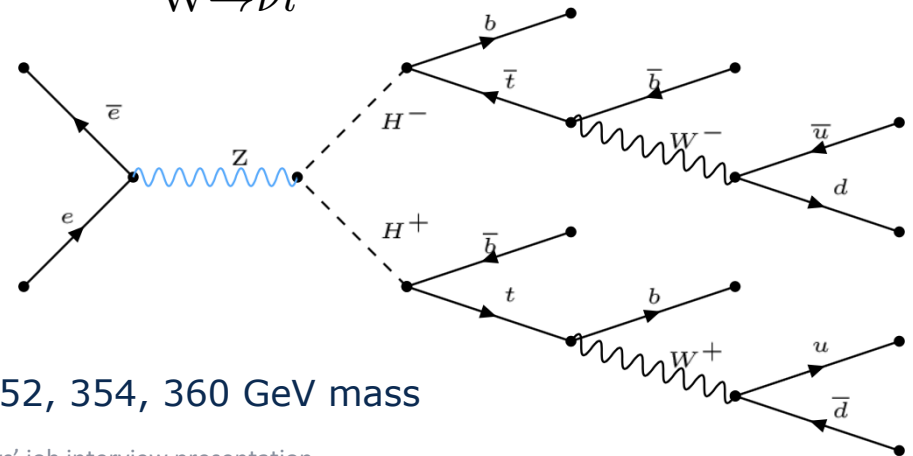




## Overview

- Full simulation study of ILC/ILD
- $m_{H^\pm} = 350 \text{ GeV}$  cross section = 9 fb BR( $H^\pm \rightarrow bt$ ) = 90%
- $E^+e^- \rightarrow H^+H^- \rightarrow tb \, tb \rightarrow Wbb \, Wbb \xrightarrow{W \rightarrow 2 \text{ jets}} 8 \text{ jets (hadronic)}$   
 $Wbb \, Wbb \xrightarrow{W \rightarrow 2 \text{ jets}} 6 \text{ jets + lepton}$   
 $W \rightarrow \nu l$
- Major background:
  - $ttH/ttZ/ttg \rightarrow ttbb$
  - $Tt \rightarrow bWbW$
  - $H_A \rightarrow bbbb$  (SUSY)
  - $H/A \rightarrow tt$  at resonance
  - Ignoring SUSY background
- Goal:  $m_{H^\pm}$  measurement
  - Samples with 340, 346, 348, 350, 352, 354, 360 GeV mass



## Neutrino four momentum

- Missing-Energy-Method (MEM)

$$p_{\text{vis}} = \sum_{i=1}^{N_{\text{PFO}}} p_i \quad p_{\text{CMS}} = (1000, 0, 0, 1000 \cdot \sin(0.014/2))$$

$$p_{\nu, \text{MEM}} = (p_{\text{CMS}} - p_{\text{vis}})$$

- Should I Sum pfos or jets? LCFIplus doesn't cluster all particles to jets?
- Neutrino-Direction-Method (NDM)

- Using the Direction of Missing-Energy-Method and calculation the Energy by fixing W-Mass

$$E_{\nu, \text{NDM}} = \frac{m_W^2}{E_l(1 - \alpha)} \quad \alpha = \frac{\vec{p}_{\nu, \text{MEM}} \cdot \vec{p}_l}{|\vec{p}_{\nu, \text{MEM}}| |\vec{p}_l|}$$

$$p_{\nu, \text{NDM}} = \left( E_{\nu, \text{NDM}}, E_{\nu, \text{NDM}} \frac{\vec{p}_{\nu, \text{MEM}}}{|\vec{p}_{\nu, \text{MEM}}|} \right)$$

## Neutrino four momentum

- Missing Momentum Method (MMM)
  - Using momentum from MEM for energy estimation

$$p_{\nu, \text{MMM}} = (|\vec{p}_{\nu, \text{MEM}}|, \vec{p}_{\nu, \text{MEM}})$$

- Missing Transversal Momentum Method (MTMM)
  - Using only the momentum in transversal momentum

$$\frac{m_W^2}{2} = E_\nu E_\ell - \vec{p}_\nu \vec{p}_\ell = E_\ell \sqrt{p_{\nu x}^2 + p_{\nu y}^2 + p_{\nu z}^2} - p_{\nu x} p_{\ell x} - p_{\nu y} p_{\ell y} - p_{\nu z} p_{\ell z}$$

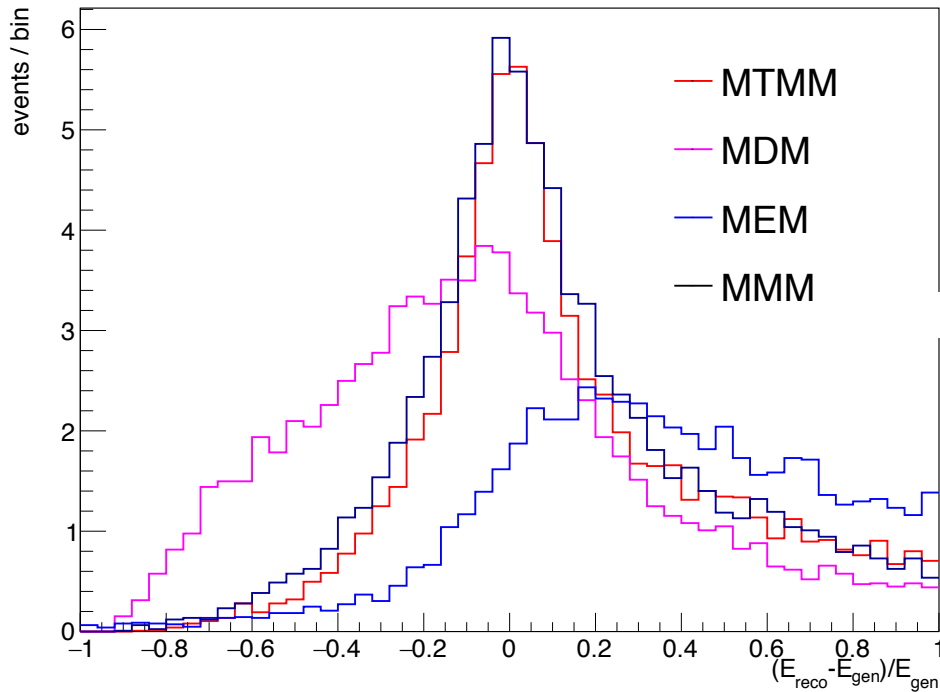
has two solutions

$$p_{\nu z} = \frac{\pm K + p_{\ell z} [2(p_{\ell y} p_{\nu y} + p_{\ell x} p_{\nu x}) + m_W^2]}{2(p_{\ell x}^2 + p_{\ell y}^2)}$$

$$K = E_\ell \sqrt{4[(2p_{\ell x} p_{\nu x} + m_W^2) p_{\ell y} p_{\nu y} - p_{\ell x}^2 p_{\nu y}^2 - p_{\ell y}^2 p_{\nu x}^2 + m_W^2 p_{\ell x} p_{\nu x}] + m_W^4}$$

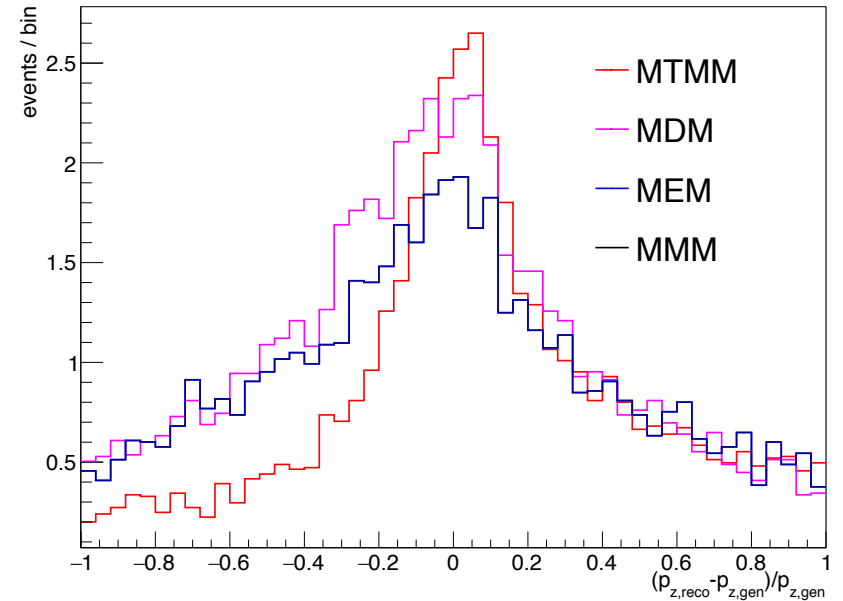
# Neutrino reconstruction

## Neutrino energy



MTMM	Transversal momentum
MDM	Direction
MEM	Standard with missing energy
MMM	Only using momentum

## Neutrino momentum in z-direction



## Event selection

- Different event selections were used
  - Static cuts
  - BDT
- Optimizations
  - Signal significance
  - Significance for correctly paired signal (BDT + separate BDTG)

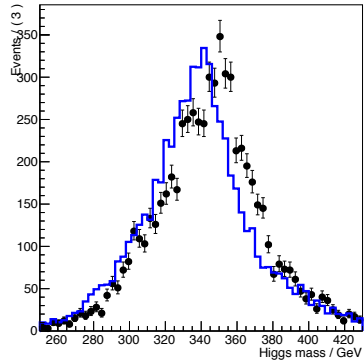
Cut type	Optim. type	Mode	Sig	o. Sig	Z(h)	$t\bar{t}Z$	$t\bar{t}b\bar{b}$	$t\bar{t}(sl)$	$t\bar{t}(h)$	$t\bar{t}h(sl)$	$t\bar{t}h(h)$	other
Static cuts		(h)	1982	46	0	138	106	454	16	200	12	0
Static cuts		(sl)	3090	586	139	208	181	95	678	53	327	26
Static cuts	corr. paired	(h)	579	699	0	50	61	112	2	103	4	0
Static cuts	corr. paired	(sl)	721	1154	0	46	54	12	122	12	121	0
BDT		(h)	2156	59	0	136	104	363	12	206	18	5
BDT		(sl)	3495	519	139	215	161	59	640	39	373	23
BDT	corr. paired	(h)	671	483	0	24	27	65	2	54	2	0
BDT	corr. paired	(sl)	865	936	0	18	30	5	63	4	69	0

**Table 2.10:** Remaining background after the event selections; (h) stands for hadronic and (sl) stands for semi-leptonic

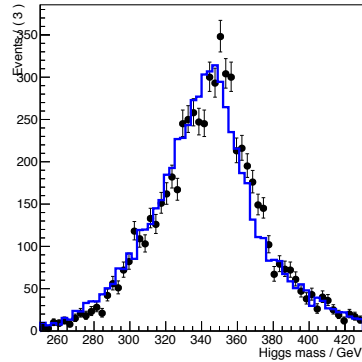
## Mass measurement

- Template method
  - Compare mass distribution shape -> calculation  $\chi^2$
  - Get uncertainty from  $\chi^2$  parabola
- Shape method
  - Get shape of BG, correctly paired signal and false paired signal
  - Calibrate fitted mean to Higgs mass
- Combined method
  - Reduce fitting variables to Higgs mass from cor. and false paired signal

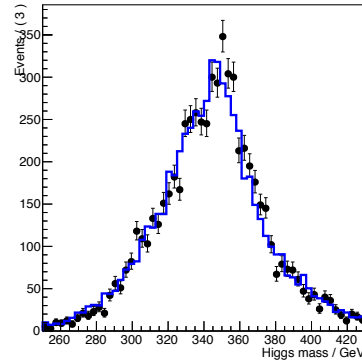
Template fit for  $m_{H^\pm} = 340$  GeV



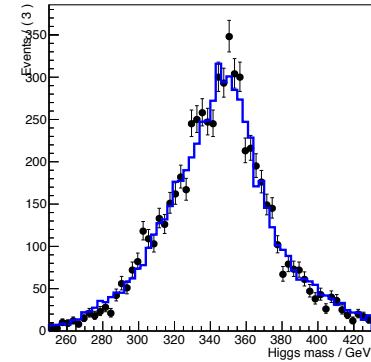
Template fit for  $m_{H^\pm} = 346$  GeV



