



CP Violation at the ILC: Production of Neutralinos and Charginos

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Motivation

What about CP violating phases at the linear collider (ILC) ?

- MSSM may have several phases: $\varphi_\mu, \varphi_{M_1}, \varphi_{A_\tau}, \dots$ (and many more)
- how to measure them? \rightarrow find sensitive observables and processes

Low-energy restrictions of the phases?

- measurements of electric dipole moments impose strong constraints.
- however: cancellations of loop contributions to EDMs, or other models (e.g. with flavor violation) may weaken constraints
- \rightarrow ILC could provide independent measurements of phases!

CP violation at the ILC: production of neutralinos and charginos

- Constructing CP observables: triple products
- Results for e^+e^- linear collider:
 - neutralino production
 - chargino production
- Summary and conclusions

Impact of complex parameters

- couplings become **complex**
- masses, cross sections, distributions, etc. change their value

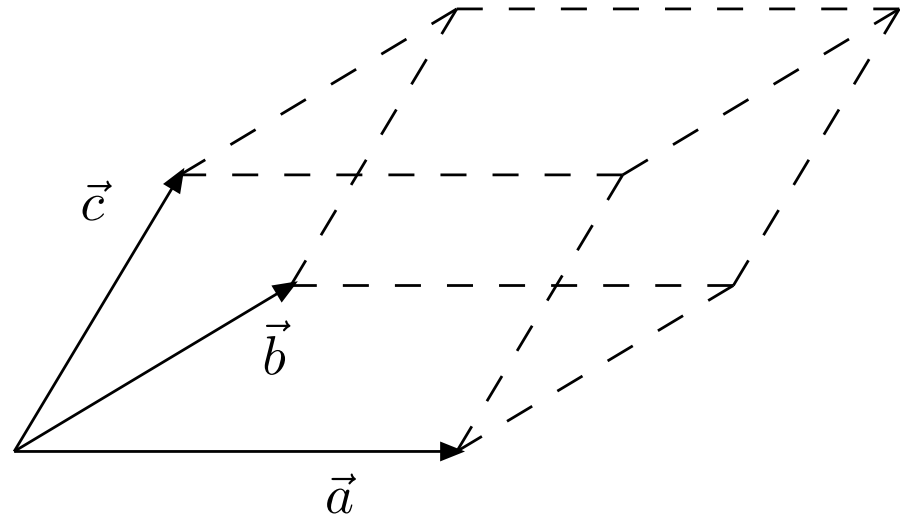
Are there observables A which are
CP-sensitive \Leftrightarrow $A = 0$ if CP is conserved
 $A \neq 0$ if CP is violated

How to construct them? \Rightarrow **triple products**

Triple products

$$[\vec{a}, \vec{b}, \vec{c}] = (\vec{a} \times \vec{b}) \cdot \vec{c}$$

spins or momenta



- **time reversal** $T(t \rightarrow -t)$: $T[\vec{a}, \vec{b}, \vec{c}] = -[\vec{a}, \vec{b}, \vec{c}] \Rightarrow$ T-odd
CPT-theorem: T-odd observables are also CP-odd
- **source**: $\text{Tr}\{\gamma_5 \not{a} \not{b} \not{c} \not{d}\} = 4i \epsilon_{\mu\nu\rho\sigma} a^\mu b^\nu c^\rho d^\sigma$
interference with **complex parameters**

T odd asymmetry

$$A := \frac{\sigma(\mathcal{J} > 0) - \sigma(\mathcal{J} < 0)}{\sigma(\mathcal{J} > 0) + \sigma(\mathcal{J} < 0)}$$

- triple product: $\mathcal{J} = (\vec{p}_a \times \vec{p}_b) \cdot \vec{p}_c$
- cross section: σ

$$\Rightarrow A = \frac{\int \text{Sign}[\mathcal{J}] |T|^2 d\text{Lips}}{\int |T|^2 d\text{Lips}}$$

- Amplitude: $|T|^2$
- Lorentz-invariant phase space: Lips

Geometrical interpretation

- Asymmetry A is an **angular distribution**:

$$A = \frac{N_+ - N_-}{N_+ + N_-} \Leftrightarrow \begin{array}{c} \vec{c} \\ \vec{b} \\ \vec{a} \end{array} - \begin{array}{c} \vec{b} \\ \vec{a} \\ \vec{c} \end{array}$$

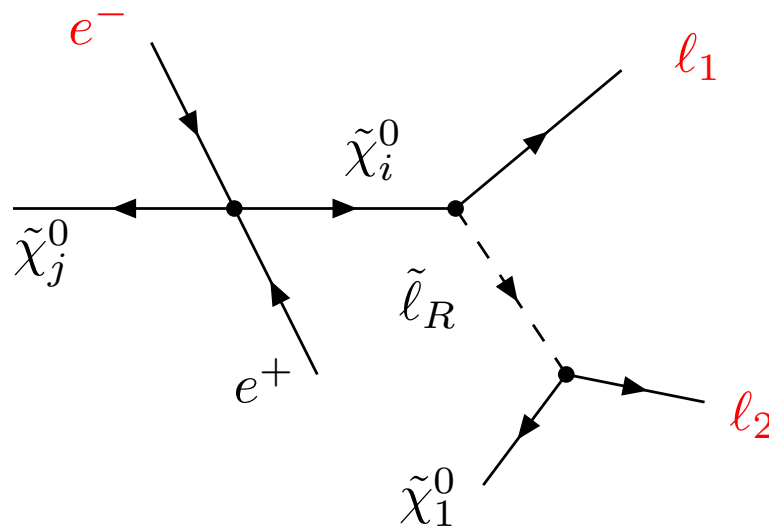
- $N_+(N_-)$: events with particle c
above (below) plane spanned by $\vec{p}_a \times \vec{p}_b$

Remember: A is CP-sensitive \Rightarrow CP violation can be tested directly!

