

# EFT fit on top quark EW couplings

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## Acknowledging input/contributions from:

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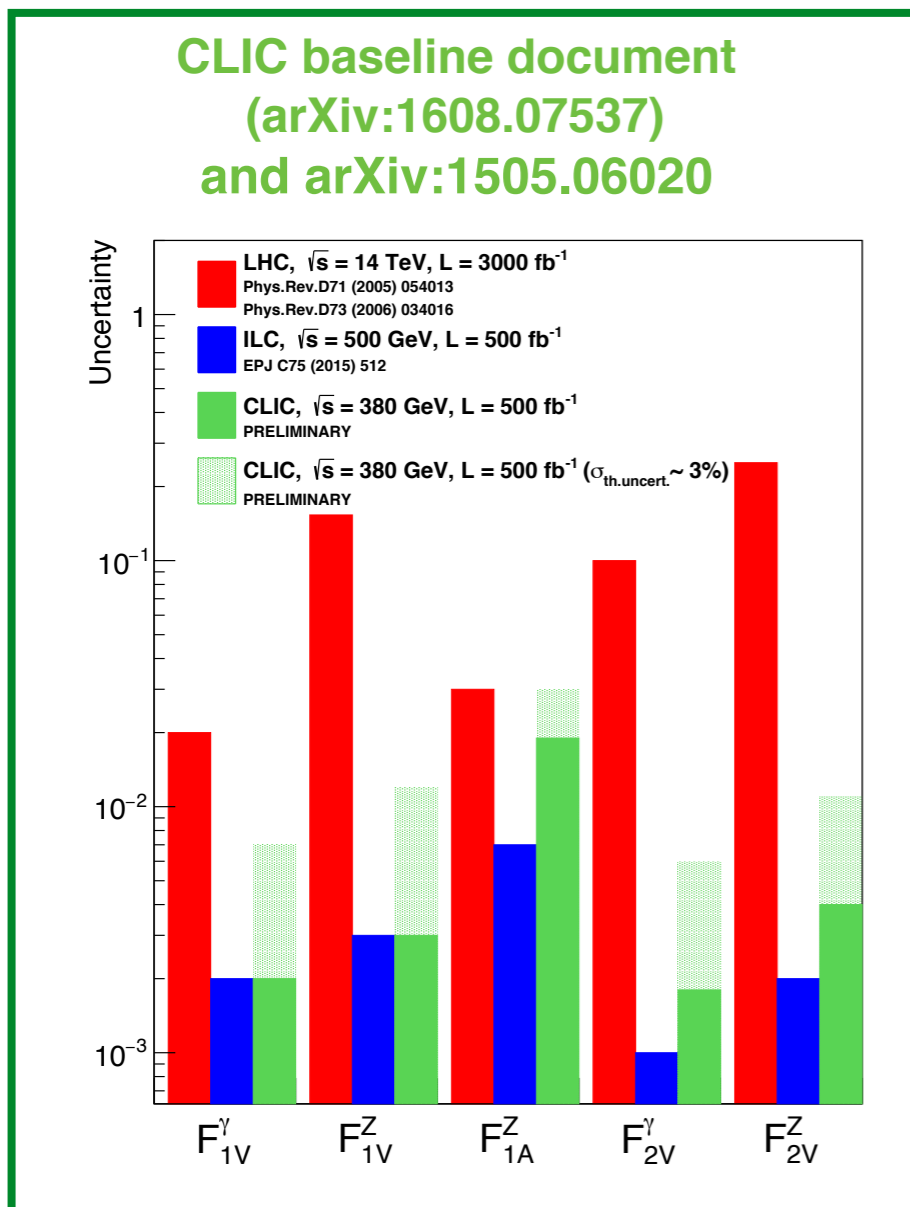
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# Introduction

# Top quark couplings: form factors

**Objective:** to study the potential of a global fit in the top EW sector.

**Form-factors**  $\Gamma_{\mu}^{t\bar{t}X}(k^2, q, \bar{q}) = ie \left\{ \underbrace{\gamma_{\mu} (F_{1V}^X(k^2) + \gamma_5 F_{1A}^X(k^2))}_{\text{CP Conserving}} - \frac{\sigma_{\mu\nu}}{2m_t} (q + \bar{q})^{\nu} \underbrace{(iF_{2V}^X(k^2) + \gamma_5 F_{2A}^X(k^2))}_{\text{CPV}} \right\}$



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## CP-violating top quark couplings at future linear $e^+e^-$ colliders

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**Abstract** We study the potential of future lepton colliders to probe top quark sector. In certain extensions of the Standard Model, such as sizeable anomalous top quark dipole moments can arise, that may impact top quark pair production. We present results from detailed Monte Carlo simulations for the production of top quark pairs with subsequent decay into  $W$  and  $Z$  bosons. We find that precise measurements in  $e^+e^- \rightarrow t\bar{t}$  production with subsequent decay into  $W$  and  $Z$  bosons can provide sufficient sensitivity to detect Higgs-boson-induced CP violation. The potential of a linear  $e^+e^-$  collider to detect CP factors of the top quark exceeds the prospects of the HL-LHC by a factor of 10.

**Keywords** CP violation · top physics ·  $e^+e^-$  collider

Form Factor	HL-LHC, $\sqrt{s} = 14$ TeV, L = 3000 fb $^{-1}$	ILC initial, $\sqrt{s} = 500$ GeV, L = 500 fb $^{-1}$	ILC nominal, $\sqrt{s} = 500$ GeV, L = 4000 fb $^{-1}$	CLIC initial, $\sqrt{s} = 380$ GeV, L = 500 fb $^{-1}$	CLIC, $\sqrt{s} = 3$ TeV, L = 3000 fb $^{-1}$
$\text{Re}[F_{2A}^Y]$	~0.12	~0.005	~0.002	~0.015	~0.003
$\text{Re}[F_{2A}^Z]$	~0.25	~0.007	~0.003	~0.02	~0.004
$\text{Im}[F_{2A}^Y]$	~0.12	~0.005	~0.002	~0.015	~0.003
$\text{Im}[F_{2A}^Z]$	~0.25	~0.01	~0.004	~0.03	~0.005

# Top quark couplings: EFT

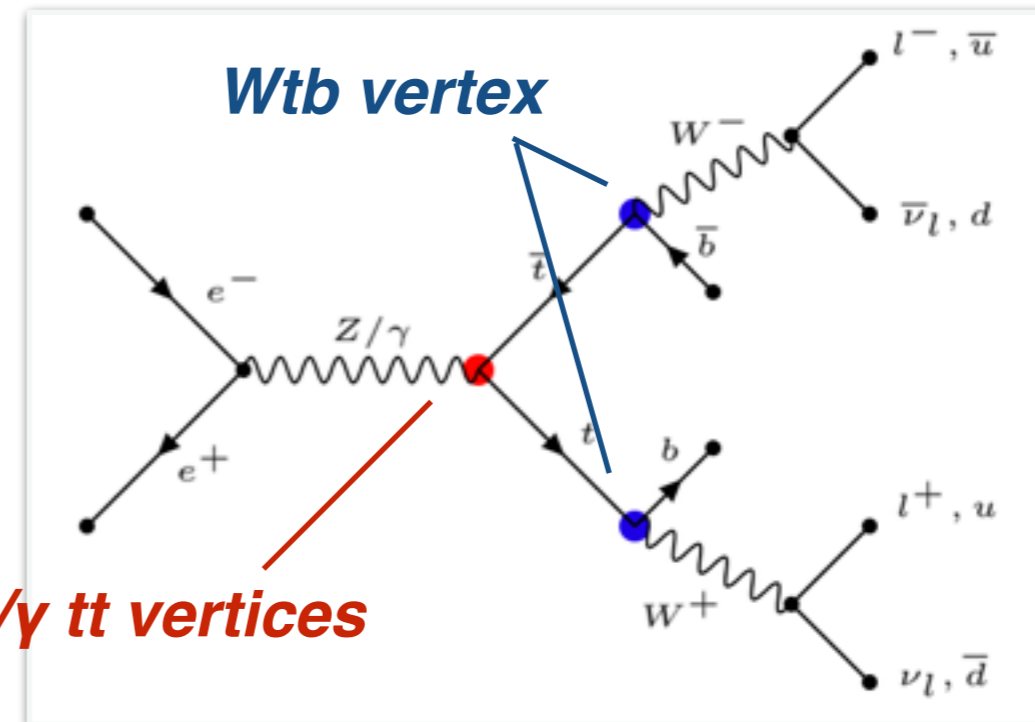
## Effective Field Theory

$$\mathcal{L}_{eff} = \mathcal{L}_{SM} + \frac{1}{\Lambda^2} \sum_i C_i O_i + \mathcal{O}(\Lambda^{-4})$$

See “EFT formalism for top physics” from C. Grojean on Tuesday for a **theory motivation**

**dim-6 operators** on tt production and decay...

$$\begin{aligned}
 O_{\varphi q}^1 &\equiv \frac{y_t^2}{2} \bar{q} \gamma^\mu q \varphi^\dagger i \overleftrightarrow{D}_\mu \varphi \\
 O_{\varphi q}^3 &\equiv \frac{y_t^2}{2} \bar{q} \tau^I \gamma^\mu q \varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi \\
 O_{\varphi u} &\equiv \frac{y_t^2}{2} \bar{u} \gamma^\mu u \varphi^\dagger i \overleftrightarrow{D}_\mu \varphi \\
 O_{\varphi ud} &\equiv \frac{y_t^2}{2} \bar{u} \gamma^\mu d \varphi^T \epsilon i D_\mu \varphi \\
 O_{uG} &\equiv y_t g_s \bar{q} \tau^A \sigma^{\mu\nu} u \epsilon \varphi^* G_{\mu\nu}^A \\
 O_{uW} &\equiv y_t g_W \bar{q} \tau^I \sigma^{\mu\nu} u \epsilon \varphi^* W_{\mu\nu}^I \\
 O_{dW} &\equiv y_t g_W \bar{q} \tau^I \sigma^{\mu\nu} d \epsilon \varphi^* W_{\mu\nu}^I \\
 O_{uB} &\equiv y_t g_Y \bar{q} \sigma^{\mu\nu} u \epsilon \varphi^* B_{\mu\nu}
 \end{aligned}$$

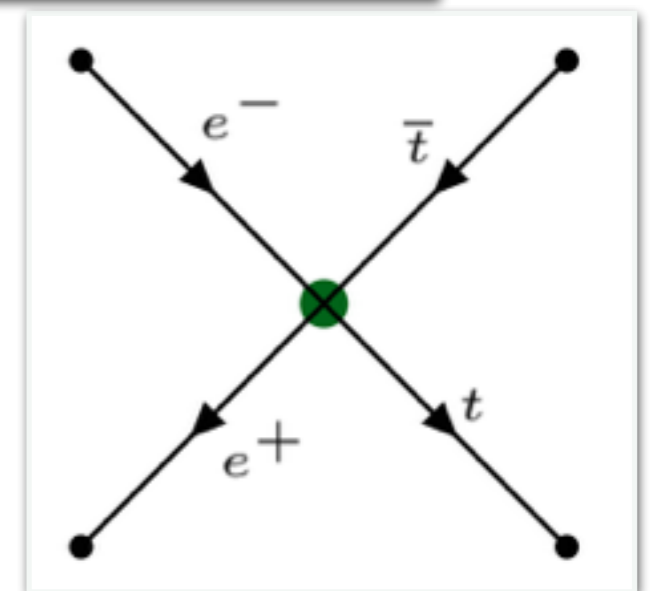


## Contact interactions

$$\begin{aligned}
 O_{lq}^1 &\equiv \bar{q} \gamma_\mu q \bar{l} \gamma^\mu l \\
 O_{lq}^3 &\equiv \bar{q} \tau^I \gamma_\mu q \bar{l} \tau^I \gamma^\mu l \\
 O_{lu} &\equiv \bar{u} \gamma_\mu u \bar{l} \gamma^\mu l \\
 O_{eq} &\equiv \bar{q} \gamma_\mu q \bar{e} \gamma^\mu e \\
 O_{eu} &\equiv \bar{u} \gamma_\mu u \bar{e} \gamma^\mu e
 \end{aligned}$$

$$O_{lequ}^T \equiv \bar{q} \sigma^{\mu\nu} u \epsilon \bar{l} \sigma_{\mu\nu} e$$

$$\begin{aligned}
 O_{lequ}^S &\equiv \bar{q} u \epsilon \bar{l} e \\
 O_{ledq} &\equiv \bar{d} q \bar{l} e
 \end{aligned}$$



# Different EFT basis

## Transformation between effective operators and form-factors:

$$\begin{aligned}
 F_{1,V}^Z - F_{1,V}^{Z,SM} &= \frac{1}{2} \left( \underline{C_{\varphi Q}^{(3)}} - \underline{C_{\varphi Q}^{(1)}} - C_{\varphi t} \right) \frac{m_t^2}{\Lambda^2 s_W c_W} = -\frac{1}{2} \underline{C_{\varphi q}^V} \frac{m_t^2}{\Lambda^2 s_W c_W} \\
 F_{1,A}^Z - F_{1,A}^{Z,SM} &= \frac{1}{2} \left( -\underline{C_{\varphi Q}^{(3)}} + \underline{C_{\varphi Q}^{(1)}} - C_{\varphi t} \right) \frac{m_t^2}{\Lambda^2 s_W c_W} = -\frac{1}{2} \underline{C_{\varphi q}^A} \frac{m_t^2}{\Lambda^2 s_W c_W} \\
 F_{2,V}^Z &= \left( \underline{\text{Re}\{C_{tW}\} c_W^2 - \text{Re}\{C_{tB}\} s_W^2} \right) \frac{4m_t^2}{\Lambda^2 s_W c_W} = \text{Re}\{ \underline{C_{uZ}} \} \frac{4m_t^2}{\Lambda^2} \\
 F_{2,V}^\gamma &= \left( \underline{\text{Re}\{C_{tW}\} + \text{Re}\{C_{tB}\}} \right) \frac{4m_t^2}{\Lambda^2} = \text{Re}\{ \underline{C_{uA}} \} \frac{4m_t^2}{\Lambda^2} \\
 [F_{2,A}^Z, F_{2,A}^\gamma] &\propto \underline{[\text{Im}\{C_{tW}\}, \text{Im}\{C_{tB}\}]}
 \end{aligned}$$

We can change to an alternative basis  
(**Vector/Axial - Vector**)

**10 operators** in the global fit:

- 4 CP-conserving ttX vertices
- 2 CP-violating ttX vertices
- 4 contact interactions

## Contact interactions:

$$\begin{aligned}
 C_{lq}^V &\equiv C_{lu} + C_{lq}^{(1)} - C_{lq}^{(3)} & C_{eq}^V &\equiv C_{eu} + C_{eq} \\
 C_{lq}^A &\equiv C_{lu} - C_{lq}^{(1)} + C_{lq}^{(3)} & C_{eq}^A &\equiv C_{eu} - C_{eq}
 \end{aligned}$$

