

Non-Standard Interactions of W and Z Bosons: Simplified Models

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Outline

1. Generic new physics in electroweak interactions (Higgs, W , Z)
2. Recipe for a generic, meaningful phenomenological description
3. Results from calculations

Interactions of W , Z , Higgs

in the pure SM

- ▶ Signals and backgrounds: calculable.
- ▶ LC experimental precision requires further theoretical effort

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New Physics

- ▶ May be related to **Naturalness, Baryogenesis, Dark Matter**
- ▶ May be coupled only to **Higgs or weak interactions**
- ▶ Effect has been unobservable, so far
- ▶ But anything is possible: **no preferred type of model**

Goal of this Project

Universal phenomenological description of non-SM electroweak interactions in the high-energy range

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Could be useful for

- ▶ Studies of collider sensitivity
- ▶ Comparison and studies of LHC / LC complementarity
- ▶ Combination of low-energy and high-energy data
- ▶ Initial understanding w/o hidden theoretical assumptions

Guidelines

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Low-Energy Boundary Condition

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High-energy boundary condition

- ▶ New physics leads to enhancement \Rightarrow SM as lower limit
- ▶ Any physics leads to unitary amplitudes \Rightarrow upper limit

Low Energy: Effective Theory

(“Higgs”) Effective Field Theory = double expansion

- ▶ powers of gauge-invariant interactions
- ▶ perturbative EW/QCD corrections

Electroweak Observables, class I

1. Flavour precision observables: currents
2. Low-energy electroweak observables
3. Higgs decays

Intermediate Energy: Ineffective Theory

Electroweak Observables, class II

1. Vector-boson production (VV , VVV , ...)
2. Vector-boson scattering ($VV \rightarrow VV$)
3. Higgs/associated production (H , HV , HH , ...)

Production processes – “unlimited” in energy (LHC, CLIC)

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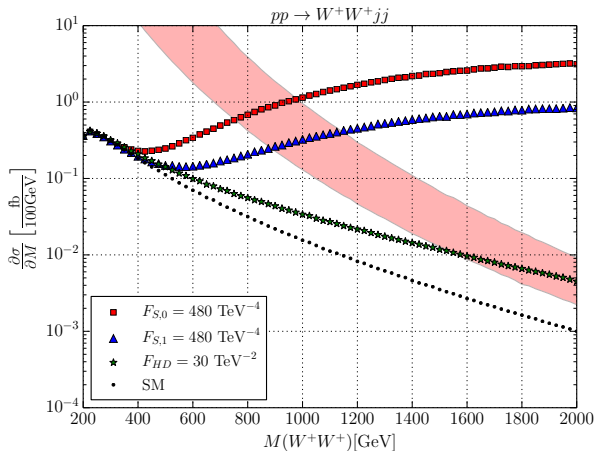
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HEFT fails as a phenomenological model.

EFT Failure at the LHC



Calculation: WHIZARD (M. SEKULLA)

High Energy: Asymptotic Theory

Any set of amplitudes is constrained by the conservation of probability.

Electroweak Observables, class III

1. Physical dampening effect: **rescattering**
2. Interactions eventually reach saturation
3. **Suppression** of asymptotics due to decoupling fermion currents

⇒ Phenomenological description must incorporate rescattering,

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Rates are low, so **further details may not matter**.

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- ⇒ small parameter set, for initial exploration
- ⇒ **enable off-shell evaluation and exclusive event-sample generation**

Recipe for Unitary Simplified Models

- ▶ Construct **arbitrary model** \Rightarrow amplitudes (T_0 matrix elements)
- ▶ Incorporate **rescattering**:
Recalculate amplitudes \Rightarrow **unitary model**

$$T = \frac{\text{Re} T_0}{\mathbb{1} - \frac{i}{2} T_0^\dagger} \quad \text{or} \quad T = \frac{1}{\text{Re} \left(\frac{1}{T_0} \right) - \frac{i}{2} \mathbb{1}} .$$

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- ▶ Asymptotic limits are automatically satisfied
- ▶ Asymptotic details (phases, channels) arbitrary – but largely irrelevant
- ▶ Extend for off-shell evaluation.

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Cross check: **Pole** \Rightarrow **Breit-Wigner resonance**.

Process List

1. VV scattering ($V = W, Z$), longitudinal and transversal V -polarization
2. VV production, EFT expansion beyond $D = 6$
3. VVV production, all polarizations
4. Higgs-associated production, all polarizations
5. HH production, EFT expansion beyond Higgs potential

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Scenario List

1. Standard Model

- ▶ reference model, all new parameters vanish

2. Featureless, **strongly interacting continuum**

- ▶ unitary extrapolation of plain EFT (higher-D operators)

3. **Resonances** above continuum

- ▶ Extensions of extrapolated EFT, classify by global symmetries

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- ▶ Inelastic channels opening up

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(all BSM **non-perturbative** but reduce to SM/EFT at low energy.)

