

# Investigation of the beam halo and momentum tail at the ATF

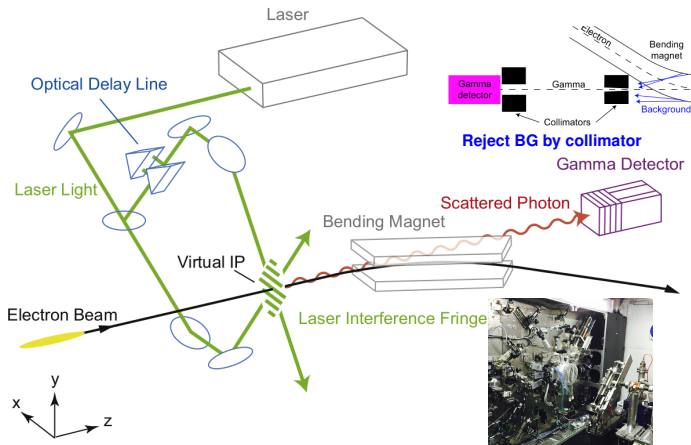
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May 28, 2018

# Motivations

- Background induced by halo particles loss upstream of IP might reduce the modulation resolution of *Shintake* monitor
- To understand the genesis of halo and its distribution !

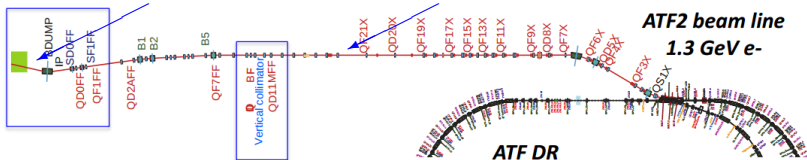
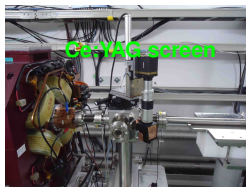


\* Figures from [1] J. Yan, et al., NIMA 740(2014) 31-137; [2] T. Suehara, et al., NIMA 616(2010) 1-8

- Instrumentations for halo diagnostic: DS and YAG/OTR
- Vertical beam halo formation: BGS process
- Horizontal halo/momentum tail: Touschek scattering?
- Conclusion

# Instrumentations for beam halo diagnostics

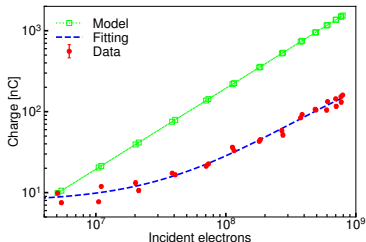
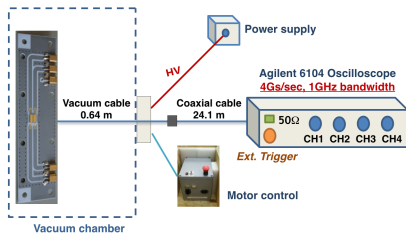
- First measurement: wire scanners at the previous EXT line, 2005
- New diagnostics: diamond sensor (DS) detector and YAG/OTR monitor



DS:  $\eta_x \approx 1$  m,  $\eta_y \approx 0$ ; YAG/OTR:  $\eta_x \approx 0$ ,  $\eta_y$  tunable!



# in vacuum diamond sensor detector

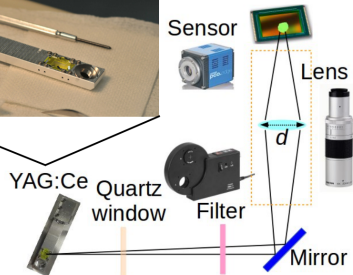
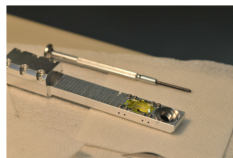
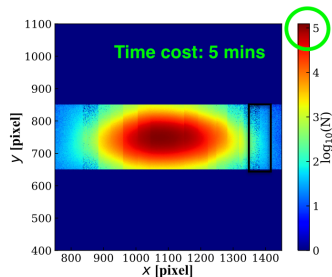


- Two  $1.5 \text{ mm} \times 4 \text{ mm}$  and two  $0.1 \text{ mm} \times 4 \text{ mm}$  sCVD DS strips
- **Dynamic range**  $d_R \approx 10^5$ 
  - \* Lower limit: induction current/noise level  
 $> 2 \times 10^{-3} \text{ nC}$  ( $> 1 \times 10^3 e$ )
  - \* Upper limit: charge collection saturation  
 $\sim 1 \times 10^2 \text{ nC}$
- Signal of core is re-scaled by "self-calibration" thanks to WS upstream of DS
  - \* Approximating charge collected in the core by extrapolating WS measurement
  - \* Re-scaling factor  
$$\kappa(n_e) = Q_{exp}/Q_{meas}$$

[1] S. Liu, *et al.*, NIMA, 832 (2016)

# A novel Ce:YAG/OTR monitor

- YAG  $\rightarrow$  core/halo; OTR  $\rightarrow$  core (saturation-free)
- Collaboration among KEK, CERN and LAL
- Critical Performance:  
 **$\text{DNR} > 10^5$  and resolution  $< 10\ \mu\text{m}$**
- Scanning (x or y) using YAG + ND filter  
 $\rightarrow$  avoiding the blooming effect
- Multi-shot measurements  
 $\rightarrow$  Position/beam size jitter  $< 5\%$

