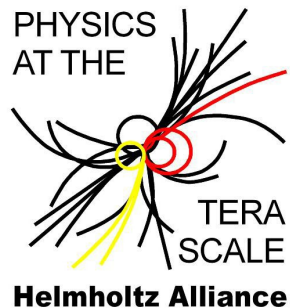




Track reconstruction of GridPix data

Amir Noori Shirazi
Siegen University

LCTPC Collaboration Meeting
30 November 2017
DESY



Bundesministerium
für Bildung
und Forschung

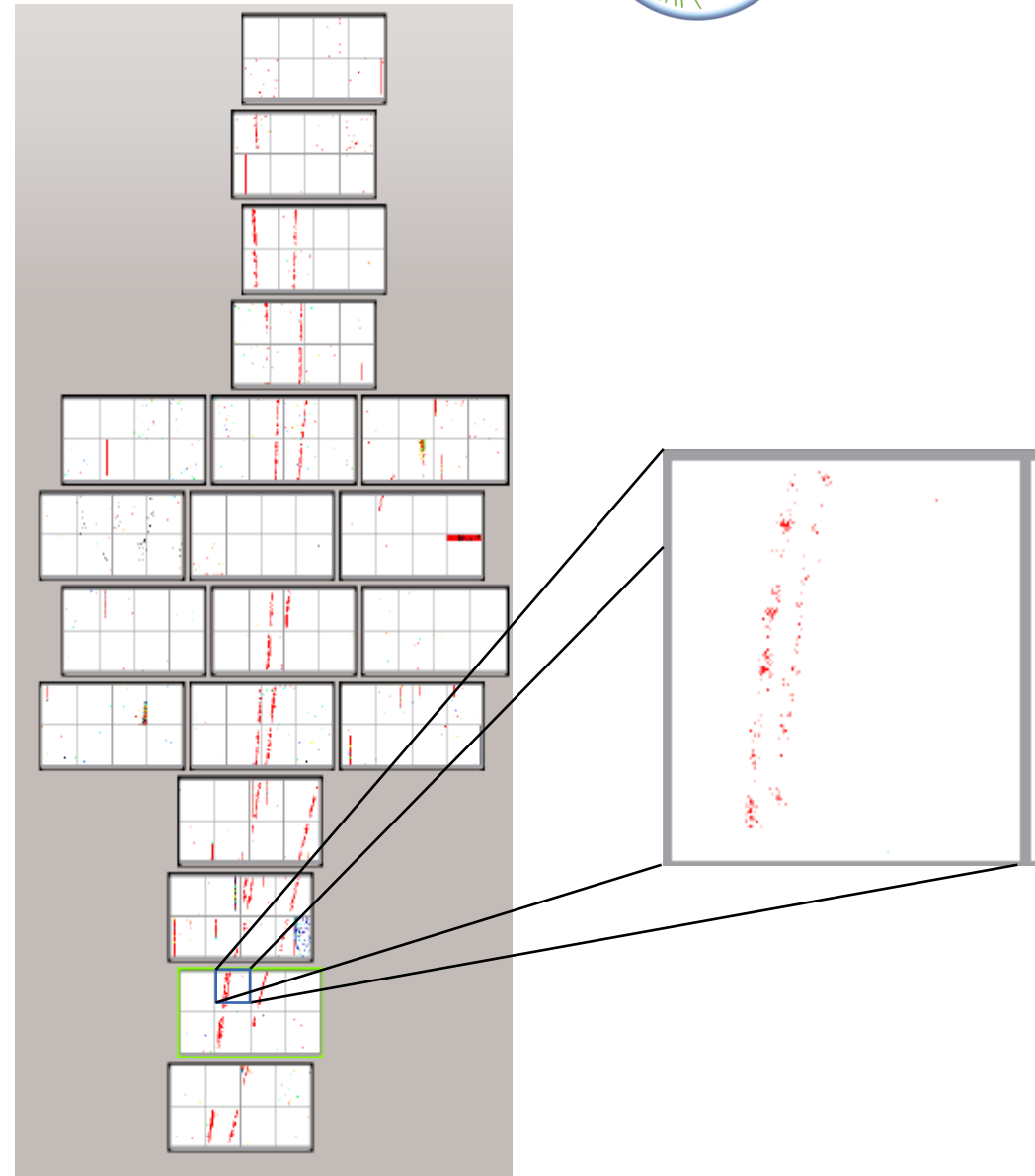
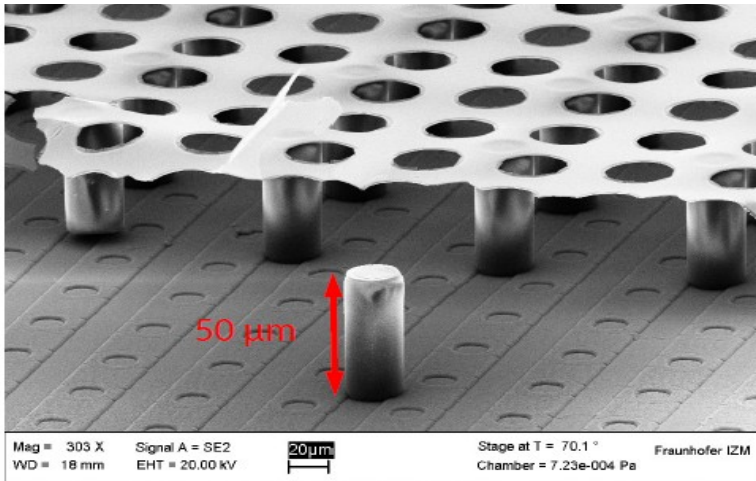


Timepix:

- Number of pixels: 256 X 256 pixels
- Pixel size: 55 X 55 μm^2

InGrid:

- Micromegas on top of a Timepix chip
- Mesh holes aligned with pixels of the chip:
 - single e^- measurement
- Many hits per track's length ≈ 10 hits per mm
- Every 8 InGrid chips are aligned in an Octoboard
- Using the unit of the Octoboard as a segment of the track calling tracklet



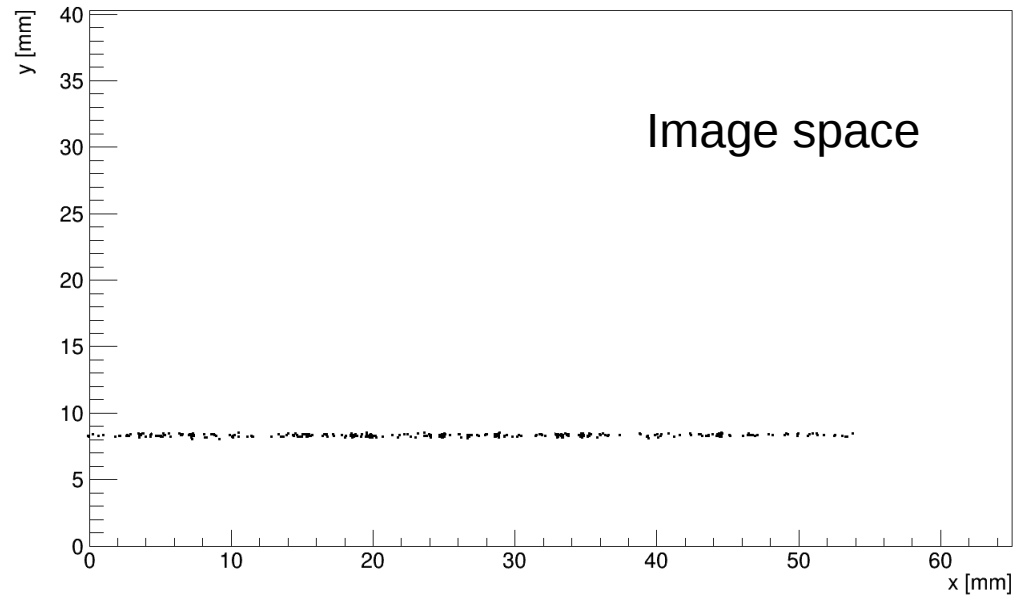
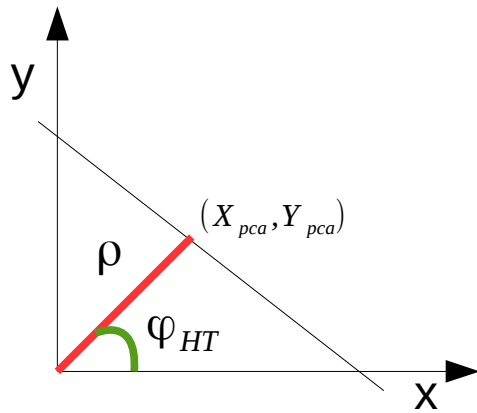
Hough Transform

- Bin with maximum entries returns φ_{HT} and ρ_{HT}

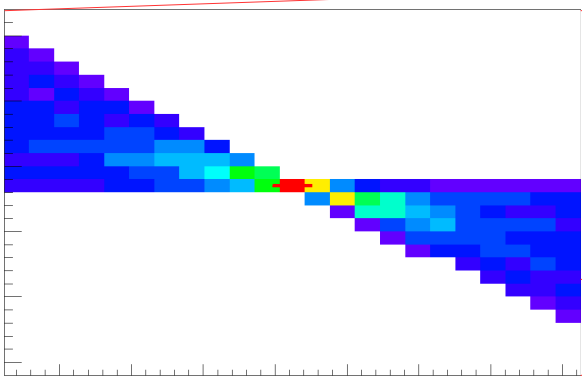
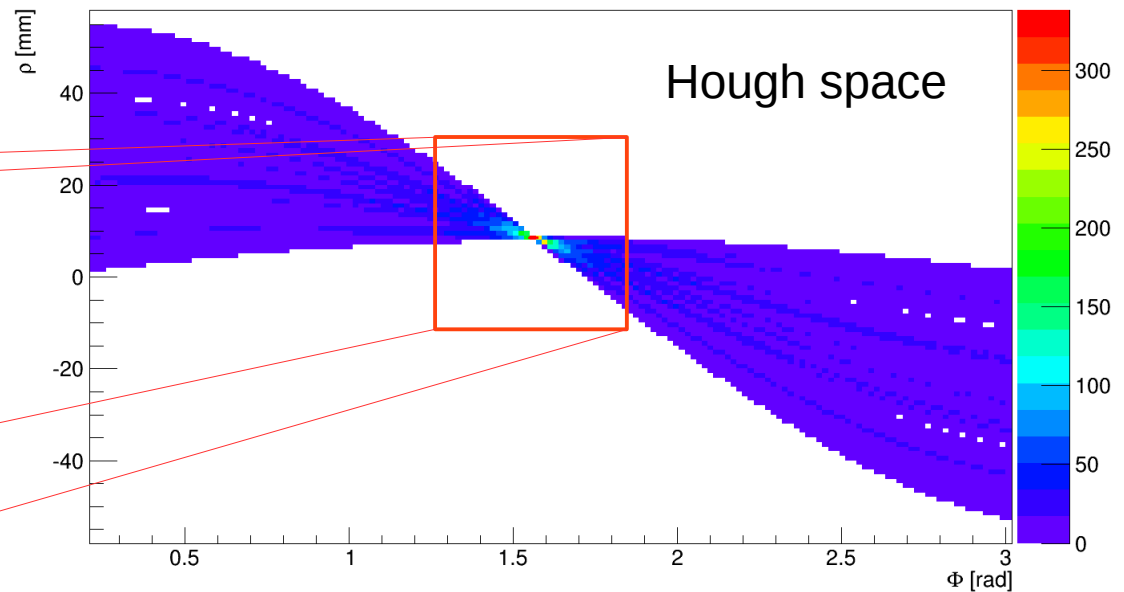
- $\rho_{HT} = x \cos(\varphi_{HT}) + y \sin(\varphi_{HT})$

