# Study of fermion pair productions at the ILC with center-of-mass energy of 250 GeV

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#### Abstract

Precise measurements of electroweak processes at the International Linear Collider (ILC) will provide unique opportunities to explore new physics beyond the Standard Model. Fermion pair productions are sensitive to a new contact interaction or a new heavy gauge boson by comparing cross section and angular distribution with expectations of the new physics models. In this proceedings we report a simulation study of fermion pair productions at a center-of-mass energy of 250 GeV, with a focus on lepton pairs, to demonstrate the potential of the first phase of the ILC.

#### 1 Introduction

The International Linear Collider (ILC) is a next generation  $e^+e^-$  linear collider. As recently proposed [8], the first stage of the ILC will be operated at a center-of-mass energy ( $\sqrt{s}$ ) of 250 GeV, mainly targeting precise measurements of the Higgs boson. However, the ILC is also a unique facility to probe new physics not only by direct searches of colorless new particles, but also indirectly by precise measurements of Standard Model (SM) processes. The fermion pair production  $e^+e^- \rightarrow f\bar{f}$ is one of such processes, and any deviations in the total and differential cross sections from the expectations of the SM can be regarded as an indirect evidence for new physics. Unlike the case at the Large Hadron Collider (LHC), both theoretical calculations and experimental measurements of this process can be done with O(0.1%) precision because the production and decay of the Z boson are purely electroweak. We conducted a full simulation study of the  $e^+e^- \rightarrow \ell^+\ell^-$  ( $\ell = e, \mu$  and  $\tau$ ) at  $\sqrt{s} = 250$  GeV, and discuss possibility to discover new physics and identify physics models.

# 2 Simulation Conditions

We utilized ILCSoft[1] package of version v01-16-02-p1 for this study. The event generation was done by WHIZARD [2] with PYTHIA [3] for hadronization. The full Monte Carlo simulation was

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done with Mokka based on Geant4 [4] framework with the reference geometry of the International Large Detector (ILD) concept used in the studies of Detailed Baseline Design report [5], ILD\_v1\_05 model. The model includes silicon pixel and strip detectors, a time projection chamber, precisely segmented electromagnetic and hadron calorimeters (ECAL and HCAL) and a 3.5 Tesla solenoid magnet. Event reconstruction was done with Marlin processors [6], including tracking and particle flow reconstruction by PandoraPFA algorithm [7] to obtain track-cluster matching. For the lepton tagging, simple criteria based on cluster energies in both ECAL and HCAL and track momentum are used. Details are described in Section 3.

We assume the 250 GeV stage of H20 running scenario [8] with a total luminosity of 2000 fb<sup>-1</sup>, with 45%  $e_L^- e_R^+$  and 45%  $e_R^- e_L^+$  polarization, where  $|P(e^-)| = 0.8$  and  $|P(e^+)| = 0.3$  are assumed. We included all 2-fermion and 4-fermion pure-leptonic final states and 2-fermion hadronic final states as background. The statistics of the Monte Carlo samples correspond to 11 to 680 fb<sup>-1</sup>, which is not the full statistics of H20 staging scenario, but we applied event weights to recover the statistics.

For  $e^+e^- \rightarrow e^+e^-$  (Bhabha) events, we applied a preselection of  $|\cos\theta| < 0.97$  for each track and energy sum of  $e^+e^-$  more than 200 GeV to avoid too much event simulation.

### **3** Event Selection

Here we select the  $e^+e^- \rightarrow \ell^+\ell^-$  by following selection criteria, where  $e^+e^-$  and  $\mu^+\mu^-$  final states are selected similarly except the lepton tagging, while a different strategy is applied for selection of  $\tau^+\tau^-$  final states.

