

# EFT fit on top quark EW couplings

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## Acknowledging input/contributions from:

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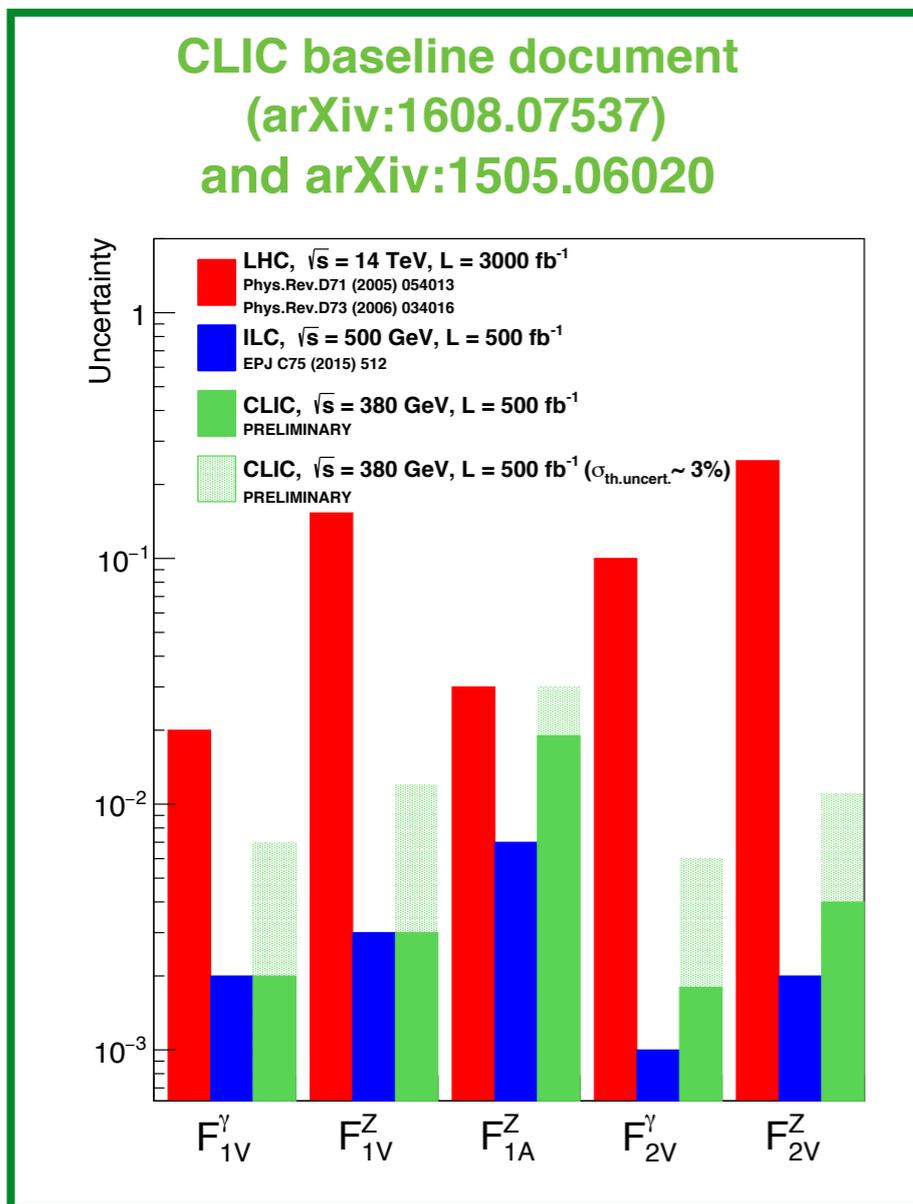
R. Pöschl, F. Richard (Orsay, LAL)

# **Introduction**

# Top quark couplings: form factors

**Objective:** to study the potential of a global fit in the top EW sector.

**Form-factors**  $\Gamma_{\mu}^{t\bar{t}X}(k^2, q, \bar{q}) = ie \left\{ \underbrace{\gamma_{\mu} (F_{1V}^X(k^2) + \gamma_5 F_{1A}^X(k^2))}_{\text{CP Conserving}} - \frac{\sigma_{\mu\nu}}{2m_t} (q + \bar{q})^{\nu} \left( \underbrace{iF_{2V}^X(k^2)}_{\text{CPV}} + \gamma_5 \underbrace{F_{2A}^X(k^2)}_{\text{CPV}} \right) \right\}$



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## CP-violating top quark couplings at future linear $e^+e^-$ colliders

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**Abstract** We study the potential of future lepton colliders to probe top quark sector. In certain extensions of the Standard Model, such as sizeable anomalous top quark dipole moments can arise, that may be probed in top quark pair production. We present results from detailed Monte Carlo simulations for the HL-LHC and CLIC at 380 GeV and use parton-level simulations to explore the sensitivity of these colliders to detect Higgs-boson-induced anomalous top quark couplings. We find that precise measurements in  $e^+e^- \rightarrow t\bar{t}$  production with s-channel Higgs production can provide sufficient sensitivity to detect Higgs-boson-induced anomalous top quark couplings. The potential of a linear  $e^+e^-$  collider to detect CP factors of the top quark exceeds the prospects of the HL-LHC by a factor of 10.

**Keywords** CP violation · top physics ·  $e^+e^-$  collider

Parameter	HL-LHC (red)	ILC initial (purple)	ILC nominal (blue)	CLIC initial (green)	CLIC (dark green)
$\text{Re}[F_{2A}^Y]$	~0.12	~0.005	~0.002	~0.015	~0.003
$\text{Re}[F_{2A}^Z]$	~0.25	~0.007	~0.003	~0.02	~0.003
$\text{Im}[F_{2A}^Y]$	~0.12	~0.005	~0.002	~0.015	~0.003
$\text{Im}[F_{2A}^Z]$	~0.25	~0.01	~0.004	~0.03	~0.009

# Top quark couplings: EFT

## Effective Field Theory

$$\mathcal{L}_{eff} = \mathcal{L}_{SM} + \frac{1}{\Lambda^2} \sum_i C_i O_i + \mathcal{O}(\Lambda^{-4})$$

### dim-6 operators

$$O_{\varphi q}^1 \equiv \frac{y_t^2}{2} \bar{q} \gamma^\mu q \varphi^\dagger i \overleftrightarrow{D}_\mu \varphi$$

$$O_{\varphi q}^3 \equiv \frac{y_t^2}{2} \bar{q} \tau^I \gamma^\mu q \varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi$$

$$O_{\varphi u} \equiv \frac{y_t^2}{2} \bar{u} \gamma^\mu u \varphi^\dagger i \overleftrightarrow{D}_\mu \varphi$$

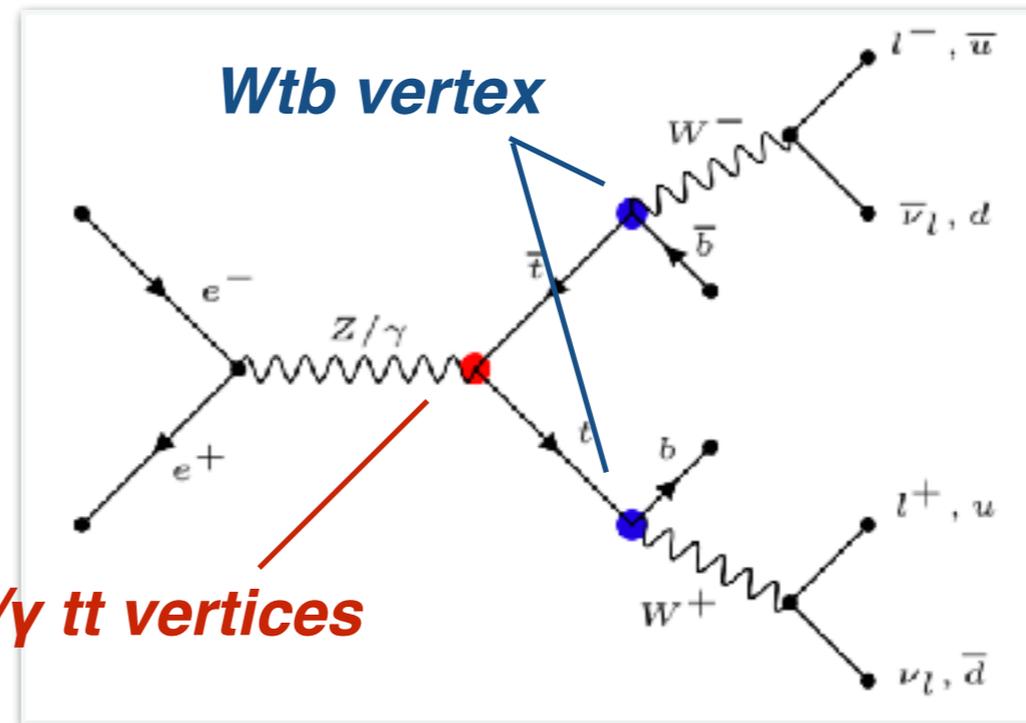
$$O_{\varphi ud} \equiv \frac{y_t^2}{2} \bar{u} \gamma^\mu d \varphi^T \epsilon i D_\mu \varphi$$

$$O_{uG} \equiv y_t g_s \bar{q} \tau^A \sigma^{\mu\nu} u \epsilon \varphi^* G_{\mu\nu}^A$$

$$O_{uW} \equiv y_t g_W \bar{q} \tau^I \sigma^{\mu\nu} u \epsilon \varphi^* W_{\mu\nu}^I$$

$$O_{dW} \equiv y_t g_W \bar{q} \tau^I \sigma^{\mu\nu} d \epsilon \varphi^* W_{\mu\nu}^I$$

$$O_{uB} \equiv y_t g_Y \bar{q} \sigma^{\mu\nu} u \epsilon \varphi^* B_{\mu\nu}$$



### Contact interactions

$$O_{lq}^1 \equiv \bar{q} \gamma_\mu q \bar{l} \gamma^\mu l$$

$$O_{lq}^3 \equiv \bar{q} \tau^I \gamma_\mu q \bar{l} \tau^I \gamma^\mu l$$

$$O_{lu} \equiv \bar{u} \gamma_\mu u \bar{l} \gamma^\mu l$$

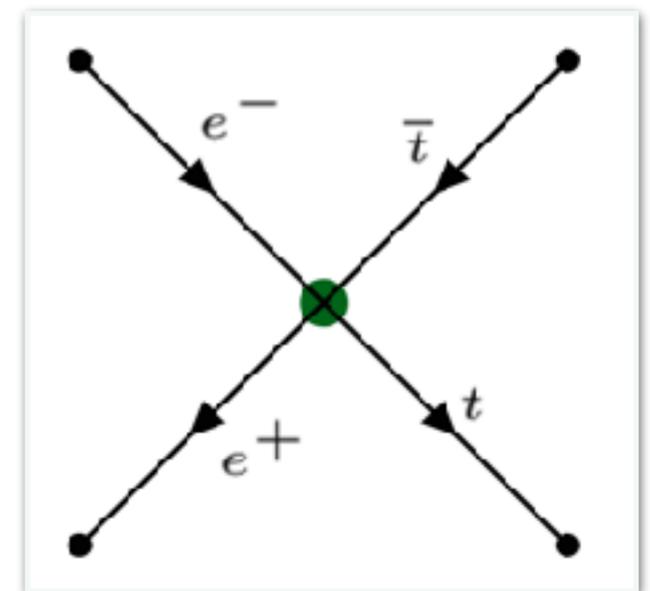
$$O_{eq} \equiv \bar{q} \gamma_\mu q \bar{e} \gamma^\mu e$$

$$O_{eu} \equiv \bar{u} \gamma_\mu u \bar{e} \gamma^\mu e$$

$$O_{lequ}^T \equiv \bar{q} \sigma^{\mu\nu} u \epsilon \bar{l} \sigma_{\mu\nu} e$$

$$O_{lequ}^S \equiv \bar{q} u \epsilon \bar{l} e$$

$$O_{ledq} \equiv \bar{d} q \bar{l} e$$



# Different EFT basis

## Transformation between effective operators and form-factors:

$$\begin{aligned}
 F_{1,V}^Z - F_{1,V}^{Z,SM} &= \frac{1}{2} \left( \underline{C_{\varphi Q}^{(3)}} - \underline{C_{\varphi Q}^{(1)}} - C_{\varphi t} \right) \frac{m_t^2}{\Lambda^2 s_W c_W} = -\frac{1}{2} \underline{C_{\varphi q}^V} \frac{m_t^2}{\Lambda^2 s_W c_W} \\
 F_{1,A}^Z - F_{1,A}^{Z,SM} &= \frac{1}{2} \left( -\underline{C_{\varphi Q}^{(3)}} + \underline{C_{\varphi Q}^{(1)}} - C_{\varphi t} \right) \frac{m_t^2}{\Lambda^2 s_W c_W} = -\frac{1}{2} \underline{C_{\varphi q}^A} \frac{m_t^2}{\Lambda^2 s_W c_W} \\
 F_{2,V}^Z &= \left( \underline{\text{Re}\{C_{tW}\} c_W^2 - \text{Re}\{C_{tB}\} s_W^2} \right) \frac{4m_t^2}{\Lambda^2 s_W c_W} = \underline{\text{Re}\{C_{uZ}\}} \frac{4m_t^2}{\Lambda^2} \\
 F_{2,V}^\gamma &= \left( \underline{\text{Re}\{C_{tW}\} + \text{Re}\{C_{tB}\}} \right) \frac{4m_t^2}{\Lambda^2} = \underline{\text{Re}\{C_{uA}\}} \frac{4m_t^2}{\Lambda^2} \\
 [F_{2,A}^Z, F_{2,A}^\gamma] &\propto \underline{[\text{Im}\{C_{tW}\}, \text{Im}\{C_{tB}\}]}
 \end{aligned}$$

We can change to an alternative basis  
(**Vector/Axial - Vector**)

**10 operators** in the global fit:

- 4 CP-conserving ttX vertices
- 2 CP-violating ttX vertices
- 4 contact interactions

## Conversion to V/A - V basis in contact interactions:

$$\begin{aligned}
 C_{lq}^V &\equiv C_{lu} + C_{lq}^{(1)} - C_{lq}^{(3)} & C_{eq}^V &\equiv C_{eu} + C_{eq} \\
 C_{lq}^A &\equiv C_{lu} - C_{lq}^{(1)} + C_{lq}^{(3)} & C_{eq}^A &\equiv C_{eu} - C_{eq}
 \end{aligned}$$

# Observables

# Observables sensitivity: $A_{\text{FB}}$ + cross-section

$e^+e^- \rightarrow t\bar{t}$ , LO

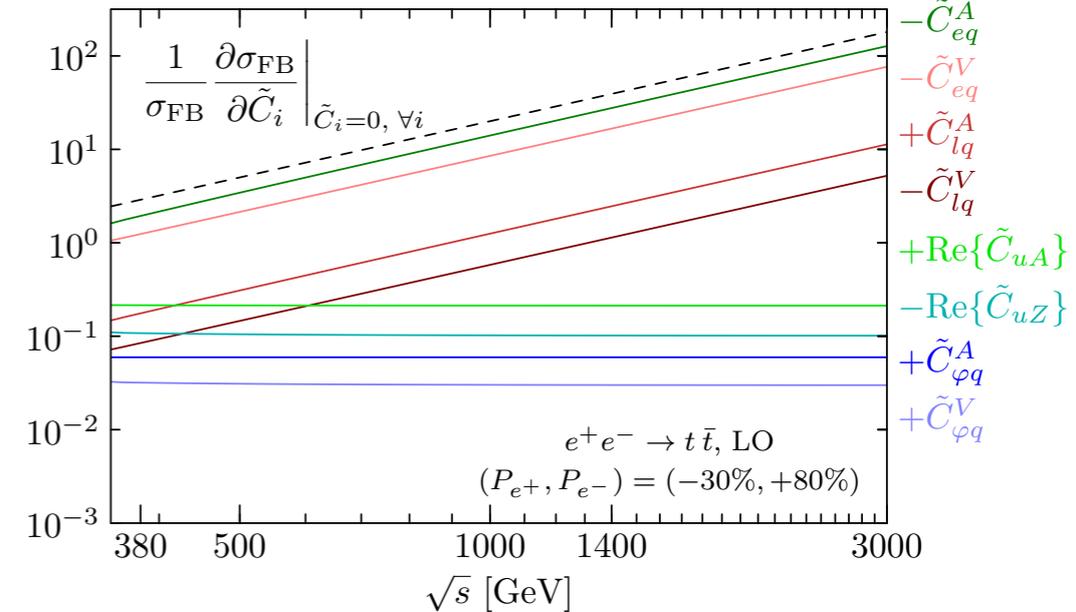
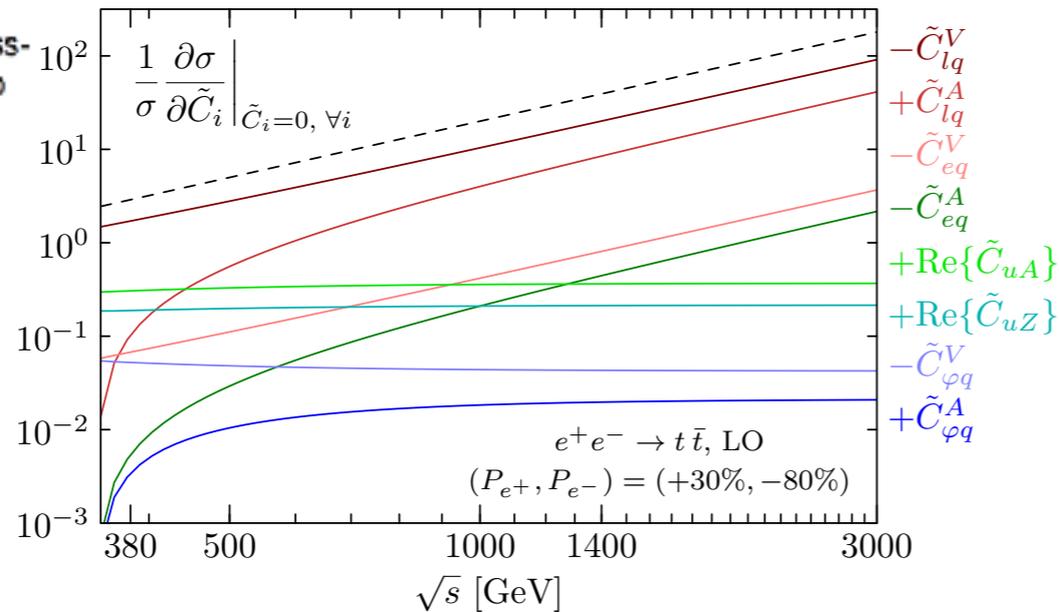
Durieux, Perelló, Vos, Zhang, to be published

