

INTERNATIONAL WORKSHOP ON FUTURE LINEAR COLLIDERS

LCWS

Dark Spectroscopy

—a proposal for an ILC study—

International Advisory Committee

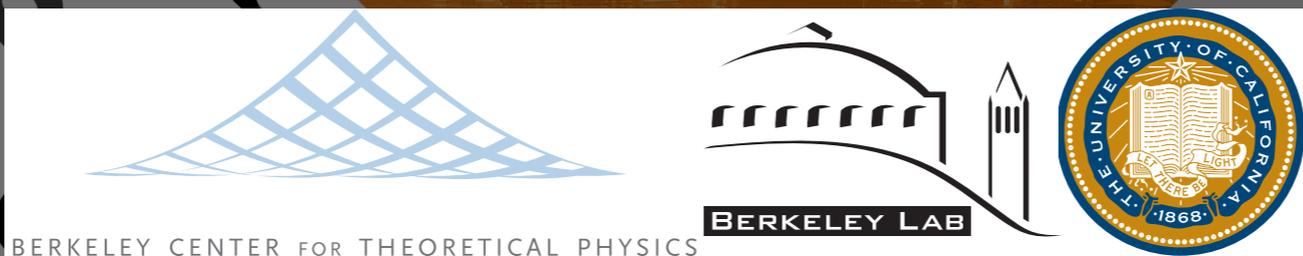
- H. Abramowicz (Tel-Aviv Univ.)
- J. Bagger (TRIUMF)
- U. Bassler (IN2P3)
- S. Bentveltsen (NIKHEF)
- G. Blair (STFC)
- E. Elsen (CERN)
- A.I. Etievre (Irfu)
- A. Grassellino (FNAL)
- S. Henderson (JBL)
- R. Heuer (DPG)
- J. Hewett (SLAC)
- S. Komamiya (Tokyo Univ.)
- F. Le Diberder (LAL)
- V. Matveev (JINR)
- J. Mnich (DESY)
- Y. Okada (KEK)
- A. Patwa (DoE)
- L. Rivkin (EPFL)
- A. Stocchi (LAL)
- Y. Wang (IHEP)
- M. Yamauchi (KEK)

Programme Committee

- T. Behnke (DESY)
- A. Bellerive (Carlton Univ.)
- A. Besson (IPHC)
- J. Brau (Oregon Univ.)
- J.C. Briant (LLR)
- P. Burrows (Oxford Univ.)
- M. Demarteau (ANL)
- D. Denisov (FNAL)
- K. Desch (Bonn Univ.)
- L. Evans (Imperial College)
- K. Fujii (KEK)
- J. Fuster (IFIC-Valencia)
- J. Gao (IHEP)
- R. Godbole (IISC)
- C. Grojean (DESY)
- M. Harrison (BNL)
- B. List (DESY)
- J. List (DESY)
- S. Michizono (KEK)
- H. Montgomery (JBL)
- H. Murayama (Berkeley)
- T. Nakada (EPFL)
- O. Napoly (Irfu)
- M. Peskin (SLAC)
- R. Pöschl (LAL)
- P. Roloff (CERN)
- S. Stapnes (CERN, Chair of PC)
- G. Taylor (Melbourne)
- M. Titov (Irfu, PC Secretary)

Hitoshi Murayama (Berkeley, Kavli IPMU)
 LCWS 2017, Strasbourg, Oct 26, 2017

+Yonit Hochberg, Eric Kuflik

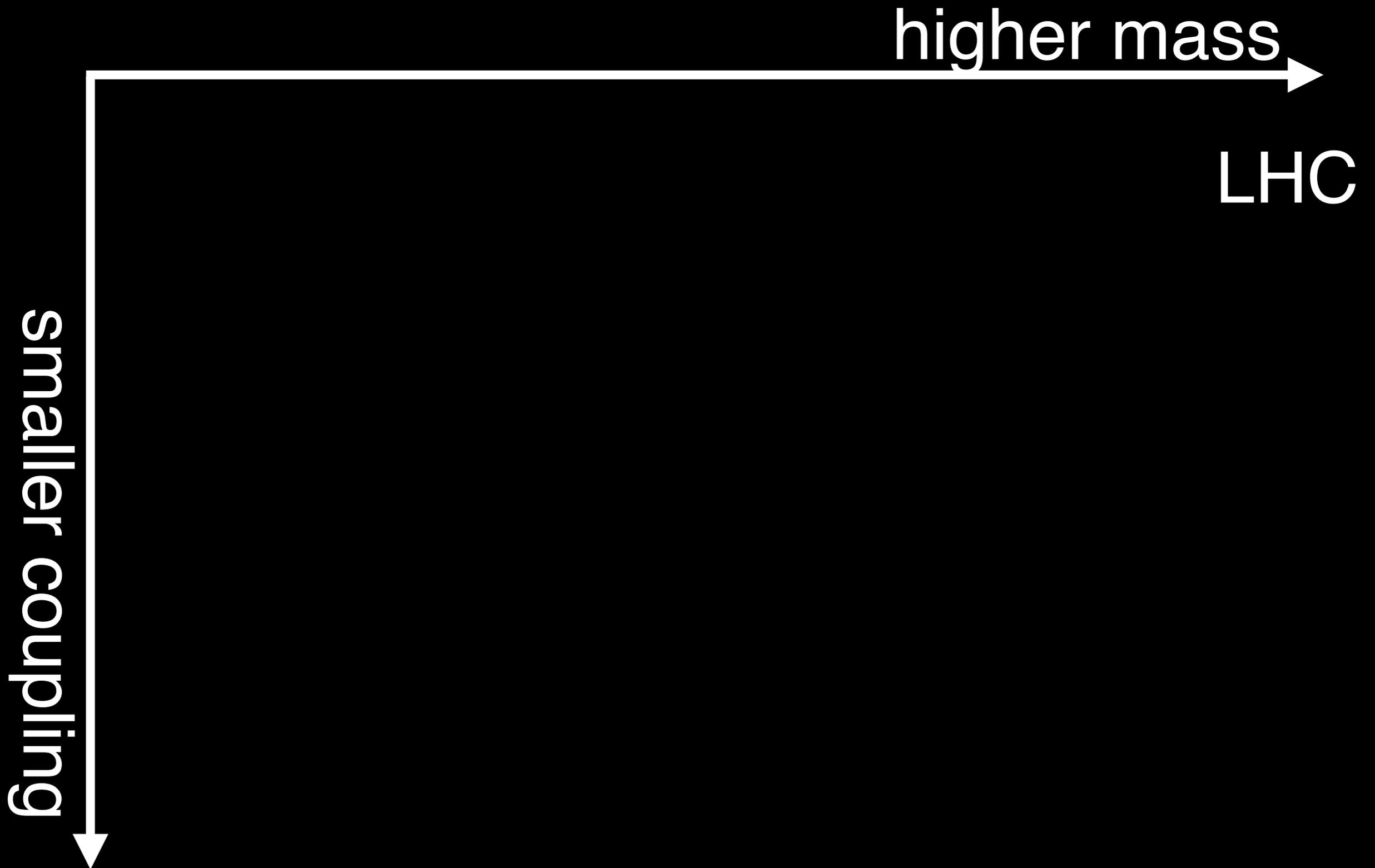
October

Where is new physics?

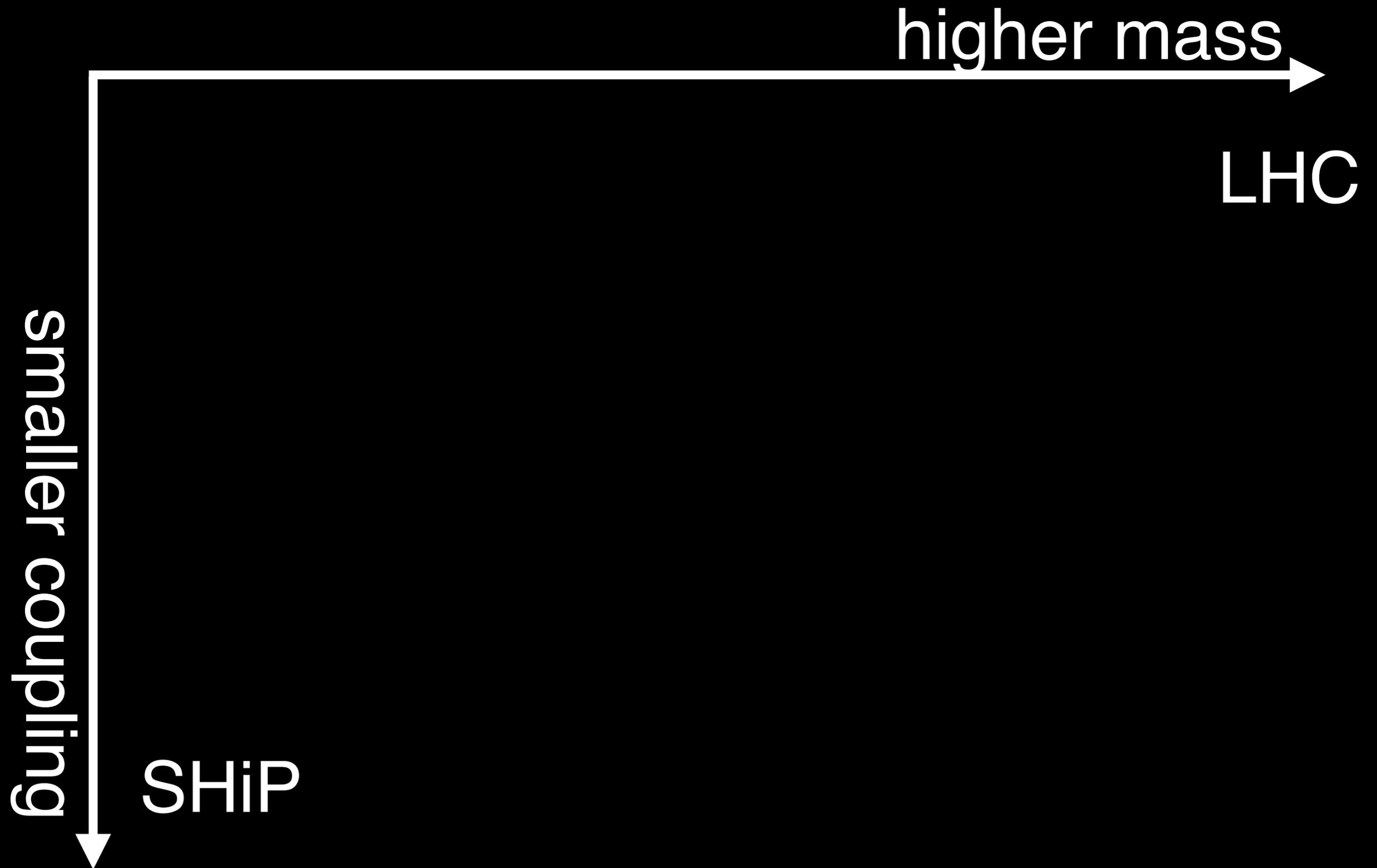
Where is new physics?



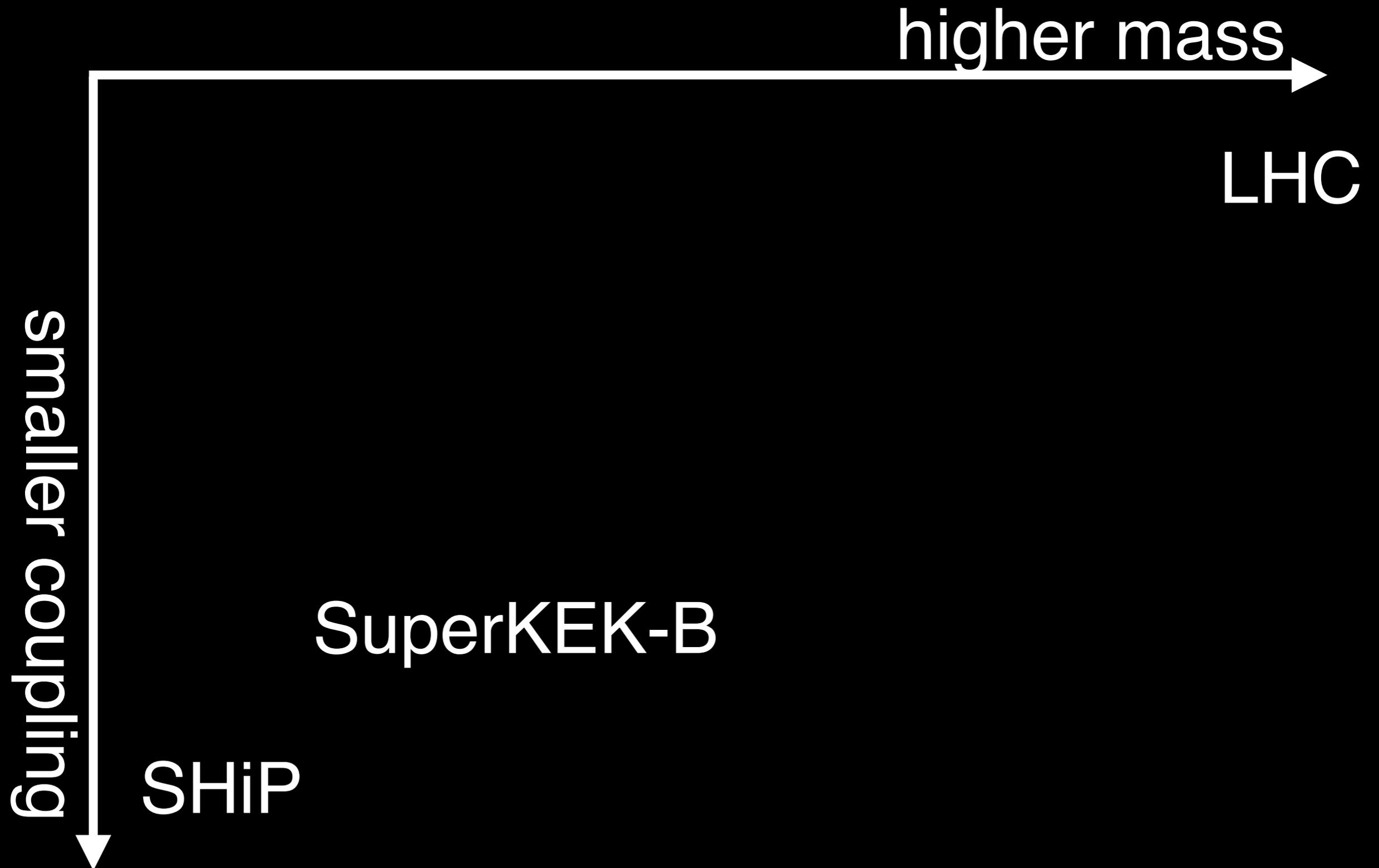
Where is new physics?



Where is new physics?



Where is new physics?



Where is new physics?

