



Top identification and top pair production at CLIC

Workshop on top physics at the LC 2018,
June 4-6, 2018

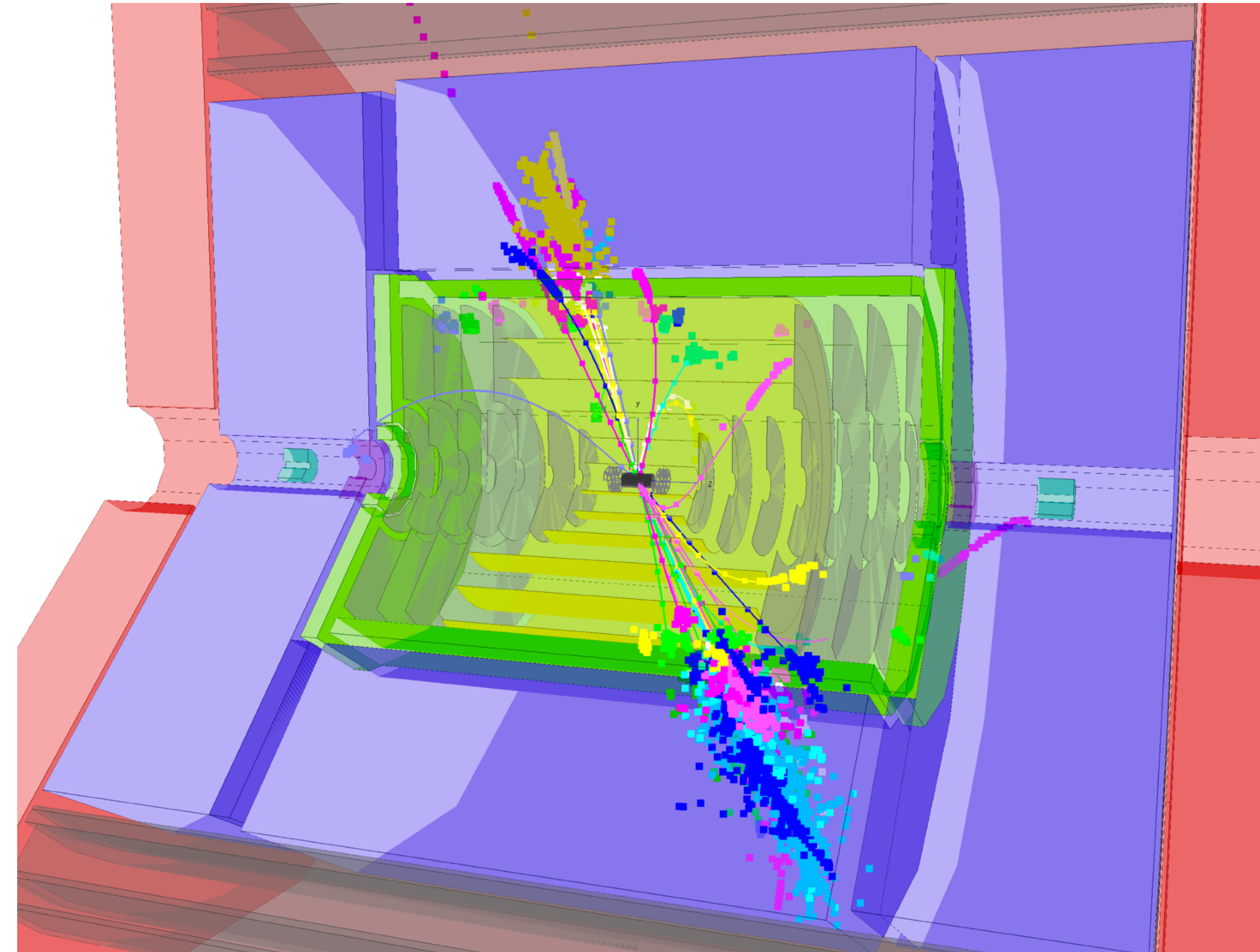
On behalf of the CLICdp Collaboration

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- Top pair production at CLIC
- General analysis strategy
- Analysis at 380 GeV
- Analyses above 1 TeV
 - Top identification above 1 TeV
- Results



$e^+e^- \rightarrow tt \rightarrow qqqq\mu\nu_\mu$ at 3 TeV in **CLICdet**
 CLICdet described in **CLICdp-Note-2017-001**



Top quark production at CLIC

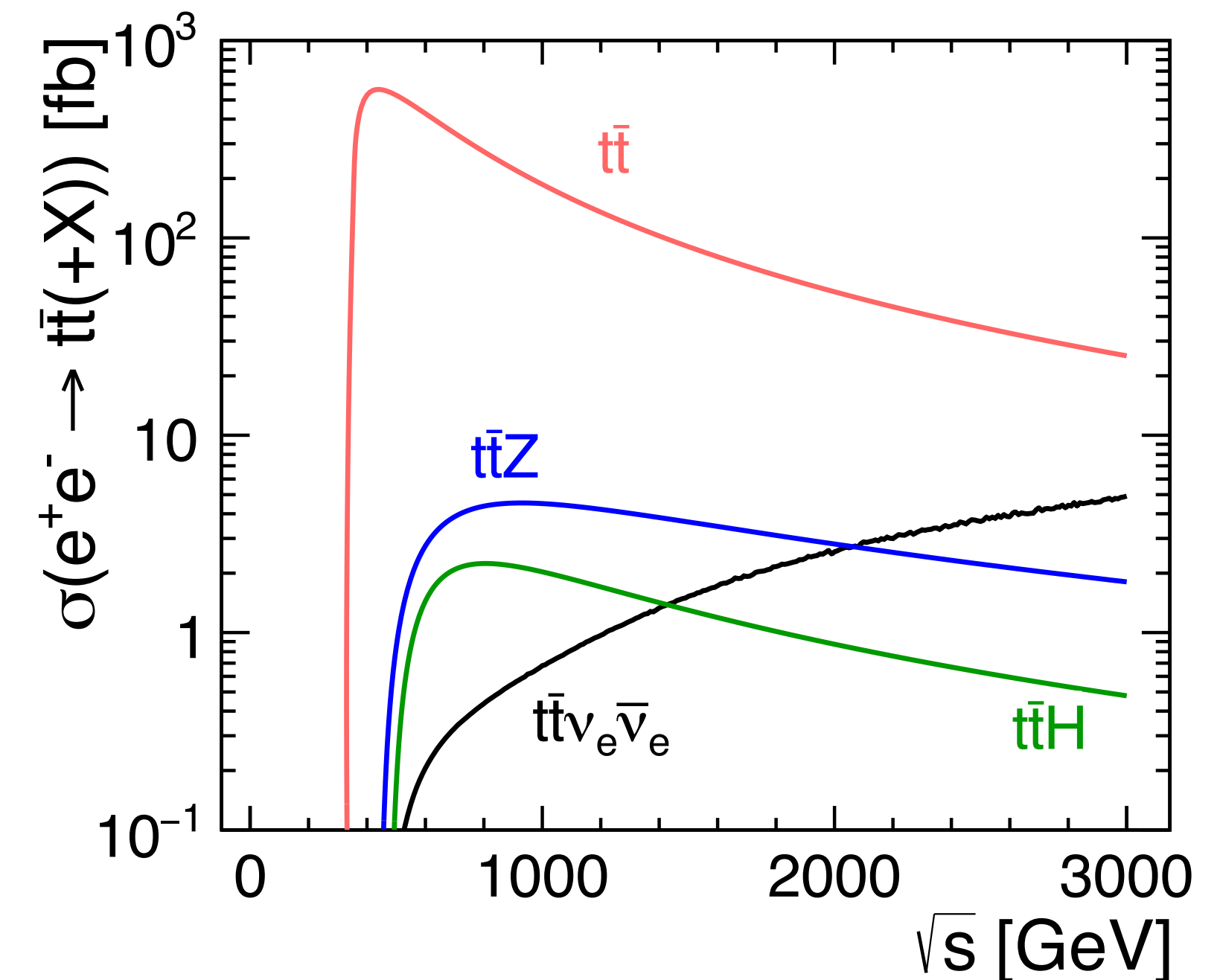


- CLIC staging baseline: [CERN-2016-004](#)
- Top quarks are produced at all stages of CLIC (threshold and continuum)
- Dedicated threshold scan at 350 GeV (talk by Frank Simon tomorrow); top mass determination above threshold by ISR (talk by Pablo Gomis Lopez tomorrow)
- Top pair production up to 3 TeV; **this talk** + talk on EFT interpretation by Martín Perelló Roselló (later today)
- FCNC top decays at 380 GeV; talk by Filip Zarnecki (tomorrow)
- Associated production ($t\bar{t}H$, VBF) > 1 TeV, talk by Yixuan Zhang on $t\bar{t}H$ (next)

• **Top physics overview paper in collaboration review (to be published 2018)**

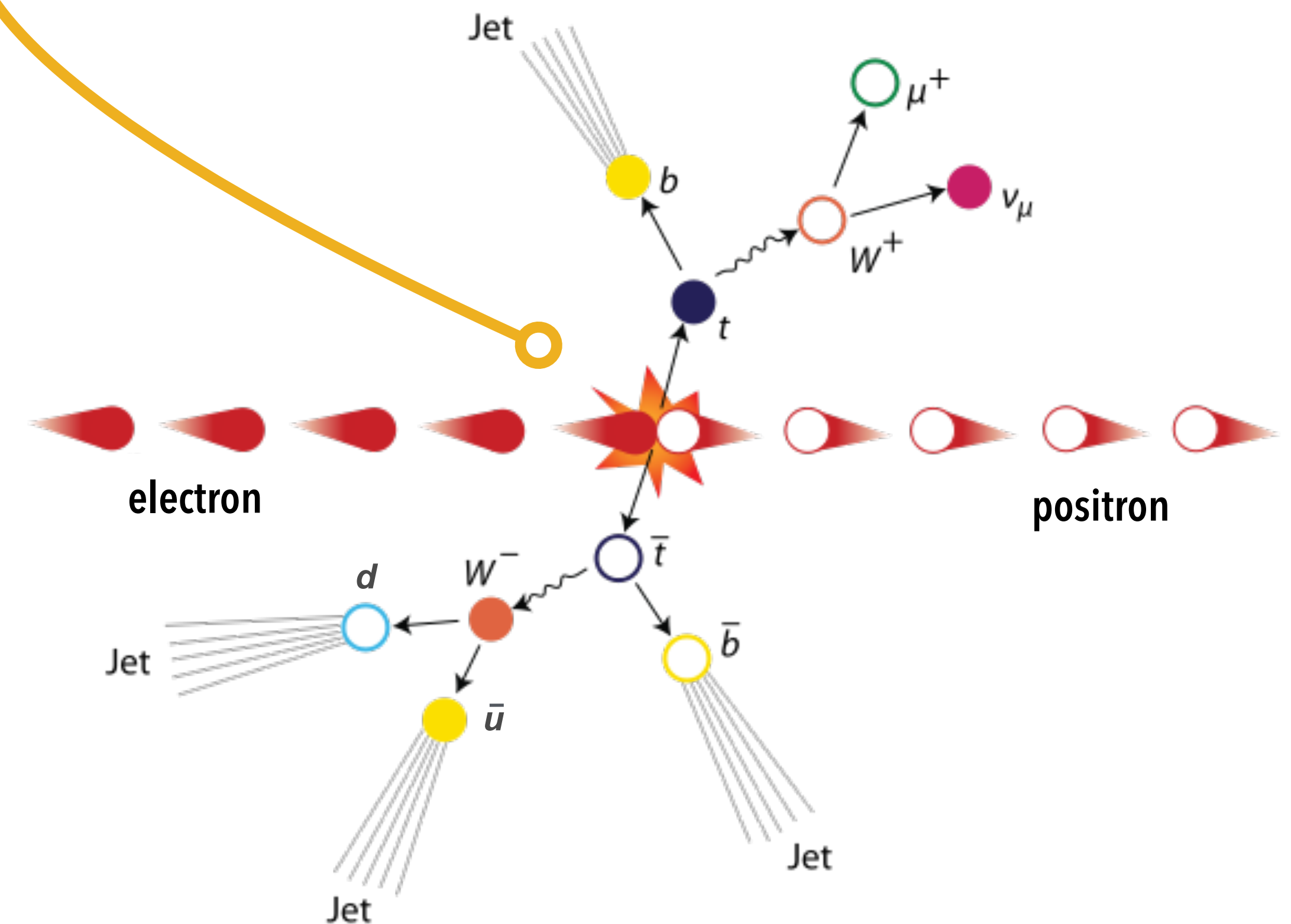


Stage	\sqrt{s} [GeV]	$\mathcal{L}_{int.}$ [fb^{-1}]	L [km]
1	380	500	11,4
	350	100	
2	1500	1500	29,0
3	3000	3000	50,1

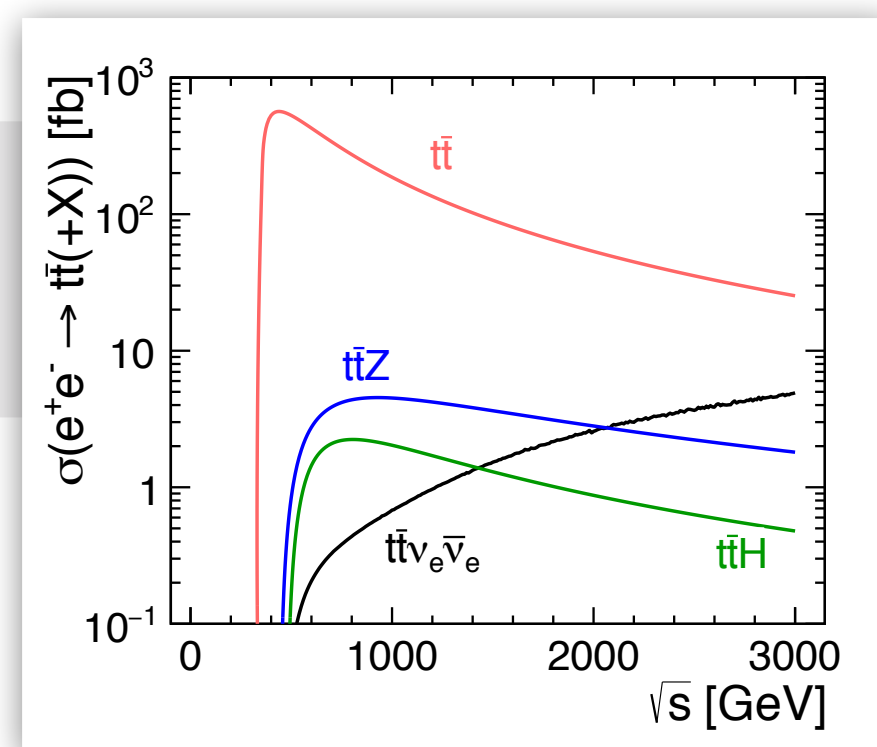


- Top mass and couplings to Z and γ are among the main focuses of the initial stage of CLIC
- **New**: Extended top coupling study to higher energy stages by using methods developed for boosted topologies
- Precision measurements on anomalous electroweak couplings yield sensitivity to new physics at scales well beyond the direct reach
- Reconstruction methods also useful for other BSM searches

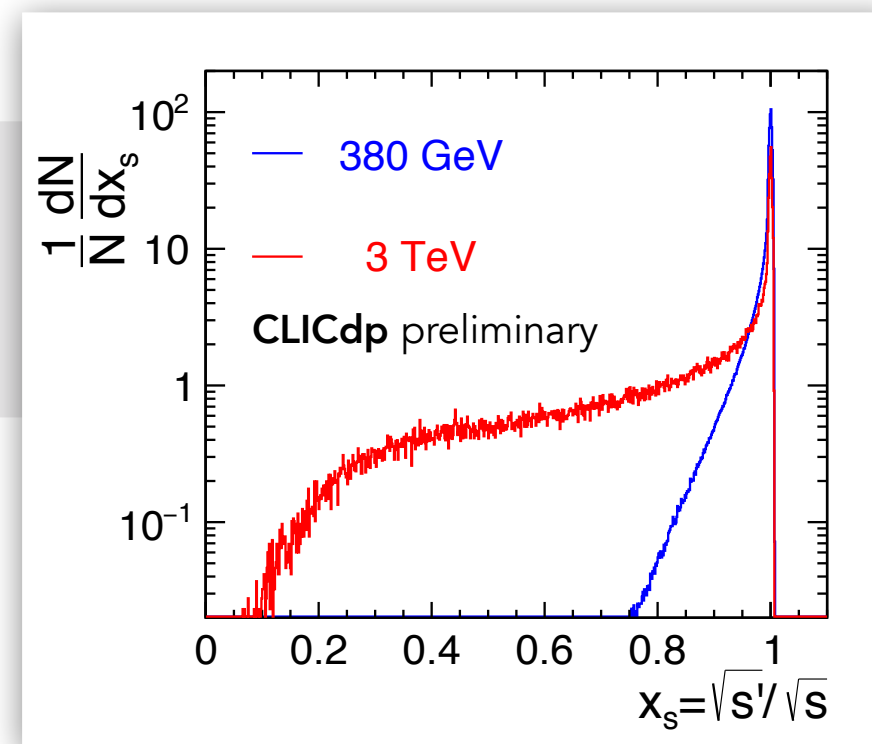
- **Cross-section σ**
- **Forward-backward asymmetry A_{FB}**
- **Statistically optimal observables**



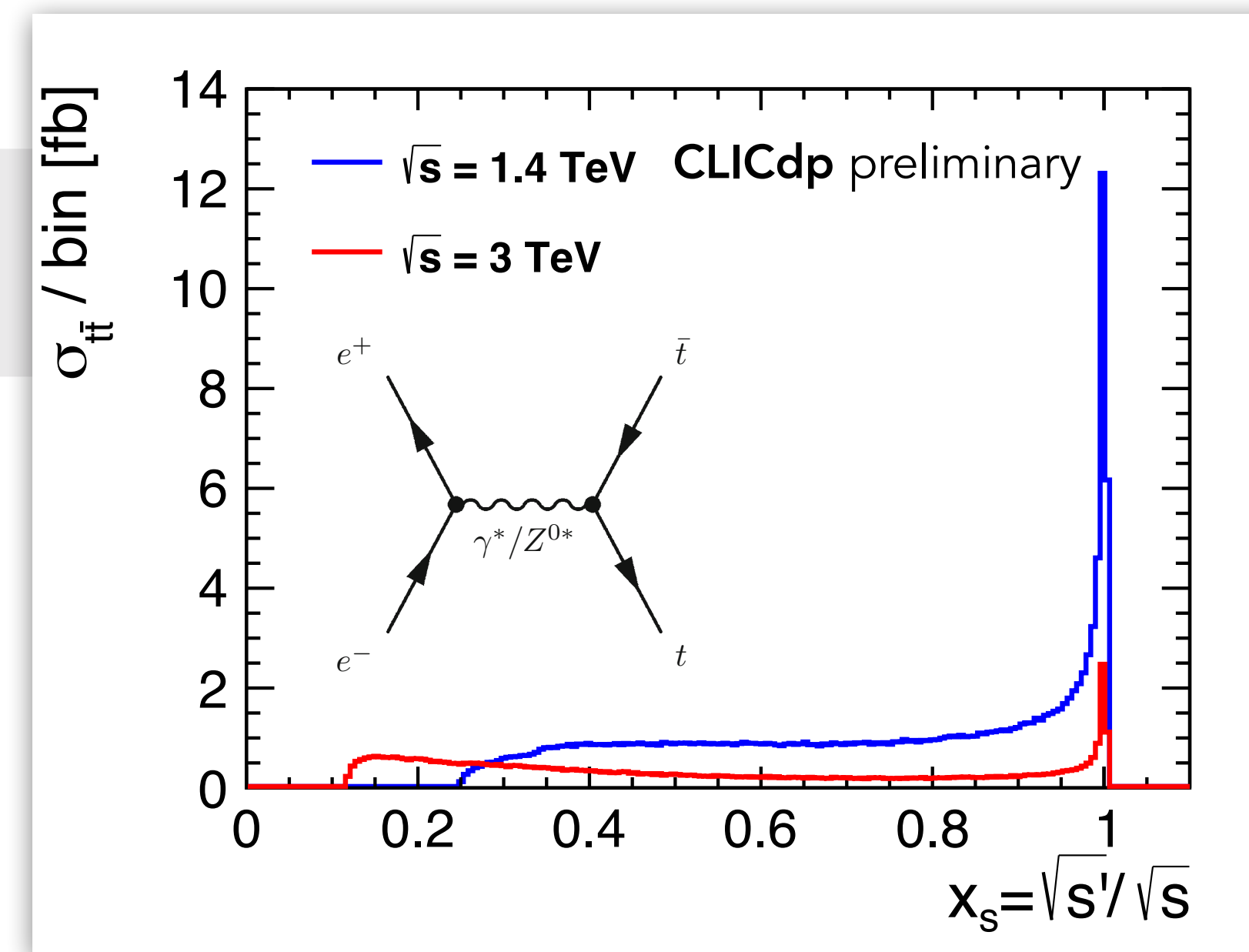
Cross section $e^+e^- \rightarrow t\bar{t}$ @LO incl. ISR, unpolarised



