

# ***Right-handed neutrino dark matter under the $B-L$ gauge interaction***

Kunio Kaneta (IBS-CTPU)



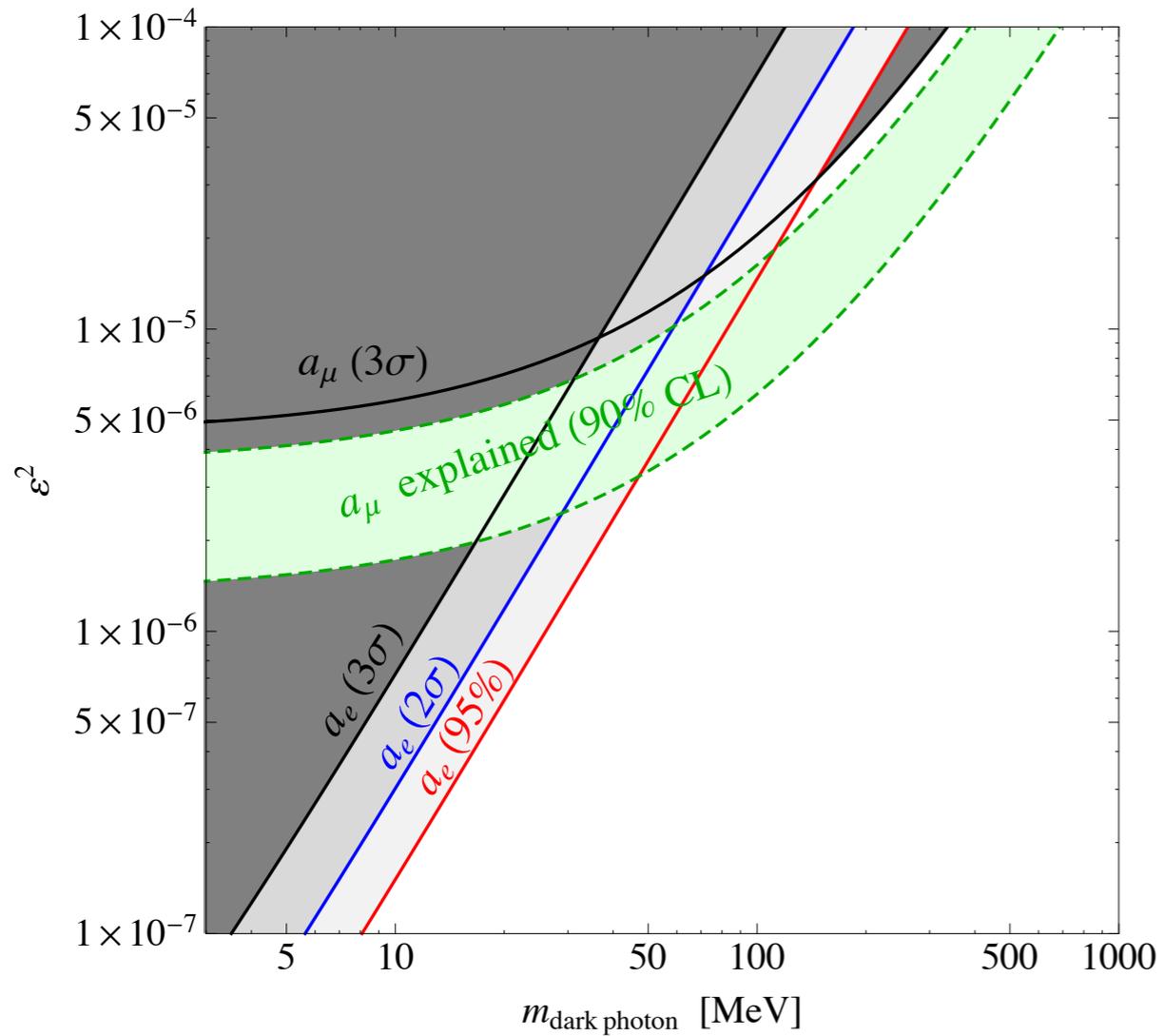
in collaboration with Zhaofeng Kang (KIAS) and Hye-Sung Lee (IBS-CTPU)

Reference: 1606.09317

ILC Summer Camp 2016, July 23-26, 2016, Iwate

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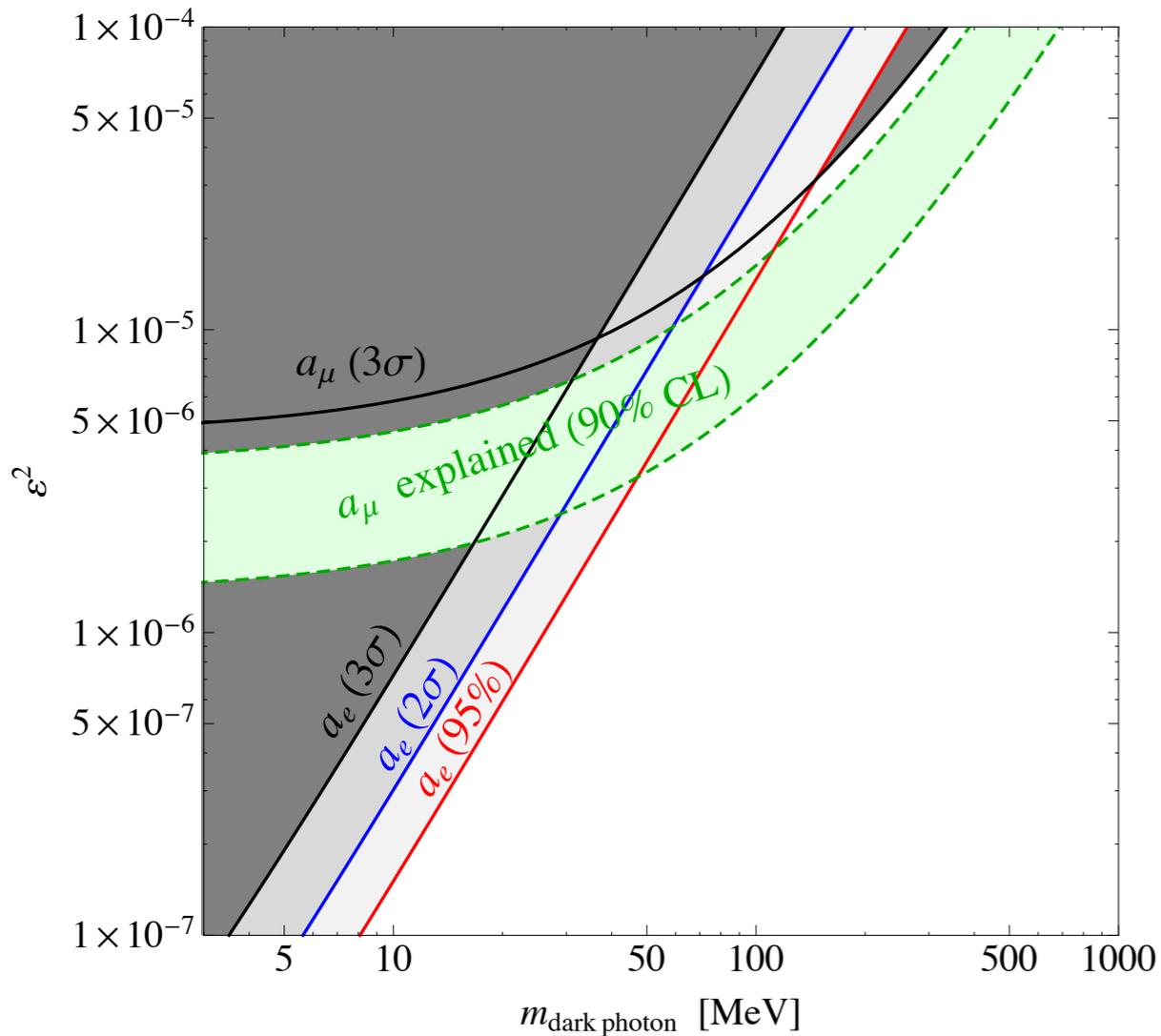
[green band: Pospelov, '08]



(figure by H.-S. Lee)

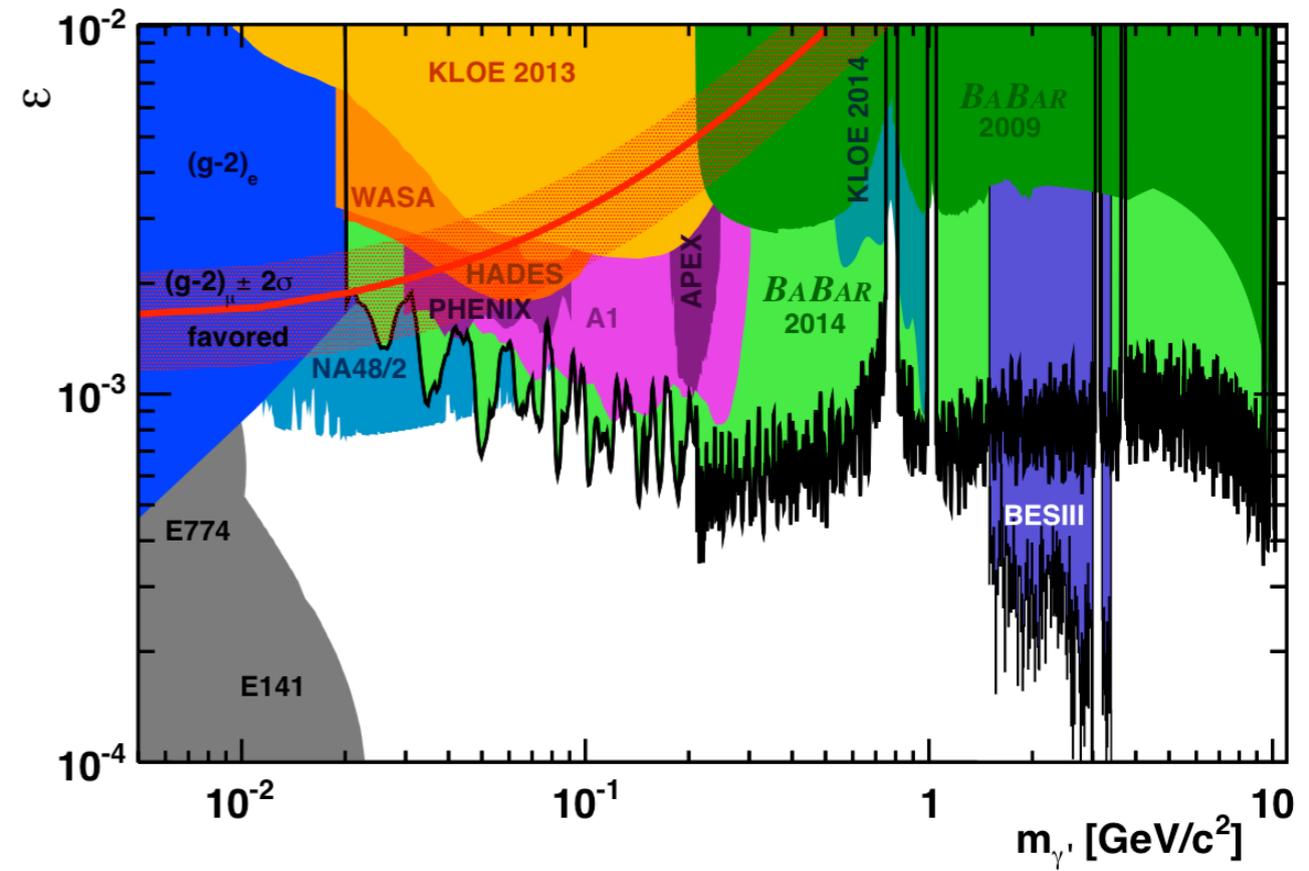
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- However, **whole green band** is excluded now. (The last small portion is closed by CERN NA48/2)