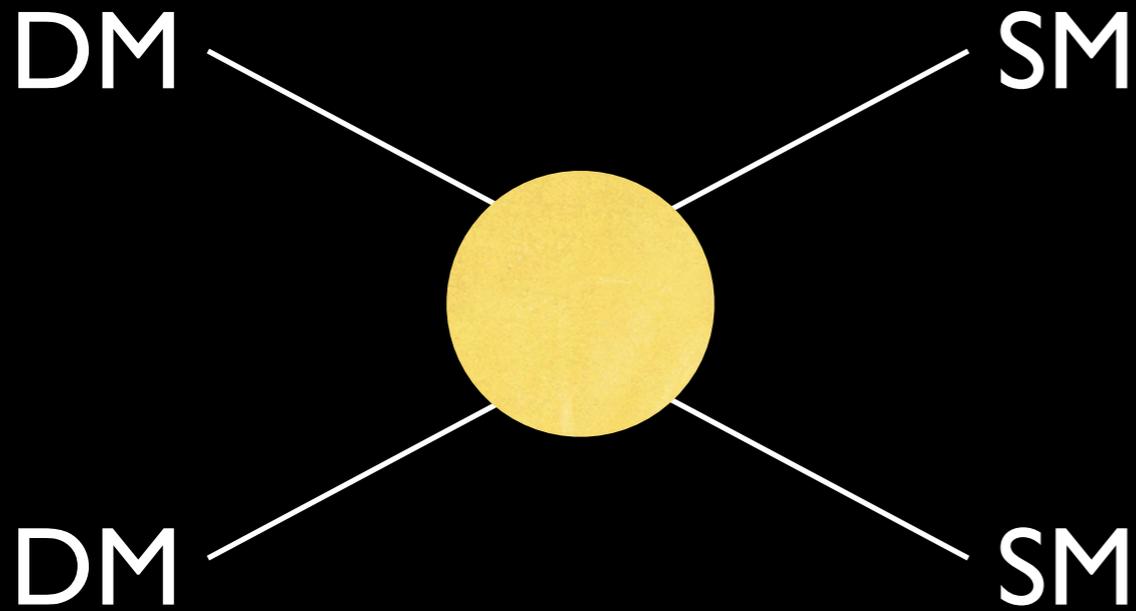




$$\frac{n_{\text{DM}}}{s} = 4.4 \times 10^{-10} \frac{\text{GeV}}{m_{\text{DM}}}$$



Dark Matter Miracles



$$\langle \sigma_{2 \rightarrow 2\nu} \rangle \approx \frac{\alpha^2}{m^2}$$

$$\alpha \approx 10^{-2}$$

$$m \approx 300 \text{ GeV}$$

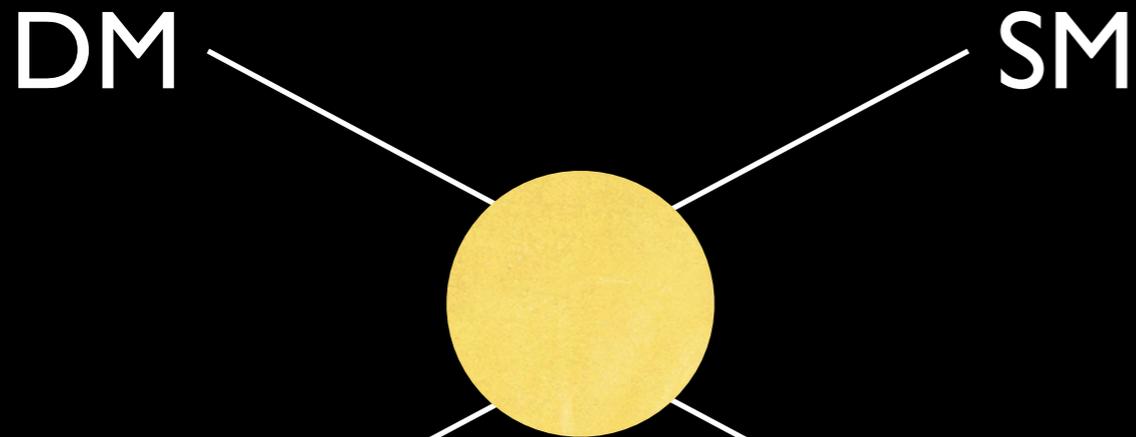
WIMP miracle!



$$\frac{n_{\text{DM}}}{s} = 4.4 \times 10^{-10} \frac{\text{GeV}}{m_{\text{DM}}}$$



Dark Matter Miracles

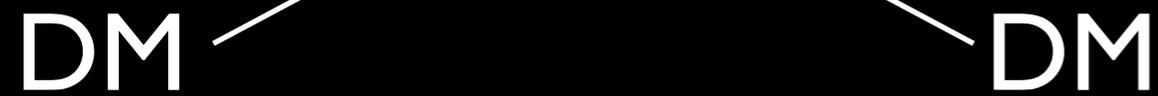
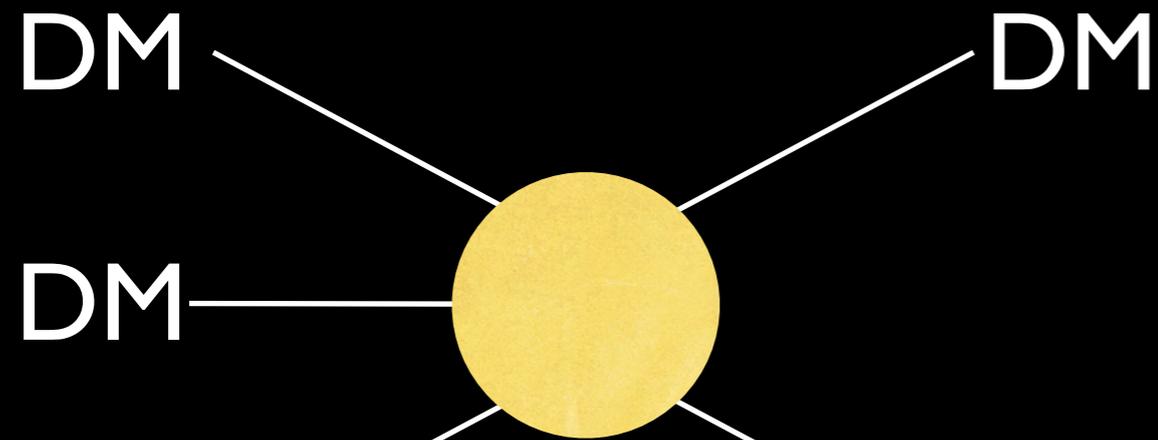
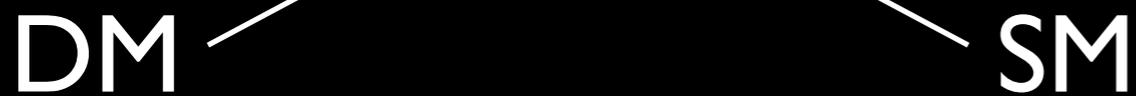


$$\langle \sigma_{2 \rightarrow 2\nu} \rangle \approx \frac{\alpha^2}{m^2}$$

$$\alpha \approx 10^{-2}$$

$$m \approx 300 \text{ GeV}$$

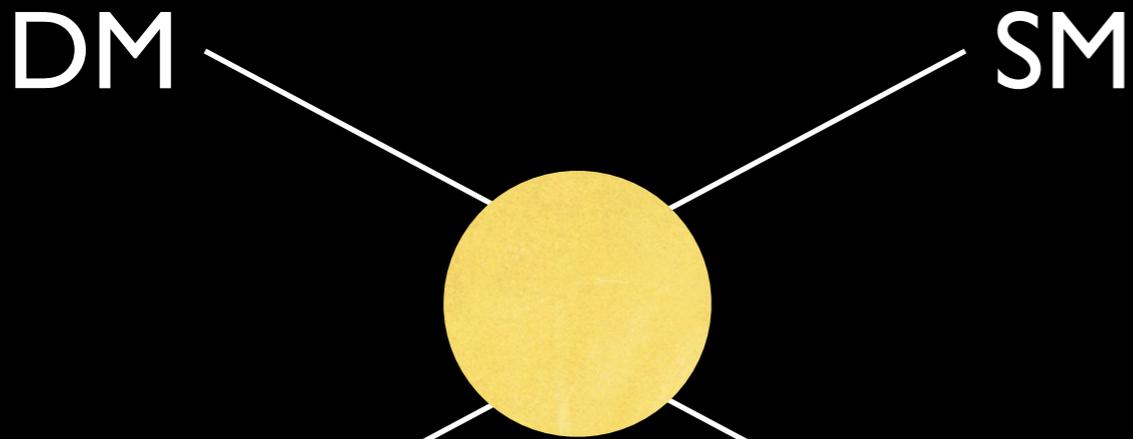
WIMP miracle!





$$\frac{n_{\text{DM}}}{s} = 4.4 \times 10^{-10} \frac{\text{GeV}}{m_{\text{DM}}}$$

Dark Matter Miracles

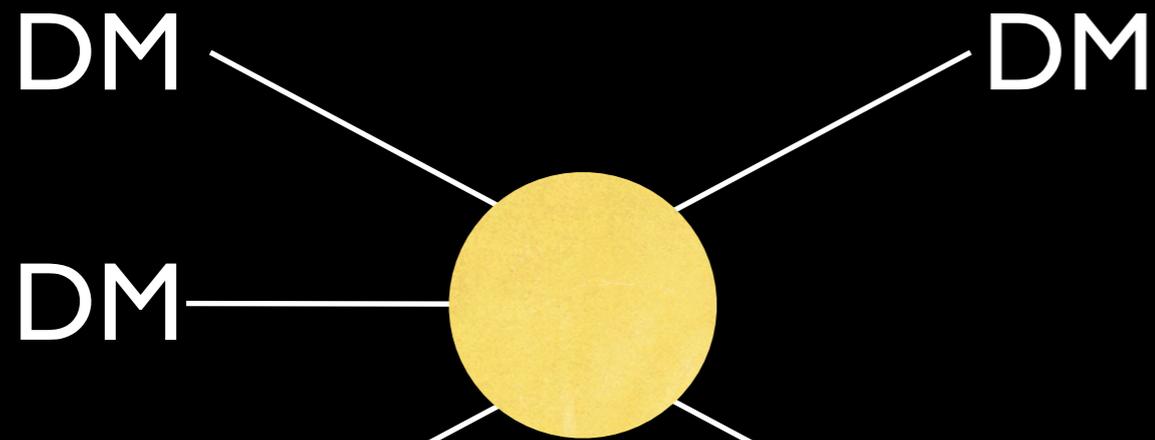
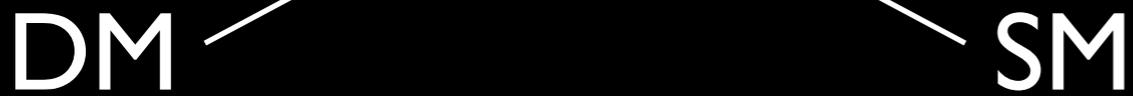


$$\langle \sigma_{2 \rightarrow 2\nu} \rangle \approx \frac{\alpha^2}{m^2}$$

$$\alpha \approx 10^{-2}$$

$$m \approx 300 \text{ GeV}$$

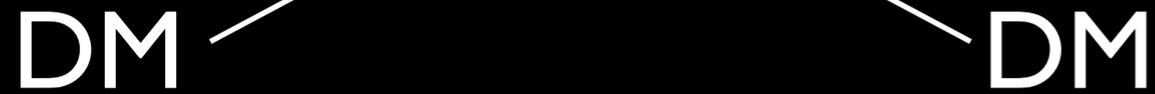
WIMP miracle!



$$\langle \sigma_{3 \rightarrow 2\nu^2} \rangle \approx \frac{\alpha^3}{m^5}$$

$$\alpha \approx 4\pi$$

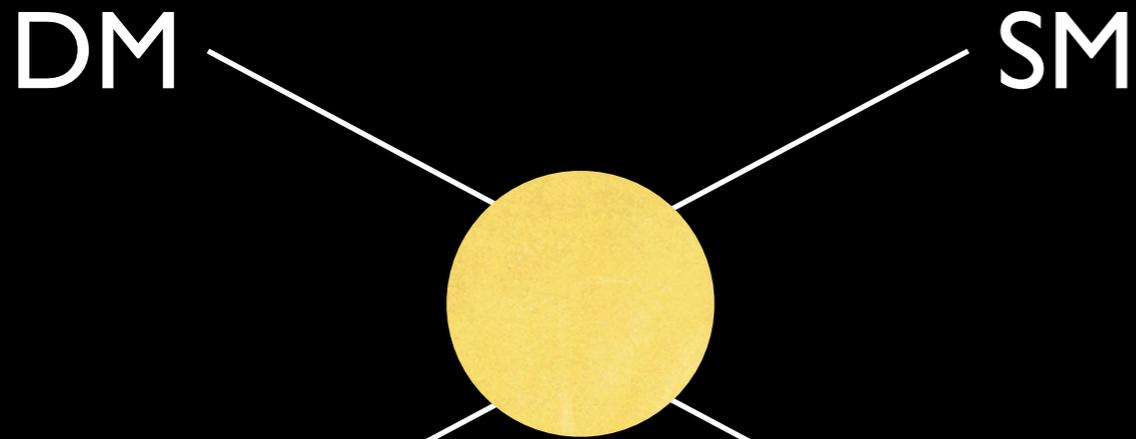
$$m \approx 300 \text{ MeV}$$





$$\frac{n_{\text{DM}}}{s} = 4.4 \times 10^{-10} \frac{\text{GeV}}{m_{\text{DM}}}$$

Dark Matter Miracles

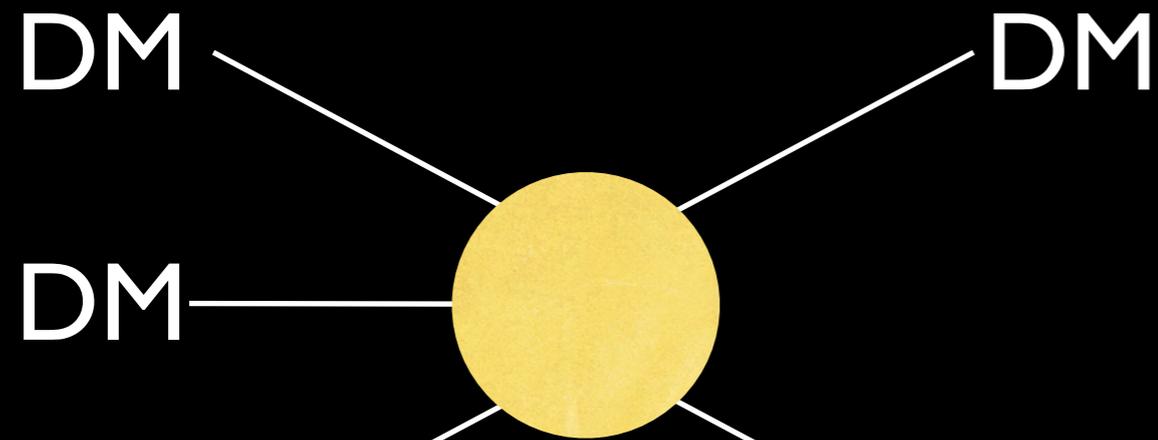
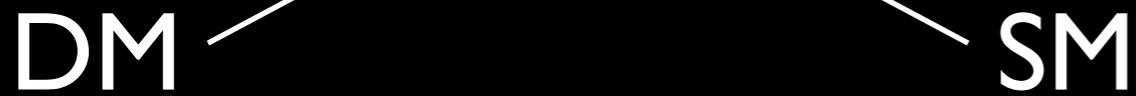


$$\langle \sigma_{2 \rightarrow 2\nu} \rangle \approx \frac{\alpha^2}{m^2}$$

$$\alpha \approx 10^{-2}$$

$$m \approx 300 \text{ GeV}$$

WIMP miracle!

