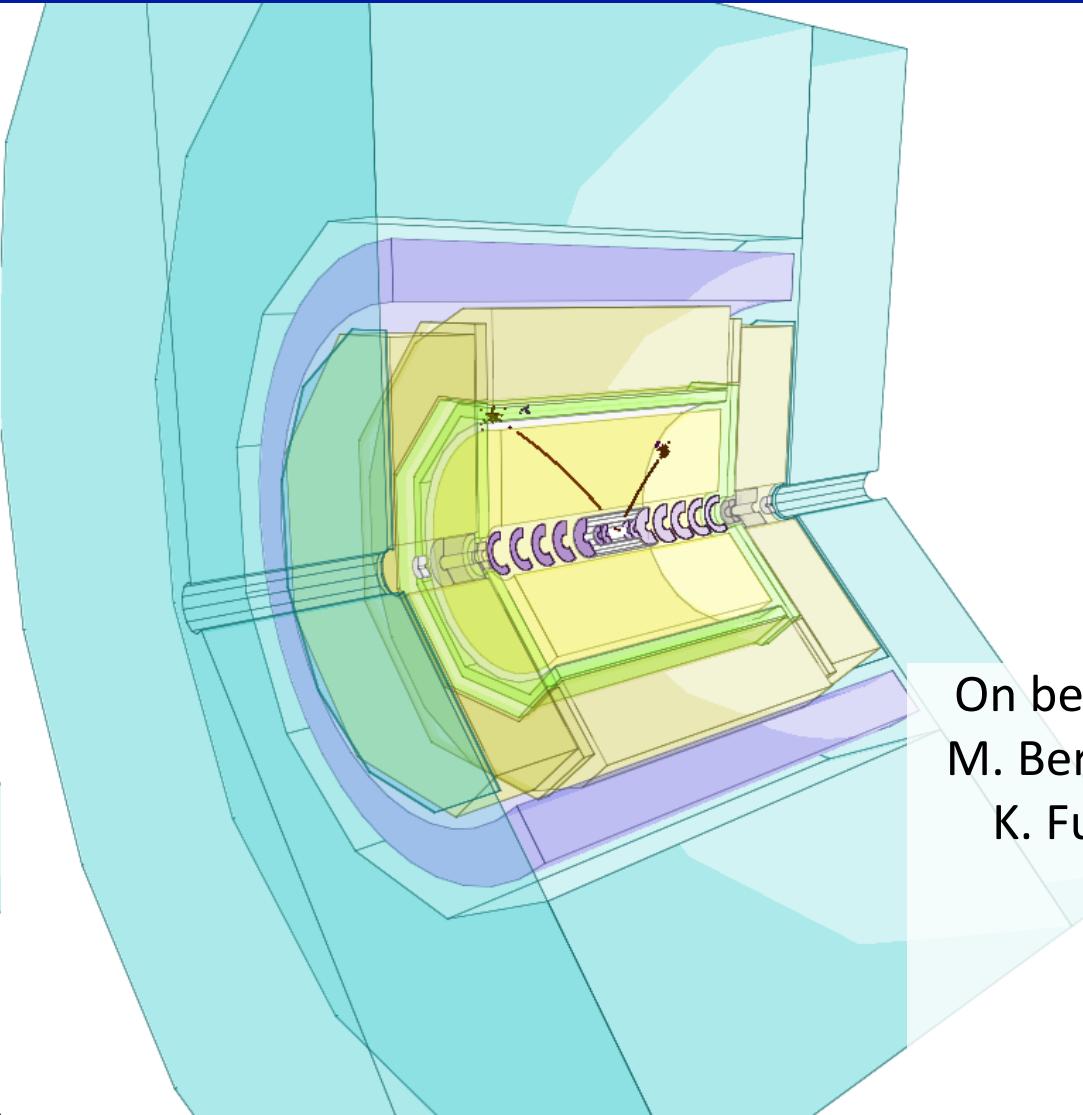


# Characterizing Light Higgsinos from Natural SUSY at ILC $\sqrt{s} = 500$ GeV



Jacqueline Yan (KEK)  
On behalf of H. Baer (Univ of Oklahoma),  
M. Berggren, S.-L. Lehtinen, J. List (DESY),  
K. Fujii (KEK), T. Tanabe (Univ of Tokyo)

**ILD Software  
and Analysis Meeting**

July 13, 2016

# Outline

- ◆ Motivation of study
- ◆ Event selection
- ◆ Extraction of Higgsino mass and cross section
- ◆ SUSY parameter determination
- ◆ Goals and plans

# Motivation for Searching Light Higgsinos with Small $\Delta M$

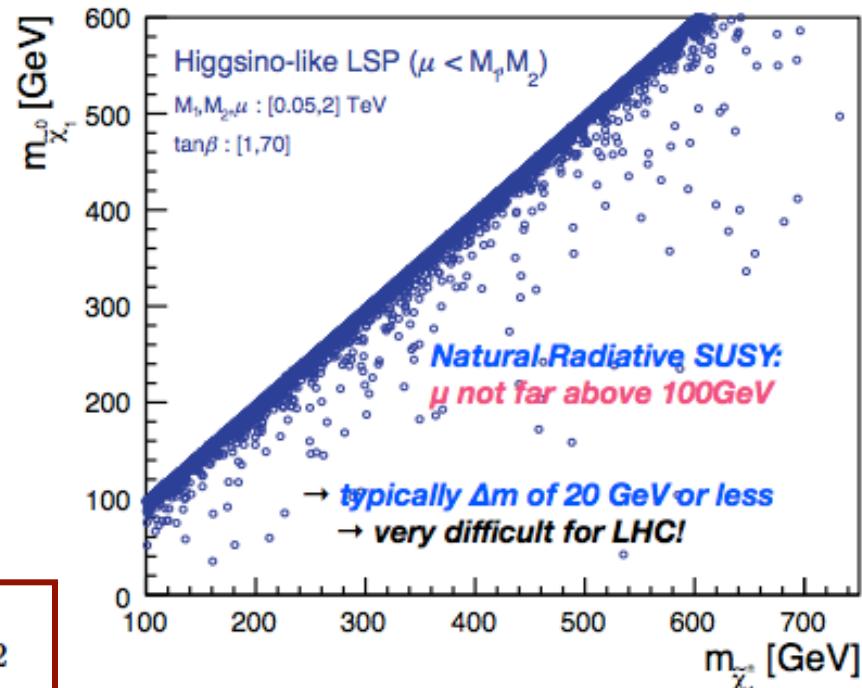
## ❖ From experimental point of view:

- LHC already excluded large regions with large  $\Delta M = M(\text{NLSP}) - M(\text{LSP})$
- Remaining region with compressed spectrum very small visible energy release, near impossible to probe at LHC  
→ ILC is essential

## ❖ From theoretical point of view:

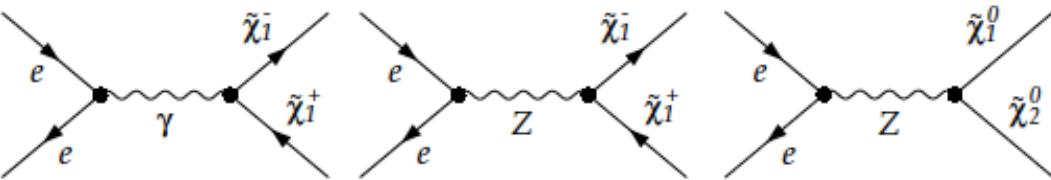
**Compressed Higgsino spectra related to naturalness** [e.g. arXiv:1212.2655, arXiv:1404.7510]

$$\frac{M_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2$$



- To maintain **small electroweak fine tuning  $\Delta EW$  ( $<\sim 3\%$ )**, all contributions on right-hand-side should be comparable to  $M(Z)$  → requires  $\mu \sim 100\text{--}300 \text{ GeV}$   
top and bottom squarks in the few TeV regime, gluino mass 2–4 TeV,  
1st, 2nd generation squarks and sleptons in the 5–30 TeV regime
- $\mu$  feeds mass to both SM (W, Z, h) and SUSY particles (Higgsinos)
- Higgsino masses not too far from masses of W, Z, h ( $\sim 100$  GeV)

# Benchmarks in this Study



**RNS model** (Radiatively-driven natural SUSY)

- **4 light Higgsinos:**  $\tilde{\chi}_1^0$     $\tilde{\chi}_2^0$     $\tilde{\chi}_1^+$     $\tilde{\chi}_1^-$   
(LSP)
- **$\Delta M$  about 10-20 GeV complies with naturalness** (ISR tag not needed)

This study:  $\sqrt{s} = 500 \text{ GeV}$   
Full detector simulation

Currently studying ILC1 benchmark

(Pe-, Pe+)	(-1.0,+1.0)	(+1.0,-1.0)
$\sigma(\chi_1^+ \chi_1^-) [\text{fb}]$	1800	335
$\sigma(\chi_1^0 \chi_2^0) [\text{fb}]$	491	379

$\text{BR}(\chi_1^+ \rightarrow \chi_1^0 \text{ qq'})$	67%
$\text{BR}(\chi_1^+ \rightarrow \chi_1^0 \text{ l}\nu)$ ( $\text{l}=\text{e},\mu$ )	22%
$\text{BR}(\chi_2^0 \rightarrow \chi_1^0 \text{ qq'})$	58%
$\text{BR}(\chi_2^0 \rightarrow \chi_1^0 \text{ ll})$ ( $\text{l}=\text{e},\mu$ )	7.4%

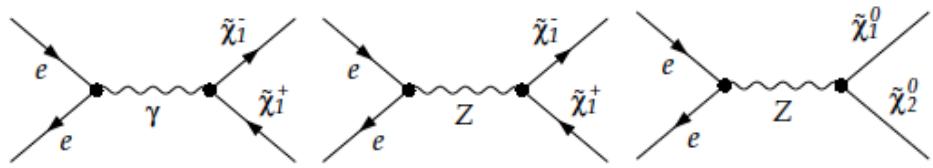
NUHM2 model parameters [arXiv:1404.7510]

Benchmark	ILC1	ILC2
$M_0 \text{ [GeV]}$	7025	5000
$M_{1/2} \text{ [GeV]}$	568.3	1200
$A_0 \text{ [GeV]}$	-10427	-8000
$\tan\beta$	10	15
$\mu \text{ [GeV]}$	115	150
$M_A \text{ [GeV]}$	1000	1000
$M(\chi_1^0) \text{ [GeV]}$	102.7	148.1
$M(\chi_1^\pm) \text{ [GeV]}$	117.3	158.3
$M(\chi_2^0) \text{ [GeV]}$	124.0	157.8
$M(\chi_3^0) \text{ [GeV]}$	267.0	538.8