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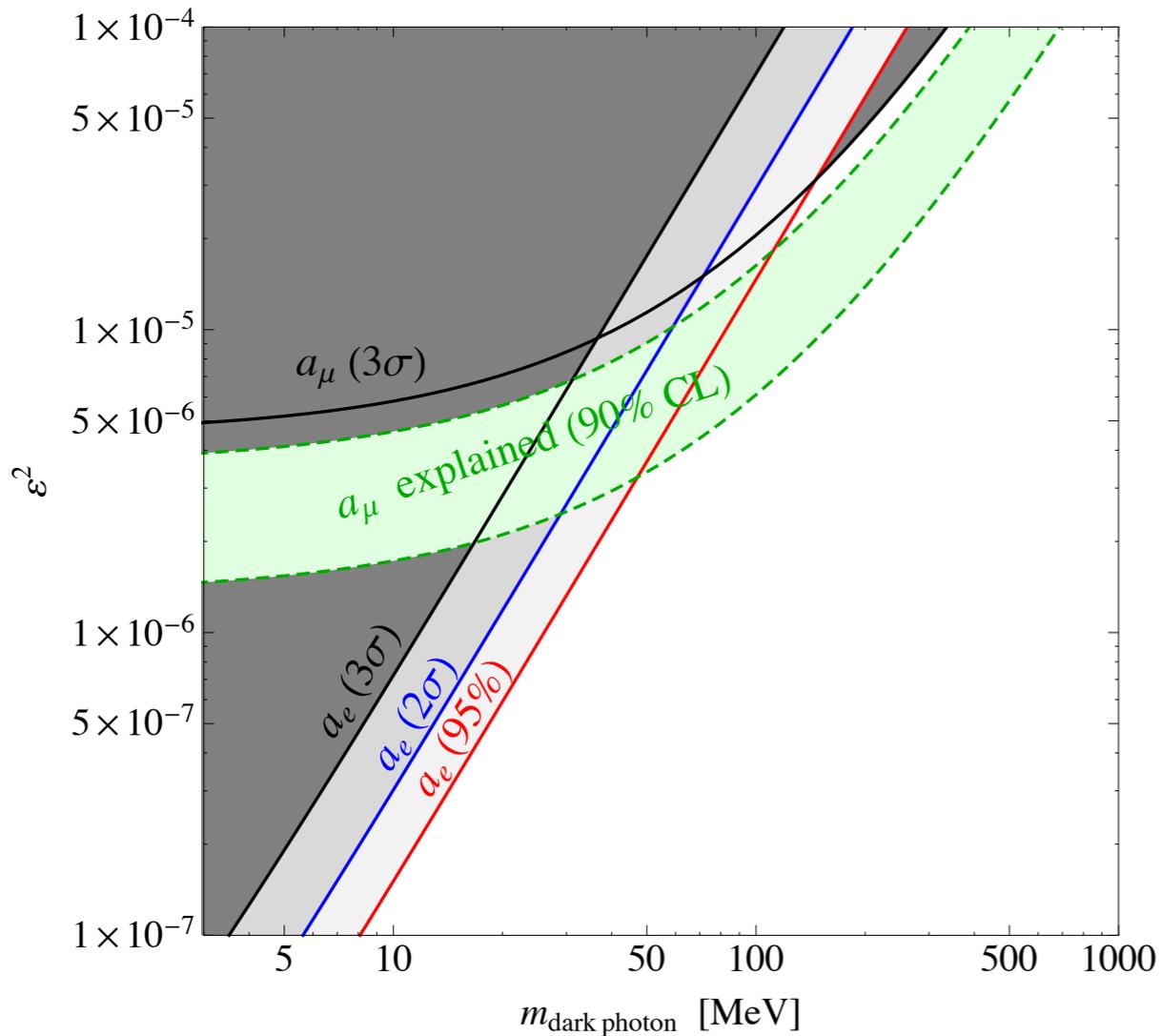
(figure by H.-S. Lee)

[Soffer, '15]

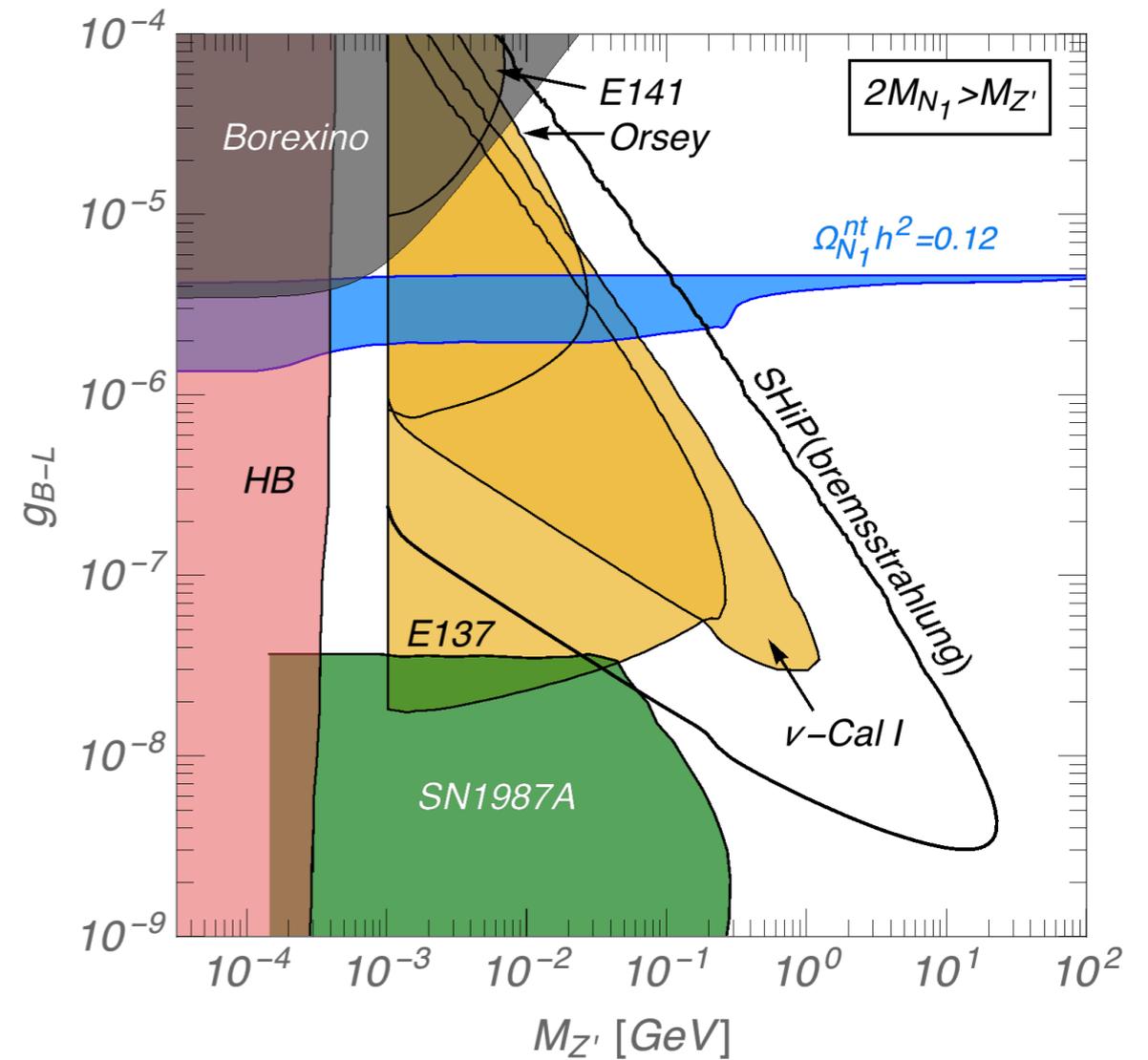


- Until 2015, **muon g-2** had provided a strong motivation for the light dark photon.
- However, **whole green band** is excluded now. (The last small portion is closed by CERN NA48/2)
- **We will try to provide another well-motivated parameter space for  $Z'$ .**

[green band: Pospelov, '08]



(figure by H.-S. Lee)



# ***Outline***

1. Introduction
2. Dark matter under the  $B-L$  gauge force
3. Implications
4. Summary

# ***1. Introduction***

## Right-handed neutrinos as a missing piece to the SM

- Neutrino oscillations imply non-zero masses of neutrinos
- Presumably neutrino masses indicate the existence of chiral partners: right-handed neutrinos
- Right-handed neutrinos also play an important role in addressing other issues, e.g., dark matter and baryon asymmetry of the universe

## The Nobel Prize in Physics 2015



Photo: A. Mahmoud  
Takaaki Kajita  
Prize share: 1/2



Photo: A. Mahmoud  
Arthur B. McDonald  
Prize share: 1/2

The Nobel Prize in Physics 2015 was awarded jointly to Takaaki Kajita and Arthur B. McDonald "for the discovery of neutrino oscillations, which shows that neutrinos have mass"

## Three right-handed neutrinos?

- A minimal framework is just **the SM + three right-handed (Majorana) neutrinos**

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + i\bar{N}_i \not{\partial} N_i - \left( y_{\alpha i} \bar{L}_\alpha N_i \tilde{H} + \frac{M_i}{2} \bar{N}_i^c N_i + h.c. \right) \quad (\nu\text{MSM})$$

[Asaka, Blanchet, Shaposhnikov, '05]

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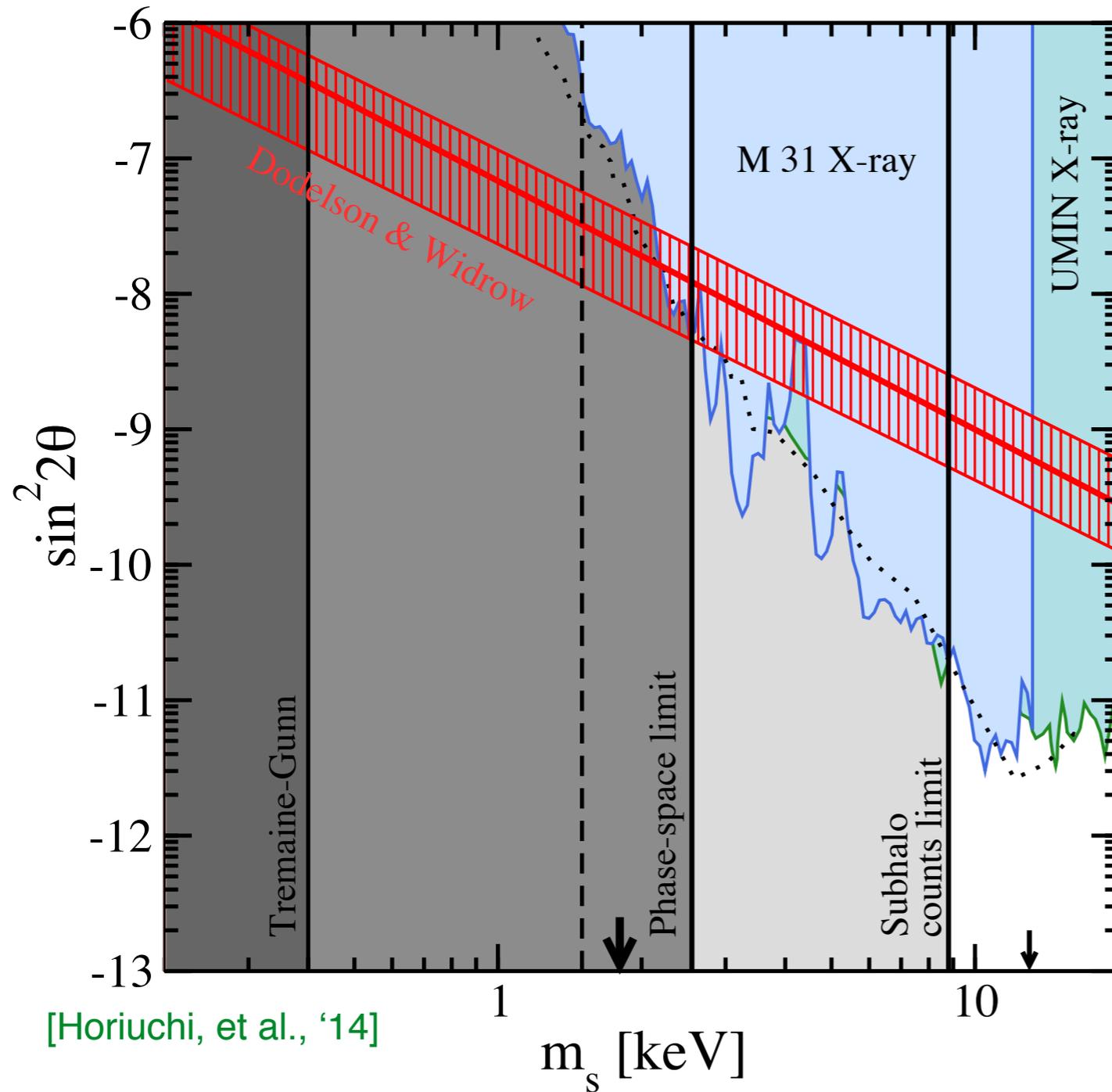
- The lightest right-handed neutrino  $N_1$  can be (keV-scale) dark matter via Dodelson-Widrow mechanism

[Dodelson, Widrow, '94]

$$\Omega_{N_1} h^2 \sim 0.12 \times (\sin^2 2\theta / 7 \times 10^{-8})^{1.23} (M_{N_1} / \text{keV})$$

[K.Abazajian, '06]

## Constraints on the simplest dark matter production scenario



- Red region: whole amount of dark matter number density is explained by Dodelson-Widrow mechanism

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- X-ray observations and phase-space density of dSphs give stringent constraints

- **Alternative production mechanism is necessary**

(Cf. [R.Adhikari et al, '16])

**We discuss a possible scenario for viable production mechanism**

## Success of the SM and the gauge principle

- The SM is a phenomenologically successful model so far, and its success is supported by the *gauge principle*:  $G_{SM} = SU(3)_C \times SU(2)_L \times U(1)_Y$
- Gauge symmetry plays a role to regulate not only the gauge interactions but also the matter contents by means of the anomaly cancellation

*By following this success, the  $U(1)_{B-L}$  gauge symmetry is the most attractive symmetry that offers three right-handed neutrinos*

## Our framework

- Under the gauge symmetry  $G = G_{SM} \times U(1)_{B-L}$ , we have following new fields:
  - three right-handed neutrinos ( $N_1, N_2, N_3$ ;  $B-L$  charge -1)
  - A singlet Higgs field ( $\Phi_S$ ;  $B-L$  charge -2)
  - $B-L$  gauge boson ( $Z'$ )
- Our framework  $\sim$  the local  $U(1)_{B-L}$  extended version of the vMSM (we call this *UvMSM*)

*The  $B-L$  gauge interaction can provide viable dark matter production mechanisms;  
**freeze-in and freeze-out***

