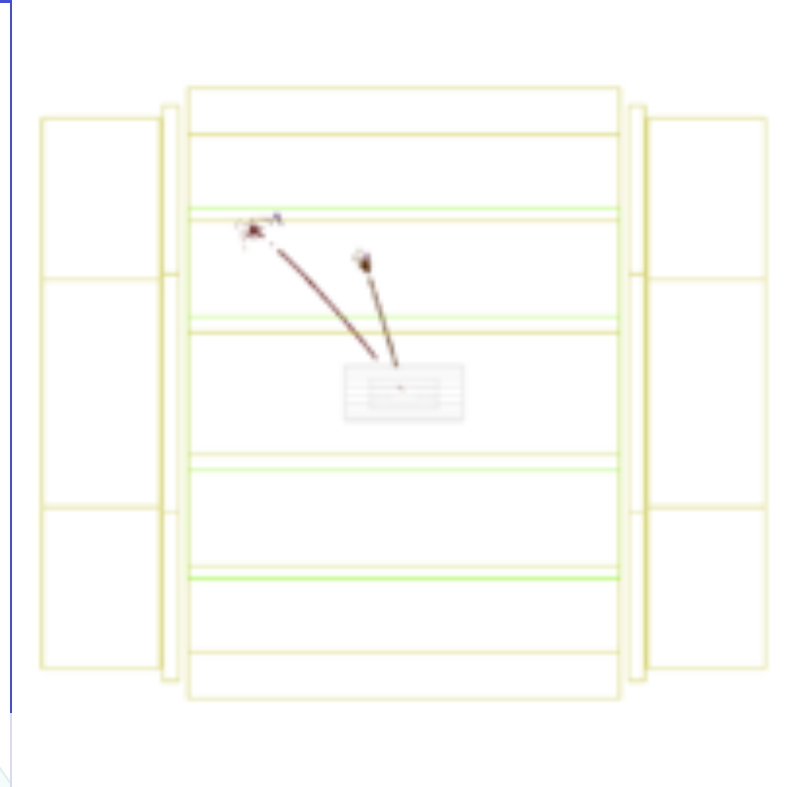
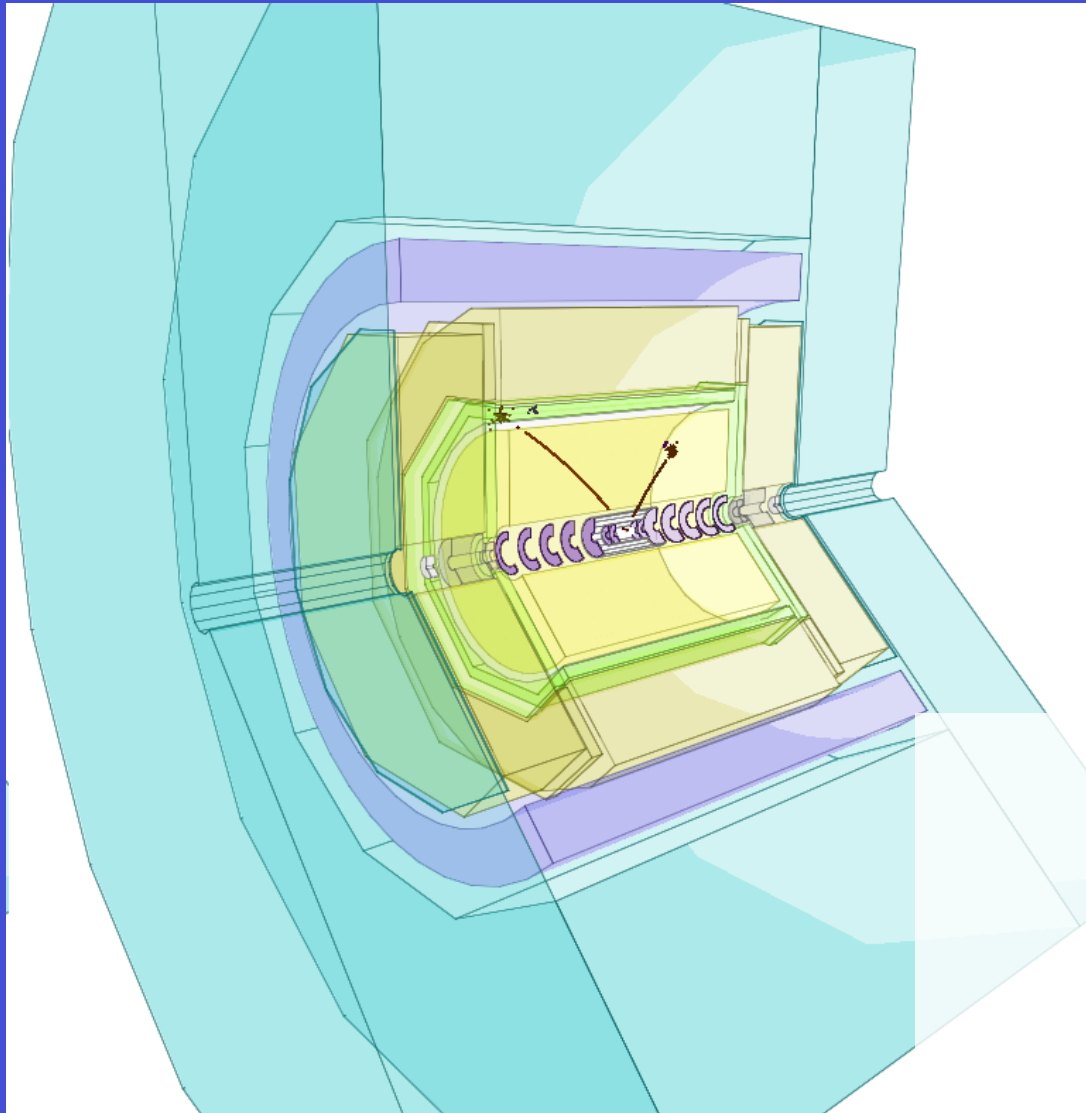


# Characterizing Light Higgsinos from Natural SUSY at ILC $\sqrt{s} = 500$ GeV



Jacqueline Yan (KEK)

Friday Meeting

8/19/2016

# Outline

- ◆ Update on edge and xsec extraction
  - now using new full sim samples
  - Extracted kinematic edge and cross section for just about all channels,  
both polarizations
- ◆ calculated propagation of uncertainty of observables to Higgsino mass
- ◆ Plans

# Extraction of Higgsino Mass

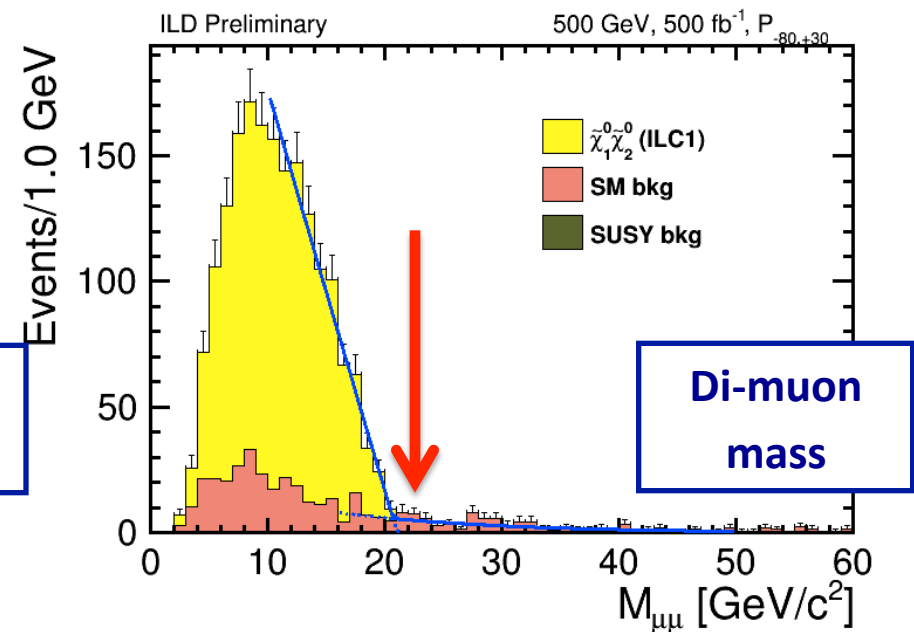
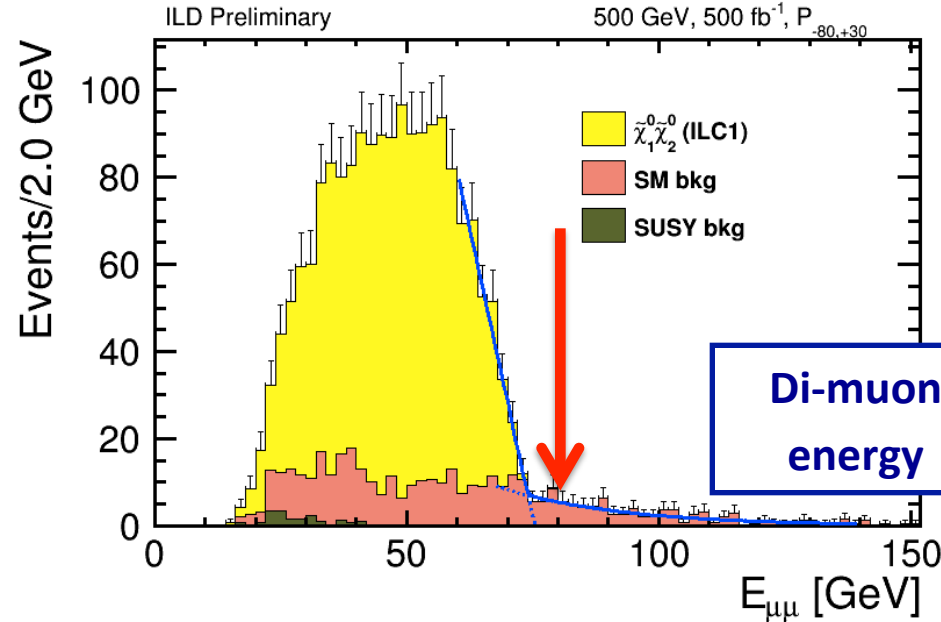
*Almost done*

Neutralino mixed production with leptonic decay

$$e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \ell^+ \ell^-$$

- The position of the kinematic edges of the dilepton energy ( $E_{ll}$ ) and invariant mass ( $M_{ll}$ ) are functions of CM energy and the two neutralino masses.
- The maximum values  $E_{ll,max}$  and  $M_{ll,max}$  are extracted by a fit to obtain the neutralino masses after correcting for detector/reconstruction effects`

Similar for case of chargino pair production ( $ll \rightarrow jj$ )



Edge precision  $\sim 1\%$

Cuts have been designed so as not to destroy upper edge

- Use toy MC (generated from MC data fit) to evaluate statistical uncertainty
- Making progress in kinematic edge extraction

# Edge extraction

*What has been changed since last time (July 13)*

**Optimized method for extraction of edge and cross section**

- Modeling of complex signal and bkg distributions (energy , invariant mass)
- Bin width, fitting range

**Still fine tuning in aim of better precision**

e.g. Loosen cuts for edge extraction, tighter cuts for cross section extraction (?)

**Now using full simulation bkg samples**

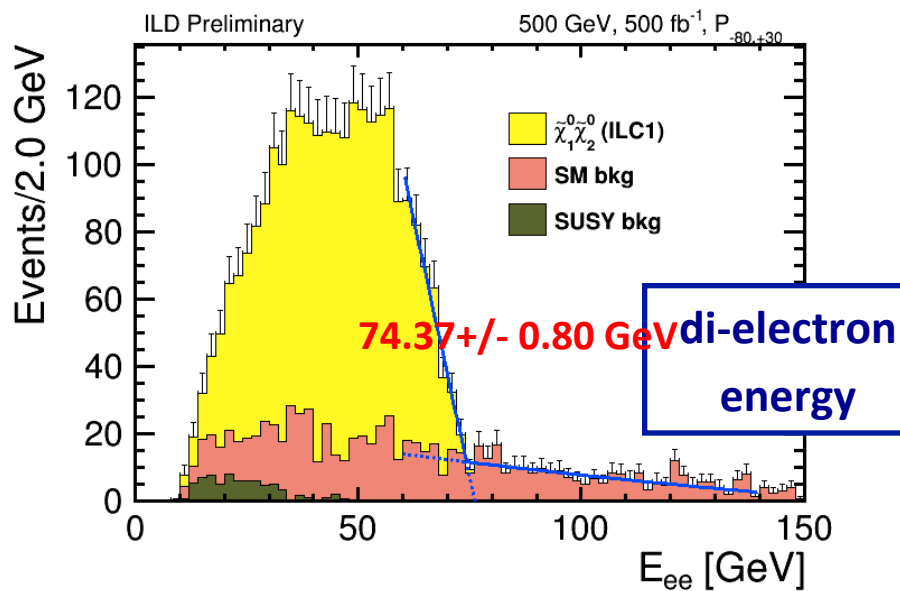
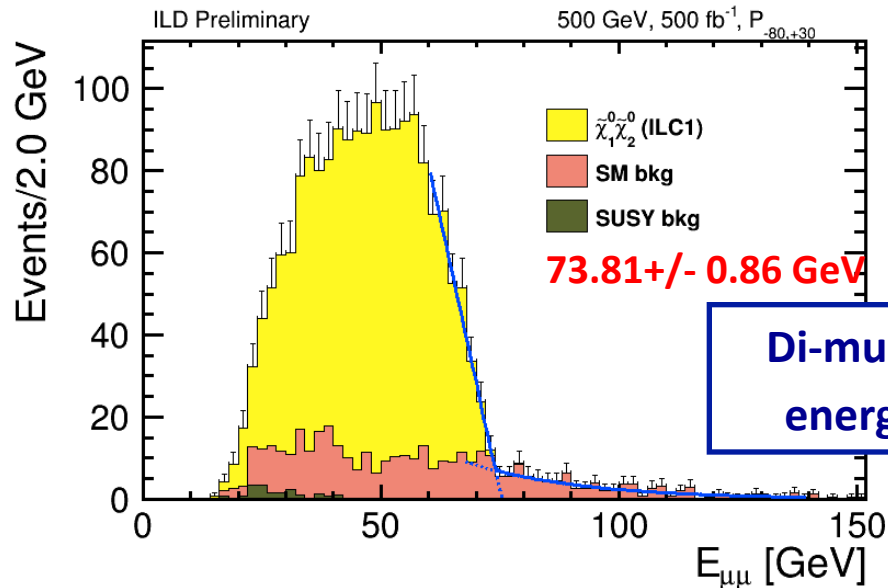
(thanks to Miyamoto-san and others in the software group)