Asymmetry for neutralino production

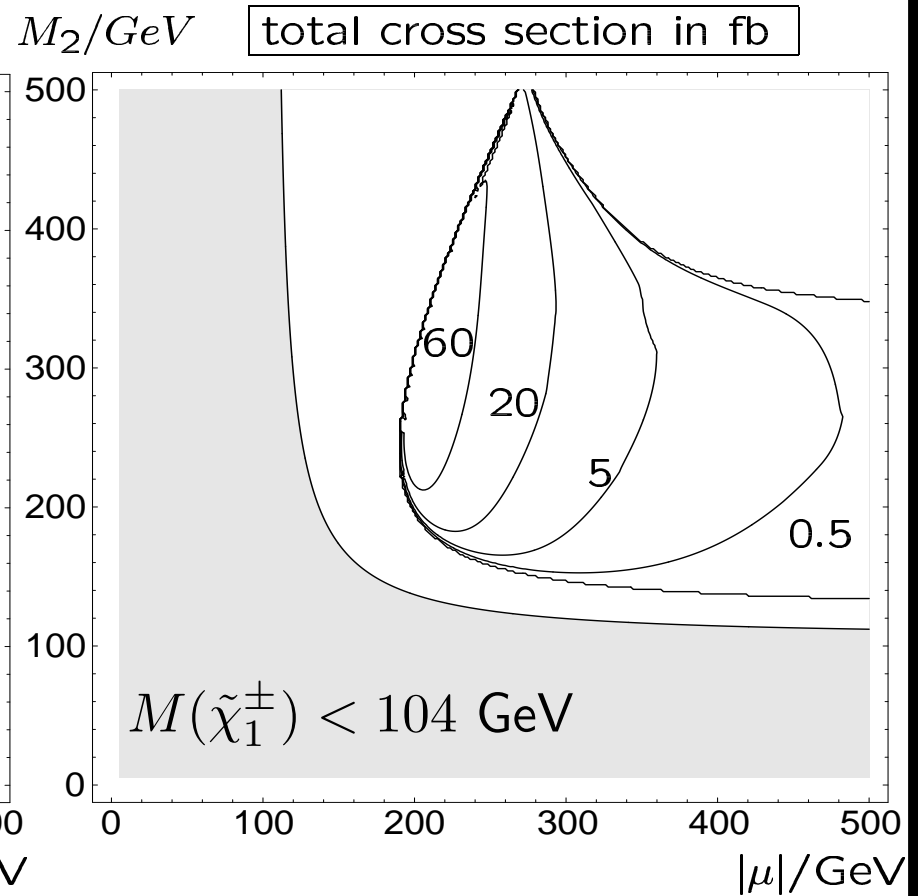
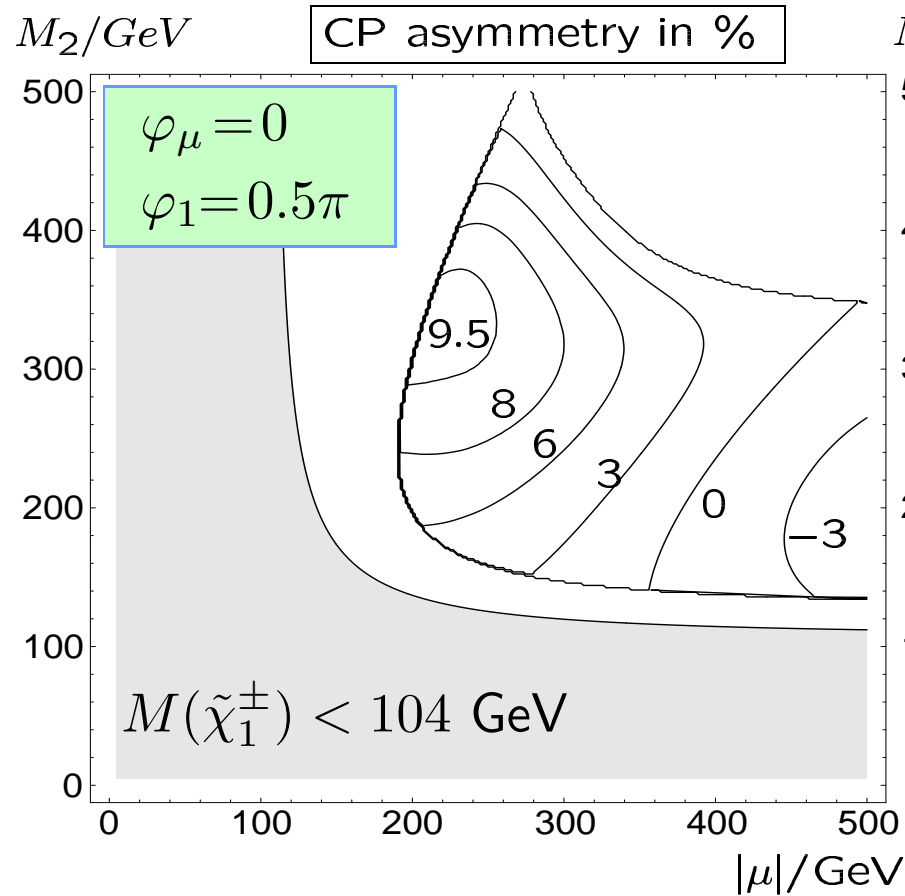
$$A = \frac{\sigma(\mathcal{T} > 0) - \sigma(\mathcal{T} < 0)}{\sigma(\mathcal{T} > 0) + \sigma(\mathcal{T} < 0)}$$

$$\mathcal{T} = [\vec{p}(e^-) \times \vec{p}(l_1)] \cdot \vec{p}(l_2)$$



$$e^+e^- \longrightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0; \quad \tilde{\chi}_2^0 \longrightarrow \tilde{l}_R l_1; \quad \tilde{l}_R \longrightarrow \tilde{\chi}_1^0 l_2 \quad \text{at } \sqrt{s} = 500 \text{ GeV};$$

