

# CLIC DR design using variable bends and high-field wigglers

S. Papadopoulou<sup>1,2</sup>, F. Antoniou<sup>1</sup>, Y. Papaphilippou<sup>1</sup>

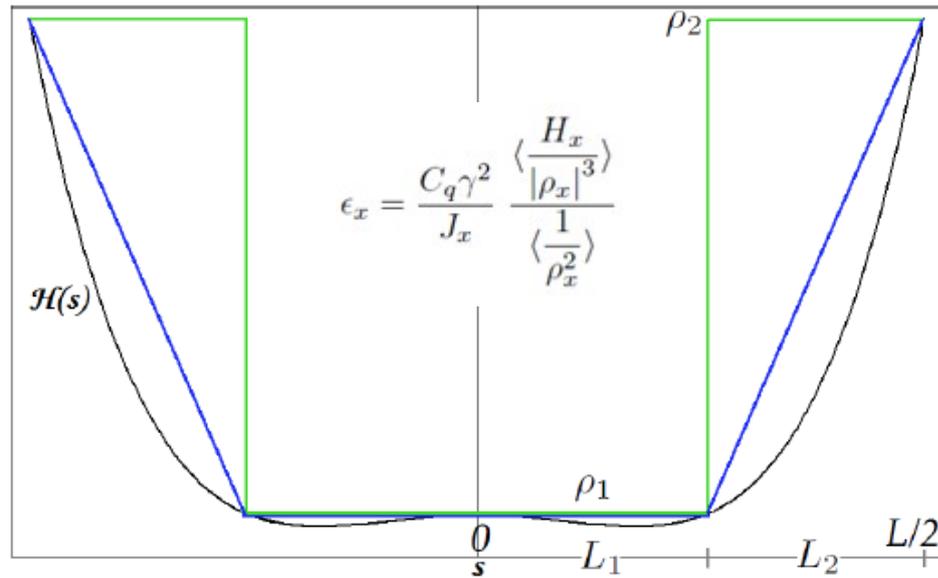
<sup>1</sup>CERN, <sup>2</sup>University of Crete



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- **Optimization of the arc TME cell**
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# Longitudinally variable bends<sup>[1]</sup>



$$\rho_{st}(s) = \begin{cases} \rho_1, & 0 < s < L_1 \\ \rho_2, & L_1 < s < L_1 + L_2 \end{cases}$$

$$\rho_{tr}(s) = \begin{cases} \rho_1, & 0 < s < L_1 \\ \rho_1 + \frac{(L_1 - s)(\rho_1 - \rho_2)}{L_2}, & L_1 < s < L_1 + L_2 \end{cases}$$

Bending radii ratio

$$\rho = \frac{\rho_1}{\rho_2}$$

Lengths ratio

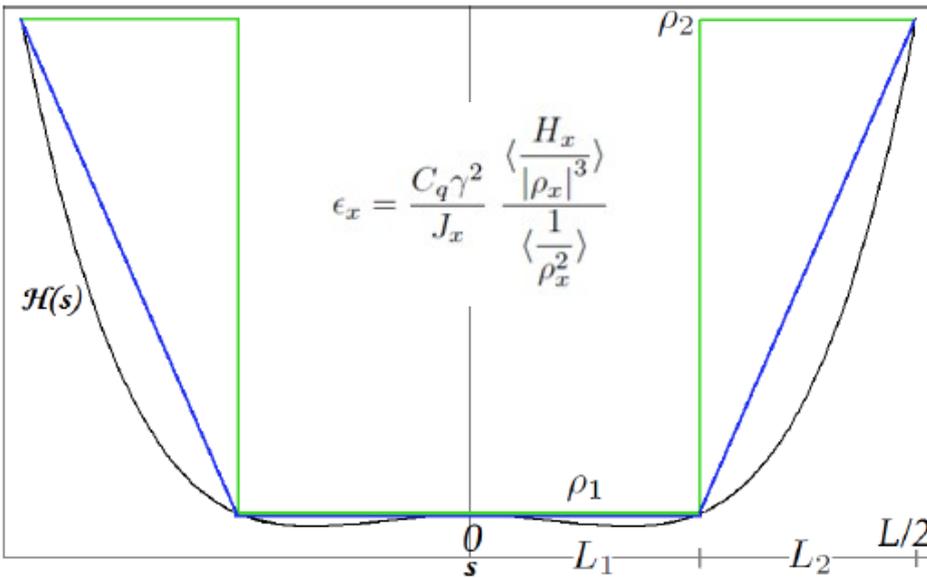
$$\lambda = \frac{L_1}{L_2}$$

Emittance  
reduction factor

$$F_{TME} = \frac{\epsilon_{TME_{uni}}}{\epsilon_{TME_{var}}}$$

$$F_{TME} > 1$$

# Longitudinally variable bends<sup>[1]</sup>



$$\epsilon_x = \frac{C_q \gamma^2}{J_x} \frac{\left\langle \frac{H_x}{|\rho_x|^3} \right\rangle}{\left\langle \frac{1}{\rho_x^2} \right\rangle}$$

$$\rho_{st}(s) = \begin{cases} \rho_1, & 0 < s < L_1 \\ \rho_2, & L_1 < s < L_1 + L_2 \end{cases}$$

$$\rho_{tr}(s) = \begin{cases} \rho_1, & 0 < s < L_1 \\ \rho_1 + \frac{(L_1 - s)(\rho_1 - \rho_2)}{L_2}, & L_1 < s < L_1 + L_2 \end{cases}$$

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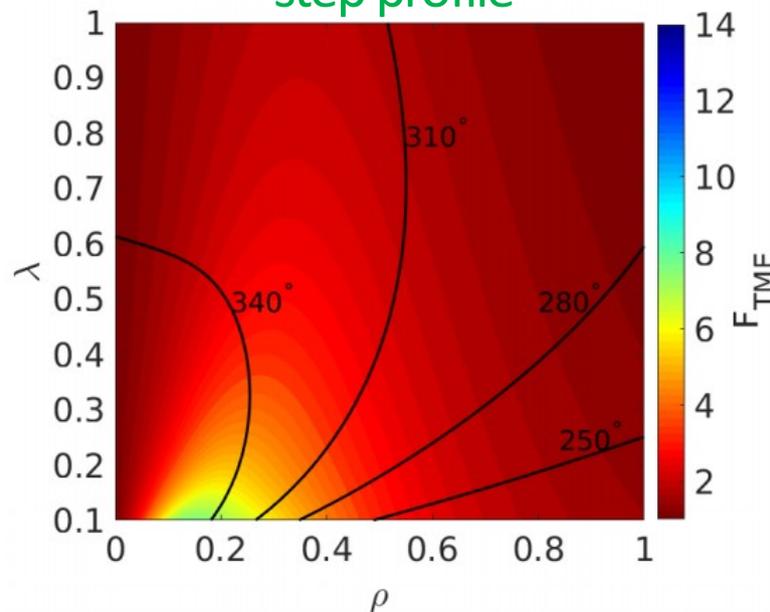
$$\lambda = \frac{L_1}{L_2}$$