Took a while to check the samples and interpret difference between SGV

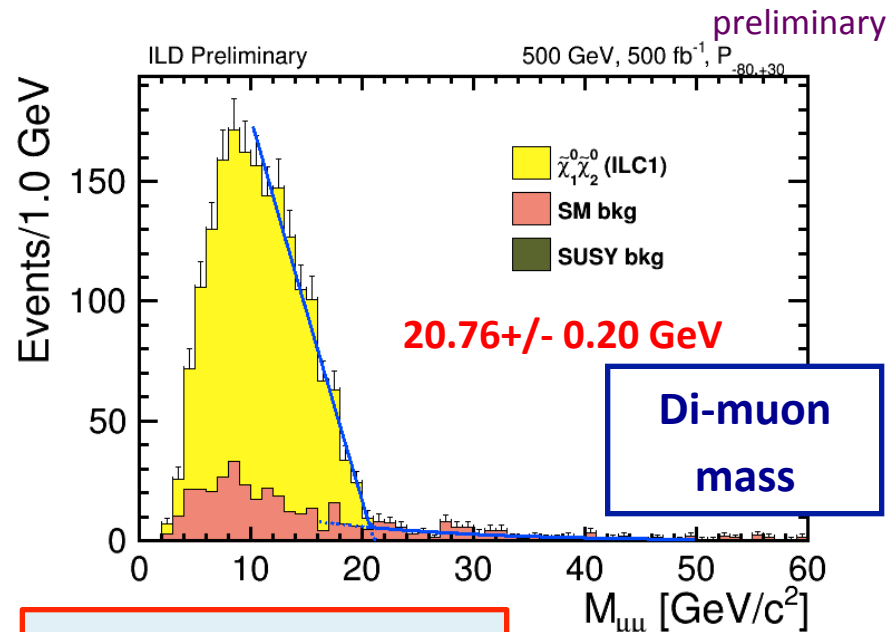
**Analysis has been done for right-handed polarization as well.**

# Neutralino mixed production with leptonic decay

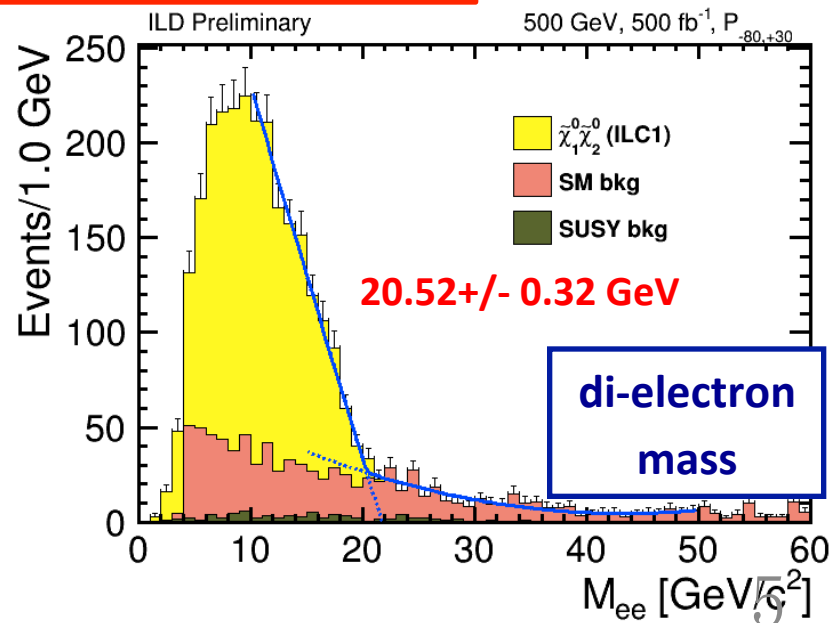
$$e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 l^+ l^-$$



# Polarization (P<sub>e-</sub>, P<sub>e+</sub>) = (-0.8, +0.3)



**Edge precision ~ 1%**

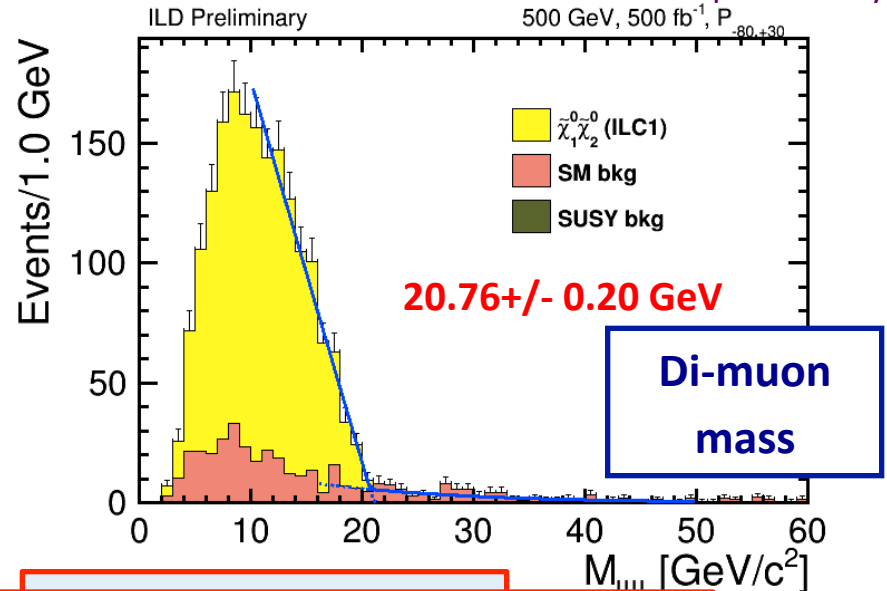
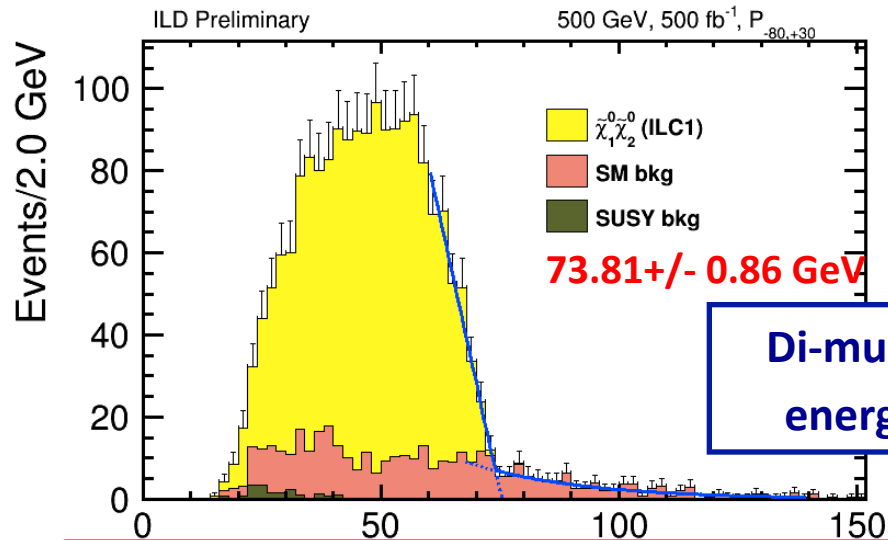


**Neutralino mixed production with leptonic decay**

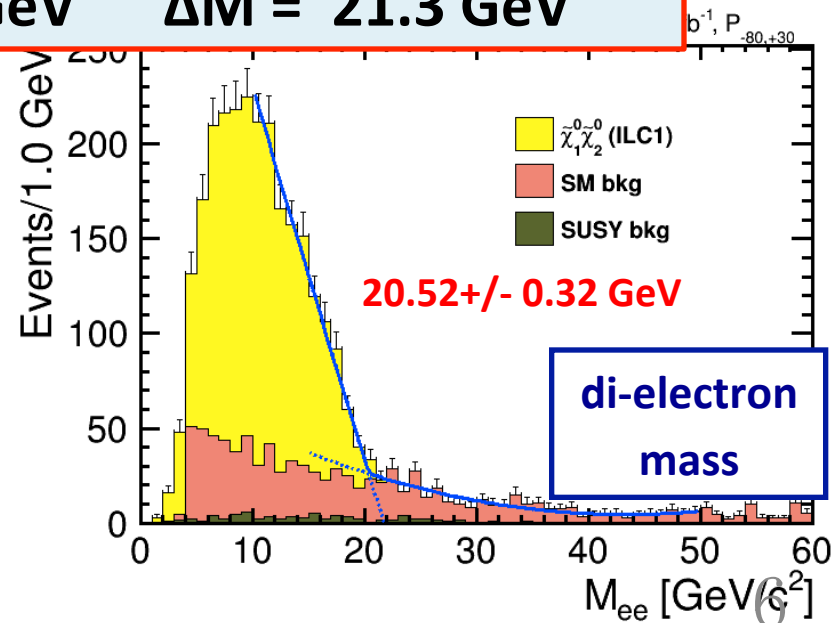
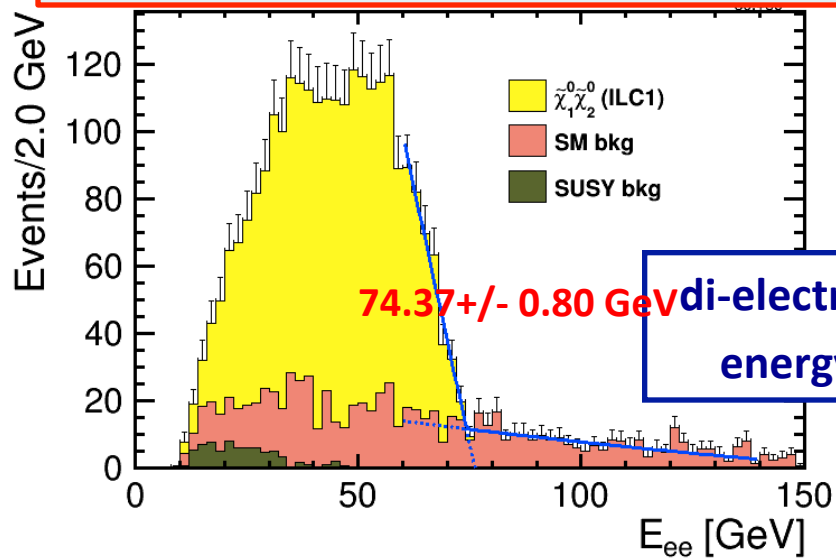
$$e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 l^+ l^-$$

