



Roman Pöschl



R.P. is indebted to many authors from whom I have reused their material

- Chapter 1: Introduction
- Chapter 2: Higgs Physics at the ILC
- Chapter 3: Top Physics at the ILC

Many thoughts, argumentations, plots taken from:

The ILC's Potential for Discovering New Particles

Document Supporting the ICFA Response Letter to the ILC Advisory Panel

The LCG Physics Working Group

1. Introduction

Coronation of the Standard Model
and
First step on a road yet largely unexplored
Slightly modified citation of Barbieri arXiv:1309.3447



HIGGS

HIGGS

Chip Brook, Snowmass Summary Talk

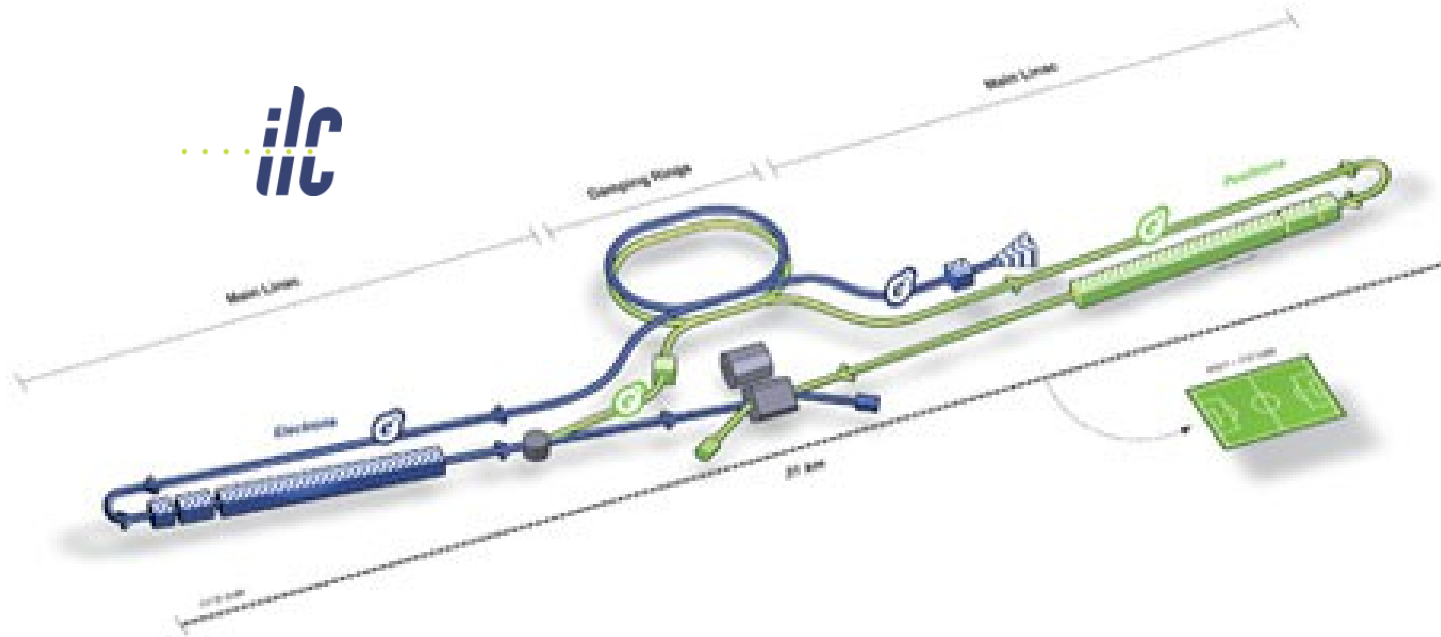
Where do we go from here?



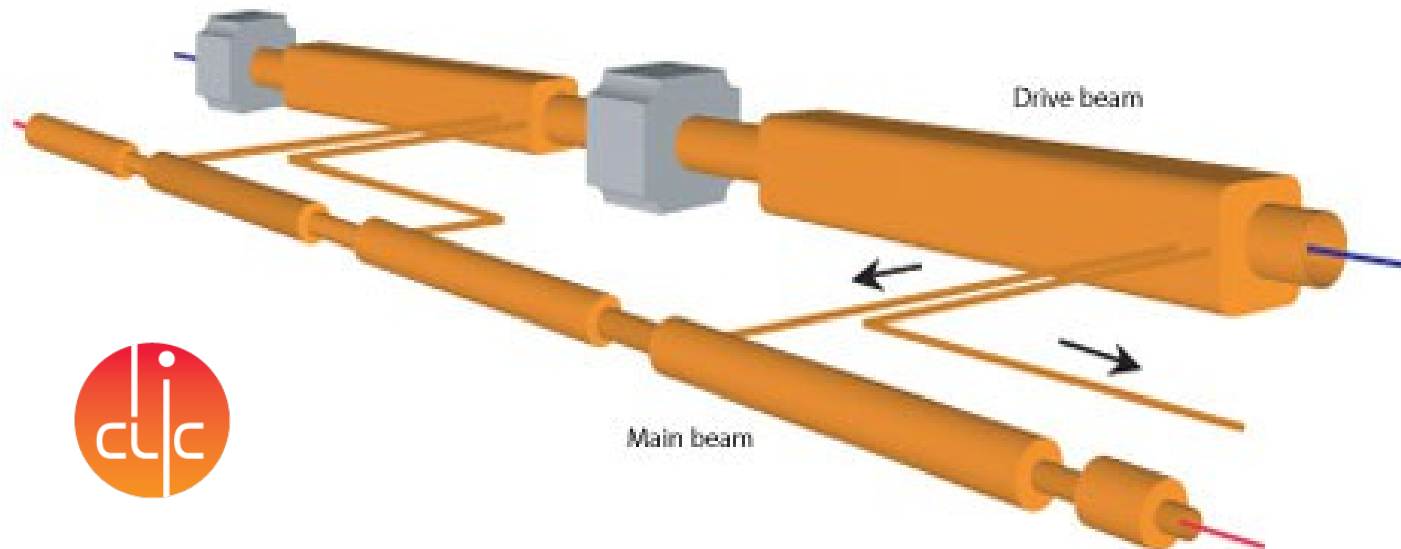
- 1) Collisions at energies well above the electroweak scale
 - Requires now and in the foreseeable future Hadron colliders
 - Direct production of new particles
 - Produce large number of rare particles and study rare decays
 - First precision measurements of key particles of electroweak theory-> High energy, High luminosity LHC

- 2) **e+e-Collisions at energies at the electroweak scale**
 - Probe the electroweak scale with high precision
 - ... in particular particles that carry the “imprint of the Higgs Field such as W, Z and top”-> **LC**

- 3) e+e- collisions at 'smaller' energies
 - Requires high luminosity to get sensitive to tiny quantum effects-> SuperKEKB



Energy: 0.1 - 1 TeV
Electron (and positron)
polarisation
TDR in 2013
+ DBD for detectors
 Footprint 31 km



Energy: 0.4 - 3 TeV
CDR in 2012
 Footprint 48km



Track momentum: $\sigma_{1/p} < 5 \times 10^{-5}/\text{GeV}$ (1/10 x LEP)

(e.g. Measurement of Z boson mass in Higgs Recoil)

Impact parameter: $\sigma_{d_0} < [5 \oplus 10/(p[\text{GeV}]\sin^{3/2}\theta)] \mu\text{m}$ (1/3 x SLD)

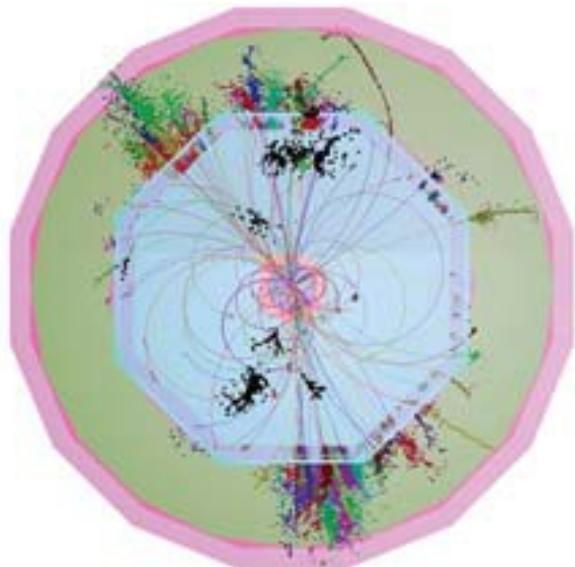
(Quark tagging c/b)

Jet energy resolution : $dE/E = 0.3/(E(\text{GeV}))^{1/2}$ (1/2 x LEP)

(W/Z masses with jets)

Hermeticity : $\theta_{\min} = 5 \text{ mrad}$

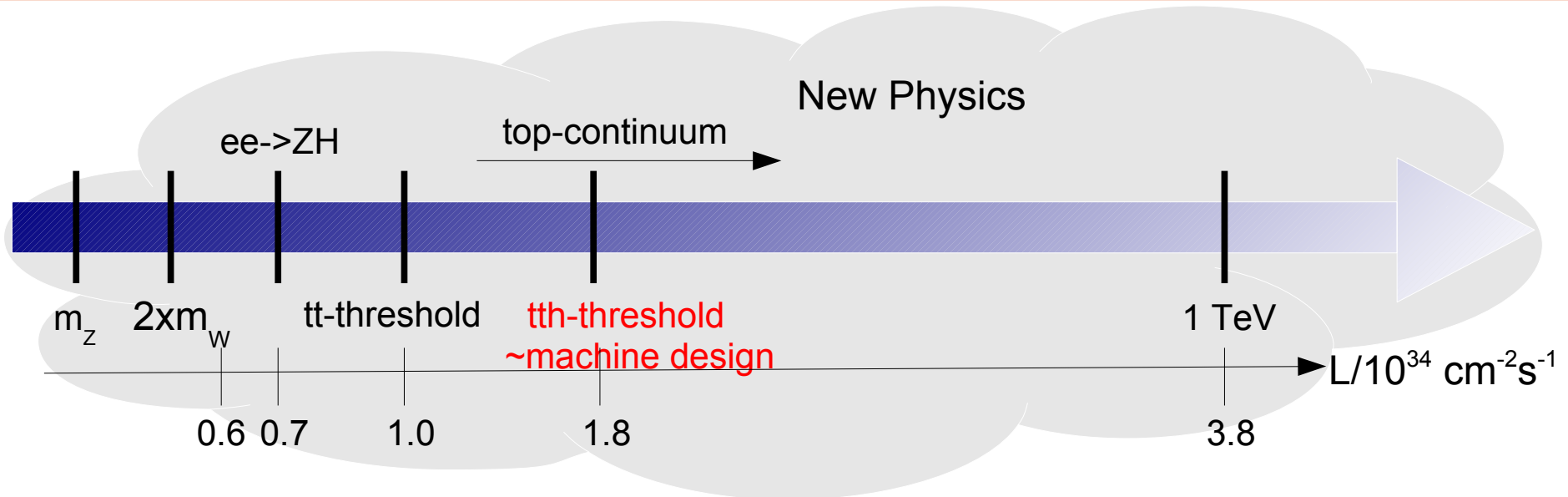
(for events with missing energy e.g. SUSY)



Final state will comprise events with a large number of charged tracks and jets(6+)

- High granularity
- Excellent momentum measurement
- High separation power for particles

- Particle Flow Detectors
ILD, SiD and CLIC Detector



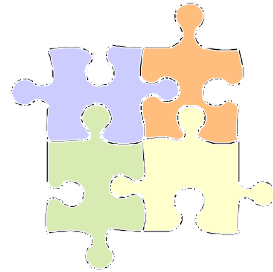
- All Standard Model particles within reach of LC
 - High precision tests of Standard Model over wide range to detect onset of New Physics
- Machine settings can be “tailored” for specific processes
 - Centre-of-Mass energy
 - Beam polarisation

$$\sigma_{P,P'} = \frac{1}{4} [(1 - PP')(\sigma_{LR} + \sigma_{RL}) + (P - P')(\sigma_{RL} - \sigma_{LR})]$$

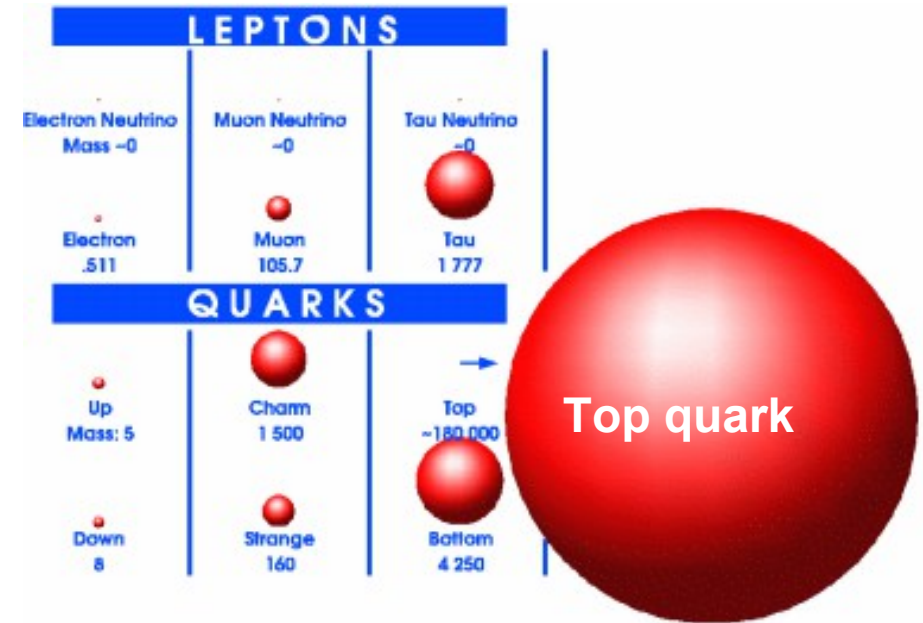
- **Background free** searches for BSM through beam polarisation



Elementary Scalar?



Composite object?



- Higgs and top quark are intimately coupled!

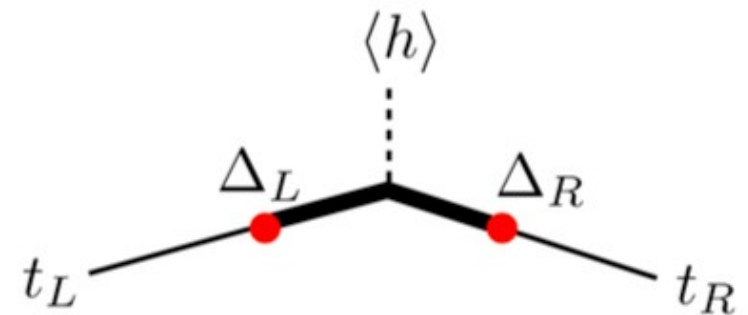
Top Yukawa coupling $O(1)$!

=> Top mass important SM Parameter

- New physics by compositeness?

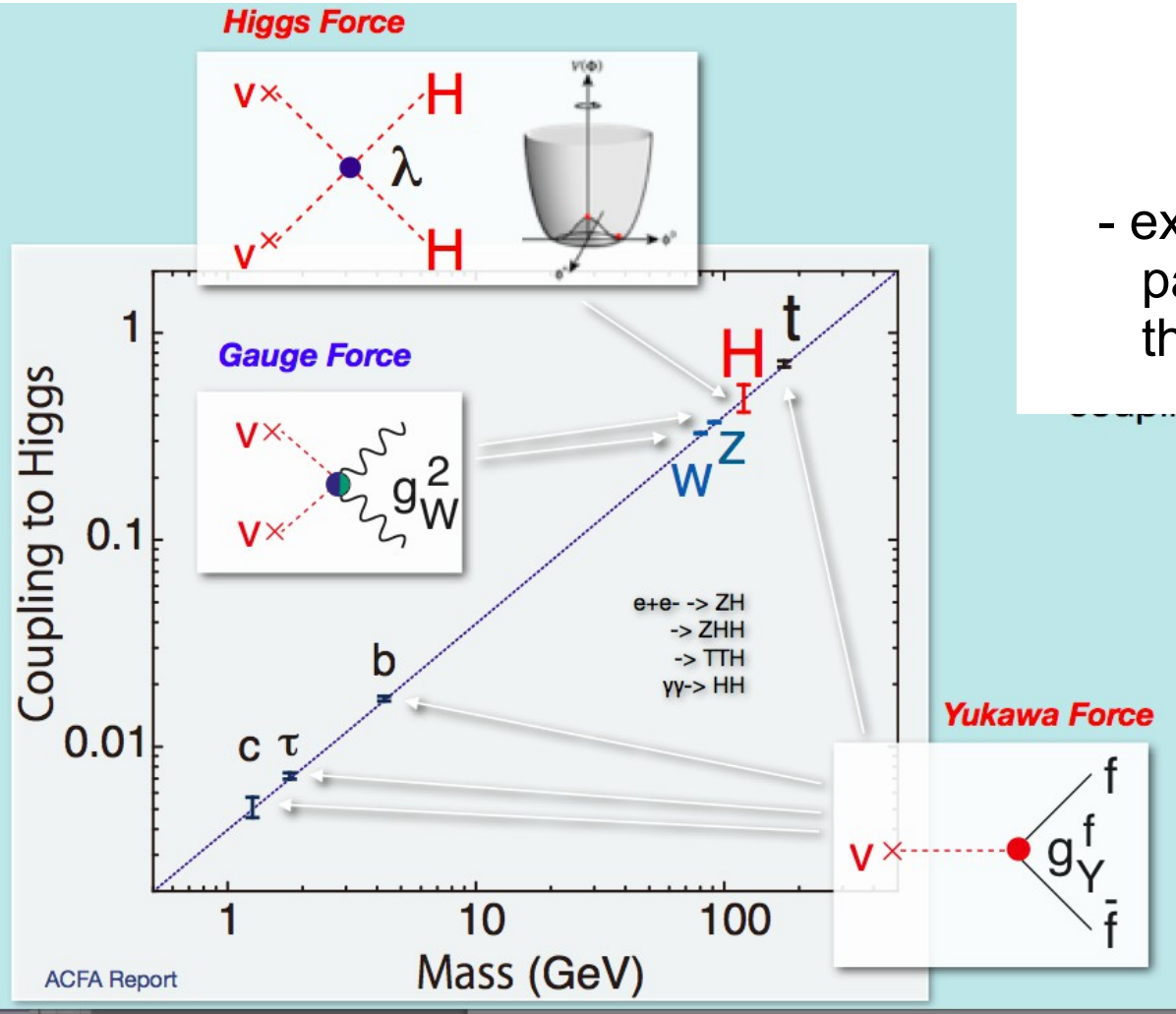
Higgs and top composite objects?

- LC perfectly suited to decipher both particles



Courtesy of S. Rychkov

2. Higgs Physics at the ILC



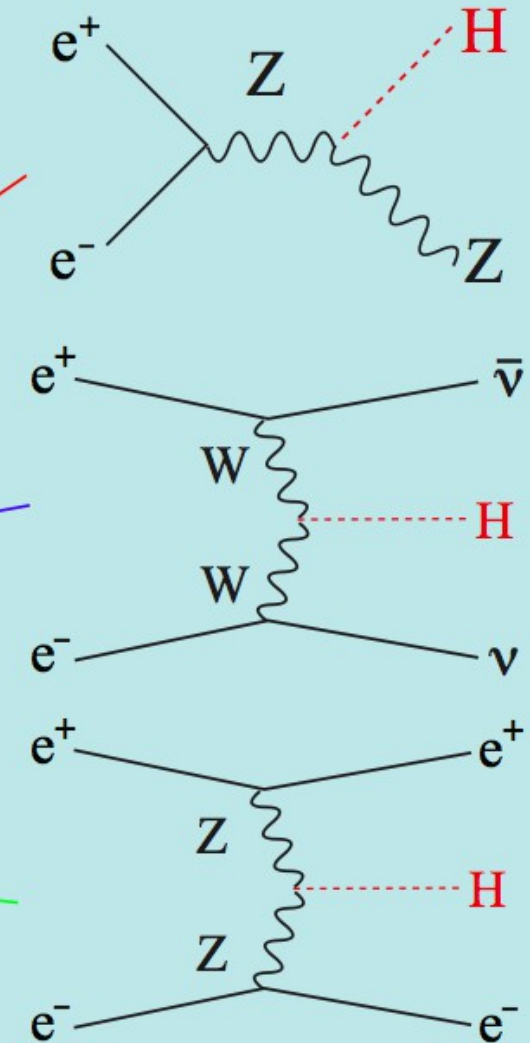
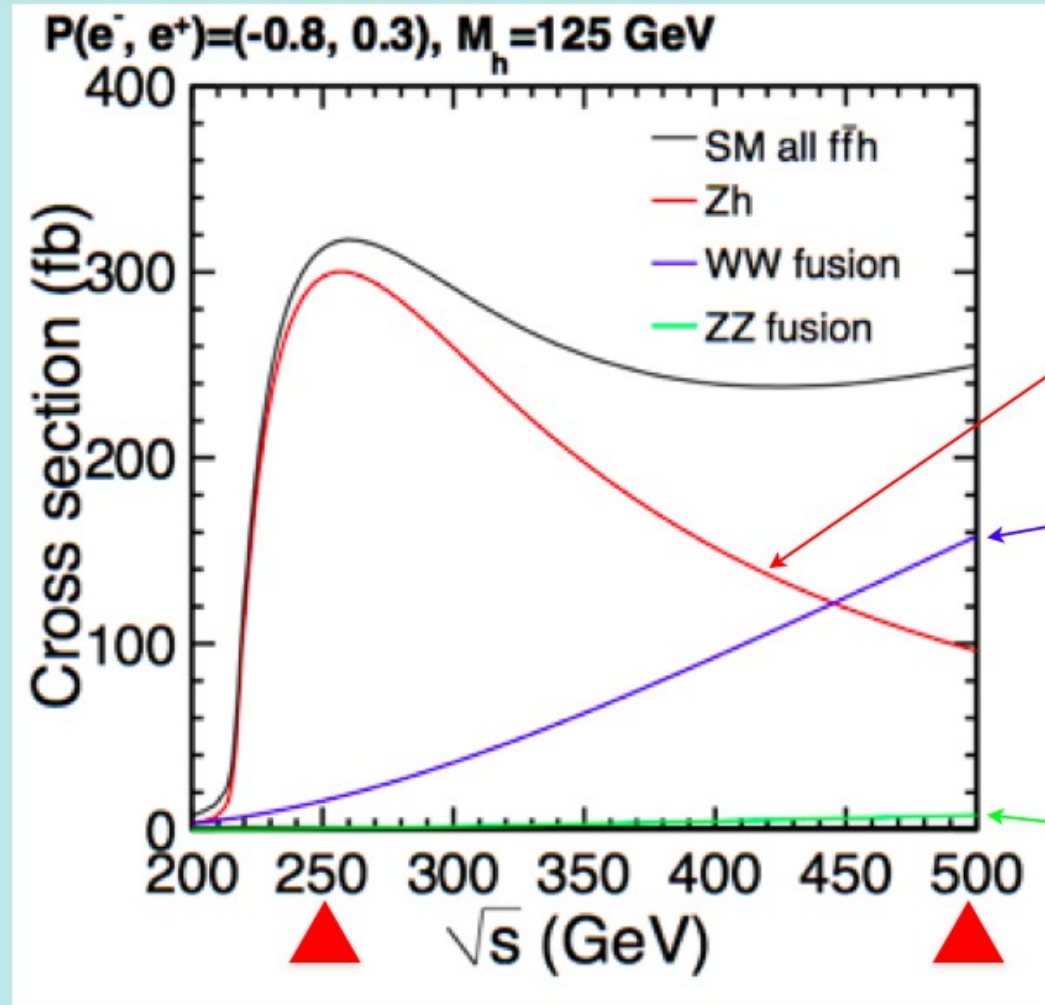
- exact correlation between particle masses couplings to the Higgs in Standard Model

