
Transversely and Longitudinally Polarized Beams and SUSY CP Searches

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Outline

- Introduction
 - MSSM with complex parameters
 - Complex parameters in chargino/neutralino sectors
- CP-odd and T-odd asymmetries using transverse beam polarization
- T-odd triple product asymmetries and longitudinal beam polarization
- Summary and outlook

- General MSSM:
 - **Complex parameters** in Higgs potential and soft SUSY breaking terms
 - Physical phases of the parameters
 - M_1 : U(1) gaugino mass parameter
 - μ : Higgs-higgsino mass parameter
 - A_f : trilinear couplings of sfermions
 - $m_{\tilde{g}}$: gluino mass
 - Introduction of **CP violation**
 - May help to explain baryon asymmetry of universe
 - Constraints from electric dipole moments (EDMs) of e, n, Hg, Tl
 - [Ibrahim, Nath, '99; Barger, Falk, Han, Jiang, Li, Plehn, '01; Abel, Khalil, Lebedev, '01]
 - [Oshimo, Nihei, Fujita, '05; Pospelov, Ritz, '05; Olive, Pospelov, Ritz, Santoso, '05]
 - **Aim:** analysis the CP structure of theory and determination of phases
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● **Chargino** mass matrix:

$$X = \begin{pmatrix} M_2 & \sqrt{2} m_W s_\beta \\ \sqrt{2} m_W c_\beta & \mu \end{pmatrix}$$

● **Neutralino** mass matrix:

$$Y = \begin{pmatrix} M_1 & 0 & -m_Z s_W c_\beta & m_Z s_W s_\beta \\ 0 & M_2 & m_Z c_W c_\beta & -m_Z c_W s_\beta \\ -m_Z s_W c_\beta & m_Z c_W c_\beta & 0 & -\mu \\ m_Z c_W c_\beta & -m_Z c_W s_\beta & -\mu & 0 \end{pmatrix}$$

$$s_\beta \equiv \sin \beta, c_\beta \equiv \cos \beta$$

μ : Higgs-higgsino mass parameter $\rightarrow |\mu|, \varphi_\mu$

M_1 : U(1) gaugino mass parameter $\rightarrow |M_1|, \varphi_{M_1}$

M_2 : SU(2) gaugino mass parameter

● Diagonalization \Rightarrow **complex** mixing matrices \rightarrow enter $\tilde{\chi}^{\pm}, \tilde{\chi}^0$ couplings

Transverse beam polarization

Chargino/neutralino production

$$e^+e^- \longrightarrow \tilde{\chi}_i + \tilde{\chi}_j$$

with **transverse beam polarization** (4-vector t_{\pm}^{μ} , polarization degree $\mathcal{P}_{e^{\pm}}^T$)

- Terms in amplitude squared $|T|^2 = P$ depending on $\mathcal{P}_{e^{\pm}}^T$:

$$P_T \sim \mathcal{P}_{e^-}^T \mathcal{P}_{e^+}^T [f_1 \Delta_1 r_1 + f_2 \Delta_2 r_2] \quad (\text{in limit } m_e = 0!)$$

f_i : couplings; Δ_i : propagators; r_i : products of t_{\pm} and momenta

\Rightarrow **both beams have to be polarized**

[POWER report, hep-ph/0507011]

- r_1 is real; r_2 is imaginary, consisting of products like $i\epsilon_{\mu\nu\rho\sigma} t_{\pm}^{\mu} p_i^{\nu} p_j^{\rho} p_k^{\sigma}$

\Rightarrow with **complex couplings** f_2 : real contributions to observables

\Rightarrow CP-odd terms $\sim \text{Im}(f_2 \Delta_2) \text{Im}(r_2)$ at tree level

