

Search for CP violation effects in the $h \rightarrow \tau\tau$ decay at future e^+e^- colliders

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X. Chen and Y. Wu, [arXiv:1703.04855](https://arxiv.org/abs/1703.04855)

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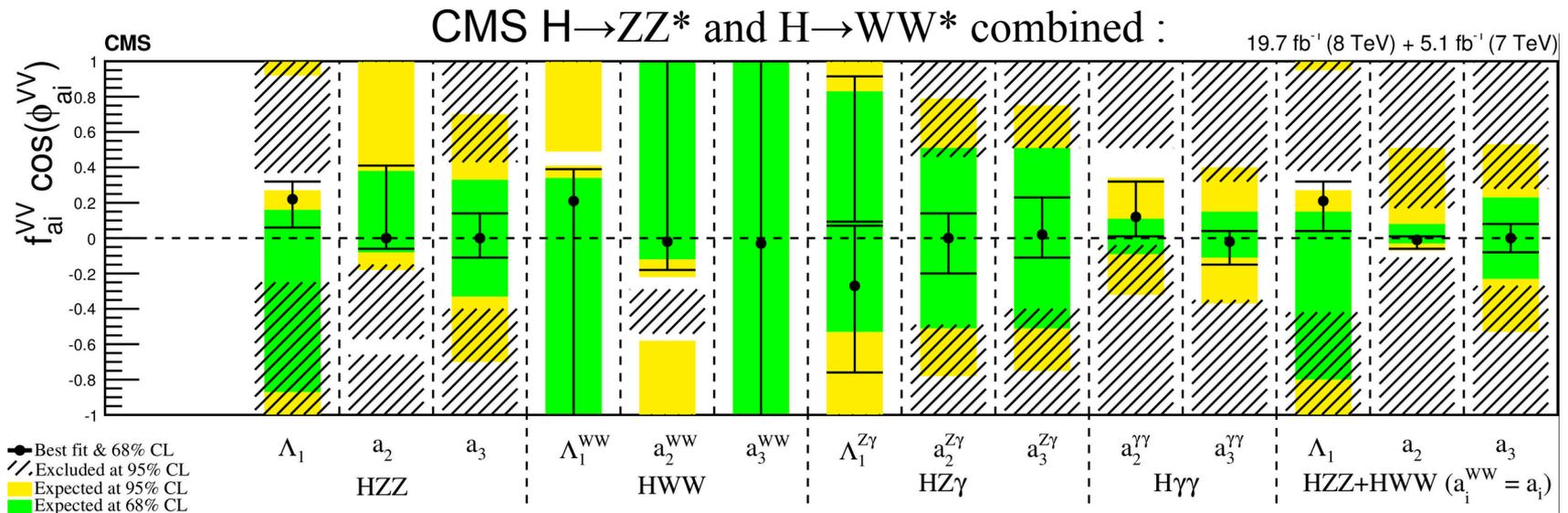
Introduction

- After the Higgs was discovered in 2012, understanding its properties, and looking for any possible deviations from the SM prediction, becomes a very important task of LHC
- CP violation is a necessary condition for baryogenesis, a process leading to matter-antimatter imbalance in the universe. Understanding Higgs' CP property is one of the important topics that can be done at the LHC or future e^+e^- colliders, but perhaps with better precision for the latter
 - ❖ If Higgs is in a pure CP eigen state: is it CP even or odd ?
 - ❖ If Higgs is in a CP mixture: gives rise to CP violation. This is a more exciting scenario, as the current known CP violation source (a single complex phase in CKM) is too small to explain the matter-antimatter imbalance
- Unlike the CP odd Higgs effective coupling to bosons which are dim-6 operators, the CP odd Higgs coupling to fermions is dim-4 and the CP violation effect can be sizable

LHC Higgs CP test

- ATLAS/CMS considered the mixture of SM and BSM CP even/odd in the HVV tensor structure, using either ME-based variables or templates

$$L(\text{HVV}) \sim \underbrace{a_1 \frac{m_Z^2}{2} \text{HZ}^\mu \text{Z}_\mu}_{\text{SM}} - \underbrace{\frac{\kappa_1}{(\Lambda_1)^2} m_Z^2 \text{HZ}_\mu \square \text{Z}^\mu - \frac{1}{2} a_2 \text{HZ}^{\mu\nu} \text{Z}_{\mu\nu}}_{\text{BSM CP-even}} - \underbrace{\frac{1}{2} a_3 \text{HZ}^{\mu\nu} \tilde{\text{Z}}_{\mu\nu}}_{\text{BSM CP odd}} + \dots$$



The non-SM tensor couplings are consistent with zero for both ATLAS and CMS

CP test in VBF $H \rightarrow \tau\tau$ with ATLAS

[arXiv:1602.04516
(accepted to EPJC)]

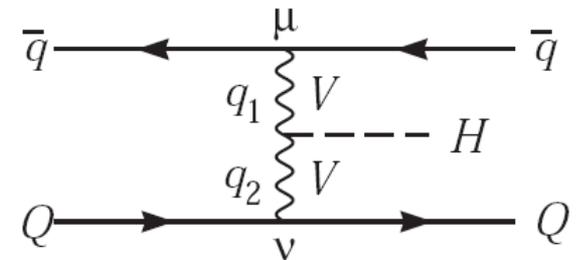
- The Optimal Observable (OO) is expected to perform better than $\Delta\Phi$. It is

defined as:
$$OO = \frac{2 \operatorname{Re}(\mathcal{M}_{\text{SM}}^* \mathcal{M}_{\text{CP-odd}})}{|\mathcal{M}_{\text{SM}}|^2}$$

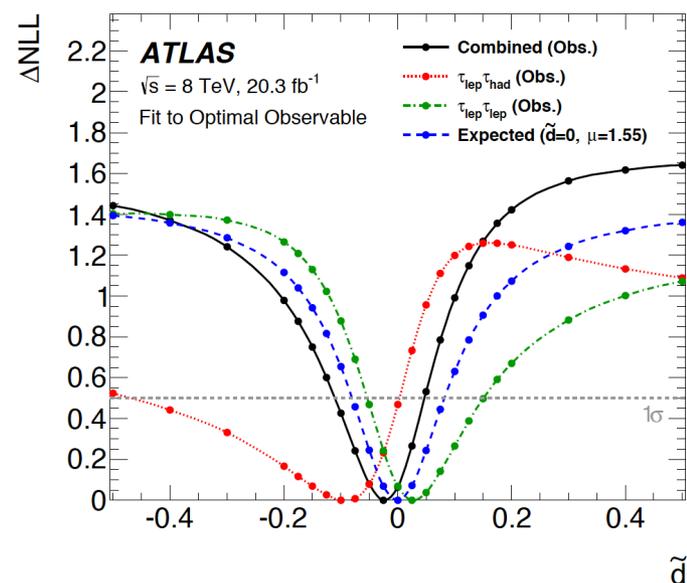
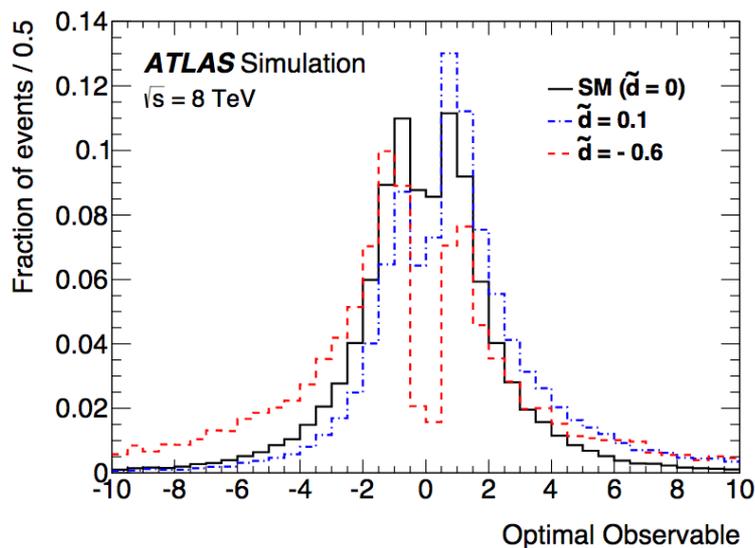
with the Matrix Element for VBF production being