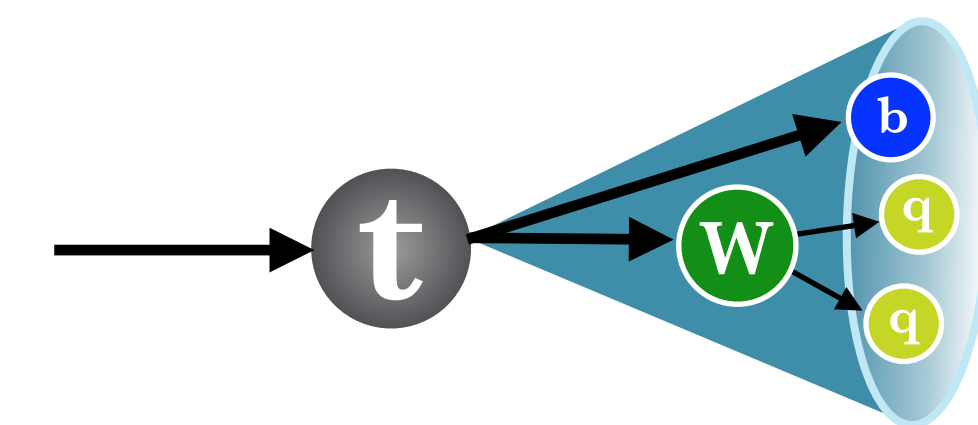
CLIC luminosity spectrum



Effective centre-of-mass energy $\sqrt{s'}$



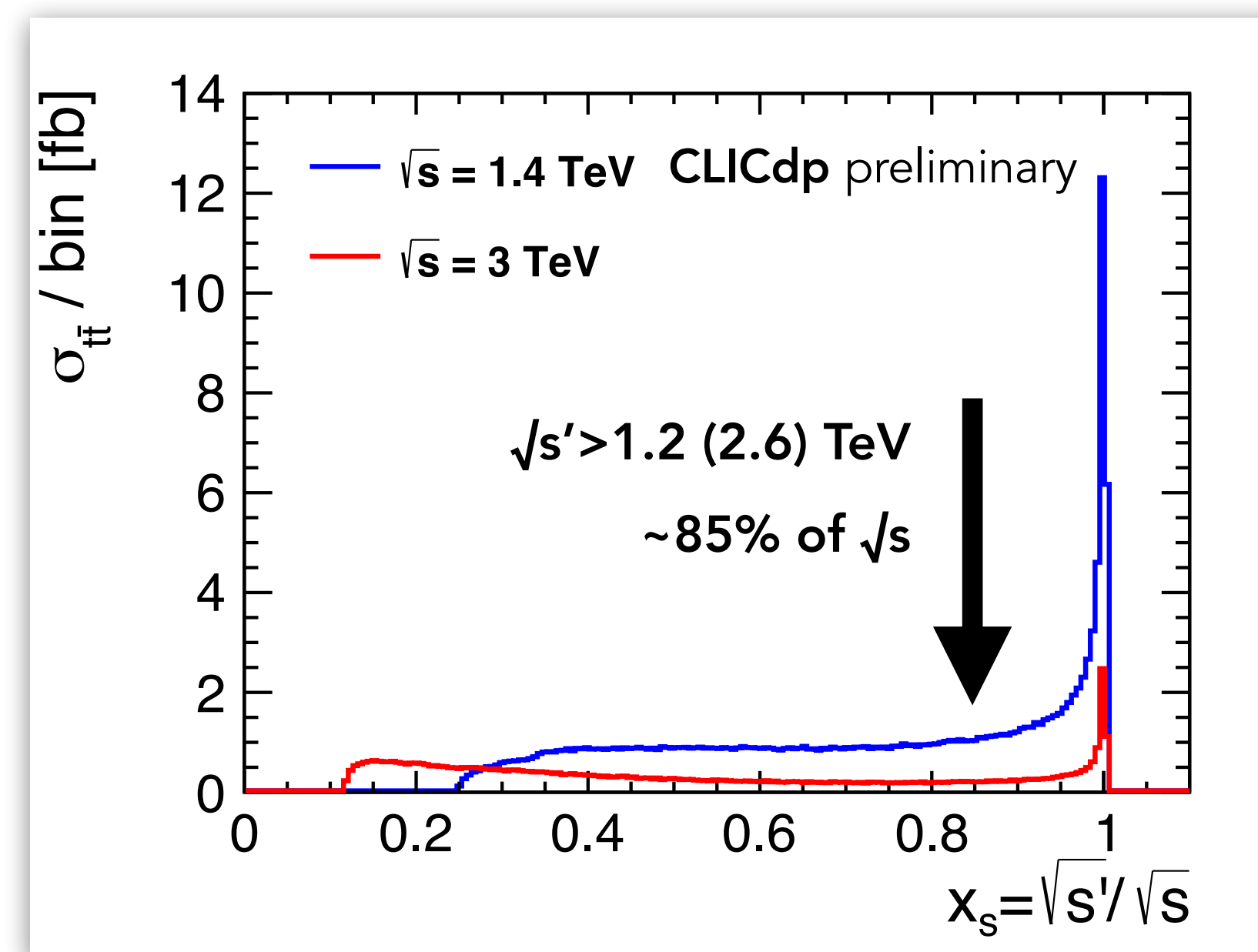
- Operation at $\sqrt{s} > 1\text{TeV}$ leads to more highly collimated jet environments
- **Resolved strategy**
 - Production close to threshold
 - Combine jets, b-tagging, etc.
- **Boosted strategy (large R-jets/fat-jets)**
 - Standard identification techniques challenging since tracks are very close to each other and the W decay products are not isolated from each other or b-jet
 - b-tagging alone no longer viable
 - Instead tag tops by identifying prongy jet sub-structure



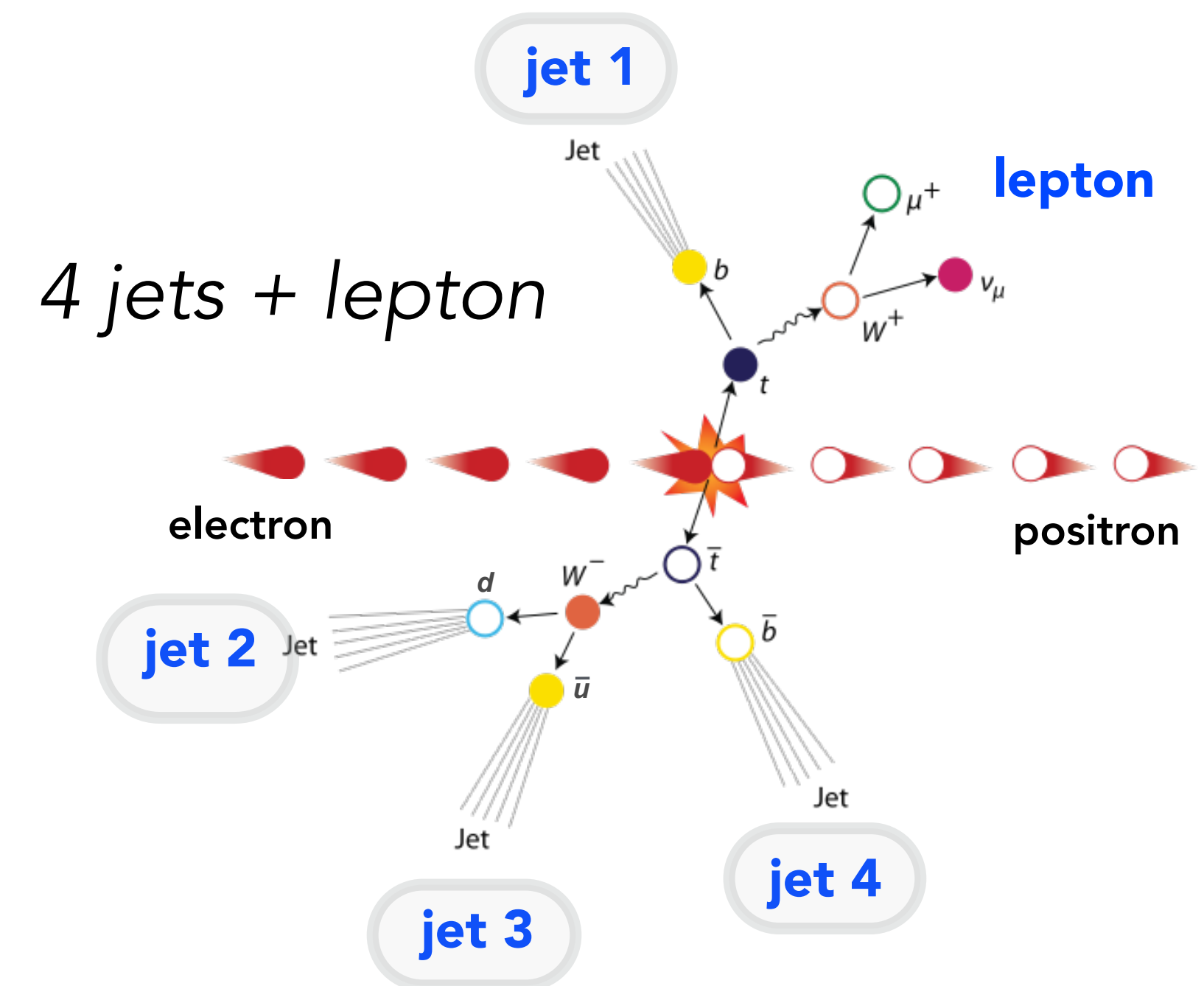
Fully merged top quark

- **Semi-leptonic ttbar events** ($tt \rightarrow qqqlv$, $l=e,\mu$)
- Use lepton charge to reconstruct the charge of the top/anti-top
- Six-fermion final states are generally dominated by ttbar but have a sizeable contribution from single-top and triple gauge boson production above 1 TeV
- Backgrounds considered: fully-hadronic ttbar, fully-leptonic ttbar, non-ttbar qqqlv, di-jet, WW-fusion, ZZ-fusion
- Top pair production studied at the nominal collision energies as 380 GeV, 1.4 TeV, and 3 TeV
- In addition, radiative events are studied at $\sqrt{s} = 1.4$ TeV
- Studies done for CLIC_ILD using full simulation/reconstruction

Effective centre-of-mass energy $\sqrt{s'}$



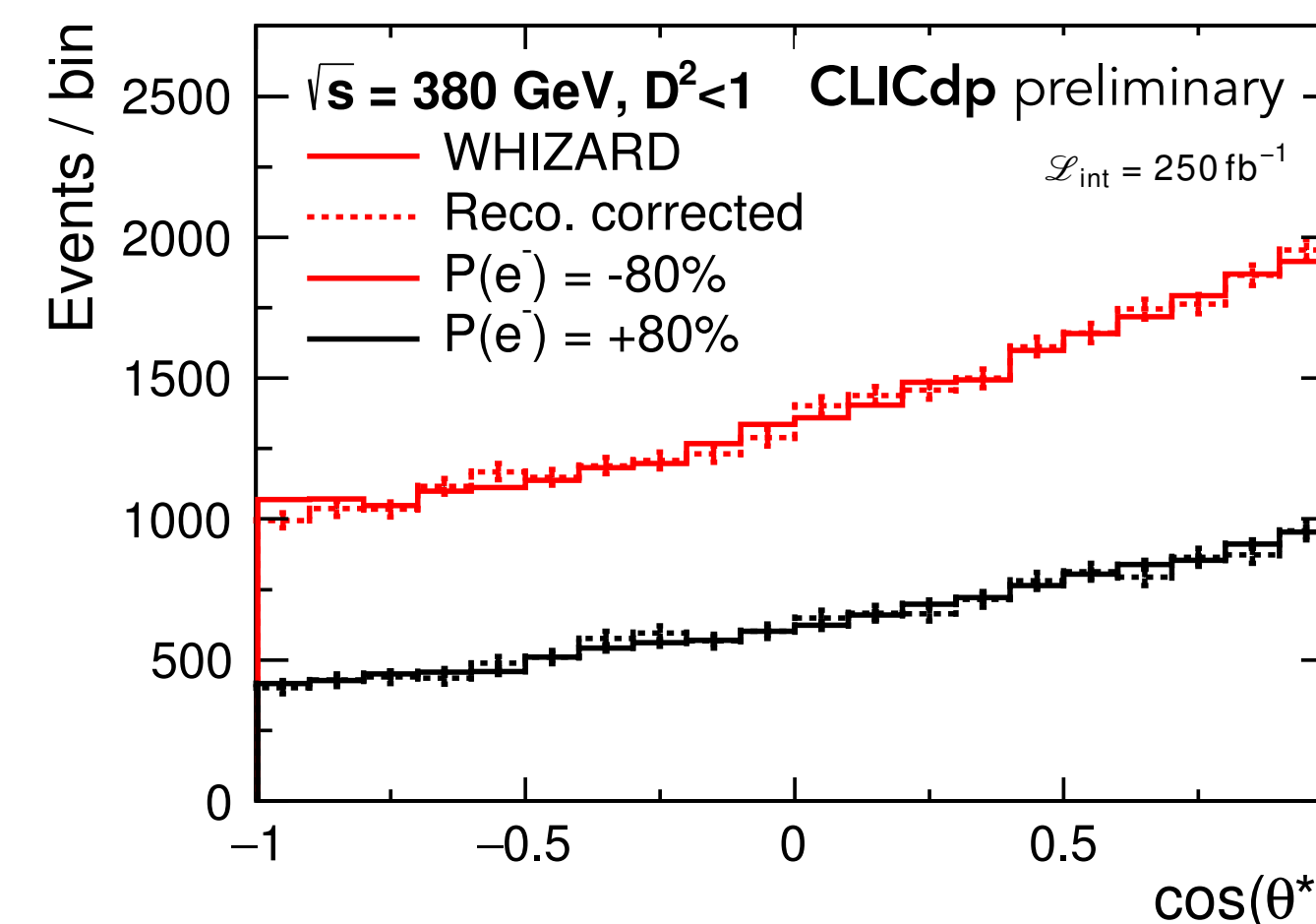
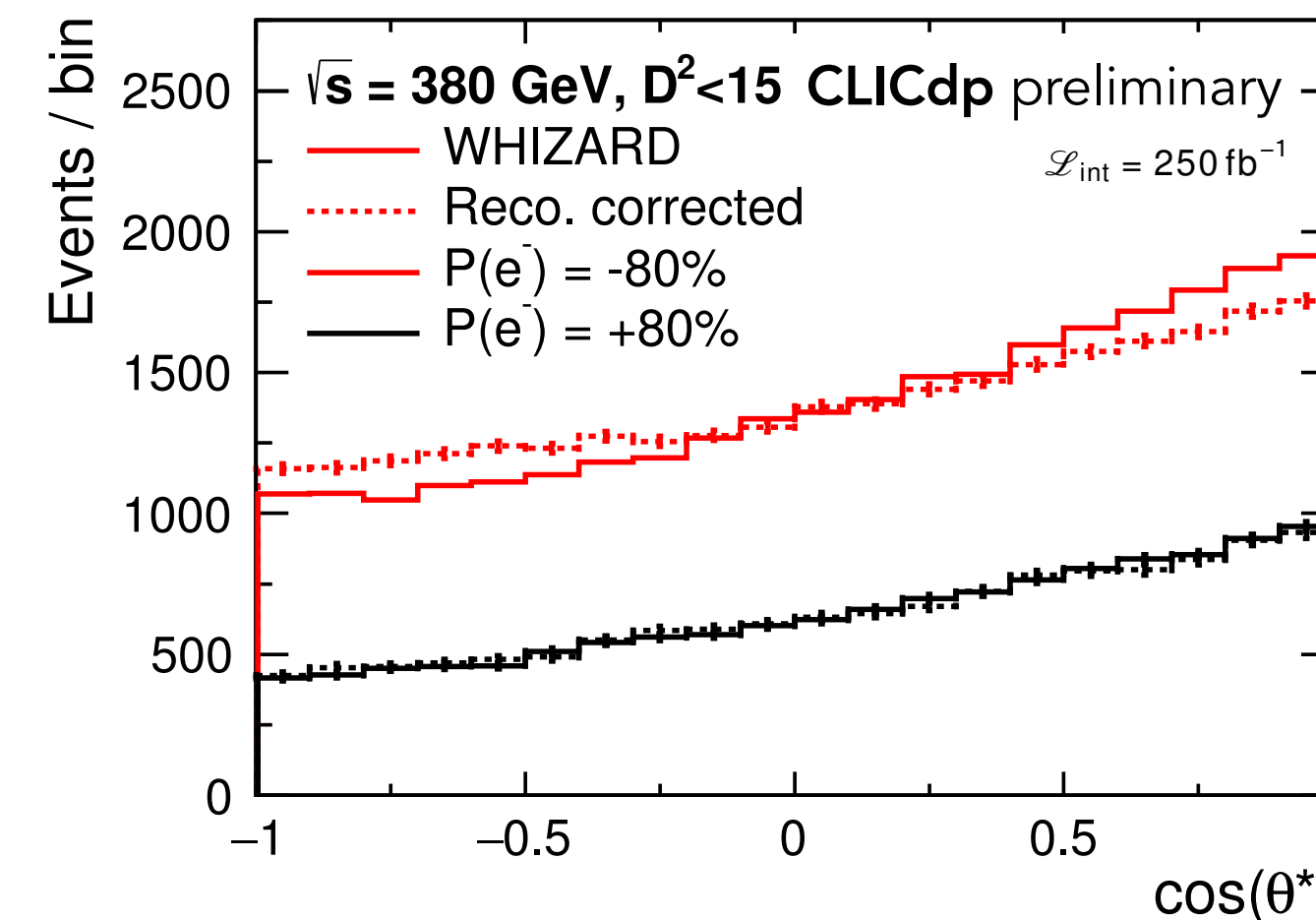
- Top-quark candidates are formed by combining jets
- Large-R possible due to clean environment, PFO clustered into **4 exclusive jets** using the VLC algorithm ([Eur. Phys. J. C78 \(2016\) 144](#))
- Analysis is based on that developed in [Eur. Phys. J. C75 \(2015\) 512](#)
- Further details are available in [CERN-THESIS-2016-214](#) by I. G. García