## ***2. Dark matter under the B-L gauge force***

## Our setup

➤ Lagrangian of the  $U(1)_{B-L}$  is given by

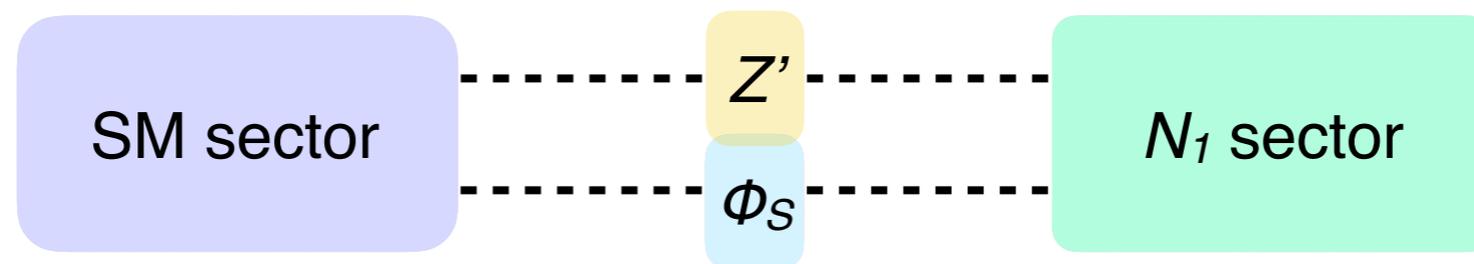
$$\mathcal{L} = \mathcal{L}_{\text{SM}} + i\bar{N}_i \not{D} N_i - \left( y_{\alpha i} \bar{L}_\alpha N_i \tilde{\Phi}_H + \frac{\kappa_i}{2} \Phi_S \bar{N}_i^c N_i + h.c. \right) + |D_\mu \Phi_S|^2 - V(\Phi_H, \Phi_S) - \frac{1}{4} Z'_{\mu\nu} Z'^{\mu\nu}$$

$$V(\Phi_H, \Phi_S) = \frac{\lambda_H}{2} (|\Phi_H|^2 - v_H^2)^2 + \frac{\lambda_S}{2} (|\Phi_S|^2 - v_S^2)^2 + \lambda_{HS} (|\Phi_H|^2 - v_H^2) (|\Phi_S|^2 - v_S^2)$$

➤ As  $\Phi_S$  develops the vacuum expectation value,  $\langle \Phi_S \rangle = v_S$ ,  $N_i$  and  $Z'$  acquire the mass:

$$M_{N_i} = \kappa_i v_S, \quad M_{Z'}^2 = 8g_{B-L}^2 v_S^2$$

➤ We take  $M_{N_1} < M_{N_2}, M_{N_3}$ , so that  $N_1$  can be a (decaying) dark matter when the Yukawa coupling ( $y_{\alpha 1}$ ) is sufficiently small



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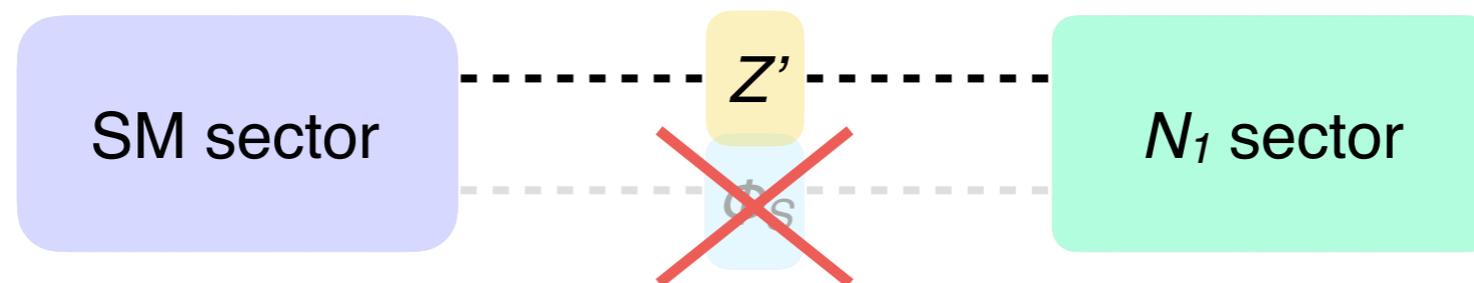
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➤ To concentrate on the  $Z'$  effect, we turn off the Higgs portal coupling  $\lambda_{HS} (\rightarrow 0)$

## Relevant reactions for thermalization of $N_1$

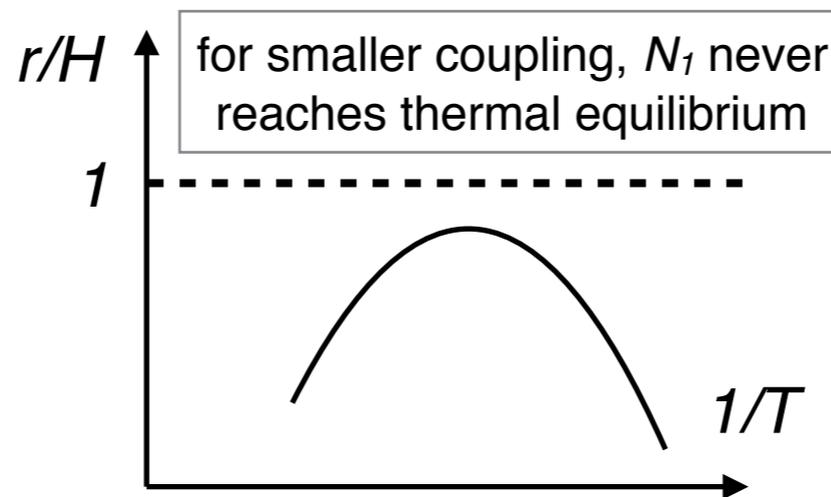
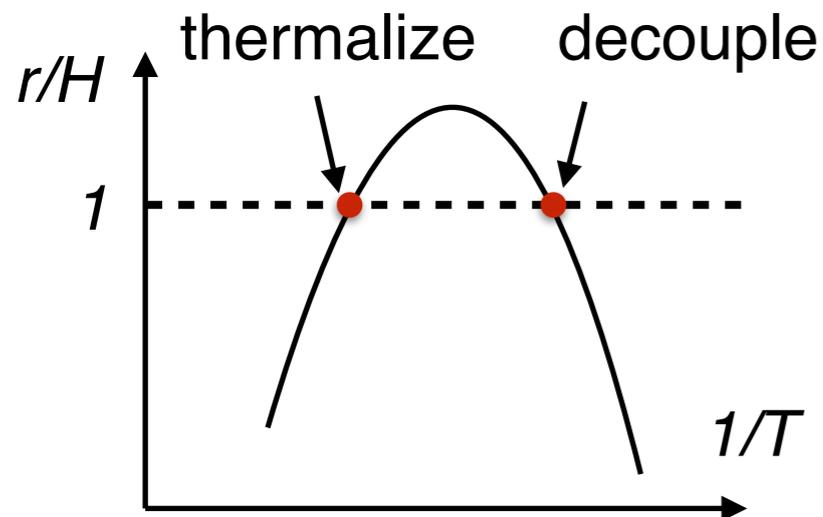
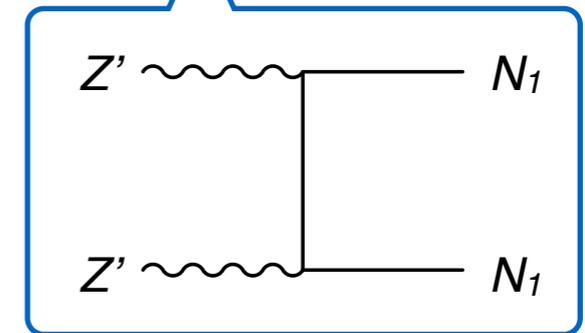
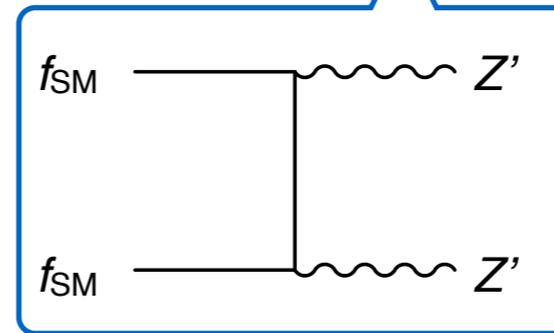
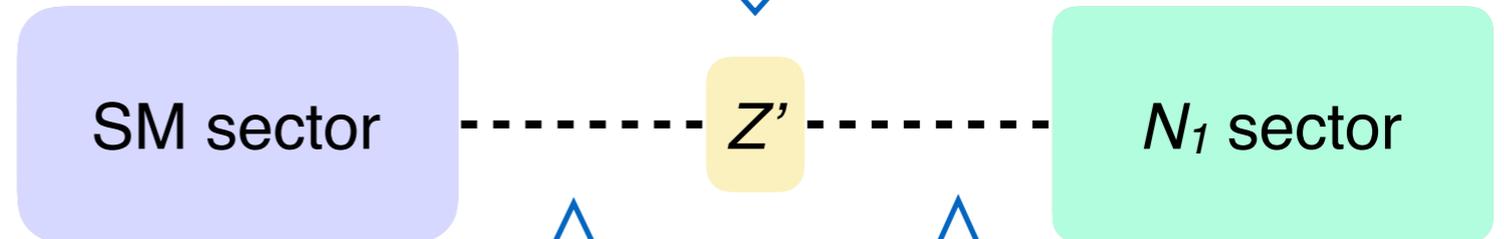
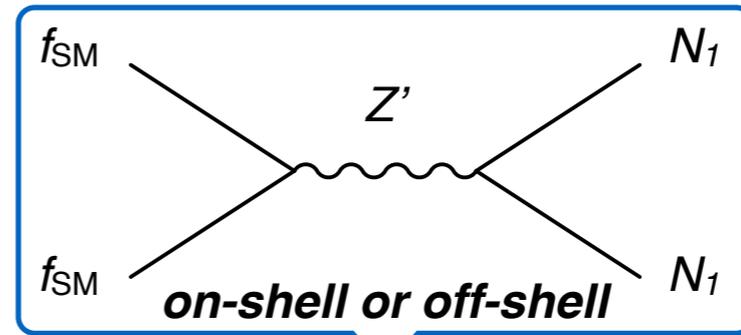
➤ There are mainly three processes that can bring  $N_1$  into the thermal bath

➤ Reaction rates:

$$r(N_1 \leftrightarrow f_{SM}), r(N_1 \leftrightarrow Z'), r(Z' \leftrightarrow f_{SM})$$

➤ In most of parameter spaces,  $r(N_1 \leftrightarrow f_{SM})$  determines whether  $N_1$  is thermalized or not

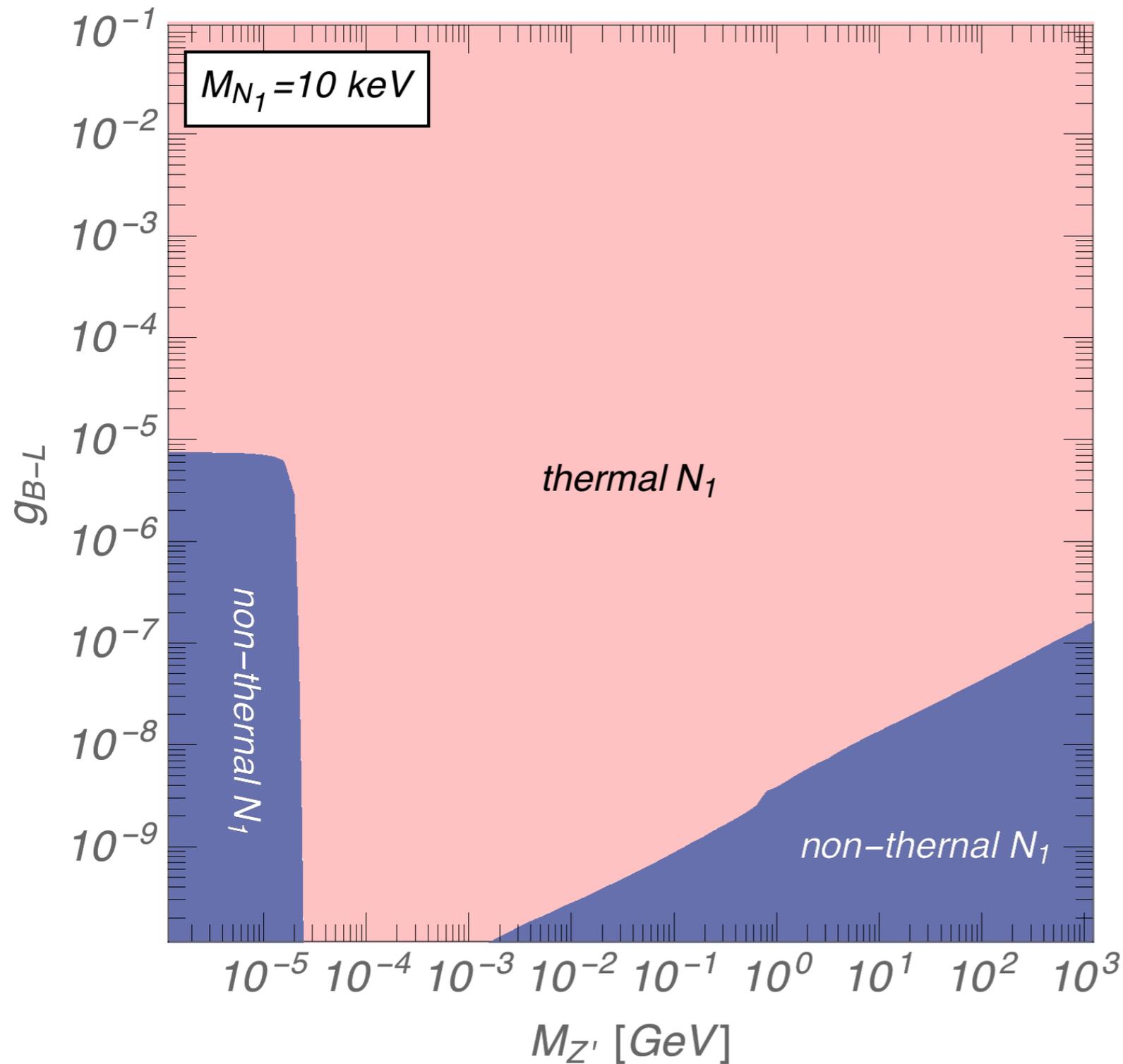
➤  $r(N_1 \leftrightarrow f_{SM})/H \sim 1$  at the thermalization and the freeze-out temperature



➤ Dark matter scenario drastically changes, depending on whether  $N_1$  is thermalized or not.