Emittance reduction factor

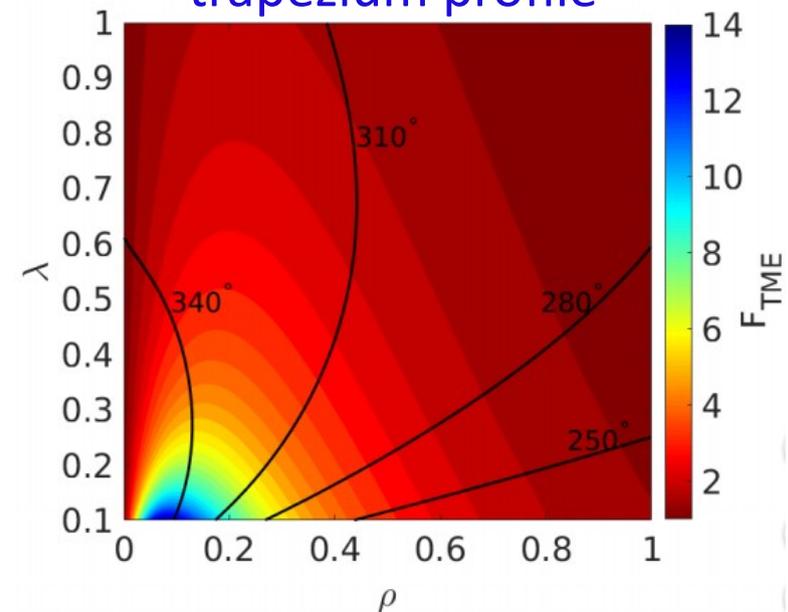
$$F_{TME} = \frac{\epsilon_{TME_{uni}}}{\epsilon_{TME_{var}}}$$

$$F_{TME} > 1$$

step profile



trapezium profile



The parameterization of the emittance reduction factor  $F_{TME}$  with the bending radii ratio  $\rho$  and the lengths ratio  $\lambda$ , always for  $\lambda > 0.1$ .

# Fixing the dipole's characteristics (bending angle, length and minimum bending radius)

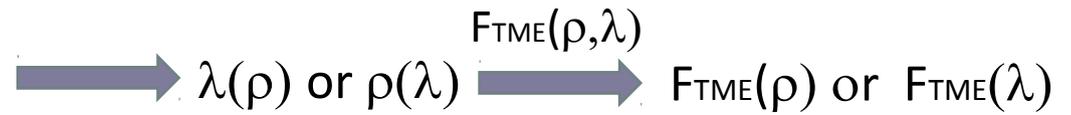
$$\theta_{step} = \frac{L(\lambda + \rho)}{\rho_1(1 + \lambda)}$$

$$\theta_{trapezium} = \frac{L(\lambda(-1 + \rho) + \rho \ln \rho)}{\rho_1(-1 + \rho)(1 + \lambda)}$$

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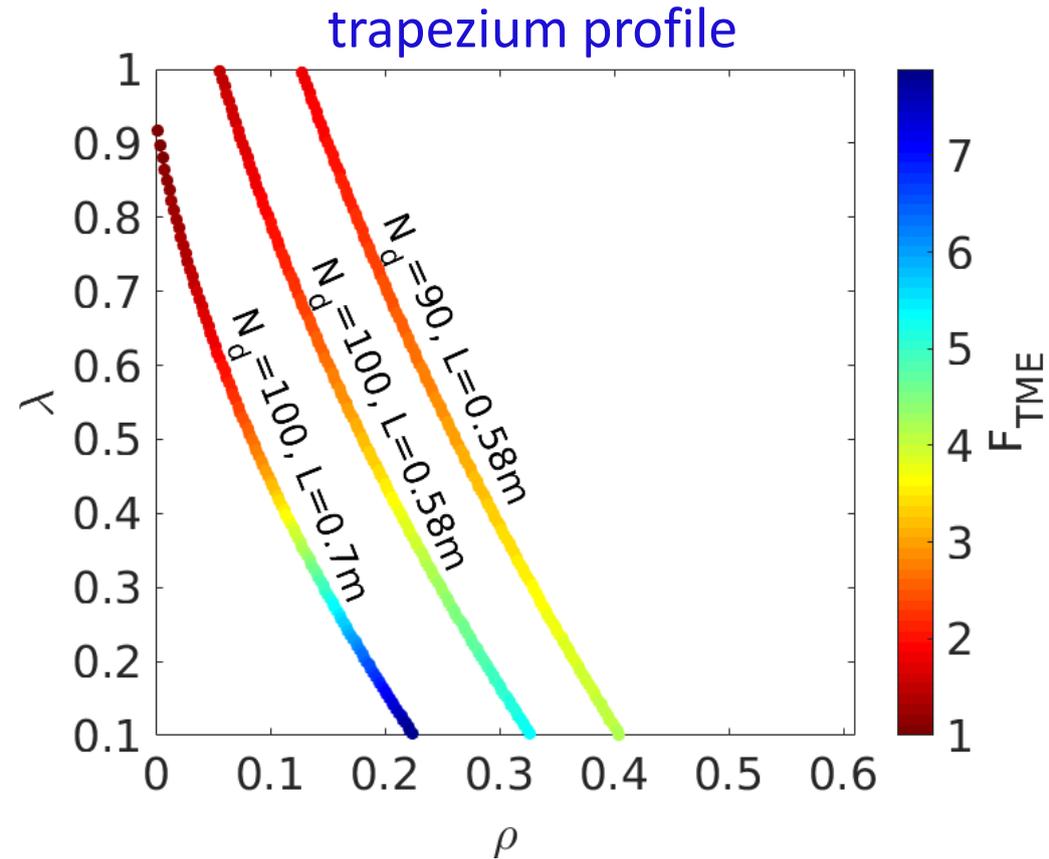
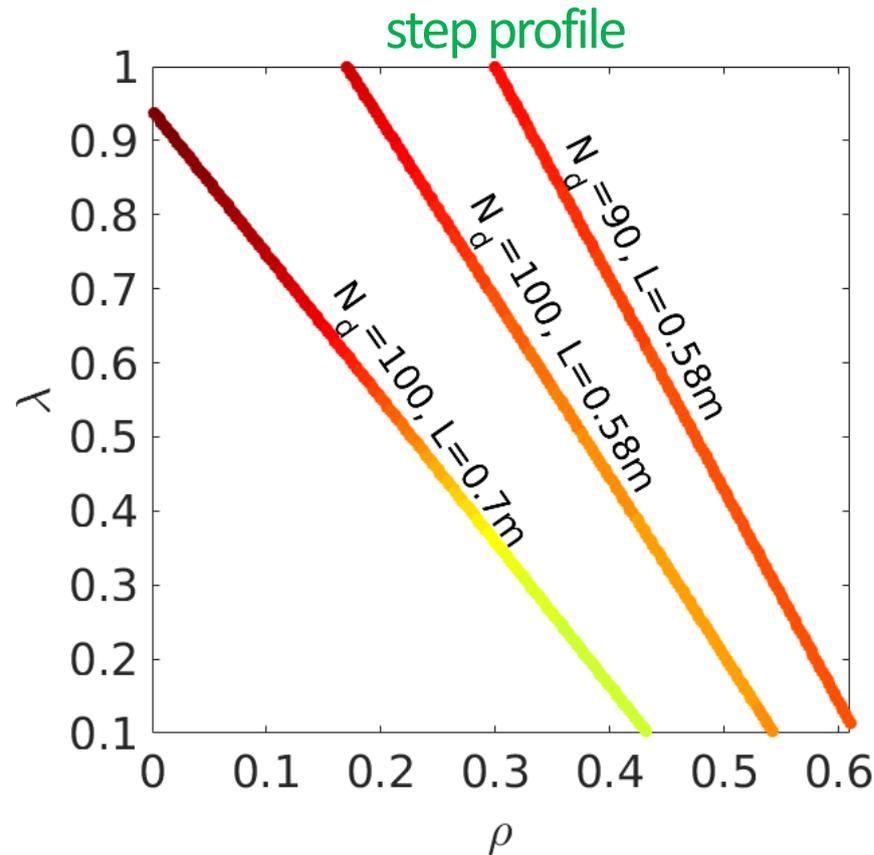