- Any tiny deviation is New Physics

- Need precision on Higgs couplings at 1% level

| | ΔhVV | Δhtt | Δhbb |
|--------------------------------|--------------|--------------|--------------------------------------|
| Mixed-in Singlet | 6% | 6% | 6% |
| Composite Higgs | 8% | tens of % | tens of % |
| Minimal Supersymmetry | < 1% | 3% | 10% ^a , 100% ^b |
| LHC 14 TeV, 3 ab ⁻¹ | 8% | 10% | 15% |

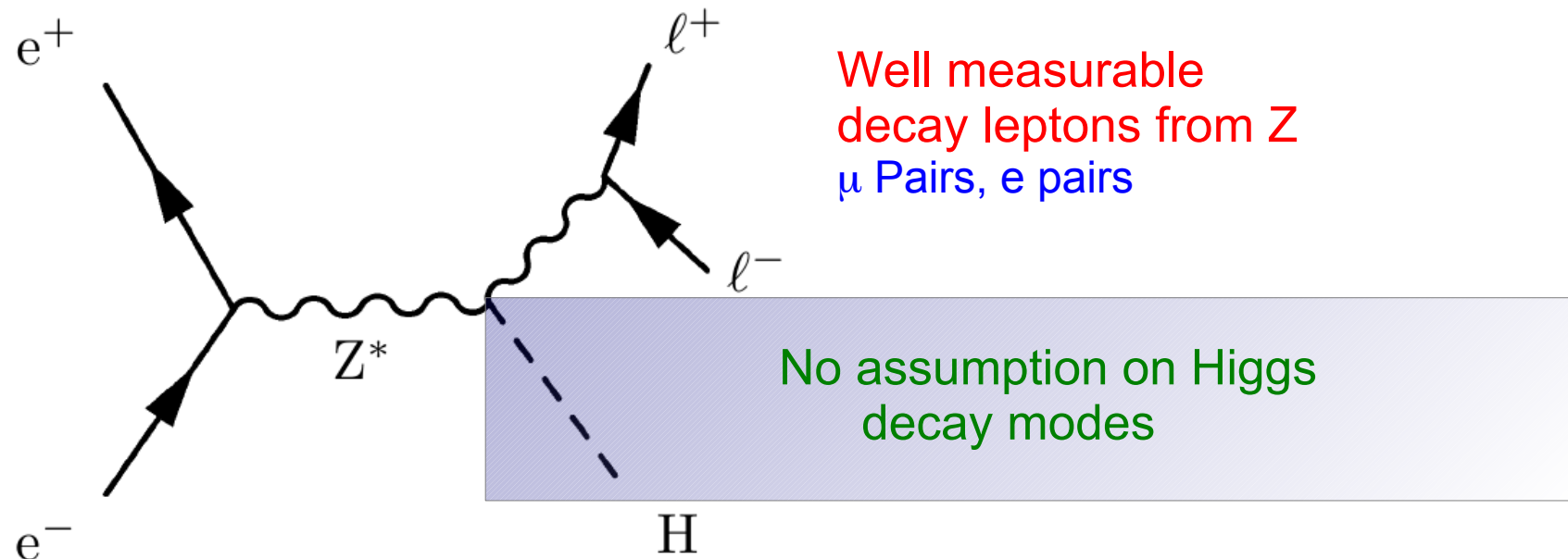
Production cross section



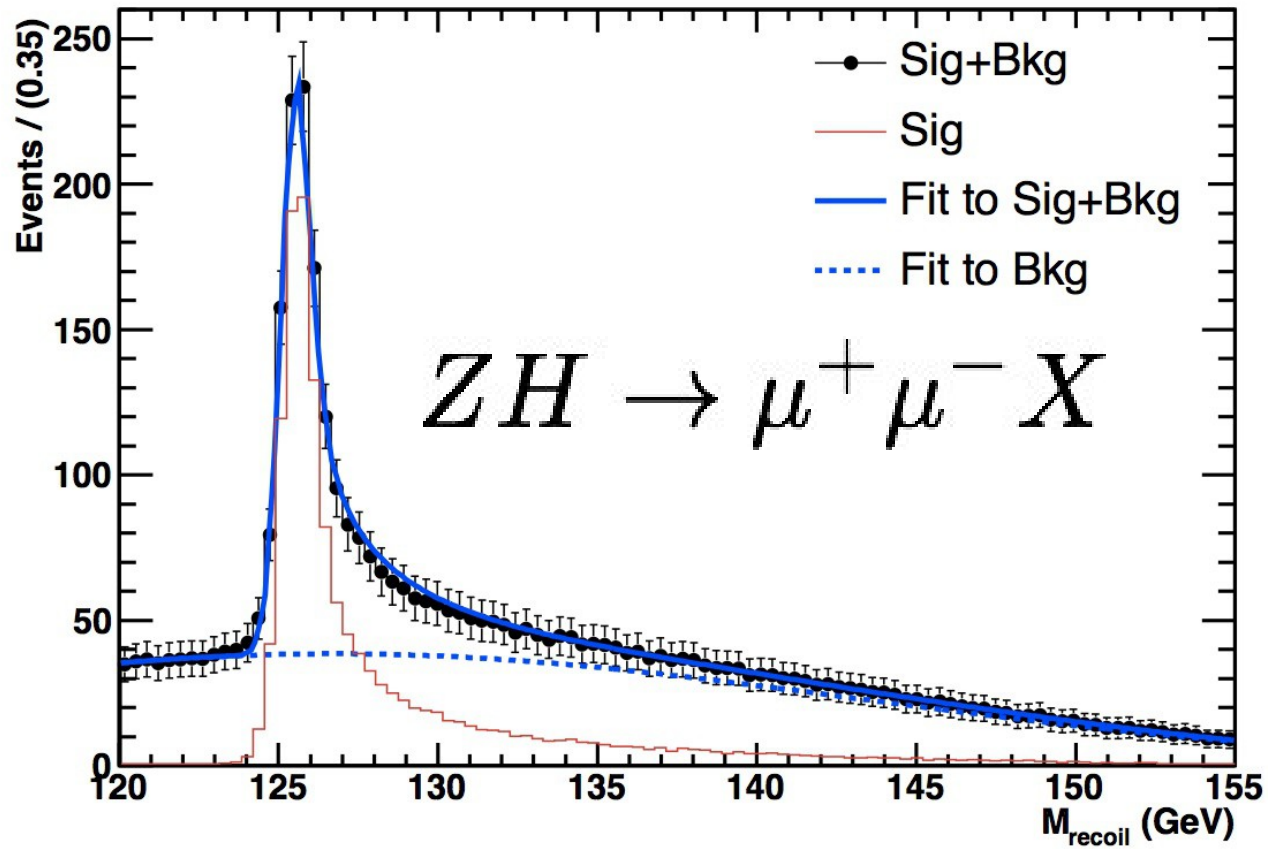
ZH dominates at 250 GeV
(~80k ev: 250 fb⁻¹)

vvH takes over at 500 GeV
(~125k ev: 500 fb⁻¹)

Higgs Mass and ZZH coupling by **Model Independent** measurement



Higgs Recoil Mass: $M_h^2 = M_{recoil}^2 = s + M_Z^2 - 2 E_Z \sqrt{s}$



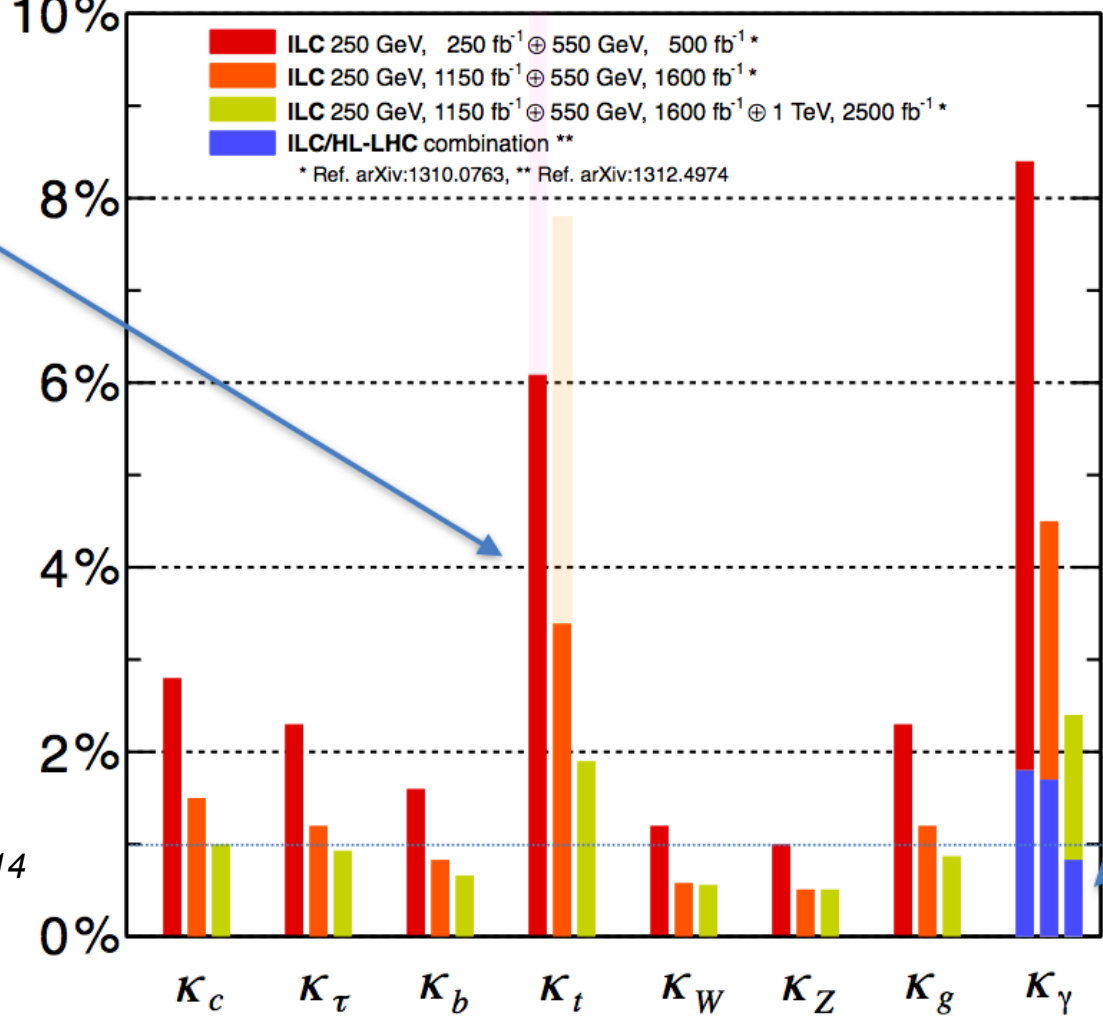
$$M_h = 125.3 \pm 0.03 \text{ GeV}$$

$$\sigma_{ZH} = 10.32 \pm 0.37 \text{ fb, } 3.6\%$$

Top Yukawa improves by going to 550 GeV

Near threshold → a factor of 4 enhancement of σ_{tth} by going from 500 GeV to 550 GeV

Projected Higgs Coupling Precision, Model-Independent Fit



LHC can precisely measure $BR(h \rightarrow \gamma\gamma) / BR(h \rightarrow ZZ^*) = (K_\gamma / K_Z)^2$

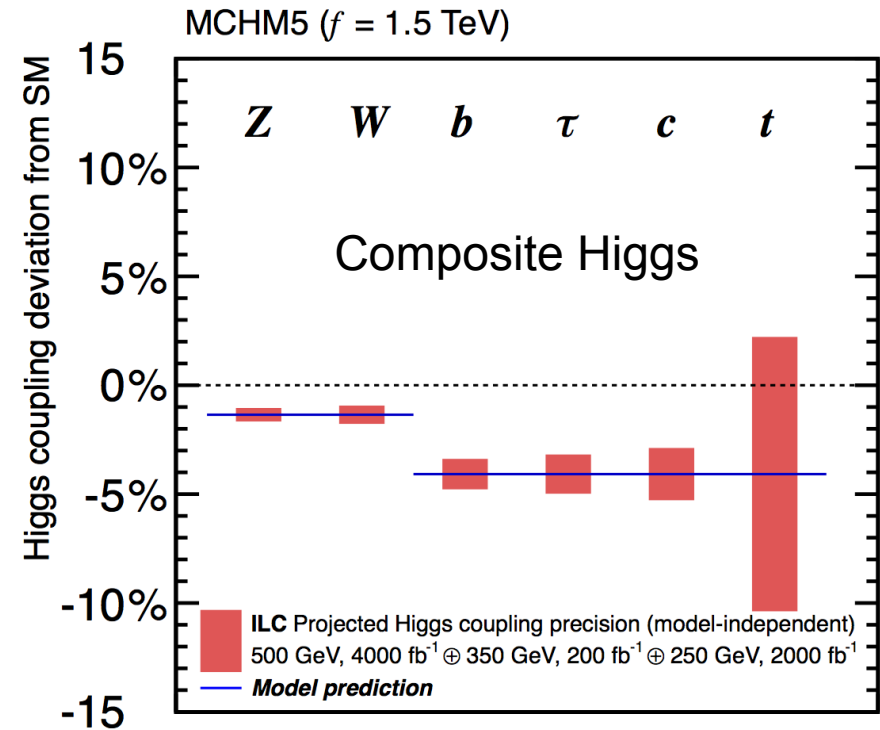
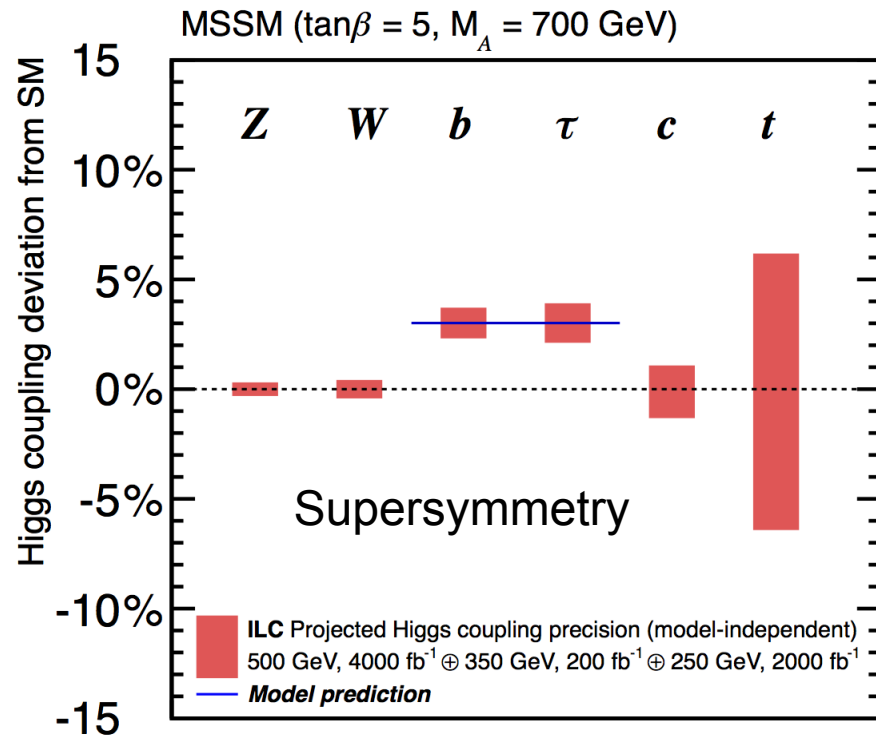
ILC can precisely measure K_Z

Better $h\gamma\gamma$ with LHC/ILC synergy

T. Tanabe, K. Fuji, LCWS14

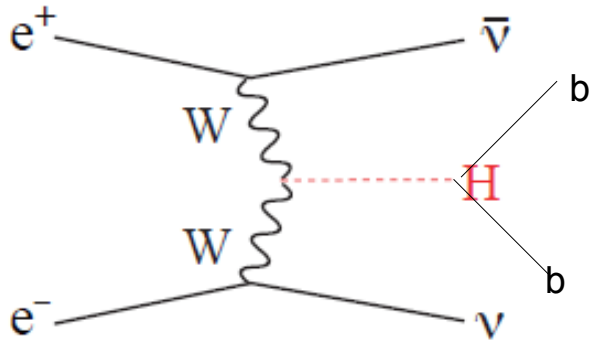
Precise measurements of relevant Higgs couplings

Coupling precision after full ILC programme



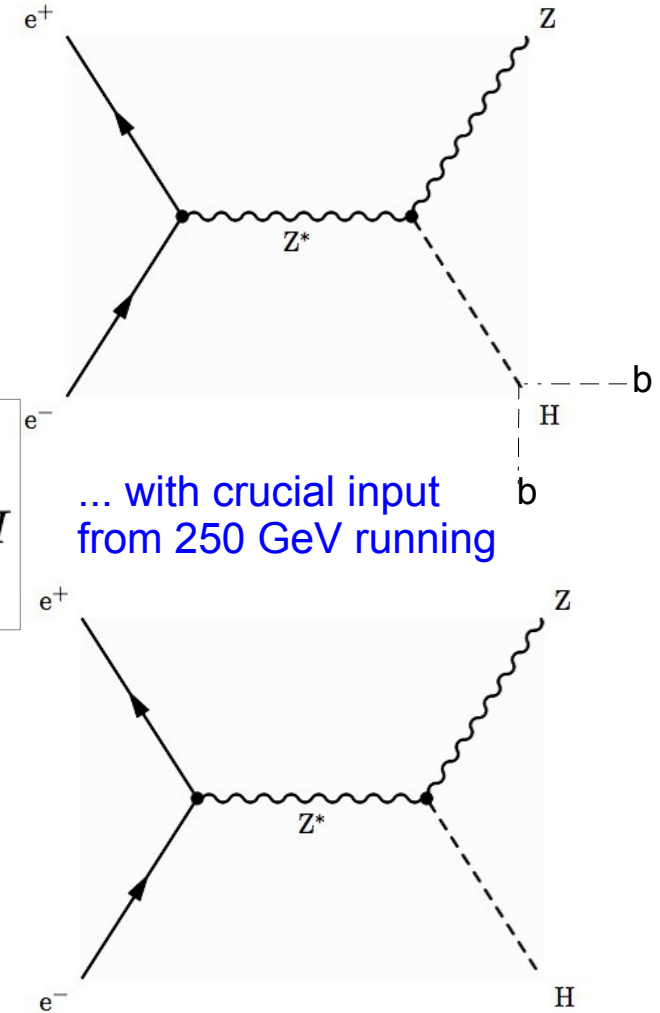
- Different new physics models lead to different patterns
- Full pattern can **only** be measured at Linear Collider

Can be derived from model independent measurements

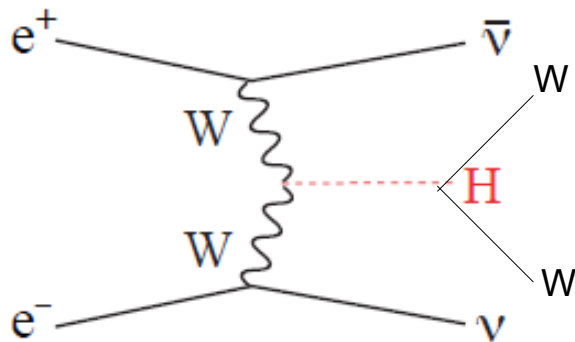


Requires running
at 500 GeV

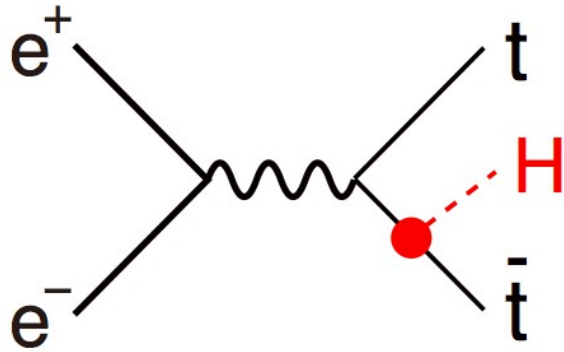
$$\Gamma_t \sim \frac{(\sigma_{\nu\bar{\nu}b\bar{b}}/\sigma_{Zb\bar{b}})^2}{(\sigma_{\nu\bar{\nu}WW}/\sigma_{ZH})} \times \sigma_{ZH}$$



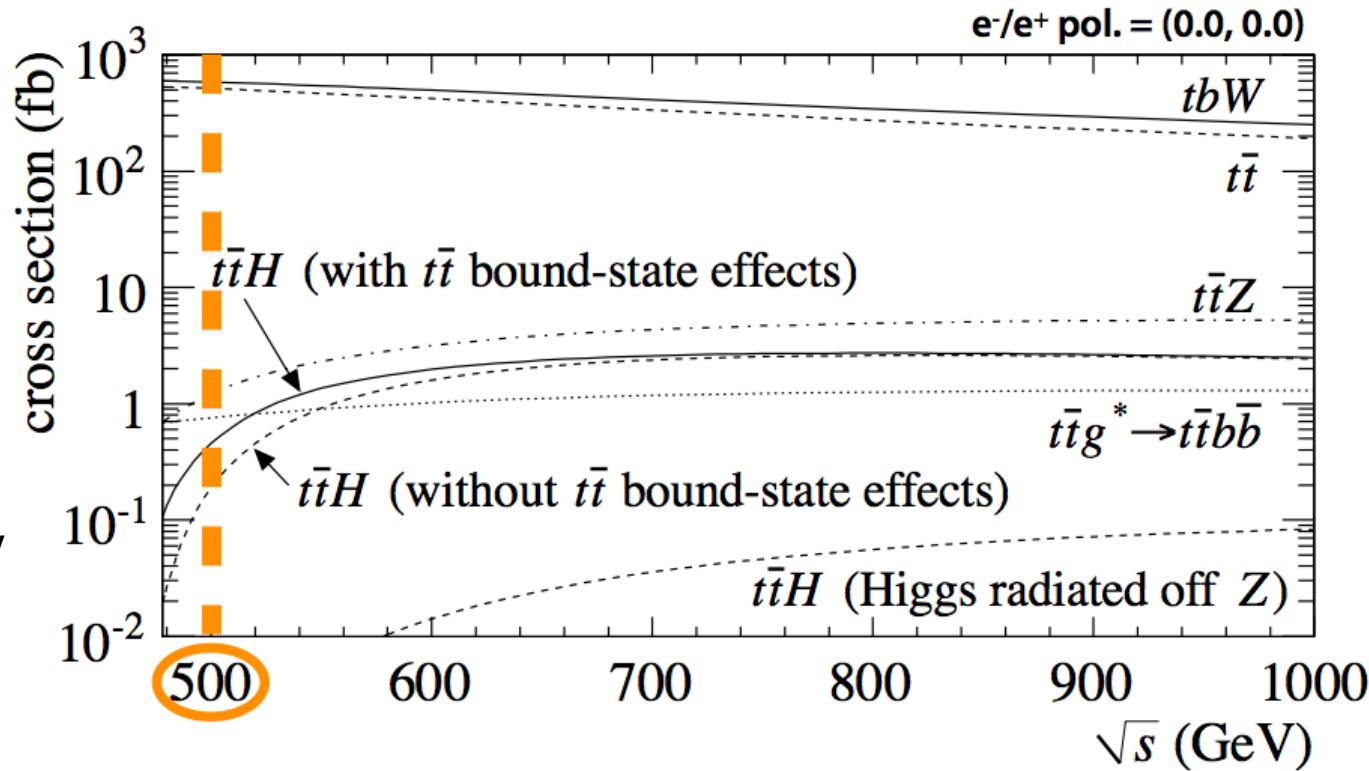
... with crucial input
from 250 GeV running