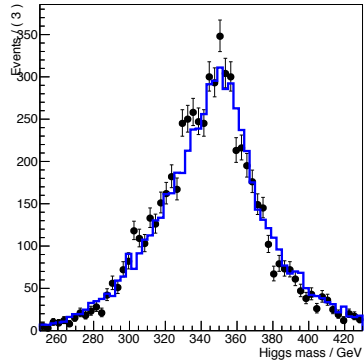
Template fit for  $m_{H^\pm} = 348$  GeV



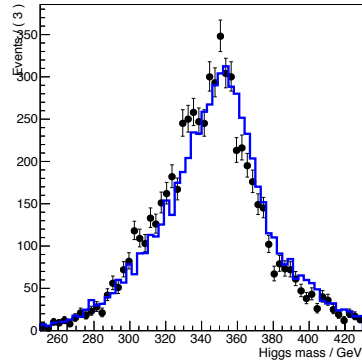
Template fit for  $m_{H^\pm} = 350$  GeV



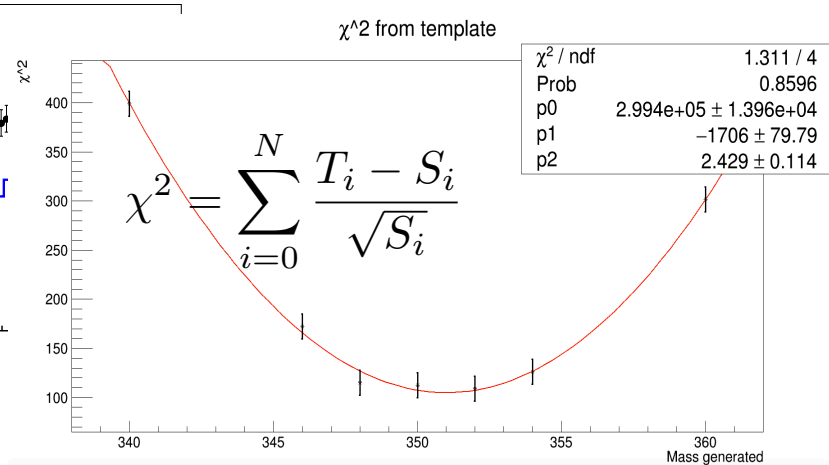
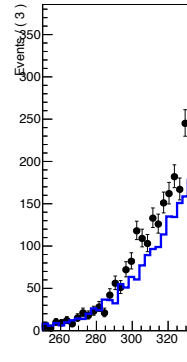
Template fit for  $m_{H^\pm} = 352$  GeV



Template fit for  $m_{H^\pm} = 354$  GeV



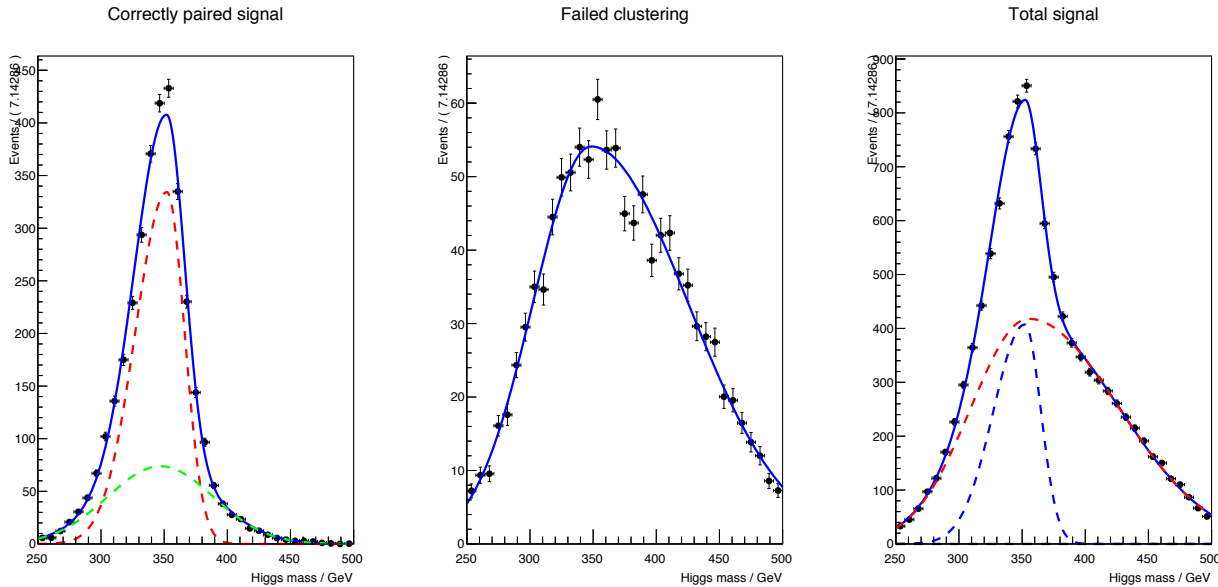
Template fit for  $m_{H^\pm} = 360$  GeV





# Shape method

- Get signal shape (Static Cuts)

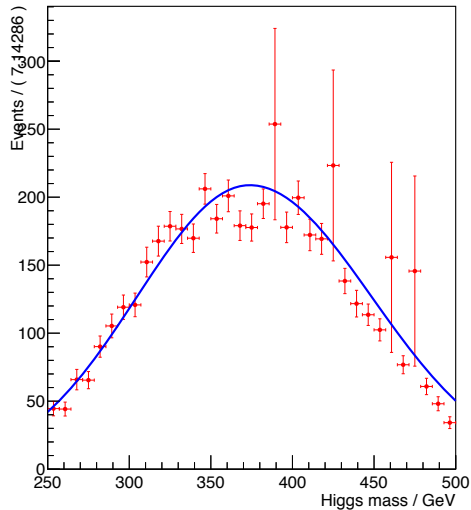


**Static cuts**  
 $N_s$  (exp.) = 5491  
**Correctly paired (24.5%):**  
 $\mu$ : 352.1 GeV  
 $\sigma_L$ : 24.8 GeV  
 $\sigma_R$ : 12.8 GeV  
**Wrong paired (75.5%):**  
 $\mu$ : 355.1 GeV  
 $\sigma_L$ : 45.6 GeV  
 $\sigma_R$ : 71.5 GeV  
 red.  $\chi^2 = 2.05$

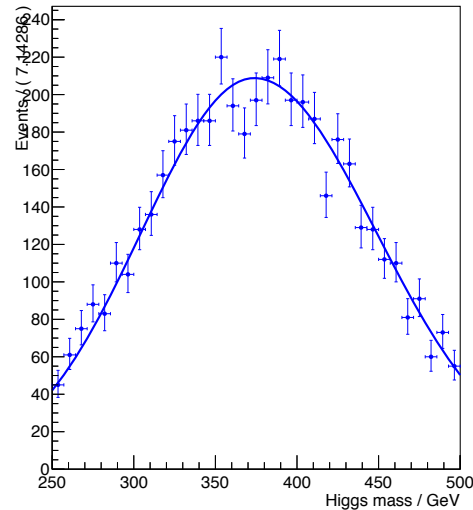
## Shape method

- Get background shape (Static Cuts)

Background fit to BiGauss (original)



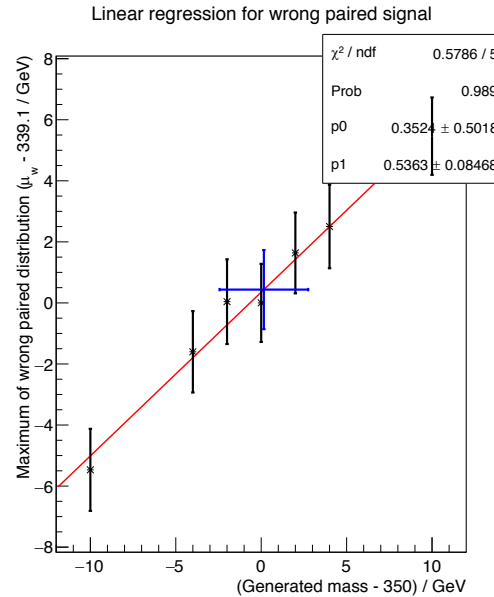
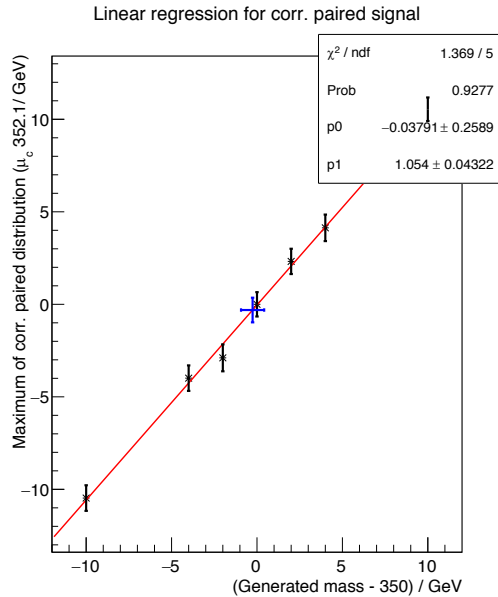
Background p.d.f. and generated data set



**Static cuts**  
 **$N_B$  (exp.) = 2418**  
 **$\mu = 373.8$  GeV**  
 **$\sigma_L = 69.2$  GeV**  
 **$\sigma_R = 74.8$  GeV**  
**red.  $\chi^2$  (original BG) = 3.06**  
**red.  $\chi^2$  (gen BG) = 0.96**

## Shape method – mass estimation (BDT – correctly paired)

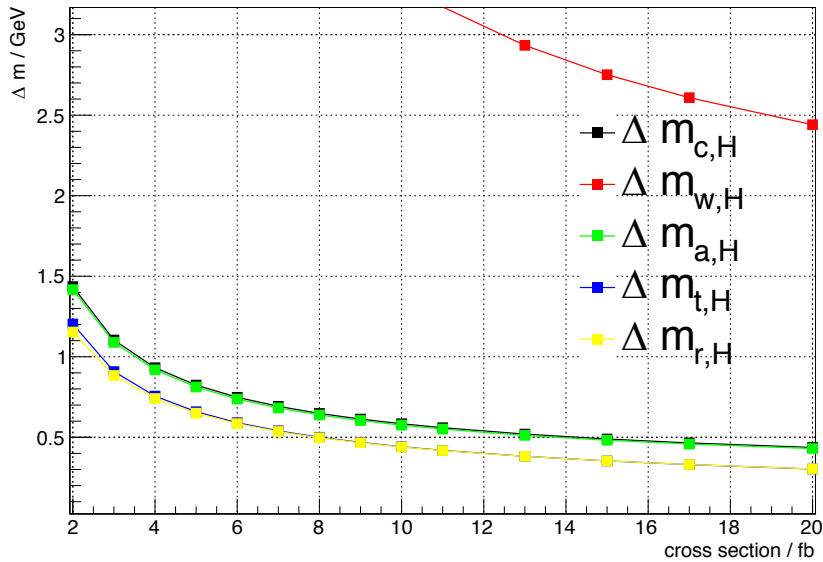
- Linear regression for signal distribution maximum and generated mass
- Test data set (blue)