\Rightarrow CP-odd asymmetries $\sim \mathcal{P}_{e^-}^T \mathcal{P}_{e^+}^T$

Transverse beam polarization

- Chargino production: [Bartl, Hohenwarter-Sodek, Kernreiter, Rud, hep-ph/0403265]
Dirac particles: couplings $f_2\Delta_2$ have to be real (CPT invariance)
 - ⇒ CP-odd terms $f_2\Delta_2r_2$ vanish
 - CP-even asymmetries can be defined with help of $f_1\Delta_1r_1$
 - Neutralino production:
[Bartl, Fraas, SH, Hohenwarter-Sodek, Kernreiter, Moortgat-Pick, hep-ph/0510029]
Majorana particles: t and u channels contribute
 - ⇒ CP-odd terms $f_2\Delta_2r_2 \neq 0$ allowed
 - ⇒ CP-odd observables can be defined
- more details → Karl Hohenwarter-Sodek's talk in SUSY session

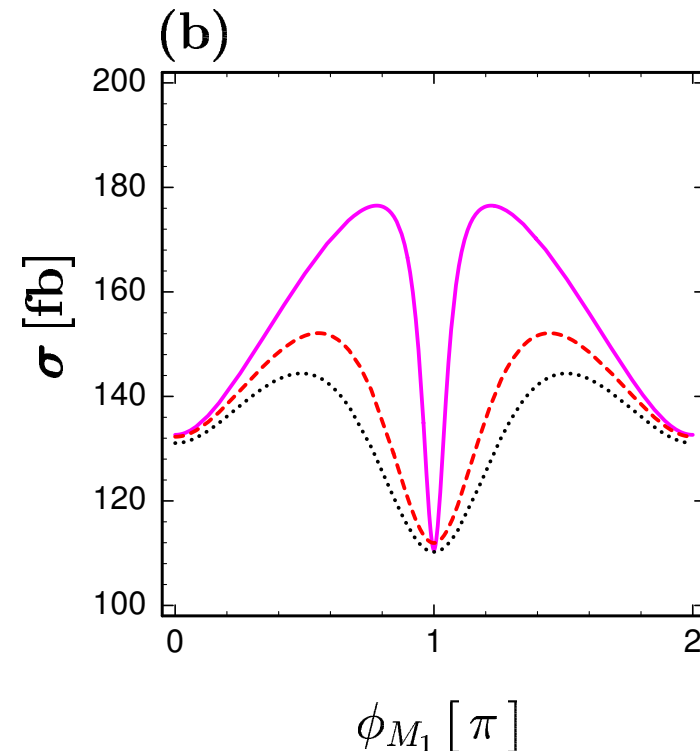
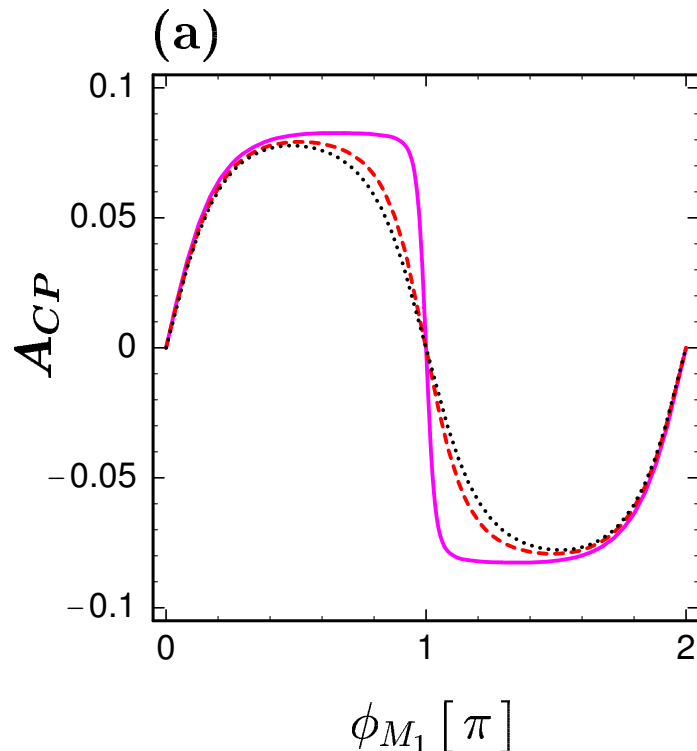
Transverse beam polarization

