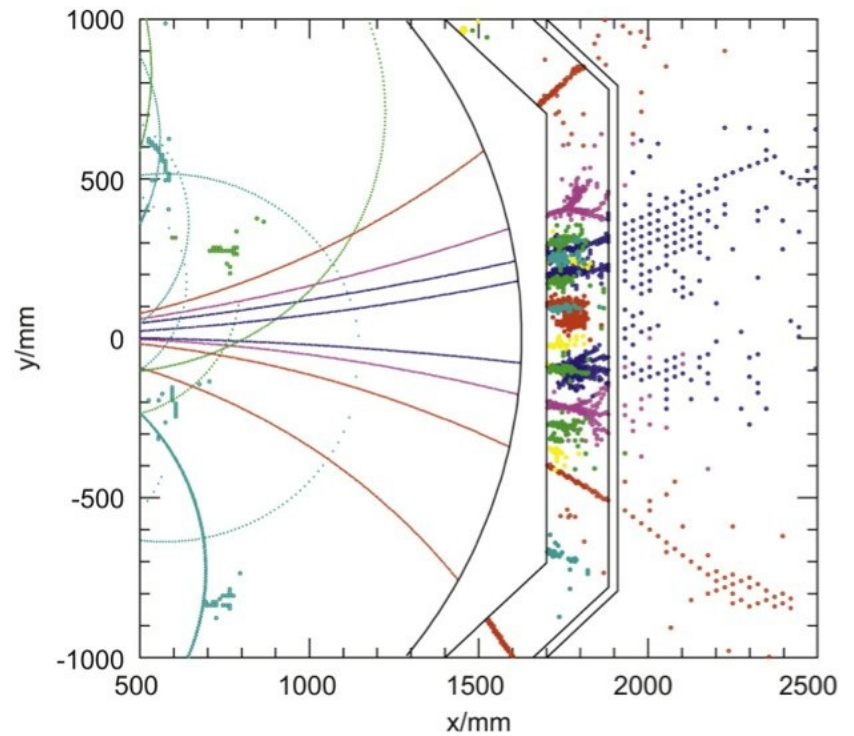
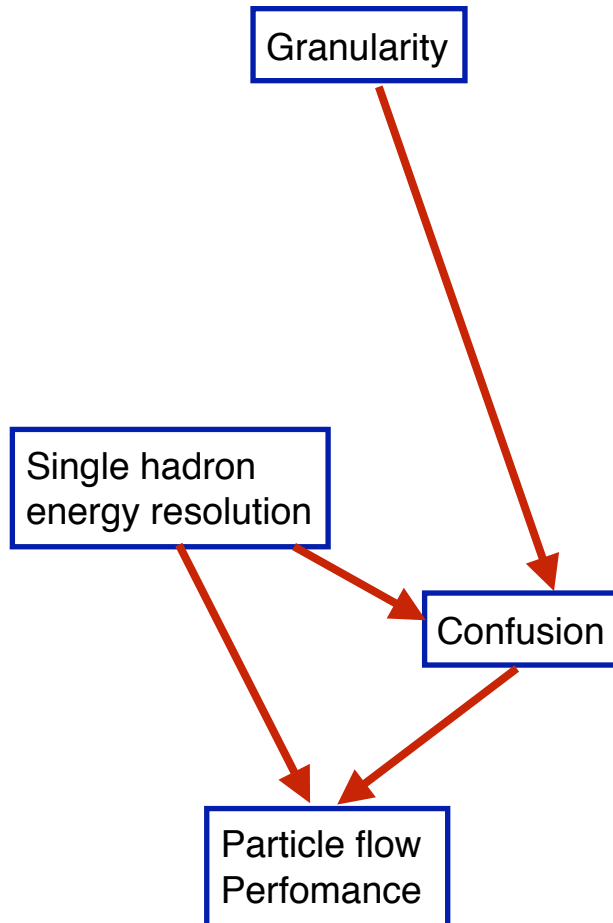


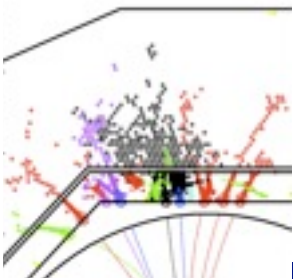
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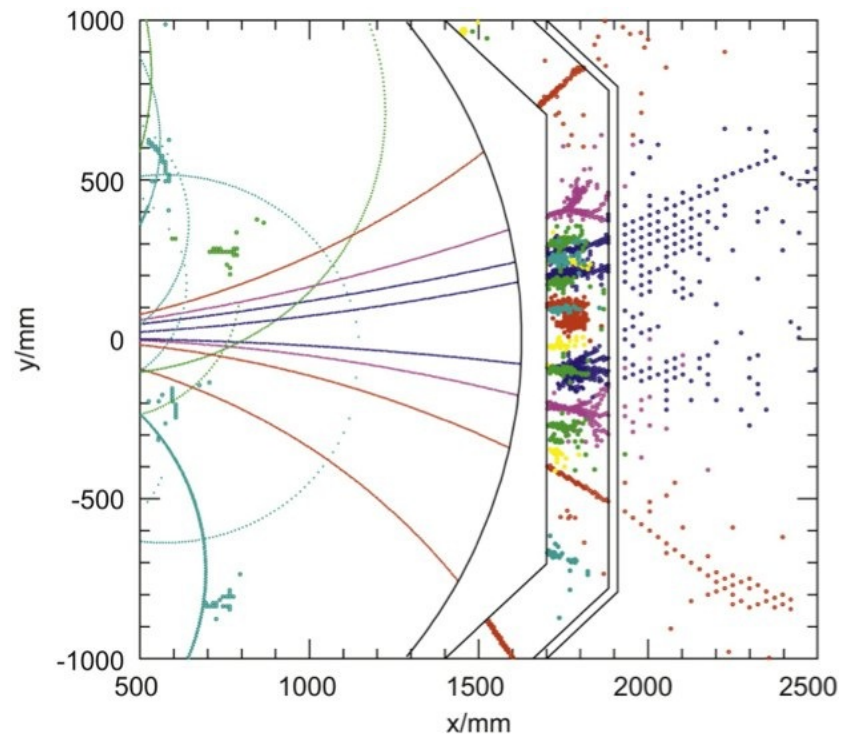
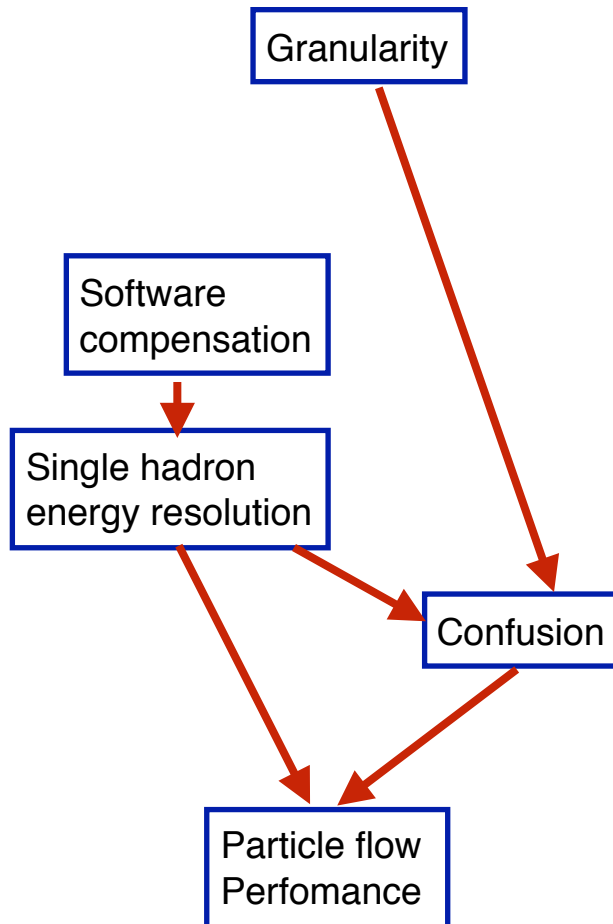


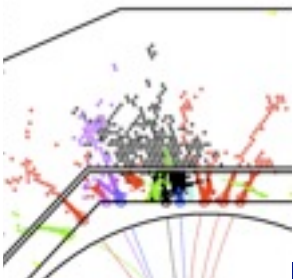
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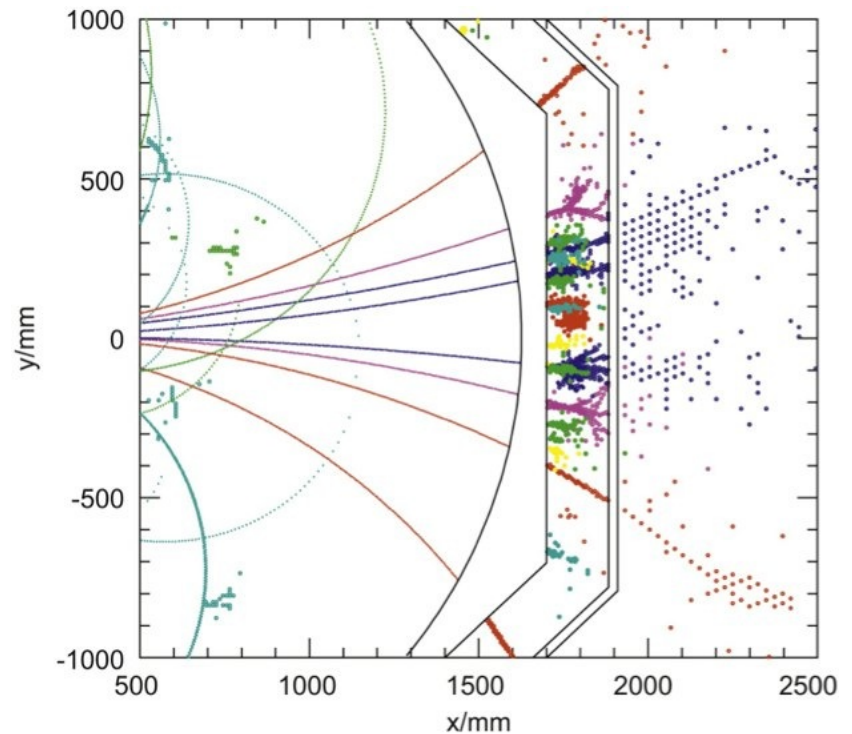
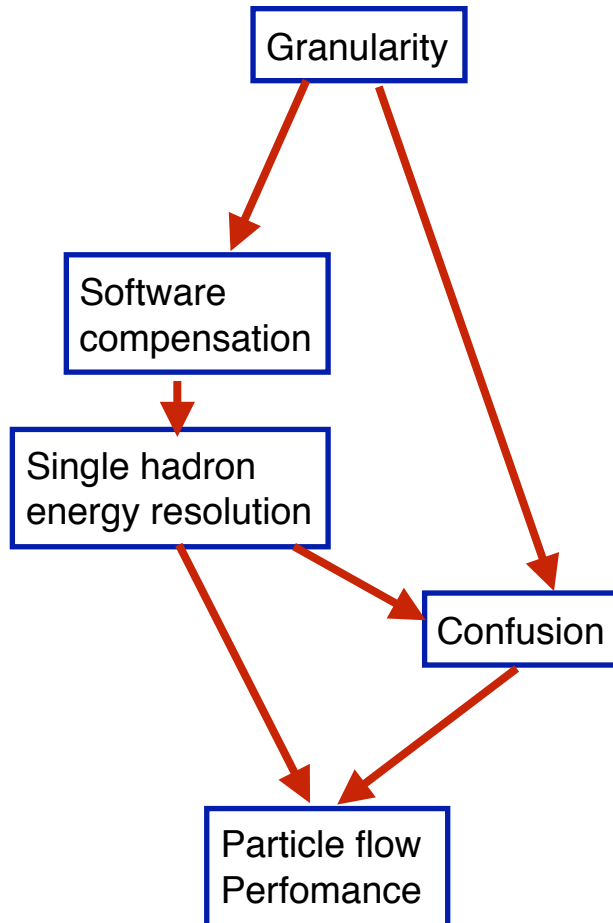