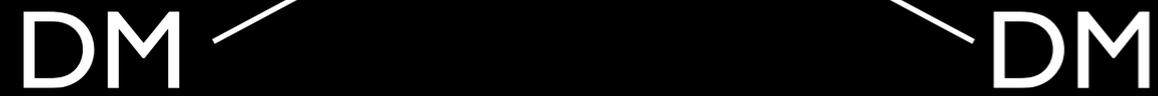


$$\langle \sigma_{3 \rightarrow 2\nu^2} \rangle \approx \frac{\alpha^3}{m^5}$$

$$\alpha \approx 4\pi$$

$$m \approx 300 \text{ MeV}$$

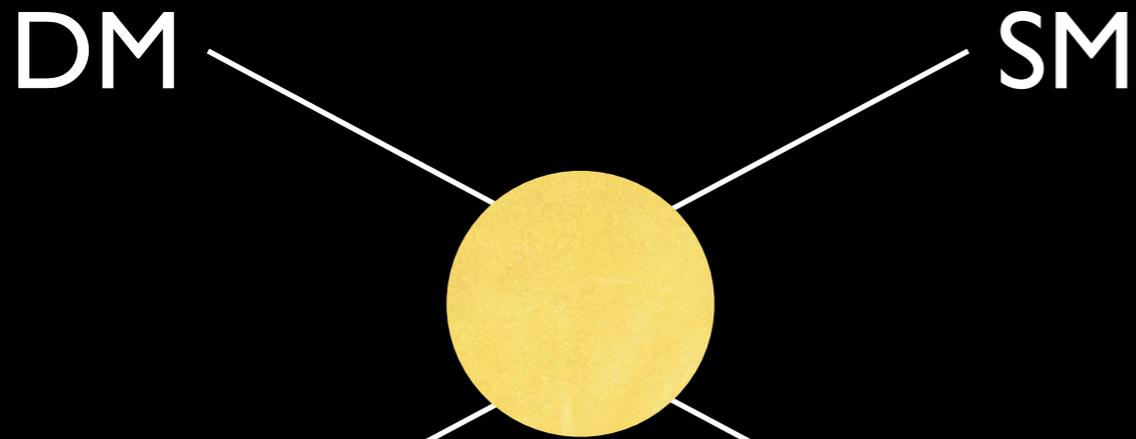
SIMP miracle!





$$\frac{n_{\text{DM}}}{s} = 4.4 \times 10^{-10} \frac{\text{GeV}}{m_{\text{DM}}}$$

Dark Matter Miracles

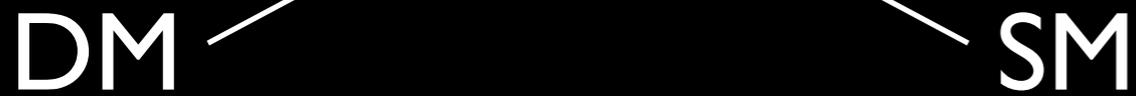


$$\langle \sigma_{2 \rightarrow 2\nu} \rangle \approx \frac{\alpha^2}{m^2}$$

$$\alpha \approx 10^{-2}$$

$$m \approx 300 \text{ GeV}$$

WIMP miracle!



$$\langle \sigma_{3 \rightarrow 2\nu^2} \rangle \approx \frac{\alpha^3}{m^5}$$

$$\alpha \approx 4\pi$$

$$m \approx 300 \text{ MeV}$$

SIMP miracle!

dark pion?

LAGRANGIANS

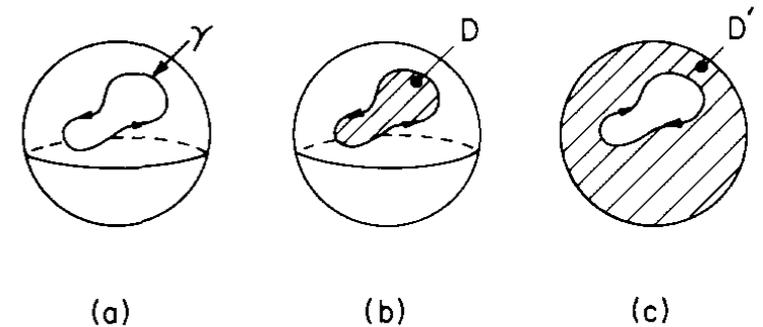
QCD with massive quarks

$$\mathcal{L}_{\text{quark}} = -\frac{1}{4} F_{\mu\nu}^a F^{\mu\nu a} + \bar{q}_i i \not{D} q_i - \frac{1}{2} m_Q J^{ij} q_i q_j + h.c.$$

Chiral Lagrangian

$$\mathcal{L}_{\text{Sigma}} = \frac{f_\pi^2}{16} \text{Tr} \partial_\mu \Sigma \partial^\mu \Sigma^\dagger - \frac{1}{2} m_Q \mu^3 \text{Tr} J \Sigma + h.c. - \frac{i N_c}{240 \pi^2} \int \text{Tr} (\Sigma^\dagger d\Sigma)^5$$

Perturbation theory



$$\mathcal{L}_{\text{pion}} = \frac{1}{4} \text{Tr} \partial_\mu \pi \partial^\mu \pi - \frac{m_\pi^2}{4} \text{Tr} \pi^2 + \frac{m_\pi^2}{12 f_\pi^2} \text{Tr} \pi^4 - \frac{1}{6 f_\pi^2} \text{Tr} (\pi^2 \partial^\mu \pi \partial_\mu \pi - \pi \partial^\mu \pi \pi \partial_\mu \pi) + \frac{2 N_c}{15 \pi^2 f_\pi^5} \epsilon^{\mu\nu\rho\sigma} \text{Tr} [\pi \partial_\mu \pi \partial_\nu \pi \partial_\rho \pi \partial_\sigma \pi] + \mathcal{O}(\pi^6)$$

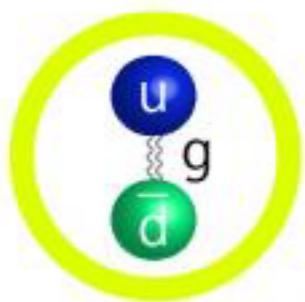
LAGRANGIANS

QCD with massive quarks

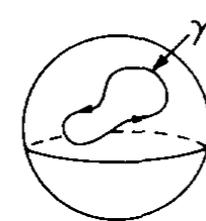
$$\mathcal{L}_{\text{quark}} = -\frac{1}{4} F_{\mu\nu}^a F^{\mu\nu a} + \bar{q}_i i \not{D} q_i - \frac{1}{2} m_Q J^{ij} q_i q_j + h.c.$$

Chiral Lagrangian

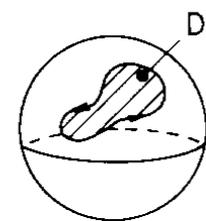
$$\mathcal{L}_{\text{Sigma}} = \frac{f_\pi^2}{16} \text{Tr} \partial_\mu \Sigma \partial^\mu \Sigma^\dagger - \frac{1}{2} m_Q \mu^3 \text{Tr} J \Sigma + h.c. - \frac{i N_c}{240 \pi^2} \int \text{Tr} (\Sigma^\dagger d\Sigma)^5$$



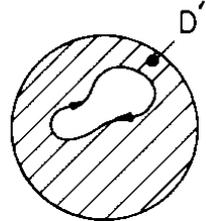
Perturbation theory



(a)

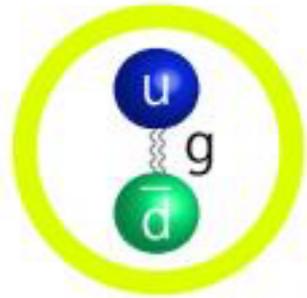


(b)

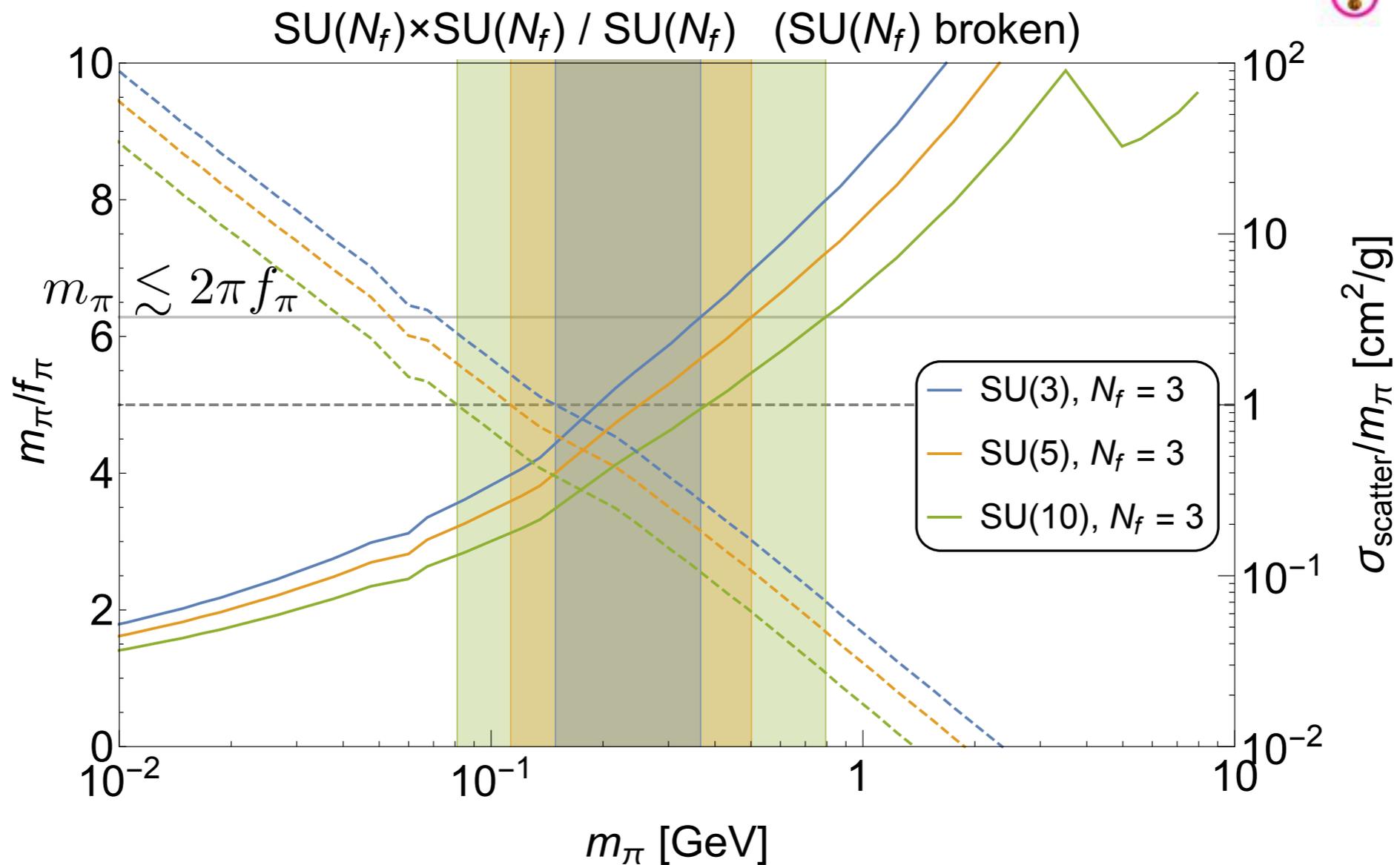
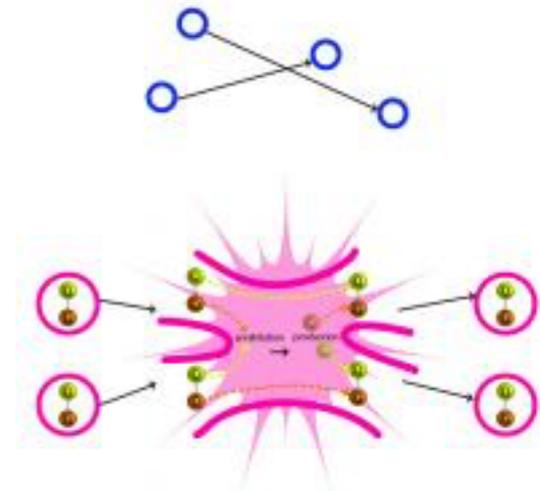


(c)

$$\mathcal{L}_{\text{pion}} = \frac{1}{4} \text{Tr} \partial_\mu \pi \partial^\mu \pi - \frac{m_\pi^2}{4} \text{Tr} \pi^2 + \frac{m_\pi^2}{12 f_\pi^2} \text{Tr} \pi^4 - \frac{1}{6 f_\pi^2} \text{Tr} (\pi^2 \partial^\mu \pi \partial_\mu \pi - \pi \partial^\mu \pi \pi \partial_\mu \pi) + \frac{2 N_c}{15 \pi^2 f_\pi^5} \epsilon^{\mu\nu\rho\sigma} \text{Tr} [\pi \partial_\mu \pi \partial_\nu \pi \partial_\rho \pi \partial_\sigma \pi] + \mathcal{O}(\pi^6)$$



The Results



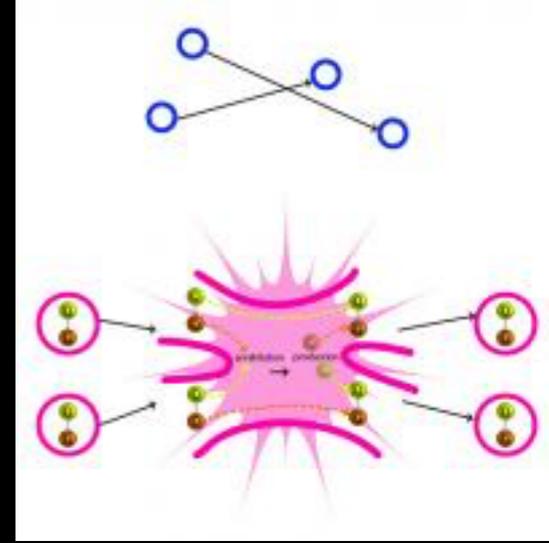
Solid curves: solution to Boltzmann eq.

Dashed curves: along that solution

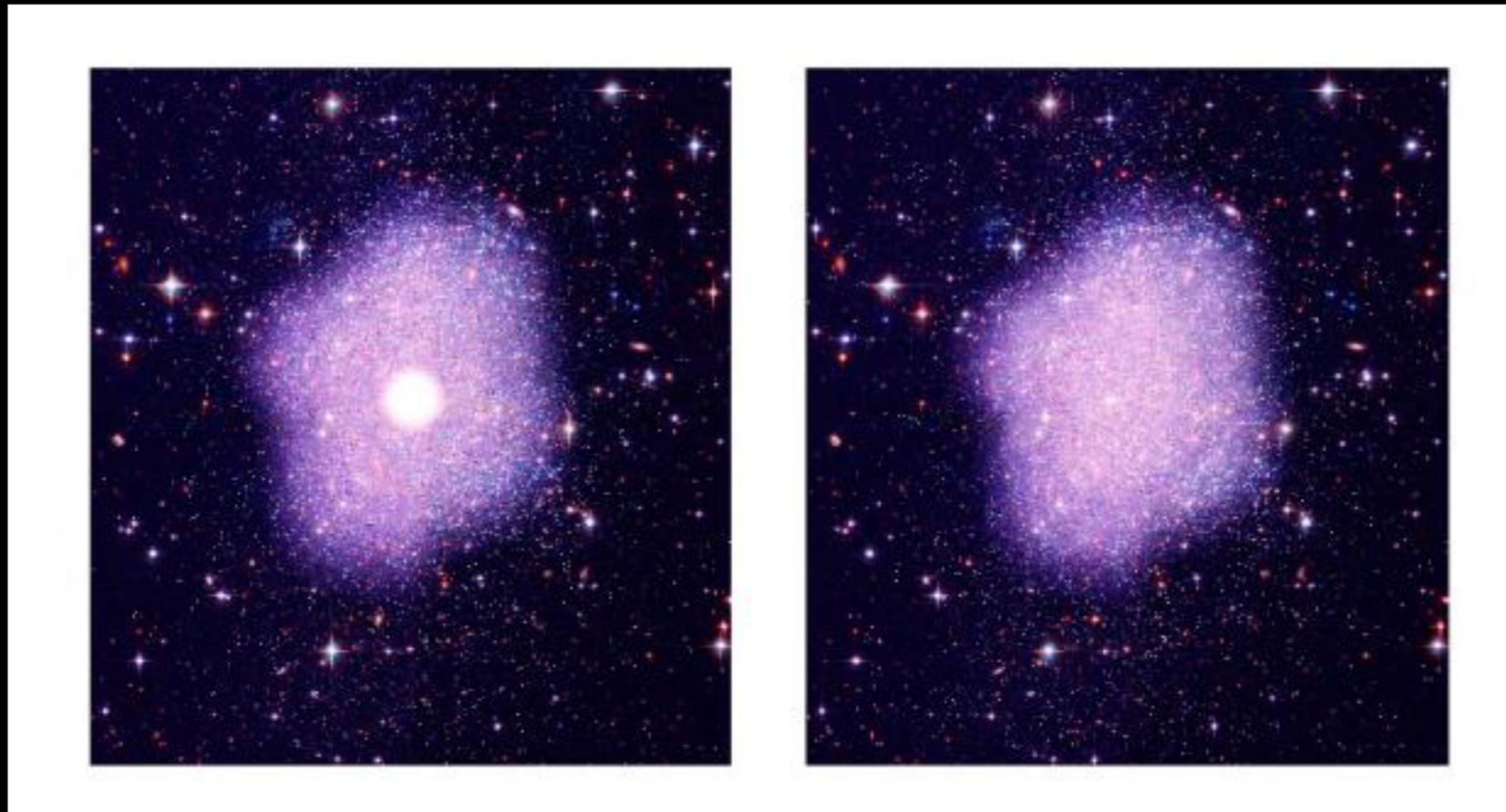
$$\frac{m_\pi}{f_\pi} \propto m_\pi^{3/10}$$