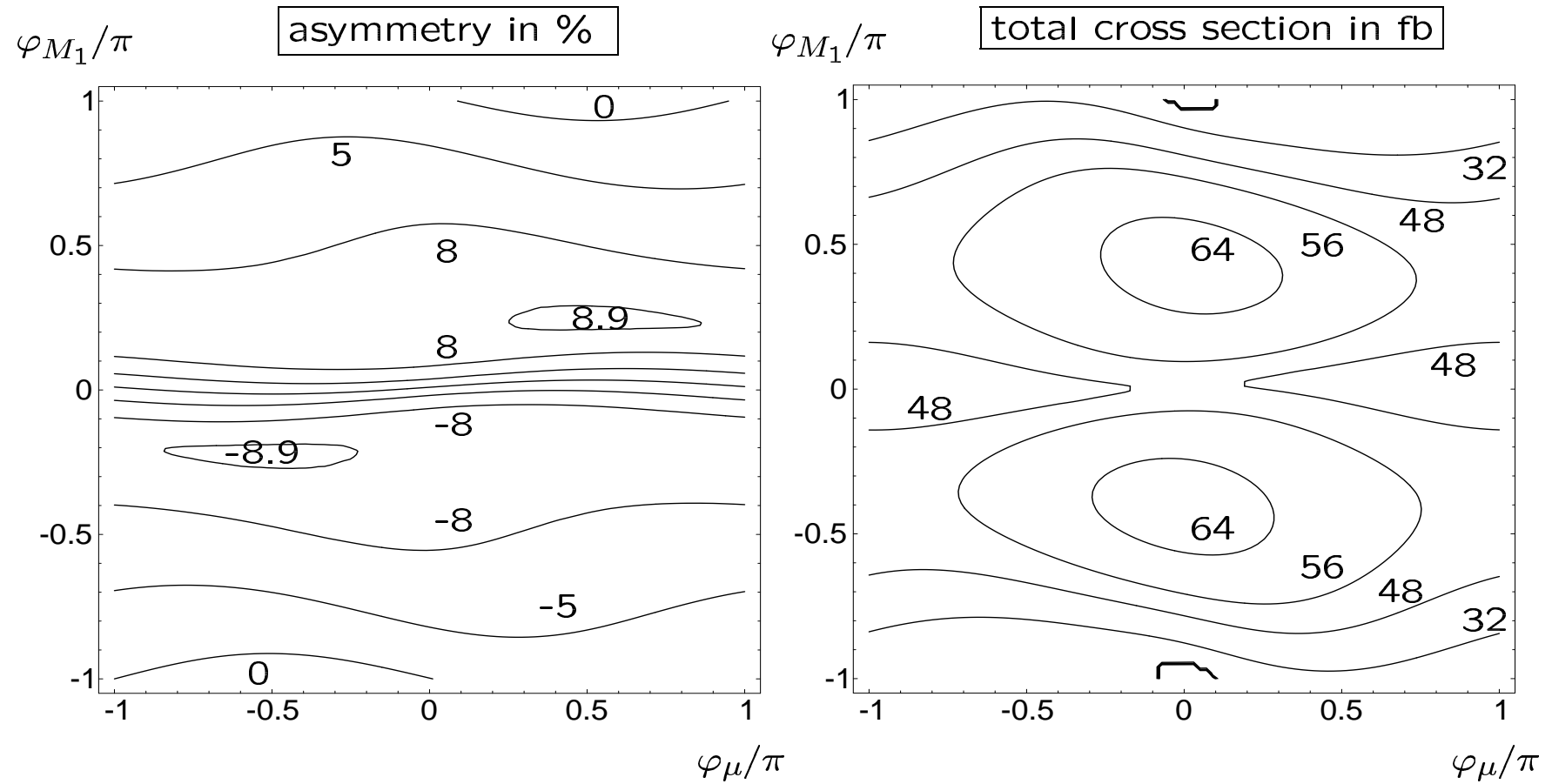
$$\tan \beta = 10; \quad m_0 = 100 \text{ GeV}; \quad P(e^-|e^+) = (0.8| - 0.6)$$



$$e^+e^- \longrightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0; \quad \tilde{\chi}_2^0 \longrightarrow \tilde{l}_R l_1; \quad \tilde{l}_R \longrightarrow \tilde{\chi}_1^0 l_2$$

$$|\mu| = 240 \text{ GeV}; \quad M_2 = 400 \text{ GeV}$$

dependence on the phases



$$e^+e^- \longrightarrow \tilde{\chi}_1^0\tilde{\chi}_2^0; \quad \tilde{\chi}_2^0 \longrightarrow \tilde{l}_R l_1; \quad \tilde{l}_R \longrightarrow \tilde{\chi}_1^0 l_2$$

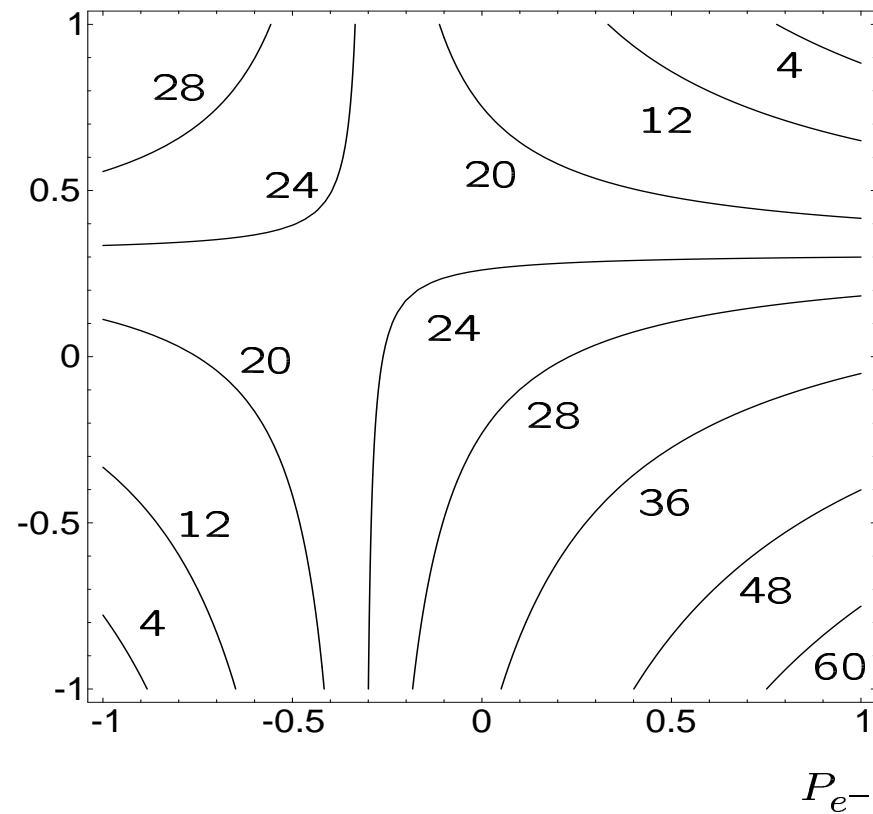
$$|\mu| = 240 \text{ GeV}; \quad M_2 = 400 \text{ GeV}$$