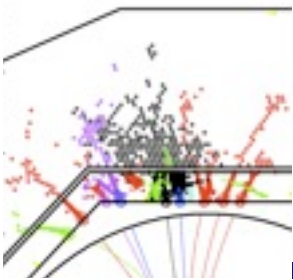
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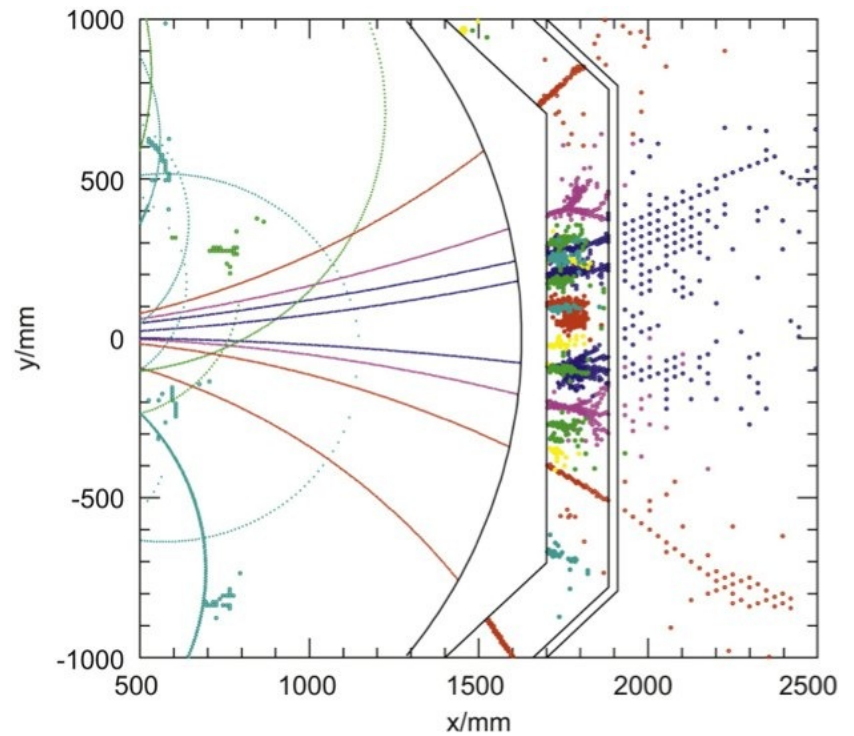
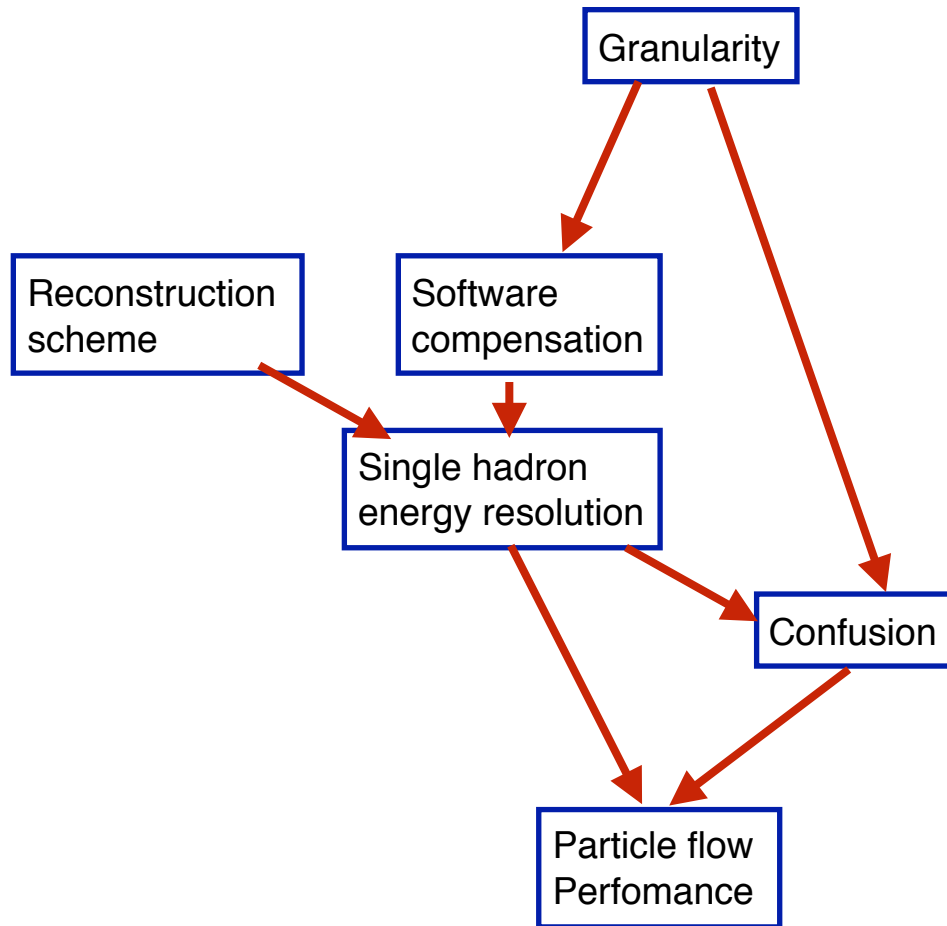


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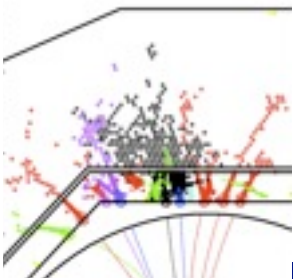




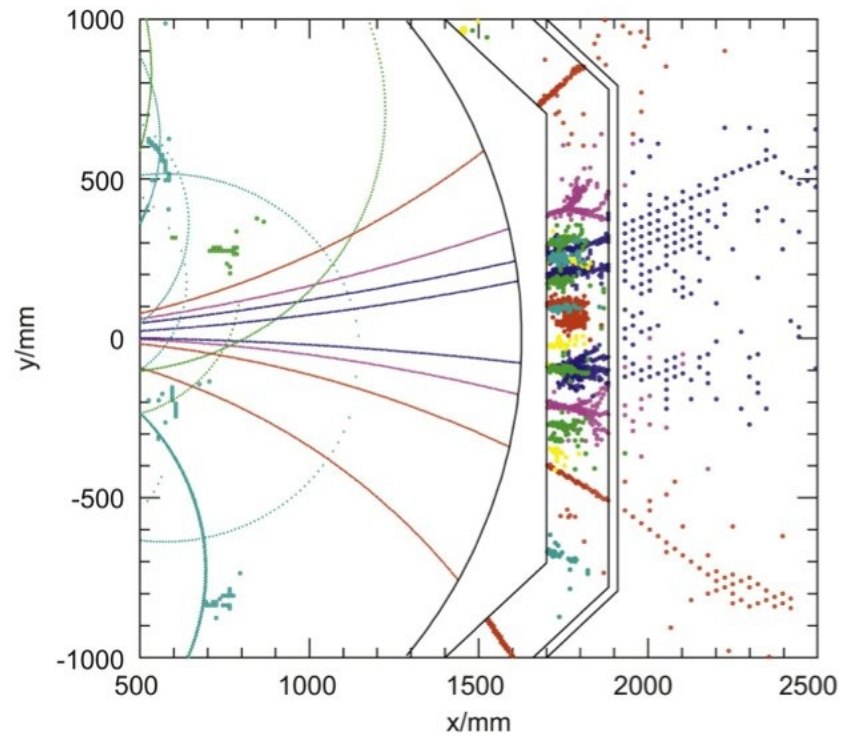
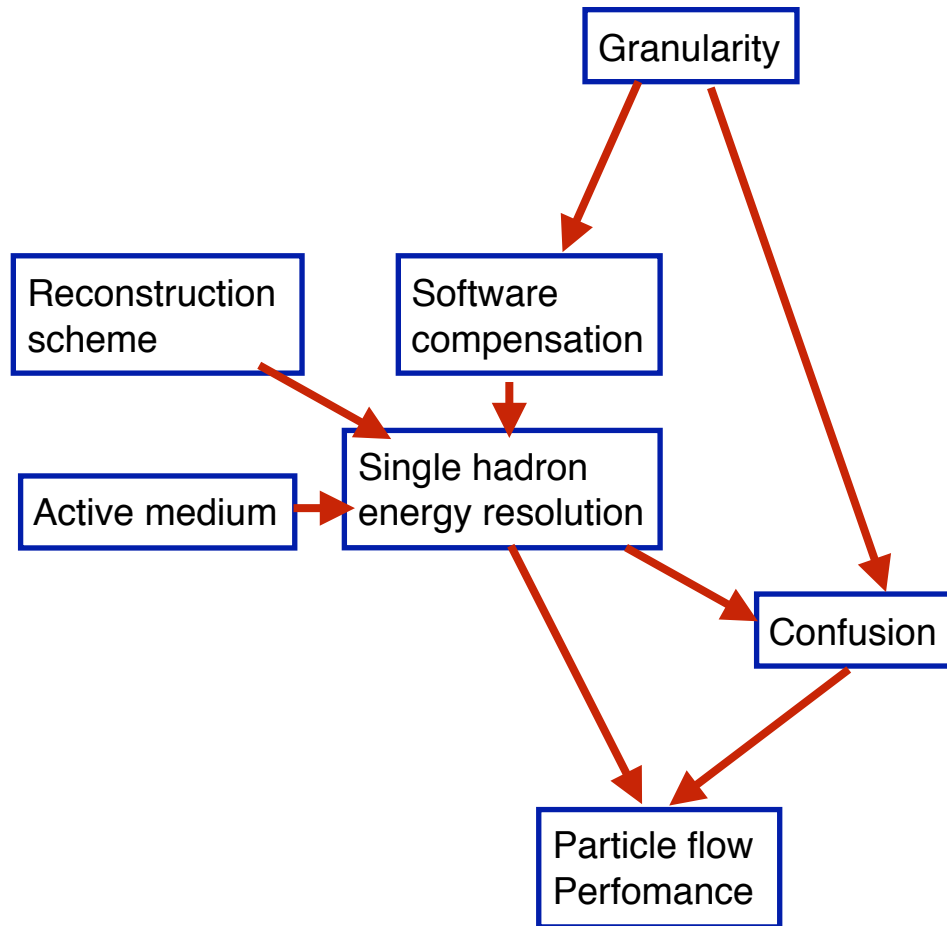
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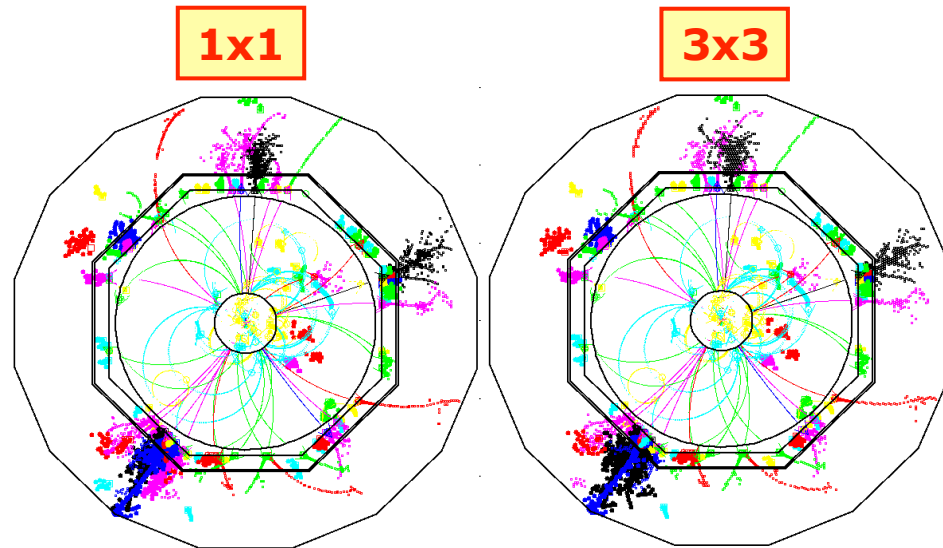