Higgs precision  
measurements useful for  
parameter determination

Defined at GUT scale  
Defined at weak scale  
Observables

# Goal of Light Higgsino Study



## This study

Demonstrate measurement precision of Higgsino masses and production cross sections

Masses and cross sections as input

## Determine SUSY parameters

e.g.  $M_1, M_2, \mu, \tan\beta$

S.-L. Lehtinen et al

### Why?

- To get info about unobserved sparticles
- To test GUT-scale models
- Global  $\chi^2$  fit of to observables

### How?

Study input parameters and required precision for parameter extraction; interplay with Higgs precision measurements

## Existing studies

### (1) "Tackling light higgsinos at the ILC", M. Berggren et al. [arXiv:1307.3566]

- $\sqrt{s} = 500 \text{ GeV}, \Delta M \sim 1 \text{ GeV} \rightarrow$  use ISR tag, , Based on full ILD simulation

### (2) "Physics at a Higgsino Factory", H. Baer et al. [arXiv:1404.7510]

- $\sqrt{s} = 250 \text{ (340)} \text{ GeV}$  for ILC1 (ILC2),  $\Delta M = 10-20 \text{ GeV}$ , detector effects based on resolution formula

## Ongoing studies

### Light Higgsinos with $\Delta M = 10 - 20 \text{ GeV}$ , J. Yan, T. Tanabe et al

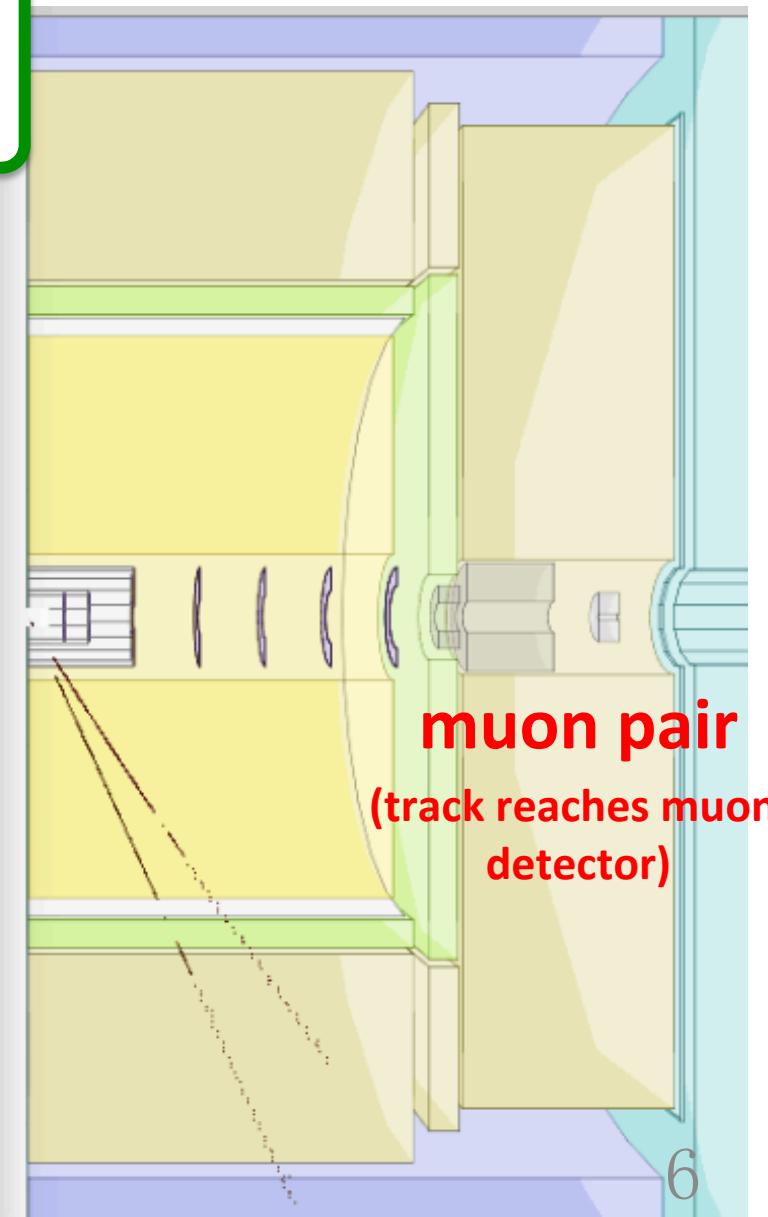
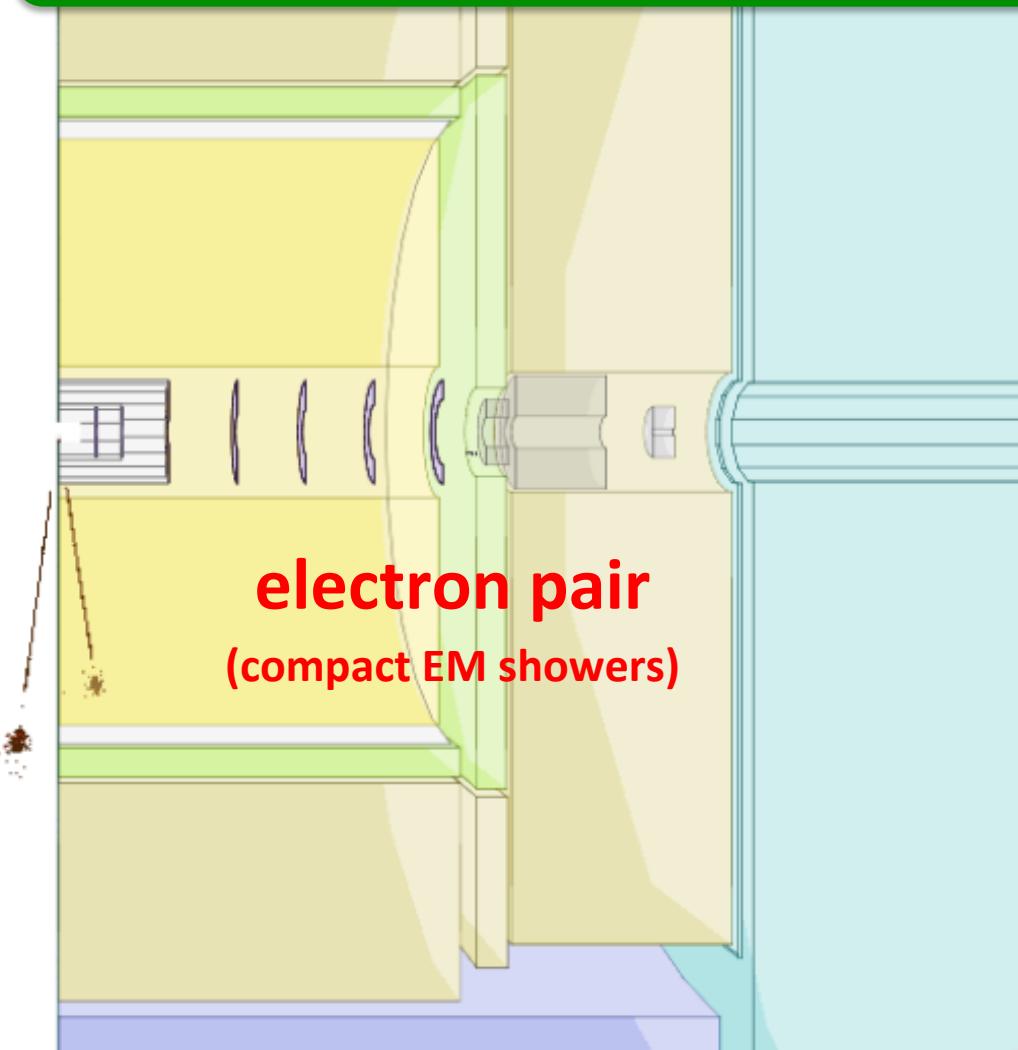
- $\sqrt{s} = 500 \text{ GeV}, \Delta M \sim 10-20 \text{ GeV}, \text{ Based on full ILD simulation}$