$$\mathcal{M} = \mathcal{M}_{\text{SM}} + \tilde{d} \cdot \mathcal{M}_{\text{CP-odd}}$$

$$|\mathcal{M}|^2 = |\mathcal{M}_{\text{SM}}|^2 + \tilde{d} \cdot 2 \operatorname{Re}(\mathcal{M}_{\text{SM}}^* \mathcal{M}_{\text{CP-odd}}) + \tilde{d}^2 \cdot |\mathcal{M}_{\text{CP-odd}}|^2$$



- With all 4-momenta of the final state particles (Higgs and two tagging jets) measured (not possible with $H \rightarrow WW^*$), the LO ME of SM and CP-odd can be calculated from HAWK, and then OO can be calculated per event



CP test in $H \rightarrow \tau\tau$ decay

- CP-odd Yukawa coupling can enter the Lagrangian at dim-4, thus sensitive at tree-level rather than with the dim-6 operators in HVV

$$-g_\tau (\cos\phi \bar{\tau}\tau + \sin\phi \bar{\tau}i\gamma_5\tau) h \quad \Phi \text{ is the mixing angle. } \Phi=0 \text{ (}\Phi=\pi/2\text{) means SM (CP odd)}$$

- CP of $H\tau\tau$ coupling can be distinguished by the transverse tau spin correlations

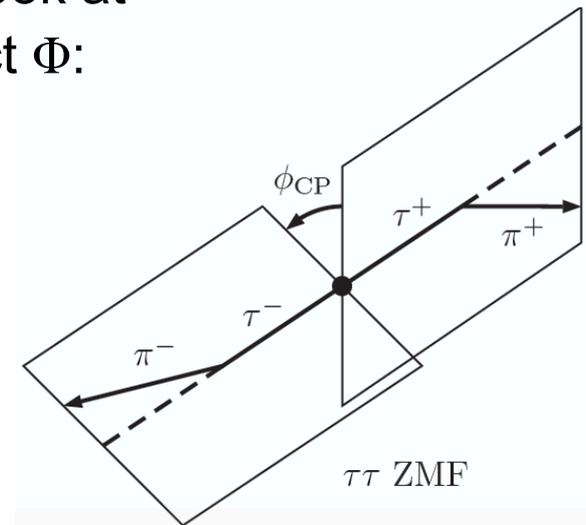
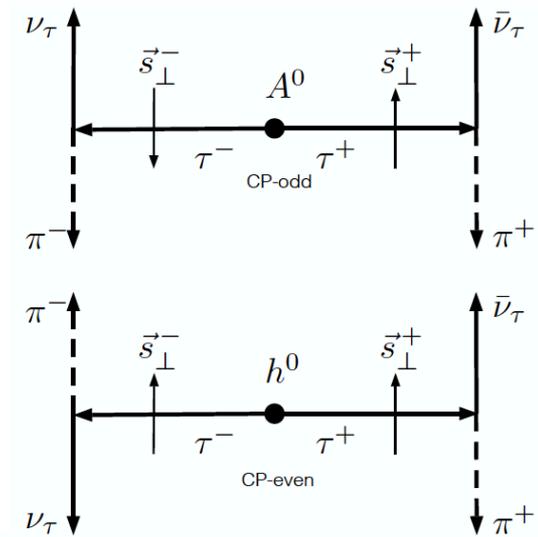
$$\Gamma(H, A \rightarrow \tau^-\tau^+) \sim 1 - s_z^{\tau^-} s_z^{\tau^+} \pm s_T^{\tau^-} s_T^{\tau^+}$$

Sensitive to CP (H vs A)

- For example, with the $\tau \rightarrow \pi\nu$ decay, one can look at the angle between tau decay planes to extract Φ :

$$\frac{d\Gamma(h \rightarrow \tau\tau \rightarrow \pi^+\pi^- + 2\nu)}{d\phi_{CP}} \propto 1 - \frac{\pi^2}{16} \cos(\phi_{CP} - 2\phi)$$

- It is experimentally challenging because the neutrinos are not reconstructed



CP test in $H \rightarrow \tau\tau$ decay

- There are two methods to extract CP from $H \rightarrow \tau\tau$ decay:

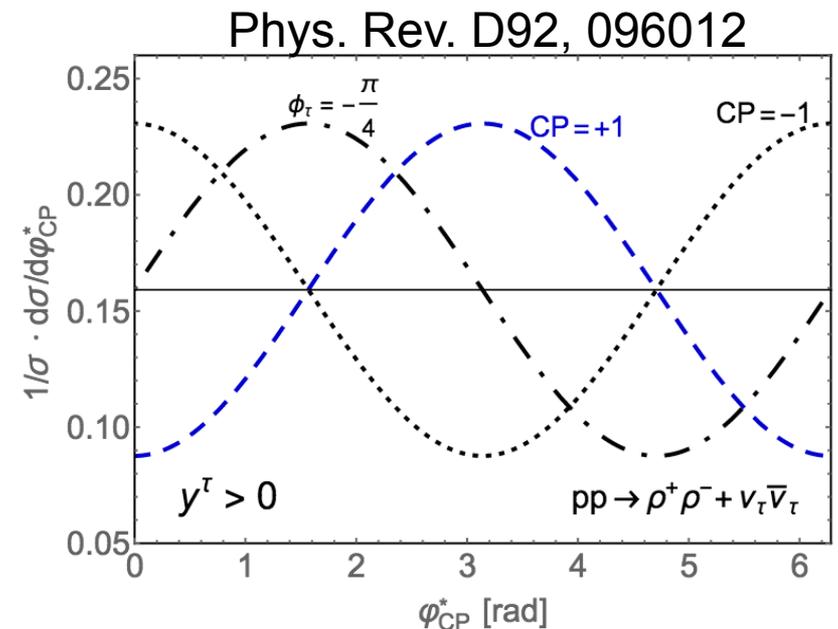
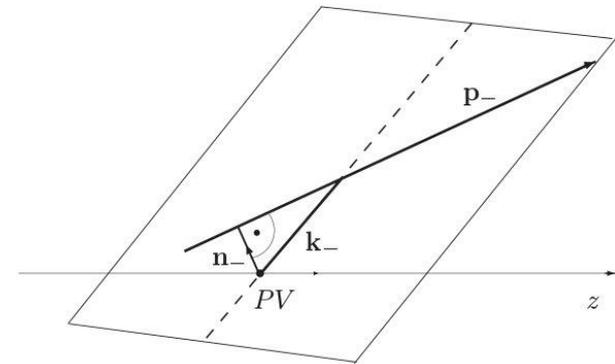
Impact Parameter (IP) method:

- Approximately reconstruct the tau decay plane from its leading track and IP
- Best for the $\tau \rightarrow \pi\nu$ decay. The analyzing power is compromised for other tau decays

Using the $\tau \rightarrow \rho\nu \rightarrow \pi^\pm \pi^0 \nu$ decay:

- The tau decay plane can be approximately reconstructed by the track and neutral pion
- However, the relative energy of π^\pm, π^0 need to be classified in order to maximize the analyzing power

- In order to use the two methods, the **tau decay modes (substructure)** need to be well differentiated (next few slides)

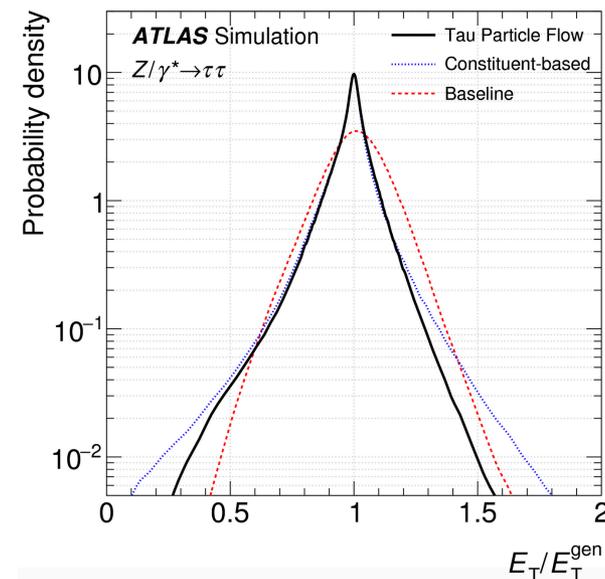
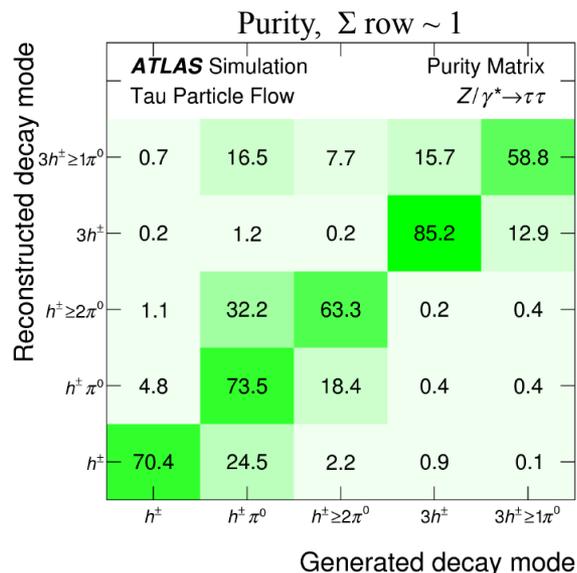
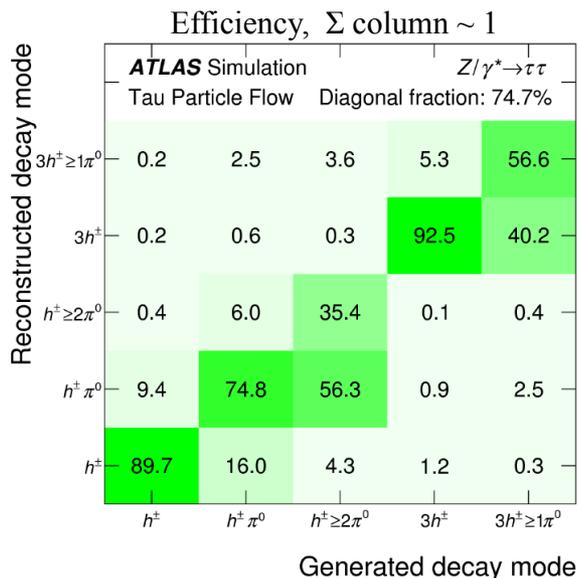


A few extra references:

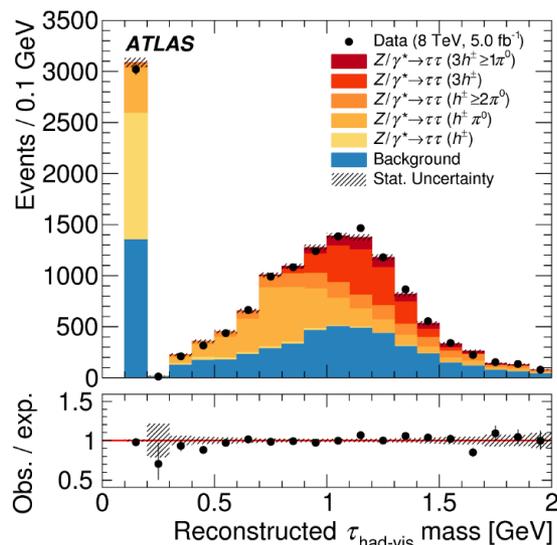
EPJC 74 (2014) 3164, Phys. Rev. D88 076009,