$$\frac{\sigma_{\text{scatter}}}{m_\pi} \propto m_\pi^{-9/5}$$

self interaction

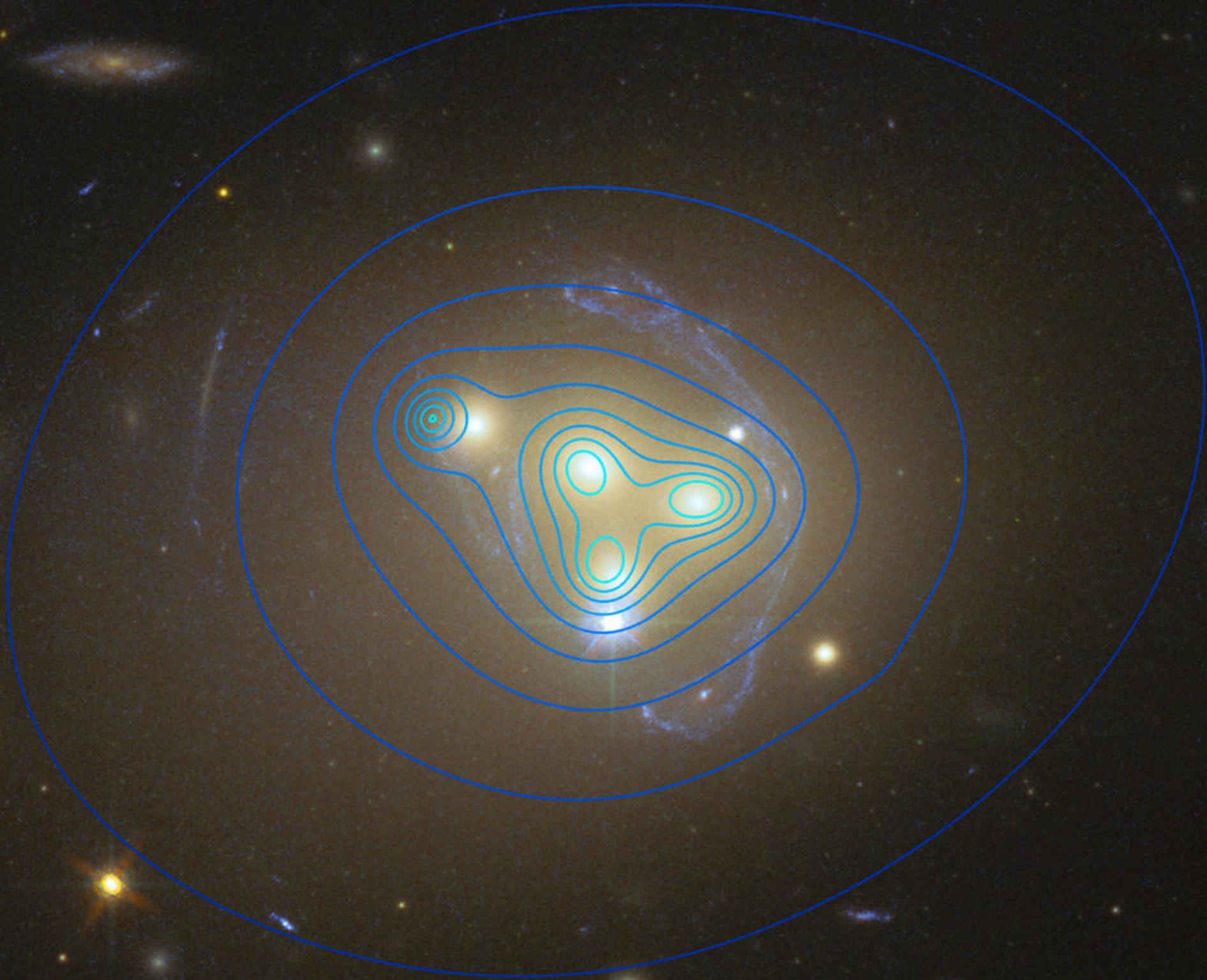


- $\sigma/m \sim \text{cm}^2/\text{g} \sim 10^{-24} \text{cm}^2 / 300 \text{MeV}$
- flattens the cusps in NFW profile
- actually desirable for dwarf galaxies?

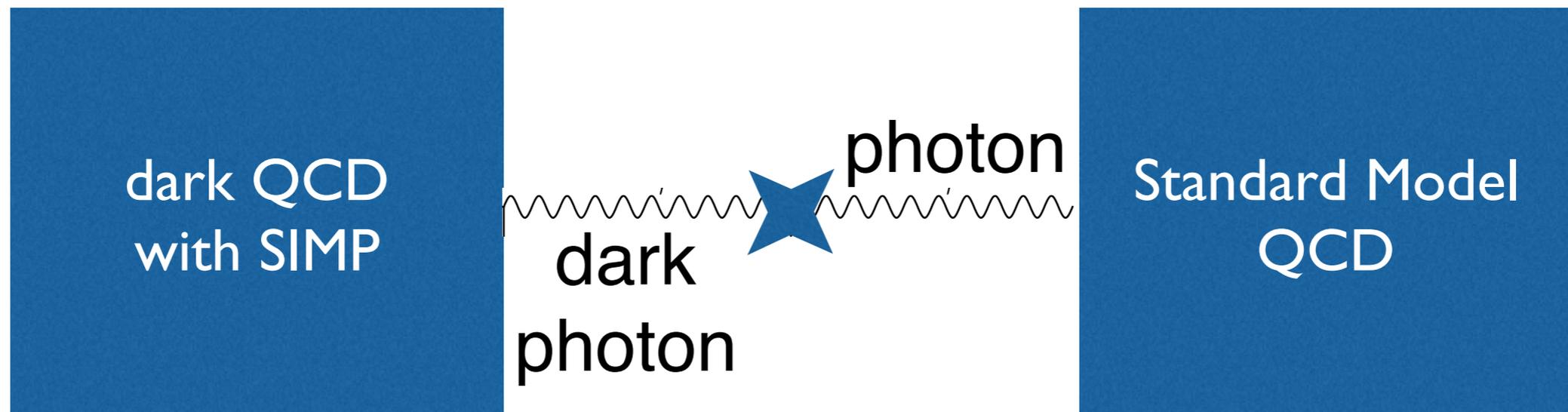




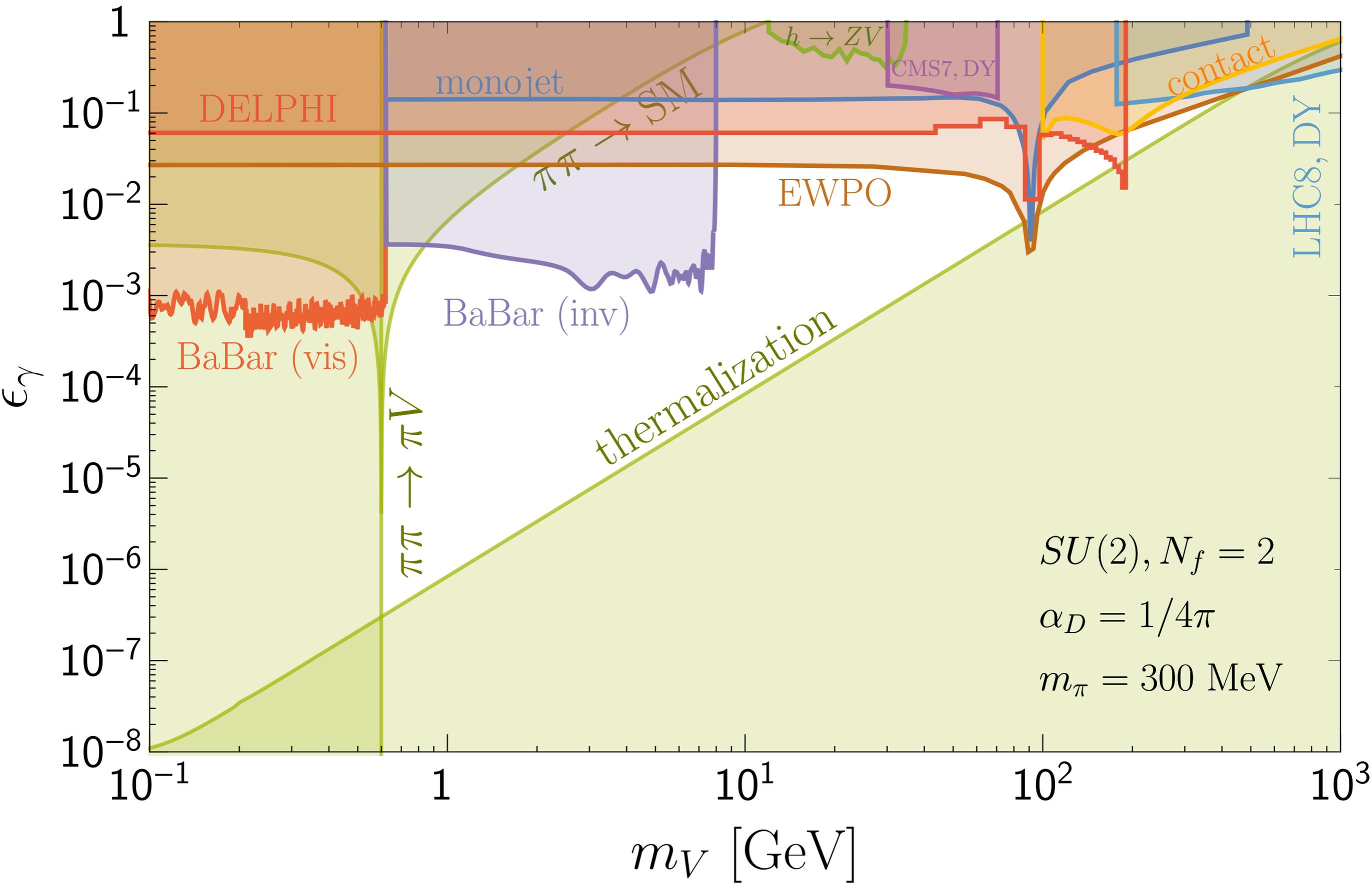
$$\frac{\sigma}{m} \approx 1.5 \frac{\text{cm}^2}{g} = \frac{0.27\text{b}}{100\text{MeV}}$$



