

# Composite 2 Higgs doublet models

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Collaboration with

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# Introduction

Higgs boson was found at **125 GeV** at the LHC, but ...

The Higgs sector is still mystery... In fact, we do not know

- ❑ The **Nature** of the Higgs boson.
- ❑ The **true shape** of the Higgs sector.
- ❑ The reason for the **small Higgs mass** with respect to a NP scale.

2 important paradigms (dynamics)

- ❑ **Supersymmetry** (weak) and **Compositeness** (strong)

Both scenarios can provide a **2HDM** as a low energy EFT.

Can we distinguish these scenarios from the 2HDM property?

# Plan of the talk

- ▣ Introduction to composite (pNGB) Higgs
- ▣ Composite 2HDM (C2HDM)
- ▣ Results
- ▣ Summary

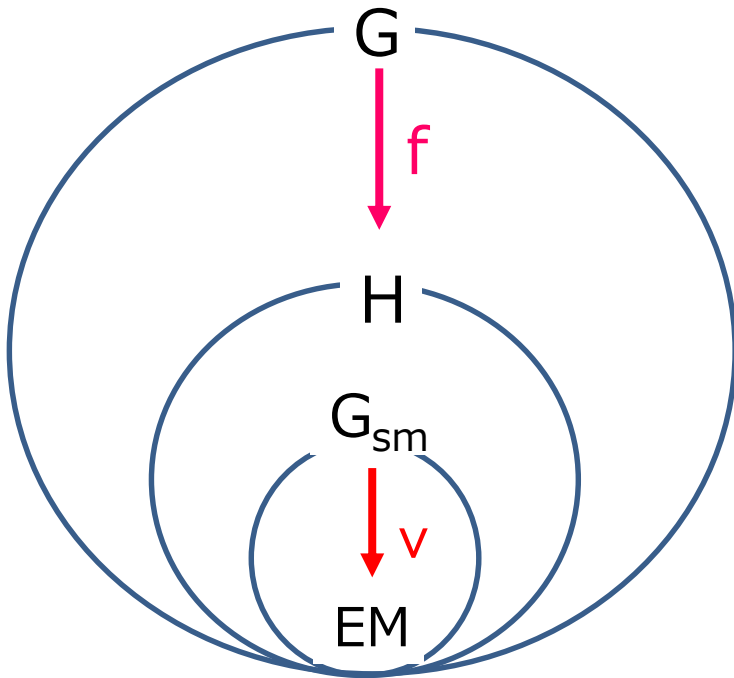
# Pion Physics $\leftrightarrow$ Higgs Physics

- From now on, let me say “**Composite Higgs**” as **pNGB Higgs**. *Georgi, Kaplan 80's*
- This scenario can be understood by analogy of the pion physics.

	Pion Physics	Higgs Physics
Fundamental Theory	QCD	QCD-like theory
Spontaneous sym. breaking	$SU(2)_L \times SU(2)_R \rightarrow SU(2)_V$	$G \rightarrow H$
pNGB modes	$(\pi^0, \pi^\pm) \sim 135 \text{ MeV}$	$h \sim 125 \text{ GeV}$
Other resonances	$\rho \sim 770 \text{ MeV}, \dots$	New spin 1 and $\frac{1}{2}$ states $\sim \text{Multi-TeV}$

# Basic Rules for Composite Higgs

- ▣ Suppose there is a **global symmetry  $G$**  at scale above  $f$  ( $\sim \text{TeV}$ ), which is spontaneously broken down into a **subgroup  $H$** .
- ▣ The structure of the Higgs sector is determined by the **coset  $G/H$** .
- ▣  $H$  should contain the custodial  **$SO(4) \simeq SU(2)_L \times SU(2)_R$**  symmetry.
- ▣ The number of NGBs ( $\dim G - \dim H$ ) must be 4 or larger.



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$G$	$H$	$N_G$	NGBs rep. $[H] = \text{rep.}[SU(2) \times SU(2)]$
$SO(5)$	$SO(4)$	4	$\mathbf{4} = (\mathbf{2}, \mathbf{2})$
$SO(6)$	$SO(5)$	5	$\mathbf{5} = (\mathbf{1}, \mathbf{1}) + (\mathbf{2}, \mathbf{2})$
$SO(6)$	$SO(4) \times SO(2)$	8	$\mathbf{4}_{+2} + \bar{\mathbf{4}}_{-2} = 2 \times (\mathbf{2}, \mathbf{2})$
$SO(7)$	$SO(6)$	6	$\mathbf{6} = 2 \times (\mathbf{1}, \mathbf{1}) + (\mathbf{2}, \mathbf{2})$
$SO(7)$	$G_2$	7	$\mathbf{7} = (\mathbf{1}, \mathbf{3}) + (\mathbf{2}, \mathbf{2})$
$SO(7)$	$SO(5) \times SO(2)$	10	$\mathbf{10}_0 = (\mathbf{3}, \mathbf{1}) + (\mathbf{1}, \mathbf{3}) + (\mathbf{2}, \mathbf{2})$
$SO(7)$	$[SO(3)]^3$	12	$(\mathbf{2}, \mathbf{2}, \mathbf{3}) = 3 \times (\mathbf{2}, \mathbf{2})$
$Sp(6)$	$Sp(4) \times SU(2)$	8	$(\mathbf{4}, \mathbf{2}) = 2 \times (\mathbf{2}, \mathbf{2}), (\mathbf{2}, \mathbf{2}) + 2 \times (\mathbf{2}, \mathbf{1})$
$SU(5)$	$SU(4) \times U(1)$	8	$\mathbf{4}_{-5} + \bar{\mathbf{4}}_{+5} = 2 \times (\mathbf{2}, \mathbf{2})$
$SU(5)$	$SO(5)$	14	$\mathbf{14} = (\mathbf{3}, \mathbf{3}) + (\mathbf{2}, \mathbf{2}) + (\mathbf{1}, \mathbf{1})$

*Table from Mrazek, Pomarol, Rattazi, Redi, Serra, Wulzer NPB 853 (2011) 1-48*

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SO(5)	SO(4)	4	<b>4 = (2, 2)</b>
SO(6)	SO(5)	15	15 = (2, 2) + (2, 2) + (2, 2) + (2, 2) + (2, 2)
SO(7)	SO(6)	21	21 = (2, 2) + (2, 2) + (2, 2) + (2, 2) + (2, 2) + (2, 2)
SO(7)	$G_2$	14	14 = (2, 2) + (2, 2) + (2, 2) + (2, 2)
SO(7)	$SO(5) \times SO(2)$	15	15 = (2, 2) + (2, 2) + (2, 2) + (2, 2) + (2, 2)
SO(7)	$[SO(3)]^3$	12	(2, 2, 3) = 3 × (2, 2)
Sp(6)	$Sp(4) \times SU(2)$	8	(4, 2) = 2 × (2, 2), (2, 2) + 2 × (2, 1)
SU(5)	$SU(4) \times U(1)$	8	$4_{-5} + \bar{4}_{+5} = 2 \times (2, 2)$
SU(5)	SO(5)	14	14 = (3, 3) + (2, 2) + (1, 1)

## 1 Doublet: Minimal Composite Higgs Model

*Agashe, Contino, Pomarol (2005)*

*Kanemura, Kaneta, Machida, Shindou (2014)*

*Table from Mrazek, Pomarol, Rattazi, Redi, Serra, Wulzer NPB 853 (2011) 1-48*

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$\text{SO}(6)$	$\text{SO}(5)$	5	$5 = (1, 1) + (2, 2)$
$\text{SO}(6)$	$\text{SO}(4) \times \text{SO}(2)$	6	$4 + 1 + 1 + 2 + 2 + 2$
$\text{SO}(7)$	$\text{SO}(6)$	7	$7 = 1 + 1 + 1 + 1 + 1 + 1 + 1$
$\text{SO}(7)$	$\text{SO}(5) \times \text{SO}(2)$	10	$10_0 = (3, 1) + (1, 3) + (2, 2)$
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*Gripaios, Pomarol, Riva, Serra (2009)*

**1 Doublet + 1 Singlet** *Redi, Tesi (2012)*

*Table from Mrazek, Pomarol, Rattazi, Redi, Serra, Wulzer NPB 853 (2011) 1-48*



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In this talk, I take  $SO(6) \rightarrow SO(4) \times SO(2)$ .