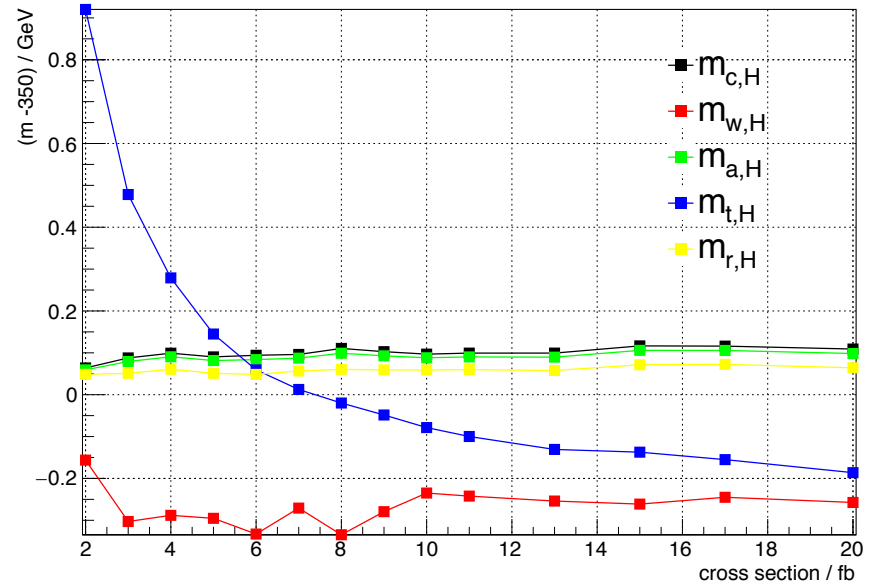
<b>BDT correctly paired</b>
$m_{c,H}/\text{GeV} = 349.74 \pm 0.68$ (Corr. pairing)
$m_{w,H}/\text{GeV} = 350.16 \pm 2.59$ (Wrong pairing)
$m_{a,H}/\text{GeV} = 349.77 \pm 0.66$ (combined)
$m_{r,H}/\text{GeV} = 349.83 \pm 0.46$ (reduced)
$\Delta_{c,\text{const}}: 0.2456$
$\Delta_{c,\text{linear}}: -0.012$
$\Delta_{c,\text{fit}}: 0.6319$
$m_{c,H}/\text{GeV} = (1.05 \pm 0.04) \mu_c + (352.1 \pm 0.26)$
$m_{w,H}/\text{GeV} = (0.54 \pm 0.08) \mu_w + (339.09 \pm 0.5)$

## MC toy with varied cross section (BDT – correctly paired)

Mass uncertainty with TMVA correctly paired optimized



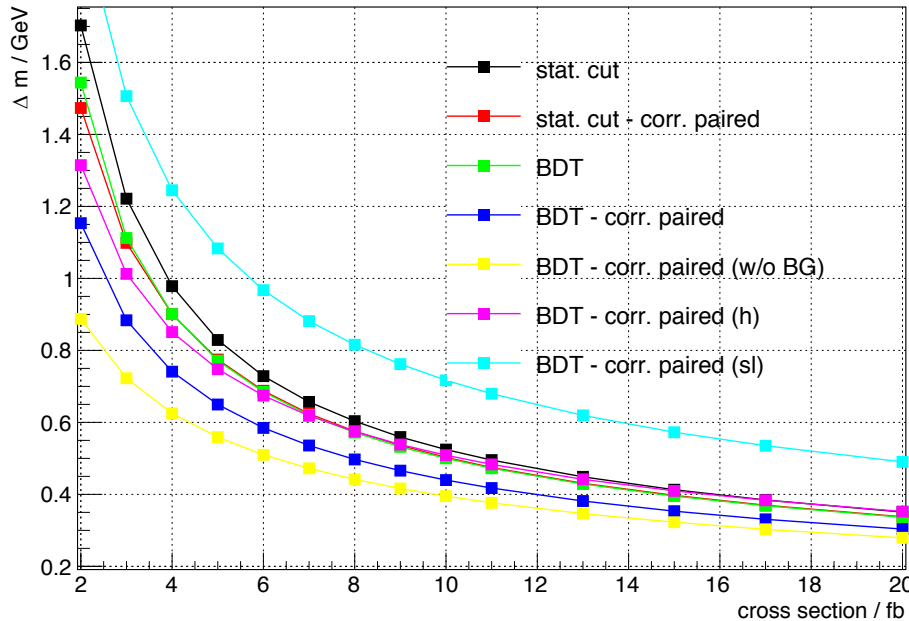
Mass deviation with TMVA correctly paired optimized



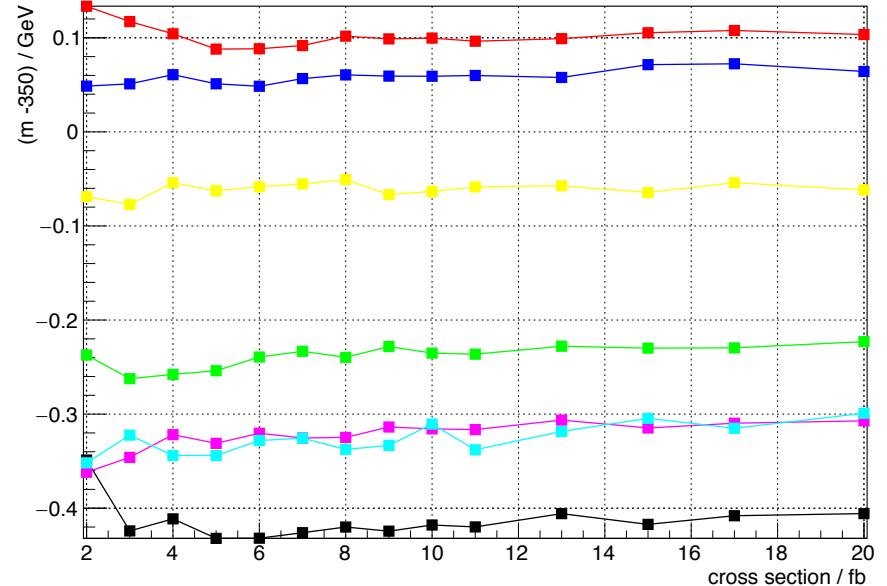
- Result from 10 000 toy MC

# MC toy with varied cross section (BDT – correctly paired)

Mass uncertainty with reduced shape method



Mass deviation with reduced shape method



- Result from 10 000 toy MC

## Result

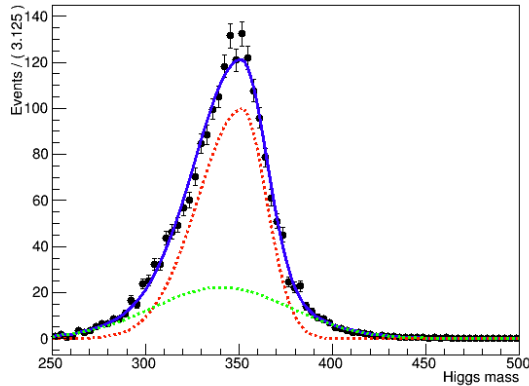
- 0.5 GeV mass precision
- Neutrino four momentum reconstruction with Missing Momentum Method was used
- Missing Transversal Momentum Method has great potential

Cut type	Optim. type	Mode	Corr. pair				mass precision with $\sigma = 9$ fb
			Signif.	Signif.	Effi.	Purity	
Static cuts		hadronic	44.6	17.9	65 %	64 %	0.56 GeV
Static cuts		semi-lep.	36.5	17.3	43 %	67 %	
Static cuts	corr. paired	hadronic	37.2	21.9	62 %	66 %	0.54 GeV
Static cuts	corr. paired	semi-lep.	31.5	19.0	55 %	63 %	
BDT		hadronic	49.1	20.9	73 %	67 %	0.53 GeV
BDT		semi-lep.	38.6	19.4	46 %	71 %	
BDT	corr. paired	hadronic	38.5	26.6	74 %	82 %	0.47 GeV
BDT	corr. paired	semi-lep.	31.5	23.0	64 %	79 %	

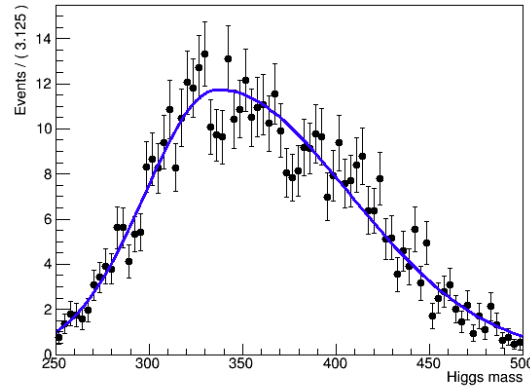
# Backup

# Static cuts

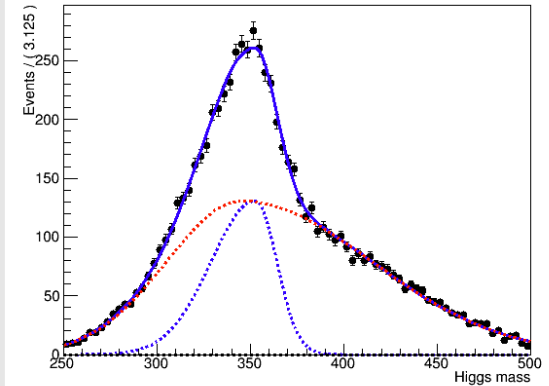
Correct paired Signal fit to Breit-Wigner



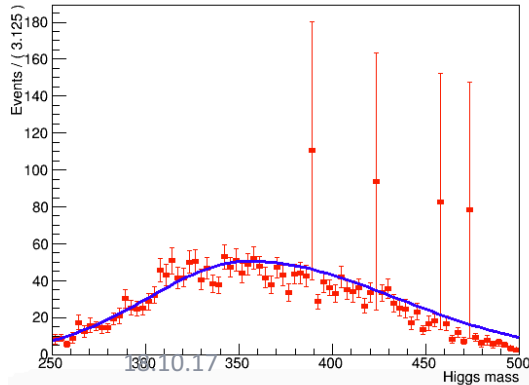
very false paired



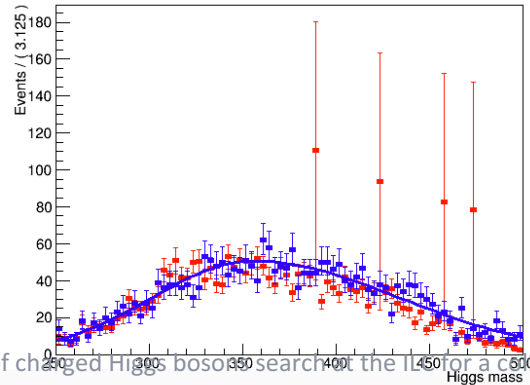
All Signal



Background fit to BiGauss (original)

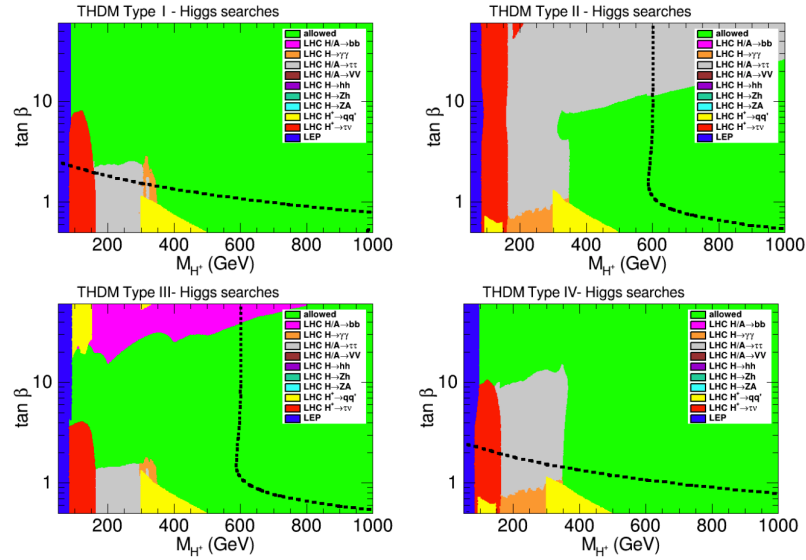


Background fit to BiGauss (both)

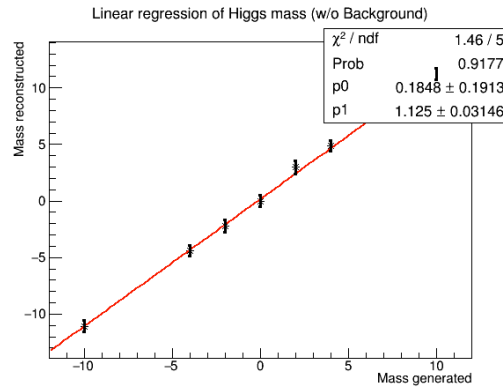
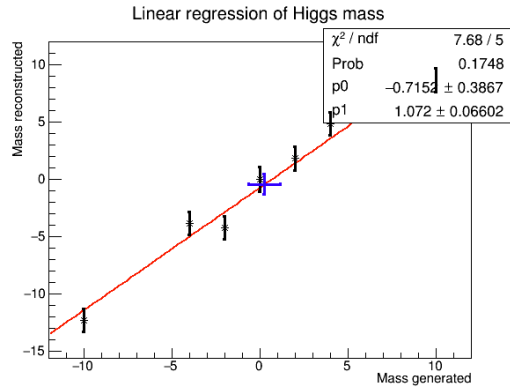


no cut  $m_{H1}/m_{H2}$   
 $\chi^2$  (cor. pair) = 0.0  
 $\chi^2$  (false pair) = 1.17941674959  
 $\chi^2$  (all signal) = 1.32537570011  
 $\chi^2$  (original BG) = 4.59289973065  
 $\chi^2$  (gen BG) = 1.1154077007