beam polarization dependence

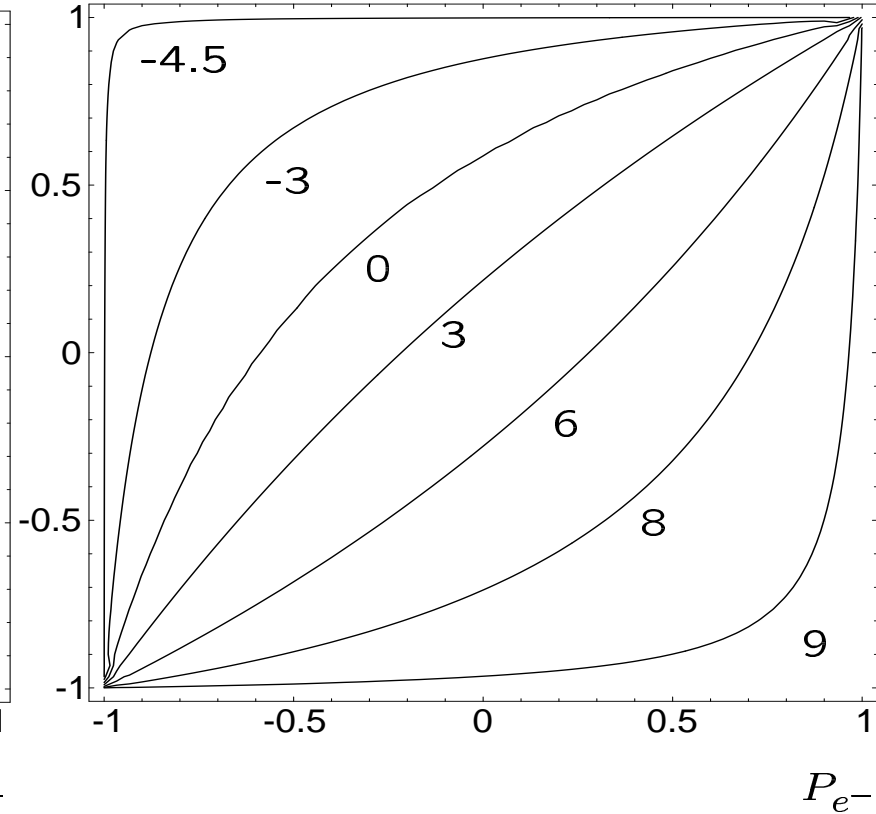
$$\varphi_\mu = 0$$

$$\varphi_1 = 0.2\pi$$

P_{e^+} $\sigma_{tot}(e^+e^- \rightarrow \tilde{\chi}_1^0\tilde{\chi}_1^0 l_1 l_2)$ in fb



P_{e^+} \mathcal{A}_T in %

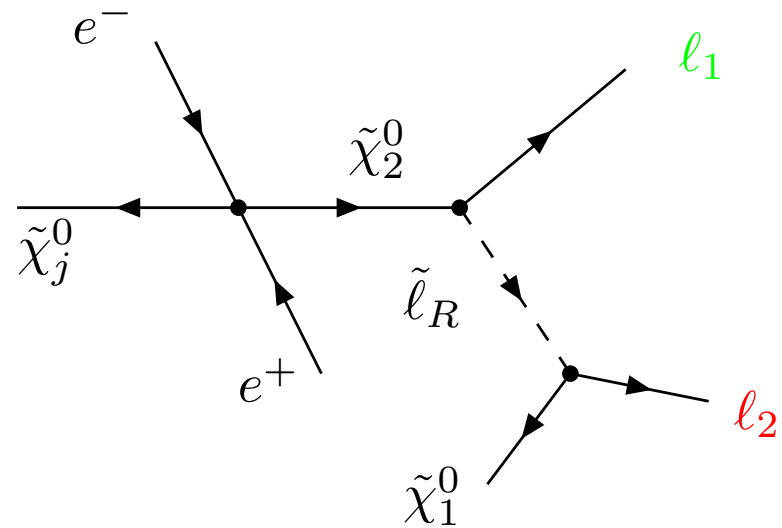
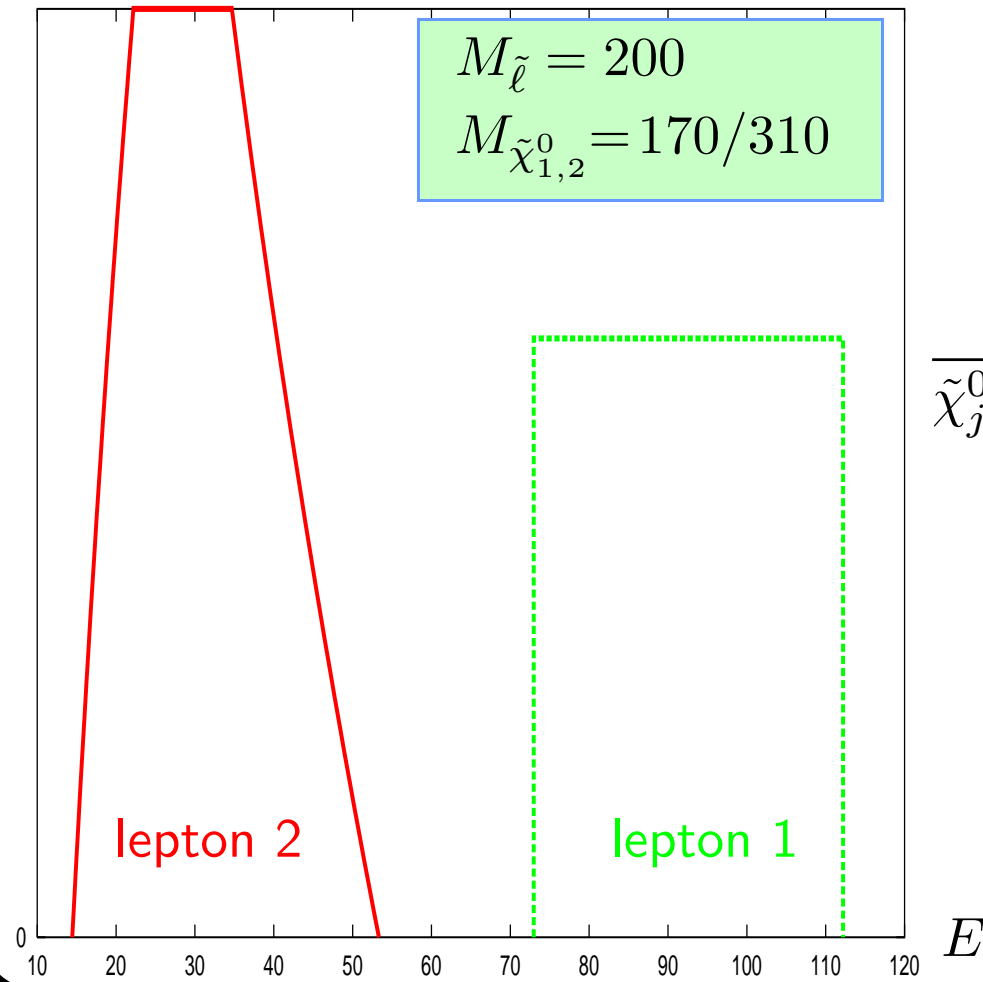


A bit of statistics

- How many events $N = \mathcal{L} \times \sigma$ are needed to measure the CP-asymmetry A ?
- Statistical significance is given by: $S = A \sqrt{N}$
- An example: asymmetry of $A = 5\%$ and cross section $\sigma = 20$ fb would yield a CL of 5 (luminosity $\mathcal{L} = 500 \text{ fb}^{-1}$).
- However, since A and σ vary a lot over the MSSM parameter space, it is difficult to make global statements, whether phases could be measured or not.