**Polarization (P<sub>e-</sub>, P<sub>e+</sub>) = (-0.8, +0.3)**

preliminary



**Theoretical values: E<sub>max</sub> = 74.9 GeV ΔM = 21.3 GeV**

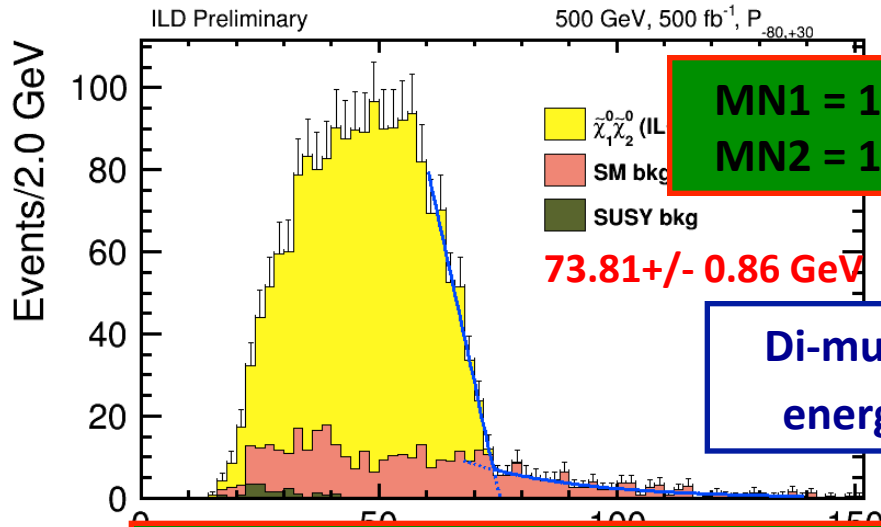


**Neutralino mixed production with leptonic decay**

$$e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 l^+ l^-$$

**Polarization (P<sub>e-</sub>, P<sub>e+</sub>) = (-0.8, +0.3)**

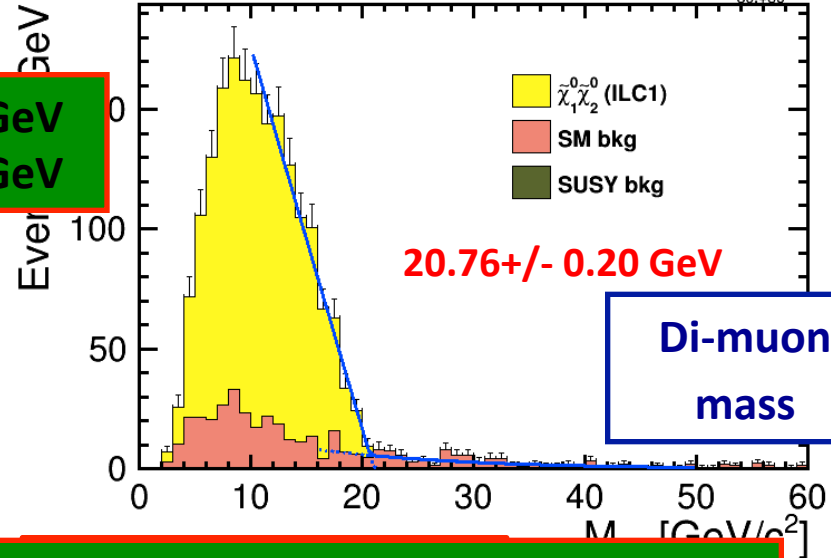
preliminary



**73.81 +/- 0.86 GeV**

**MN1 = 102.3 GeV  
MN2 = 123.0 GeV**

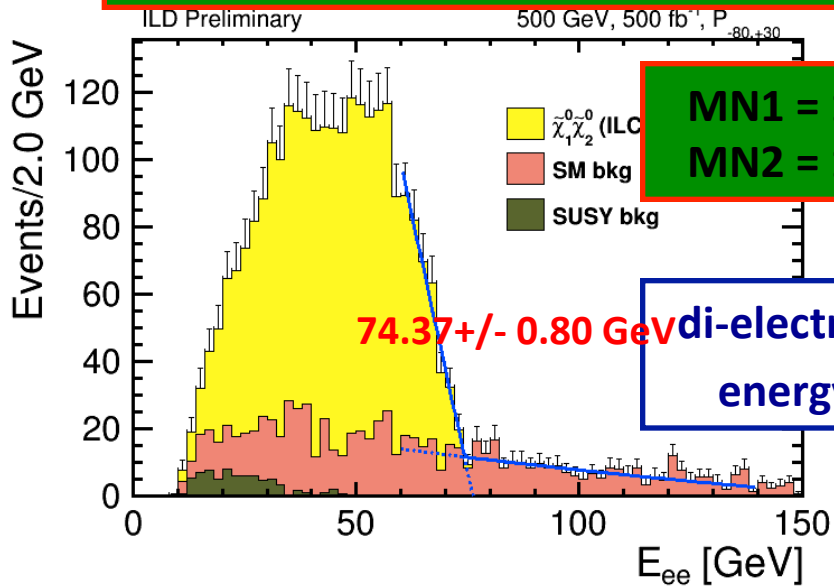
**Di-muon  
energy**



**20.76 +/- 0.20 GeV**

**Di-muon  
mass**

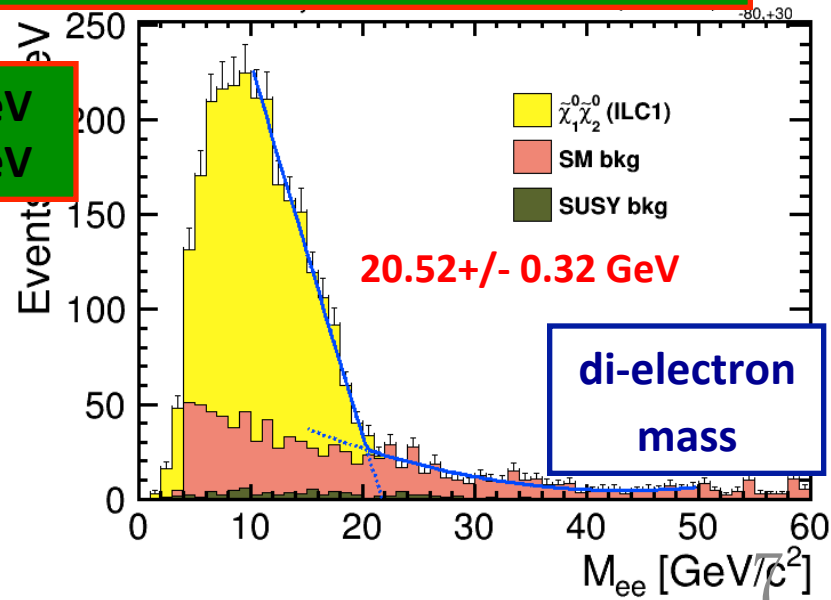
**Theoretical values: MN1 = 102.7 GeV MN2 = 124.0 GeV**



**74.37 +/- 0.80 GeV**

**MN1 = 100.3 GeV  
MN2 = 120.8 GeV**

**di-electron  
energy**



**20.52 +/- 0.32 GeV**

**di-electron  
mass**

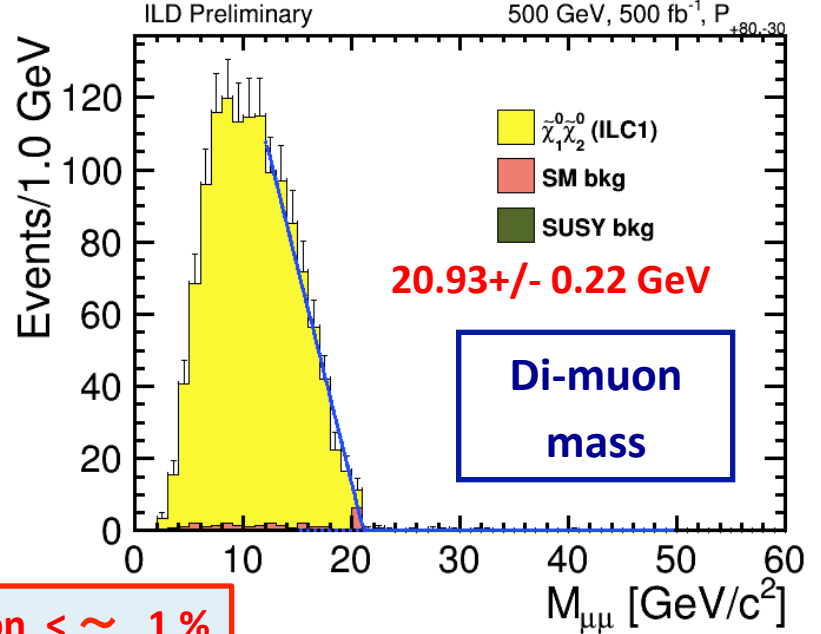
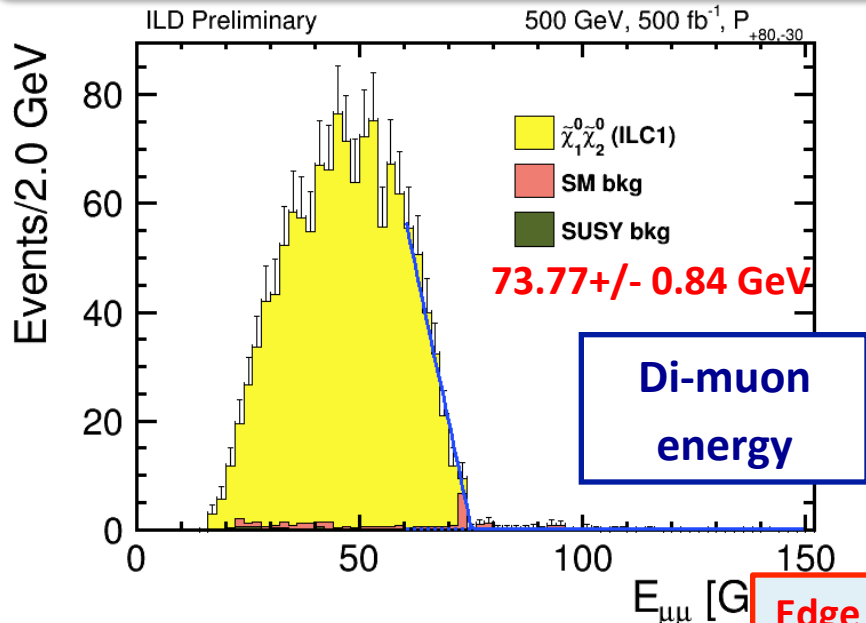
**Neutralino mixed production with leptonic decay**

$$e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 l^+ l^-$$

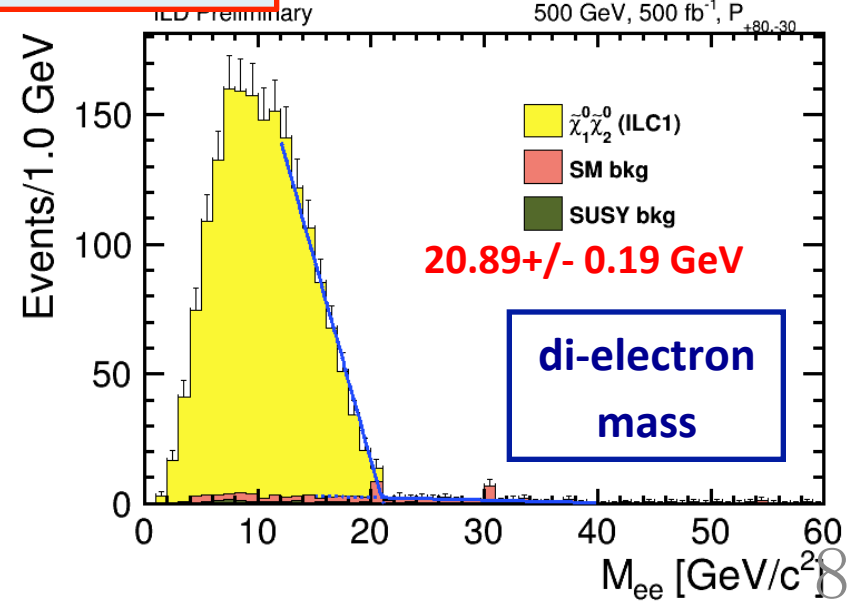
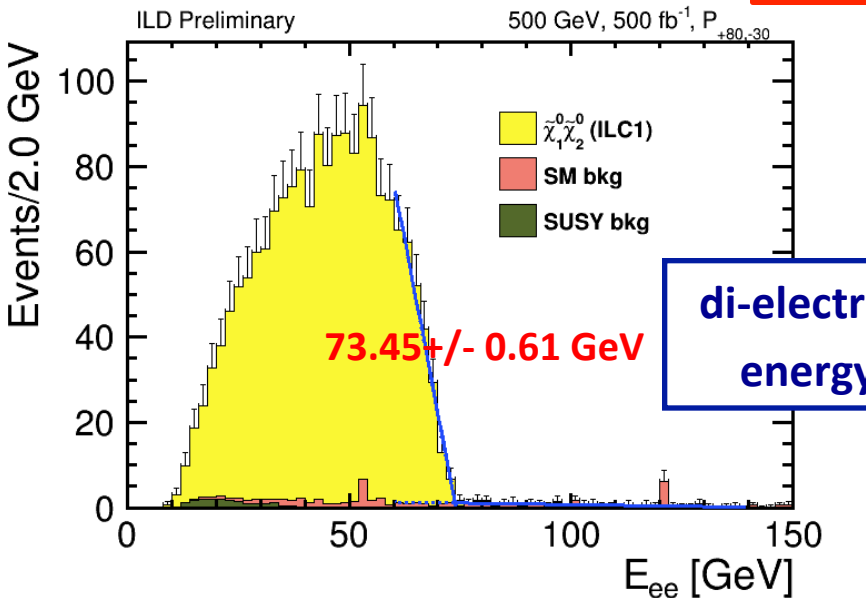
**Polarization (Pe-,Pe+) = (+0.8, -0.3)**