Cross-section

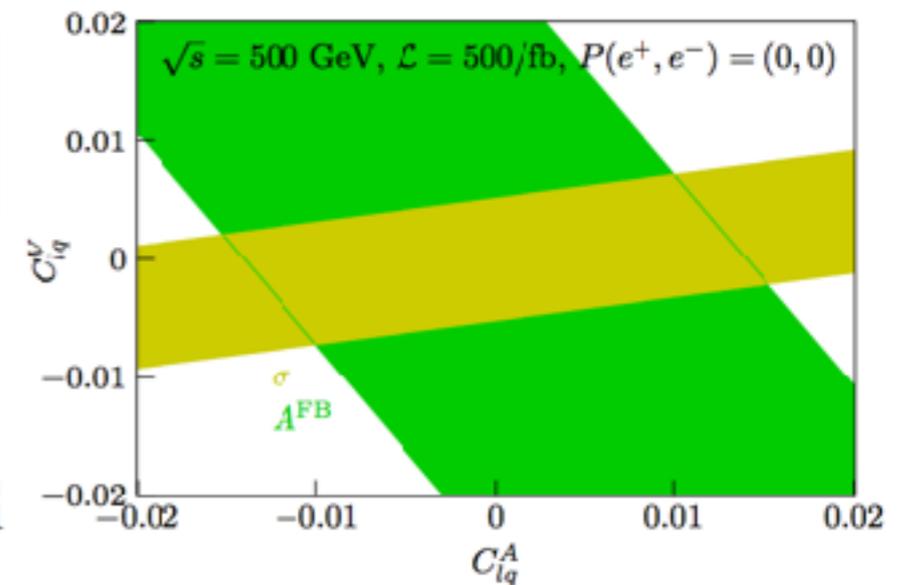
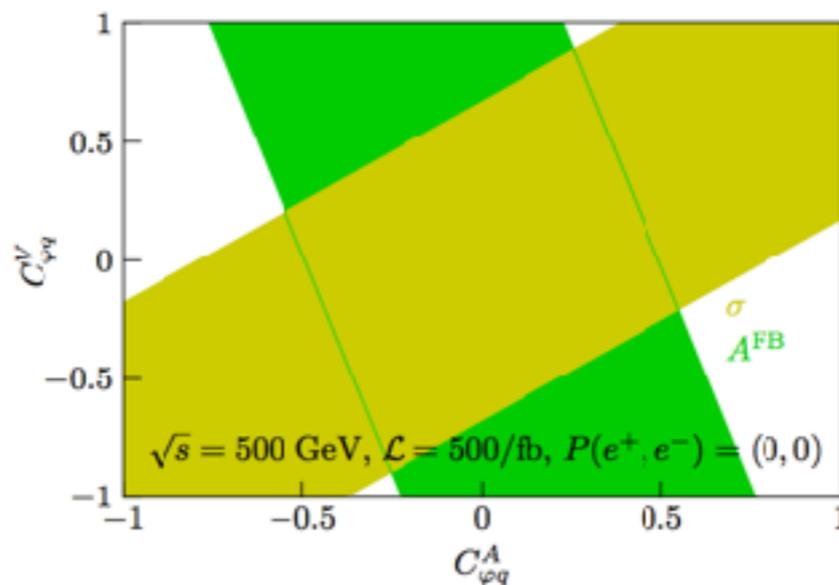
Forward-backward asymmetry

**Sensitivity:**

Relative change in cross-section due to non-zero operator coefficient  
 $\Delta\sigma(C)/\sigma/\Delta C$



Nice complementarity between Afb and cross-section to **disentangle** vector and axial operators.



# Observables sensitivity: $A_{\text{FB}}$ + cross-section

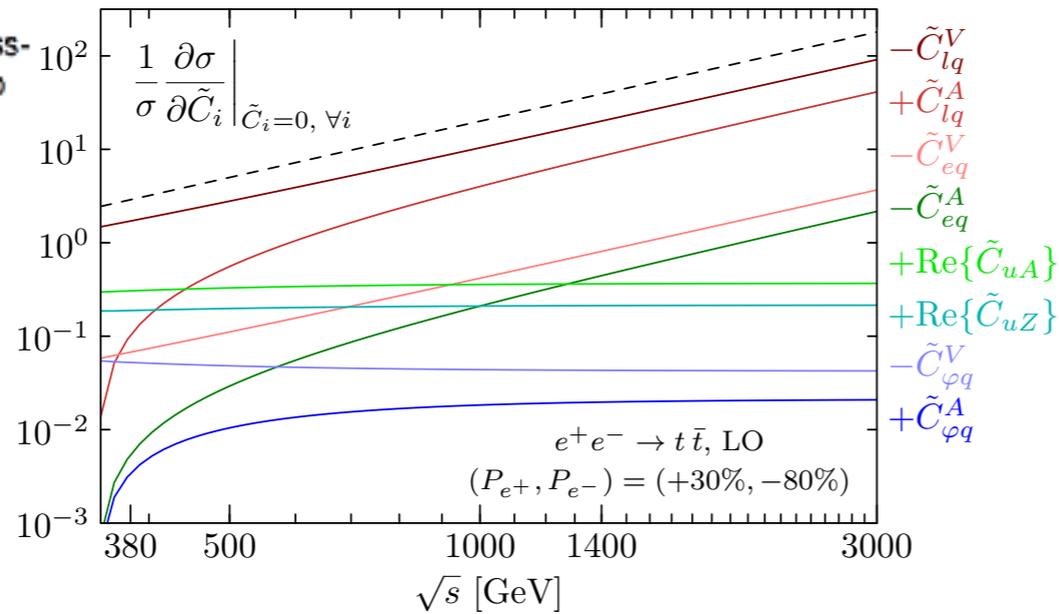
$e^+e^- \rightarrow t\bar{t}$ , LO

Durieux, Perelló, Vos, Zhang, to be published

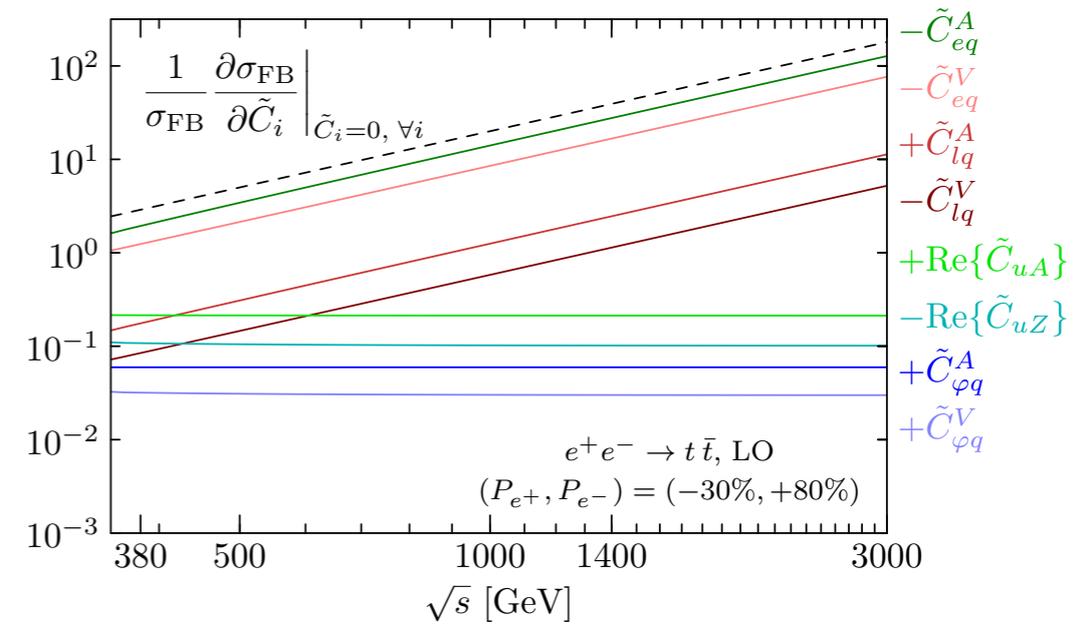
Cross-section

**Sensitivity:**

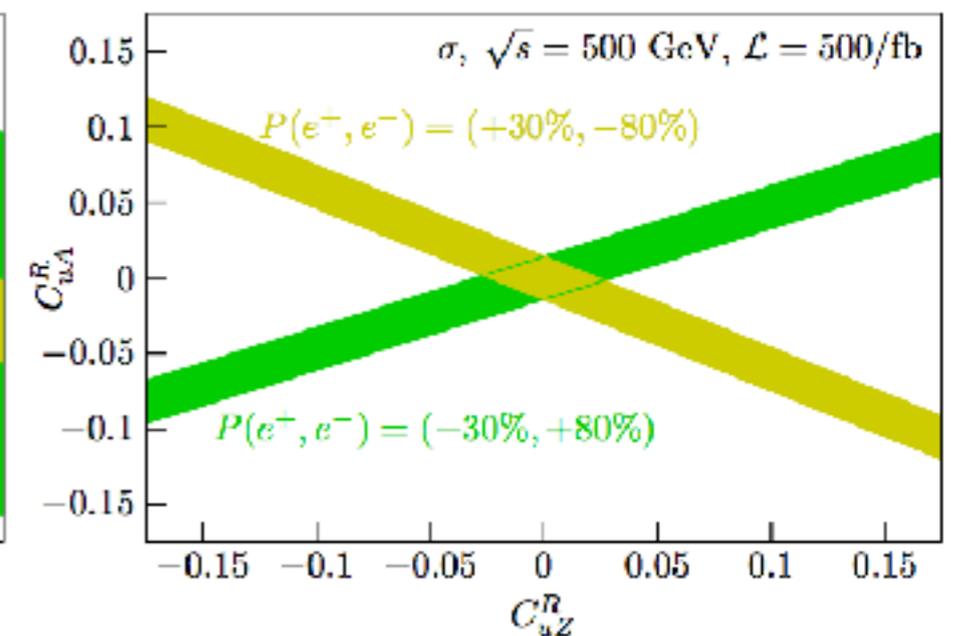
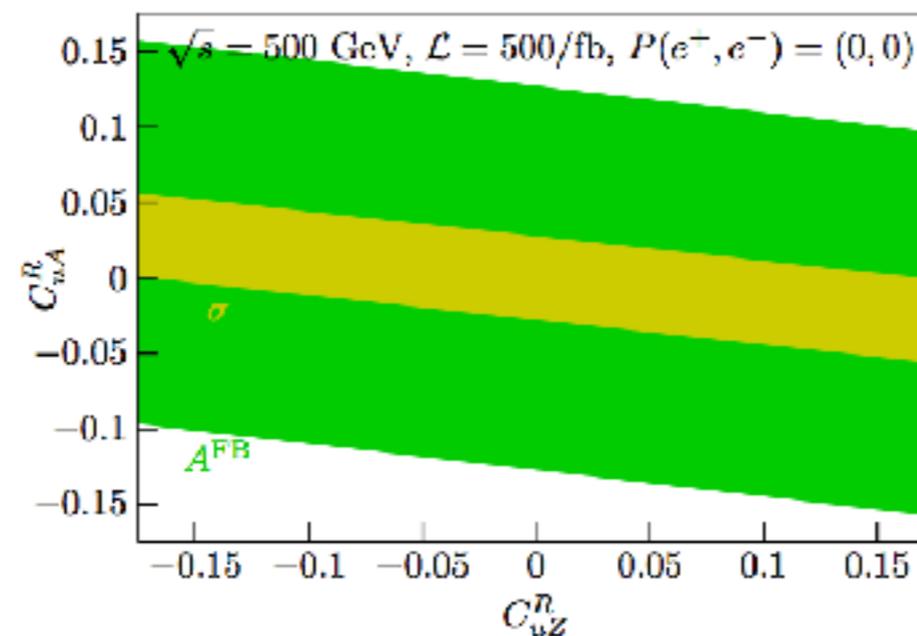
Relative change in cross-section due to non-zero operator coefficient  
 $\Delta\sigma(C)/\sigma/\Delta C$



Forward-backward asymmetry



Role of beams polarization:



# Observables sensitivity: $A_{FB}$ + cross-section

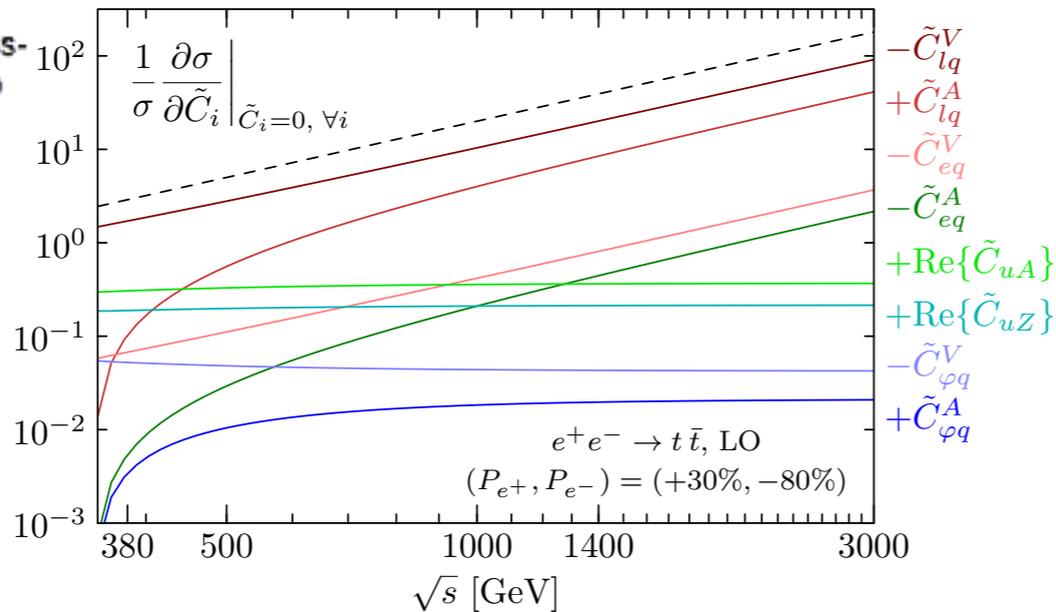
$$e^+e^- \rightarrow t\bar{t}, \text{ LO}$$