Phys. Lett. B579 (2004) 157, Phys. Lett. B543 (2002) 227

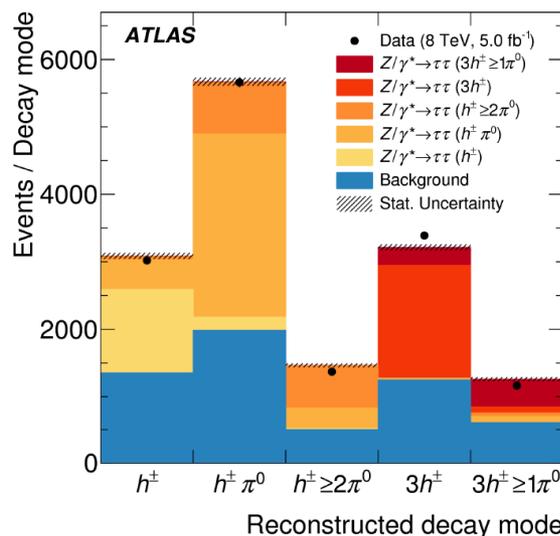
Tau substructure in ATLAS



In general, non-negligible fraction of 2/1 π^0 reconstructed as 1/0 π^0



Good reconstruction of tau mass in different decay modes



Good tau decay classification

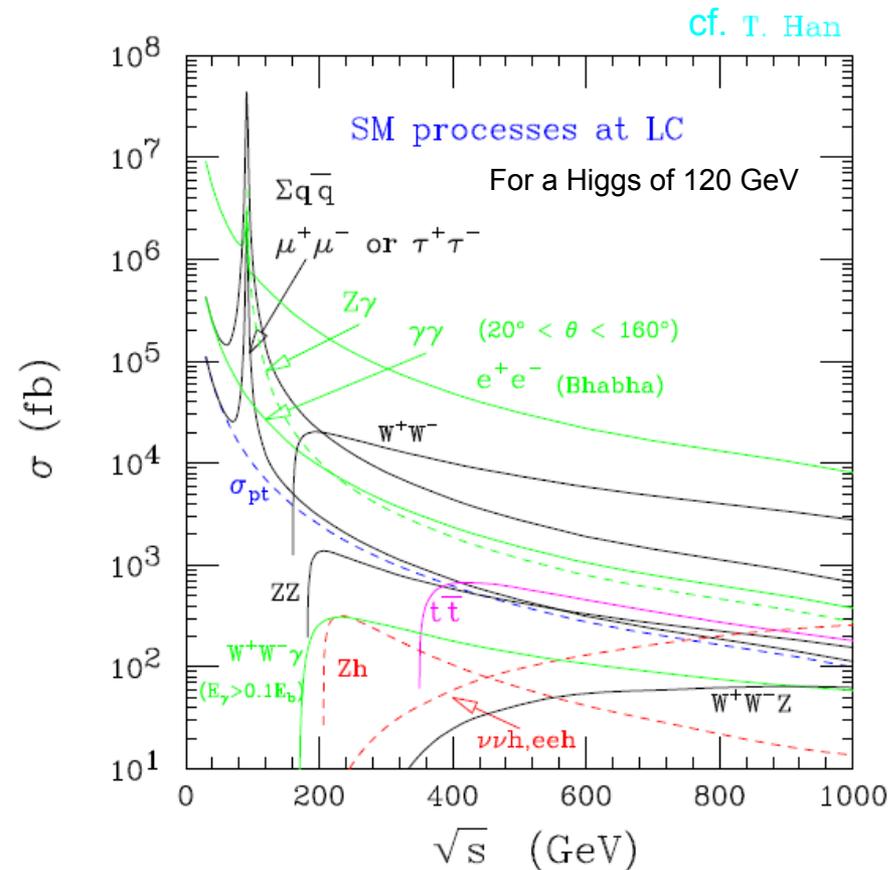
- ❖ With the substructure, a factor of 2 improvement of tau energy w.r.t. the calo-based at low p_T (~ 0.16 for neutral π^0)
- ❖ A factor of 5 improvement in the angular resolution
 - neutral π^0 η : ~ 0.006
 - neutral π^0 Φ : ~ 0.012

$h \rightarrow \tau\tau$ at the e^+e^- collider

- At a e^+e^- collider, the Higgs can be produced via Zh or VBF productions
- We assume a 250 GeV collision energy where the Higgs is mainly produced by the Zh mode. This corresponds to low-energy ILC running

- Three main decay channels are investigated:

Mode	BR (%)
ν_τ / ν_l	35.04
$\nu_\tau \pi^\pm$	10.77
$\nu_\tau \pi^\pm \pi^0$	25.37



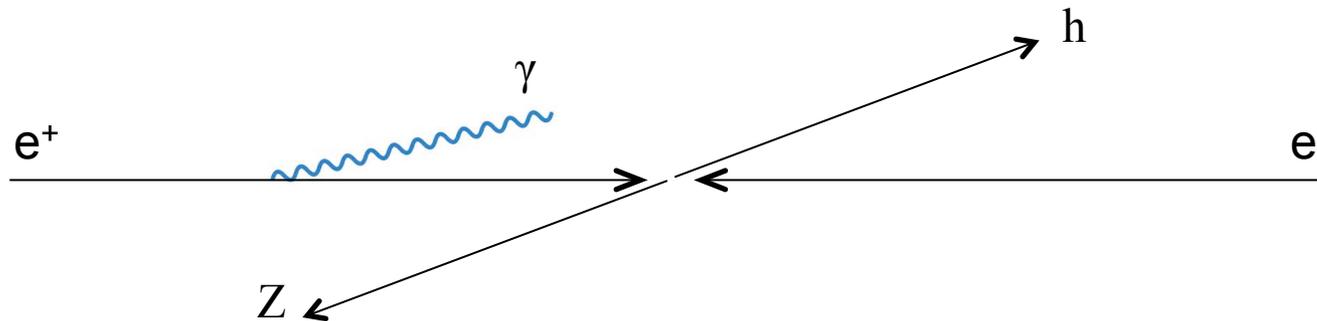
- Encouraged by the tau substructure techniques from ATLAS, it is assumed that π^0 can be resolved with a 10% energy resolution in this analysis. It is further assumed that no cross talk between different modes

$h \rightarrow \tau\tau$ simulation

- The Zh process is produced by MG5, the boson decay and parton shower are handled by Pythia8, and detector response are simulated by DELPHES, with the following parametrization
 - ❖ A magnetic field of 3.5 T, fiducial tracking up to $|\eta|=2.4$. Track direction resolution of 0.001 in η/ϕ , and momentum resolution of $\sqrt{0.01^2 + (10^{-4} p_T)^2}$. Track efficiency is 99%, ID efficiency for e/μ is 95%
 - ❖ The calorimeter energy resolution follows $\sqrt{A^2 E^2 + B^2 E}$, where $A=1.0\%$ (1.5%) and $B=15\%$ (50%) for the EM (hadronic) calorimeter. Particle flow (PF) objects are formed from the tracks and calo clusters. A loose relative lepton isolation of <0.7 is applied to reject leptons from jets
 - ❖ The hadronic taus (τ_{had}) are tagged on Anti-kt $R=0.4$ jets from PF objects with an efficiency of 60% (0.5%) for real (fake) taus. For the $Z \rightarrow jj$ decay, after masking out the leptons and taus, all remaining PF objects are exclusively clustered into two jets
 - ❖ The tracks from tau should have $p_T > 5$ GeV, and the track impact parameter resolution is 5 μm (10 μm) in the transverse (beam) direction

Refined Higgs momentum

- Compared with a hadron collider, the e^+e^- collider has the advantage to resolve the Higgs momentum in z-axis by the recoil of Z, but subject to the ISR photons



- With the known Higgs mass, the fraction of momentum carried away by the collinear photon can be solved, subject to a two-fold ambiguity

$$x = \frac{E_{\text{CM}}^2 - 2E_{\text{CM}}E + m^2 - m_h^2}{\pm E_{\text{CM}}^2 \mp E_{\text{CM}}E + E_{\text{CM}}p_z}$$