# Construction of 2 pNGB Doublets

- 15 SO(6) generators:  $T^A = \{\underbrace{T_{L,R}^a}_{6 \text{ SO(4)}}, \underbrace{T_S}_{1 \text{ SO(2)}}, \underbrace{T_{1,2}^{\hat{a}}}_{8 \text{ Broken}}\}$  (A=1-15, a=1-3,  $\hat{a}$ =1-4)

$$\Phi \equiv (\phi_1^{\hat{a}}, \phi_2^{\hat{a}})$$

- pNGB matrix:  $U(\phi_1^{\hat{a}}, \phi_2^{\hat{a}}) \equiv \exp \left[ \sqrt{2}i \left( T_1^{\hat{a}} \frac{\phi_1^{\hat{a}}}{f} + T_2^{\hat{a}} \frac{\phi_2^{\hat{a}}}{f} \right) \right] = \exp \left[ \begin{pmatrix} 0_{4 \times 4} & \Phi \\ -\Phi^T & 0_{2 \times 2} \end{pmatrix} \right]$

U is transformed **non-linearly** under SO(6):  $U \rightarrow g U h^{-1}(g, \phi_{1,2}^{\hat{a}})$

- Linear rep.  **$\Sigma(\mathbf{15})$** :  $\mathbf{15} = (\mathbf{6}, \mathbf{1}) \oplus (\mathbf{4}, \mathbf{2}) \oplus (\mathbf{1}, \mathbf{1})$  under  $\text{SO}(4) \times \text{SO}(2)$

$$\Sigma = U \Sigma_0 U^T = \begin{pmatrix} \Sigma(\mathbf{6}, \mathbf{1}) & \Sigma(\mathbf{4}, \mathbf{2}) \\ -\Sigma^T(\mathbf{4}, \mathbf{2}) & \Sigma(\mathbf{1}, \mathbf{1}) \end{pmatrix} \quad \Sigma_0 = i\sqrt{2}T_S = \begin{pmatrix} 0_{4 \times 4} & 0_{4 \times 2} \\ 0_{2 \times 4} & i\sigma_2 \end{pmatrix}$$

$\Sigma$  is transformed **linearly** under SO(6):  $\Sigma \rightarrow g \Sigma g^{-1}$  and  $\Sigma_0 \rightarrow h \Sigma_0 h^{-1}$

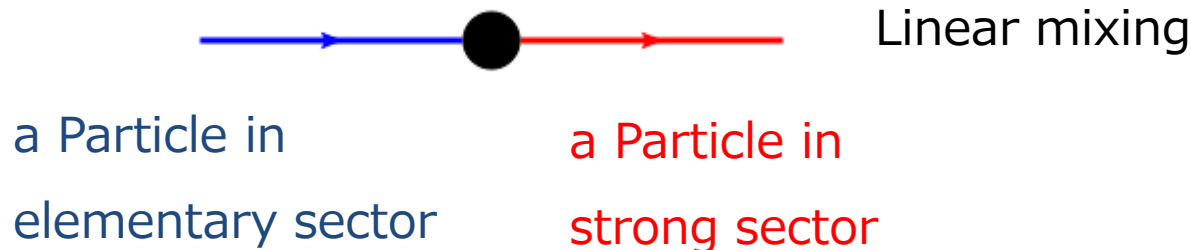
# Higgs Potential

- The potential becomes 0 because of the **shift symmetry** of the NGB.  
→ the Higgs mass also becomes 0.

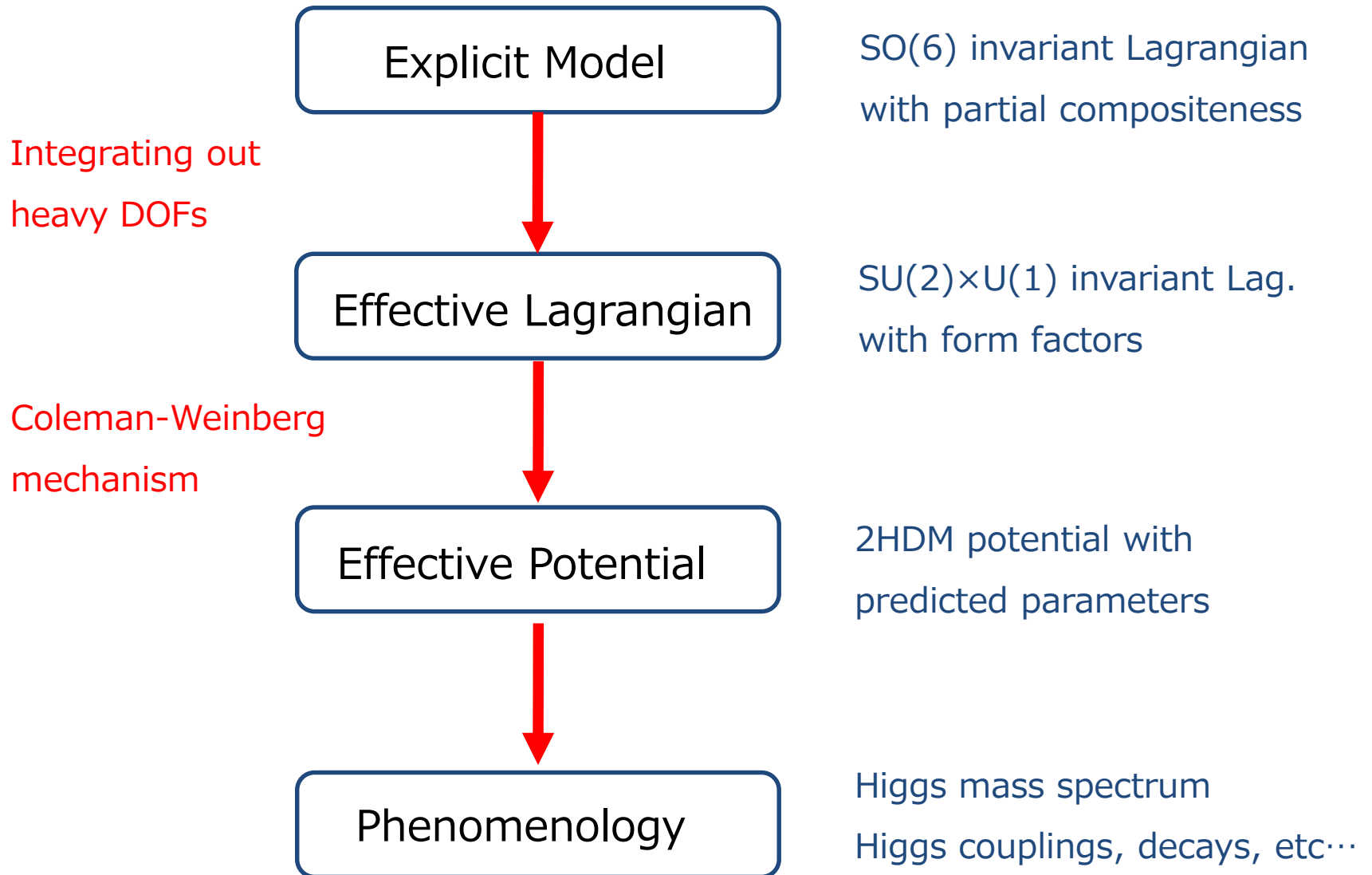
- We need to introduce the **explicit breaking** of G.  
→ NGB Higgs becomes **p**NGB with a finite mass.

*Kaplan, PLB365, 259 (1991)*

- Explicit breaking can be realized by **partial compositeness**



# Strategy



# Explicit Model

*Based on the 4DCHM, De Curtis, Redi, Tesi, JHEP04 (2012) 042*

$$\mathcal{L} = \mathcal{L}_{\text{elem}} + \mathcal{L}_{\text{str}} + \mathcal{L}_{\text{mix}}$$

Elementary Sector

$$\begin{aligned} & \text{SU}(2)_L \times \text{U}(1)_Y \\ & W_\mu^a, q_L, t_R \end{aligned}$$

Strong Sector

$$\begin{aligned} & \text{SO}(6) \times \text{U}(1)_X \\ & \rightarrow \text{SO}(4) \times \text{SO}(2) \times \text{U}(1)_X \\ & \rho_\mu^A, \Psi^6, \Sigma \end{aligned}$$