The  $e^+e^-$  and  $\mu^+\mu^-$  events have two lepton tracks and basically nothing else in their final states. Firstly we select a positive and a negative tracks with highest energies, and their energies must be more than 10 GeV. Then, we apply a lepton tagging criteria for each track based on its energy calculated from the track curvature  $E_{\rm tr}$ , reconstructed energy deposits in ECAL ( $E_{\rm ECAL}$ ) and HCAL( $E_{\rm HCAL}$ ). Electrons can be identified by that most of their energy is deposited at the ECAL than HCAL, and muons can be identified by penetration of calorimeters. For electrons,  $(E_{\rm ECAL} + E_{\rm HCAL})/E_{\rm tr} > 0.6$  and  $E_{\rm ECAL}/(E_{\rm ECAL} + E_{\rm HCAL}) > 0.9$  are required, while for muons,  $(E_{\rm ECAL} + E_{\rm HCAL})/E_{\rm tr} < 0.6$  and  $E_{\rm ECAL}/(E_{\rm ECAL} + E_{\rm HCAL}) < 0.5$  are required. Both of the tracks should pass the criteria to be recognized as  $e^+e^-$  and  $\mu^+\mu^-$  final states. After that, we apply a kinematic cut that energy sum of the two tracks  $E_{\rm sum}$  must be larger than 230 GeV and both of the tracks should be in an angular region  $|\cos \theta| < 0.95$ , where  $\theta$  is the angle with respect to the beam axis. The first selection rejects most of  $W^+W^-$ ,  $\tau^+\tau^-$  and  $Z\gamma \to \ell^+\ell^-\gamma$  events and the second selection rejects most of  $w^+w^-$ . The cut statistics are shown in Tables 1 and 2.

The  $\tau$  pair final state needs slightly different selection since a  $\tau$  lepton decays to multiple particles. So we need "tau clustering". Our clustering method is described in [9], which is basically clustering of particles with an invariant mass less than 2 GeV. We select a positive and a negative clusters with highest energies as the  $\tau$  candidates. We require the cluster energy  $E_{\rm clu} > 10$  GeV for each of them. Then the opening angle between the clusters ( $\theta_{cc}$ ) is required to be larger than 178 degree to reject  $Z\gamma$  events, the visible energy should be between 50 and 200 GeV to separate  $e^+e^$ and  $\mu^+\mu^-$  events, and the  $\tau$  clusters are in the angular region  $|\cos \theta| < 0.95$  to reject *t*-channel events. The cut statistics are shown in Table 3.

Selection of $e^+e^- \rightarrow e^+e^-$	$e_L^- e_R^+$			$e_R^- e_L^+$		
	signal	2f bkg.	4f bkg.	signal	2f bkg.	4f bkg.
All events after preselection	216M	11.7M	44.9M	210M	9.34M	1.24M
Two tracks with $E_{\rm tr} > 10 {\rm ~GeV}$	212M	8.75M	$3.65 \mathrm{M}$	207M	$6.77 \mathrm{M}$	966k
Electron tagging	209M	410k	849k	204M	309k	565k
$E_{\rm sum} > 230  {\rm GeV}$	105M	44	40.0k	102M	29	38.7k
$ \cos\theta  < 0.95$	55.8M	33	9.95k	54.5M	12	9.56k

Table 1: Cut statistics of  $e^+e^- \rightarrow e^+e^-$  channel. The "Two tracks with  $E_{\rm tr} > 10$  GeV" row includes the selection of having two oppositely-charged particles. Details of electron tagging is described in the text.

Selection of $e^+e^- \to \mu^+\mu^-$	$e_L^- e_R^+$			$e_R^- e_L^+$		
	signal	2f bkg.	4f bkg.	signal	2f bkg.	4f bkg.
All events after preselection	6.13M	221M	44.9M	5.01M	214M	1.24M
Two tracks with $E_{\rm tr} > 10 {\rm ~GeV}$	5.03M	216M	$3.65 \mathrm{M}$	3.94M	208M	966k
Muon tagging	3.96M	79.6k	550k	3.11M	57.9k	70.3k
$E_{\rm sum} > 230 {\rm GeV}$	1.61M	11	743	1.34M	1	596
$ \cos\theta  < 0.95$	1.52M	11	71	1.27M	1	578

Table 2: Cut statistics of  $e^+e^- \rightarrow \mu^+\mu^-$  channel. The "Two tracks with  $E_{\rm tr} > 10$  GeV" row includes the selection of having two oppositely-charged particles. Details of muon tagging is described in the text.

