

# Off-shell Higgs effects (~~propagation~~) of a classically scale invariant model in $e^+e^-$ processes ( ~~$ee \rightarrow Ztt$~~ )

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# Higgs and vacuum structure

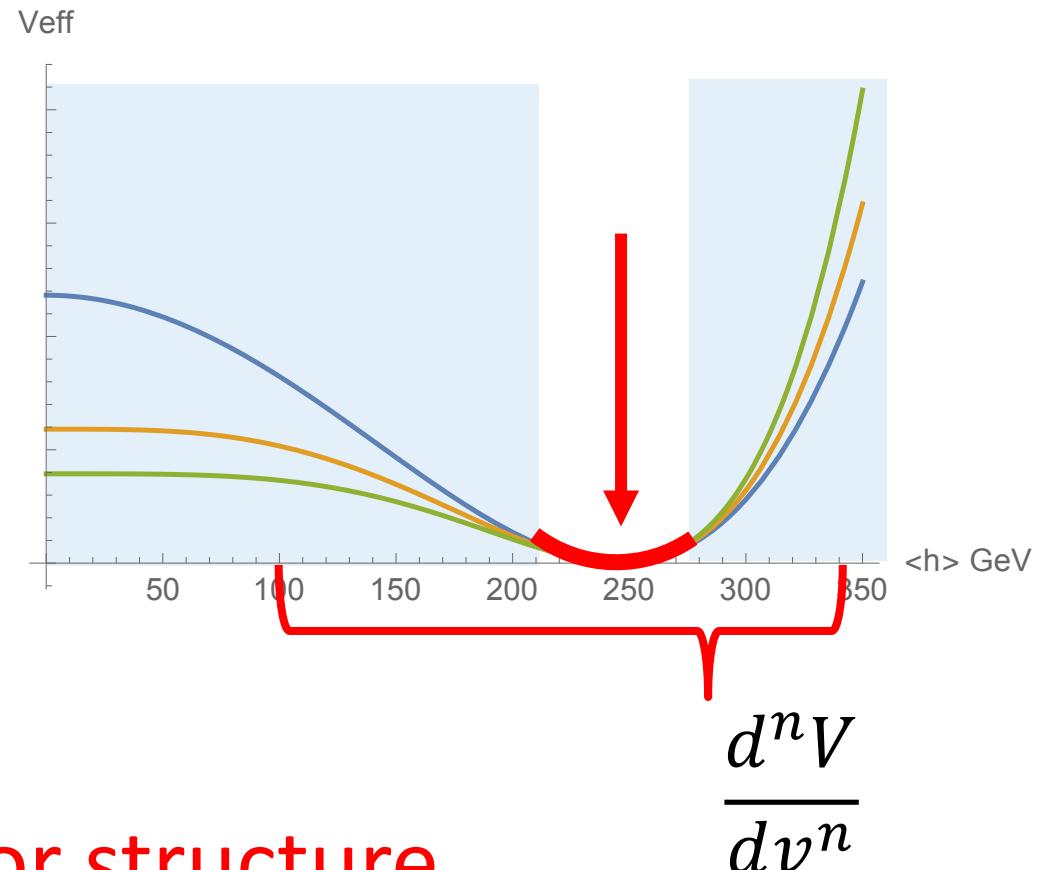
After Higgs boson discovery, we know

$$\text{VEV} \leftrightarrow 0 = \frac{dV}{d\nu} \quad m_h^2 \leftrightarrow \frac{d^2V}{d\nu^2}$$

Global Shape of pot. is unknown

$$\text{Higgs self interaction} \quad \lambda_{hhh} \leftrightarrow \frac{d^3V}{d\nu^3}$$

We don't know Higgs sector structure.



# Classically Scale Invariant (CSI)-model

$$\mathcal{L} = \mathcal{L}_{\text{SM}} \Big|_{\mu^2 \rightarrow 0} + \frac{1}{2} (\partial_\mu \vec{S})^2 - \lambda_{\text{HS}} (H^\dagger H) (\vec{S} \cdot \vec{S}) - \frac{\lambda_S}{4} (\vec{S} \cdot \vec{S})^2$$

Foot et.al., 2007; Endo, Sumino 2015

~~$\mu^2 H^\dagger H - \lambda_H (H^\dagger H)^2$~~

$\vec{S}$  → SM singlet scalar w/  $O(N)$  sym.