# Static cuts



mean\_test: (340.50544556077364, 0.8972169561338035)

m\_H\_test: 350.256557321 ± 0.911446596581

m\_H\_test: 351.780104696 ± 4.91384948219 (False pairing)

m\_H\_test: 351.018331008 ± 0.644490069132 (combined)

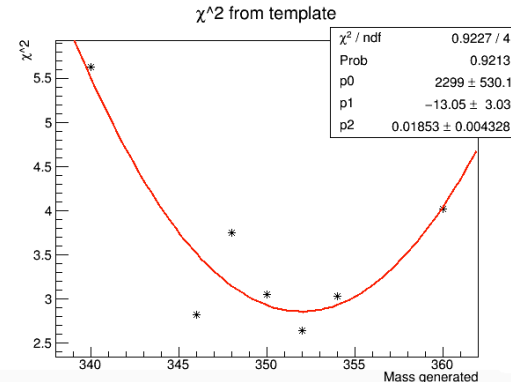
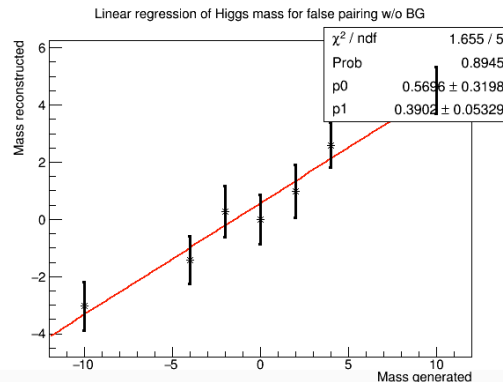
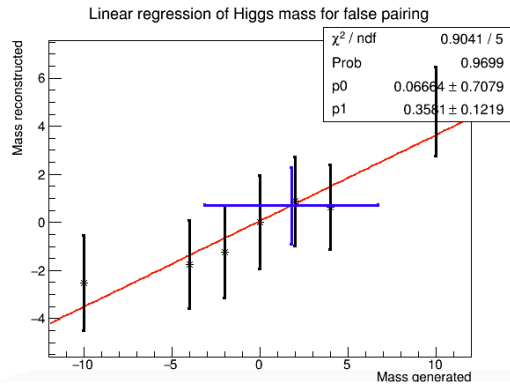
$\Delta_{\text{const}}$ : 0.360645772729

$\Delta_{\text{linear}}$ : -0.0252633508819

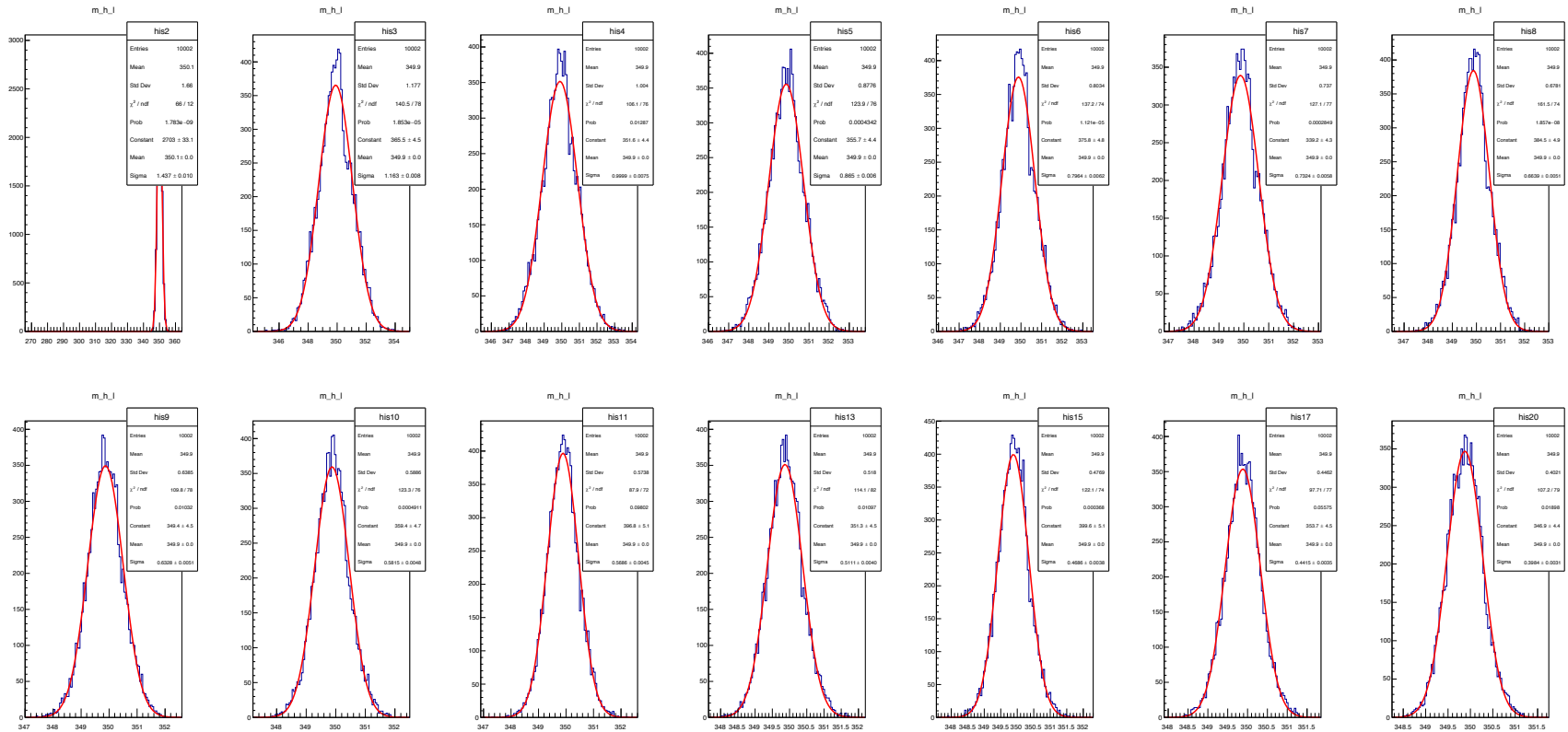
$\Delta_{\text{fit}}$ : 0.836678724561

**b**: 1.0723554093 ± 0.0660187568936

**a**: -0.71516969819 ± 0.386740445229

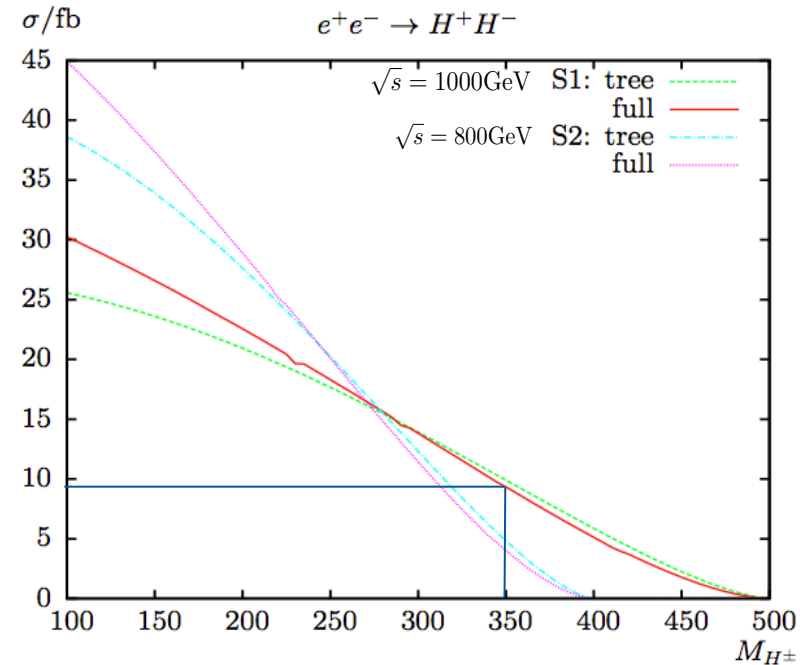


# MC toy with varied cross section



## Cross section

- $\sigma \approx 9$  fb with  $P = (-80\%, 20\%)$  10.4 fb
- $\mathcal{L} = 1000$  1/fb
- $N = 9000$   $H^\pm$  events
- Assuming  $BR(H^\pm \rightarrow tb) = 90\%$
- $BR(t \rightarrow bW) = 100\%$
- $BR(W \rightarrow 2\text{jets}) = 67.6\%$
- $BR(W \rightarrow e\nu) = 10.75$
- $BR(W \rightarrow e\nu) = 10.57$
- Hadronic: 5100 events
- Semileptonic: 3200 events

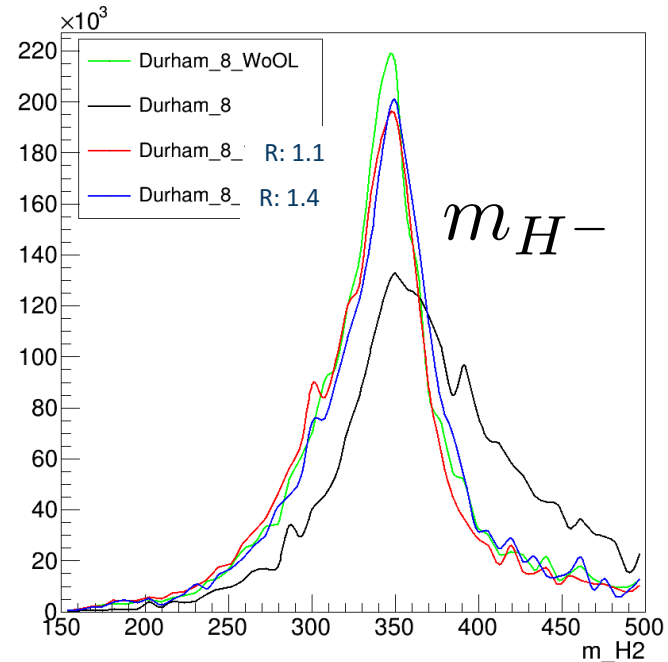
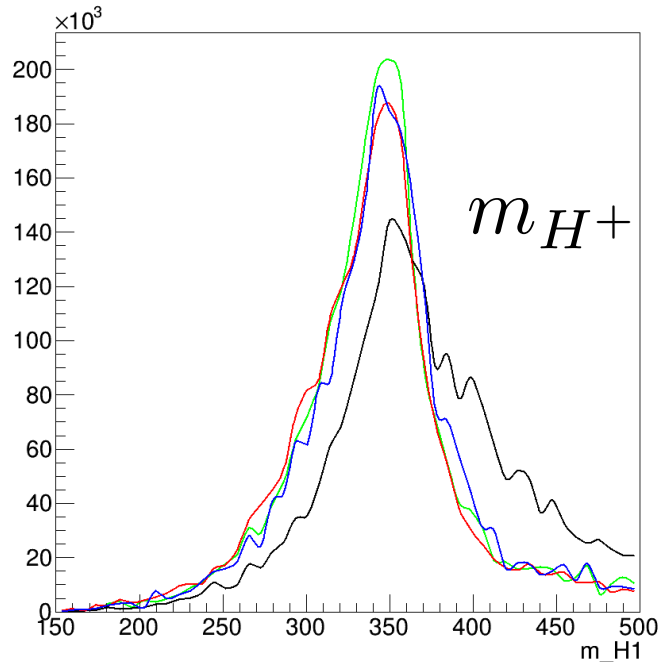


Source: ***Charged Higgs Boson production at ee colliders in the complex MSSM: a full one-loop analysis***  
Heinemeyer, S. and Schappacher, C. Eur. Phys. J. (2016)