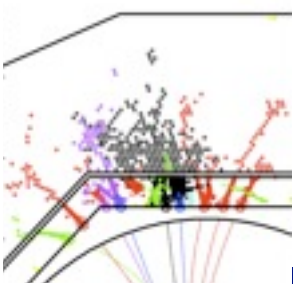


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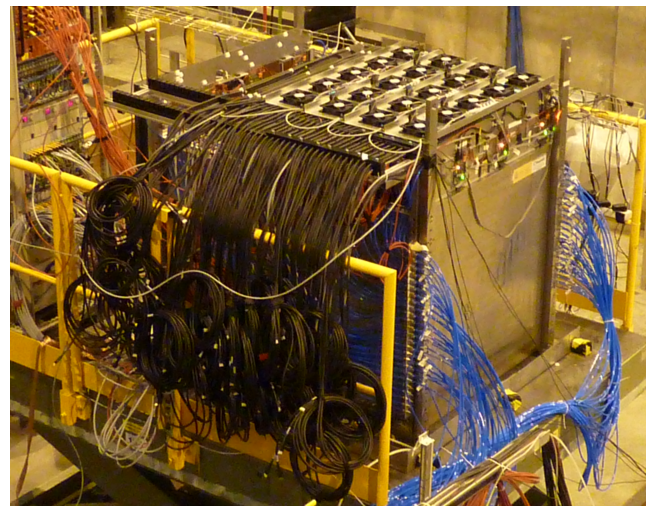
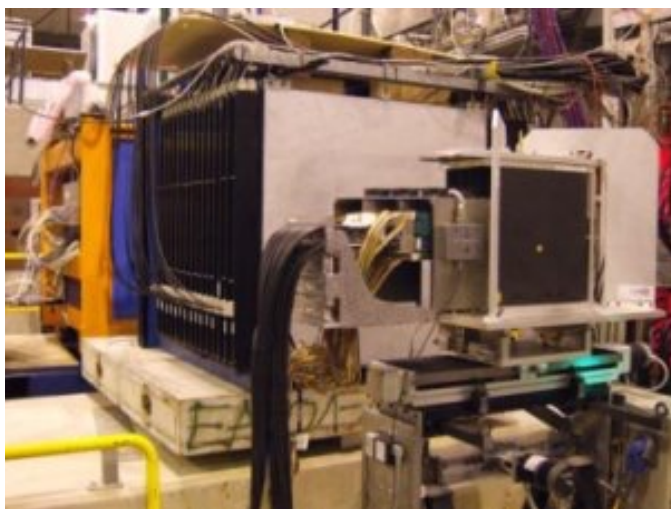
# Analogue and (semi-) digital reconstruction of single hadrons

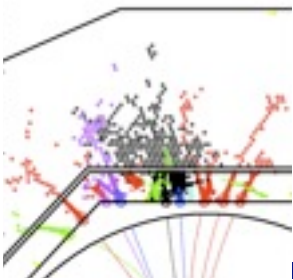




# AHCAL and SDHCAL

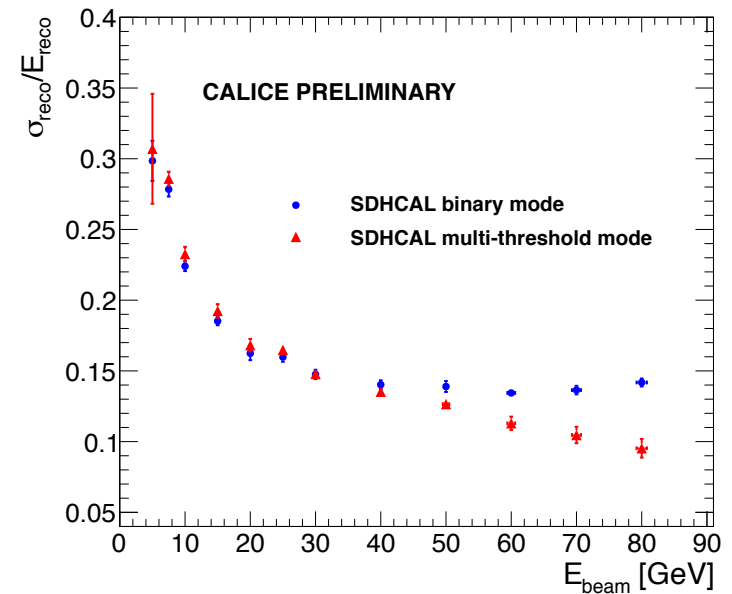
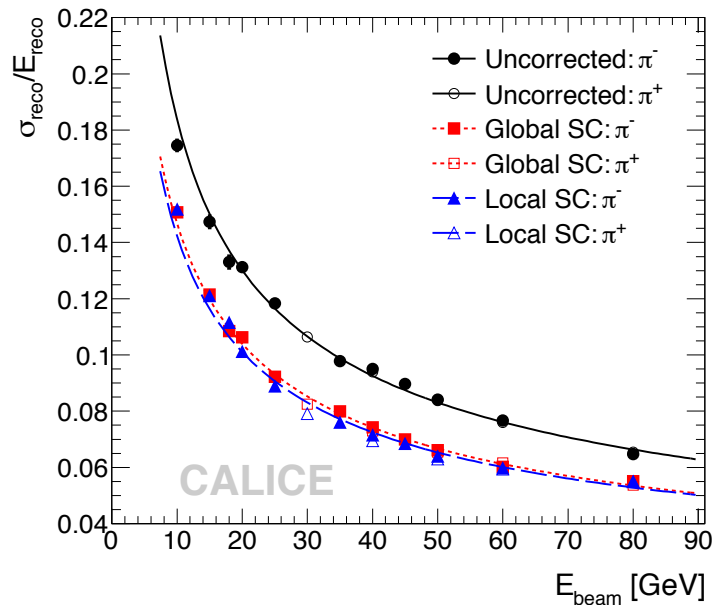
- Scint and gas prototypes differ in medium, cell size and read-out scheme
- All of them affect single hadron and jet energy resolution
- Disentangle with validated simulations, and optimise, incl. s/w comp

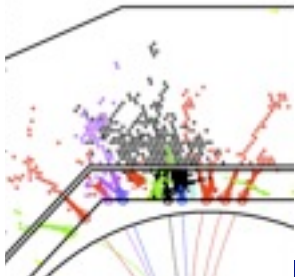




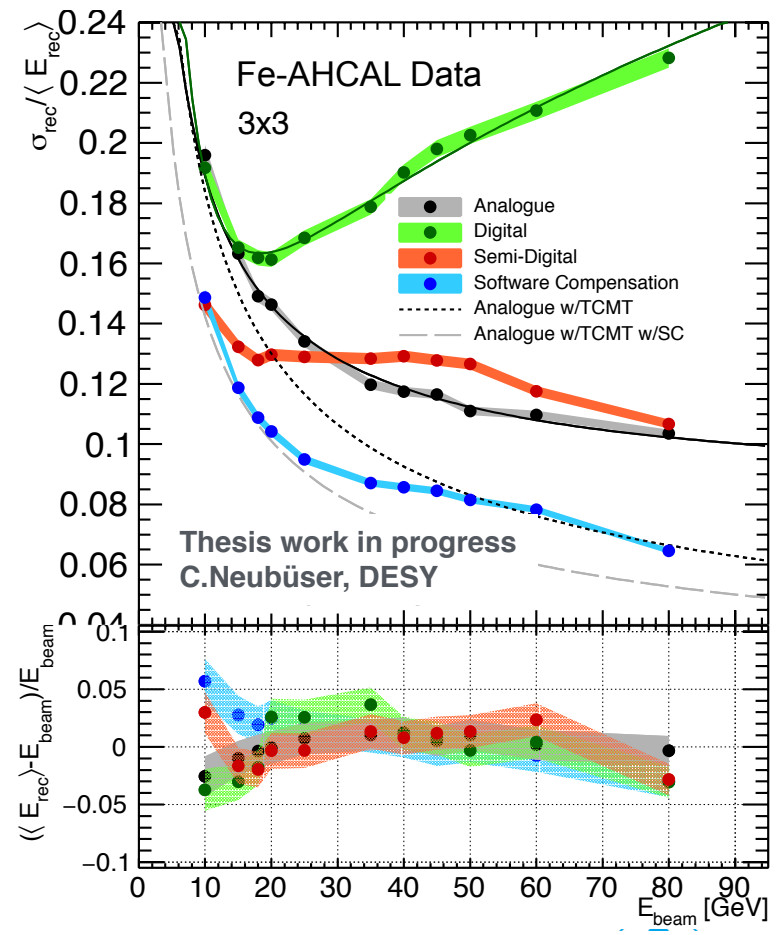
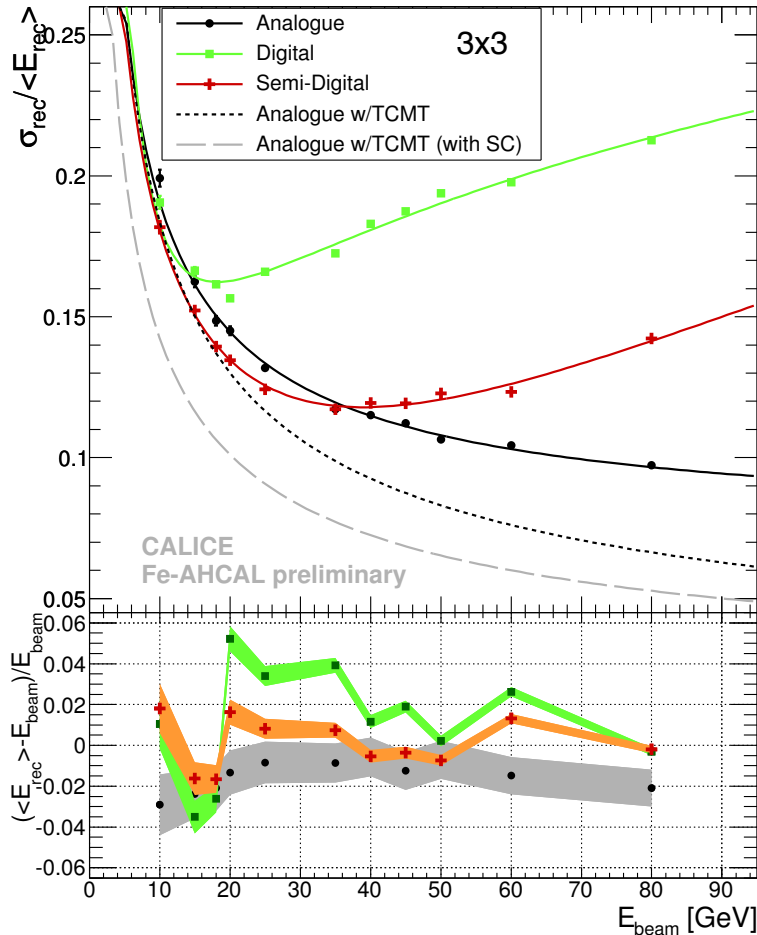
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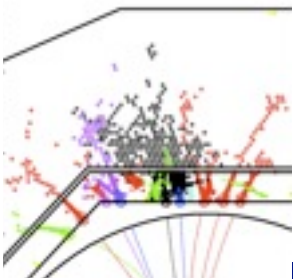




