

Light Flavor Branching Fractions in $e^+e^- \rightarrow q\bar{q}$

ILD Software & Analysis Meeting

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Hamburg, 25.07.2018

Introduction

- Idea: Leading particle flavor content correlated to jet flavor \rightarrow tag light flavor jets by identifying highest momentum hadrons above a threshold momentum.
- Original method developed for LEP experiments.
- Problem: Tags are not unambiguous due to additional production of u, d and s quarks from the QCD sea.
- Solution: Measure hadrons containing different flavors to resolve ambiguities (π^\pm , K^\pm , p , K_S^0 , Λ).
- Observables: Number of jets N_i tagged with hadron i and number of double tagged events N_{ij} .
- Use standard b and c tagging techniques to determine and subtract heavy flavor content.

$$\frac{N_i}{N_{had}} = 2 \times \sum_q \eta_q^i R_q$$

$$\frac{N_{ij}}{N_{had}} = (2 - \delta_{ij}) \times \sum_q \rho_{ij} \eta_q^i \eta_q^j R_q$$

- $\eta_q^i = \frac{N_{q \rightarrow i}}{N_q}$ is the probability that a quark of flavor q creates a leading hadron i .
- $R_q = \frac{\Gamma_{ee \rightarrow qq}}{\Gamma_{had}}$ is the branching fraction of $e^+e^- \rightarrow q\bar{q}$.
 - Alternative use $R'_q = \frac{R_q}{1 - R_c - R_b}$
- ρ_{ij} are jet correlation factors.
- N_{had} is the total number of $e^+e^- \rightarrow q\bar{q}$ events.

Additional Assumptions

- Additional assumptions are required to solve the equation system.
- Hadronization Symmetries (K^0 includes K_S^0 and K_L^0):

$$\eta_d^{\pi^\pm} = \eta_u^{\pi^\pm}$$

$$\eta_d^{K^0} = \eta_u^{K^\pm}$$

$$\eta_u^{K^0} = \eta_d^{K^\pm}$$

$$\eta_s^{K^0} = \eta_s^{K^\pm}$$

$$\eta_u^\Lambda = \eta_d^\Lambda$$

- Are broken by $< 2\%$.
- Normalization of branching fractions:
 $\sum_q R_q = 1$ or $\sum_q R'_q = 1$
- From weak isospin structure: $R_d = R_s$