Distinguish the leptons by energy distributions

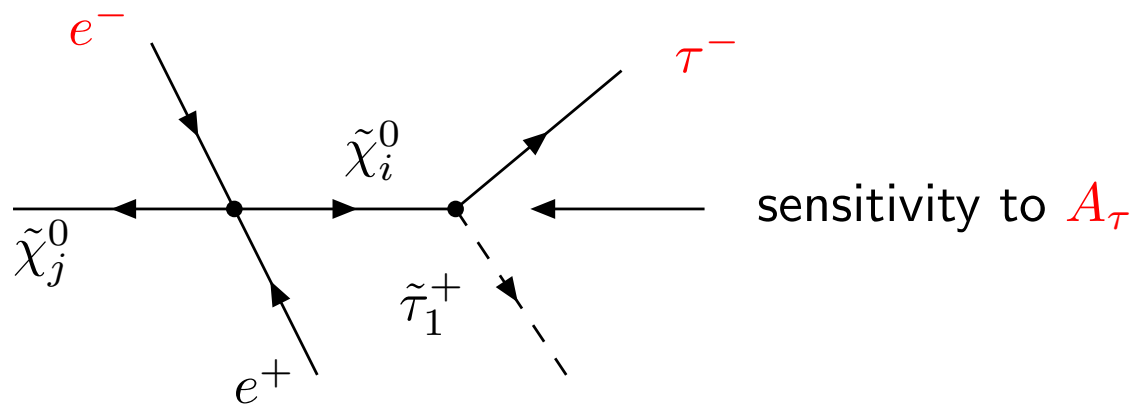
$$\frac{d\sigma}{dE}$$



Transverse tau polarization as CP-asymmetry

$$A = P_{\perp} = \tau\text{-polarization} \perp \vec{p}(e^{-}), \vec{p}(\tau)$$

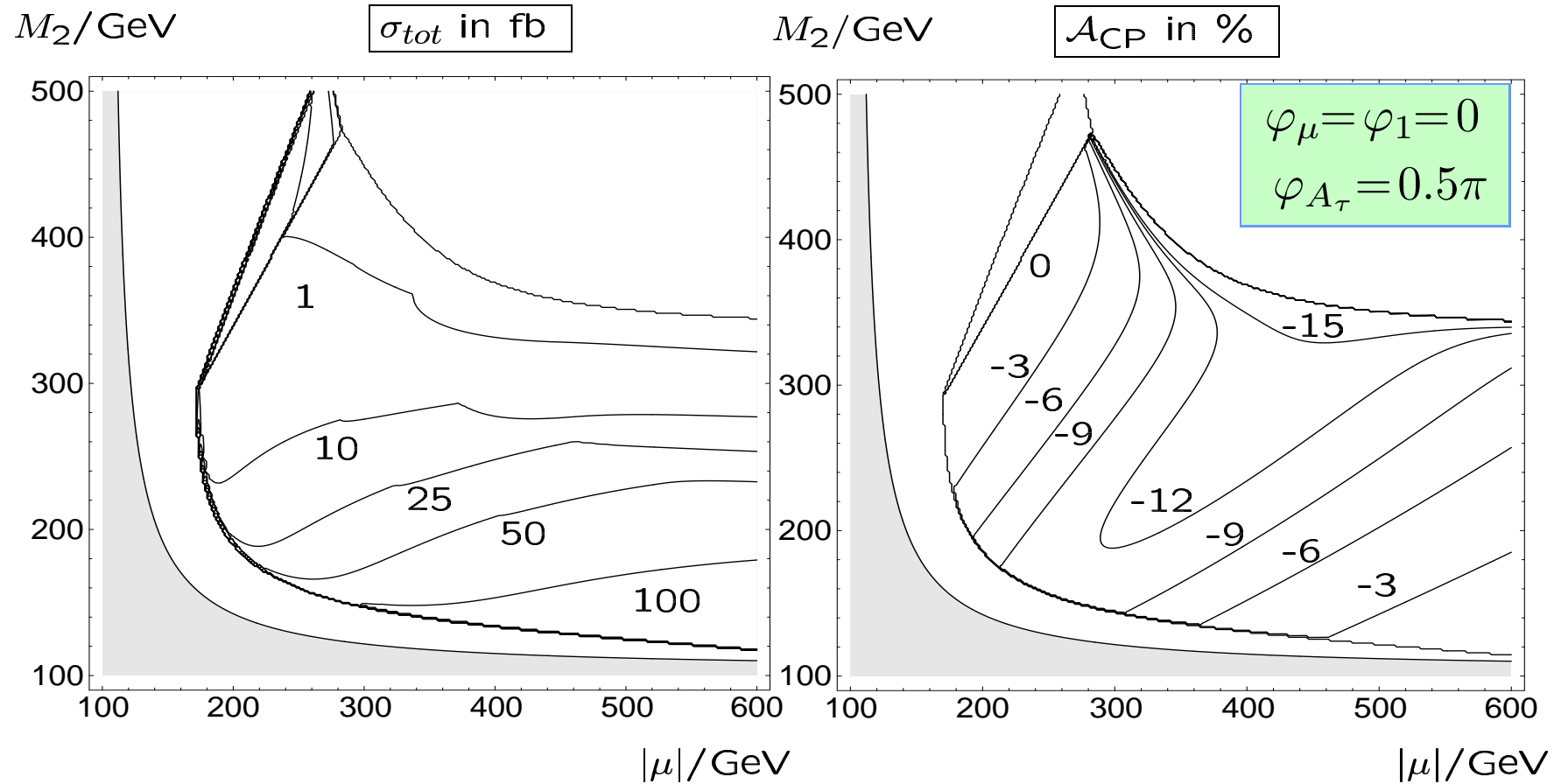
$$\text{triple product: } \mathcal{T} = [\vec{p}(e^{-}) \times \vec{p}(\tau)] \cdot \vec{P}_{\perp}$$