# 4 Analysis

Figure 1 shows the angular distributions after the event selection. These distributions are used to evaluate the precision of the ILC measurements on *i*-th  $\cos \theta$  bin,  $\delta \sigma_i / \sigma_i$  (SM), by

$$\frac{\delta\sigma_i}{\sigma_i(\mathrm{SM})} = \frac{\sqrt{S_i + N_i}}{S_i} \tag{1}$$

where  $S_i$  and  $N_i$  are the number of signal and background events in each bin. In this study systematic uncertainty is not considered.

Here we investigated possibility to search for two types of new physics models based on the obtained precision. The first is Z' models [10], where Z' is an additional neutral vector gauge boson coupled to SM fermions. The coupling constants differ depending on models, and we used SSM (Sequential Standard Model), and  $E_6$  models. The SSM assumes the same coupling constants as SM Z. On the other hand, the  $E_6$  is a string-motivated model which naturally introduces Z' as a linear combination of the two extra U(1) gauge bosons  $Z_{\psi}$  and  $Z_{\chi}$ :  $Z' = Z_{\chi} \cos \beta + Z_{\psi} \sin \beta$ . We investigated three  $\beta$  parameters:  $\beta = 0$  ( $\chi$  model),  $\beta = \pi/2$  ( $\psi$  model) and  $\beta = \pi - \arctan\sqrt{5/3}$  ( $\eta$  model). ALR (Alternative Left-Right symmetric) is another model also introduced from  $E_6$ , which gives extra  $SU(2)_R$  in addition to SM  $SU(2)_L$ . This introduces an additional  $Z_R$  boson phenomenologically treated as Z', which behaves like SM Z, but gives different couplings to SM particles.

Selection of $e^+e^- \to \tau^+\tau^-$	$e_L^- e_R^+$			$e_R^- e_L^+$		
	signal	2f bkg.	4f bkg.	Signal	2f bkg.	4f bkg.
All events	5.56M	222M	44.9M	4.33M	215M	1.24M
Two tau clusters with $E_{\rm clu} > 10 {\rm ~GeV}$	1.89M	132M	2.02M	1.44M	128M	238k
$\theta_{cc} > 178 \text{ deg.}$	705k	11.6k	46.6k	568k	112M	40.7k
$50 \text{ GeV} < E_{\text{vis}} < 200 \text{ GeV}$	658k	61.2M	8.30k	530k	$59.4 \mathrm{M}$	4.10k
$ \cos\theta  < 0.95$	587k	12.9k	3.55k	455k	13.6k	304

Table 3: Cut statistics of  $e^+e^- \rightarrow \tau^+\tau^-$  channel. The "Two tau clusters with  $E_{\rm tr} > 10$  GeV" row includes the selection of having two oppositely-charged clusters.

The LHC experiments already gave lower limits at around 4.5 TeV ( $Z' \rightarrow e^+e^-$  and  $\mu^+\mu^-$  combined) and around 2.4 TeV ( $Z' \rightarrow \tau^+\tau^-$ ) [11, 12] with direct reconstruction of the mass peak assuming the SSM model, but the LHC experiments have not given limits assuming other models.

The new physics model is a generic search of a WIMP (weakly-interacting massive particle) dark matter [13]. In the  $e^+e^- \to f\bar{f}$  process, WIMP ( $\chi$ ) can be introduced in a  $Z \to \chi\chi \to Z$  loop diagram, which gives a correction to the coupling constant. The correction basically only depends on a group structure, spin and mass of  $\chi$  and is independent of model details. We investigated three well-motivated types of WIMPs: wino  $(SU(2)_L \text{ triplet and } U(1)_Y \text{ hypercharge of } 0)$ , Higgsino  $(SU(2)_L \text{ doublet and } U(1)_Y \text{ hypercharge of } \pm 1/2)$  and Minimal Dark Matter  $(SU(2)_L \text{ pentet and } U(1)_Y \text{ hypercharge of } 0)$ .