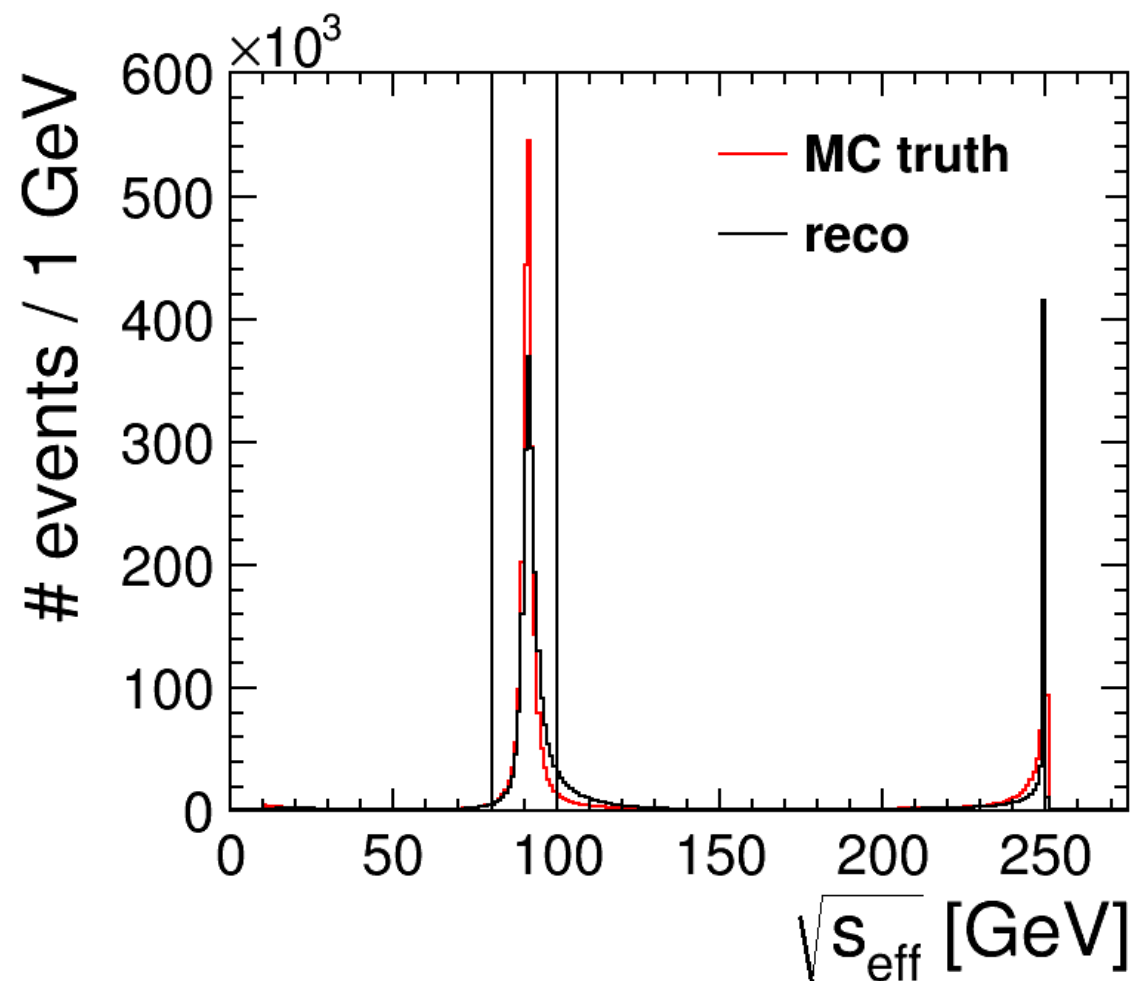
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Data & Event Treatment

- Using DBD data: 2.86×10^6 events.
 - $\sqrt{s} = 250$ GeV, Dijet events
- Weighted to 2 ab^{-1} : 119.45×10^6 events.
 - Split (45%, 45%, 5%, 5%) between (+-, -+, ++, --).
- ISR is identified by MC truth and removed.
 - Methods like kinematic fits have been shown to reliably recover ISR.
- Rest of event is boosted into CM system after ISR.
- Event is split into hemispheres by projecting particle momenta onto thrust axis.
- In each hemisphere the particle with the highest momentum (leading particle) is identified.