## Analysis Overview

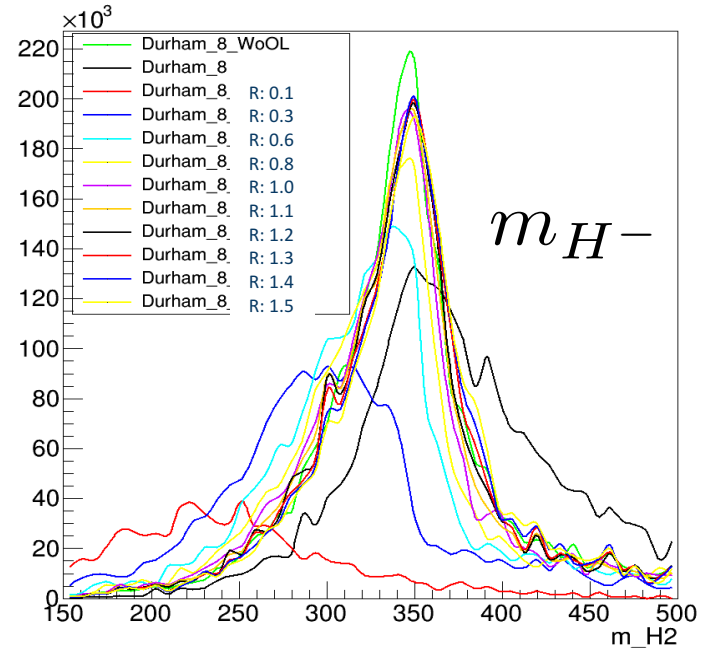
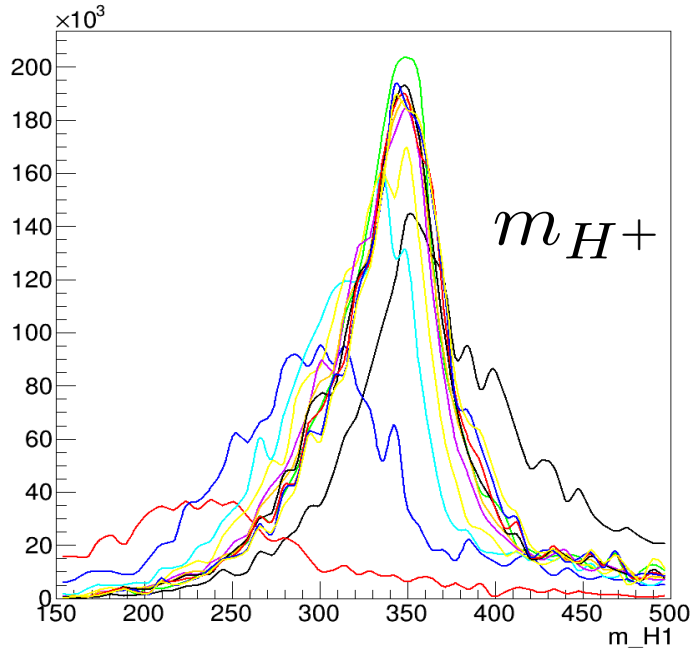
- Isolated Lepton selection
- Reduce beam background by kt-Algorithm
- Jet-clustering and flavor tagging (LCFIplus)
- Calculating neutrino four-momentum (only semi-leptonic)
- Jet-pairing
- Extracting signal and background mass shape
- Added fit to find Higgs-mass

## Find R for kt-Algorithm




Reconstructed  $H^+$  and  $H^-$  mass with realistic clustering and pairing with generator information

## Find R for kt-Algorithm



Reconstructed  $H^+$  and  $H^-$  mass with realistic clustering and pairing with generator information

## Chi<sup>2</sup> - Jet Pairing (hadronic)

	w/o overlay	R: 1.3	with overlay	
B-tag efficiency 	44.6	42.5	38.0	the 4 b-jets have highest b-tag in the event
Clustering works well	50.7	49.4	40.2	For every color singlet there are 2 jets with a major fraction from this singlet
Pairing works	27.8	<b>25.0</b>	17.2	Jet pairing agrees with major color singlet fraction in jet

$$\chi^2 = \left| \frac{(m_{j_1 j_2 j_3 j_4})^2 - (m_{j_5 j_6 j_7 j_8})^2}{2\sigma_{H^+}^2} \right| + \left( \frac{m_{j_2 j_3 j_4} - M_t}{\sigma_t} \right)^2$$

$$+ \left( \frac{m_{j_6 j_7 j_8} - M_t}{\sigma_t} \right)^2 + \left( \frac{m_{j_3 j_4} - M_W}{\sigma_W} \right)^2 + \left( \frac{m_{j_7 j_8} - M_W}{\sigma_W} \right)^2$$



## Lepton Selection

- Using the IsolatedLeptonTaggingProcessor
  - From MarilnReco
  - Based on MVA
- Open task: reduce false Lepton Tag in hadronic Channel
  - With event shape or b-tag
  - But actually the pairing efficiency is not effected

	Total (%)	w/o tau (%)
Lepton Tag	60.3	90.4
Correct Tag	60.0	90.0
False Lepton Tagged	0.3	0.4
Electron	29.5	89.4 (w/o tau and myon)
Myon	30.3	90.5 (w/o tau and electron)
False Lepton Tag in hadronic	2.1	

## Neutrino Four-vector

- Method 1: Missing-Energy-Method (MEM)

$$p_{\text{vis}} = \sum_{i=1}^{N_{\text{PFO}}} p_i \quad p_{\text{CMS}} = (1000, 0, 0, 1000 \cdot \sin(0.014/2))$$

$$p_{\nu, \text{MEM}} = (p_{\text{CMS}} - p_{\text{vis}})$$

- Should I Sum pfos or jets? LCFIplus doesn't cluster all particles to jets?
- Method 2: Neutrino-Direction-Method (NDM)
  - Using the Direction of Missing-Energy-Method and calculation the Energy by fixing W-Mass

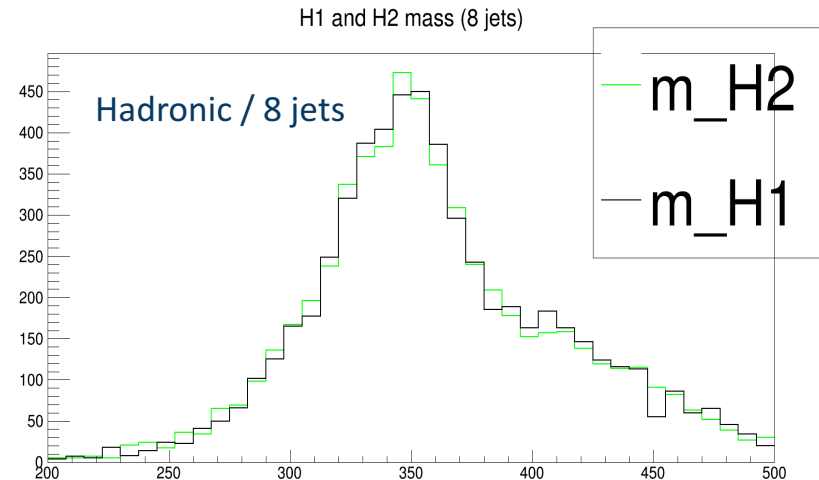
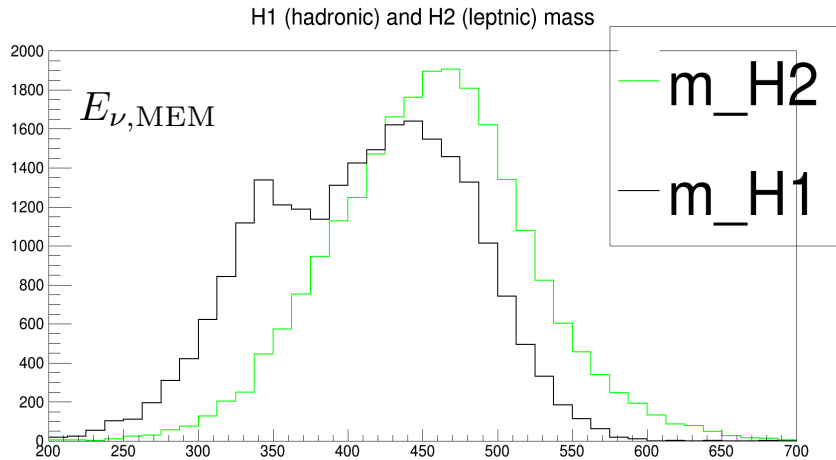
$$E_{\nu, \text{NDM}} = \frac{m_W^2}{E_l(1 - \alpha)} \quad \alpha = \frac{\vec{p}_{\nu, \text{MEM}} \cdot \vec{p}_l}{|\vec{p}_{\nu, \text{MEM}}| |\vec{p}_l|}$$

$$p_{\nu, \text{NDM}} = \left( E_{\nu, \text{NDM}}, E_{\nu, \text{NDM}} \frac{\vec{p}_{\nu, \text{MEM}}}{|\vec{p}_{\nu, \text{MEM}}|} \right)$$

## Higgs mass reconstructed with Jet pairing

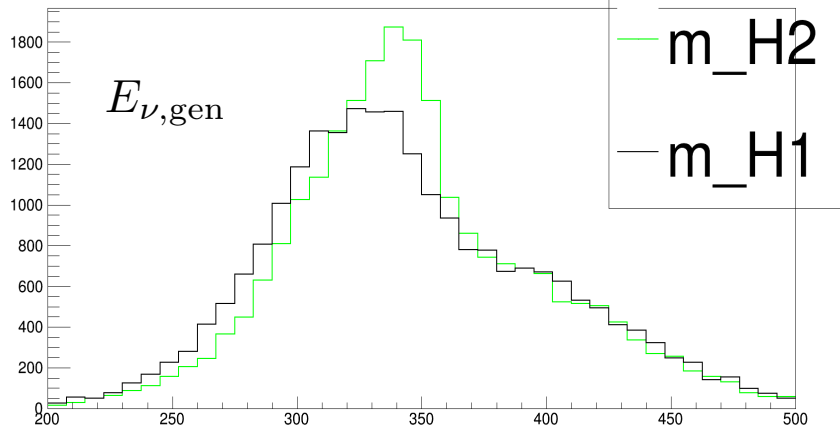
- Chi<sup>2</sup> minimization method

$$\chi^2 = \left| \frac{(m_{j_1 j_2 j_3 j_4})^2 - (m_{j_5 j_6 j_7 j_8})^2}{2\sigma_{H^+}^2} \right| + \left( \frac{m_{j_2 j_3 j_4} - M_t}{\sigma_t} \right)^2 + \left( \frac{m_{j_6 j_7 j_8} - M_t}{\sigma_t} \right)^2 + \left( \frac{m_{j_3 j_4} - M_W}{\sigma_W} \right)^2 + \left( \frac{m_{j_7 j_8} - M_W}{\sigma_W} \right)^2$$

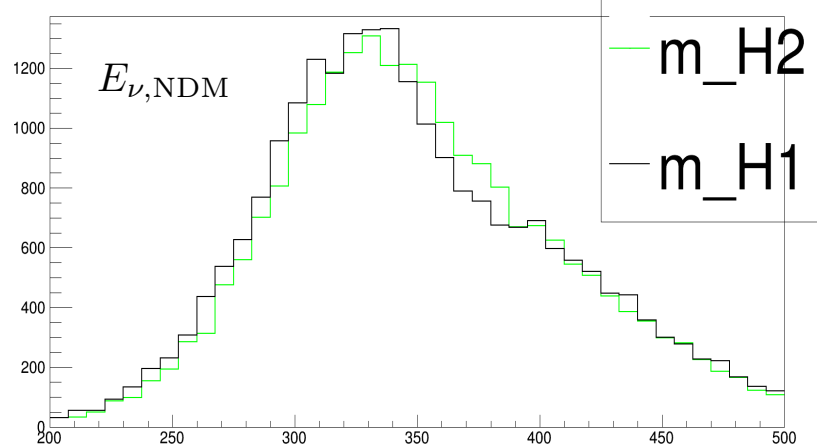




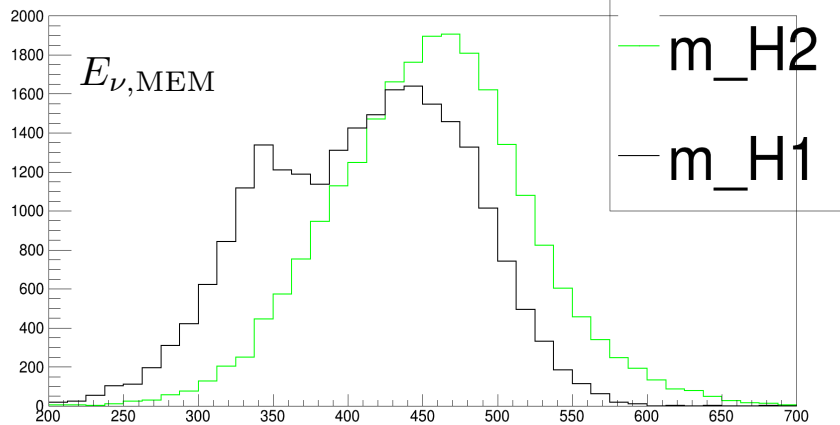
H1 (hadronic) and H2 (leptnic) mass (ny 4-momentum from gen)