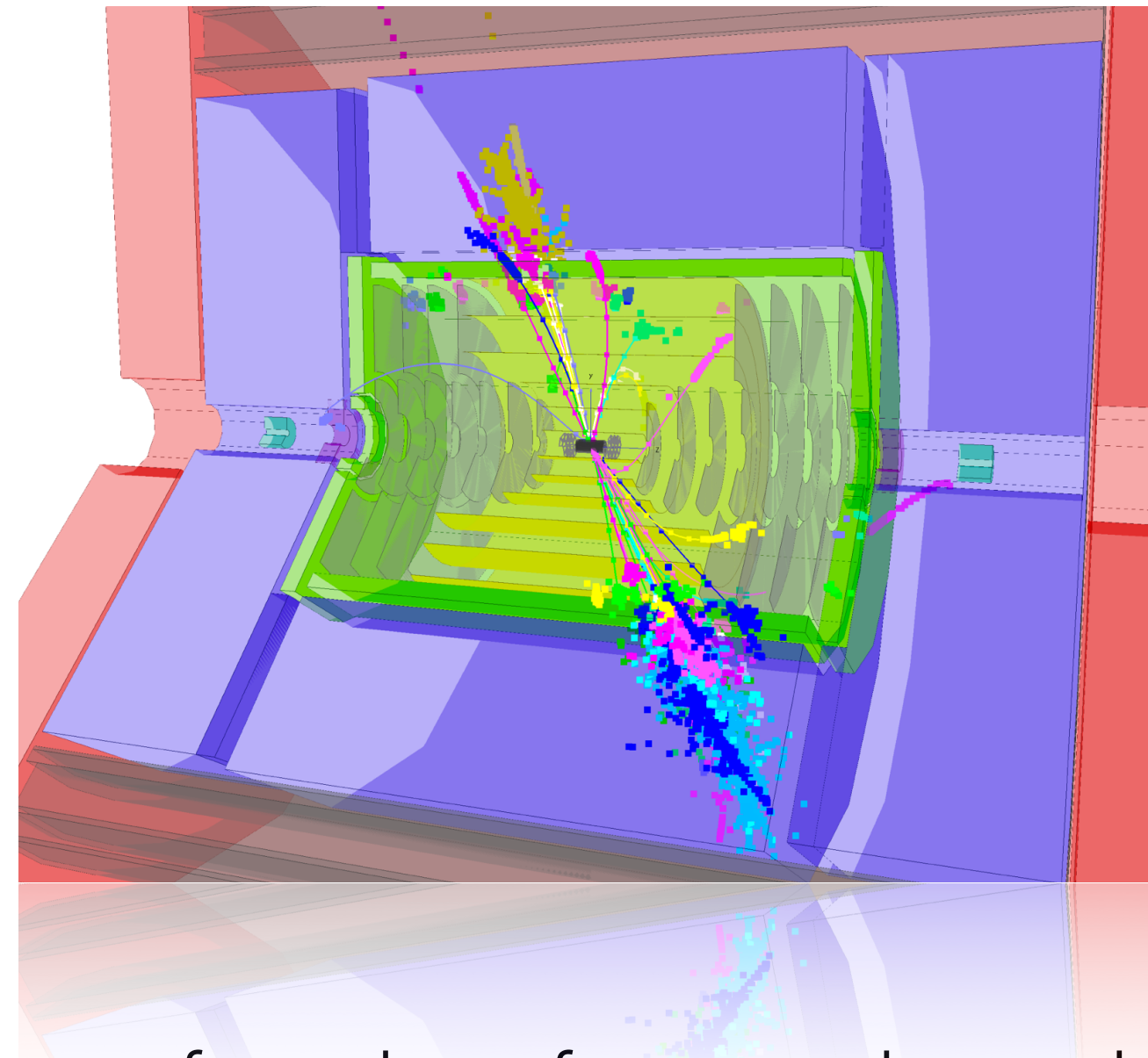
- **Event selection:**

- 1 isolated lepton (electron or muon)
- 2 b-tagged jets
- Each of the non-b-tagged jets: $E_{\text{jet}} > 15$ GeV
- Top-quark candidates are formed by merging each b-tagged jet with the two remaining non-b-tagged jets (best candidate selected)
- Mass cuts on the resulting system: $m_t \in [100, 250]$ GeV, $m_W \in [40, 190]$ GeV
- Minimising D^2 – reduce the effect of migrations in the top polar angle distribution for A_{FB} measurement in $P(e^-) = -80\%$

$$D^2 = \left(\frac{\gamma_t - \langle \gamma_t \rangle}{\sigma_{\gamma_t}} \right)^2 + \left(\frac{E_b^* - 68 \text{ GeV}}{\sigma_{E_b^*}} \right)^2 + \left(\frac{\cos \theta_{bW} - \langle \cos \theta_{bW} \rangle}{\sigma_{\cos \theta_{bW}}} \right)^2$$

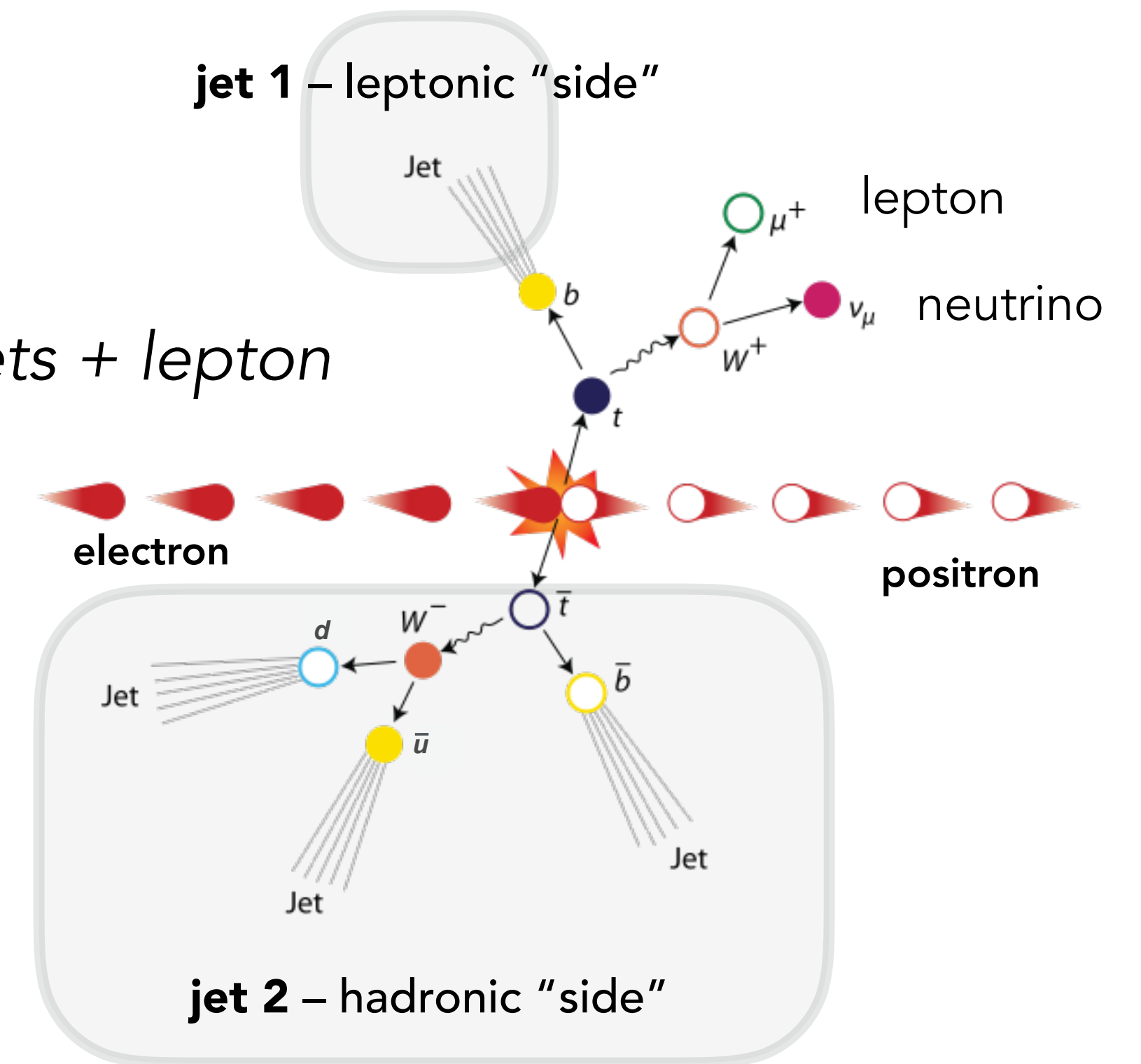


$e^+e^- \rightarrow tt \rightarrow qqqq\mu\nu_\mu$
at 3 TeV **CLICdet**



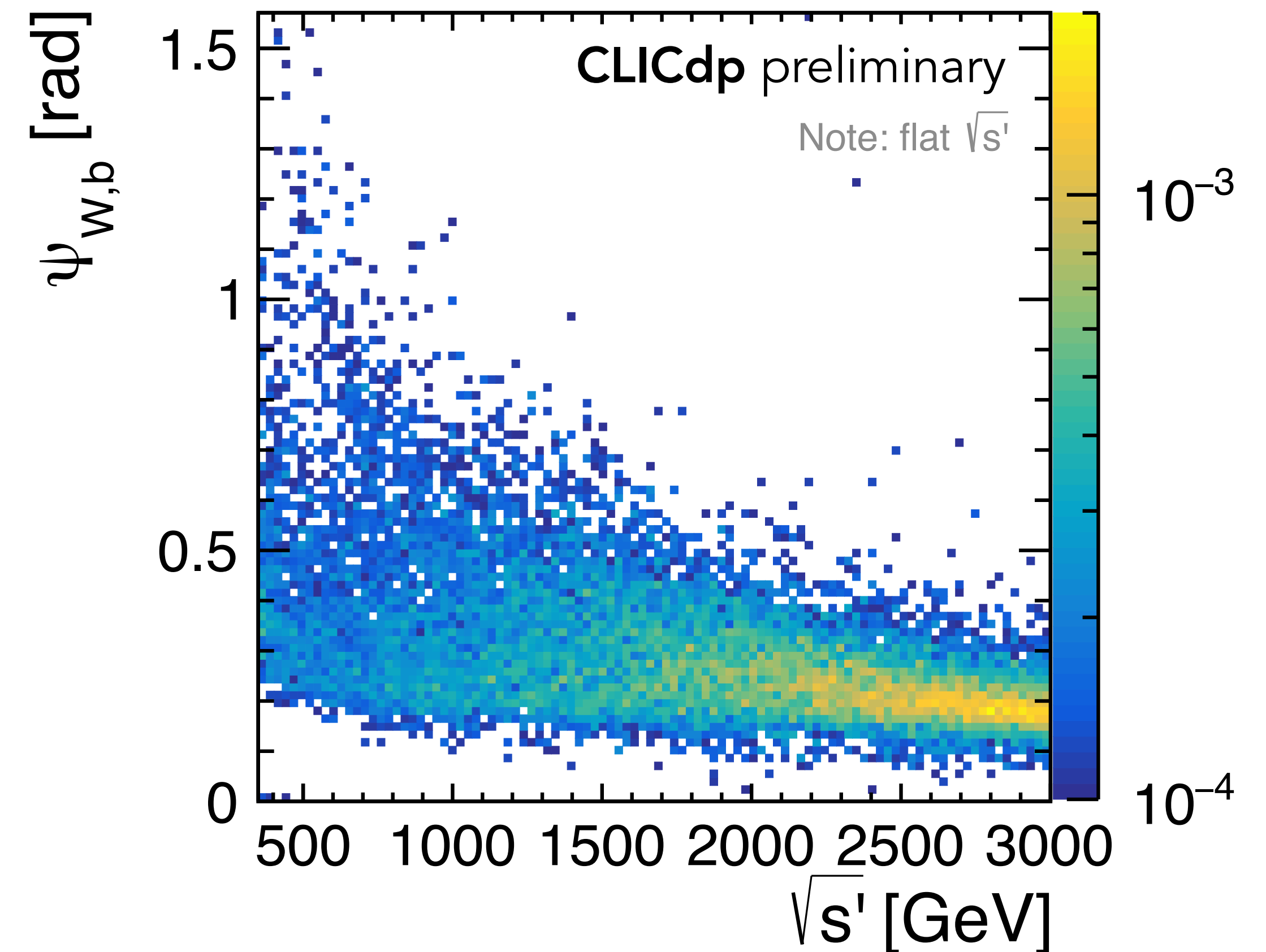
- Event topology very different from that of top quarks produced close to the threshold that have an isotropic topology; the boosted tops are more easily distinguishable from each other \rightarrow less migrations
- Large-R possible due to clean environment, jet clustering on pre-trimmed PFO collection; **2 exclusive jets** using the VLC algorithm with $R=1.4(1.5)$, $\beta=1.0$, $\gamma=1.0$ (VLC14, VLC15)

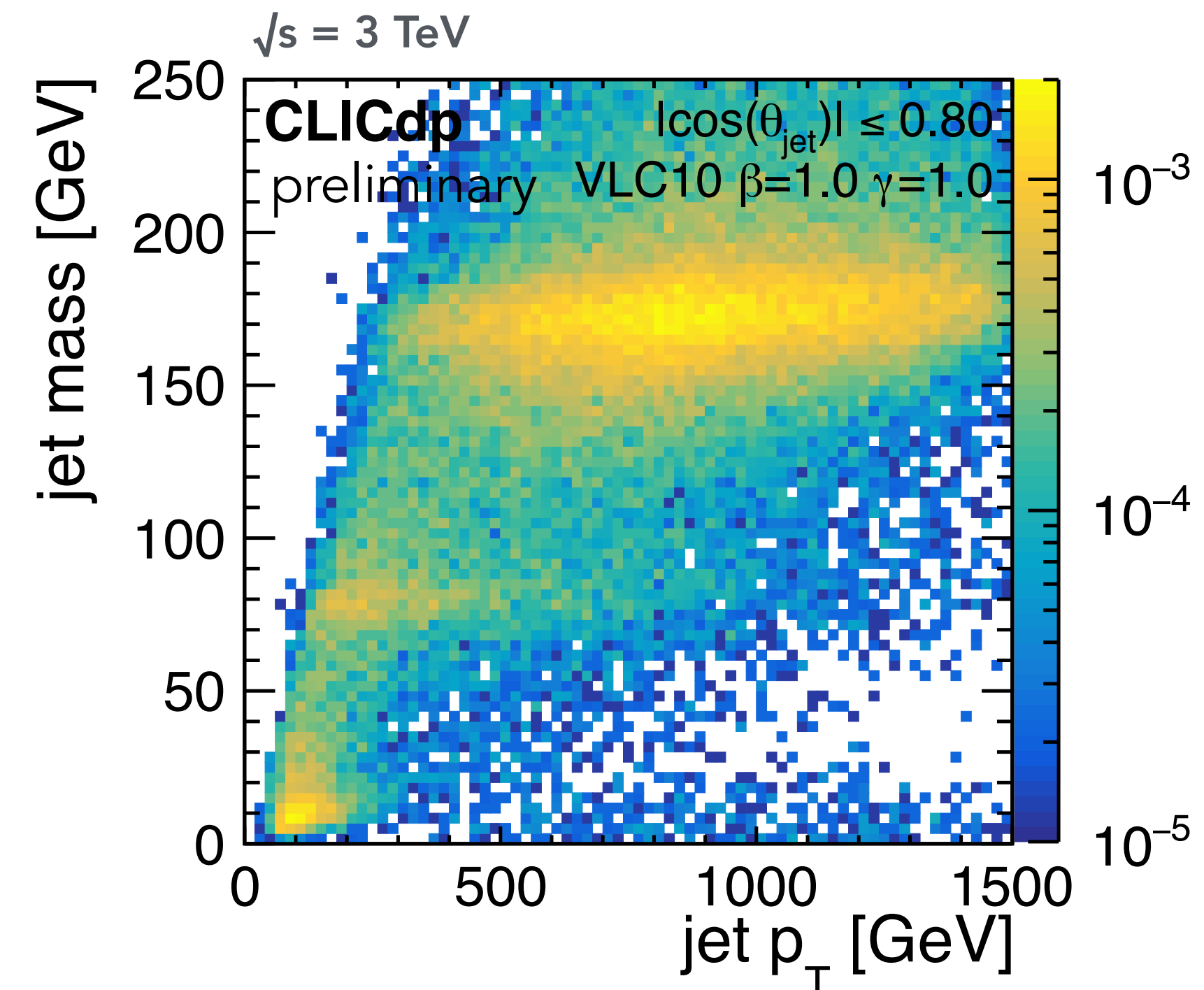
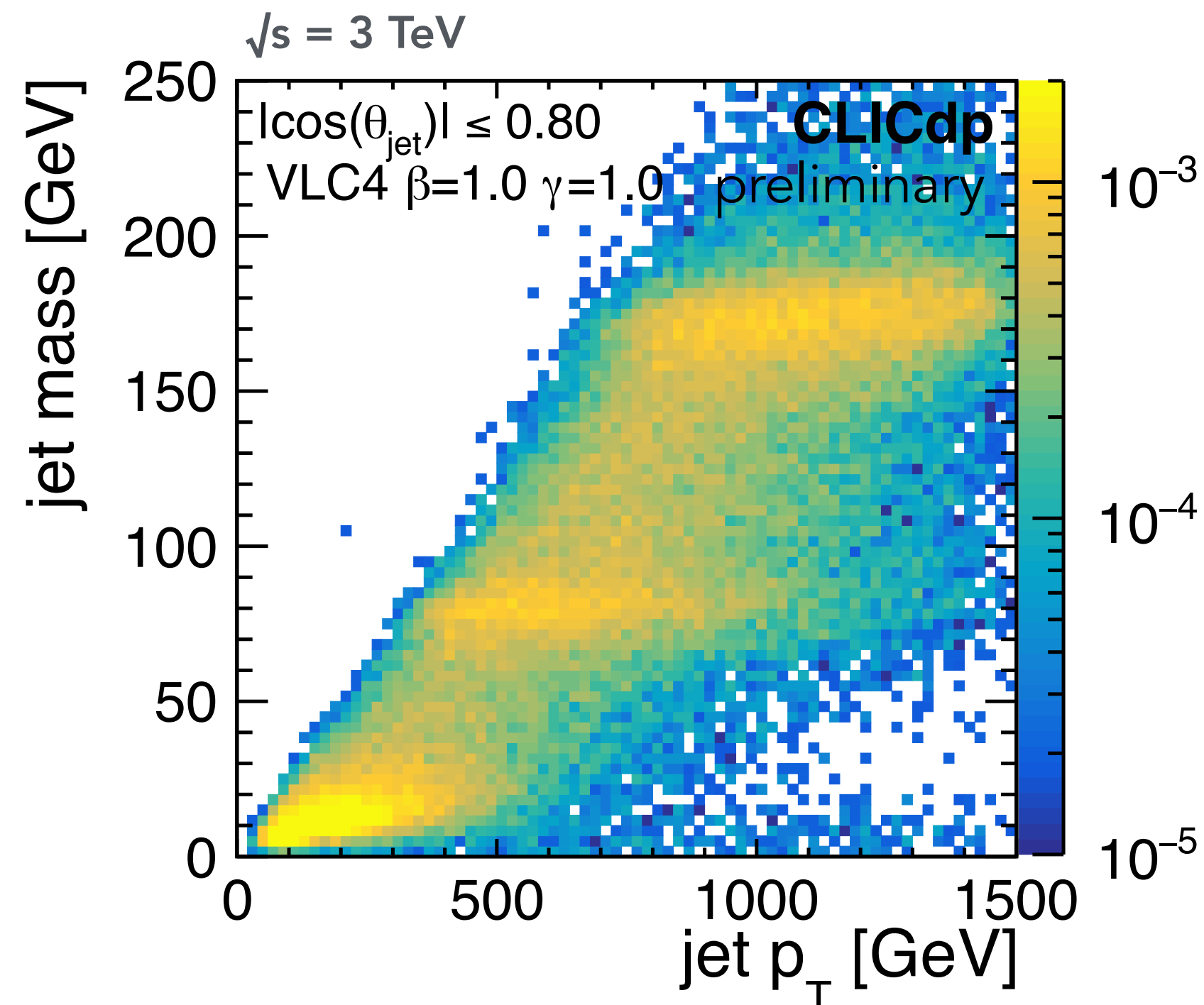
2 large-R jets + lepton