$\vec{S} \cdot \vec{S}$  → Higgs portal coupling

- EWSB → Radiative Breaking (tree + 1 loop at Leading Order(LO))
- Log-like potential (non-SM-like) → Large deviation
- Parameters  $\lambda_{H,\text{HS}}$  are fixed at LO.

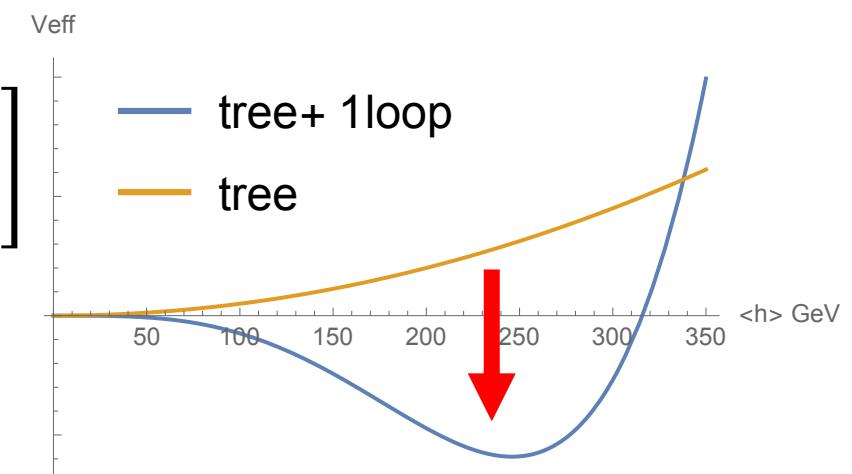
# Order counting: $\xi$ -expansion

The eff. pot. has  $V_{\text{EV}}(\neq 0)$   
at tree + (parts of ) 1 loop order.

$$0 = \frac{d}{d\varphi} V = \varphi^3 \left[ -\frac{u^2}{\varphi^2} + \lambda_H - \frac{\lambda_{\text{HS}}^2}{(4\pi)^2} (\dots) + \frac{3y_t^4}{(4\pi)^2} (\dots) + \dots \right]$$

$\xrightarrow{\quad}$   $= 0$

$$\lambda_H \rightarrow \xi^2 \lambda_H, \lambda_{\text{HS}} \rightarrow \xi \lambda_{\text{HS}}, y_t \rightarrow \xi^{1/2} y_t, \text{others} \rightarrow O(\xi^2)$$