Durieux, Perelló, Vos, Zhang, to be published

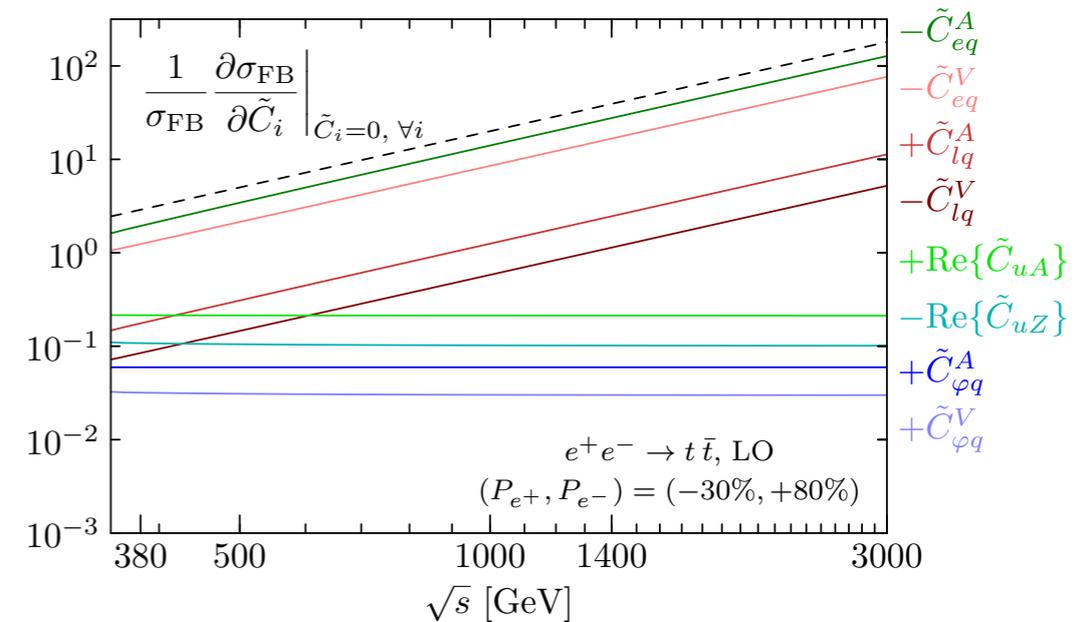
Cross-section

**Sensitivity:**

Relative change in cross-section due to non-zero operator coefficient  
 $\Delta\sigma(C)/\sigma/\Delta C$



Forward-backward asymmetry

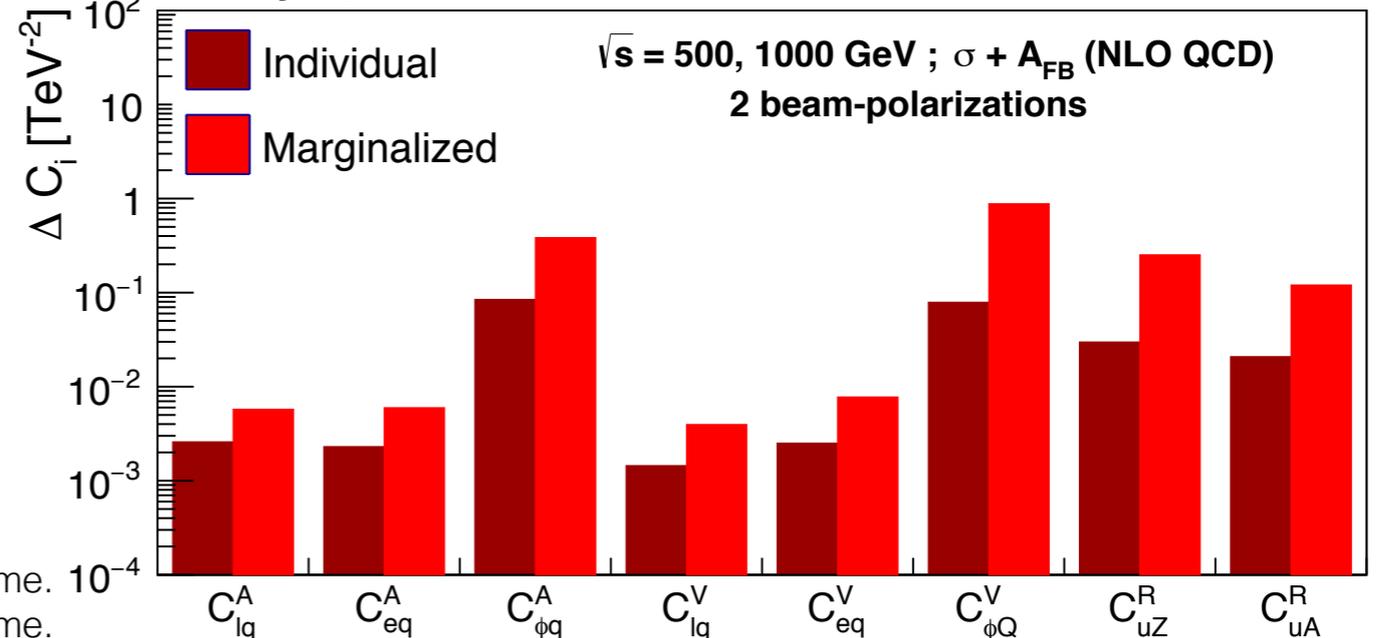


Nothing can be done with only one energy point!

- At least we need **one low energy with high statistics for the vertices**, and **one high energy for the contact interactions**.

**Need for new observables** to reduce the difference between individual and marginalized fits

Theory fit, no full-simulation included.



**Individual:** assuming variation in only 1 parameter each time.

**Marginalized:** assuming variation in all the parameters at the same time.

The **CP-violating effects** in  $e^+e^- \rightarrow t\bar{t}$  manifest themselves in specific **top-spin effects**, namely **CP-odd top spin-momentum correlations and  $t\bar{t}$  spin correlations**.

$$e^+(\mathbf{p}_+, P_{e^+}) + e^-(\mathbf{p}_-, P_{e^-}) \rightarrow t(\mathbf{k}_t) + \bar{t}(\mathbf{k}_{\bar{t}})$$

$$t \bar{t} \rightarrow \ell^+(\mathbf{q}_+) + \nu_\ell + b + \bar{X}_{\text{had}}(\mathbf{q}_{\bar{X}})$$

$$t \bar{t} \rightarrow X_{\text{had}}(\mathbf{q}_X) + \ell^-(\mathbf{q}_-) + \bar{\nu}_\ell + \bar{b}$$

- **CP-odd observables** are defined with the **four momenta available in  $t\bar{t}$  semi-leptonic decay channel**

$$\mathcal{O}_+^{\text{Re}} = (\hat{\mathbf{q}}_{\bar{X}} \times \hat{\mathbf{q}}_+^*) \cdot \hat{\mathbf{p}}_+,$$

$$\mathcal{O}_+^{\text{Im}} = -\left[1 + \left(\frac{\sqrt{s}}{2m_t} - 1\right)(\hat{\mathbf{q}}_{\bar{X}} \cdot \hat{\mathbf{p}}_+)^2\right] \hat{\mathbf{q}}_+^* \cdot \hat{\mathbf{q}}_{\bar{X}} + \frac{\sqrt{s}}{2m_t} \hat{\mathbf{q}}_{\bar{X}} \cdot \hat{\mathbf{p}}_+ \hat{\mathbf{q}}_+^* \cdot \hat{\mathbf{p}}_+$$

- The way to **extract** the **CP-violating form factor** is to construct **asymmetries sensitive to CP-violation effects**

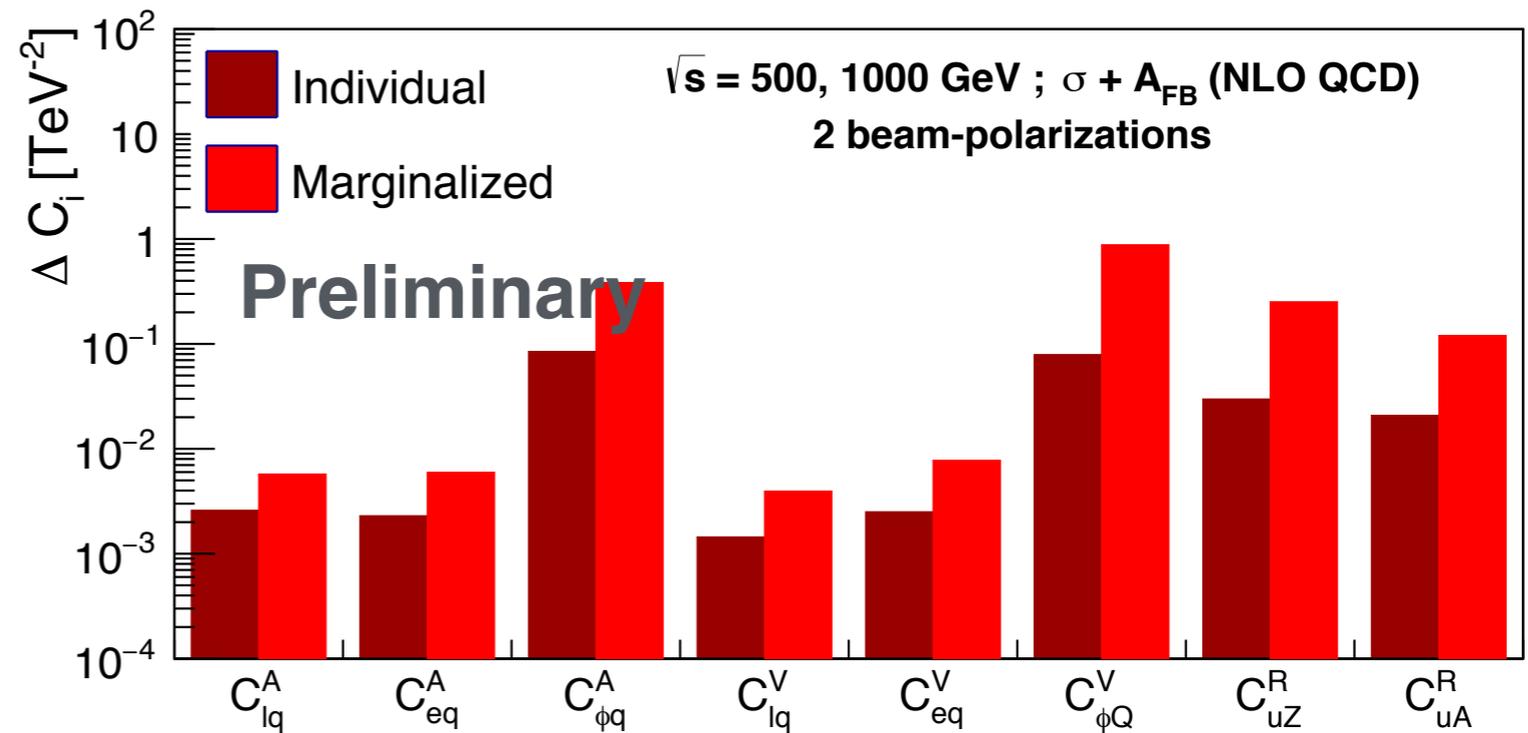
$$\mathcal{A}^{\text{Re}} = \langle \mathcal{O}_+^{\text{Re}} \rangle - \langle \mathcal{O}_-^{\text{Re}} \rangle = c_\gamma(s) \text{Re}F_{2A}^\gamma + c_Z(s) \text{Re}F_{2A}^Z$$

$$\mathcal{A}^{\text{Im}} = \langle \mathcal{O}_+^{\text{Im}} \rangle - \langle \mathcal{O}_-^{\text{Im}} \rangle = \tilde{c}_\gamma(s) \text{Im}F_{2A}^\gamma + \tilde{c}_Z(s) \text{Im}F_{2A}^Z$$

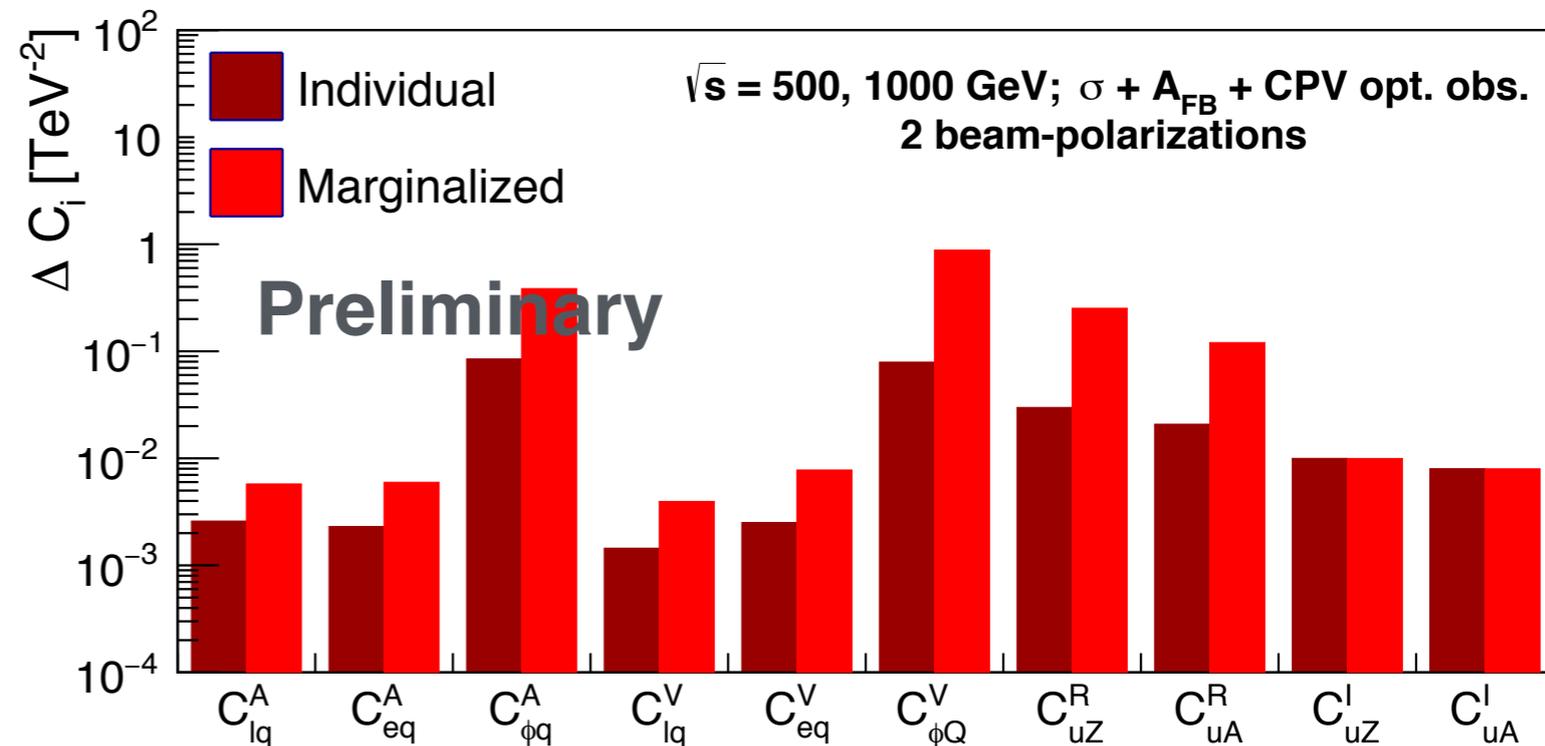
$$\begin{array}{cc} \mathcal{A}_{\gamma,Z}^{\text{Re L}} & \mathcal{A}_{\gamma,Z}^{\text{Re L}} \\ \mathcal{A}_{\gamma,Z}^{\text{Im R}} & \mathcal{A}_{\gamma,Z}^{\text{Im R}} \end{array}$$

**Including CPV observables in the EFT global fit doesn't solve the problem**

**We still need to improve the marginalized fit**



Theory fit, no full-simulation included.



**Individual:** assuming variation in only 1 parameter each time.

**Marginalized:** assuming variation in all the parameters at the same time.

# Statistically optimal observables

G. Durieux @TopLC 2017:

<https://indico.cern.ch/event/595651/contributions/2573918/>

## Statistically optimal observables

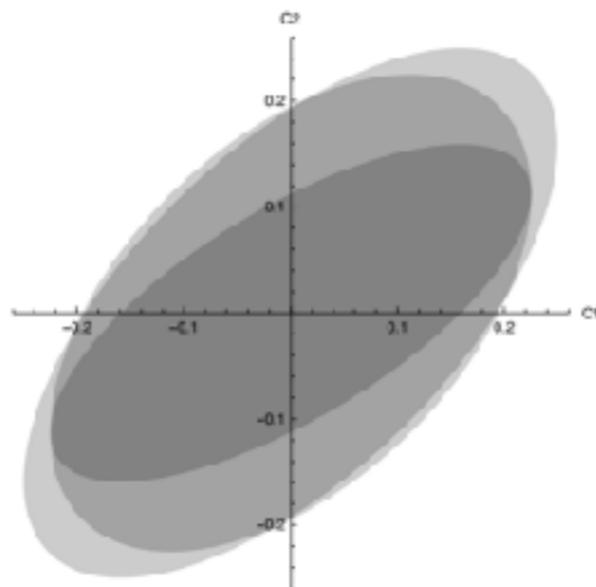
[Atwood, Soni '92]

[Diehl, Nachtmann '94]

minimize the one-sigma ellipsoid in EFT parameter space.