- Reconstruction of top quark in a large-R jet with identification of substructure
- Studied ~10 years for the LHC
- New and active effort for CLIC
- **Strategy I:**
 - “Top tagging – parsing jet substructure”
 - described here; applied for the analysis at nominal collision energy, \sqrt{s} , of 1.4 and 3 TeV
- **Strategy II:**
 - “MVA-based – using substructure variables”
 - applied for the analysis of radiative events at $\sqrt{s} = 1.4$ TeV (three intervals below \sqrt{s})

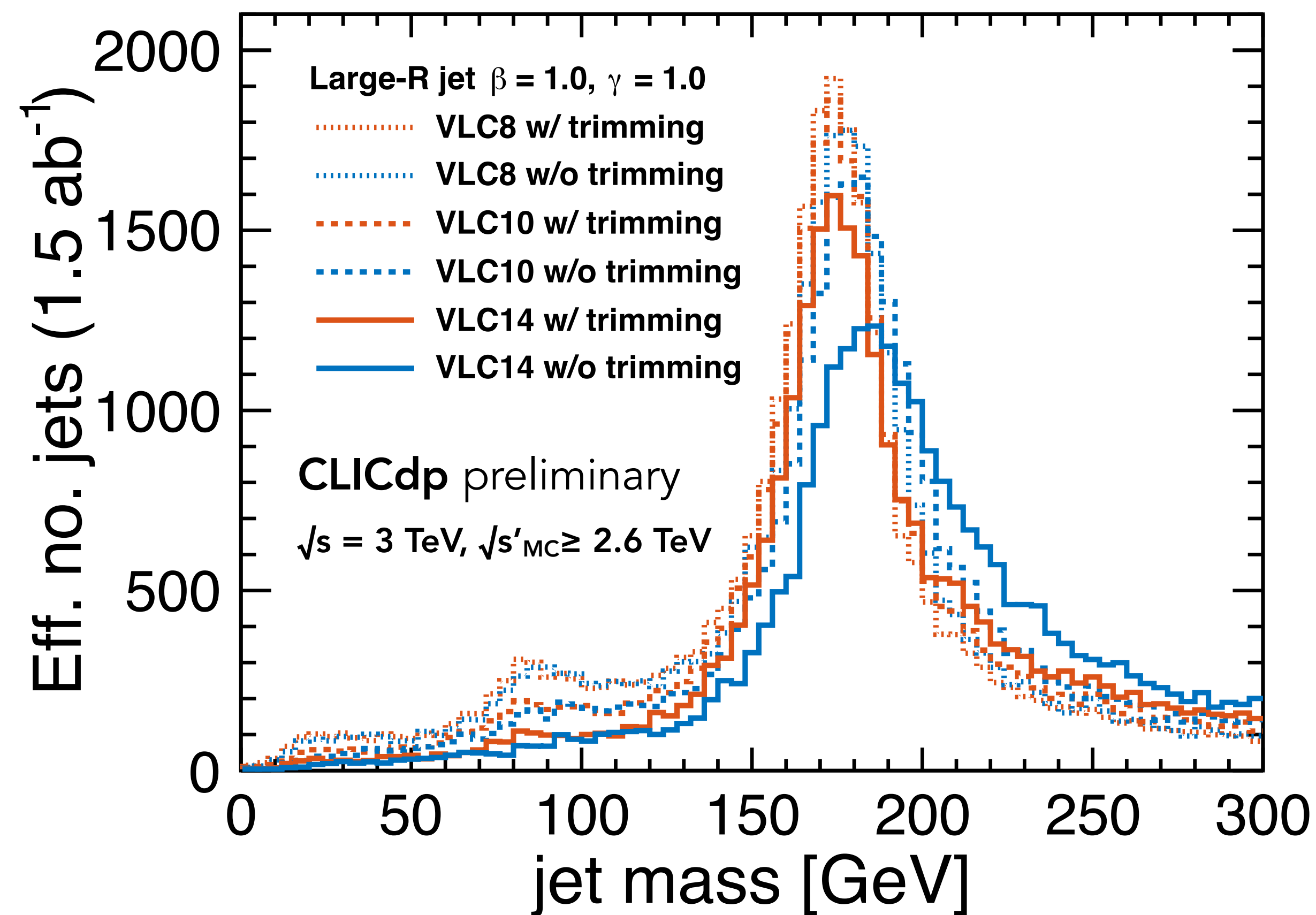
Angle between top decay products: W and b





- Tendency of higher \sqrt{s} ' events to be more collimated
- Large jet radius needed
 - see CLICdp-Note-2017-007 by Sascha Dreyer (for WW/ZZ: optimal $R \sim 0.8$)
 - adding b-quark $\rightarrow R=1.4(1.5)$ at 1.4 TeV (radiative), and $R=1.0$ at 3 TeV

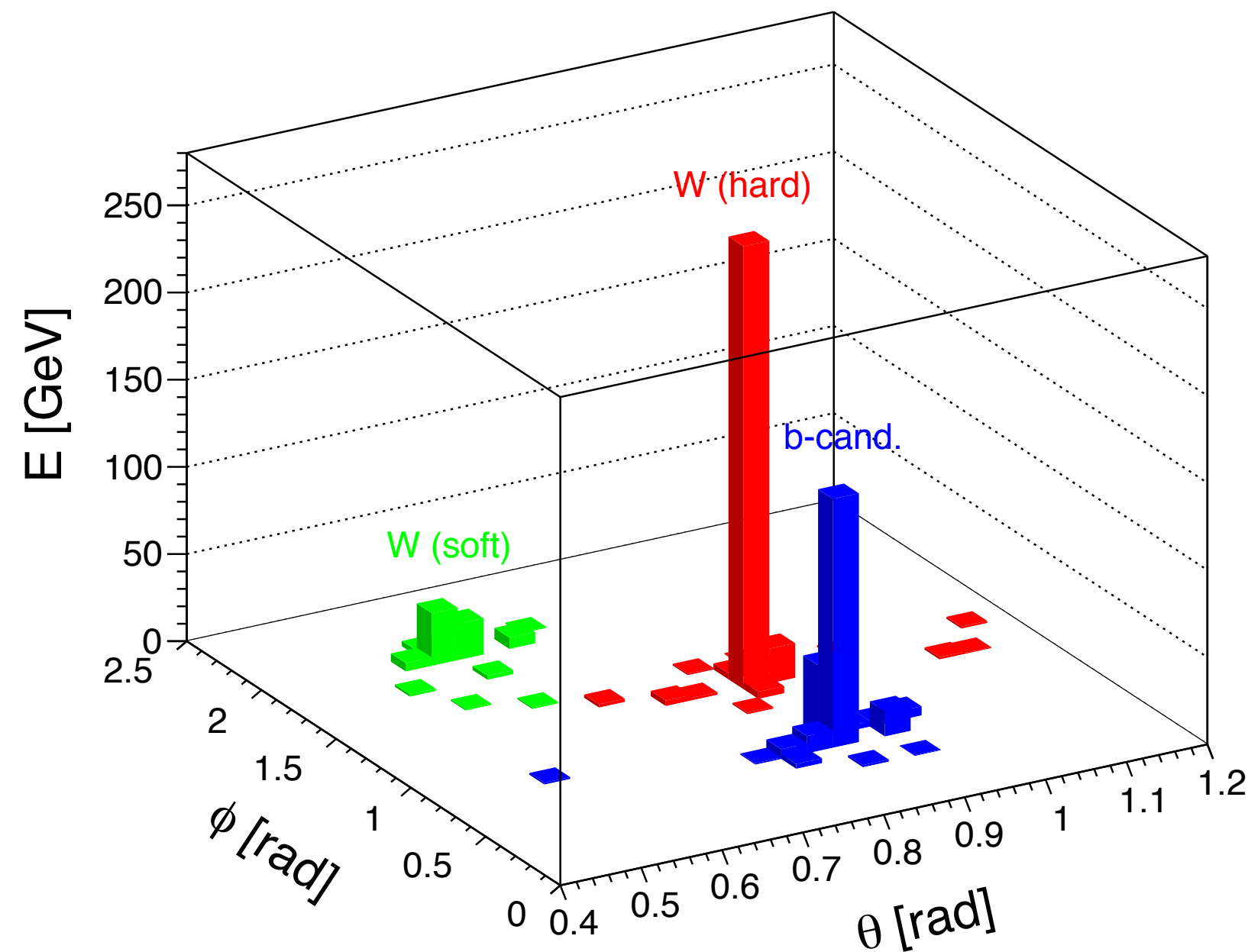
- Jet parameter optimisation done on fully-hadronic $t\bar{t}$ events (qqqqqq)
- VLC algorithm with 2 exclusive jets
 - The γ parameter - evolution of beam jet area with polar angle $\rightarrow 1.0$
 - The β parameter - changes the clustering order $\rightarrow 1.0$
- Pre-trimming of PFO collection useful; complementary way to reduce the impact from beamstrahlung
 - Pre-clustering into micro-jets ($R=0.4$); inclusive clustering with minimum p_T threshold ($E_{th}=5$ GeV)
 - Used for results at nominal collision energies: 1.4 TeV and 3 TeV



Strategy I: Top tagging

- The top-tagging is based on the Johns-Hopkins top tagger as implemented in FastJet ([DOI: 10.1103/PhysRevLett.101.142001](https://doi.org/10.1103/PhysRevLett.101.142001))
 - Iteratively decluster jet to search for true three- or four-prongy structures (de-clustering steered by two parameters: δ_R, δ_P)
 - Mass cuts on the resulting system:

$$m_t \in [120, 230] \text{ GeV}, m_W \in [50, 110] \text{ GeV}$$
- Since the background level is generally low at a lepton collider, the top tagger was optimised for high signal efficiency: qqqqqq (fully-hadronic ttbar sample). Previous studies show that MVA are powerful in removing remaining background.
- Optimisation: minimise four-quark background to provide **70% integrated signal efficiency for jet $p_T \in [500, 1500] \text{ GeV}$ and $\cos(\theta_{\text{jet}}) \leq 0.8$**
- Corresponding background efficiency: 4.4% (8.8%) for jets from the four-quark (di-jet) events