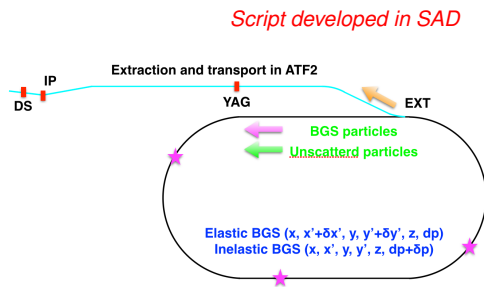
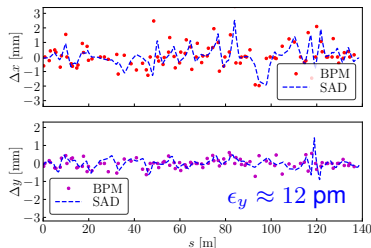


# Monte Carlo simulation of BGS

- Analytical approximations based on K. Hirata's model
- Realistic COD in the DR  
→ approach the operation  $\epsilon_y$
- Two atoms per molecule with  $A=\sqrt{50}$   
→ represent residual gas
- Tracking scattered & unscattered particles separately

Main parameters of ATF DR

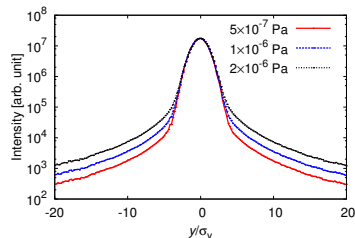
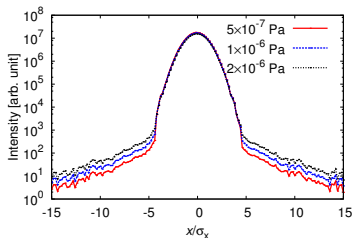
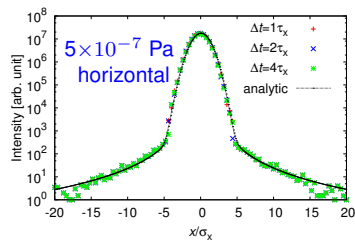
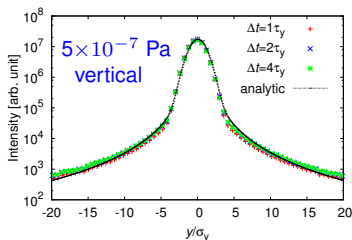
Beam energy [GeV]	1.282
Circumference [m]	138.56
Ver. emittance [ $\mu\text{m}$ ]	12
Hor. emittance [nm]	1.17
Energy spread [%]	0.056
Bunch length [mm]	5.3
Damping time [ms]	27.0/19.8/20.6



[1] K. Hirata and K. Yokoya, Part. Accel. 39, 147 (1992)

# Numerical predictions from two methods

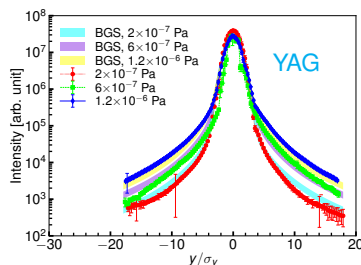
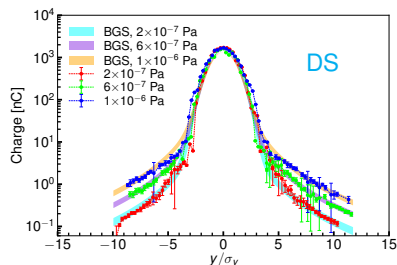
- Two predictions agree well: vacuum pressures  $< 2 \times 10^{-6}$  Pa
- Vertical tail is more significant, in the  $y/\sigma_y$  coordinate



- So, how about the halo distribution in the real world...

# Vertical beam halo due to BGS

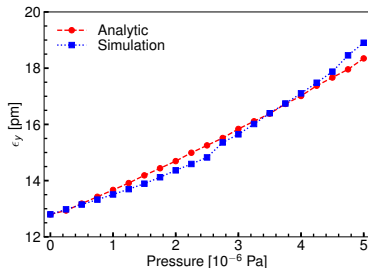
- Beam profiles measured by DS after re-scaling and that by YAG monitor are in good agreement with the numerical predictions
- Higher tail for the worsened vacuum:  $2 \times 10^{-7}$  Pa  $\rightarrow$   $1 \times 10^{-6}$  Pa
- Vertical beam halo is dominated by elastic BGS<sup>1</sup>!



<sup>1</sup> See, R. Yang, *et al.*, Phys. Rev. Accel. Beams 21, 051001 (2018)

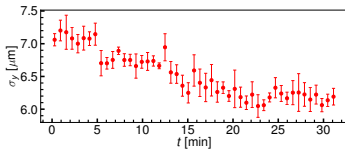
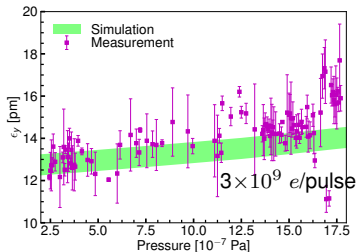
# Vertical emittance growth due to BGS

- Small-angle beam-gas scattering  
→ ver. emittance dilution
- Long ver. damping time (27 ms)
- Numerical estimations predict a  $\epsilon_y$  growth from 12.8 pm to 18.7(18.9) pm for a vacuum pressure of  $5 \times 10^{-6}$  Pa



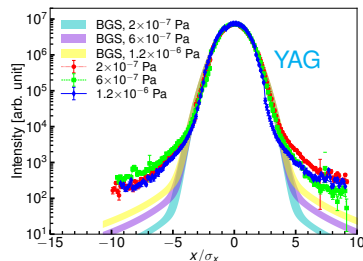
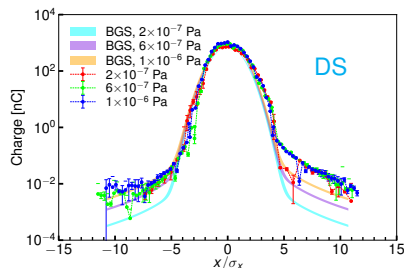
Measurable and significant!