Mixing

Partial Compositeness

# Explicit Model

Based on the 4DCHM, De Curtis, Redi, Tesi, JHEP04 (2012) 042

Embeddings into SO(6) multiplets :

$$W_\mu^a \in W_\mu^A \quad q_L \in q_L^6 \quad t_R \in t_R^6$$

**Elementary Sector**

$$SU(2)_L \times U(1)_Y$$

$$W_\mu^a, q_L, t_R$$

**Mixing**

**Partial Compositeness**

**Strong Sector**

$$SO(6) \times U(1)_X$$

$$\rightarrow SO(4) \times SO(2) \times U(1)_X$$

$$\rho_\mu^A, \Psi^6, \Sigma$$

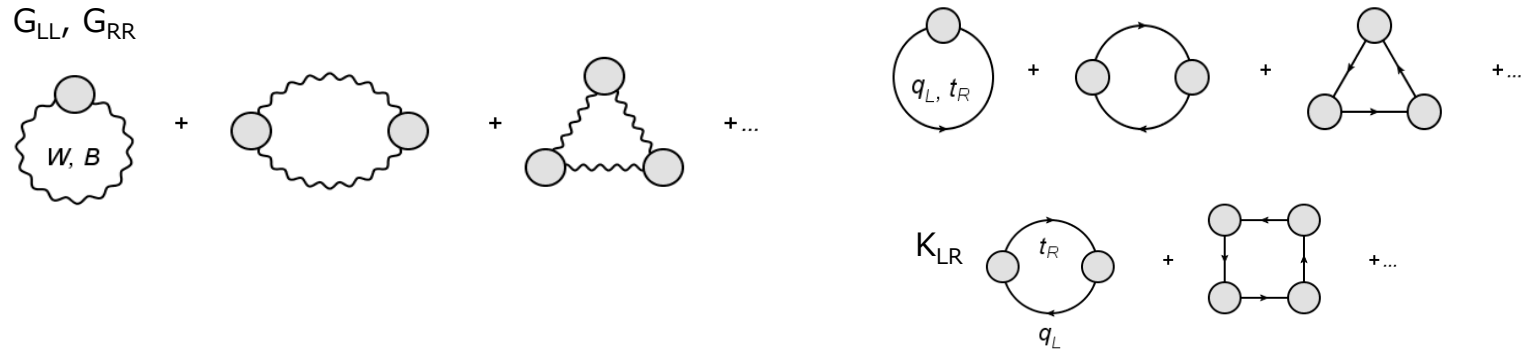
$$\mathcal{L}_{\text{mix}} = (f^2 g_\rho g_W) W_\mu^A \rho^{A\mu} + (\Delta_L \bar{q}_L^6 \Psi_R^6 + \Delta_R \bar{t}_R^6 \Psi_L^6 + \text{h.c.})$$

# Effective Lagrangian

- All the strong sector information are encoded into the form factors:

$$\mathcal{L}_{\text{eff}} = (W_\mu, B_\mu) \begin{pmatrix} G_{LL} & G_{LR} \\ G_{LR} & G_{RR} \end{pmatrix} \begin{pmatrix} W^\mu \\ B^\mu \end{pmatrix} + (\bar{q}_L, \bar{t}_R) \begin{pmatrix} \not{q} K_{LL} & K_{LR} \\ K_{LR} & \not{q} K_{RR} \end{pmatrix} \begin{pmatrix} q_L \\ t_R \end{pmatrix}$$


- We then calculate the 1-loop CW potential.



$$V = \frac{1}{f^4} \int \frac{d^4 k}{(2\pi)^4} \left( \frac{3}{2} \ln \det G - 2N_c \ln \det K \right)$$



# Effective Potential


$$\begin{aligned} V(\Phi_1, \Phi_2) = & m_1^2 \Phi_1^\dagger \Phi_1 + m_2^2 \Phi_2^\dagger \Phi_2 - \left[ m_3^2 \Phi_1^\dagger \Phi_2 + \text{h.c.} \right] \\ & + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) \\ & + \frac{\lambda_5}{2} (\Phi_1^\dagger \Phi_2)^2 + \lambda_6 (\Phi_1^\dagger \Phi_1) (\Phi_1^\dagger \Phi_2) + \lambda_7 (\Phi_2^\dagger \Phi_2) (\Phi_1^\dagger \Phi_2) + \text{h.c.} + O(\Phi^6) \end{aligned}$$

All the potential parameters  $\mathbf{m}_i^2$  and  $\boldsymbol{\lambda}_i$  are given as a function of strong parameters:

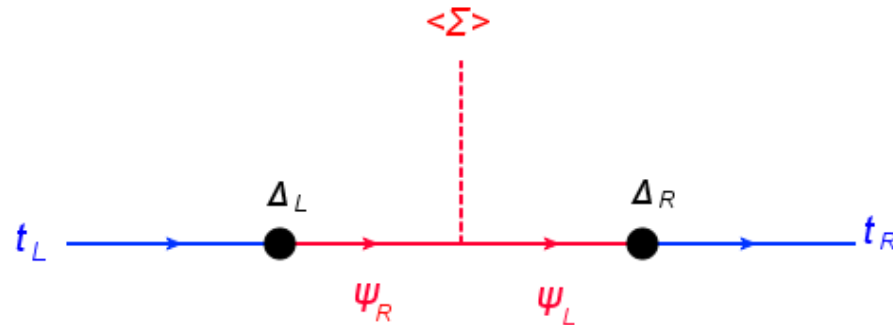
$$m_i^2 = m_i^2(g_\rho, f, \dots) \quad \lambda_i = \lambda_i(g_\rho, f, \dots)$$

# Matching Conditions

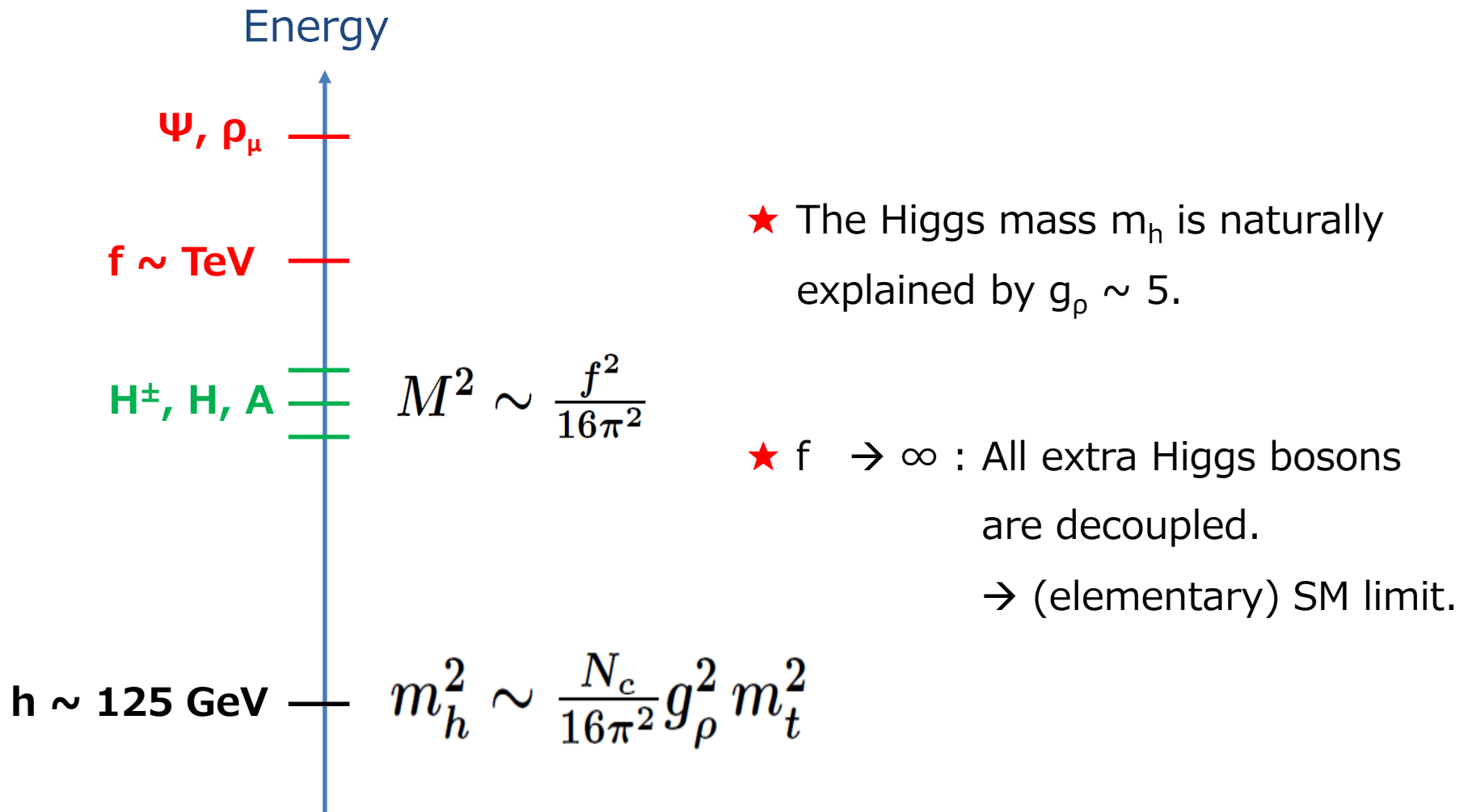
□ We need to reproduce the top mass and the weak boson mass.