Example for CP-odd asymmetry A_{CP} for $e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0$

[Bartl, Fraas, SH, Hohenwarter-Sodek, Kernreiter, Moortgat-Pick, hep-ph/0510029]

$M_2 = 245$ GeV, $|M_1| = 123.3$ GeV, $|\mu| = 160$ GeV, $\phi_\mu = 0$, $m_{\tilde{e}_L} = 400$ GeV, $m_{\tilde{e}_R} = 150$ GeV

$\sqrt{s} = 500$ GeV, $(\mathcal{P}_{e^-}^T, \mathcal{P}_{e^+}^T) = (100\%, 100\%)$, $\tan \beta = 3, 10, 30$



(factor 0.54 for $(\mathcal{P}_{e^-}^T, \mathcal{P}_{e^+}^T) = (90\%, 60\%)$)

T-odd triple product asymmetries

Chargino and neutralino production and decay

$$e^+e^- \longrightarrow \tilde{\chi}_i + \tilde{\chi}_j \longrightarrow \tilde{\chi}_i + \tilde{\chi}_1^0 f \bar{f}^{(')}$$

- **Full spin correlation** between production and decay

[Moortgat-Pick, Fraas, '97; Moortgat-Pick, Fraas, Bartl, Majerotto, '98, '99; Choi, Song, Song, '99]

- Amplitude squared $|T|^2 = PD + \Sigma_P^a \Sigma_D^a$

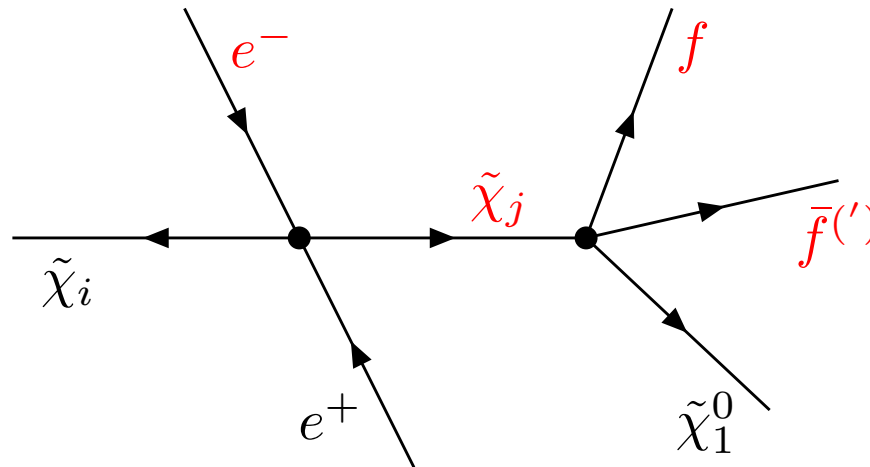
- In Σ_P^a and Σ_D^a : products like $i\epsilon_{\mu\nu\rho\sigma} p_i^\mu p_j^\nu p_k^\rho p_l^\sigma$

⇒ with **complex couplings**: real contributions to observables

⇒ CP violation at tree level

T-odd triple product asymmetries

Triple products: $\mathcal{T} = \vec{p}_{e^-} \cdot (\vec{p}_f \times \vec{p}_{\bar{f}'})$ or $\mathcal{T} = \vec{p}_{e^-} \cdot (\vec{p}_{\tilde{\chi}_j} \times \vec{p}_f)$



→ T-odd asymmetry:

$$A_T = \frac{\sigma(\mathcal{T} > 0) - \sigma(\mathcal{T} < 0)}{\sigma(\mathcal{T} > 0) + \sigma(\mathcal{T} < 0)} = \frac{\int \text{sign}(\mathcal{T}) |\mathcal{T}|^2 d\text{Lips}}{\int |\mathcal{T}|^2 d\text{Lips}}$$