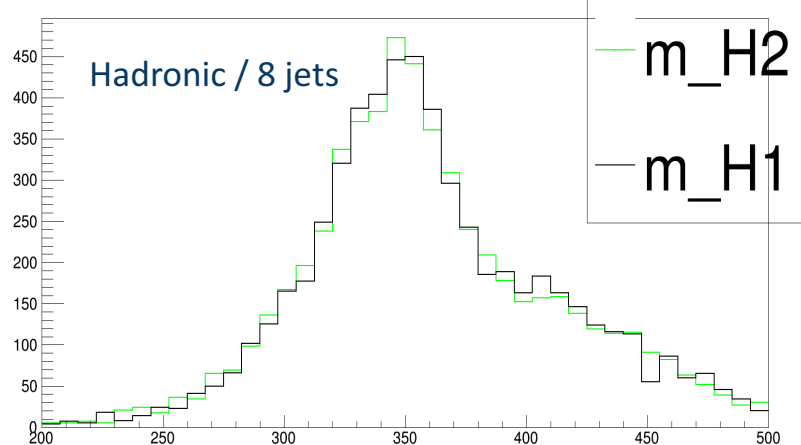
H1 (hadronic) and H2 (leptnic) mass (ny E from M\_W)



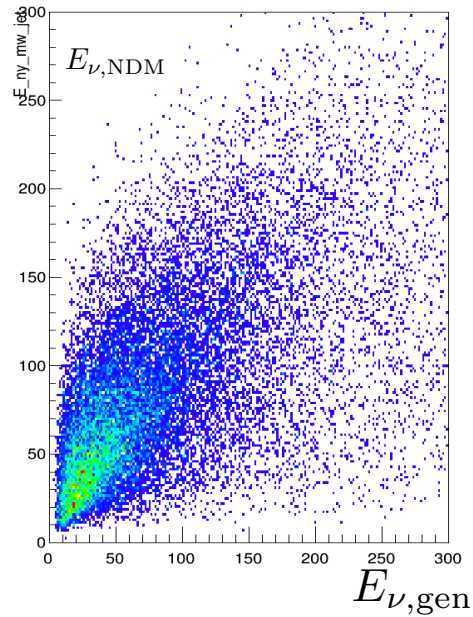
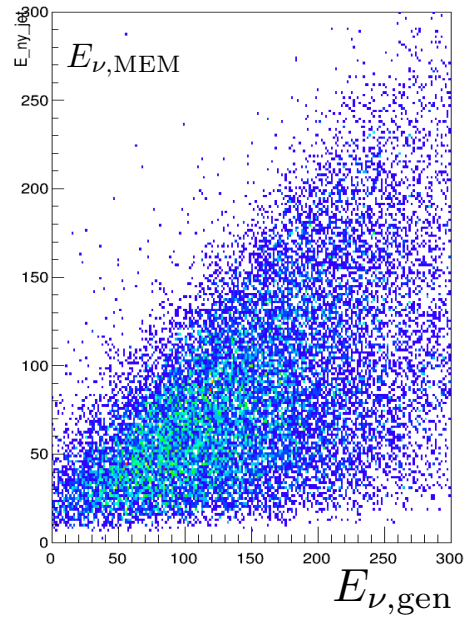
H1 (hadronic) and H2 (leptnic) mass



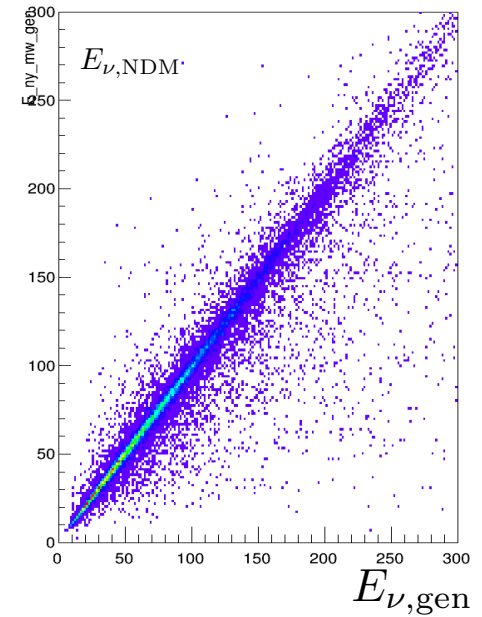
H1 and H2 mass (8 jets)



# Neutrino Four-vector

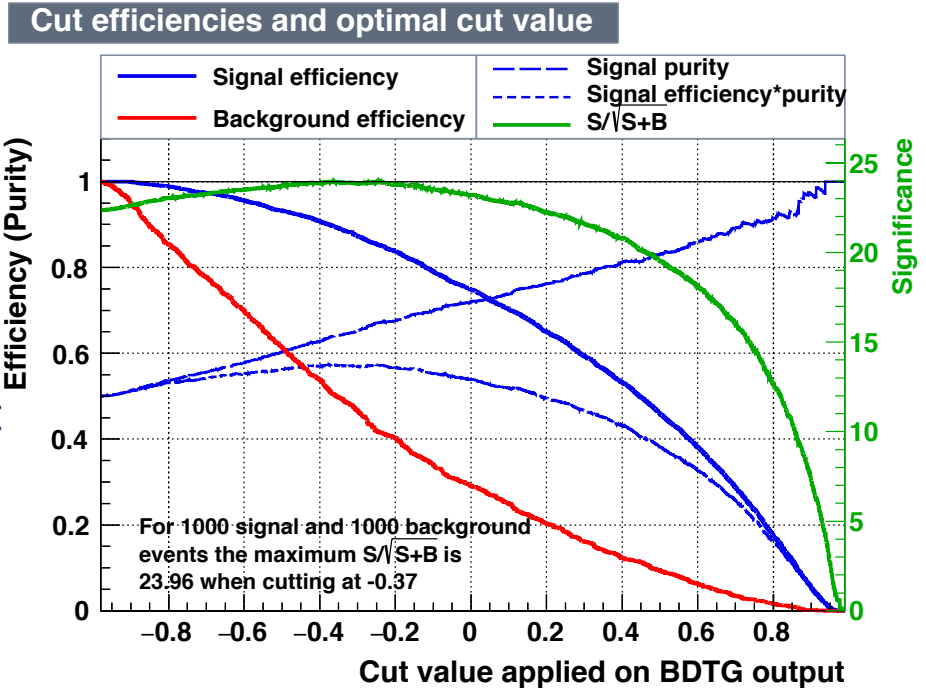


## Neutrino direction from Generator



## Boosted Decision Tree

- For further Background reduction
- Here for hadronic
- Trained only on main background after static cuts
- About  $1.5\sigma$  gain
- Its quite difficult to apply result of TMVA to cuts

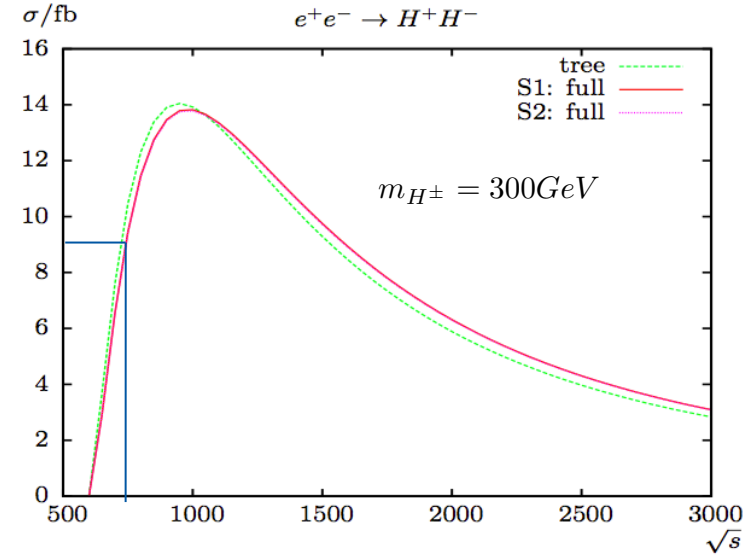
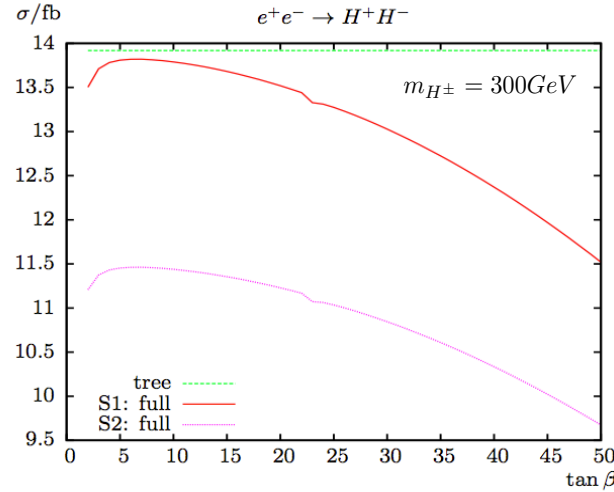


## Plan

- Toy Monte Carlo Study
- Add pt Method for neutrino four momentum
- Do fitting for semi-leptonic mode
- Goal:
  - mass fit -> mass resolution measurement
  - Detection efficiency  
-> cross section times branching ratio
- Bonus: (most probable imposible)
  - Research how to distinguish  $H^+$  and  $H^-$
  - Study of CP-violation measurement

## Cross section

- $\sigma(\tan\beta)$  const. on tree-level
- 1 TeV below maximum of  $\sigma$

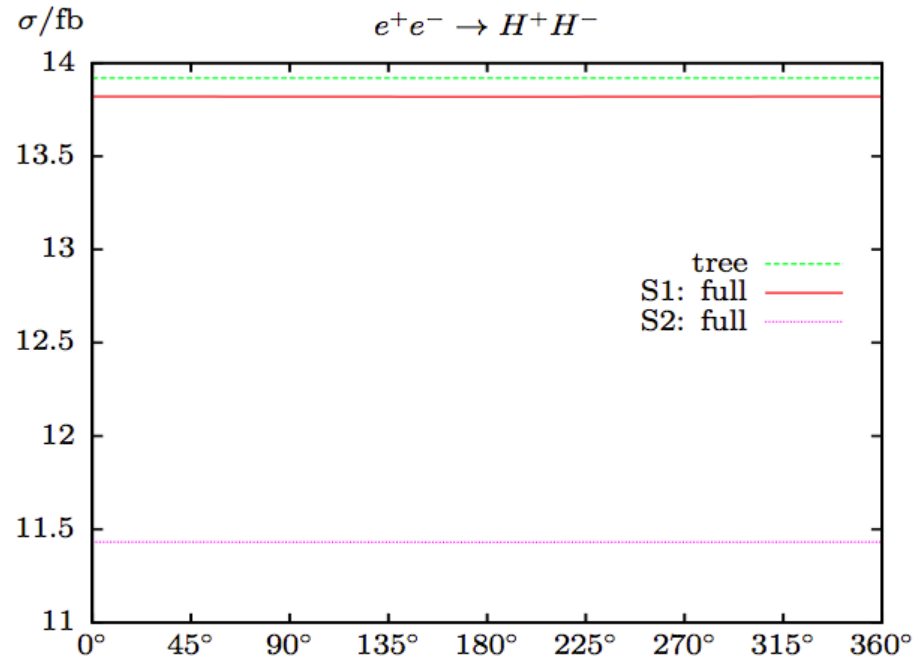


Scen.	$\sqrt{s}$	$t_\beta$	$\mu$	$M_{H^\pm}$	$M_{\tilde{Q}, \tilde{U}, \tilde{D}}$	$M_{\tilde{L}, \tilde{E}}$	$ A_{t,b,\tau} $	$M_1$	$M_2$	$M_3$
S1	1000	7	200	300	1000	500	$1500 + \mu/t_\beta$	100	200	1500
S2	800	4	200	300	1000	500	$1500 + \mu/t_\beta$	100	200	1500