# How do these signals look in the detector? (1)

$\sqrt{s} = 500 \text{ GeV}$

Neutralino mixed production with leptonic decay

$$e^+ e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \ell^+ \ell^-$$

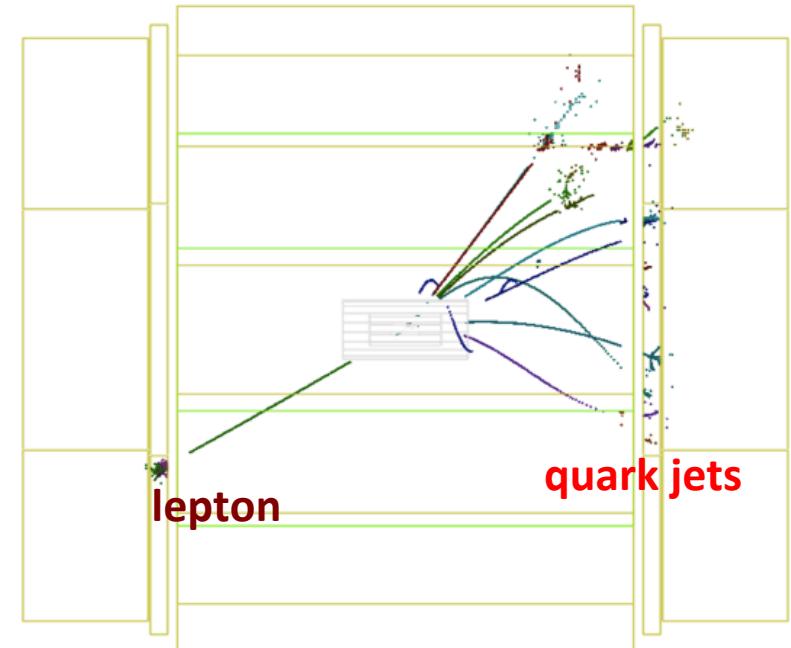
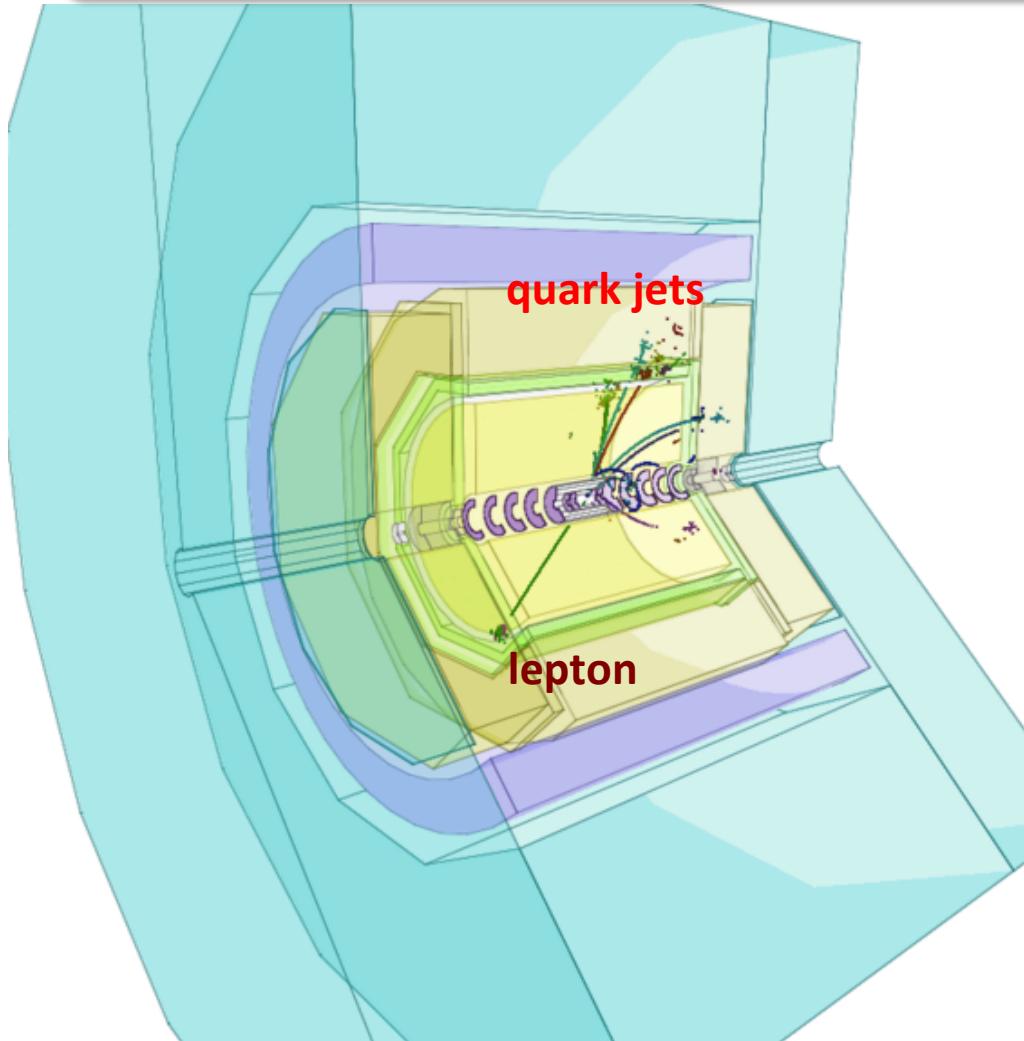


# How do these signals look in the detector? (2)

$\sqrt{s} = 500 \text{ GeV}$

Chargino pair production with semileptonic decay

$$e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 q \bar{q}' \ell \nu$$



# Event Selection

**Neutralino mixed production with leptonic decay**

$$e^+ e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \ell^+ \ell^-$$

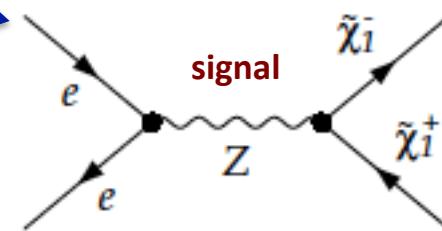
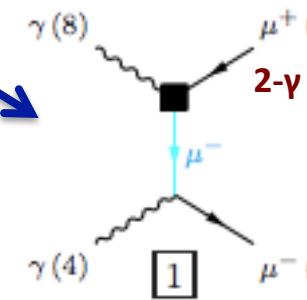
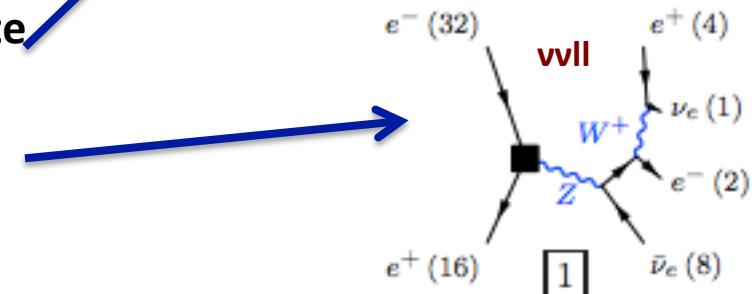
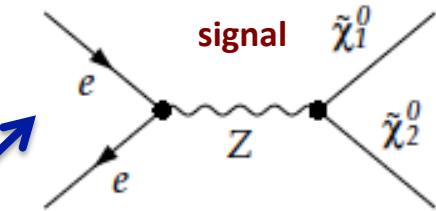
- Reconstruct **two leptons (ee or  $\mu\mu$ ) which originate from  $Z^*$  emission in decay of  $\tilde{\chi}_2^0$  to  $\tilde{\chi}_1^0$**
- Major residual bkg. are 4f processes accompanied by large missing energy (vvll)
- 2- $\gamma$  processes are removed by BeamCal veto, cuts on lepton track  $p_T$ , and coplanarity

**Chargino pair production with semileptonic decay**

$$e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 q \bar{q}' \ell \nu$$

- Reconstruct **two jets which originate from  $W^*$  emission in decay of  $\tilde{\chi}_1^\pm$  to  $\tilde{\chi}_1^0$**
- Use lepton ( $e$  or  $\mu$ ) from the other chargino as tag
- BeamCal veto, cuts on missing  $p_T$ , # of tracks, # of leptons, and coplanarity remove almost all bkg.

(signal significance  $> 100$ )



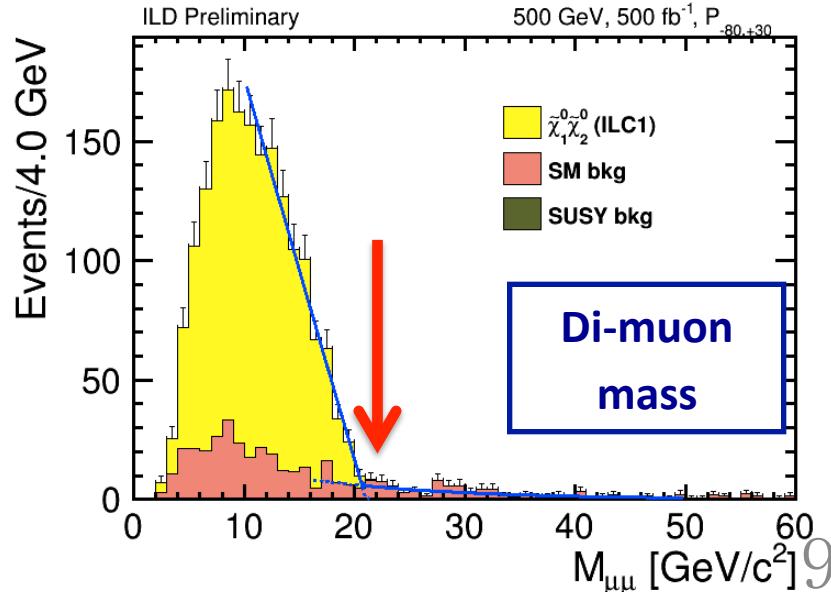
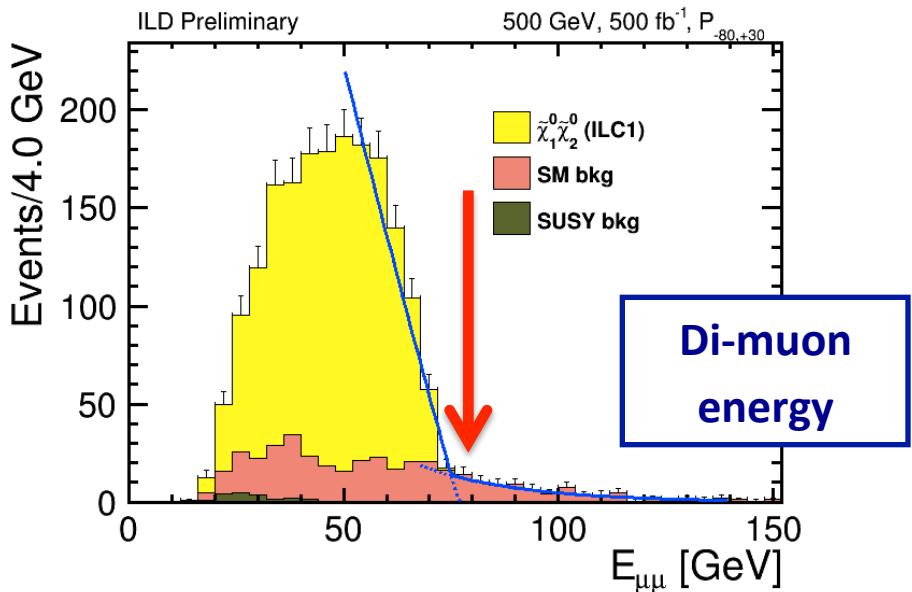
# Extraction of Higgsino Mass [work in progress]

Neutralino mixed production with leptonic decay

$$e^+ e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \ell^+ \ell^-$$

- The position of the kinematic edges of the dilepton energy ( $E_{||}$ ) and invariant mass ( $M_{||}$ ) are functions of CM energy and the two neutralino masses.
- The maximum values  $E_{||,\text{max}}$  and  $M_{||,\text{max}}$  are extracted by a fit to obtain the neutralino masses after correcting for detector/reconstruction effects`

Similar for case of chargino pair production ( $\text{II} \rightarrow \text{jj}$ )



Cuts have been designed so as not to destroy upper edge

- Use toy MC (generated from MC data fit) to evaluate statistical uncertainty
- Making progress in kinematic edge extraction