# Observables

# Observables sensitivity: $A_{\text{FB}}$ + cross-section

$e^+e^- \rightarrow t\bar{t}$ , LO

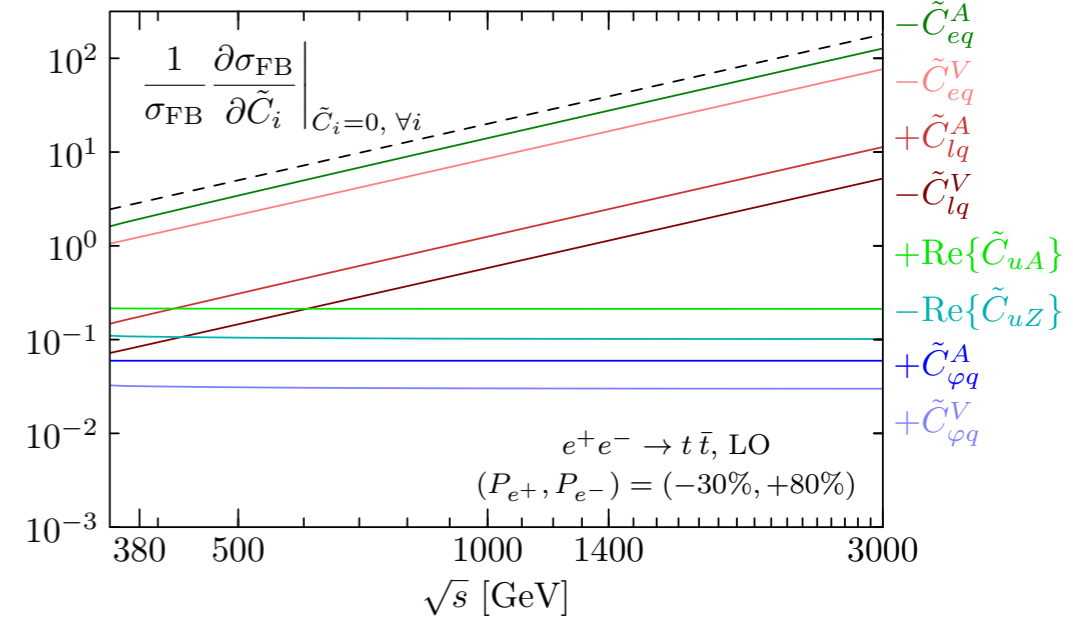
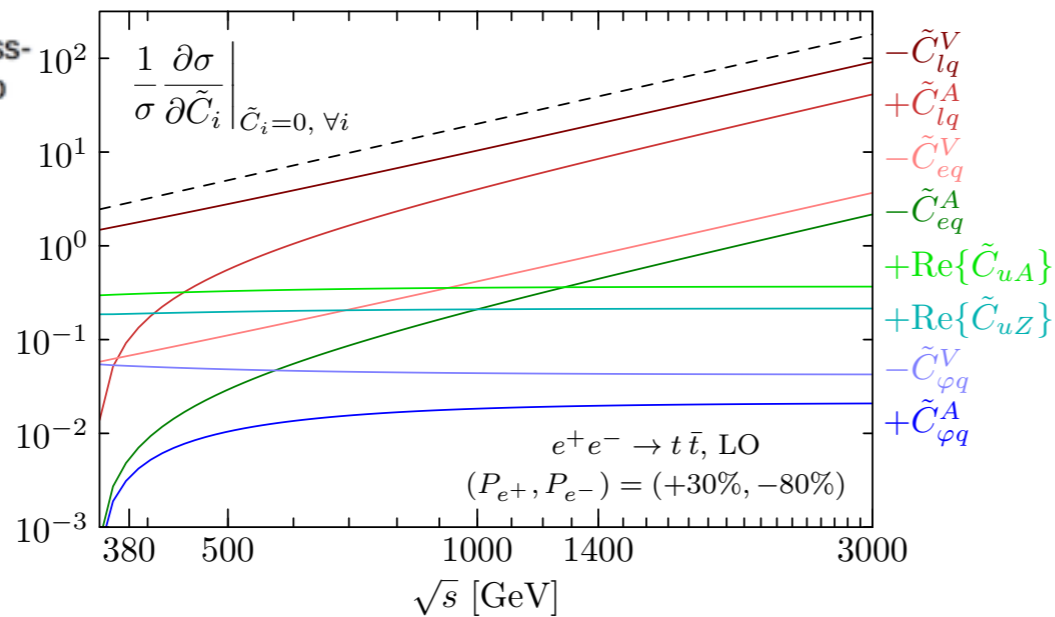
Durieux, Perelló, Vos, Zhang, to be published

Cross-section

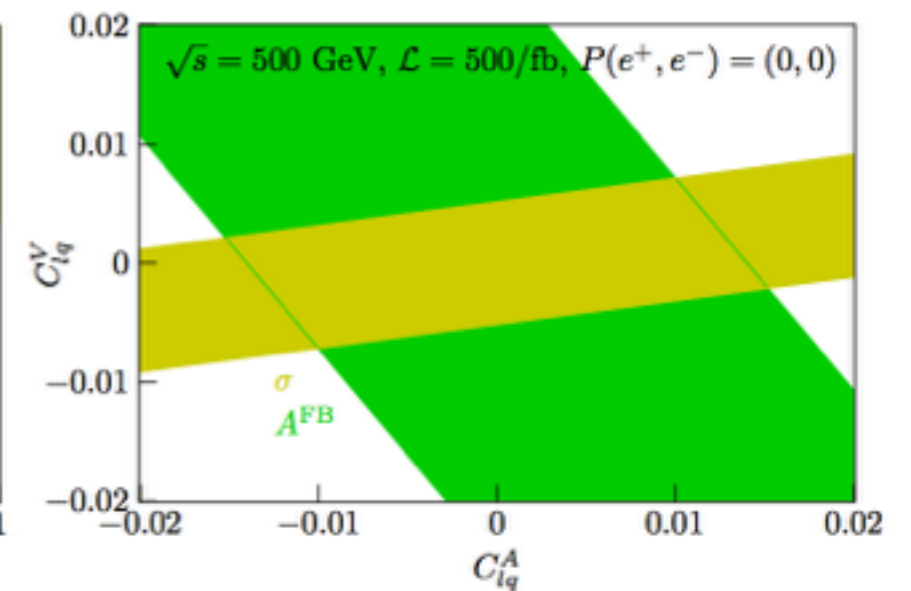
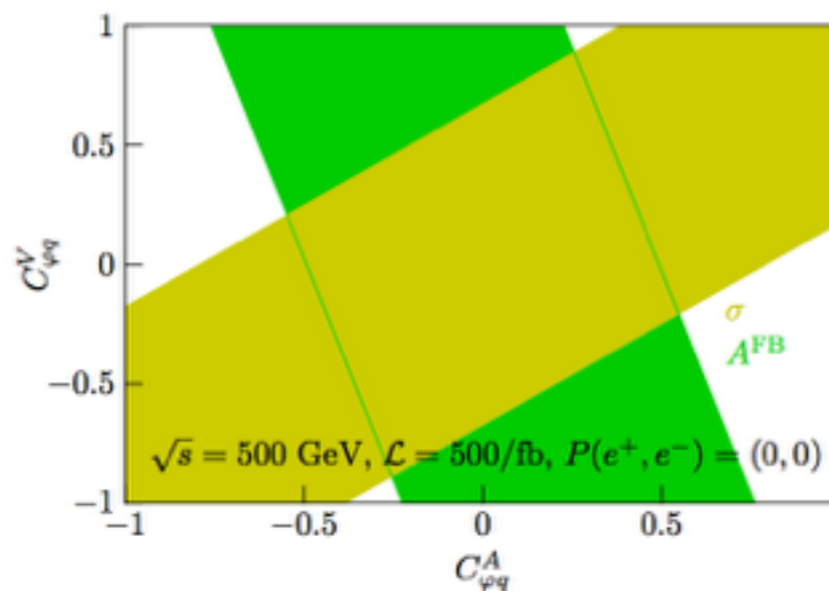
Forward-backward asymmetry

**Sensitivity:**

Relative change in cross-section due to non-zero operator coefficient  
 $\Delta\sigma(C) / \sigma / \Delta C$



Nice complementarity between Afb and cross-section to **disentangle** vector and axial operators.



# Observables sensitivity: $A_{\text{FB}}$ + cross-section

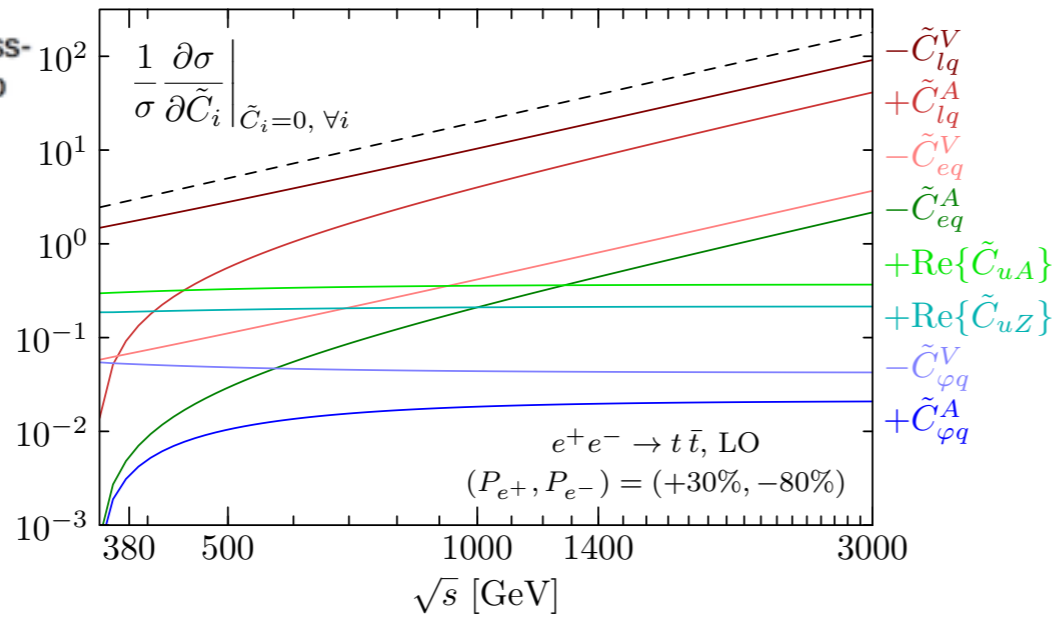
$e^+e^- \rightarrow t\bar{t}$ , LO

Durieux, Perelló, Vos, Zhang, to be published

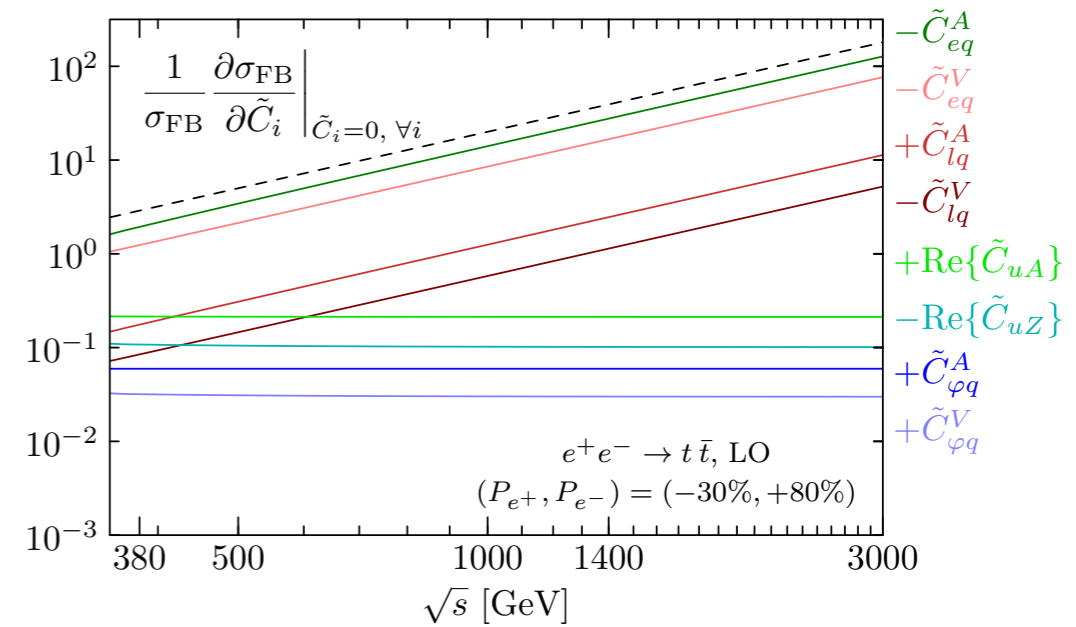
Cross-section

Sensitivity:

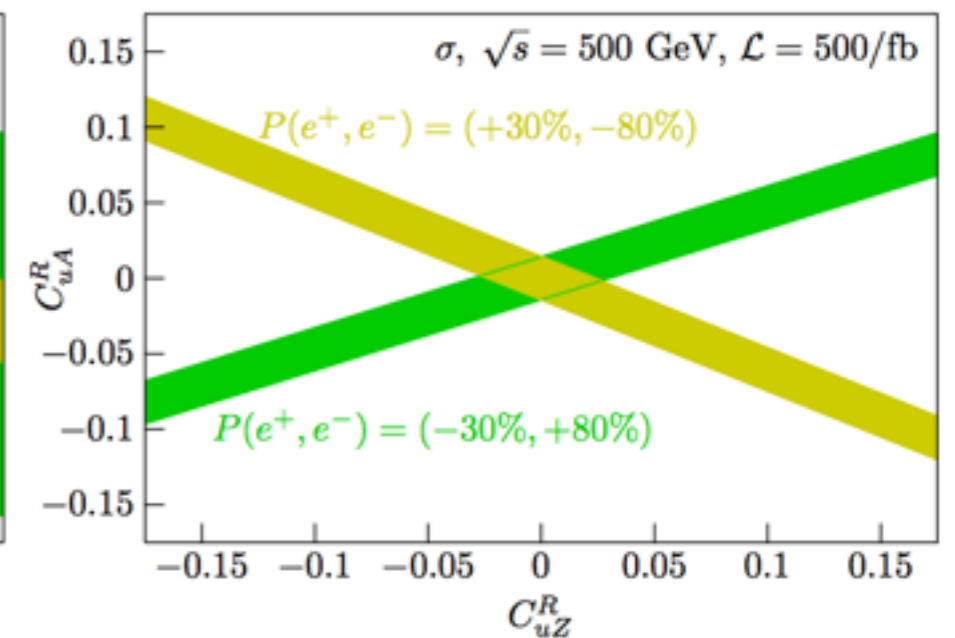
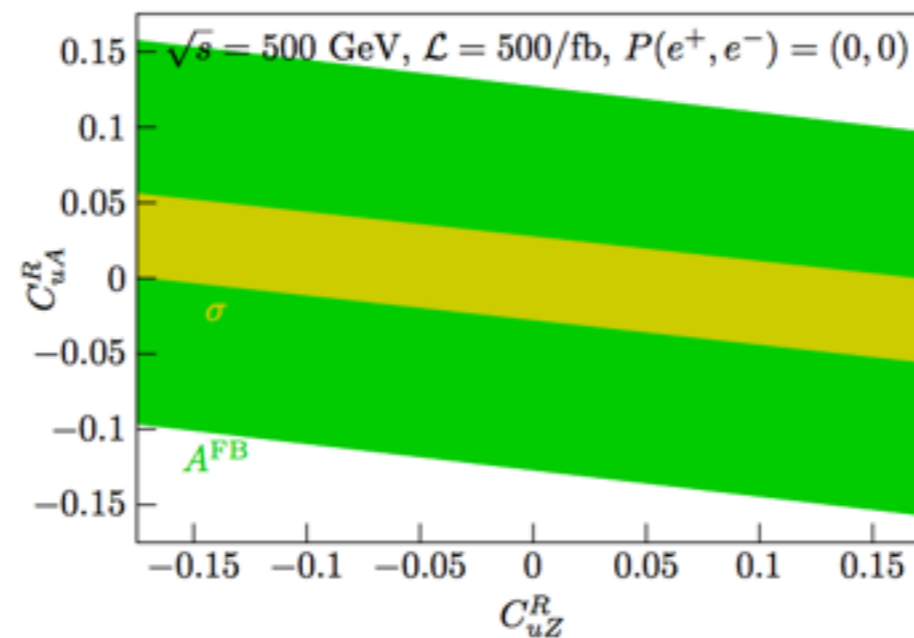
Relative change in cross-section due to non-zero operator coefficient  
 $\Delta\sigma(C)/\sigma/\Delta C$



Forward-backward asymmetry



Role of beams polarization:





# Observables sensitivity: $A_{FB}$ + cross-section

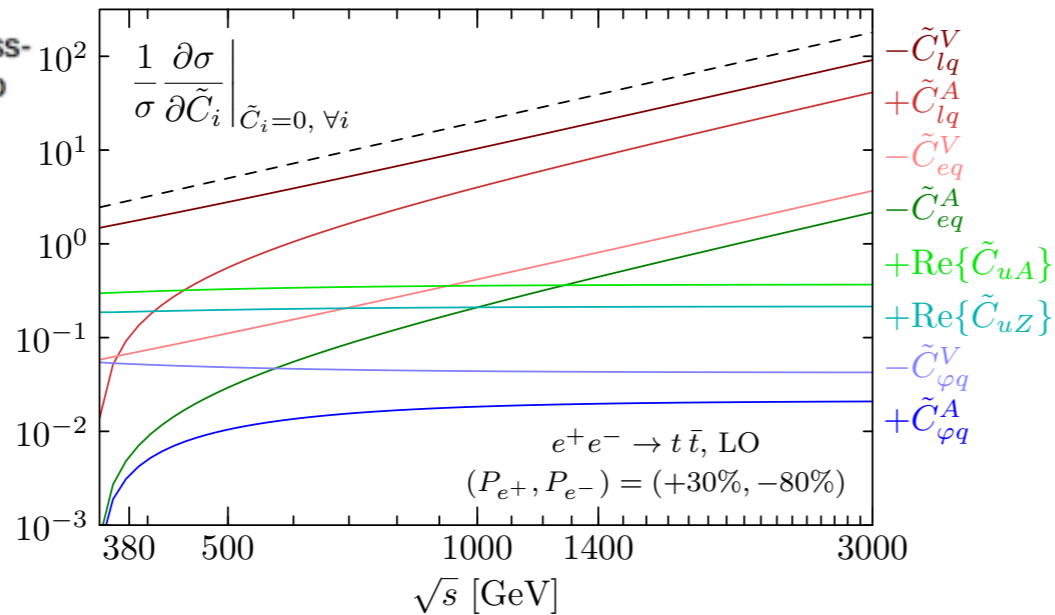
$$e^+e^- \rightarrow t\bar{t}, \text{ LO}$$

Durieux, Perelló, Vos, Zhang, to be published

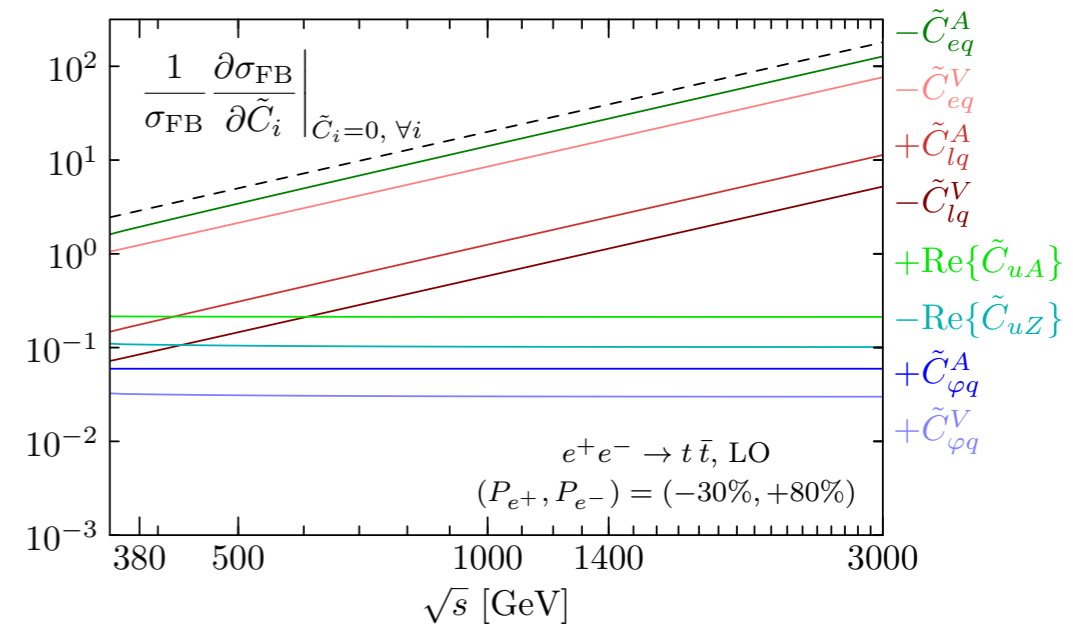
Cross-section

**Sensitivity:**

Relative change in cross-section due to non-zero operator coefficient  
 $\Delta\sigma(C)/\sigma/\Delta C$



Forward-backward asymmetry

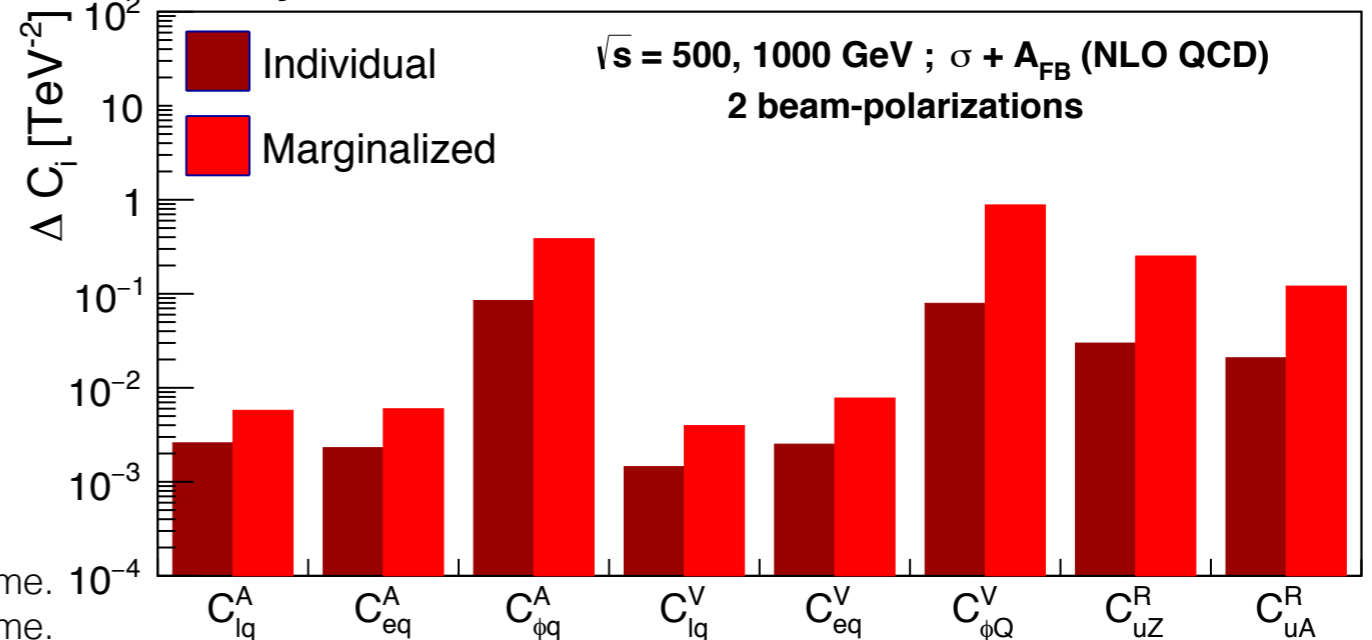


Nothing can be done with only one energy point!

- At least we need **one low energy with high statistics for the vertices**, and **one high energy for the contact interactions**.

**Need for new observables** to reduce the difference between individual and marginalized fits

Theory fit, no full-simulation included.



**Individual:** assuming variation in only 1 parameter each time.

**Marginalized:** assuming variation in all the parameters at the same time.

The **CP-violating effects** in  $e^+e^- \rightarrow t\bar{t}$  manifest themselves in specific **top-spin effects**, namely **CP-odd top spin-momentum correlations and  $t\bar{t}$  spin correlations**.

$$e^+(\mathbf{p}_+, P_{e^+}) + e^-(\mathbf{p}_-, P_{e^-}) \rightarrow t(\mathbf{k}_t) + \bar{t}(\mathbf{k}_{\bar{t}})$$

$$t \bar{t} \rightarrow \ell^+(\mathbf{q}_+) + \nu_\ell + b + \bar{X}_{\text{had}}(\mathbf{q}_{\bar{X}})$$

$$t \bar{t} \rightarrow X_{\text{had}}(\mathbf{q}_X) + \ell^-(\mathbf{q}_-) + \bar{\nu}_\ell + \bar{b}$$

- **CP-odd observables** are defined with the **four momenta available in  $t\bar{t}$  semi-leptonic decay channel**

$$\mathcal{O}_+^{Re} = (\hat{\mathbf{q}}_{\bar{X}} \times \hat{\mathbf{q}}_+^*) \cdot \hat{\mathbf{p}}_+,$$

$$\mathcal{O}_+^{Im} = -\left[1 + \left(\frac{\sqrt{s}}{2m_t} - 1\right)(\hat{\mathbf{q}}_{\bar{X}} \cdot \hat{\mathbf{p}}_+)^2\right] \hat{\mathbf{q}}_+^* \cdot \hat{\mathbf{q}}_{\bar{X}} + \frac{\sqrt{s}}{2m_t} \hat{\mathbf{q}}_{\bar{X}} \cdot \hat{\mathbf{p}}_+ \hat{\mathbf{q}}_+^* \cdot \hat{\mathbf{p}}_+$$

- The way to **extract** the **CP-violating form factor** is to construct **asymmetries sensitive to CP-violation effects**

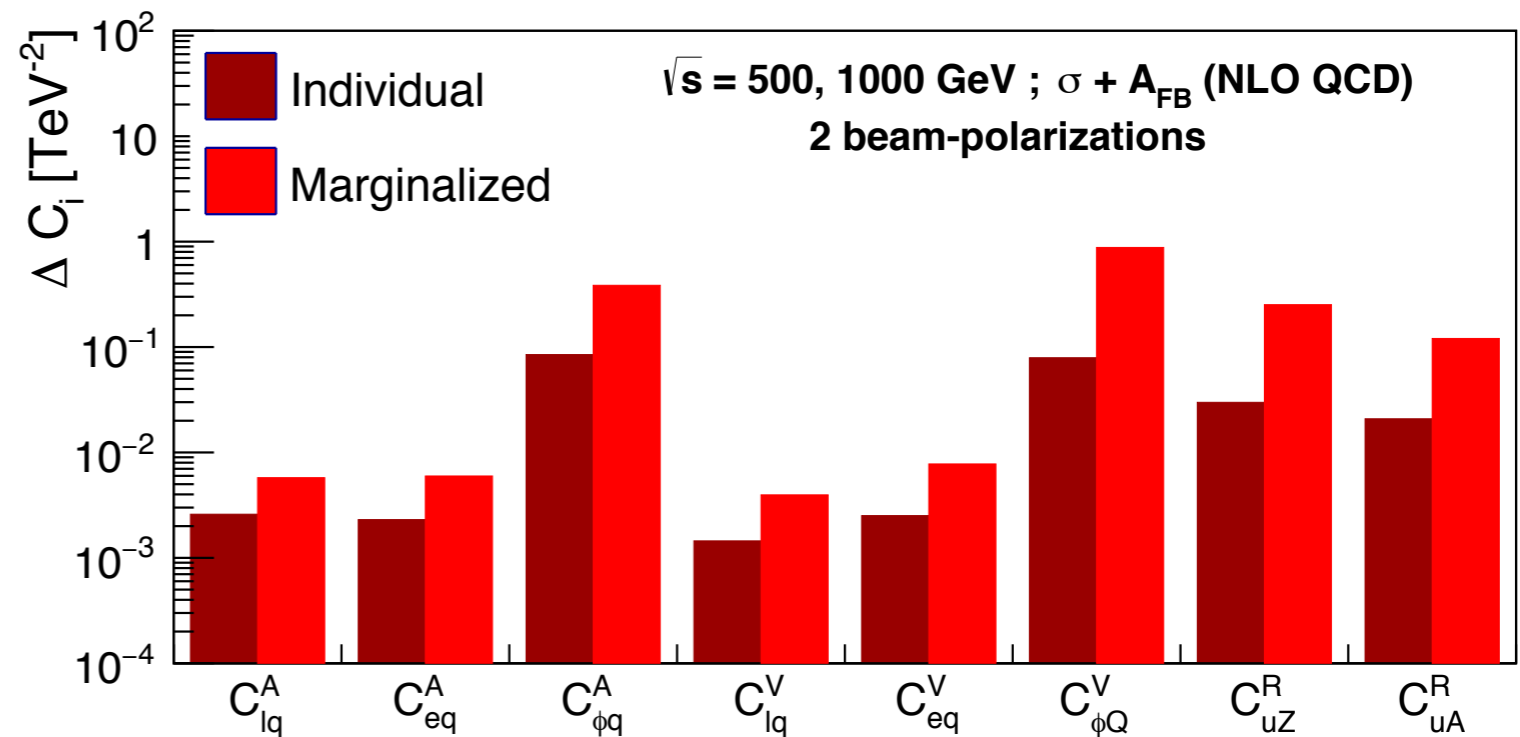
$$\mathcal{A}^{Re} = \langle \mathcal{O}_+^{Re} \rangle - \langle \mathcal{O}_-^{Re} \rangle = c_\gamma(s) \text{Re}F_{2A}^\gamma + c_Z(s) \text{Re}F_{2A}^Z$$

$$\mathcal{A}^{Im} = \langle \mathcal{O}_+^{Im} \rangle - \langle \mathcal{O}_-^{Im} \rangle = \tilde{c}_\gamma(s) \text{Im}F_{2A}^\gamma + \tilde{c}_Z(s) \text{Im}F_{2A}^Z$$