- Ver. emittance obtained using an X-ray SR monitor;  $2 \times 10^{-7}$  Pa to  $1.75 \times 10^{-6}$  Pa
- More than 10% emittance growth!



# Horizontal profile measurements

- Measurements are higher than the numerical predictions (BGS)
- Asymmetric distribution, more particles on the high energy side
- No significant change for the degraded vacuum
- Other dominating mechanisms (Touschek scattering?)

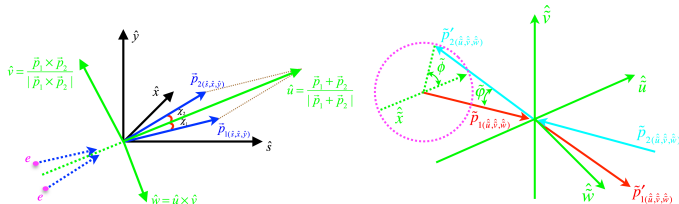


PS: Optical aberration and secondary emission in ATF2, and the imperfect extraction kicker field → demonstrated to be small

# Tail from Coulomb scattering of particles?

- IBS/Touschek scattering is very strong in the ATF DR
- Large-angle collisions result in large  $\delta_p \rightarrow$  Touschek lifetime
- Particles after large-angle  $\theta$  collisions and remain within the separatrix  
 $\rightarrow$  Momentum tail and hor. tail (?)

$$\Delta \vec{p}_{1,2} = \pm p_{1,2} \begin{pmatrix} \gamma_t [\gamma_t (\cos \chi_{1,2} - \beta_t / \beta_{1,2}) \cos \tilde{\varphi} + \sin \chi \sin \tilde{\varphi} \cos \tilde{\phi}] - \gamma_t \tilde{p}_s / p_{1,2} \\ \sqrt{\gamma_t^2 (\cos \chi_{1,2} - \beta_t / \beta_{1,2})^2 + \sin^2 \chi} \sin \tilde{\varphi} \sin \tilde{\phi} \\ \sin \chi (\cos \tilde{\varphi} - 1) - \gamma_t (\cos \chi_{1,2} - \beta_t / \beta_{1,2}) \sin \tilde{\varphi} \cos \tilde{\phi} \end{pmatrix}_{\hat{u}, \hat{v}, \hat{w}}$$



Momentum tail is more "clean", i.e., less influence from transverse non-linearity  
 $\rightarrow$  Momentum tail imaging

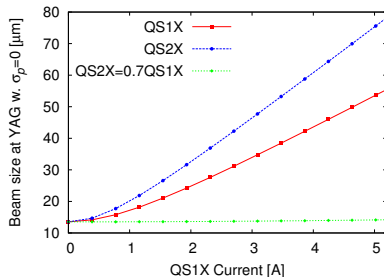
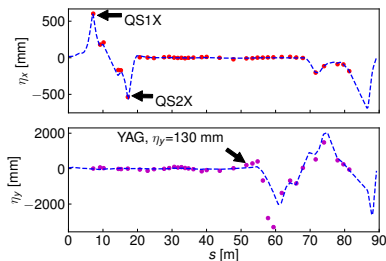


# Design of energy spectrum measurement (1)

- Min. distinguishable energy deviation

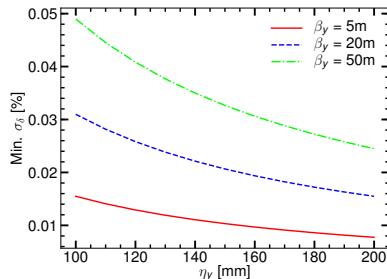
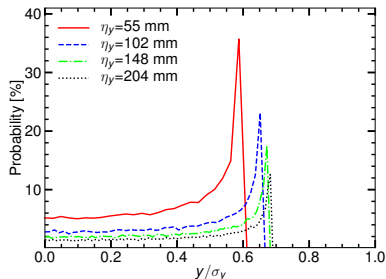
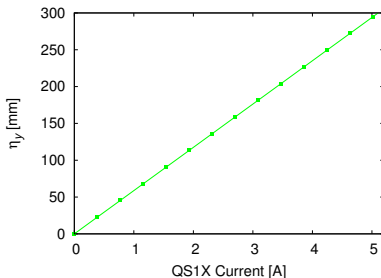
$$\delta_{m,sep} \geq 2\sqrt{\epsilon\beta}/\eta$$

- Small  $\beta$  and large  $\eta$ , but  $\epsilon_x \approx 100\epsilon_y \rightarrow$  vertical observation is superior!
- Vertical dispersion blowing up:
  - Adjusting  $\eta_y$  by tuning QS1X/QS2X with specific ratio, e.g., 10:7
  - Ver. profile  $\leftarrow$  energy spectrum if  $\eta_y$  is large enough ( $>150$  mm)



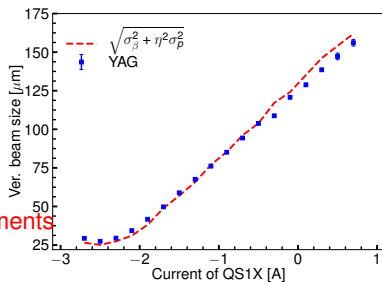
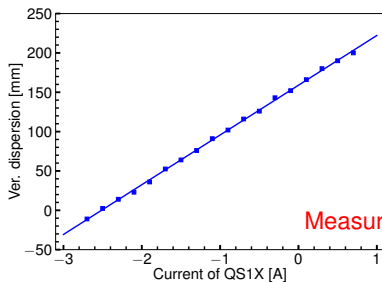
# Design of energy spectrum measurement (2)

