
Determination of NMSSM parameters by combined LHC/ILC analyses

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based on

G. Moortgat-Pick, S. Hesselbach, F. Franke, H. Fraas, JHEP **06** (2005) 048 [hep-ph/0502036]

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Outline

- Introduction
- Model discrimination in neutralino and Higgs sector
- NMSSM scenario
- Parameter determination at ILC
- SUSY searches at LHC
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- Outlook: Implementation of NMSSM in Fittino
- Conclusion

Introduction

- Revealing of underlying supersymmetric model:
Essential goal of LHC and ILC
↔ combined **LHC-ILC analysis** might be crucial
- **Next-to-minimal Supersymmetric Standard Model (NMSSM):**
Extension of MSSM by **singlet/singlino superfield \hat{S}**
- In superpotential: μ -term replaced by trilinear terms

$$\mu\hat{H}_1\hat{H}_2 \rightarrow \lambda\hat{H}_1\hat{H}_2\hat{S} + \frac{\kappa}{3}\hat{S}^3$$

$$\Rightarrow \mu \rightarrow \mu_{\text{eff}} = \lambda x \text{ with } x \equiv \langle S \rangle$$

- Possible solution of μ problem, less fine-tuning
- Extended neutralino and Higgs sectors:
5 neutralinos $\tilde{\chi}_i^0$, 3 scalars S_i , 2 pseudoscalars P_i

Introduction

- Distinguishing NMSSM \leftrightarrow MSSM possible via
 - Neutralino sector:
 - Additional neutralinos with singlino admixture accessible
 - Different polarization behavior
 - Higgs sector:
 - Light singlet-dominated scalars or pseudoscalars
- Here we analyze scenario where
 - Higgs sector allows no distinction at LHC or ILC because only MSSM-like lightest scalar S_1 accessible
 - Masses, cross sections and BRs of neutralinos/charginos at LHC or ILC₅₀₀ ($\sqrt{s} = 500$ GeV) consistent with MSSM

Neutralino sector

- 5 neutralinos $\tilde{\chi}_i^0$ (additional **singlino** state)

[e.g. Franke, Fraas, '95; Choi, Miller, Zerwas, '04]

- Hints for NMSSM:

- Singlino-dominated LSP [Ellwanger, Hugonie, '97, '98; S.H., Franke, Fraas, '00]

→ displaced vertices possible for $x = \langle S \rangle \gg m_W$

- Direct production of singlino-dominated $\tilde{\chi}_i^0$:

→ detectable at ILC up to $x = \mathcal{O}(10 \text{ TeV})$

↔ singlino purity $\approx 99\%$

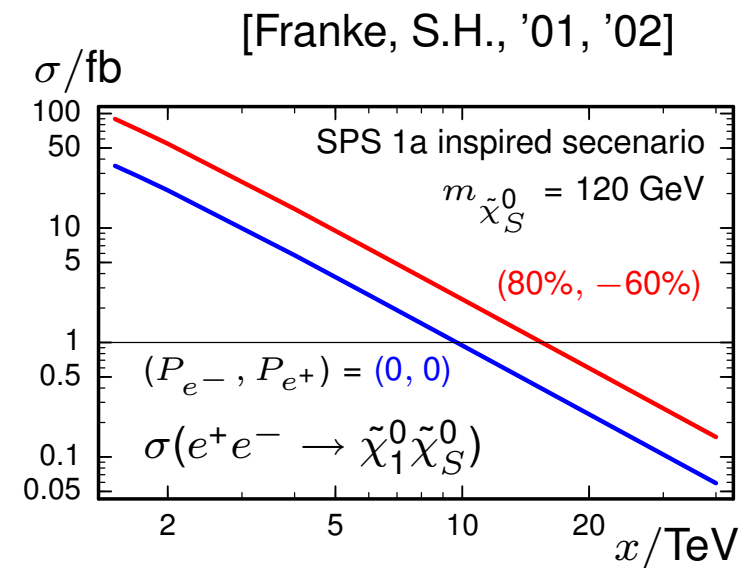
→ similar in E_6 inspired SUSY models with additional U(1) factors