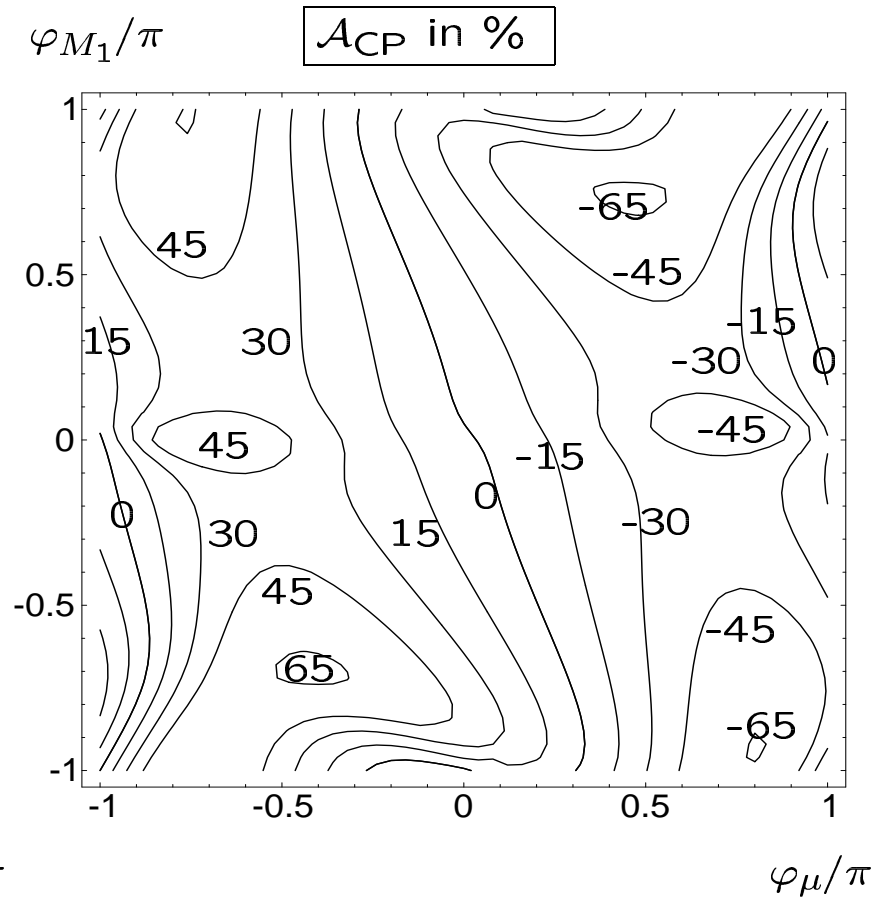
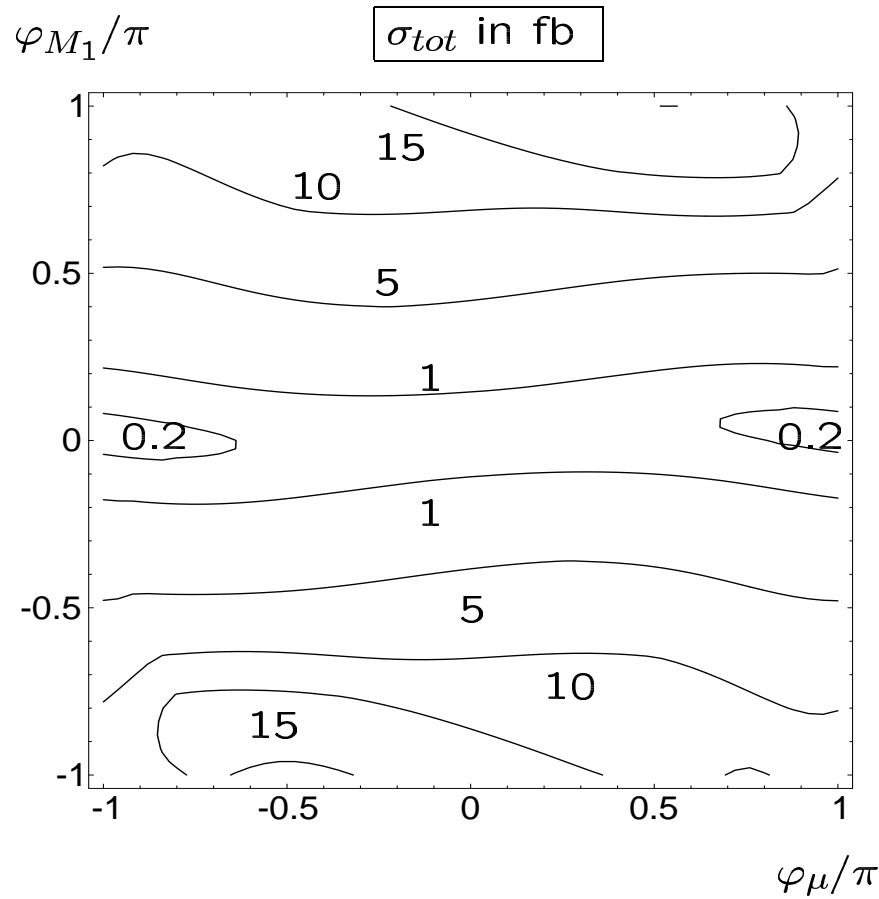
$$e^+e^- \longrightarrow \tilde{\chi}_1^0\tilde{\chi}_2^0; \quad \tilde{\chi}_2^0 \longrightarrow \tilde{\tau}_1\tau \quad \text{at } \sqrt{s} = 500 \text{ GeV};$$

$$A_\tau = 1 \text{ TeV}; \quad \tan\beta = 5; \quad m_0 = 100 \text{ GeV}; \quad P(e^-|e^+) = (-0.8|0.6)$$

gray shaded area: $M(\tilde{\chi}_1^\pm) < 104 \text{ GeV}$

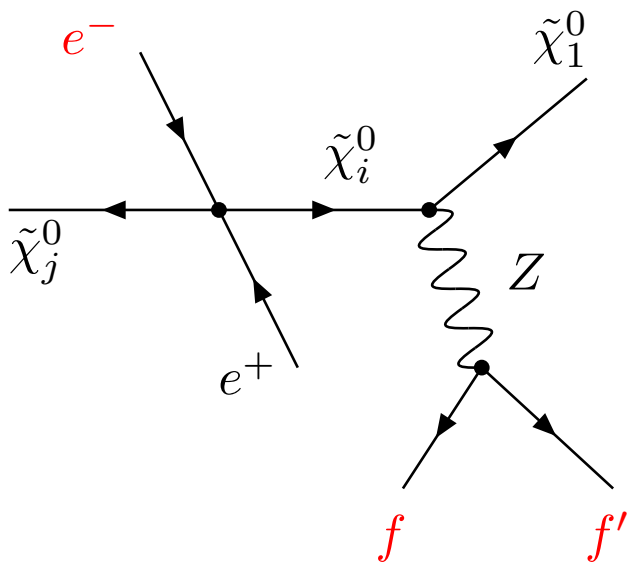


$e^+e^- \longrightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0; \tilde{\chi}_2^0 \longrightarrow \tilde{\tau}_1 \tau$ at $\sqrt{s} = 500$ GeV;
 $A_\tau = 250$ GeV; $\tan \beta = 5$; $m_0 = 100$ GeV; $P(e^-|e^+) = (-0.8|0.6)$
 $|\mu| = 240$ GeV; $M_2 = 400$ GeV



