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# HIDDEN LIGHT SINGLET HIGGS BOSONS IN NMSSM WITH TEV SCALE MIRAGE MEDIATION

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Based on K.Hagimoto, T.Kobayashi, H. Makino, K.O., T.Shimomura  
arXiv:1509.05327



# Introduction

- \* Supersymmetry is attractive BSM candidate.
  - \* Big hierarchy + Unification
  - \* Light SM like Higgs (125 GeV): weak self-coupling
- \* Little hierarchy problem
  - \* Missing superpartners ( $m_{\tilde{q}} \sim > 1.5$  TeV LHC7+8)
  - \* Higgs is too heavy  $\rightarrow$  multi-TeV stop ?
  - \* Fine tuning  $< 1\%$

$$\frac{M_Z^2}{2} \simeq |m_{H_u}^2| - \mu^2 + \mathcal{O}\left(\frac{1}{\tan^2 \beta}\right)$$

“TeV scale mirage mediation in NMSSM” still fine !

 light ( $\sim 100$  GeV) almost decoupled singlet

# Mirage mediation

Soft SUSY breaking terms= (Moduli + Anomaly) Mediation

K.Choi A.Falkowski H.P.Niles M.Olechowski and S.Pokorski (2005)

$$-\mathcal{L}_{\text{Soft}} = M_a \overline{\lambda}_a \lambda_a + m_i^2 |\phi_i|^2 + \left\{ + \frac{1}{3!} Y_{ijk} A_{ijk} \phi_i \phi_j \phi_k + \text{h.c.} \right\}$$

$$M_a(M_G) = M_0 + (\text{Anomaly Mediation})$$

$$A_{ijk}(M_G) = (c_i + c_j + c_k) M_0 + (\text{Anomaly Mediation})$$

$$m_i^2(M_G) = c_i |M_0|^2 + (\text{Anomaly Mediation}) \quad c_i = 0, 1/3, 1/2, 1$$

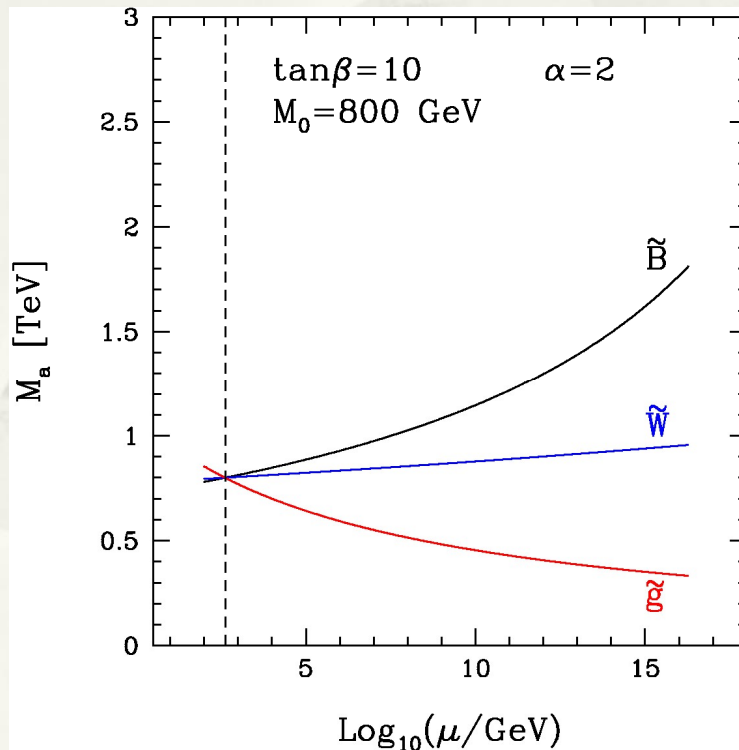
RG corrections cancel with anomaly mediation at  $M_{\text{mir}}$ .

$$M_{\text{mir}} = \frac{M_G}{(M_{Pl}/m_{3/2})^{\alpha/2}} \quad \alpha \equiv \frac{m_{3/2}}{M_0 \ln(M_{Pl}/m_{3/2})} \quad c_i + c_j + c_k = 1 \text{ for } Y_{ijk} = \mathcal{O}(1)$$

# TeV scale Mirage mediation

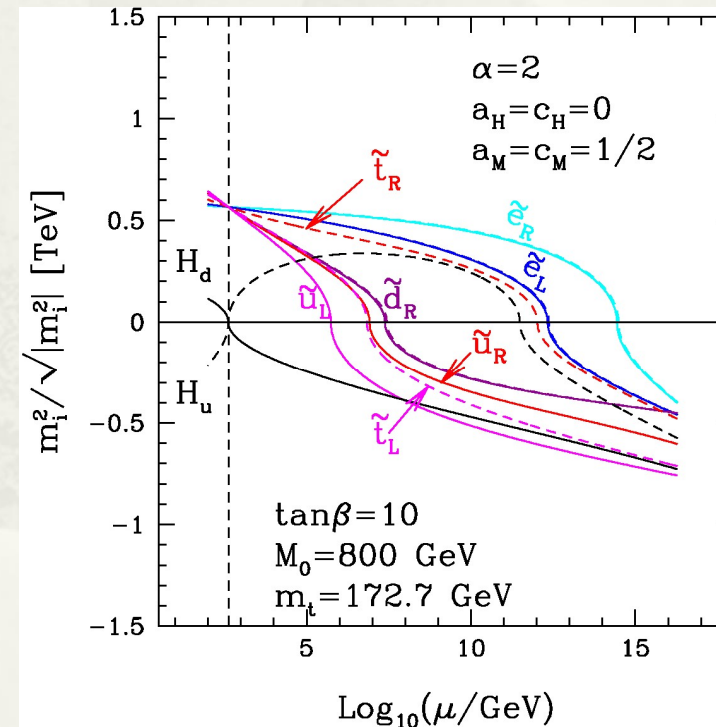
$$M_{\text{mir}} \simeq \text{TeV}, \quad c_{H_u} = 0$$

Gaugino Mass:  $M_a$



“Natural Little Hierarchy”

Sfermion Mass:  $m_i^2$



Two problems:  $B \approx 8\pi^2 M_0$ ,  $m_h = 125$  GeV requires multi-TeV stop.