[S.H., Franke, Fraas, '01]

- Different polarization behavior

[Moortgat-Pick, S.H., Franke, Fraas, '99]

[S.H., Franke, Fraas, '00]



Higgs sector

- 5 neutral Higgs bosons: 3 scalars S_i , 2 pseudoscalars P_i
[e.g. Franke, Fraas, '95; Miller, Nevzorov, Zerwas, '03]
- Light singlet dominated $S_1, P_1 \rightarrow$ hint for NMSSM
 - Higgs decays: $S_2 \rightarrow S_1 S_1$ ($S_1 \rightarrow P_1 P_1$)
for singlet dominated S_1 (P_1) [Ellwanger, Gunion, Hugonie, Moretti '03, '04]
[Gunion, Szleper, '04]
[Ellwanger, Gunion, Hugonie, '05]
 - Singlet dominated S_1 in LHC/ILC analyses [Miller, Moretti '04]
 - Sfermion decays: $\tilde{f}_2 \rightarrow \tilde{f}_1 + S_1, P_1$ [Kraml, Porod '05]
- **However**, additional trilinear soft scalar mass parameters A_λ and A_κ
 - \rightarrow singlet dominated Higgs bosons may also be heavy
 - \rightarrow our study in the following

Higgs sector

- In our scenario ($\tan\beta = 10$, $x = 915$ GeV, $\lambda = 0.5$, $\kappa = 0.2$):

Scan with NMHDECAY over A_λ and A_κ [Ellwanger, Gunion, Hugonie, '04]

→ theoretical and experimental constraints satisfied for

$$2740 \text{ GeV} < A_\lambda < 5465 \text{ GeV} \quad \text{and} \quad -553 \text{ GeV} < A_\kappa < 0 \text{ GeV}$$

- For $-440 \text{ GeV} \lesssim A_\kappa \lesssim -90 \text{ GeV}$:

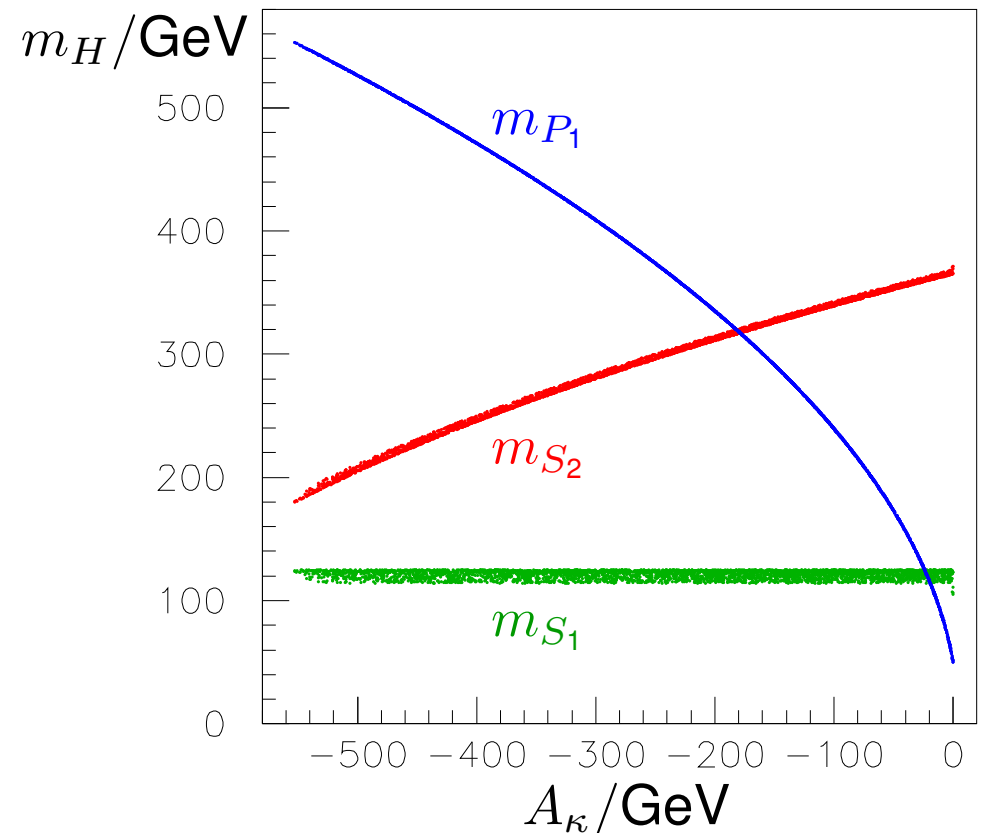
S_1 MSSM-like,

singlet dominated S_2 , P_1 heavy

e.g. $m_{S_1} = 124$ GeV,

$m_{S_2} = 311$ GeV, $m_{P_1} = 335$ GeV

for $A_\lambda = 4$ TeV, $A_\kappa = -200$ GeV



NMSSM Scenario

- NMSSM scenario

$$M_1 = 360 \text{ GeV}, M_2 = 147 \text{ GeV}, \tan \beta = 10, x = 915 \text{ GeV}, \lambda = 0.5, \kappa = 0.2$$

$$m_{\tilde{e}_L} = 240 \text{ GeV}, m_{\tilde{e}_R} = 220 \text{ GeV}, m_{\tilde{\nu}_e} = 226 \text{ GeV}$$

- Neutralino/chargino masses and mixing

	$m_{\tilde{\chi}_i^0}/\text{GeV}$	mixing character in % {gaugino, higgsino, singlino}
$\tilde{\chi}_1^0$	138	{94.7, 4.7, 0.5}
$\tilde{\chi}_2^0$	337	{41.1, 16.1, 42.9}
$\tilde{\chi}_3^0$	367	{56.6, 1.4, 42.0}
$\tilde{\chi}_4^0$	468	{0.8, 98.6, 0.6}
$\tilde{\chi}_5^0$	499	{6.8, 79.2, 14.0}

	$m_{\tilde{\chi}_i^\pm}/\text{GeV}$
$\tilde{\chi}_1^\pm$	139
$\tilde{\chi}_2^\pm$	474

→ small $\Delta(m_{\tilde{\chi}_1^\pm} - m_{\tilde{\chi}_1^0})$

→ similar to AMSB

Cross sections and errors

- Cross sections at ILC₅₀₀
(only $\tilde{\chi}_{1,2}^0, \tilde{\chi}_1^\pm$ accessible)
- Error estimation:
 - Statistical error for
 $\int \mathcal{L} = 100 \text{ fb}^{-1}$
 - Polarization uncertainty
 $\Delta \mathcal{P}_{e^\pm} / \mathcal{P}_{e^\pm} = 0.5\%$
 - Mass uncertainties:
1.5%: $\tilde{\chi}_{2,3}^0, \tilde{e}_{L,R}, \tilde{\nu}$
2%: $\tilde{\chi}_1^0, \tilde{\chi}_1^\pm$