$$m_W^2 = \langle G_{LL} \rangle_{q^2 \rightarrow 0} = \frac{1}{4} \underbrace{\frac{g_W^2 g_\rho^2}{g_W^2 + g_\rho^2}}_{g^2} \underbrace{f^2 \sin^2 \frac{v}{f}}_{V_{\text{sm}}^2 \sim (246 \text{ GeV})^2} \quad \begin{array}{l} v^2 = v_1^2 + v_2^2 \\ \tan \beta = v_2/v_1 \end{array}$$

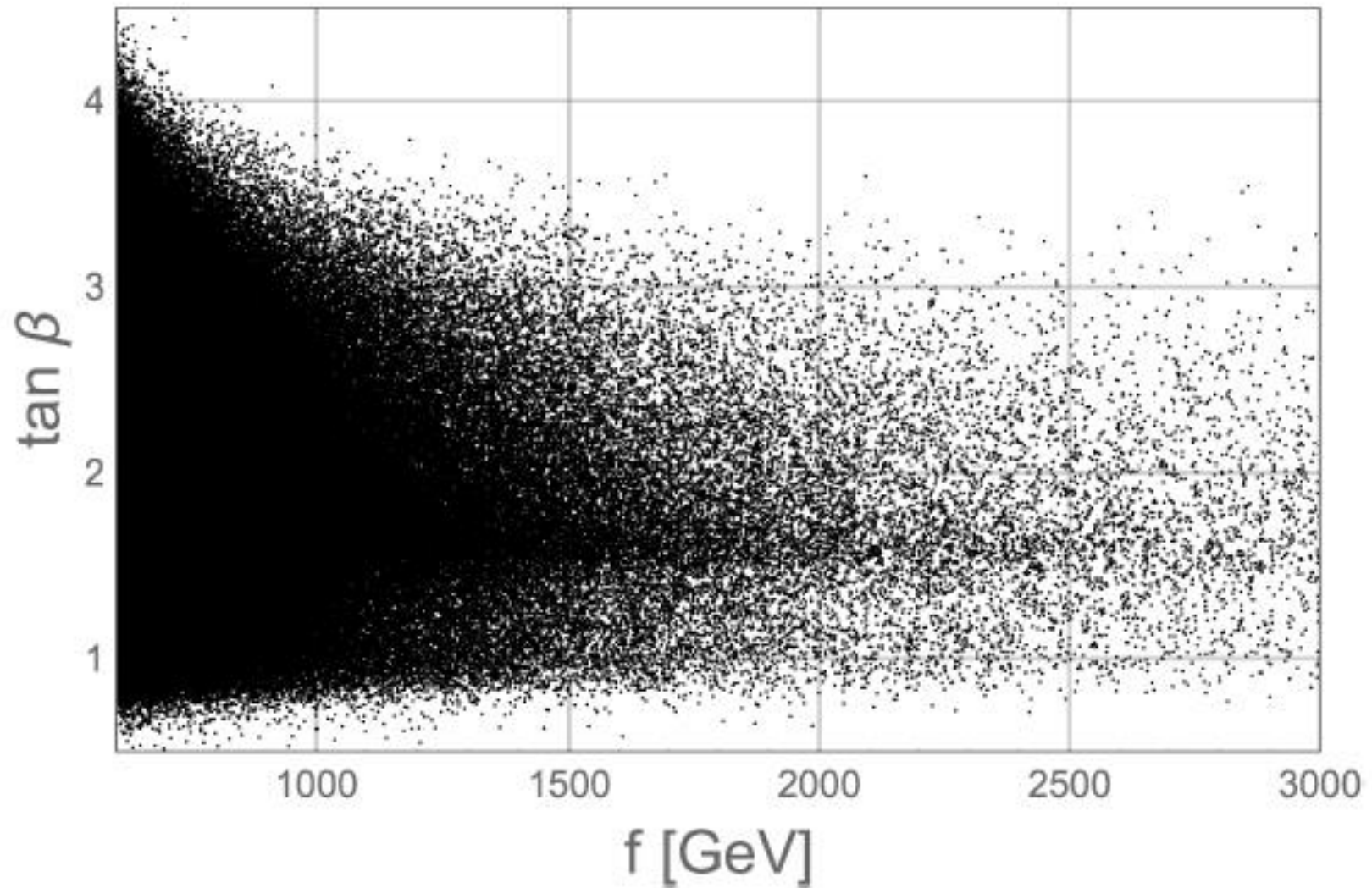
$$m_t \sim \langle K_{LR} \rangle_{q^2 \rightarrow 0} \sim \frac{v}{\sqrt{2}} \underbrace{\frac{\Delta_L \Delta_R}{m_\Psi^2}}_{Y_t}$$