- $d_0 = \rho_{HT}$

- $\varphi_{track} = \varphi_{HT} - \frac{\pi}{2}$



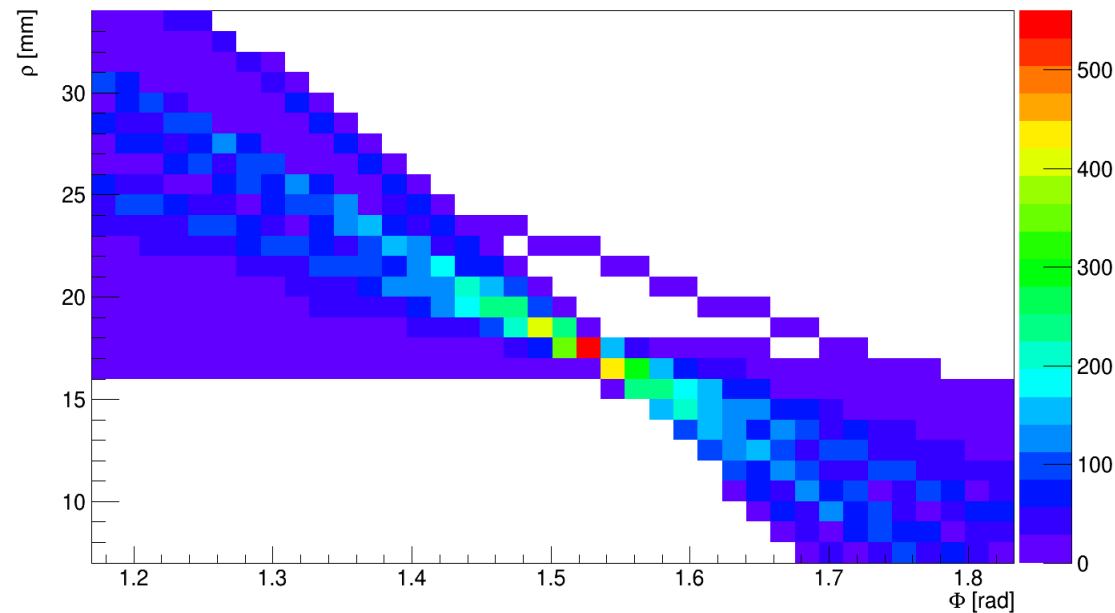
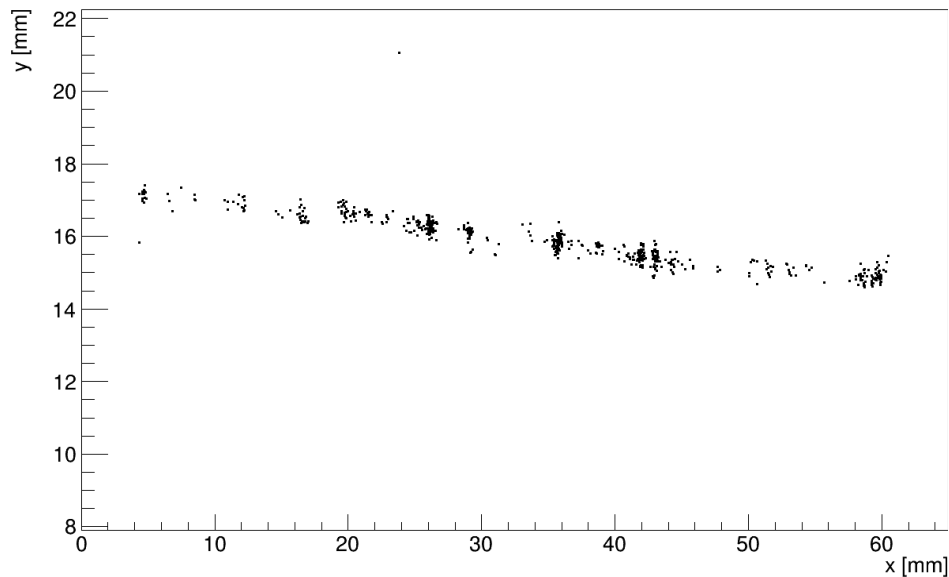
$$\rho = x \cos(\Phi) + y \sin(\Phi)$$



Hough Transform



- Bin size in the X-Y plane: in the ρ direction σ_D
- Bin Size in the S-Z plane: in the Z direction $2.355 \sigma_L$
- Because of the diffusion, some lines of hits pass through other bins around the bin with maximum entries.



- Calculating resolution of the track in Hough space
- Using Bivariate Normal Distribution for vicinity of the bin with maximum entries



Diffusion and covariance matrix:

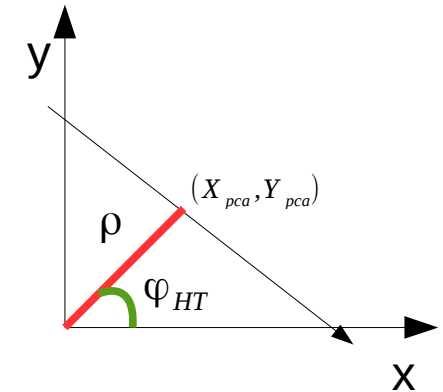
➤ X-Y Plane:

➤ Transverse resolution:

$$\begin{bmatrix} \sigma_{\rho}^2 & \sigma_{\rho\varphi} \\ \sigma_{\varphi\rho} & \sigma_{\varphi}^2 \end{bmatrix} = \nabla f \begin{bmatrix} \sigma_D^2 & 0 \\ 0 & \sigma_D^2 \end{bmatrix} \nabla f^T$$

$$\rho = x \cos(\varphi) + y \sin(\varphi)$$

$$\sigma_D^2 = ZD_T^2$$



➤ S-Z Plane:

➤ Longitudinal resolution:

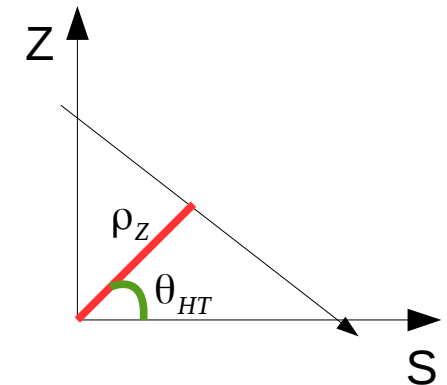
➤ Arc length for straight line:

$$\begin{bmatrix} \sigma_{\rho_z}^2 & \sigma_{\rho_z\theta} \\ \sigma_{\theta\rho_z} & \sigma_{\theta}^2 \end{bmatrix} = \nabla f \begin{bmatrix} \sigma_S^2 & 0 \\ 0 & \sigma_L^2 \end{bmatrix} \nabla f^T$$

$$\rho_z = s \cos(\theta_{HT}) + z \sin(\theta_{HT})$$

$$\sigma_L^2 = ZD_L^2$$

$$S = \sqrt{(x_{hit} - x_{pca})^2 + (y_{hit} - y_{pca})^2}$$



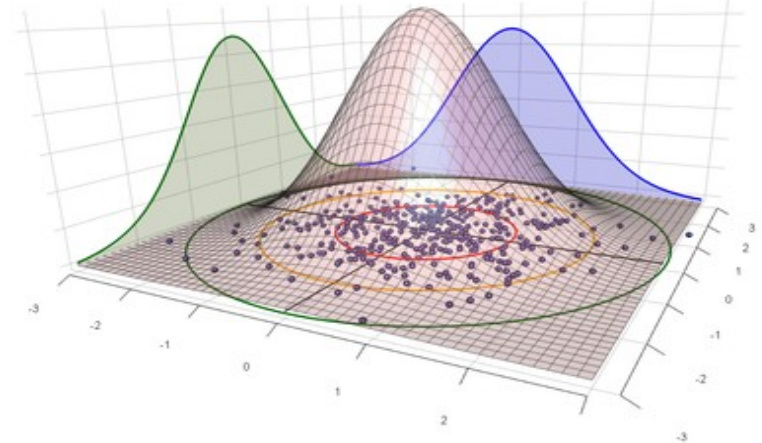
Bivariate Normal Distribution (BND):

$$G(\varphi, \rho) = \frac{1}{2\pi\sigma_\rho\sigma_\varphi\sqrt{1-r^2}} \exp\left[\frac{-c}{2(1-r^2)}\right]$$

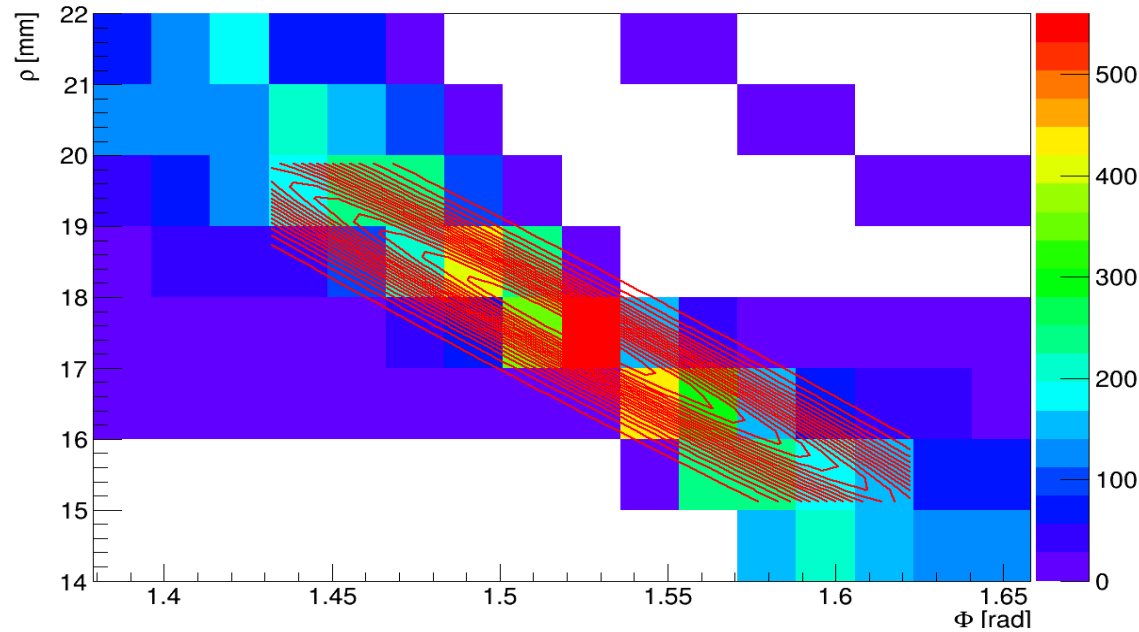
$$c \equiv \frac{(\varphi - \mu_\varphi)^2}{\sigma_\varphi^2} + \frac{(\rho - \mu_\rho)^2}{\sigma_\rho^2} - \frac{2r(\varphi - \mu_\varphi)(\rho - \mu_\rho)}{\sigma_\varphi\sigma_\rho}$$

Correlation :

$$r \equiv \frac{\sigma_{\rho\varphi}}{\sigma_\rho\sigma_\varphi}$$



http://ballistipedia.com/index.php?title=Closed_Form_Precision



Ellipse: minor and major axes



Ellipse equation of 1/e of Peak of BND:

- Finding ellipse equation from BND:

$$1 = \frac{(\varphi - \mu_\varphi)^2}{q \sigma_\varphi^2} + \frac{(\rho - \mu_\rho)^2}{q \sigma_\rho^2} - \frac{2r(\varphi - \mu_\varphi)(\rho - \mu_\rho)}{q \sigma_\varphi \sigma_\rho} \quad (1)$$

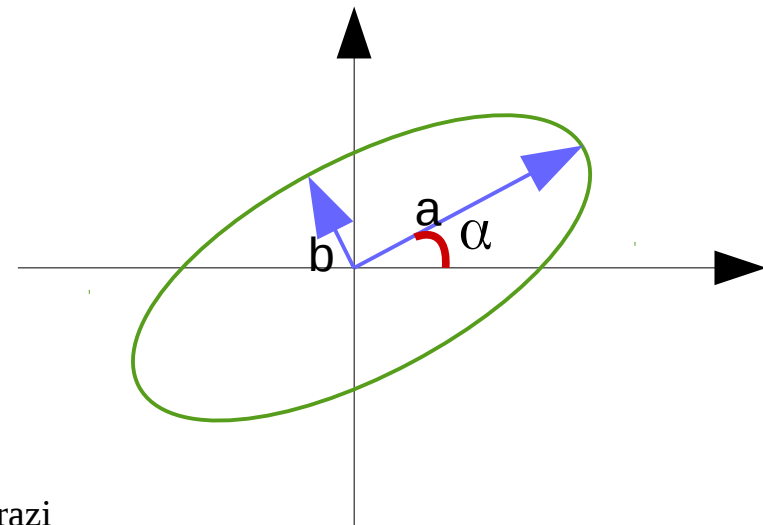
- Rotated ellipse:

$$1 = \left(\frac{\cos^2(\alpha)}{a^2} + \frac{\sin^2(\alpha)}{b^2} \right) x^2 - 2 \cos(\alpha) \sin(\alpha) \left(\frac{1}{a^2} - \frac{1}{b^2} \right) xy + \left(\frac{\sin^2(\alpha)}{a^2} + \frac{\cos^2(\alpha)}{b^2} \right) y^2 \quad (2)$$

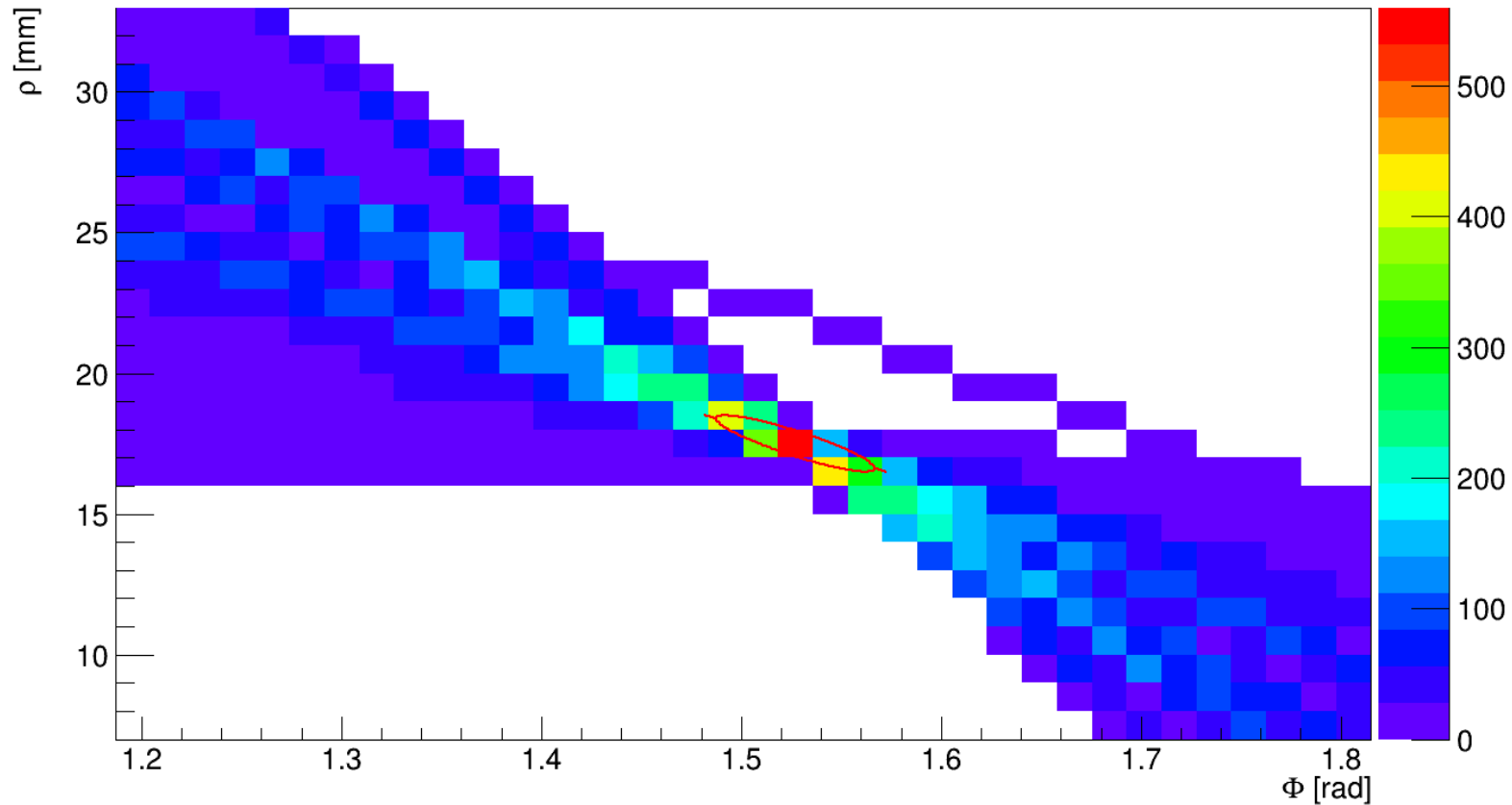
- From (1) and (2):

$$a^2 = \frac{q \sigma_\varphi^2 \sigma_\rho^2 \cos(2\alpha)}{\sigma_\rho^2 \cos^2(\alpha) - \sigma_\varphi^2 \sin^2(\alpha)}$$

$$b^2 = \frac{-q \sigma_\varphi^2 \sigma_\rho^2 \cos(2\alpha)}{\sigma_\rho^2 \sin^2(\alpha) - \sigma_\varphi^2 \cos^2(\alpha)}$$

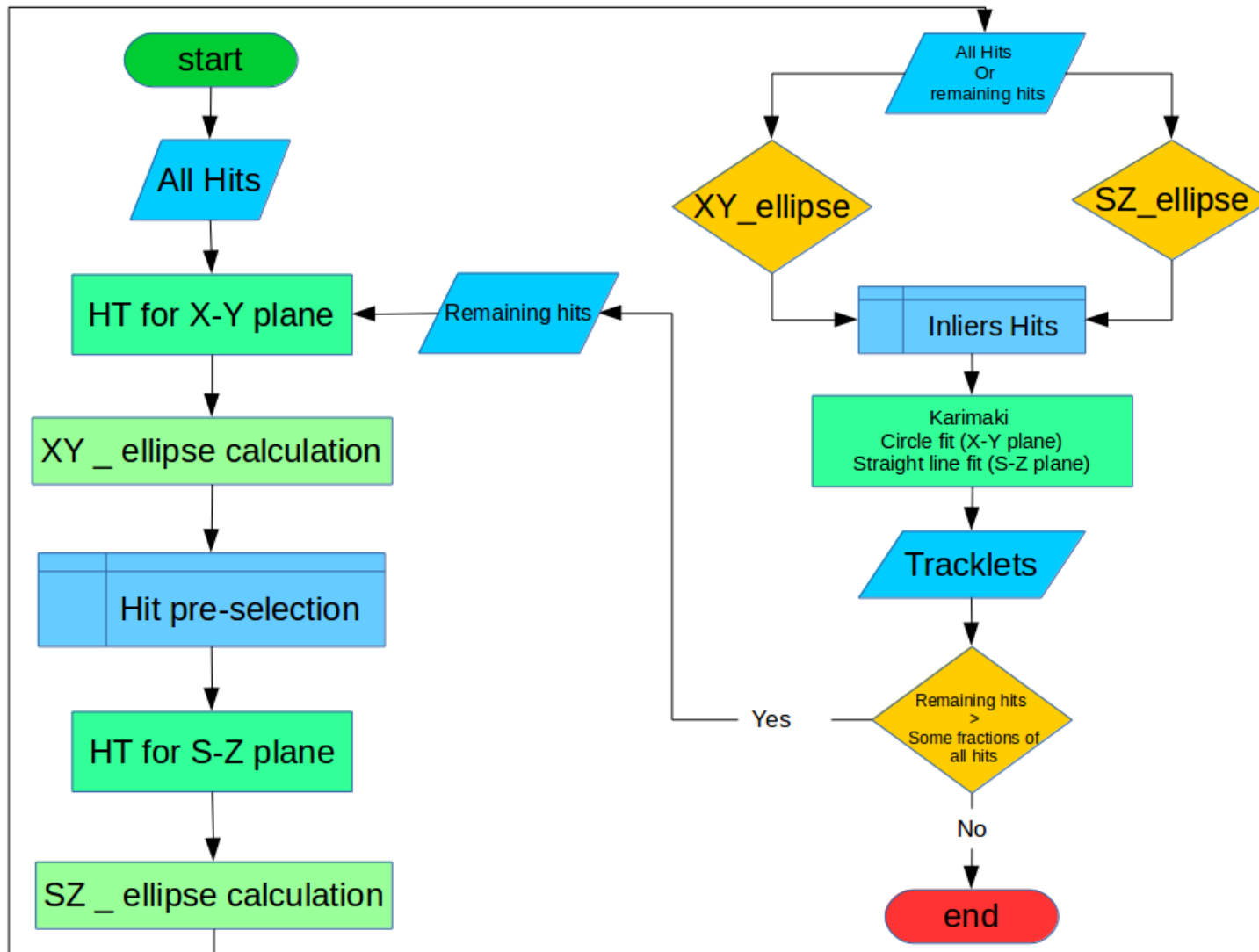


Inliers and 1/e of peak of BND:



- Collecting all hits inside the ellipse => **Inliers**
- The fit range and the size of the ellipse are changeable => Number of inliers is changeable too
- They are adjusted automatically based on the drift length.