**Much less bkg**  
**Precision slightly better (?)**

preliminary



**Edge precision < ~ 1%**





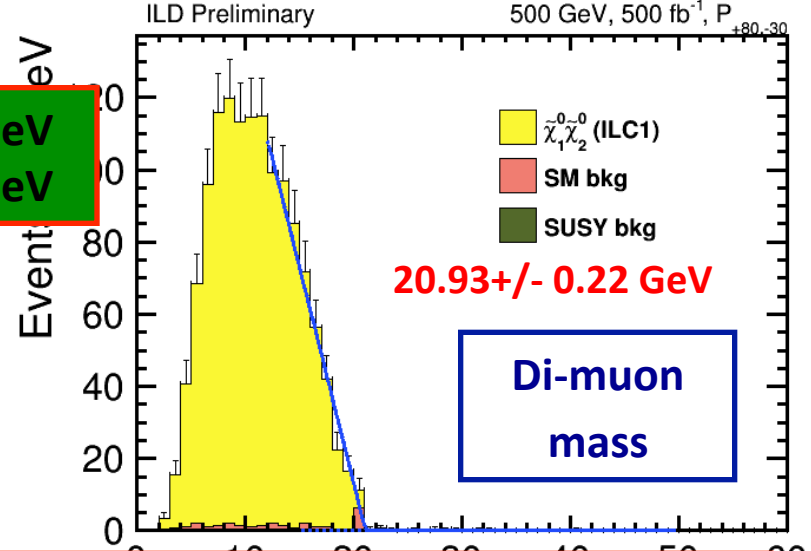
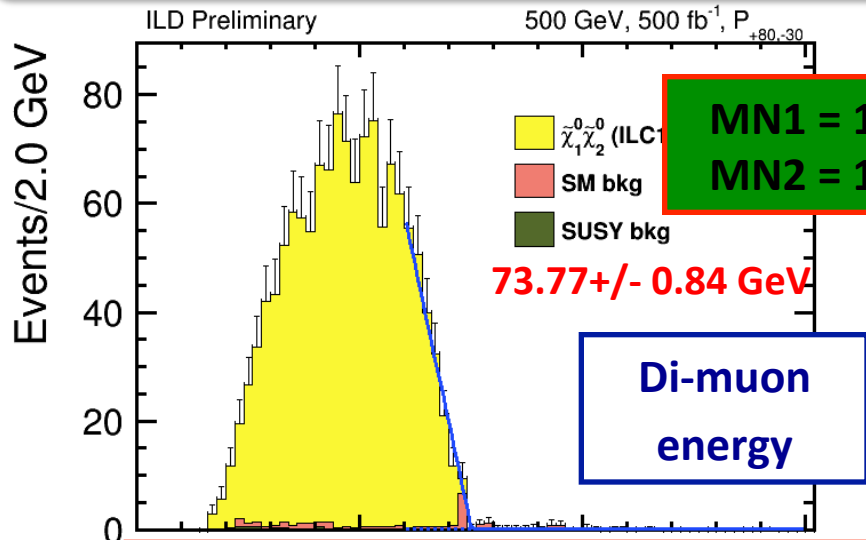
**Neutralino mixed production with leptonic decay**

$$e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 l^+ l^-$$

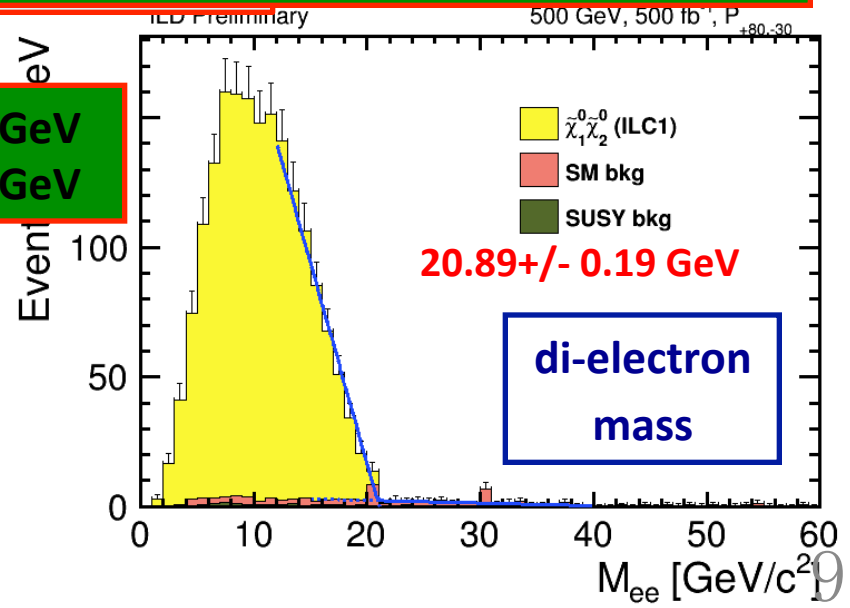
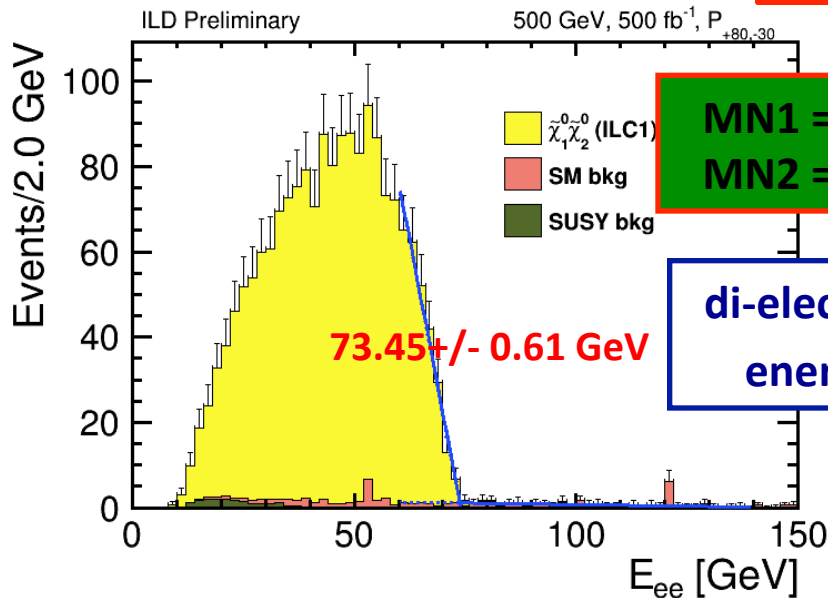
**Polarization (Pe-,Pe+) = (+0.8, -0.3)**

**Much less bkg**  
**Precision slightly better (?)**

preliminary



**Theoretical values: MN1 = 102.7 GeV MN2 = 124.0 GeV**



Chargino pair production with semileptonic decay

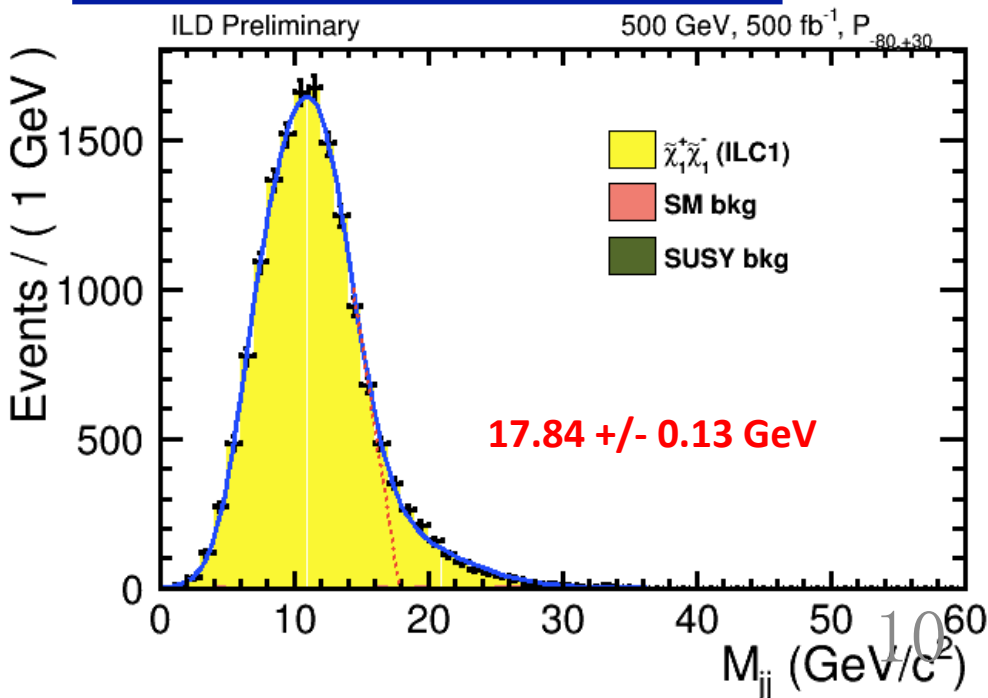
$$e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 qq' l \nu$$

Polarization (Pe-,Pe+) = (-0.8, +0.3)

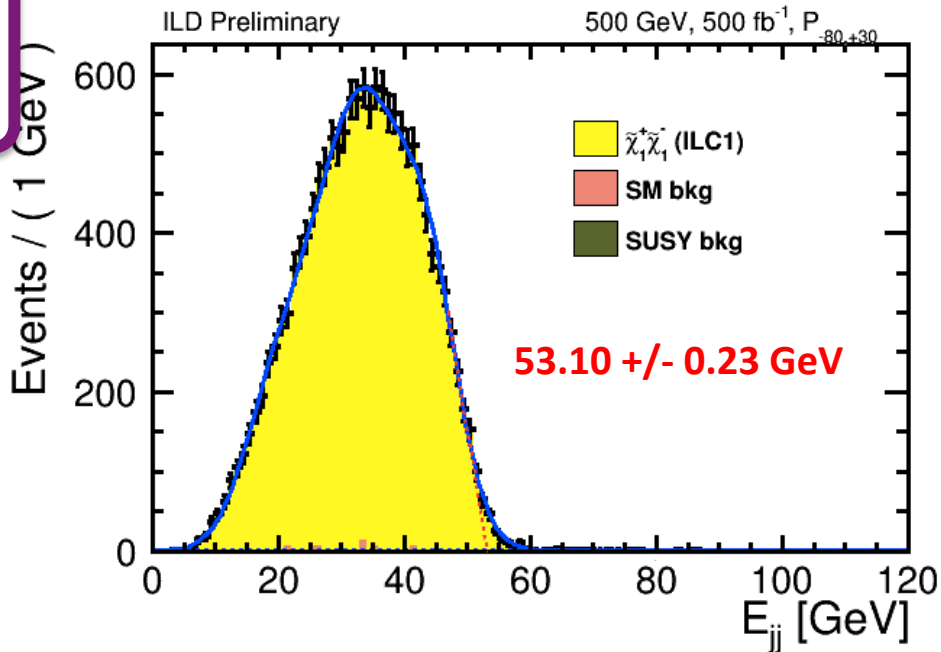
SM and SUSY backgrounds almost fully eliminated

Edge precision  $< \sim 0.5\%$

di-jet mass w/ electron tag



di-jet energy w/ electron tag



Edge extraction: steepest slope method

Theoretical values:

$E_{\text{max}} = 56.4 \text{ GeV}$      $\Delta M = 15.1 \text{ GeV}$

# Error Propagation

- Edge precision  $\sim 1\%$   
 → uncertainty of Higgsino mass 1.5 – 2%
- $\sim 0.5\%$  for Chargino

## Propagation of edge error to Higgsino mass error

In this section, the relevant symbols are defined as follow:

$E_{max}$ : higher kinematic edge of dilepton energy;  $\delta E_{max}$ : its uncertainty (from fit)

$\Delta M$ : mass difference between  $\tilde{\chi}_2^0$  and  $\tilde{\chi}_1^0$ ;  $\delta \Delta M$ : its uncertainty (from fit)

$M_{1(2)}$ : mass of  $\tilde{\chi}_{1(2)}^0$

$\beta$ : boost of  $\tilde{\chi}_2^0$  in the lab frame;  $\gamma = 1/\sqrt{1 - \beta^2}$

$P$ : momentum of  $\tilde{\chi}_2^0$  in the lab frame

The uncertainty of the mass of  $\tilde{\chi}_2^0$  ( $M_2$ ) is expressed using  $\delta E_{max}$  and  $\delta \Delta M$  as

$$\delta M_2 = \sqrt{\left(\frac{\partial M_2}{\partial \Delta M}\right)^2 \delta \Delta M^2 + \left(\frac{\partial M_2}{\partial E_{max}}\right)^2 \delta E_{max}^2} \quad (0.1)$$

Both  $E_{max}$  and  $\Delta M$ , along with their uncertainties, are obtained through a fit to the observed distributions of dilepton and invariant mass, respectively.