(joint efficient set of estimators, saturating the Rao-Cramér-Fréchet bound:  $V^{-1} = I$ )

For small  $C_i$ , with a phase-space distribution  $\sigma(\Phi) = \sigma_0(\Phi) + \sum_i C_i \sigma_i(\Phi)$ ,  
the statistically optimal set of observables is:  $O_i(\Phi) = \sigma_i(\Phi)/\sigma_0(\Phi)$ .



e.g.  $\sigma(\phi) = 1 + \cos(\phi) + C_1 \sin(\phi) + C_2 \sin(2\phi)$

1. asymmetries:  $O_i \sim \text{sign}\{\sin(i\phi)\}$

2. moments:  $O_i \sim \sin(i\phi)$

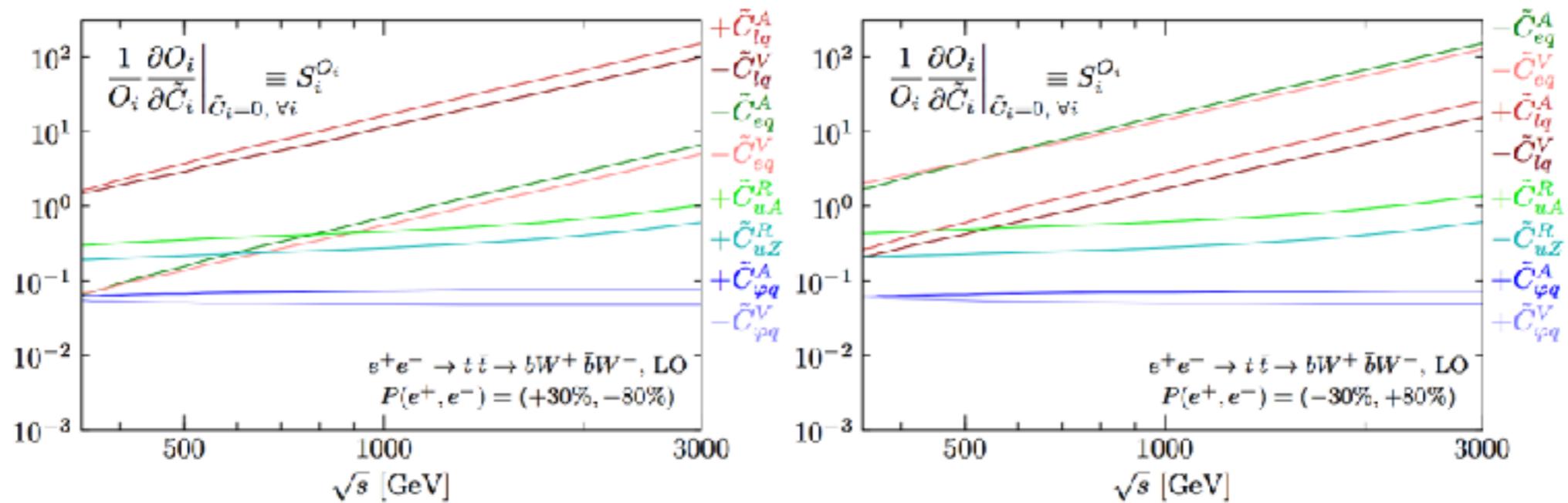
3. statistically optimal:  $O_i \sim \frac{\sin(i\phi)}{1 + \cos \phi}$

$\Rightarrow$  area ratios 1.9 : 1.7 : 1

Previous applications in  $e^+e^- \rightarrow t\bar{t}$ :

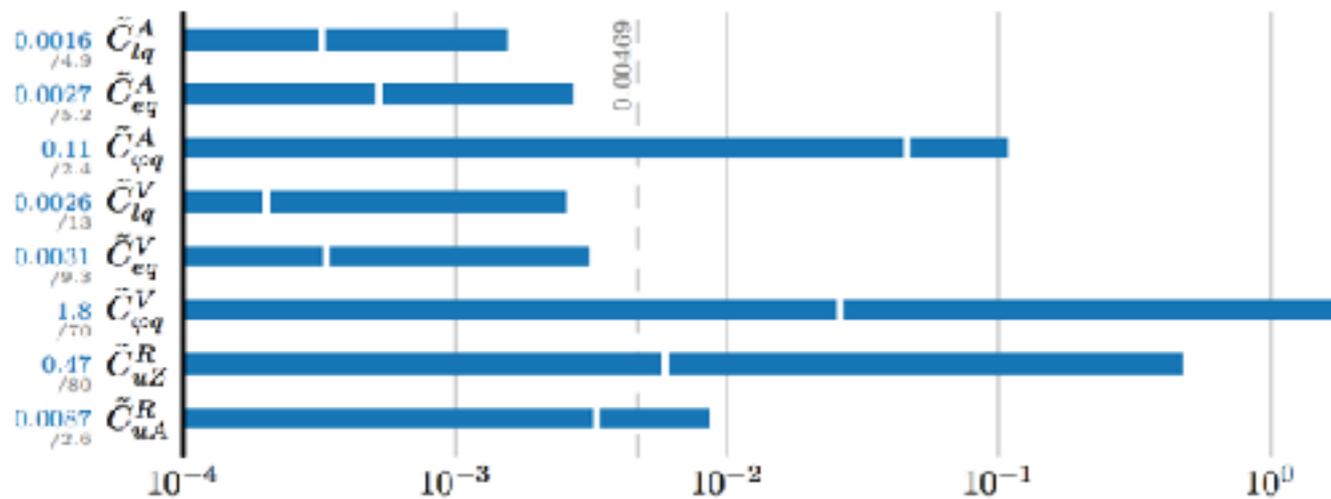
[Grzadkowski, Hioki '00] [Janot '15] [Khiem et al '15]

# Statistically optimal observables sensitivities

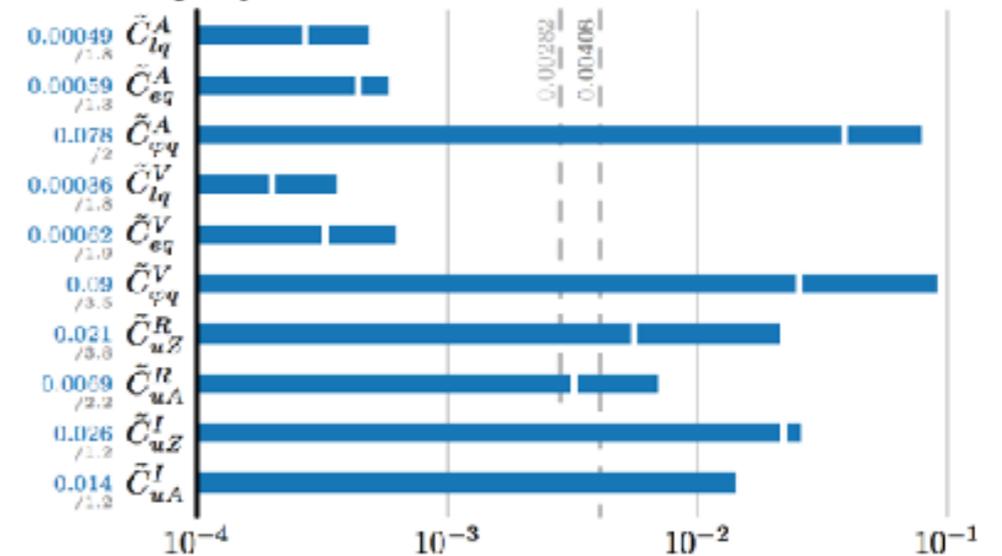


Comparison in the global limits (500GeV + 1TeV for 2 pols.):

$\sigma + A_{FB}$



Statistically optimal observables:

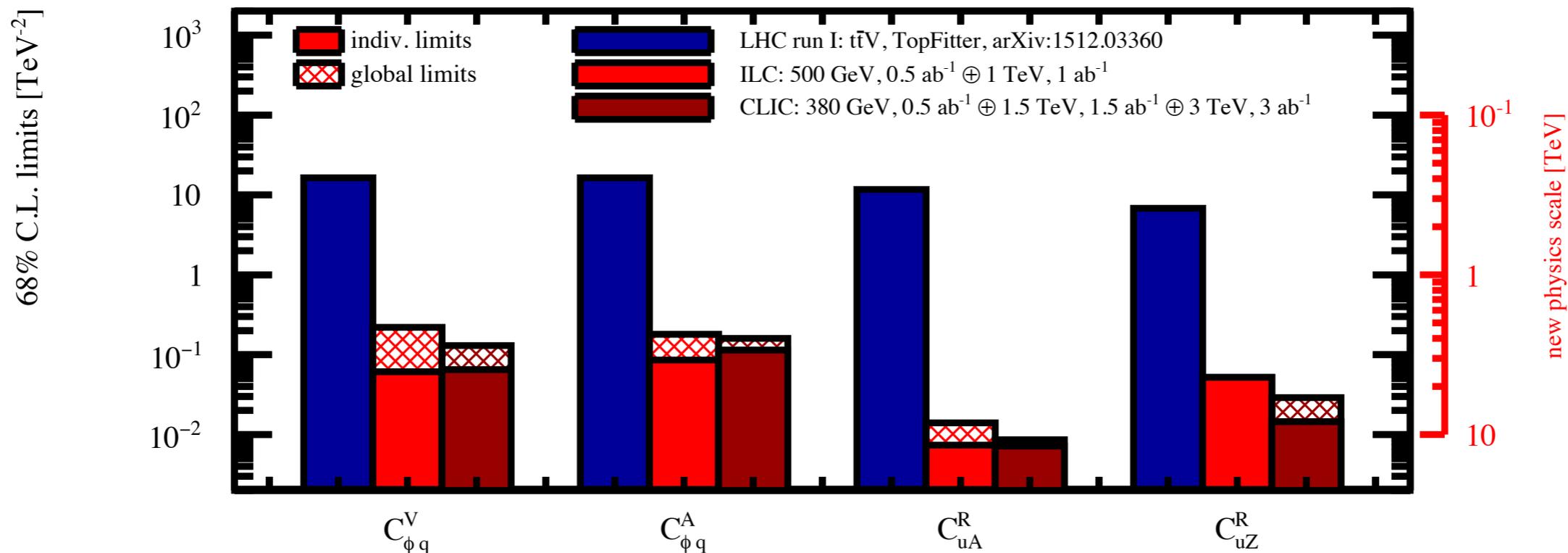


- Even better individual limits
- Global limits within a factor 1.3 to 3.5

# **Comparison with the LHC**

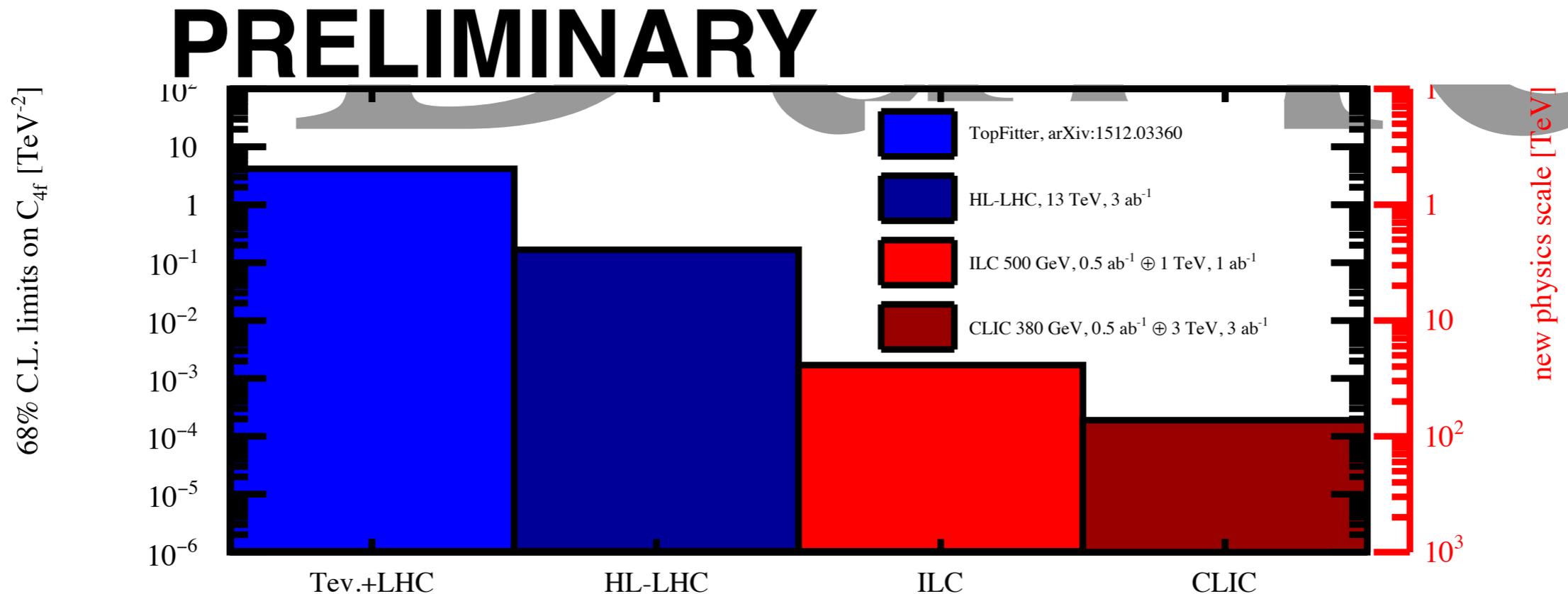
# Comparison with the LHC: vertices

## PRELIMINARY



- Still **preliminary**, final results for ILC still coming.
- Limits between 2 and 3 orders of magnitude better than LHC.
- LHC limits could improve in future stages, but not prospects of this possible improvement at the moment.

# Comparison with the LHC: contact interactions



- Still **preliminary**, final results for ILC still coming.
- Top-philic scenario allows for a comparison between  $q\bar{q}t\bar{t}$  and  $e\bar{e}t\bar{t}$  contact interaction.
- LHC results could be improved using boosted measurements on (MP, Vos, arXiv:1512.07542), but even so couldn't surpass LC limits (3 - 4 orders of magnitude better at the moment).

# Conclusions

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- Cross-section +  $A_{FB}$  are not enough for global EFT fit.
- CP-odd operators well constrained by CP-odd optimal observables.
- Optimal observables seem to be the proper solution to the global fit.
- Results on the global fit ready for the CLICdp top quark paper.
- Preparing pheno paper including ILC scenario.