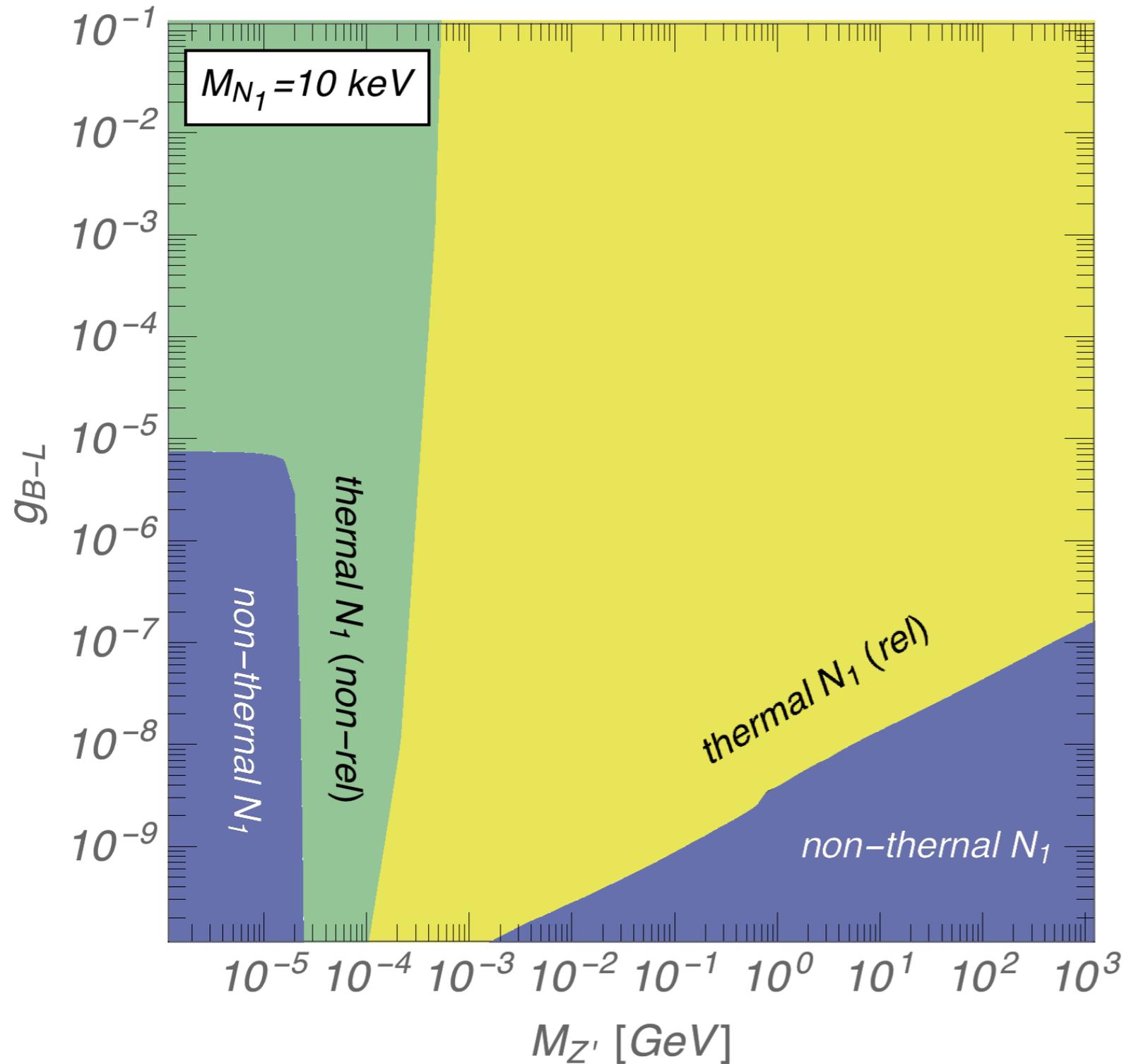
## $N_1$ production and relevant experimental constraints

- For thermal  $N_1$ , usual **freeze-out** mechanism can work
- For non-thermal  $N_1$ , **freeze-in** mechanism can work [L.Hall, et al. '09]



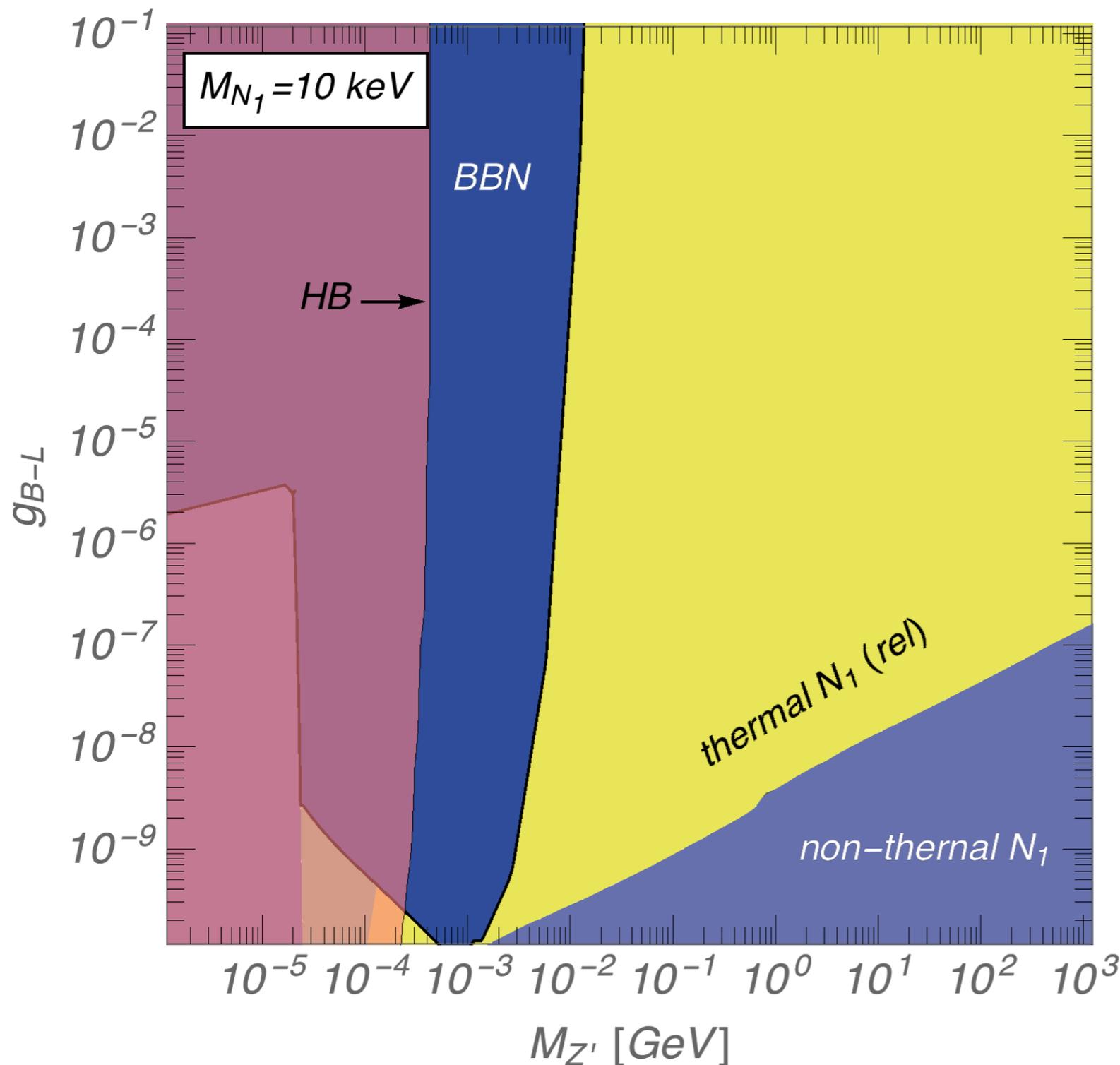
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- Constraints from BBN and Horizontal Branch (HB) stars exclude non-rel.  $N_1$
- Rel.  $N_1$  has large number density (due to the lack of Boltzmann suppression)

$$\Omega_{N_1} h^2 = \frac{s_0 M_{N_1}}{\rho_c h^{-2}} \times \frac{n_{N_1}}{s} \Big|_{T_{N_1}^{\text{dec}}}$$

$$\simeq 110 \times \left[ \frac{M_{N_1}}{10 \text{ keV}} \right] \left[ \frac{10.75}{g_*(T_{N_1}^{\text{dec}})} \right]$$

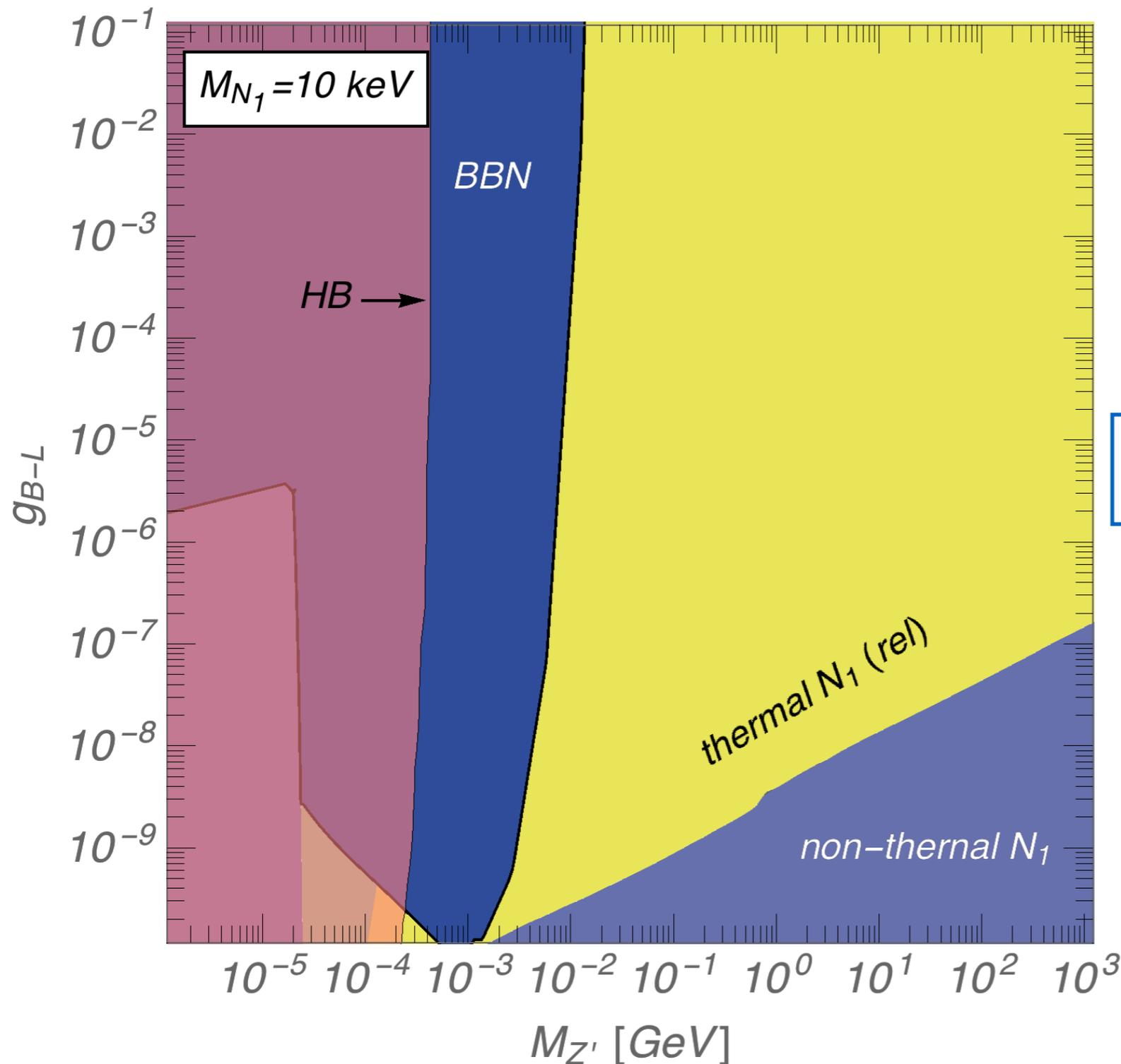
(over production)

- Some dilution mechanism is necessary (e.g., the late time entropy production by the decay of  $N_{2,3}$ )

[Bezrukov, et al., '10]

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$$f_{SM} f_{SM} \rightarrow N_1 N_1$$