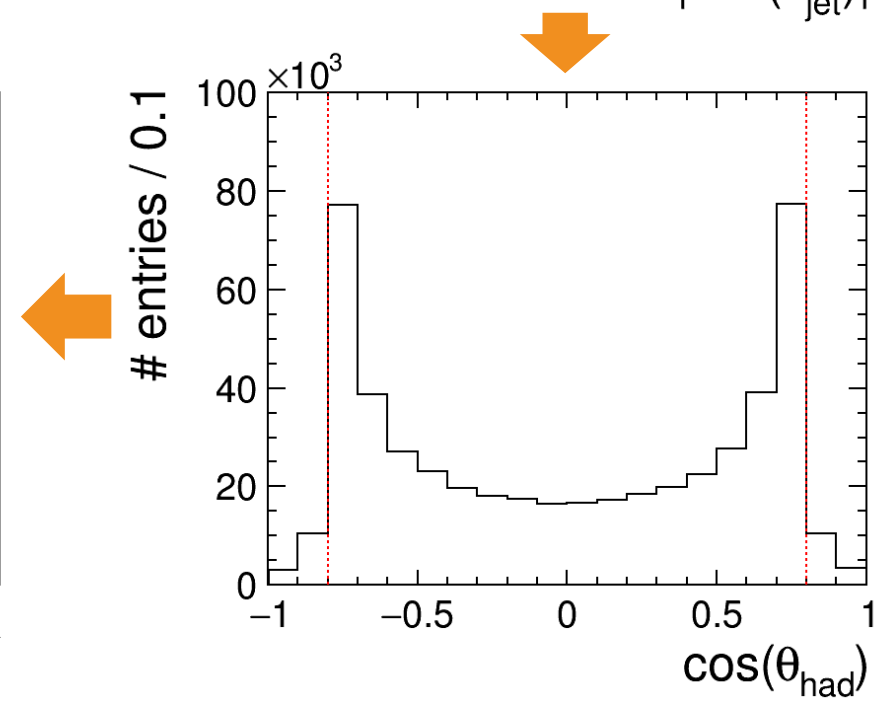
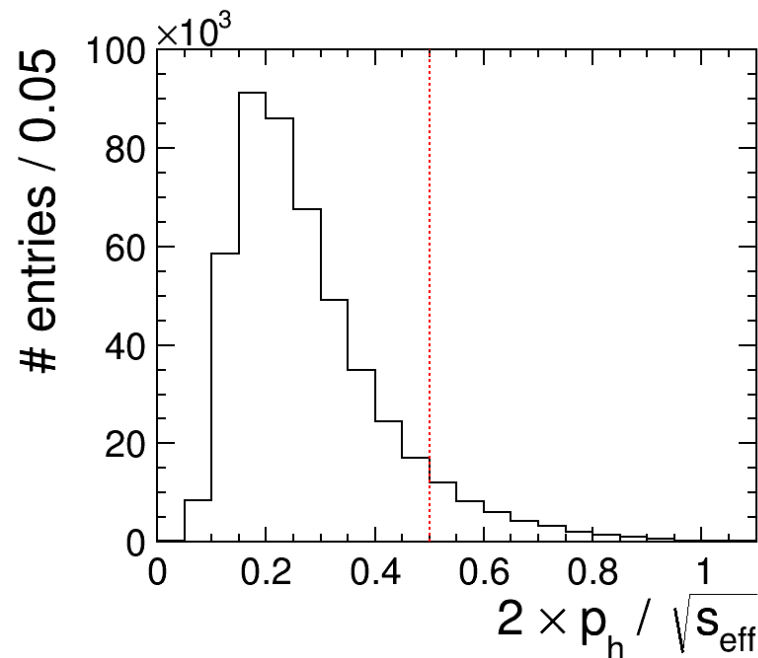