Current prospects - $\delta\Gamma_{\text{tot}} \sim 5\% @ 500 \text{ GeV}$
 $\sim 4\% @ 1 \text{ TeV}$ (2% technically possible)

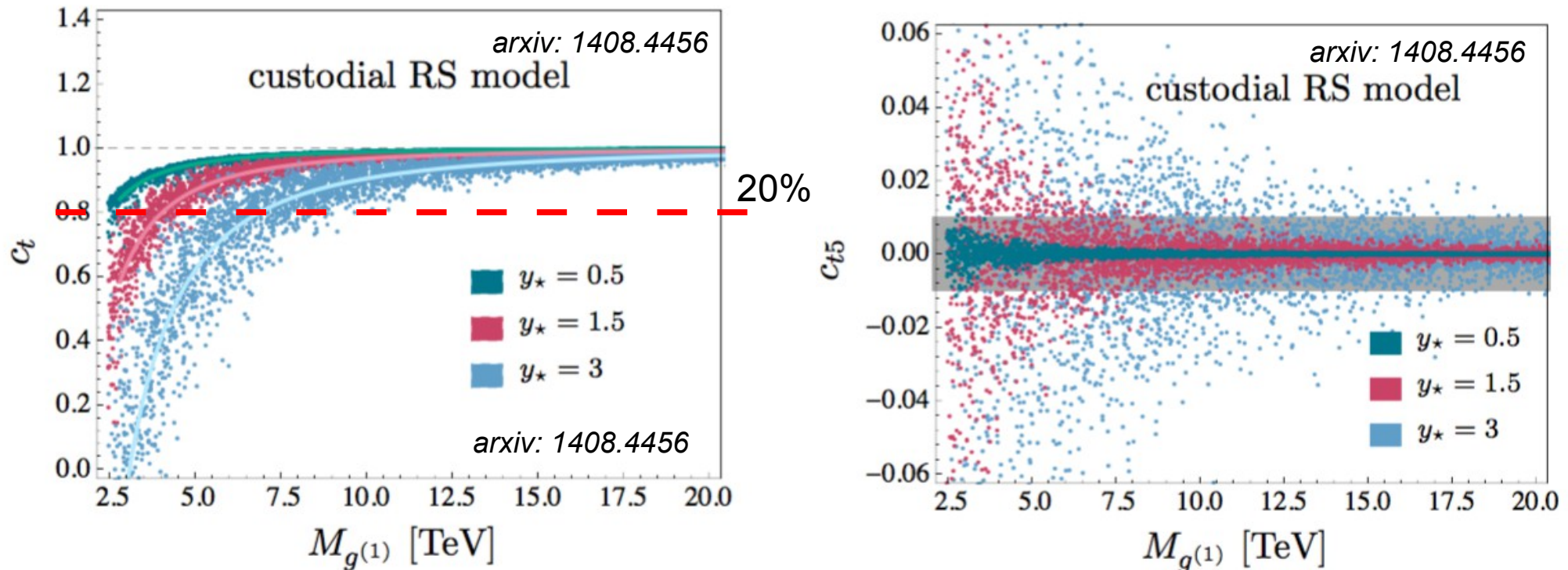


- Coupling of Higgs to heaviest particle known today
- Up to eight final state jets

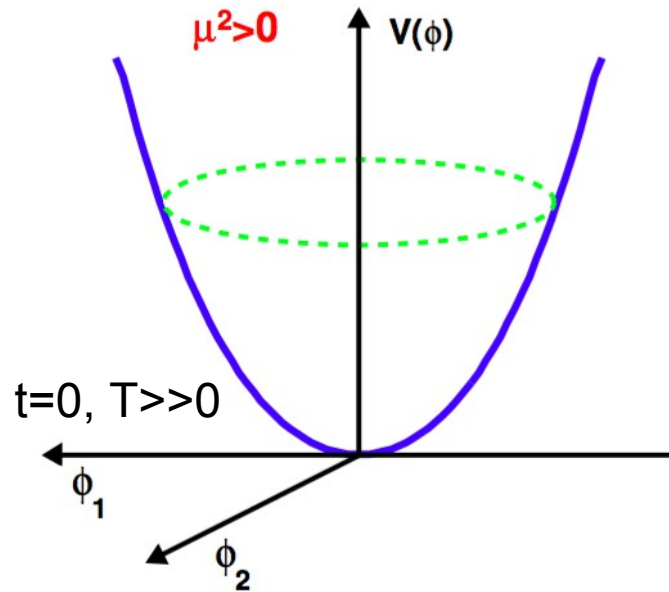


| | | |
|----------------------------|---------|---------|
| $\Delta g_{ttH} / g_{ttH}$ | 500 GeV | + 1 TeV |
| Snowmass | 7.8% | 2.0% |
| H20 | 6.3% | 1.5% |

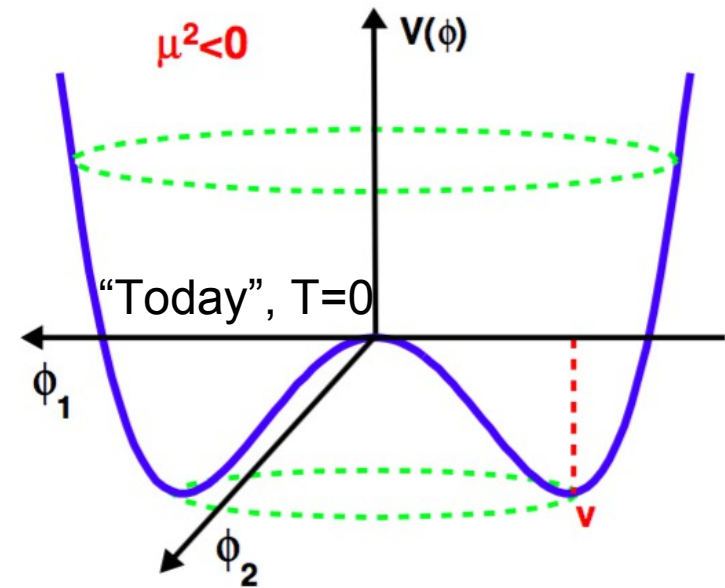
Top-Higgs couplings in “presence” of heavy particles



- Heavy particles, e.g. (Kaluza Klein) “duplicas” of SM particles provoke sizable effects
- Sensitivity to CP Violation !?



Perfect (electroweak) symmetry
and massless particles

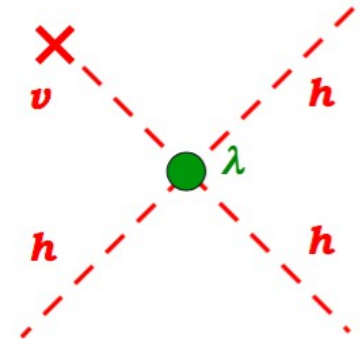


Broken (electroweak) symmetry
and massive particles

Two questions:

- Shape of “today's” Higgs Potential?

$$V(\eta) = \frac{1}{2}m^2\eta^2 + \lambda v\eta^3 + \frac{1}{4}\lambda\eta^4 \Rightarrow \text{Triple Higgs-self coupling}$$

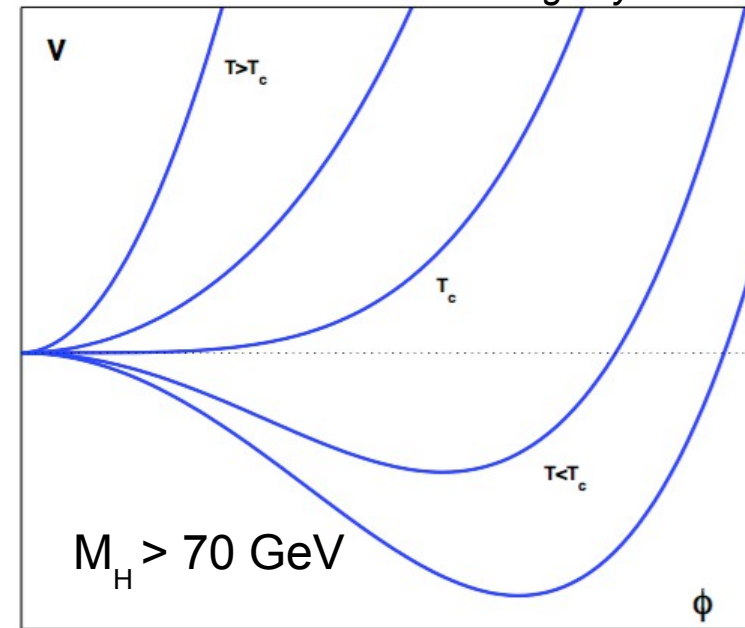
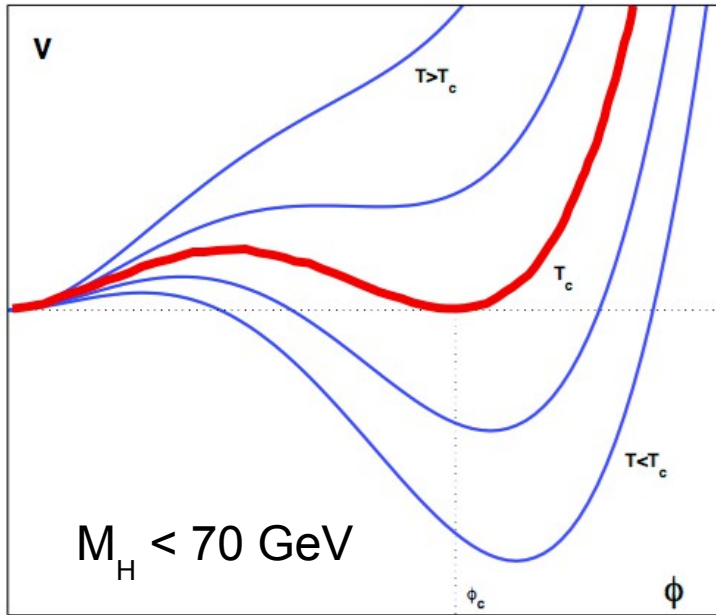


- Transition from symmetric, unbroken to broken phase?

Phase Transition in SM

Electroweak Baryogenesis requires 1st Order PT

Drawings by Y. Nir



- Coexistence Two minima at **0 and v_c at T_c**

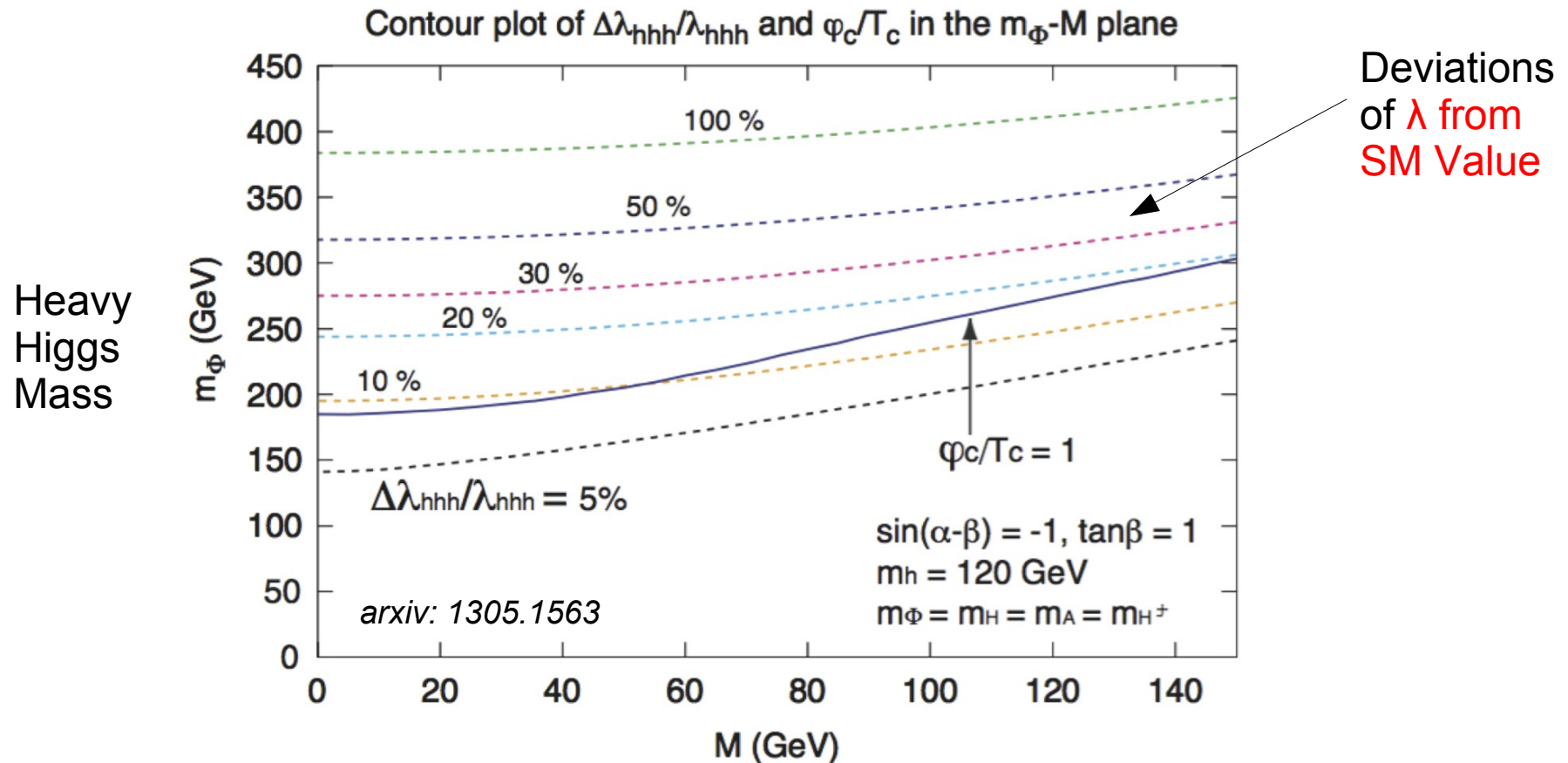
=> 1st order phase transition
and development into “today's” shape at $T=0$

- No coexistence of two minima at **0 and v_c**

=> Cross over into
“today's” shape at $T=0$

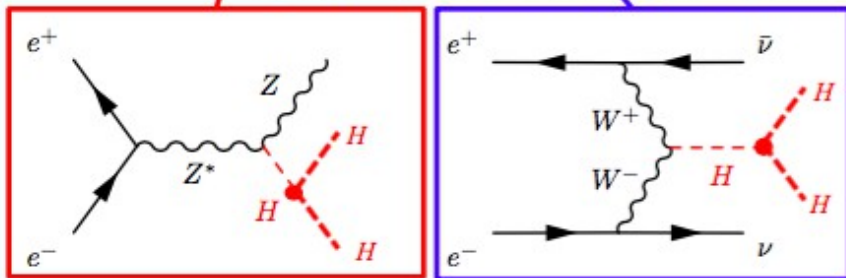
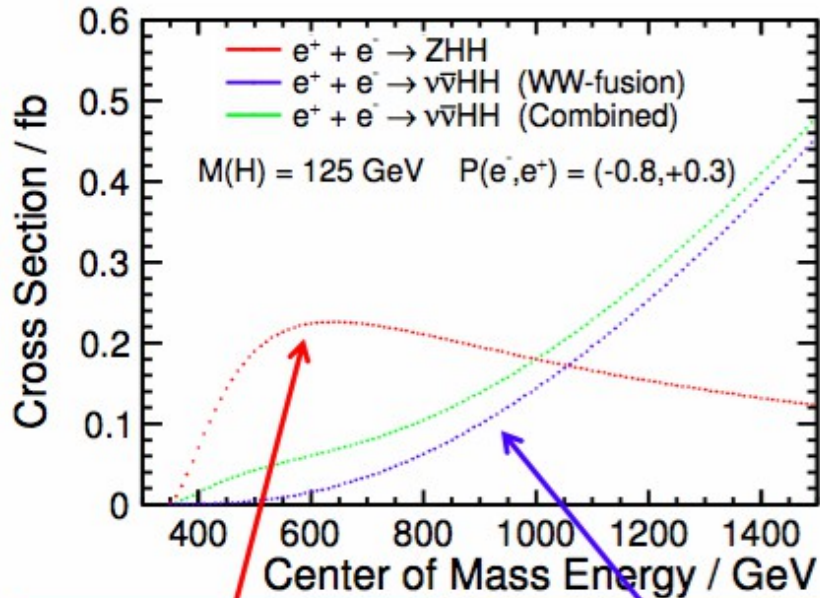
The discovered Higgs is too heavy to provoke a 1st order phase transition

=> New physics needed



- New (bosonic) particle may modify λ and enable 1st order phase transition
- Impact on measurements and achievable precisions of λ ?

Cross section vs CM energy (e+e-)



Diagrams with triple-Higgs coupling

Expected precision based on
full detector simulation studies:

ILC
500 GeV, 4 ab⁻¹
 $\delta\lambda = 27\%$

ILC
500 GeV, 4 ab⁻¹
& 1 TeV, 8 ab⁻¹
 $\delta\lambda = 10\%$

References:

J. Tian, LC-REP-2013-003
M. Kurata, LC-REP-2014-025
C. Duerig, Ph.D. thesis at DESY, 2016
HH→bbbb, bbWW* combination

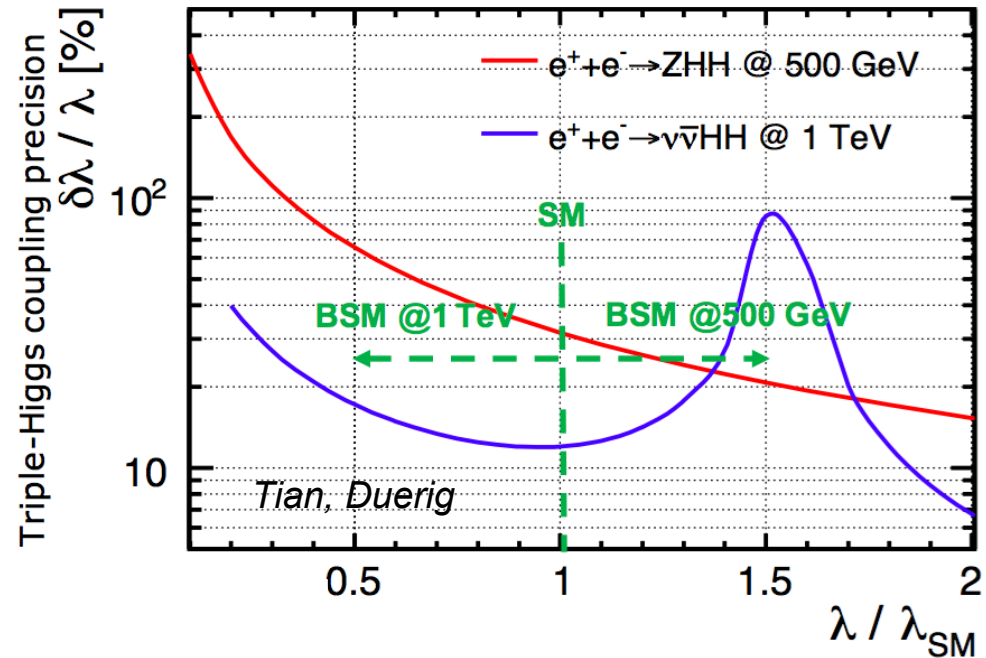
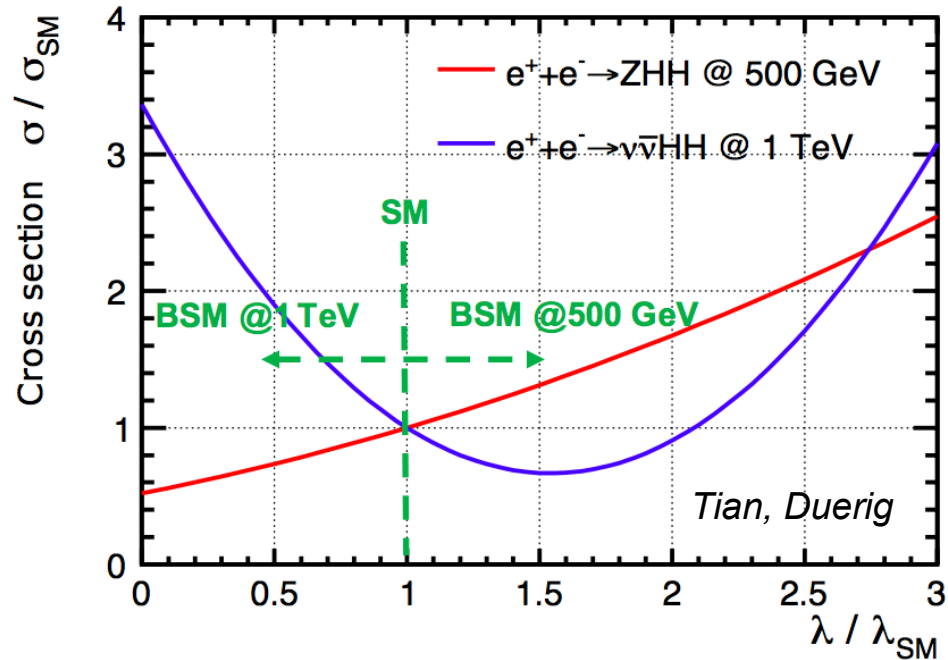
CLIC
1.4 TeV, 1.5 ab⁻¹
 $\delta\lambda = 21\%$