To investigate the performance of search for WIMP in these models, we obtained the deviation of  $e^+e^- \rightarrow f\bar{f}$  cross section:  $\delta\sigma_i(\text{BSM})/\sigma_i(\text{SM})$  by theoretical prediction and obtain the  $\chi^2$  value for each model as

$$\chi^{2}(\text{BSM}) = \sum_{i} \left\{ \left( \frac{\delta \sigma_{i}(\text{BSM})}{\sigma_{i}(\text{SM})} / \frac{S_{i}}{\sqrt{S_{i} + N_{i}}} \right)^{2} + 1 \right\},$$
(2)

to calculate the rejection probability of each model with pure-SM distribution.

Figures 2, 3 and 4 shows the  $\delta\sigma_i(\text{BSM})/\sigma_i(\text{SM})$  and  $\delta\sigma_i(\text{BSM})/\sigma_i(\text{SM})$  of  $e^+e^- \to e^+e^-$ ,  $\mu^+\mu^$ and  $\tau^+\tau^-$  final states. Here we only show the distribution on  $e_L^-e_R^+$  which is much more powerful than  $e_R^-e_L^+$  polarization. The plots show that 2.5 TeV Z' is easily discovered for most of the models while 5.0 TeV Z' is hard to identify.

The calculated probability based on the  $\chi^2$  with various Z' masses is shown in Figure 5. The obtained  $3\sigma$  limit of the model rejection is shown in Table 4.

Z' model	mass reach at $3\sigma$
SSM	$2.8 \mathrm{TeV}$
ALR	$4.0 \mathrm{TeV}$
$\chi$	$2.9 \mathrm{TeV}$
$\psi$	$1.4 \mathrm{TeV}$
$\eta$	1.8 TeV

Table 4: The minimal Z' mass observed as the  $3\sigma$  deviation from the SM by  $e^+e^- \rightarrow \ell^+\ell^-$  measurements of 250 GeV ILC.

Figure 6 is similar to Figures 2, 3 and 4, but for generic WIMP search of various WIMP masses. The probability distribution and  $3\sigma$  limit is shown in Figure 7 and Table 5. It shows that the mass reach is higher than the beam energy, which means we can extend the searching power of WIMP by using this measurement.

WIMP Model	mass reach at $3\sigma$
higgsino $e_L^- e_R^+$	$150 \mathrm{GeV}$
MDM $e_L^- e_R^+$	$330 { m GeV}$
wino $e_L^- e_R^+$	$150 \mathrm{GeV}$

Table 5: The minimal WIMP mass observed as the  $3\sigma$  deviation from the SM by  $e^+e^- \rightarrow \ell^+\ell^-$  measurements at  $\sqrt{s} = 250$  GeV at the ILC.

# 5 Summary and Prospects

We investigated the  $e^+e^- \rightarrow \ell^+\ell^-$  final states at  $\sqrt{s} = 250$  GeV for a new physics study. Precise measurements of total and differential cross sections of the process can be a good probe to new physics including a Z' or a WIMP. In our study, Z' can be probed up to 1.4-4.0 TeV depending on the models, and WIMP can be searched for up to 150-330 GeV, which significantly extends the possibility to discover these new particles from direct searches. We are investigating more new physics models, such as the Gauge Higgs Unification model described at [14] We plan to include the hadronic final states in the near future to conclude this study. For the hadronic final states, charge identification of jets is essential, which is a good challenge for the ILC detectors and the reconstruction software. The performance of the jet charge identification has been studied in [15], which can be applicable to this study.

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#### References

- [1] http://ilcsoft.desy.de/portal/
- [2] W. Kilian, T. Ohl, J. Reuter, WHIZARD: Simulating Multi-Particle Processes at LHC and ILC, Eur. Phys. J. C71 (2011) 1742.
- [3] Torbjörn Sjöstrand et al., PYTHIA 6.4 physics and manual, J. High Energ. Phys. 05 (2006) 026.
- [4] GEANT4 Working Group, http://geant4.web.cern.ch/geant4