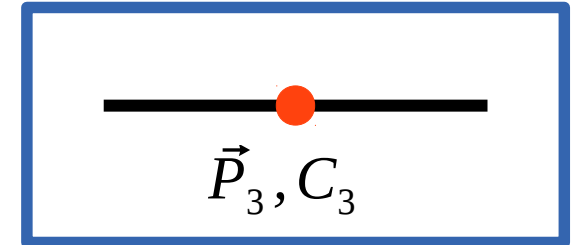
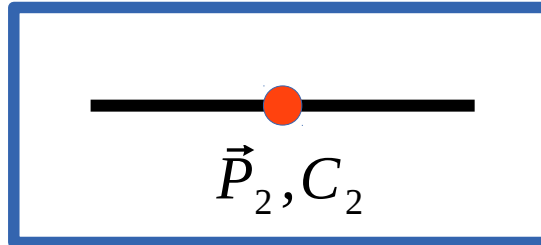
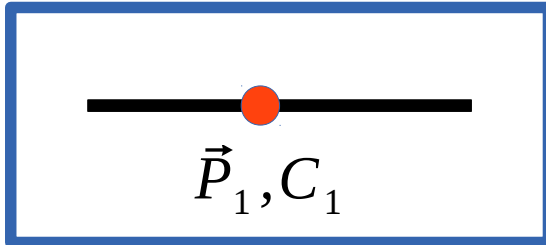
Flow chart



Merging Tracklets



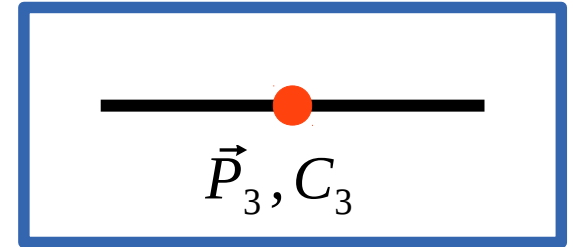
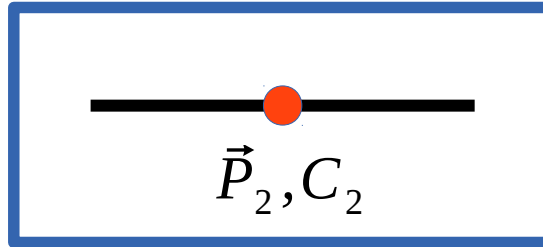
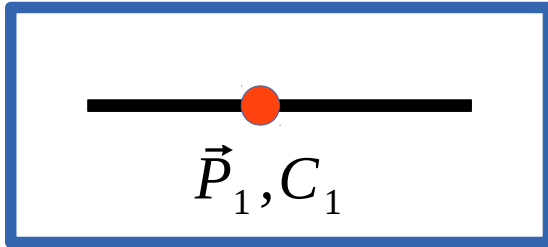
P: parameter vector of the tracklet
C: covariance Matrix of the tracklet



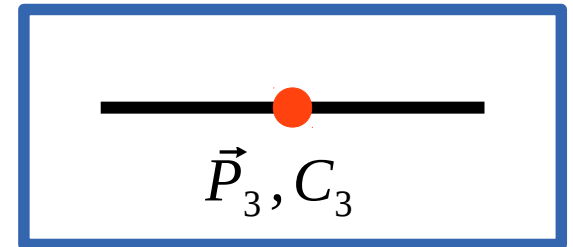
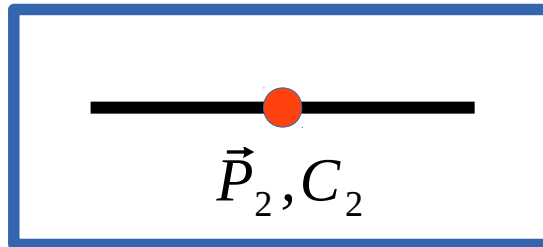
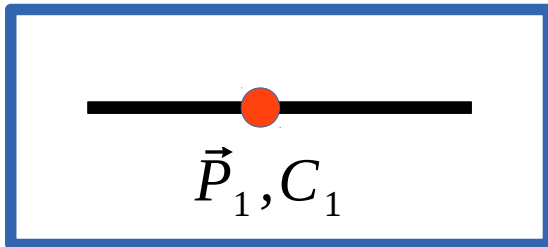
Merging Tracklets



$$(\vec{P}'_1, C'_1)(\vec{P}'_2, C'_2)$$

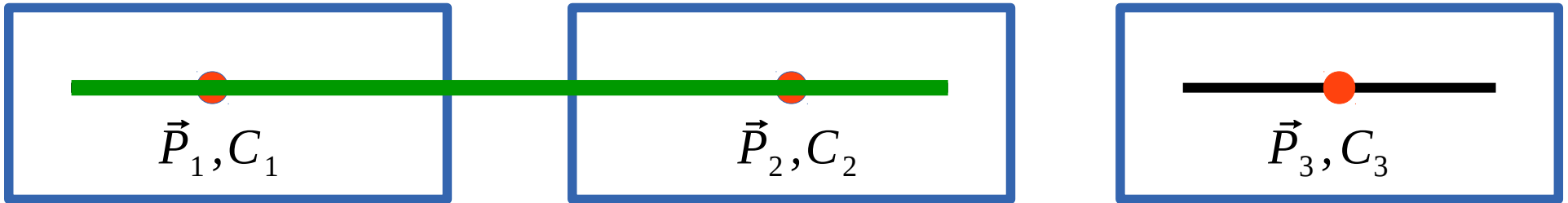


$$(\vec{P}'_1, C'_1)(\vec{P}'_2, C'_2)$$



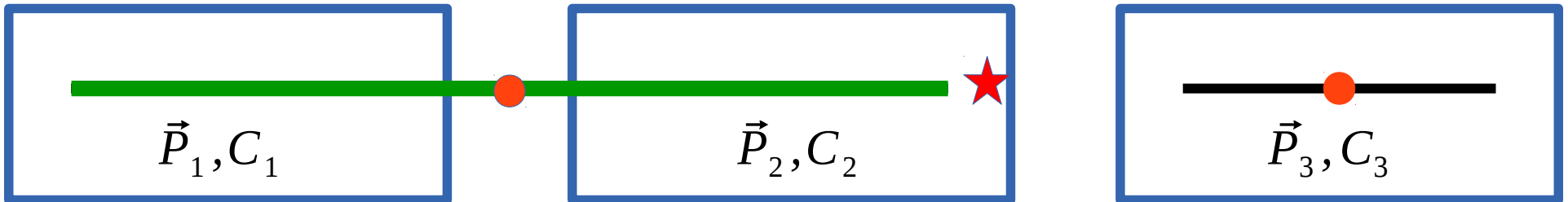
$$\chi_1^2 = (\vec{P}'_1 - \vec{P}'_2)(C'_1 + C'_2)^{-1}(\vec{P}'_1 - \vec{P}'_2)^T$$

$$(\vec{P}'_1, C'_1)(\vec{P}'_2, C'_2)$$



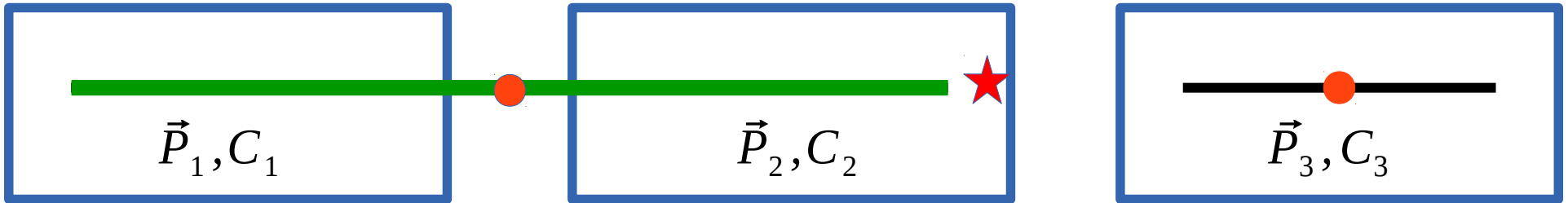
$$\chi_1^2 = (\vec{P}'_1 - \vec{P}'_2)(C'_1 + C'_2)^{-1}(\vec{P}'_1 - \vec{P}'_2)^T \Rightarrow (\vec{P}_{12}, C_{12})$$

$$(\vec{P}'_1, C'_1)(\vec{P}'_2, C'_2) \quad (\vec{P}'_{12}, C'_{12})(\vec{P}'_3, C'_3)$$



$$\chi_1^2 = (\vec{P}'_1 - \vec{P}'_2)(C'_1 + C'_2)^{-1}(\vec{P}'_1 - \vec{P}'_2)^T \Rightarrow (\vec{P}_{12}, C_{12})$$

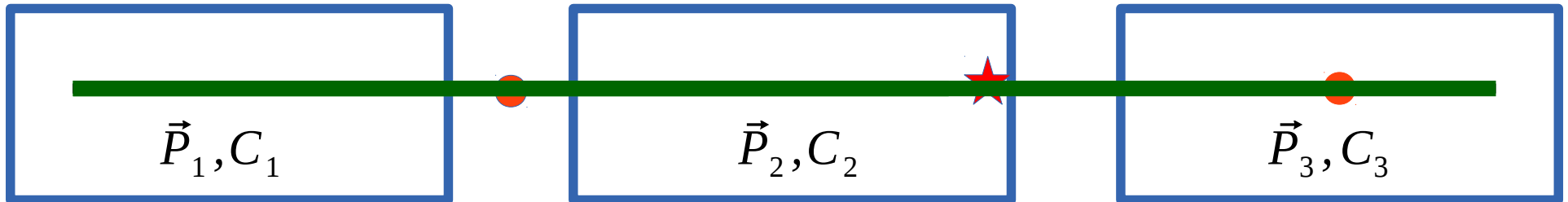
$$(\vec{P}'_1, C'_1)(\vec{P}'_2, C'_2) \quad (\vec{P}'_{12}, C'_{12})(\vec{P}'_3, C'_3)$$



$$\chi_1^2 = (\vec{P}'_1 - \vec{P}'_2)(C'_1 + C'_2)^{-1}(\vec{P}'_1 - \vec{P}'_2)^T \Rightarrow (\vec{P}_{12}, C_{12})$$

$$\chi_2^2 = (\vec{P}'_{12} - \vec{P}'_3)(C'_{12} + C'_3)^{-1}(\vec{P}'_{12} - \vec{P}'_3)^T$$

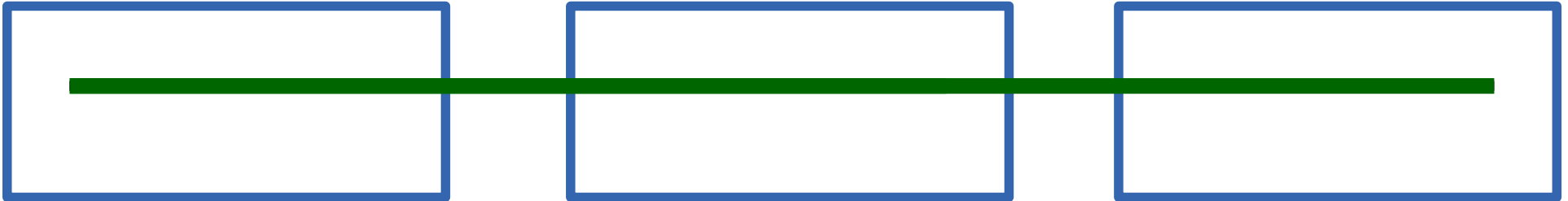
$$(\vec{P}'_1, C'_1)(\vec{P}'_2, C'_2) \quad (\vec{P}'_{12}, C'_{12})(\vec{P}'_3, C'_3)$$



$$\chi_1^2 = (\vec{P}'_1 - \vec{P}'_2)(C'_1 + C'_2)^{-1}(\vec{P}'_1 - \vec{P}'_2)^T \Rightarrow (\vec{P}_{12}, C_{12})$$

$$\chi_2^2 = (\vec{P}'_{12} - \vec{P}'_3)(C'_{12} + C'_3)^{-1}(\vec{P}'_{12} - \vec{P}'_3)^T \Rightarrow (\vec{P}_T, C_T)$$

$$(\vec{P}'_1, C'_1)(\vec{P}'_2, C'_2) \quad (\vec{P}'_{12}, C'_{12})(\vec{P}'_3, C'_3)$$