**Back up**

# **Full-simulation**

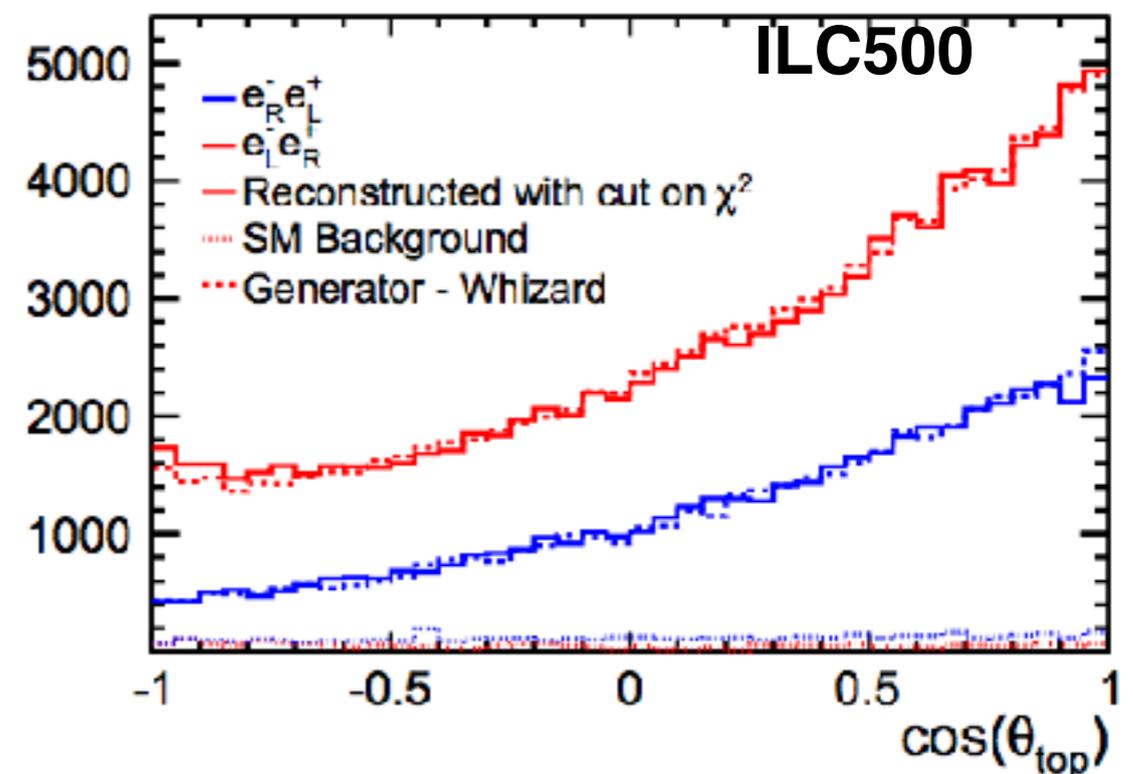
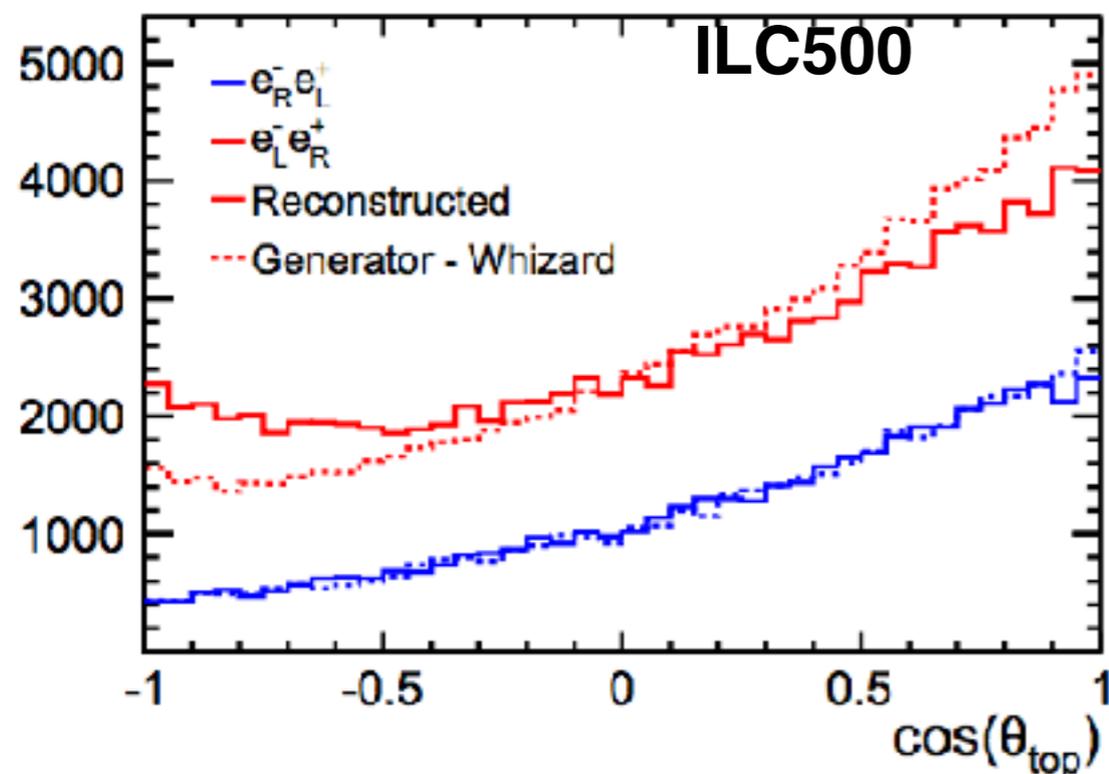
# Full-simulation: low energies

## Studies at CLIC380 and ILC500 included in I. Garcia thesis

(<https://cds.cern.ch/record/2239794?ln=en>)

- **Resolved analysis for a semileptonic  $t\bar{t}$  decay** - Production near threshold (lower effective centre-of-mass due to ISR, beamstrahlung), use b-tagging, search for W, or 3 jets with a combined invariant mass near  $m_t$

**Problem on migrations (bad W-b pairing) in some angular distributions, solved using a quality cut with the consequent penalty in efficiency.**



# Full-simulation: low energies

## Studies at CLIC380 and ILC500 included in I. Garcia thesis

(<https://cds.cern.ch/record/2239794?ln=en>)

- **Resolved analysis** - Production near threshold (lower effective centre-of-mass due to ISR, beamstrahlung), use b-tagging, search for W, or 3 jets with a combined invariant mass near  $m_t$

Results for CLIC380 have been revisited for the CLICdp top paper

### CLIC@380GeV L=500fb<sup>-1</sup>

$\sqrt{s}$	380 GeV <sup>a</sup>	
P(e <sup>-</sup> )	-80%	+80%
$\sigma_{t\bar{t}}$ [fb]	161.00	75.97
stat. unc. [fb]	1.04	0.75
$A_{FB}$	0.1761	0.206
stat. unc.	0.0090	0.0085

### ILC@500GeV L=500fb<sup>-1</sup> [arXiv:1505.06020]

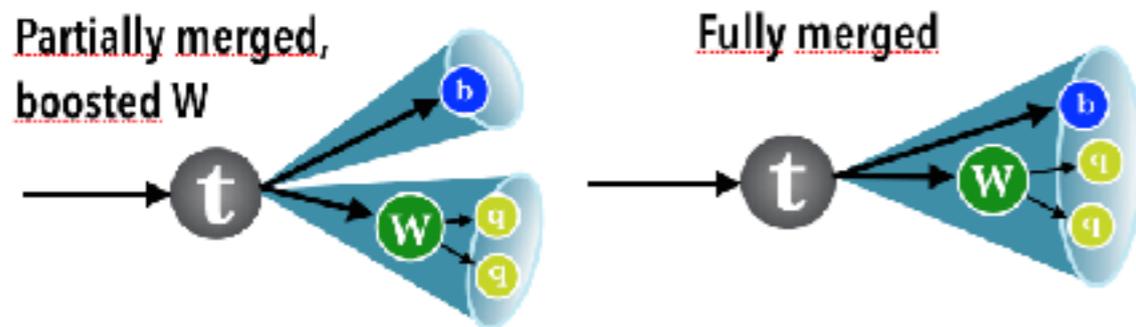
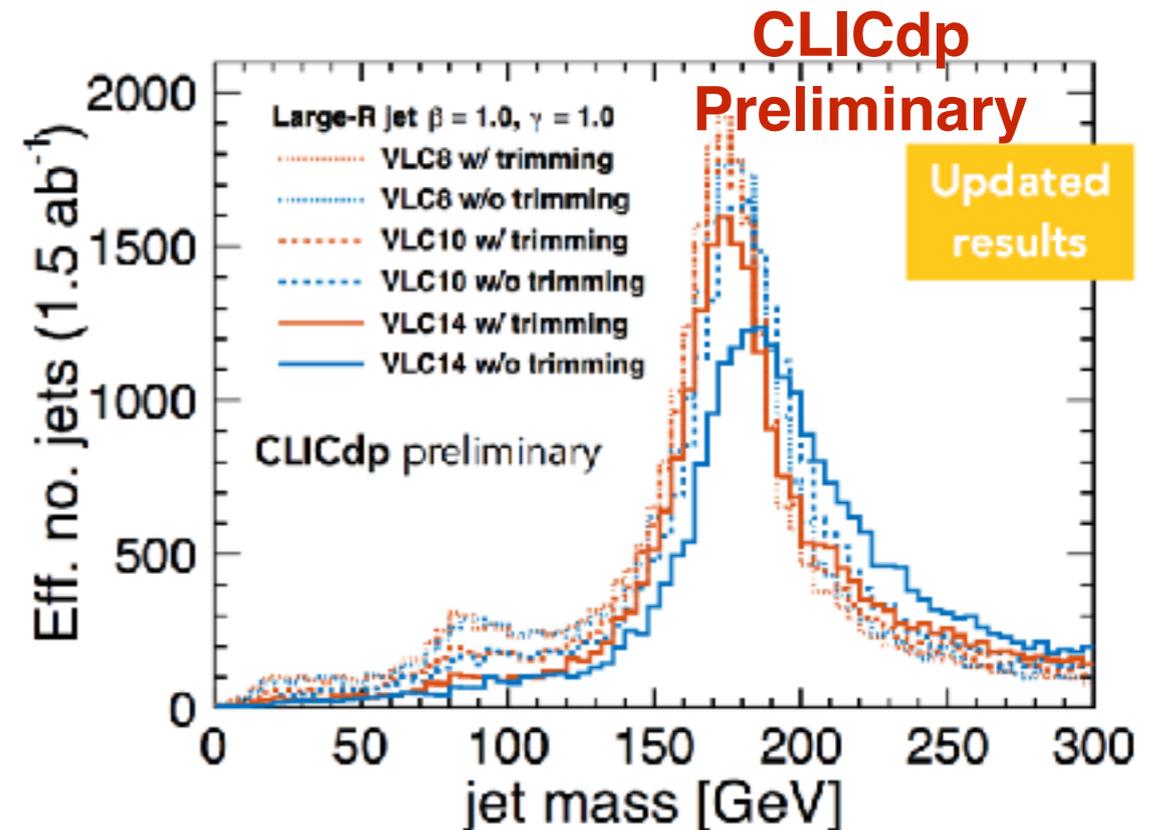
$\mathcal{P}_{e^-}, \mathcal{P}_{e^+}$	$(\delta\sigma/\sigma)_{\text{stat.}} (\%)$	$(\delta A_{FB}^t/A_{FB}^t)_{\text{stat.}} (\%)$
-0.8, +0.3	0.47	1.8
+0.8, -0.3	0.63	1.3

CLICdp Preliminary

# Full-simulation: high energies

- Collimated decay products - Identify and correctly assign the top decay products
- **Boosted analysis** - **Standard identification techniques may not work**: b-tagging not foreseen, tracks are very close to each other, W decay products not isolated from each other or b-jet,
  - Idea: tag tops by identifying prongy sub-structure

Optimization in jet clustering parameters  
Fully-hadronic decay mode reconstruction

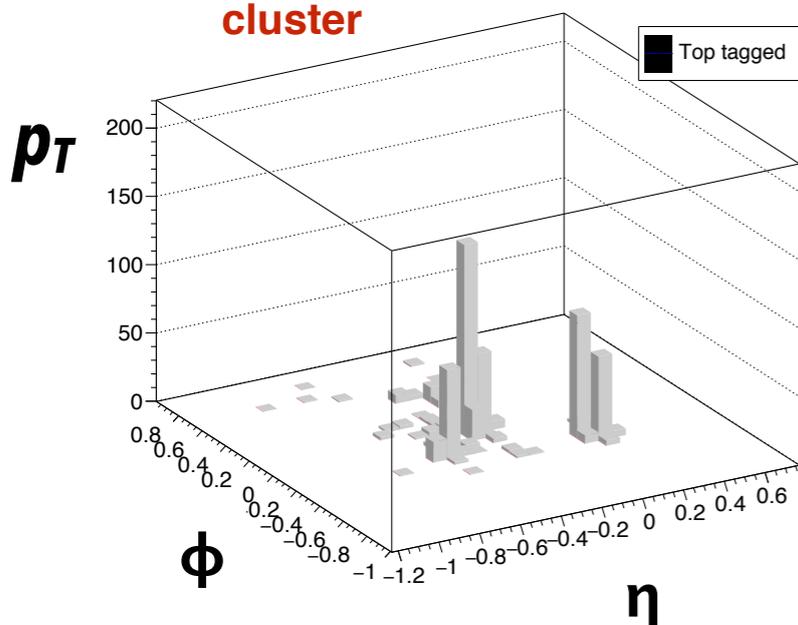


- Jet clustering (incl. trimming)
- 2 exclusive large-R jets
- Jet tagging:
  - Parsing sub-structure
  - Flavour-tagging (sub-jet, fat-jet)