$E_{max}$  can be expressed as

$$E_{max} = \gamma(1 + \beta) \frac{\Delta M}{2} \left(1 + \frac{M_2 - \Delta M}{M_2}\right) \quad (0.2)$$

$\beta$  and  $P$  are functions of  $M_2$ ,  $\Delta M$ , and  $\sqrt{s}$ , given by

$$\beta = P / \sqrt{P^2 + M_2^2} \quad (0.3)$$

$$P = \frac{\sqrt{s}}{2} \sqrt{1 - 2 \left[ \left(\frac{M_2 - \Delta M}{\sqrt{s}}\right)^2 + \left(\frac{M_2}{\sqrt{s}}\right)^2 \right] + \left[ \left(\frac{M_2 - \Delta M}{\sqrt{s}}\right)^2 - \left(\frac{M_2}{\sqrt{s}}\right)^2 \right]^2} \quad (0.4)$$

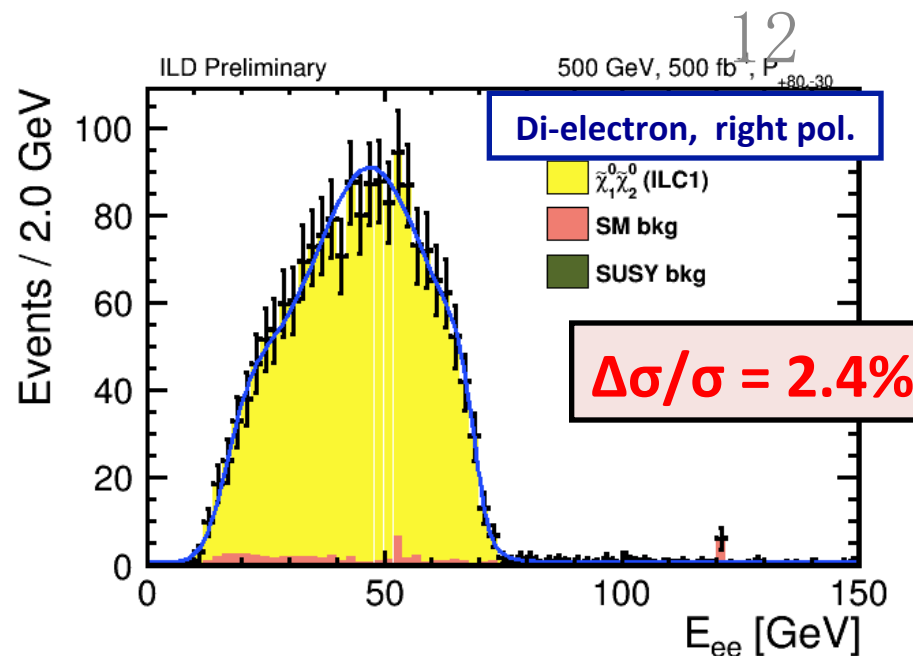
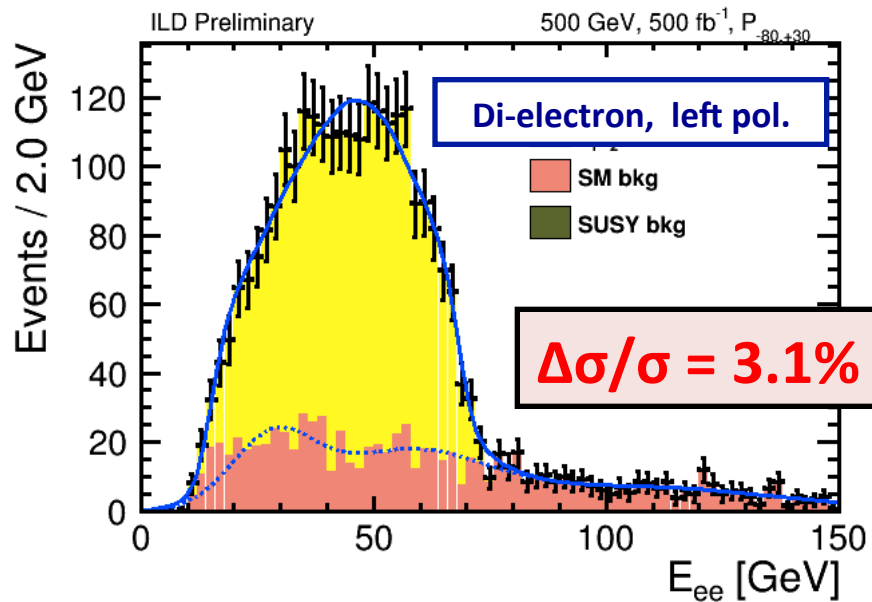
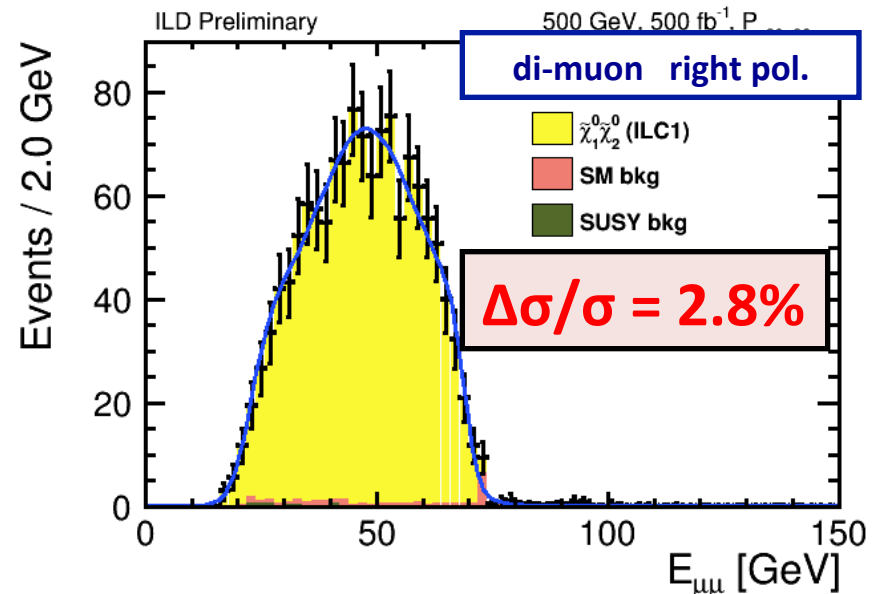
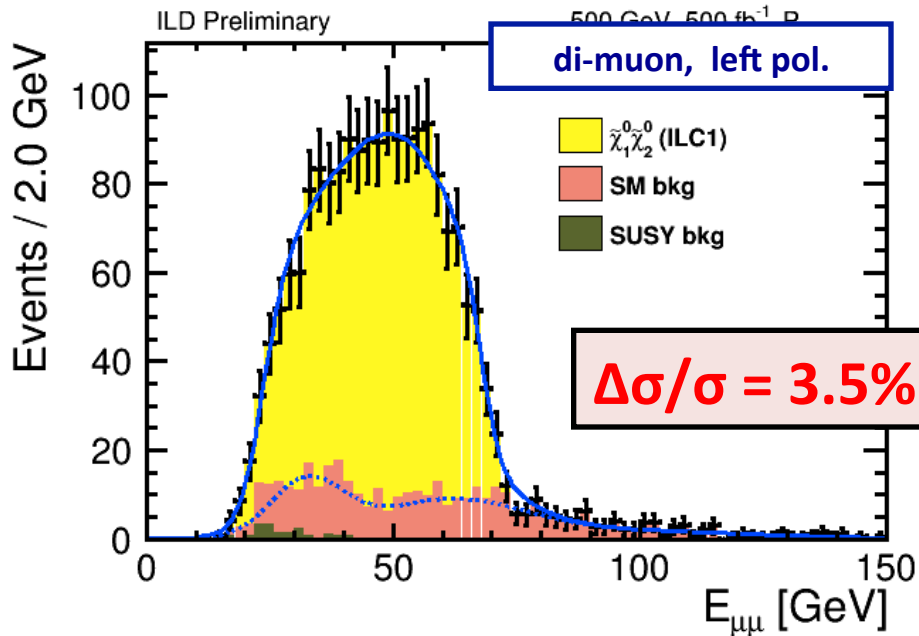
In order to make use of Equation 0.2, the first term in Equation 0.1 can be expressed as

$$\frac{\partial M_2}{\partial \Delta M} = \frac{\partial E_{max}}{\partial \Delta M} \cdot \frac{\partial M_2}{\partial E_{max}} = \frac{\frac{\partial E_{max}}{\partial \Delta M}}{\frac{\partial E_{max}}{\partial M_2}} \quad (0.5)$$

		calculated	calculate	observed	observed	observed	observed	calculated	calculated	calculated	calculated
		M1	M2	delta_M	Δ delta_M	E <sub>max</sub>	Δ E <sub>max</sub>	Δ M1	Δ M1/M1	Δ M2	Δ M2/M2
N1N2	mm	102.255	123.015	20.76	0.2	73.81	0.86	1.7697	1.73%	1.7583	1.43%
left	ee	100.296	120.811	20.5156	0.324223	74.3688	0.798674	2.1711	2.16%	2.1468	1.78%
N1N2	mm	103.058	123.988	20.93	0.22	73.77	0.84	1.8189	1.76%	1.8056	1.46%
right	ee	103.409	124.299	20.89	0.19	73.45	0.61	1.4406	1.39%	1.4280	1.15%

# Extraction of Cross Section

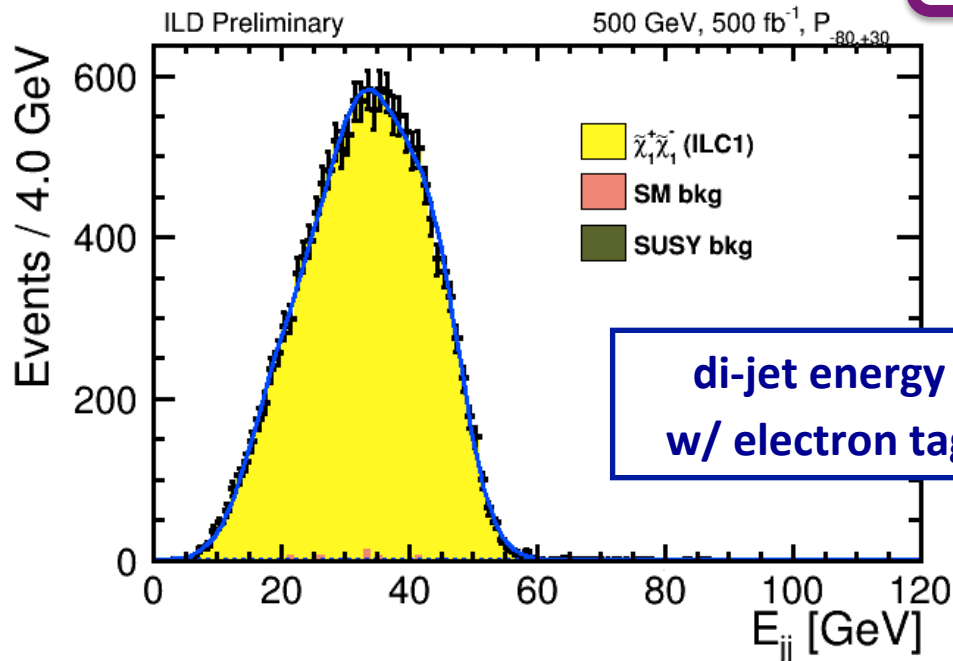
Uncertainty of right pol is about  $\frac{3}{4}$  of left pol  
(evaluated using Toy MC)



# Extraction of Cross Section

Chargino pair production with semileptonic decay

$$e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 qq' \ell \nu$$



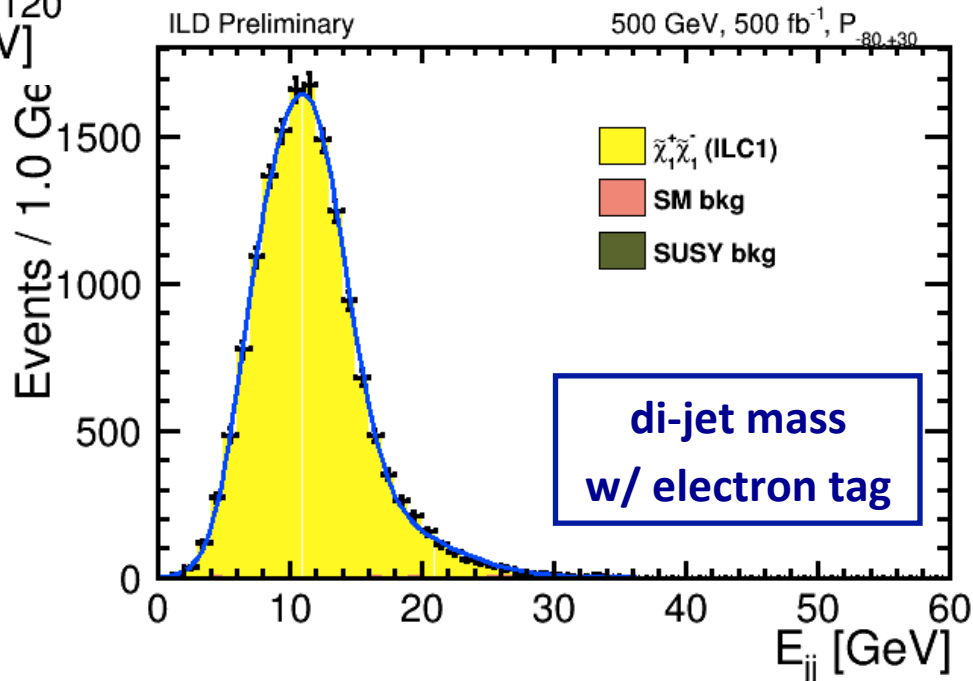
Polarization (P<sub>e-</sub>, P<sub>e+</sub>) = (-0.8, +0.3)

$$\Delta\sigma/\sigma = 0.8\%$$

Get same  $\Delta\sigma/\sigma$  whether we use  $E_{jj}$  or  $M_{jj}$

Fit with triple Gaussian

Other channels have similar shapes in the case of chargino



# Summary

## preliminary results for most channels

- **Neutralino:** Edge precision  $\sim 1\%$   $\rightarrow$  uncertainty of Higgsino mass 1.5 – 2%
- Edge values not far from theoretical values, need some correction for detector effects
- Cross section precision 3-4 % for left pol, 2.8% for right pol
  
- **Chargino :** edge precision  $\sim 0.5\%$   $\rightarrow$  uncertainty of Higgsino mass 0.5%
- Cross section precision : 0.8%,

## To Do / Plans

- Justify method for edge extraction (chargino) : use MC truth (?)
- explain deviation between extracted and theoretic values
  
- Converge current analysis to a full set of results  
 $\rightarrow$  input to document which demonstrates ILC new physics discovery potential
- Need to implement gamma gamma overlay bkg
  