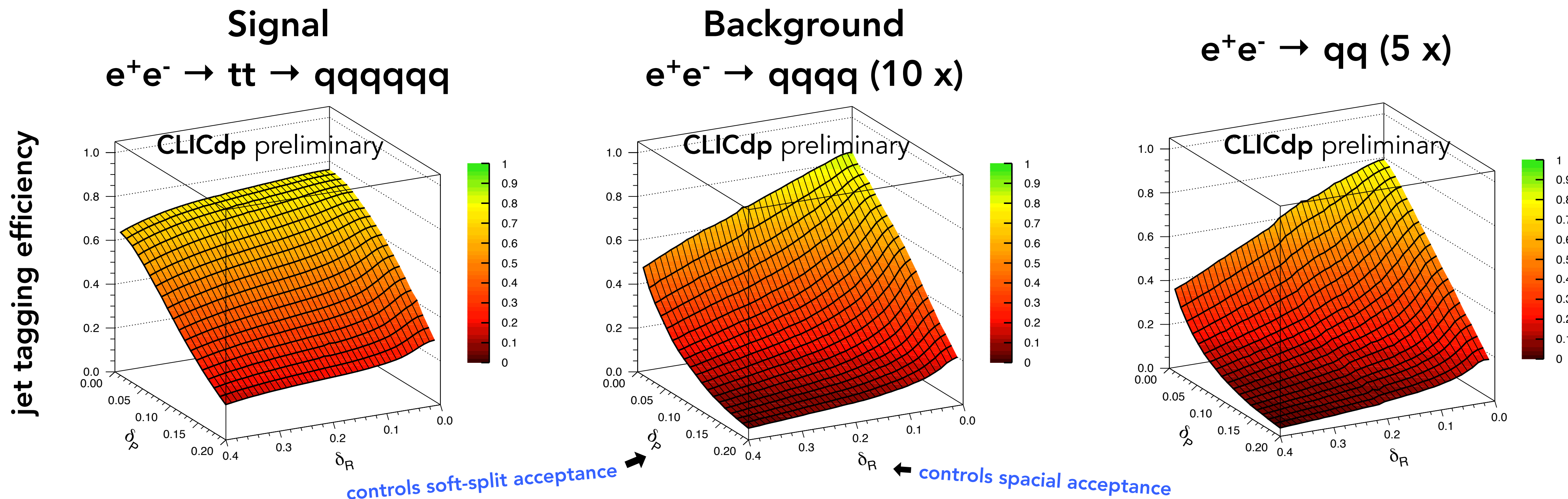


Top tagger optimisation at 1.4 TeV



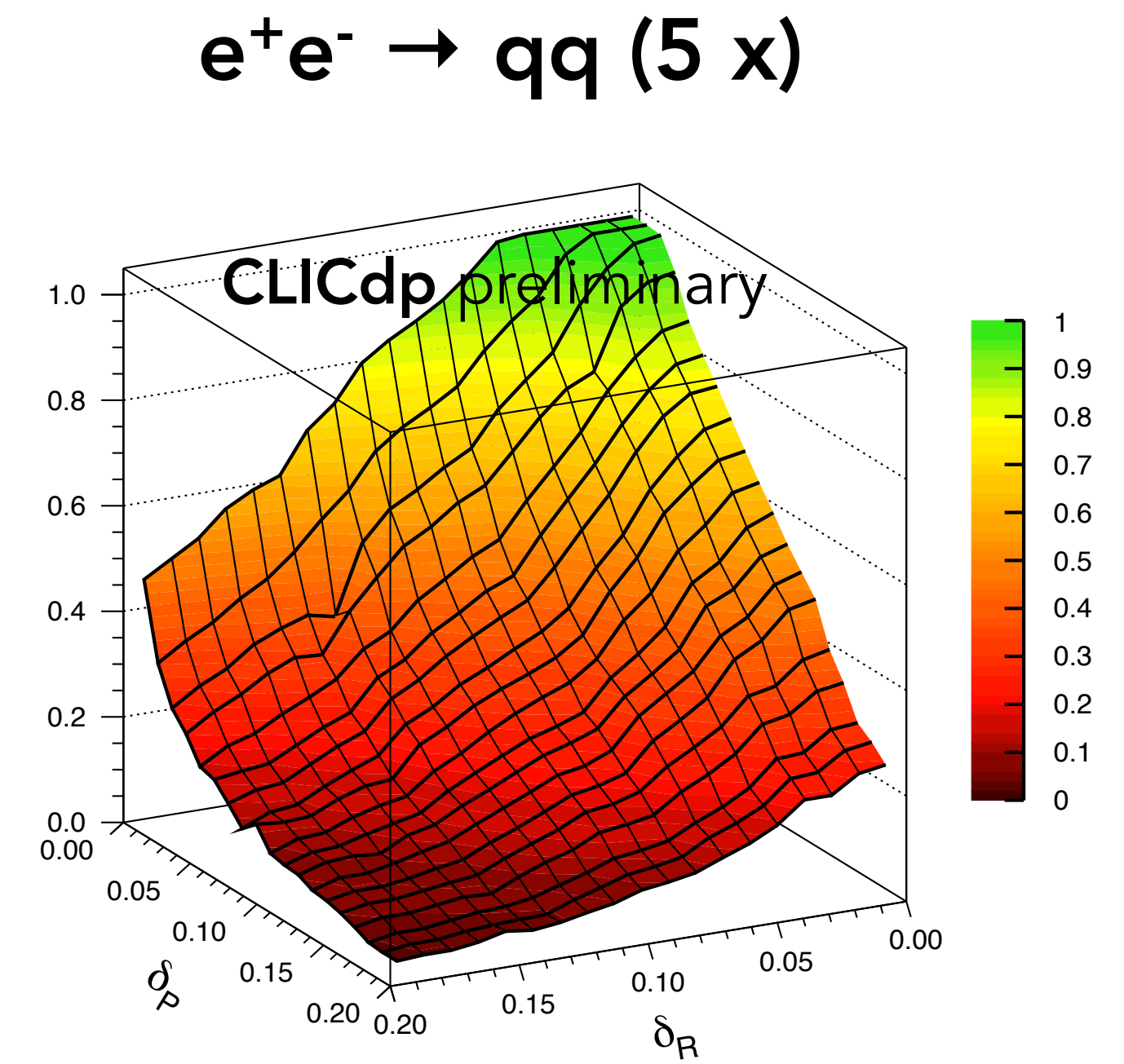
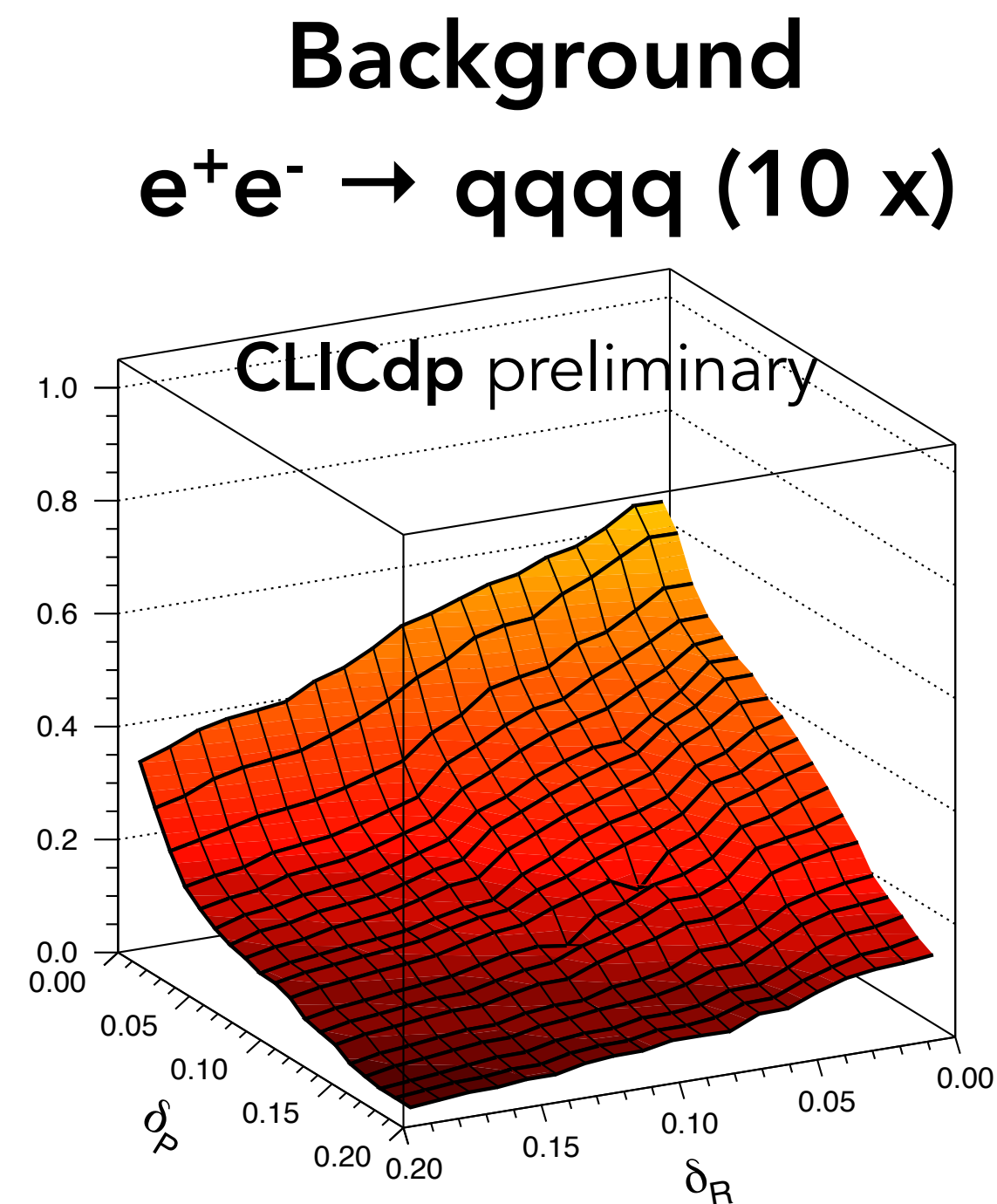
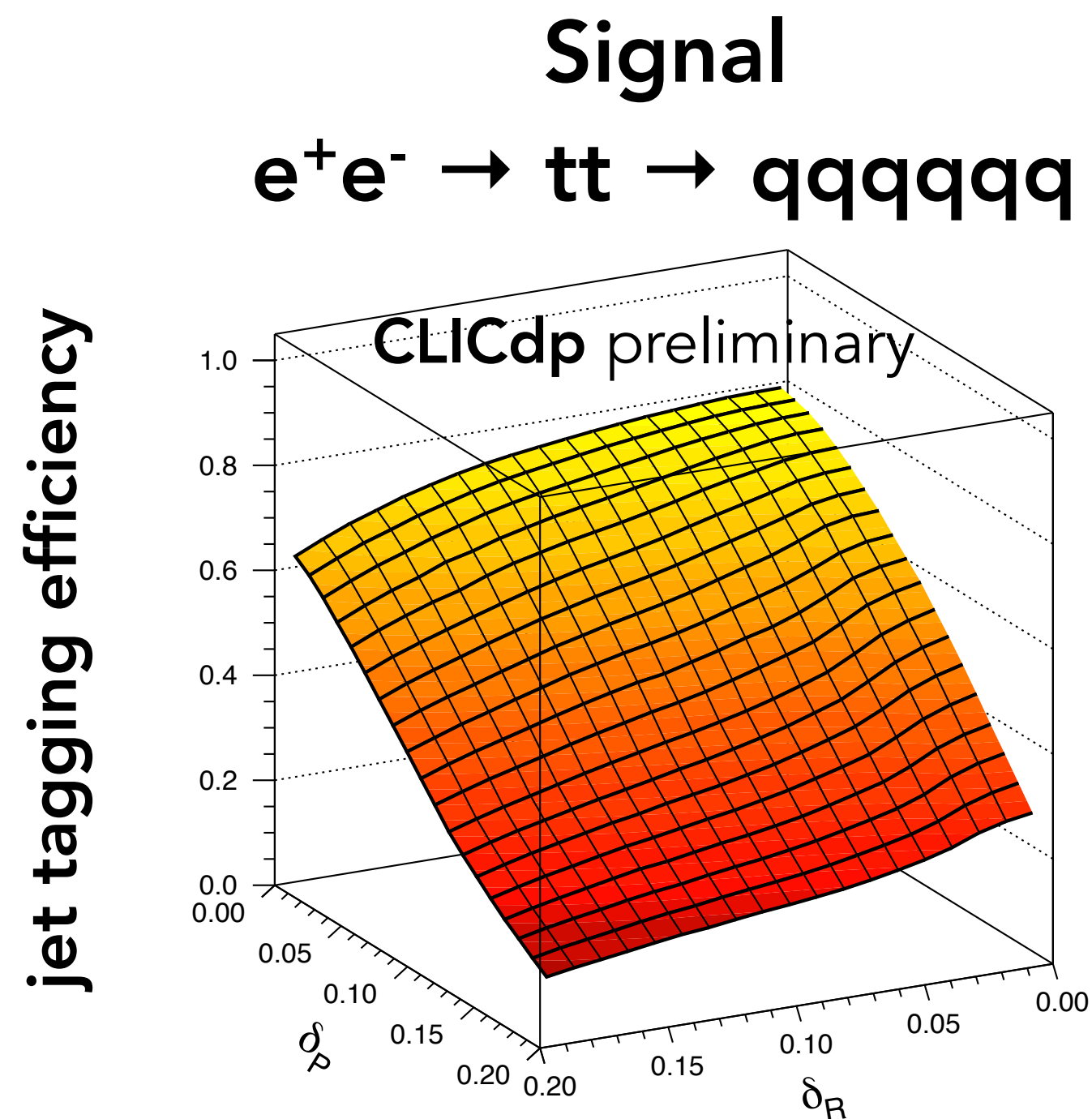
- VLC14 ($\beta=1.0$, $\gamma=1.0$), 2 exclusive, $0.00 \leq |\cos(\theta)| \leq 0.80$
- $50 \leq m_W \leq 110$, $120 \leq m_{\text{top}} \leq 230$ (loose)
- Hadronic tops optimised against hadronic W/Z background
- Optimal parameters: $\delta_R = 0.25$, $\delta_P = 0.03$

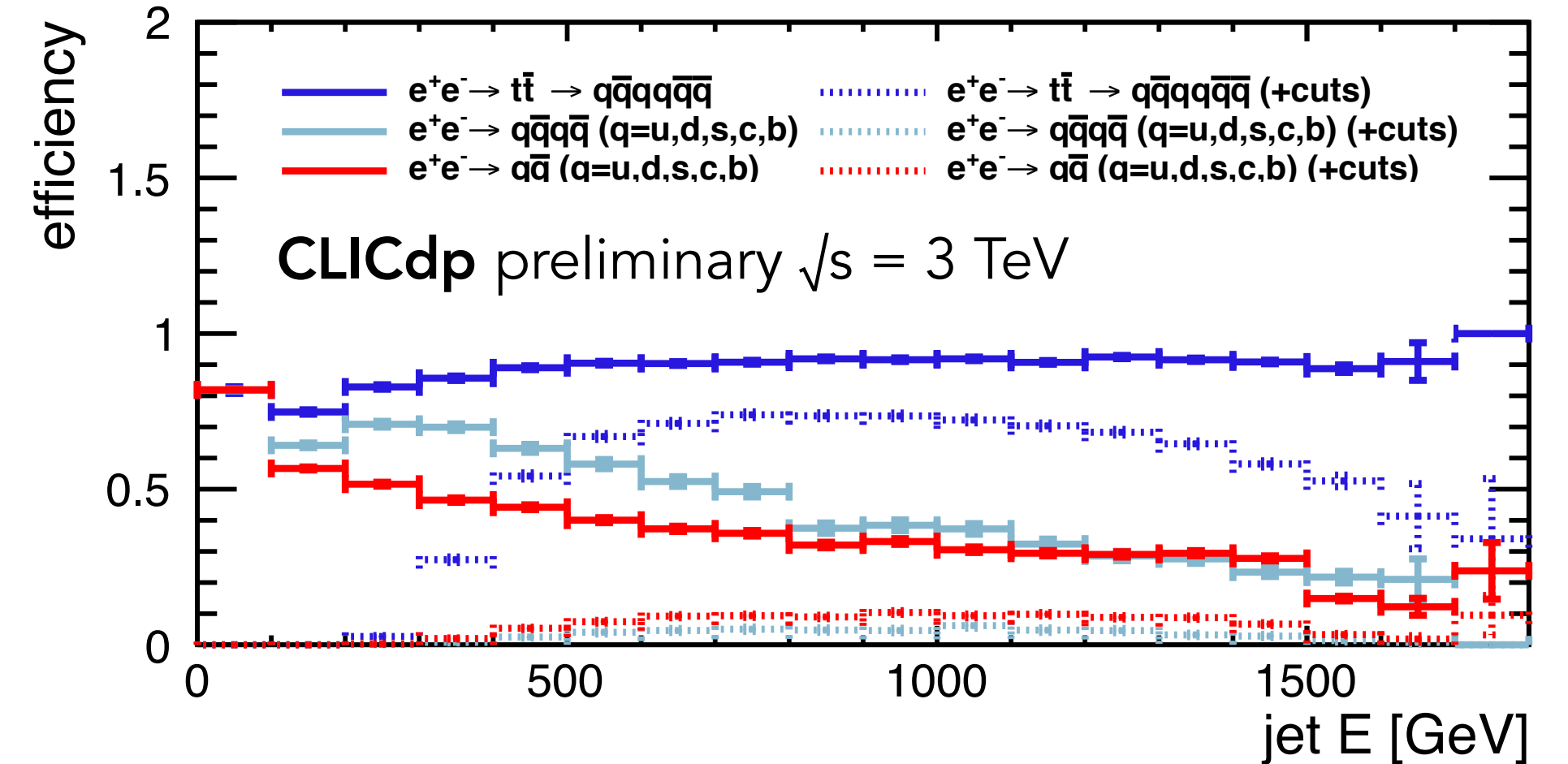
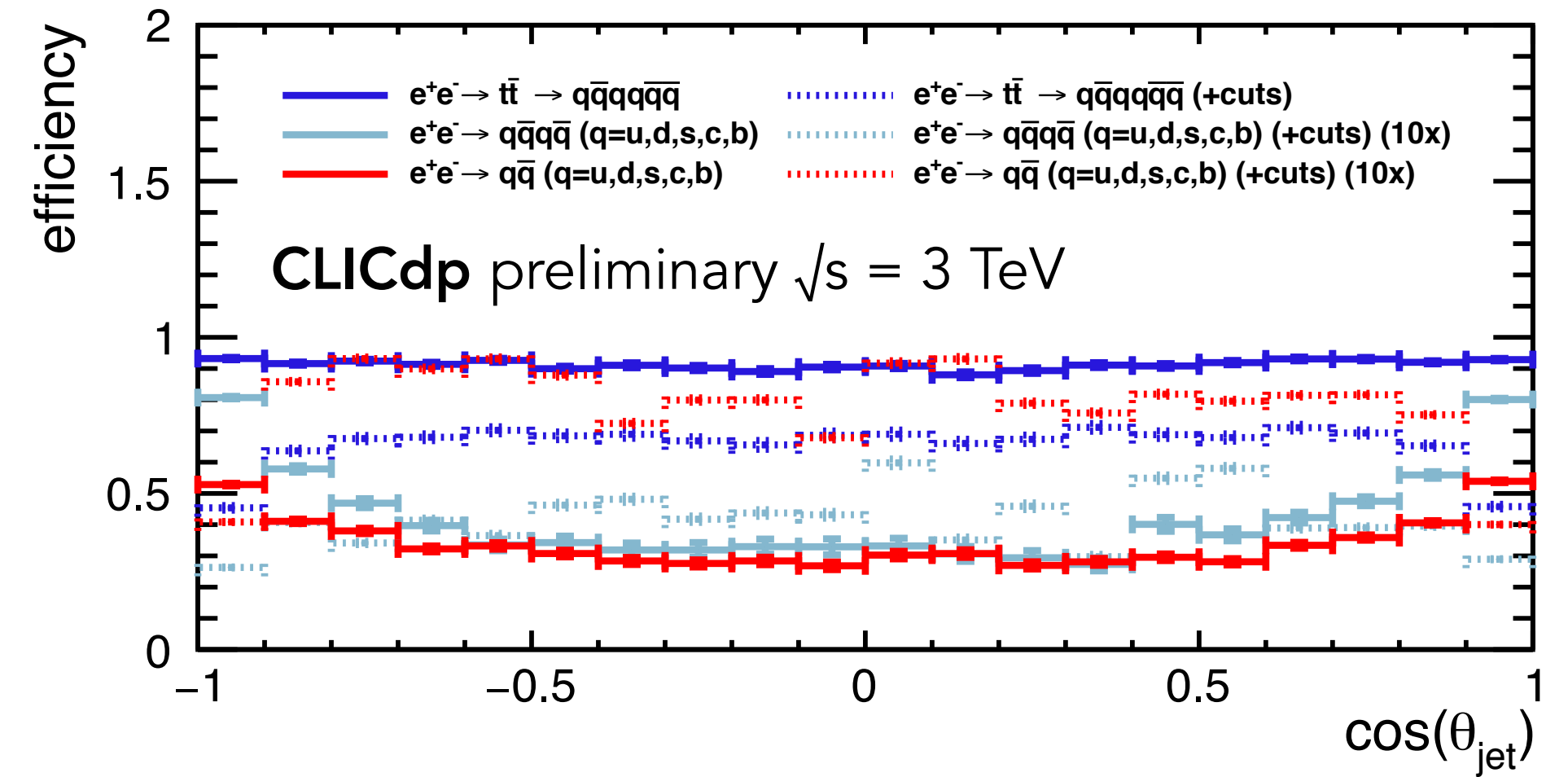
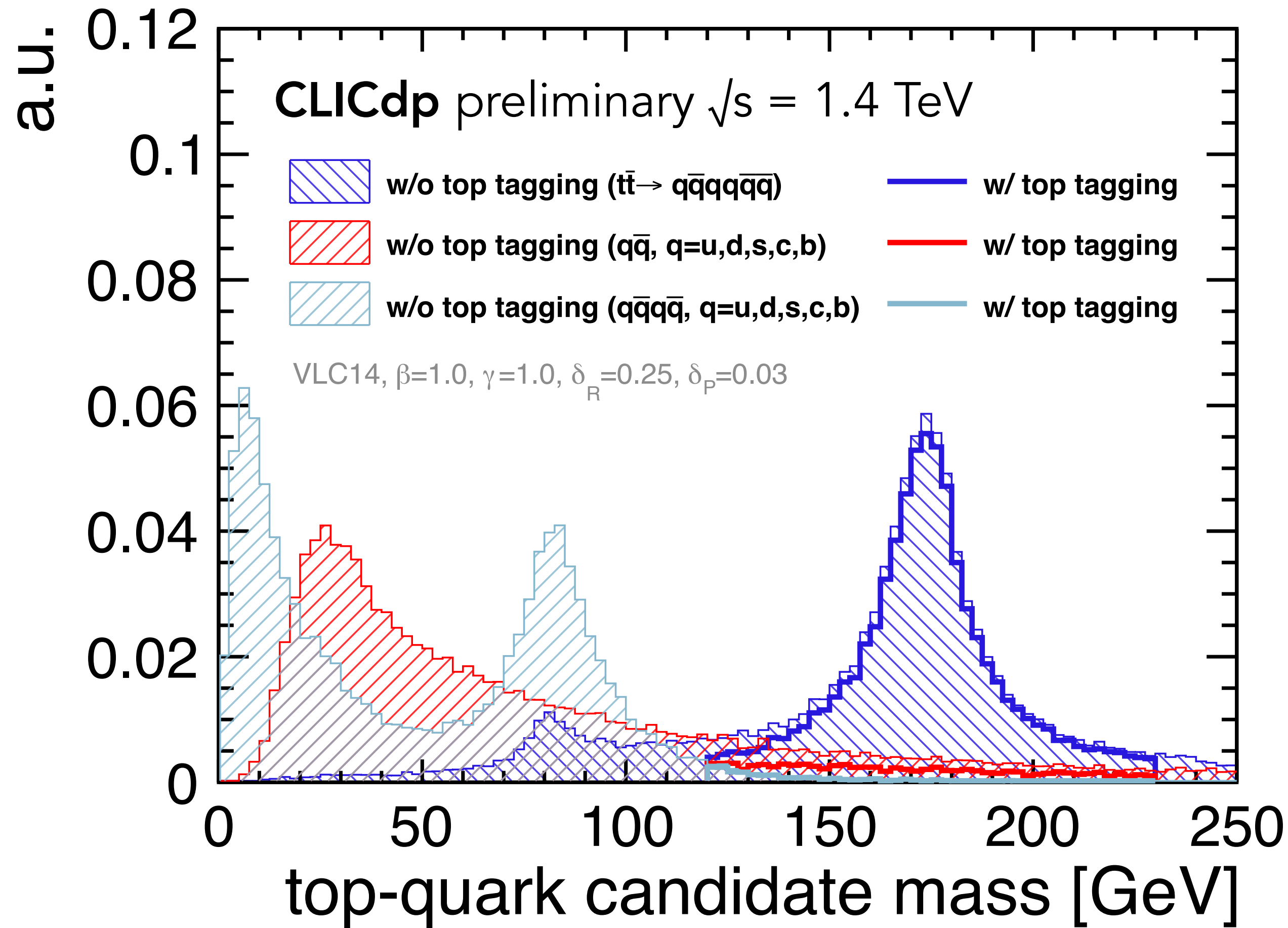
Optimisation: minimise four-quark background to provide **70% integrated signal efficiency for jet $p_T \in [500, 1500]$ GeV and $\cos(\theta_{\text{jet}}) \leq 0.8$**



- VLC10 ($\beta=1.0, \gamma=1.0$), 2 exclusive, $0.00 \leq |\cos(\theta)| \leq 0.80$
- $50 \leq m_W \leq 110, 120 \leq m_{\text{top}} \leq 230$ (loose)
- Hadronic tops optimised against hadronic W/Z background
- Optimal parameters: $\delta_R = 0.11, \delta_P = 0.03$

Optimisation: minimise four-quark background to provide **70% integrated signal efficiency for jet $p_T \in [500, 1500]$ GeV and $\cos(\theta_{\text{jet}}) \leq 0.8$**