Asymmetry for neutralino decay into Z

$$A = \frac{\sigma(\mathcal{T} > 0) - \sigma(\mathcal{T} < 0)}{\sigma(\mathcal{T} > 0) + \sigma(\mathcal{T} < 0)}; \quad \mathcal{T} = [\vec{p}(e^-) \times \vec{p}(f)] \cdot \vec{p}(f')$$

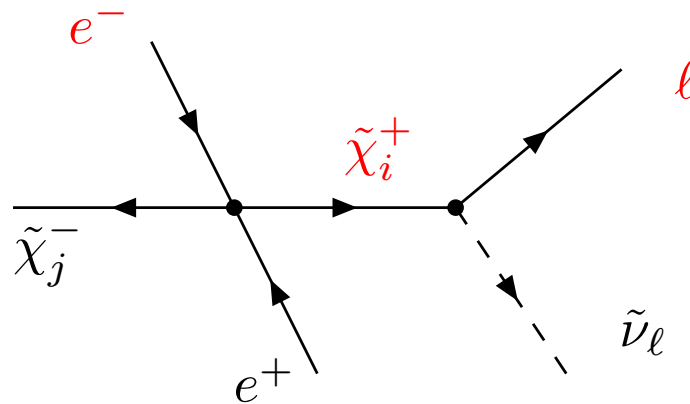


- also CP contributions to A from decay $\tilde{\chi}_i^0 \rightarrow \tilde{\chi}_1^0 Z$
- $A \propto \frac{|L|^2 - |R|^2}{|L|^2 + |R|^2} = 0.15(0.94)$ for $Z \rightarrow \ell^+ \ell^- (b \bar{b})$
 $\Rightarrow A \approx 3\%(18\%)$ for leptonic (hadronic) decays
- CP sensitive matrix elements of Z spin matrix

Asymmetry for chargino production

$$A = \frac{\sigma(\mathcal{T} > 0) - \sigma(\mathcal{T} < 0)}{\sigma(\mathcal{T} > 0) + \sigma(\mathcal{T} < 0)}$$

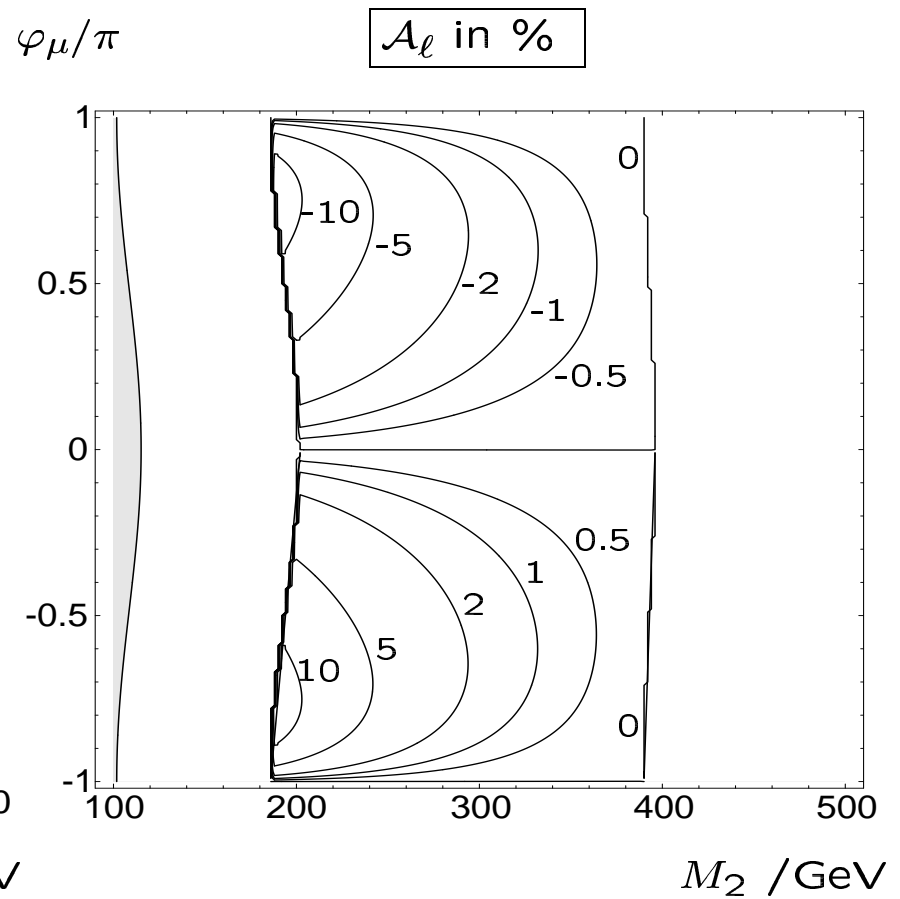
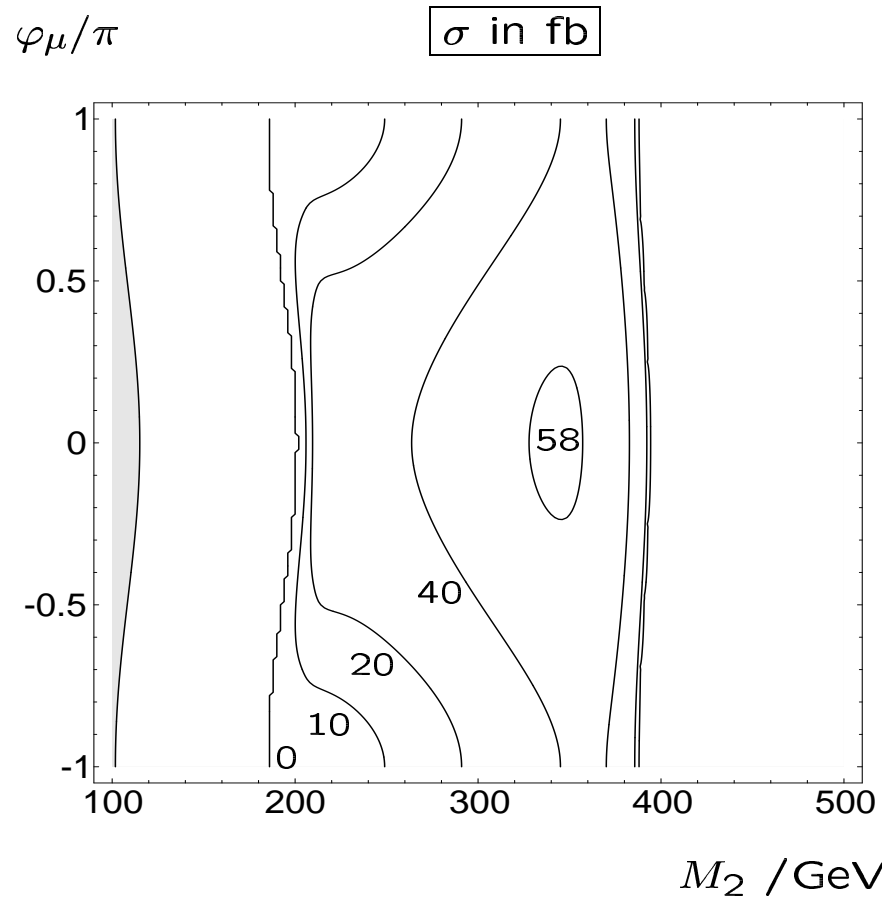
$$\mathcal{T} = [\vec{p}(e^-) \times \vec{p}(\tilde{\chi}_i^+)] \cdot \vec{p}(\ell)$$