→ CP-odd, if final state interactions and finite-widths effects can be neglected

T-odd triple product asymmetries

- Chargino/neutralino production with subsequent three-body decays
 - [Bartl, Fraas, SH, Hohenwarter-Sodek, Moortgat-Pick, hep-ph/0406190]
 - [Bartl, Fraas, SH, Hohenwarter-Sodek, Moortgat-Pick, in preparation]
- Chargino/neutralino production with subsequent two-body decays
 - Leptonic decays
 - [Bartl, Fraas, Kittel, Majerotto, hep-ph/0308141, hep-ph/0308143]
 - [Bartl, Fraas, Kernreiter, Kittel, Majerotto, hep-ph/0310011]
 - [Bartl, Fraas, Kittel, Majerotto, hep-ph/0406309]
 - Decays into W and Z
 - [Bartl, Fraas, Kittel, Majerotto, hep-ph/0402016]
 - [Kittel, Bartl, Fraas, Majerotto, hep-ph/0410054]
 - CP asymmetries using tau polarization for $\ell = \tau$
 - [Bartl, Kernreiter, Kittel, hep-ph/0309340; Choi, Drees, Gaissmaier, Song, hep-ph/0310284]
- Monte Carlo study for neutralino production and decay
 - [Aguilar-Saavedra, hep-ph/0404104]

→ more details → Olaf Kittel's talk in SUSY session

T-odd asymmetries and beam polarization

Asymmetry A_T

for $e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \ell^+ \ell^-$

[Bartl, Fraas, SH, Hohenwarter-Sodek, Moortgat-Pick,
hep-ph/0406190; POWER report, hep-ph/0507011]

$\tan \beta = 10$, $M_2 = 300$ GeV, $|M_1| = 150$ GeV, $|\mu| = 200$ GeV

$\varphi_{M_1} = 0.5\pi$, $\varphi_\mu = 0$, $m_{\tilde{e}_L} = 267.6$ GeV, $m_{\tilde{e}_R} = 224.4$ GeV

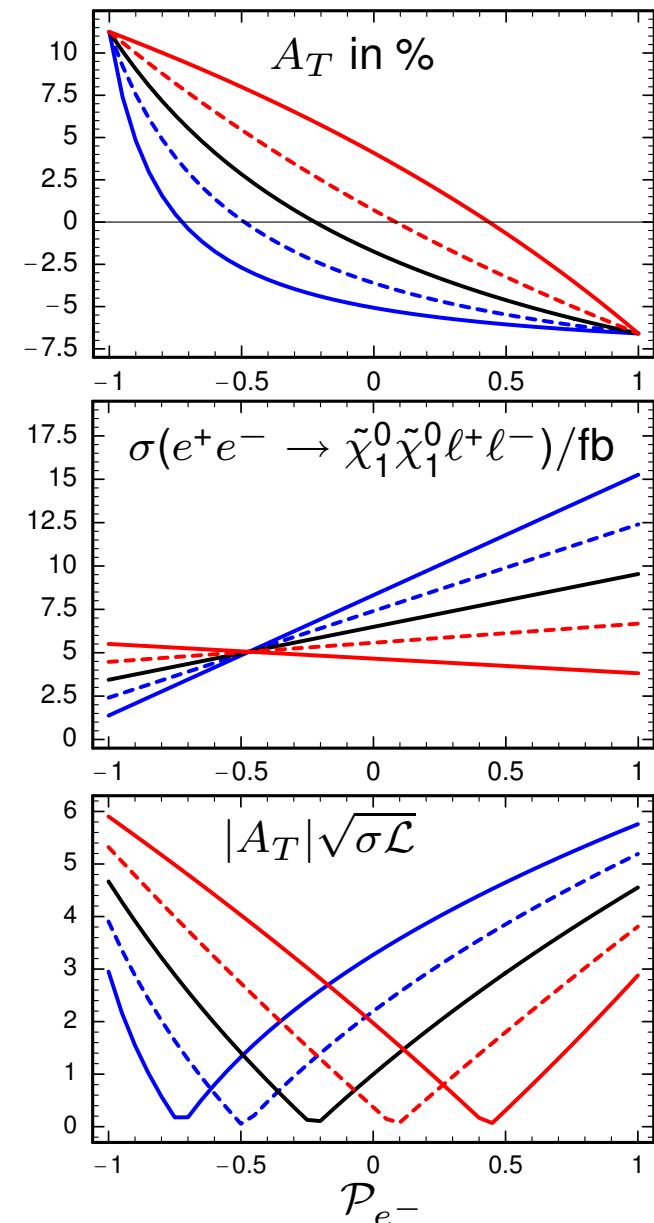
$\sqrt{s} = 500$ GeV, $\mathcal{L} = 500$ fb $^{-1}$, $\mathcal{P}_{e^+} = +0.6, +0.3, 0, -0.3, -0.6$