- For  $2M_{N_1} < M_{Z'}$ , the relic abundance of  $N_1$  is roughly given by

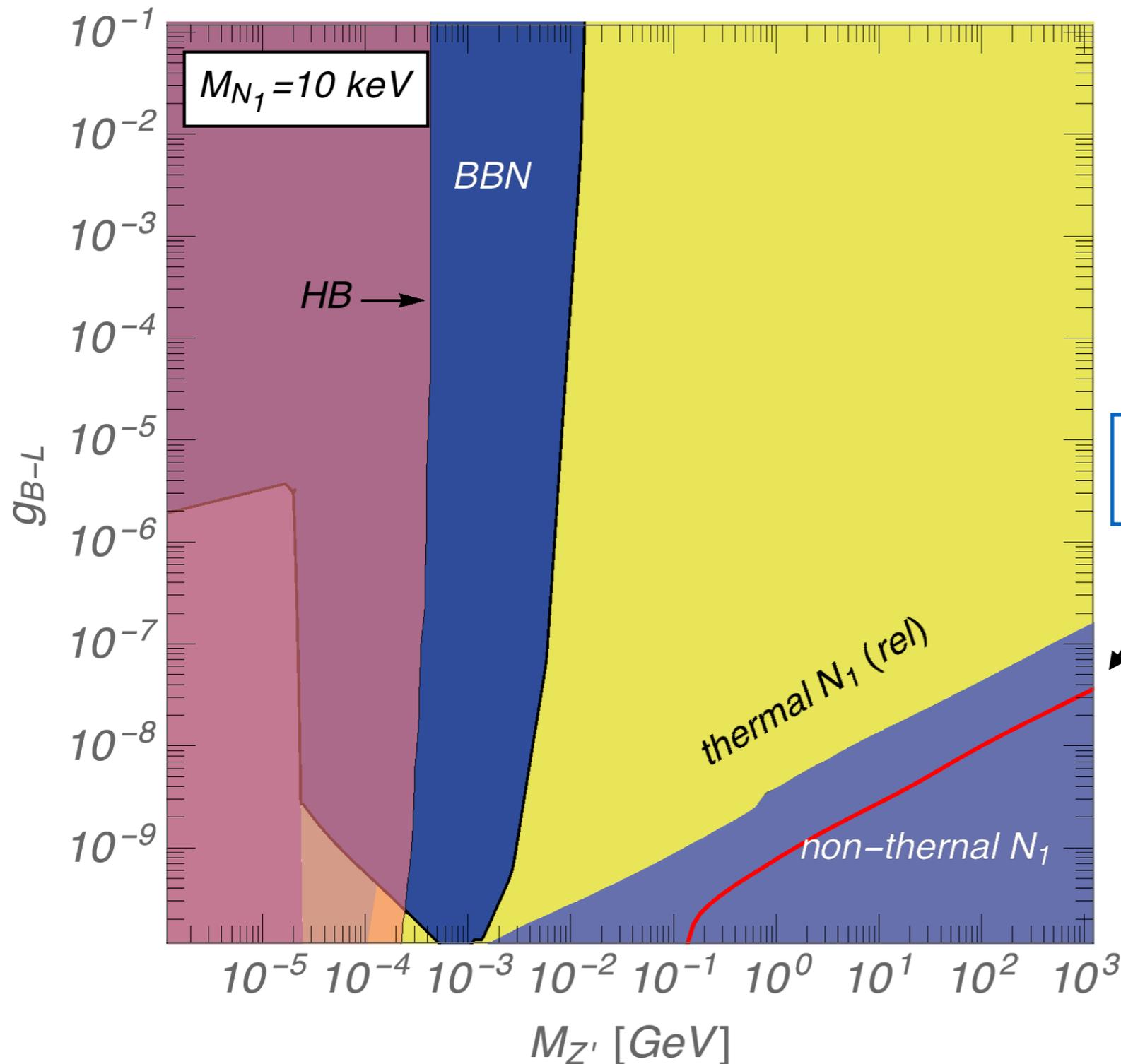
$$\Omega_{N_1} h^2 \simeq 0.12 \times \left(\frac{100}{g_*}\right)^{3/2} \left(\frac{g_{B-L}}{6.3 \times 10^{-12}}\right)^2 \left(\frac{43/6}{C_f}\right) f(\tau)$$

$$\Gamma_{Z'} \sim C_f \frac{g_{B-L}^2}{12\pi} M_{Z'}$$

$$f(\tau) = \tau(2 + \tau^2) \sqrt{1 - \tau^2} \quad (\tau = 2M_{N_1}/M_{Z'})$$

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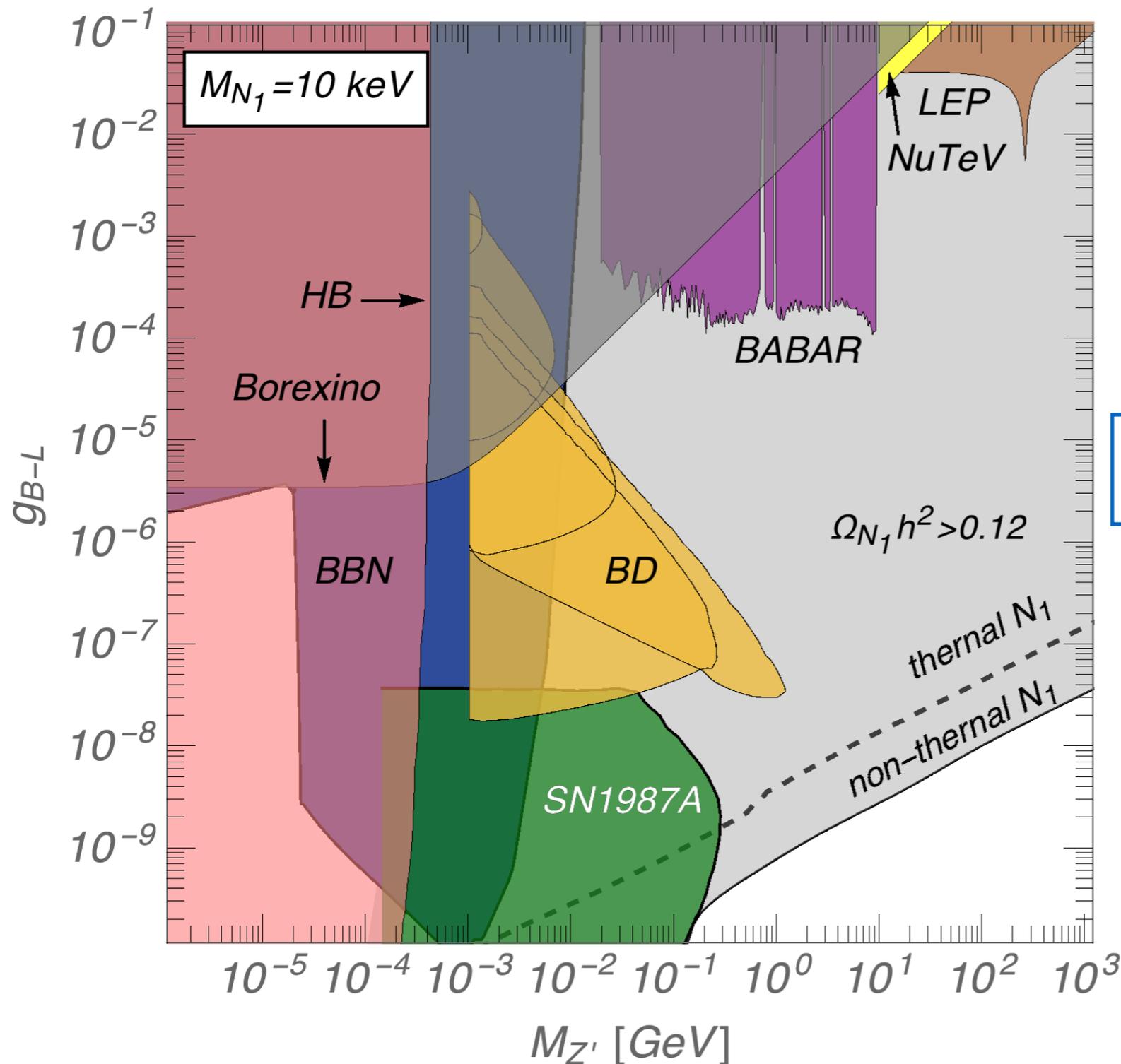
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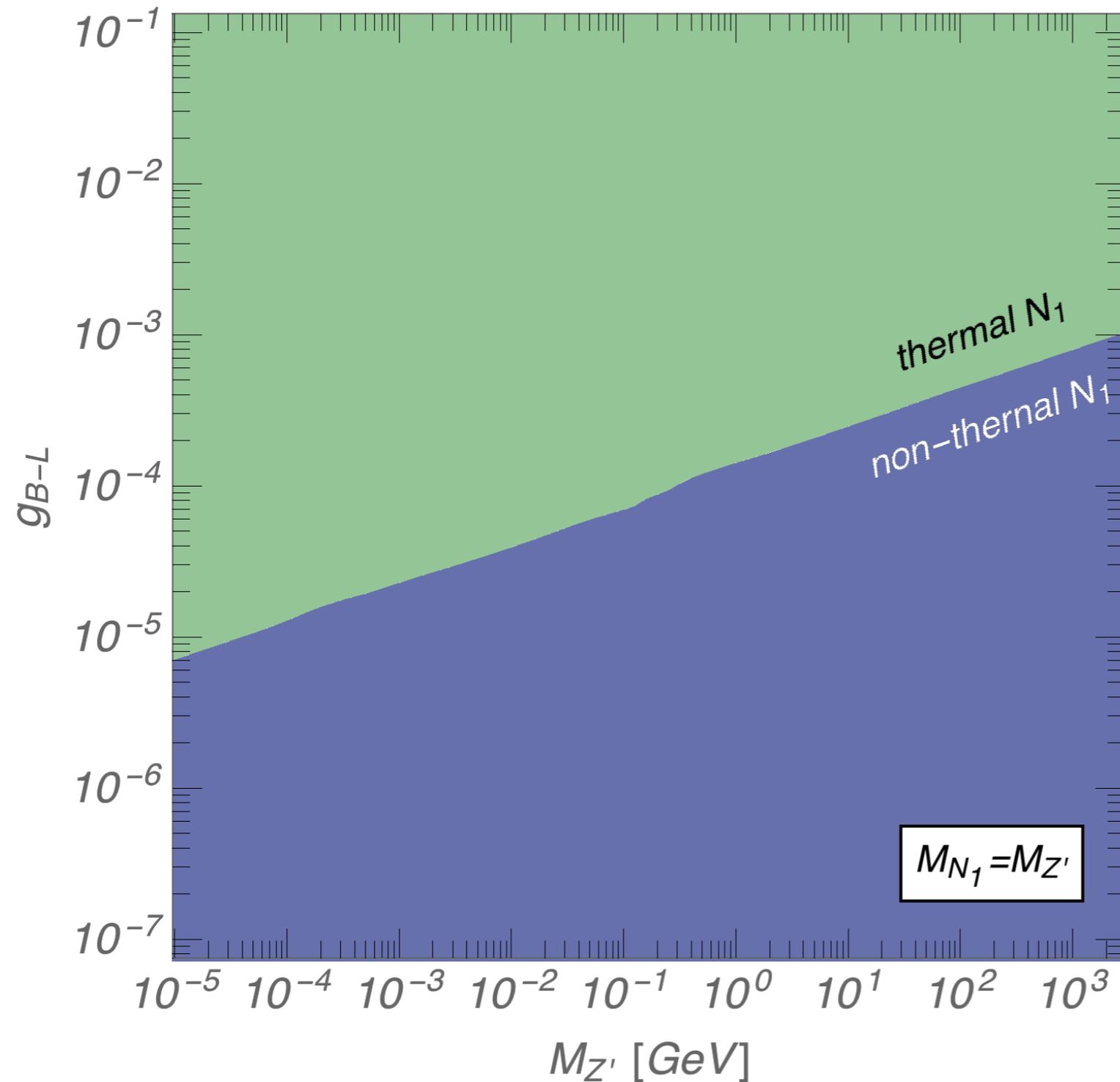
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- together with all relevant limits