# Fixing the dipole's characteristics (bending angle, length and minimum bending radius)

$$\theta_{step} = \frac{L(\lambda + \rho)}{\rho_1(1 + \lambda)}$$

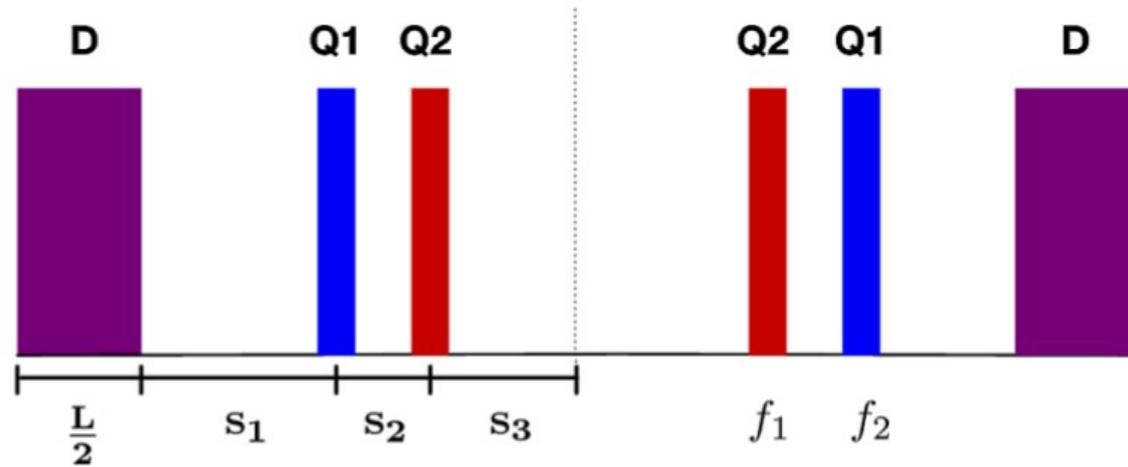
$$\theta_{trapezium} = \frac{L(\lambda(-1 + \rho) + \rho \ln \rho)}{\rho_1(-1 + \rho)(1 + \lambda)}$$

→  $\lambda(\rho)$  or  $\rho(\lambda)$  →  $F_{TME}(\rho, \lambda)$  →  $F_{TME}(\rho)$  or  $F_{TME}(\lambda)$



↓  $L, N_d$  → ↓  $F_{TME}$

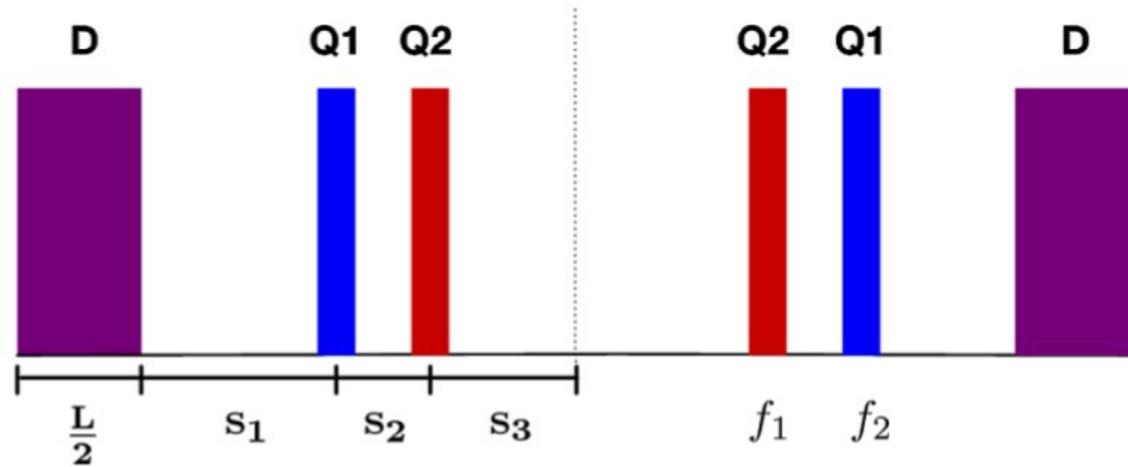
# Optimization of the arc TME cell



Fixing the dipoles' characteristics

(bending radii ratio  $\rho$  and lengths ratio  $\lambda$ , dipole's length  $L$  and bending angle  $\theta$  or else the total number of dipoles  $N_d$ ) in order to get a large  $F_{\text{TME}}$