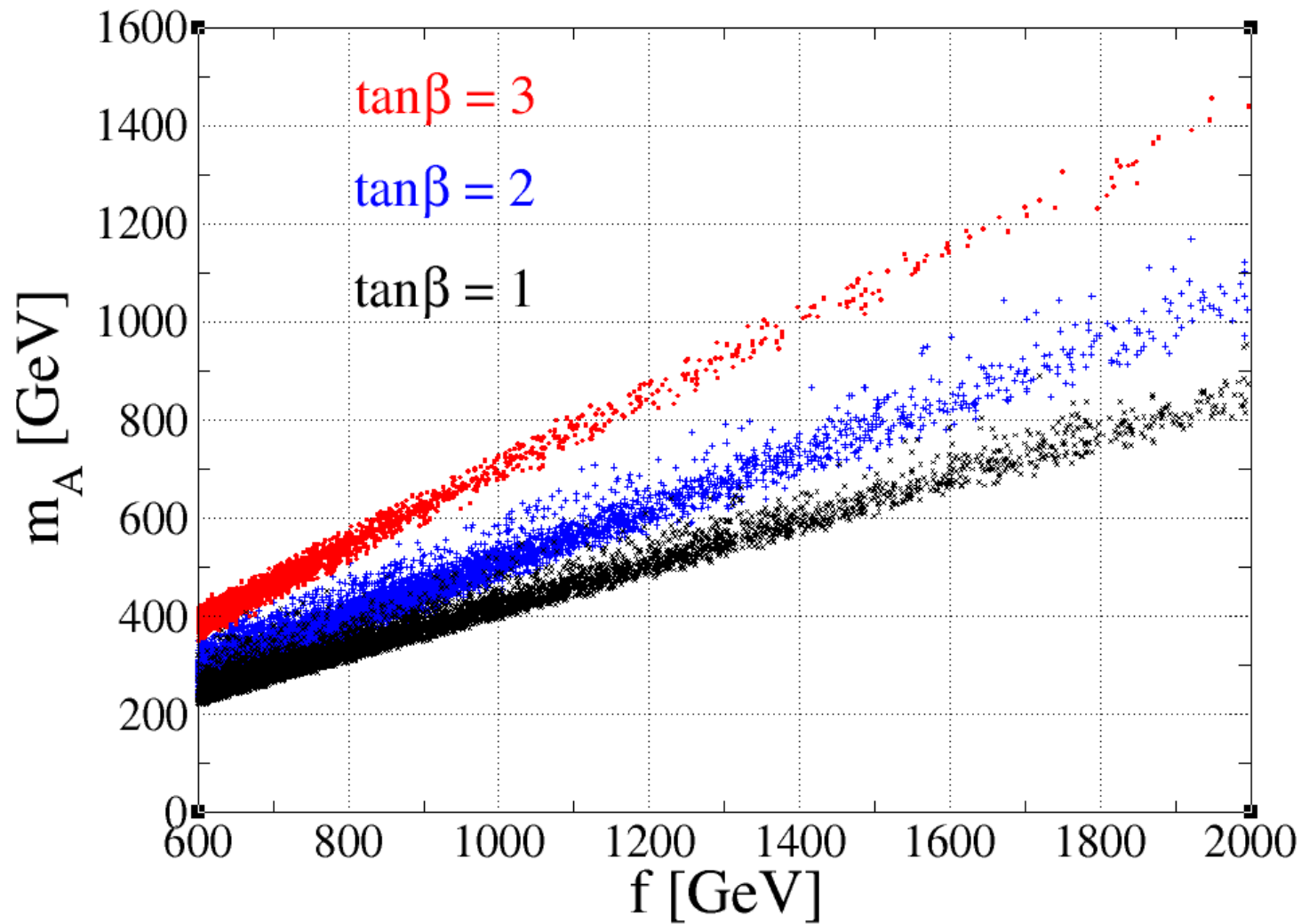
# Typical Prediction of Mass Spectrum



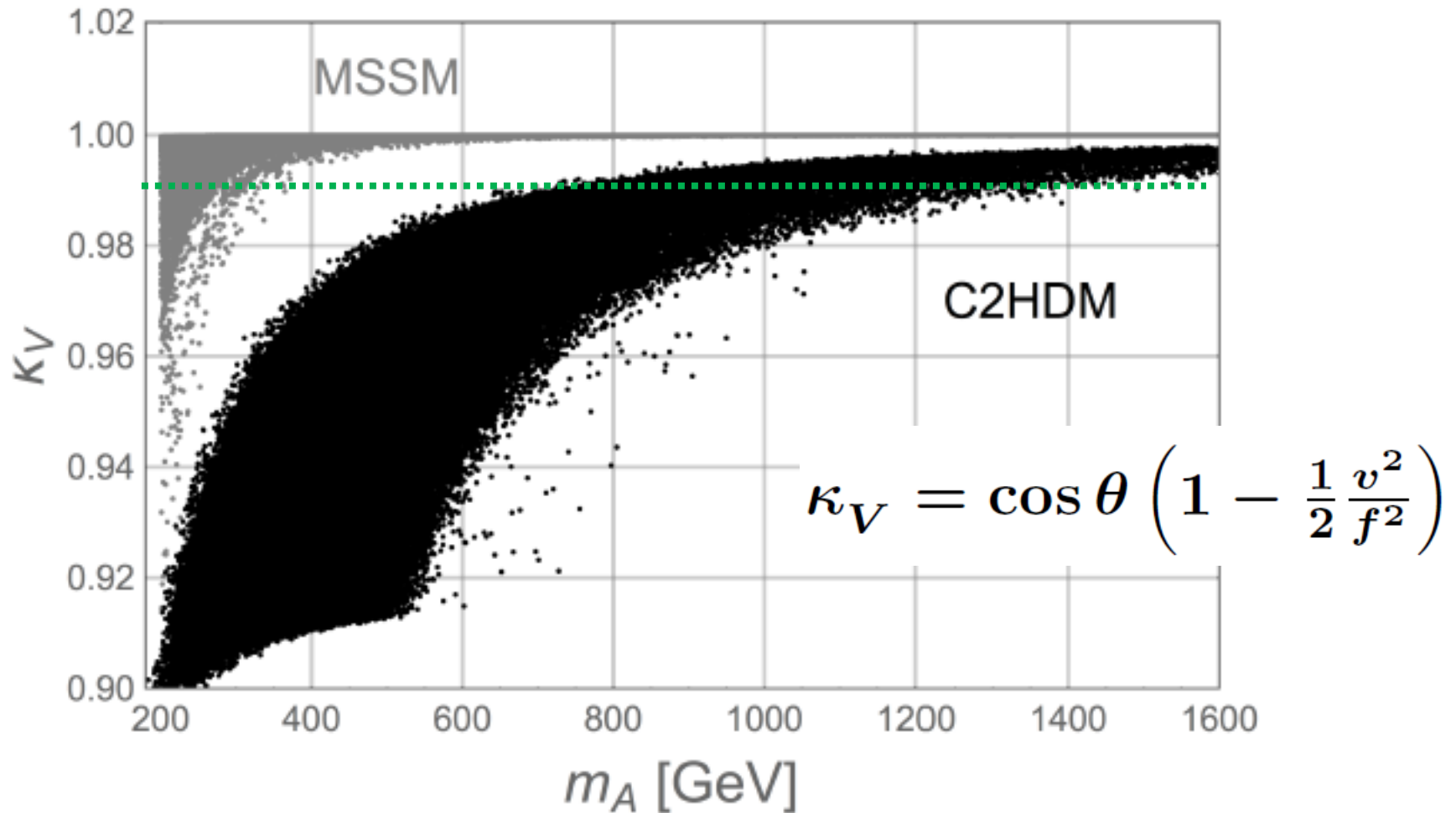
# $f$ VS $\tan\beta$



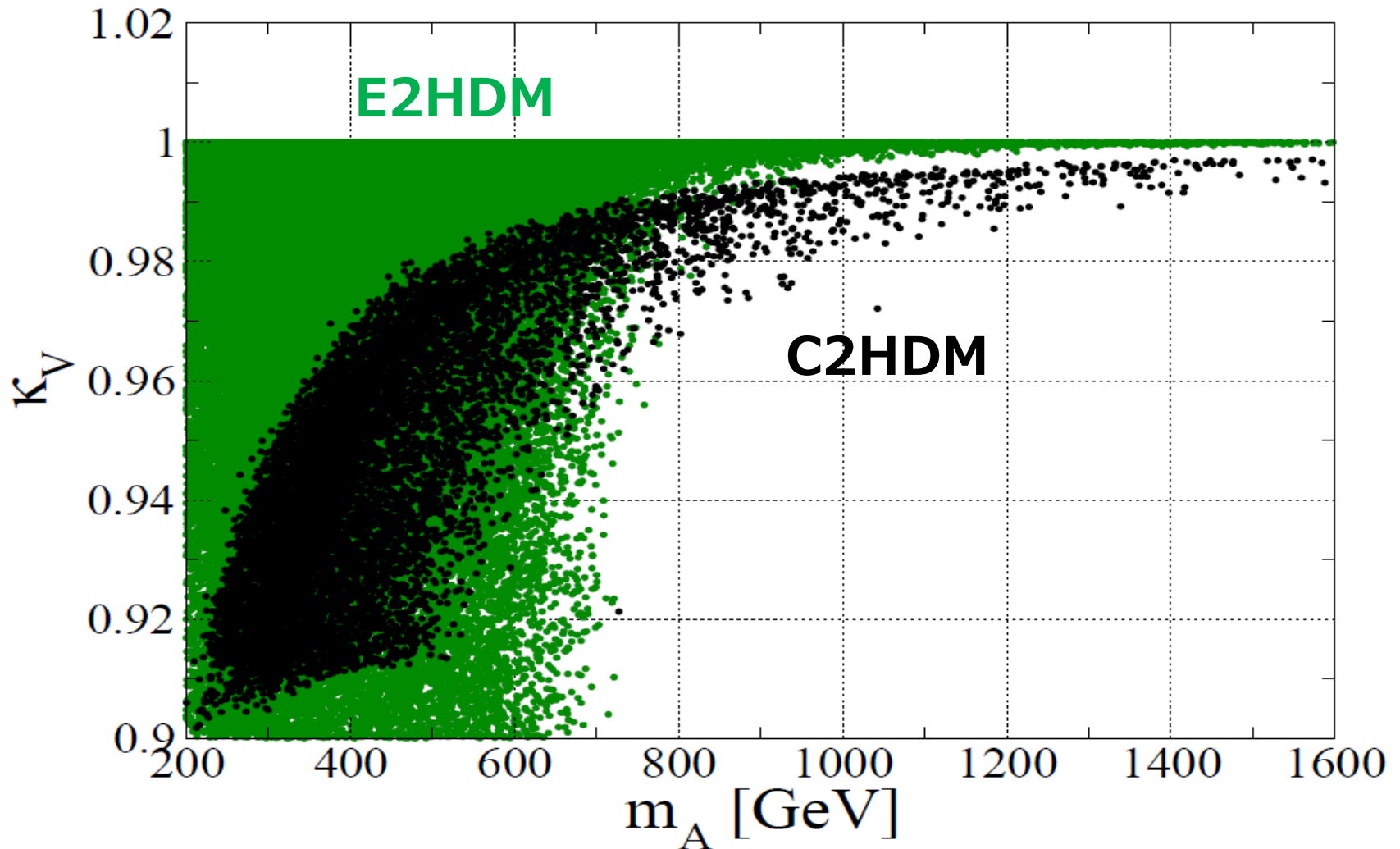
# Correlation b/w $f$ and $m_A$



# Correlation b/w $m_A$ and $\kappa_V (= g_{hVV}/g_{hVV}^{\text{SM}})$



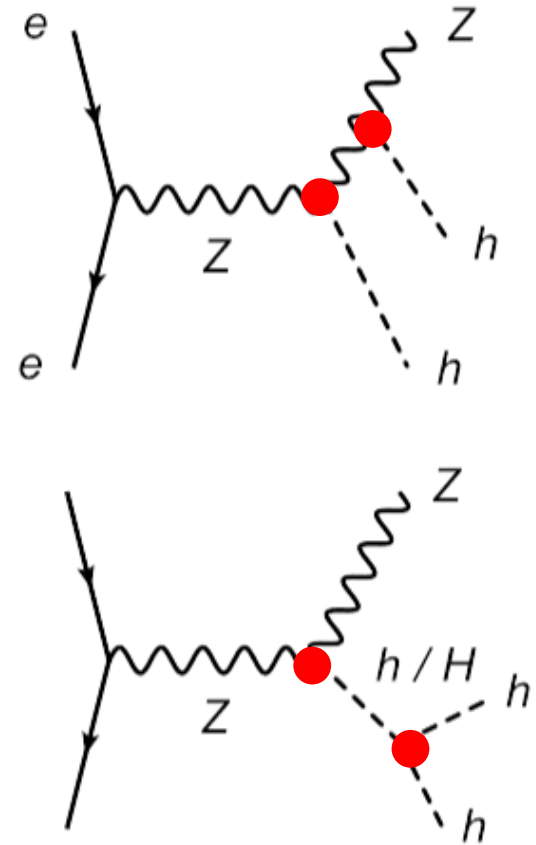
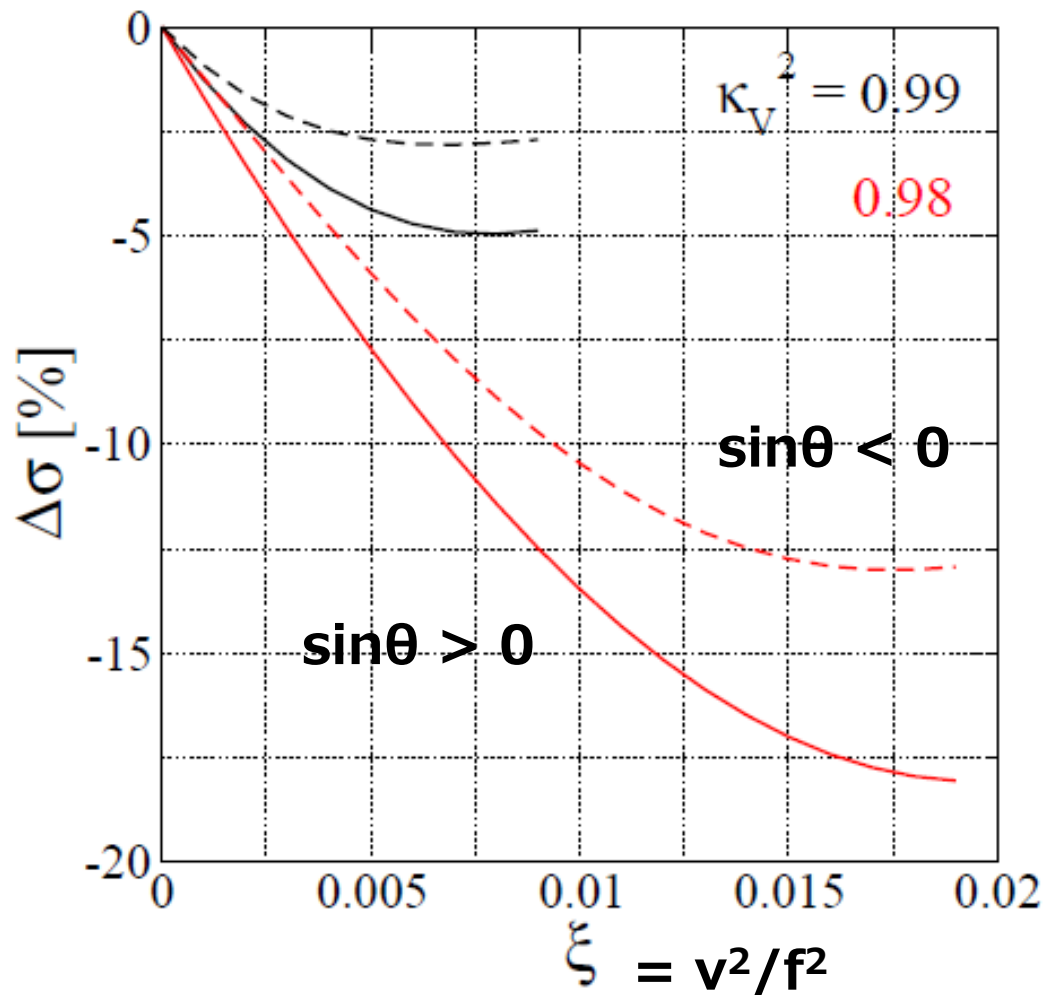
# Correlation b/w $m_A$ and $\kappa_V (= g_{hVV}/g_{hVV}^{\text{SM}})$



# Ratio of $\sigma(e^+e^- \rightarrow Zh h)$ @ $\sqrt{s} = 1$ TeV

*De Curtis, Moretti, KY, Yildirim, PRD95 095026*