- Vertical dispersion at the YAG can be increased to around 300 mm
- Impact of the betatron  $xy$  coupling ( $R_{31}$ ,  $R_{32}$ ) is small, e.g.,  $< 0.6 \sigma_y$  for  $2J_x = 400\epsilon_x$
- Min. distinguishable momentum deviation:  
around  $3 \times 10^{-4}$  for  $\eta_y > 160$  mm



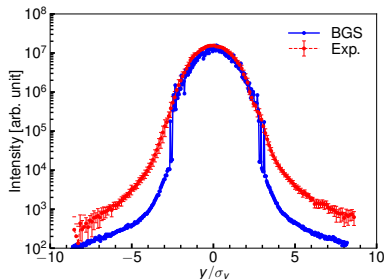
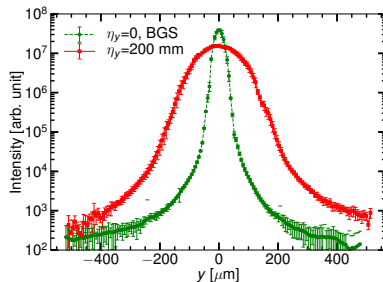
# Increase of the vertical dispersion

- Residual ver. dispersion  $\rightarrow$  non-zero current of QS1X/QS2X
- Dispersion at YAG is approached by that measured by a BPM attached to QM16 quad. ( $\Delta s \approx 30$  mm)
- $\beta_y \approx 50$  m; Dispersion domain for  $\eta_y > 160$  mm  
 $\rightarrow$  Measurements for  $\eta_y \approx 200$  mm @ YAG



# First observation of energy spectrum

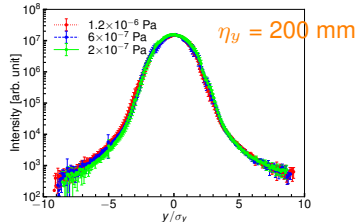
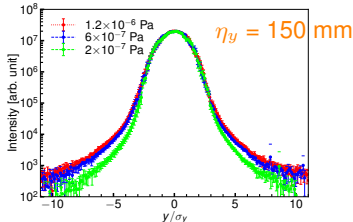
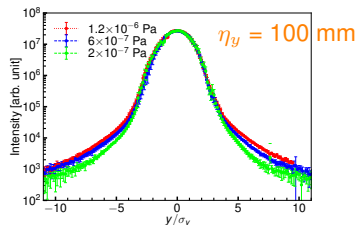
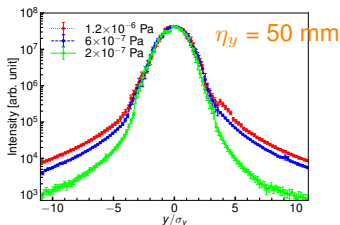
- Simulations with the measured vertical betatron profile at EXT kicker
- For  $\eta_y = 200$  mm, the measured vertical tail is higher than the prediction by at least a factor of 4 → Momentum profile!?



- Influence of the betatron halo (BGS) and  $xy$  coupling terms? Due to Touschek scattering?

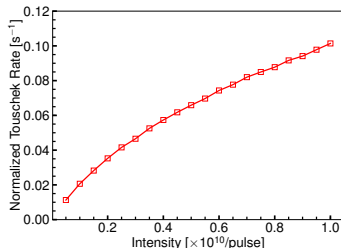
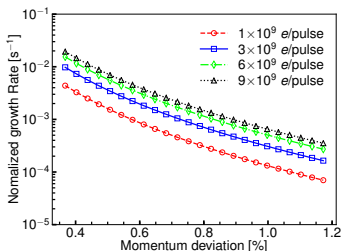
# Energy spectrum - vacuum dependence

- BGS process results in the vertical betatron halo  
→ Variation of vertical tail/halo for various vacuum pressures ?
- $\eta_y = 50 \text{ mm} \rightarrow 200 \text{ mm}$   
Betatron distribution + momentum deviation → momentum distribution



# Energy spectrum - intensity dependence

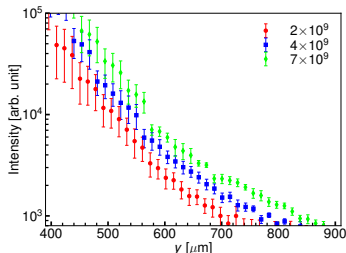
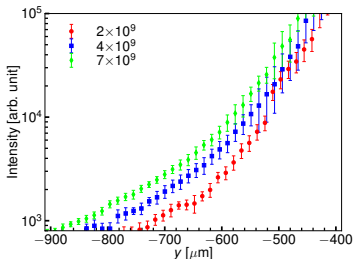
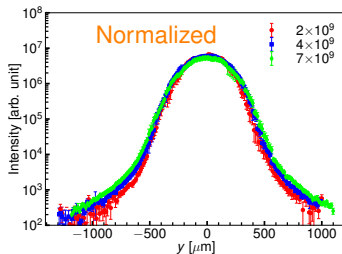
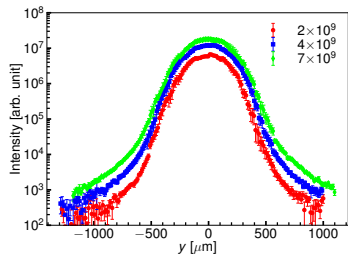
- Touschek scattering depends on beam intensity and emittances
- Higher beam intensity  $\rightarrow$  higher Tous. scattering rate  $\rightarrow$  higher tail (?)
- Analytical estimation based on Piwinski's model  
 $\rightarrow$  Intensity from  $1 \times 10^9$  e/pulse to  $6 \times 10^9$  e/pulse, the scattering rate increase from  $2 \times 10^8$ /s to  $4 \times 10^9$ /s for  $0.35\% < \delta < 1.2\%$