→ e^- polarization considerably enhances A_T

→ e^+ polarization enhances σ

Measurability of A_T : $\sim |A_T| \sqrt{\sigma \mathcal{L}}$

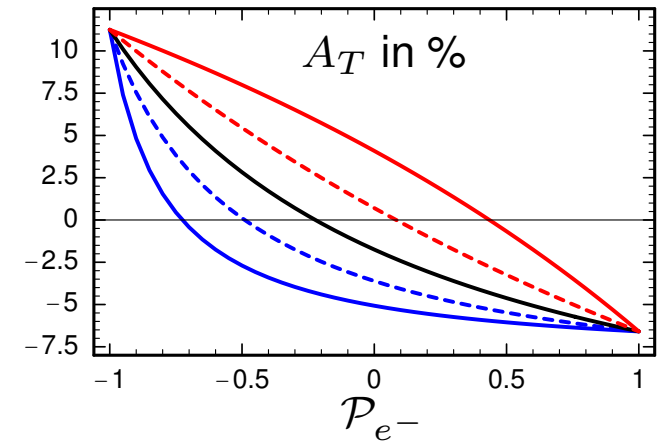
→ e^+ polarization enhances
measurability by $\sim 30\%$



T-odd asymmetries and beam polarization

Explanation for behavior of A_T

- For $m_{\tilde{e}_L} = 267.6 \text{ GeV} \sim m_{\tilde{e}_R} = 224.4 \text{ GeV}$: contributions from \tilde{e}_L and \tilde{e}_R exchange to A_T have similar size, but opposite sign
- Unpolarized beams: \tilde{e}_L and \tilde{e}_R contributions cancel \Rightarrow small asymmetries A_T
- $\mathcal{P}_{e^-} = -0.9$: \tilde{e}_L contributions dominate \Rightarrow large asymmetries A_T
- $\mathcal{P}_{e^-} = +0.9$: \tilde{e}_R contributions dominate \Rightarrow large A_T with opposite sign
- Additional e^+ polarization: only small enhancement of A_T