$$\Delta\sigma = \sigma(\text{C2HDM})/\sigma(\text{E2HDM}) - 1$$





# Summary

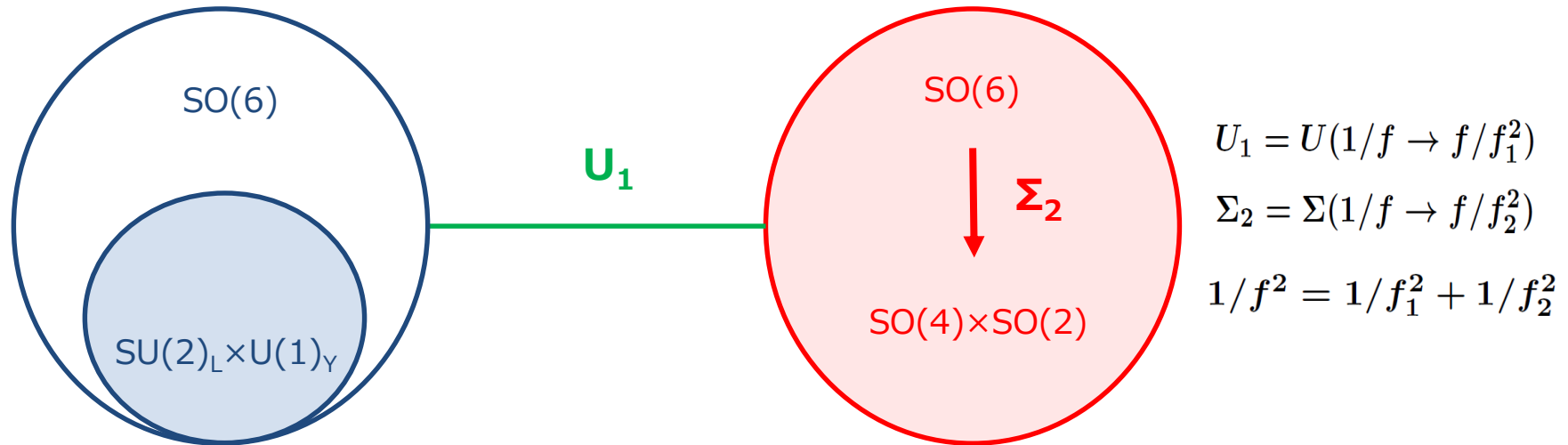
- ❑ Composite (=pNGB) Higgs can naturally explain the **light Higgs** .
- ❑ Taking the  $SO(6)/SO(4)*SO(2)$  coset, we obtain C2HDMs as a low energy EFT, where 2HDM parameters can be **predicted** by the **strong dynamics**.
- ❑ The MSSM and C2HDM can be distinguished by looking at the **decoupling behavior ( $\kappa V$ -mA)** .
- ❑ The C2HDM can be further distinguished from E2HDMs from the decoupling behaviour or by looking at  **$e^+e^- \rightarrow Zh h$**  process.