- Wake potential distortion is not included and can further weaken the intensity dependence

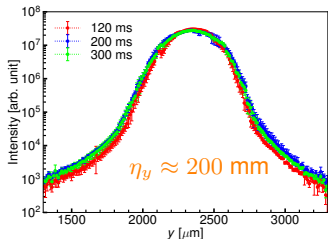
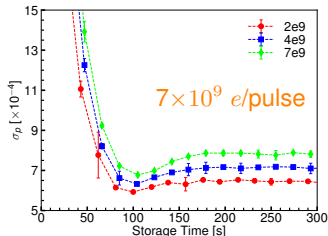
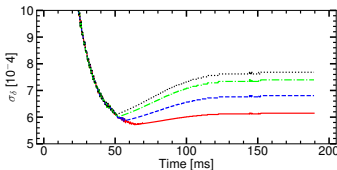
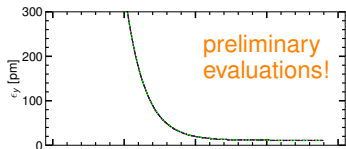
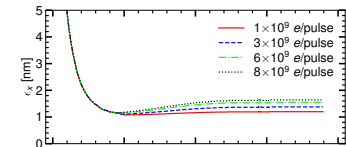
# Energy spectrum - intensity dependence

- Experiment conditions:  $\eta_y \approx 200$  mm, DR vacuum  $2 \times 10^{-7}$  Pa
- Significant dilution of the rms energy spread and increase of momentum tail



# Energy spectrum vs. extraction time

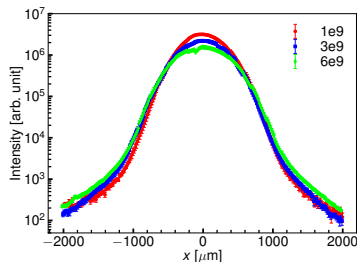
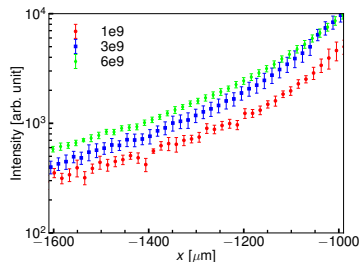
- Emittances and Touschek scattering rate  $\sim$  the storage time (damping, IBS)
- Evolution of  $\sigma_p$  and momentum tail seems consistent !





# Touschek scattering → Horizontal tail?

- Measurements of the momentum tail indicate a highly possible influence of Touschek scattering
- Tous. scattering induce also horizontal tail/halo due to a large  $\eta_x$ ?
- Increased hor. tail/halo for a higher beam intensity → consistent with the intensity dependence of momentum tail



- Detailed simulations of Touschek scattering are of critical importance!

# Summary

- DS detector and a novel YAG/OTR monitor has been developed and operated for beam halo studies
- Vertical halo is mainly induced by elastic BGS in the damping ring, demonstrated by numerical estimations and measurements
- Momentum tail was visualized through a proper adjustment of the vertical dispersion. Evolutions of momentum tail as a function of intensity, gas pressure and extraction time are qualitatively consistent with the presence of Touschek scattering
- Monte Carlo simulations of Touschek scattering is underway...

Many thanks to ATF collaboration!

Thank you for your attention!



Back up...

# Numerical approximation of BGS halo

- Solving the diffusion equation in the presence of RAD, QE and IBS

$$\frac{d\vec{x}}{ds} = -[H(\vec{x}, s), \vec{x}] + \xi(\vec{x}, s)$$

- Distribution function of normalized coordinate  $u = x/\sqrt{\beta}$ :

$$\psi(u) = \frac{1}{2\pi} \int e^{i\omega u} \tilde{\psi}_t(\omega) \tilde{\psi}_f(\omega) d\omega$$

- Final expression derived using Campbell's theorem

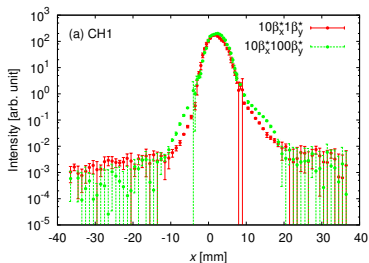
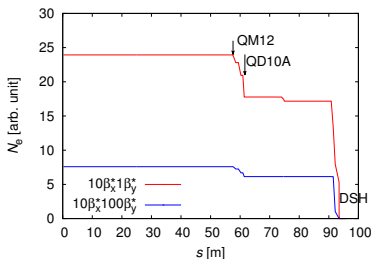
$$\psi(x_i) = \frac{1}{\pi} \int_0^\infty \cos(\omega x_i) \exp\left(-\frac{\omega^2 \sigma_{x_i}^2}{2} + \frac{N}{\alpha} \hat{f}(\omega \sqrt{\beta} \beta_i)\right) d\omega$$

with

$$\begin{aligned} \hat{f}(\tilde{\omega}) &= \frac{2}{\pi} \int_0^1 d\zeta \frac{\Re[\tilde{f}(\tilde{\omega}\zeta)] - 1}{\zeta} \cos^{-1} \zeta \\ \tilde{f}(\tilde{\omega}) &= \int d\theta_x f(\theta_x) \cos(\tilde{\omega}\theta_x) \end{aligned}$$