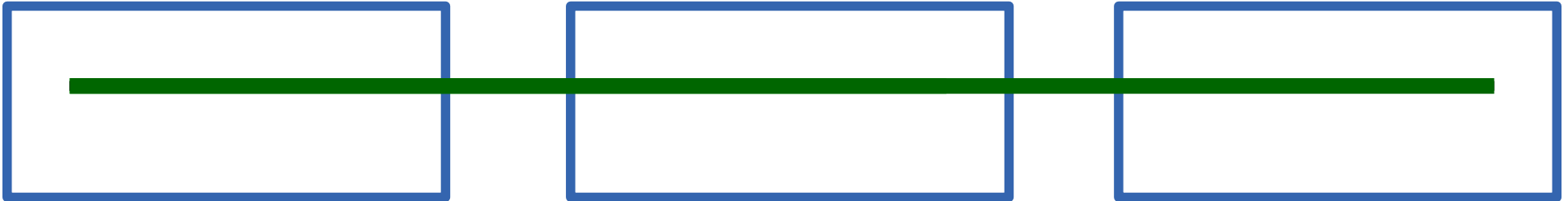


$$\chi_1^2 = (\vec{P}'_1 - \vec{P}'_2)(C'_1 + C'_2)^{-1}(\vec{P}'_1 - \vec{P}'_2)^T \Rightarrow (\vec{P}_{12}, C_{12})$$

$$\chi_2^2 = (\vec{P}'_{12} - \vec{P}'_3)(C'_{12} + C'_3)^{-1}(\vec{P}'_{12} - \vec{P}'_3)^T \Rightarrow (\vec{P}_T, C_T)$$

- Using General Broken lines (GBL) for fitting

$$(\vec{P}'_1, C'_1)(\vec{P}'_2, C'_2) \quad (\vec{P}'_{12}, C'_{12})(\vec{P}'_3, C'_3)$$

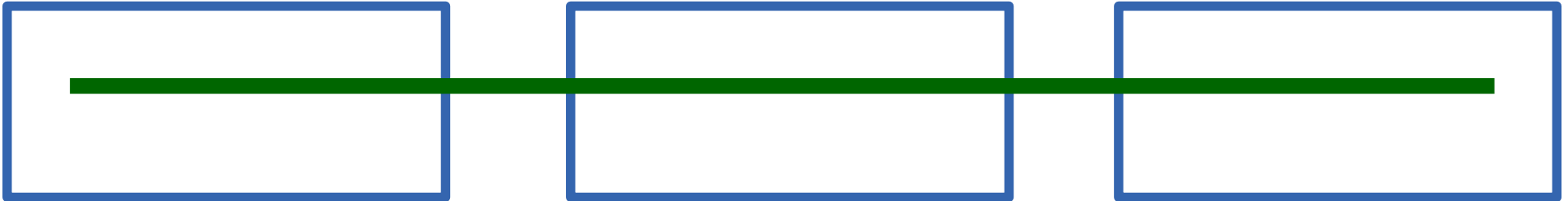


$$\chi_1^2 = (\vec{P}'_1 - \vec{P}'_2)(C'_1 + C'_2)^{-1}(\vec{P}'_1 - \vec{P}'_2)^T \Rightarrow (\vec{P}_{12}, C_{12})$$

$$\chi_2^2 = (\vec{P}'_{12} - \vec{P}'_3)(C'_{12} + C'_3)^{-1}(\vec{P}'_{12} - \vec{P}'_3)^T \Rightarrow (\vec{P}_T, C_T)$$

- Using General Broken lines (GBL) for fitting
- Recollection remaining hits

$$(\vec{P}'_1, C'_1)(\vec{P}'_2, C'_2) \quad (\vec{P}'_{12}, C'_{12})(\vec{P}'_3, C'_3)$$



$$\chi_1^2 = (\vec{P}'_1 - \vec{P}'_2)(C'_1 + C'_2)^{-1}(\vec{P}'_1 - \vec{P}'_2)^T \Rightarrow (\vec{P}_{12}, C_{12})$$

$$\chi_2^2 = (\vec{P}'_{12} - \vec{P}'_3)(C'_{12} + C'_3)^{-1}(\vec{P}'_{12} - \vec{P}'_3)^T \Rightarrow (\vec{P}_T, C_T)$$

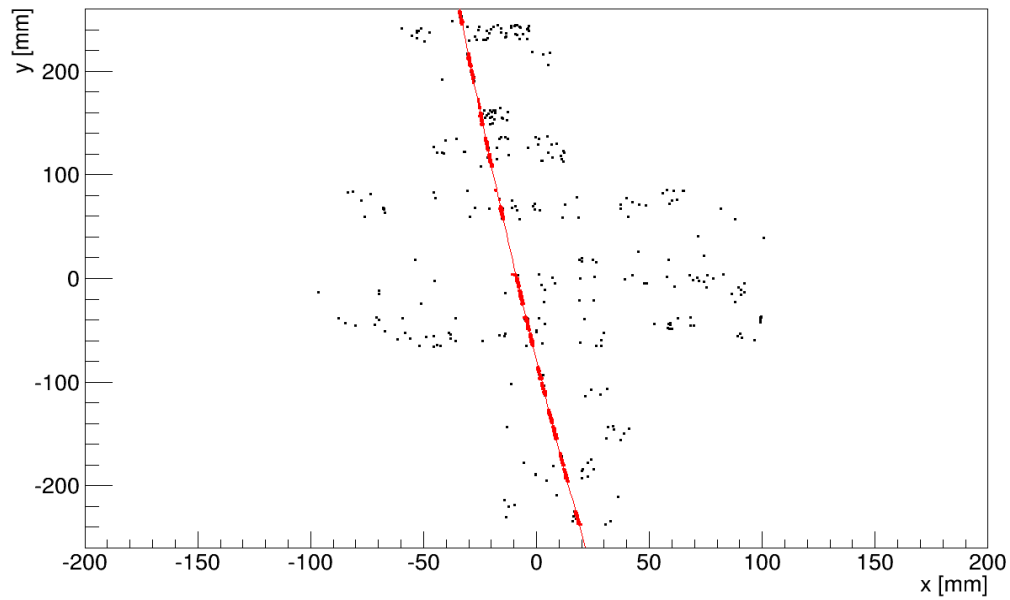
- Using General Broken lines (GBL) for fitting
- Recollection remaining hits
- Using GBL again for the final fit