CLIC
1.4 TeV, 1.5 ab⁻¹
& 3 TeV, 2 ab⁻¹
 $\delta\lambda = 10\%$

References:

arXiv: 1307.5288
HH→bbbb only, upgrade in progress including bbWW*

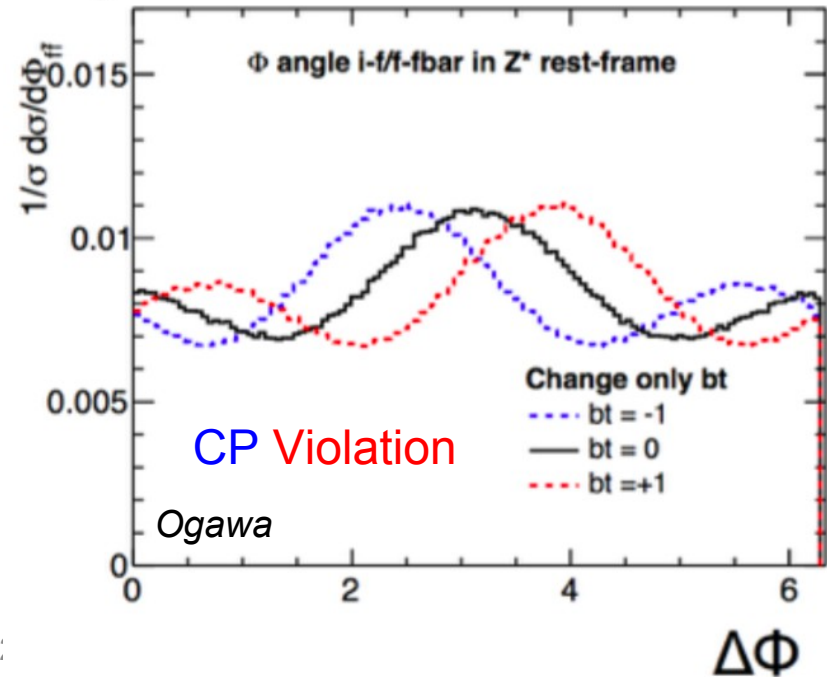
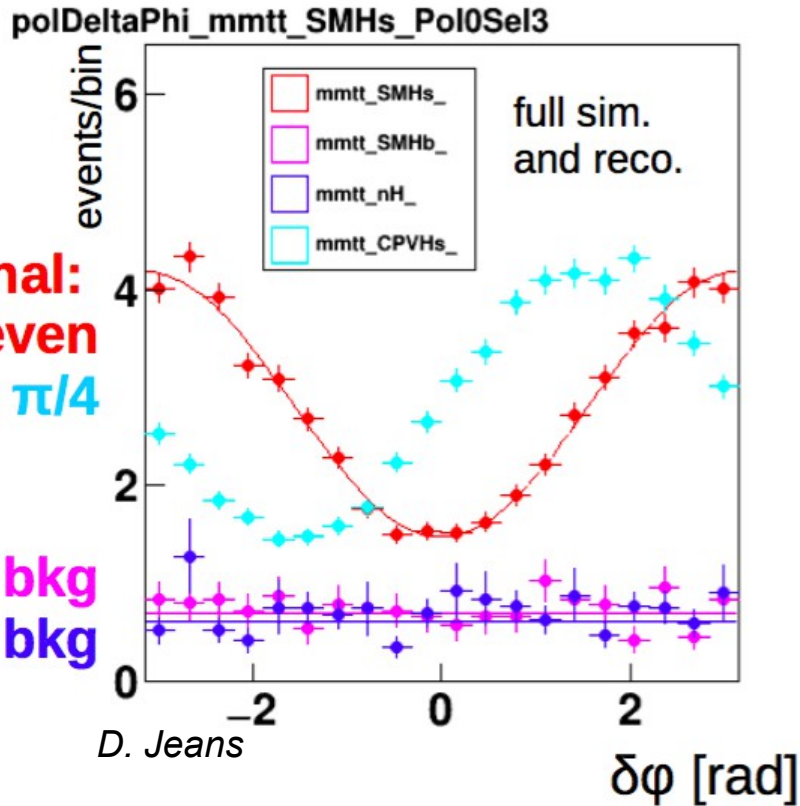
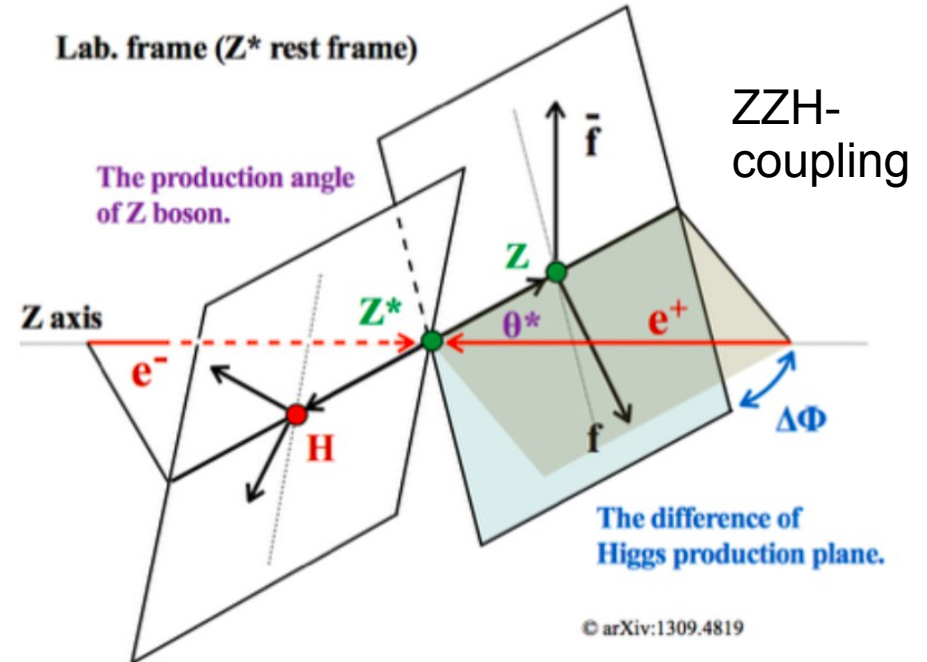
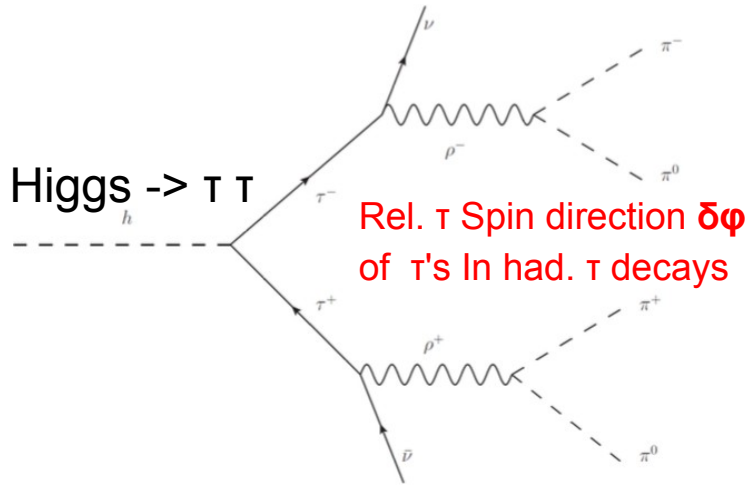
Manifestation of new physics in observables and extracted results?



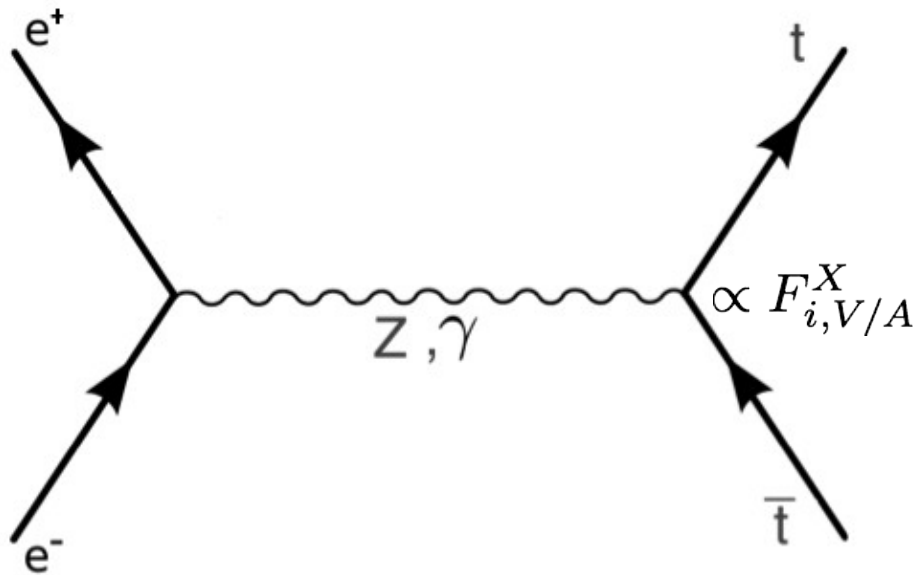
- Remarkable sensitivity of 500 GeV machine in case of large upward deviation
- 1 TeV machine superior for large upward and downward deviations

T. Tanabe, Higgs Coupling 2016

CP Violation in Higgs studies



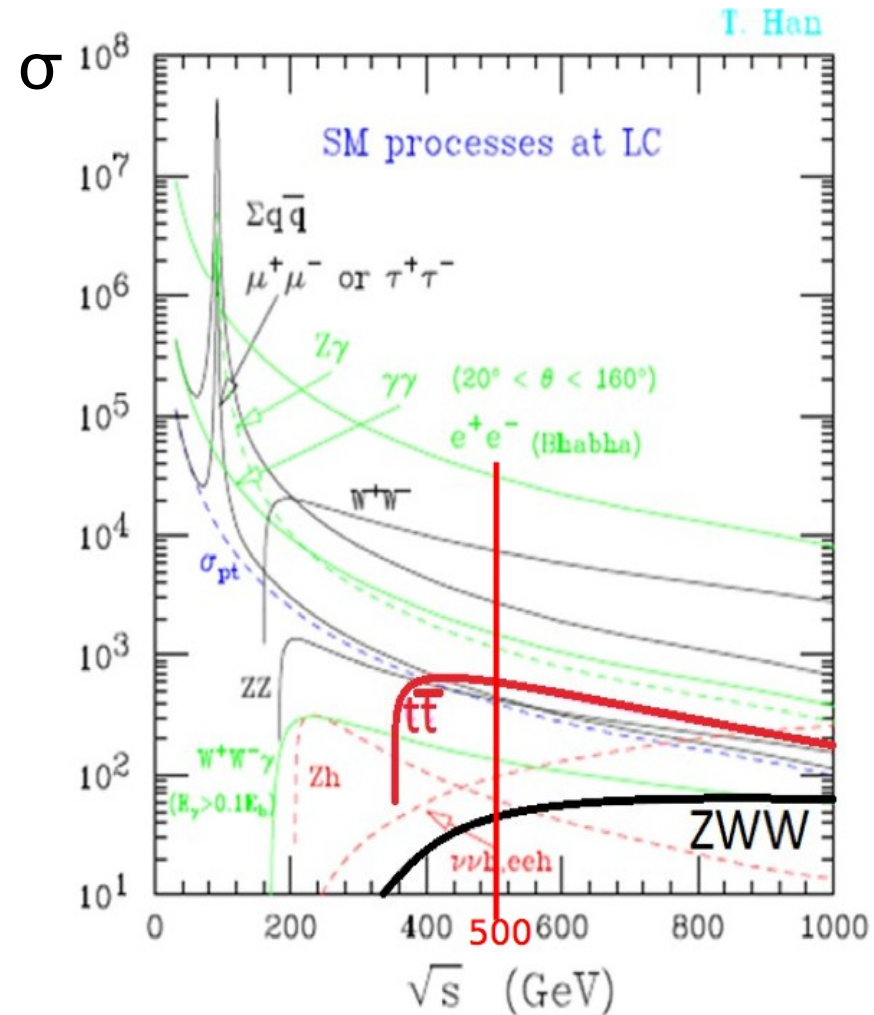
3. Top physics at the ILC



- Top quark production through electroweak processes
no competing QCD production => Small theoretical errors!

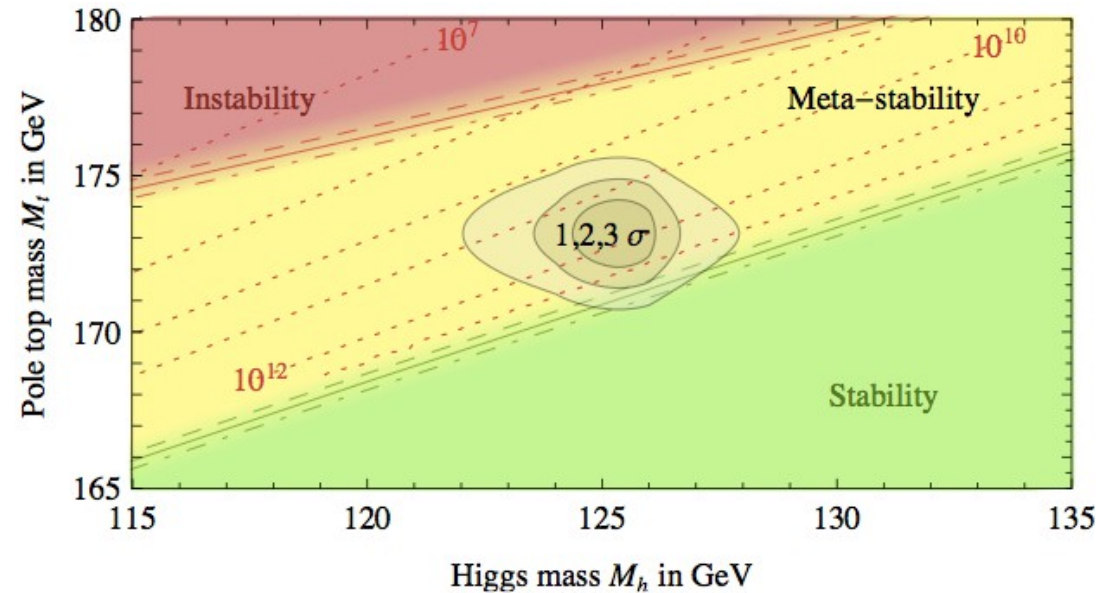
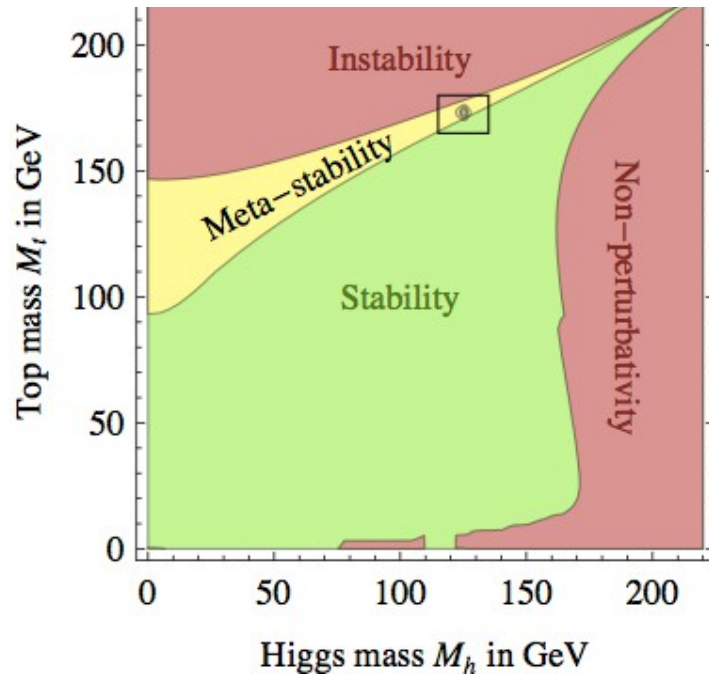
- High precision measurements

- Top quark mass at ~ 350 GeV through threshold scan
- Polarised beams allow testing chiral structure at $t\bar{t}X$ vertex
=> Precision on form factors F



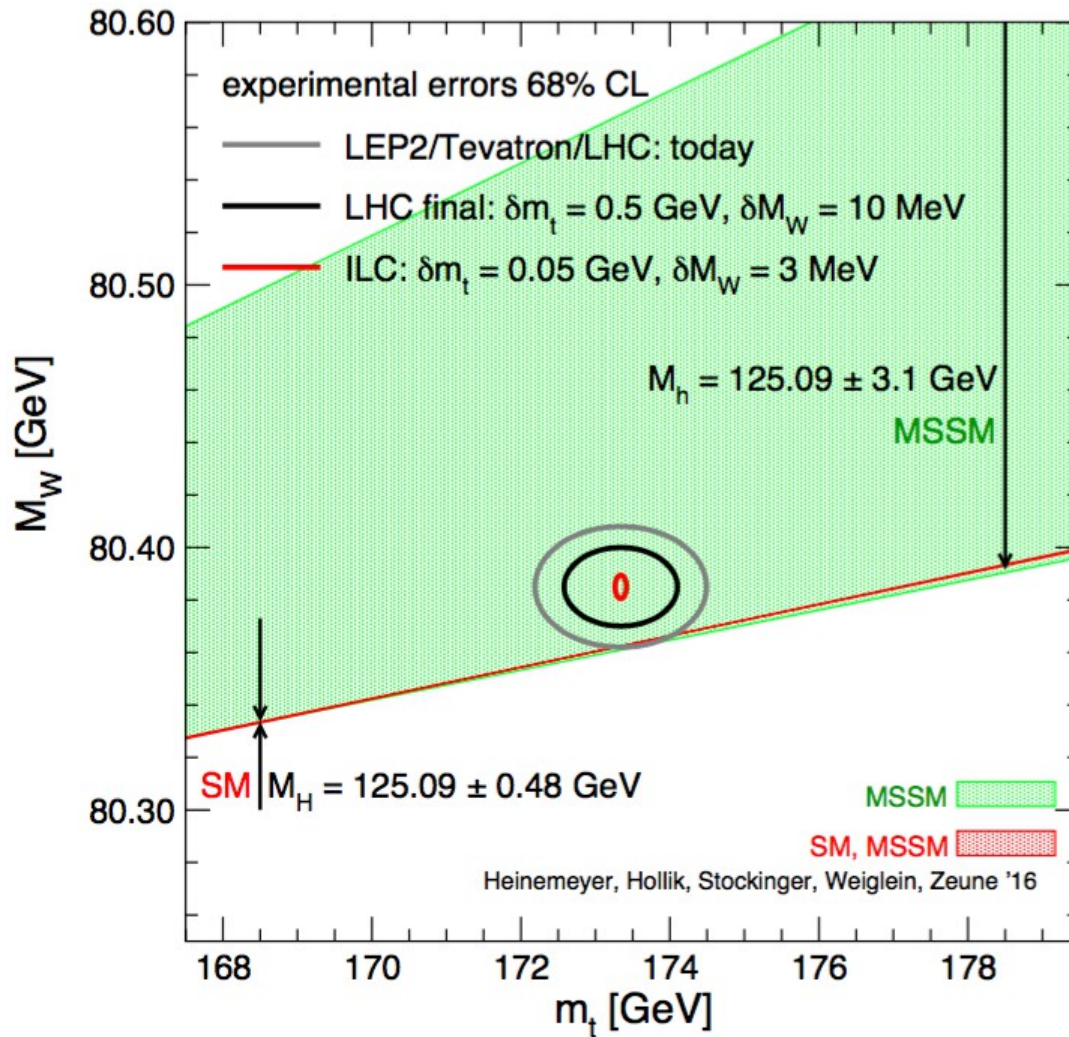


$$M_h \text{ [GeV]} > 129.4 + 1.4 \left(\frac{M_t \text{ [GeV]} - 173.1}{0.7} \right) - 0.5 \left(\frac{\alpha_s(M_Z) - 0.1184}{0.0007} \right) \pm 1.0_{\text{th}} .$$



| Type of error | Estimate of the error | Impact on M_h |
|-------------------|---|---------------------------------|
| M_t | experimental uncertainty in M_t | ± 1.4 GeV |
| α_s | experimental uncertainty in α_s | ± 0.5 GeV |
| Experiment | Total combined in quadrature | ± 1.5 GeV |
| λ | scale variation in λ | ± 0.7 GeV |
| y_t | $\mathcal{O}(\Lambda_{\text{QCD}})$ correction to M_t | ± 0.6 GeV |
| y_t | QCD threshold at 4 loops | ± 0.3 GeV |
| RGE | EW at 3 loops + QCD at 4 loops | ± 0.2 GeV |
| Theory | Total combined in quadrature | ± 1.0 GeV |

Uncertainty on (**pole**)
top quark mass dominates
uncertainty on stability
conditions



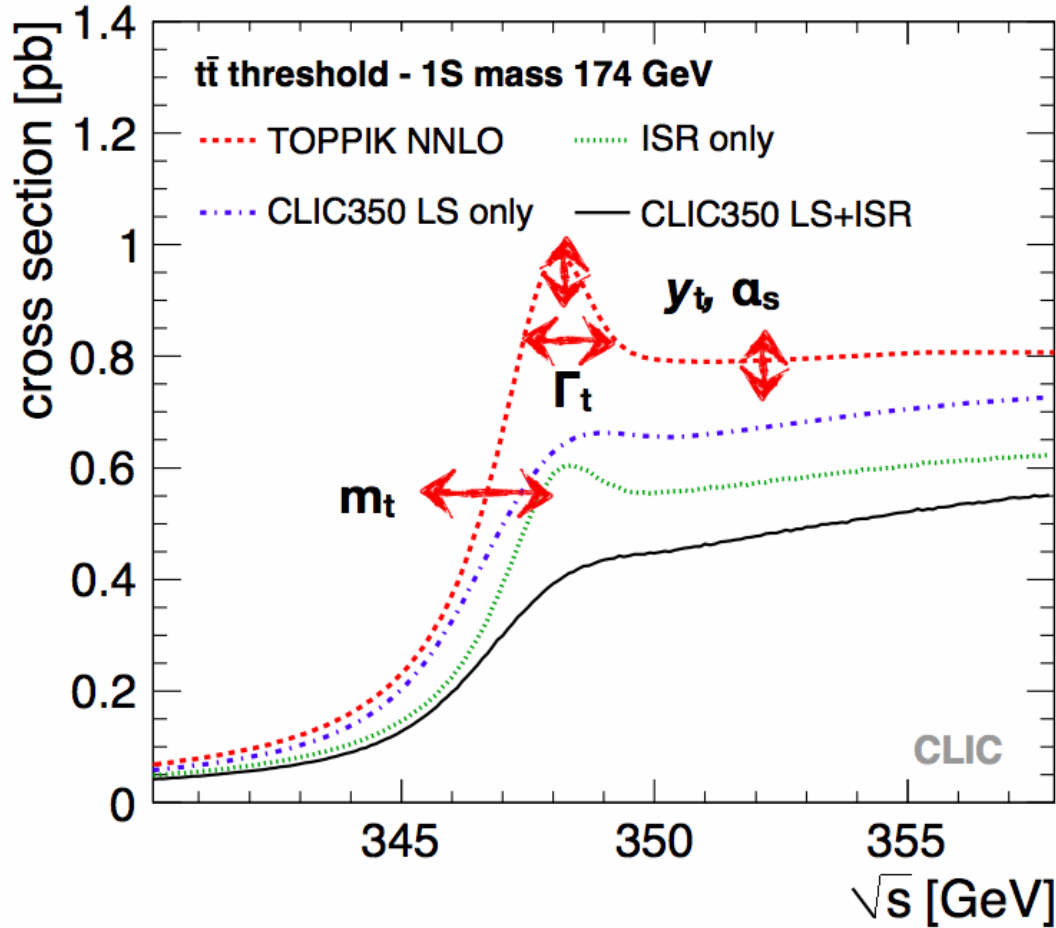
Precise Top (and W) mass crucial to test compatibility of measured Higgs mass

MS might not be sufficient to explain Higgs mass

LHC may not reach sufficient discriminative power

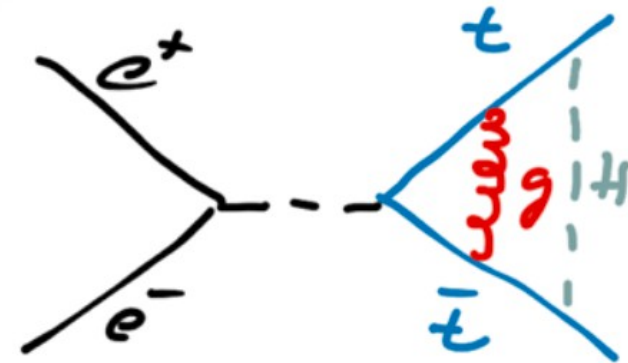
A lepton collider will

Small size of $t\bar{t}$ “bound state” at threshold ideal premise for precision physics



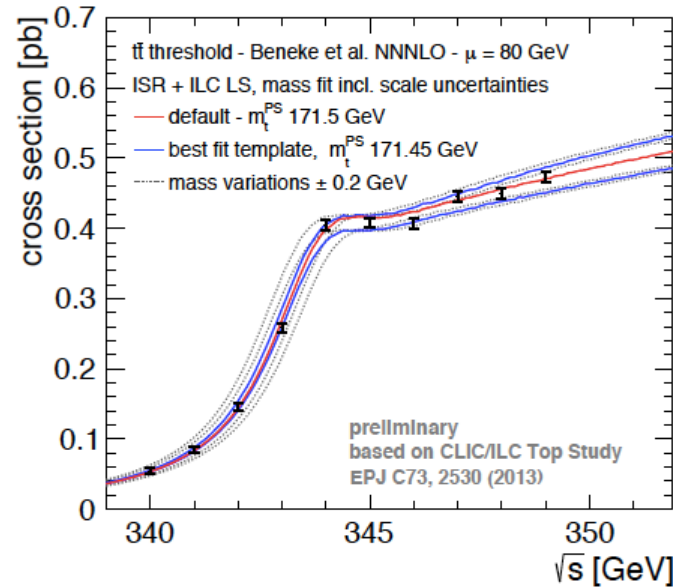
Cross section around threshold is affected by several properties of the top quark and by QCD