- Plans for publication
- Conduct analysis at other CM energies and polarizations  
 $\rightarrow$  as input for studies on SUSY parameter determination (DESY)

# **Additional Material**

**Chargino pair production with semileptonic decay**

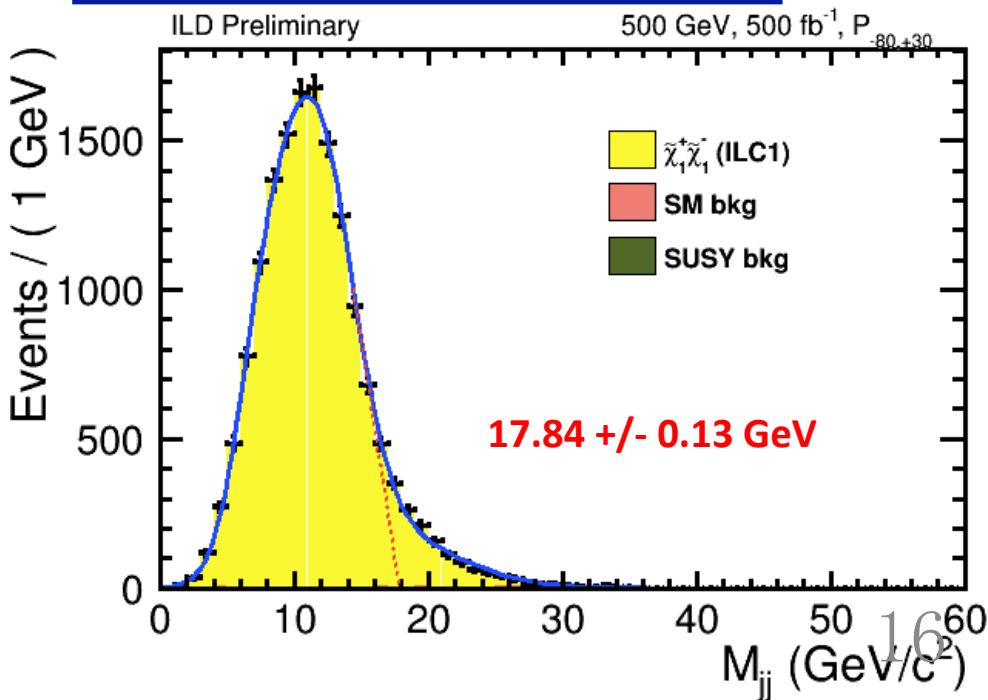
$$e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 qq' l \nu$$

**Polarization (Pe-,Pe+) = (-0.8, +0.3)**

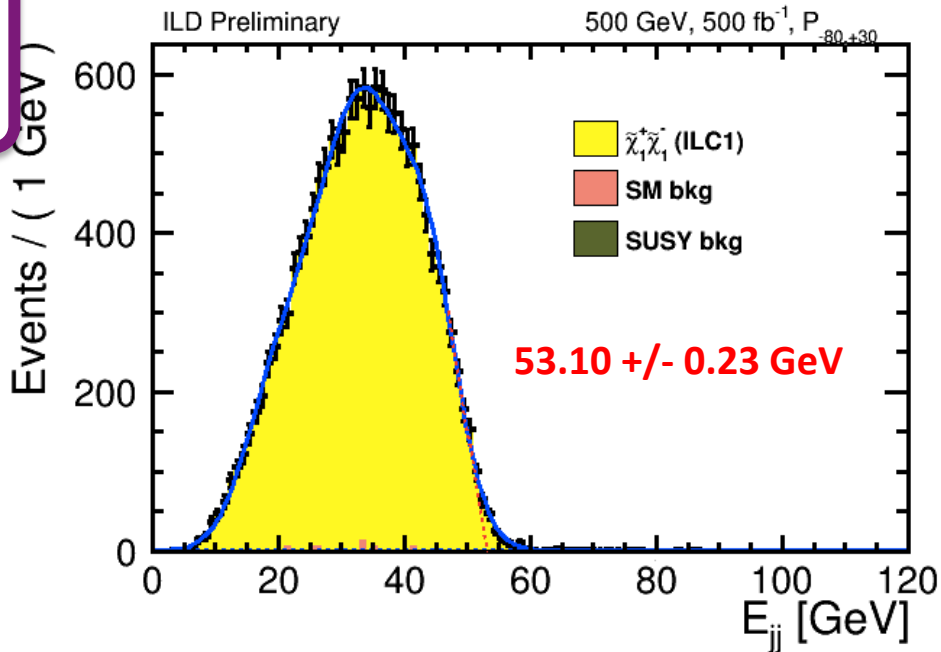
**SM and SUSY backgrounds almost fully eliminated**

**Edge precision < ~ 0.5 %**

**di-jet mass w/ electron tag**



**di-jet energy w/ electron tag**



**MN1 = 125.5 GeV MC1 = 143.4 GeV**

**Edge extraction: steepest slope method**

**Theoretical values:**

**E\_max = 56.4 GeV    ΔM = 15.1 GeV**  
**MN1 = 102.7 GeV    MC1 = 117.8 GeV**

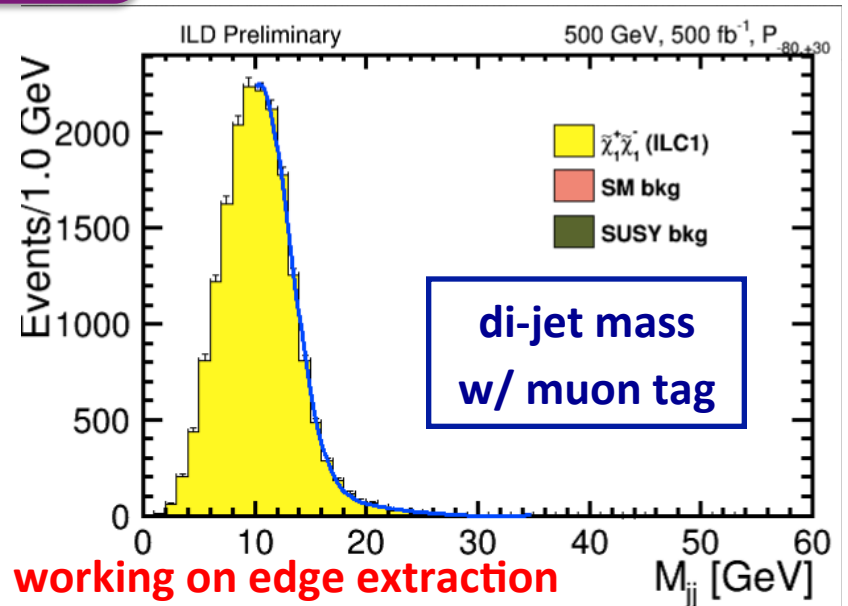
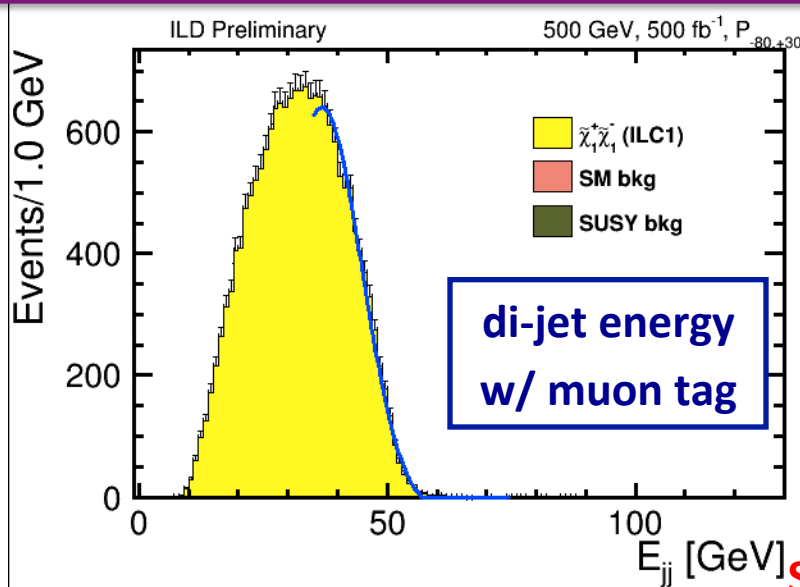


# Chargino pair production with semileptonic decay

$$e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 qq' \ell \nu$$

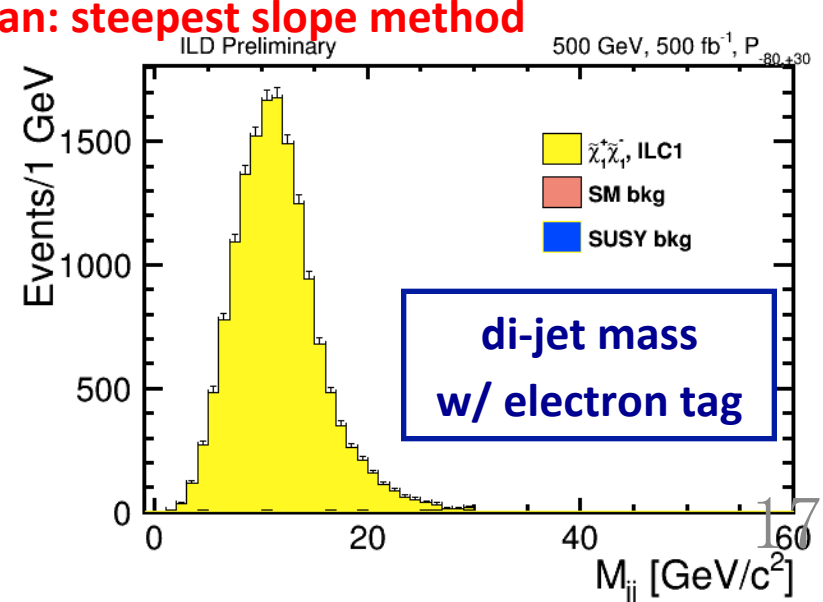
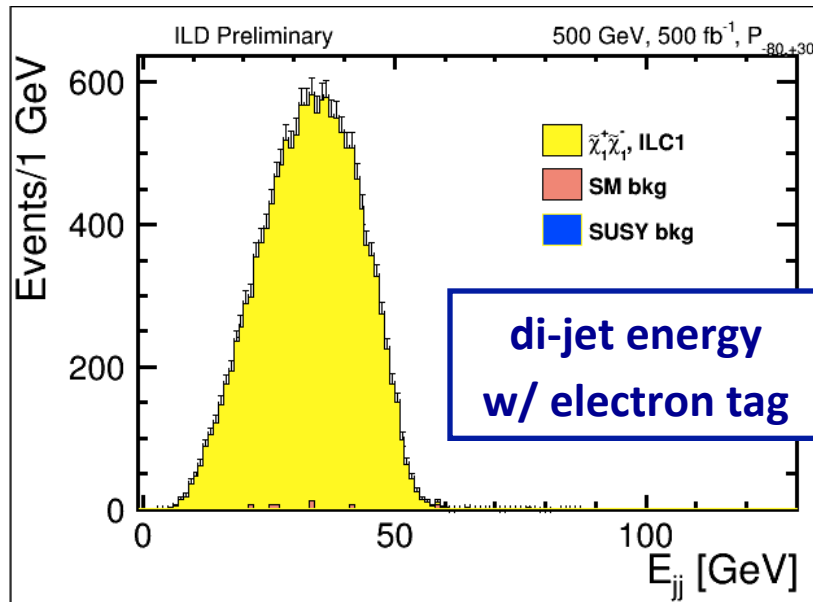
Polarization (Pe-,Pe+) = (-0.8, +0.3)  
SM and SUSY backgrounds  
almost fully eliminated