# NMSSM

$$W_H = -\lambda S H_u H_d + \frac{\kappa}{3} S^3 \quad (Z_3)$$

- \* New F-term potential  $\rightarrow$  Tree-level Higgs mass

$$\Delta V_F = \lambda^2 |H_u H_d|^2$$

- \* Landau pole  $\lambda \lesssim 0.6$
- \* F-term (  $\sin^2 2\beta$  ) max  $\rightarrow$  D-term (  $\cos^2 2\beta$  ) min
- \* Mixing with S
- \* No gain in FT  $\frac{M_Z^2}{2} \simeq |m_{H_u}^2| - \mu_{eff}^2 \quad \mu_{eff} = \lambda \langle S \rangle$
- \* Dimensionless  $\rightarrow$  sol. of  $B_\mu$  problem in MM



# NMSSM in TeV scale mirage mediation

The soft SUSY breaking terms in Higgs sector are given by,

$$V_{\text{soft}} = m_{H_u}^2 |H_u|^2 + m_{H_d}^2 |H_d|^2 + m_S^2 |S|^2 - \lambda A_\lambda S H_u H_d + \frac{\kappa}{3} A_\kappa S^3 + h.c.$$

We chose the modular weights as  $c_{H_d} = 1$ ,  $c_{H_u} = 0$ ,  $c_S = 0$ ,  $c_{q,\ell} = \frac{1}{2}$

$$M_a = M_0$$

$$m_{H_d}^2 = M_0^2$$

$$A_\lambda = M_0$$

TeV scale

$$m_{\tilde{q},\tilde{\ell}}^2 = \frac{1}{2} M_0^2$$

$$m_{H_u}^2 \approx 0, \quad m_S^2 \approx 0$$

$$A_\kappa \approx 0$$

$$\leftarrow \sim \frac{M_0}{\sqrt{8\pi^2}} \quad 100 \text{ GeV}$$

Small parameters, Uncontrollable 1-loop corrections

# Improved fine-tuning in TeV scale

## MM

$$c_{H_d} = 1, \quad c_{H_u} = 0$$

K.Choi K.S.Jeong T.Kobayashi K.i.Okumura (2006)

$$\begin{matrix} H_d & H_u \end{matrix} \quad B_\mu = A_\lambda$$

$$\mathcal{M}_H^2 = \begin{matrix} H_d \\ H_u \end{matrix} \begin{pmatrix} M_0^2 + \mu^2 & M_0 \mu \\ M_0 \mu & \mu^2 \end{pmatrix}$$

$$c_S = 0$$

$$\text{Det}(\mathcal{M}_H^2) = M_H^2 M_h^2 = (M_0^2 + \mu^2)\mu^2 - M_0^2\mu^2 = \mu^4$$

$$M_H \approx M_0 \rightarrow M_h \approx \mu \frac{\mu}{M_0} \quad !$$

Pot. minimum chooses:

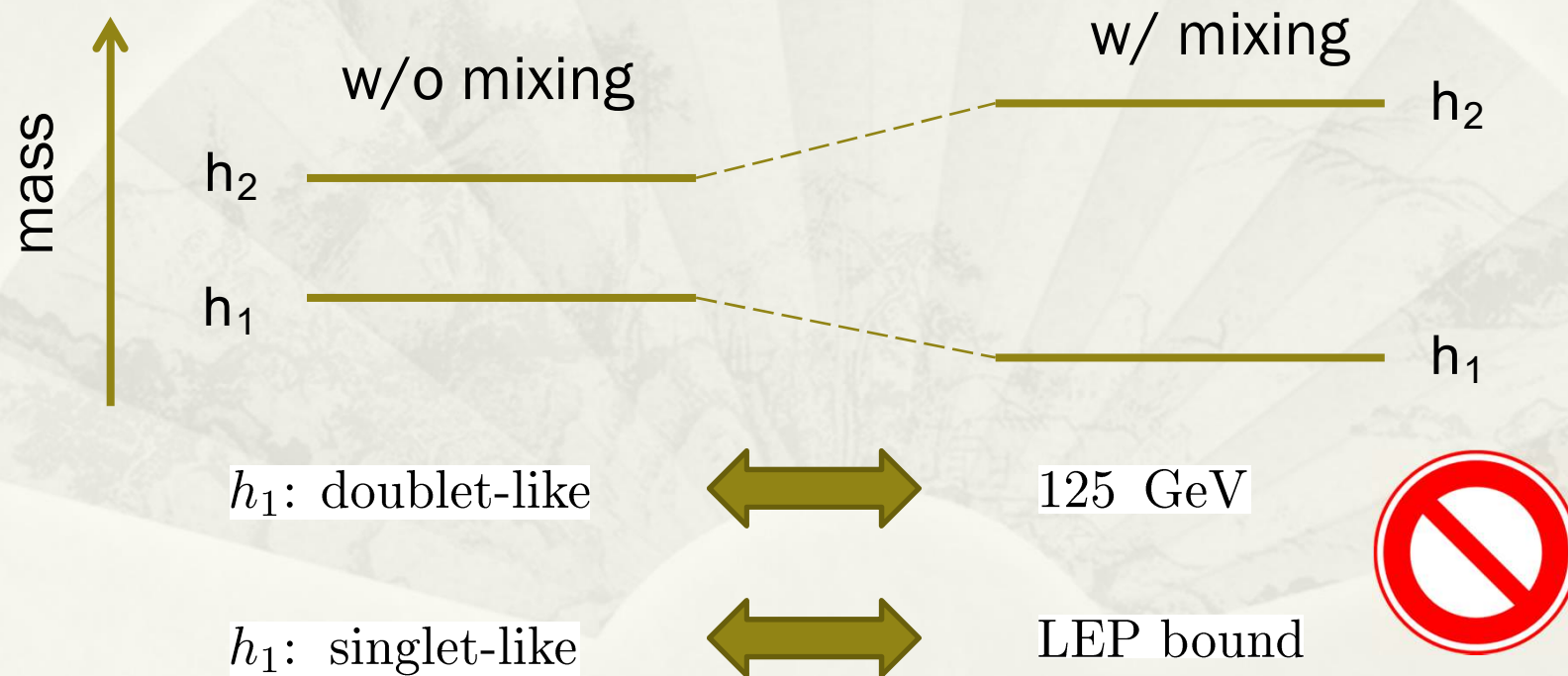
$$\frac{M_Z^2}{2} \simeq |m_{H_u}^2| + \overbrace{\left( -\mu^2 + \frac{m_{H_d}^2}{\tan^2 \beta} \right)}^{\text{Cancel}}$$

$\mu$  term can be large

$$\mu \sim \sqrt{m_Z M_0}$$

# Doublet-Singlet mixing

In NMSSM, mixing with the singlet may destroy the  $\mu$  cancellation  
In addition, if the doublet-singlet mixing in the mass matrix is large,



We show [approximate scale symmetries](#) suppress the mixing



# Scale symmetry IN NMSSM

In  $\kappa = m_S^2 = 0$  limit, the scalar potential has an approximate scale symmetry,

$$H_u(x) = e^{2\phi} H'_u(e^\phi x)$$

$$H_d(x) = e^{2\phi} H'_d(e^\phi x)$$

$$S(x) = S'(e^\phi x)$$

$$W_H = -\lambda S H_u H_d$$

$$V_{\text{soft}} = m_{H_u}^2 |H_u|^2 + m_{H_d}^2 |H_d|^2 - \lambda A_\lambda S H_u H_d + h.c.$$

explicitly broken by  $\mathcal{K}_S = S^\dagger S$  and **D-term**.