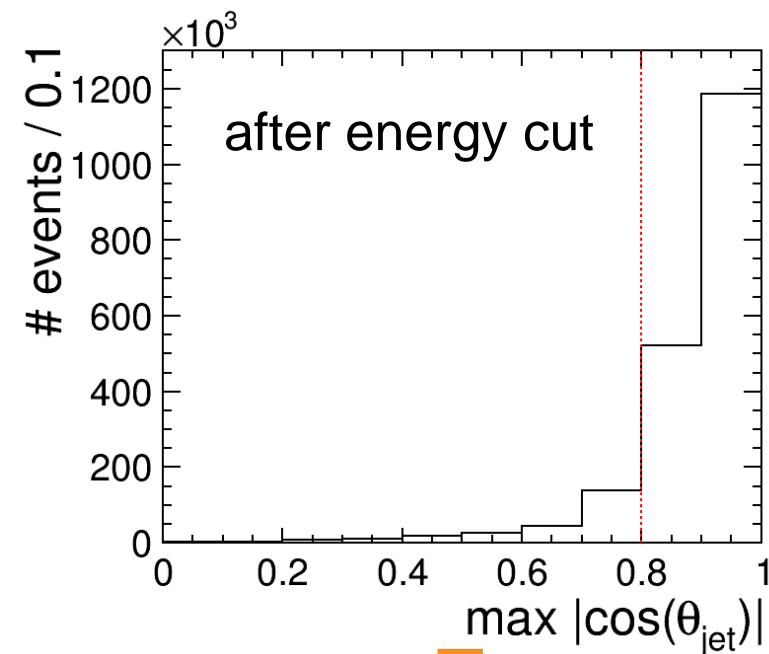
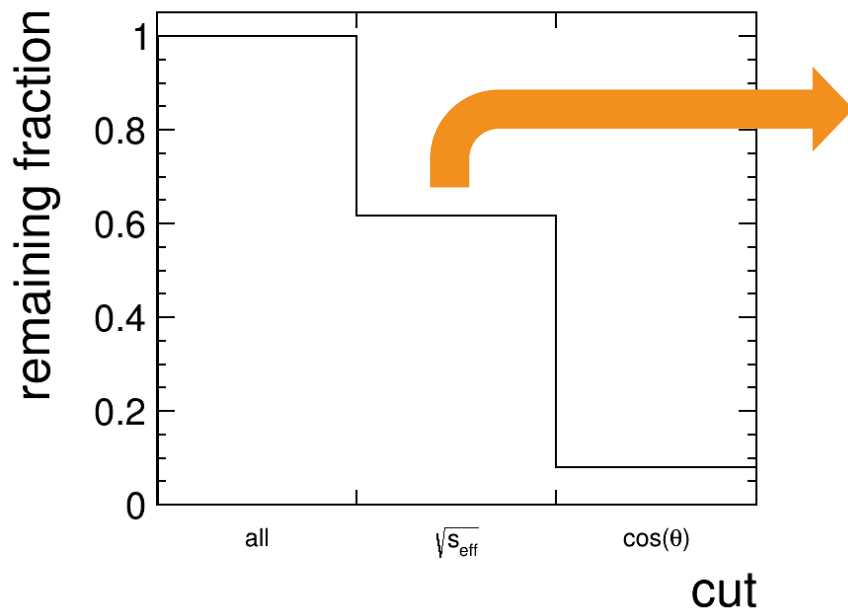