E , m and p_z are for the recoiling Z boson. $E_{\text{CM}}=250$ GeV

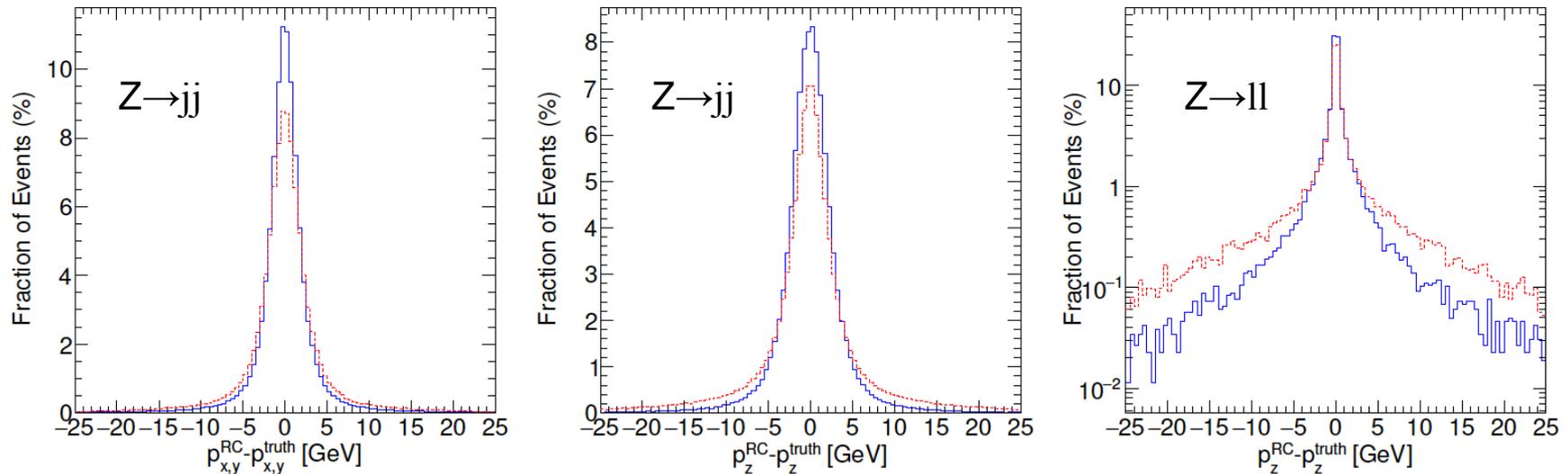
Refined Higgs momentum

- To resolve the ambiguity, collinear approximation (neutrinos from the tau are collinear with the visible products) is used and the following χ^2 is minimized

$$\chi^2 = \sum_{i=0}^3 \left(\frac{p_{h,i} - p_{h,i}^{\text{RC}}}{0.5} \right)^2 + \left(\frac{m_Z - 91.2}{2.5} \right)^2 + \left(\frac{f_{j1} - 1}{0.06} \right)^2 + \left(\frac{f_{j2} - 1}{0.06} \right)^2$$

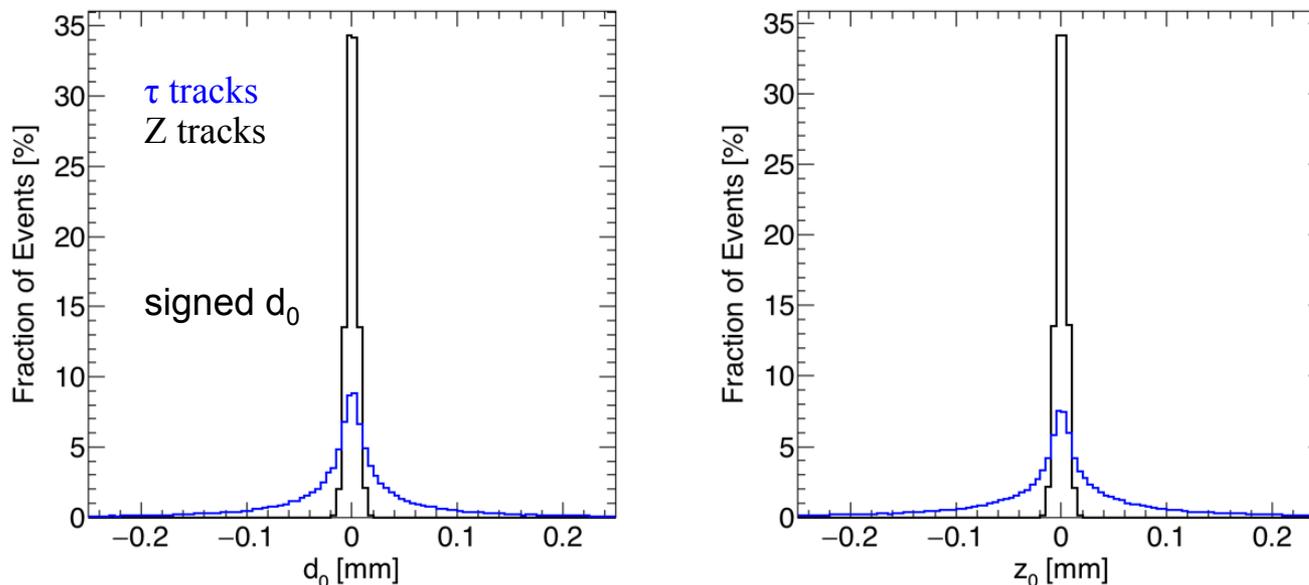
p_h and p_h^{RC} are Higgs 4-momentum from collinear calculation and Z recoil respectively. The $f_{1,2}$ are correction factors for the jets from Z decay

- After minimization, not only the x ambiguity is resolved, but also the Higgs recoil momentum is improved



The impact parameters

- Tracks from taus have broader impact parameter (IP) distributions than the prompt tracks such as the leptons from Z decay

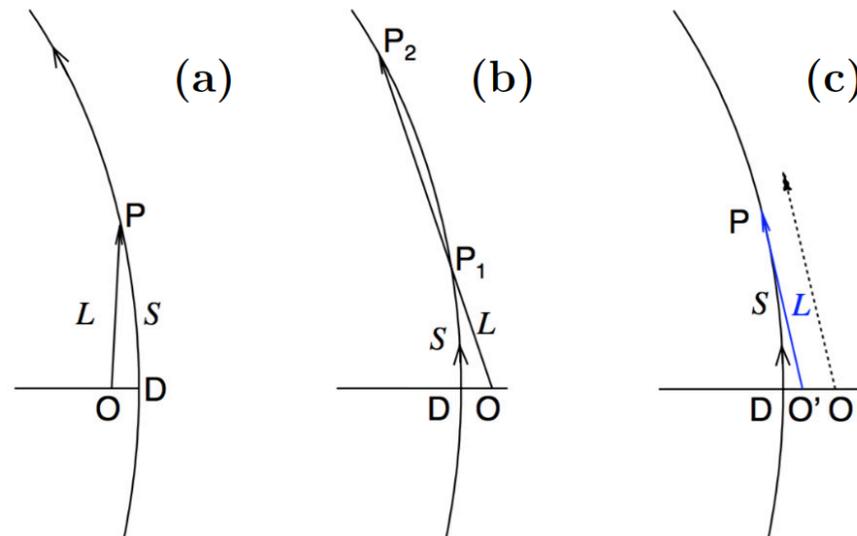


- The impact parameters are additional helpful information to reconstruct the neutrinos from tau decay [A. Rouge hep-ex/0505014; D. Jeans arXiv:1507.01700]. Since the resolution of d_0/z_0 may not be small, we take a less aggressive approach by treating them as extra constraints

We first find the intersection of tau flight direction with the track trajectory in the transverse plane, and deduce z_0 by $z_0 = L \sinh \eta_\tau - S \sinh \eta_{\text{track}}$

The impact parameters

- The collision point (O) can be inside (a) or outside the track path curvature (b, c)
- In the case of (b), two solutions exist and both are tested. In the case of (c), it is assumed to be from resolution effect