LO ( $\xi$ -expansion)  $\leftrightarrow$  tree + singlet loop + top loop

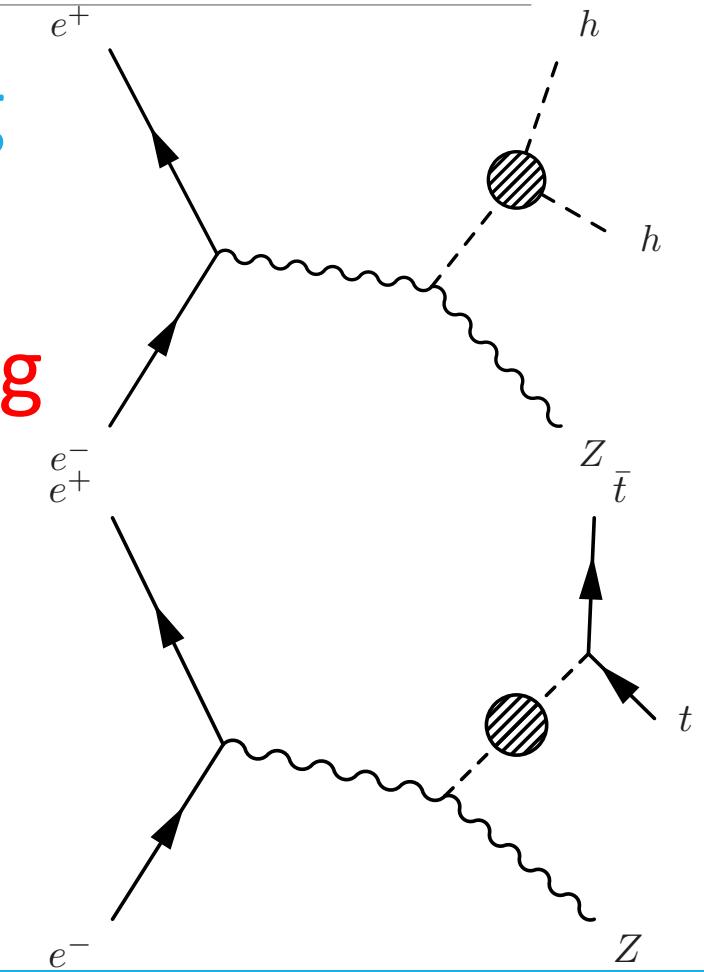
# Observables in Higgs portal model

Additional Scalar **with SM charge or mixing**

-> See EW coupling

In CSI model, S **has no SM charge and mixing**

- EW coupling at  $N^nLO$
- Off-shell effects of  $h$ 
  - Higgs **self coupling**  $h^* \rightarrow hh$
  - Off-shell Higgs **propagation**  $h^* \rightarrow t\bar{t}$



# Higgs triple coupling of CSI-model

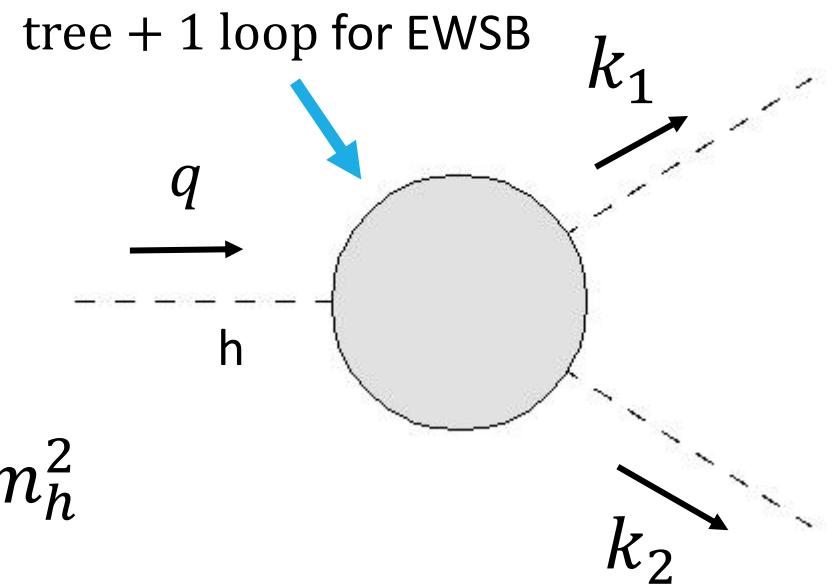
From the effective potential, the Higgs triple coupling is

$$\lambda_{hhh}^{\text{CSI}} = \frac{1}{v} \frac{d^3V}{dv^3} = \frac{5m_h^2}{v^2} = \frac{5}{3} \lambda_{hhh}^{\text{SM}} \rightarrow +67\%$$

Chway, et.al. 2013; Endo,Sumino 2015;  
Hashino,Kanemura,Orikasa,2015

$$\lambda_{hhh} = \frac{1}{v} \frac{d^3V}{dv^3} + f(q^2), \quad q^2 \sim O(m_h^2), \quad k_{1,2}^2 = m_h^2$$

can be same order (1 loop)



We have to compare them in **physical process**.