$H_{u,d}$  VEVs break the symmetry and **the light doublet** ( $H_u/H_d = \tan \beta$ ) corresponds to **the NG boson**.

$$\left[ \begin{array}{l} \text{In } \kappa = m_{H_u}^2 = 0 \text{ limit, there's another scale symmetry, } S \leftrightarrow H_u \\ \text{Singlet-like Higgs } (S + H_d) \rightarrow \text{NG boson} \end{array} \right]$$

# Scale Symmetry in NMSSM (CONT'D)

$$\mathcal{SM}_S^2 \mathcal{S}^\dagger \approx \text{diag}(m_Z^2 \cos^2 2\beta + \lambda^2 v^2 \sin^2 2\beta, \quad A_\lambda^2 + (m_Z^2 - \lambda^2 v^2) \sin^2 2\beta, \quad \lambda^2 v^2 \sin^2 2\beta)$$

$$\mathcal{S}^\dagger = \begin{pmatrix} \Delta H_d \\ \Delta H_u \\ \Delta S \end{pmatrix} \begin{pmatrix} \cos \beta & -\sin \beta & \lambda \frac{v}{A_\lambda} \sin \beta \\ \sin \beta & \cos \beta & \lambda \frac{v}{A_\lambda} \cos \beta \\ -\lambda \frac{v}{A_\lambda} \sin 2\beta & -\lambda \frac{v}{A_\lambda} \cos 2\beta & 1 \end{pmatrix} + \mathcal{O}\left(\frac{v}{A_\lambda}\right)^2,$$

singlet-doublet mixing is suppressed by  $\frac{v}{A_\lambda}$  and  $1/\tan \beta$

In  $\kappa = m_S^2 = m_{H_u}^2 = \langle H_d \rangle = 0$  limit  $\rightarrow$

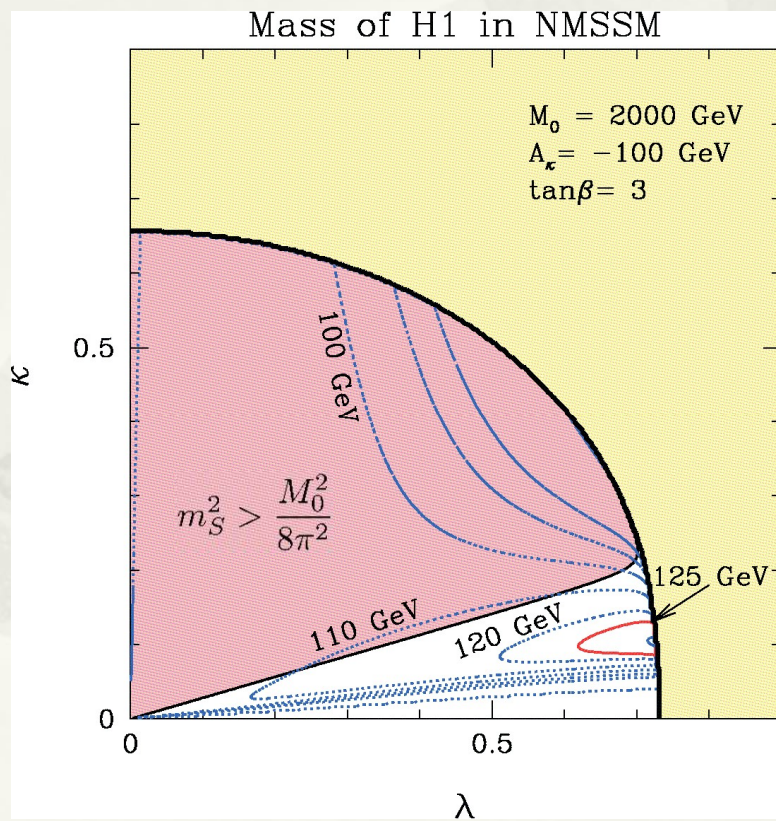
two NG bosons,  $H_u$ ,  $S$  (mass eigenstates)

$\mathcal{S}_{31}^\dagger$  and  $\mathcal{S}_{23}^\dagger$  must break the two symmetries and decouple with  $M_0$ .

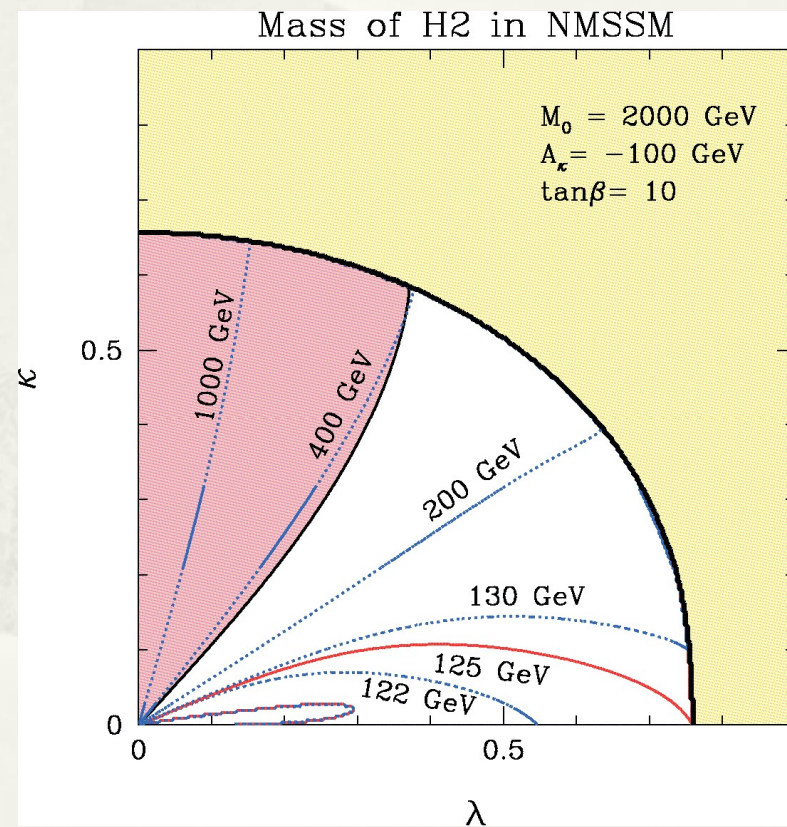
$$\kappa \frac{\langle S \rangle}{M_0}, \quad \frac{\langle H_d \rangle}{M_0}, \quad \frac{\langle H_u \rangle \langle S \rangle}{M_0^2}, \quad \frac{m_S^2 \langle S \rangle}{M_{10/22}^3}, \quad \frac{m_{H_u}^2 \langle H_u \rangle}{M_0^3}, \quad \frac{m_S^2 m_{H_u}^2}{M_0^4}$$