# (Semi-) digital reconstruction of AHCAL

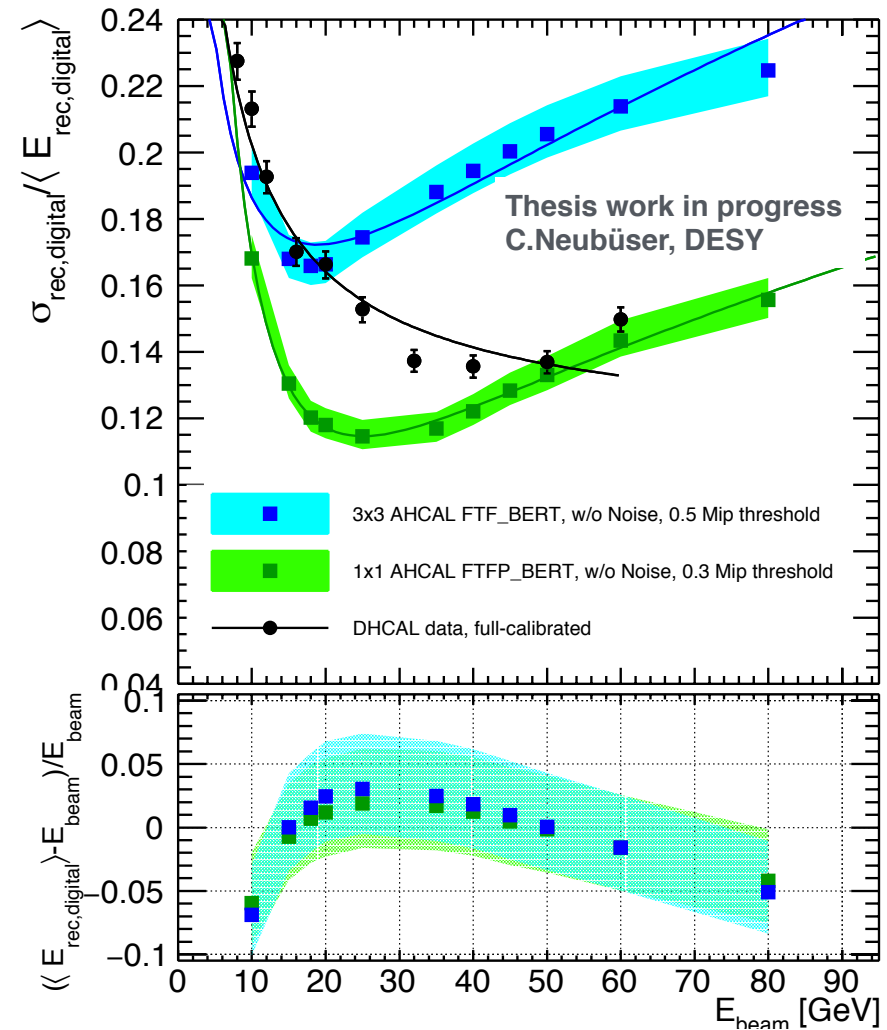


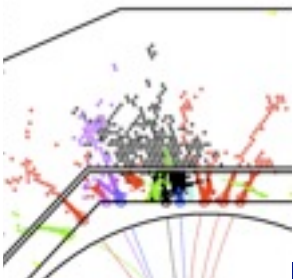
- Update of CAN-049 in preparation
  - optimise semi-digital weights, add software compensation



# Simulate smaller granularities

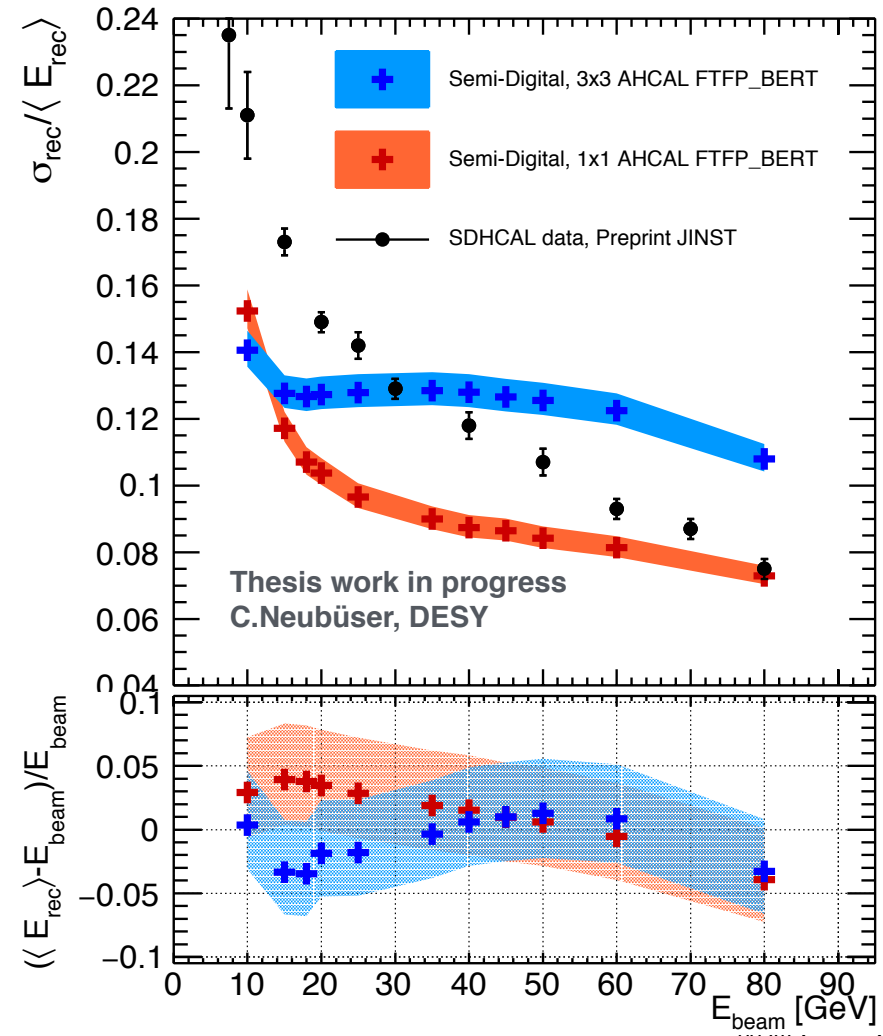
- Simulate with same degree of realism as in AHCAL test beam
  - except noise (not an issue with present SiMs)
  - and adjust threshold in order to obtain similar linearity
- Apply digital and (re-optimised) semi-digital reconstruction
- Differences between gas and scintillator to be understood
  - validated simulations on their way

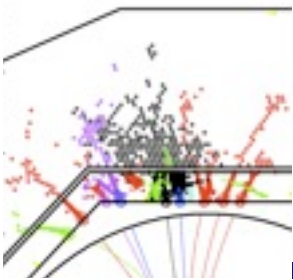




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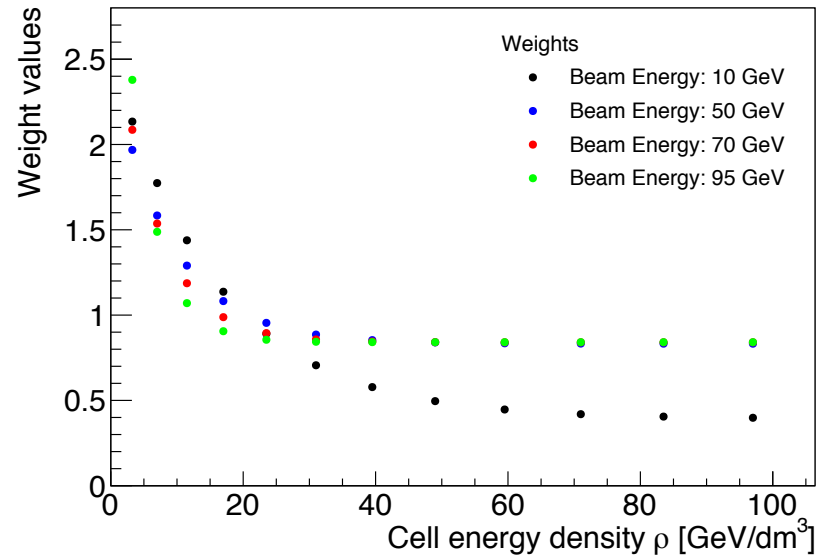
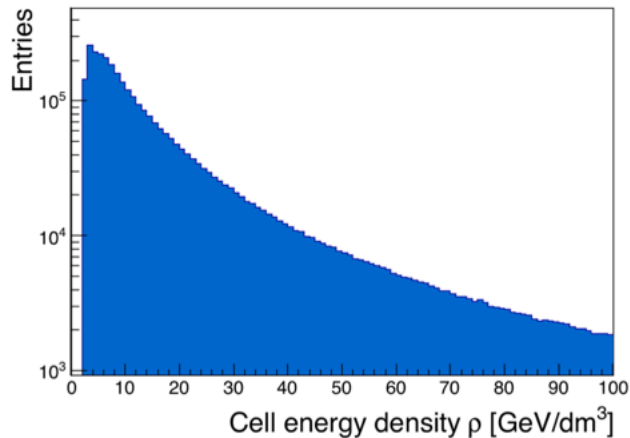
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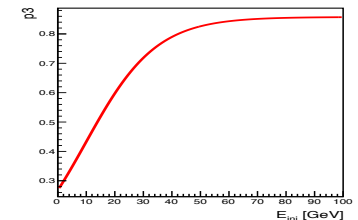
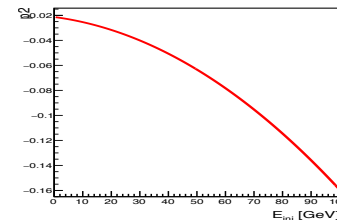
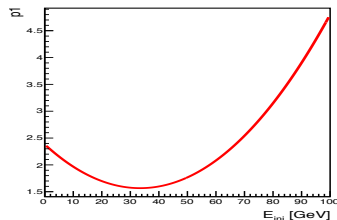


# Software compensation

- Electromagnetic showers: higher density, larger response
- Software compensation: weight has according to cell energy