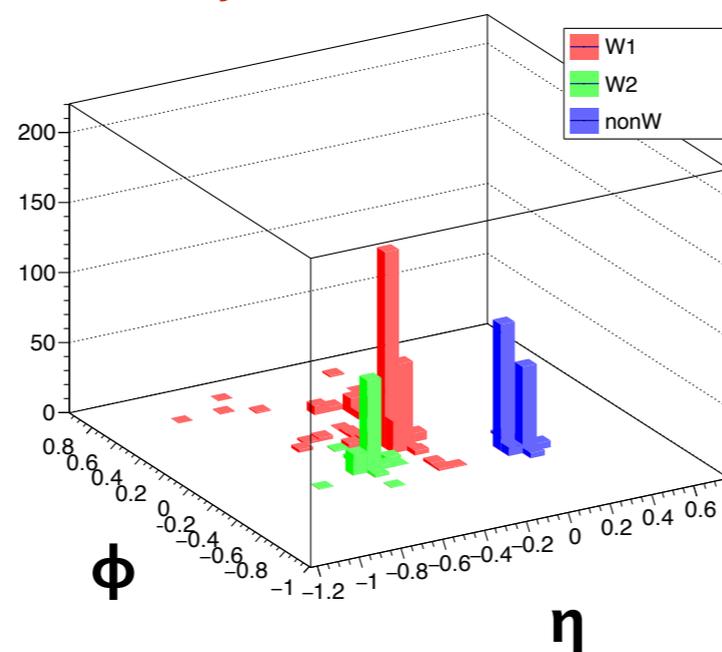
# Parsing sub-structure

Jet de-clustering (FastJet extension), DOI: 10.1103/PhysRevLett.101.142001

Parsing through jet cluster



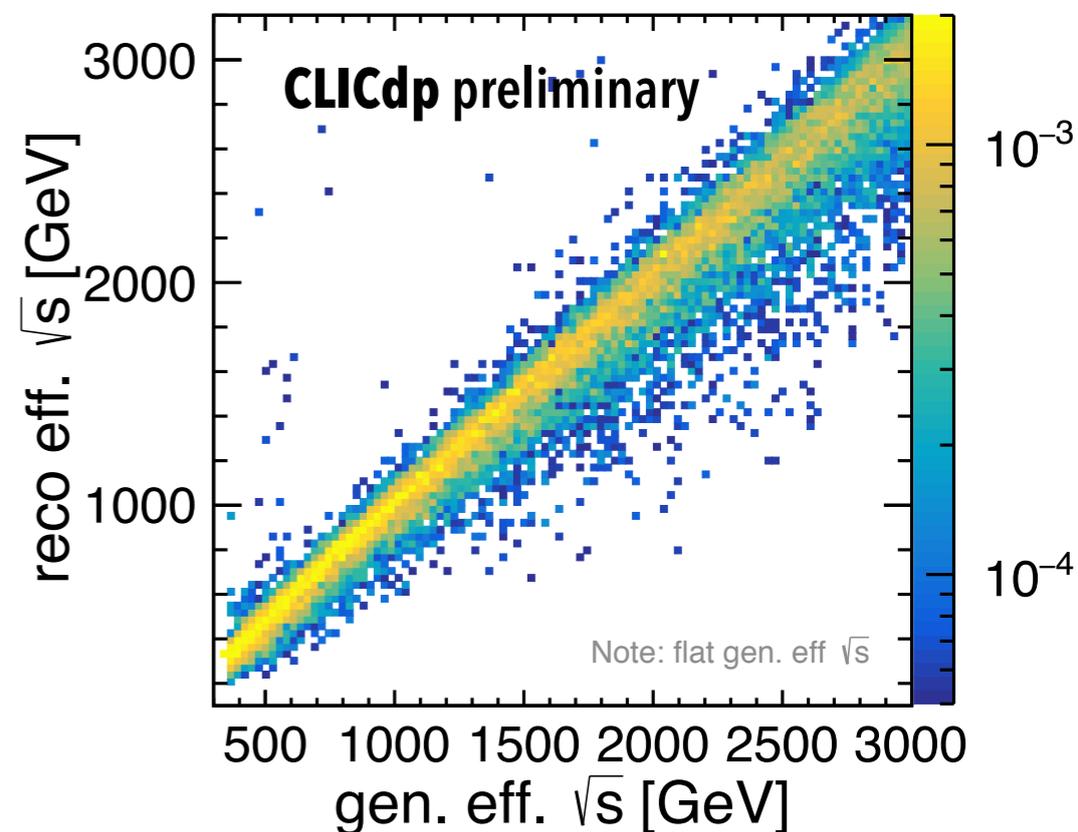
Three subjects identified



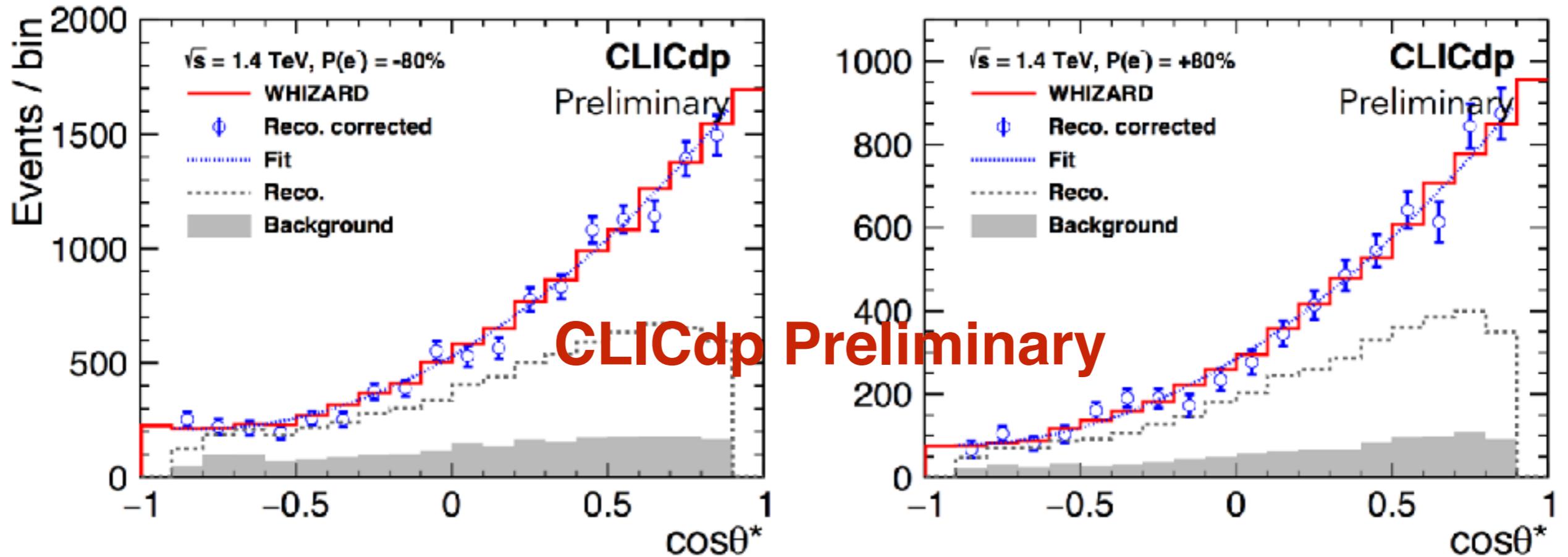
- VLC jet clustering algorithm ( $R=1.5$ ,  $\beta=1$ ,  $\gamma=1$ ) + trimming
- “JH Top Tagger”
- kinematic cuts ( $m_t \in [145, 205]$  GeV,  $m_W \in [65, 95]$  GeV)

## Event selection

- Technical cut (gen. level) in  $\sqrt{s}$  (same cut can be done at reconstruction level)
- 1 isolated lepton, 1 top tagged jet (“JH Top Tagger”)
- Flavour tagging (fat-jet / sub-jet)  $\rightarrow$  BDT
- Exploiting kinematics of semi-leptonic side  $\rightarrow$  BDT



# Full-simulation: high energies



*Numerical results will appear soon in the CLICdp top quark paper*

Some technical numbers at reconstruction  
<https://cds.cern.ch/record/2239794?ln=en>

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CLIC380 (Repository <https://twiki.cern.ch/twiki/bin/view/CLIC/MonteCarloSamplesForTopPhysics>)

- Jet clustering: VLC algorithm ( $R=1.6$ ,  $\beta = 0.8$ ,  $\gamma = 0.8$ ).

ILC500

- Jet clustering: VLC algorithm ( $R=1.2$ ,  $\beta = 0.8$ ,  $\gamma = 0.8$ ).

Collider	ILC	CLIC
Sample	$e^+e^- \rightarrow l^\pm \nu b \bar{b} q' \bar{q}$	$e^+e^- \rightarrow 6f (t\bar{t} \text{ compatible})$
$\sqrt{s}$ [GeV]	500	380
Luminosity [ $\text{fb}^{-1}$ ]	500	500
$P(e^-), P(e^+)$	$\mp 1, \pm 1$	$\mp 0.8, 0$
Detector model	ILD_o1_v05 [54]	CLIC_ILD_CDR [53]
Number of BX	1	300
Background	1.7 $\gamma\gamma \rightarrow \text{hadrons} / \text{BX}$	0.0464 $\gamma\gamma \rightarrow \text{hadrons} / \text{BX}$

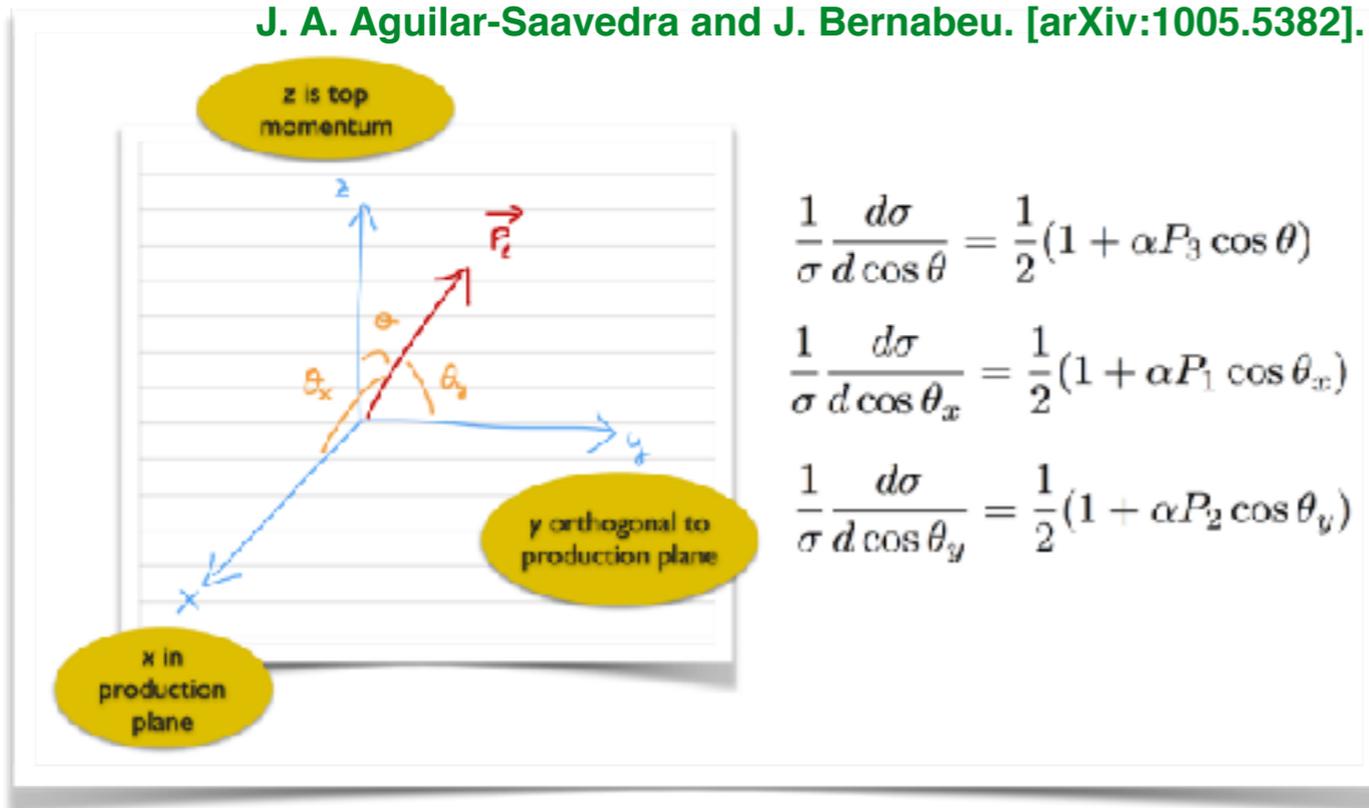
[53] L. Linssen, A. Miyamoto, M. Stanitzki and H. Weerts, Physics and Detectors at CLIC: CLIC Conceptual Design Report, 1202.5940.

[54] H. Abramowicz et al., The International Linear Collider Technical Design Report - Volume 4: Detectors, 1306.6329.

**Further ideas using  
information from the decay:  
top quark polarization**

# Top quark polarization at different axes

J. A. Aguilar-Saavedra and J. Bernabeu. [arXiv:1005.5382].



Studied process

$$e^- e^+ \rightarrow t \bar{t} \rightarrow W^+ b W^- \bar{b} \rightarrow l \nu b \bar{b} q \bar{q}$$

Using the lepton from the leptonic W as a polarimeter, we can calculate the top polarization in 3 different axes.

$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta_i} = \frac{1}{2} (1 + \alpha_i P \cos \theta_i)$$

**Helicity axis (z):** measuring top polarization in the z top momentum direction.

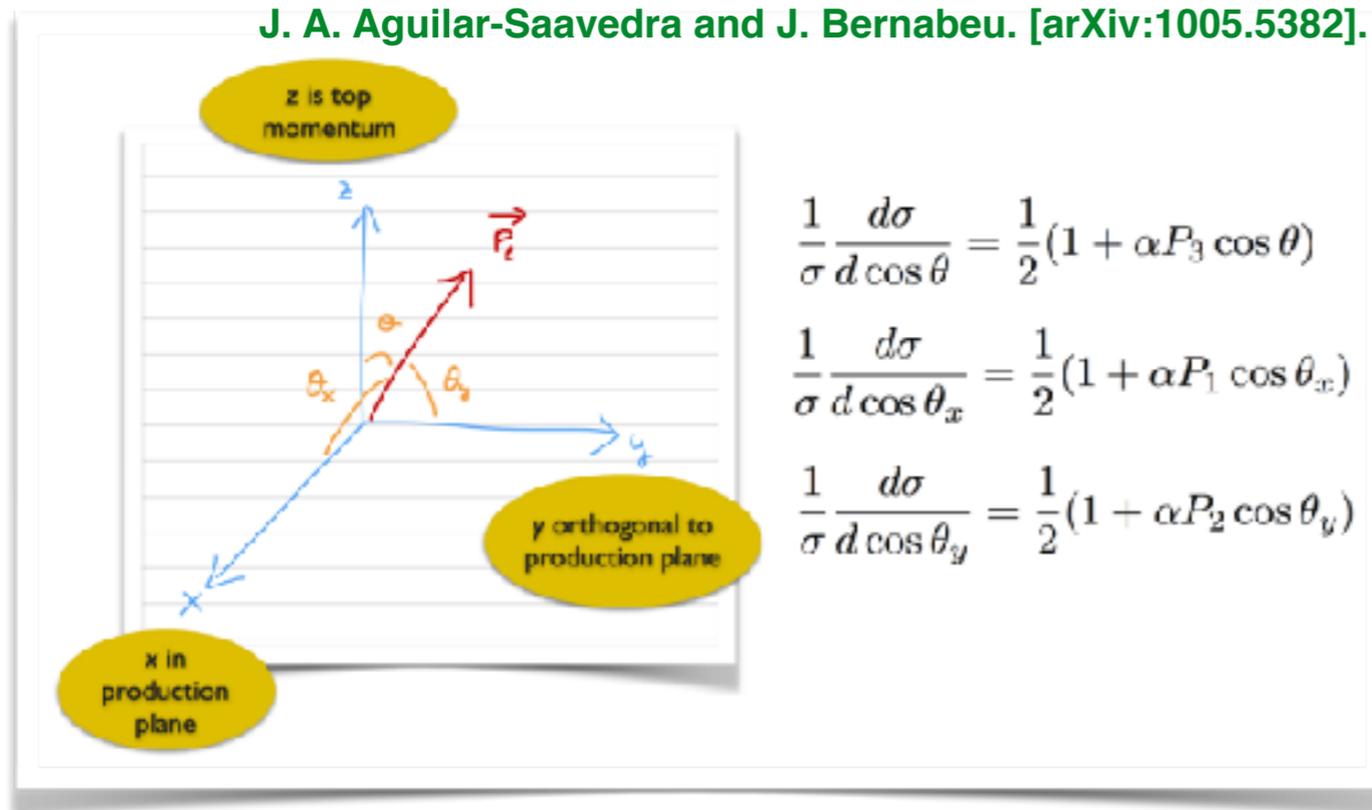
**Overlapping with the forward-backward asymmetry.**

*arXiv:1505.06020v2*

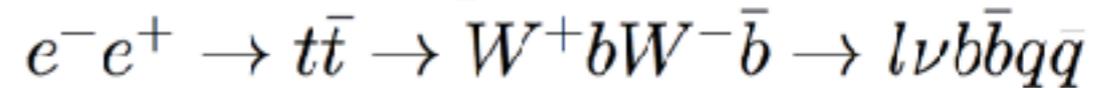
**No new information.**

# Top quark polarization at different axes

J. A. Aguilar-Saavedra and J. Bernabeu. [arXiv:1005.5382].



Studied process



Using the lepton from the leptonic W as a polarimeter, we can calculate the top polarization in 3 different axes.

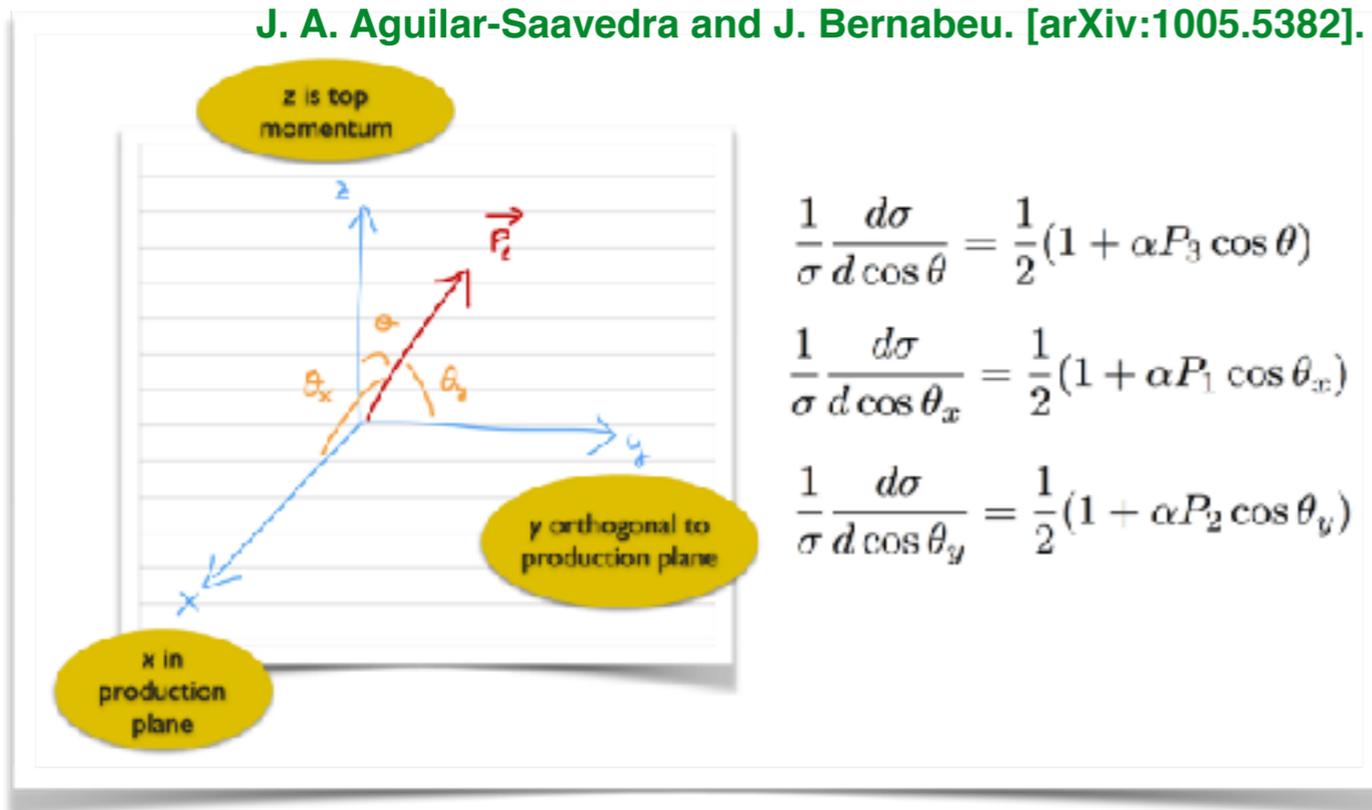
$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta_i} = \frac{1}{2} (1 + \alpha_i P \cos \theta_i)$$