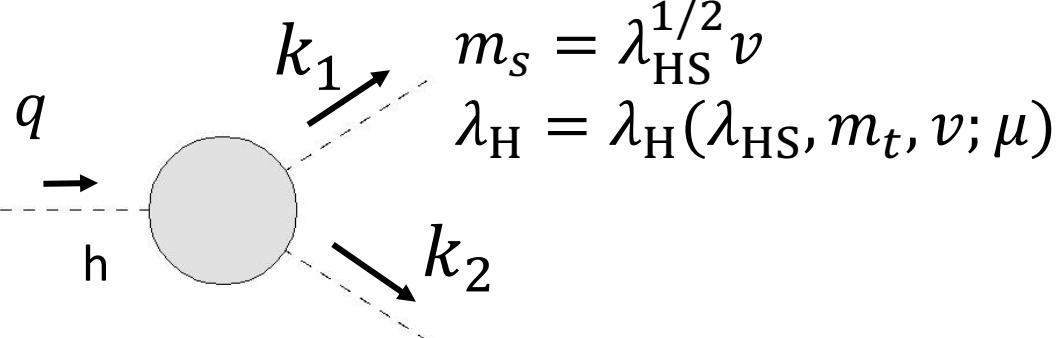
# $\lambda_{hhh}$ w/ momentum dependence