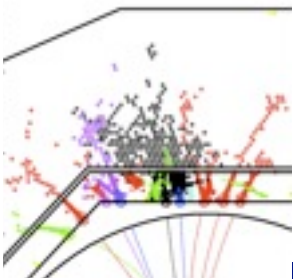


$$\omega(\rho) = p_1 \cdot \exp(p_2 \cdot \rho) + p_3$$



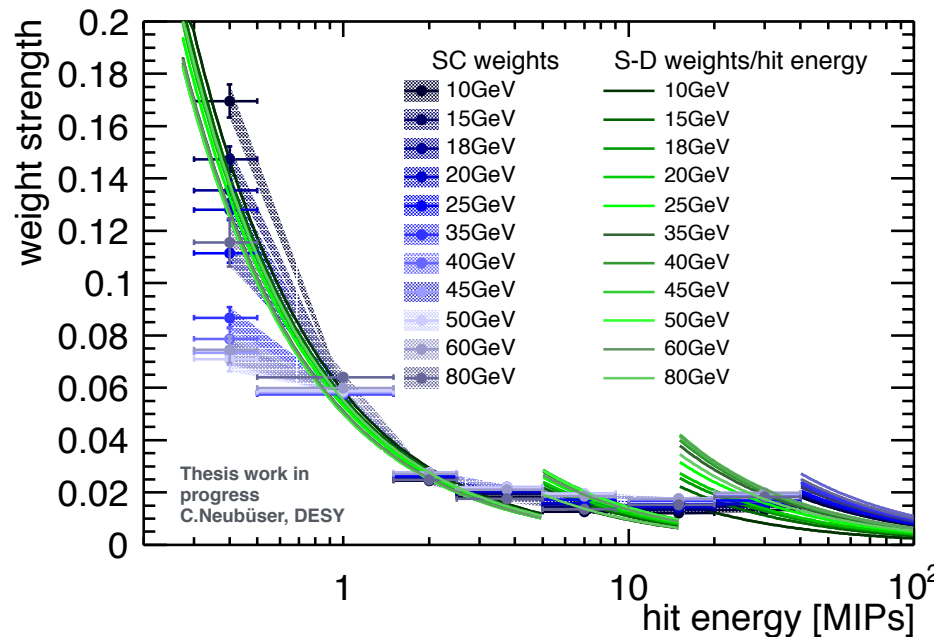
→ E<sub>beam</sub>



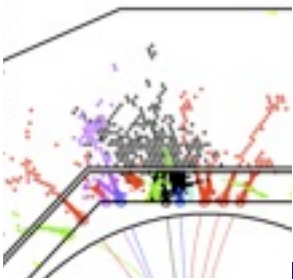


# Analogue and digital weighting

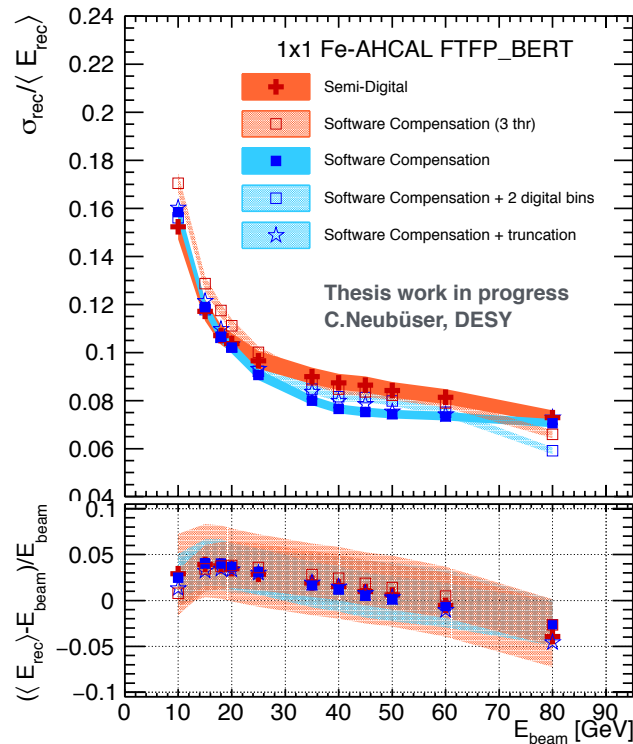
- Analogue:  $E_{rec,SC} = \sum_i \omega_{SC,i} \cdot E_i$      $\omega = \omega(E_i, E_{tot})$
- Semi-digital:  $E_{rec,semi-digital} = \alpha \cdot N_1 + \beta \cdot N_2 + \gamma \cdot N_3$      $a = a(N_{tot}), N_{tot} \sim E_{tot}^a$
- Counting is equivalent to weighting with  $1/E_{hit}$ :  $\omega = a/E_{hit}$
- Use common formalism and learn from each other



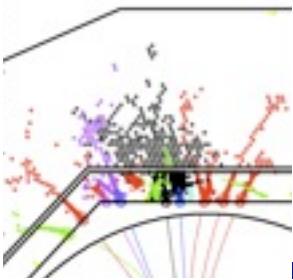
in principle the same  
differences in detail



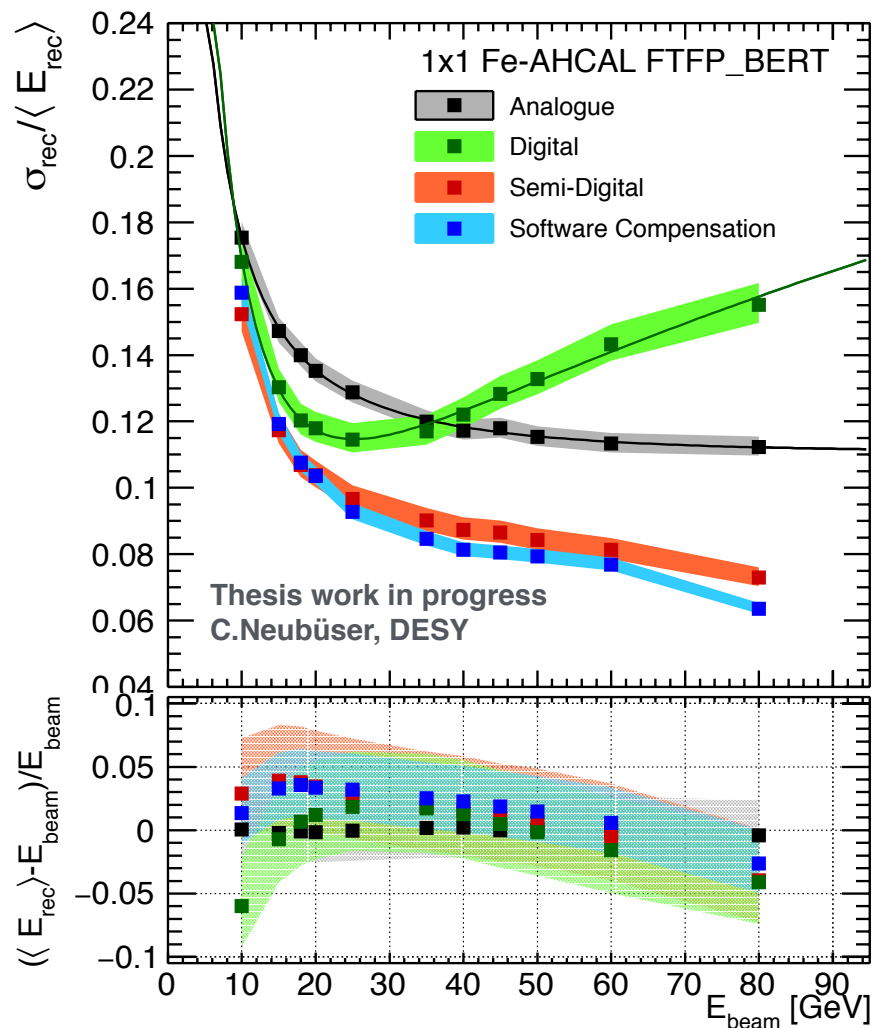
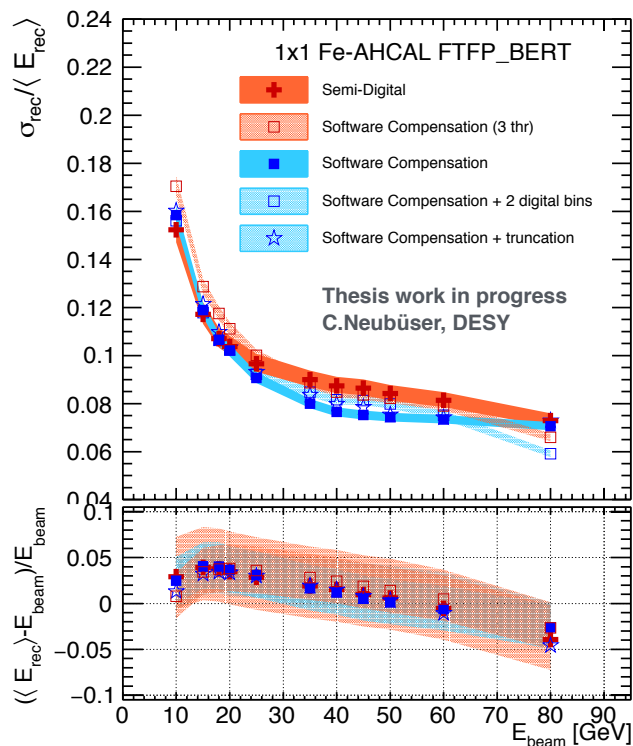
# Read-out scheme and resolution



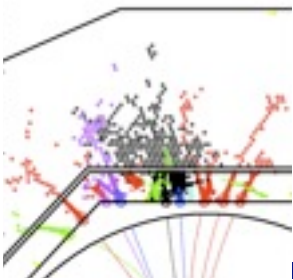
- vary number of bins and energy dependence within bins
- small differences once some weighting is applied



# Read-out scheme and resolution

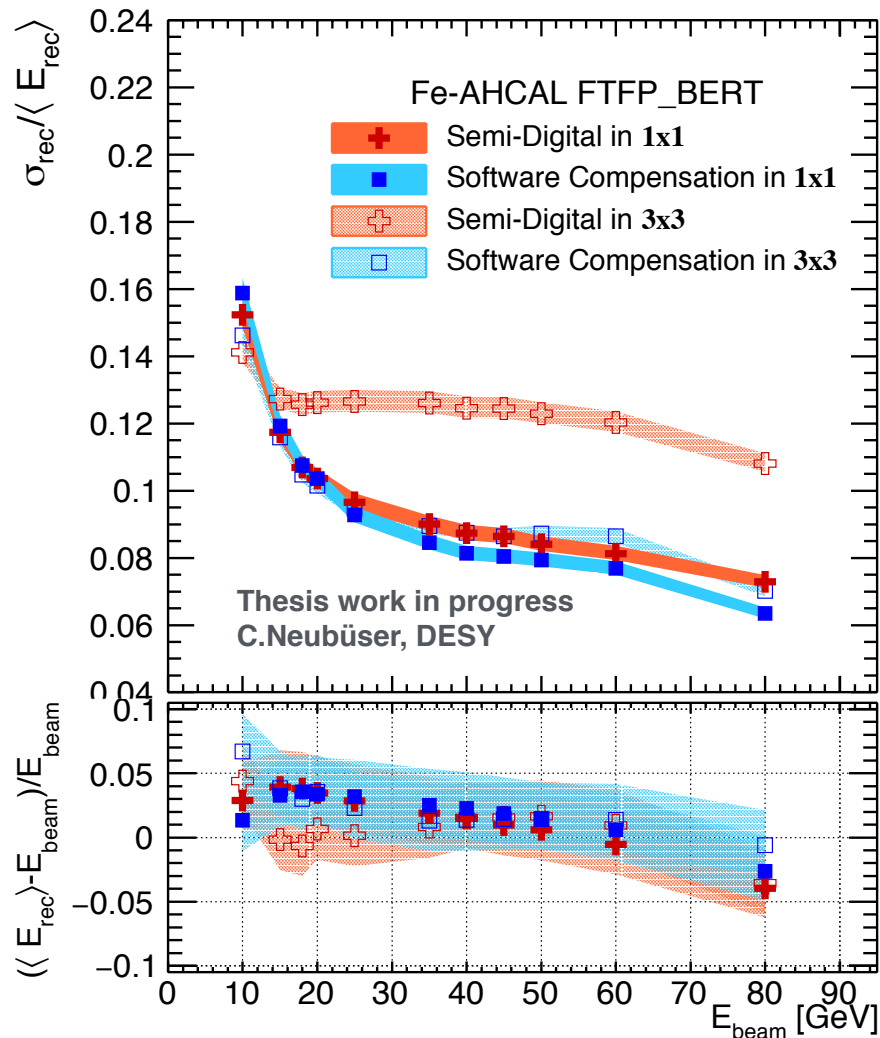


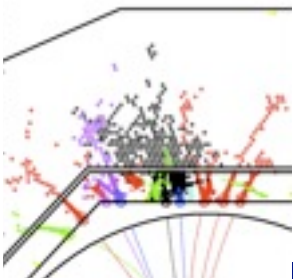
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# Granularity and resolution 1