Testbeam data 2015

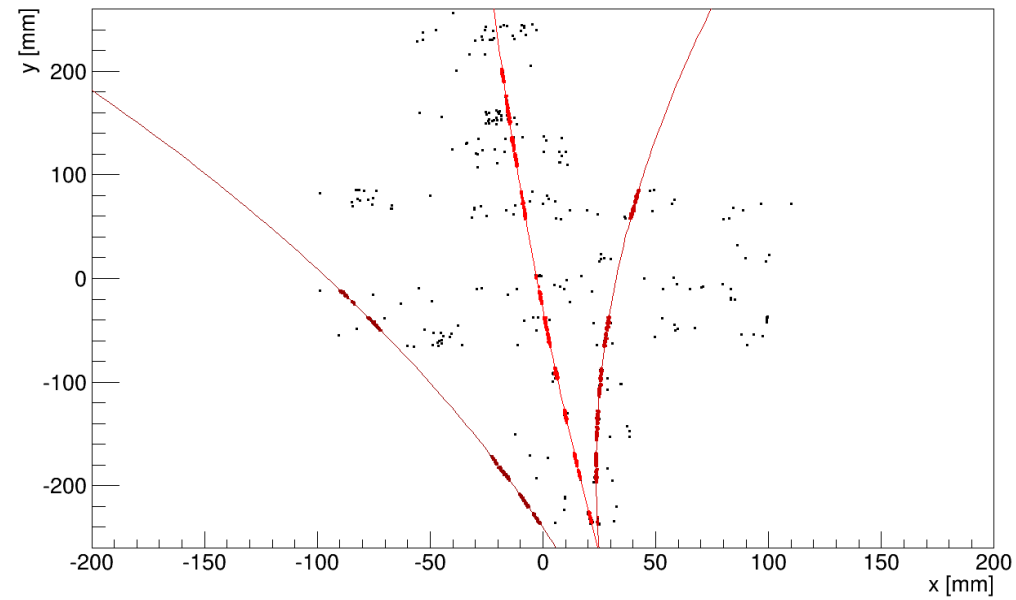


- Run_136
- $B = 1T$
- 5 GeV

Event_2_Drawing_1_Tracks_3036_Hits



Event_39_Drawing_3_Tracks_5819_Hits

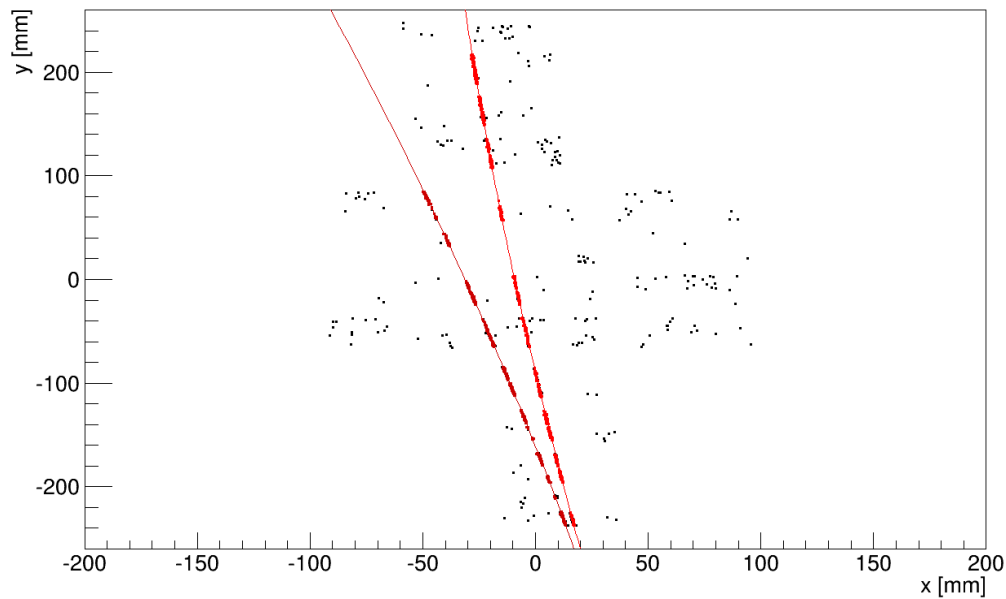


Testbeam data 2015

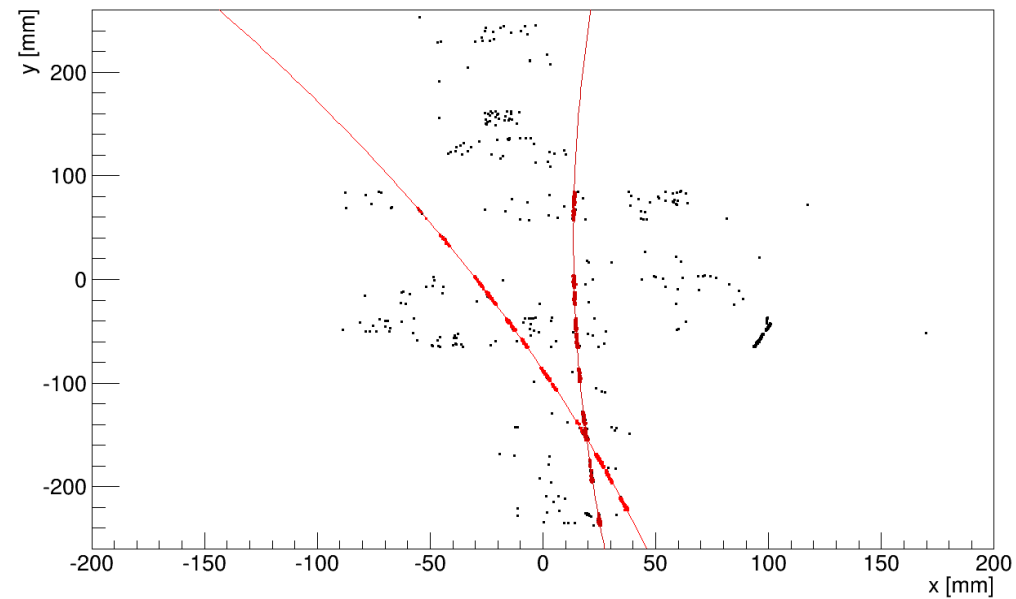


- Run_136
- $B = 1T$
- 5 GeV

Event_72_Drawing_2_Tracks_4739_Hits

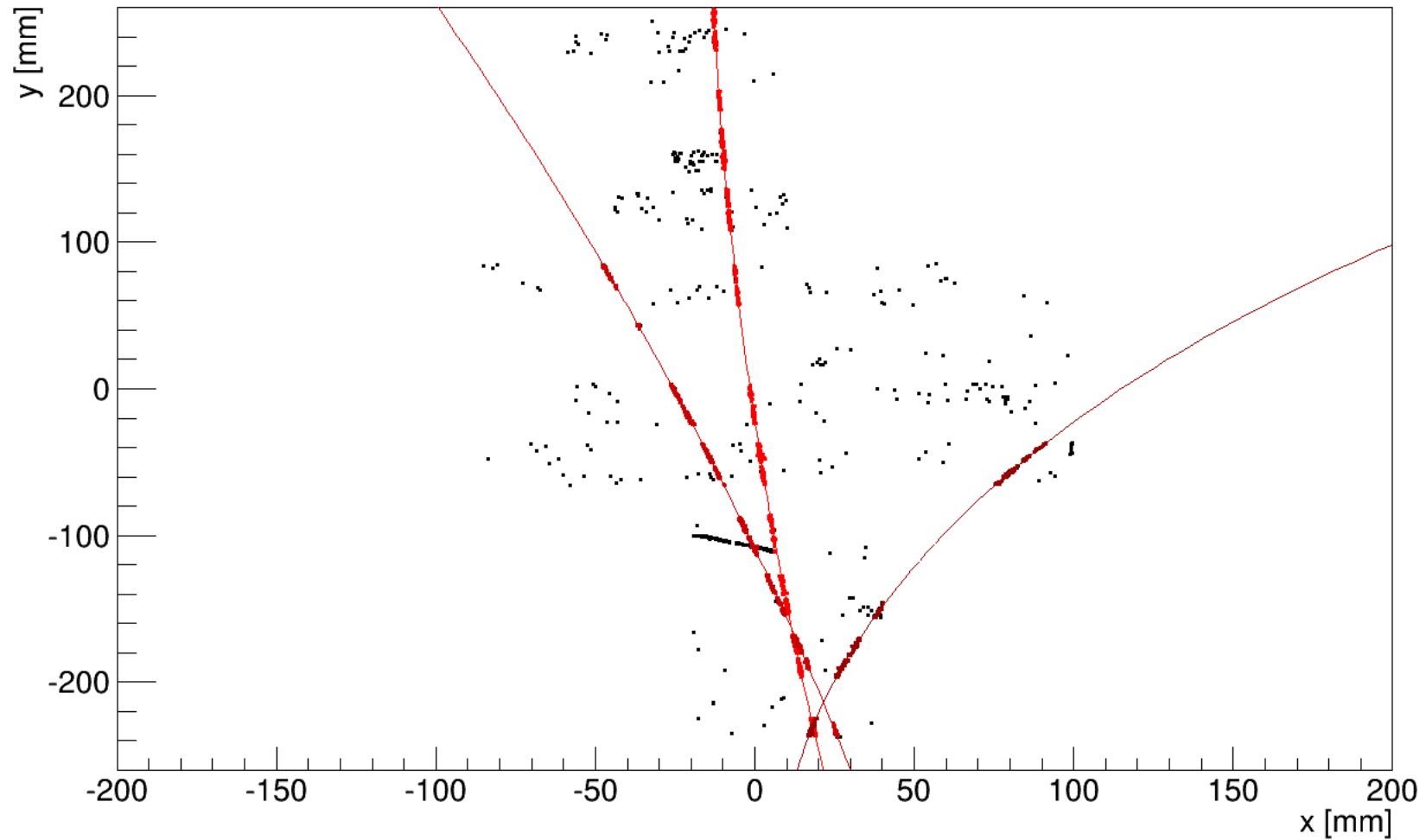


Event_43_Drawing_2_Tracks_4167_Hits



- Run_136
- $B = 1T$
- 5 GeV

Event_9_Drawing_3_Tracks_6572_Hits

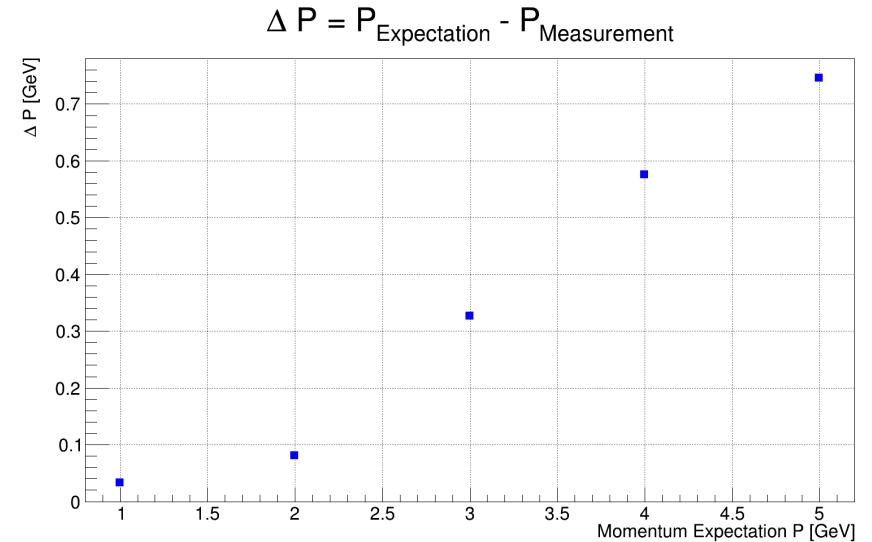




- Transverse Momentum Resolution:

$$\frac{\sigma_{P_t}}{P_t^2}$$

- Transverse Momentum for Real data
- Each run: **10000** events
- Plot $1/P_t$ and using Crystal Ball function for fit
- $P_t=1$ / Mean of fit
- Momentum Resolution= σ of fit



Run	Energy (GeV)	Pt	Momentum Resolution (GeV) ⁻¹
140	1	0.983	0.06169
139	2	1.949	0.01783
138	3	2.773	0.01422
137	4	3.510	0.01069
136	5	4.261	0.00868

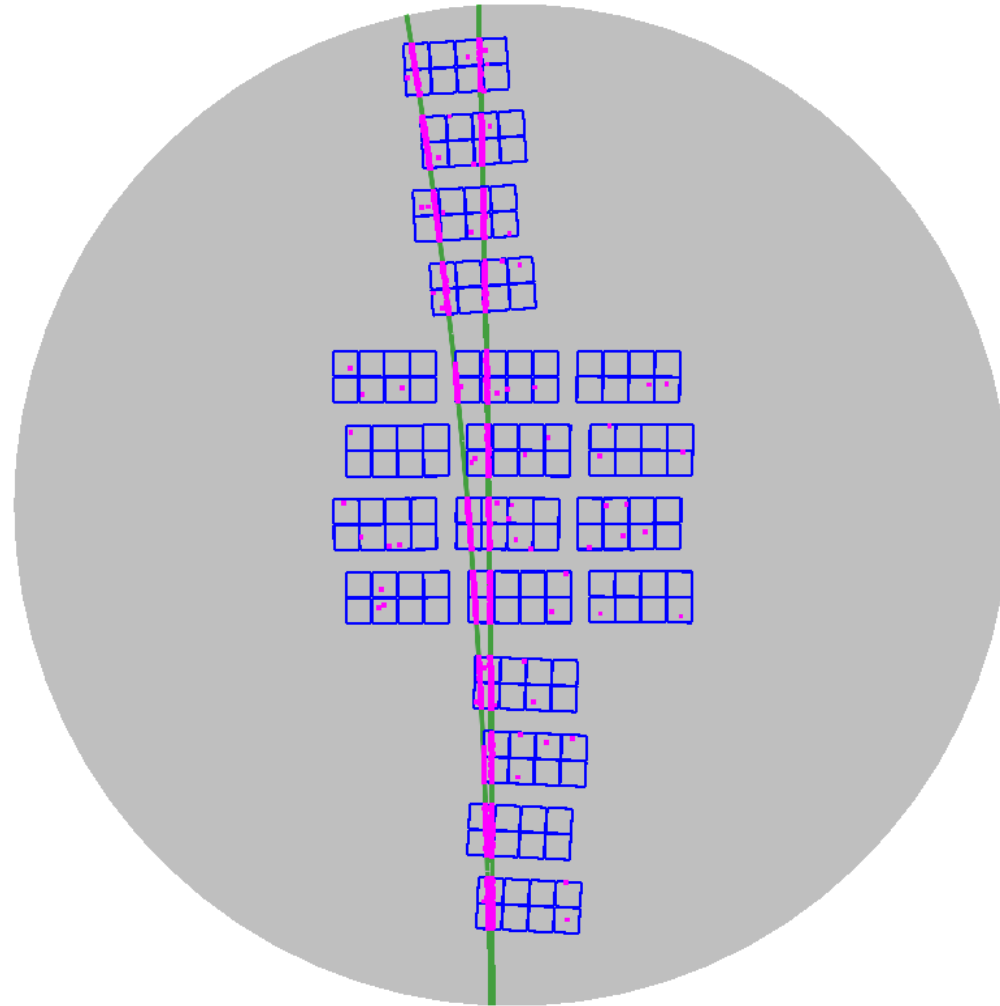


Summary and Outlook:

- Collecting inliers directly in the Hough space by a bivariate normal distribution fit in the Hough space
- Merging tracklets to have full track
- Recollecting remaining hits along the track
- [Analysis of testbeam data is ongoing](#)

Acknowledgment:

- I sincerely thank **Claus Kleinwort** for all his guidance and help.
- I also thank all my colleagues in Siegen, DESY, Bonn and Nikhef.