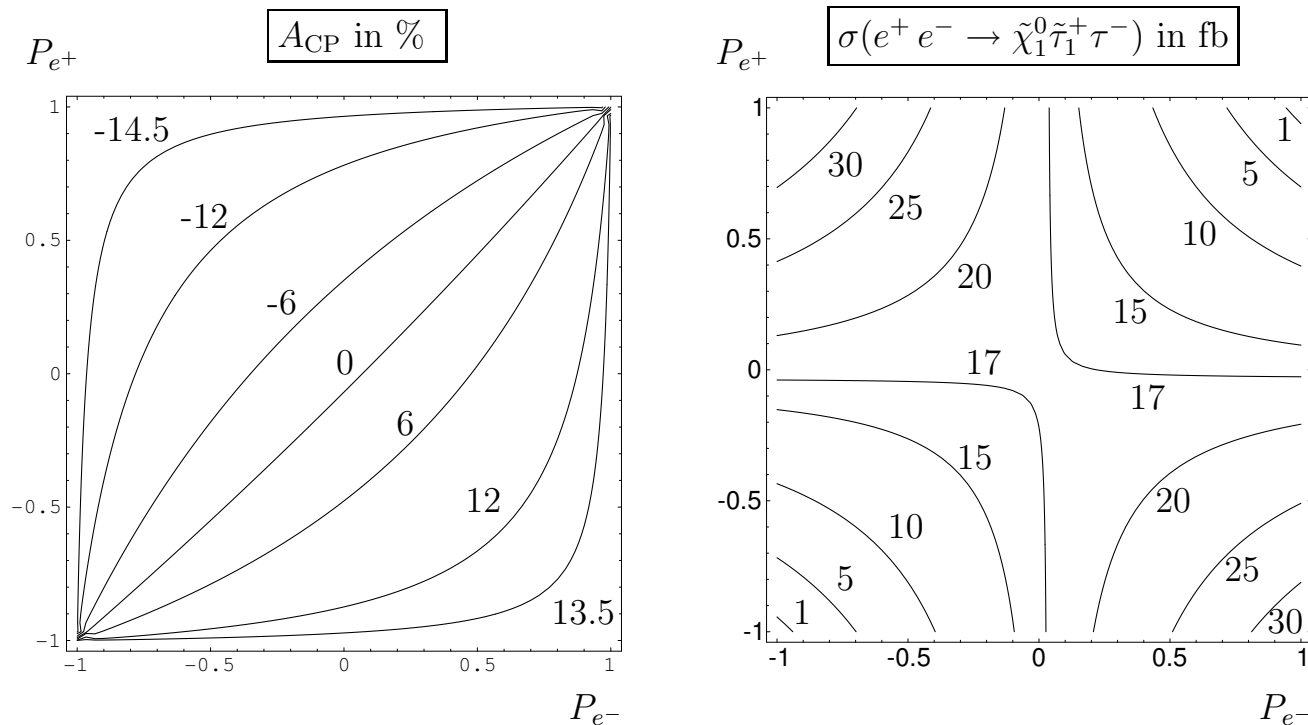


T-odd asymmetries and beam polarization

Asymmetry A_{CP} for $e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\tau}_1^+ \tau^-$

[Bartl, Fraas, Kernreiter, Kittel, Majerotto, hep-ph/0310011; POWER report, hep-ph/0507011]

$\tan \beta = 5$, $M_2 = 200$ GeV, $|M_1| = 5/3 M_2 \tan^2 \theta_W$, $|\mu| = 250$ GeV, $\varphi_{M_1} = 0$, $\varphi_\mu = 0$
 $|A_\tau| = 1500$ GeV, $\varphi_{A_\tau} = 0.5\pi$, $m_{\tilde{\tau}_1} = 143$ GeV, $m_{\tilde{\tau}_2} = 210$ GeV



→ Additional e^+ polarization enhances mainly σ

Summary and outlook

- CP-odd asymmetries and transverse beam polarization
 - Asymmetries in neutralino production and decay $\sim \mathcal{P}_{e^-}^T \mathcal{P}_{e^+}^T$
 - ⇒ Polarized positrons necessary to measure asymmetries
 - $e^+e^- \rightarrow \gamma Z$: asymmetries $\sim \mathcal{P}_{e^-}^T \mathcal{P}_{e^+}^T$ [POWER report, hep-ph/0507011]
(sensitive to CP-violating $\gamma\gamma Z$, γZZ couplings)
 - $e^+e^- \rightarrow t\bar{t}$: asymmetries $\sim \frac{1}{2}(\mathcal{P}_{e^-}^T - \mathcal{P}_{e^+}^T)$ [POWER report, hep-ph/0507011]
(sensitive to new CP-violating (pseudo-)scalar or tensor couplings)
- CP-odd asymmetries and longitudinal beam polarization
 - Positron polarization enhances cross section
 - ⇒ For $\mathcal{P}_{e^+} = 60\%$: 30% better measurability of asymmetry possible