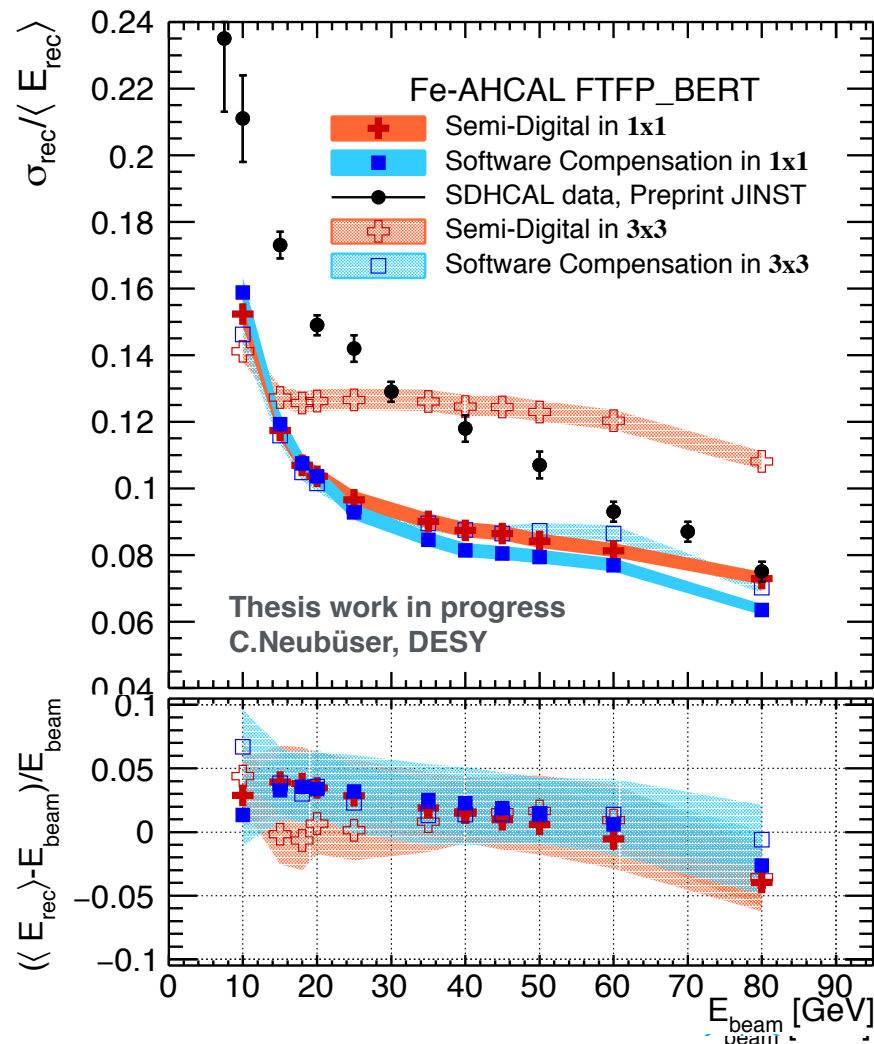
- 1x1: semi-digital as good as analogue with s/w comp
  - 2 bits are enough
- 3x3: analogue with s/w comp better than SD, as good as 1x1
  - for analogue read-out 3x3 is enough

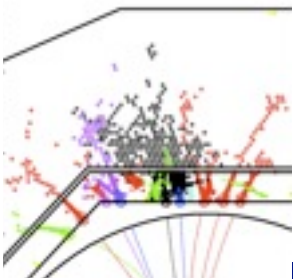




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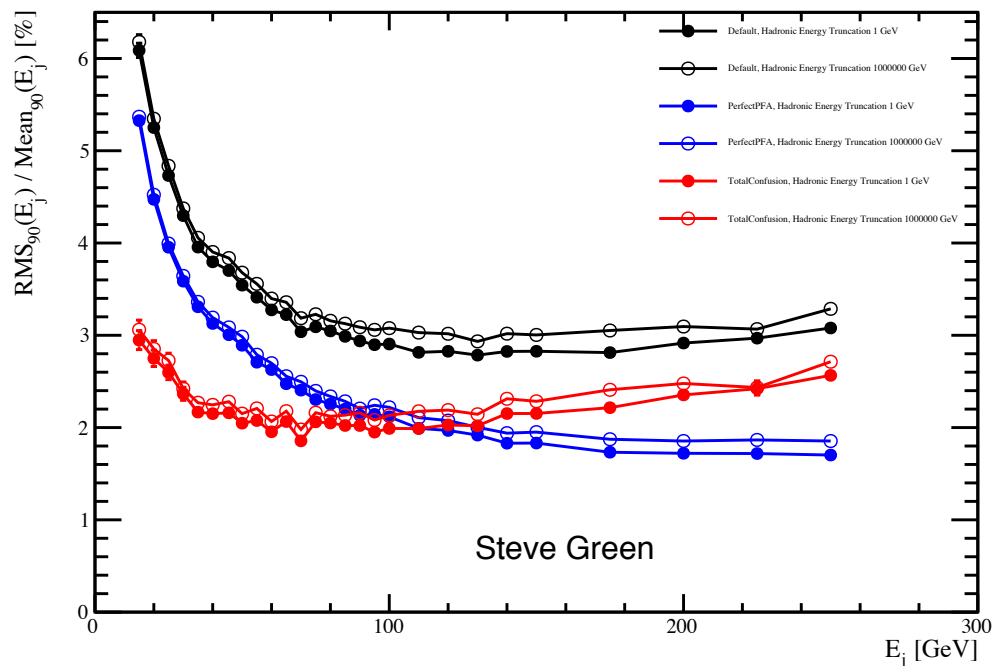


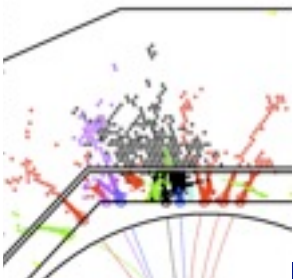


# s/w compensation and PFLOW

- Jet energy resolution is the goal
- In principle can benefit in two-fold way:
  - improve resolution for neutral objects - done
  - improve cluster energy estimators for track-cluster association - on its way

studies with Pandora PFA



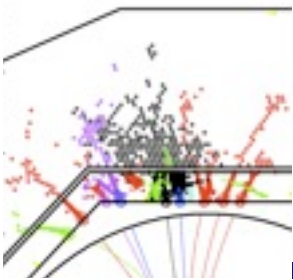


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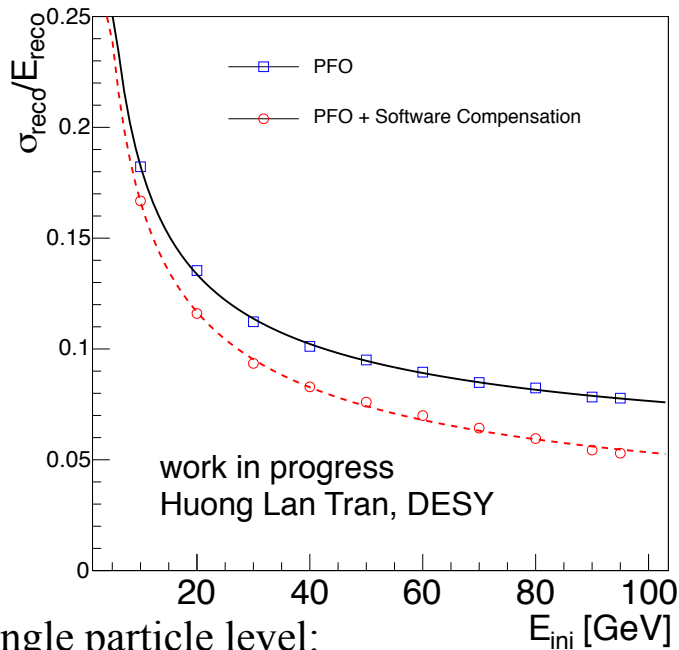
studies with Pandora PFA



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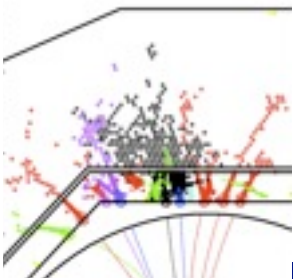
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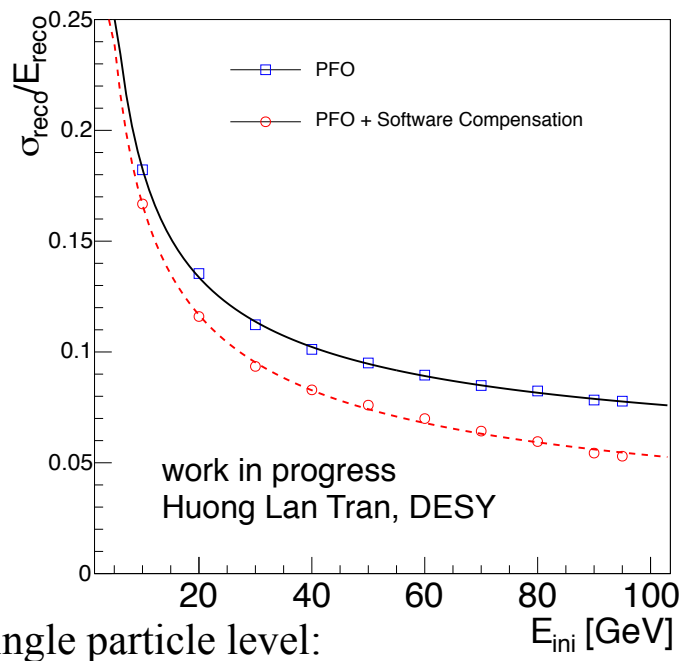
Single particle level:



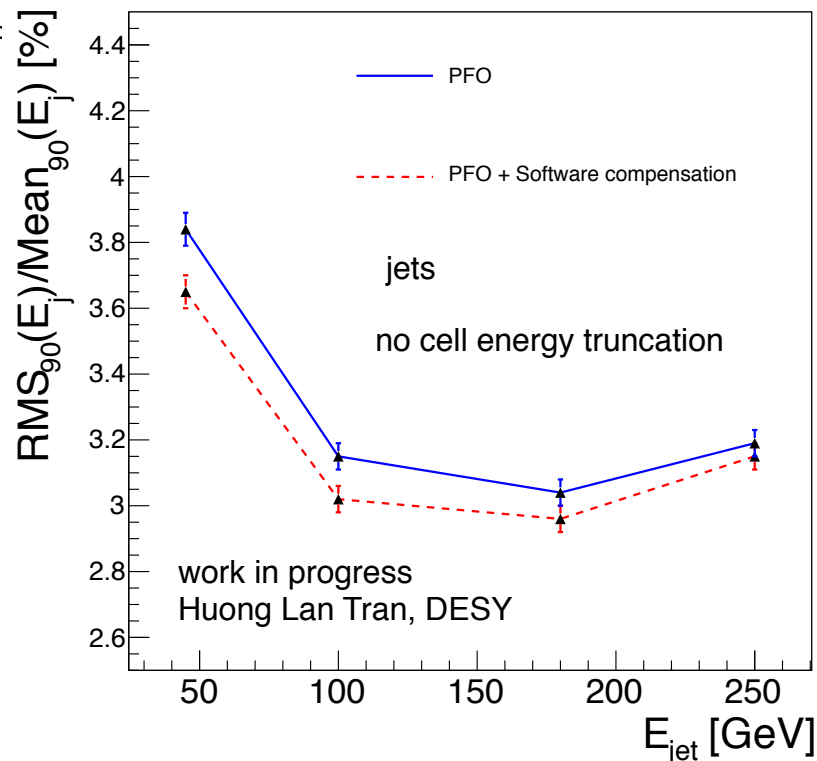


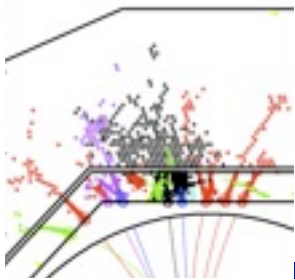
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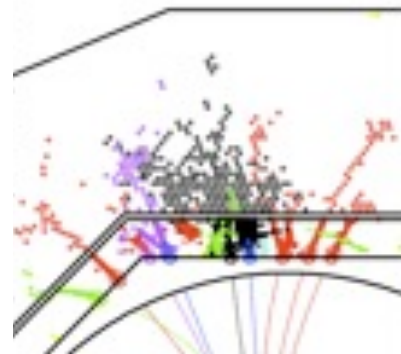
studies with F