Data

$$80 \text{ GeV} < \sqrt{s_{eff}} < 100 \text{ GeV}$$

$$p_{had} > 0.5 \times \sqrt{s_{eff}}/2$$

- Event cuts:
 - $80 \text{ GeV} < \sqrt{s_{eff}} < 100 \text{ GeV}$
 - $|\cos \theta_{jet}| < 0.8$ for both jets
- Leading particle cuts:
 - $|\cos \theta_{had}| < 0.8$
 - $p_{had} > 0.5 \times \sqrt{s_{eff}}/2$
- Considering $\pi^\pm, K^\pm, p, K_S^0, \Lambda$



Particle ID

$80 \text{ GeV} < \sqrt{s_{eff}} < 100 \text{ GeV}, p_{had} > 0.5 \times \sqrt{s_{eff}}/2$

- K_S^0 and Λ are identified by V0Finder in standard reconstruction.
- No dE/dx PID done in DBD samples.
- Applying toy PID to leading particles based on dE/dx separation power calculated by Uli Einhaus on iLCSoft v01-19-05.

PID purities

Assigned PID	$\Lambda(\bar{\Lambda})$	K_S^0	$p(\bar{p})$	K^\pm	π^\pm	other
	0.0163	0.00163		0.00163	0.0703	0.871
	0.000778				0.968	0.0117
	0.0558	0.0125	0.496	0.407		0.00606
	0.0066	0.28	0.633	0.0501		0.00159
	0.00334	0.855	0.11	0.00136	0.00209	
True PID						
	other	π^\pm	K^\pm	$p(\bar{p})$	K_S^0	$\Lambda(\bar{\Lambda})$

PID efficiencies

Assigned PID	$\Lambda(\bar{\Lambda})$	K_S^0	$p(\bar{p})$	K^\pm	π^\pm	other
	0.000984	8.66e-05		0.000557	0.0138	0.308
	9.84e-05				0.399	0.00867
	0.0136	0.00269	0.154	0.56		0.00867
	0.00285	0.107	0.348	0.122		0.00404
	0.00315	0.709	0.131	0.00724	0.00641	
True PID						
	other	π^\pm	K^\pm	$p(\bar{p})$	K_S^0	$\Lambda(\bar{\Lambda})$