Source: **Charged Higgs Boson production at ee colliders in the complex MSSM: a full one-loop analysis**  
Heinemeyer, S. and Schappacher, C. Eur. Phys. J. (2016)



## Cross section



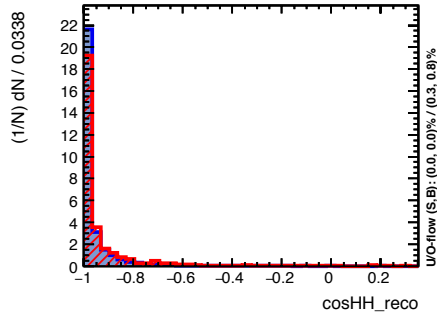
Scen.	$\sqrt{s}$	$t_\beta$	$\mu$	$M_{H^\pm}$	$M_{\tilde{Q}, \tilde{U}, \tilde{D}}$	$M_{\tilde{L}, \tilde{E}}$	$ A_{t,b,\tau} $	$M_1$	$M_2$	$M_3$
S1	1000	7	200	300	1000	500	$1500 + \mu/t_\beta$	100	200	1500
S2	800	4	200	300	1000	500	$1500 + \mu/t_\beta$	100	200	1500

Source: **Charged Higgs Boson production at  $ee$  colliders in the complex MSSM: a full one-loop analysis**

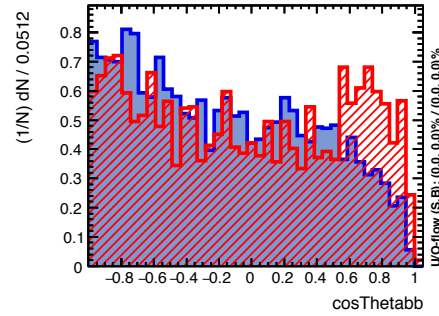
Heinemeyer, S. and Schappacher, C. Eur. Phys. J. (2016)

# Boosted Decision Tree (Input)

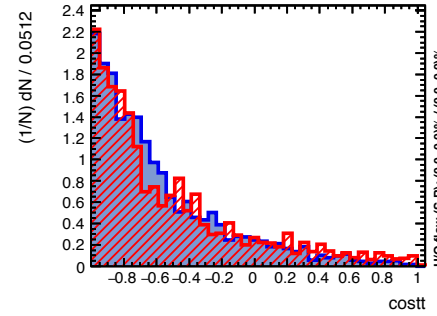
Input variable: cosHH\_reco



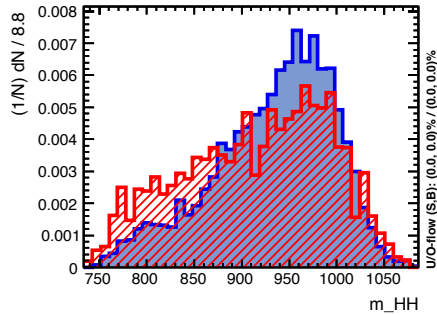
Input variable: cosThetabb



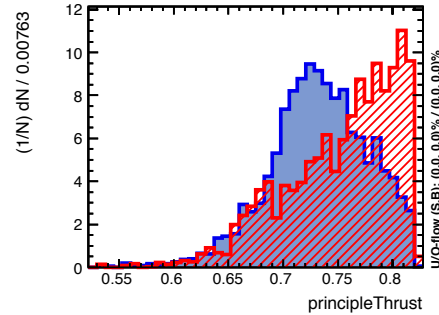
Input variable: costt



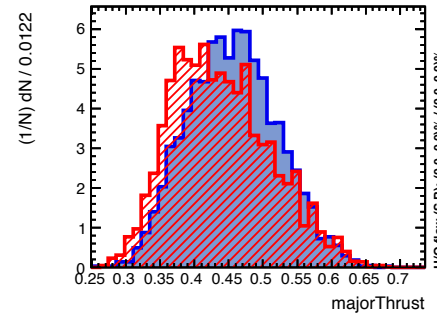
Input variable: m\_HH



Input variable: principleThrust

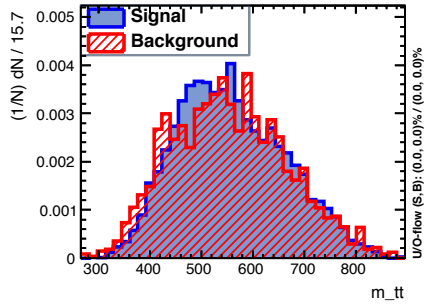


Input variable: majorThrust

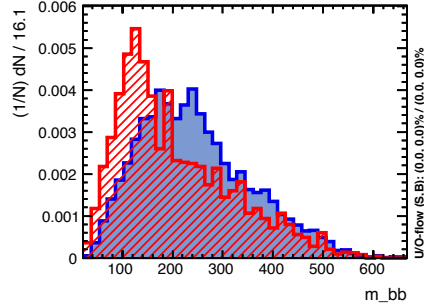


# Boosted Decision Tree

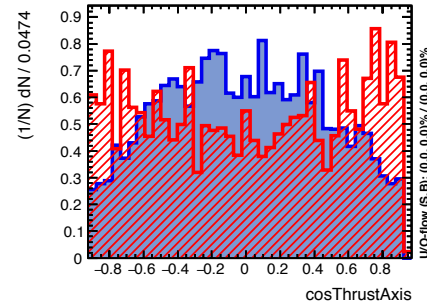
Input variable: m\_tt



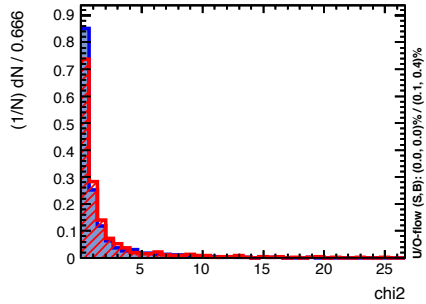
Input variable: m\_bb



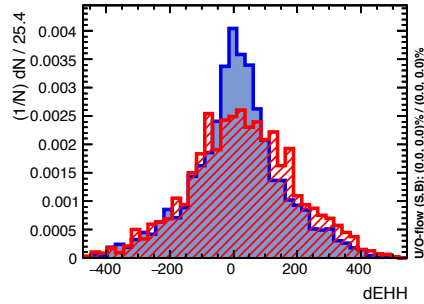
Input variable: cosThrustAxis



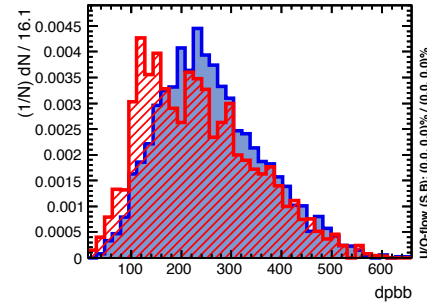
Input variable: chi2



Input variable: dEHH

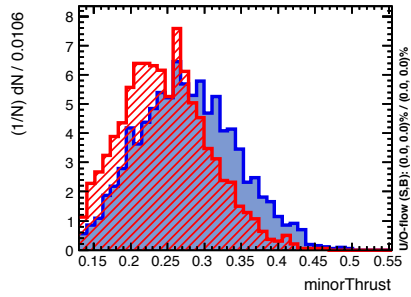


Input variable: dpbb

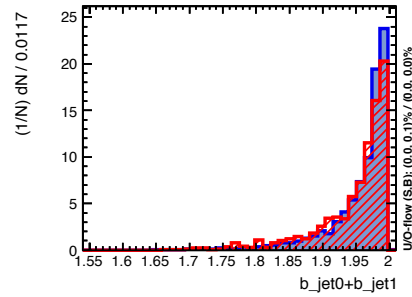


# Boosted Decision Tree

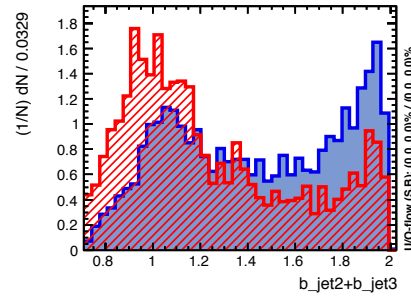
Input variable: minorThrust



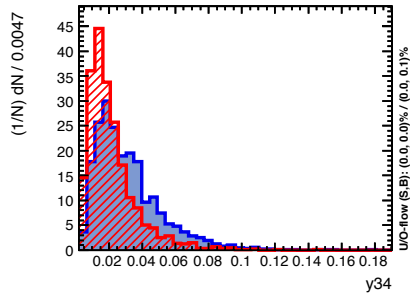
Input variable: b\_jet0+b\_jet1



Input variable: b\_jet2+b\_jet3

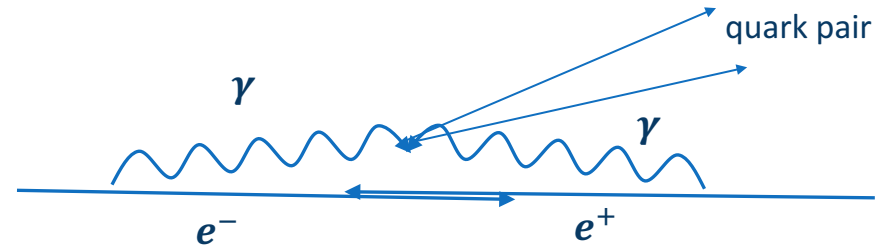


Input variable: y34



## Analysis Strategy – Beam Background

- In average 2.7 beam background events per bunch crossing
- In these samples old number of 4.1 events per bunch crossing
- Has major influence on jet clustering
- Use kt-algorithm from fastjet package to reduce background
  - R: Generalized radius of jets
  - Vary R to optimal mass resolution
- Use Satoru Jetfinder for clustering