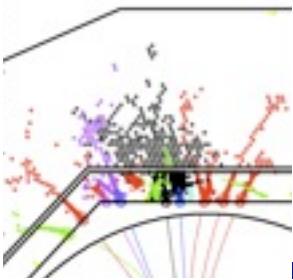




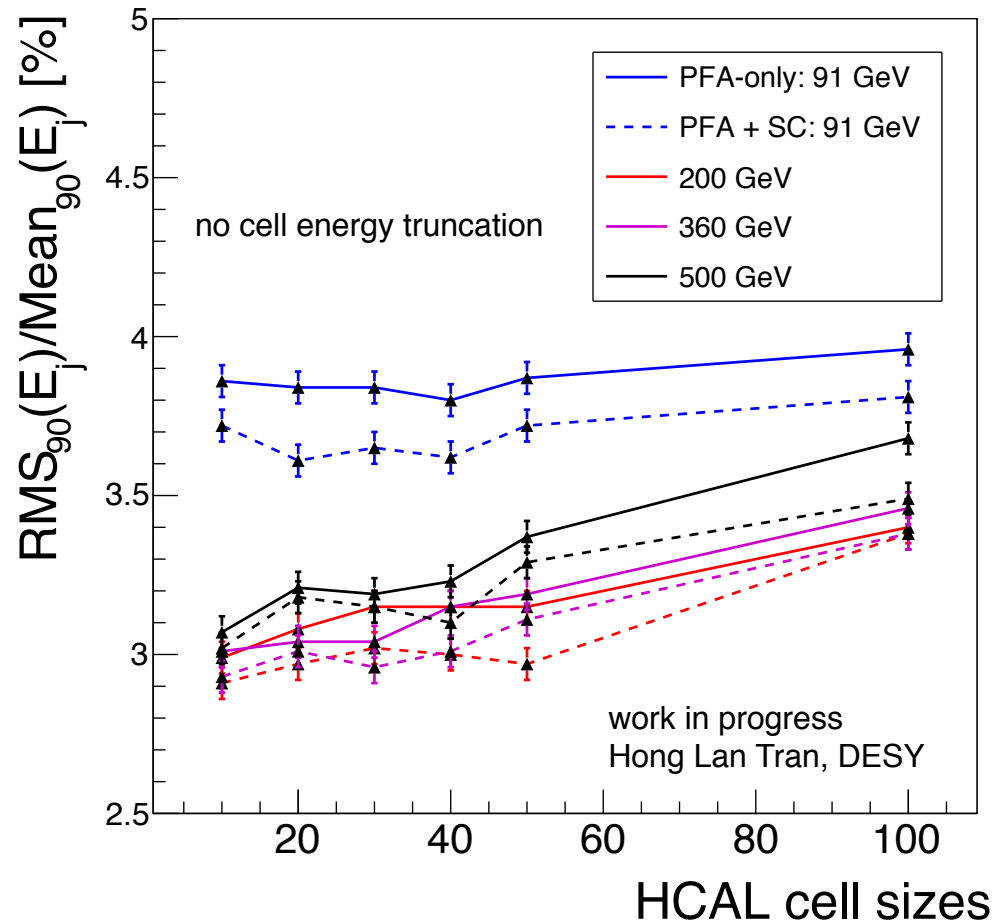
# s/w compensation and clustering

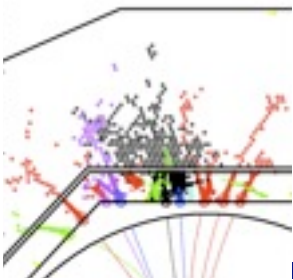
- Hypothesis testing at re-clustering stage
  - use track energy
  - benefits demonstrated earlier (fractal dim.)
- However: Weighting the energy before or during the clustering stage of particle flow reconstruction is not straightforward
  - In general  $\omega = \omega(E_i, E_{\text{tot}})$
  - Easy only for truncation
- General issue for all weighting schemes, inevitable for digital and semi-digital reconstruction
- Non-linear response: cannot revert to plain E flow in dense environments
  - $\omega E_1 + \omega E_2 \neq \omega (E_1 + E_2)$



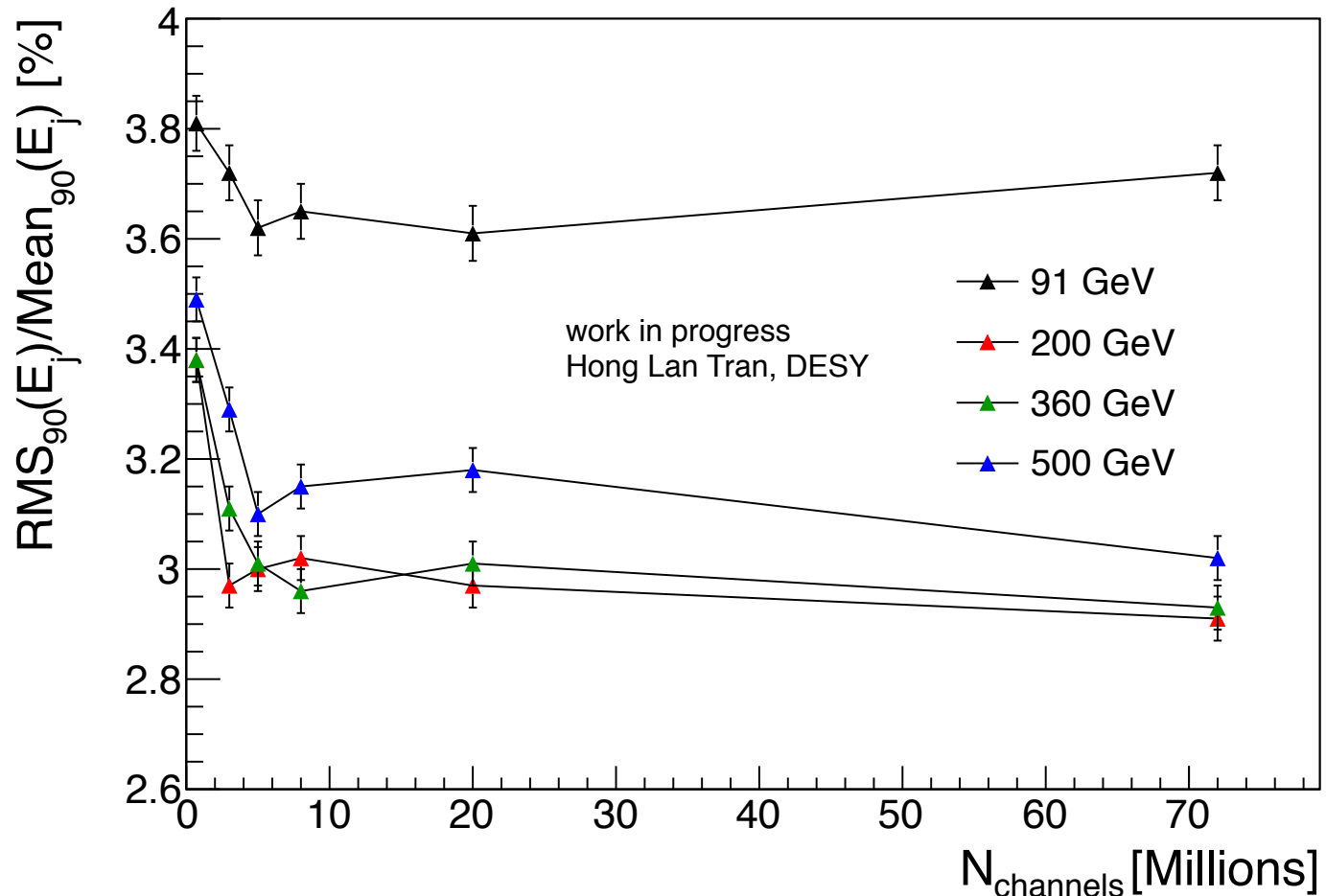


# Granularity and resolution 2

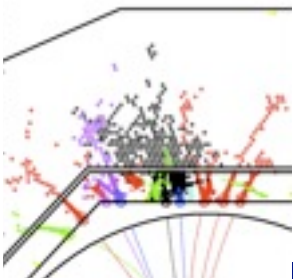




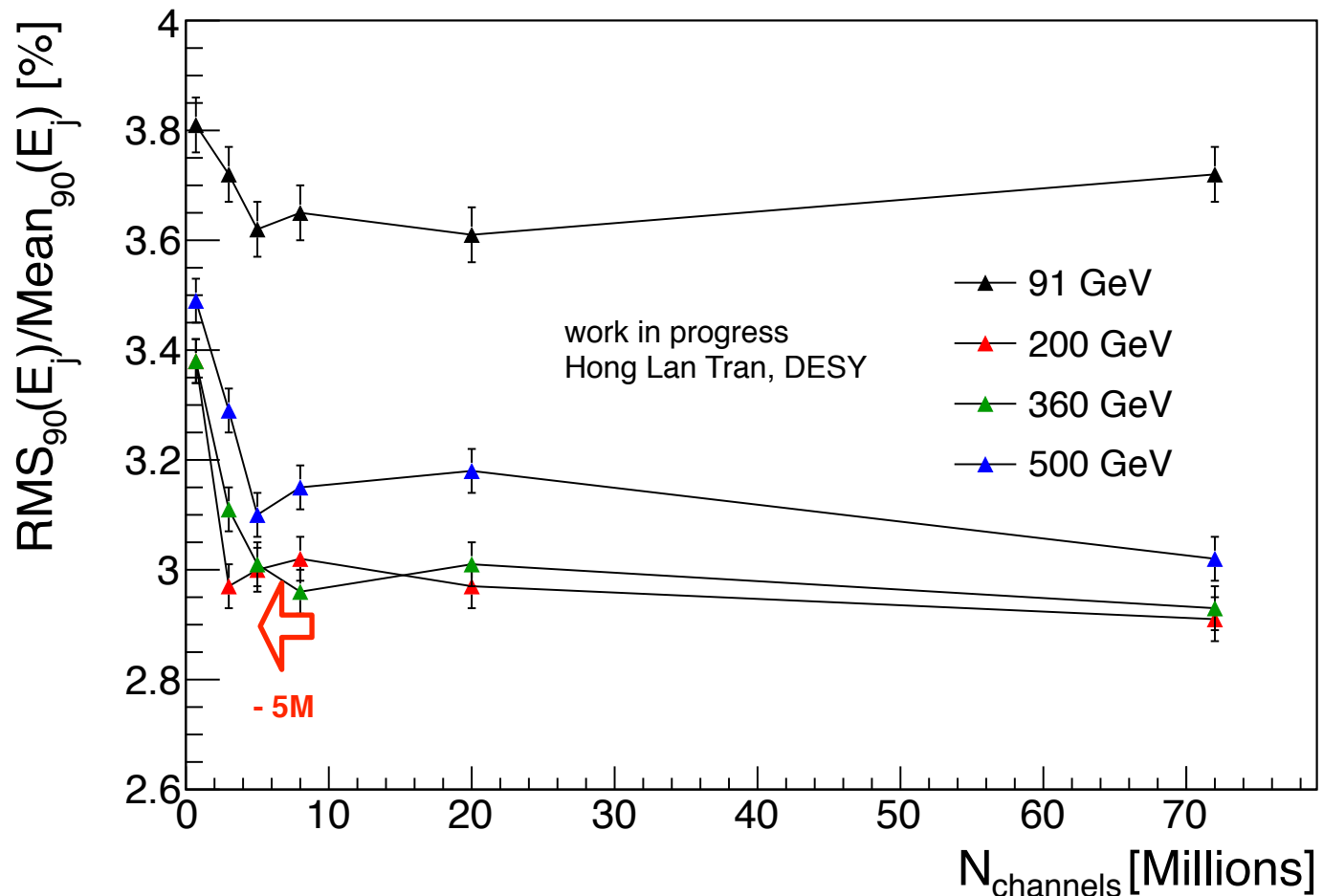
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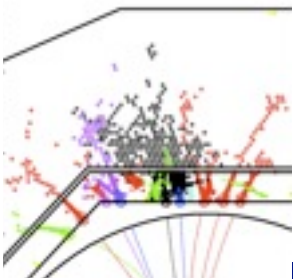
- 3 cm still a very reasonable choice