Top pair production at $\sqrt{s} = 1.4$ (3) TeV

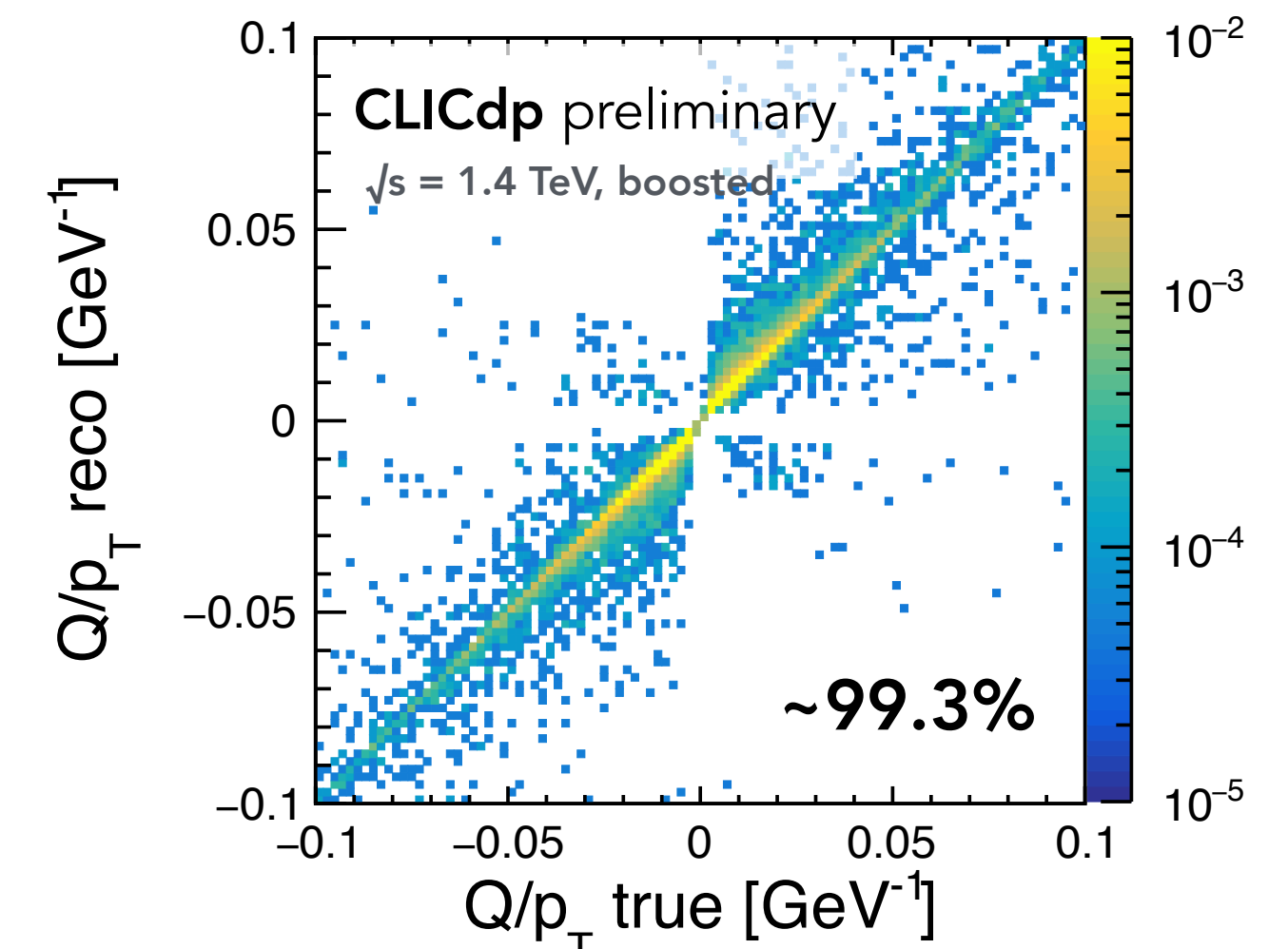
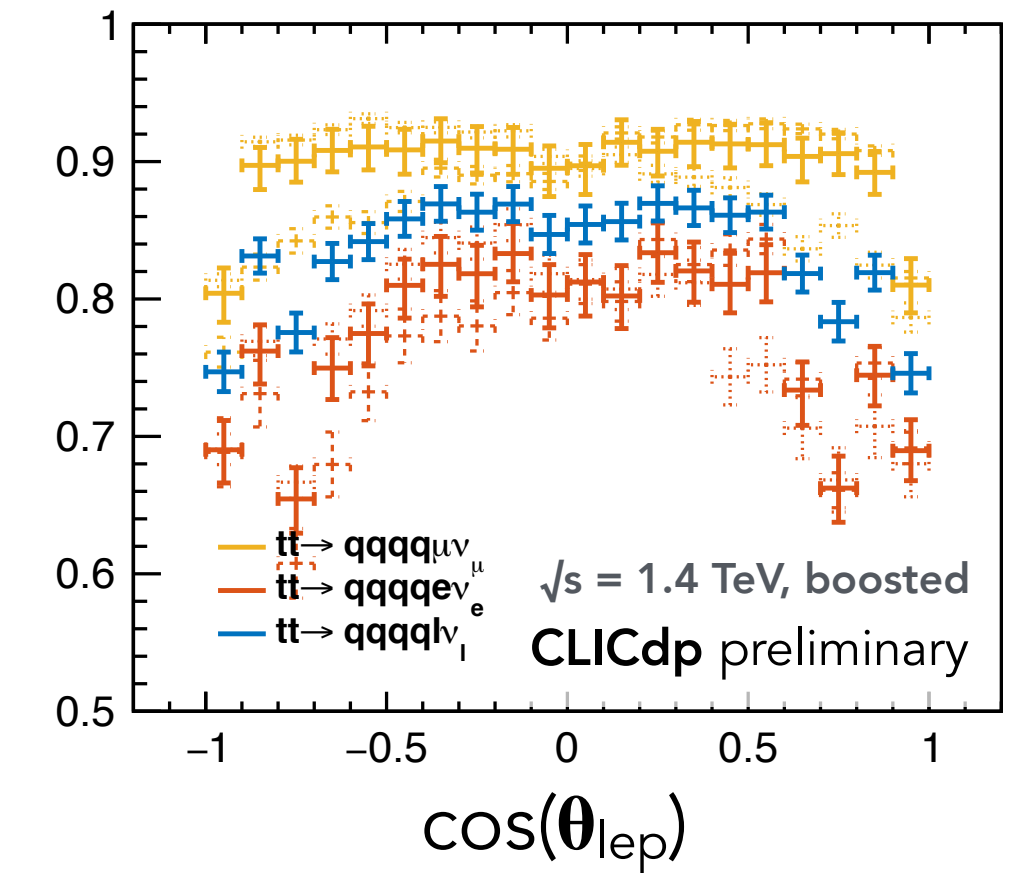


- Event selection using top-quark identification **strategy I – “Top tagging – parsing jet substructure”**

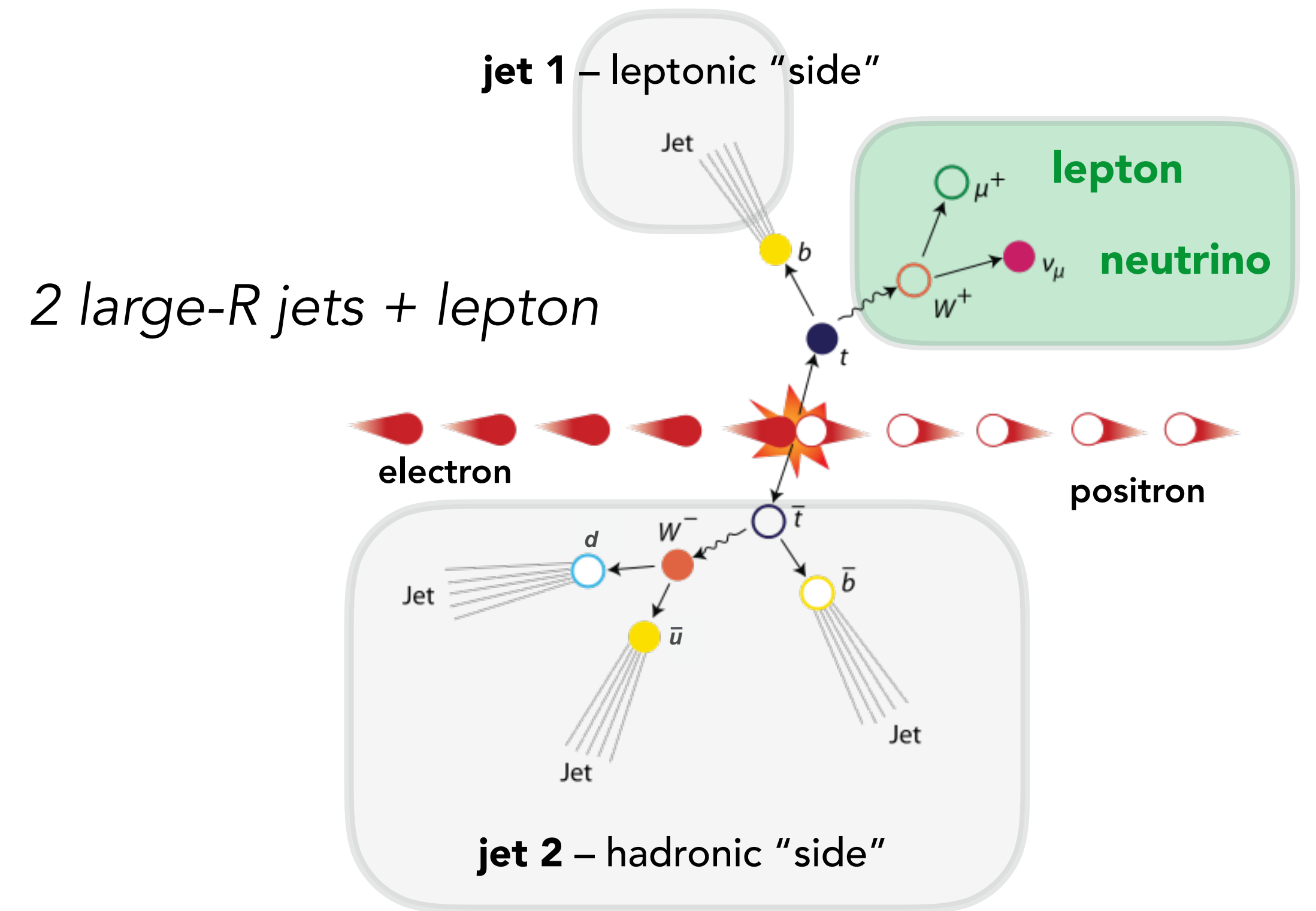
- 1 isolated lepton (electron or muon)
- 1 top-tagged large-R jet (hadronic top-quark candidate)
- No isolated high-energy photons
- Effective collision energy $\sqrt{s'}$ is reconstructed; cut applied at $\sqrt{s'} \geq 1.2$ (2.6) TeV (matching cut is applied at MC true level)
- Multivariate analysis exploiting kinematics of both the hadronically and leptonically decaying top quark (including the detailed output from the top-tagger), event missing p_T , visible energy and event shape, lepton kinematics, flavour tagging, jet splitting scales, and substructure variables

Isolated lepton

Isolated lepton efficiency vs. lepton polar angle



- The effective collision energy $\sqrt{s'}$ is reconstructed to be able to study the electroweak production at/close-to the nominal collision energy
- Reconstruction:
 - In addition to the neutrino, missing energy/momentum also appear in the forward direction (ISR, beamstrahlung)
 - Assumption: neutrino $p_T = \sqrt{(p_x^2 + p_y^2)}$ (MET)
 - The lepton+neutrino system constrained to m_W
 - The equation is quadratic in p_z , and has no solution if X is imaginary. In such cases the MET is scaled to provide a real solution ($X=0$)
 - We select the solution closest to m_{top} when combined with one of the large-R jets

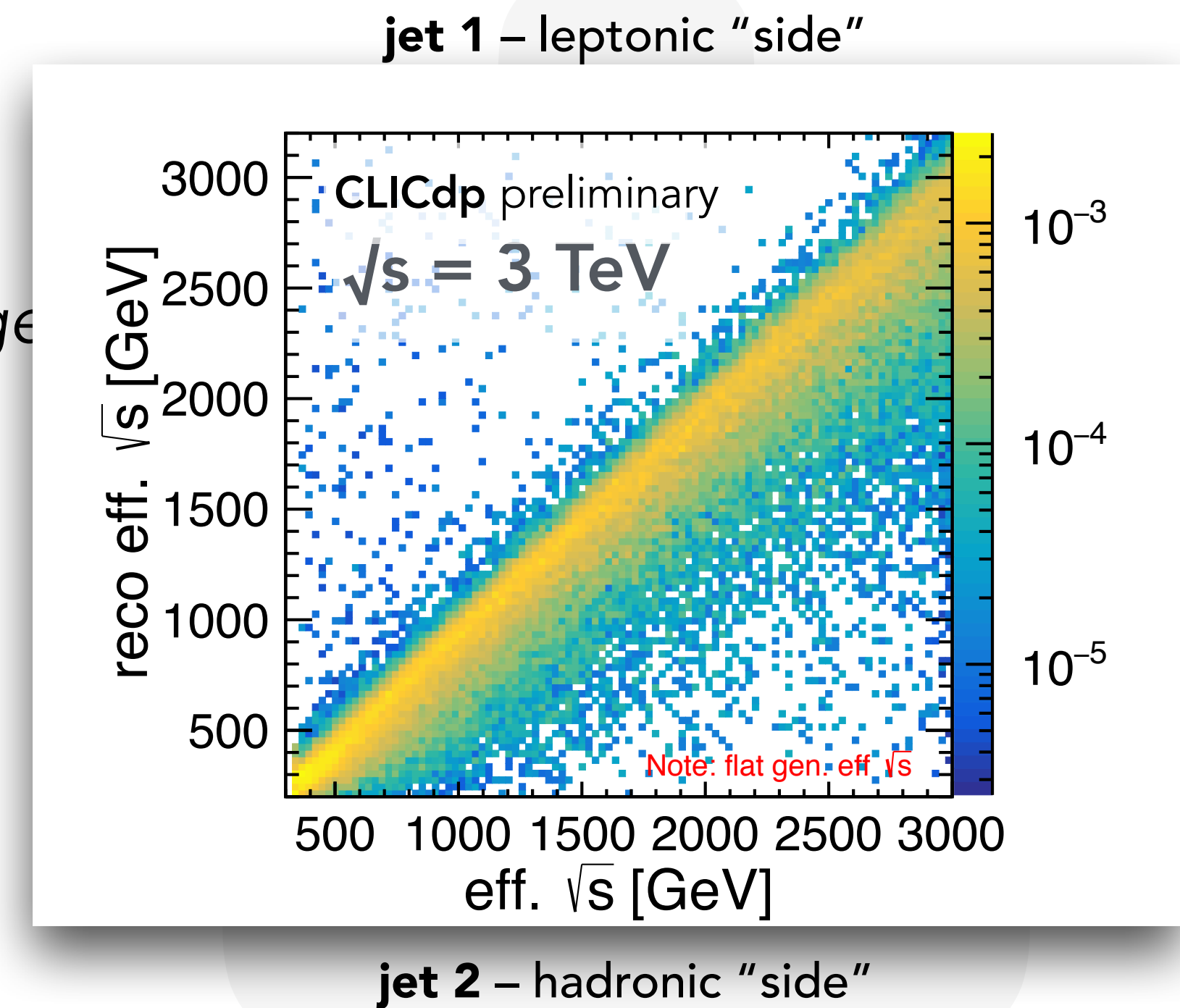


$$p_{\nu,z} = \frac{1}{2(p_{l,z}^2 - E_l^2)} (p_{l,z} m_l^2 - p_{l,z} M_W^2 - 2p_{l,x} p_{l,z} p_{\nu,x} - 2p_{l,y} p_{l,z} p_{\nu,y} + X)$$

$$X = \sqrt{E_l^2 [(M_W^2 - m_l^2 + 2(p_{l,x} \cdot p_{\nu,x} + p_{l,y} \cdot p_{\nu,y}))^2 + 4\mathcal{E}_T^2 (-E_l^2 + p_{l,z}^2)]}$$

- The effective collision energy $\sqrt{s'}$ is reconstructed to be able to study the electroweak production at/close-to the nominal collision energy
- Reconstruction:
 - In addition to the neutrino, missing energy/momentum also appear in the forward direction (ISR, beamstrahlung)
 - Assumption: neutrino $p_T = \sqrt{(p_x^2 + p_y^2)}$ (MET)
 - The lepton+neutrino system constrained to m_W
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2 large

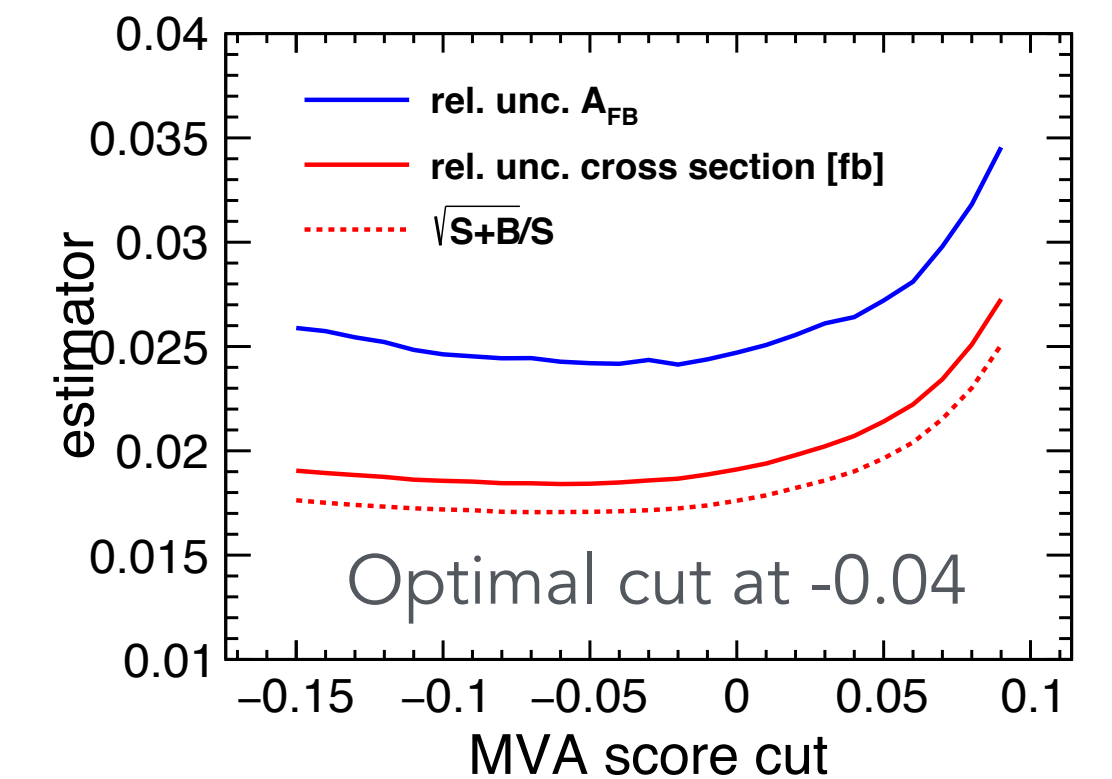


$$p_{\nu,z} = \frac{1}{2(p_{l,z}^2 - E_l^2)} (p_{l,z} m_l^2 - p_{l,z} M_W^2 - 2p_{l,x} p_{l,z} p_{\nu,x} - 2p_{l,y} p_{l,z} p_{\nu,y} + X)$$