Edge extraction precision  $\sim 1\%$

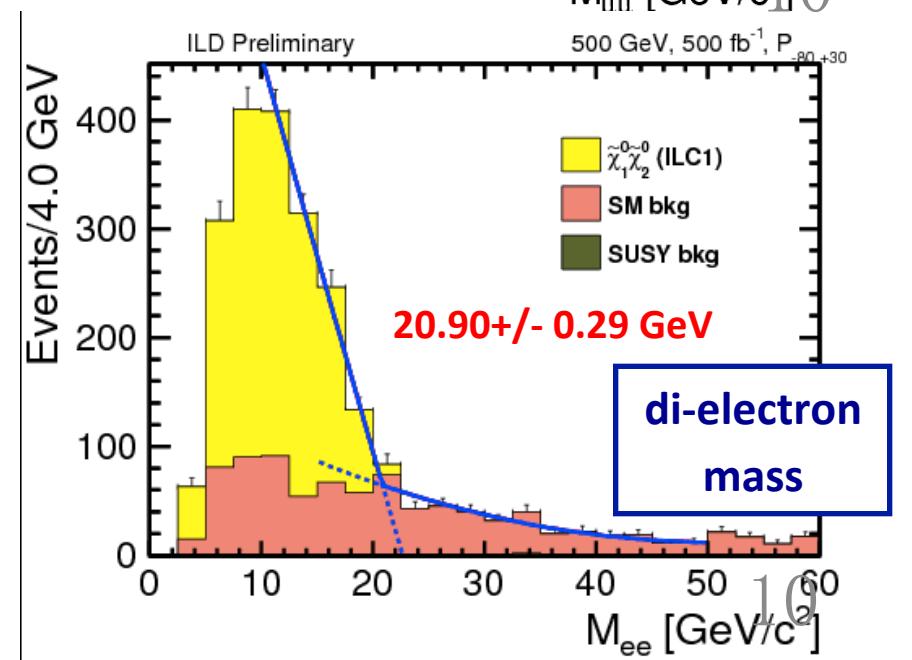
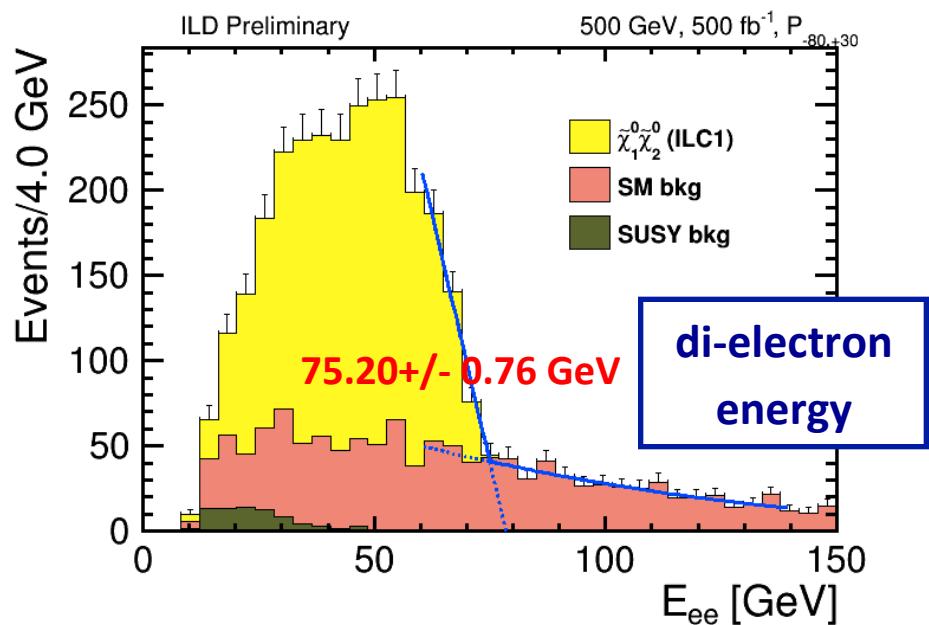
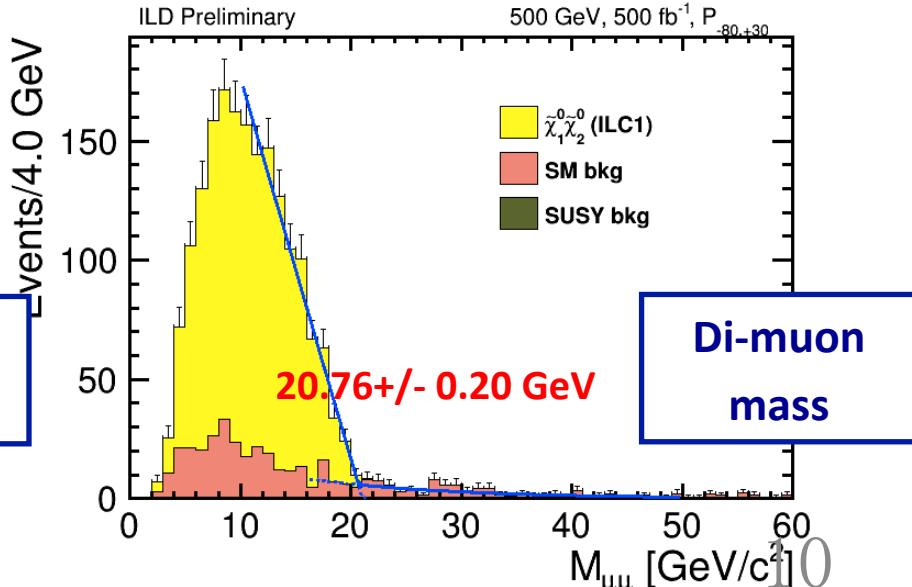
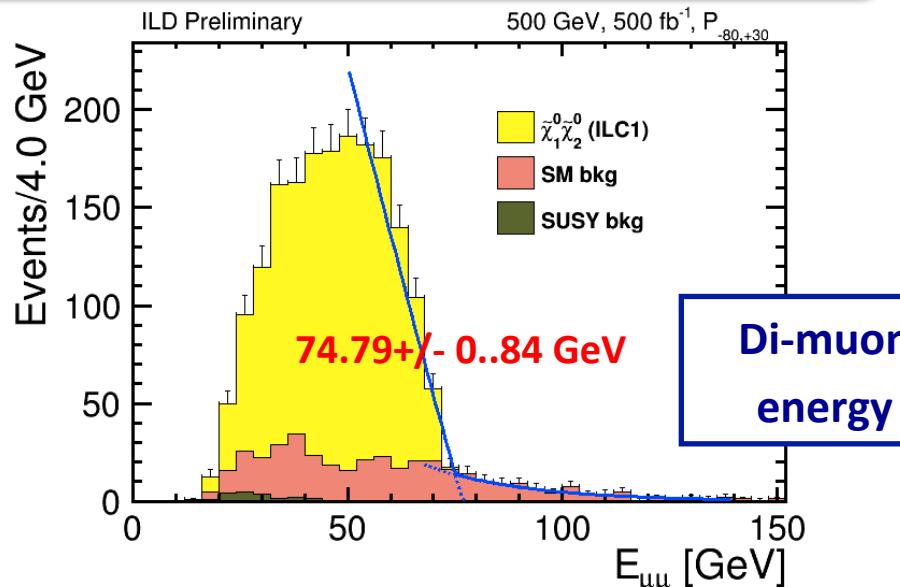
# Neutralino mixed production with leptonic decay

$$e^+ e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \ell^+ \ell^-$$

Polarization ( $\text{Pe}^-, \text{Pe}^+$ ) = (-0.8, +0.3)

statistical precision 1.0 – 1.5 %

preliminary



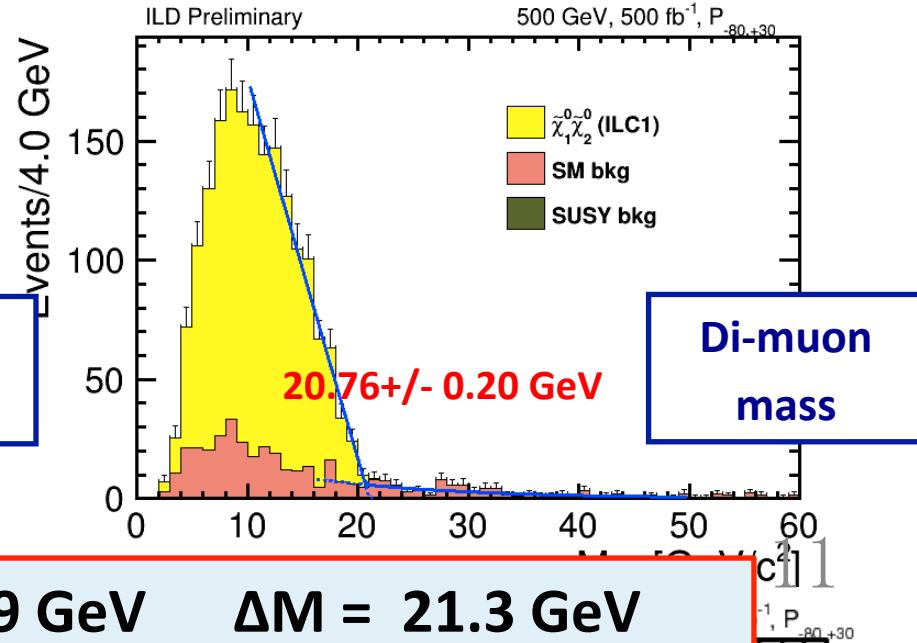
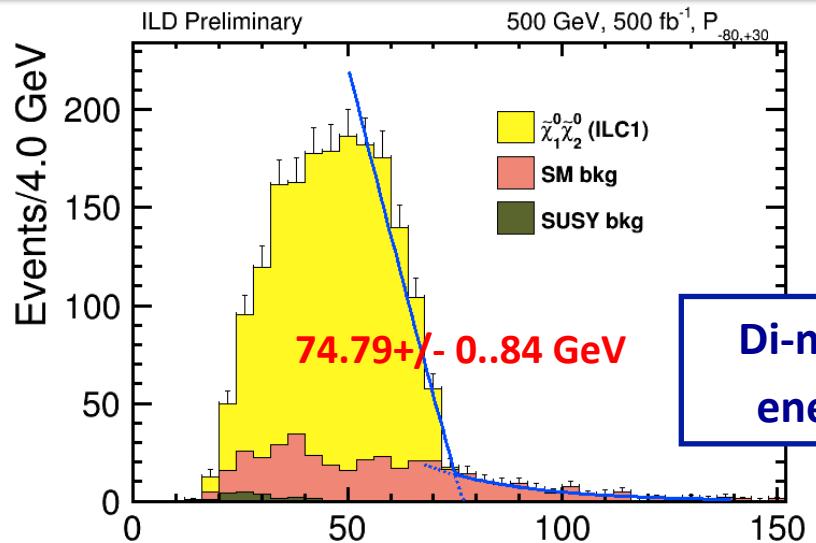
# Neutralino mixed production with leptonic decay