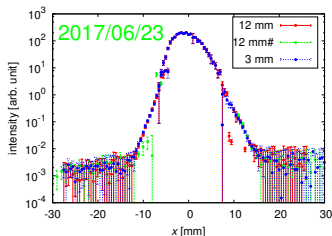
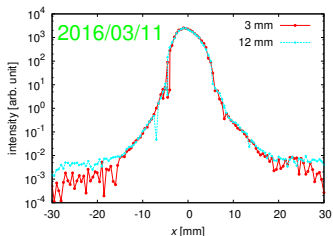
# Horizontal halo at DSh for $1\beta_y^*$ and $100\beta_y^*$ optics

- Few influence of chromaticity and aberration in FF, and less beam loss in high  $\beta_y$  region for  $10\beta_x^*100\beta_y^*$  optics
- Higher horizontal tail/halo when  $1\beta_y^* \rightarrow 100\beta_y^*$  observed by DS.
  - Effect of chromaticity and aberration in FF was negligible for nominal optics!



# Influence of secondary emission in FF

- Beam loss at FF and BDUMP and secondary particles shower are controlled by a vertical collimator upstream (12 mm/3 mm half-aperture)
- Experiment in 2016 shows observable effect of secondary shower
  - Insignificant influence due to larger fluctuation in June, 2017

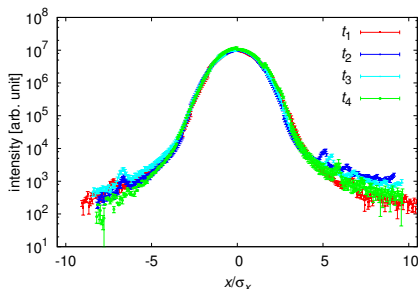
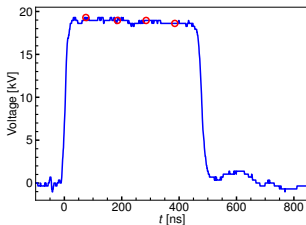


- Horizontal halo at Post-IP seems not dominated by aberration or secondary emission in FF. But, we should avoid their influences! -> YAG

# Halo from imperfect EXT kicker field



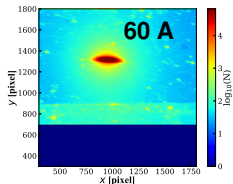
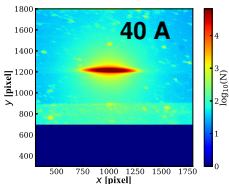
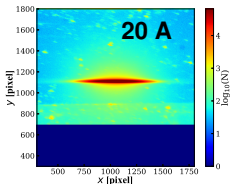
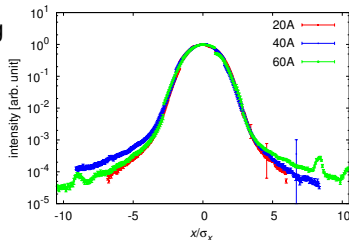
- Imperfection of extraction kicker field will drive particles to be large amplitude, and it is difficult to simulation thus influence
- Horizontal profile was measured for several locations of kick timing (difference larger than 28 ns) using YAG/OTR monitor
- Horizontal tail/halo was slightly changed!



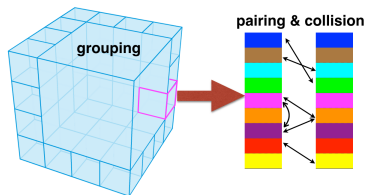
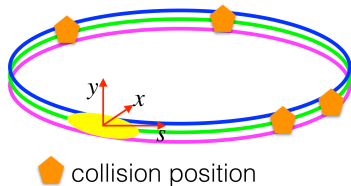


# Influence of optical focusing

- Beam profile is modulated by varying the strength of quad. QF21 upstream of YAG/OTR monitor
- Horizontal dispersion has been corrected
- Horizontal halo and its asymmetry depend on the optical focusing!



# Monte Carlo simulation with SIRE



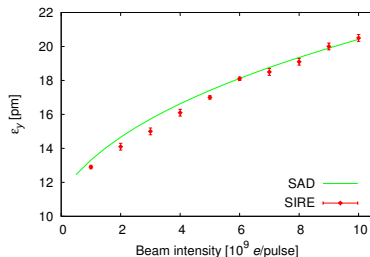
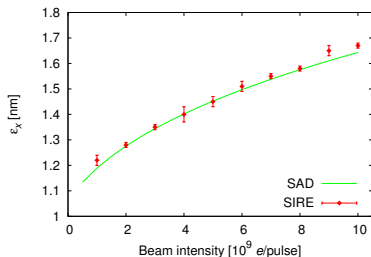
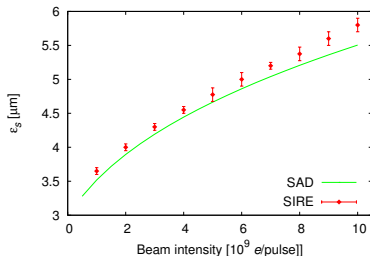
- T & A binary collision model (BCM)
- Routine:
  - Generate particles in action-angle frame ( $J, \Phi$ )
  - Track particle element-by-element,  $J = \text{const}$  and **random phase advance**
  - Perform grouping, pairing and collision at each elementThe variance of polar angle  $\langle \theta^2 \rangle$  is expressed as

$$\langle \theta^2 \rangle = \frac{4\pi\rho_v r_e^2 c_0 \Delta t}{\beta_{cm}^3} (\log)$$