# Optimization of the arc TME cell



Fixing the dipoles' characteristics

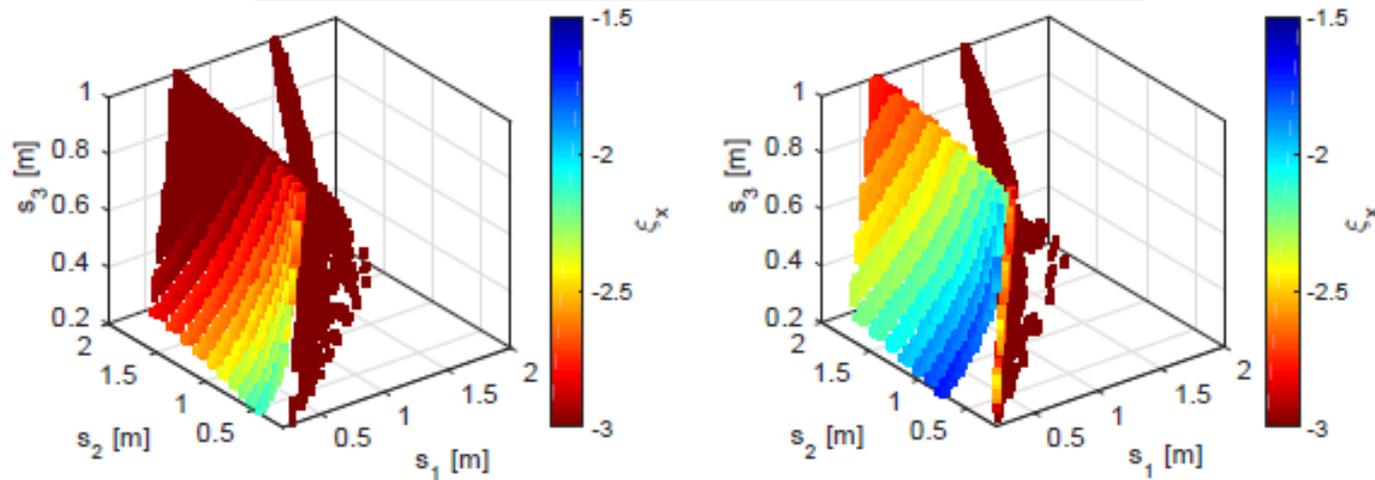
(bending radii ratio  $\rho$  and lengths ratio  $\lambda$ , dipole's length  $L$  and bending angle  $\theta$  or else the total number of dipoles  $N_d$ ) in order to get a large  $F_{TME}$

Aiming to reduce the DRs circumference and get the required output parameters, it is necessary to find:

- the lengths of the elements and of the drifts that result in a compact cell.
- the optimal phase advances for which:
  - the horizontal and vertical emittances are  $\gamma\varepsilon_x < 500\text{nm}$ ,  $\varepsilon_1 < 6\text{ keV m}$
  - the low chromaticities in both planes guarantee an adequate dynamic aperture
  - and the quadrupole strengths are  $k_1, k_2 < 100\text{ T/m}$ .

# Optimization of the arc TME cell

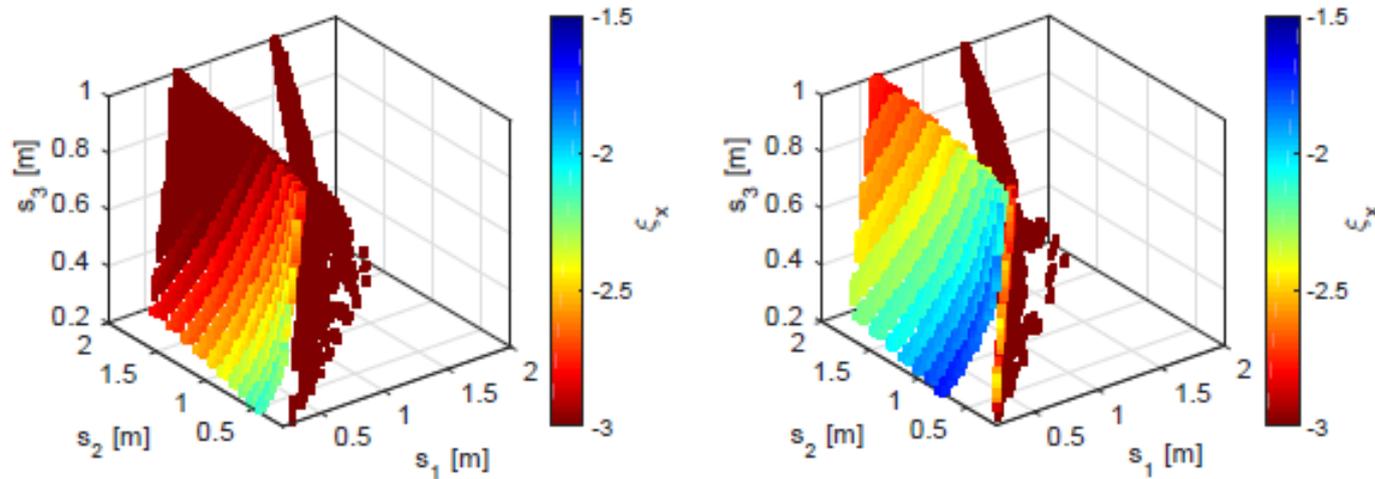
Parametrization with the drift lengths



*The horizontal chromaticity  $\xi_x$  is parameterized with the drift lengths  $s_1$ ,  $s_2$ ,  $s_3$  for the TME, for the step (left) and the trapezium (right) profile*

# Optimization of the arc TME cell

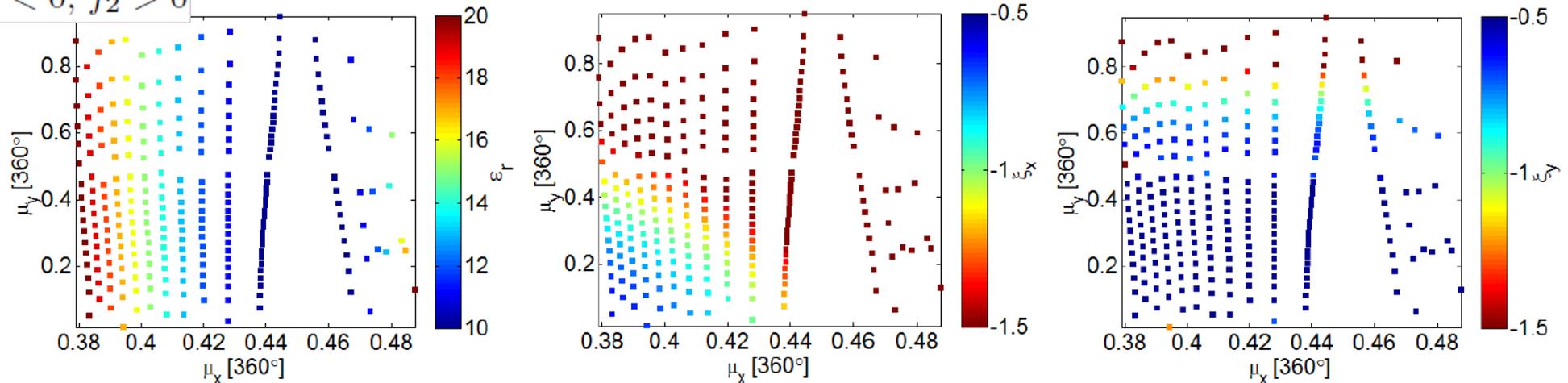
## Parametrization with the drift lengths



The horizontal chromaticity  $\xi_x$  is parameterized with the drift lengths  $s_1$ ,  $s_2$ ,  $s_3$  for the TME, for the step (left) and the trapezium (right) profile

## Parametrization with the phase advances

$$f_1 < 0, f_2 > 0$$



The parameterization of the detuning factor  $\varepsilon_r$  ( $\varepsilon_r = \varepsilon_x / \varepsilon_{TME}$ ) and of the horizontal and vertical chromaticities ( $\xi_x$  and  $\xi_y$ ) with the horizontal and vertical phase advances  $\mu_x$  and  $\mu_y$ , only for the trapezium profile.