$$e^+ e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \ell^+ \ell^-$$

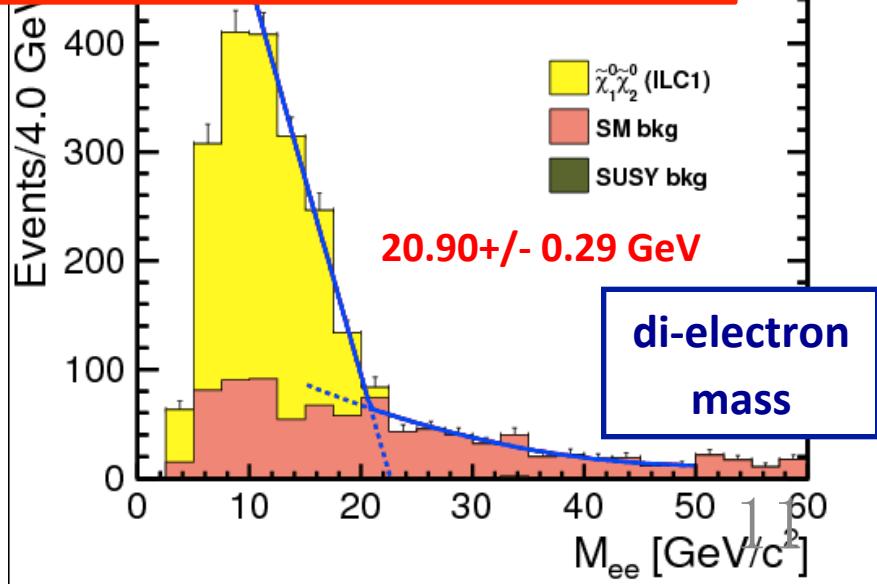
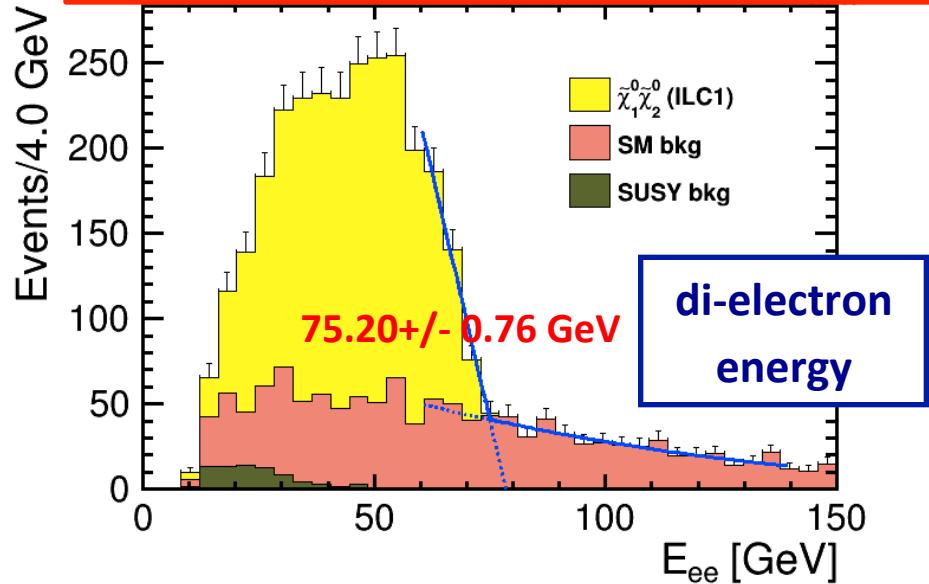
Polarization ( $\text{Pe}^-, \text{Pe}^+$ ) = (-0.8, +0.3)

statistical precision 1.0 – 1.5 %

preliminary

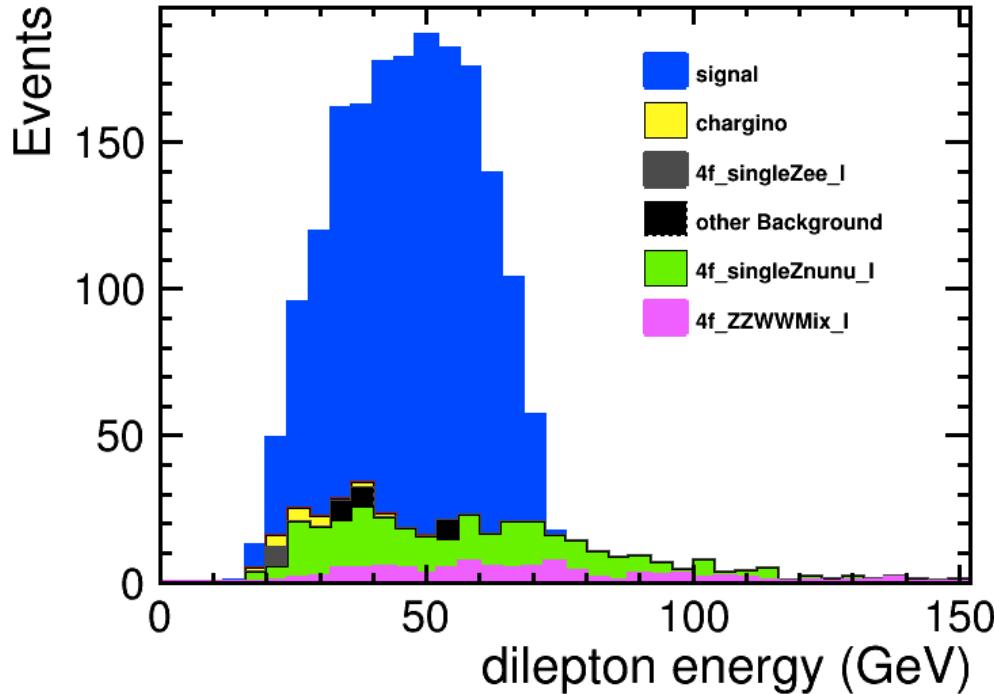


Theoretical values: E\_max = 74.9 GeV ΔM = 21.3 GeV



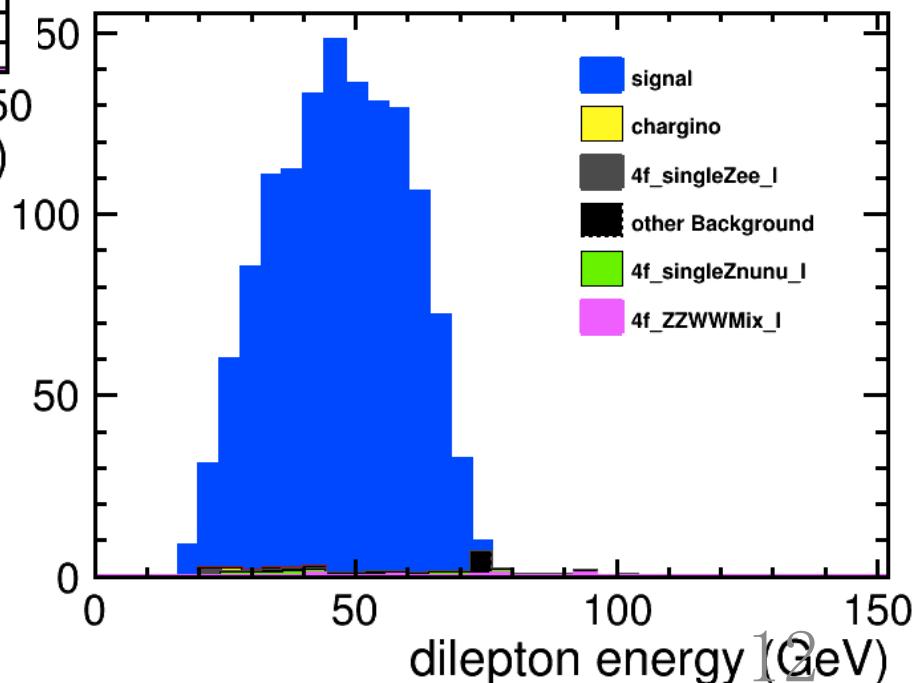
Di-muon energy

(Pe-,Pe+) = (-0.8, +0.3)



Background is greatly suppressed  
for right-hand polarization

Di-muon energy  
(Pe-,Pe+) = (+0.8, -0.3)