# Higgs mass

Small  $\tan \beta$ :  $H_1 = \text{SM like}$

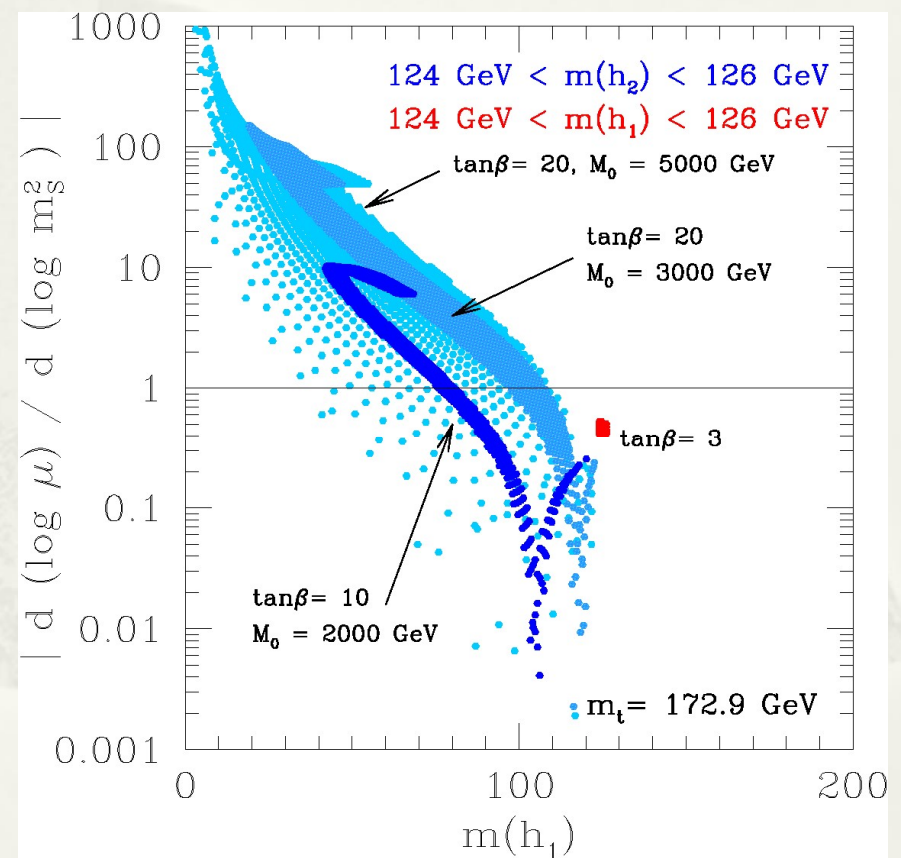
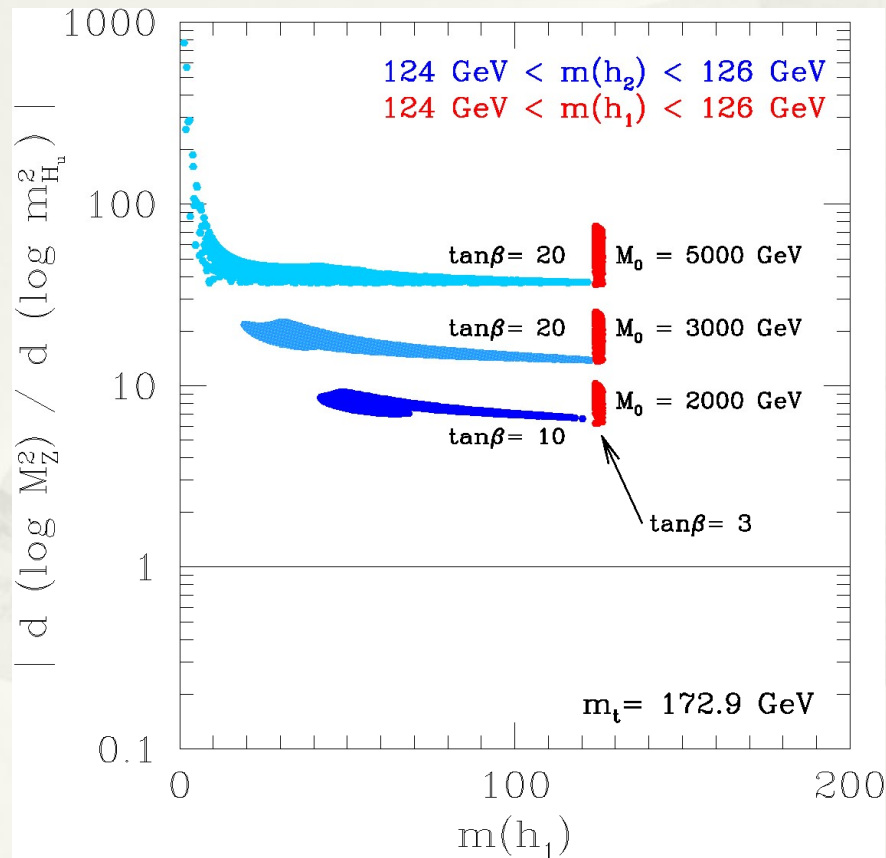


Large  $\tan \beta$ :  $H_2 = \text{SM like}$





# Fine-Tuning measures



$M_0 = 5 \text{ TeV}$  is acceptable in the standard of conventional 1 TeV models !

# Higgs effective coupling constants

The effective coupling constants of CP-even Higgs bosons are defined as,

$$\mathcal{L} = \sum_{i=1}^3 \left[ C_V^i \frac{\sqrt{2}m_W^2}{v} h_i W_\mu^+ W^{-\mu} + C_V^i \frac{m_Z^2}{\sqrt{2}v} h_i Z_\mu Z^\mu - \sum_f C_f^i \frac{m_f}{\sqrt{2}v} h_i \bar{f} f \right. \\ \left. + C_g^i \frac{\alpha_s}{12\sqrt{2}\pi v} h_i G_{\mu\nu}^a G^{a\mu\nu} + C_\gamma^i \frac{\alpha}{\sqrt{2}\pi v} h_i A_{\mu\nu} A^{\mu\nu} \right]$$

For the SM,  $C_V^{SM} = C_f^{SM} = 1$ ,  $C_g^{SM} \approx 1.03$ ,  $C_\gamma^{SM} \approx -0.81$

Their deviations from the SM value (or existence itself) encode information of new physics.