Data

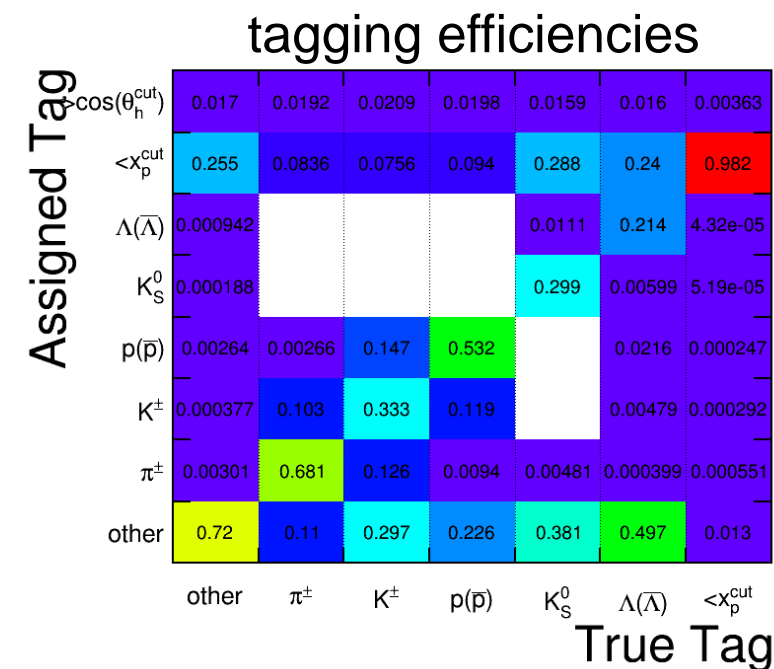
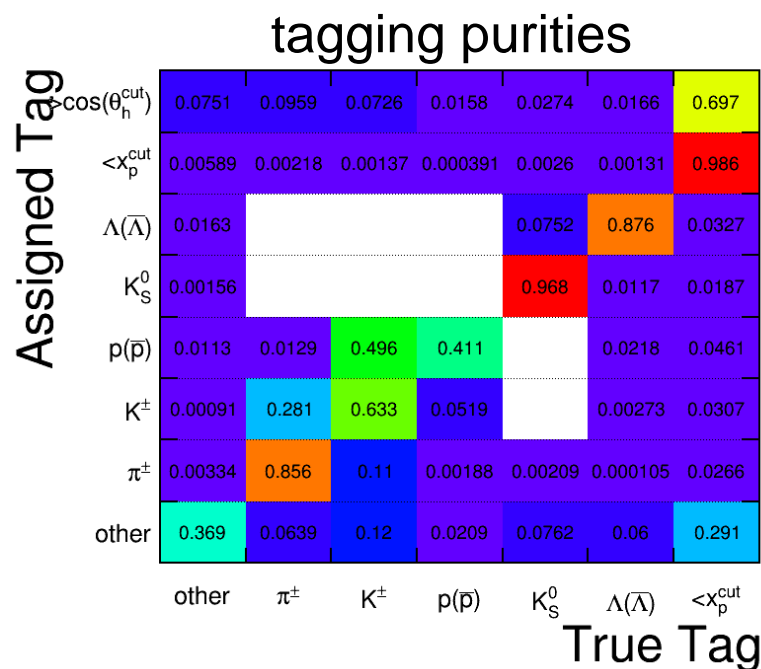
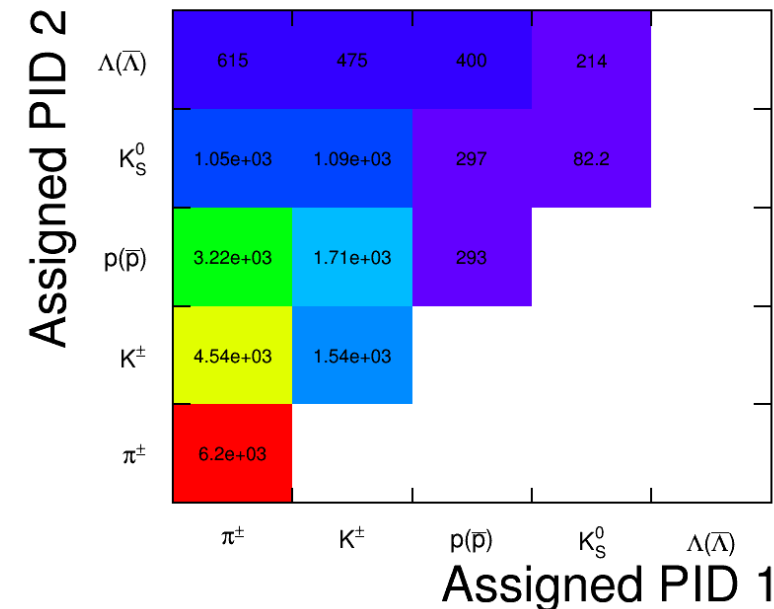
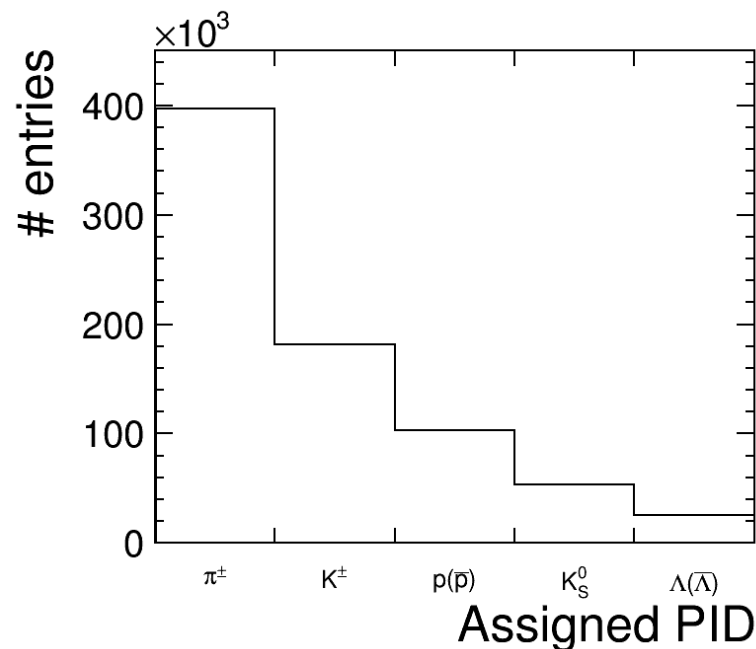
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- Considering π^\pm , K^\pm , p , K_S^0 , Λ
- Tagging efficiencies determined from MC.
- Applying tagging efficiencies to reconstructed data:

$$\eta_q^{i,exp} = \sum_j \mathcal{E}_i^j \eta_q^j$$

- Determination of heavy quark contamination in reconstructed samples is cheated with MC truth.