# Optimization of the arc TME cell

$$\frac{\epsilon_{var}}{\epsilon_{uni}} < 1$$

$$\frac{\epsilon_{var}}{\epsilon_{uni}} = \frac{\epsilon_{r_{var}} \epsilon_{TME_{var}}}{\epsilon_{r_{uni}} \epsilon_{TME_{uni}}} = \frac{\epsilon_{r_{var}}}{\epsilon_{r_{uni}}} \frac{1}{F_{TME}}$$

$$\frac{\epsilon_{r_{var}}}{\epsilon_{r_{uni}}} < F_{TME}$$

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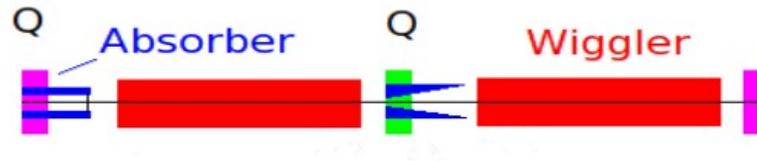
For optimized variable bends characteristics, lower emittances than the ones of the current design are reached. This gives us the flexibility to reduce the existing TME cells of the arcs, till the point we get the required output parameters.

procedure followed in MADX

removing TME cells  
checking the output parameters

The optimal solutions are found to be  $N_d=96$  for the step and  $N_d=90$  for the trapezium profile, instead of the existing arc's cell that are  $N_d=100$ .

# Optimization of the wiggler FODO cell



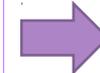
Results obtained after the optimization of the arc TME cell.



When increasing the wigglers' peak field  $B_w$  up to a certain point, the emittance and the IBS effect are lowered<sup>[3]</sup>.

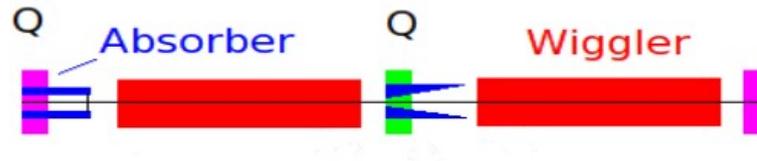


Based on the technological restrictions, a new working point for the damp. wiggler is proposed to be at 3.5T (prev. 2.5T), with 49mm period length<sup>[4]</sup>



Removing some FODO cells from the existing straight section ( $N_{\text{FODO}}=13$  per section) is possible.

# Optimization of the wiggler FODO cell



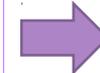
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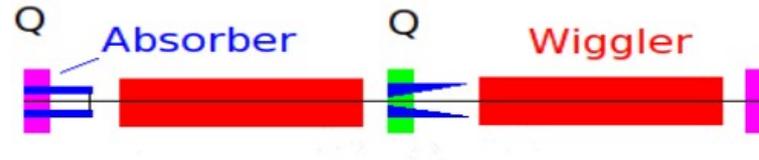
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$N_{\text{FODO}}=10$  per straight section

# Optimization of the wiggler FODO cell



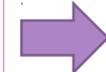
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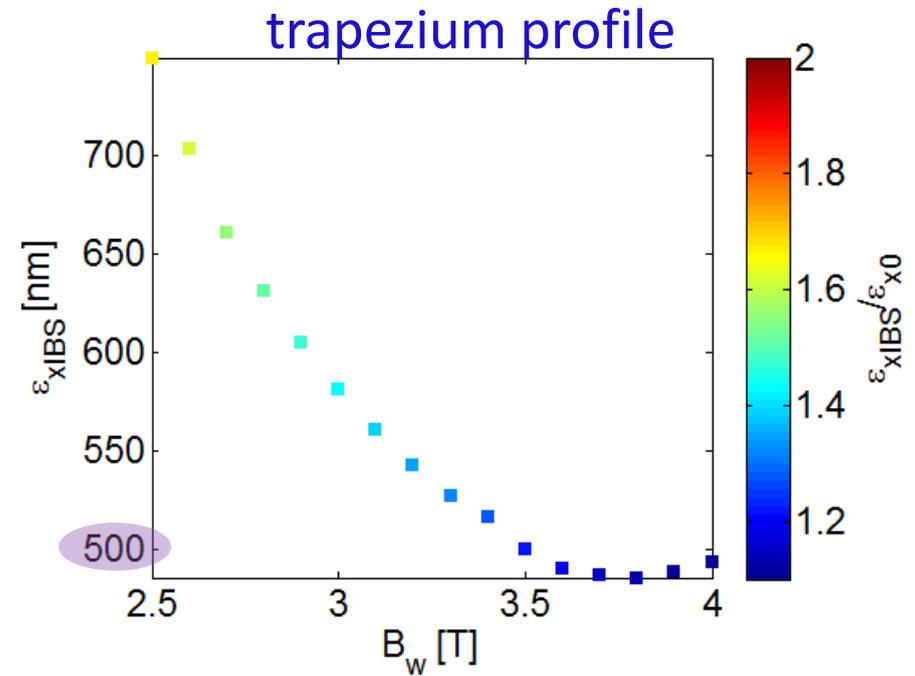
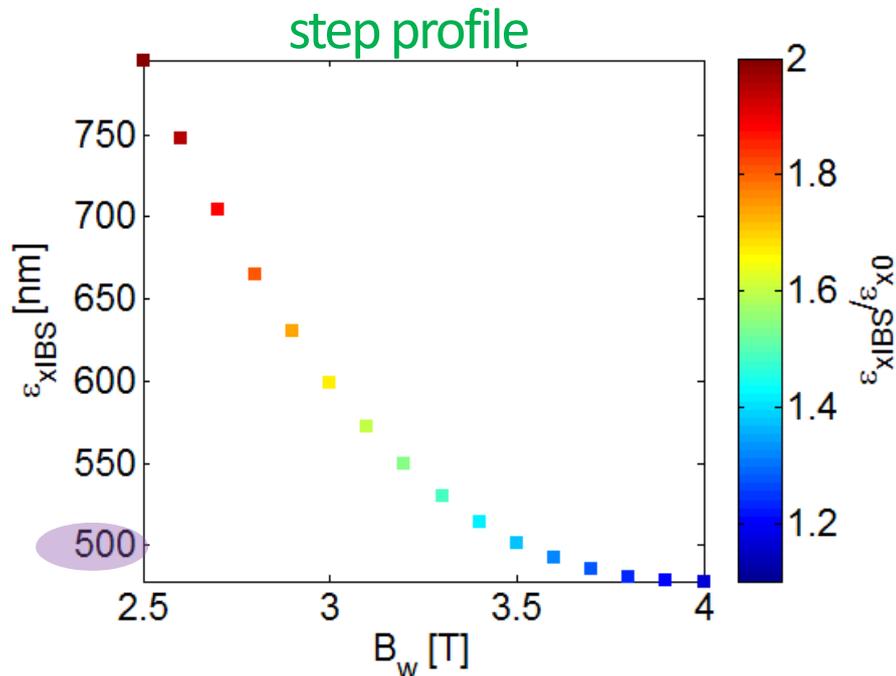