- Top mass, width Yukawa coupling
- Strong coupling constant



Effects of some parameters are correlated:
Dependence on Yukawa coupling rather weak,
Precise external α_s helps

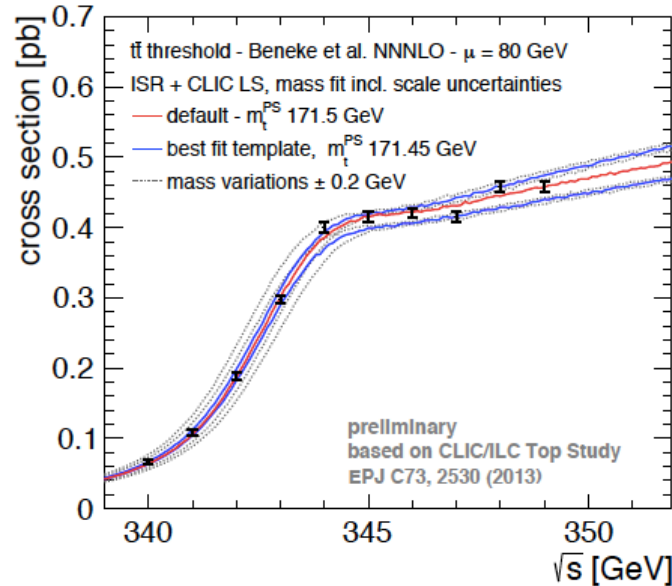
-> α_s discussion in top/QCD parallel by Kluth



ILC

Fit uncertainty:
28.5 MeV (18 MeV stat)

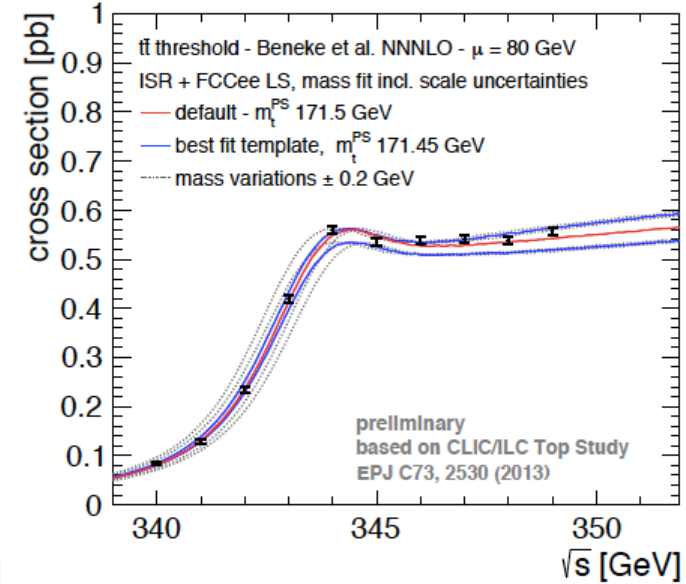
Scale uncertainty:
40 MeV



CLIC

Fit uncertainty:
31 MeV (21 MeV stat)

Scale uncertainty:
42 MeV

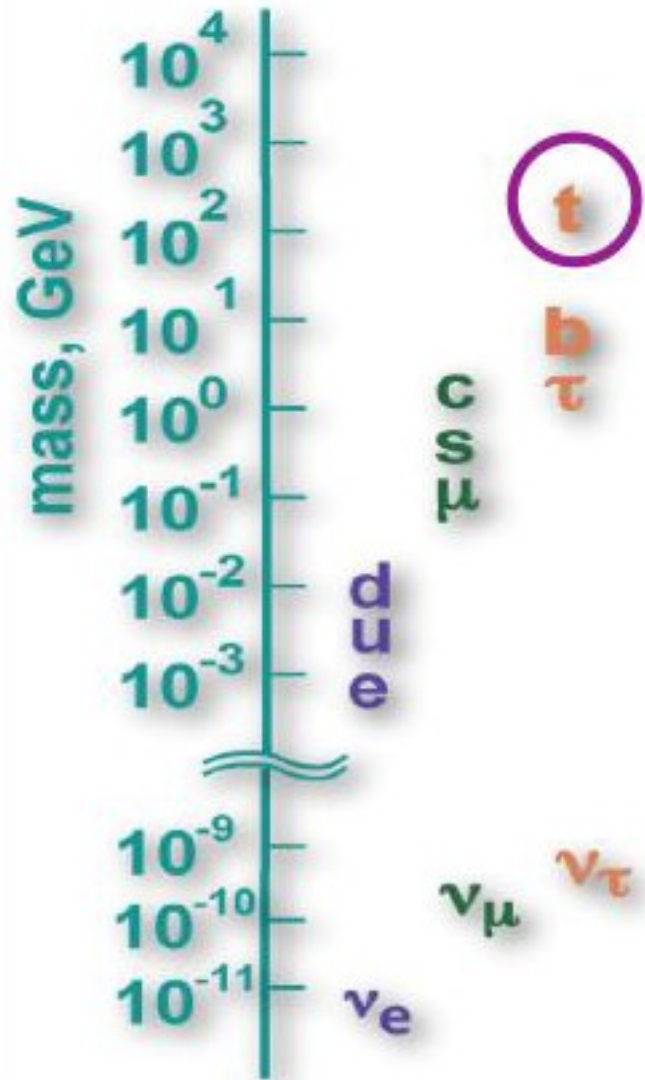


FCC-ee

Fit uncertainty:
27 MeV (15 MeV stat)

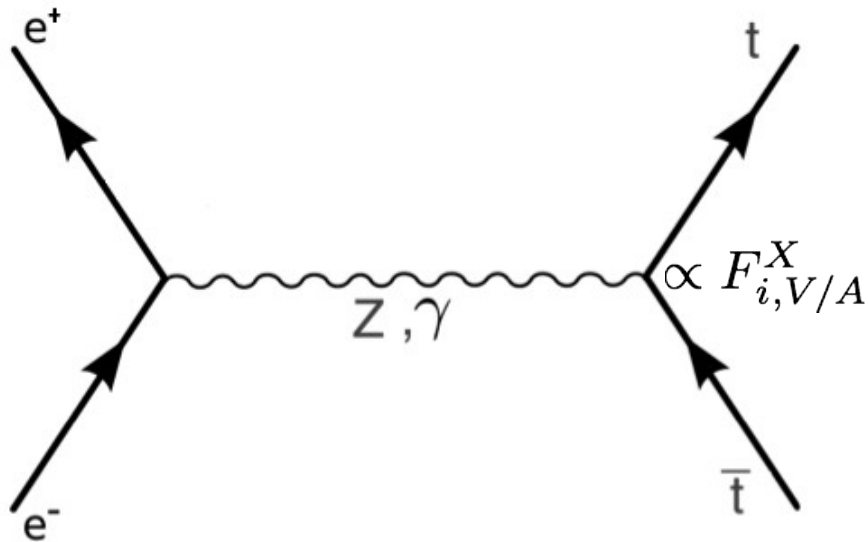
Scale uncertainty:
40 MeV

New ideas on top mass determination see talks by Fuster, Maier and Marquardt



- SM does not provides no explanation for mass spectrum of fermions (and gauge bosons)
- Fermion mass generation closely related to the origin electroweak symmetry breaking
- Expect residual effects for particles with masses closest to symmetry breaking scale
 - A_{FB} anomaly at LEP for b quark

Strong motivation to study chiral structure of top vertex in high energy e^+e^- collisions



Manifestation of New Physics:

- Modification of Z_{tt} coupling

Mixing between top and partners
Mixing Z/Z'

- s-channel exchange of New Z'
Including interference effects

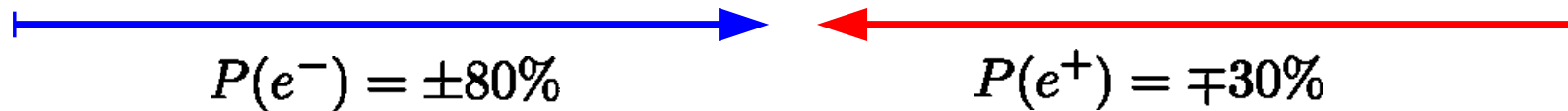
$$\Gamma_{\mu}^{ttX}(k^2, q, \bar{q}) = -ie \left\{ \gamma_{\mu} (F_{1V}^X(k^2) + \gamma_5 F_{1A}^X(k^2)) + \frac{\sigma_{\mu\nu}}{2m_t} (q + \bar{q})^{\nu} (iF_{2V}^X(k^2) + \gamma_5 F_{2A}^X(k^2)) \right\}, \quad (2)$$

Pure γ or pure Z^0 : $\sigma \sim (F_i)^2 \Rightarrow$ No sensitivity to sign of Form Factors

Z^0/γ interference : $\sigma \sim (F_i) \Rightarrow$ Sensitivity to sign of Form Factors

At ILC **no** separate access to ttZ or tty vertex, but ...

ILC 'provides' two beam polarisations



There exist a number of observables sensitive to chiral structure, e.g.

$$\sigma_I \quad A_{FB,I}^t = \frac{N(\cos\theta > 0) - N(\cos\theta < 0)}{N(\cos\theta > 0) + N(\cos\theta < 0)} \quad (F_R)_I = \frac{(\sigma_{t_R})_I}{\sigma_I}$$

x-section

Forward backward asymmetry

Fraction of right handed top quarks

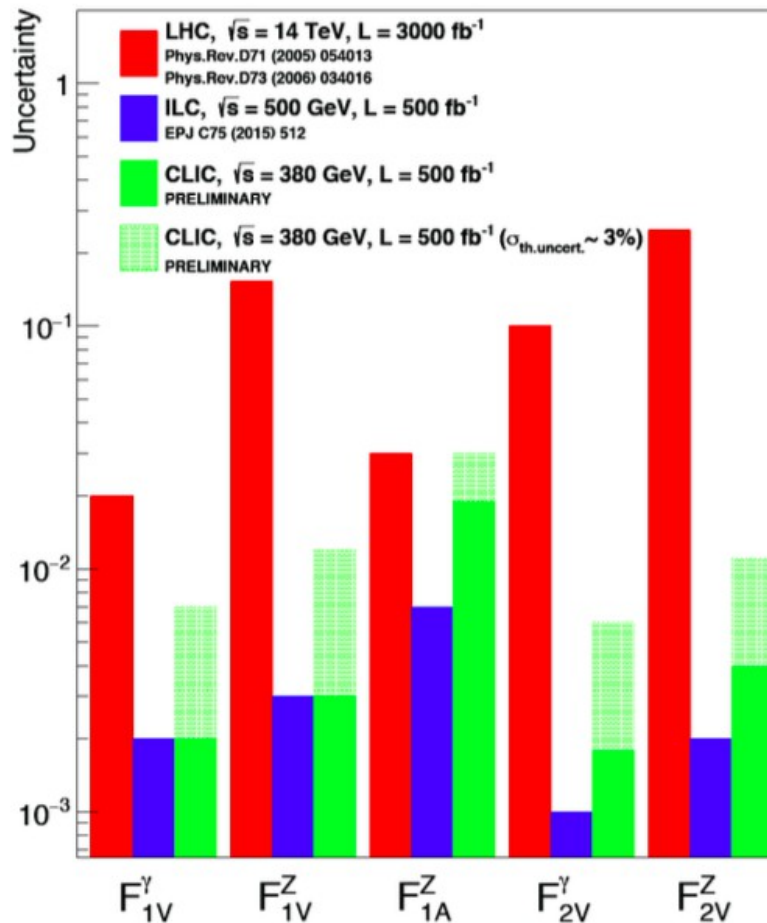


Extraction of relevant unknowns

$$F_{1V}^\gamma, F_{1V}^Z, F_{1A}^\gamma = 0, F_{1A}^Z \quad \text{or equivalently} \quad g_L^\gamma, g_R^\gamma, g_L^Z, g_R^Z$$

$$F_{2V}^\gamma, F_{2V}^Z$$

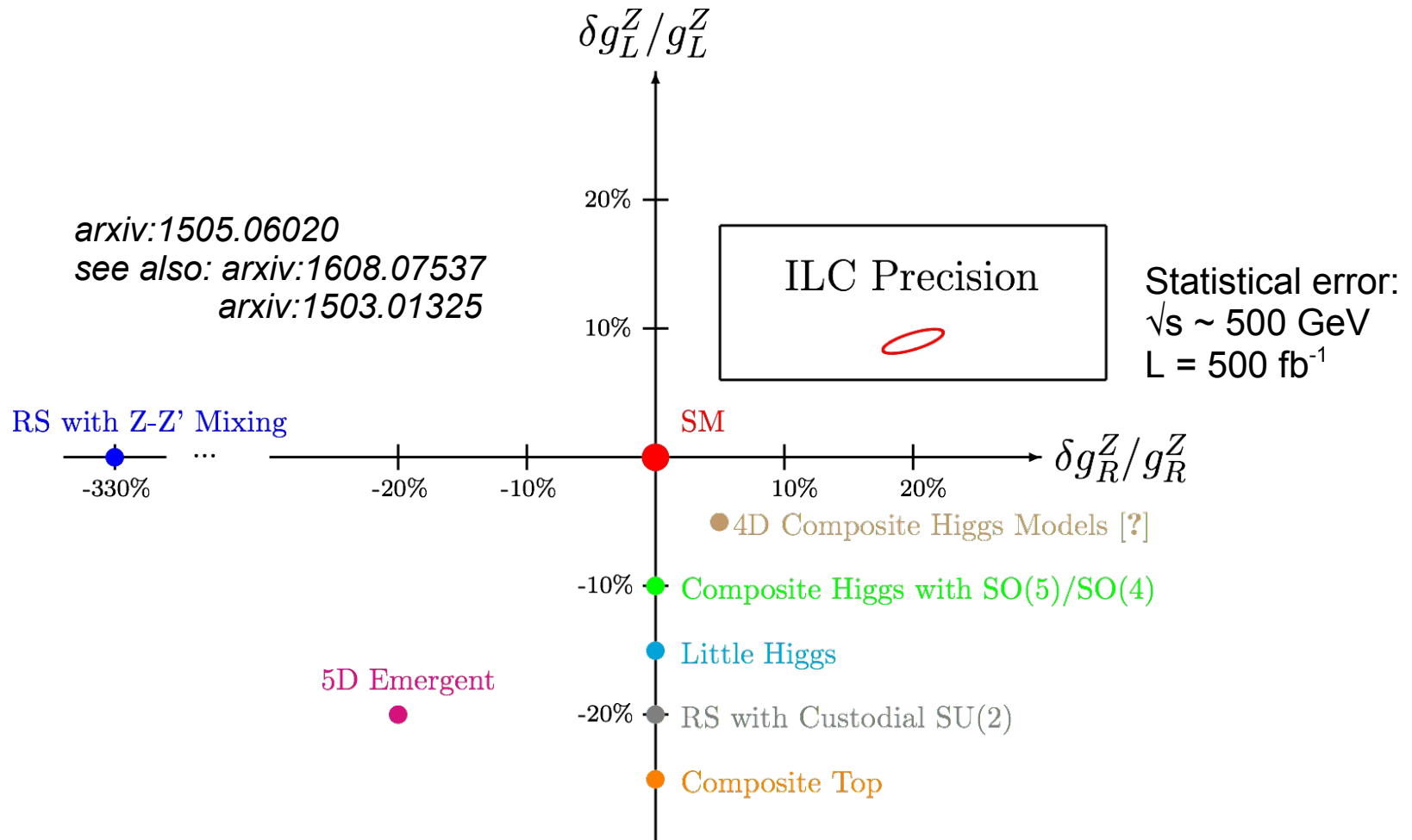
Accuracy on CP conserving couplings



- ILC might be up to two orders of magnitude more precise than LHC ($\sqrt{s} = 14$ TeV, 3000 fb $^{-1}$)
- Large disentangling of couplings for ILC thanks to polarised beams
- One variable at a time for LHC
LHC projections from 8 years old study
- Note
Minimal Lumi scenario for ILC
Maximal Lumi scenario for CLIC
Maximal Lumi scenario for LHC
- CP Violating couplings see talk by Vos
- Alternative by Matrix Element Method see talk by Sato

LC promises to be high precision machine for electroweak top couplings

Top is primary candidate to be a messenger new physics in many BSM models
Incorporating compositeness and/or extra dimensions



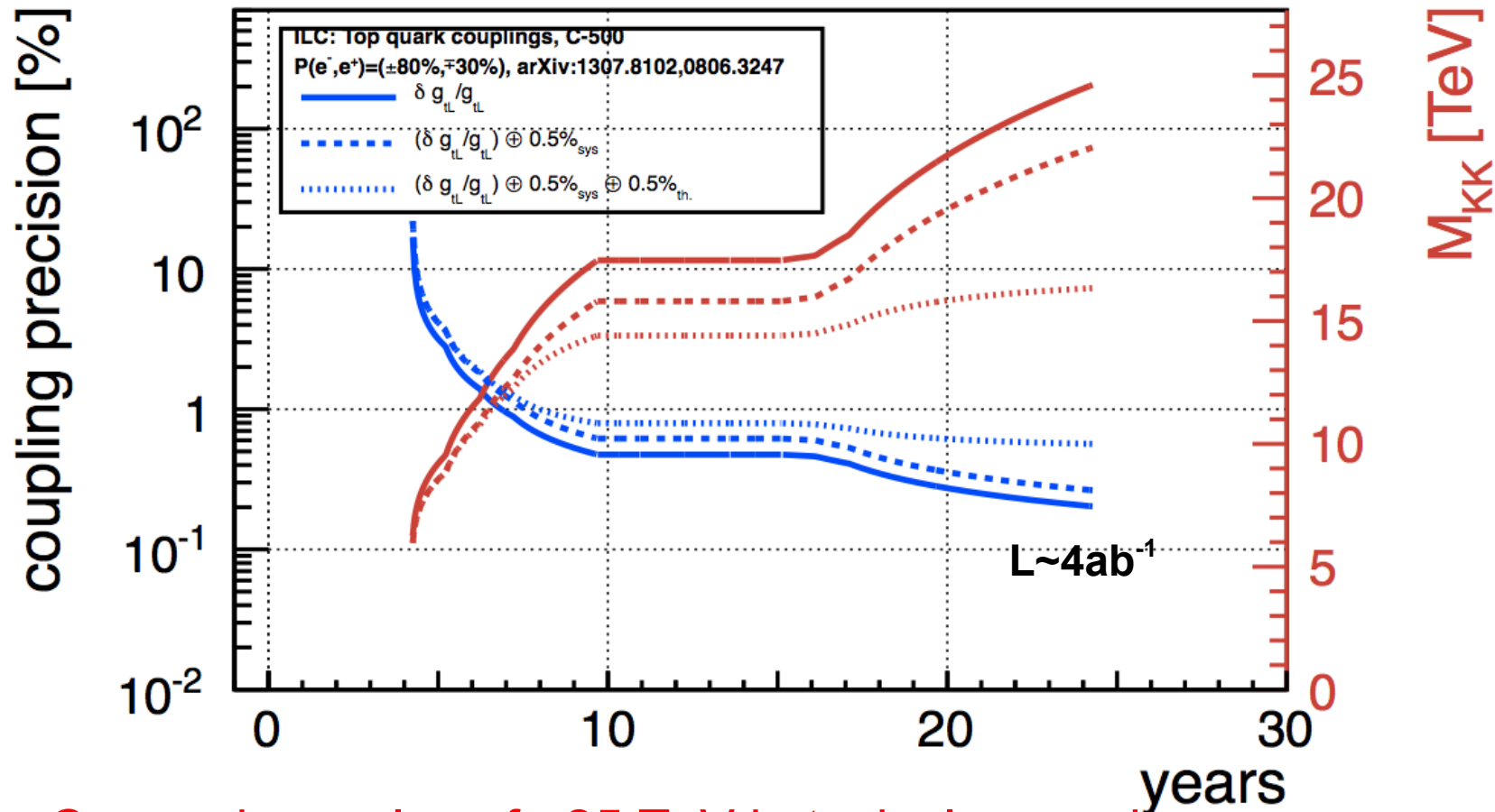
Precision expected for top quark couplings will allow distinguishing between models

Remark: All presented models are compatible with LEP elw. precision data

Interpretation in EFT Framework, see talk by Vos

New physics reach for typical BSM scenarios with composite Higgs/Top and or extra dimensions

Based on phenomenology described in Pomerol et al. arXiv:0806.3247



Can probe scales of ~ 25 TeV in typical scenarios

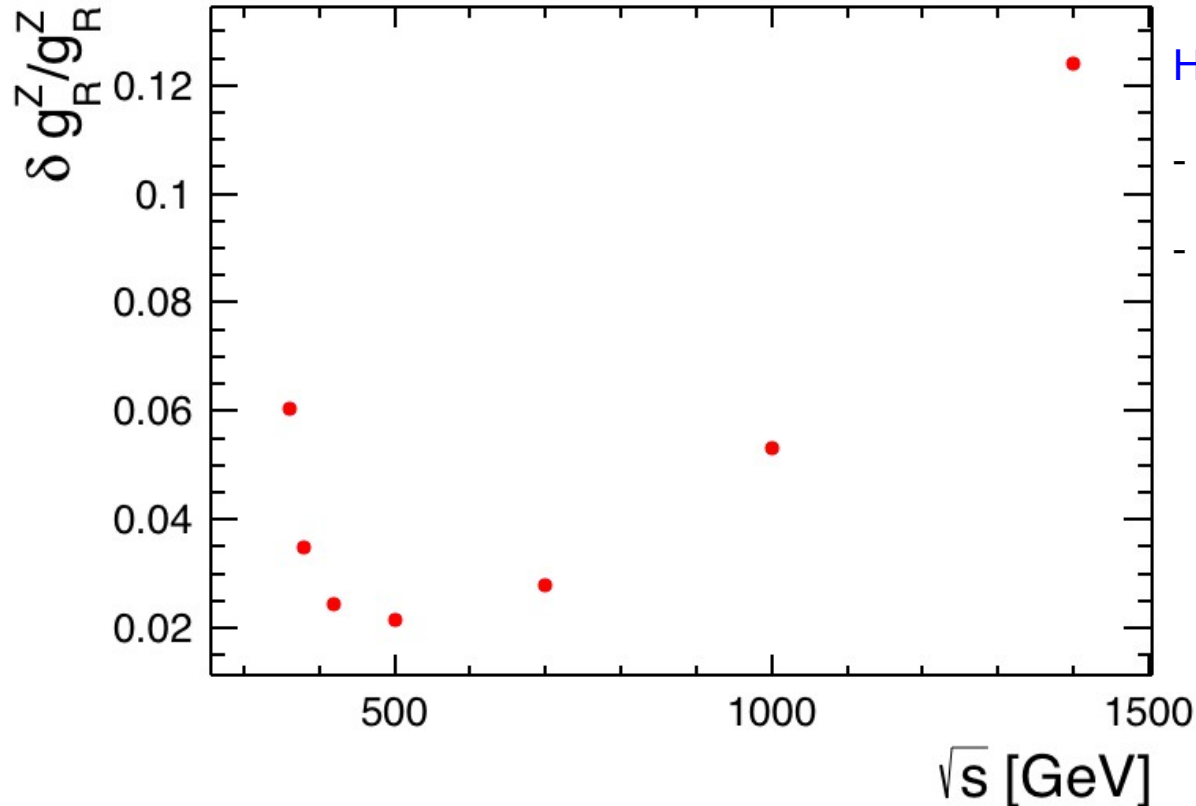
(... and up to 80 TeV for extreme scenarios)

=> Important guidance for e.g. 100 TeV pp-collider

... simplified discussion

Small cms energies:

- Vanishing axial vector coupling
- QCD uncertainties
- Lumi decreases at linear colliders



High cms energies:

- Quickly decreasing cross section
- ... partially compensated by increasing luminosity

Broad minimum between 400 and 700 GeV

$\sqrt{s} \sim 500$ GeV is “sweet spot” for coupling measurements

However:

- Sensitivity to CP violating Higgs at smaller cms energies
- New physics at higher energies may increase cross section



- LC is versatile machine for precision physics at the TeV scale
Polarised beams to test chiral theory!
- Higgs and top quark are physics guaranteed
(My conviction) both are messengers to New Physics
- Exciting Discovery potential

Full set of SM couplings to Higgs

Discovery of invisible decays by Higgs-strahlung

Direct Measurement of Higgs self-coupling: **Unique at LC**

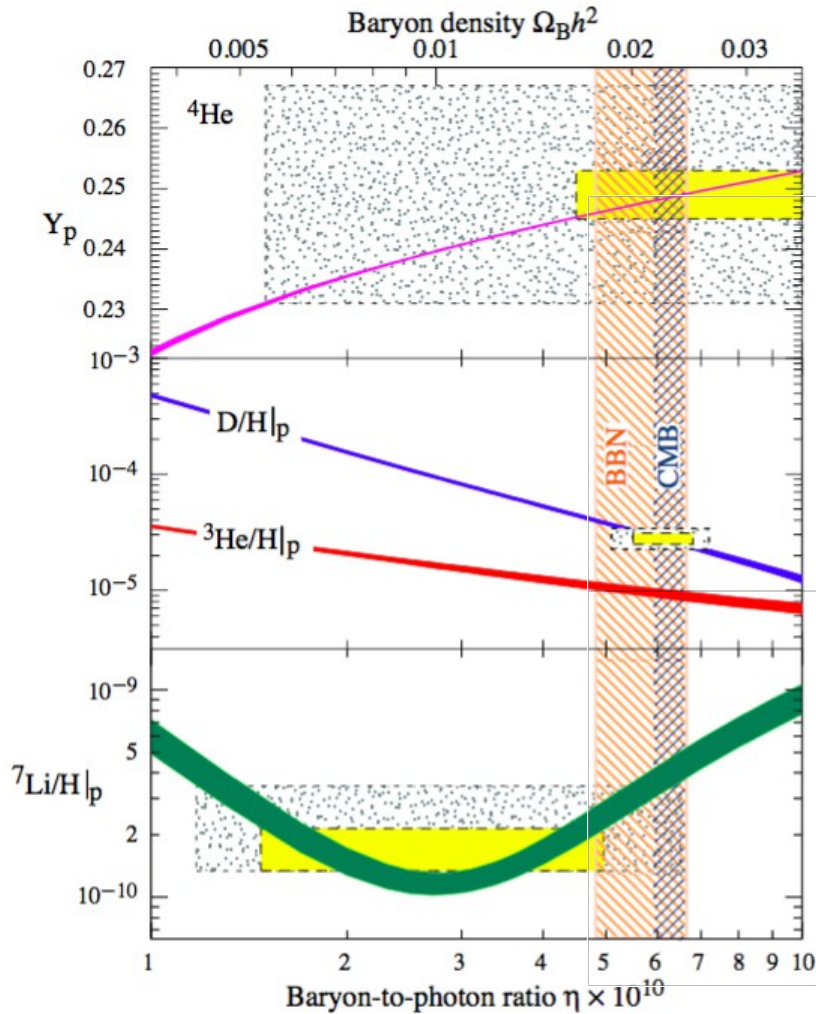
Direct Top-Higgs coupling: **LC only e+e- machine**

Precision of top couplings: **Unique at LC**

Top physics programme completed by superb mass measurement

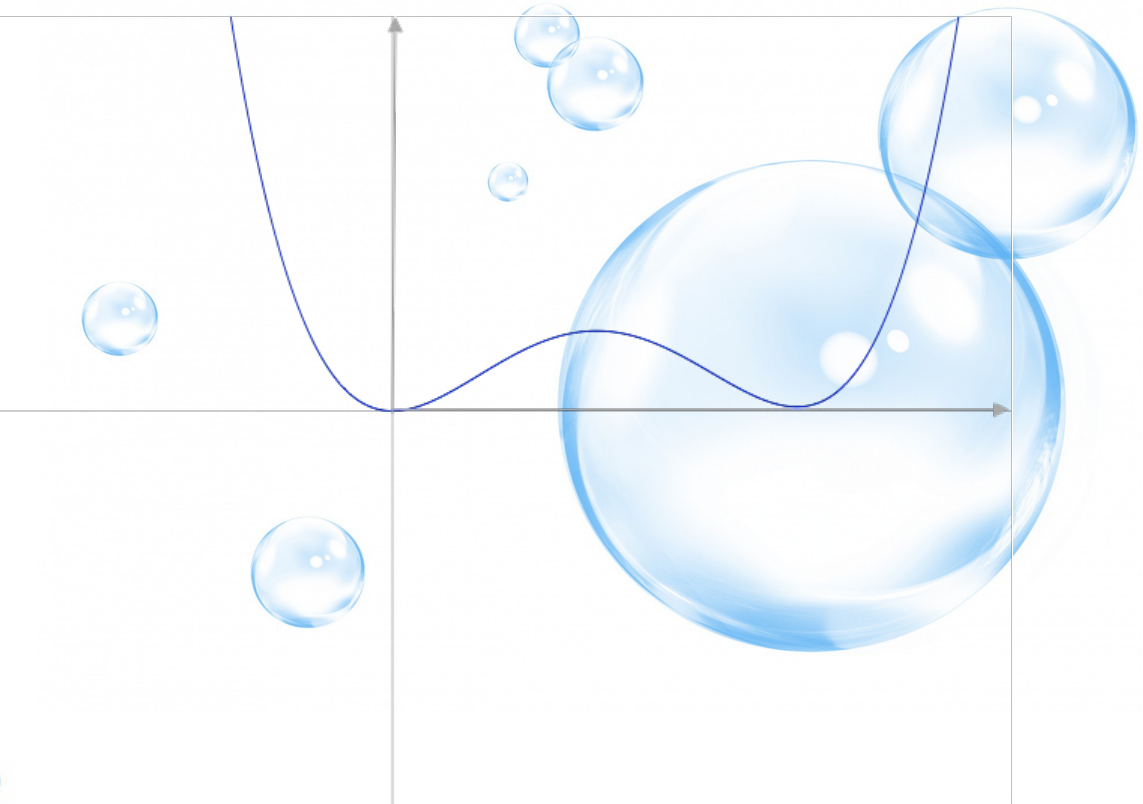
Backup

Baryon Asymmetry of the Universe BAU



Abundance of light elements

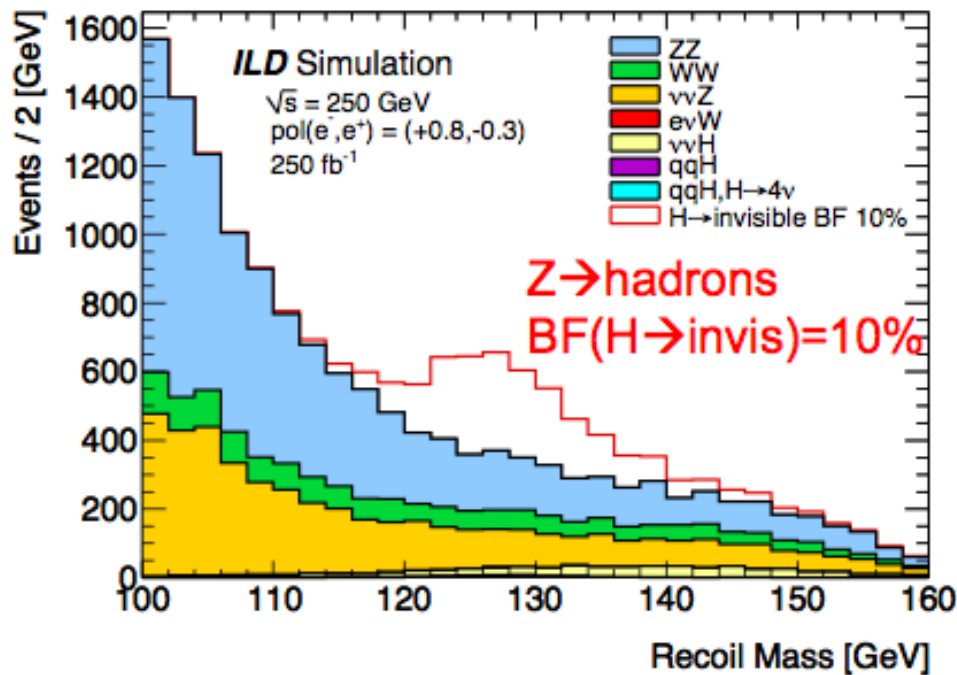
Sakharov conditions for BAU include
First order Phase Transition
(of electroweak vacuum)



Coexistence of two phases at $T = T_c$
Two minima at 0 and v_c in scalar potential

WIMP searches at colliders are complementary to direct/indirect searches.
Examples at the ILC:

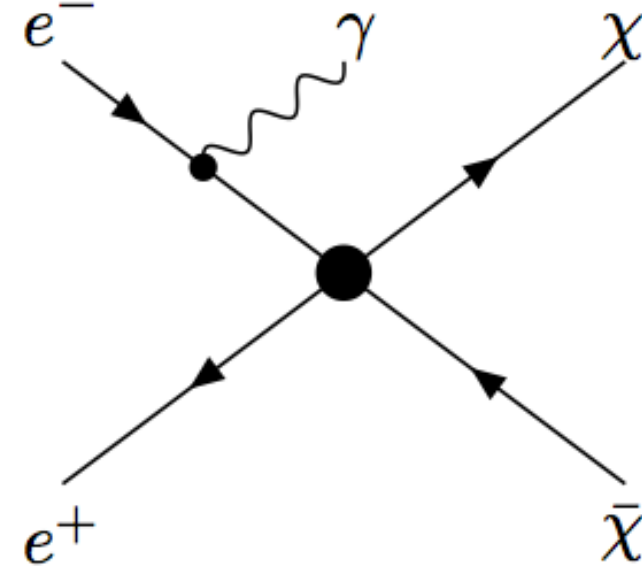
Higgs Invisible Decays



$BR(H \rightarrow \text{invis.}) < 0.4\%$ at 250 GeV, 1150 fb^{-1}

Impact of jet energy resolution

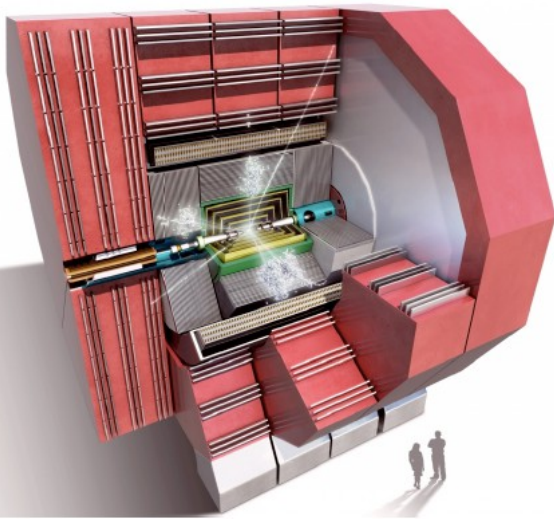
Monophoton Searches



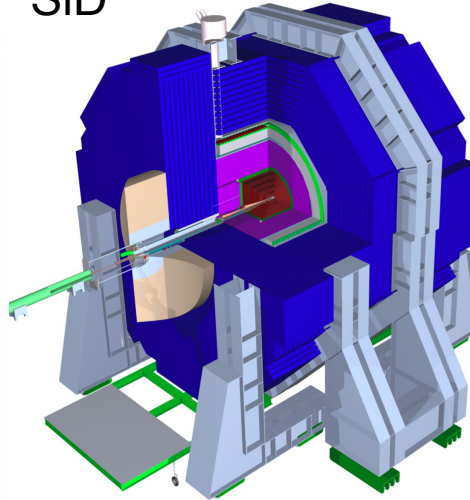
→ DM mass sensitivity nearly half \sqrt{s}

Soft photons, forward detectors

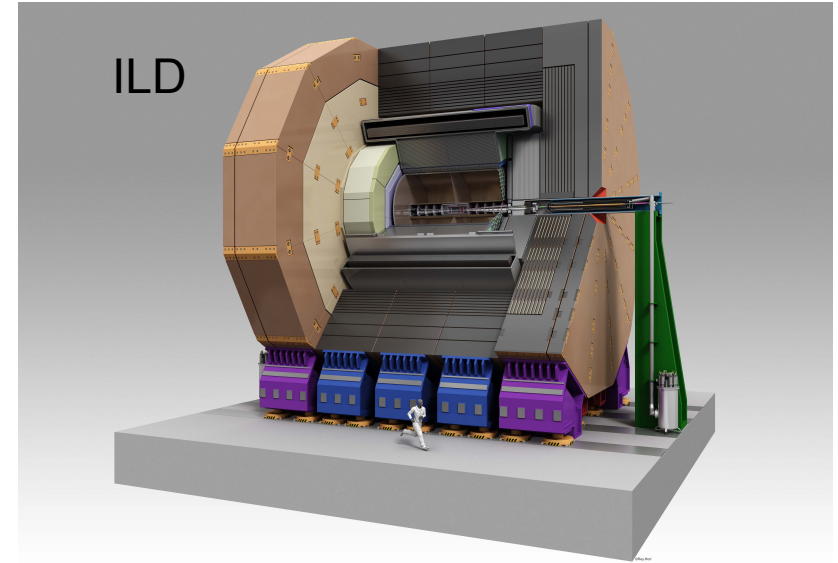
CLIC Detector



SiD



ILD



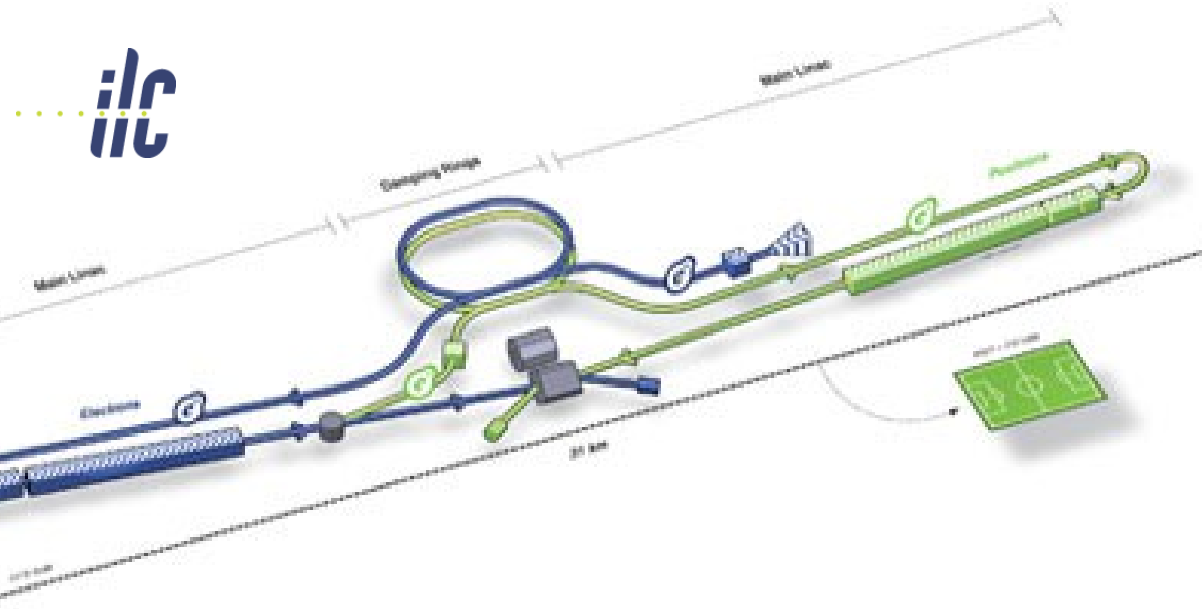
Highly granular calorimeters
 Central tracking
 with silicon
 Inner tracking with silicon

Central tracking
 with TPC

- CDR 2012
 Revised since

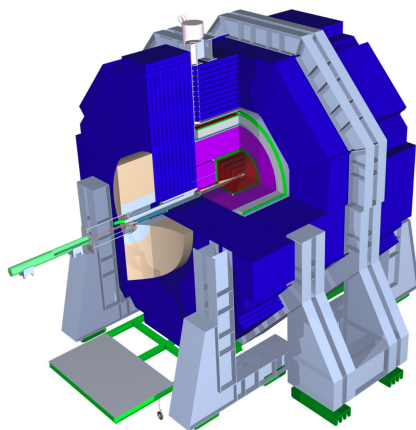
- LOI's Validated by IDAG in 2009
 - Publication of **D**etector **B**aseline **D**esign in 2013, together with TDR

Concepts based on input from physics studies and detector R&D organised in R&D collaborations

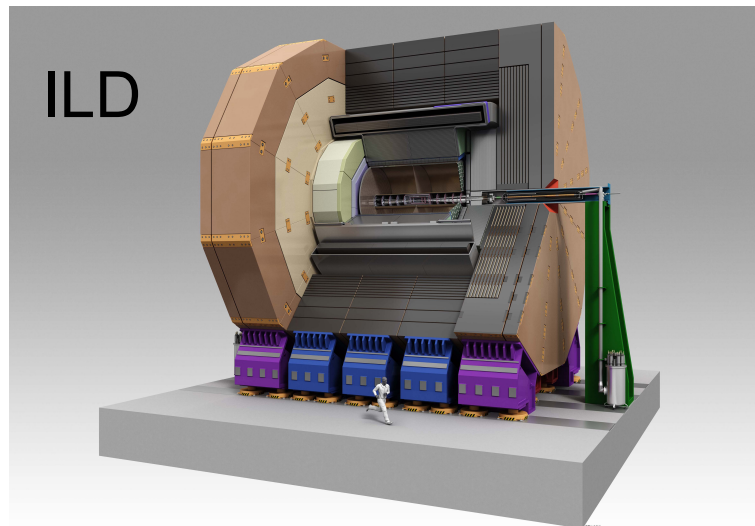


| ILC design parameters | |
|-----------------------|---|
| \sqrt{s} | 91-500 GeV |
| \mathcal{L} | $2 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ |
| P_{e^-} | >80% |
| P_{e^+} | ~30% |
| Length | ~31 km |

-> Talk by Steinar Stapnes



SiD



ILD

Talks by:

Imad Laktineh
Frank Simon
Marek Idzik
Lucie Linssen

Machine TDR in 2013 + DBD for detectors

| ILC design parameters | |
|-----------------------|---|
| \sqrt{s} | 91-500 GeV |
| \mathcal{L} | $2 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ |
| P_{e^-} | >80% |
| P_{e^+} | upto 30% |
| Length | ~31 km |

Comment

500 GeV is baseline
Option to upgrade to 1 TeV

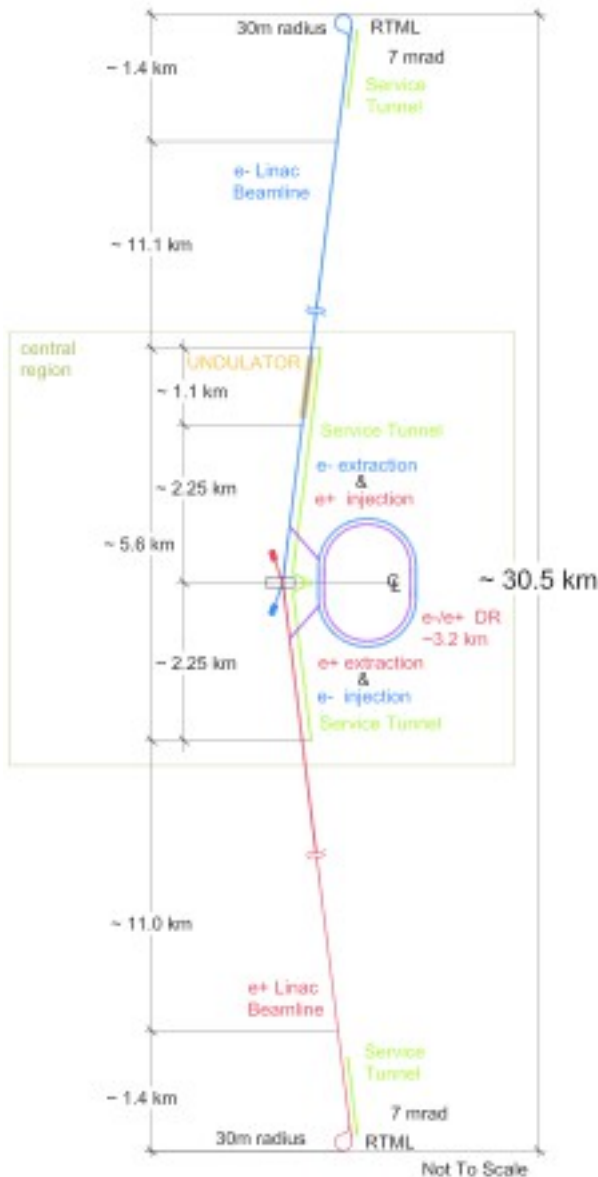
~Factor 4 technically possible

Proven by SLC

~Conservative estimate

Current site allows for 50km

- Discussion on possible running scenarios has started
- Luminosity and running time to achieve at a ~25 years research programme
That includes running at 250 GeV, 350 GeV, 500 GeV and 1 TeV
- No official statement yet but integrated luminosities indicated in following transparencies are realistic



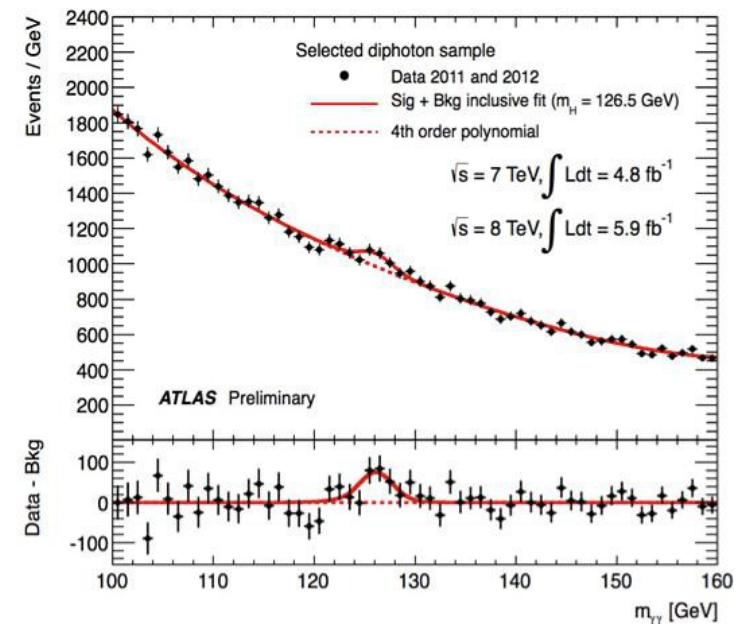
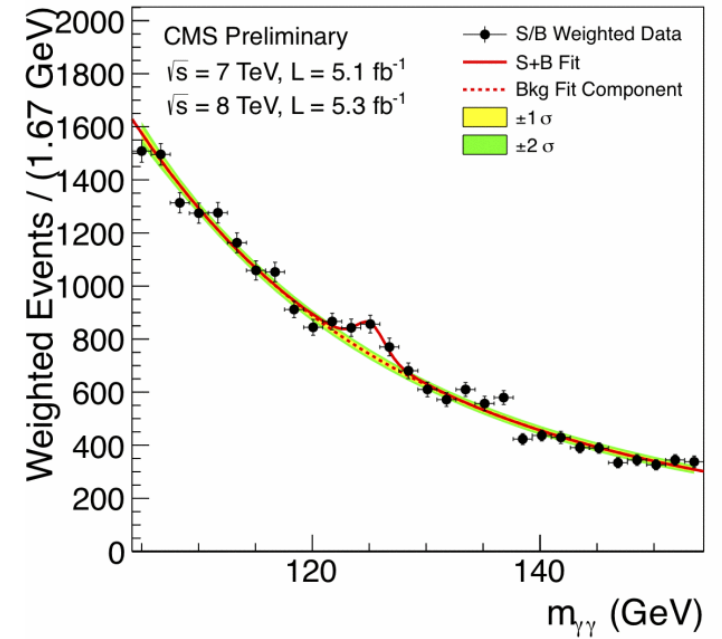
• SCRF Technology