$$\nu = 246 \text{ GeV}$$

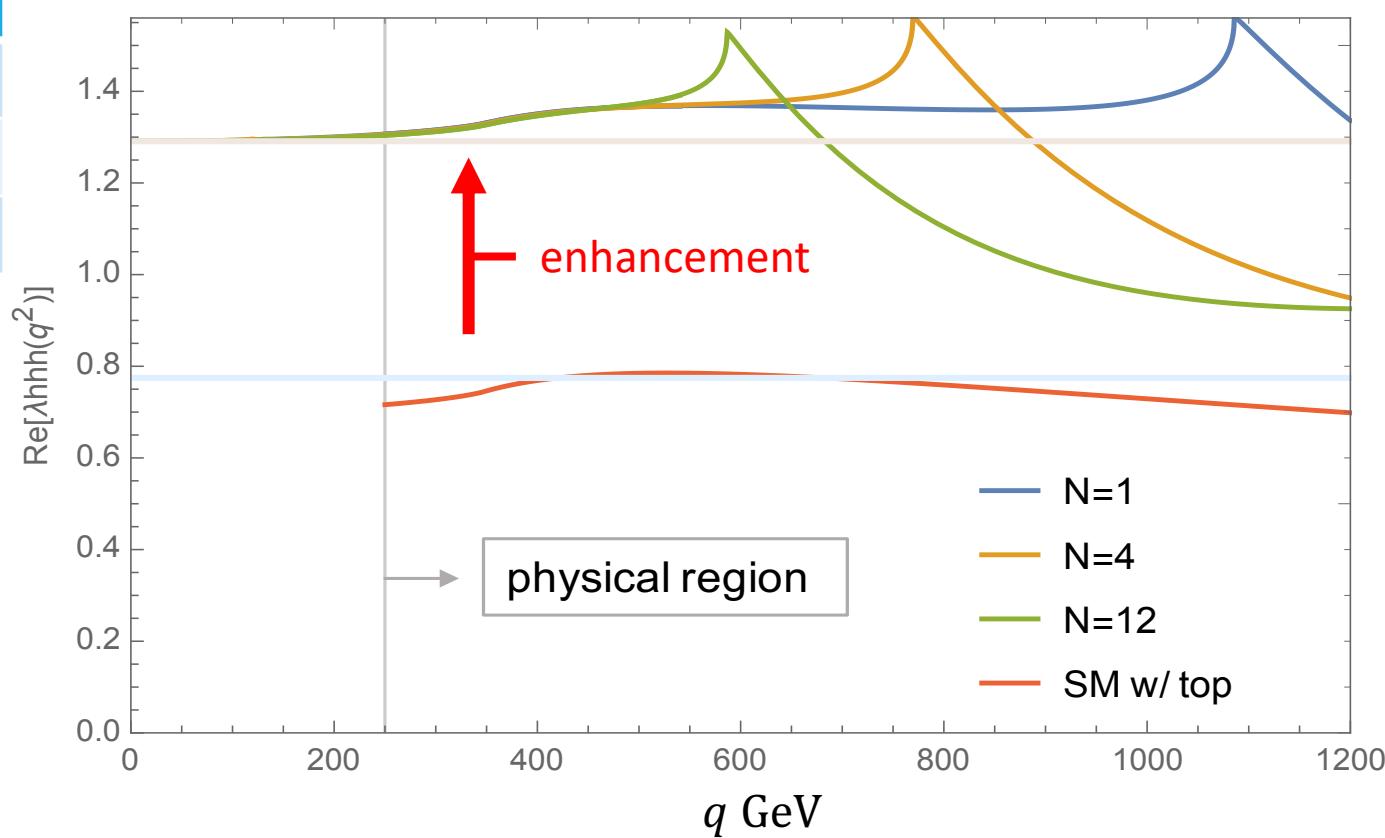
$$m_h = 125 \text{ GeV}$$

$$m_t = 173 \text{ GeV}$$

N	$m_s$ GeV	$\lambda_{HS}$
1	543	4.87
4	385	2.45
12	293	1.42

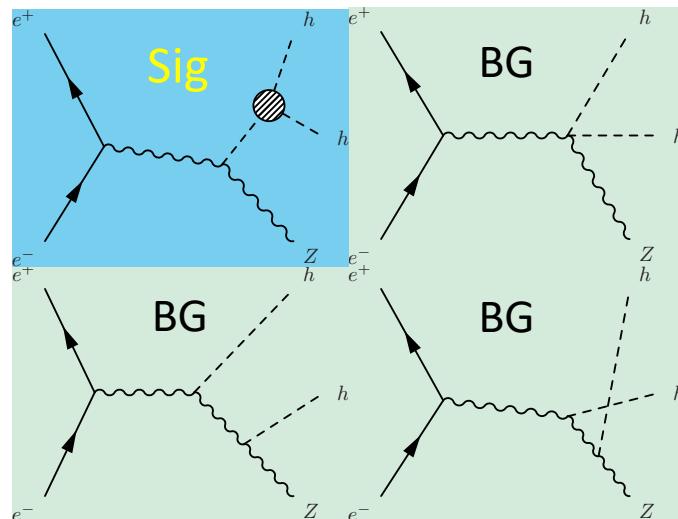


$$\lambda_{hhh}(q^2) = \text{tree} + (\text{singlet, top loop}) \text{ at LO } O(\xi^2)$$