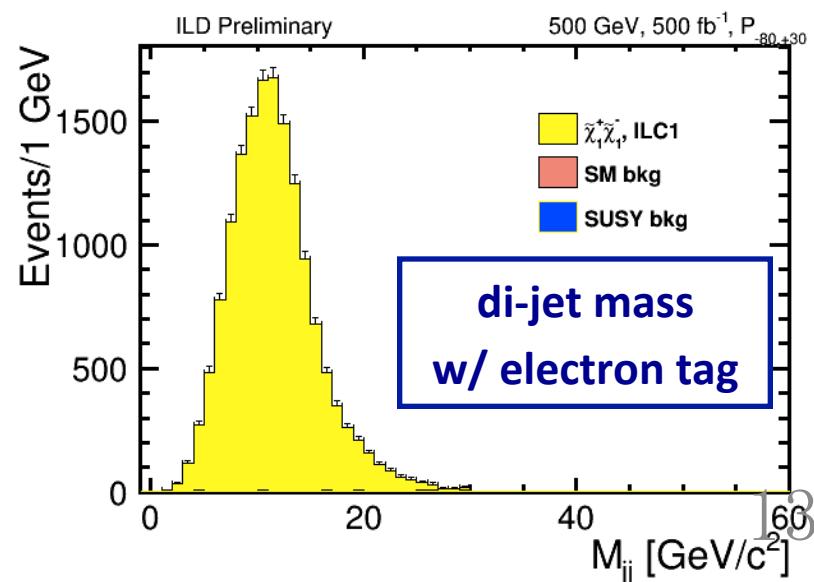
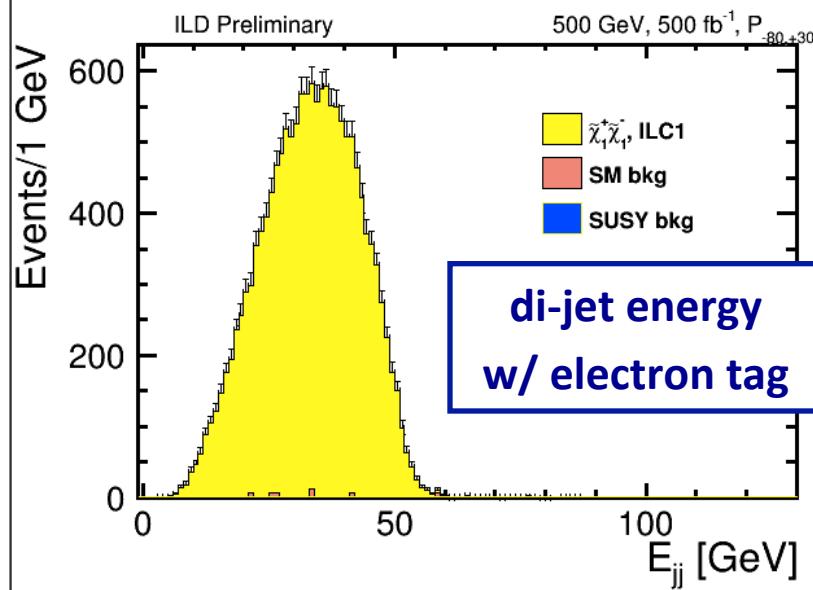
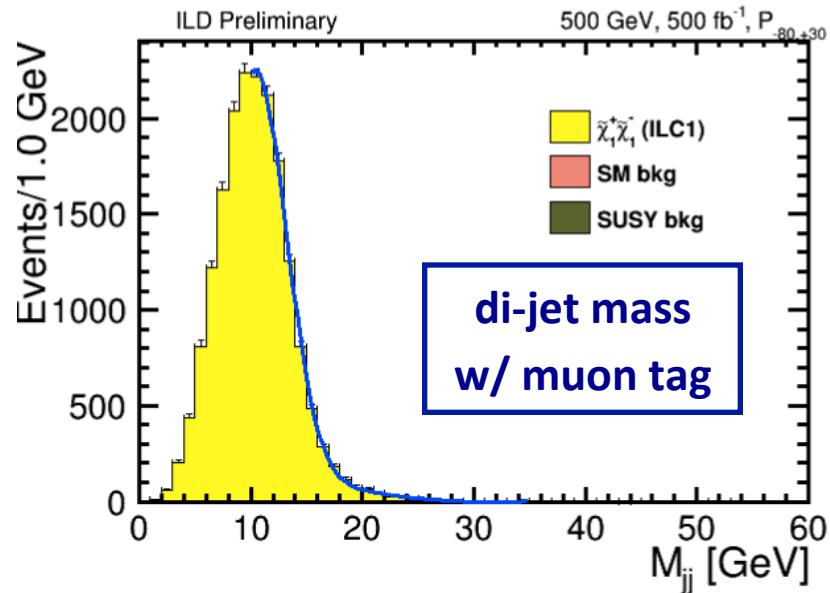
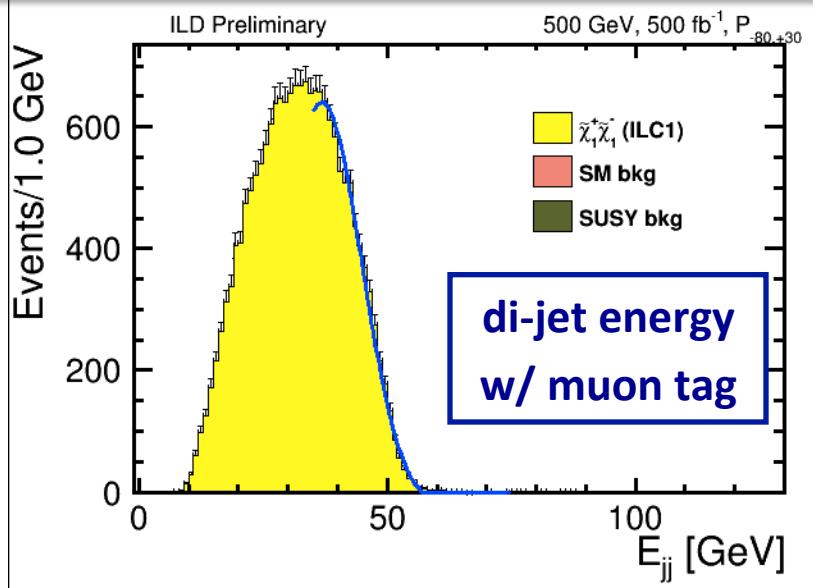


We will study the difference in statistical  
precisions of edge and cross sections

# Chargino pair production with semileptonic decay

$$e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 q\bar{q}' \ell\nu$$

Polarization (Pe-,Pe+) = (-0.8, +0.3)  
 SM and SUSY backgrounds  
 almost fully eliminated  
 preliminary



# Extraction of Cross Section [work in progress]

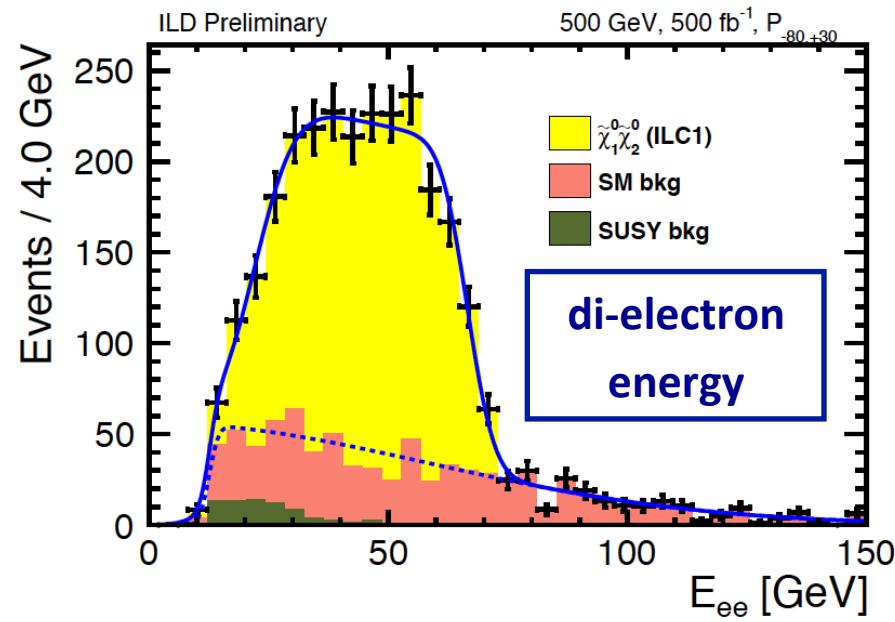
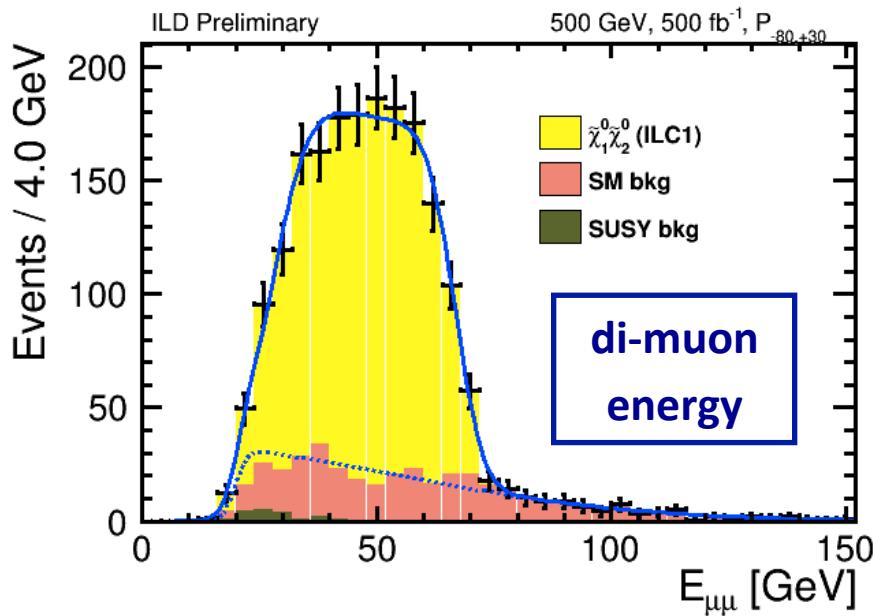
Strategy: Fit overall shape to estimate total number of signal events

Neutralino mixed production with leptonic decay

$$e^+ e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \ell^+ \ell^-$$

$$\Delta\sigma / \sigma = 3 - 5 \%$$

preliminary



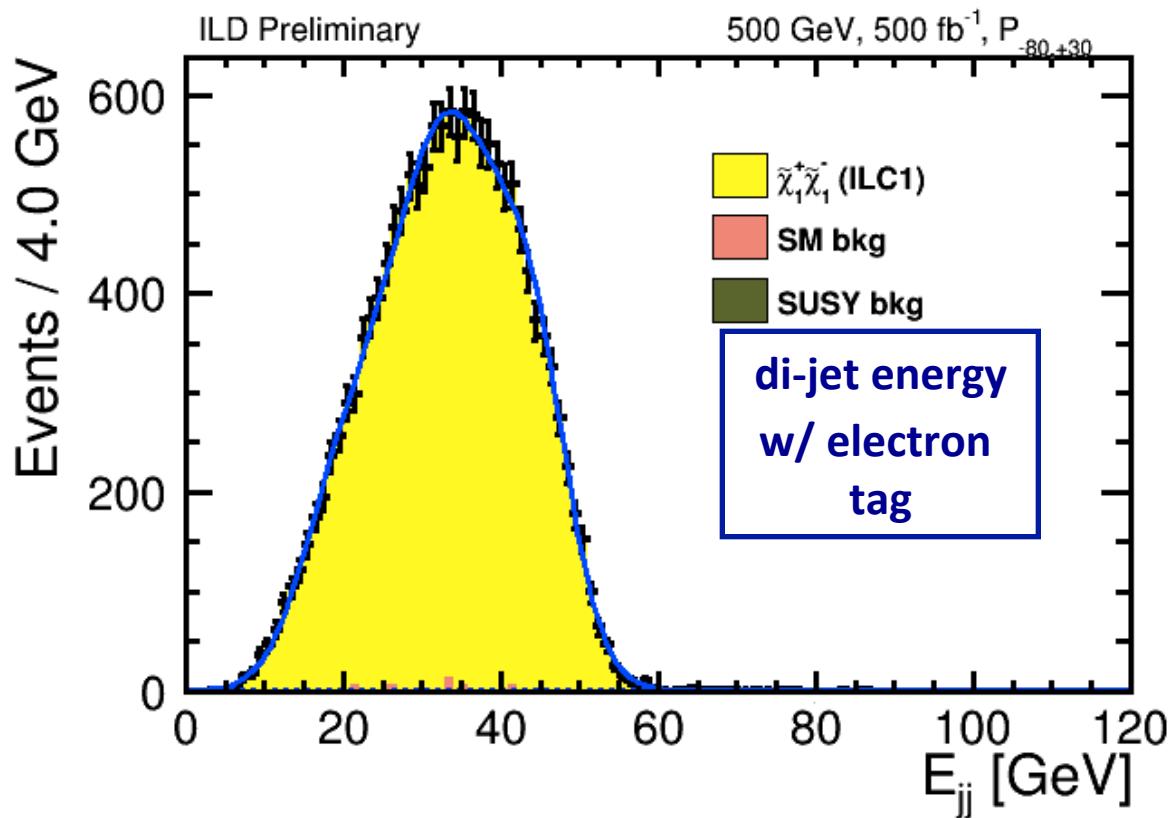
The results of Higgsino mass and cross section become input to the parameter fit to extract SUSY parameters (e.g. Wino and Bino masses, tanβ, etc.)