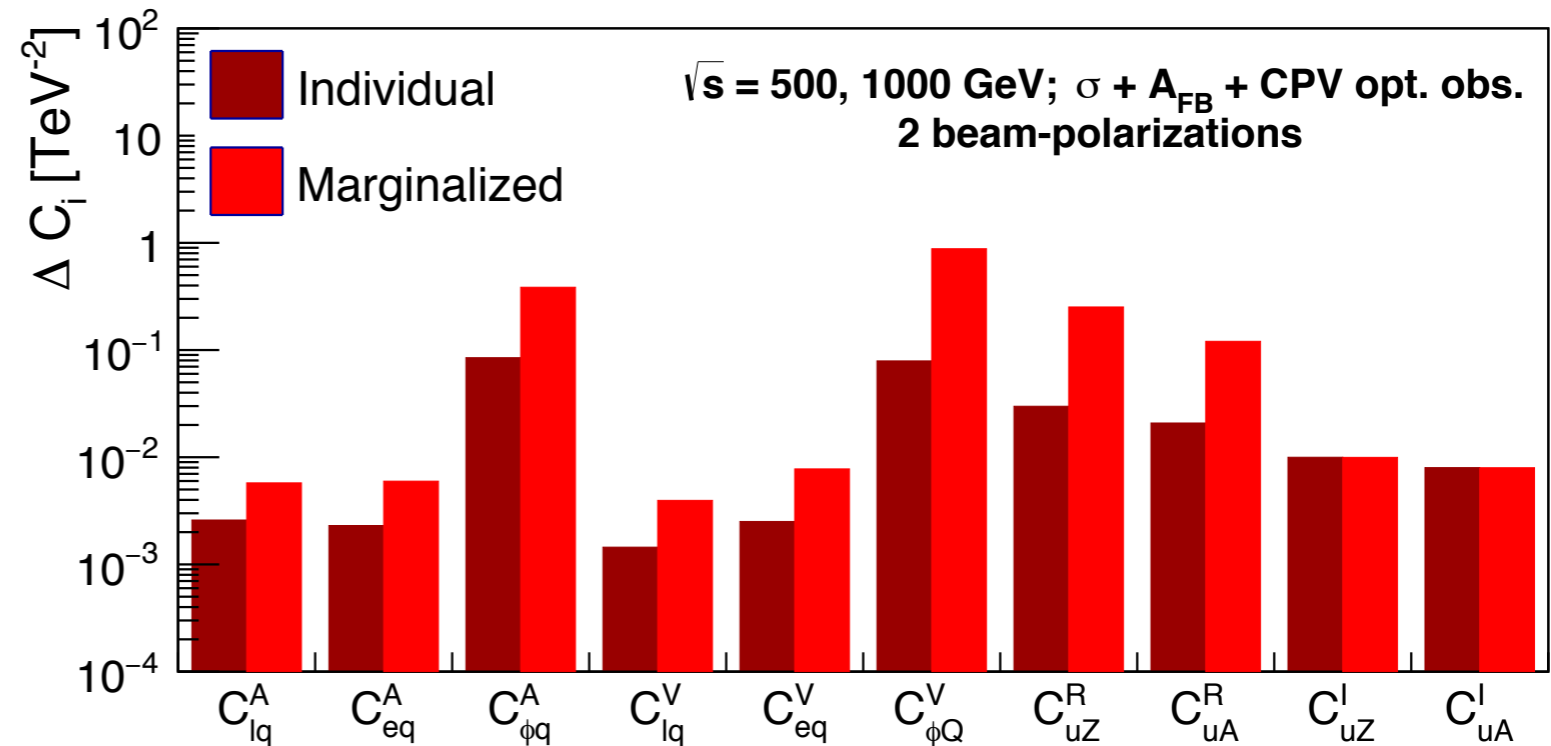
$$\begin{array}{cc} \mathcal{A}_{\gamma,Z}^{Re L} & \mathcal{A}_{\gamma,Z}^{Re L} \\ \mathcal{A}_{\gamma,Z}^{Im R} & \mathcal{A}_{\gamma,Z}^{Im R} \end{array}$$

**Including CPV observables in the EFT global fit doesn't solve the problem**

**We still need to improve the marginalized fit**



**Theory fit, no full-simulation included.**



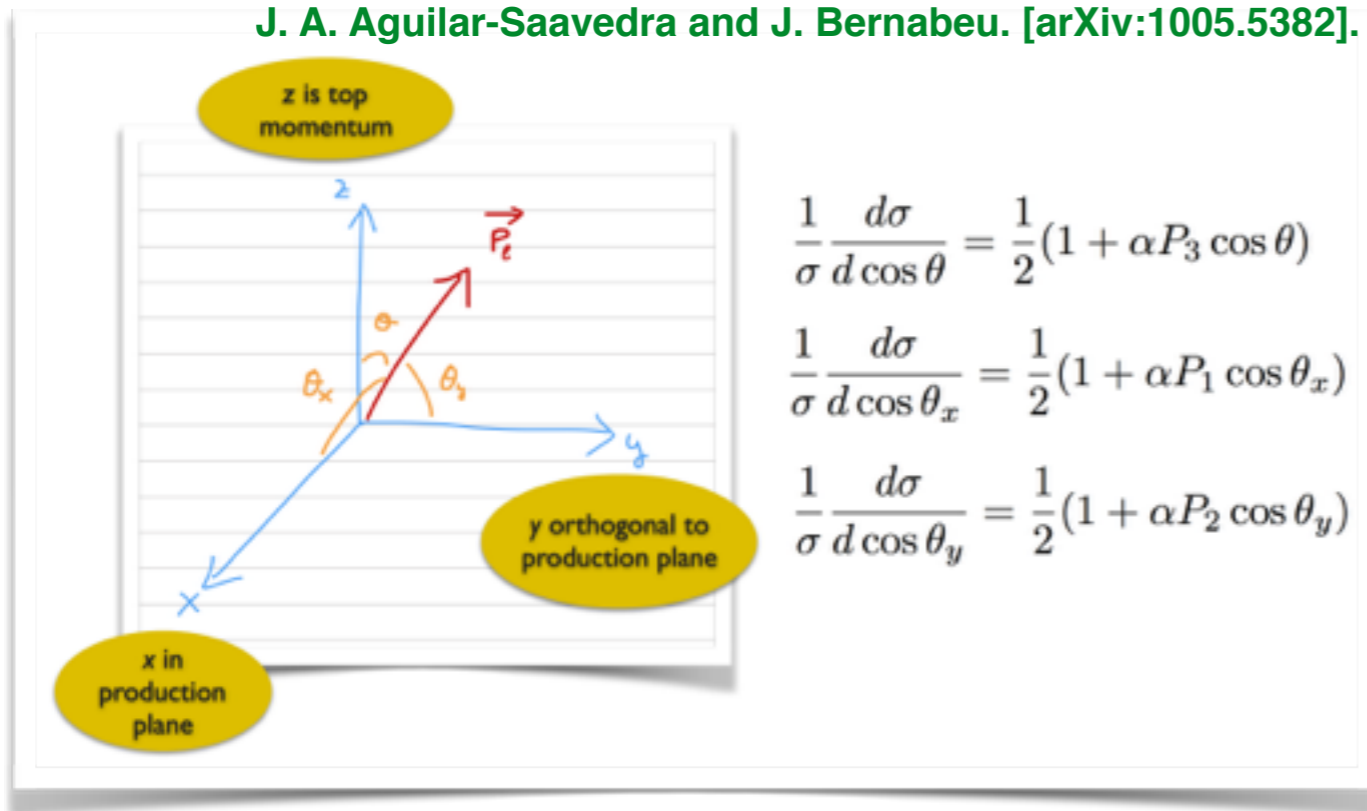
**Individual:** assuming variation in only 1 parameter each time.

**Marginalized:** assuming variation in all the parameters at the same time.

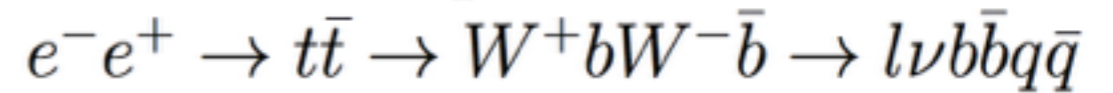
**Further ideas using  
information from the decay:  
top quark polarization**

# Top quark polarization at different axes

J. A. Aguilar-Saavedra and J. Bernabeu. [arXiv:1005.5382].



Studied process



Using the lepton from the leptonic W as a polarimeter, we can calculate the top polarization in 3 different axes.

$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta_i} = \frac{1}{2} (1 + \alpha_i P \cos \theta_i)$$

**Helicity axis (z):** measuring top polarization in the z top momentum direction.

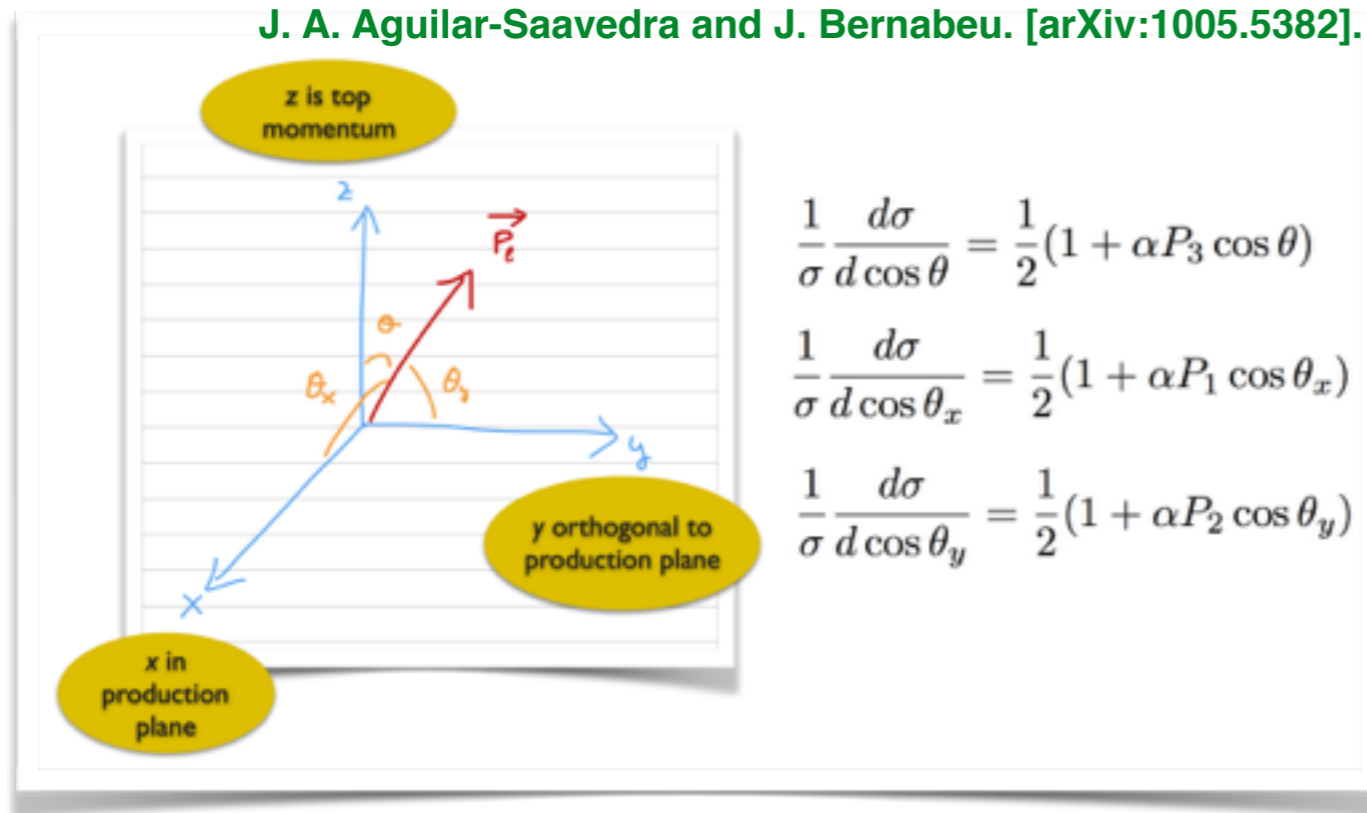
**Overlapping with the forward-backward asymmetry.**

*arXiv:1505.06020v2*

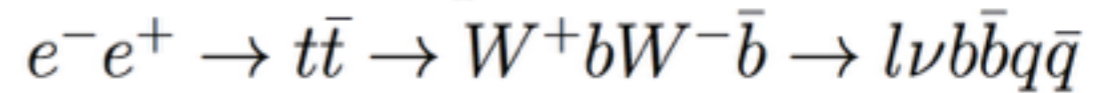
**No new information.**

# Top quark polarization at different axes

J. A. Aguilar-Saavedra and J. Bernabeu. [arXiv:1005.5382].



Studied process



Using the lepton from the leptonic W as a polarimeter, we can calculate the top polarization in 3 different axes.