Thank you for your attention

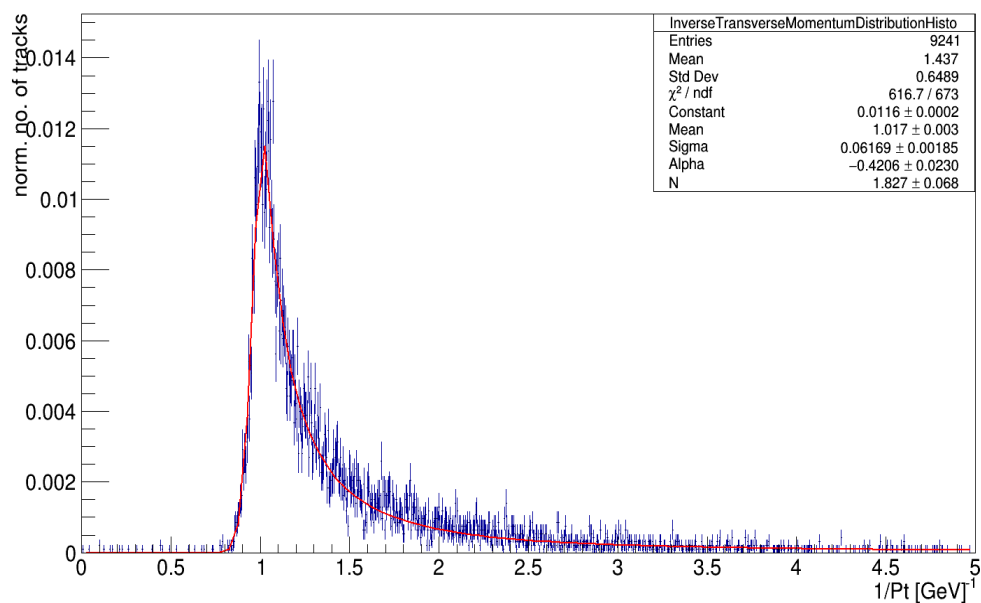
Backup

Testbeam data



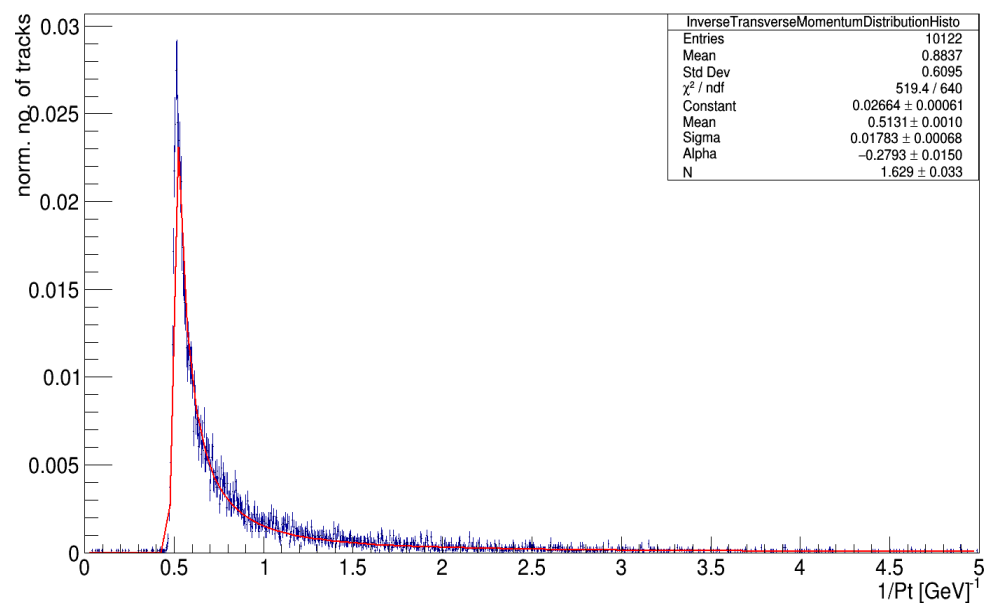
Inverse Momentum

InverseTransverseMomentumDistributionHisto



Run_140: 1 GeV

InverseTransverseMomentumDistributionHisto



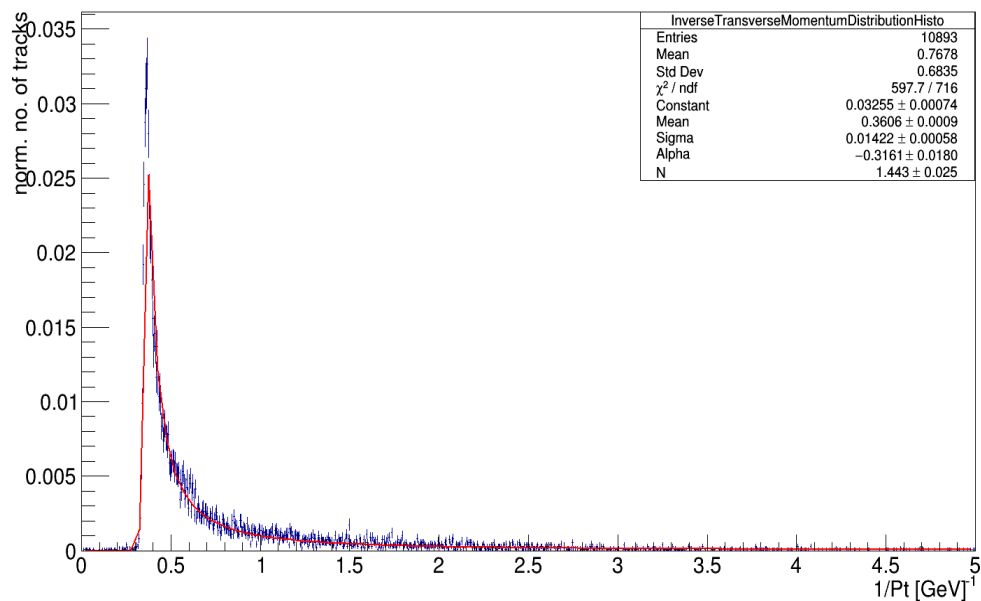
Run_139: 2 GeV

Testbeam data



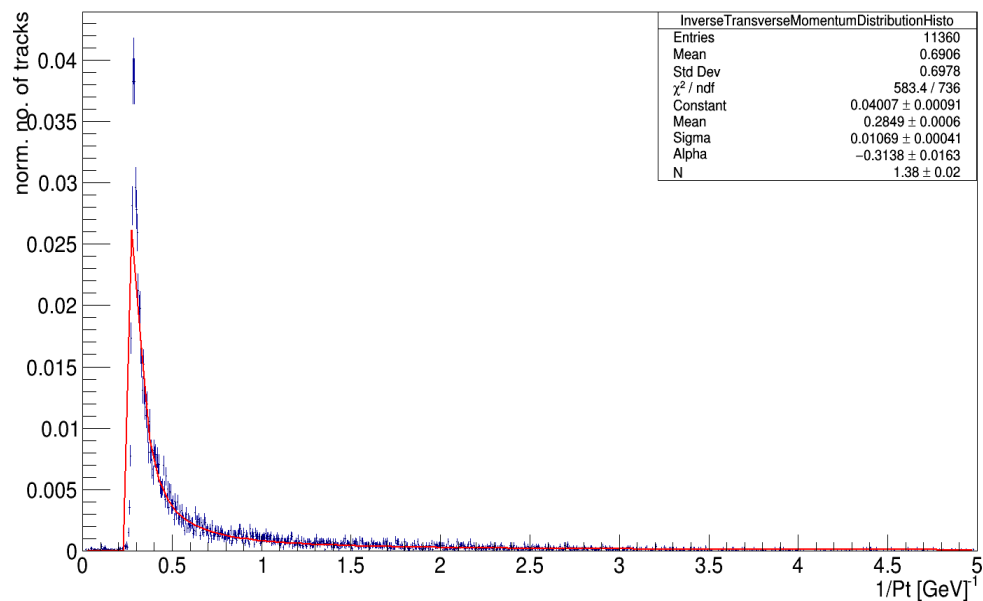
Inverse Momentum

InverseTransverseMomentumDistributionHisto



Run_138: 3 GeV

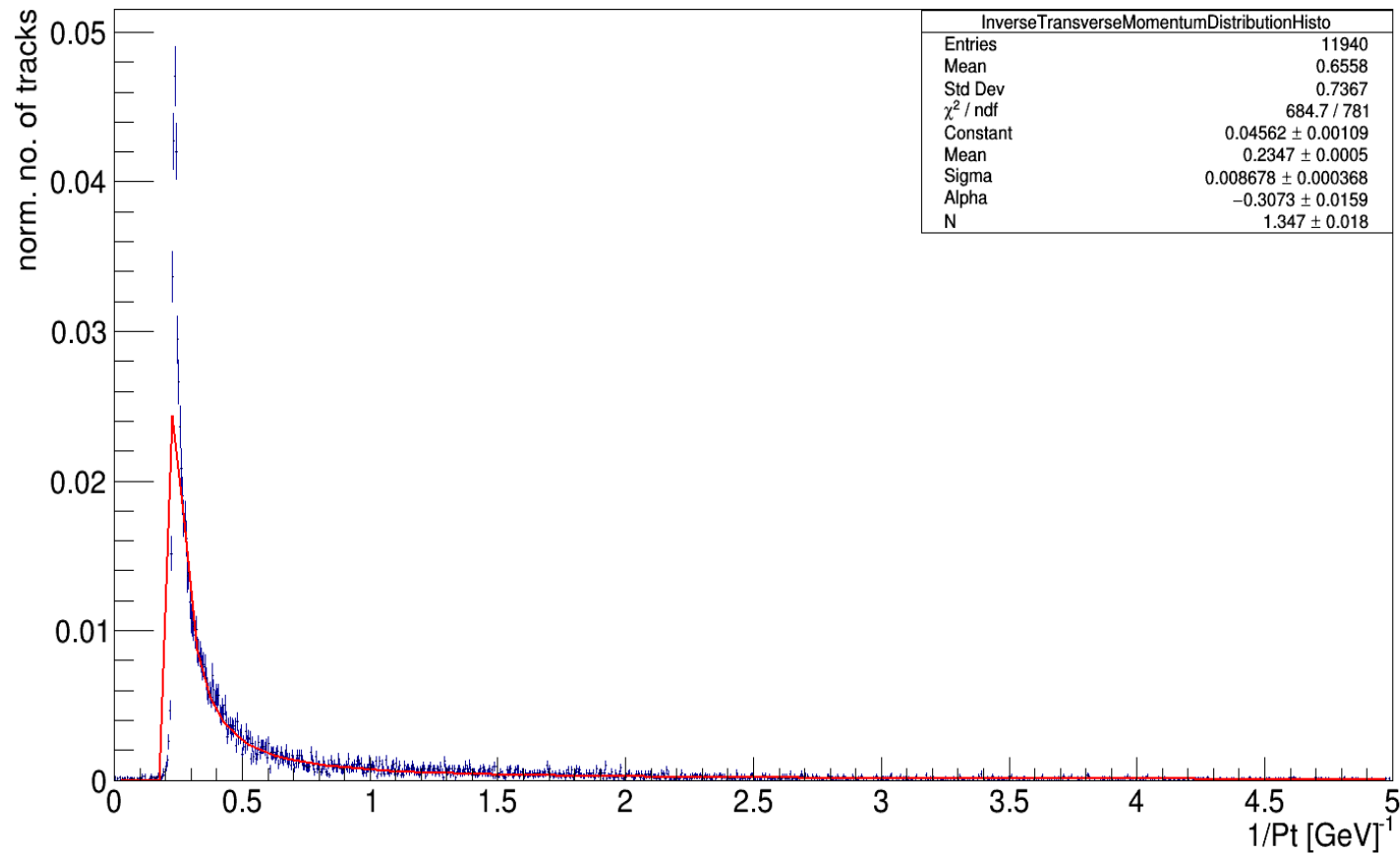
InverseTransverseMomentumDistributionHisto