- When the fitted impact parameters are in the physical regime, the χ^2 is

$$\chi^2 = \left(\frac{d_0^{\text{fit}} - d_0}{\sigma_d} \right)^2 + \left(\frac{z_0^{\text{fit}} - z_0}{\sigma_z} \right)^2$$

- Otherwise, in the example case of (c), the χ^2 reads (so that the best-fit perigee point for O' is D)

$$\chi^2 = \left(\frac{d_0^{\text{fit}} + d_0 - 2d_0^{\text{C}}}{\sigma_d} \right)^2 + \left(\frac{z_0^{\text{fit}} - z_0}{\sigma_z} \right)^2$$

Neutrino momentum

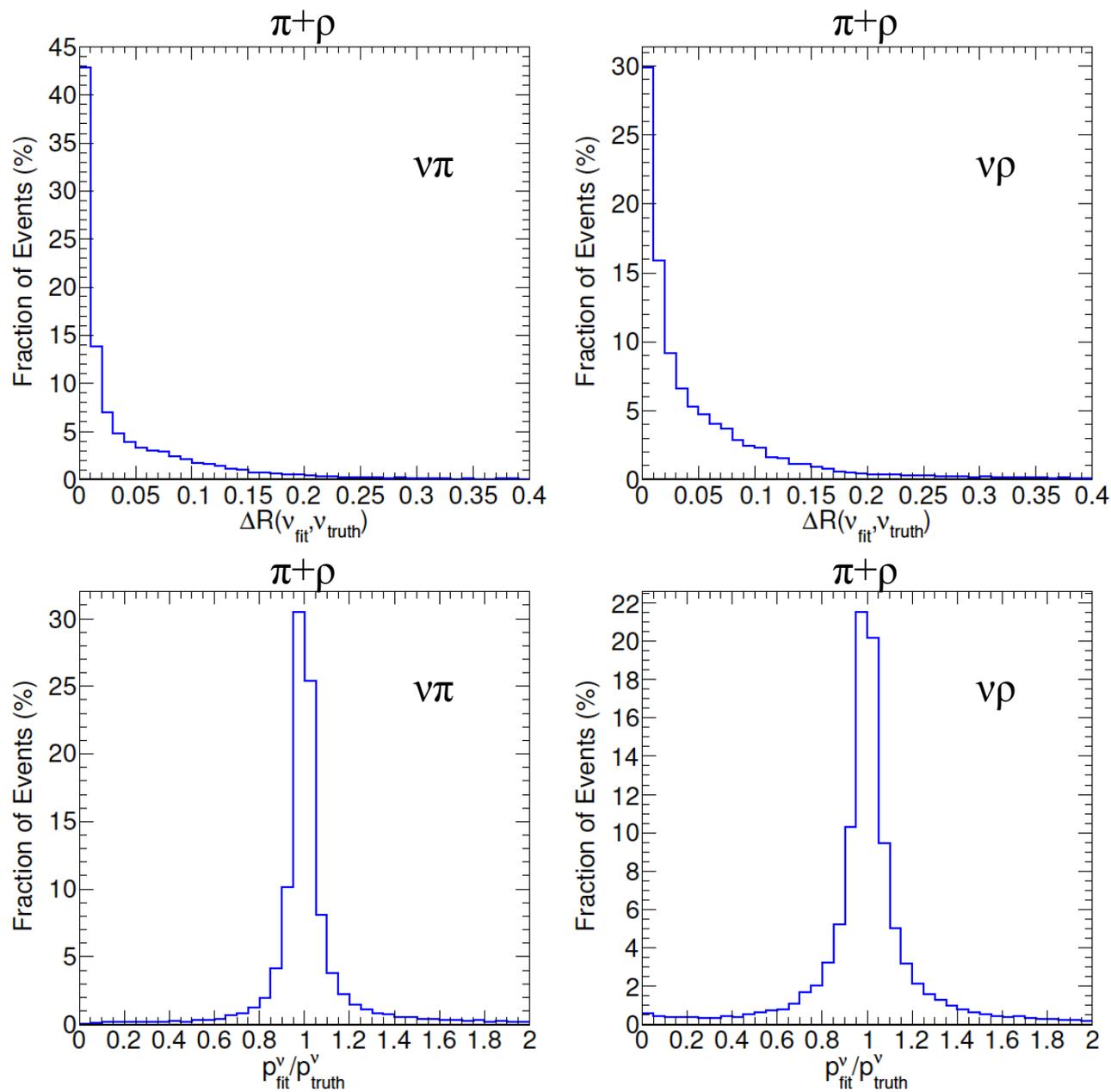
- The momenta of neutrinos from taus can be reconstructed with full constraints in the event

$$\chi^2 = \sum_{i=0}^3 \left(\frac{p_{h,i} - p_{h,i}^{\text{RC}}}{\sigma_{\text{RC}}} \right)^2 + \left(\frac{m_{\tau 1} - 1.777}{\sigma_{\tau 1}} \right)^2 + \left(\frac{m_{\tau 2} - 1.777}{\sigma_{\tau 2}} \right)^2 + \chi_{\text{IP}}^2$$

Higgs 4-momentum, tau mass, IP

- For hadronic (leptonic) tau decays, there are 3 (4) unknowns for the neutrinos momenta (less than the constraints)
- We perform the χ^2 minimization by scanning the η/φ of one neutrino, calculate its momentum by the tau mass, and get the other neutrino's information through the total Higgs 4-momentum. The scan is repeated by starting from the other neutrino
- For leptonic taus, the extra unknown, the neutrino pair mass, is also scanned
- After the global minimal point is obtained by scanning, a MINUIT fit is performed for a better estimation

Neutrino momentum



Cleaning cuts

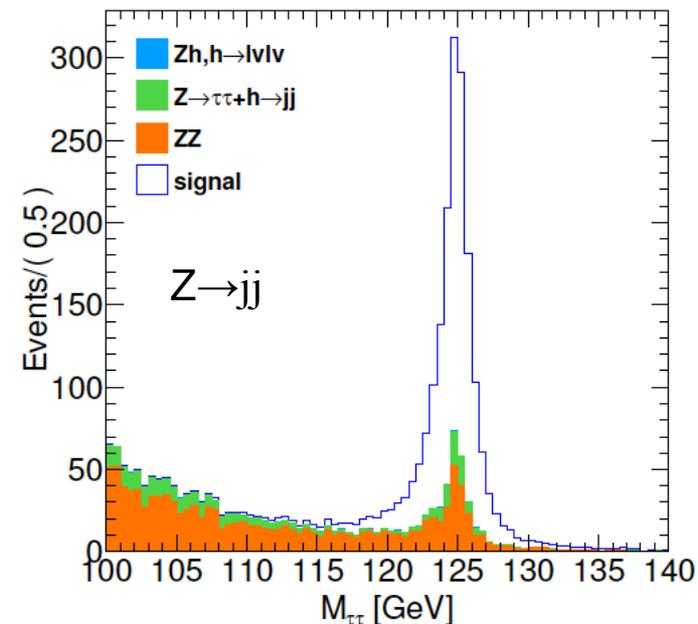
- The combined efficiencies after objects selection (due to jet resolution and neutrino pair, the lepton+Z→jj modes are not considered):