Status of this Project

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Plan

- ▶ EW NLO for SM and EFT
- ▶ Combined model set for relevant processes, including Higgs

Study I: Simplified Models for Longitudinal Scattering

- ▶ Look at simplified models
which at low energy reduce to purely longitudinal couplings:

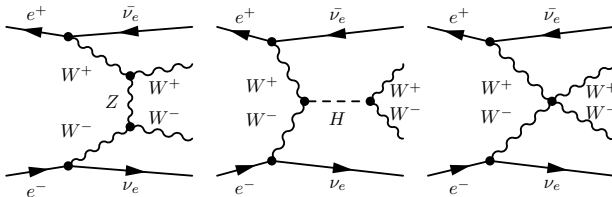
$$\mathcal{L}_{S,0} = F_{S,0} \text{Tr}[(\mathbf{D}_{\mu} \mathbf{H})^{\dagger} (\mathbf{D}_{\nu} \mathbf{H})] \text{Tr}[(\mathbf{D}^{\mu} \mathbf{H})^{\dagger} (\mathbf{D}^{\nu} \mathbf{H})]$$

$$\mathcal{L}_{S,1} = F_{S,1} \text{Tr}[(\mathbf{D}_{\mu} \mathbf{H})^{\dagger} (\mathbf{D}^{\mu} \mathbf{H})] \text{Tr}[(\mathbf{D}_{\nu} \mathbf{H})^{\dagger} (\mathbf{D}^{\nu} \mathbf{H})]$$

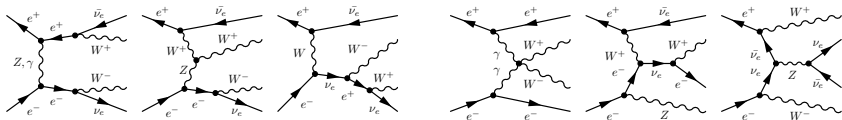
- ▶ Physics: **anomalous Goldstone interactions**, gauge interactions unchanged
- ▶ Signal is confined to $VV \rightarrow VV$ where $V = W, Z$ (or H).

Vector Boson Scattering: Feynman graphs (SM)

Signal



Background



Collider Setup: CLIC Parameters

Energy stages and int. luminosities

- ▶ ($E_1 = 350/375 \text{ GeV}$, $\mathcal{L}_{int,1} = 500 \text{ fb}^{-1}$)
- ▶ $E_2 = 1400 \text{ GeV}$, $\mathcal{L}_{int,2} = 1500 \text{ fb}^{-1}$
- ▶ $E_3 = 3000 \text{ GeV}$, $\mathcal{L}_{int,3} = 2000 \text{ fb}^{-1}$

Initial state polarization: $e^- : 80\%$, $e^+ : 0\%$

Low angle coverage M. Idzik: DOI: 10.5506/APhysPolB.46.1297

- ▶ LumiCal: 38-110 mrad
- ▶ BeamCal: 15-38 mrad

W and Z identification J. S. Marshall, A. Mnich, M. A. Thomson: arXiv:1209.4039

- ▶ $\approx 88 \%$ (with photon induced bkg.: 71-79 %)

Total cross sections without cuts

Process	1400 GeV	3000 GeV	Factor
$W^+ W^- \nu \bar{\nu}$	47.1	132	1
$W^+ W^- e^+ e^-$	1570	3820	1
$W^\pm Z e^\mp \nu$	138	408	0.136
$ZZ e^+ e^-$	3.78	4.70	0.019
$W^+ W^- (Z \rightarrow \nu \bar{\nu})$	11.7	9.35	1
$ZZ \nu \bar{\nu}$	15.7	57.5	1
$ZZ e^+ e^-$	3.78	4.70	1
$W^\pm Z e^\mp \nu$	138	408	0.136
$W^+ W^- e^+ e^-$	1570	3820	0.019
$ZZ (Z \rightarrow \nu \bar{\nu})$	0.484	0.237	1

Table : Total cross sections in fb without cuts.