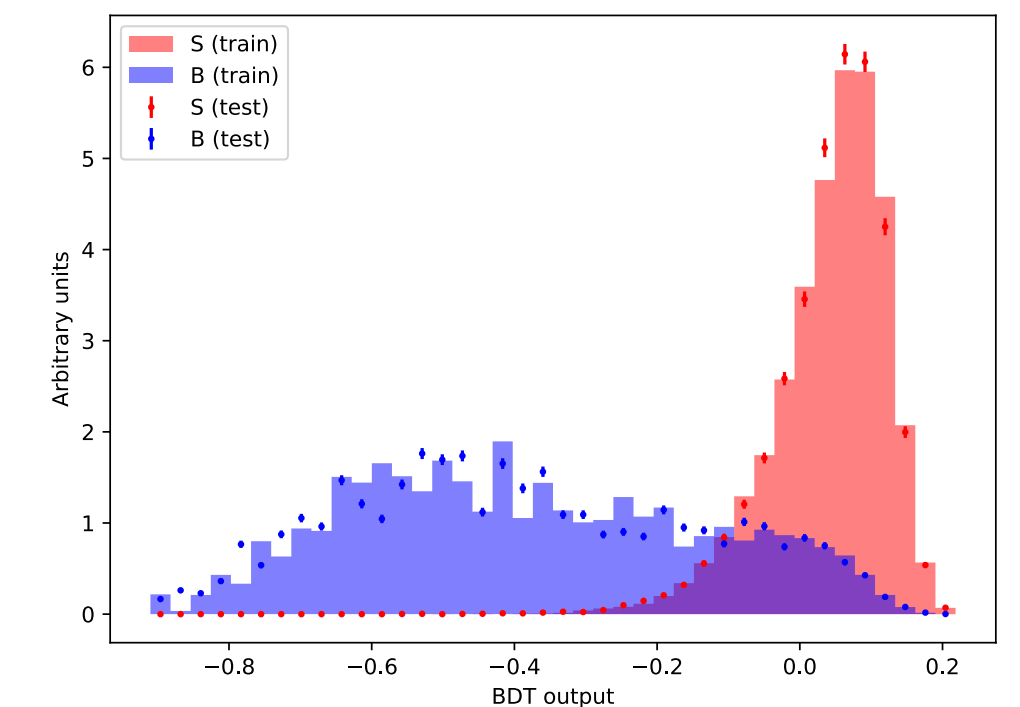
$$X = \sqrt{E_l^2 [(M_W^2 - m_l^2 + 2(p_{l,x} \cdot p_{\nu,x} + p_{l,y} \cdot p_{\nu,y}))^2 + 4\mathcal{E}_T^2 (-E_l^2 + p_{l,z}^2)]}$$

- Background rejection performance limited with single MVA, likely due to the large variety of backgrounds (some mimicking signal well and others not)
- Found that dedicated MVAs targeting certain backgrounds separately was useful
- Pre-MVA scores are fed into final MVA
- Using 2→1 approach
 - MVA1 focus on qq++ events (qq, qqvv, qqll, qqlv, qqlvlv)
 - MVA2 focus qqqq, qqqqqq
 - MVA3 focus on all backgrounds
- Each MVA uses the 20 most important variables and the parameters of the algorithm are tuned to reduce overtraining
- Examples of important variables: score from MVA1/MVA2, missing p_T , event shape variables, top mass/energy, NSubjettiness τ_3/τ_2 , sum of b-tags, y_{34} , mass of leptonic top
- MVA cut optimisation done on final observables: cross section and A_{FB}

$\sqrt{s} = 1.4 \text{ TeV } P(e^-) = -80\%$



$\sqrt{s} = 1.4 \text{ TeV } P(e^-) = -80\%$





Event selection summary



Event selection summary for the analysis of events at nominal collision energy 380 GeV, 1.4 TeV and 3 TeV

Dataset		Signal $e^+e^- \rightarrow tt \rightarrow qqql\nu$ ($l=e,\mu$)	
\sqrt{s}	P(e^-)	(Reconstructed events)	Signal purity
380 GeV	-80 %	25540	85 %
	+80%	12687	85 %
1.4 TeV	-80 %	5051	68 %
	+80%	2854	72 %
3 TeV	-80 %	1711	60 %
	+80%	1038	66 %



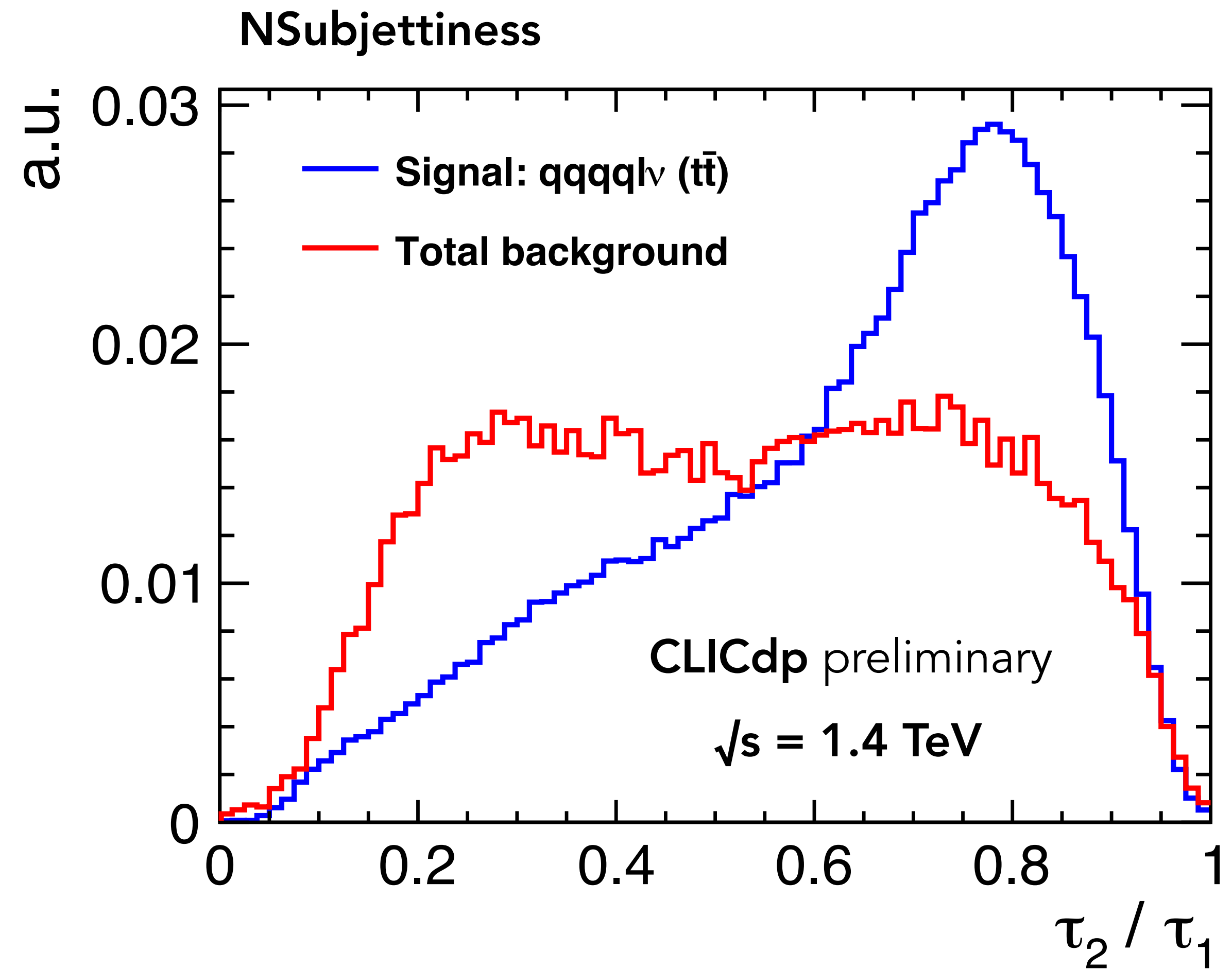
Analysis of radiative events at 1.4 TeV



- Event selection using top-quark identification **strategy II - "MVA-based – using substructure variables"**
 - 1 isolated lepton (electron or muon)
 - Associate large-R jet with highest energy with the hadronically decaying top
 - Pre-cuts to remove background
 - Quality-cuts to reduce the effect of migrations
 - Effective collision energy $\sqrt{s'}$ is reconstructed using a kinematic fit; cuts applied to define three regions-of-interest (matching cuts are applied at MC true level)
 - Multivariate analysis exploiting for example kinematics of both the hadronically and leptonically decaying top quark, visible p_T/E , lepton kinematics, flavour tagging, event shape, jet splitting scales, and substructure variables

- **Substructure variables:**

- Jet multiplicity (number of PFO within large-R jet)
- NSubjettiness (metric for determining the number of subjets within fat-jet) (J.Thaler, K. Van Tilburg, arXiv:1011.2268)
- Angular relations (relative angles between subjet pairs, identifies forced splitting)





Event selection summary



Event selection summary for the analysis of radiative events at nominal collision energy 1.4 TeV

Dataset $\sqrt{s} = 1.4 \text{ TeV}$	$P(e^-)$	Signal $e^+e^- \rightarrow tt \rightarrow qqql\nu$ ($l=e,\mu$) (Reconstructed events)	Signal purity
$0.40 \leq \sqrt{s'} \leq 0.90 \text{ TeV}$	-80 %	449	44 %
	+80%	300	50 %
$0.90 \leq \sqrt{s'} \leq 1.2 \text{ TeV}$	-80 %	2352	36 %
	+80%	1116	36 %
$1.2 \leq \sqrt{s'} \leq 1.4 \text{ TeV}$	-80 %	4349	58 %
	+80%	2244	58 %

$$\frac{d\sigma}{d(\cos(\theta^*))} = \sigma_1(1 + \cos(\theta^*))^2 + \sigma_2(1 - \cos(\theta^*))^2 + \sigma_3(1 - \cos^2(\theta^*))$$

- Equation describes the differential cross section for the top quarks in the $t\bar{t}$ centre-of-mass system
- At tree level the three terms can be related to the cross sections for producing top-quark pairs with different helicity combinations in the final state
- Note that anti-tops are added with inverted sign
- The cross section and asymmetry are **extracted from fit**
- Detector efficiency included
- Statistical uncertainty from background included



Observable definitions:

$$\sigma_{t\bar{t}} = \sigma_F + \sigma_B = (4/3)(2\sigma_1 + 2\sigma_2 + \sigma_3)$$

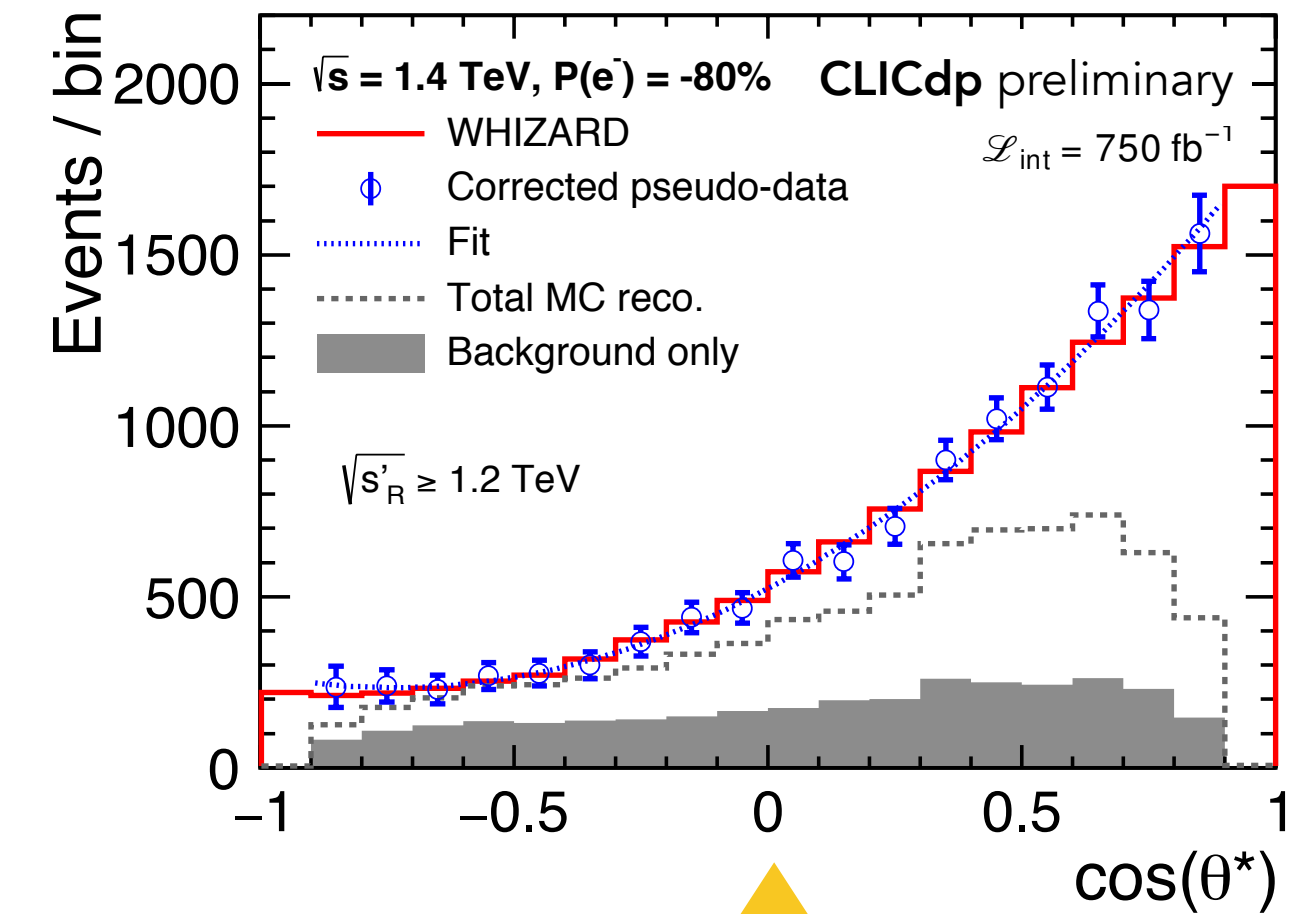
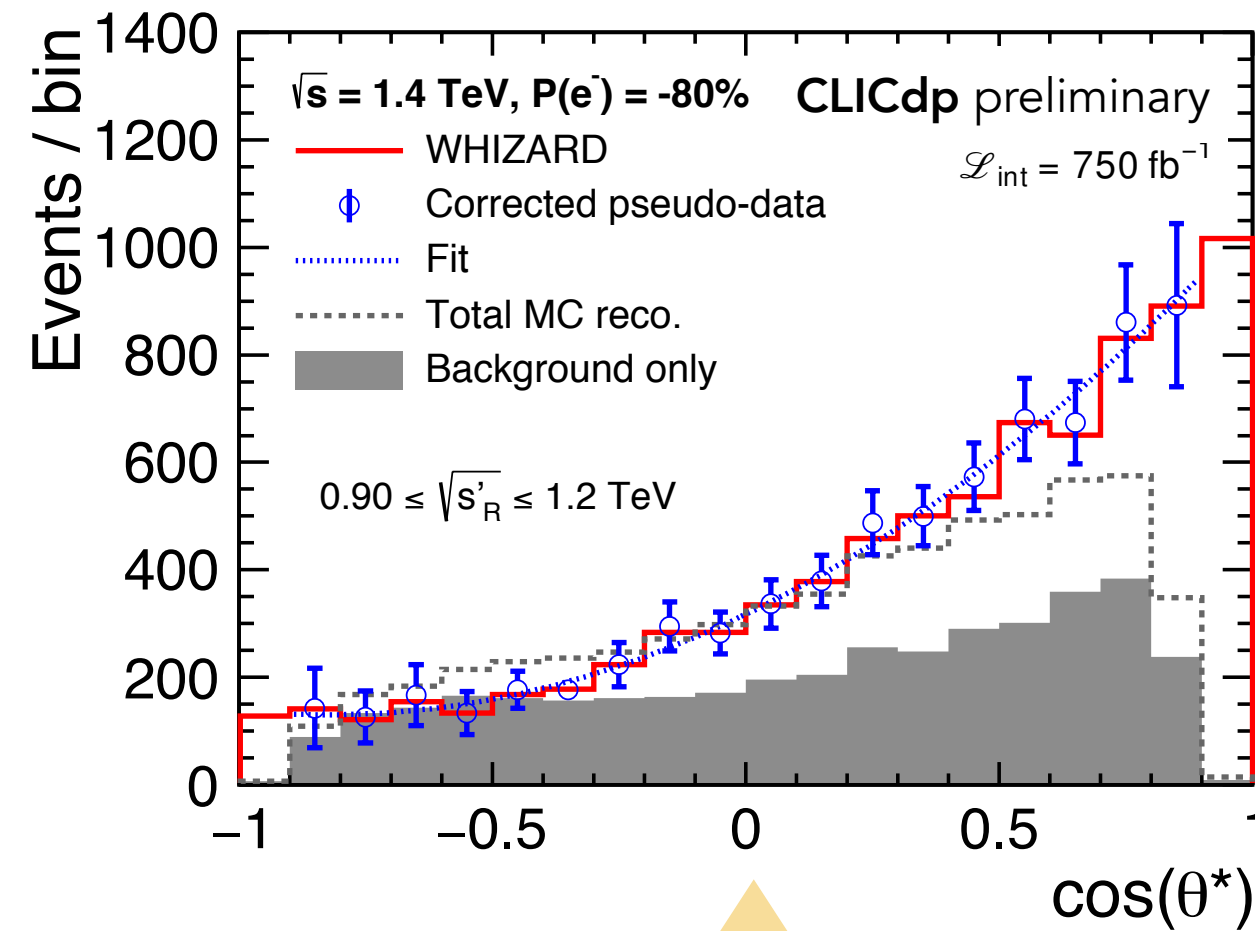
$$A_{\text{FB}} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} = \frac{1}{\sigma_{t\bar{t}}} 2(\sigma_1 - \sigma_2)$$