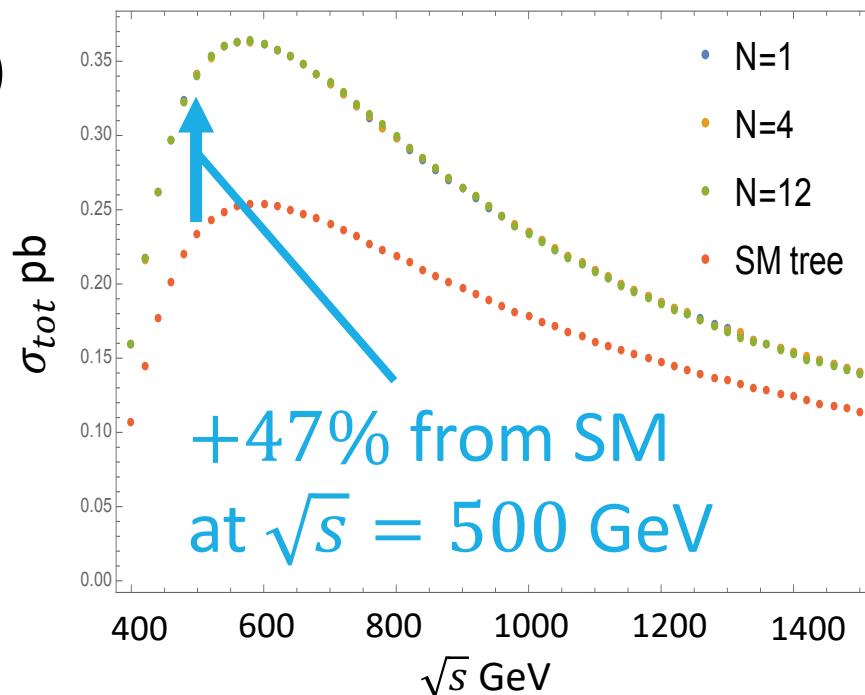


# $e^+e^- \rightarrow Zhh$ total and diff. cross section

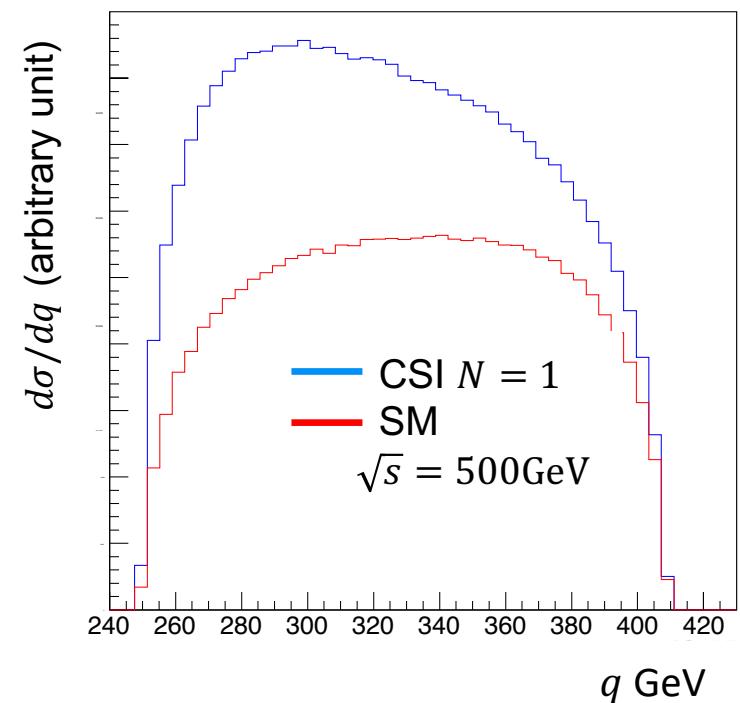
$$P(e^+, e^-) = (0.3, -0.8)$$



$\lambda_{hhh}^{\text{CSI}}$  can be tested!

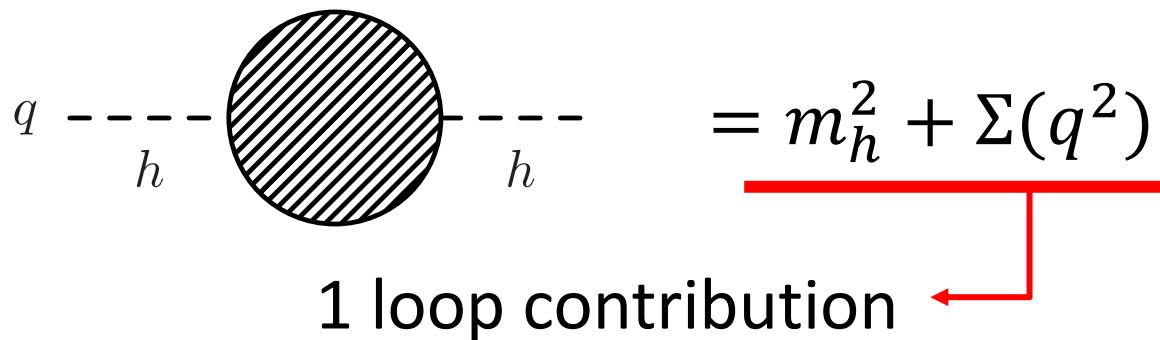


Integrated Luminosity to discover  $5\sigma$ /exclude  $3\sigma$   
 $710/260 \text{ fb}^{-1}$  Based on LC-REP-2013-003,  $1\sigma \approx N_{sig}/\sqrt{N_{BG}}$