- [5] Ties Behnke *et al.*, Technical Design Report Volume 4: Detectors. 2013, arXiv:1306.6329.
- [6] F. Gaede, "Marlin and LCCD Software tools for the ILC ", Nucl. Instrum. Meth.A 559 (2006) 177 - 180.
- [7] M.A. Thomson, Particle Flow Calorimetry and the PandoraPFA Algorithm. Nucl. Instrum. Meth. A611 (2009) 25-40.
- [8] Keisuke Fujii *et al.*, Physics Case for the 250 GeV Stage of the International Linear Collider, arXiv:1710.07621.
- [9] Taikan Suehara, Analysis of Tau-pair process in the ILD reference detector model, arXiv:0909.2398.
- [10] JoAnne L. HEWETT, Thomas G.RIZZO, Energy phenomenology of superstring-inspired E<sub>6</sub> models, Physics reports 183, Nos.5 & 6 (1989) 193-383.
- [11] ATLAS Collaboration, Search for new high-mass phenomena in the dilepton final state using 36 fb<sup>-1</sup> of proton-proton collision data at  $\sqrt{s} = 13$  TeV, J. High Energ. Phys. (2017) **2017**: 182.
- [12] CMS Collaboration, Search for heavy resonances decaying to tau lepton pairs in proton-proton collisions at √s = 13 TeV, J. High Energ. Phys. (2017) 2017: 48.
  CMS Collaboration, Multiplicity and rapidity dependence of strange hadron production in pp, pPb, and PbPb collisions at the LHC, Phys. Lett. B768(2017) 103-129.
- [13] Keisuke Harigaya, Koji Ichikawa, Anirban Kundu, Shigeki Matsumoto, Satoshi Shirai, Indirect Probe of Electroweak-Interacting Particles at Future Lepton Colliders, J. High Energ. Phys. (2015) 2015: 105.
- [14] Shuichiro Funatsu, Hisaki Hatanaka, Yutaka Hosotani, Yuta Orikasa, Distinct signals of the gauge-Higgs unification in  $e^+e^-$  collider experiments, Phys. Lett. **B755** (2017) 297-302.
- [15] S. Bilokin *et al.*, Measurement of b quark EW couplings at ILC, arXiv:1709.04289.

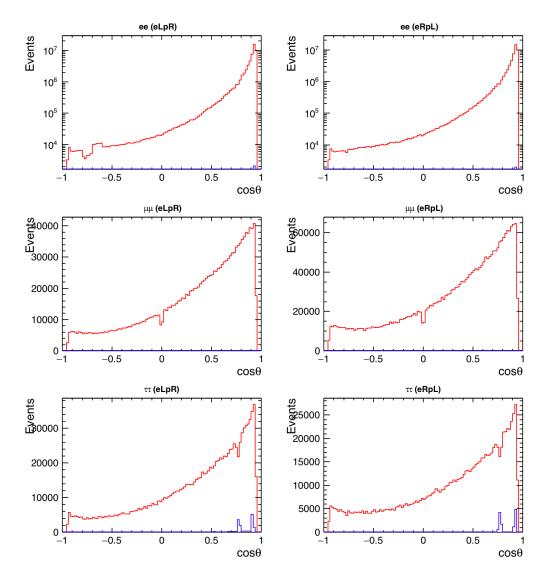


Figure 1: Angular distributions after the event selections. Left (right) figures show the distributions of  $e_L^- e_R^+$  ( $e_R^- e_L^+$ ) polarization. The upper, the middle and the lower figures show  $e^+ e^-$ ,  $\mu^+ \mu^-$  and  $\tau^+ \tau^-$  channels, respectively. The  $e^+ e^-$  channels are shown in logarithmic scales while the other channels are shown in linear scales. Red (blue) lines show distributions of signal (background) events.