# Gauge Sector Lagrangian (in unitary gauge)

*De Curtis, Redi, Tesi, JHEP04 (2012) 042*

**Elementary Sector ( $g_W, W_\mu$ )**

**Strong Sector ( $g_\rho, \rho_\mu$ )**



$$\mathcal{L}_{\text{str}} = \frac{f_1^2}{4} \text{tr}(D_\mu U_1)^\dagger (D^\mu U_1) + \frac{f_2^2}{4} \text{tr}(D_\mu \Sigma_2)^T (D^\mu \Sigma_2) - \frac{1}{4} \text{tr} \rho_{\mu\nu}^A \rho^{A\mu\nu}$$

$$D_\mu U_1 = \partial_\mu U_1 - ig_W W_\mu U_1 + ig_\rho U_1 \rho_\mu$$

$$D_\mu \Sigma_2 = \partial_\mu \Sigma_2 - ig_\rho [\rho_\mu, \Sigma_2]$$

# Explicit Model

Based on the 4DCHM, De Curtis, Redi, Tesi, JHEP04 (2012) 042

$$\mathcal{L}_{\text{elem}} = -\frac{1}{4} W_{\mu\nu}^a W^{a\mu\nu} + \bar{q}_L i \not{D} q_L + \bar{t}_R i \not{D} t_R$$

Elementary Sector

$$\text{SU}(2)_L \times \text{U}(1)_Y$$
$$W_{\mu}^a, q_L, t_R$$

Mixing

Partial Compositeness

Strong Sector

$$\text{SO}(6) \times \text{U}(1)_X$$
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$$\mathcal{L}_{\text{str}} = \bar{\Psi}^6 (i \not{D} - m_\Psi) \Psi^6 - \bar{\Psi}_L^6 (Y_1 \Sigma + Y_2 \Sigma^2) \Psi_R^6 + \text{h.c.}$$

$$- \frac{1}{4} \text{tr} \rho_{\mu\nu}^A \rho^{A\mu\nu} + \frac{m_\rho^2}{2} (\rho^A)_\mu (\rho^A)^\mu + (\Sigma\text{-}\rho) \text{ interactions}$$

# Explicit Model

Based on the 4DCHM, De Curtis, Redi, Tesi, JHEP04 (2012) 042

$C_2$  symmetry  
(to avoid FCNCs)

$$U(\phi_1^{\hat{a}}, \phi_2^{\hat{a}}) \rightarrow C_2 U(\phi_1^{\hat{a}}, \phi_2^{\hat{a}}) C_2 = U(\phi_1^{\hat{a}}, -\phi_2^{\hat{a}})$$

$$\Sigma \rightarrow -C_2 \Sigma C_2$$

$$\Psi^6 \rightarrow C_2 \Psi^6$$

$$C_2 = \text{diag}(1, 1, 1, 1, 1, -1)$$

## Elementary Sector

$$SU(2)_L \times U(1)_Y$$

$$W_\mu^a, q_L, t_R$$

Mixing

Partial Compositeness

## Strong Sector

$$SO(6) \times U(1)_X$$

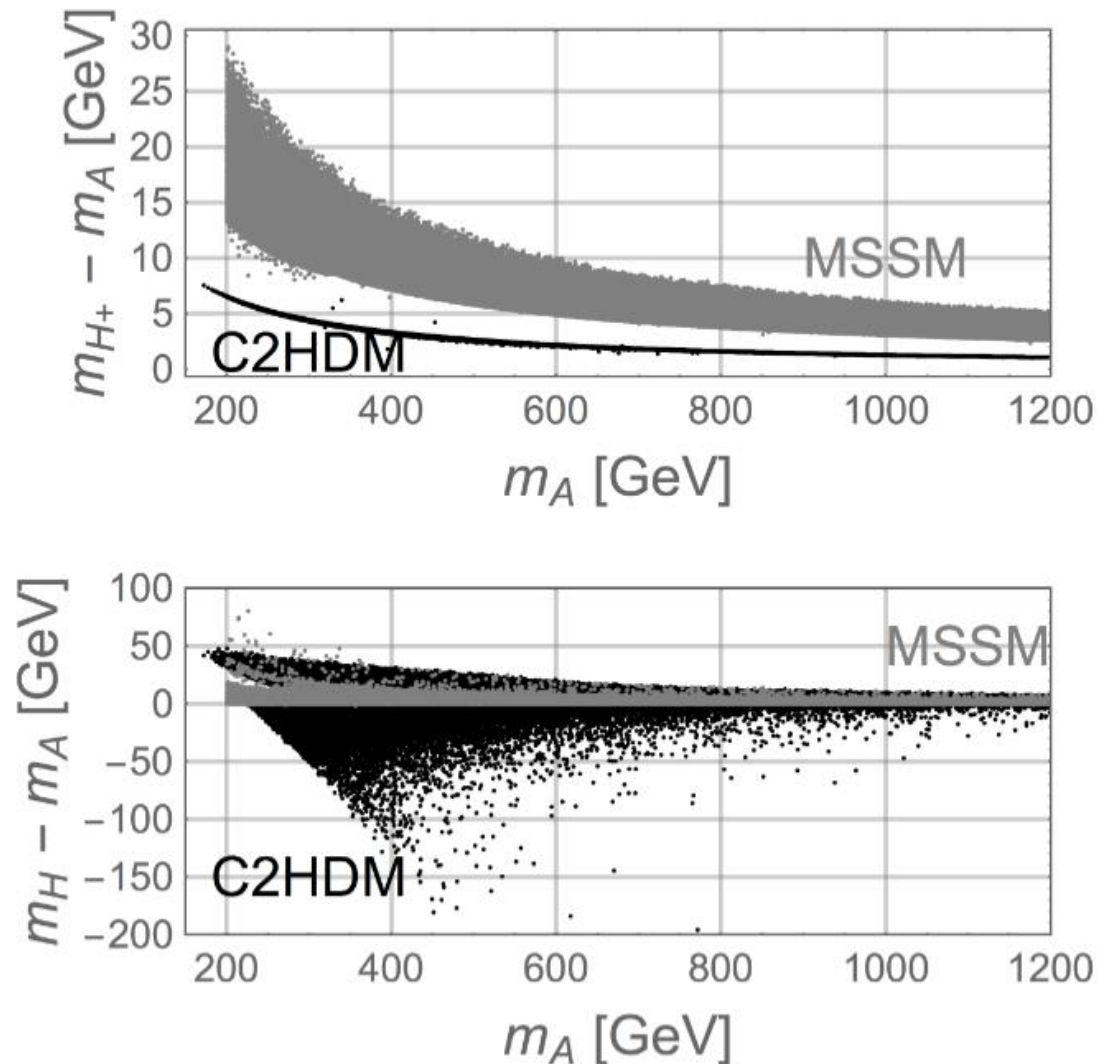
$$\rightarrow SO(4) \times SO(2) \times U(1)_X$$

$$\rho_\mu^A, \Psi^6, \Sigma$$

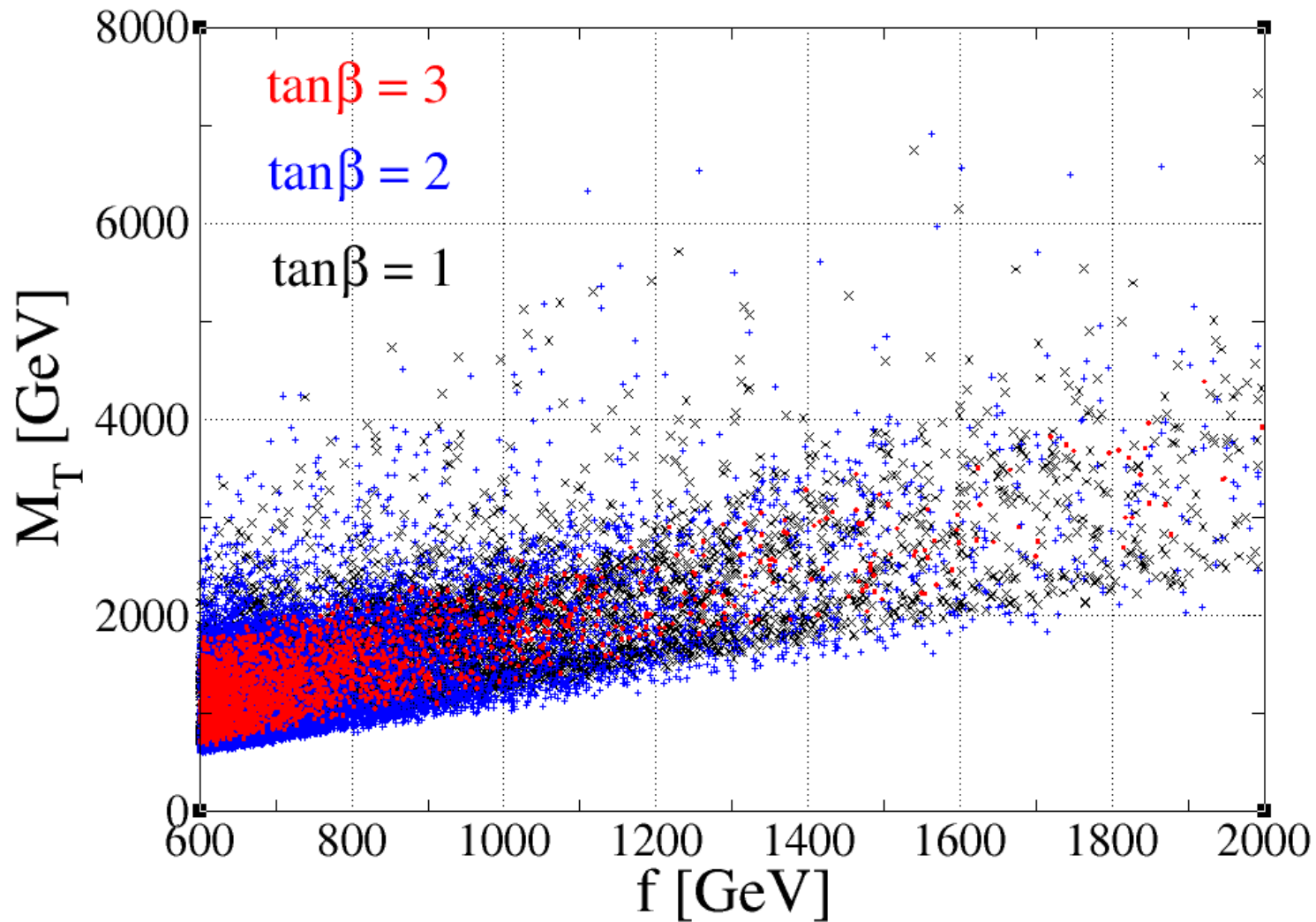
$$\mathcal{L}_{\text{str}} = \bar{\Psi}^6 (i \not{D} - m_\Psi) \Psi^6 - \bar{\Psi}_L^6 (Y_1 \Sigma + Y_2 \Sigma^2) \Psi_R^6 + \text{h.c.}$$