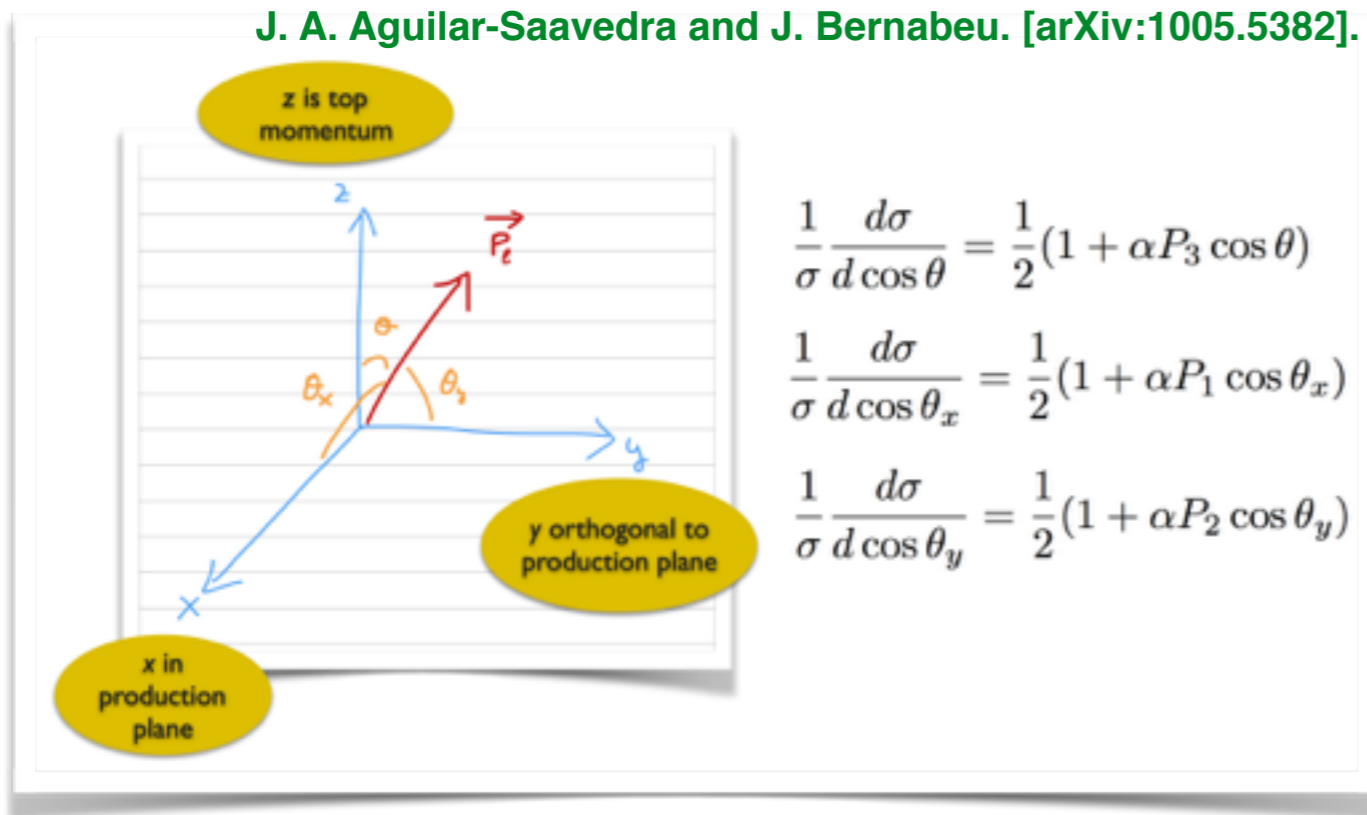
$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta_i} = \frac{1}{2} (1 + \alpha_i P \cos \theta_i)$$

**Normal axis (x):** measuring top polarization in the x direction, perpendicular to the production plane.

**Same definition that the CPV observable ORe (see CPV slide). Insensitive to CP conserving operators.**

# Top quark polarization at different axes

J. A. Aguilar-Saavedra and J. Bernabeu. [arXiv:1005.5382].



Studied process

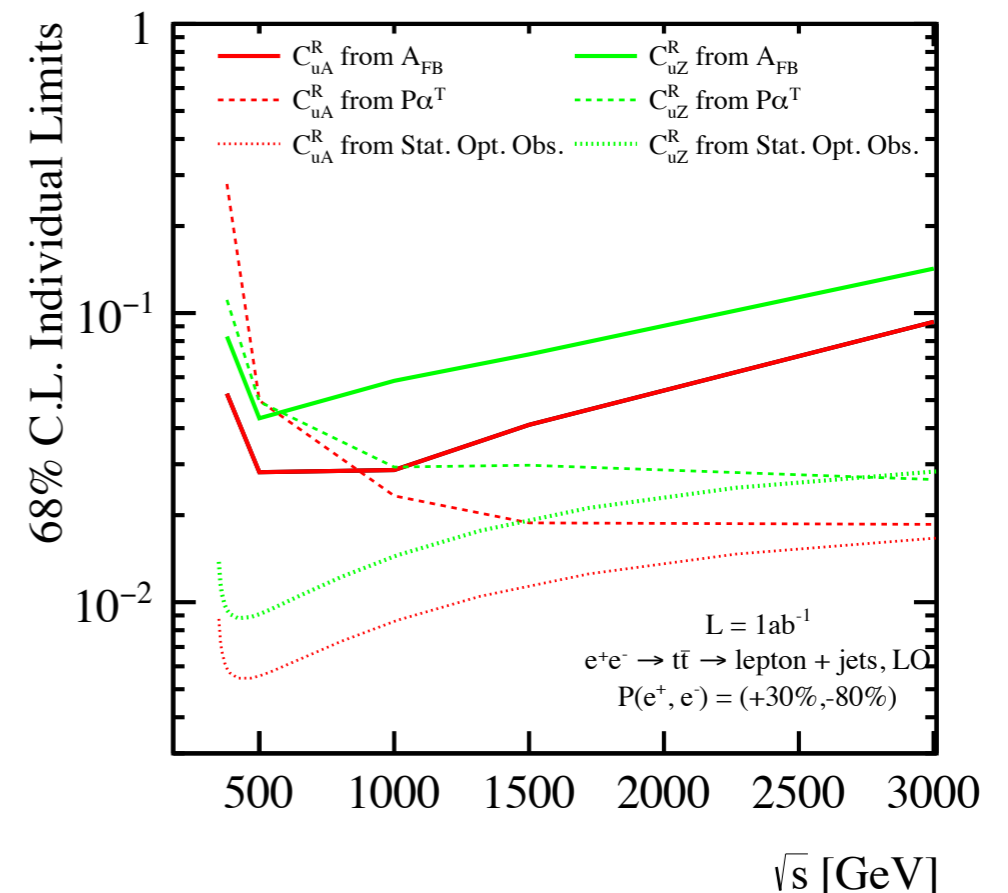
$$e^- e^+ \rightarrow t \bar{t} \rightarrow W^+ b W^- \bar{b} \rightarrow l \nu b \bar{b} q \bar{q}$$

Using the lepton from the leptonic W as a polarimeter, we can calculate the top polarization in 3 different axes.

$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta_i} = \frac{1}{2} (1 + \alpha_i P \cos \theta_i)$$

**Transverse axis (y):** measuring top polarization in the y direction, perpendicular to the x-z plane.

**Seems to be good for constraining the real part of the dipole operators (CuA and CuZ)**



# **Wtb vertex and W polarization**



# Wtb vertex

$$O_{uW} \equiv y_t g_W \bar{q} \tau^I \sigma^{\mu\nu} u \epsilon \varphi^* W_{\mu\nu}^I$$

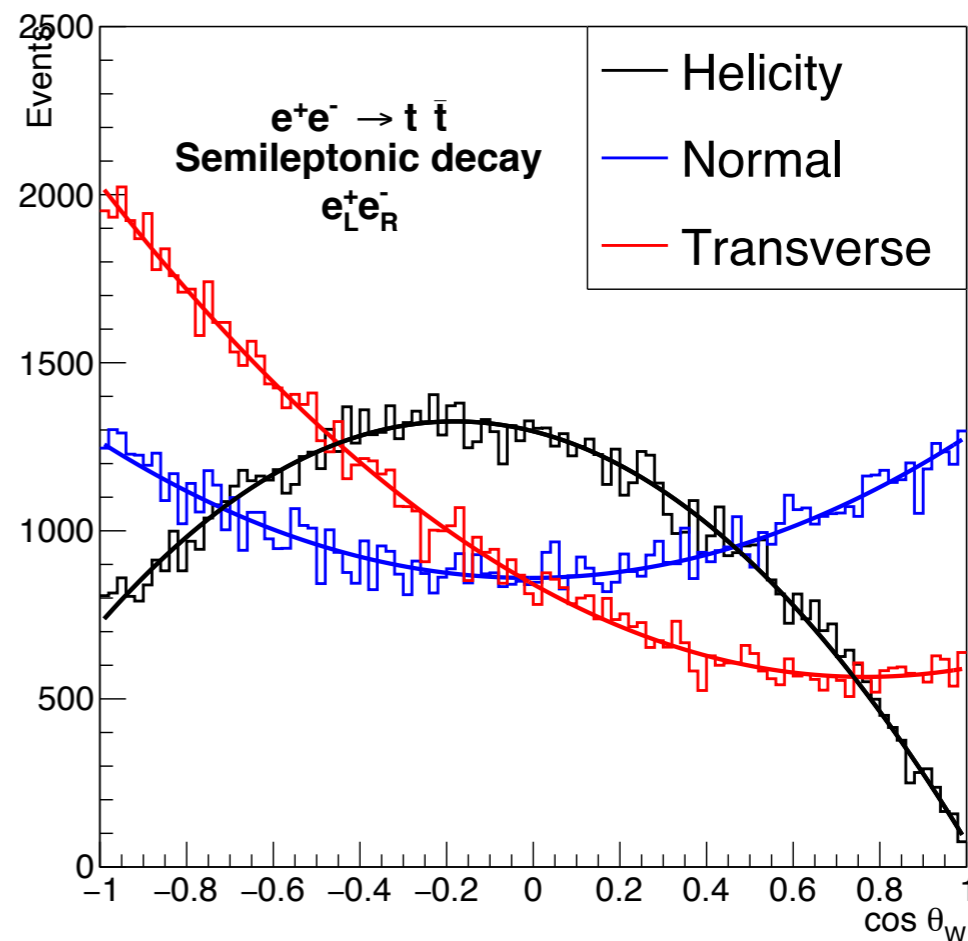
$$O_{\varphi q}^3 \equiv \frac{y_t^2}{2} \bar{q} \tau^I \gamma^\mu q \varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi$$

$$O_{\varphi ud} \equiv \frac{y_t^2}{2} \bar{u} \gamma^\mu d \varphi^T \epsilon i D_\mu \varphi$$

$$O_{dW} \equiv y_t g_W \bar{q} \tau^I \sigma^{\mu\nu} d \epsilon \varphi^* W_{\mu\nu}^I$$

4 operators affecting to the top quark decay, 2 of them appear at production too.

Using the lepton from the leptonic W as a polarimeter, we can calculate the W polarization in 3 different axes (*same motivation than top polarization*).



J. A. Aguilar-Saavedra and J. Bernabeu. [arXiv:1005.5382].

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_l^*} = \frac{3}{8} F_+ (1 + \cos \theta_l^*)^2 + \frac{3}{4} F_0 \sin^2 \theta_l^* + \frac{3}{8} F_- (1 - \cos \theta_l^*)^2$$

# Wtb vertex

$$O_{uW} \equiv y_t g_W \bar{q} \tau^I \sigma^{\mu\nu} u \epsilon \varphi^* W_{\mu\nu}^I$$

$$O_{\varphi q}^3 \equiv \frac{y_t^2}{2} \bar{q} \tau^I \gamma^\mu q \varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi$$

$$O_{\varphi ud} \equiv \frac{y_t^2}{2} \bar{u} \gamma^\mu d \varphi^T \epsilon i D_\mu \varphi$$

$$O_{dW} \equiv y_t g_W \bar{q} \tau^I \sigma^{\mu\nu} d \epsilon \varphi^* W_{\mu\nu}^I$$

4 operators affecting to the top quark decay, 2 of them appear at production too.

Defining:  $A_{FB}^W \equiv \frac{3}{4}(F_+ - F_-)$

*AT is proportional to the top quark transverse polarization*

- $O_{\varphi ud}$  and  $O_{dW}$  only contribute quadratically (no SM interference).
- For these observables the dependence on  $O_{\varphi q}^3$  also completely drops out.

## Sensitivity to the **real part of $O_{uW}$ at 500 GeV** (*Durieux, MP, Vos, Chang PRELIMINARY*)

$P(e^+, e^-)$ observables	(+30%, -80%)		(-30%, +80%)	
	$A^T$	$A_{FB}^W$	$A^T$	$A_{FB}^W$
SM predictions	-0.6	-0.17	0.57	-0.29
in production	$38 \pm 1$	$9 \pm 2$	$-25 \pm 1$	X
in decay	X	$16 \pm 2$	X	$11 \pm 3$
in prod. & decay	$37 \pm 1$	$26 \pm 2$	$-24 \pm 1$	$10 \pm 3$

# Statistically optimal observables

G. Durieux @TopLC 2017:

<https://indico.cern.ch/event/595651/contributions/>

## Statistically optimal observables

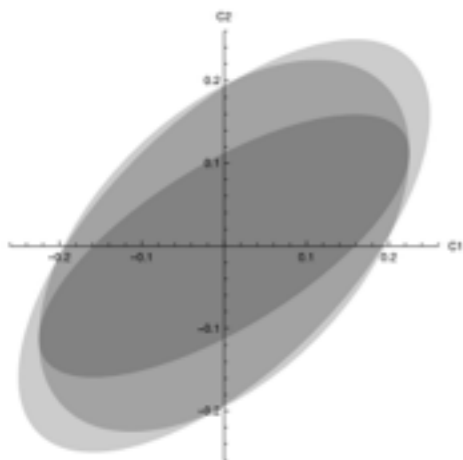
[Atwood,Soni '92]

[Diehl,Nachtmann '94]

minimize the one-sigma ellipsoid in EFT parameter space.