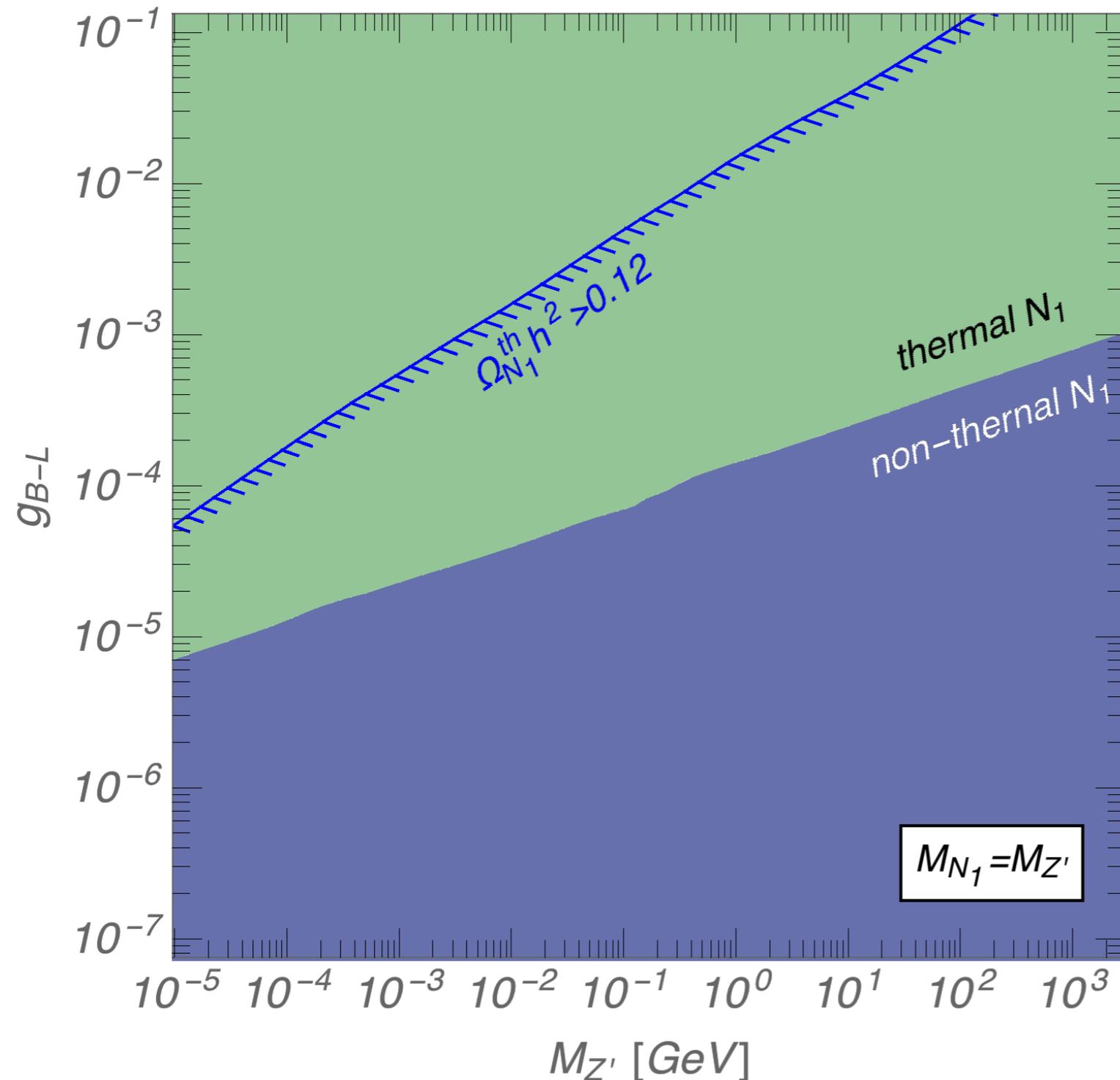
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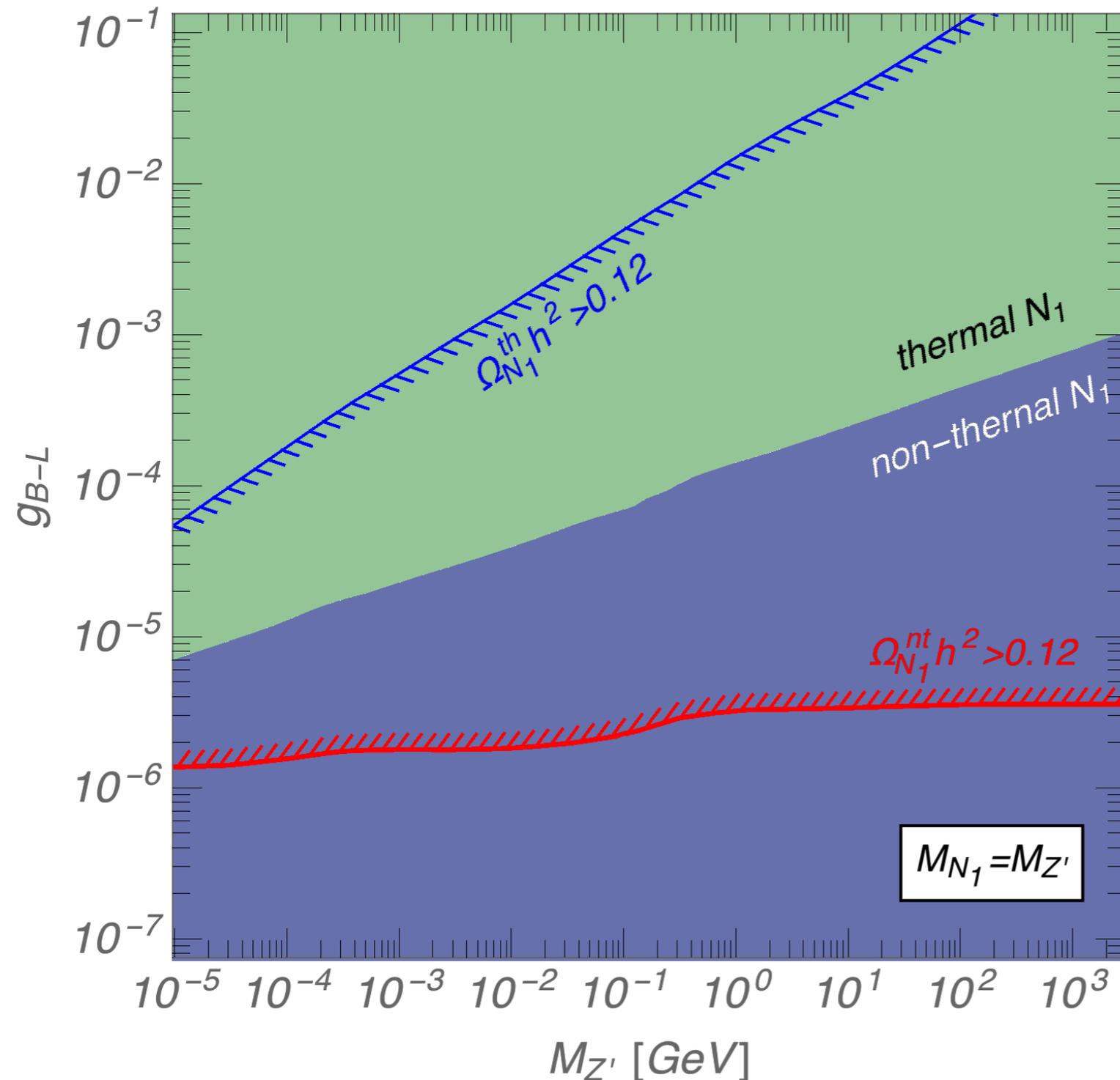


- For thermal  $N_1$ ,  $N_1$  is ordinary cold dark matter produced by freeze-out mechanism

$$\Omega_{N_1}^{th} h^2 = \frac{s_0 M_{N_1} Y_{N_1}^{th}}{\rho_c h^{-2}} \propto \frac{1}{\sigma V} \Big|_{T \sim T_{N_1}^{dec}}$$

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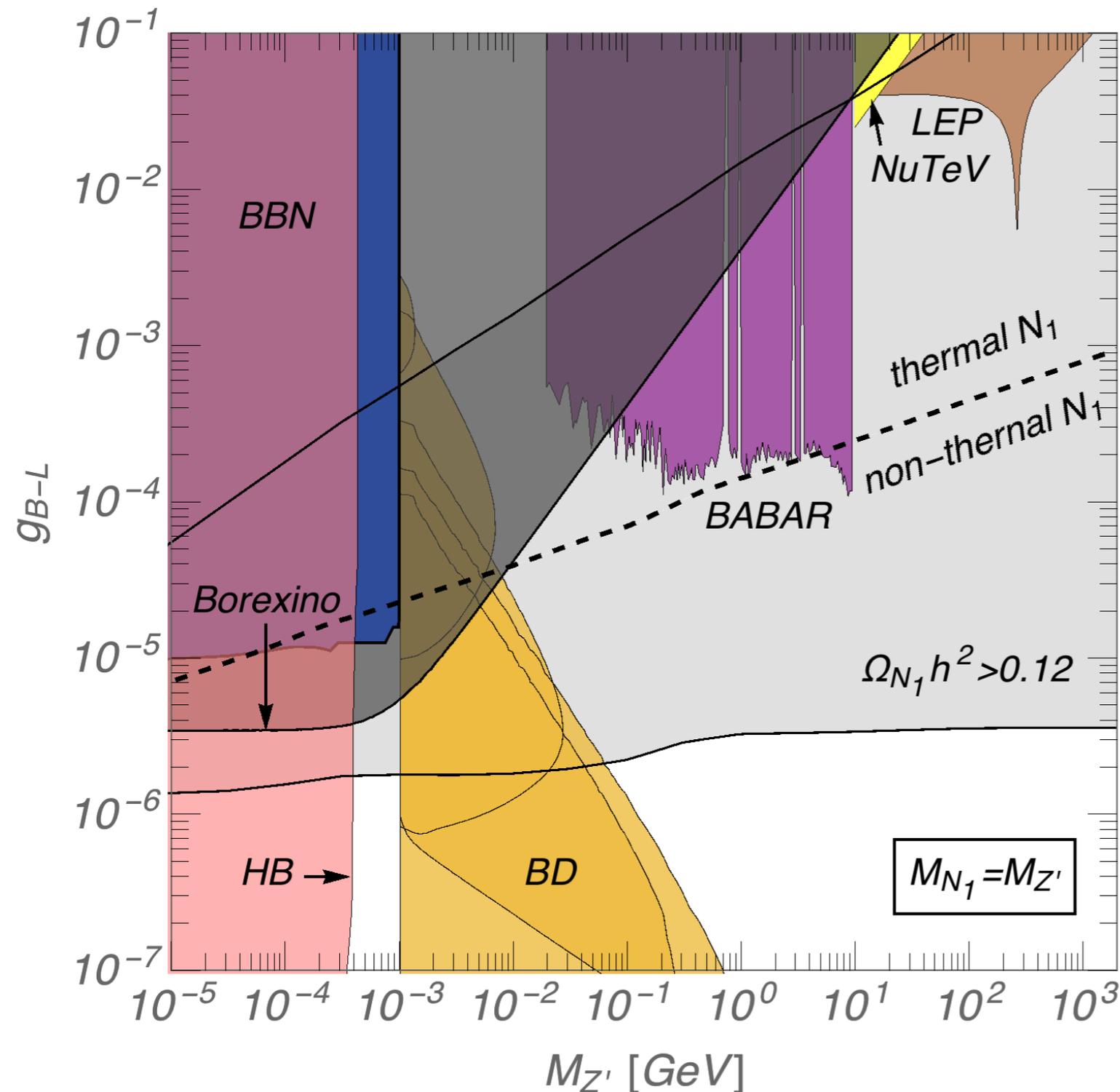
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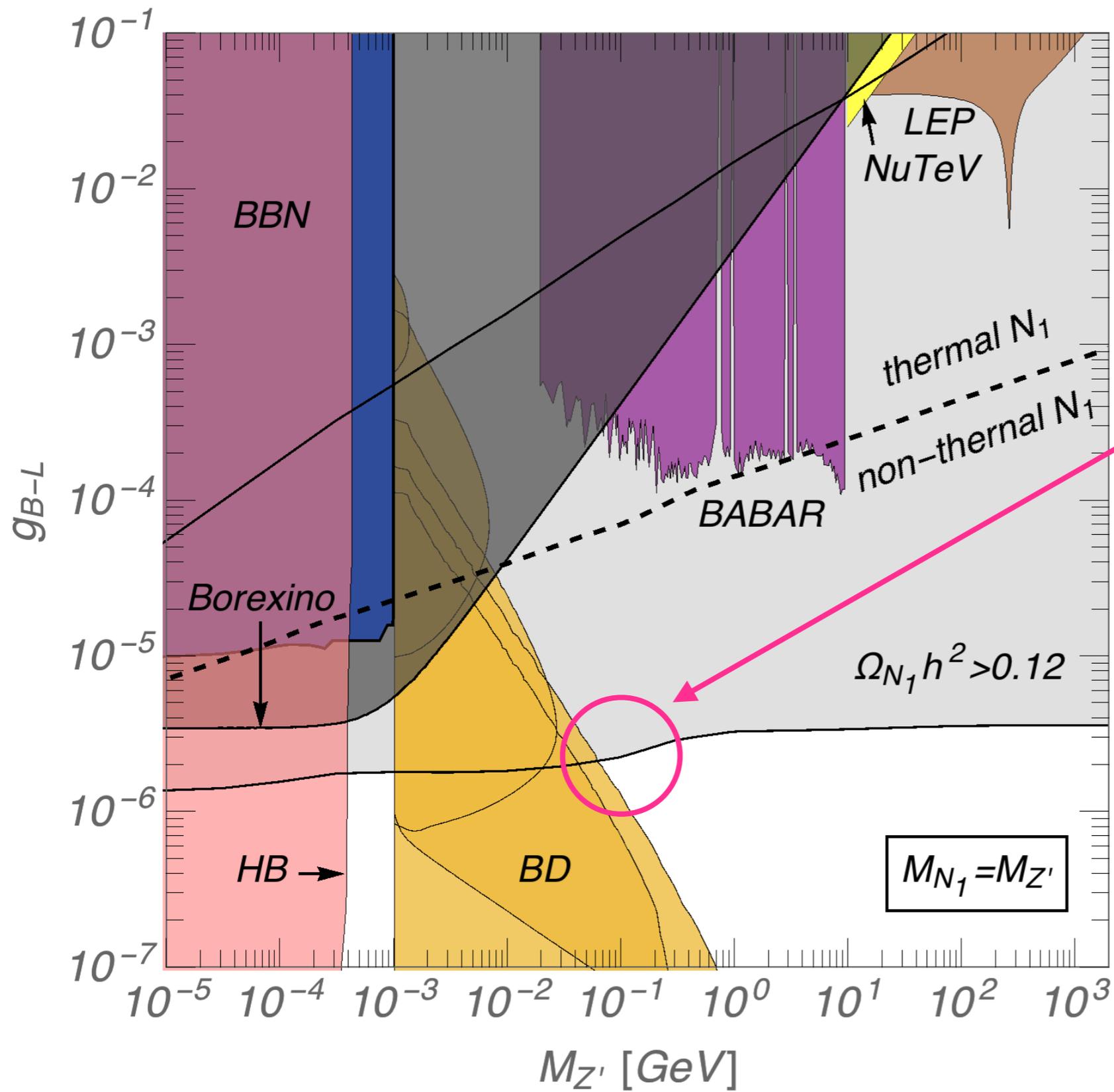
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- Relevant constraints