- Damping and quantum excitation are considered in each turn

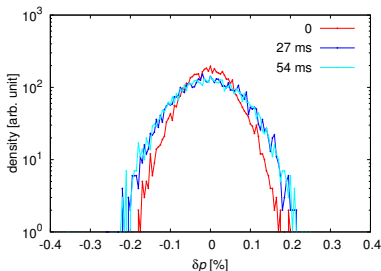
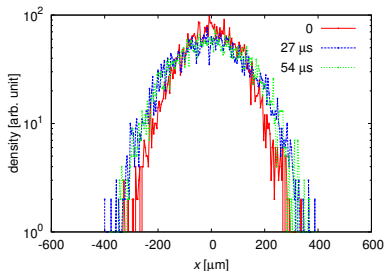
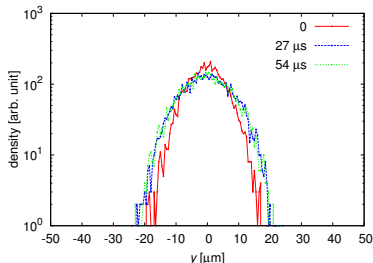
# Emittance dilution due to IBS

- Equilibrium emittance could be calculated by envelope matrix method (multi-iteration) in SAD Gaussian phase-space distribution, including dispersion,  $xy$  coupling and tail cut (log) $\approx 10$
- Good agreement for  $\epsilon_x$  and  $\epsilon_s$  with varying (log) in simulation, but larger  $\epsilon_y$  predicted by simulation

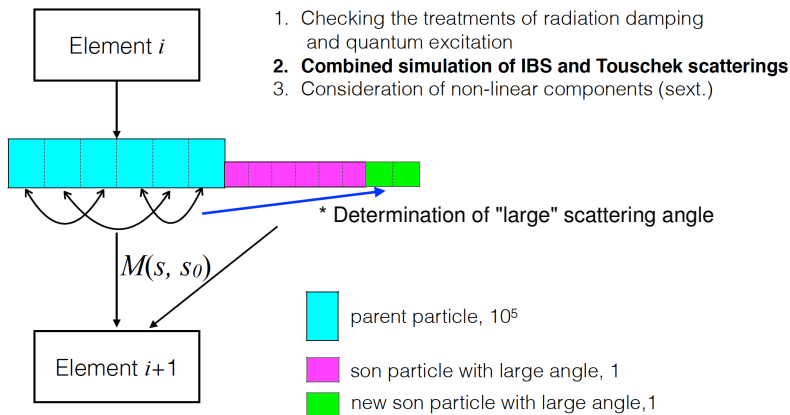


# Evolution of beam profiles with IBS diffusion

- Diffused transverse and momentum profiles remain Gaussian distribution
- To observe the possible tail from large angle collisions, we attempt to combine IBS & Touschek scattering in simulation...



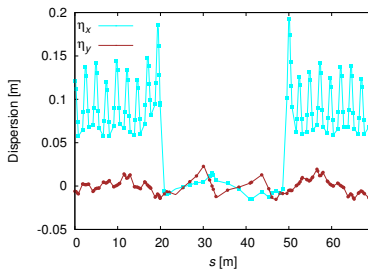
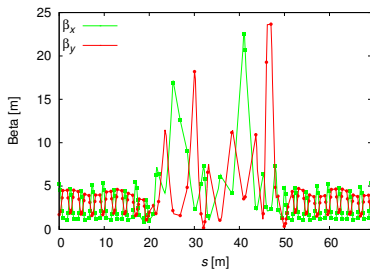
# Simulation of tail from large angle collisions



- Meanwhile, we also attempted to find evidence of halo from IBS by the measurement of momentum tail

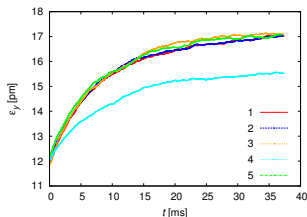
# Twiss parameters of ATF ring in SIRE

- 250 observation points after lattice compression ( $\Delta z > 10$  cm)

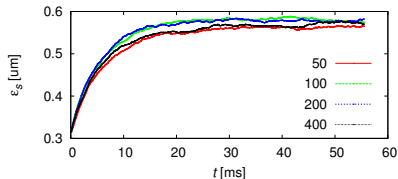
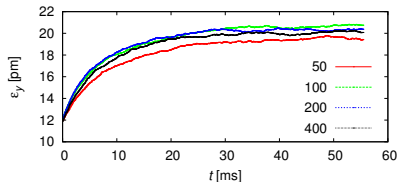
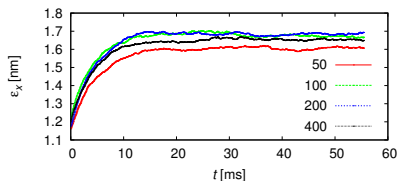


# Emittance growth due to IBS

- Multiple tracking are essential for Monte Carlo simulation (large deviation)

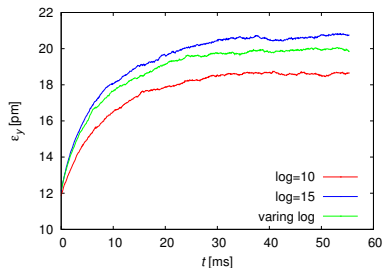
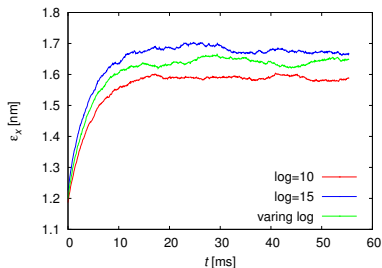
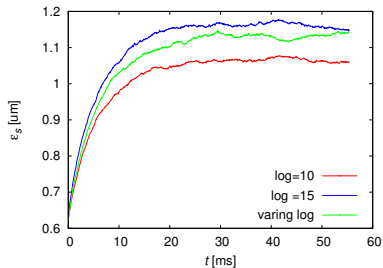