	$\ell + \pi$	$\ell + \rho$	$\pi + \pi$	$\pi + \rho$	$\rho + \rho$
$Z \rightarrow ee/\mu\mu$	31.4%	27.2%	19.2%	18.5%	15.7%
$Z \rightarrow jj$	34.8%	30.8%	24.5%	21.3%	18.9%

- A sequence of cuts are applied to suppress the background, and to purify well reconstructed signal events

$Z \rightarrow \ell\ell$	$Z \rightarrow jj$
$m_Z > 70 \text{ GeV}$	$m_Z < 105 \text{ GeV}$
$m_h^{\text{RC}} > 120 \text{ GeV}$	$m_h^{\text{RC}} > 110 \text{ GeV}$
$m_{h,\text{fit}}^{\text{RC}} > 122 \text{ GeV}$	$80 \text{ GeV} < m_Z^{\text{fit}} < 100 \text{ GeV}$
$120 \text{ GeV} < m_h < 130 \text{ GeV}$	
$1.5 \text{ GeV} < m_\tau < 2.0 \text{ GeV}$	
$m_\rho > 0.3 \text{ GeV}$ (for channels with ρ)	

With 5 ab^{-1} of data, expect to have about 1519 (133) signal (background) events



Higgs CP

- With all final state particles reconstructed, we can perform a Matrix Element based analysis of the underlying Higgs CP mixing angle Φ . The Higgs decay amplitude can be expressed as

$$\begin{aligned} |\mathcal{M}|^2 &\propto A + B \cos(2\phi) + C \sin(2\phi), \\ &\propto I_1 \cos^2(\phi) + I_2 \sin(\phi) \cos(\phi) + I_3 \sin^2(\phi) \end{aligned}$$

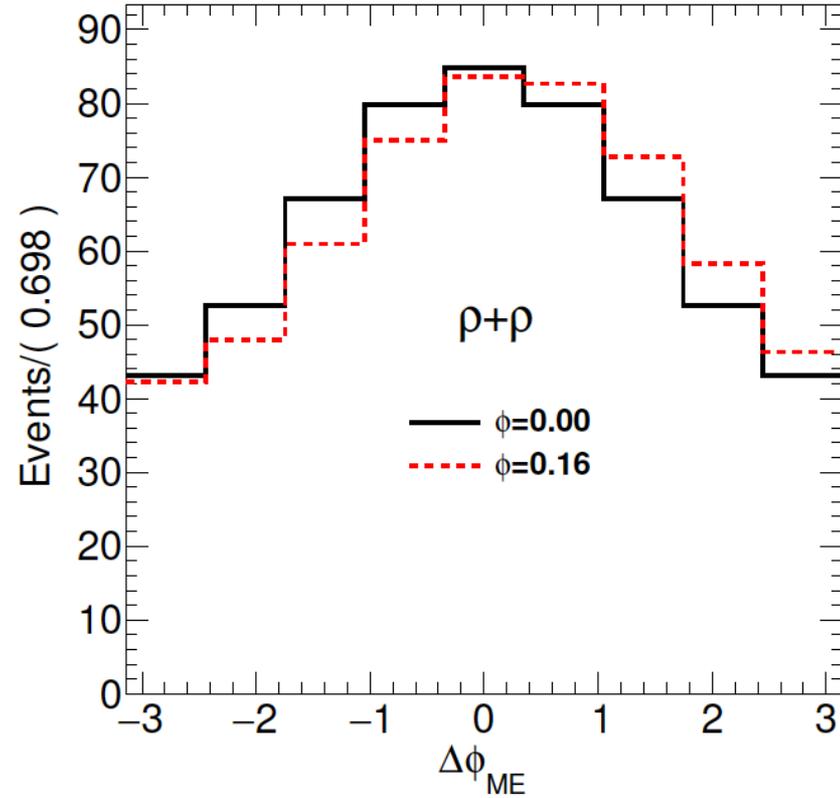
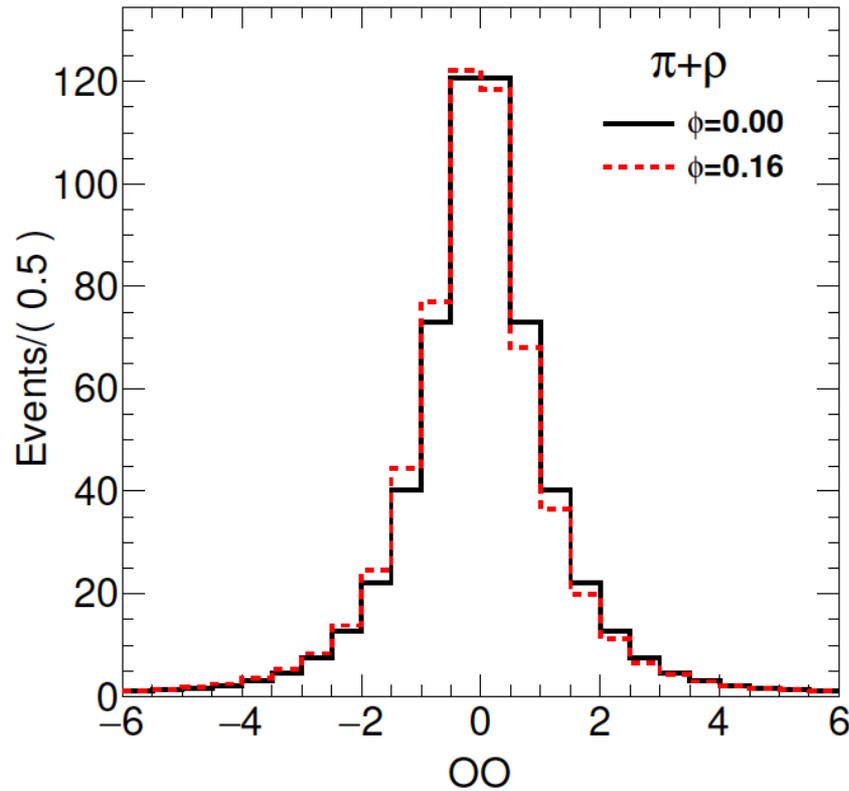
- Two observables can be reconstructed per event for the CP test
 - ❖ Optimal Observable (M. Davier et. al, Phys. Lett. B306,1993, 411): $OO = I_2/I_1$
 - ❖ ME angle $\Delta\Phi_{ME}$, defined as

$$\begin{aligned} |\mathcal{M}|^2 &\propto A + \sqrt{B^2 + C^2} \cos(\Delta\phi_{ME} - 2\phi) \\ \cos(\Delta\phi_{ME}) &= \frac{B}{\sqrt{B^2 + C^2}}, \quad \sin(\Delta\phi_{ME}) = \frac{C}{\sqrt{B^2 + C^2}} \end{aligned}$$

At low mixing angle values, the two perform similarly, while in high values of Φ , $\Delta\Phi_{ME}$ is better

Higgs CP

- The OO and $\Delta\Phi_{ME}$ distributions in the $\pi+\rho$ and $\rho+\rho$ channels for CP even and $\Phi=0.16$