### ***3. Implications***

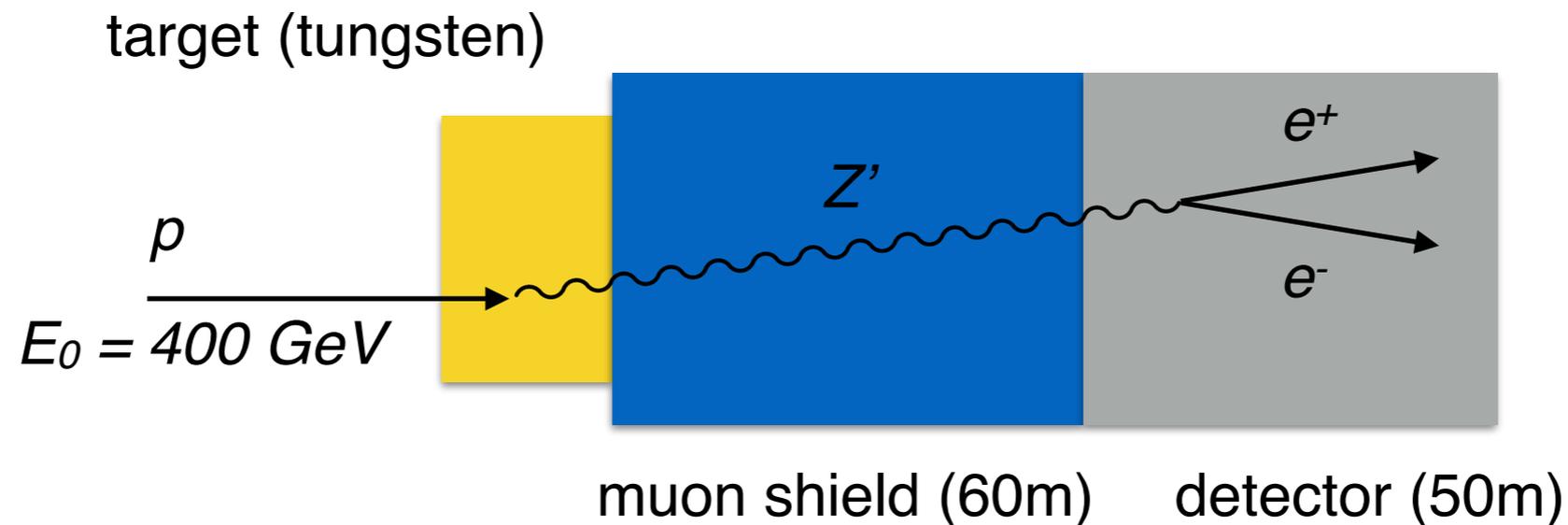
### 3. Implications



**Beam dump experiments can test this region**

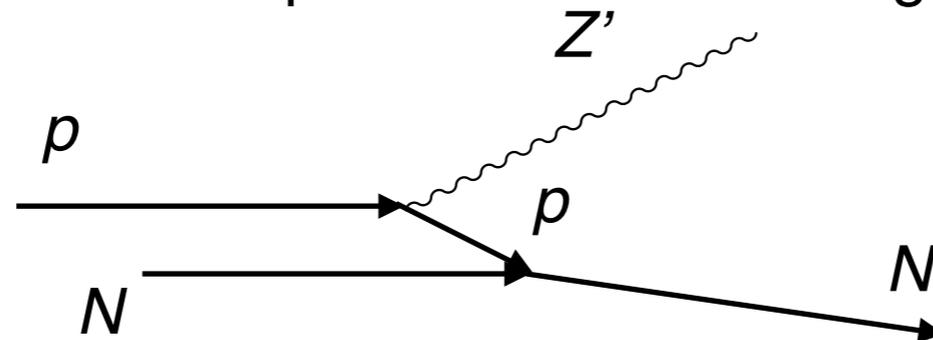
## The Search for Hidden Particles (SHiP) experiment

- SHiP: A new proton beam dump experiment at CERN
- The SHiP utilizes 400 GeV proton beam from the SPS with  $\sim 10^{20}$  protons on target



- The number of signal events:  $N_{sig} \sim N_{POT} \times R_{prod} \times P_{det}$

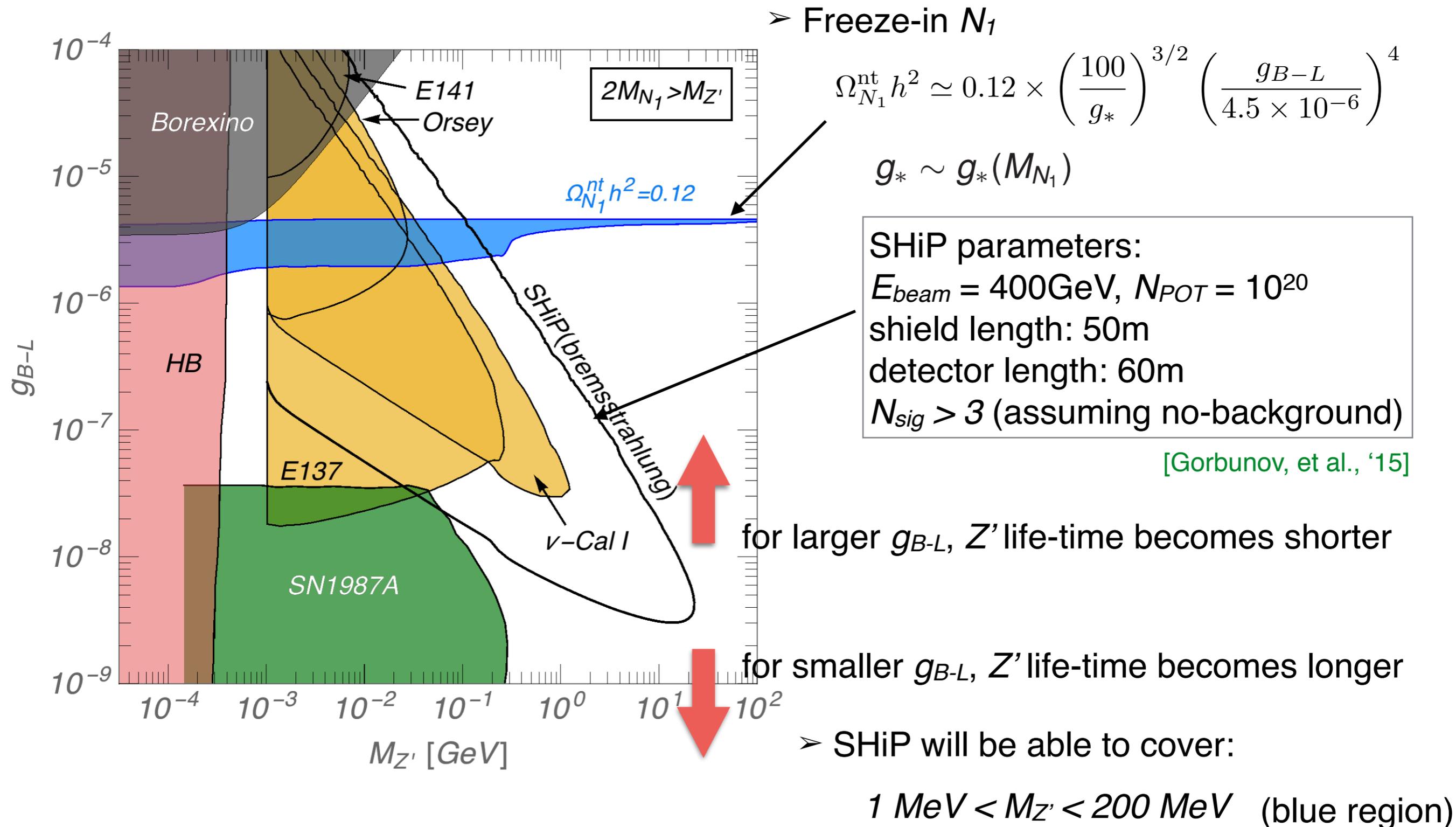
-  $Z'$  production: proton bremsstrahlung



-  $P_{det}$ : probability that  $Z'$  decays inside the detector

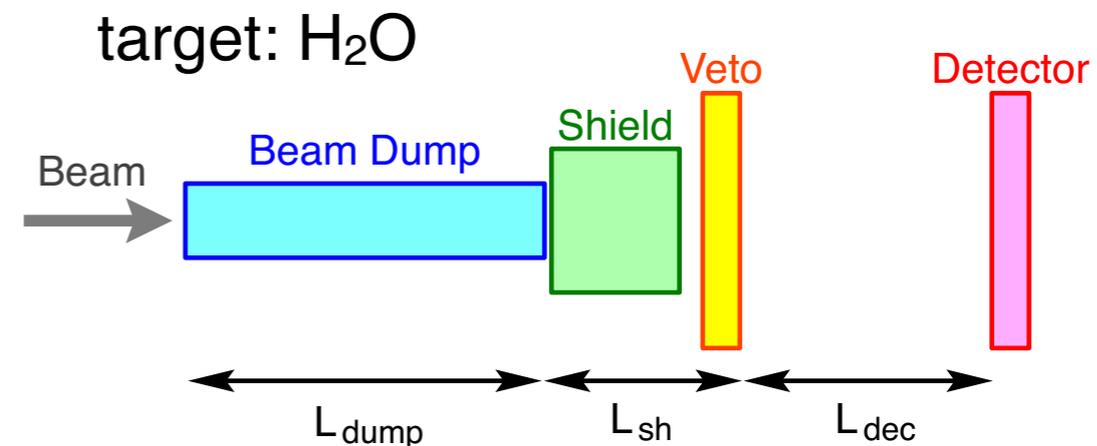
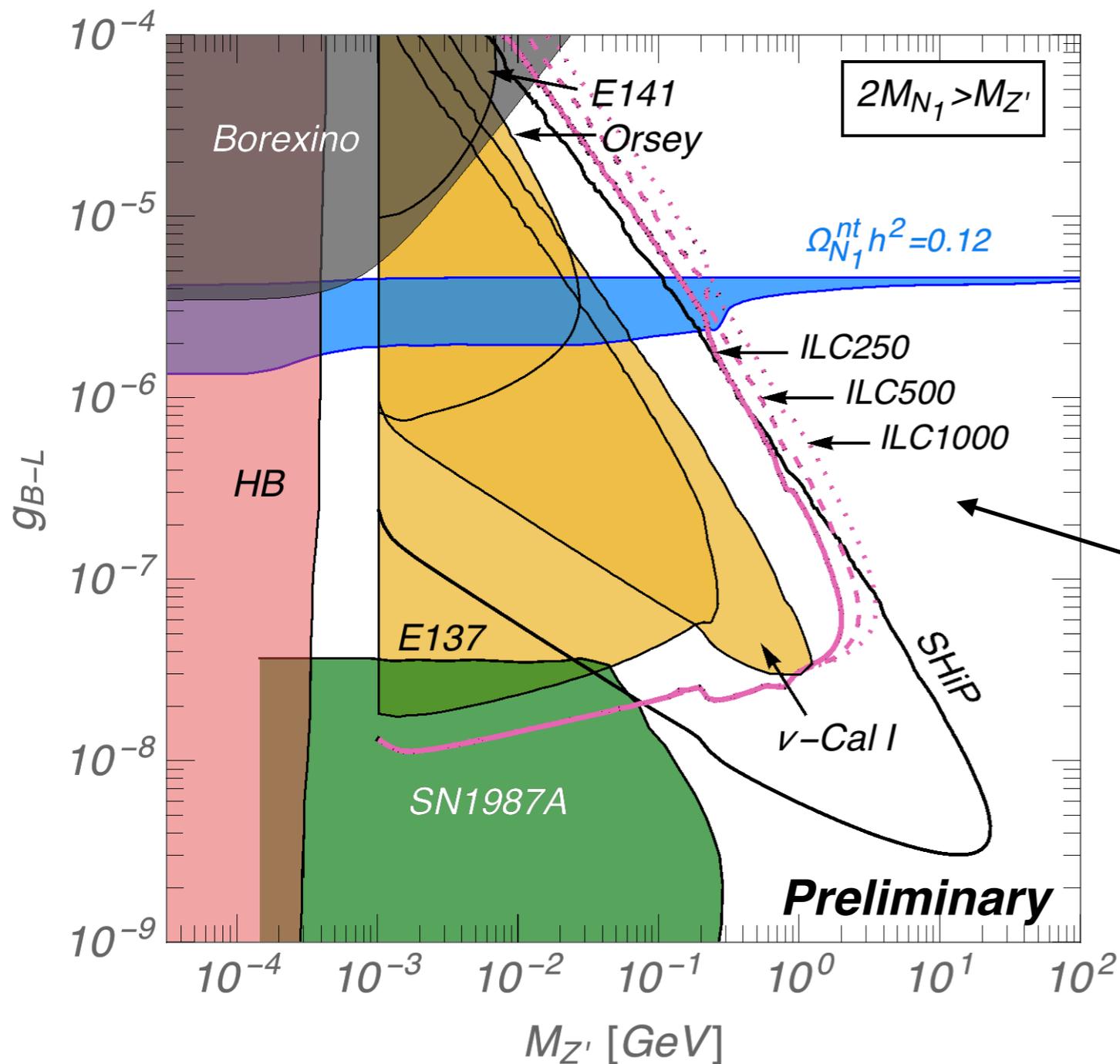
If the life-time of  $Z'$  is too short or too long,  $Z'$  can not be observed