Differential cross sections

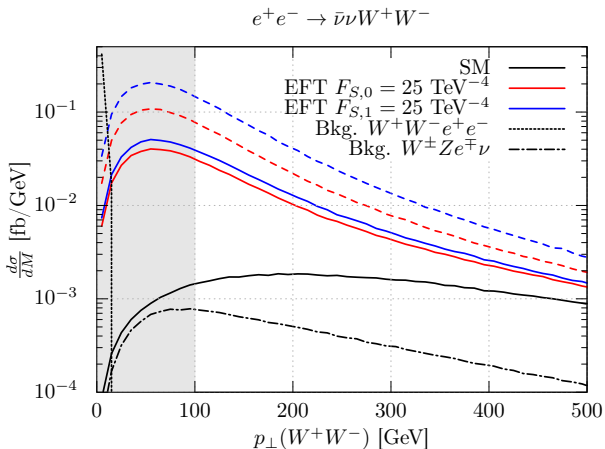


Figure : Differential cross sections depending on the transverse momentum of the W boson pair at $\sqrt{s} = 3000 \text{ GeV}$.

Used cuts

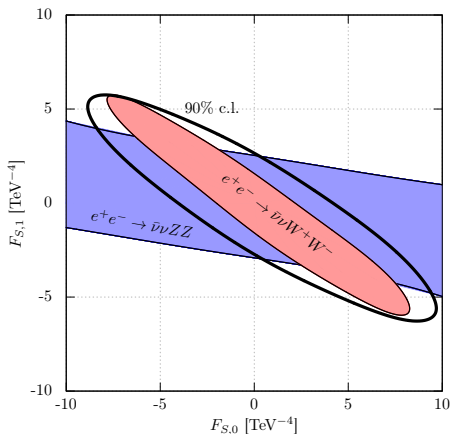
1. $M_{inv}(\bar{\nu}\nu) > 230(175) \text{ GeV}$
(neutrinos from Z, bg from W^+W^- , QCD 4j)
2. $|\cos\theta(W/Z)| < 0.8$
and $p_{\perp}(W/Z) > 300(180) \text{ GeV}$
(bg from t-channel $W/Z/\gamma$)
3. $\theta(e) > 15 \text{ mrad}$
and $p_{\perp}(WW) > 100(50) \text{ GeV}$, $p_{\perp}(ZZ) > 60(40) \text{ GeV}$
(bg from $\gamma\gamma$)
4. $900(800) \text{ GeV} < M_{inv}(WW) < 1900(1175) \text{ GeV}$,
 $850(800) \text{ GeV} < M_{inv}(ZZ) < 1900(1175) \text{ GeV}$
(non scattered W/Z)

Cross sections with cuts

Process	1400 GeV	3000 GeV	Factor
$W^+ W^- \nu \bar{\nu}$	0.119	0.790	1
$W^+ W^- e^+ e^-$	0.000	0.000	1
$W^\pm Z e^\mp \nu$	0.269	1.200	0.136
$ZZ e^+ e^-$	0.000	0.000	0.019
$W^+ W^- (Z \rightarrow \nu \bar{\nu})$	0.039	0.610	1
$ZZ \nu \bar{\nu}$	0.084	0.790	1
$ZZ e^+ e^-$	0.000	0.000	1
$W^\pm Z e^\mp \nu$	0.288	1.593	0.136
$W^+ W^- e^+ e^-$	0.000	0.000	0.019
$ZZ (Z \rightarrow \nu \bar{\nu})$	0.000	0.000	1

Table : Total cross sections in fb with cuts (error $\approx 1\%$).

Exclusion contours and exclusion sensitivities at 3000 GeV



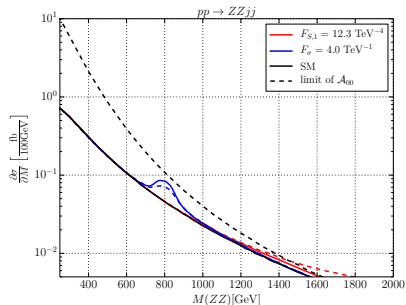
\Rightarrow 90% exclusion sensitivity $\approx 5 - 7 \text{ TeV}^{-4}$

Resonances

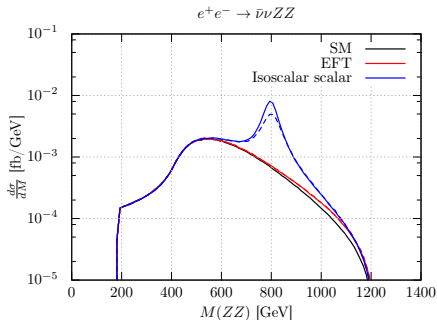
Looked at four simple cases (multiplets)

- ▶ Isoscalar – **Scalar** (neutral)
- ▶ Isotensor – Scalar (5 states: $++$, $+$, 0 , $-$, $--$)
- ▶ Isoscalar – **Tensor** (neutral)
- ▶ Isotensor – Tensor (5 states: $++$, $+$, 0 , $-$, $--$)