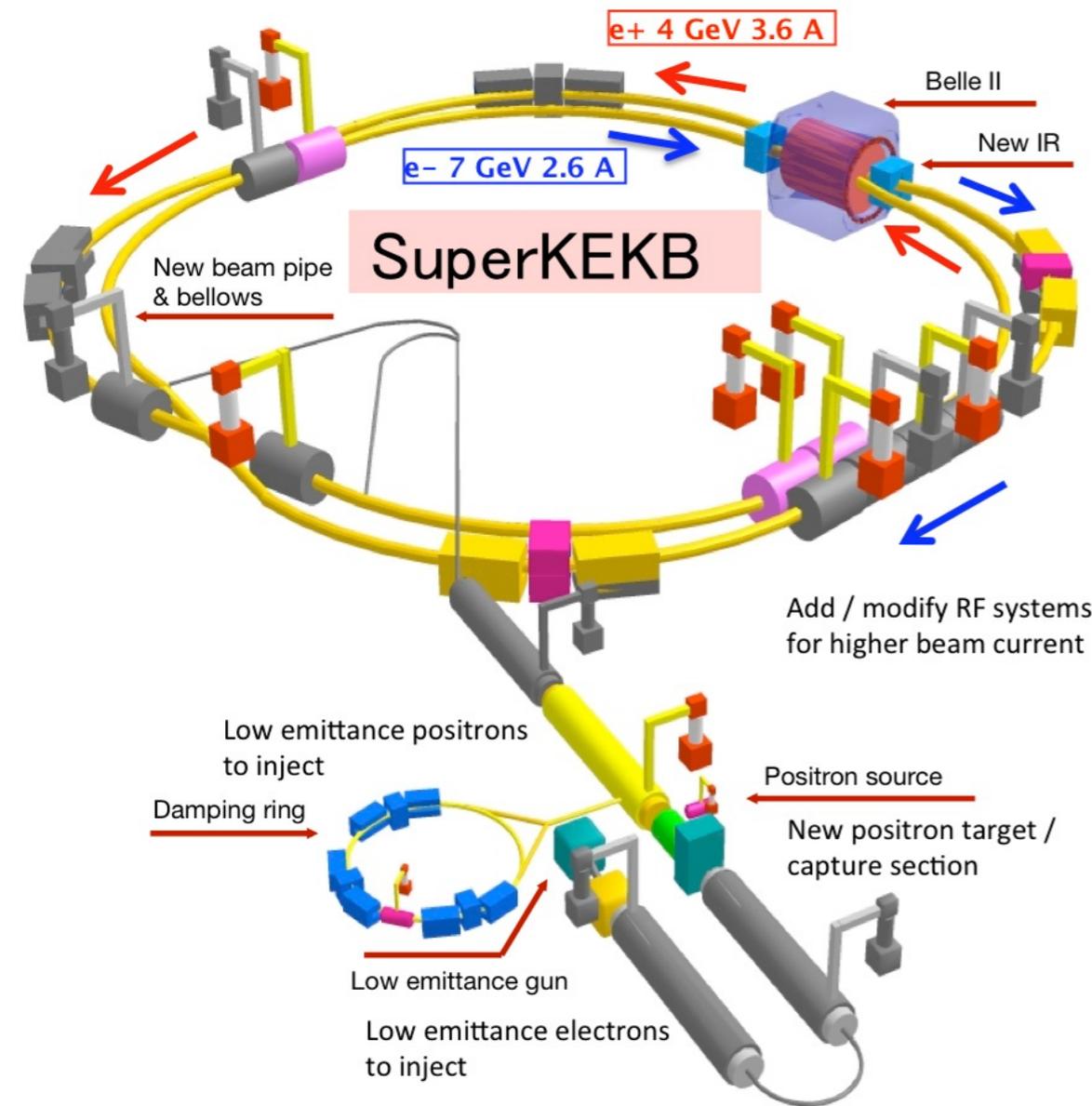
vector portal



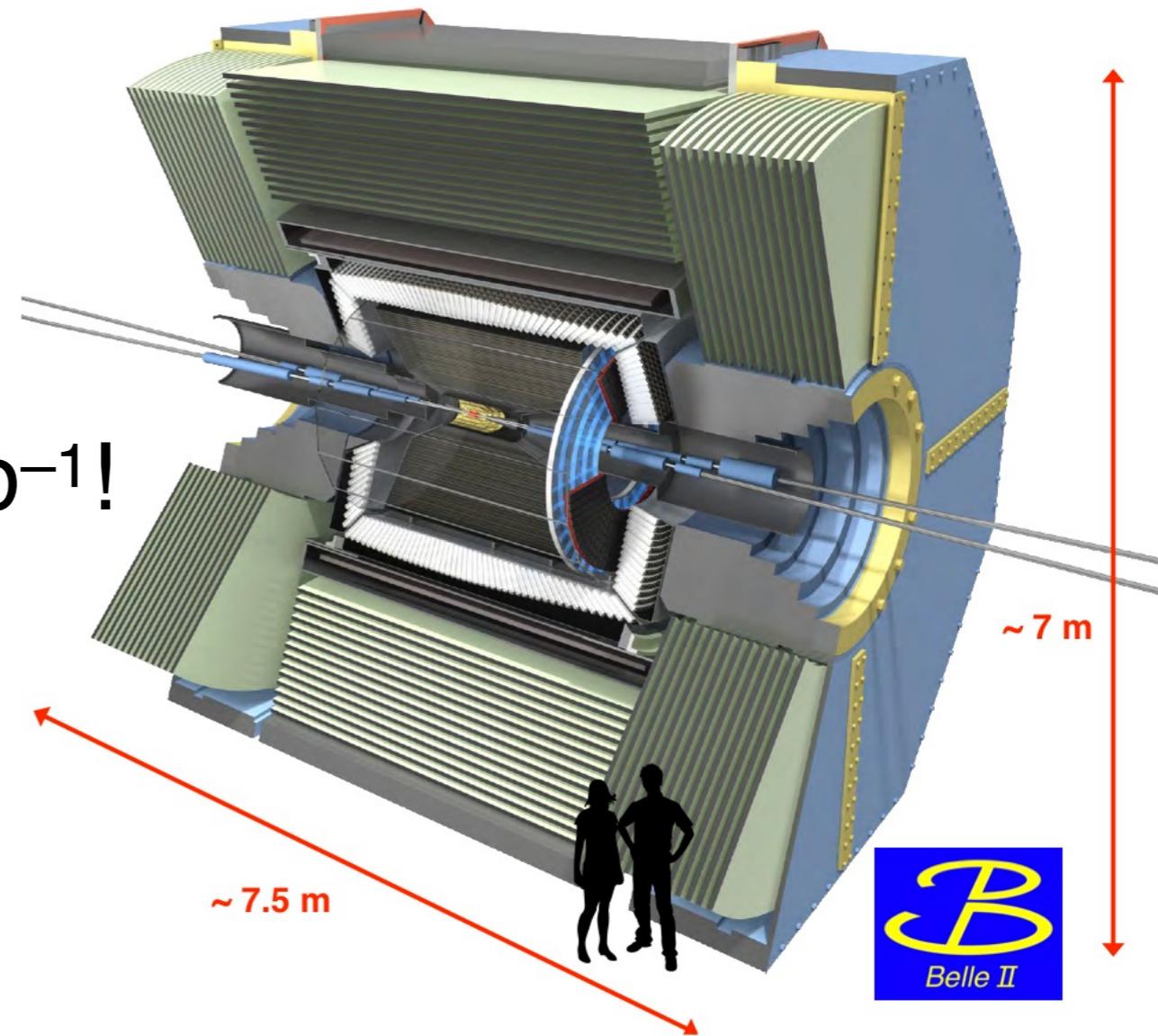
$$\frac{\epsilon_\gamma}{2c_W} B_{\mu\nu} F_D^{\mu\nu}$$



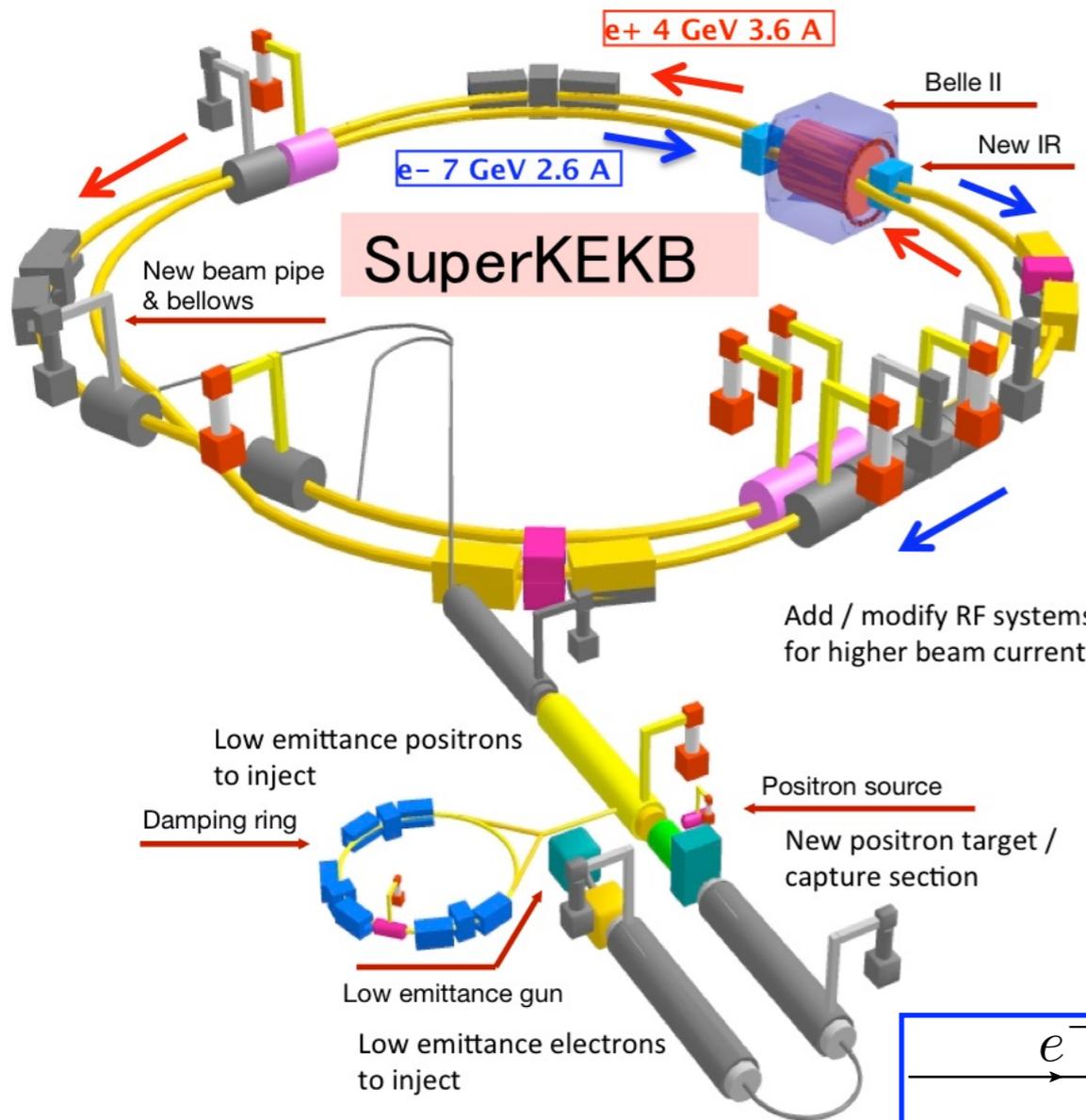
$e^+ e^-$ colliders



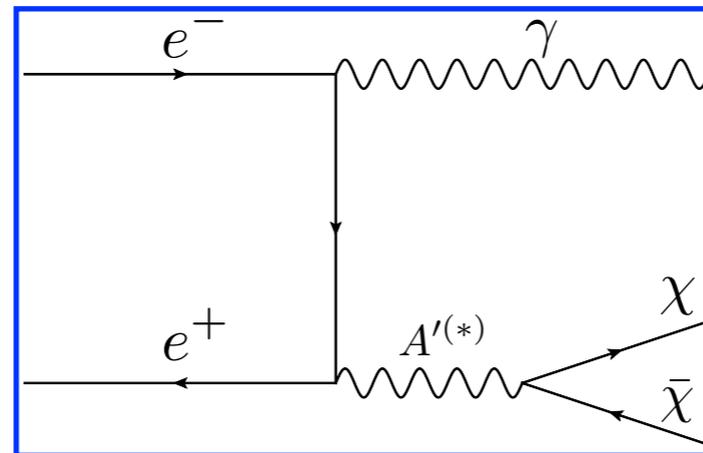
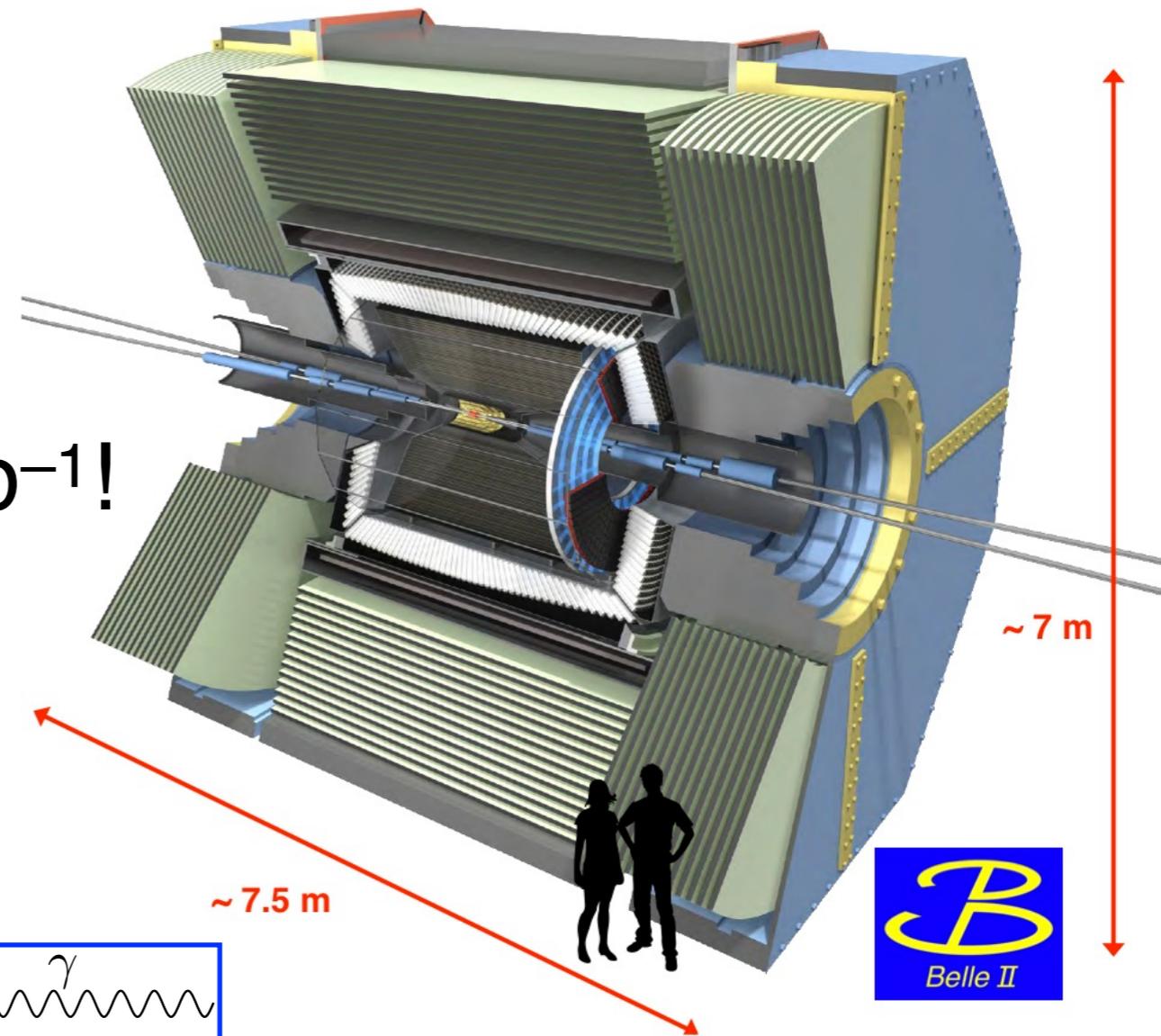
50 ab^{-1} !