(joint efficient set of estimators, saturating the Rao-Cramér-Fréchet bound:  $V^{-1} = I$ )

For small  $C_i$ , with a phase-space distribution  $\sigma(\Phi) = \sigma_0(\Phi) + \sum_i C_i \sigma_i(\Phi)$ ,  
the statistically optimal set of observables is:  $O_i(\Phi) = \sigma_i(\Phi)/\sigma_0(\Phi)$ .



e.g.  $\sigma(\phi) = 1 + \cos(\phi) + C_1 \sin(\phi) + C_2 \sin(2\phi)$

1. asymmetries:  $O_i \sim \text{sign}\{\sin(i\phi)\}$

2. moments:  $O_i \sim \sin(i\phi)$

3. statistically optimal:  $O_i \sim \frac{\sin(i\phi)}{1 + \cos\phi}$

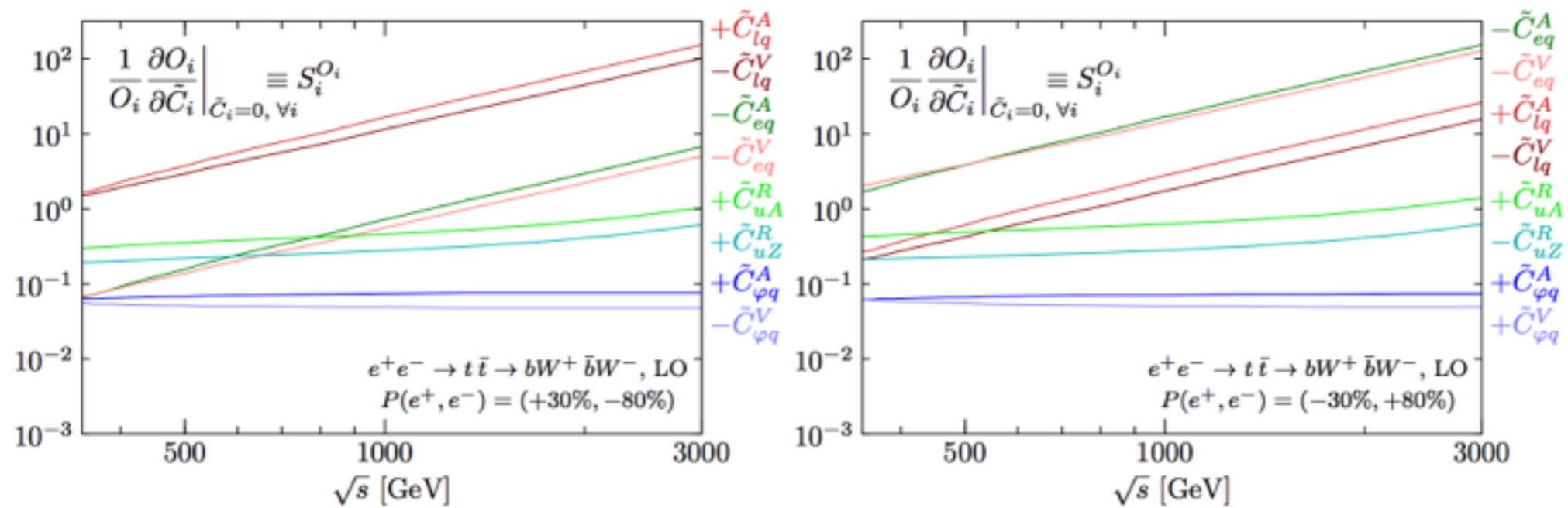
⇒ area ratios 1.9 : 1.7 : 1

Previous applications in  $e^+e^- \rightarrow t\bar{t}$ :  
[Grzadkowski, Hioki '00] [Janot '15] [Khiem et al '15]

Construction based on the decomposition of the differential  $e^+e^- \rightarrow t\bar{t} \rightarrow bW + \bar{b}W$  - cross section in terms of EFT helicity amplitudes.

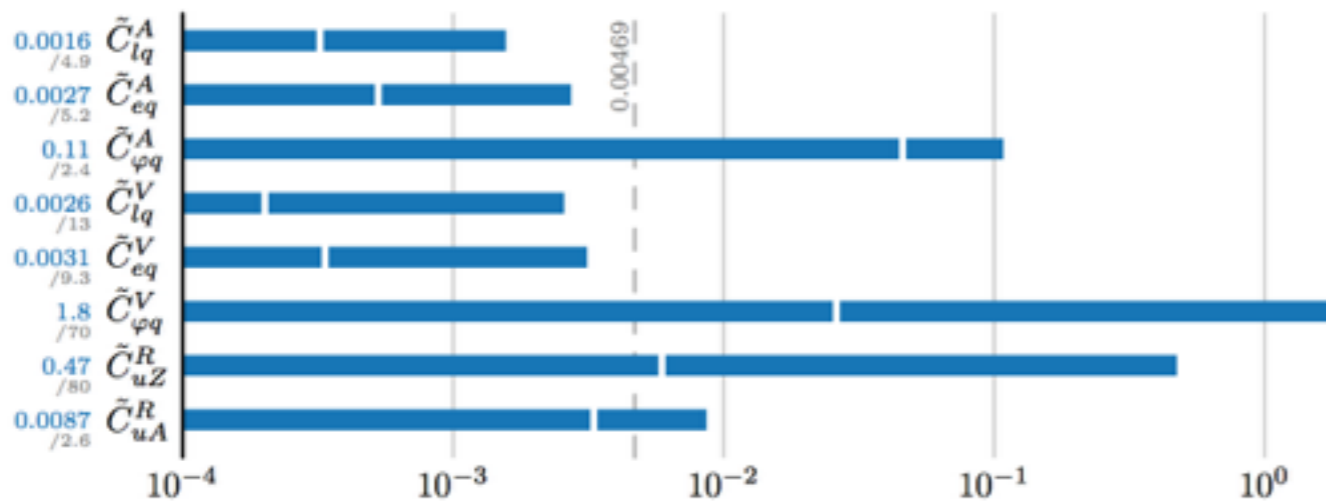
They are constructed to maximally exploit the available differential information and extract the tightest constraints on parameters whose dependence is expanded to linear order only.

# Statistically optimal observables sensitivities

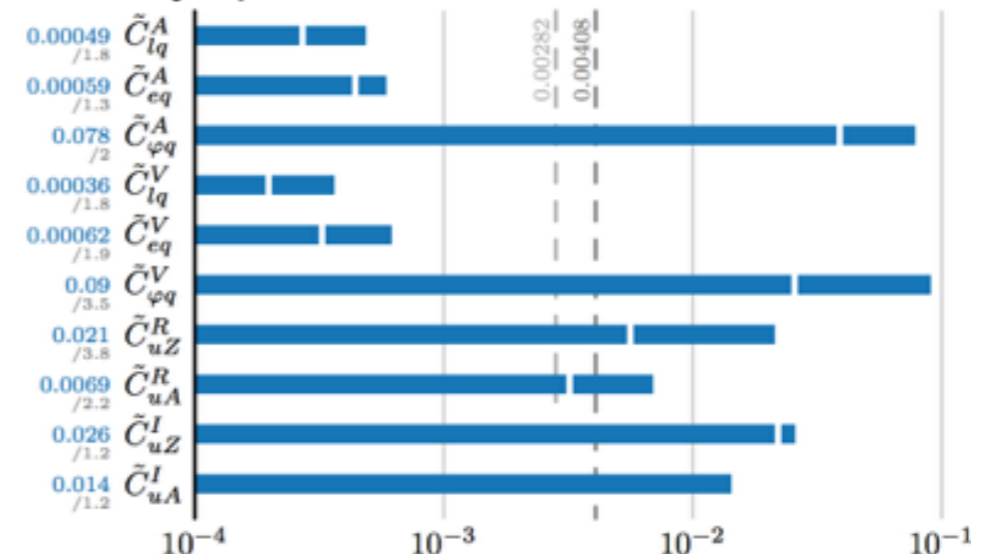


Comparison in the global limits (500GeV + 1TeV for 2 pols.):

$\sigma + A_{\text{FB}}$



Statistically optimal observables:



- **Even better individual limits**
- **Global limits within a factor 1.3 to 3.5**

# *(Few words about)* Full-simulation

See “*Top identification and  $t\bar{t}$  reconstruction at CLIC*” from **R. Ström** on Wednesday morning for  
**more details**

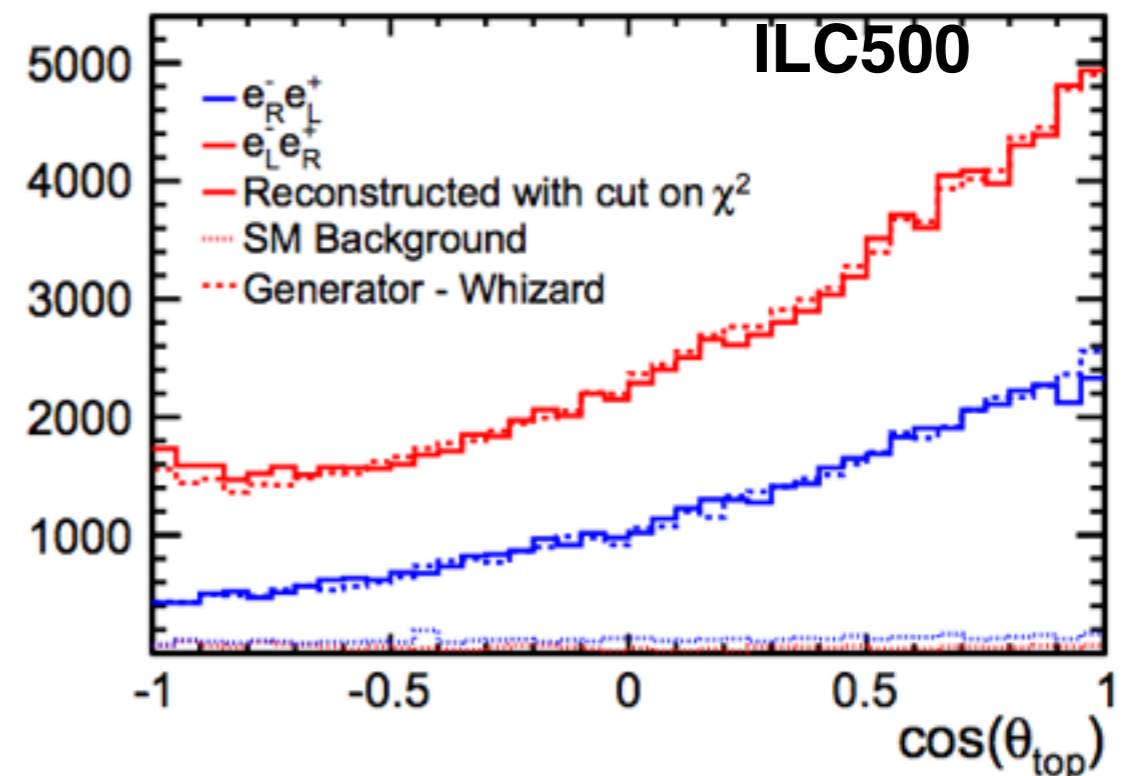
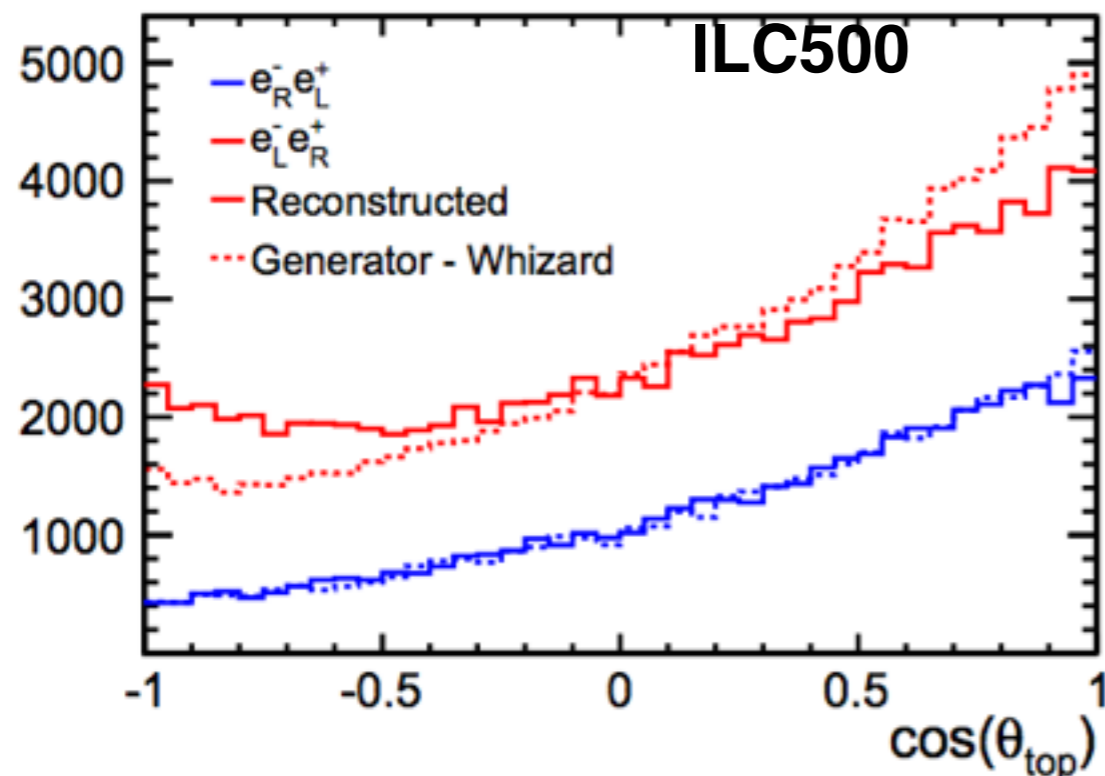
# Full-simulation

Reconstructed process:  $e^-e^+ \rightarrow tt \rightarrow 4j + \nu l$

## CLIC380 and ILC500

- **Resolved analysis** - reconstruction of 3 separated jets for the hadronic top, and 1 for the leptonic top.