Run_137: 4 GeV

Inverse Momentum

InverseTransverseMomentumDistributionHisto



Run_136: 5 GeV

Analysis: based on simulation



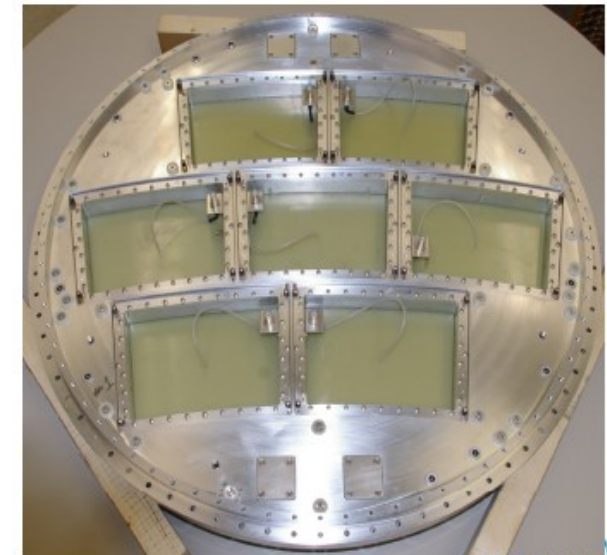
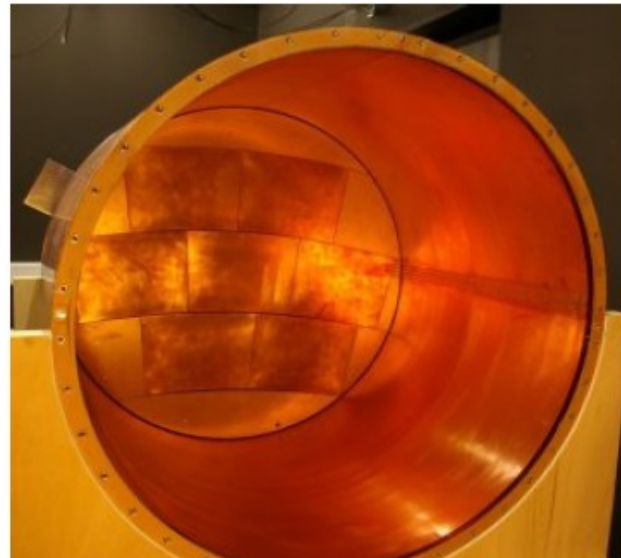
Definition: Efficiency and Purity

- **True Track:** is associated to the MC particle with the most hits on the track and more than some percentages (60% , 70%) of MC particle hits .
- **Track Efficiency:** Number of true track to number of all MC particle
- **Track Purity:** Number of true track to sum over number of true track, ghost and clone tracks
- **Right Hits:** Number of hits on the track from the associated MC particle
- **Hit Efficiency:** Number of right Hits to number of associated MC particle hits
- **Hit Purity:** Number of right hits to all hits of the true track

ILCTPC – DESY: Large Prototype TPC

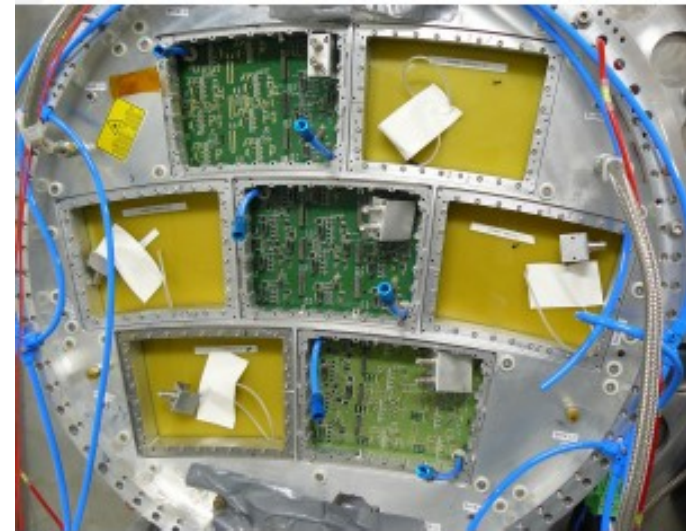
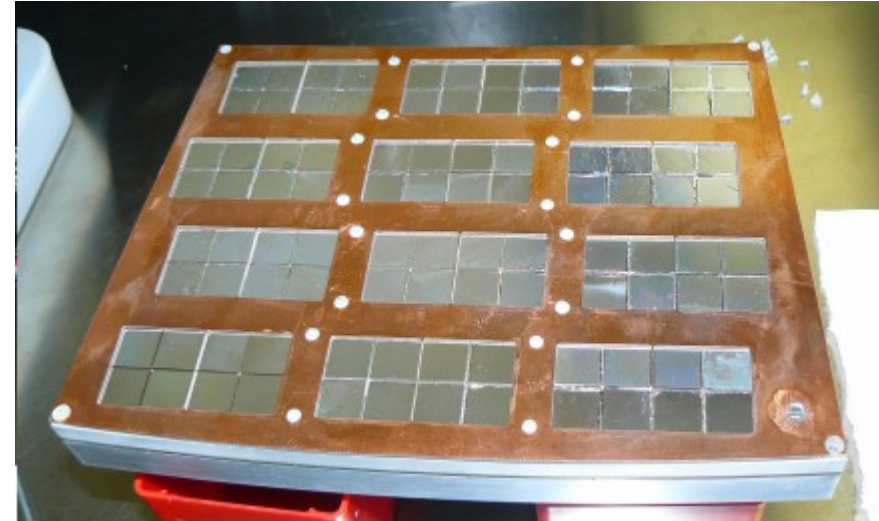


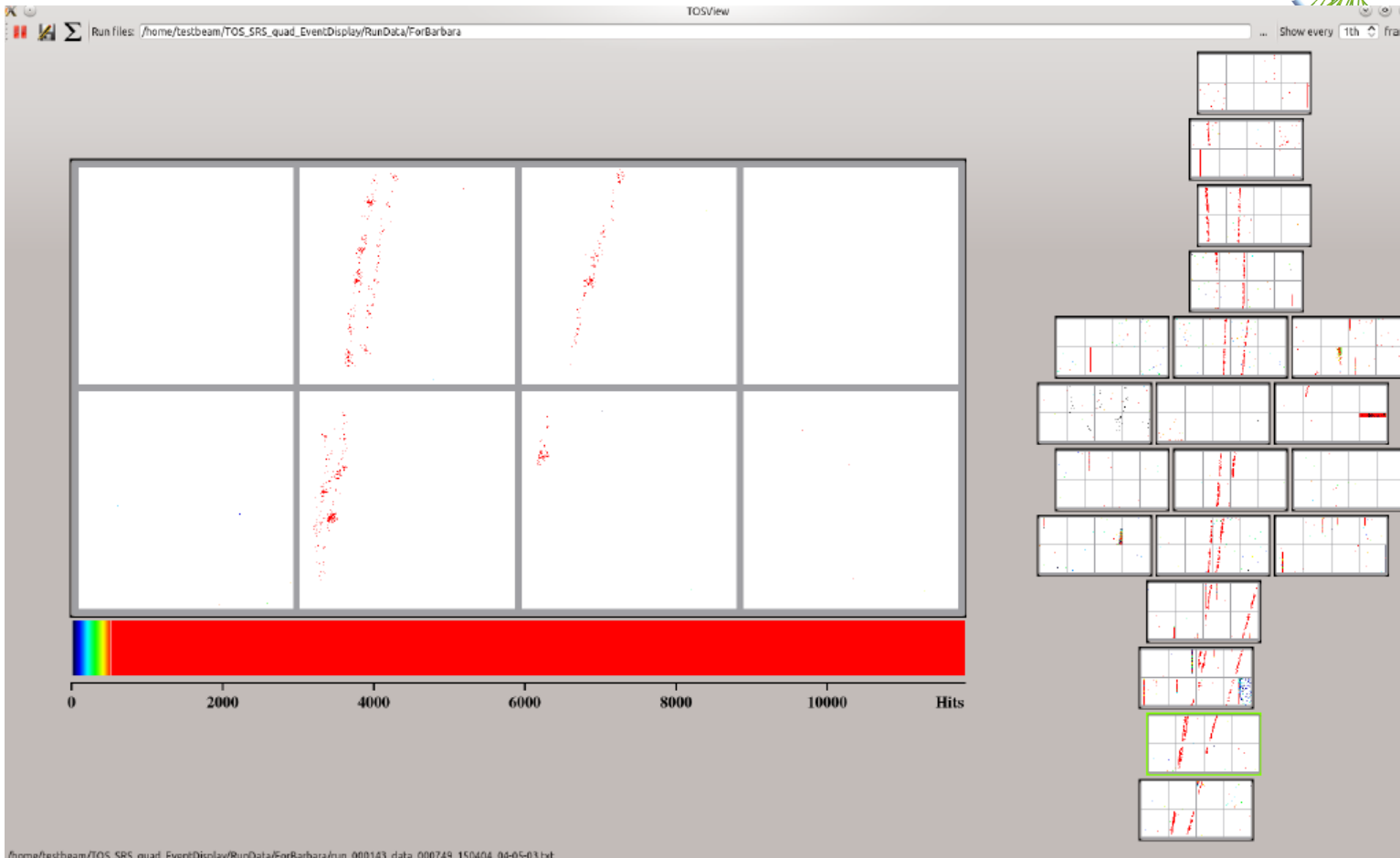
- Test beam area at DESY(1-6 GeV e^- beams)
 - Infrastructure includes a large bore 1T magnet on a movable stage
- Large Prototype (LP) built and installed to test scaling up of technologies and to compare different readout technologies on equal footing
- LP field cage parameters:
 - Length: 61 cm, Diameter: 72 cm
 - Up to 25 kV => E_{drift} up to 350 V/cm
 - Wall material budget: 1.3% X_0
- Endplate is able to host 7 readout modules (dimensions $\sim 22 \times 17 \text{ cm}^2$)



Infrastructure for test beam, TPC and Endplate from DESY group

- Test beam with 160 InGrid chips:
 - Central module with 96 chips (coverage 50 %)
 - 2 outer modules with 32 chips each
- Some Challenges:
 - InGrid production
 - Synchronized readout
 - Bonding on boards
 - LV distribution (up to 85 A @ 2.2 V)
 - Cooling
- The test beam was successful. During the test beam $\sim 10^6$ frames at a rate of around 5 Hz were collected.
- Test beam program:
 - Voltage scans (gas gain)
 - Z-scan
 - Momentum scan
 - Different angles
 - With and without magnetic field ($B = 1$ T)
 - Two different electrical drift fields





Further information about test beam results:

- Michael Lupberger, “Preliminary results from the 160 InGrid test beam”, University of Bonn, LCTPC-WP Meeting 10.09.2015,
- Jochen Kaminski, “Large Area Coverage of a TPC Endcap with GridPix Detectors”, University of Bonn, For the LCTPC collaboration , MPGD 2015, Trieste 12-15.10.2015,

➤ LC-TPC parameter

Parameter	r_{in}	r_{out}	z
Geometrical parameters	329 mm	1808 mm	± 2350 mm
Solid angle coverage	up to $\cos \theta \simeq 0.98$ (10 pad rows)		
TPC material budget	$\simeq 0.05 X_0$ including outer fieldcage in r $< 0.25 X_0$ for readout endcaps in z		
Number of pads/timebuckets	$\simeq 1-2 \times 10^6/1000$ per endcap		
Pad pitch/ no.padrows	$\simeq 1 \times 6 \text{ mm}^2$ for 220 padrows		
σ_{point} in $r\phi$	$\simeq 60 \mu\text{m}$ for zero drift, $< 100 \mu\text{m}$ overall		
σ_{point} in rz	$\simeq 0.4 - 1.4 \text{ mm}$ (for zero – full drift)		
2-hit resolution in $r\phi$	$\simeq 2 \text{ mm}$		
2-hit resolution in rz	$\simeq 6 \text{ mm}$		
dE/dx resolution	$\simeq 5 \%$		
Momentum resolution at B=3.5 T	$\delta(1/p_t) \simeq 10^{-4}/\text{GeV}/c$ (TPC only)		