- Diffusion process and equilibrium are affected by cell density
- Cell density of 100/100/100 and 200/200/100 seems acceptable (1 % unscattered)



# Determination of (log) factor

- Diffusion from IBS depends on  $\langle \theta^2 \rangle \propto (\log)$
- Varying (log) is used in IBS simulation





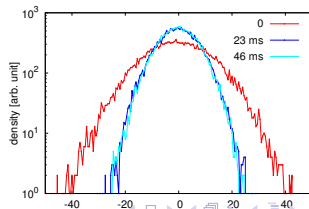
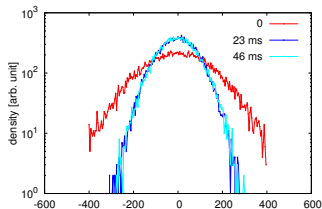
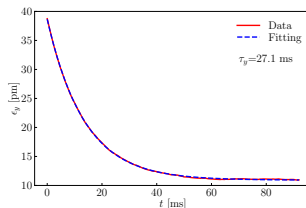
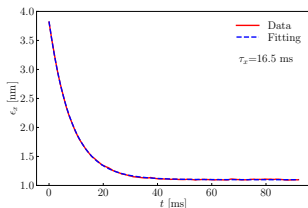
# Transverse radiation damping and fluctuation

$$Jx_{i+1} = Jx_i e^{-2T_0/\tau_x}$$

$$Jy_{i+1} = Jy_i e^{-2T_0/\tau_y}$$

$$x_{i+1} = x_i + \sqrt{\epsilon_{eq} * \beta_x (1 - e^{-2T_0/\tau_x})} * w_i$$

$$x'_{i+1} = x'_i + \sqrt{\epsilon_{eq} * \beta_x (1 - e^{-2T_0/\tau_x})} * (1 - \alpha_x) / \beta_x * w_i$$



# Longitudinal radiation damping and fluctuation

Synchrotron phase  $\phi_s$  and radiation energy loss per turn  $U_0$  is

$$\phi_s = \pi - \omega_{RF} \cdot z_s / c\beta$$

$$U_0 = V_{RF} \cdot \sin \phi_s$$

Particle energy change per turn is

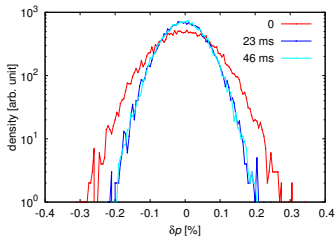
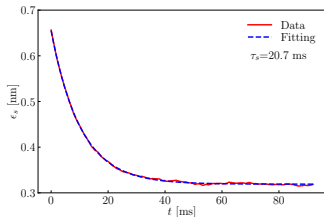
$$\delta p_{i+1} = \delta p_i + V_{RF} \sin(-z\omega_{RF}/c\beta + \phi_s) / E - U_0 /$$

Energy change due to damping and excitation is

$$\delta p'_{i+1} = \delta p_{i+1} e^{-2T_0/\tau_s} + \sigma_{p,eq} \sqrt{4T_0/\tau_s} w_i$$

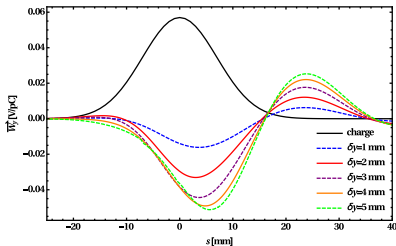
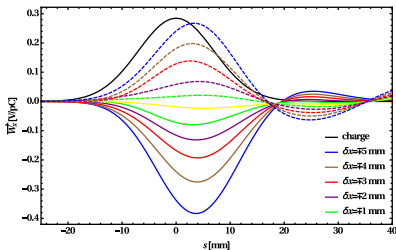
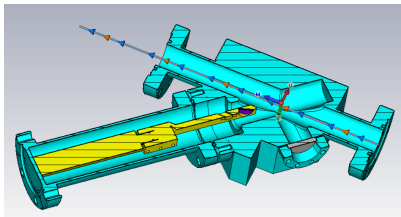
Longitudinal position shift above transition energy is

$$z_{i+1} = z_i - \delta p'_{i+1} T_0 \alpha_c c\beta$$



# Wakefield property of OTR/YAG monitor

- ▶ Benchmarking based upon Ref. cavity (thanks to A. Lyapin)
- ▶ Simulation of wakefield with a simplified chamber/holder model
- ▶ Simulation parameter:  
 $\sigma_z = 7 \text{ mm}$ ,  $Q = 1 \text{ pC}$
- ▶  $A_{wy} \approx 0.05 \text{ V/pC}$  and  $A_{wx} \approx 0.4 \text{ V/pC}$ , with beam is displaced by 5 mm



# Effect of WK at YAG monitor to nanometer beam size

- ▶ Orbit change and beam size growth at IP can be estimated by linear calculation

$$\Delta y \approx R_{34} \frac{e d_y}{E} \int_{-\infty}^{\infty} W_T(z) \rho(z) dz$$

$$\Delta \sigma_y \approx \sqrt{R_{34}^2 \left( \frac{e d_y}{E} \right)^2 \sigma_w^2}$$

- ▶ Assuming beam offset 3 mm at YAG and beam intensity as  $3 \times 10^9$ /pulse
- ▶ Effects:  $\Delta y = 0.9$  nm,  $\Delta \sigma_y = 0.5$  nm;  $\Delta x = 0.87$   $\mu$ m,  $\Delta \sigma_x = 0.02$   $\mu$ m