$\sigma(e^+e^- \rightarrow \tilde{\chi}_1^\pm \tilde{\chi}_1^\mp)/\text{fb}$ at $\sqrt{s} = 400 \text{ GeV}$	
Unpolarized beams	323.9 ± 33.5
$(\mathcal{P}_{e^-}, \mathcal{P}_{e^+}) = (-90\%, +60\%)$	984.0 ± 101.6
$(\mathcal{P}_{e^-}, \mathcal{P}_{e^+}) = (+90\%, -60\%)$	13.6 ± 1.6
$\sigma(e^+e^- \rightarrow \tilde{\chi}_1^\pm \tilde{\chi}_1^\mp)/\text{fb}$ at $\sqrt{s} = 500 \text{ GeV}$	
Unpolarized beams	287.5 ± 16.5
$(\mathcal{P}_{e^-}, \mathcal{P}_{e^+}) = (-90\%, +60\%)$	873.9 ± 50.1
$(\mathcal{P}_{e^-}, \mathcal{P}_{e^+}) = (+90\%, -60\%)$	11.7 ± 1.2
$\sigma(e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0)/\text{fb}$ at $\sqrt{s} = 500 \text{ GeV}$	
Unpolarized beams	4.0 ± 1.2
$(\mathcal{P}_{e^-}, \mathcal{P}_{e^+}) = (-90\%, +60\%)$	12.1 ± 3.8
$(\mathcal{P}_{e^-}, \mathcal{P}_{e^+}) = (+90\%, -60\%)$	0.2 ± 0.1

Strategy

- Take “measured” masses and cross sections at ILC within uncertainties
- Determine **MSSM** parameters with strategy for ILC
 - [Choi, Djouadi, Dreiner, Kalinowski, Zerwas, '98]
 - [Choi, Djouadi, Guchait, Kalinowski, Song, Zerwas, '00]
 - [Choi, Kalinowski, Moortgat-Pick, Zerwas, '01, '02]
- Calculate masses and mixings of heavier neutralinos and charginos and compare with LHC analyses
 - [Desch, Kalinowski, Moortgat-Pick, Nojiri, Polesello, '03]
 - [Allanach et al., Les Houches 2003]
 - [Moortgat-Pick, '04]

Parameter determination at ILC

2 steps:

(I) Analysis of chargino sector

Input: $m_{\tilde{\chi}_1^\pm}$, $m_{\tilde{\nu}}$, $\sigma(e^+e^- \rightarrow \tilde{\chi}_1^+\tilde{\chi}_1^-)$ at $\sqrt{s} = 400$ and 500 GeV

⇒ chargino mixing matrix elements $U_{11}^2 = [0.84, 1.0]$, $V_{11}^2 = [0.83, 1.0]$

(II) Add information from neutralino sector: $m_{\tilde{\chi}_1^0}$, $m_{\tilde{\chi}_2^0}$ and $\sigma(e^+e^- \rightarrow \tilde{\chi}_1^0\tilde{\chi}_2^0)$

⇒ constraints for MSSM parameters:

$$M_1 = (377 \pm 42) \text{ GeV}$$

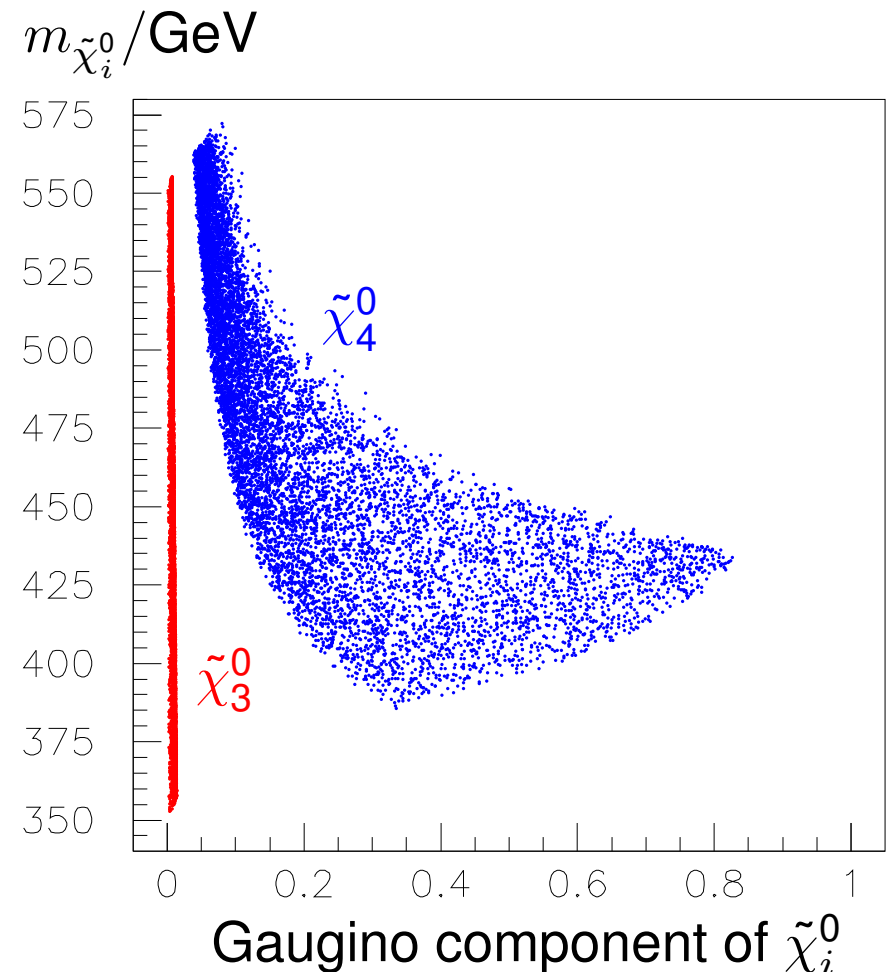
$$M_2 = (150 \pm 20) \text{ GeV}$$

$$\mu = (450 \pm 100) \text{ GeV}$$

$$\tan \beta = [1, 30]$$

Parameter determination at ILC

- “Measured” masses and cross sections compatible with MSSM
- Predictions for masses and mixings of heavier particles:
 - $\tilde{\chi}_3^0$: $m_{\tilde{\chi}_3^0} = [352, 555]$ GeV,
strong higgsino character
 - $\tilde{\chi}_4^0$: $m_{\tilde{\chi}_4^0} = [386, 573]$ GeV
larger gaugino admixture
 - $\tilde{\chi}_2^\pm$: $m_{\tilde{\chi}_2^\pm} = [450, 600]$ GeV



SUSY searches at LHC

- Cascade decays of squarks and gluinos
 - Masses of heavy gauginos accessible in invariant mass distributions
- In our NMSSM scenario: $\tilde{\chi}_3^0$ has large gaugino component
 - For simulations in mAMSB-like scenarios
see e.g. [Barr, Lester, Parker, Allanach, Richardson, JHEP 0303, 045]
 - $BR(\tilde{\chi}_3^0 \rightarrow \tilde{\ell}_{L,R}^\pm \ell^\mp) \sim 45\%$
 - ⇒ expected to see edges for $\tilde{\chi}_3^0 \rightarrow \tilde{\ell}_{L,R}^\pm \ell^\mp$