- 1.3GHz SCRF with 31.5 MV/m
- 17,000 cavities
- 1,700 cryomodules
- 2×11 km linacs

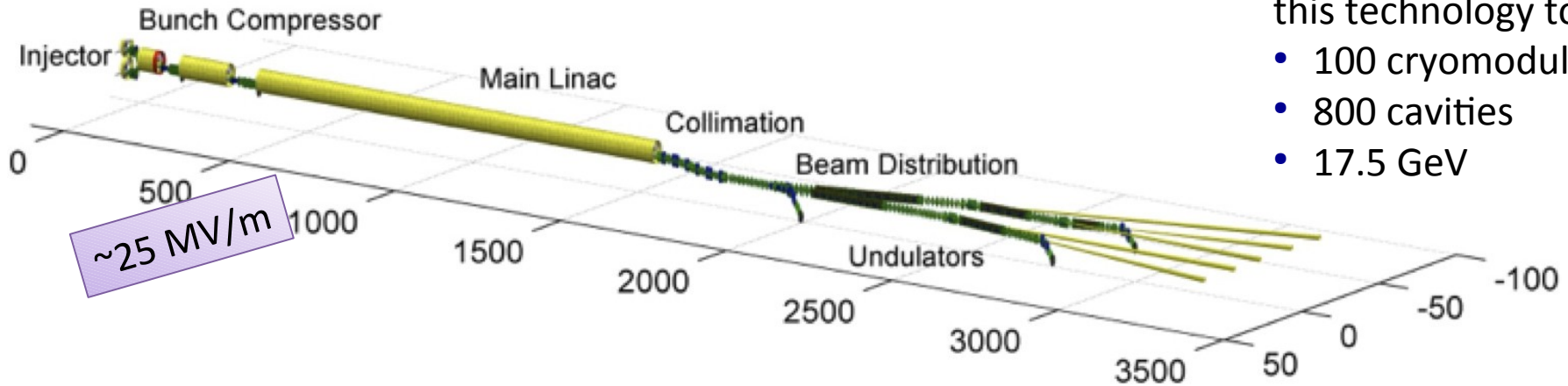
Luminosity

$$L \propto \frac{\eta_{RF} P_{RF}}{E_{cm}} \sqrt{\frac{\delta_{BS}}{\epsilon_{n,y}}} H_D$$

$\eta_{RF} \sim 40\%$ for SCRF technology
-> efficient technology



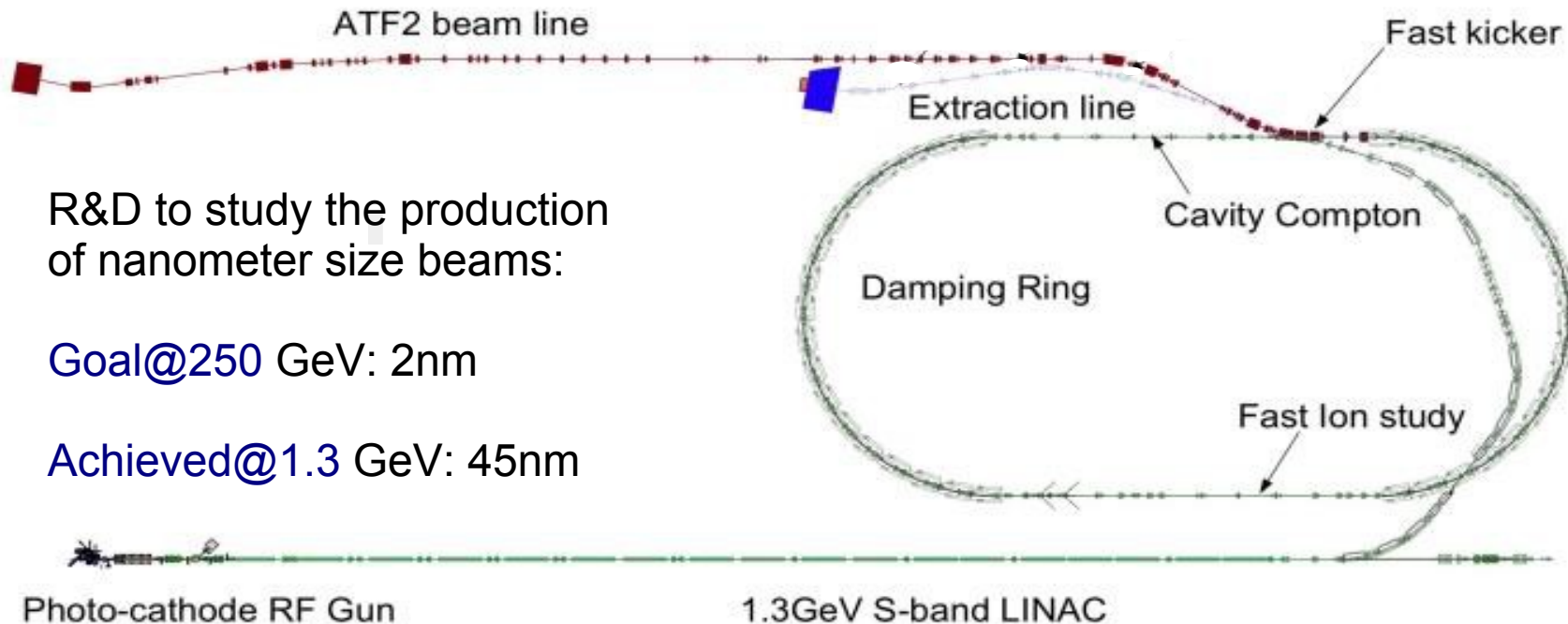
European XFEL Project: Location DESY Hamburg, Start 2015



Largest deployment of this technology to date

- 100 cryomodules
- 800 cavities
- 17.5 GeV

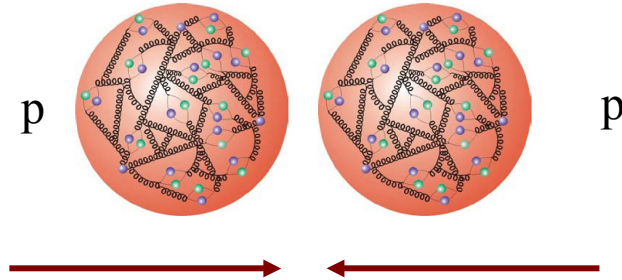
ATF at KEK Japan:



R&D to study the production of nanometer size beams:

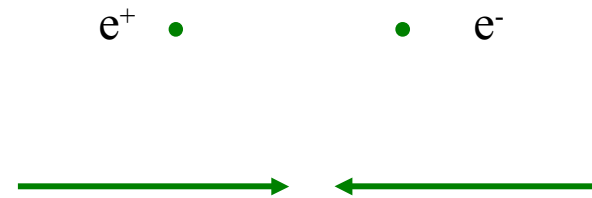
Goal@250 GeV: 2nm

Achieved@1.3 GeV: 45nm



Proton:

Composed particle (hadron)
 Unknown energy of collision partners
 Parasitic reactions
 Strong interaction
 => Considerable physics background
 Advantage: Scan of energy
 Range within one experiment

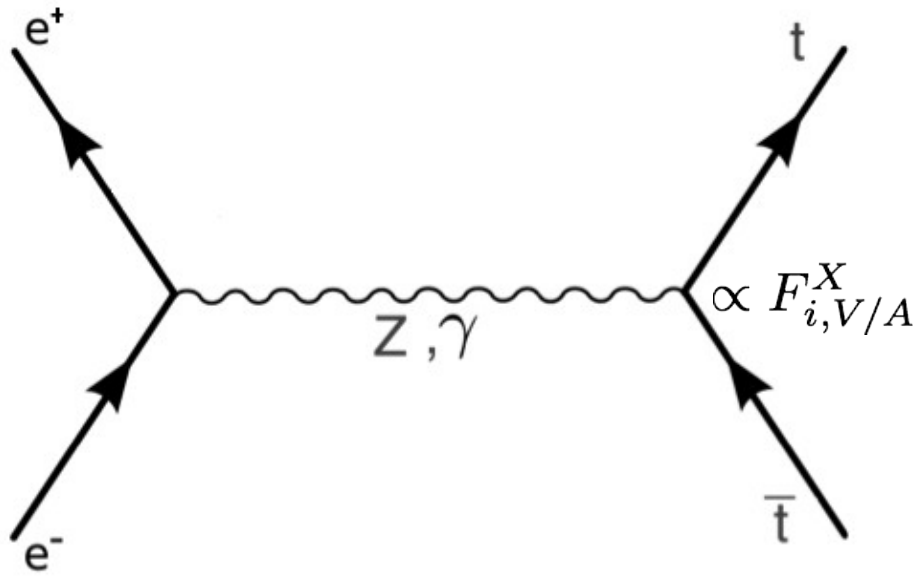


Electron:

Elementary particle
 Well known and adjustable energy of collision partners

 Each energy point needs a New set of machine parameters

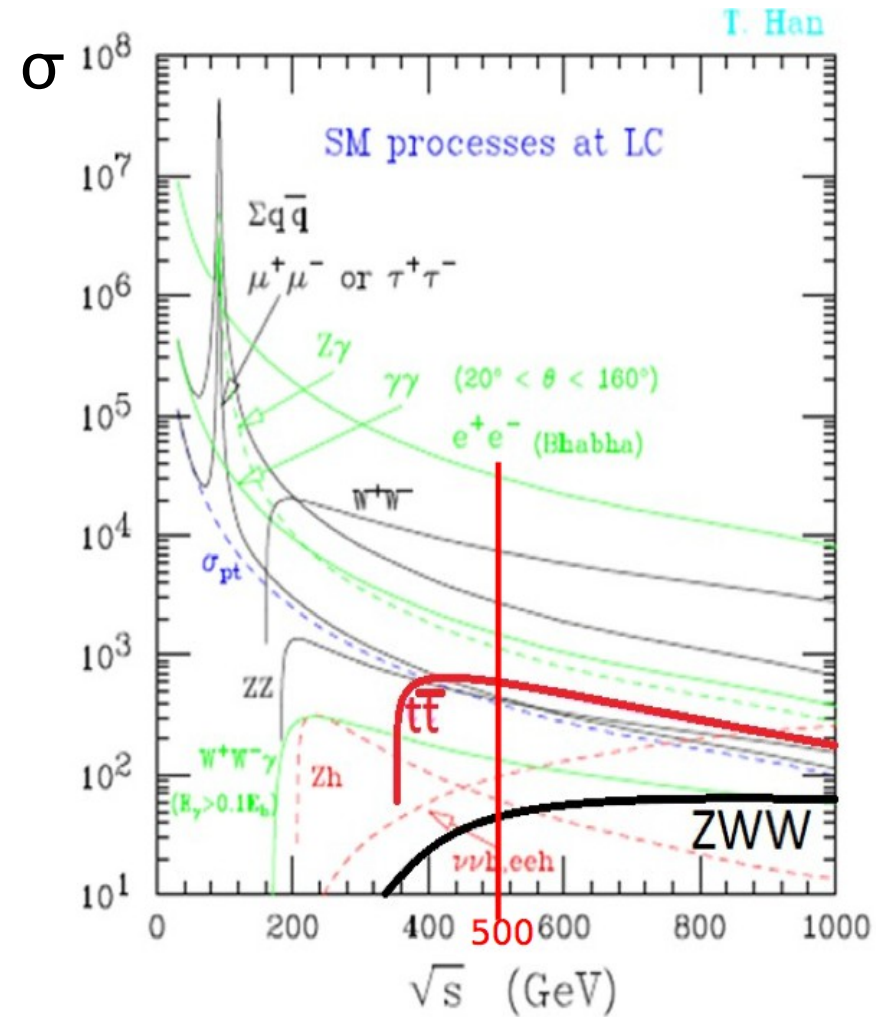
High precision measurements



- Top quark production through electroweak processes
no competing QCD production => Small theoretical errors!

- High precision measurements

- Top quark mass at ~ 350 GeV through threshold scan
- Polarised beams allow testing chiral structure at $t\bar{t}X$ vertex
=> Precision on form factors F



Higgs Mechanism

Scalar field which doesn't vanish in the vacuum

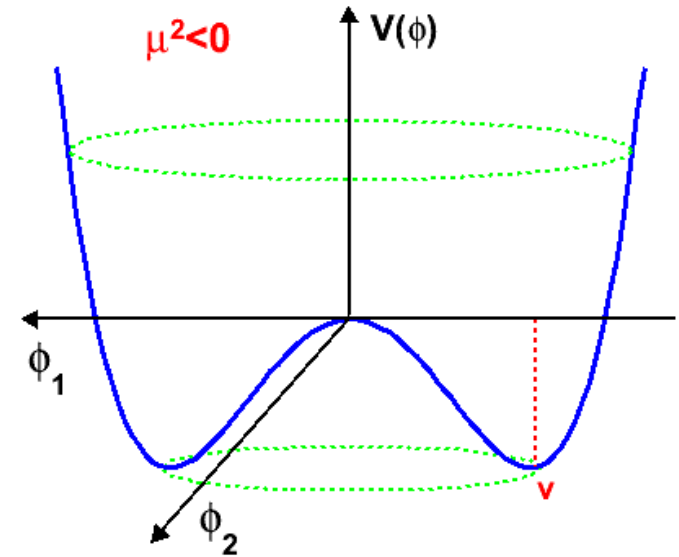
Choice in SM:
Doublet Field

$$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$$

4 degrees of freedom

Higgs Boson

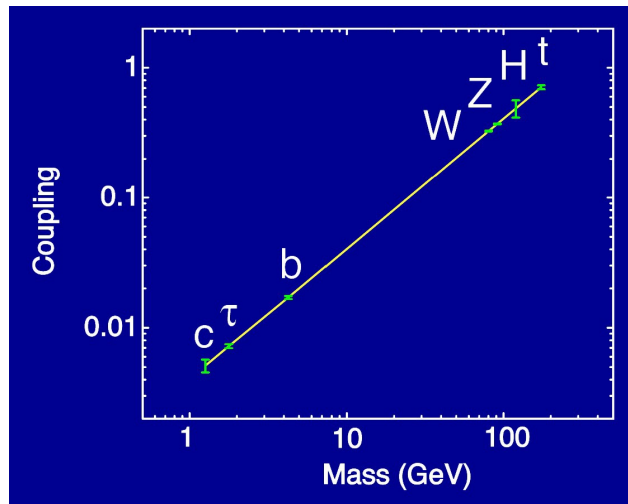
Longitudinally degrees
of W,Z Bosons



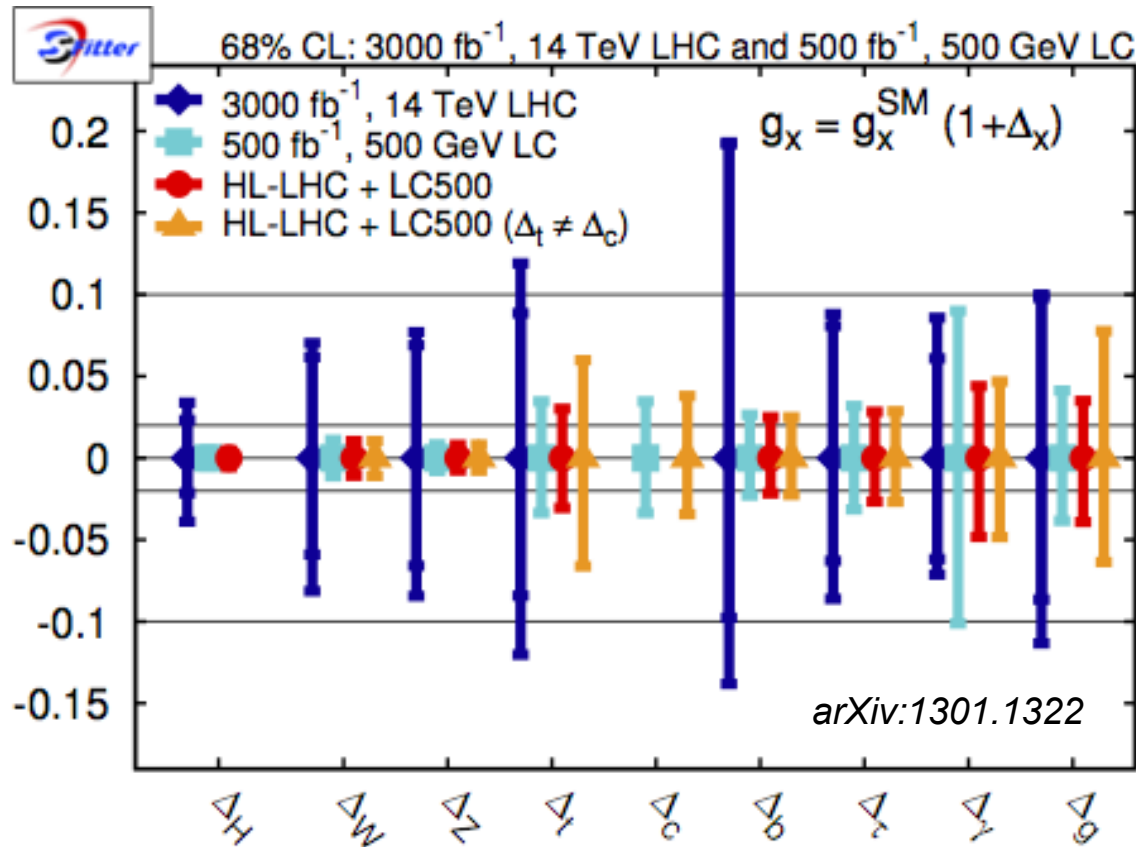
Couplings to Higgs Boson in Standard Model

Increase with particle mass

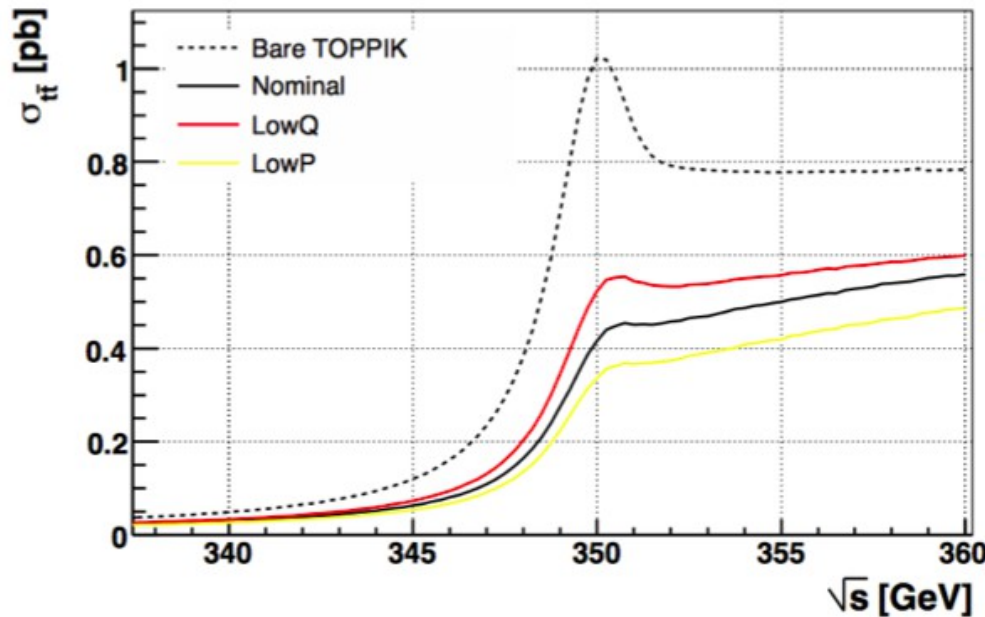
$$g_{HVV} = \frac{m_V^2}{v}$$



$$g_{Hf\bar{f}} = \frac{m_f}{v}$$



- A e+e- machine (Linear Collider) running at several energies will provide precise measurements of relevant Higgs couplings: Possibility to confirm the Higgs mechanism of the SM
- Precision matters: Detect deviations, for example due to extended Higgs sectors (SUSY, composite, ...): Expected on the 10% - 15% level in fermions, on the few % level in gauge bosons in typical Two-Higgs-Doublet models



Principle: m_t from $\sigma_{t\bar{t}}(m_t)$

Advantages:

- ▷ count number of $t\bar{t}$ events
- ▷ color singlet state
- ▷ background is non-resonant
- ▷ physics well understood
(renormalons, summations)
- Top decay protects from non-pert effects

Much of the discriminating power of the approach related to the strong mass-dependence ($t\bar{t}$ resonance).

Peak position very stable in theory predictions (threshold mass scheme).