Chi-square Function

The equation system

$$\frac{N_i}{N_{had}} = 2 \times \sum_q \eta_q^{i,exp} R_q$$

$$\frac{N_{ij}}{N_{had}} = (2 - \delta_{ij}) \times \sum_q \rho_{ij} \eta_q^{i,exp} \eta_q^{j,exp} R_q$$

leads to a chi-square function:

$$\chi^2 = \sum_i \left[\frac{\tilde{N}_i - 2N_{had} \times \sum_q \tilde{\eta}_q^i R_q}{\sqrt{\tilde{N}_i}} \right]^2 + \sum_{i,j} \left[\frac{N_{ij} - (2 - \delta_{ij}) \times \sum_q \rho \eta_q^{i,exp} \eta_q^{j,exp} R_q}{\sqrt{N_{ij}}} \right]^2$$

where

$$\tilde{N}_i = N_i - \sum_j (1 + \delta_{ij}) N_{ij}$$

and

$$\tilde{\eta}_q^i = \eta_q^{i,exp} - \sum_j \rho \eta_q^{i,exp} \eta_q^{j,exp}$$

are needed to correct for double counting between the single and double tagged samples.

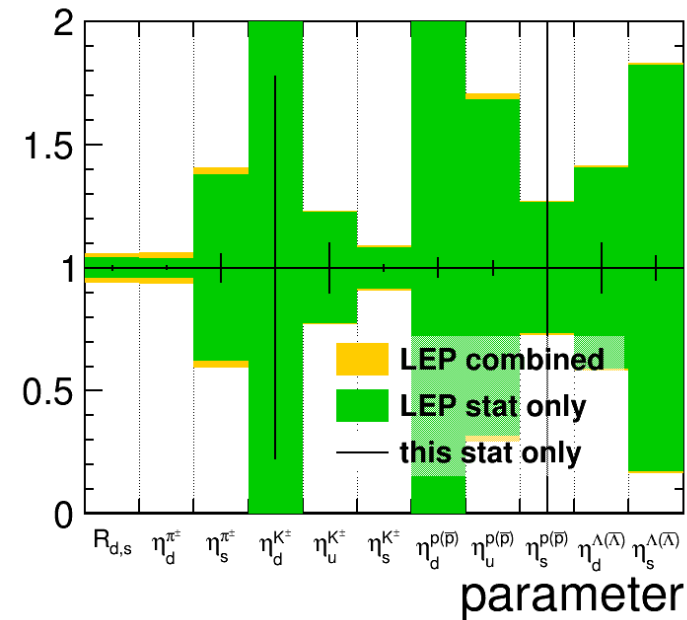
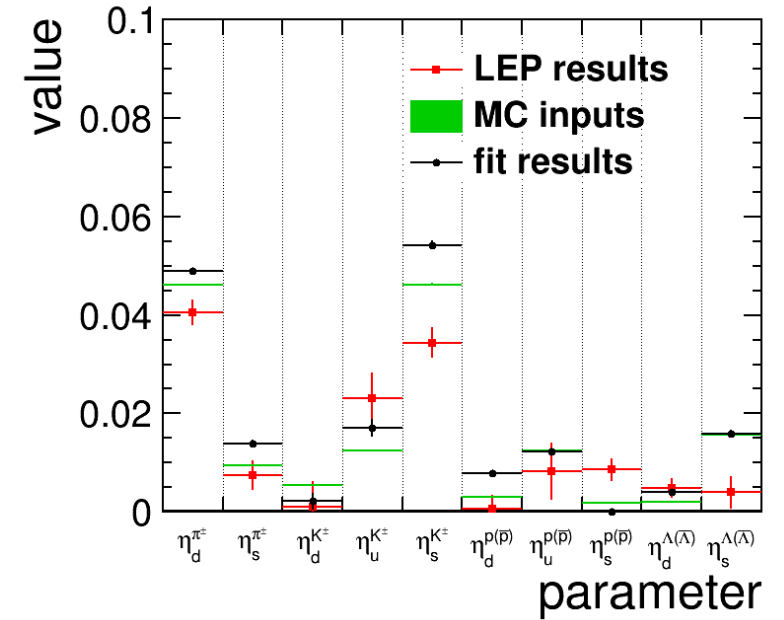
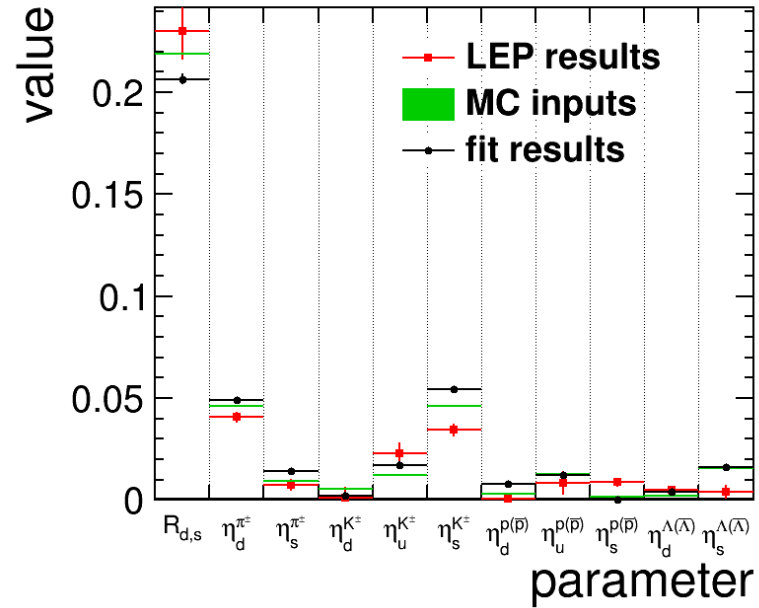
MC shows correlation factors $\rho_{ij} = \rho$ are independent of hadron type for the hadrons used here.