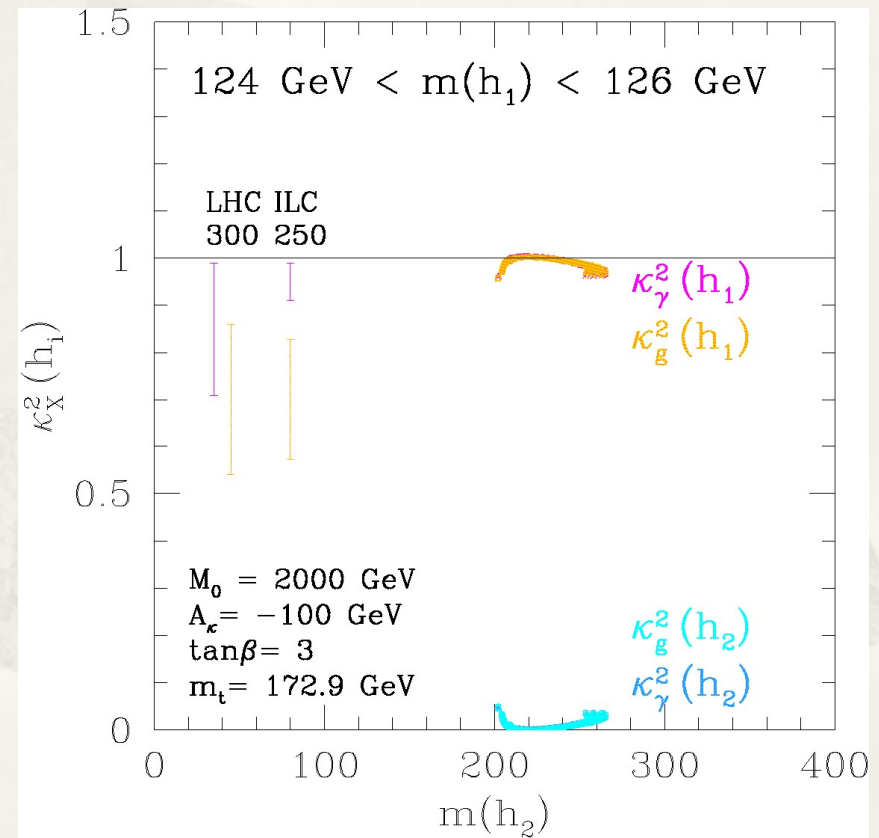
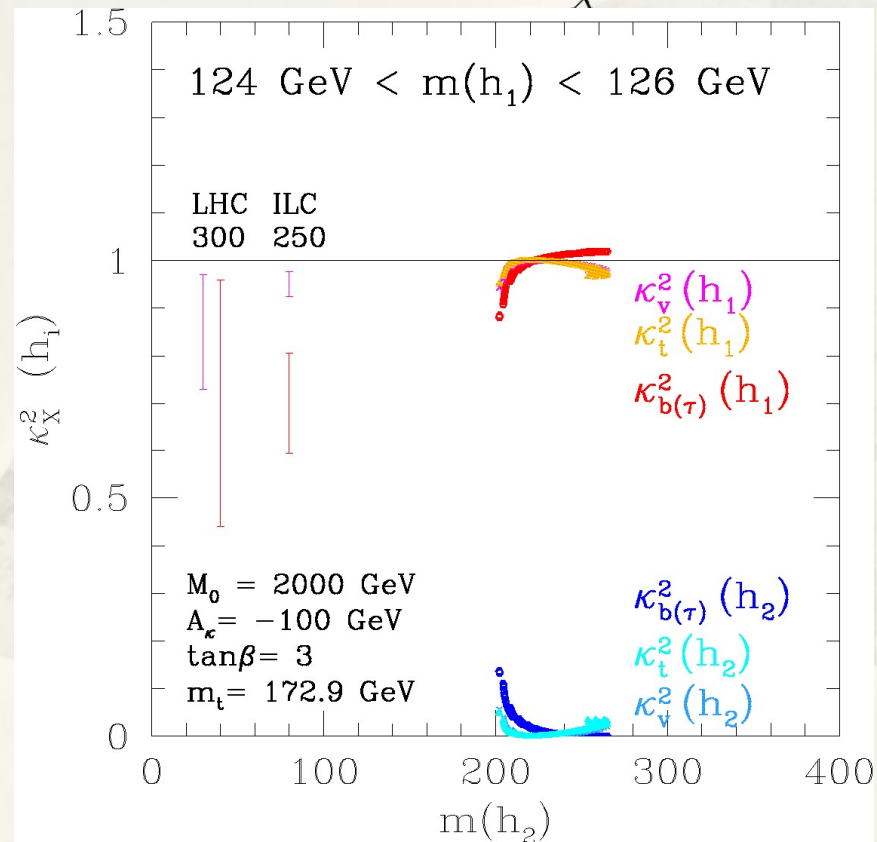
# CP even Higgs

$\tan \beta = 3$

(Calculated by NMSSMTools)

Tree  $\kappa_X^i = \frac{C_X^i}{C_X^{SM}}$

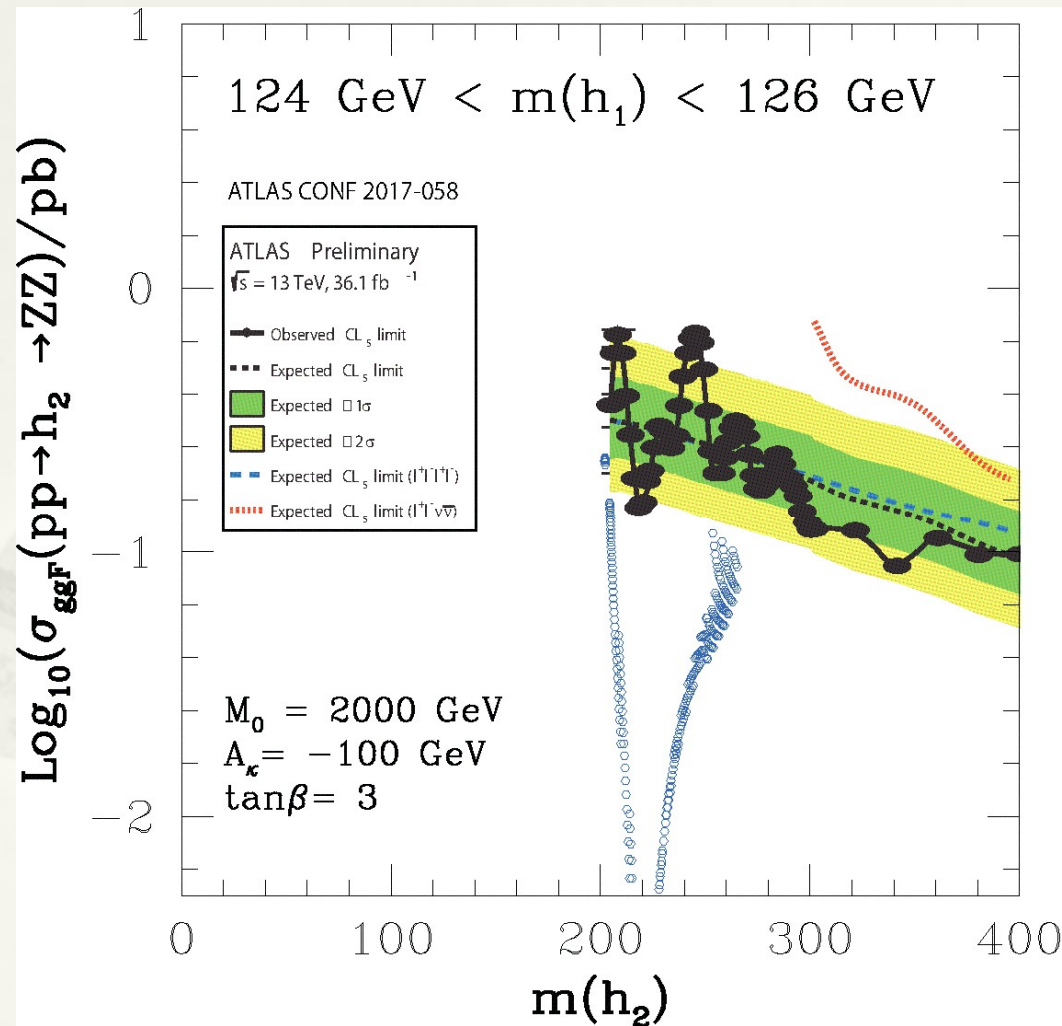
Loop



Sum rule  $(\kappa^{h_1})^2 + (\kappa^{h_2})^2 = 1$  holds well except for  $b(\tau)$ .

~ 10 % deviation from the SM Higgs is possible for tree-level couplings.