# Extraction of Cross Section [work in progress]

Chargino pair production with semileptonic decay

$$e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 q\bar{q}' \ell\nu$$

Polarization (Pe-,Pe+) = (-0.8, +0.3)



$\Delta\sigma / \sigma = 0.8 \%$

Fit with triple Gaussian

Other channels have similar shapes in the case of chargino

# Summary and Plans

## Precision measurement of light Higgsinos with small $\Delta M$ (10-20 GeV)

- Motivated by both experiment (complementary to LHC) and theory (naturalness)

This study: Full ILD detector simulation,  $L=500 \text{ fb}^{-1}$  at  $\sqrt{s} = 500 \text{ GeV}$ ,  $(P_{\text{e}-}, P_{\text{e}+}) = (-0.8, +0.3), (+0.8, -0.3)$

- Analysis of neutralino mixed production ( $\chi_1^0 \chi_2^0$ ) and chargino pair production ( $\chi_1^+ \chi_1^-$ )
- Data selection yields good S/B ratio ; almost no background for chargino
- Fit kinematic edges to extract Higgsino masses
- Fit to overall distribution to extract production cross sections in progress

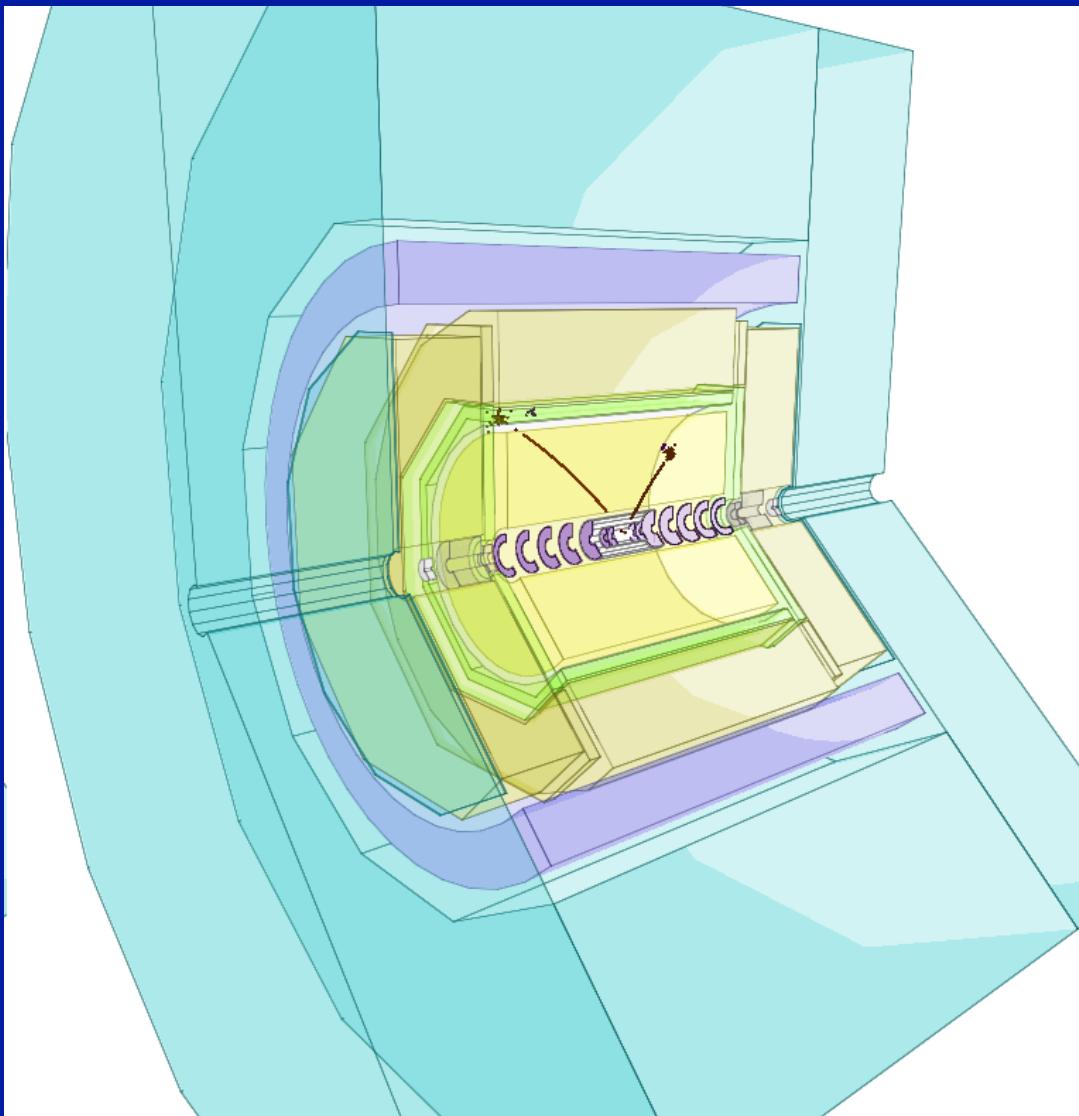
## Obtained preliminary results for some channels

- For neutralino: Edge precision 1.0 -1.5% , Cross section precision 3-5%
- Edge values generally consistent with theoretical values within uncertainty range
- For chargino : Cross section precision : 0.8%
- Still working on edge extraction : difficulties involving jet energy resolution
- Need to implement gamma gamma overlay bkg
- Other CM energies and polarizations: precise mass determination, input necessary for theoretical studies, etc...

results obtained in this study become input to SUSY parameter determination

To test GUT-scale physics and SUSY-breaking mechanism [S.-L. Lehtinen, in progress]

# Thank you for listening



# **Additional Material**

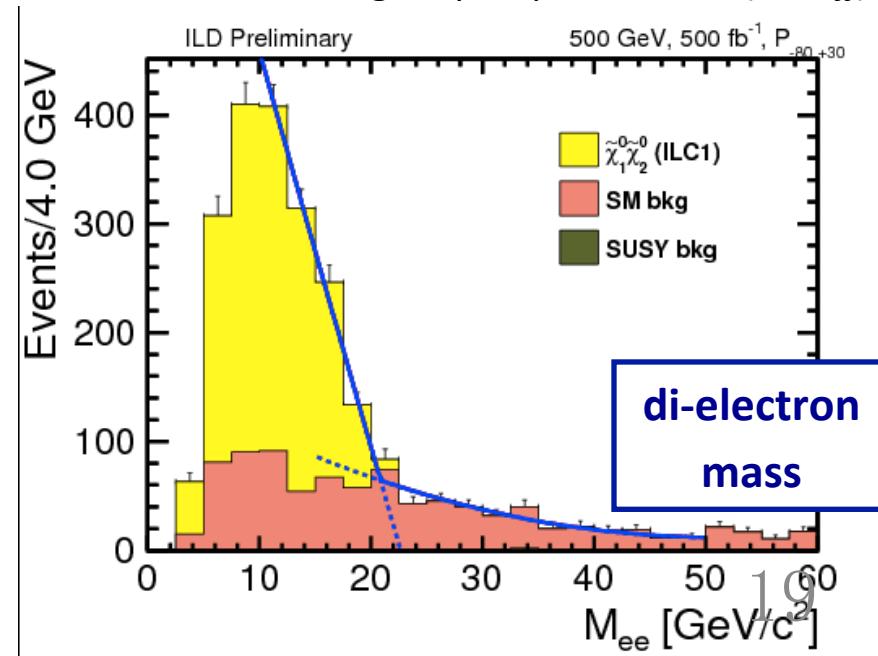
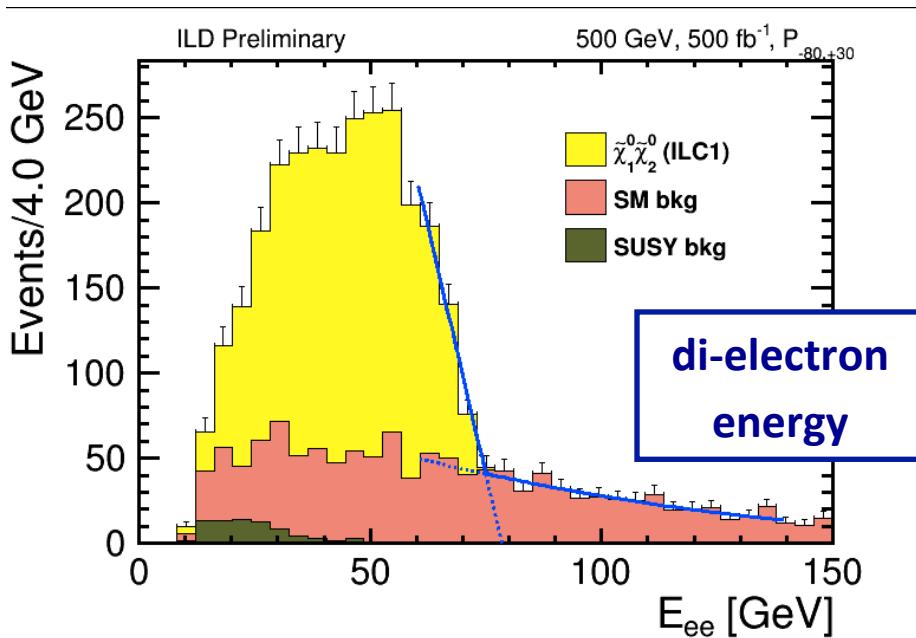
# Extraction of Higgsino Mass [work in progress]

Neutralino mixed production with leptonic decay

$$e^+ e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \ell^+ \ell^-$$

- The position of the kinematic edges of the dilepton energy ( $E_{||}$ ) and invariant mass ( $M_{||}$ ) are functions of CM energy and the two neutralino masses.
- The maximum values  $E_{||,\text{max}}$  and  $M_{||,\text{max}}$  are extracted by a fit to obtain the neutralino masses after correcting for detector/reconstruction effects`

Similar for case of chargino pair production ( $ll \rightarrow jj$ )



Cuts have been designed so as not to destroy upper edge

- Use toy MC (generated from MC data fit) to evaluate statistical uncertainty
- Making progress in kinematic edge extraction

# Fits of NUHM2 Parameters

ILC2

All 6 parameters are simultaneously varied.  
Initial values are set to be near the model  
values.