# Fastjet Finder – kt Algorithm (beam background removal)

- Calculate the distance between to all tracks

$$d_{ij} = \min(p_{Ti}^2, p_{Tj}^2) \frac{\Delta R_{ij}}{R}$$

with  $\Delta R_{ij} = (\eta_i - \eta_j)^2 + (\phi_i - \phi_j)^2$

$\eta$  pseudo rapidity,  $\phi$  azimuth

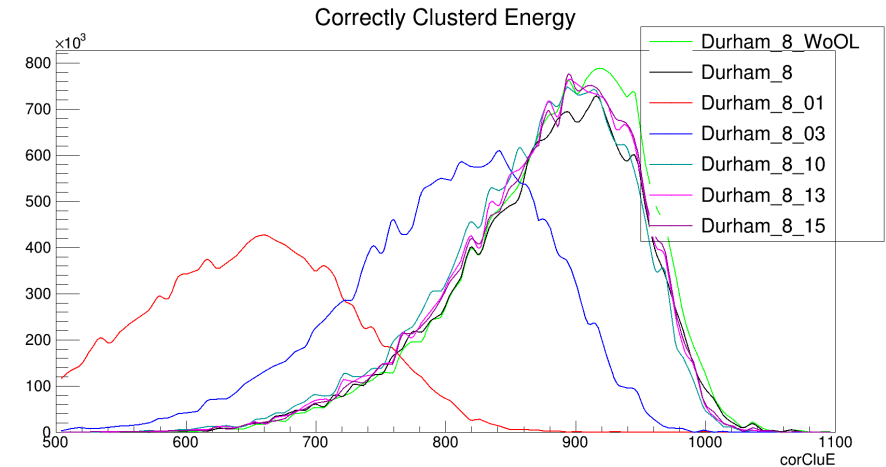
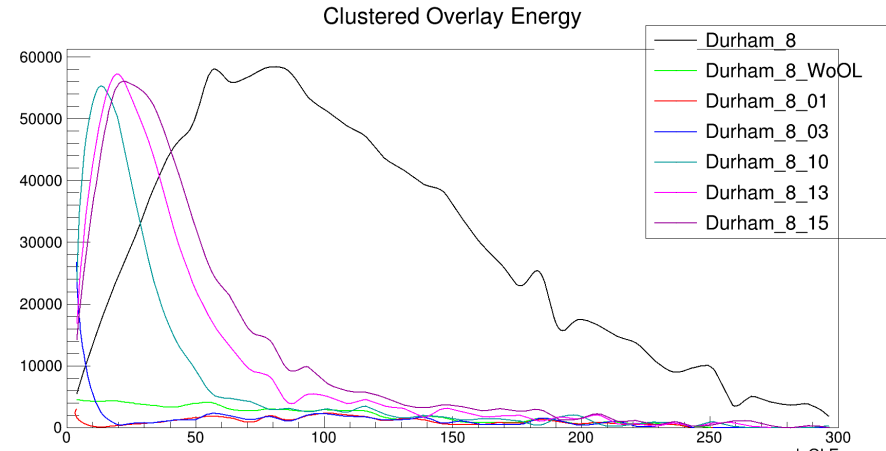
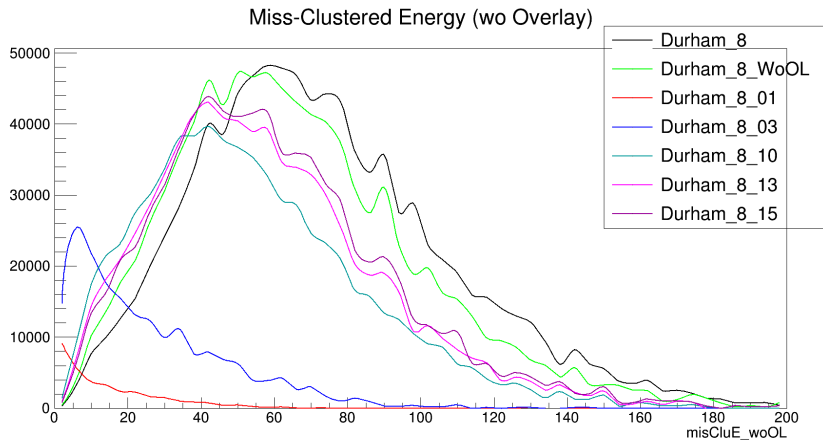
- Find smallest  $d_{ij}$
- If  $d_{ij} < d_{iB} = p_{Ti}^2$  merge tracks, if not remove Track (B: Beam)
  - Remove particles that are closer to the beam than to the closest track
- Continue to step one until there are only the requested number of jets

## Choose R for kt algorithm

Durham\_8: w/o correction

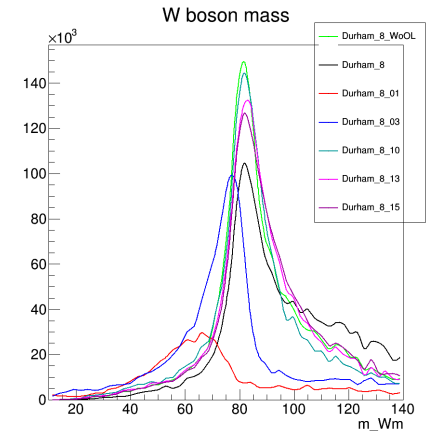
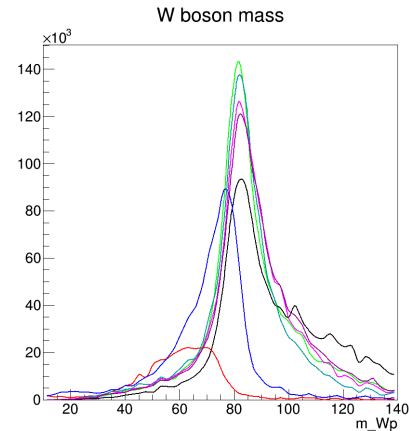
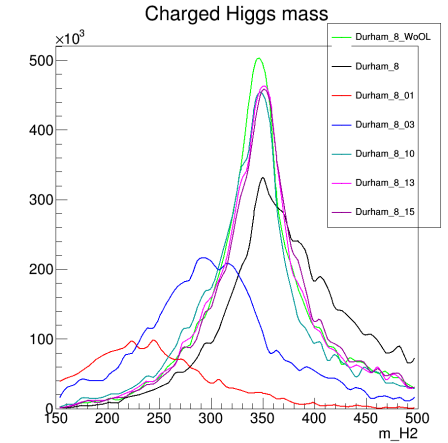
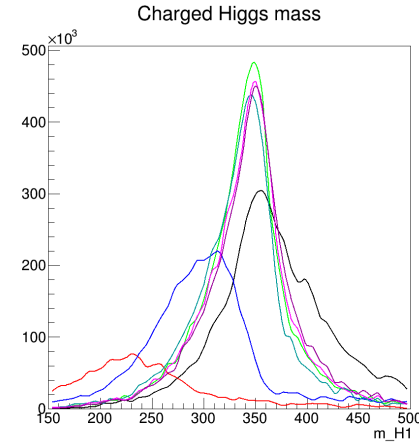
Durham\_8\_WoOL: overlay removed  
by generator information

Durham\_8\_13:  $R = 1.3$

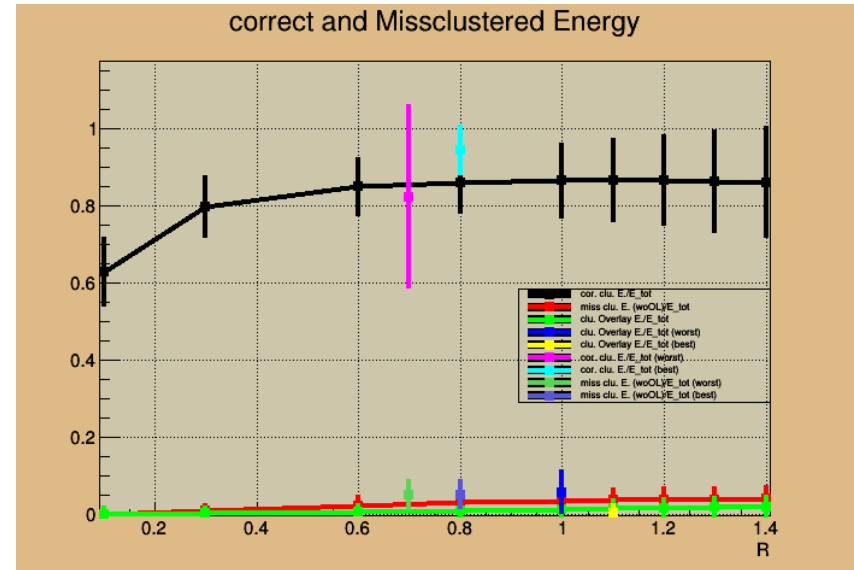
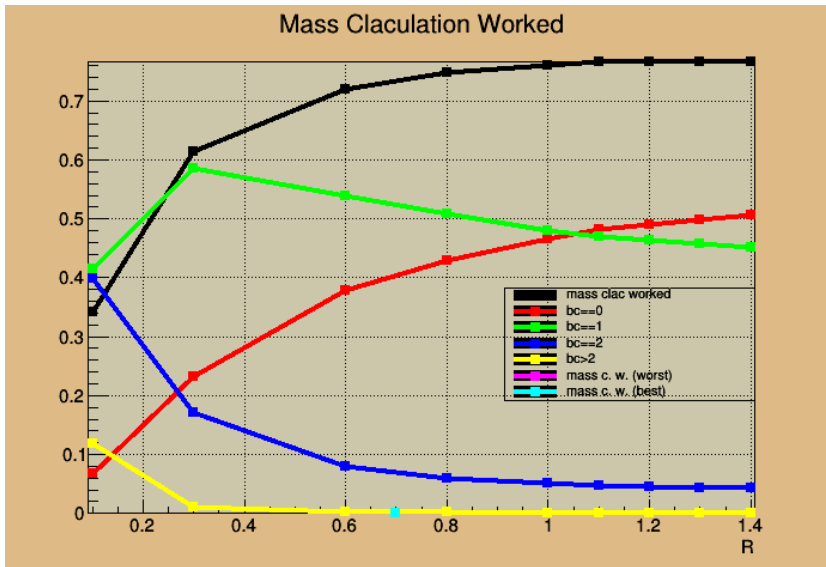


## Choose R for kt algorithm

- For W mass R = 1.0 seems best
- For H mass R = 1.3 seems best
- Maybe b-jets have a wider spread
- I will continue with 1.3







# Analysis Strategy - Chi<sup>2</sup>

- Choose  $\sigma$  from pairing with generator information
- Optimize for  $c$  for maximal pairing efficiency

$$\chi^2 = c_H \left| \frac{(m_{j_1 j_2 j_3 j_4})^2 - (m_{j_5 j_6 j_7 j_8})^2}{2\sigma_{H^+}^2} \right| + c_t \left( \frac{m_{j_2 j_3 j_4} - M_t}{\sigma_t} \right)^2$$
$$+ c_t \left( \frac{m_{j_6 j_7 j_8} - M_t}{\sigma_t} \right)^2 + c_w \left( \frac{m_{j_3 j_4} - M_W}{\sigma_W} \right)^2 + c_w \left( \frac{m_{j_7 j_8} - M_W}{\sigma_W} \right)^2$$

$$\sigma_H = \sigma_t = 80 \text{ GeV}, \quad \sigma_W = 48 \text{ GeV}$$

# Analysis Strategy - Chi<sup>2</sup>

- Choose  $\sigma$  from pairing with generator information
- Optimize for  $c$  for maximal pairing efficiency

$$\begin{aligned} \chi^2 = & c_H \left| \frac{(m_{j_1 j_2 j_3 j_4})^2 - (m_{j_5 j_6 j_7 j_8})^2}{2\sigma_{H^+}^2} \right| + c_t \left( \frac{m_{j_2 j_3 j_4} - M_t}{\sigma_t} \right)^2 \\ & + c_t \left( \frac{m_{j_6 j_7 j_8} - M_t}{\sigma_t} \right)^2 + c_w \left( \frac{m_{j_3 j_4} - M_W}{\sigma_W} \right)^2 + c_w \left( \frac{m_{j_7 j_8} - M_W}{\sigma_W} \right)^2 \\ & + c_{\cos \theta_{HH}} \left( \frac{1 - \cos \theta_{HH}}{\sigma_{\cos \theta_{HH}}} \right)^2 + c_{\theta_{HH}} \left( \frac{\theta_{HH}}{\sigma_{\theta_{HH}}} \right)^2 + c_E \left( \frac{E_{H^-} - E_{H^+}}{\sigma_E} \right)^2 + c_p \left( \frac{\vec{p} - \vec{p}_{H^+}}{\sigma_p} \right)^2 \end{aligned}$$

# Analysis Strategy - Chi<sup>2</sup>

- First test optimization for c\_H and c\_cos
- c\_H ~ 0.2 / c\_cos ~ 30 (σ\_cos = 1)
- Pairing efficiency 25 -> 27.5 %

$$\begin{aligned}\chi^2 = & c_H \left| \frac{(m_{j_1 j_2 j_3 j_4})^2 - (m_{j_5 j_6 j_7 j_8})^2}{2\sigma_{H^+}^2} \right| + c_t \left( \frac{m_{j_2 j_3 j_4} - M_t}{\sigma_t} \right)^2 \\ & + c_t \left( \frac{m_{j_6 j_7 j_8} - M_t}{\sigma_t} \right)^2 + c_w \left( \frac{m_{j_3 j_4} - M_W}{\sigma_W} \right)^2 + c_w \left( \frac{m_{j_7 j_8} - M_W}{\sigma_W} \right)^2 \\ & + c_{\cos \theta_{HH}} \left( \frac{1 - \cos \theta_{HH}}{\sigma_{\cos \theta_{HH}}} \right)^2\end{aligned}$$

# Analysis Strategy - $\chi^2$