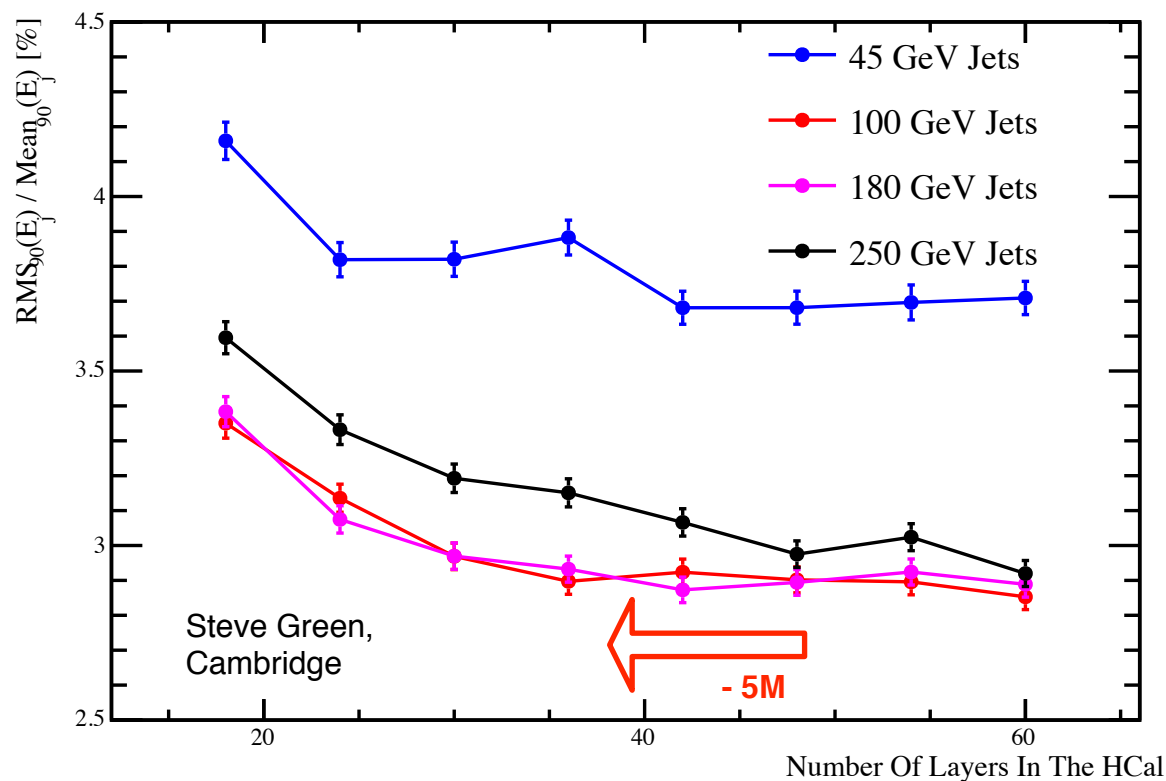
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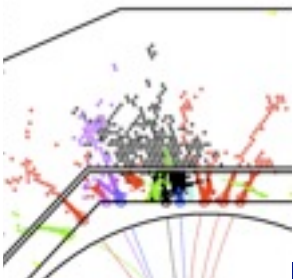
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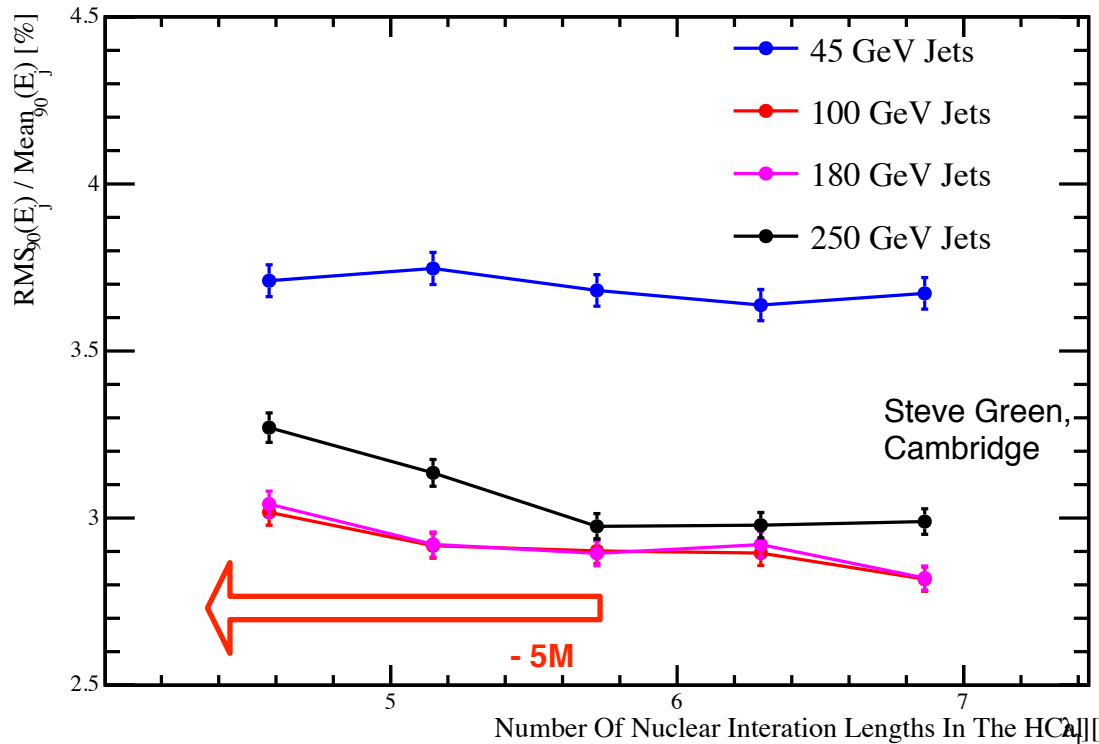
# Cost optimisation: long. sampling



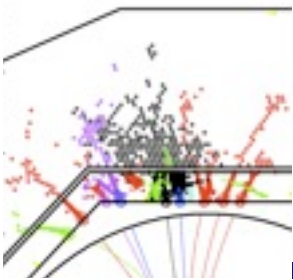
- fewer layers: not for free, but at least no knee
- not necessarily the same for SDHCAL



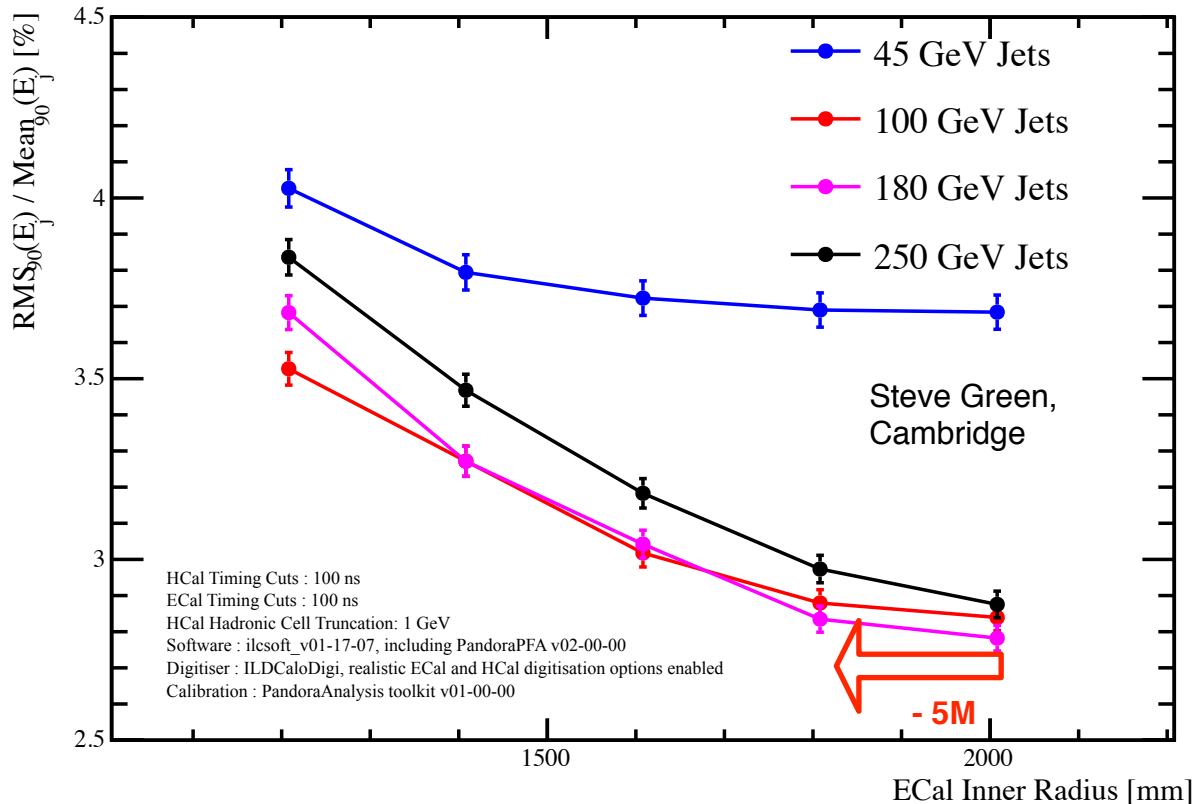
# Cost optimisation: depth



- this plot  $n(\text{layers}) = \text{const}$ ; should have constant pitch also
- additional savings from coil and yoke - or smaller reduction
- but should be studied with missing energy performance

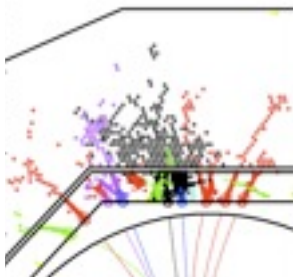


# Cost optimisation: inner radius



- shown: cost variation is for 18 cm smaller HCAL inner radius
- additional savings from coil and yoke - or smaller reduction



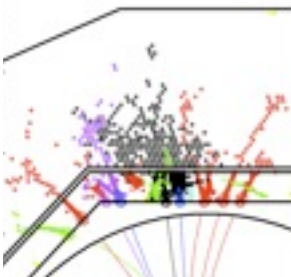


# Conclusion

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- We are getting close to collecting the remaining pieces for the complete picture
- Still some way to finalise these studies
  
- More to come:
- Scintillator and gaseous comparison
  - finalise data and simulation
- Timing cuts for energy reconstruction and pattern recognition
- Integration of ARBOR and its new algorithms
  
- Cost optimisation: from HCAL point of view smaller radius is safest way

# Back-up slides



# Granularity optimisation

- Based of Pandora PFA
- Large radius and B field drive the cost
- Both ECAL and HCAL segmentation of the order of  $X_0$ 
  - longitudinal: resolution
  - transverse: separation
- Cost optimisation to be done