Comparison: scalar-isoscalar resonance “(H’)”



LHC (14 TeV)



CLIC (1.4 TeV)

Study II: Simplified Models With Transversal Scattering

- ▶ With transversal couplings, VVV is part of the signal
 \Rightarrow combined analysis.
- ▶ Low energy limit: transversal and longitudinal couplings

$$\mathcal{L}_{S,0} = F_{S,0} \text{Tr}[(\mathbf{D}_\mu \mathbf{H})^\dagger (\mathbf{D}_\nu \mathbf{H})] \text{Tr}[(\mathbf{D}^\mu \mathbf{H})^\dagger (\mathbf{D}^\nu \mathbf{H})]$$

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$$\mathcal{L}_{M,0} = -g^2 F_{M,0} \text{Tr}[(\mathbf{D}_\mu \mathbf{H})^\dagger (\mathbf{D}^\mu \mathbf{H})] \text{Tr}[\mathbf{W}_{\nu\rho} \mathbf{W}^{\nu\rho}]$$

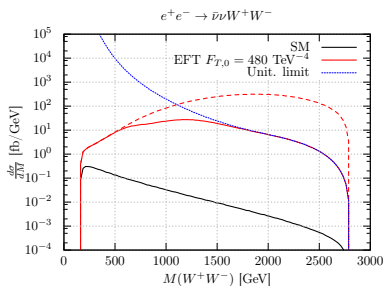
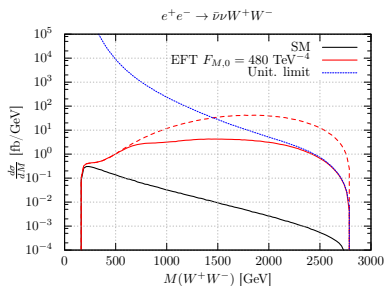
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$$\mathcal{L}_{T,0} = g^4 F_{T,0} \text{Tr}[\mathbf{W}_{\mu\nu} \mathbf{W}^{\mu\nu}] \text{Tr}[\mathbf{W}_{\alpha\beta} \mathbf{W}^{\alpha\beta}]$$

$$\mathcal{L}_{T,1} = g^4 F_{T,1} \text{Tr}[\mathbf{W}_{\alpha\nu} \mathbf{W}^{\mu\beta}] \text{Tr}[\mathbf{W}_{\mu\beta} \mathbf{W}^{\alpha\nu}]$$

$$\mathcal{L}_{T,2} = g^4 F_{T,2} \text{Tr}[\mathbf{W}_{\alpha\mu} \mathbf{W}^{\mu\beta}] \text{Tr}[\mathbf{W}_{\beta\nu} \mathbf{W}^{\nu\alpha}]$$

- ▶ Pure longitudinal couplings suppressed in VVV production, others unsuppressed

VBS with LT/TT interactions: $e^+e^- \rightarrow W^+W^-\bar{\nu}\nu$ 

Plots: WHIZARD (C. FLEPER)

(combination with W^+W^-Z and ZZZ : w.i.p.)

Summary

- ▶ Anomalous electroweak interactions are **outside the realm of perturbation theory**, EFT, or any other predictive framework.
- ▶ For a parameterization, we have to introduce phenomenological models, which
 - ▶ smoothly match to the low-energy EFT
 - ▶ display valid asymptotics = unitarity
- ▶ This can be done in the framework of a complete, exclusive Monte-Carlo simulation (WHIZARD).
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WHIZARD group / EW interactions at LC:

- ▶ Siegen: Simon Brass, Christian Fleper, WK, Zhijie Zhao
 - ▶ DESY: Bijan Chokoufe, Jürgen Reuter, So-young Shim, Christian Weiss
 - ▶ Karlsruhe: Marco Sekulla
 - ▶ Würzburg: Thorsten Ohl
1. C. Fleper, W. Kilian, J. Reuter and M. Sekulla, "Scattering of W and Z Bosons at High-Energy Lepton Colliders," arXiv:1607.03030 [hep-ph].
 2. W. Kilian, T. Ohl, J. Reuter and M. Sekulla, "Resonances at the LHC beyond the Higgs boson: The scalar/tensor case," Phys. Rev. D **93** (2016) no.3, 036004 [arXiv:1511.00022 [hep-ph]].
 3. W. Kilian, T. Ohl, J. Reuter and M. Sekulla, "High-Energy Vector Boson Scattering after the Higgs Discovery," Phys. Rev. D **91** (2015) 096007 [arXiv:1408.6207 [hep-ph]].

Further info

- ▶ WHIZARD website

<https://whizard.hepforge.org>