# CP even Higgs (cont'd)



$H_1 = \text{SM like}$

ILC250 can't reach

If we are lucky,  
LHC will find the singlet

ILC can be upgraded  
to measure it

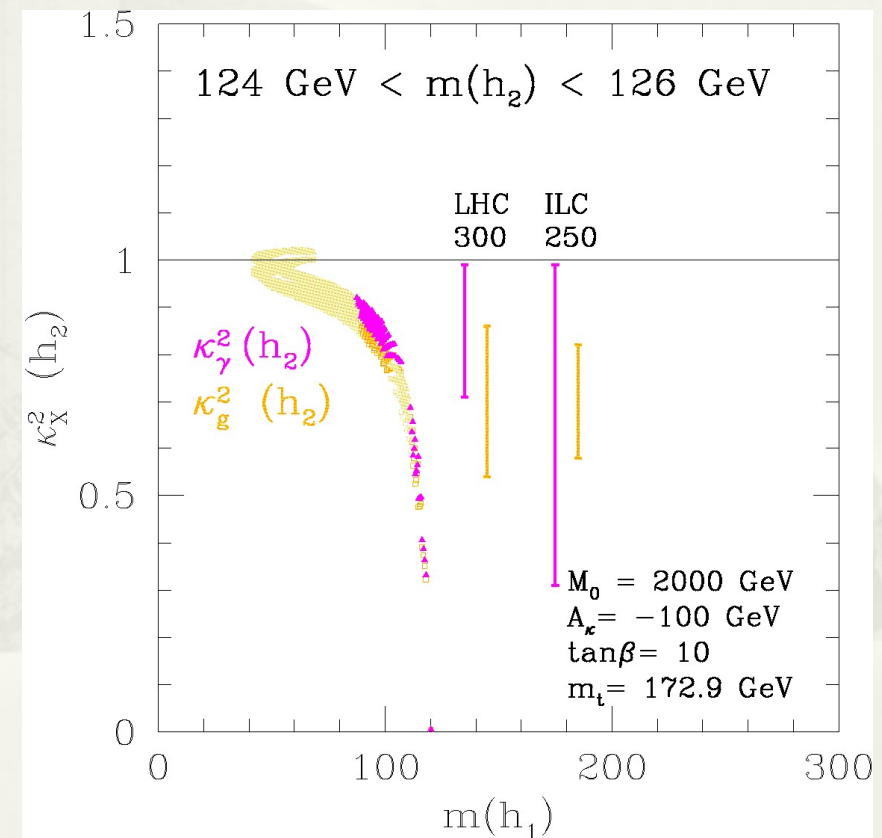
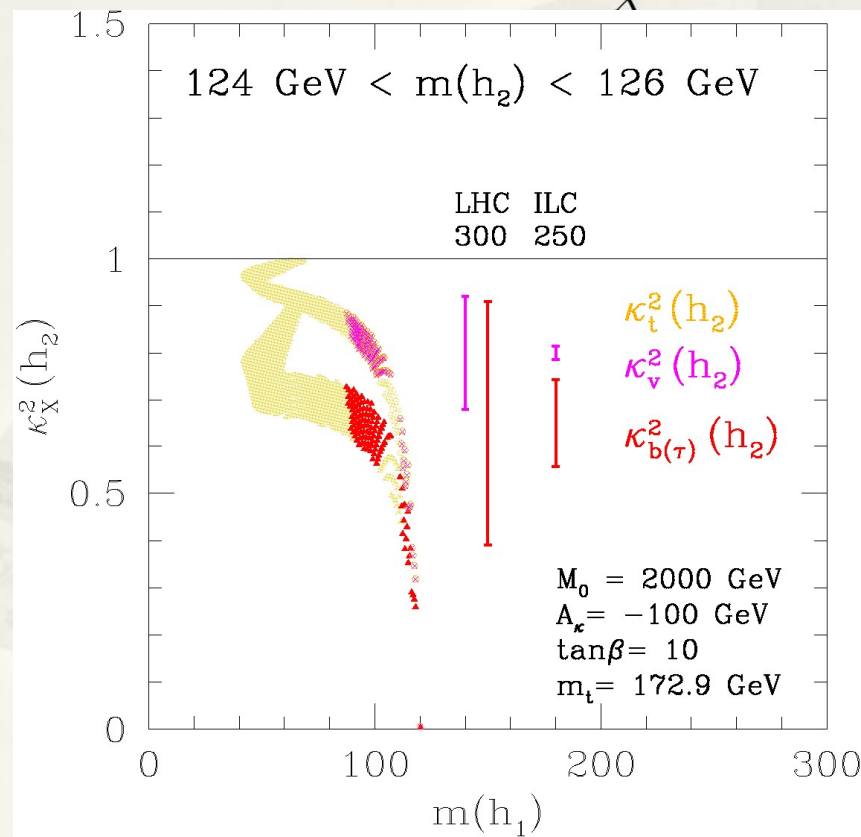
# CP even Higgs (cont'd)

$\tan \beta = 10$

Tree

$$\kappa_X^i = \frac{C_X^i}{C_X^{SM}}$$

Loop



Singlet-doublet mixing is required by  $m_{h_2} = 125$  GeV.

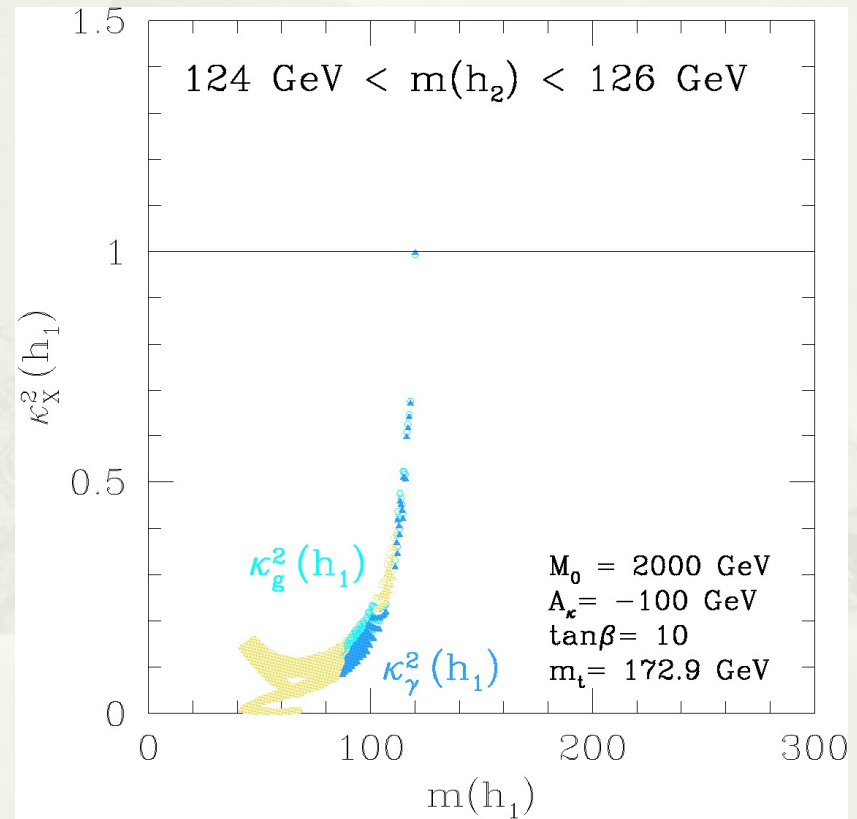
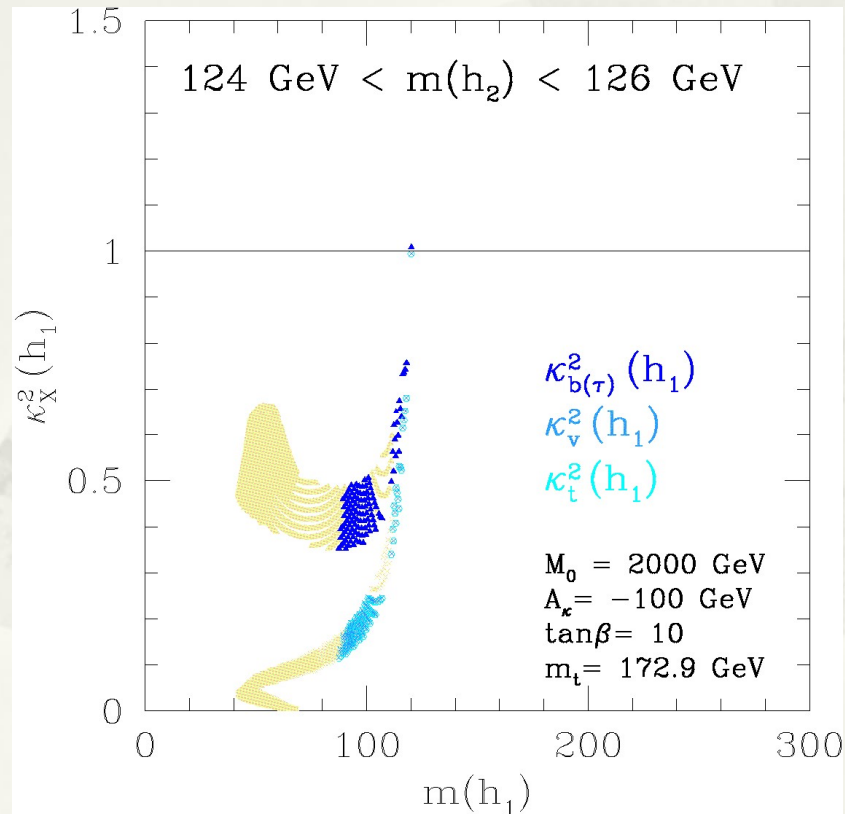
$\sim 40\%$  deviation is possible for  $\kappa_b$  (mixing with  $\tan \beta$  enhanced  $H$  coupling).