SUSY searches at LHC

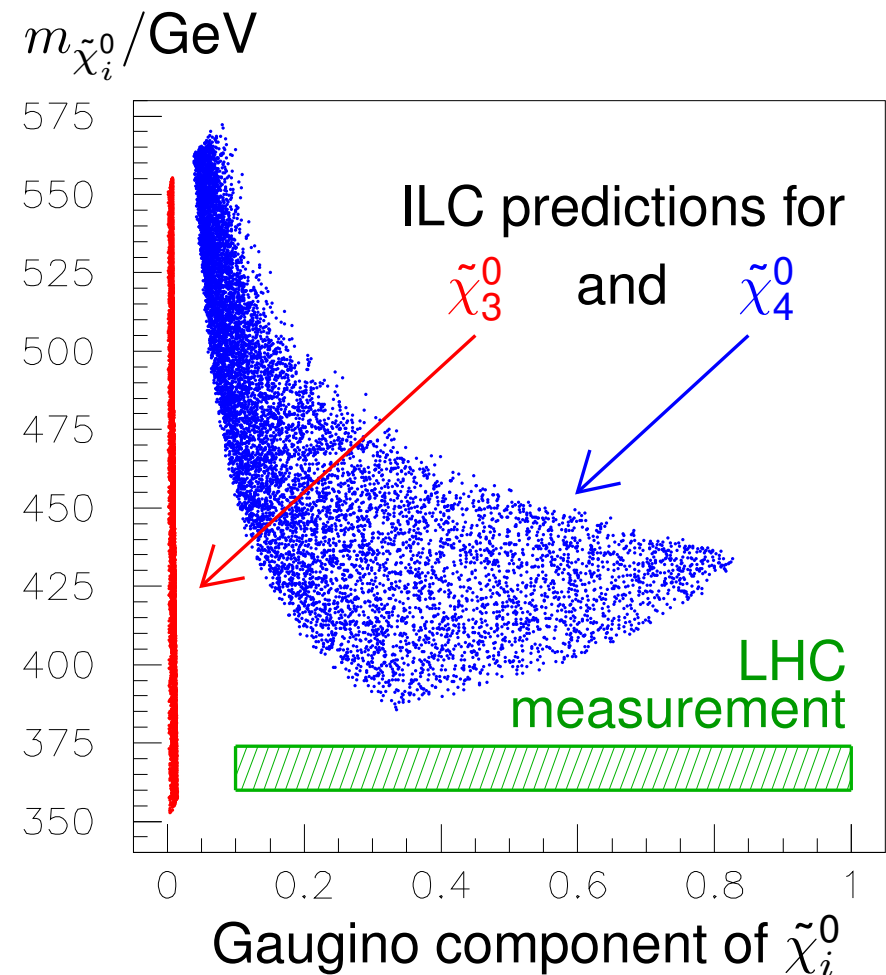
- With input from ILC measurements:

$$m_{\tilde{\chi}_1^0}, m_{\tilde{\chi}_2^0}, m_{\tilde{\ell}}, m_{\tilde{\nu}}$$

- Precision of 2% for $m_{\tilde{\chi}_3^0}$ may be possible:

$$m_{\tilde{\chi}_i^0} = (367 \pm 7) \text{ GeV}$$

- Compatible with mass predictions in MSSM, however, not with predictions for small gaugino component!



- Other possibility: Interpretation of measured gaugino as $\tilde{\chi}_4^0$: Incompatible with cross section measurements at ILC!

The ILC $_{650}^{\mathcal{L}=1/3}$ option

- Inconsistency of LHC and ILC analyses may motivate low-luminosity but higher-energy option ILC $_{650}^{\mathcal{L}=1/3}$
 $\rightarrow \sqrt{s} = 650$ GeV at a third of the luminosity without hardware changes

- $\tilde{\chi}_3^0, \tilde{\chi}_4^0, \tilde{\chi}_2^\pm$ accessible

	σ/fb at $\sqrt{s} = 650$ GeV		
	$e^+e^- \rightarrow \tilde{\chi}_1^0\tilde{\chi}_3^0$	$e^+e^- \rightarrow \tilde{\chi}_1^0\tilde{\chi}_4^0$	$e^+e^- \rightarrow \tilde{\chi}_1^\pm\tilde{\chi}_2^\mp$
Unpolarized beams	12.2 ± 0.6	5.5 ± 0.4	2.4 ± 0.3
$(\mathcal{P}_{e^-}, \mathcal{P}_{e^+}) = (-90\%, +60\%)$	36.9 ± 1.1	14.8 ± 0.7	5.8 ± 0.4
$(\mathcal{P}_{e^-}, \mathcal{P}_{e^+}) = (+90\%, -60\%)$	0.6 ± 0.1	2.2 ± 0.3	1.6 ± 0.2

- Masses $m_{\tilde{\chi}_1^0}, m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_3^0}, m_{\tilde{\chi}_4^0}, m_{\tilde{\chi}_1^\pm}, m_{\tilde{\chi}_2^\pm}$ precisely measurable