$$- \frac{1}{4} \text{tr} \rho_{\mu\nu}^A \rho^{A\mu\nu} + \frac{m_\rho^2}{2} (\rho^A)_\mu (\rho^A)^\mu + (\Sigma - \rho) \text{ interactions}$$

# Correlation b/w $m_A$ and $\kappa_V (= g_{hVV}/g_{hVV}^{\text{SM}})$

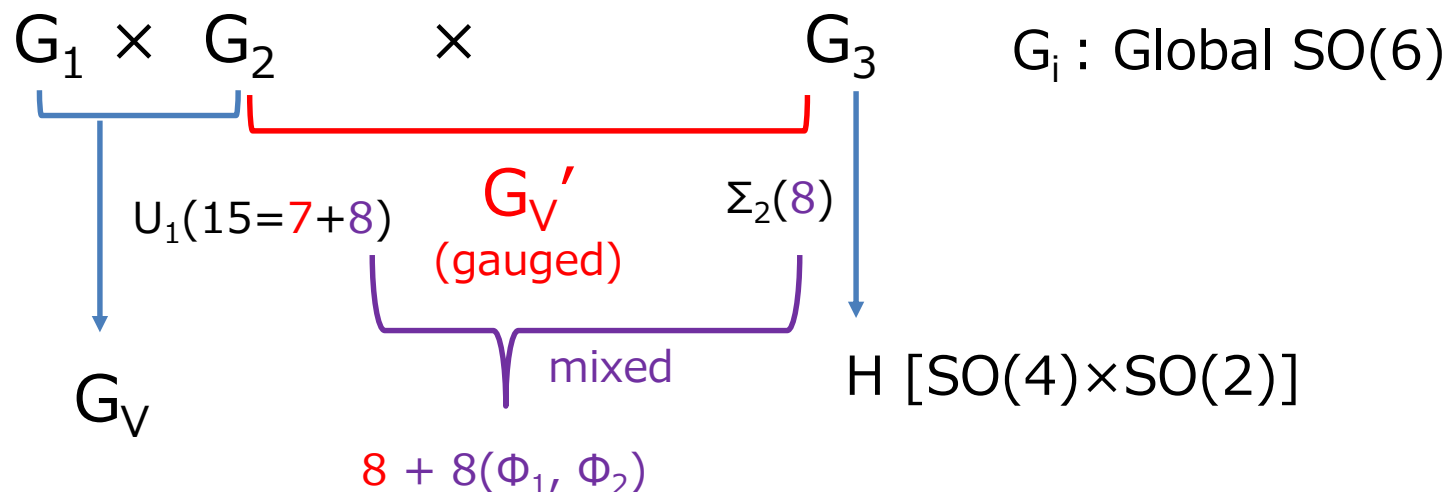


# Correlation b/w $f$ and $M_T$



# Gauge Sector Lagrangian

*De Curtis, Redi, Tesi, JHEP04 (2012) 042*



**7 + 8** NGBs are absorbed into the longitudinal components of gauge bosons of  $\text{adj}[SO(6)]$ .



# Effective Lagrangian

- Integrating out the heavy degrees of freedom ( $\rho^A$  and  $\psi^6$ ), we obtain the effective low energy Lagrangian

$$\mathcal{L}_{\text{eff}} = (W_\mu, B_\mu) \underbrace{\begin{pmatrix} G_{LL} & G_{LR} \\ G_{LR} & G_{RR} \end{pmatrix}}_{:= G} \begin{pmatrix} W^\mu \\ B^\mu \end{pmatrix} + (\bar{q}_L, \bar{t}_R) \underbrace{\begin{pmatrix} \not{G} K_{LL} & K_{LR} \\ K_{LR} & \not{G} K_{RR} \end{pmatrix}}_{:= K} \begin{pmatrix} q_L \\ t_R \end{pmatrix}$$

$$K_{LL} = I_{2 \times 2} + K_{LL}^{11} \Phi_1^c \Phi_1^{c\dagger} + K_{LL}^{22} \Phi_2^c \Phi_2^{c\dagger} + (K_{LL}^{12} \Phi_1^c \Phi_2^{c\dagger} + \text{h.c.})$$

$$K_{LR} = \Phi_1^c K_{LR}^1 + \Phi_2^c K_{LR}^2$$

# Effective Lagrangian

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$$\mathcal{L}_{\text{eff}} = (W_\mu, B_\mu) \underbrace{\begin{pmatrix} G_{LL} & G_{LR} \\ G_{LR} & G_{RR} \end{pmatrix}}_{:= G} \begin{pmatrix} W^\mu \\ B^\mu \end{pmatrix} + (\bar{q}_L, \bar{t}_R) \begin{pmatrix} \not{G} K_{LL} & K_{LR} \\ K_{LR} & \not{G} \underbrace{K_{RR}}_{:= K} \end{pmatrix} \begin{pmatrix} q_L \\ t_R \end{pmatrix}$$

$$K_{LL} = I_{2 \times 2} + \underbrace{K_{LL}^{11}}_{\text{circled}} \Phi_1^c \Phi_1^{c\dagger} + \underbrace{K_{LL}^{22}}_{\text{circled}} \Phi_2^c \Phi_2^{c\dagger} + (\underbrace{K_{LL}^{12}}_{\text{circled}} \Phi_1^c \Phi_2^{c\dagger} + \text{h.c.})$$

$$K_{LR} = \Phi_1^c \underbrace{K_{LR}^1}_{\text{circled}} + \Phi_2^c \underbrace{K_{LR}^2}_{\text{circled}}$$

These coefficients can be expanded as  $1 + c_1^{ij} \Phi_i^\dagger \Phi_j + c_2^{ij} (\Phi_i^\dagger \Phi_j)^2 + \dots$

$c_1, c_2, \dots$  are determined by strong parameters.

# Numerical Analysis

Input parameters (to be scanned):

$$f, g_\rho, Y_1, Y_2, \Delta_L, \Delta_R, M_\Psi, M_\Psi^{12}$$

Tadpole conditions:  $T_1 = T_2 = 0$

$$165 \text{ GeV} < m_t < 175 \text{ GeV}$$

$$120 \text{ GeV} < m_h < 130 \text{ GeV}$$

# Yukawa Interactions

- The structure of the Yukawa interaction is that in the Aligned 2HDM.

$$\mathcal{L}_{\text{eff}} = \frac{\sqrt{2}m_t}{v} \bar{q}_L (\Phi^c + \zeta_t \Psi^c) t_R + \text{h.c.} + \mathcal{O}(\xi^{3/2})$$

$$\zeta_t \equiv \frac{\bar{\zeta}_t - \tan \beta}{1 + \bar{\zeta}_t \tan \beta} \quad \text{with} \quad \bar{\zeta}_t = \frac{M_1^t}{M_2^t}.$$

- All  $M_1^t$ ,  $M_2^t$  and  $\tan \beta$  can be predicted by strong dynamics, so the  $\zeta_t$  factor is also predicted.

# Yukawa Interactions