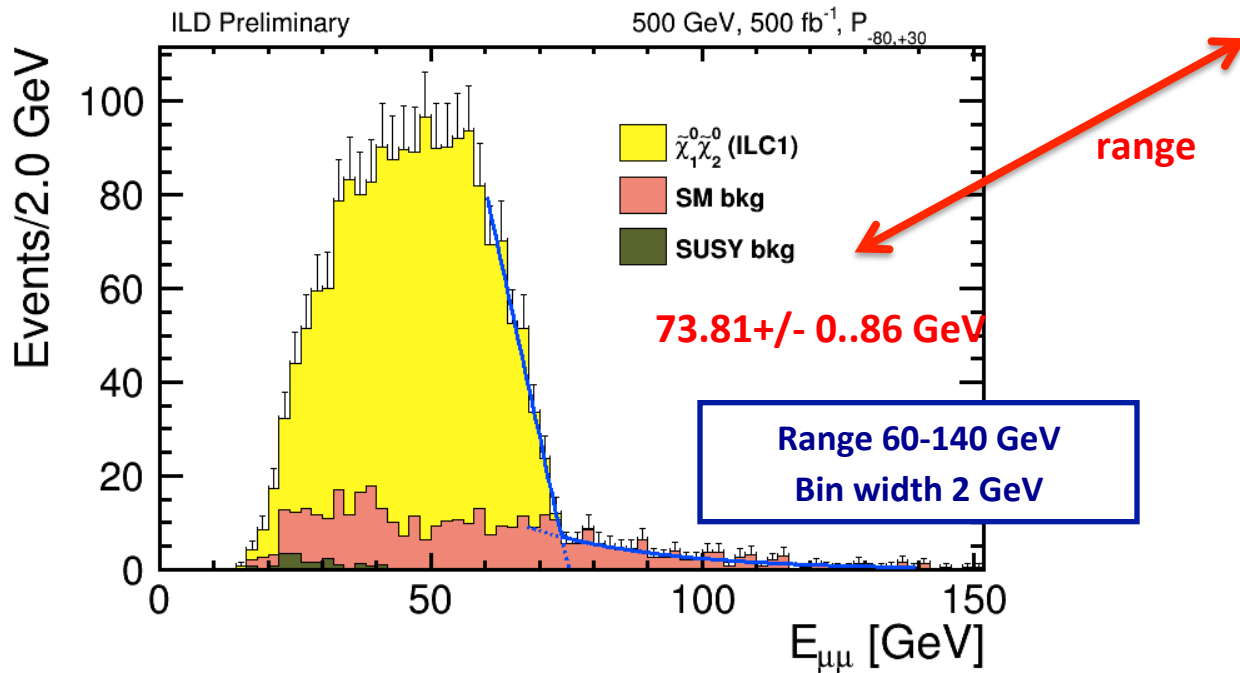
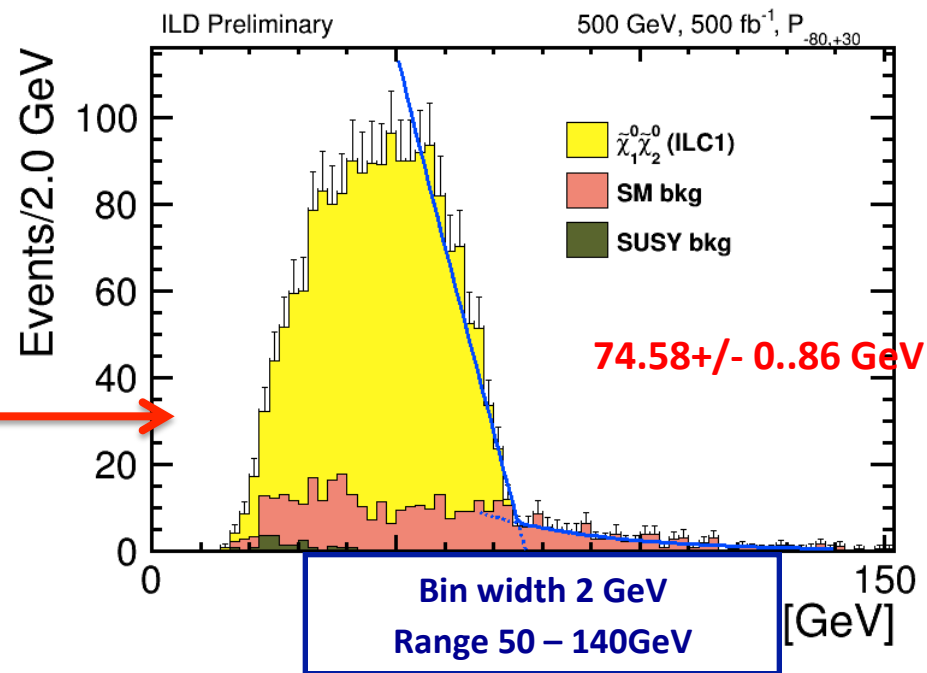
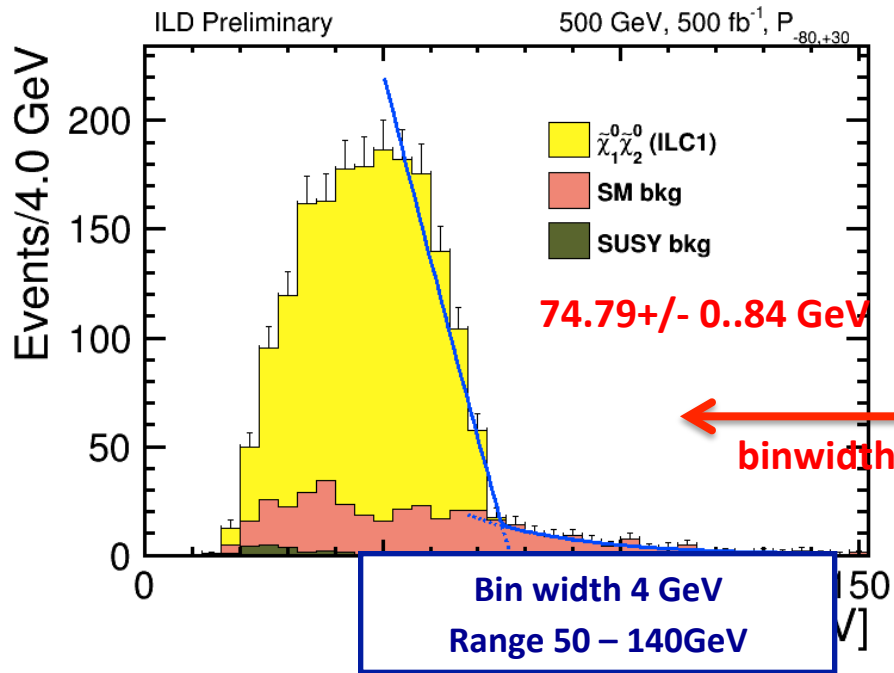
preliminary

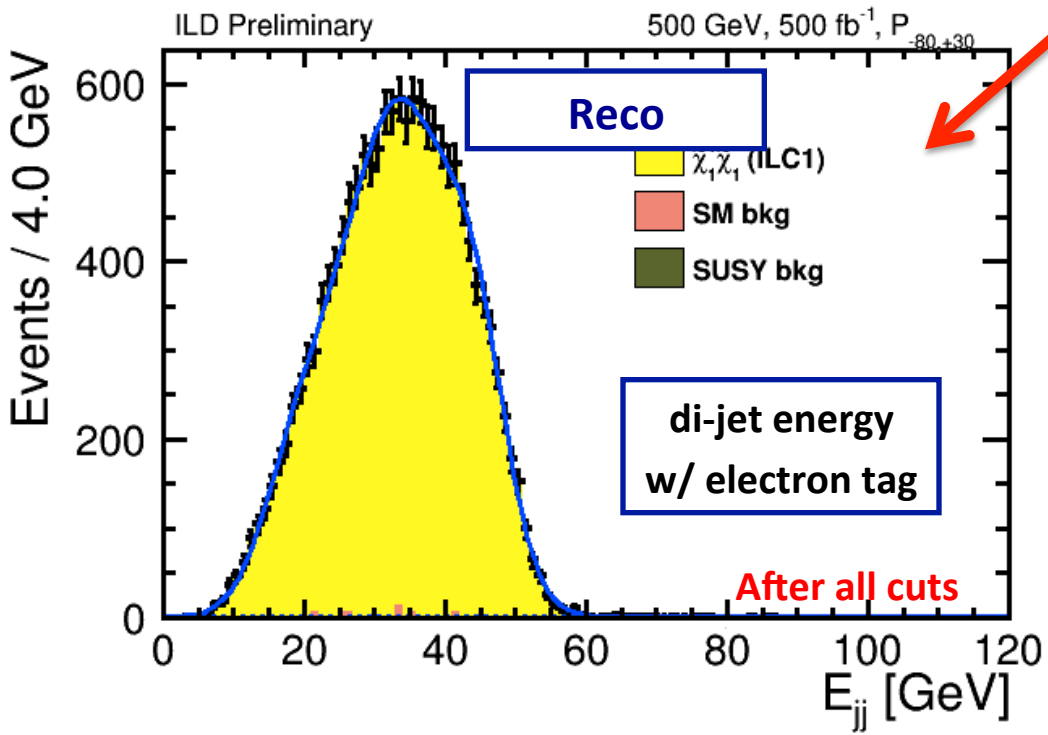
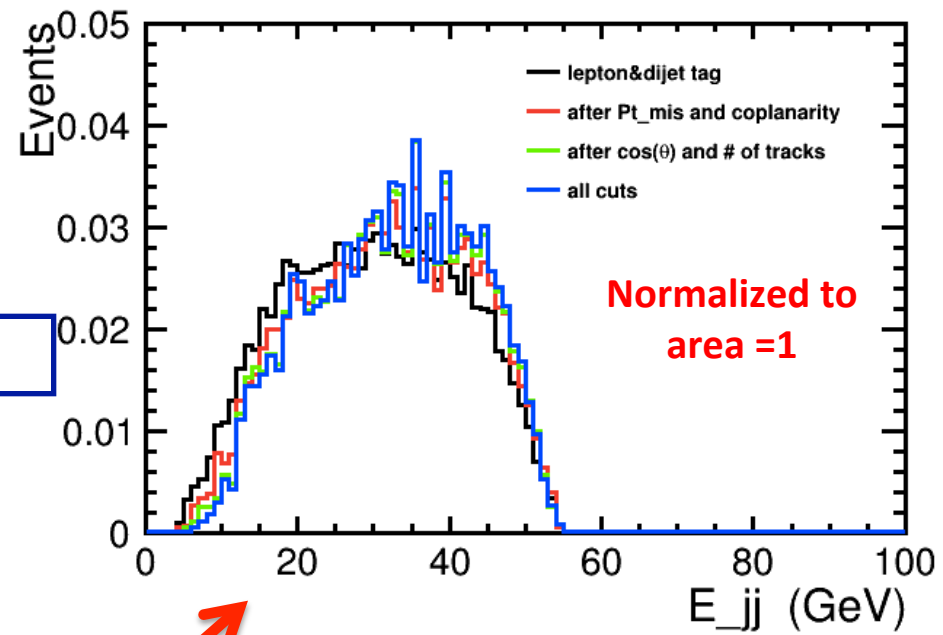
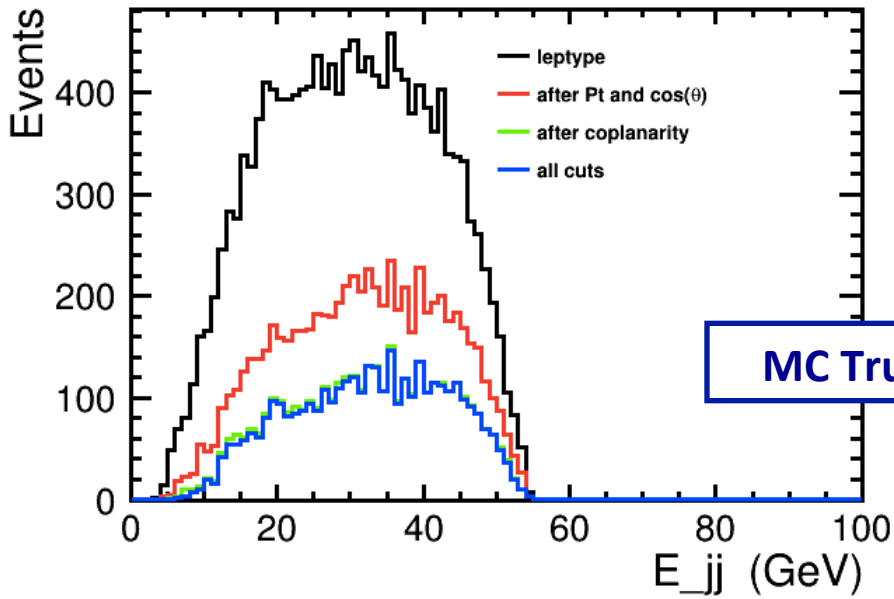


Still working on edge extraction

Plan: steepest slope method







Looks SAME

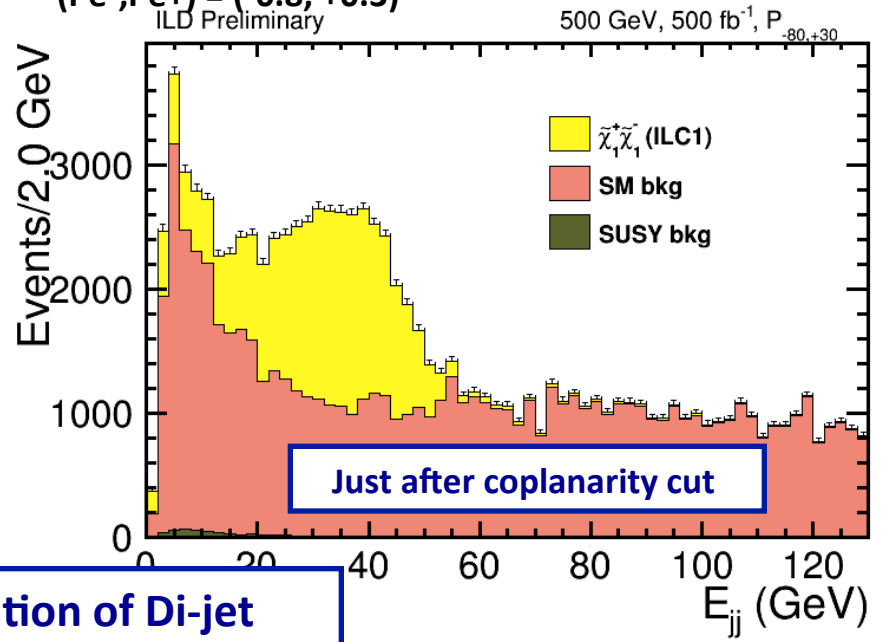
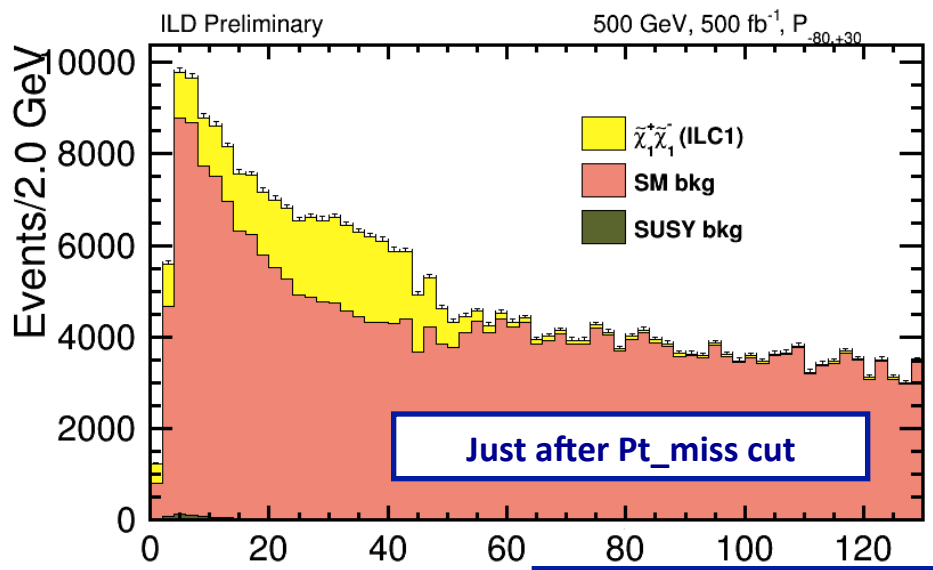
Change in distribution of Di-jet energy with respect to cuts (SIGNAL)