**Normal axis (x):** measuring top polarization in the x direction, perpendicular to the production plane.

**Same definition that the CPV observable ORe (see CPV slide). Insensitive to CP conserving operators.**

# Top quark polarization at different axes

J. A. Aguilar-Saavedra and J. Bernabeu. [arXiv:1005.5382].



Studied process

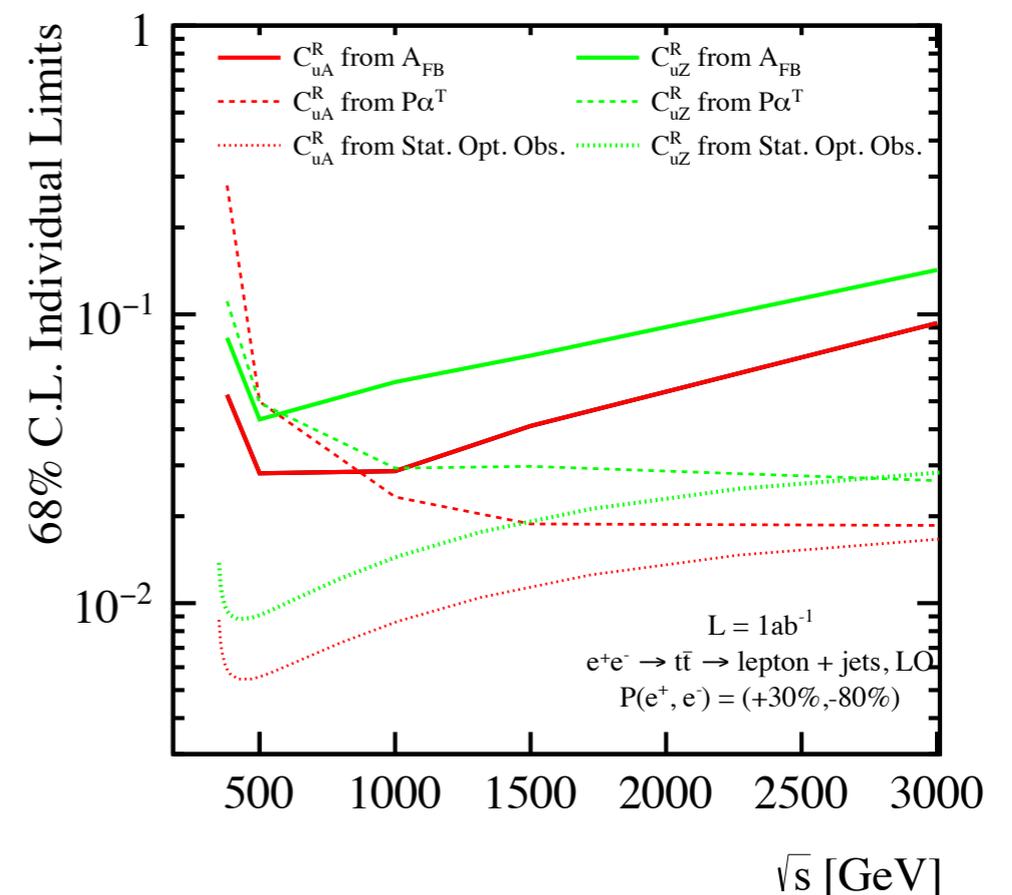
$$e^- e^+ \rightarrow t \bar{t} \rightarrow W^+ b W^- \bar{b} \rightarrow l \nu b \bar{b} q \bar{q}$$

Using the lepton from the leptonic W as a polarimeter, we can calculate the top polarization in 3 different axes.

$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta_i} = \frac{1}{2} (1 + \alpha_i P \cos \theta_i)$$

**Transverse axis (y):** measuring top polarization in the y direction, perpendicular to the x-z plane.

**Seems to be good for constraining the real part of the dipole operators (CuA and CuZ)**



# **Wtb vertex and W polarization**

# Wtb vertex

$$O_{uW} \equiv y_l g_W \bar{q} \tau^I \sigma^{\mu\nu} u \epsilon \varphi^* W_{\mu\nu}^I$$

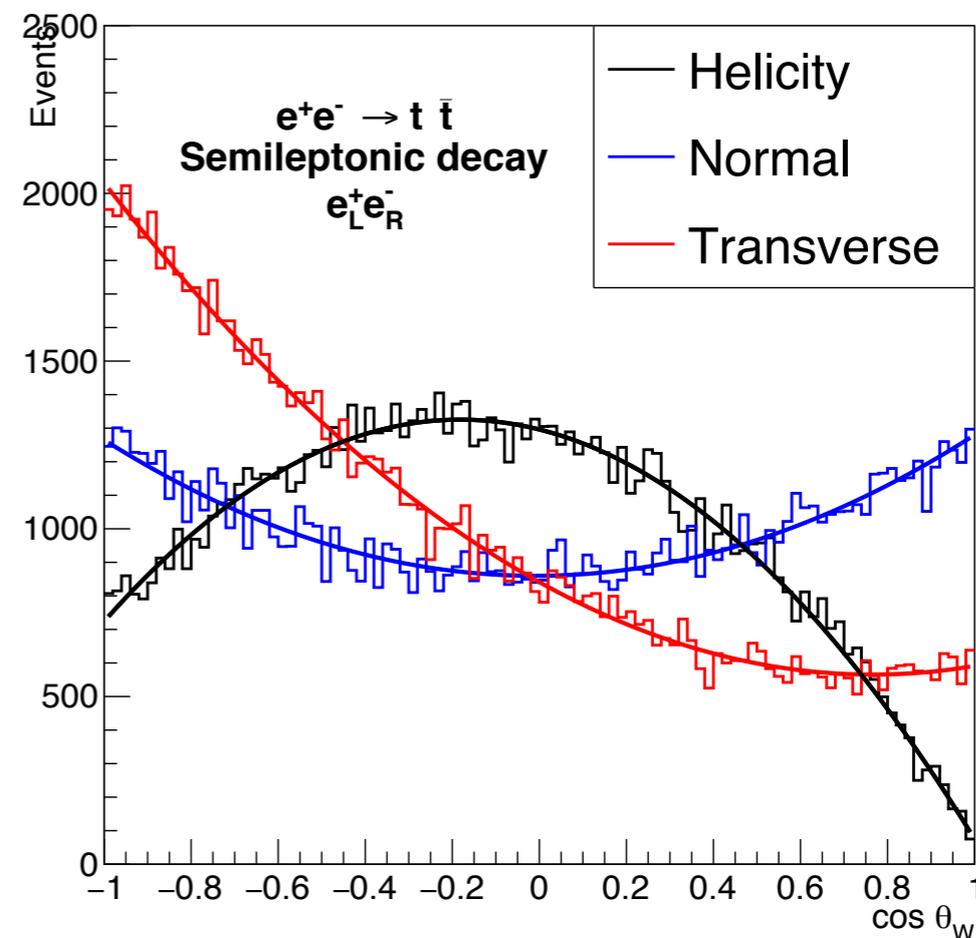
$$O_{\varphi q}^3 \equiv \frac{y_t^2}{2} \bar{q} \tau^I \gamma^\mu q \varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi$$

$$O_{\varphi ud} \equiv \frac{y_t^2}{2} \bar{u} \gamma^\mu d \varphi^T \epsilon i D_\mu \varphi$$

$$O_{dW} \equiv y_t g_W \bar{q} \tau^I \sigma^{\mu\nu} d \epsilon \varphi^* W_{\mu\nu}^I$$

4 operators affecting to the top quark decay, 2 of them appear at production too.

Using the lepton from the leptonic W as a polarimeter, we can calculate the W polarization in 3 different axes (*same motivation than top polarization*).



J. A. Aguilar-Saavedra and J. Bernabeu. [arXiv:1005.5382].

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_l^*} = \frac{3}{8} F_+ (1 + \cos \theta_l^*)^2 + \frac{3}{4} F_0 \sin^2 \theta_l^* + \frac{3}{8} F_- (1 - \cos \theta_l^*)^2$$

# Wtb vertex

$$O_{uW} \equiv y_l g_W \bar{q} \tau^I \sigma^{\mu\nu} u \epsilon \varphi^* W_{\mu\nu}^I$$

$$O_{\varphi q}^3 \equiv \frac{y_t^2}{2} \bar{q} \tau^I \gamma^\mu q \varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi$$

$$O_{\varphi ud} \equiv \frac{y_t^2}{2} \bar{u} \gamma^\mu d \varphi^T \epsilon i D_\mu \varphi$$

$$O_{dW} \equiv y_t g_W \bar{q} \tau^I \sigma^{\mu\nu} d \epsilon \varphi^* W_{\mu\nu}^I$$

4 operators affecting to the top quark decay, 2 of them appear at production too.

Defining:  $A_{FB}^W \equiv \frac{3}{4}(F_+ - F_-)$

*AT is proportional to the top quark transverse polarization*

- $O_{\varphi ud}$  and  $O_{dW}$  only contribute quadratically (no SM interference).
- For these observables the dependence on  $O_{\varphi q}^3$  also completely drops out.

## Sensitivity to the **real part of $O_{uW}$ at 500 GeV** (*Durieux, MP, Vos, Chang PRELIMINARY*)

$P(e^+, e^-)$ observables	(+30%, -80%)		(-30%, +80%)	
	$A^T$	$A_{FB}^W$	$A^T$	$A_{FB}^W$
SM predictions	-0.6	-0.17	0.57	-0.29
in production	$38 \pm 1$	$9 \pm 2$	$-25 \pm 1$	X
in decay	X	$16 \pm 2$	X	$11 \pm 3$
in prod. & decay	$37 \pm 1$	$26 \pm 2$	$-24 \pm 1$	$10 \pm 3$

**CPV backup**

# CPV: Optimal CP-odd observables

The **CP-violating effects** in  $e^+e^- \rightarrow t\bar{t}$  manifest themselves in specific **top-spin effects**, namely **CP-odd top spin-momentum correlations and  $t\bar{t}$  spin correlations**.

$$e^+(\mathbf{p}_+, P_{e^+}) + e^-(\mathbf{p}_-, P_{e^-}) \rightarrow t(\mathbf{k}_t) + \bar{t}(\mathbf{k}_{\bar{t}})$$

$$t \bar{t} \rightarrow \ell^+(\mathbf{q}_+) + \nu_\ell + b + \bar{X}_{\text{had}}(\mathbf{q}_{\bar{X}})$$

$$t \bar{t} \rightarrow X_{\text{had}}(\mathbf{q}_X) + \ell^-(\mathbf{q}_-) + \bar{\nu}_\ell + \bar{b}$$

- **CP-odd observables** are defined with the **four momenta available in  $t\bar{t}$  semi-leptonic decay channel**

$$\mathcal{O}_+^{Re} = (\hat{\mathbf{q}}_{\bar{X}} \times \hat{\mathbf{q}}_+^*) \cdot \hat{\mathbf{p}}_+,$$

$$\mathcal{O}_+^{Im} = -\left[1 + \left(\frac{\sqrt{s}}{2m_t} - 1\right)(\hat{\mathbf{q}}_{\bar{X}} \cdot \hat{\mathbf{p}}_+)^2\right] \hat{\mathbf{q}}_+^* \cdot \hat{\mathbf{q}}_{\bar{X}} + \frac{\sqrt{s}}{2m_t} \hat{\mathbf{q}}_{\bar{X}} \cdot \hat{\mathbf{p}}_+ \hat{\mathbf{q}}_+^* \cdot \hat{\mathbf{p}}_+$$

- The way to **extract** the **CP-violating form factor** is to construct **asymmetries sensitive to CP-violation effects**

$$\mathcal{A}^{Re} = \langle \mathcal{O}_+^{Re} \rangle - \langle \mathcal{O}_-^{Re} \rangle = c_\gamma(s) \text{Re}F_{2A}^\gamma + c_Z(s) \text{Re}F_{2A}^Z$$

$$\mathcal{A}^{Im} = \langle \mathcal{O}_+^{Im} \rangle - \langle \mathcal{O}_-^{Im} \rangle = \tilde{c}_\gamma(s) \text{Im}F_{2A}^\gamma + \tilde{c}_Z(s) \text{Im}F_{2A}^Z$$

$$\begin{array}{cc} \mathcal{A}_{\gamma,Z}^{Re L} & \mathcal{A}_{\gamma,Z}^{Re L} \\ \mathcal{A}_{\gamma,Z}^{Im R} & \mathcal{A}_{\gamma,Z}^{Im R} \end{array}$$

# CPV: Coefficients vs sqrt(s)

---

The sensitivity of  $A_{\text{Re}}/A_{\text{Im}}$  to  $F_{2A}$  increases strongly with the c.o.m. energy

$$P_{e^-} = -1, P_{e^+} = +1$$

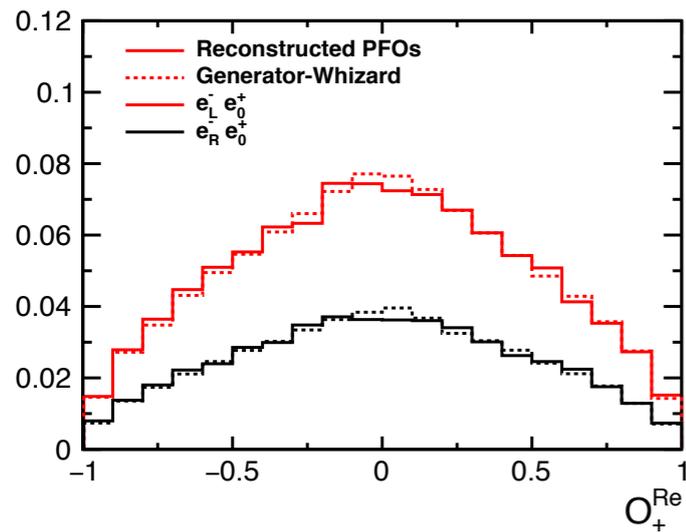
c.m. energy $\sqrt{s}$ [GeV]	$c_\gamma(s)$	$c_Z(s)$	$\tilde{c}_\gamma(s)$	$\tilde{c}_Z(s)$
380	0.245	0.173	0.232	0.164
500	0.607	0.418	0.512	0.352
1000	1.714	1.151	1.464	0.983
1400	2.514	1.681	2.528	1.691
3000	5.589	3.725	10.190	6.791

$$P_{e^-} = +1, P_{e^+} = -1$$

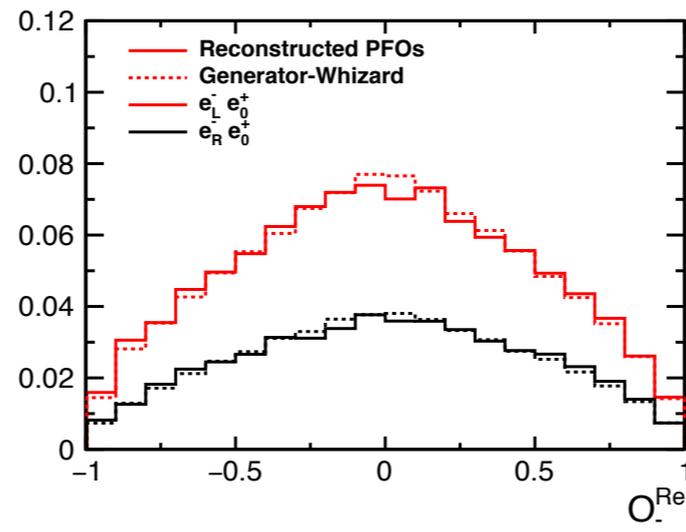
c.m. energy $\sqrt{s}$ [GeV]	$c_\gamma(s)$	$c_Z(s)$	$\tilde{c}_\gamma(s)$	$\tilde{c}_Z(s)$
380	-0.381	0.217	0.362	-0.206
500	-0.903	0.500	0.761	-0.422
1000	-2.437	1.316	2.081	-1.124
1400	-3.549	1.909	3.569	-1.920
3000	-7.845	4.205	14.302	-7.667