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Parametrization of the steady state emittance and the IBS effect with the wiggler's peak field  $B_w$

# Design parameters for the main DRs, E=2.86 GeV , 2GHz

Nb=4 .07e+09

Nb=5 .7e+09

Parameters, Symbol [Unit]	uniform	step	trapezium	trapezium
Number of arc cells/wigglers	100/52	96/40	90/40	90/40
Dipole field (max/min), B [T]	0.97/0.97	1.77/1.01	1.77/0.73	1.77/0.73
horiz. /vert. chromaticities $\xi_x/\xi_y$	-113/-82	-135/-76	-126/-72	-134/-41
Wiggler peak field $B_w$ [T] for length $L_w=2m$	2.5	3.5	3.5	3.5
Wiggler period, $\lambda_w$ [cm]	5.0	4.9	4.9	4.9
Mom. compaction, $\alpha_c$ [ $10^{-4}$ ]	1.3	1.3	1.2	1.2
Energy loss/turn, U [MeV/turn]	4	5.7	5.7	5.8
Energy spread (rms), $\sigma_\delta$ [%]	0.12	0.13	0.13	0.13
Bunch length (rms), $\sigma_s$ [mm]	1.8	1.6	1.6	1.3
Long. emittance , $\varepsilon_l$ [keV m]	5.9	6.1	6.0	5.0
Damp. times, ( $\tau_x, \tau_y, \tau_l$ ) [ms]	(2.0, 2.0, 1.0)	(1.2, 1.3, 0.6)	(1.2, 1.2, 0.6)	(1.2, 1.2, 0.6)
IBS factors hor./ver./long.	2.2/1.5/1.2	1.4/1.5/1.1	1.4/1.5/1.1	1.4/2.0/1.1
Norm. horizontal emittance (with IBS), $\gamma\varepsilon_x$ [nm]	681	502	500	579
Norm. vertical emittance (with IBS), $\gamma\varepsilon_y$ [nm]	5	5	5	6.7
Circumference, C [m]	427.5	374.1 (-14%)	359.4 (-19%)	359.4 (-19%)

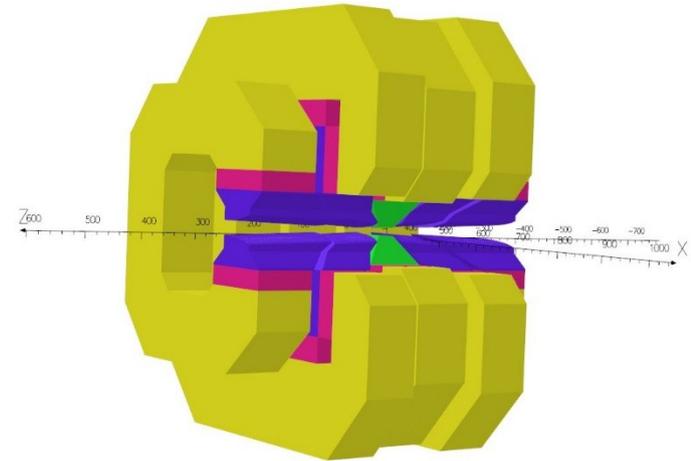
- S. Papadopoulou, F. Antoniou and Y. Papaphilippou, Alternative optics design of the CLIC Damping Rings with variable dipole bends and high-field wigglers, proc. of IPAC'15
- H. Ghasem et al. , “Nonlinear Optimization of CLIC DRS New Design with Variable Bends and High Field Wigglers”, proc. of IPAC'16

# Magnet design based on the characteristics of the variable bends for the CLIC DRs

-Based on the trapezium profile, the designed dipole has a total length of 56 cm and bends the beam by 4 degrees.

- A maximum field of 2.3 T is reached. The  $\lambda$  and  $\rho$  values achieved are 0.04 and 0.29 respectively, corresponding to a  $F_{TME}=7$ .

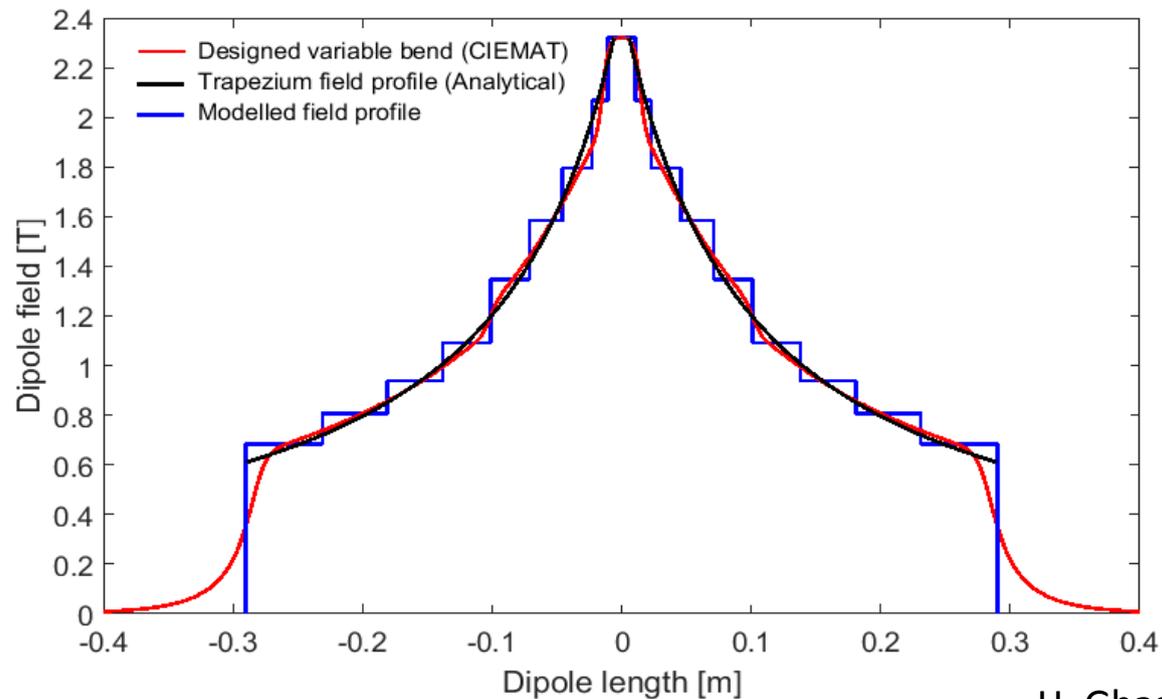
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Opera  
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M. A. Domínguez, F. Toral (CIEMAT, Spain)