Results – radiative events at 1.4 TeV



- Results from the analysis of radiative events at 1.4 TeV using **strategy II**



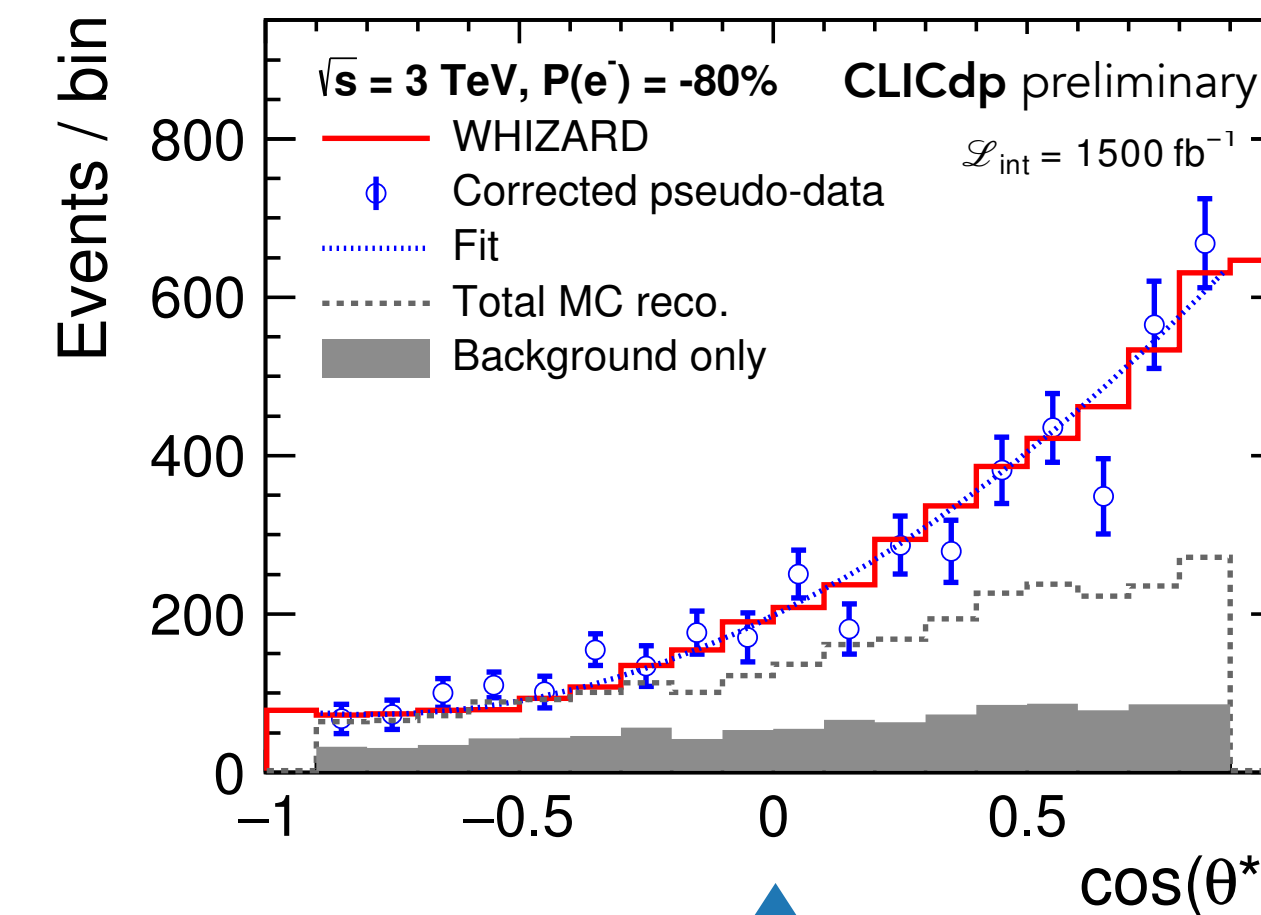
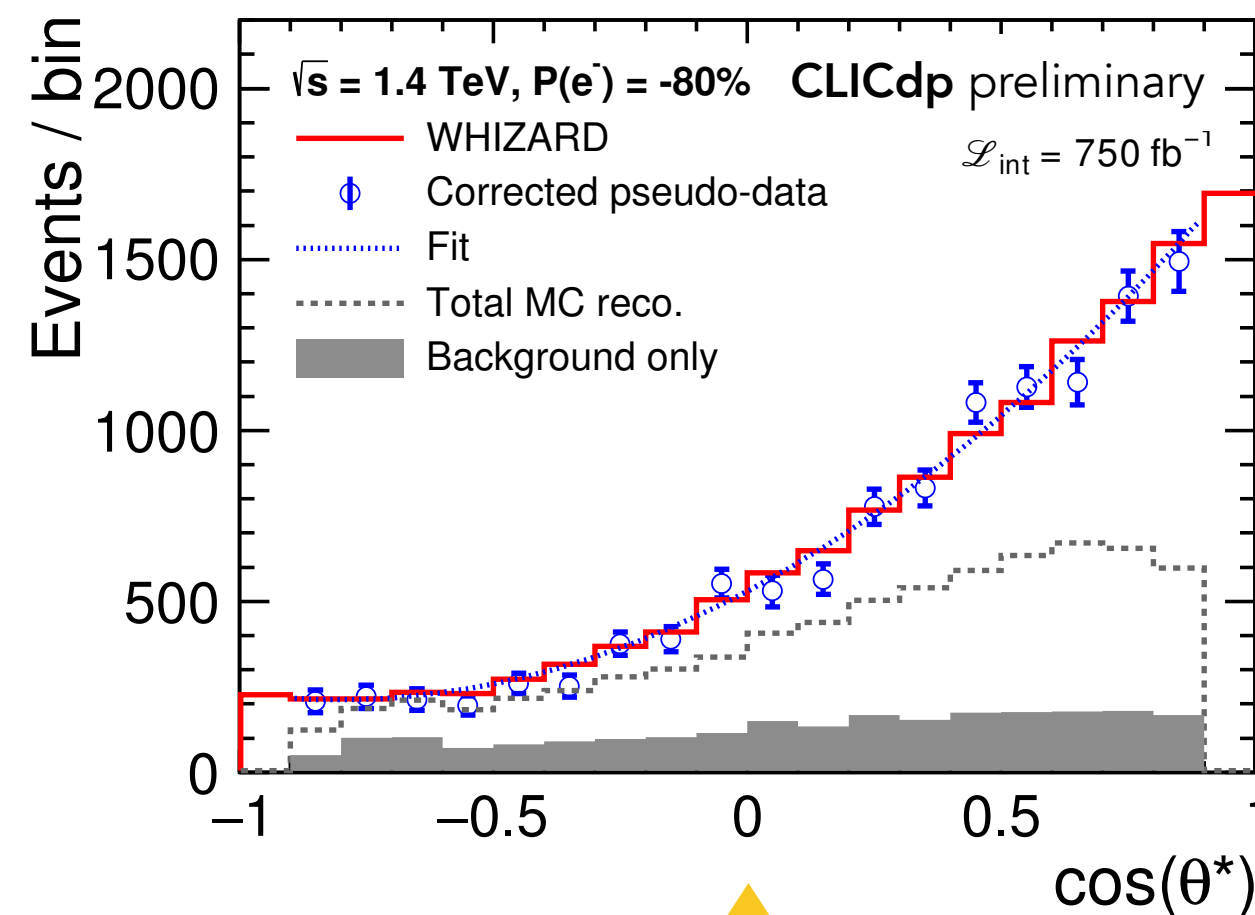
CLICdp preliminary	$0.40 \leq \sqrt{s'} \leq 0.90 \text{ TeV}$		$0.90 \leq \sqrt{s'} \leq 1.2 \text{ TeV}$		$1.2 \leq \sqrt{s'} \leq 1.4 \text{ TeV}$	
$P(e^-)$	-80 %	+80%	-80 %	+80%	-80 %	+80%
$A_{\text{FB}} \text{ Reco}$	0.458 ± 0.081 (18%)	0.514 ± 0.105 (20%)	0.546 ± 0.034 (6.2%)	0.588 ± 0.045 (7.7%)	0.562 ± 0.018 (3.2%)	0.621 ± 0.024 (3.7%)
$\sigma \text{ Reco [fb]}$	16.56 ± 1.31 (7.9%)	8.63 ± 0.83 (9.6%)	11.01 ± 0.38 (3.5%)	5.87 ± 0.29 (4.9%)	18.41 ± 0.37 (2.0%)	9.84 ± 0.28 (2.8%)



Results at nominal collision energy

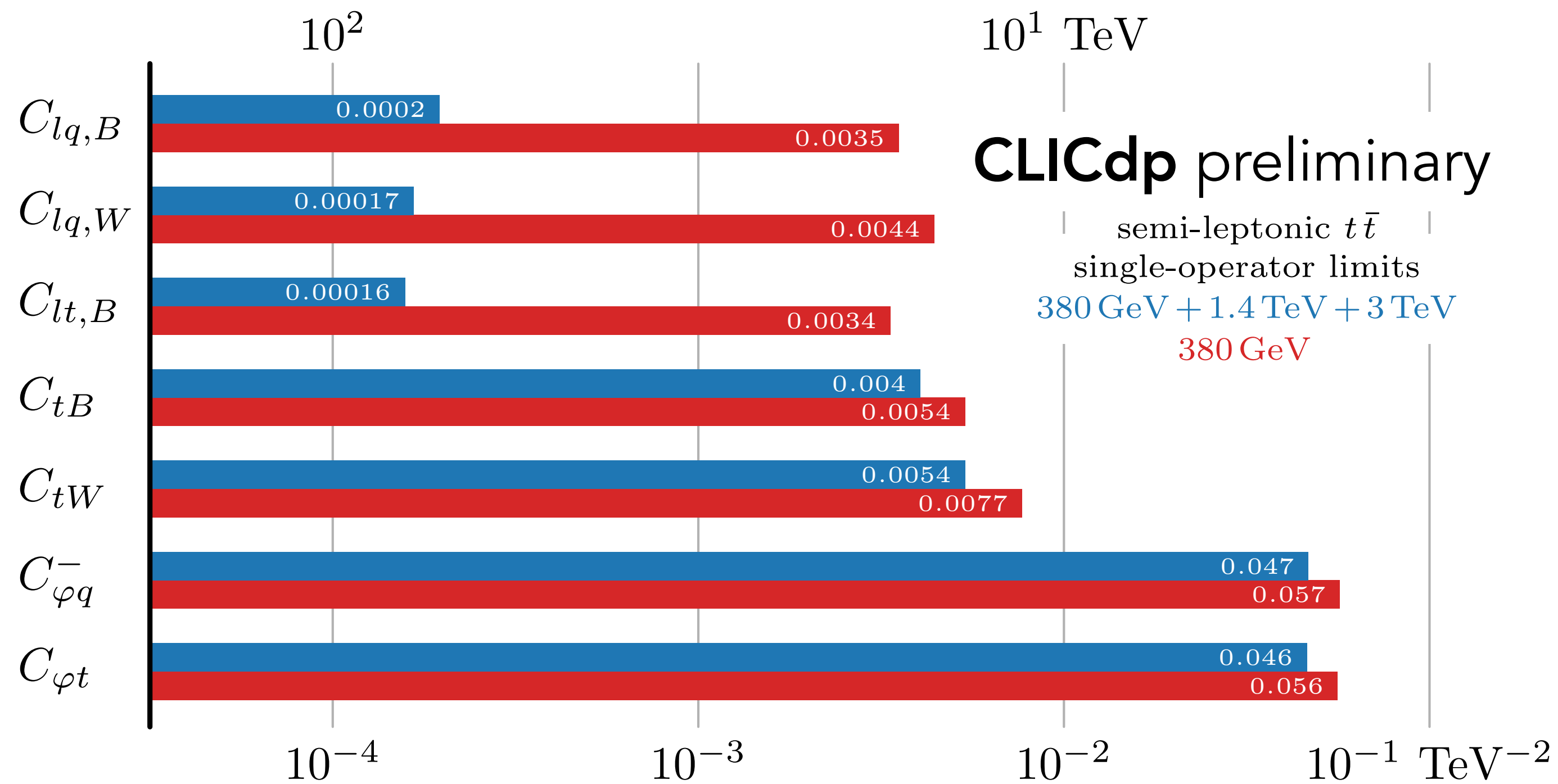


- Results from the analysis at nominal collision energy 1.4 and 3 TeV using **strategy I**



CLICdp preliminary	$\sqrt{s} = 380 \text{ GeV}$		$\sqrt{s} = 1.4 \text{ TeV}$		$\sqrt{s} = 3 \text{ TeV}$	
	$P(e^-) = -80\%$	$P(e^-) = +80\%$	$P(e^-) = -80\%$	$P(e^-) = +80\%$	$P(e^-) = -80\%$	$P(e^-) = +80\%$
$A_{\text{FB}} \text{ Reco}$	0.1761 ± 0.0094 (5.3%)	0.207 ± 0.0084 (4.1%)	0.567 ± 0.014 (2.5%)	0.620 ± 0.016 (2.6%)	0.596 ± 0.022 (3.7%)	0.645 ± 0.028 (4.3%)
$\sigma \text{ Reco [fb]}$	161.00 ± 1.09 (0.68%)	75.97 ± 0.73 (0.96%)	18.44 ± 0.34 (1.8%)	9.84 ± 0.23 (2.3%)	3.52 ± 0.12 (3.4%)	1.91 ± 0.08 (4.2%)

- Adding the multi-TeV analyses to the EFT fit leads to large improvement
- BSM effect described through effective dim-6 operators:

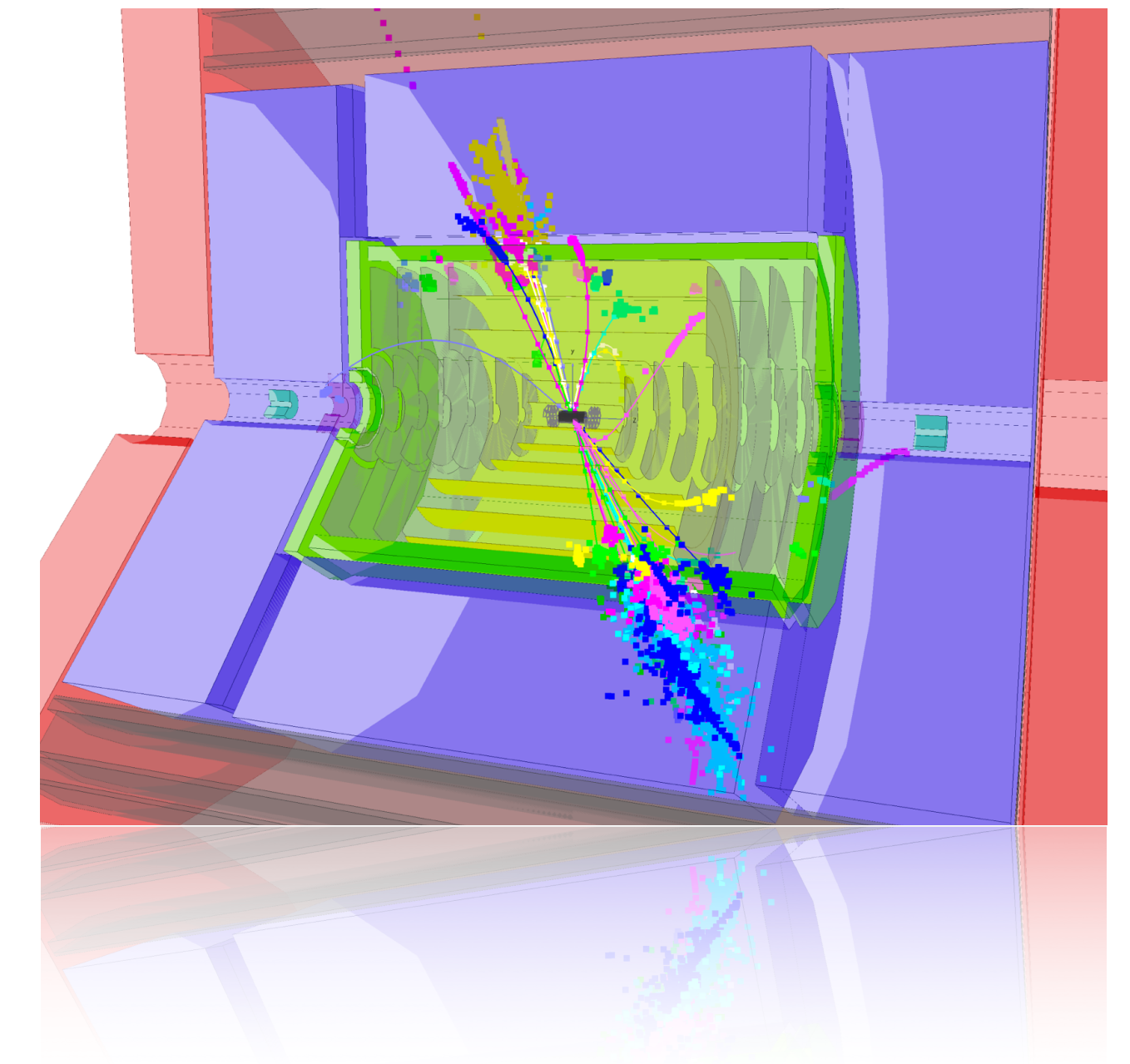


$$\mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{SM}} + \sum_i C_i Q_i$$

← Wilson coefficients

See more details in talk "EFT fits of top physics at ILC and CLIC" by Martín Perelló Roselló (later today)

- **Top pair production** is studied at all stages of **CLIC**
- Results for production cross section and forward-backward asymmetry were presented in this talk and are interpreted in a top-philic EFT approach (talk by Martín Perelló Roselló later today)
- **Multi-TeV** analyses leads to **significant improvements** for 4-fermion “contact operators” while 2-fermion “vertex operators” are best measured at 380 GeV
- **Top physics overview paper in CLICdp collaboration review**
 - See also talk by Filip Zarnecki (tomorrow) on **FCNC top decays** at 380 GeV
 - Talk by Yixuan Zhang (next) on **ttH**
 - Top threshold scan, talk by Frank Simon tomorrow
 - Top mass determination above threshold, talk by Pablo Gomis Lopez tomorrow





Top identification and top pair production at CLIC

Workshop on top physics at the LC 2018,
June 4-6, 2018

On behalf of the CLICdp Collaboration

Philipp Roloff, Rickard Ström (CERN)

Martín Perelló Roselló, Ignacio Garcia Garcia, Marcel Vos (IFIC - U. Valencia/CSIC)

Nigel Watson, Alasdair Winter (University of Birmingham)



Backup slides





Top tagger algorithm

based on the Johns-Hopkins top tagger DOI: 10.1103/PhysRevLett.101.142001

1) PFO objects are clustered into jets of size R (large jet)

- Iteratively merge 4-vector pairs with closest $\Delta R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2}$ until $\Delta R < R$

2) Iteratively decluster each resulting jet (reversing each step in the jet clustering) to search for subjets

- Split into two parts, reject softest if
- Declustering continues on the harder object until:

$$\frac{p_T^{\text{subjet}}}{p_T^{\text{jet}}} < \delta_p$$

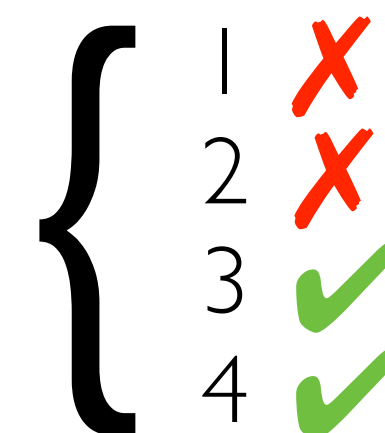
Both subjets are harder than $p_T^{\text{jet}} \cdot \delta_p$ ✓

Both subjets are too close $|\Delta\eta| + |\Delta\phi| < \delta_r$ ✗

Both subjets are softer than $p_T^{\text{jet}} \cdot \delta_p$ ✗

3) If an original jet declusters into two subjets - step 2 is repeated on those subjets

- Results in 1 (original jet), 2, 3, or 4 (additional soft gluon emission) subjets



4) Kinematic cuts

✗ = irreducible