# The Search for Hidden Particles (SHiP) experiment



# Beam dump experiment at the ILC (BDeeLC)

[Kanemura, Moroi, Tanabe, '15]



BDeeLC setup:

- $E_{beam} = 250\text{GeV}, 500\text{GeV}, 1\text{TeV}$
- $N_e = 4 \times 10^{21}$  (one-year operation)
- $L_{dump} = 11\text{m}$
- $L_{sh} = 50\text{m}$
- $L_{dec} = 50\text{m}$
- $N_{sig} > 3$  (assuming no-background)

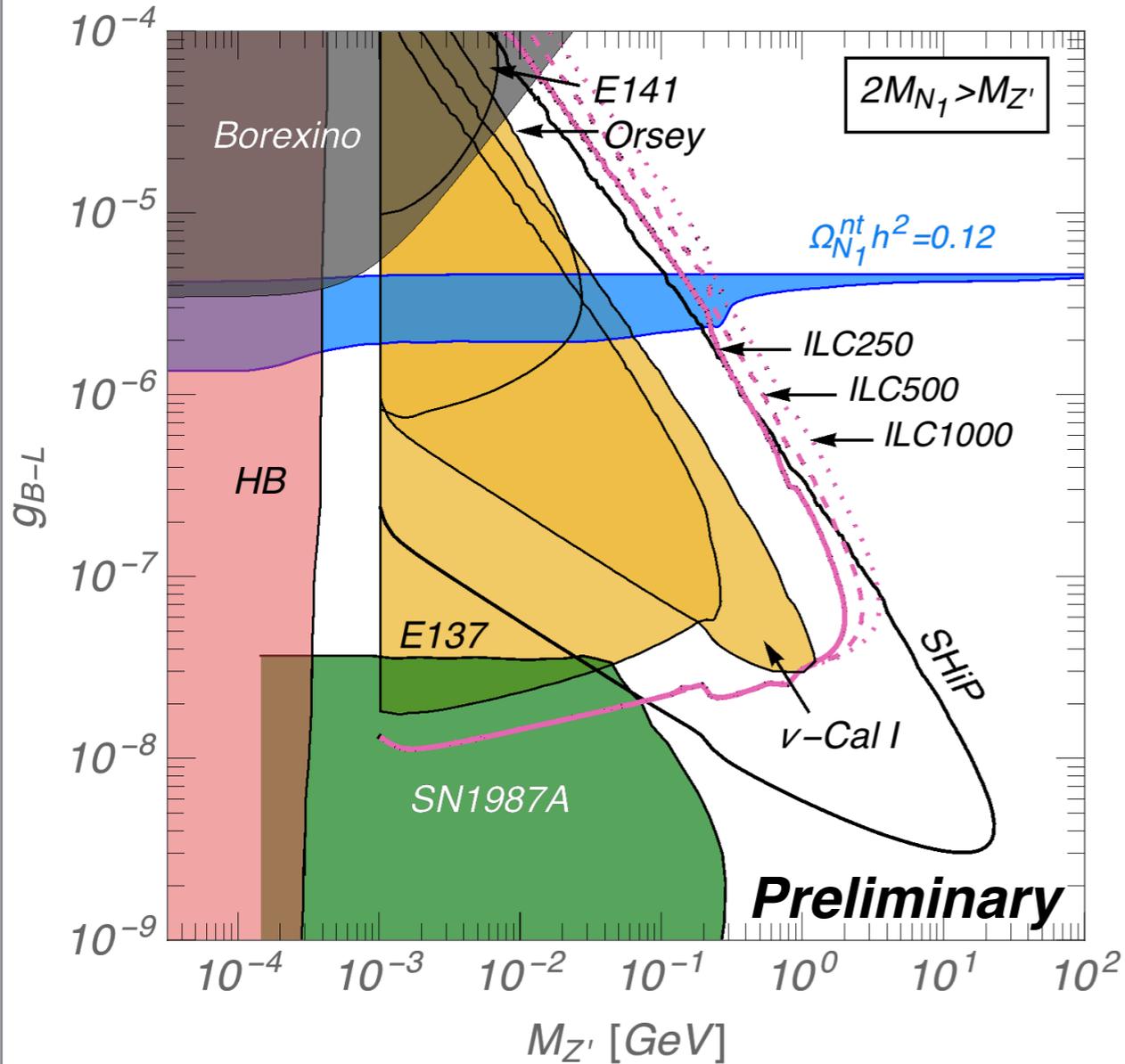
> BDeeLC will be able to cover:

$1\text{ MeV} < M_{Z'} < 300\text{ MeV} \sim 400\text{ MeV}$   
(blue region)

## Discovery reach of the SHiP and BDeeLC

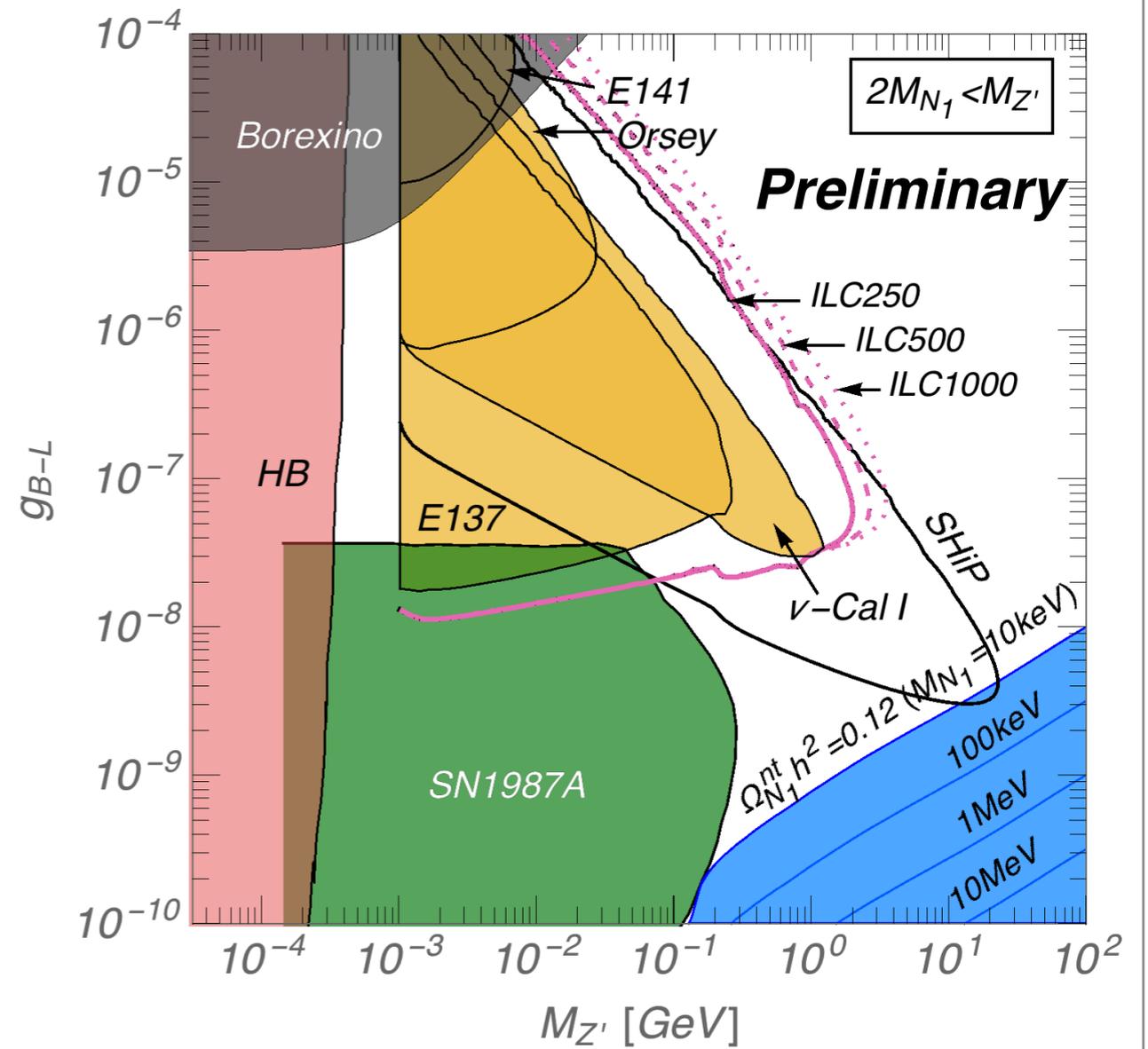
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**SHiP and BDeeLC can be a powerful tool for searching the freeze-in scenario**

## *B-L breaking scale*

- Dark matter abundance is determined by  $g_{B-L}$  and  $M_{Z'}$ , which implies  $v_S$  through

$$M_{Z'}^2 = 8g_{B-L}^2 v_S^2$$

- In the freeze-in region for off-resonance case ( $2M_{N_1} > M_{Z'}$ ), we obtain

$$v_S^2 \simeq (7.9 \times 10^4 M_{Z'})^2 \left( \frac{0.12}{\Omega_{N_1}^{\text{nt}} h^2} \right)^{1/2} \left( \frac{100}{g_*} \right)^{3/4}$$

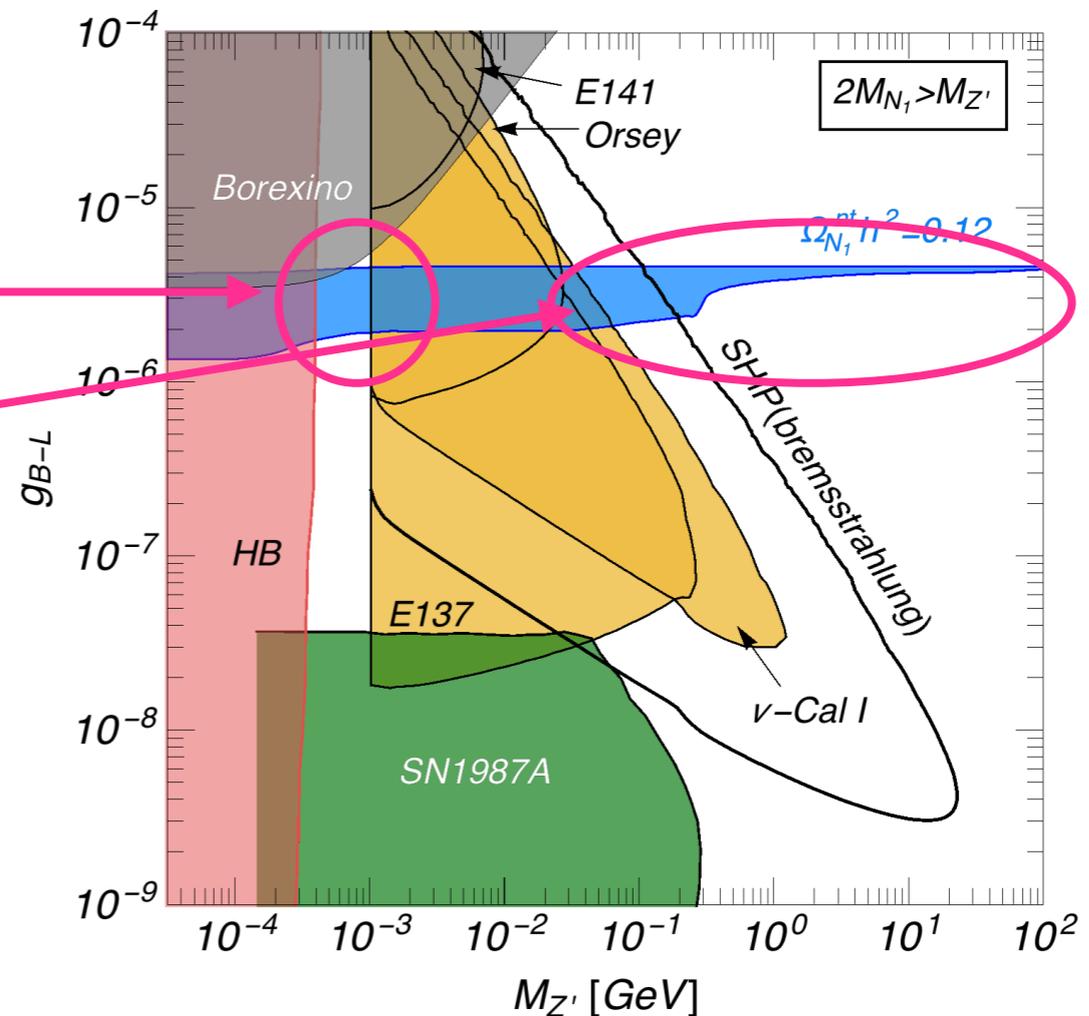
- This leads to

(taking  $\lambda_S = 4\pi$ )

$$200 \text{ GeV} \lesssim M_s \lesssim 400 \text{ GeV}$$

$$M_s \gtrsim 4 \text{ TeV}$$

$$(M_s^2 \simeq 2\lambda_S v_S^2)$$



## *Summary*

- We discussed various right-handed neutrino dark matter scenarios in the UvMSM:  $U(1)_{B-L}$  gauge extension of the vMSM.
- The  $B-L$  gauge interaction can open new windows for right-handed neutrino dark matter.
- Forthcoming fixed target experiment can test the freeze-in scenario.