see “Design of a Dipole with Longitudinally Variable Field using Permanent Magnets for CLIC DRs”

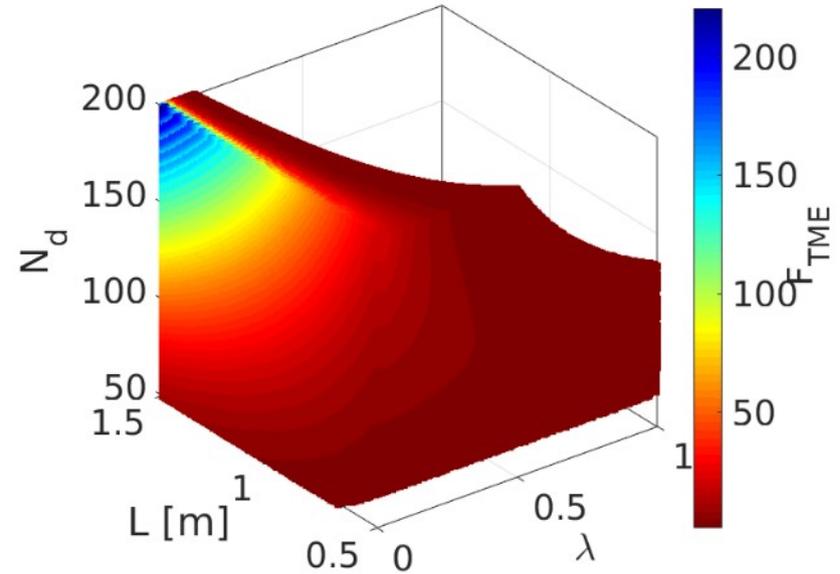
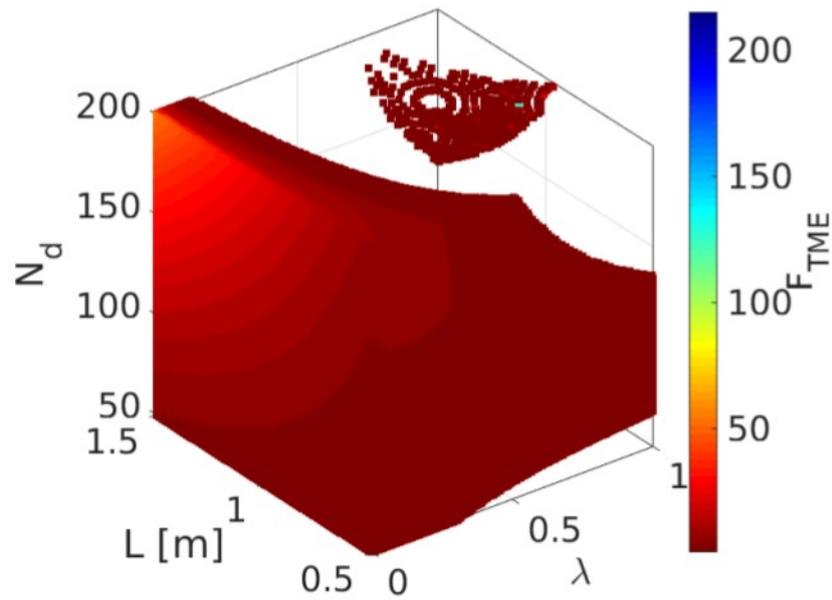


H. Ghasem

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-C.-x Wang, Y. Wang, Y. Peng, PRST-AB 14, 034001 (2011).
  
- [2] Y. Papaphilippou et al., ``Conceptual design of the CLIC damping rings'', TUPPCO86, proc. of IPAC'12, New Orleans, USA (2012).
  
- [3] -F. Antoniou, PhD thesis, NTUA, (2013)  
-D. Schoerling et al, PRST-AB 15, 042401 (2012).
  
- [4] L. Garcia Fajardo, ``Nb3Sn prototype progress'', CLIC Workshop, CERN, Geneva (2015).