**Problem on migrations (bad W-b pairing) in some angular distributions, solved using a quality cut with the consequent penalty in efficiency.**



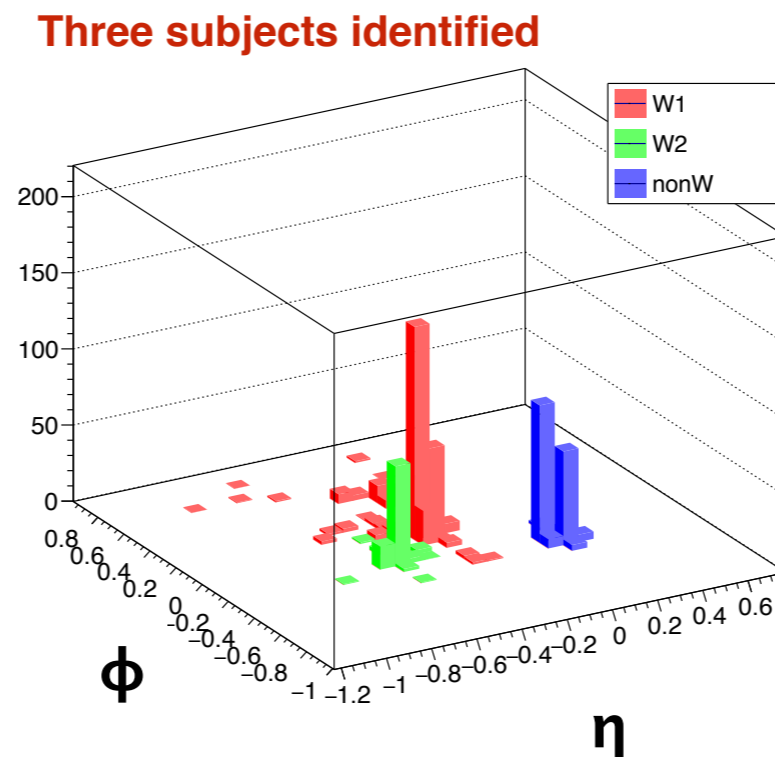
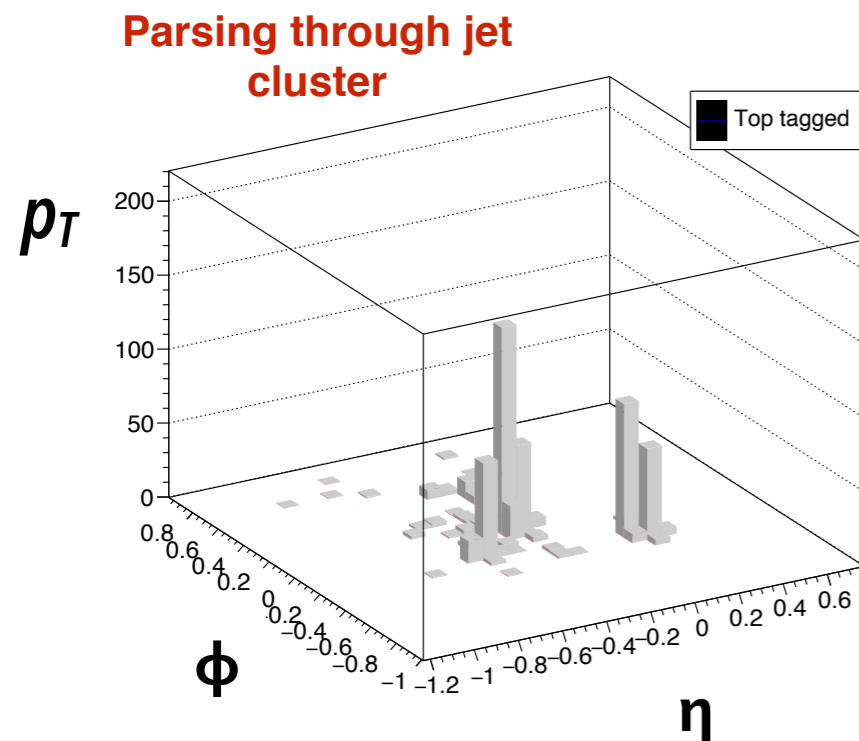
**Alternative:** reconstruction of b quark charge (see R. Poeschl talk on Tuesday afternoon)

# Full-simulation

Reconstructed process:  $e^-e^+ \rightarrow tt \rightarrow 4j + \nu l$

## CLIC1400 and CLIC3000

- **Boosted analysis** - reconstruction of 2 big jets, and then look inside them to substructure identification - *Top Tagging*.



**See R. Ström talk to understand all the work behind this method**

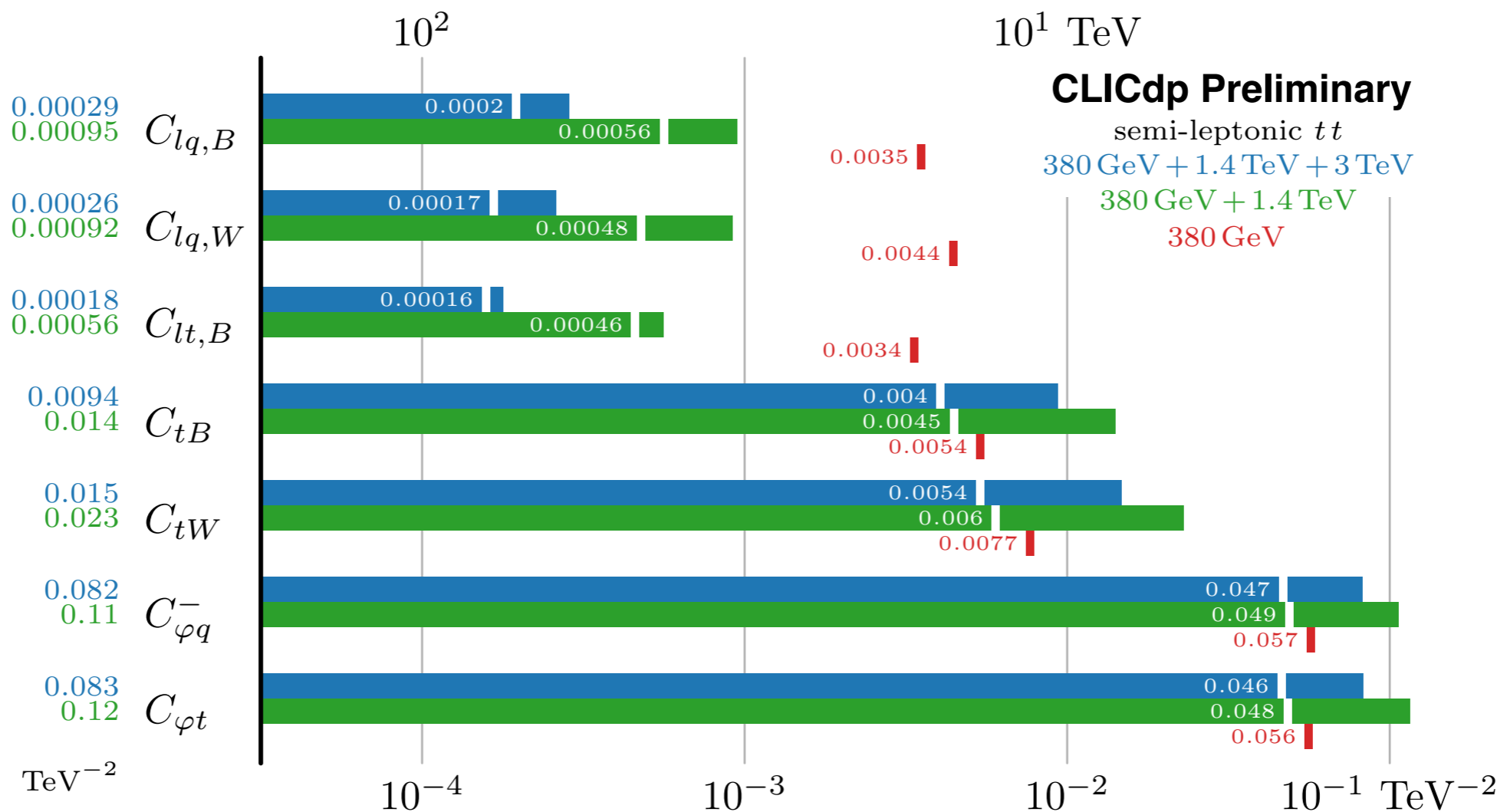
**Results based on CLIC**



# Results based on CLIC

## Top-philic basis (arXiv:1802.07237)

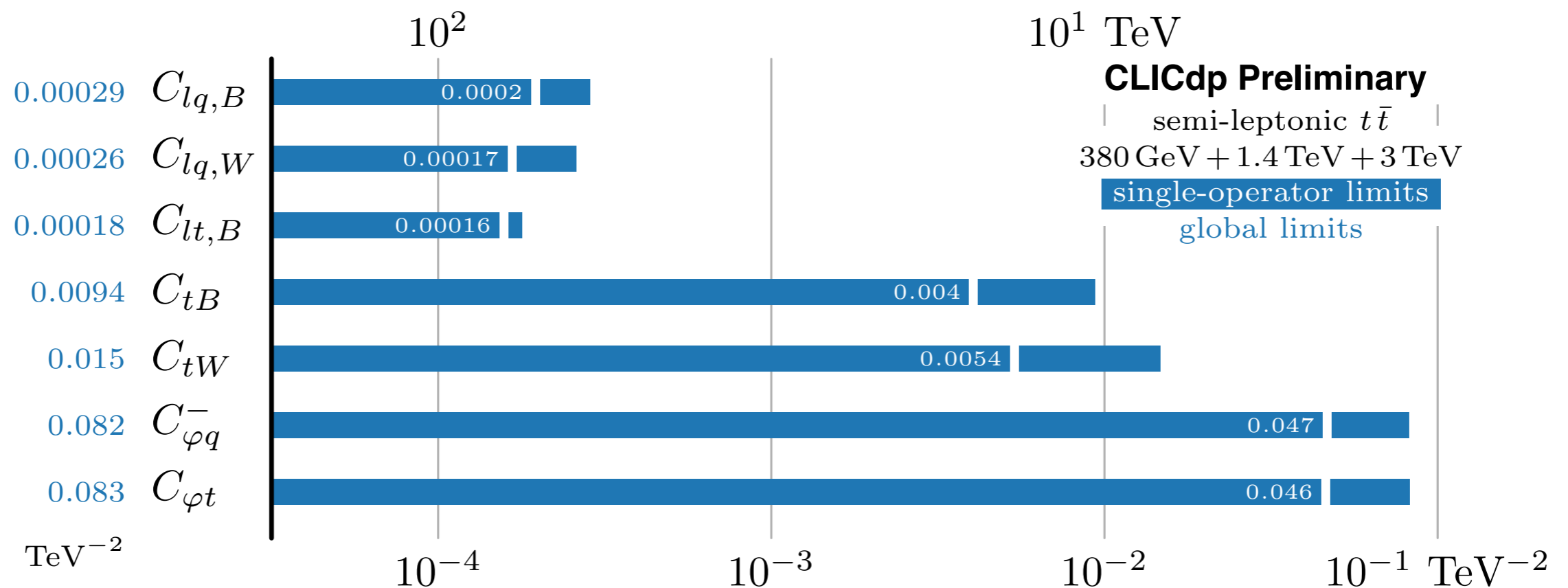
*A top-philic scenario is obtained by assuming that new physics couples dominantly to the left-handed doublet and right-handed up-type quark singlet of the third generation as well as to bosons.*



# Results based on CLIC

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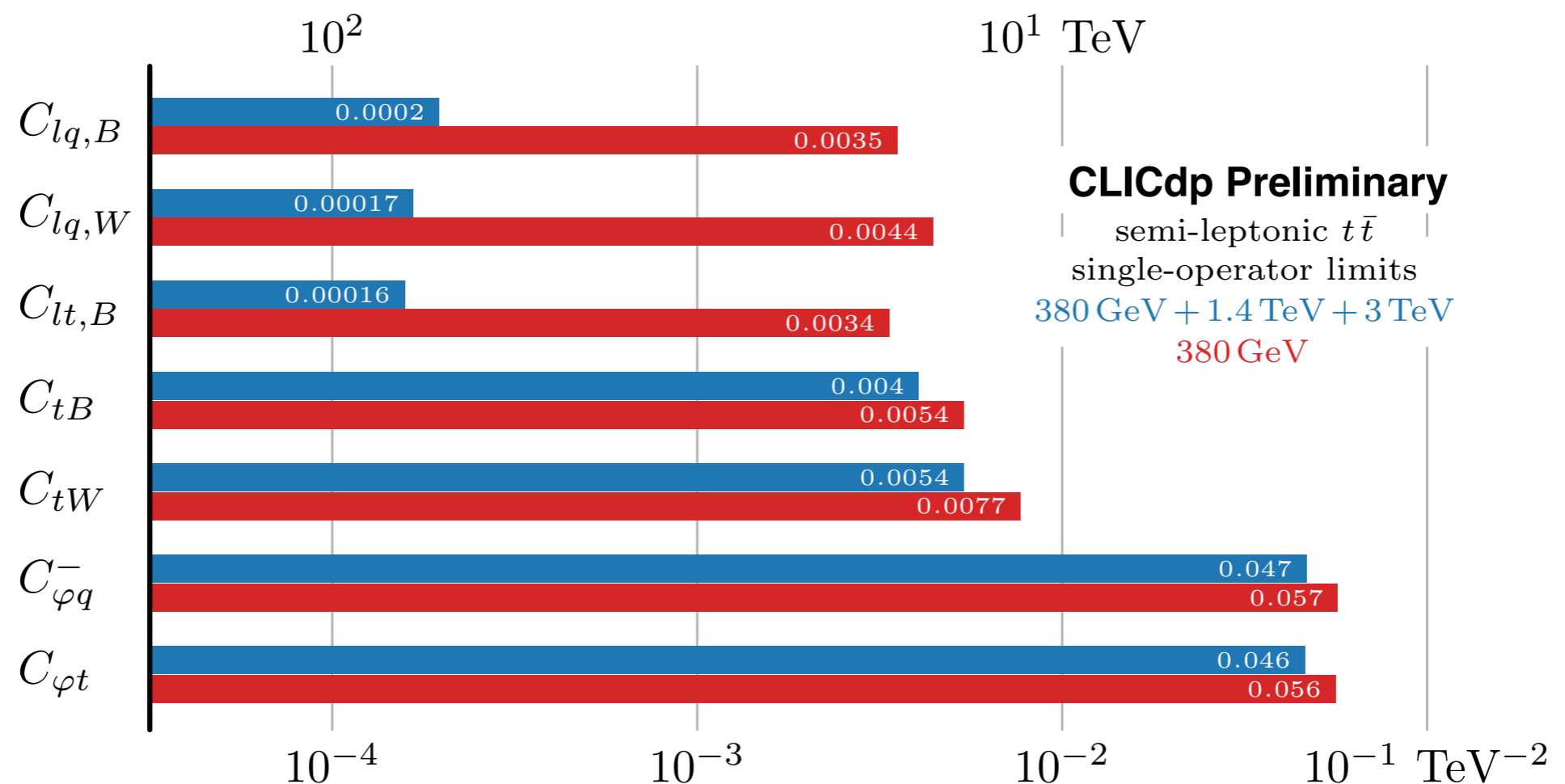


*Difference between individual and marginalised limit lower than a factor 2 for 4-fermion operators and lower than a factor 4 for 2-fermion*

# Results based on CLIC

## Top-philic basis (arXiv:1802.07237)

*A top-philic scenario is obtained by assuming that new physics couples dominantly to the left-handed doublet and right-handed up-type quark singlet of the third generation as well as to bosons.*