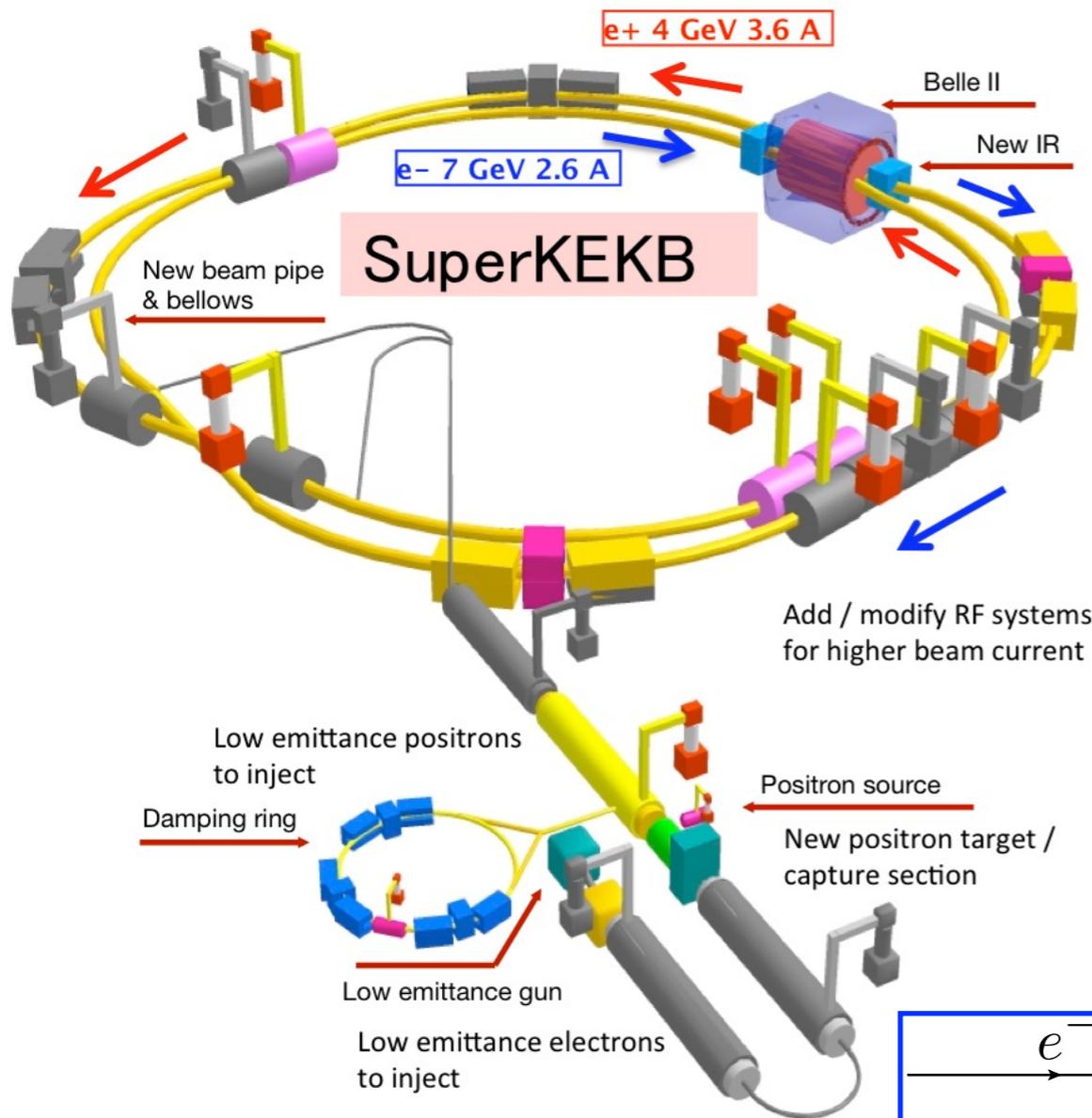
$e^+ e^-$ colliders



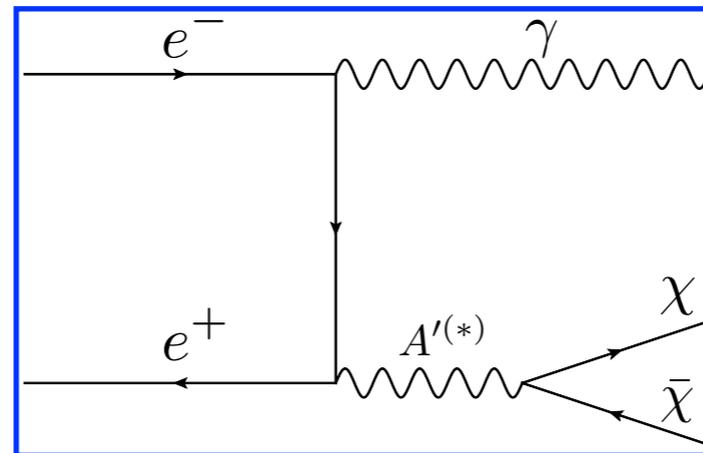
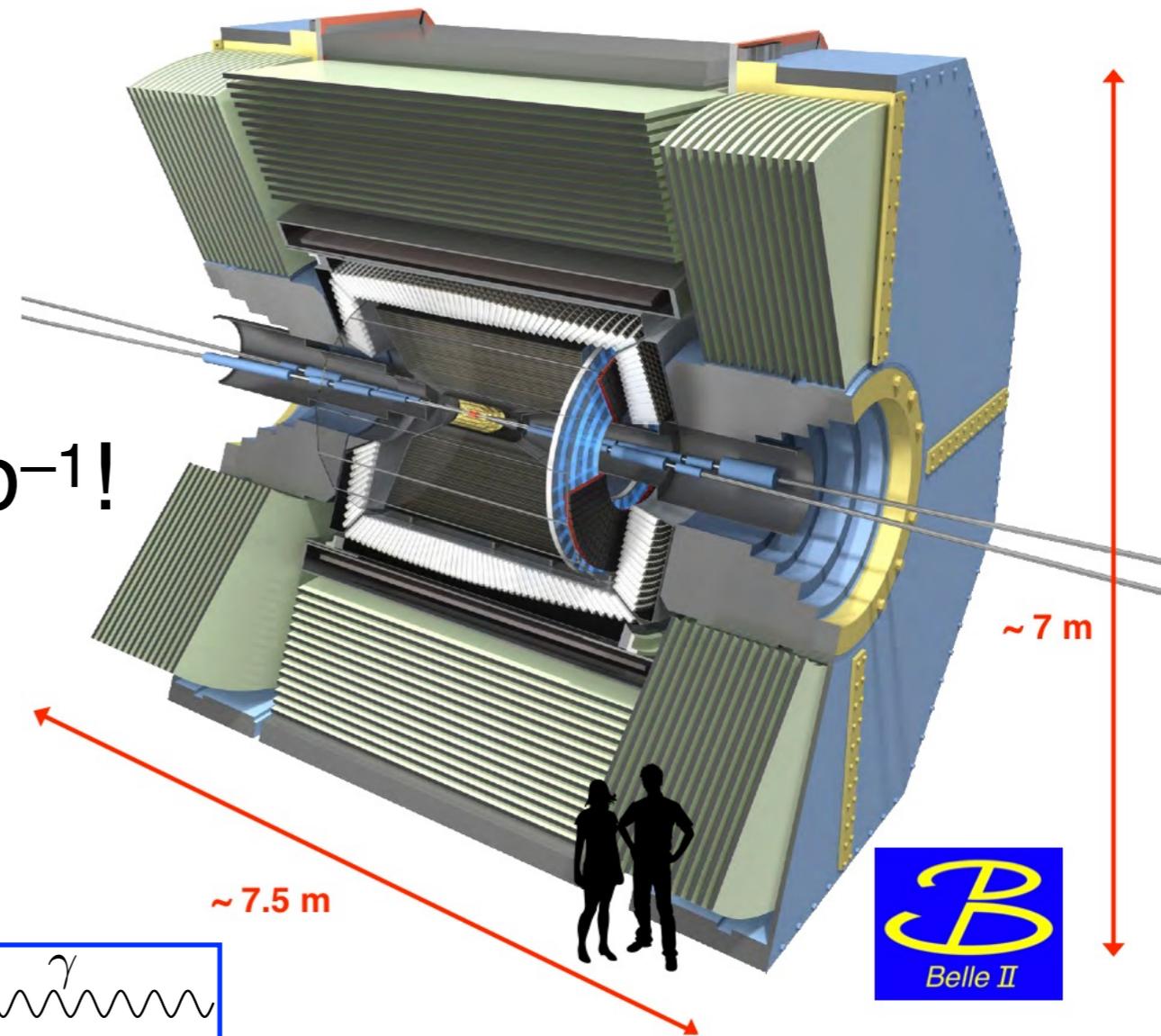
50 ab^{-1} !