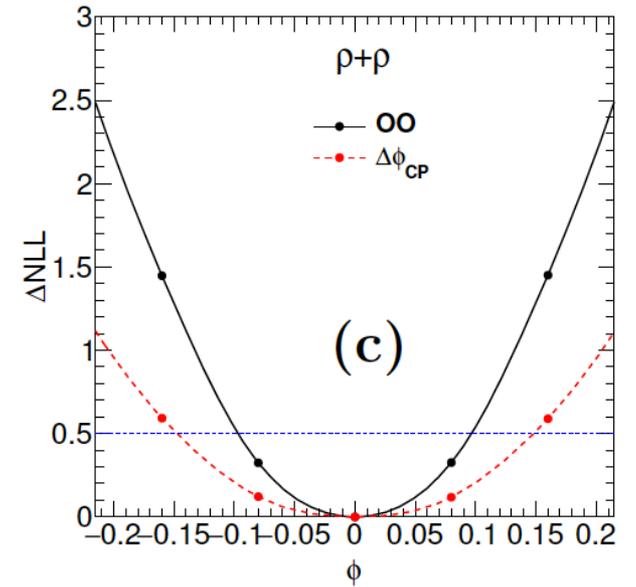
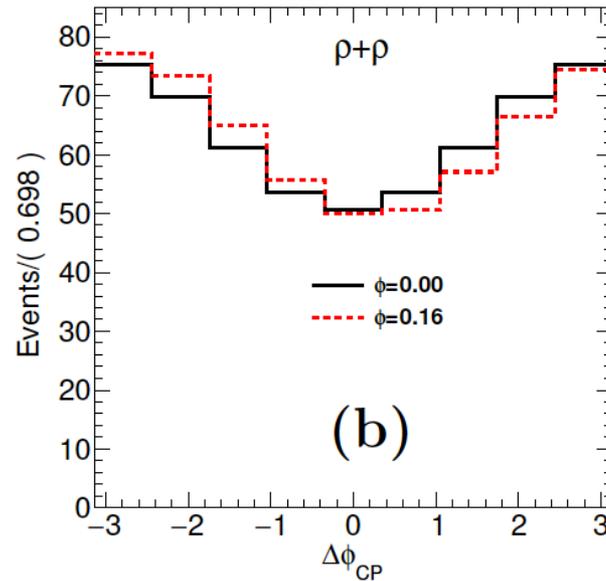
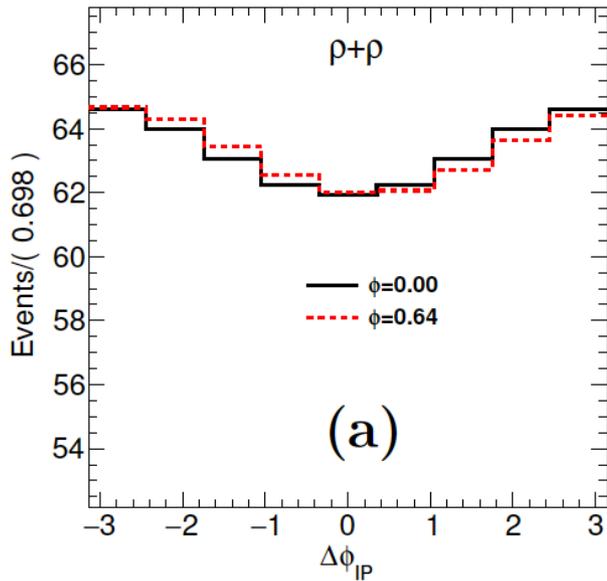
Higgs CP

- The OO or $\Delta\Phi_{\text{ME}}$ is better than the other observables such as $\Delta\Phi_{\text{IP}}$ and $\Delta\Phi_{\text{CP}}$

$$\Phi = \arccos(\hat{p}_{d1}^\perp \cdot \hat{p}_{d2}^\perp) \times \text{sgn}(\hat{p}_{m1} \cdot (\hat{p}_{d1}^\perp \times \hat{p}_{d2}^\perp))$$

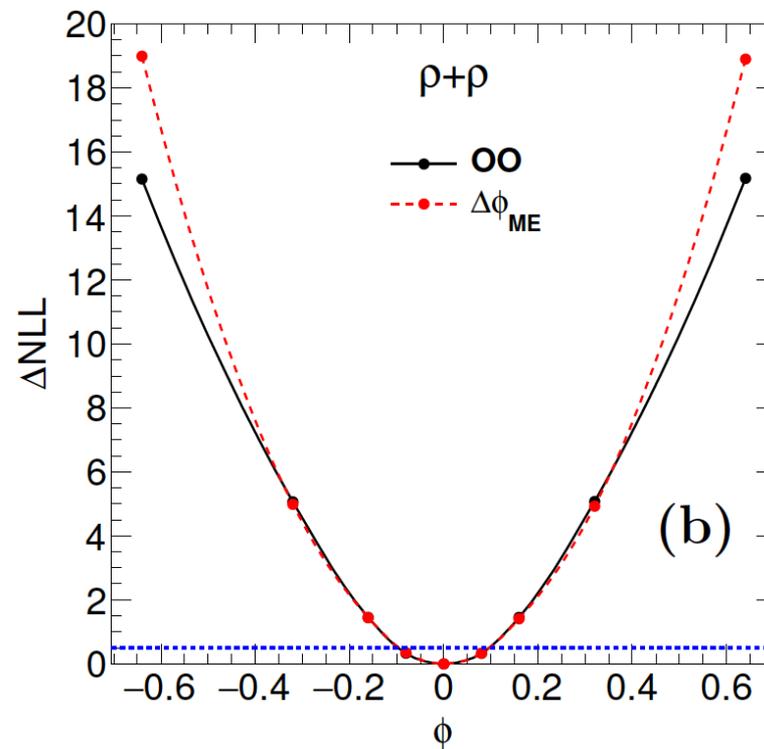
$$\text{For } \Delta\Phi_{\text{IP}}, (\hat{p}_{m1}, \hat{p}_{d1}, \hat{p}_{m2}, \hat{p}_{d2}) = (p_{\pi^+} + p_{\pi^0}, n^+, p_{\pi^-} + p_{\pi^0}, n^-)$$

$$\text{For } \Delta\Phi_{\text{CP}}, (\hat{p}_{m1}, \hat{p}_{d1}, \hat{p}_{m2}, \hat{p}_{d2}) = (p_{\pi^+}, p_{\pi^0}, p_{\pi^-}, p_{\pi^0})$$



Higgs CP

- Template PDF functions for different CP mixing angle hypotheses are prepared and fit to the pseudo-data. The difference (w.r.t. the minimum) of the Negative Log Likelihood (ΔNLL) is plotted for different Φ , from which the 1σ confidence interval can be found



With 5 (2) ab^{-1} of data, a precision of 2.9° (5.2°) can be reached for the Higgs CP mixing angle measurement

Summary

Testing the CP nature of the Higgs is one of the important tasks after its discovery. This needs a large and pure Higgs signal events with rich decay products, and can be achieved with a high precision at future e^+e^- colliders

The $H \rightarrow \tau\tau$ decay is an ideal channel for probing Higgs CP angle for possible effect of CP violation. Our study, based on three tau decay modes, show that with 5 (2) ab^{-1} of data, a precision of 2.9° (5.2°) can be reached for the CP angle measurement

Extra Slides