Typical results:

$$\rightarrow \delta m_t^{\text{exp}} \simeq 50 \text{ MeV}$$

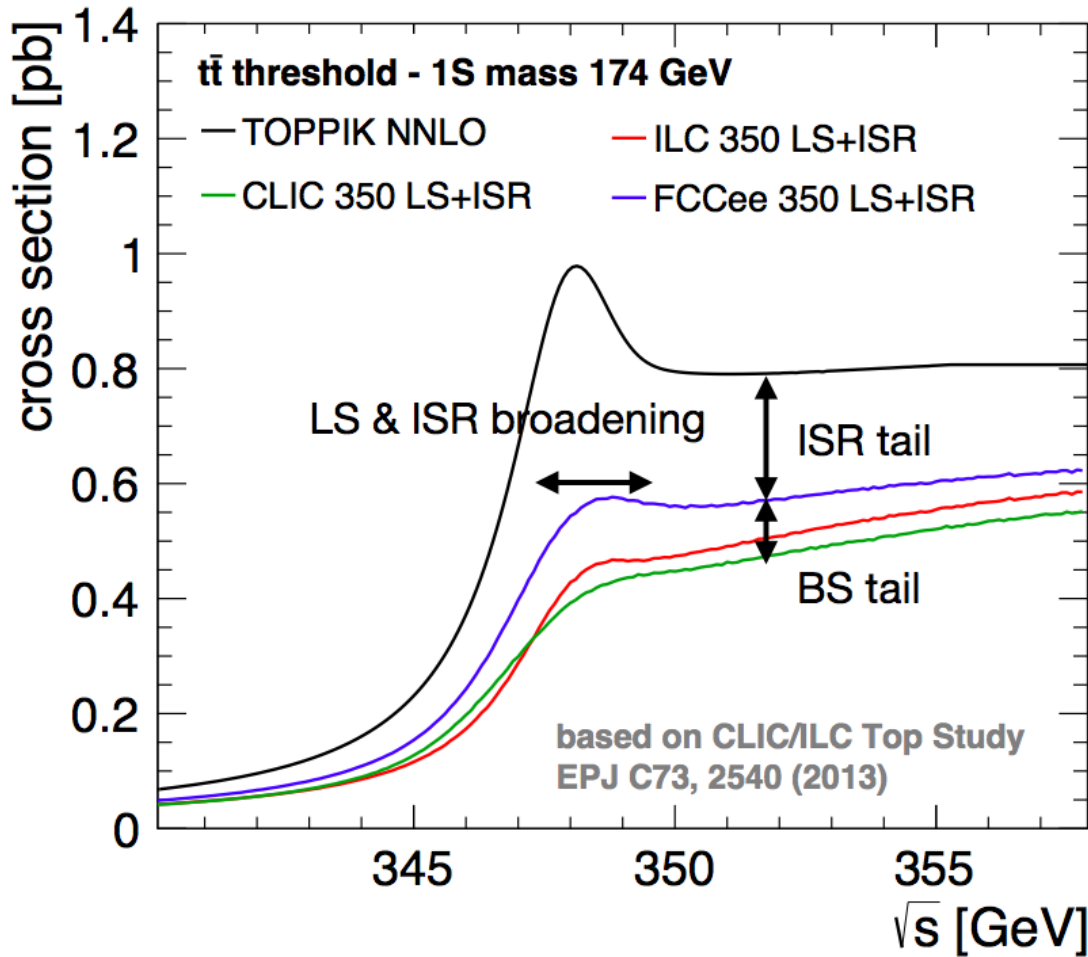
$$\rightarrow \delta m_t^{\text{th}} \simeq 100 \text{ MeV}$$

What mass?

$$\sqrt{s}_{\text{rise}} \sim 2m_t^{\text{thr}} + \text{pert.series}$$

(short distance mass: $1S \leftrightarrow \overline{MS}$)

A. Hoang

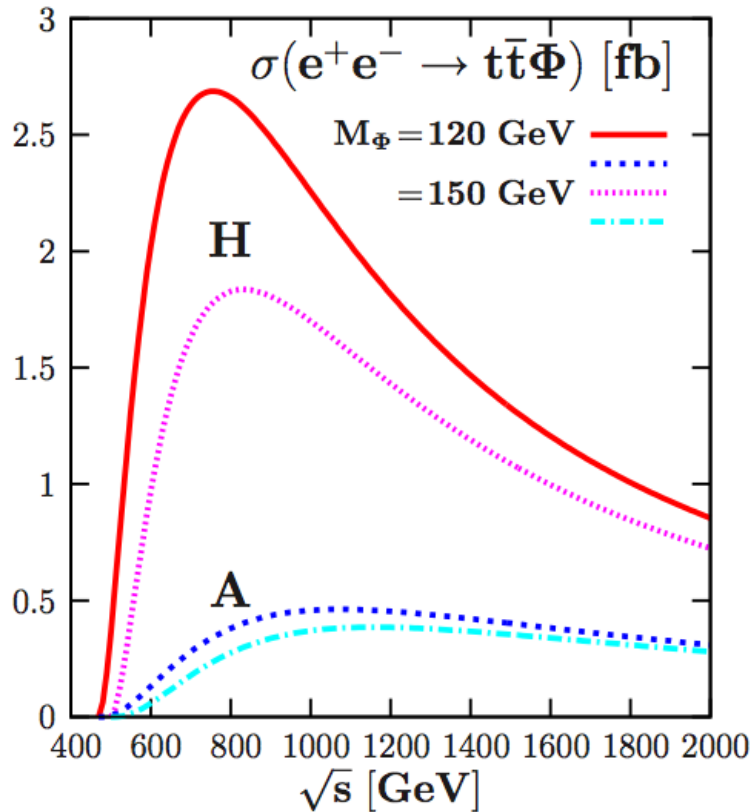


- **Initial State Radiation**
Lowers effective L at top energy
- **BeamStrahlung**
Lowers effective L at top energy
Not at FCCee Gaussian spectrum
- **Luminosity spectrum & Initial State Radiation broadening**
Smearing of cross section
Due to beam energy spread
ILC and FCCee comparable
Worse at CLIC

- 1) Main effect on L spectrum is ISR
=> Reduces Luminosity, smears out 1s bound state peak
- 2) LC somewhat smaller L due to BeamStrahlung

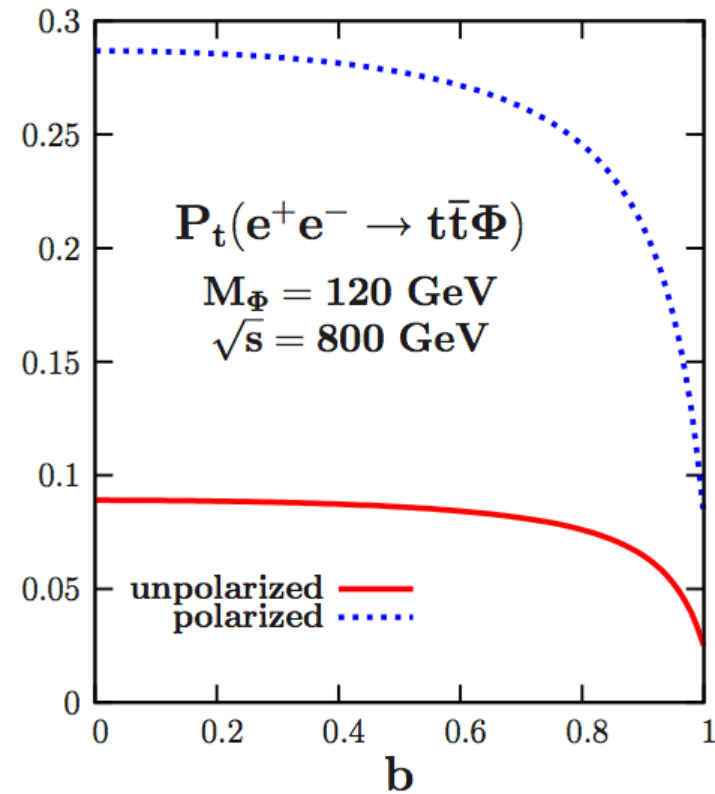
Direct coupling of top quark to CP odd and CP even scalar

Cross section



Dramatic differences for
CP odd and CP even scalar

Top quark polarisation



Sensitivity to CP odd admixture b
Merit of beam polarisation

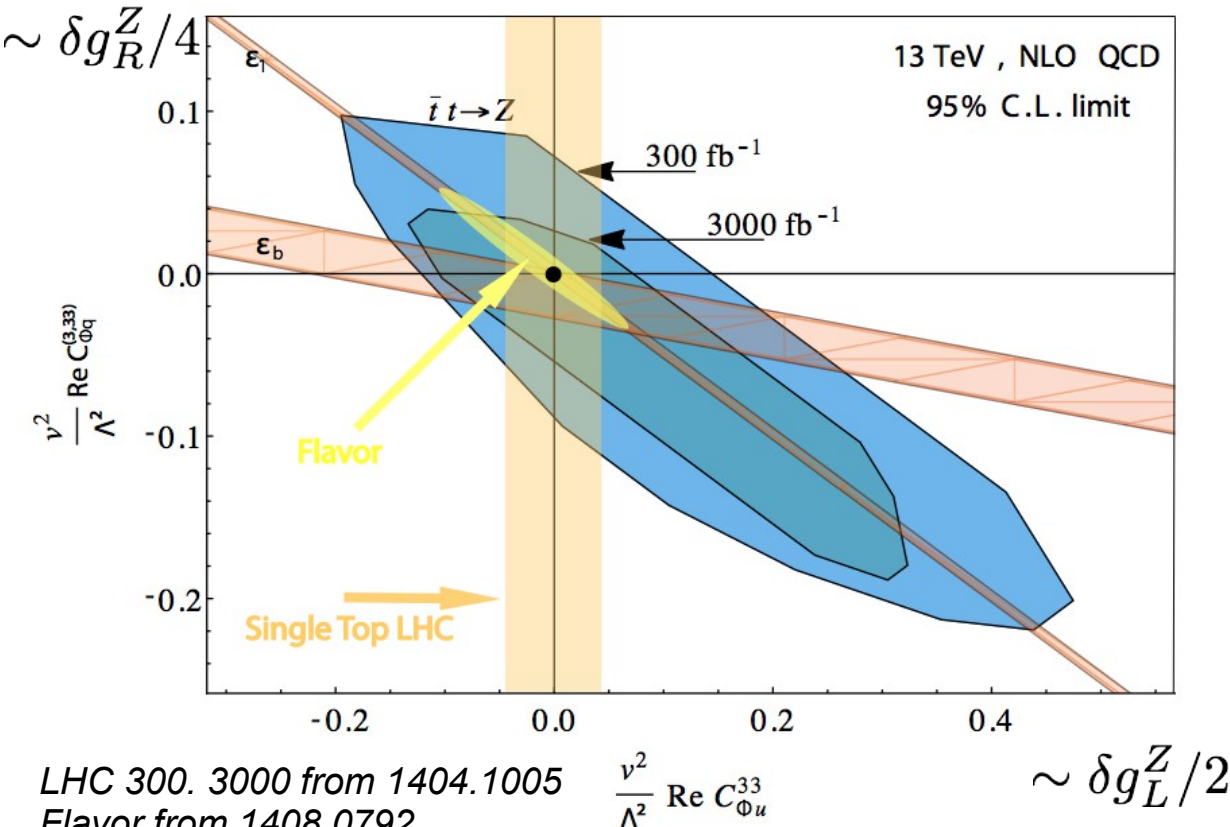
Determination of CP nature of scalar boson in an unambiguous way

Precision cross section $\sim 0.5\%$,

Precision $A_{FB} \sim 2\%$,

Precision $\lambda_t \sim 3-4\%$

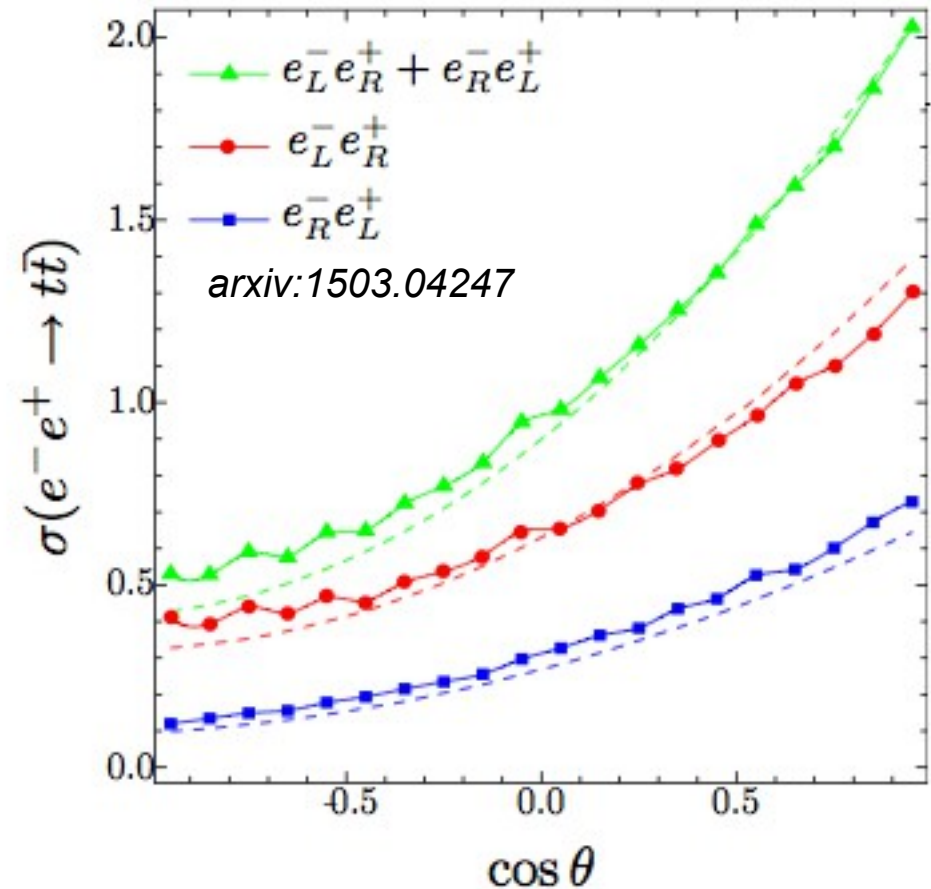
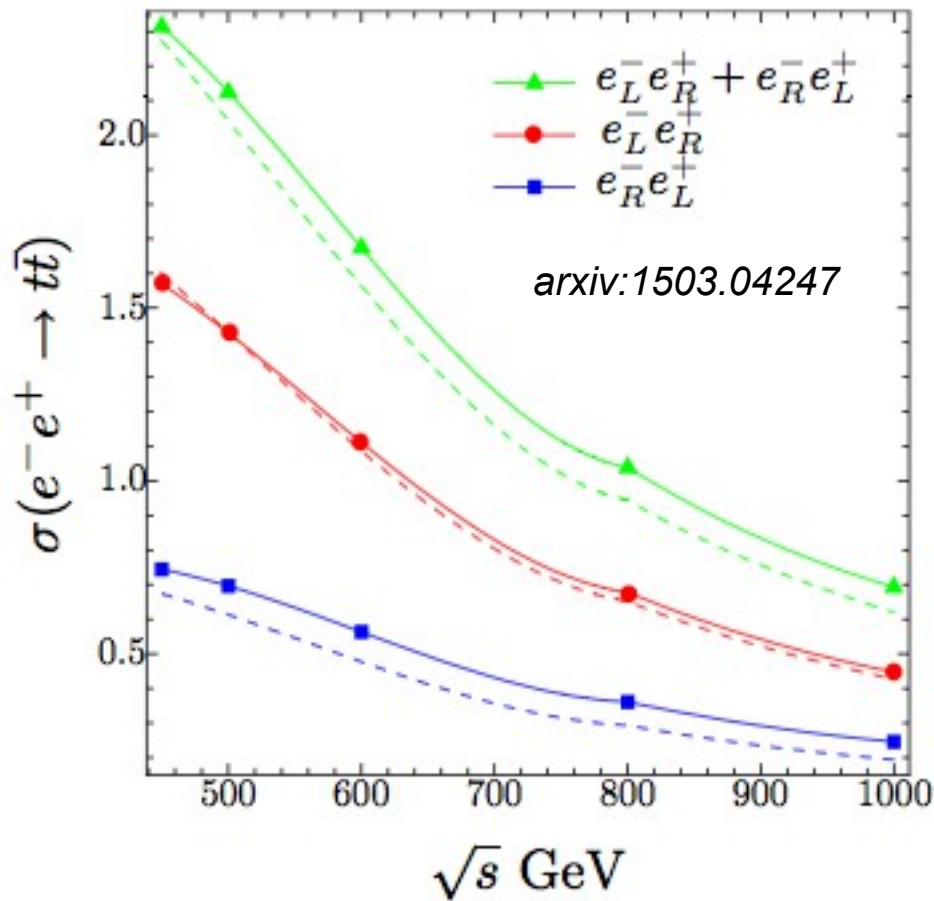
Accuracy on SM Z couplings compared with other experiments



LHC 300. 3000 from 1404.1005
Flavor from 1408.0792
LHC Single top added by F. Richard

- ILC with polarised beams outperforms all present and future experiments (Stringent limits only from LEP)
- Before ILC single top at LHC and B factories can deliver complementary information
- In particular g_R can only be constrained by ILC!
- Maintaining this high level still requires substantial experimental and theoretical work

ILC promises to be high precision machine for electroweak top couplings

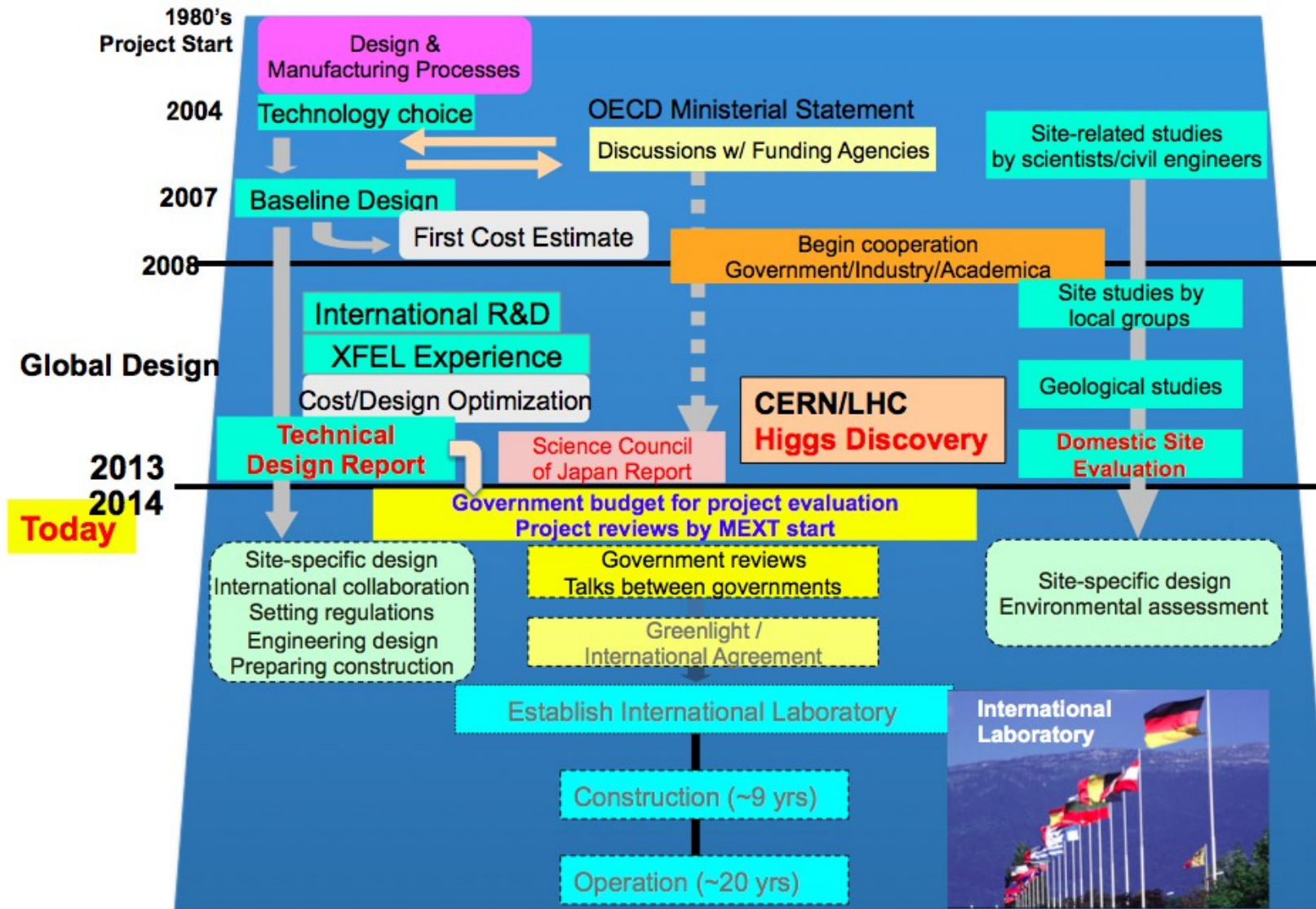


- Electroweak corrections manifest themselves differently for different beam polarisations

Beam polarisation important asset to disentangle SM and effects of new physics

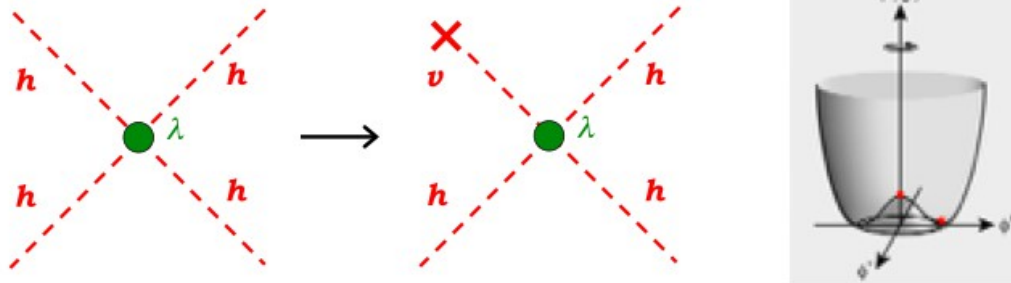
Configuration $e_R^-e_L^+$ seems to lead to “simpler” corrections

Timeline of ILC



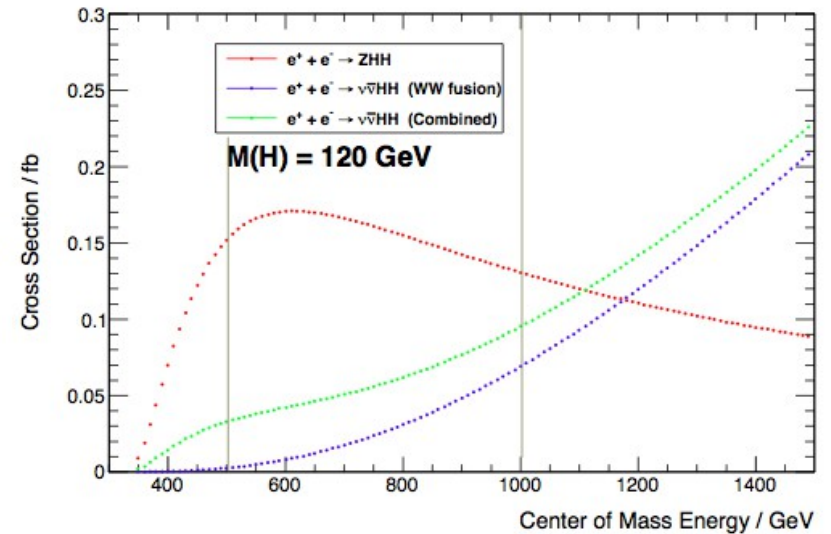
Remark R.P.: MEXT report in March 2016

Existence of hhh coupling =
Direct evidence of vacuum condensation



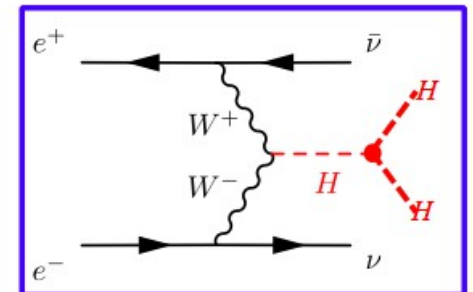
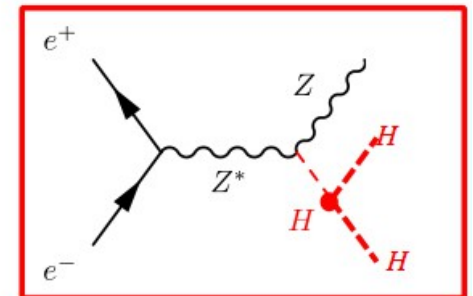
Challenging measurement because of:

- Small cross section (Zhh 0.2 fb at 500 GeV)
- Many jets in the final state
- **Presence of interference diagrams**



arXiv:1310.0763

| | ILC500 | ILC500-up | ILC1000 | ILC1000-up |
|-------------------------------------|-------------|------------------|-----------------|-----------------------|
| \sqrt{s} (GeV) | 500 | 500 | 500/1000 | 500/1000 |
| $\int \mathcal{L} dt$ (fb $^{-1}$) | 500 | 1600 ‡ | 500+1000 | 1600+2500 ‡ |
| $P(e^-, e^+)$ | (-0.8, 0.3) | (-0.8, 0.3) | (-0.8, 0.3/0.2) | (-0.8, 0.3/0.2) |
| $\sigma(ZHH)$ | 42.7% | | 42.7% | 23.7% |
| $\sigma(\nu\bar{\nu}HH)$ | - | - | 26.3% | 16.7% |
| λ | 83% | 46% | 21% | 13% |



T. Tanabe, K. Fuji, LCWS14

Hard(est) measurement, 10% accuracy seems possible

$$V(\eta) = \frac{1}{2}m^2\eta^2 + \lambda v\eta^3 + \frac{1}{4}\lambda\eta^4$$