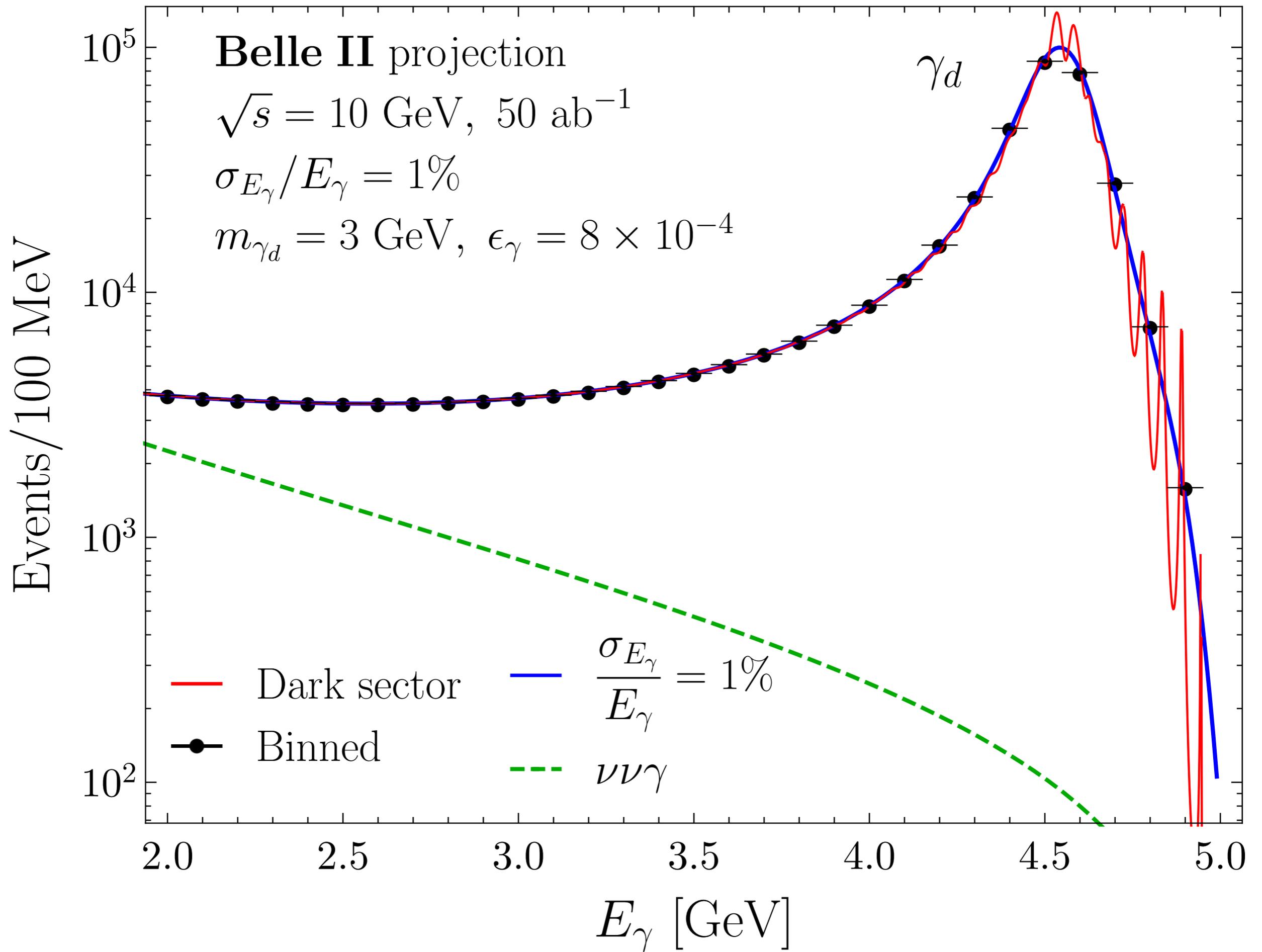
$e^+ e^-$ colliders

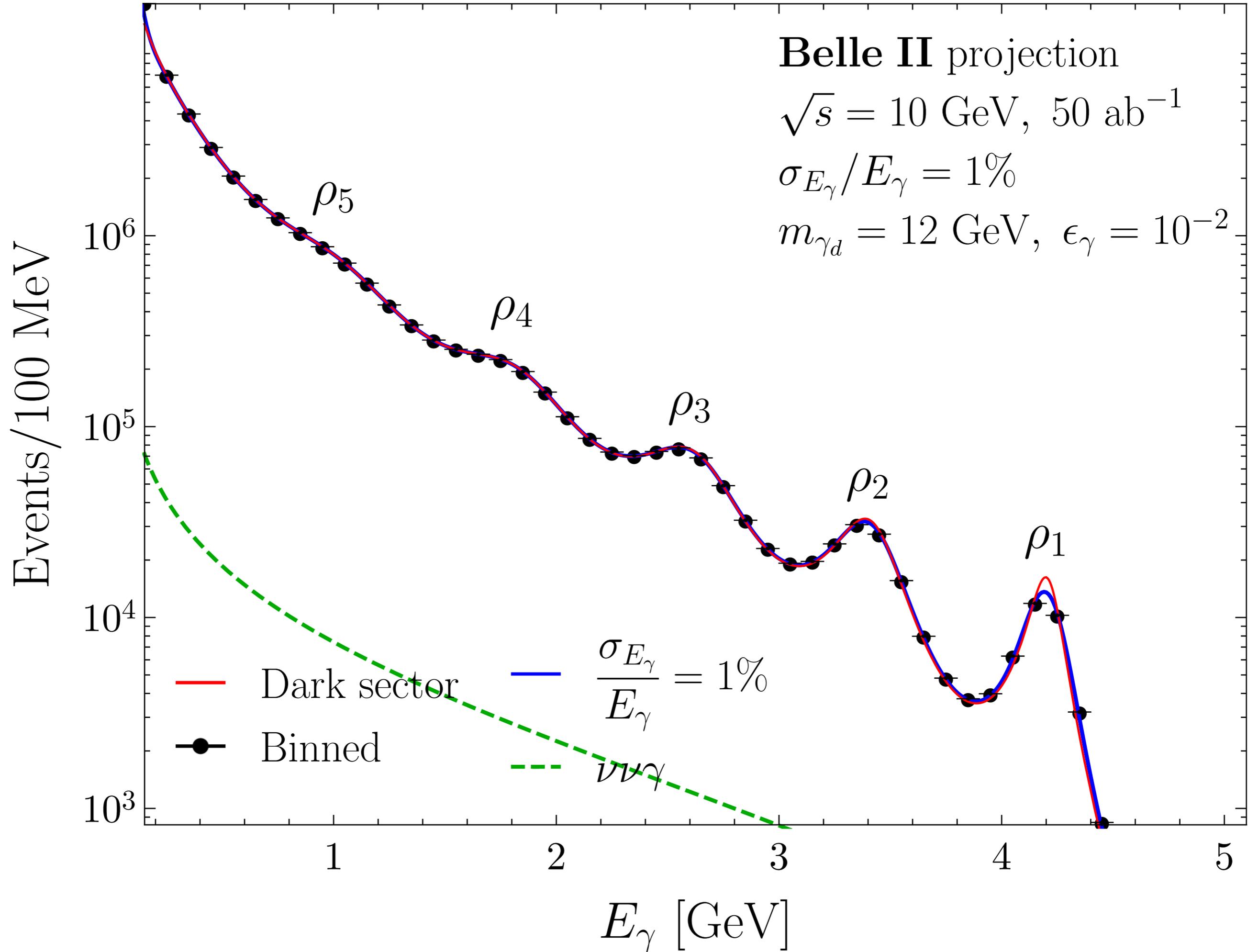


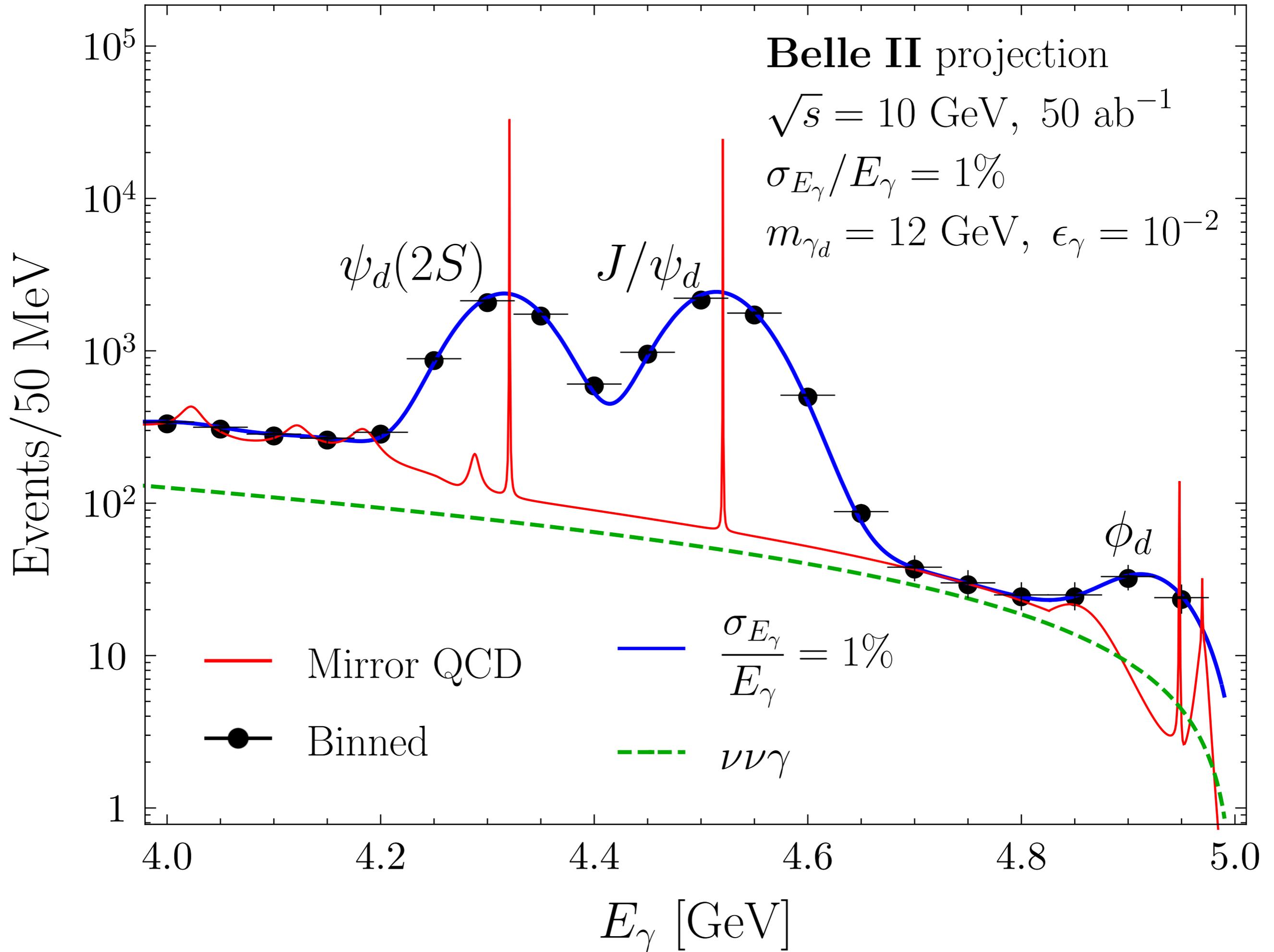
$50 \text{ ab}^{-1}!$



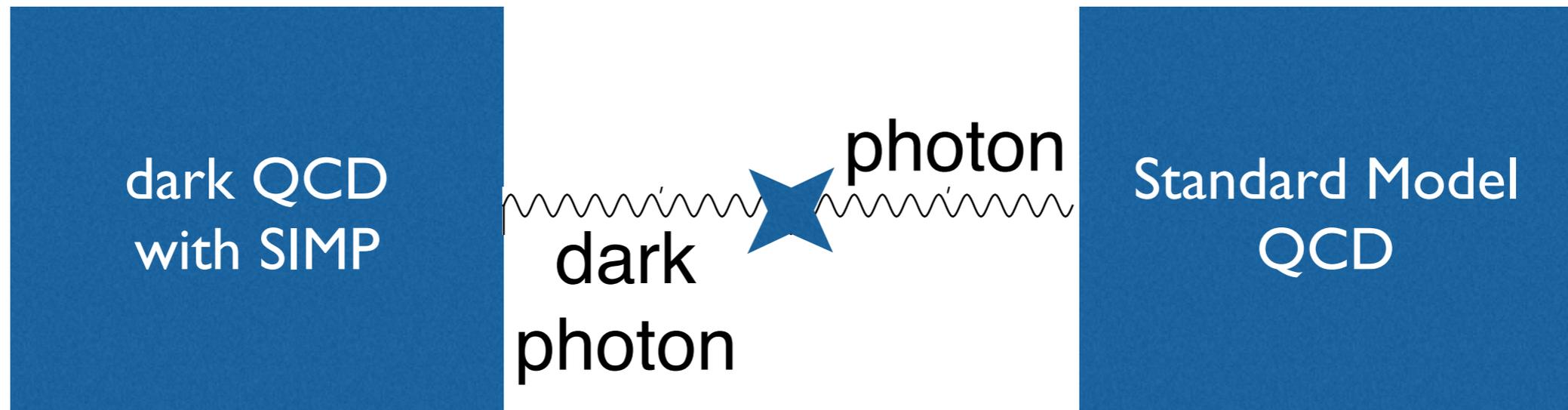
$$E_\gamma = \frac{\sqrt{s}}{2} \left(1 - \frac{M_{\text{inv}}^2}{s} \right)$$



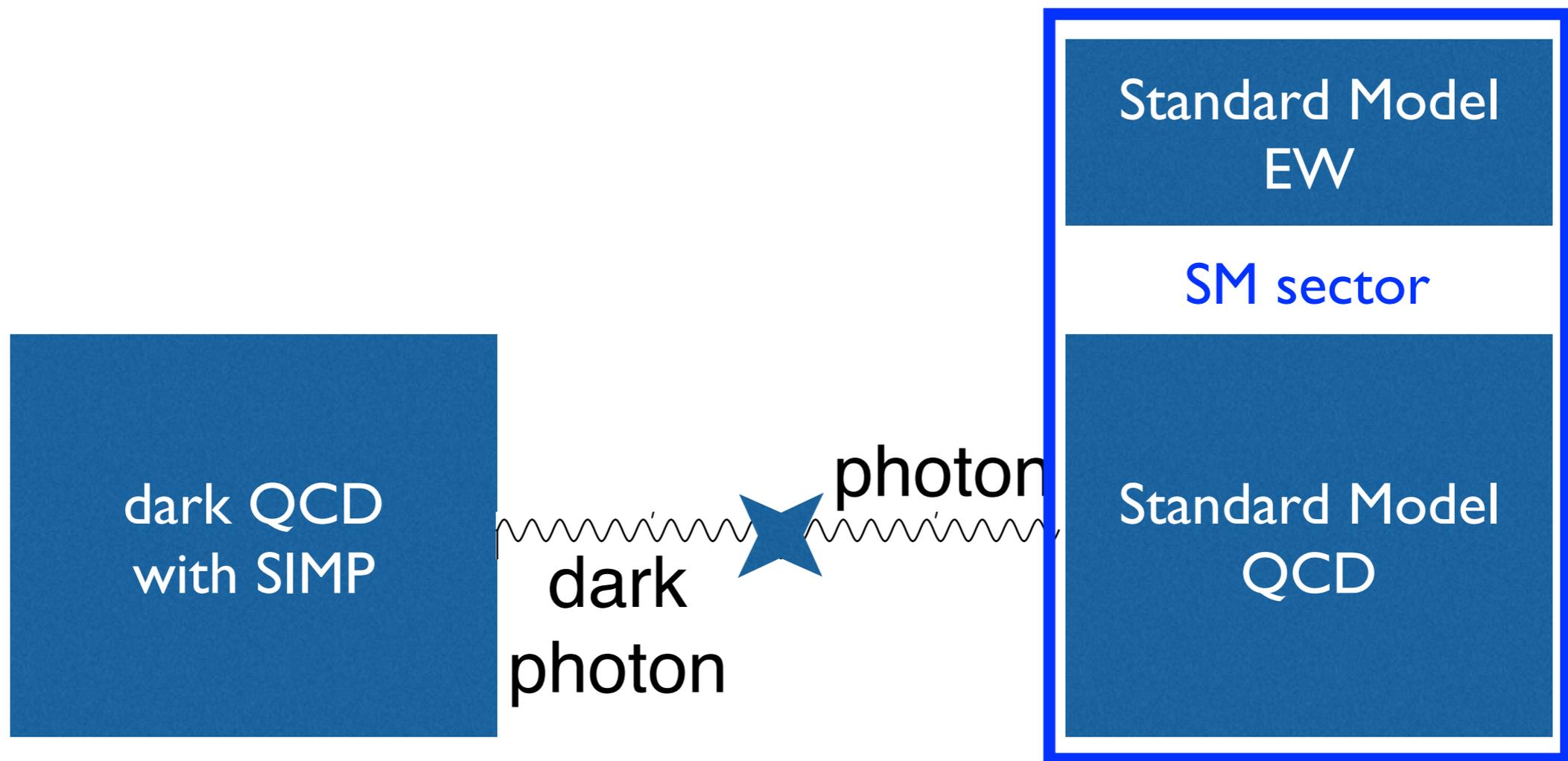




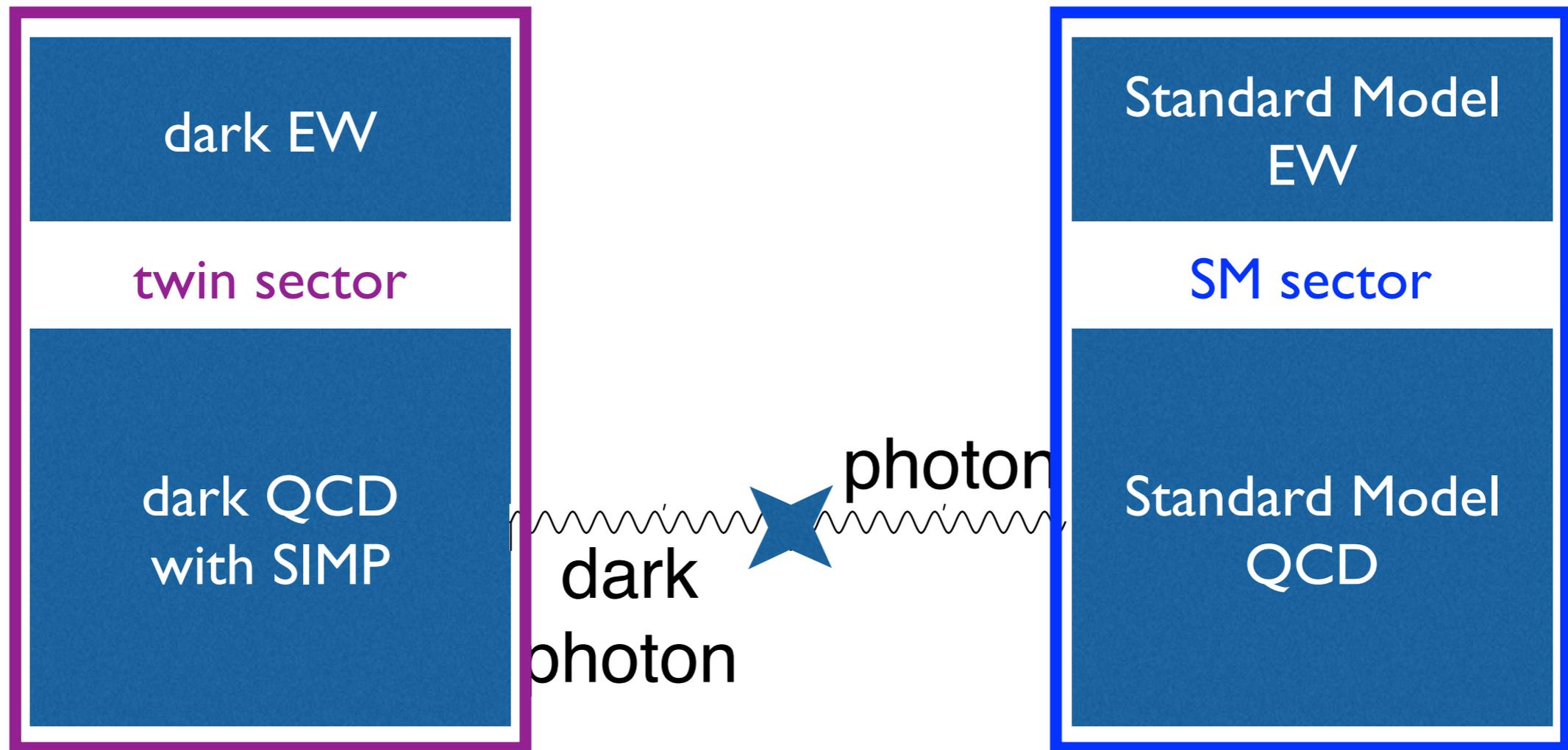
Hierarchy Problem?



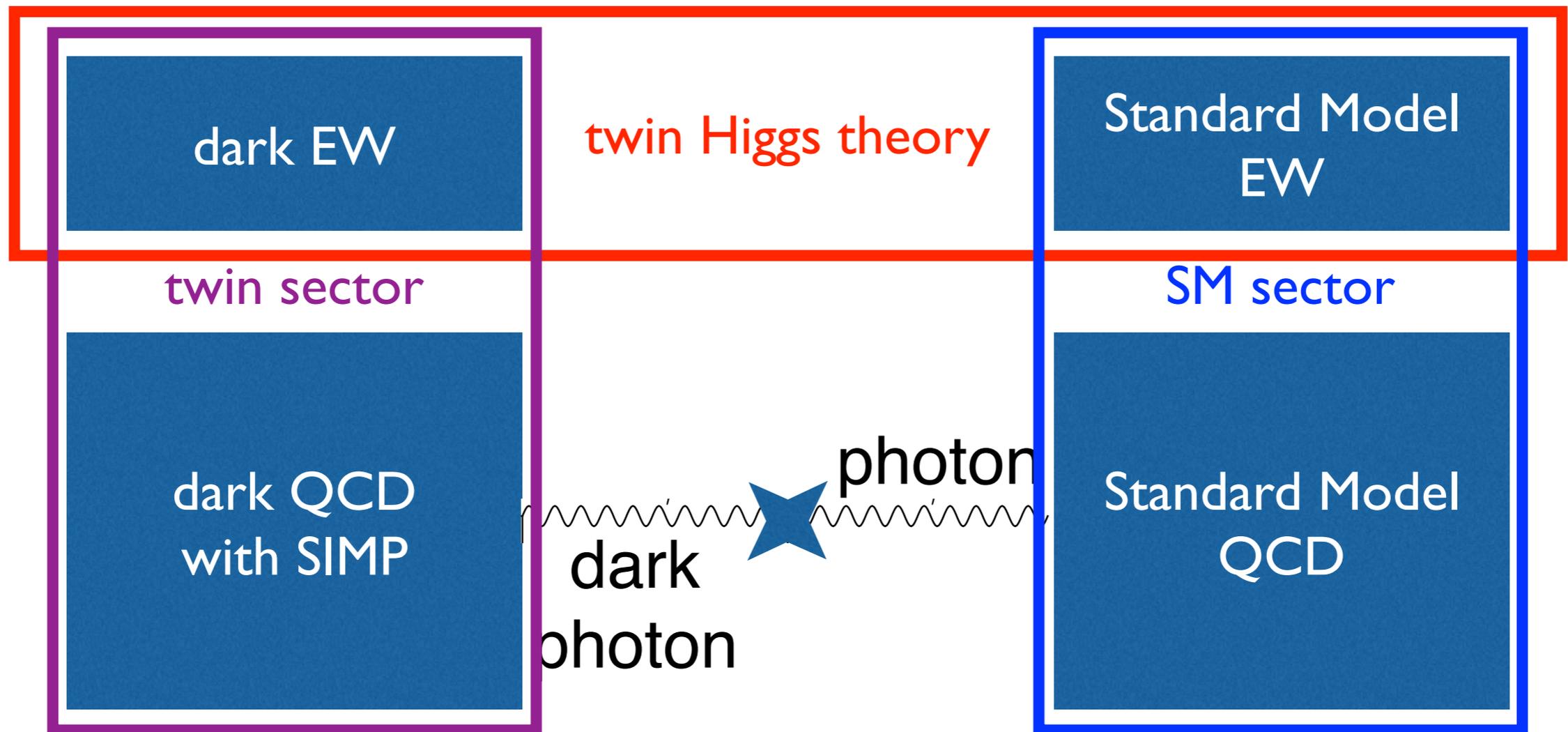
Hierarchy Problem?



Hierarchy Problem?