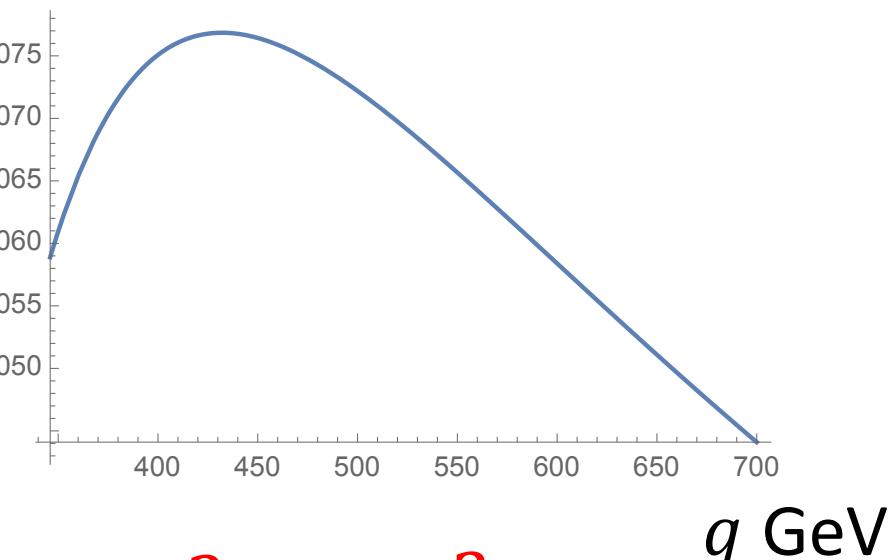


# Off-shell Higgs propagation

In CSI model, off-shell effect exists at LO



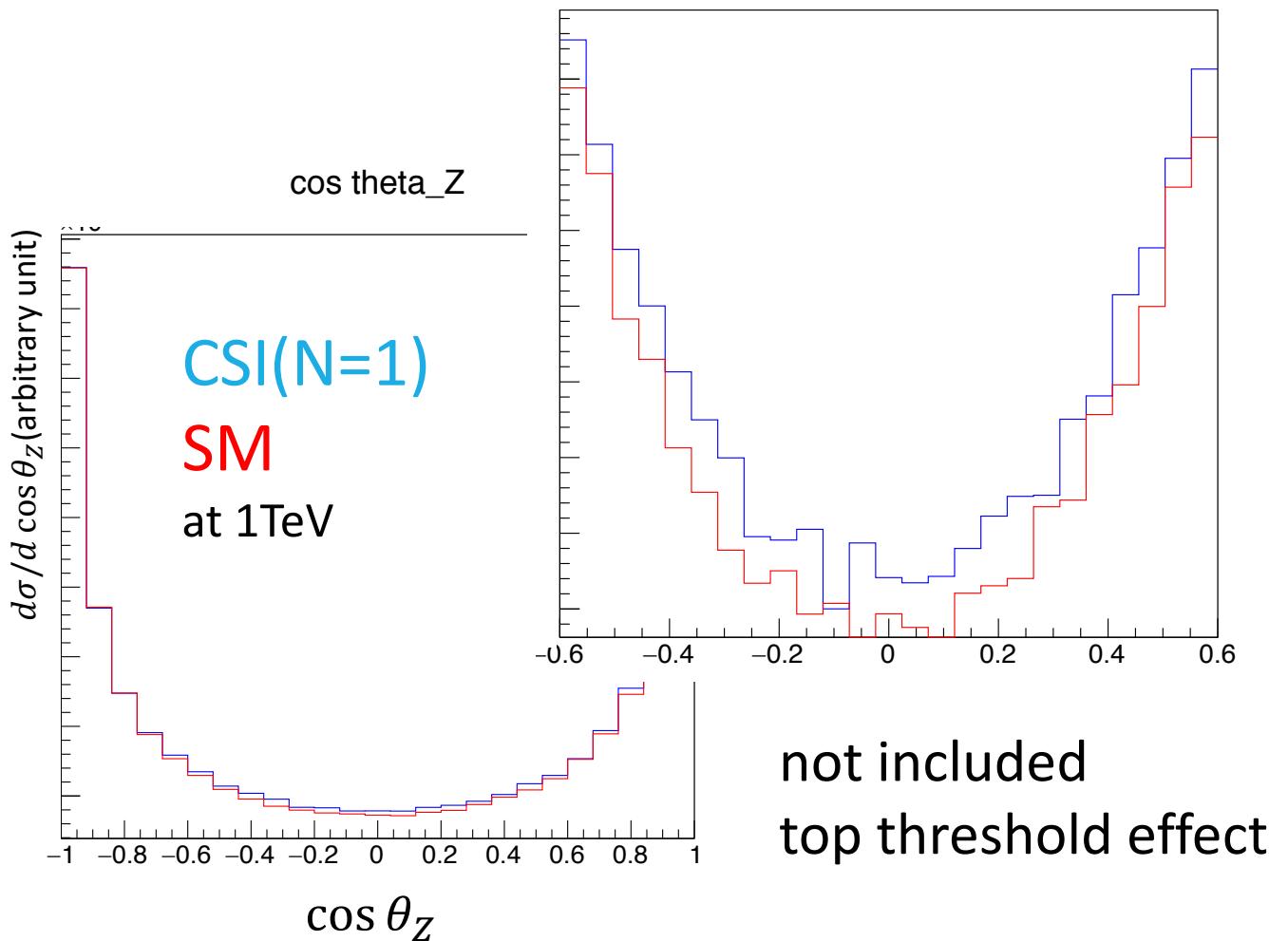
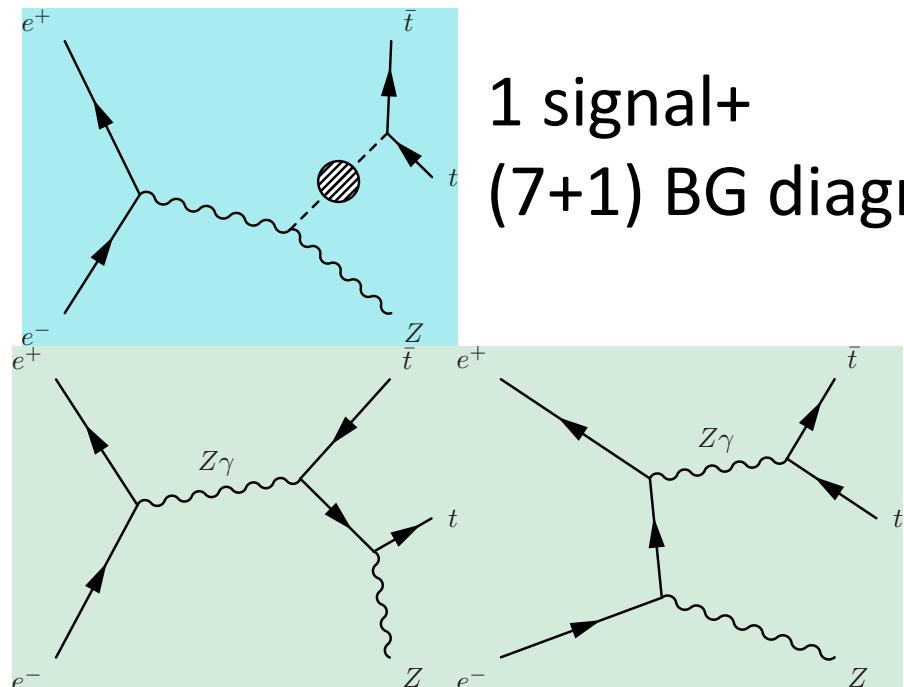
$$\left| \frac{q^2 - m_h^2}{q^2 - m_h^2 - \Sigma} \right|$$



$\Sigma(q^2) \neq 0$  and can be measurable at  $q^2 \gg m_h^2$

$$e^+ e^- \rightarrow Z t \bar{t}$$

$$P(e^+, e^-) = (0.3, -0.8)$$



not included  
top threshold effect

$$\sigma_{|\cos \theta_Z| < 0.6}^{e^+ e^- \rightarrow Z t \bar{t}} = 3.922 \text{ fb}, +3.4\% \text{ from SM tree at 1TeV}$$

# Summary

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- CSI-model breaks EW sym. by radiatively and has **large deviation** in physical processes.
- $\sigma_{\text{tot}}^{e^+ e^- \rightarrow Zhh}$  is **+47%** from SM at  $\sqrt{s} = 500$  GeV
- $\sigma_{\text{tot}}^{e^+ e^- \rightarrow Zt\bar{t}}$  has  **$O(1)\%$**  enhancement at  $\sqrt{s} = 1$  TeV w/cut
- CSI model can be tested in future ee-collider.