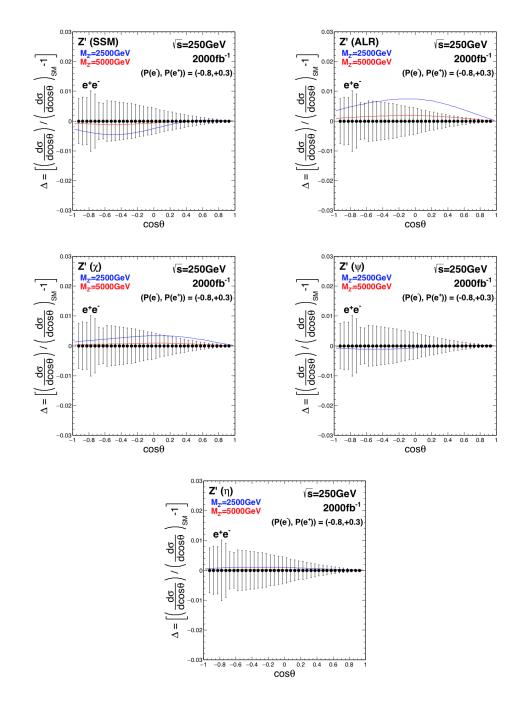


Figure 2: Effect of Z' of SSM and  $E_6$  models as deviation of the differential cross section of  $e^+e^- \rightarrow e^+e^-$  from the SM. Red (blue) lines show the deviation by Z' mass of 2.5 (5.0) TeV. The expected precision of measurements at  $\sqrt{s} = 250$  GeV is shown in the error bars, assuming H20 staging scenario written in the text.

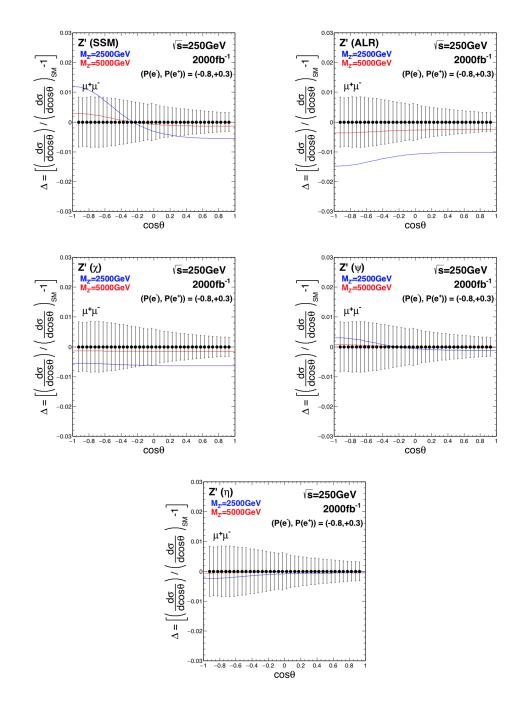


Figure 3: Effect of Z' of SSM and  $E_6$  models as deviation of the differential cross section of  $e^+e^- \rightarrow \mu^+\mu^-$  from the SM. Red (blue) lines show the deviation by Z' mass of 2.5 (5.0) TeV. The expected precision of measurements at  $\sqrt{s} = 250$  GeV is shown in the error bars, assuming H20 staging scenario written in the text.

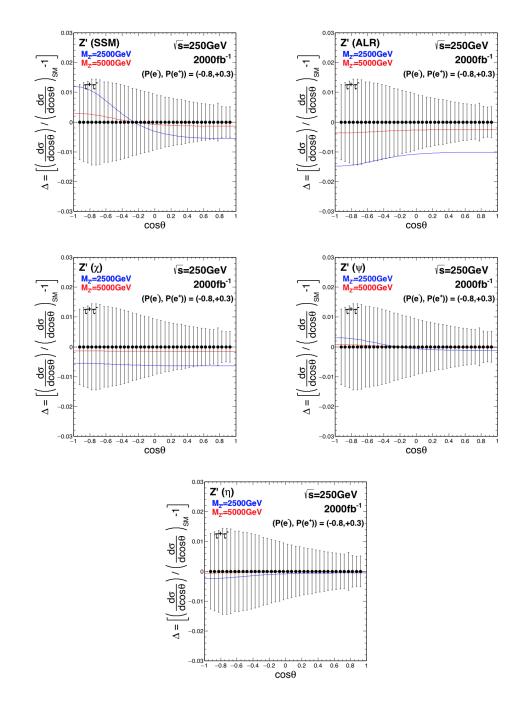


Figure 4: Effect of Z' of SSM and  $E_6$  models as deviation of the differential cross section of  $e^+e^- \rightarrow \tau^+\tau^-$  from the SM. Red (blue) lines show the deviation by Z' mass of 2.5 (5.0) TeV. The expected precision of measurements at  $\sqrt{s} = 250$  GeV is shown in the error bars, assuming H20 staging scenario written in the text.