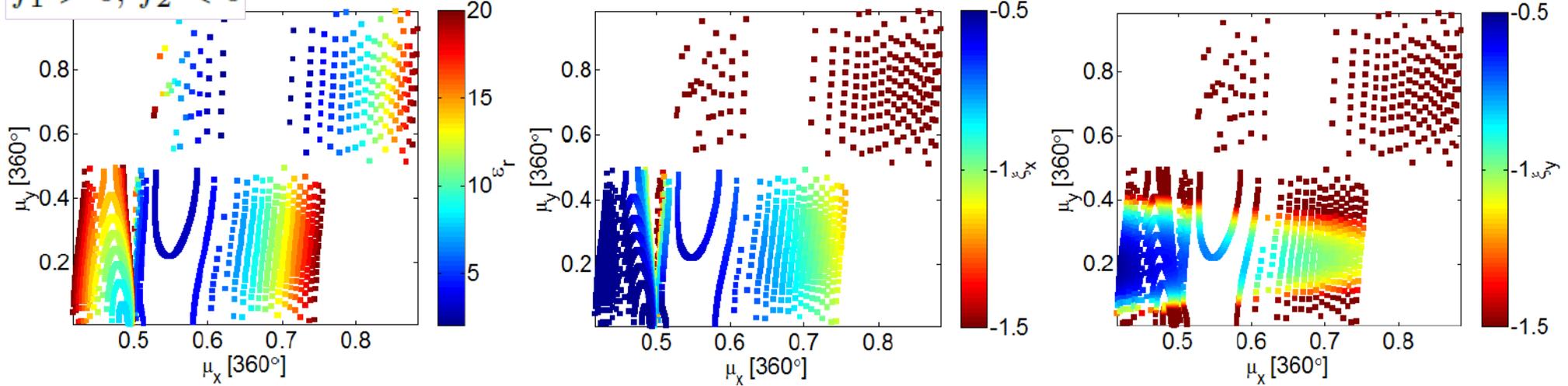
*Thank you!*



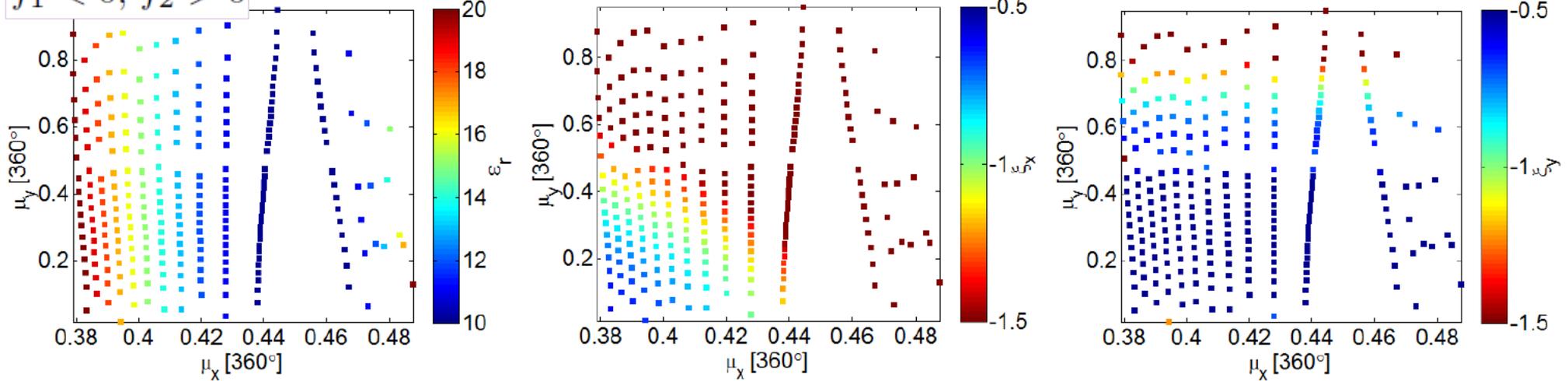
The parameterization of the emittance reduction factor  $F_{TME}$  with the lengths ratio  $\lambda$ , the dipole length  $L$  and the number of dipoles used  $N_d$  for the step (left) and the trapezium (right) profile.

# Optimization of the arc TME cell

$f_1 > 0, f_2 < 0$

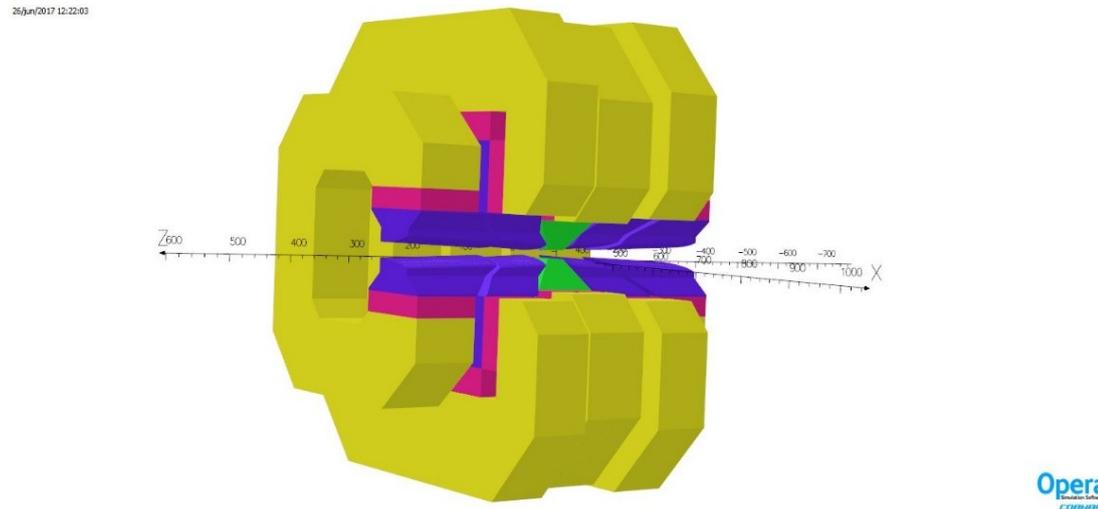
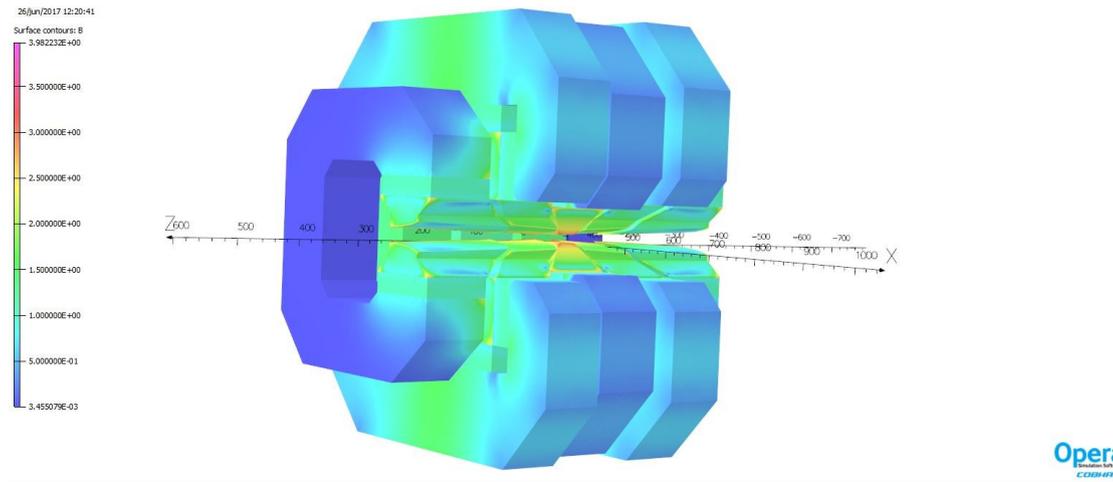


$f_1 < 0, f_2 > 0$



The parameterization of the detuning factor  $\varepsilon_r$  ( $\varepsilon_r = \varepsilon_x / \varepsilon_{TME}$ ) and of the horizontal and vertical chromaticities  $\xi_x$  and  $\xi_y$  with the horizontal and vertical phase advances  $\mu_x$  and  $\mu_y$  only for the trapezium profile.

# Magnet design based on the characteristics of the variable bends for the CLIC DRs



- Armco (pure iron) for the yokes, low and medium field poles
- Iron-cobalt in the high field pole
- SmCo in the low field permanent magnet
- NdFeBo in the medium and high field permanent magnets