Outlook: Fit of NMSSM parameters

Goal: determination of NMSSM parameters

$$M_1, M_2, \tan \beta, \lambda, x = \langle S \rangle, \mu_{\text{eff}} = \lambda x, \kappa$$

- Implementation of NMSSM in Fittino [Bechtle, Desch, Wienemann]
[Bechtle, Desch, S.H., Moortgat-Pick, Porod, Wienemann]
 - NMSSM particle spectrum from SPheno [Porod]
 - Higgs spectrum from NMHDECAY [Ellwanger, Gunion, Hugonie]
 - Input: precisely measured masses and cross sections at LHC and ILC
- Determination of NMSSM parameters

Conclusion

- NMSSM scenario that cannot be distinguished from MSSM at LHC or ILC with $\sqrt{s} = 500$ GeV
→ example for $M_2 < M_1$
- Masses and cross sections of accessible neutralinos/charginos compatible with MSSM: no contradiction in “usual” analysis
- Combined LHC+ILC analyses: show inconsistency with MSSM
- Motivates immediate use of ILC $_{650}^{\mathcal{L}=1/3}$
→ clear identification of NMSSM
- Outlook: Fit of NMSSM parameters

Neutralino cross sections at higher energies

$\sigma(e^+e^- \rightarrow \tilde{\chi}_i^0 \tilde{\chi}_j^0)/\text{fb}$, unpolarized	$\sqrt{s} = 800 \text{ GeV}$	$\sqrt{s} = 1000 \text{ GeV}$	$\sqrt{s} = 3000 \text{ GeV}$
$\tilde{\chi}_1^0 \tilde{\chi}_2^0/\text{fb}$	27.6 ± 0.2	23.6 ± 0.2	4.0 ± 0.06
$\tilde{\chi}_1^0 \tilde{\chi}_3^0/\text{fb}$	14.9 ± 0.2	13.1 ± 0.2	2.2 ± 0.05
$\tilde{\chi}_1^0 \tilde{\chi}_4^0/\text{fb}$	6.1 ± 0.1	4.4 ± 0.1	0.5 ± 0.02
$\tilde{\chi}_1^0 \tilde{\chi}_5^0/\text{fb}$	0.4 ± 0.03	0.5 ± 0.03	0.1 ± 0.01
$\tilde{\chi}_2^0 \tilde{\chi}_2^0/\text{fb}$	7.2 ± 0.1	10.6 ± 0.1	2.4 ± 0.05
$\tilde{\chi}_2^0 \tilde{\chi}_3^0/\text{fb}$	13.2 ± 0.2	24.0 ± 0.2	5.5 ± 0.07
$\tilde{\chi}_2^0 \tilde{\chi}_4^0/\text{fb}$	–	5.7 ± 0.1	0.8 ± 0.03
$\tilde{\chi}_2^0 \tilde{\chi}_5^0/\text{fb}$	–	1.2 ± 0.05	0.4 ± 0.02
$\tilde{\chi}_3^0 \tilde{\chi}_3^0/\text{fb}$	6.1 ± 0.1	15.9 ± 0.2	4.0 ± 0.06
$\tilde{\chi}_3^0 \tilde{\chi}_4^0/\text{fb}$	–	0.7 ± 0.04	0.1 ± 0.01
$\tilde{\chi}_3^0 \tilde{\chi}_5^0/\text{fb}$	–	1.5 ± 0.05	0.7 ± 0.03
$\tilde{\chi}_4^0 \tilde{\chi}_4^0/\text{fb}$	–	0.0	0.0
$\tilde{\chi}_4^0 \tilde{\chi}_5^0/\text{fb}$	–	13.7 ± 0.2	4.1 ± 0.06
$\tilde{\chi}_5^0 \tilde{\chi}_5^0/\text{fb}$	–	0.0	0.0

→ 1 σ statistical error on basis of $\mathcal{L}_{800,1000} = 500 \text{ fb}^{-1}$ and $\mathcal{L}_{3000} = 1000 \text{ fb}^{-1}$