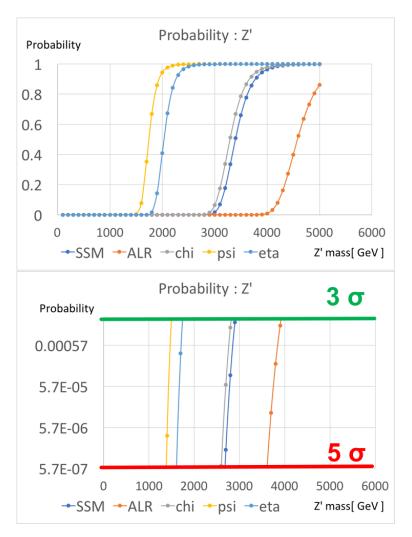


Figure 5: Probability of the distributions consistent to SM under the deviation by Z' models, calculated by the  $\chi^2$  defined in the text. The left figure shows the dependence of probability on the Z' mass on each model, and the right figure shows the minimum Z' mass which can be detected as  $3\sigma$  and  $5\sigma$  deviation from the SM. e,  $\mu$  and  $\tau$  channels are combined.

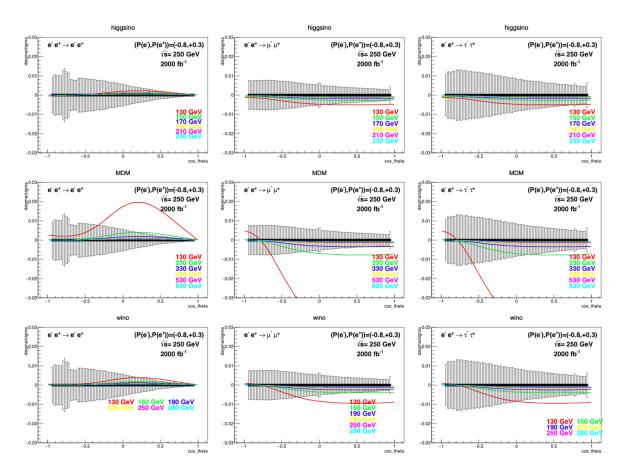


Figure 6: Effect of WIMP models as deviation of the differential cross section of  $e^+e^- \rightarrow \ell^+\ell^$ from the SM. The upper, the middle and the lower figures show the Higgsino  $(n = 2, Y = \pm 1/2)$ , wino (n = 3, Y = 0) and Mimimal Dark Matter (n = 5, Y = 0) where n is  $SU(2)_L$  n-plet and Y is the  $U(1)_Y$  hypercharge, respectively. The left, the middle and the right figures show deviation of  $e^+e^-$ ,  $\mu^+\mu^-$  and  $\tau^+\tau^-$  channels, respectively. The error bars show the expected precision at  $\sqrt{s} = 250$  GeV.

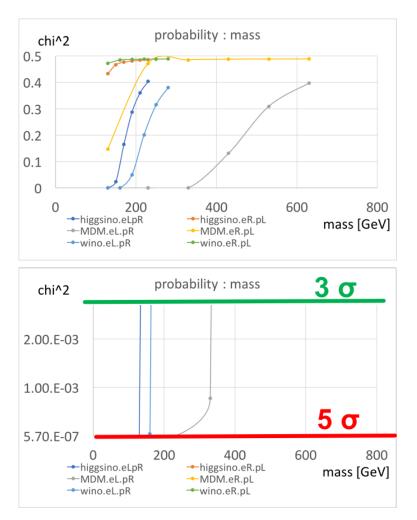


Figure 7: Probability of the distributions consistent to SM under the deviation by WIMP models, calculated by the  $\chi^2$  defined in the text. The left figure shows the dependence of probability on the WIMP mass on each model, and the right figure shows the minimum WIMP mass which can be detected as  $3\sigma$  and  $5\sigma$  deviation from the SM. e,  $\mu$  and  $\tau$  channels are combined.