# CP even Higgs (cont'd)

$\tan \beta = 10$   
Tree

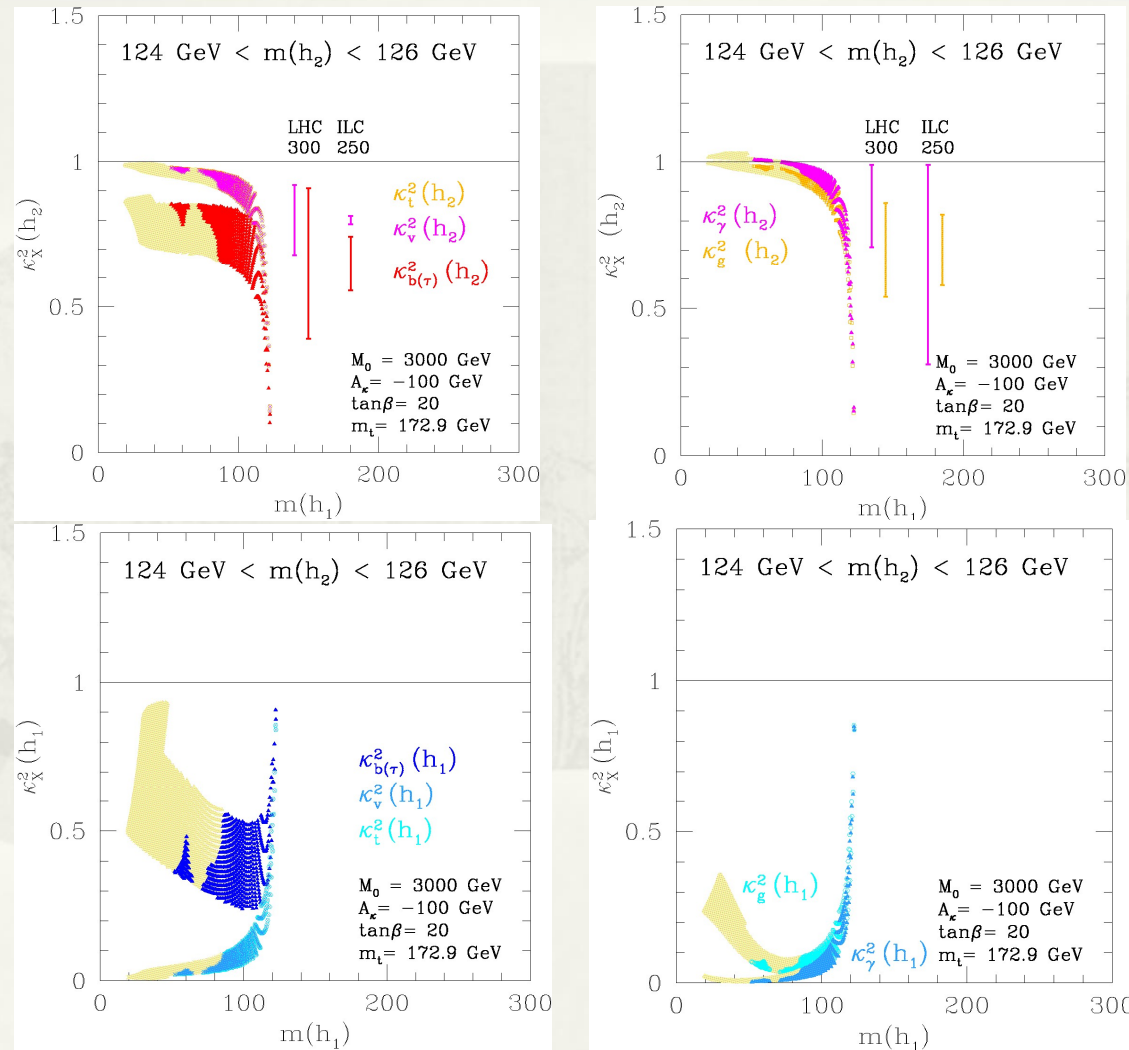
$$\kappa_X^i = \frac{C_X^i}{C_X^{SM}}$$

Loop



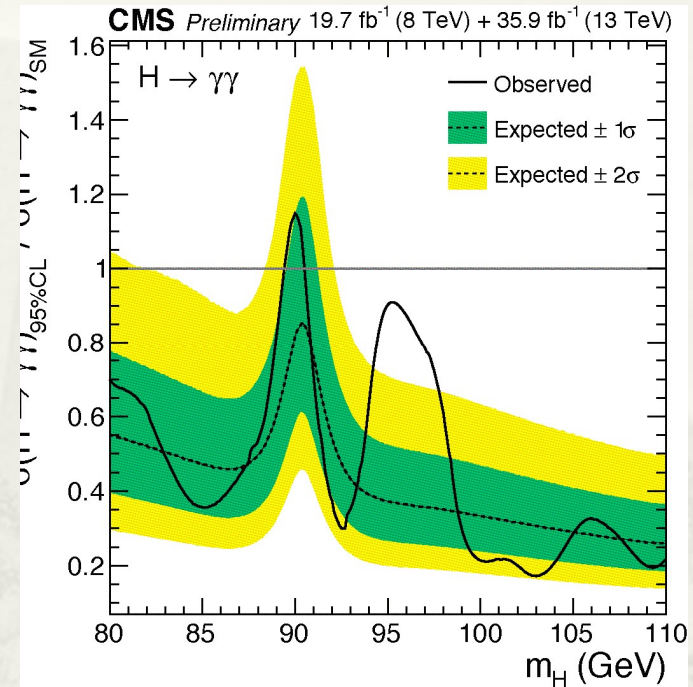
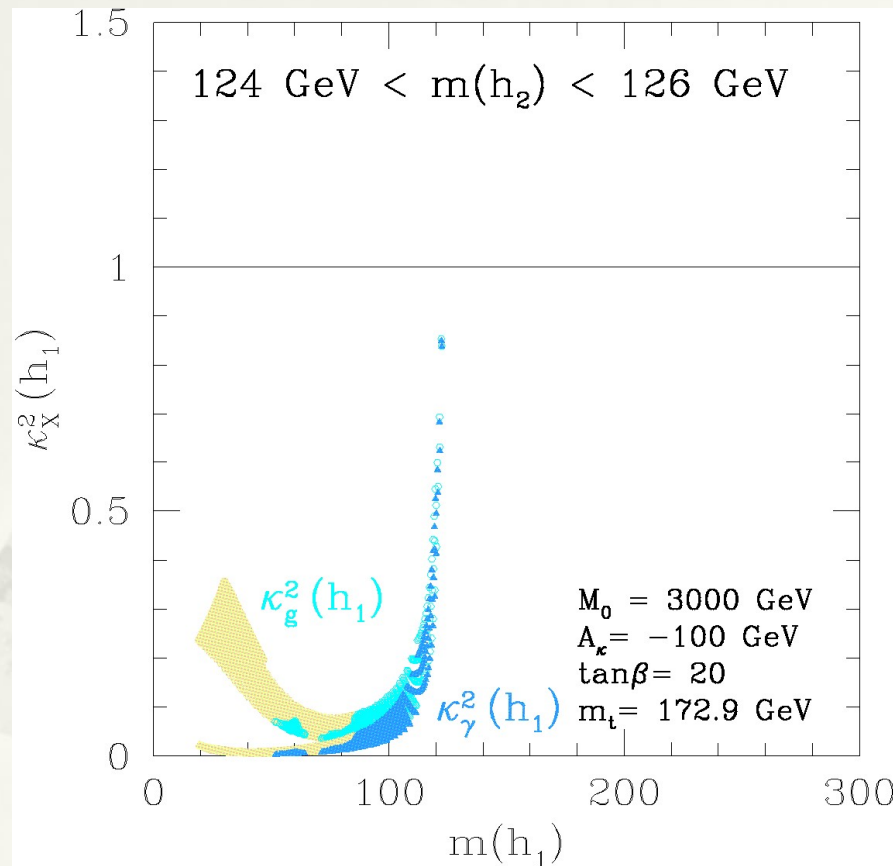
$\kappa_{t,V}$  comes from singlet-doublet mixing.  
 $\kappa_b$  is enhanced by  $\tan \beta$ .

# CP even Higgs (cont'd)



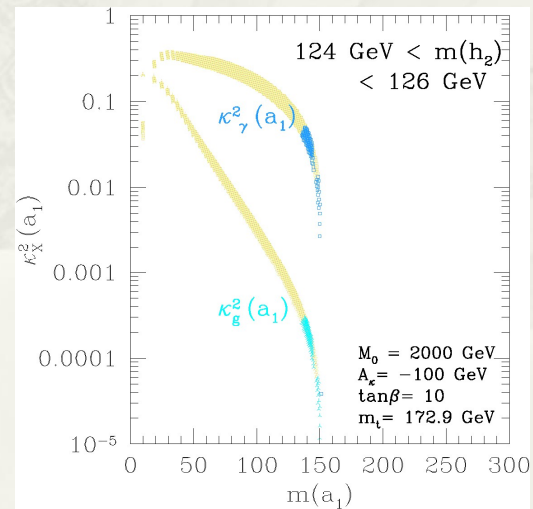
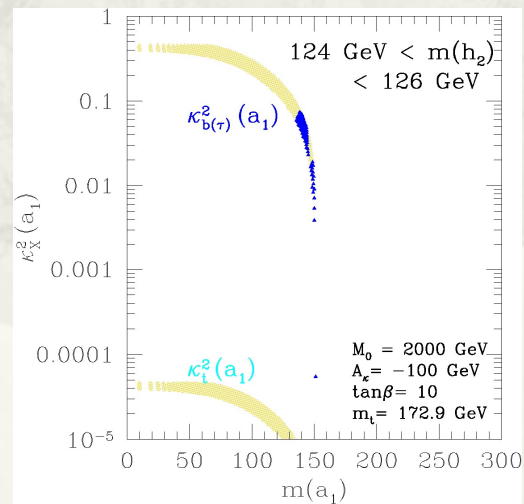
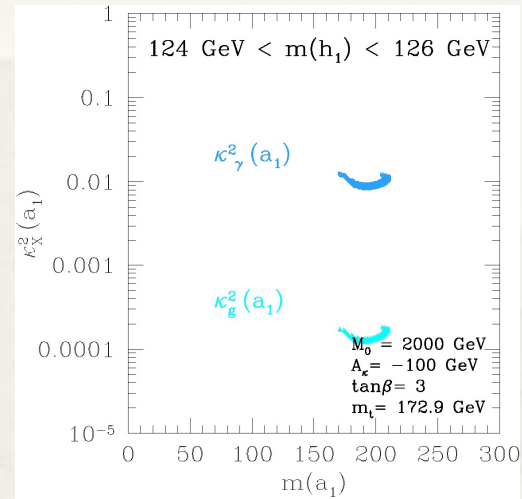
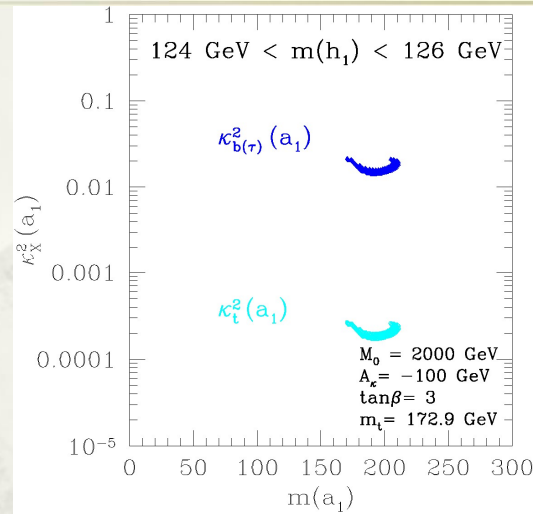


# CP even Higgs (cont'd)



It is important to find a signal  
LEP has missed

# CP odd Higgs



# Conclusion

- \* TeV scale mirage mediation in NMSSM is an attractive model.
- \* 125 GeV Higgs can be accommodated.
- \* Fine-tuning is better than 10% with 1.5 TeV stop while  $\mu$  can be as heavy as 700 GeV.
- \* Singlet-doublet mixing is suppressed due to accidental scale symmetries.
- \* 10% deviation is expected in SM-like Higgs coupling. 40% deviation is possible for  $b$  ( $\tau$ ).
- \* Hidden light singlets are characteristic and interesting targets for future colliders