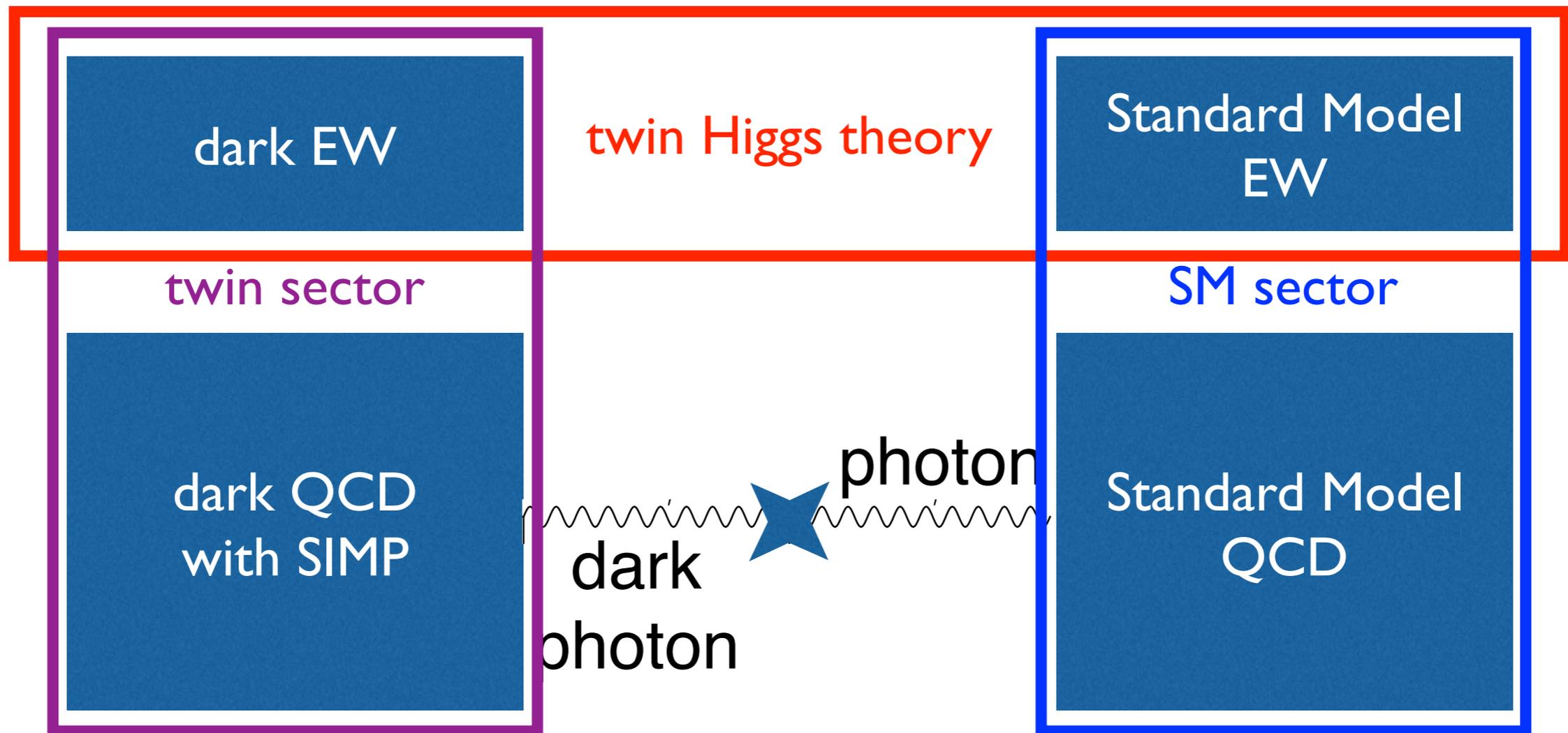


Hierarchy Problem?



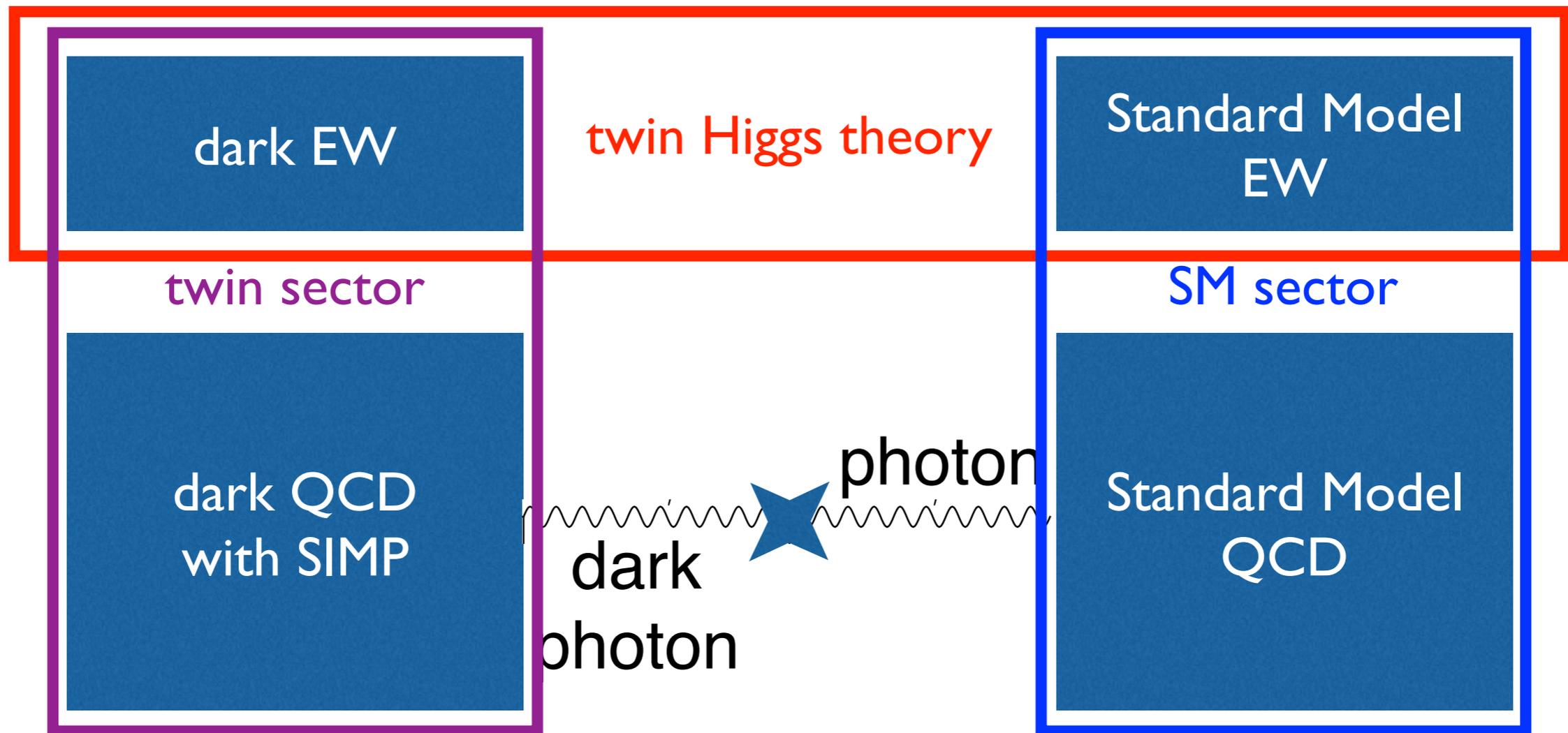
Hierarchy Problem?

$SU(4) \Rightarrow SU(3)$, SM Higgs doublet as pNGBs



Hierarchy Problem?

$SU(4) \Rightarrow SU(3)$, SM Higgs doublet as pNGBs



dark QCD is natural in twin Higgs theory with Z_2 symmetry
 dark QCD scale presumably higher $\sim (f/v)$ GeV

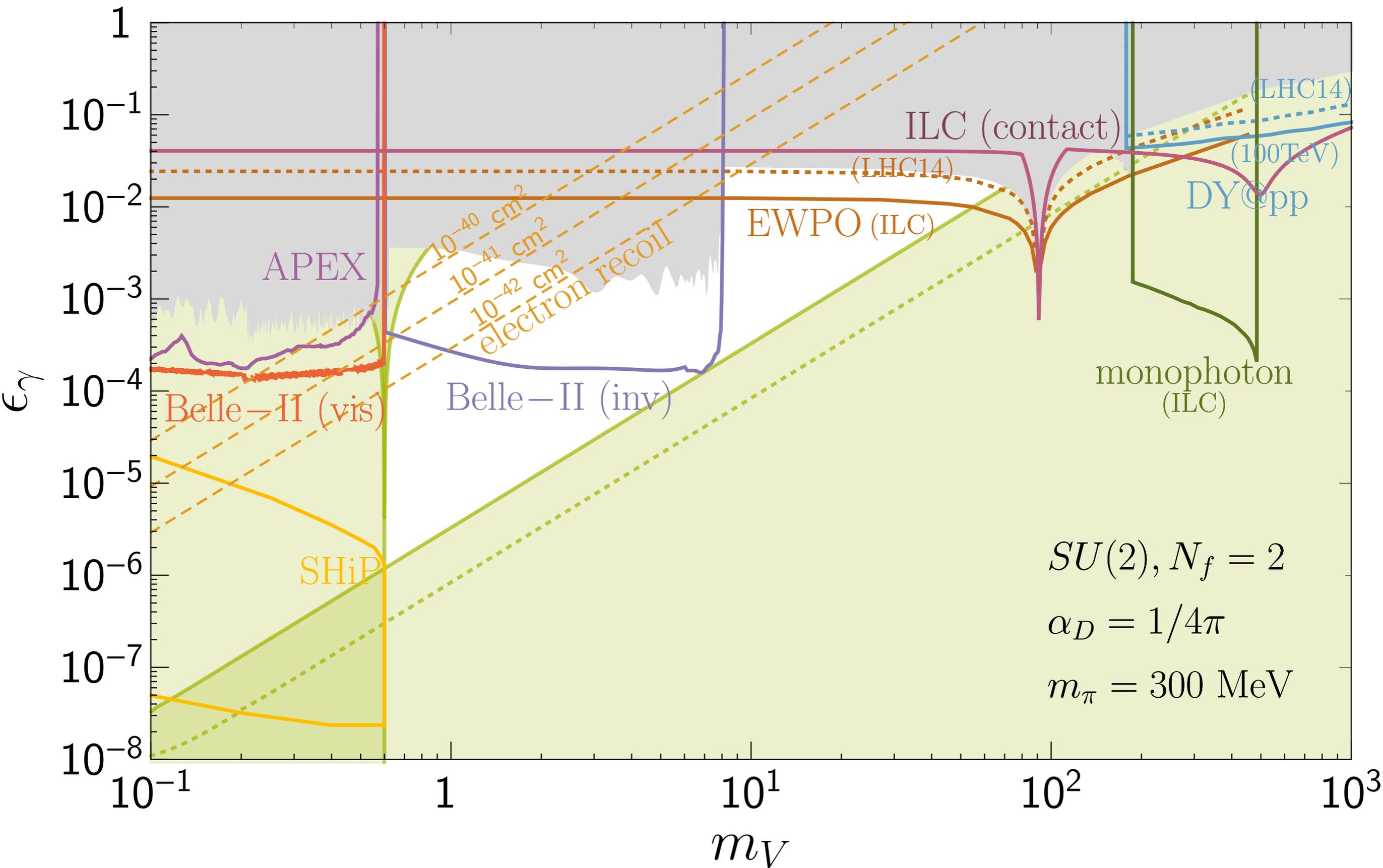
Twin SIMP

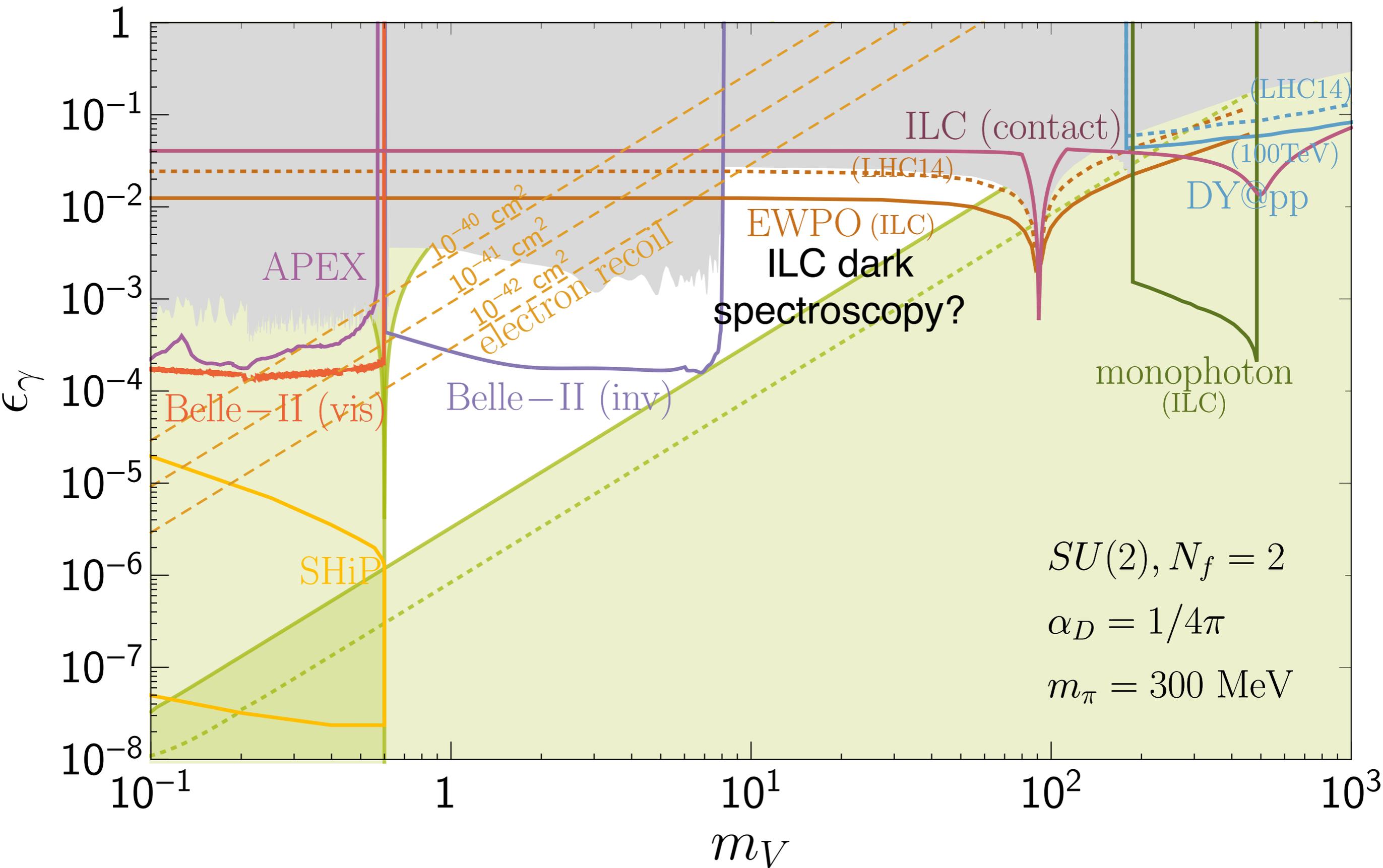
- Make all leptons $> \text{GeV}$
 - quarks: lightest particles in the twin sector
- degenerate u, d, s , no CKM mixing
 - approximate $SU(3)$ flavor symmetry
 - exact $U(1)_f, U(1)_{EM}$
 - π^+, K^+, K^0 absolutely stable
 - π^0, η decay to $\gamma_D^* \gamma_D^* \rightarrow (e^+e^-)(e^+e^-)$ before BBN limit

Twin SIMP

- Make all leptons $> \text{GeV}$
 - quarks: lightest particles in the twin sector
- degenerate u, d, s , no CKM mixing
 - approximate $SU(3)$ flavor symmetry
 - exact $U(1)_f, U(1)_{EM}$
 - π^+, K^+, K^0 absolutely stable
 - π^0, η decay to $\gamma_D^* \gamma_D^* \rightarrow (e^+e^-)(e^+e^-)$ before BBN limit

Can solve the hierarchy problem, too!





Conclusion

- surprisingly an *old* theory for dark matter
- SIMP Miracle³
 - mass \sim QCD
 - coupling \sim QCD
 - theory \sim QCD
- can solve problem with DM profile
- may also solve the hierarchy problem
- more generally, dark resonances fascinating
- *Can ILC do dark spectroscopy?*
- *absolutely unique to e^+e^-*
- Fun beyond EFT