Cuts applied on Reconstructed variables

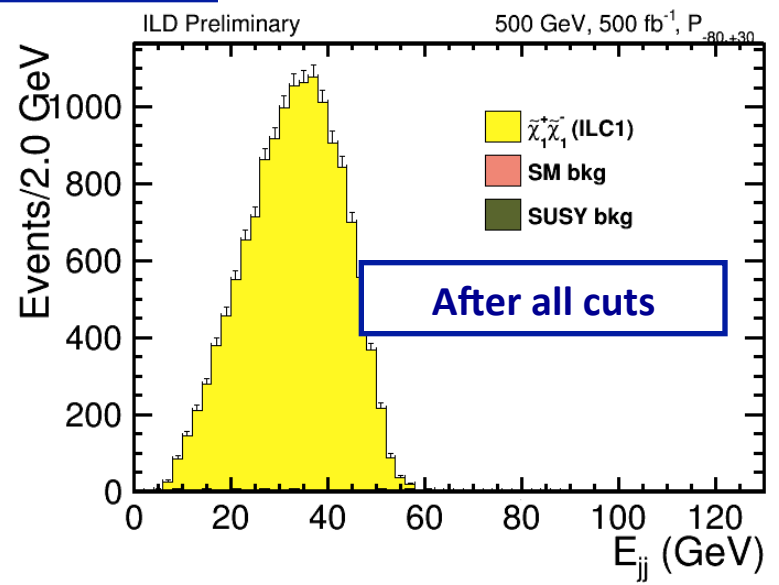
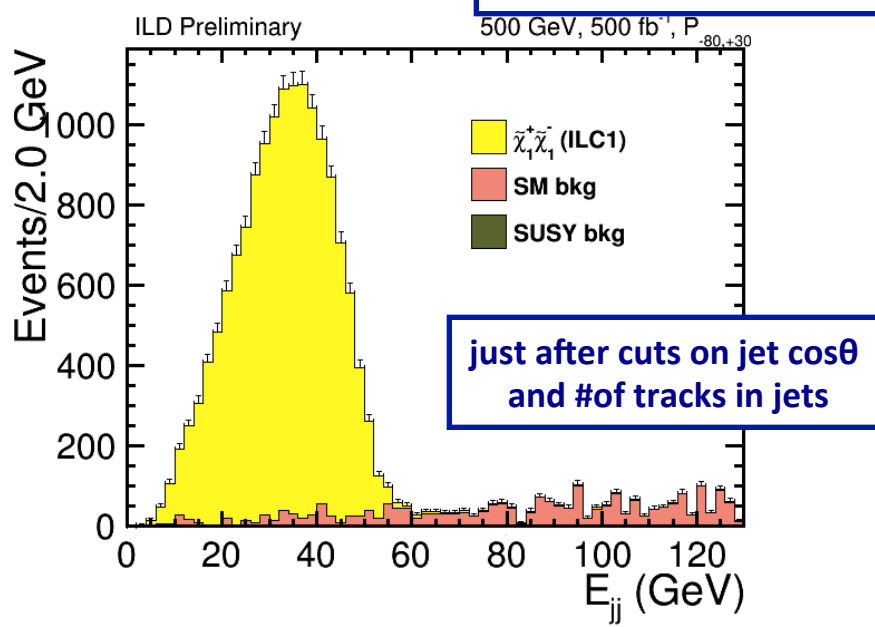
# Chargino pair production with semileptonic decay

$$e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 q q' \ell \nu$$

$(P_{e-,Pe+}) = (-0.8, +0.3)$



**Change in distribution of Di-jet energy with respect to cuts (BKG)**



# Event Selection

## Neutralino mixed production with leptonic decay

$$e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \ell^+ \ell^-$$

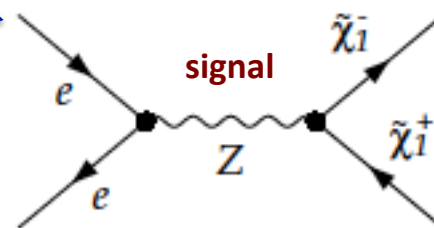
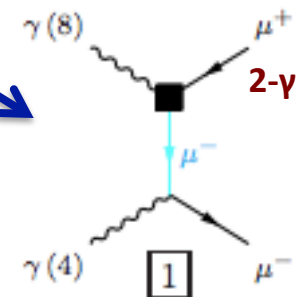
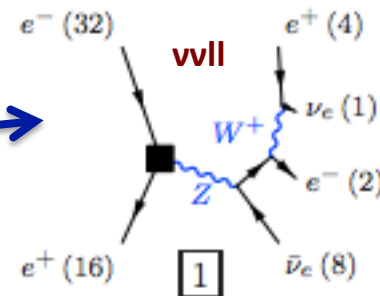
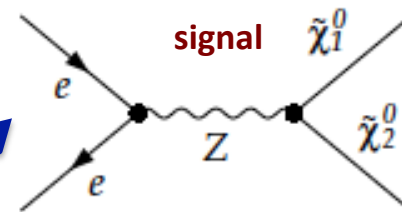
- Reconstruct **two leptons (ee or  $\mu\mu$ )** which originate from  **$Z^*$  emission in decay of  $\tilde{\chi}_2^0$  to  $\tilde{\chi}_1^0$**
- Major residual bkg. are 4f processes accompanied by large missing energy (vll)
- 2- $\gamma$  processes are removed by BeamCal veto, cuts on lepton track  $p_T$ , and coplanarity

## Chargino pair production with semileptonic decay

$$e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 qq' \ell \nu$$

- Reconstruct **two jets which originate from  $W^*$  emission in decay of  $\tilde{\chi}_1^\pm$  to  $\tilde{\chi}_1^0$**
- Use lepton (e or  $\mu$ ) from the other chargino as tag
- BeamCal veto, cuts on missing  $p_T$ , # of tracks, # of leptons, and coplanarity remove almost all bkg.

(signal significance > 100)



## Cuts for N1N2

- **lepton type ( $\mu\mu$  or  $ee$ )** : the two leptonic channels of N1N2 analysis
- **nTrack = 2** : number of charged tracks
- **no hit in BeamCal** : veto  $\gamma\gamma$ 2f BG
- **Pt\_lep1,2 > 6 GeV and  $|\cos\theta_{lep1,2}| < 0.95$ :**
- **Coplanarity < 1.0 rad** : angle between leptons in x-y plane
- **Evis – E $\gamma$ max < 40 GeV** : visible energy (very small for signal)
- **Emis > 300 GeV** : missing energy (very large for signal)
- **$|\cos\theta_{missing}| < 0.98$**  :  $\theta$  of missing energy events
- **$|\cos\theta_Z| < 0.98$**  :  $Z^*$  production angle
- **Pt\_dl < 80 GeV** : transverse momentum of dilepton
- **Minv < 50 GeV** : dilepton invariant mass: determines  $\Delta M$

last of all observe distributions of Minv and dilepton energy (E\_dl)

Kinematic edge is a function of Higgsino mass and  $\Delta M$

## Cuts for C1C1

- lepton type ( $\mu$  or e tag) and # of lepton =1
- $Pt_{mis} > 10$  GeV
- Jet Coplanarity  $< 1.0$  rad
- $|\cos\theta_{jet1,2}| < 0.95$ :
- nTrack(in jet)  $> 1$  :
- no hit in BeamCal :
- $\cos\theta_{jet1-lep} < 0.2$ ,  $\cos\theta_{jet2-lep} < 0$  angle between jets and leptons
- $E_{vis} - E_{\gamma max} < 60$  GeV :
- $E_{mis} > 400$  GeV :
- $|\cos\theta_{missing}| < 0.98$  :
- $|\cos\theta_Z| < 0.98$  :
- $Pt_{jj} < 50$  GeV :
- $Minv < 30$  GeV :

last of all observe distributions of  $Minv$  and dijet energy ( $E_{jj}$ )

Kinematic edge is a function of Higgsino mass and  $\Delta M$

## Cuts for N1N2

- **lepton type ( $\mu\mu$  or  $ee$ )** : the two leptonic channels of N1N2 analysis
- **nTrack = 2** : number of charged tracks
- **no hit in BeamCal** : veto  $\gamma\gamma$ 2f BG
- **Pt\_lep1,2 > 6 GeV and  $|\cos\theta_{lep1,2}| < 0.95$ :**
- **Coplanarity < 1.0 rad** : angle between leptons in x-y plane
- **Evis – E $\gamma$ max < 40 GeV** : visible energy (very small for signal)
- **Emis > 300 GeV** : missing energy (very large for signal)
- **$|\cos\theta_{missing}| < 0.98$**  :  $\theta$  of missing energy events
- **$|\cos\theta_Z| < 0.98$**  :  $Z^*$  production angle
- **Pt\_dl < 80 GeV** : transverse momentum of dilepton
- **Minv < 50 GeV** : dilepton invariant mass: determines  $\Delta M$

last of all observe distributions of Minv and dilepton energy (E\_dl)

Kinematic edge is a function of Higgsino mass and  $\Delta M$



## Cuts for C1C1

- lepton type ( $\mu$  or e tag) and # of lepton =1
- $Pt_{mis} > 10$  GeV
- Jet Coplanarity  $< 1.0$  rad
- $|\cos\theta_{jet1,2}| < 0.95$ :
- nTrack(in jet)  $> 1$  :
- no hit in BeamCal :
- $\cos\theta_{jet1-lep} < 0.2$ ,  $\cos\theta_{jet2-lep} < 0$  angle between jets and leptons
- $E_{vis} - E_{\gamma max} < 60$  GeV :
- $E_{mis} > 400$  GeV :
- $|\cos\theta_{missing}| < 0.98$  :
- $|\cos\theta_Z| < 0.98$  :
- $Pt_{jj} < 50$  GeV :
- $Minv < 30$  GeV :

last of all observe distributions of  $Minv$  and dijet energy ( $E_{jj}$ )

Kinematic edge is a function of Higgsino mass and  $\Delta M$

# Cut table $N_1 N_2, \mu\mu$ ( $P_{e-}, P_{e+}$ ) = (-80,+30)

	sig	bkg	4f_l	aa_2f	ae_3f	SUSY bkg
xsec	300.8	3.00E6	10566.2	2.68E6	261580	1065.2
N_gen	150395	1.50E9	5.28E6	1.34E9	1.31E8	532585
Lep_type nTrack=2	1974	9.1E8	444255	8.9E8	2.2E7	2426
BCAL veto	1950	6.0E6	149871	5.5E6	965354	2411
Pt_lep,1,2	1675	2.0E6	105721	1.4E6	295459	1986
cos $\theta$ _lep	1624	1.3E6	56001	910330	167734	1950
coplanarity	1407	48366	5272	3509	33067	22
Evis	1404	14325	2465	2248	4743	22
Emis, cos $\theta$ mis	1393	1063	929	34	9	19
cosZ, Pt_ll, Minv	1393	545	429	34	9	19

# Cut table C1C1 , $\mu_{tag}$ ( $P_{e^-}, P_{e^+}$ ) = (-80,+30)

	sig	bkg	4f_l	aa_2f	ae_3f	SUSY bkg
Xsec [fb]	1065.2	3.00E6	10566.2	2.68E6	261580	300.8
N_gen	532585	1.50E9	5.28E6	1.34E9	1.31E8	150395
nLep=1 BCAL veto	57983	1.5E9	443296	1.2E6	860530	1135
Ptmis	38240	2.7E6	377010	465397	519308	964
Jet_coplanarity	26085	1.5E6	86399	83683	109325	531
Jet_cos $\theta$ nTrack (per jet) > 1	14612	305870	3066	555	2234	22
cos $\theta$ jet-lep Evis	14308	3753	791	100	41	0
Emis, cos $\theta$ mis	14231	83	57	3	0	0
Pt_jj, M_jj	14173	51	31	3	0	0