$$e^+e^- \longrightarrow \tilde{\chi}_1^+ \tilde{\chi}_2^-; \tilde{\chi}_1^+ \longrightarrow \tilde{\nu}_\ell \ell^+ \quad \text{at } \sqrt{s} = 800 \text{ GeV};$$

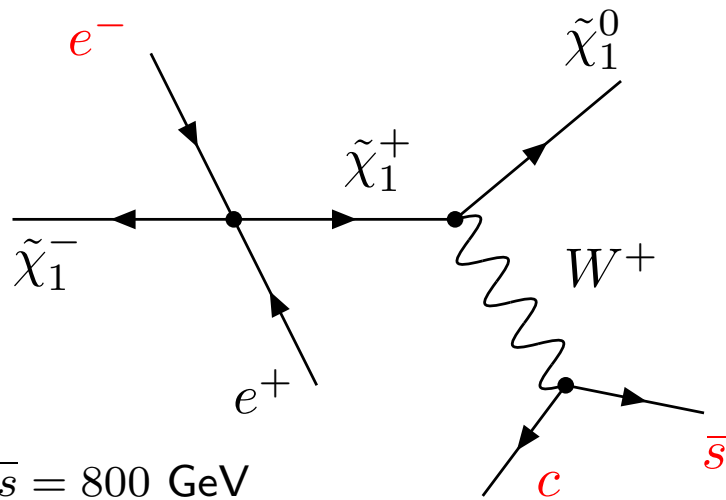
$$|\mu| = 400 \text{ GeV}; \tan \beta = 5; m_{\tilde{\nu}} = 185 \text{ GeV}; P(e^-|e^+) = (-0.8|0.6)$$

gray shaded area: $M(\tilde{\chi}_1^\pm) < 104 \text{ GeV}$



Asymmetry for chargino decay into W

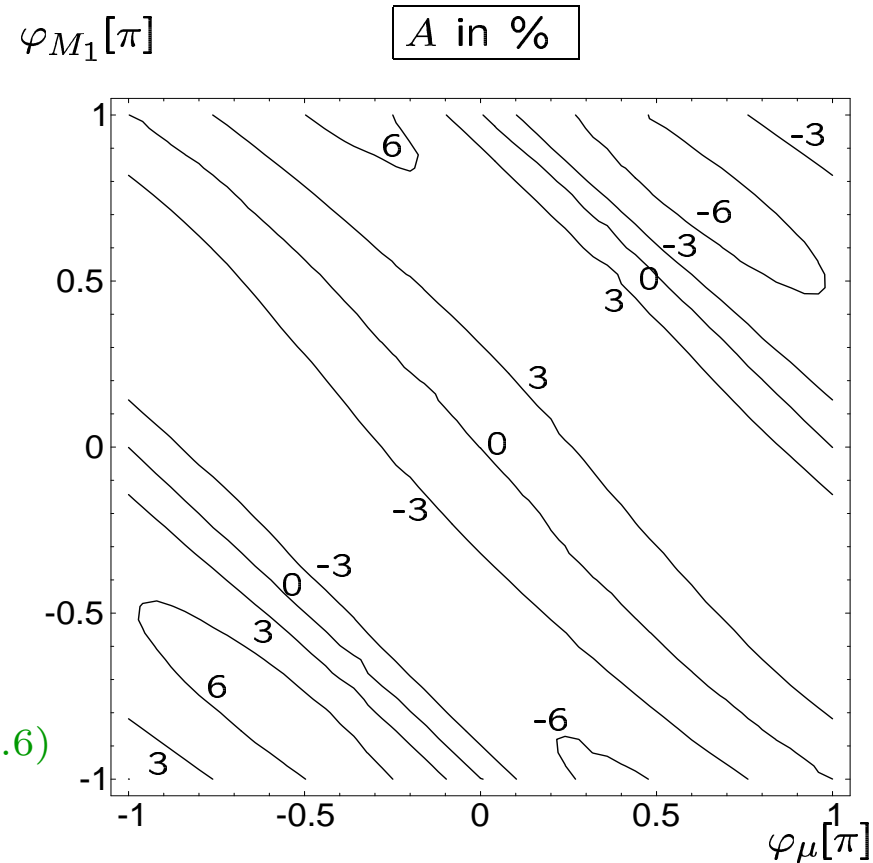
$$A = \frac{\sigma(\mathcal{T} > 0) - \sigma(\mathcal{T} < 0)}{\sigma(\mathcal{T} > 0) + \sigma(\mathcal{T} < 0)}; \quad \mathcal{T} = [\vec{p}(e^-) \times \vec{p}(c)] \cdot \vec{p}(\bar{s})$$



$\sqrt{s} = 800 \text{ GeV}$

$|\mu| = 350 \text{ GeV}; M_2 = 400 \text{ GeV};$

$\tan \beta = 5; m_0 = 300 \text{ GeV}; P(e^-|e^+) = (-.8|.6)$



Summary and conclusions

- There are new sources of CP violation in supersymmetric theories.
- Complex MSSM parameters (here phases of μ , M_1 , A_τ) have impact on the production and the decay of neutralinos and charginos.
- There are CP-sensitive observables:
triple products lead to CP-asymmetries.
- The CP-violating effects are of the order of 10%.
→ phases can be constrained/measured at future collider (ILC).