Thanks to Bernreuther

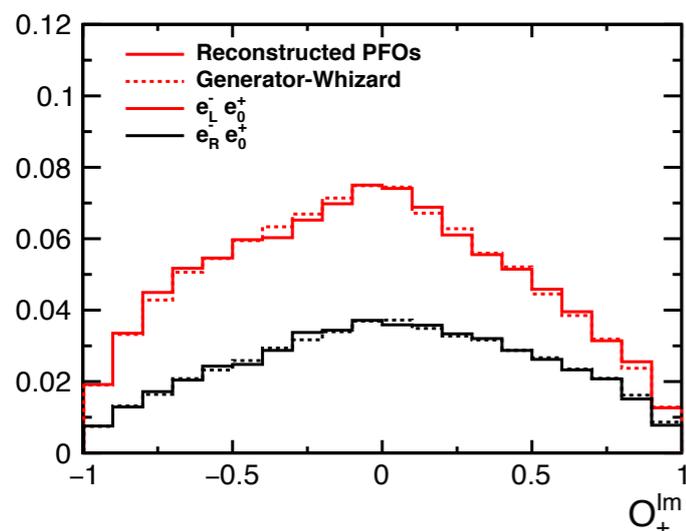
# CPV: Full-simulation: CLIC@380GeV



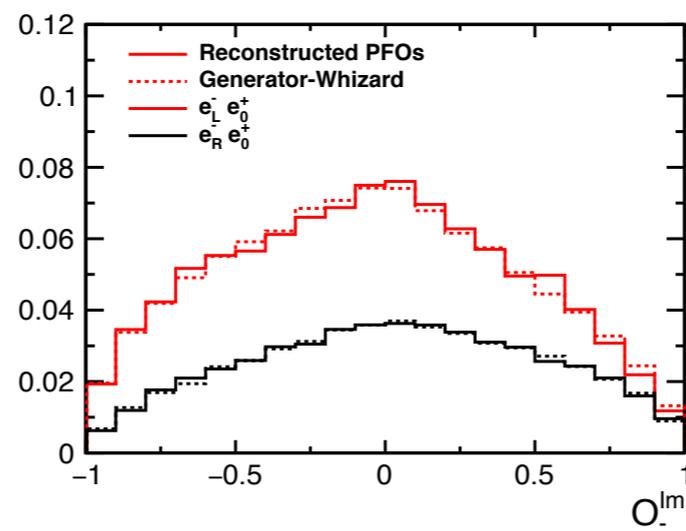
(a)  $\mathcal{O}_+^{Re}$



(b)  $\mathcal{O}_-^{Re}$



(c)  $\mathcal{O}_+^{Im}$



(d)  $\mathcal{O}_-^{Im}$

- Distributions are **centered at zero**
- **Differences** between reconstructed and generated events are **very small**.
- Any **distortions** in the reconstructed distributions are **expected to cancel in the asymmetries**  $A_{Re}$  and  $A_{Im}$
- **Asymmetries** are **compatible with zero** within the statistical error

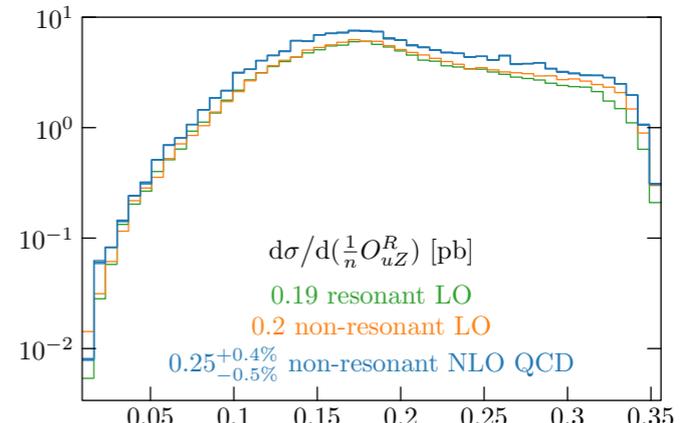
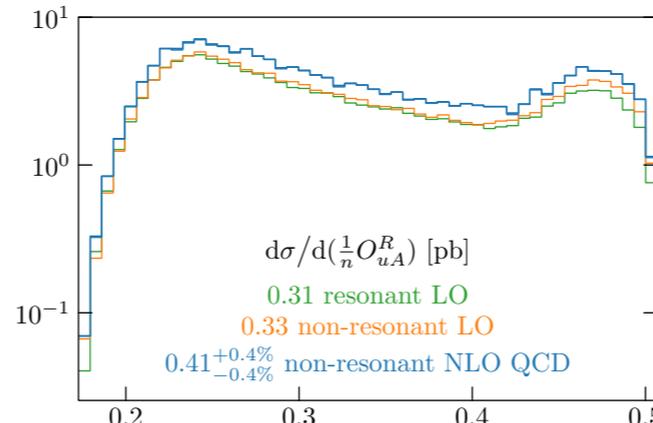
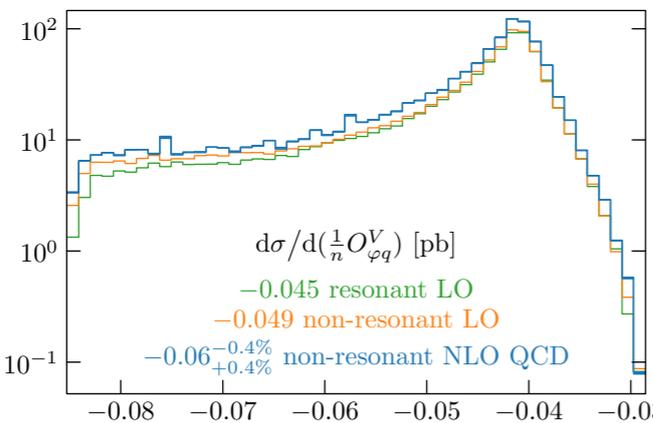
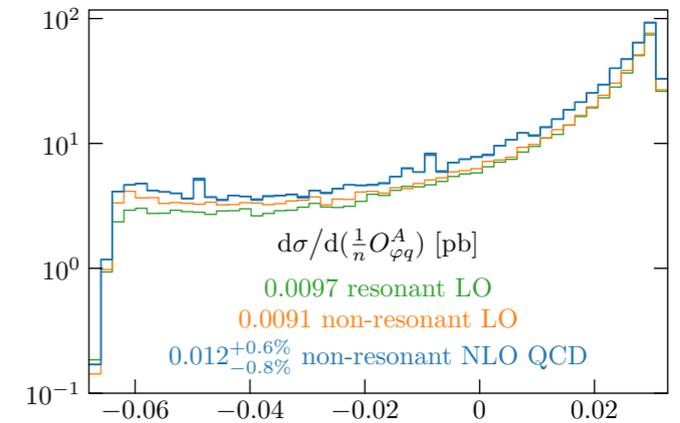
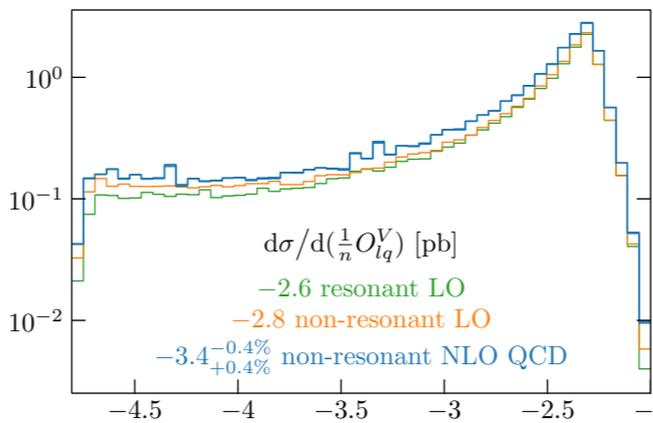
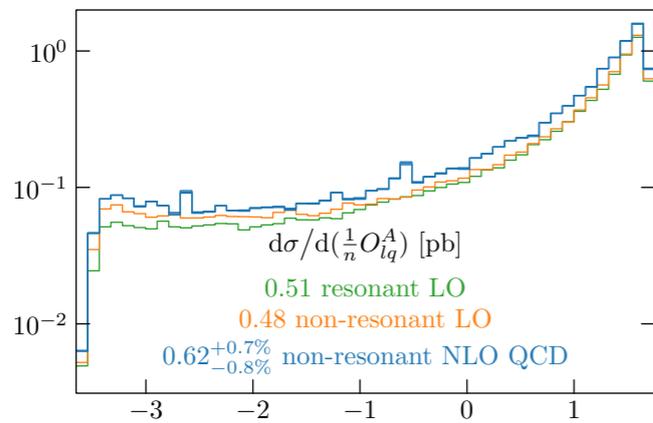
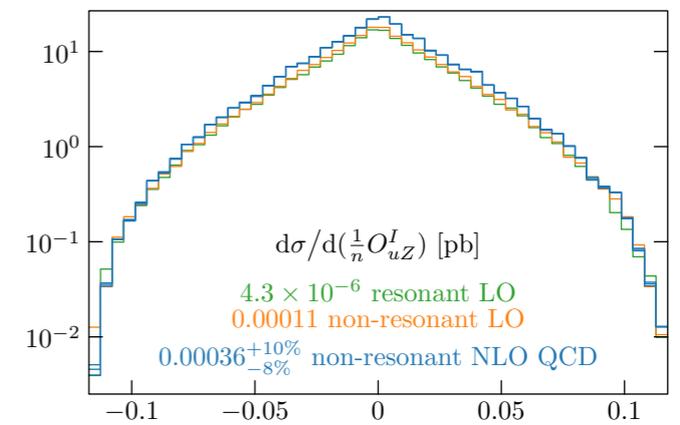
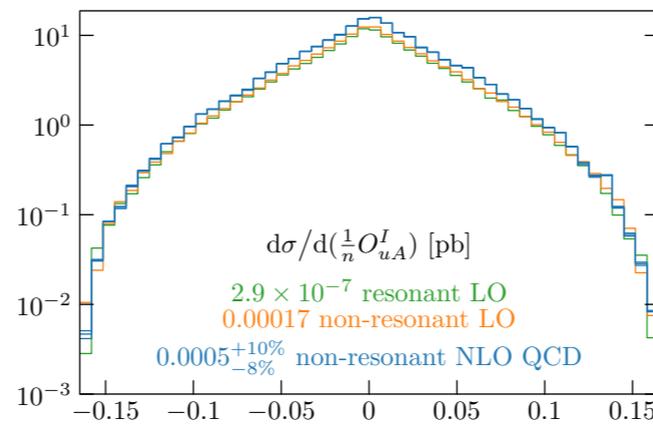
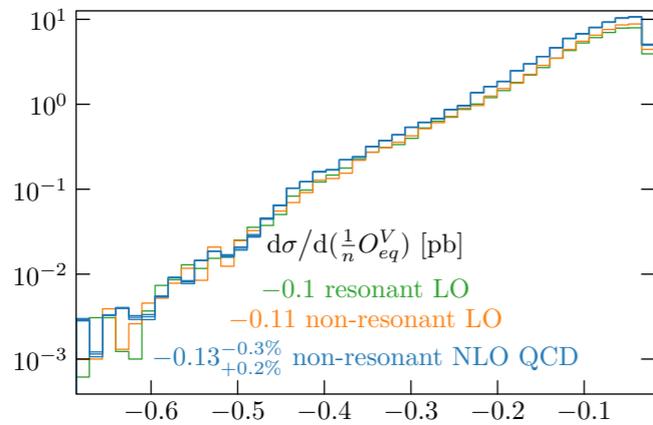
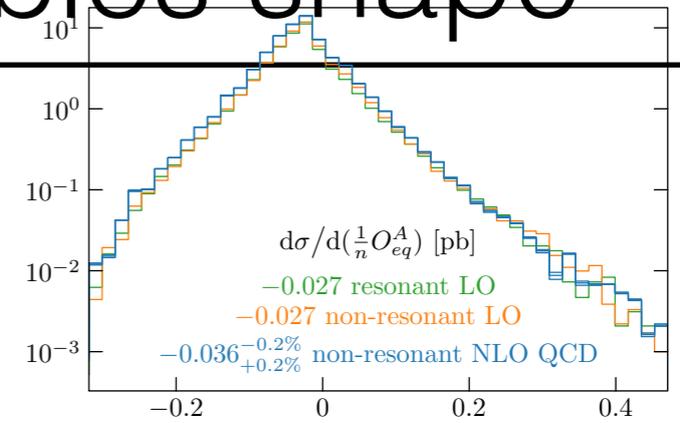
polarization	$e_L^- (P_{e^-} = -0.8)$	$e_R^- (P_{e^-} = +0.8)$
$A^{Re}$	$-0.00006 \pm 0.003$	$0.0072 \pm 0.003$
$A^{Im}$	$0.0004 \pm 0.003$	$-0.0019 \pm 0.003$

# Statistically optimal observables shape

Example for 500 GeV ( $e^-, e^+$ ) = (-0.8, 0.3)

Theory uncertainties under study

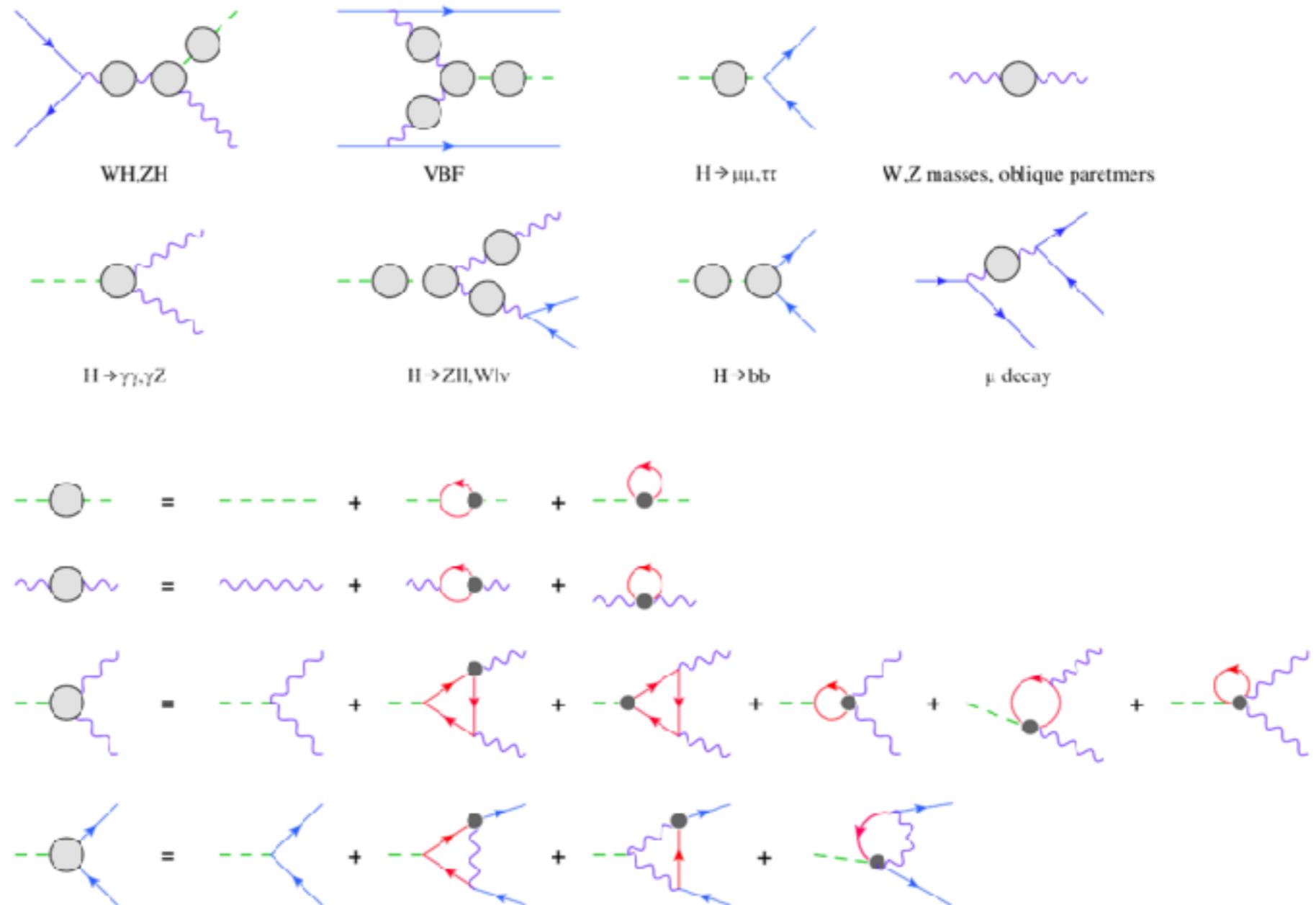
Generated plots



# Ongoing work at KEK

## Dimension-six electroweak top-loop effects in Higgs production and decay

C. Zhang and E. Vryonidou (arXiv:1804.09766)



# Ongoing work at KEK

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- **First success:** introduce numbers by Cen and Eleni to the Higgs global fit program.
- **Expected conclusion:** to add top-quark operators to the Higgs fit is not good for Higgs couplings uncertainties.
- Studied (but not yet interpreted) the impact of adding top quarks operators one by one to the fit.
- **Future:** try to collaborate with the authors of the paper and discuss deeply next steps.