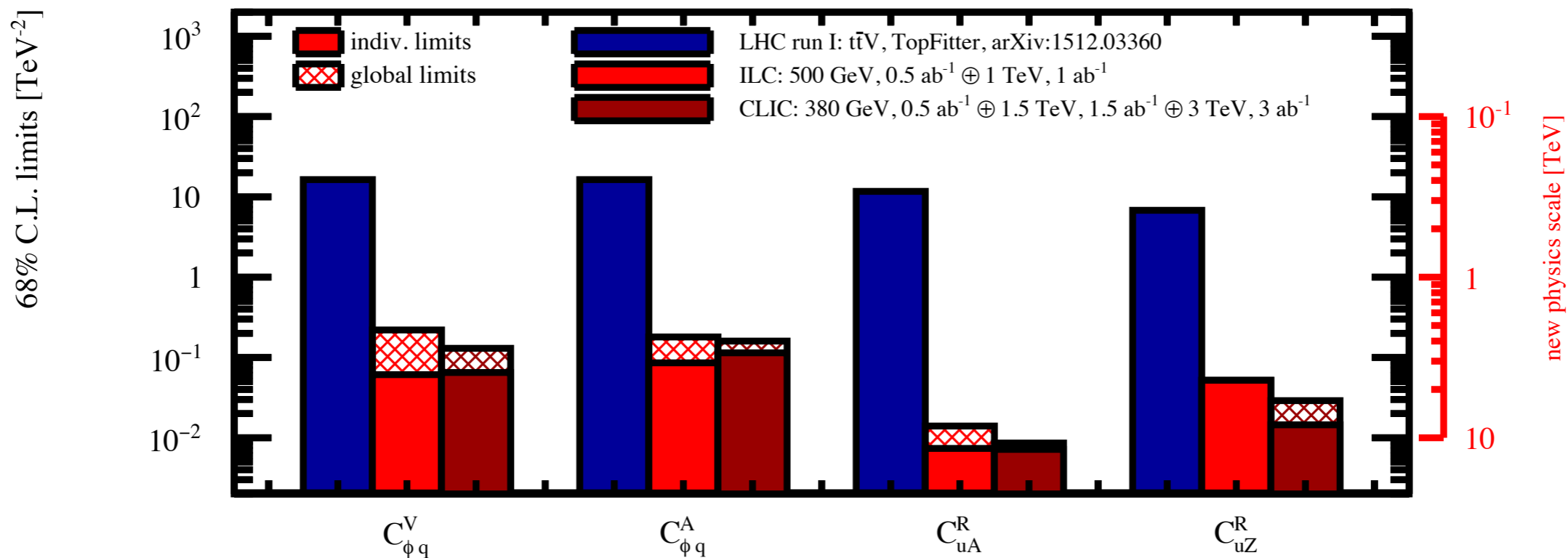


*CLIC at high energy has a great potential to constrain 4-fermion operators*

# **Comparison with the LHC**

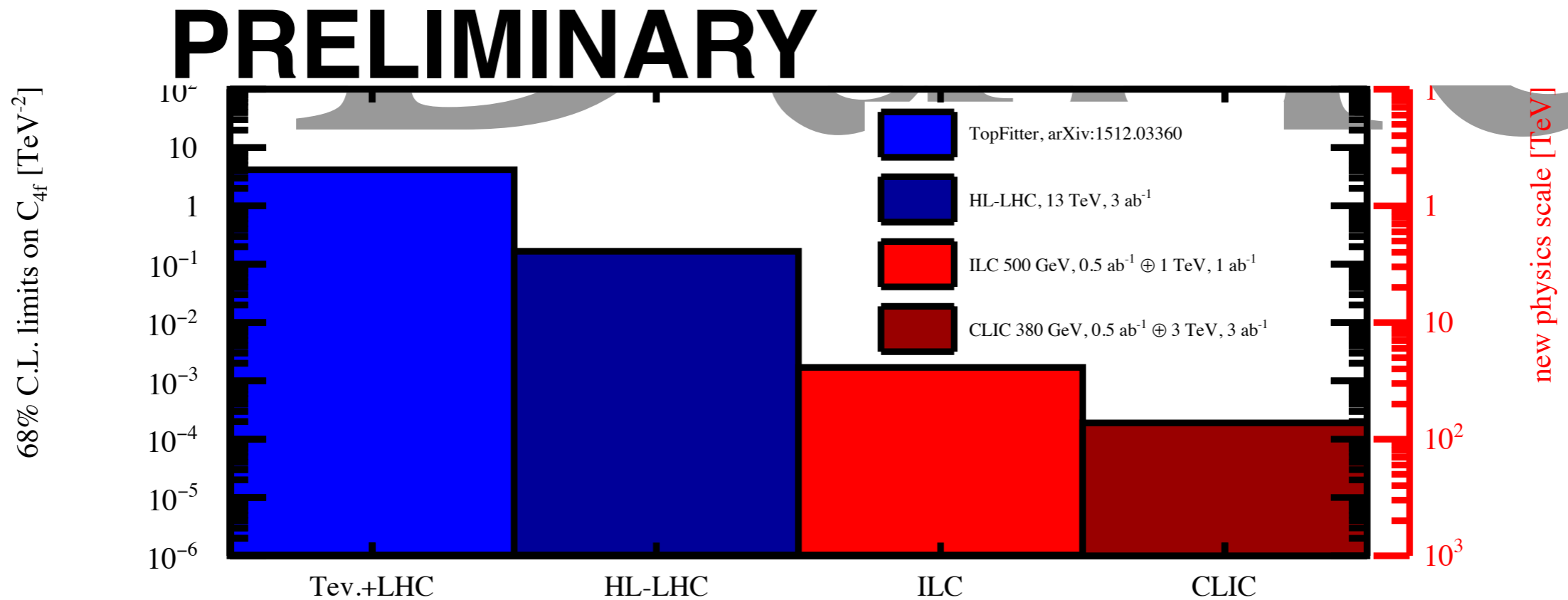
# Comparison with the LHC: vertices

## PRELIMINARY



- Still **preliminary**, final results for ILC still coming.
- Limits between 2 and 3 orders of magnitude better than LHC.
- LHC limits could improve in future stages, but not prospects of this possible improvement at the moment.

# Comparison with the LHC: contact interactions



- Still **preliminary**, final results for ILC still coming.
- Top-philic scenario allows for a comparison between  $q\bar{q}t\bar{t}$  and  $e\bar{e}t\bar{t}$  contact interaction.
- LHC results could be improved using boosted measurements on (MP, Vos, arXiv:1512.07542), but even so couldn't surpass LC limits (3 - 4 orders of magnitude better at the moment).

# Summary on the global fit

---

- Cross-section +  $A_{FB}$  alone are not optimal for a global EFT fit.
- CP-odd operators well constrained by CP-odd optimal observables.
- Only one energy point is not enough for constrain the full set of operators.
- Optimal observables seem to be the proper solution to the global fit.
- Results on the global fit ready for the CLICdp top quark paper (preparing pheno paper including ILC scenario).

**Back up**



# CPV: Optimal CP-odd observables

The **CP-violating effects** in  $e^+e^- \rightarrow t\bar{t}$  manifest themselves in specific **top-spin effects**, namely **CP-odd top spin-momentum correlations and  $t\bar{t}$  spin correlations**.

$$e^+(\mathbf{p}_+, P_{e^+}) + e^-(\mathbf{p}_-, P_{e^-}) \rightarrow t(\mathbf{k}_t) + \bar{t}(\mathbf{k}_{\bar{t}})$$

$$t \bar{t} \rightarrow \ell^+(\mathbf{q}_+) + \nu_\ell + b + \bar{X}_{\text{had}}(\mathbf{q}_{\bar{X}})$$

$$t \bar{t} \rightarrow X_{\text{had}}(\mathbf{q}_X) + \ell^-(\mathbf{q}_-) + \bar{\nu}_\ell + \bar{b}$$

- **CP-odd observables** are defined with the **four momenta available in  $t\bar{t}$  semi-leptonic decay channel**

$$\mathcal{O}_+^{Re} = (\hat{\mathbf{q}}_{\bar{X}} \times \hat{\mathbf{q}}_+^*) \cdot \hat{\mathbf{p}}_+,$$

$$\mathcal{O}_+^{Im} = -\left[1 + \left(\frac{\sqrt{s}}{2m_t} - 1\right)(\hat{\mathbf{q}}_{\bar{X}} \cdot \hat{\mathbf{p}}_+)^2\right] \hat{\mathbf{q}}_+^* \cdot \hat{\mathbf{q}}_{\bar{X}} + \frac{\sqrt{s}}{2m_t} \hat{\mathbf{q}}_{\bar{X}} \cdot \hat{\mathbf{p}}_+ \hat{\mathbf{q}}_+^* \cdot \hat{\mathbf{p}}_+$$

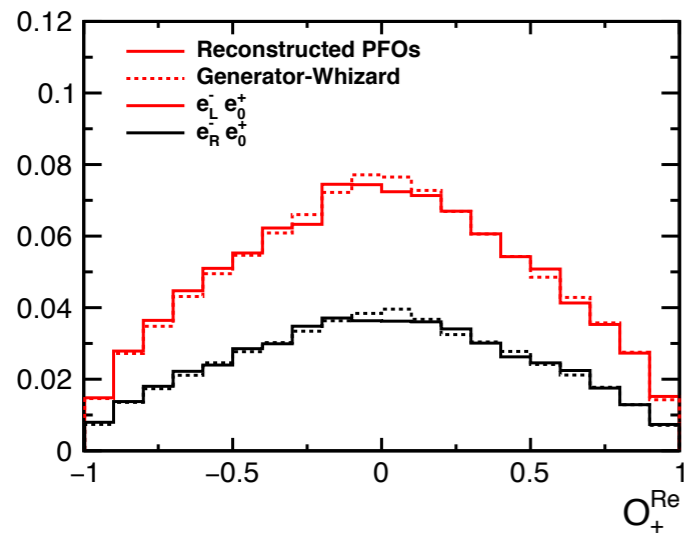
- The way to **extract** the **CP-violating form factor** is to construct **asymmetries sensitive to CP-violation effects**

$$\mathcal{A}^{Re} = \langle \mathcal{O}_+^{Re} \rangle - \langle \mathcal{O}_-^{Re} \rangle = c_\gamma(s) \text{Re}F_{2A}^\gamma + c_Z(s) \text{Re}F_{2A}^Z$$

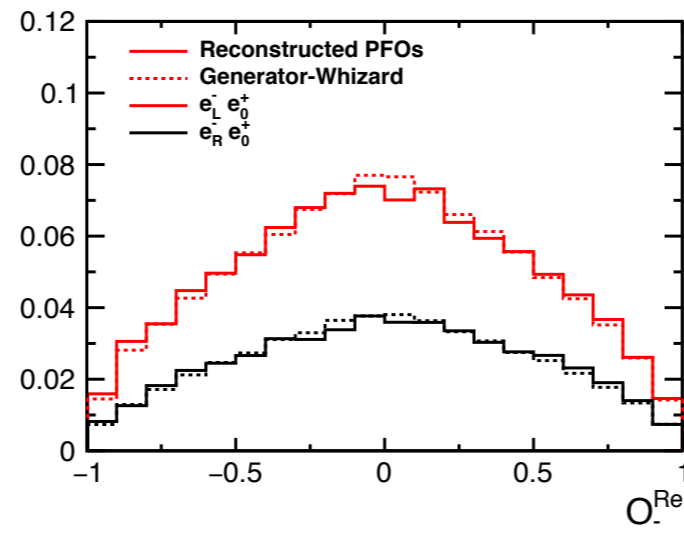
$$\mathcal{A}^{Im} = \langle \mathcal{O}_+^{Im} \rangle - \langle \mathcal{O}_-^{Im} \rangle = \tilde{c}_\gamma(s) \text{Im}F_{2A}^\gamma + \tilde{c}_Z(s) \text{Im}F_{2A}^Z$$

$$\begin{array}{cc} \mathcal{A}_{\gamma,Z}^{Re L} & \mathcal{A}_{\gamma,Z}^{Re L} \\ \mathcal{A}_{\gamma,Z}^{Im R} & \mathcal{A}_{\gamma,Z}^{Im R} \end{array}$$

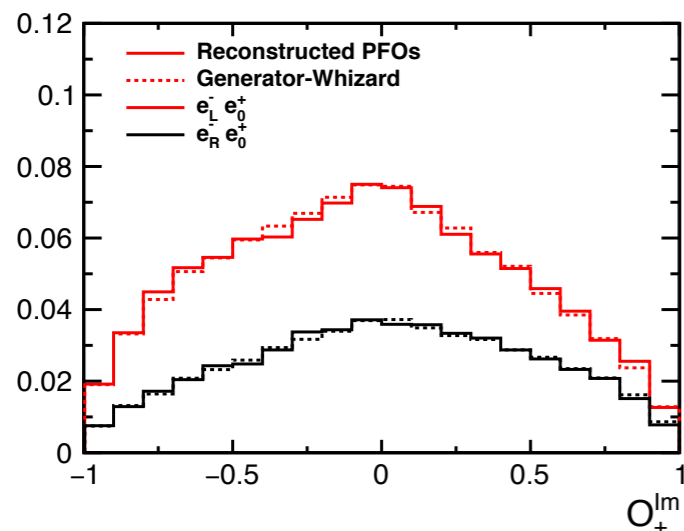
# CPV: Full-simulation: CLIC@380GeV



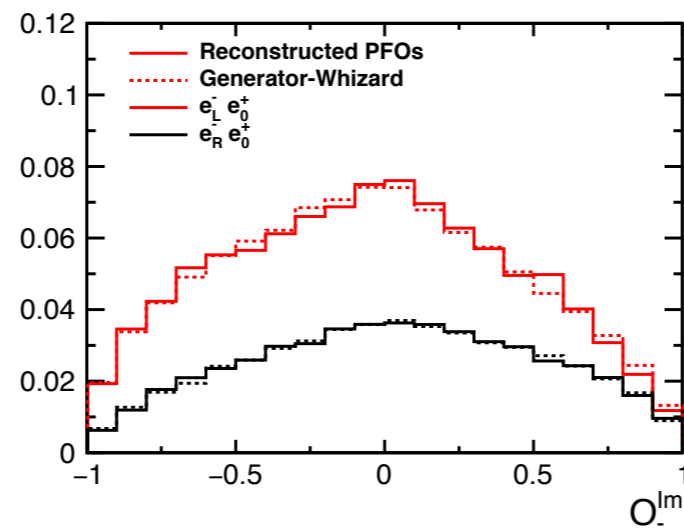
(a)  $\mathcal{O}_+^{Re}$



(b)  $\mathcal{O}_-^{Re}$



(c)  $\mathcal{O}_+^{Im}$



(d)  $\mathcal{O}_-^{Im}$

- Distributions are **centered at zero**
- **Differences** between reconstructed and generated events are **very small**.
- Any **distortions** in the reconstructed distributions are **expected to cancel in the asymmetries**  $A_{Re}$  and  $A_{Im}$
- **Asymmetries** are **compatible with zero** within the statistical error

polarization	$e_L^- (P_{e^-} = -0.8)$	$e_R^- (P_{e^-} = +0.8)$
$A^{Re}$	$-0.00006 \pm 0.003$	$0.0072 \pm 0.003$
$A^{Im}$	$0.0004 \pm 0.003$	$-0.0019 \pm 0.003$

# Statistically optimal observables shape

Example for 500 GeV ( $e^-, e^+$ ) = (-0.8, 0.3)

Theory uncertainties under study

Generated plots