Each blue point corresponds to a set of  
parameter values. The  $\chi^2$  value is computed  
for each point.

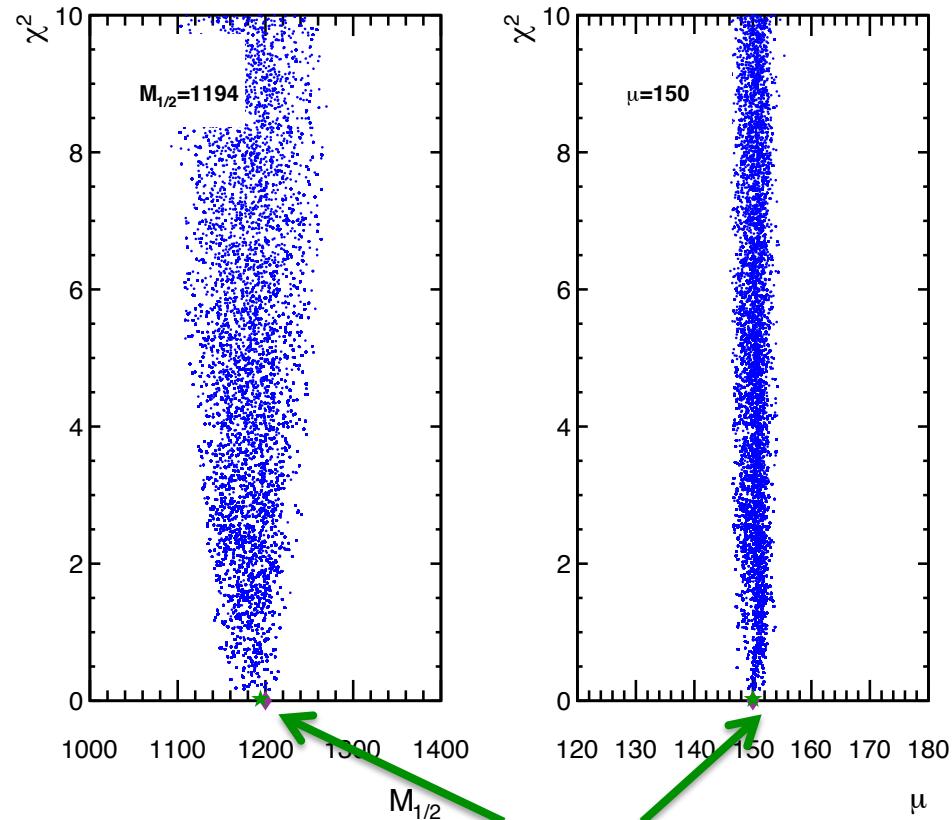
Using the  $\chi_1^0$ ,  $\chi_2^0$ ,  $\chi_1^\pm$  masses and production  
cross sections,  $M_{1/2}$  can be determined.

Adding Higgs mass and BR as measured at  
the ILC fixes  $\mu$  and possibly constrains  
other parameters

In addition, if  $\chi_3^0$  can be observed in  $\chi_2^0\chi_3^0$ ,  
 $\tan\beta$  can be constrained as well. (ILC1)

## Outlook

- Test gaugino mass unification by fitting weak scale parameters  $M_1$  and  $M_2$



Diamond = model point

Star = best fit point

# ILC1

Cross sections (pure beam polarizations)  
 $\sqrt{s}=500$  GeV with TDR beam parameters

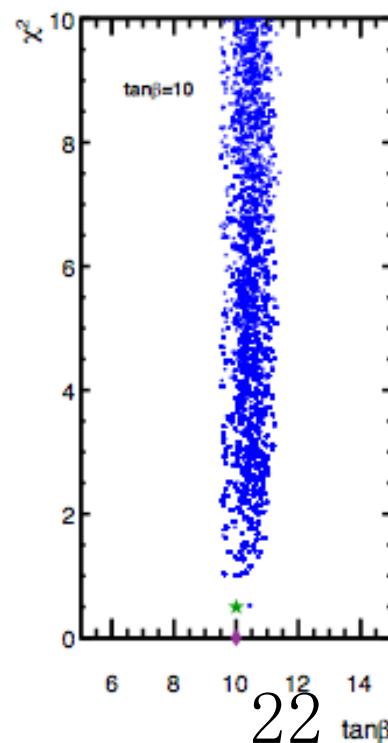
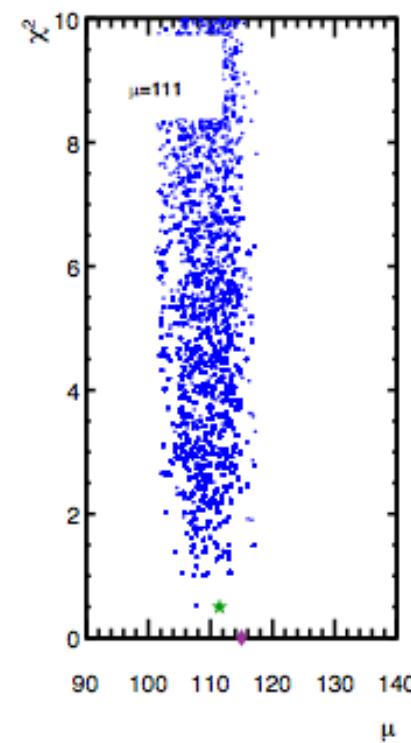
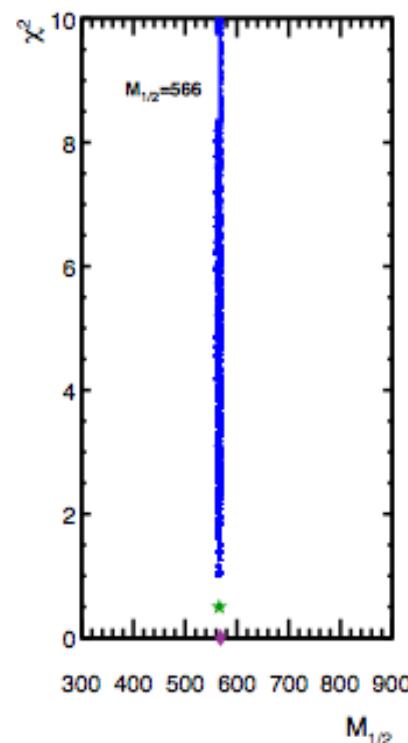
(Pe-, Pe+)	(-1.0,+1.0)	(+1.0,-1.0)
$\sigma(\chi_1^+ \chi_1^-)$ [fb]	1800	335
$\sigma(\chi_1^0 \chi_2^0)$ [fb]	491	379
$\sigma(\chi_2^0 \chi_3^0)$ [fb]	11.0	8.42
$\sigma(\chi_1^0 \chi_1^0)$ [fb]	2.03	1.56
$\sigma(\chi_2^0 \chi_2^0)$ [fb]	0.53	0.41
$\sigma(\chi_1^0 \chi_3^0)$ [fb]	0.28	0.20

Branching ratios

$BR(\chi_1^+ \rightarrow \chi_1^0 qq')$	67%
$BR(\chi_1^+ \rightarrow \chi_1^0 l\nu)$ ( $l=e,\mu$ )	22%
$BR(\chi_2^0 \rightarrow \chi_1^0 qq')$	58%
$BR(\chi_2^0 \rightarrow \chi_1^0 ll)$ ( $l=e,\mu$ )	7.4%

parameter	scale	ILC1
$m_0$	GUT	7025
$m_{1/2}$	GUT	568.3
$A_0$	GUT	-10426.6
$\tan \beta$	weak	10
$\mu$	weak	115
$m_A$	weak	1000

- $\tan\beta$  constrained if we add  $\chi_3^0$  mass and  $\chi_1^0\chi_3^0$  production cross section



# Cut table N1N2 , $\mu\mu$ (Pe-, Pe+) = (-80,+30)

	sig	bkg	4f_I	aa_2f	ae_3f	SUSY bkg
xsec	300.8	3.00E6	10566.2	2.68E6	261580	1065.2
N_gen	150395	1.50E9	5.28E6	1.34E9	1.31E8	532585
Lep_type nTrack=2	1974	9.1E8	444255	8.9E8	2.2E7	2426
BCAL veto	1950	6.0E6	149871	5.5E6	965354	2411
Pt_lep,1,2	1675	2.0E6	105721	1.4E6	295459	1986
cosθ_lep	1624	1.3E6	56001	910330	167734	1950
coplanarity	1407	48366	5272	3509	33067	22
Evis	1404	14325	2465	2248	4743	22
Emis, cosθmis	1393	1063	929	34	9	19
cosZ, Pt_ll, Minv	1393	545	429	34	9	19 23

# Cut table C1C1 , $\mu$ tag (Pe-, Pe+) = (-80,+30)

	sig	bkg	4f_I	aa_2f	ae_3f	SUSY bkg
Xsec [fb]	1065.2	3.00E6	10566.2	2.68E6	261580	300.8
N_gen	532585	1.50E9	5.28E6	1.34E9	1.31E8	150395
nLep=1 BCAL veto	57983	1.5E9	443296	1.2E6	860530	1135
Ptmis	38240	2.7E6	377010	465397	519308	964
Jet_coplanarity	26085	1.5E6	86399	83683	109325	531
Jet_cosθ nTrack (per jet) > 1	14612	305870	3066	555	2234	22
cosθjet-lep Evis	14308	3753	791	100	41	0
Emis, cosθmis	14231	83	57	3	0	0
Pt_jj, M_jj	14173	51	31	3	0	0