Results

$$80 \text{ GeV} < \sqrt{s_{eff}} < 100 \text{ GeV}$$

$$p_{had} > 0.5 \times \sqrt{s_{eff}}/2$$

- $\chi^2/ndf = 496.28/7$ with an average event weight of 41.35
 - Effective $\chi^2/ndf = 12.00/7$
 - Unweighted $\chi^2/ndf = 9.37/7$
- Statistical errors only.
- LEP (OPAL) results for comparison (full errors)

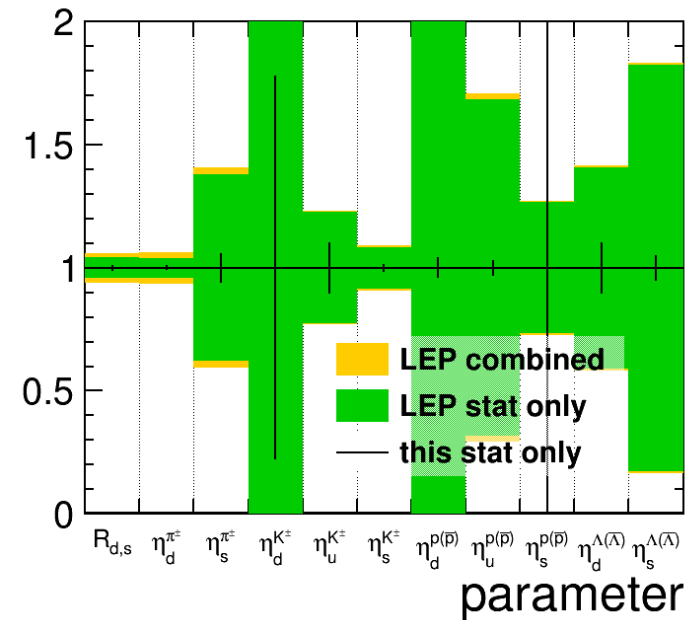
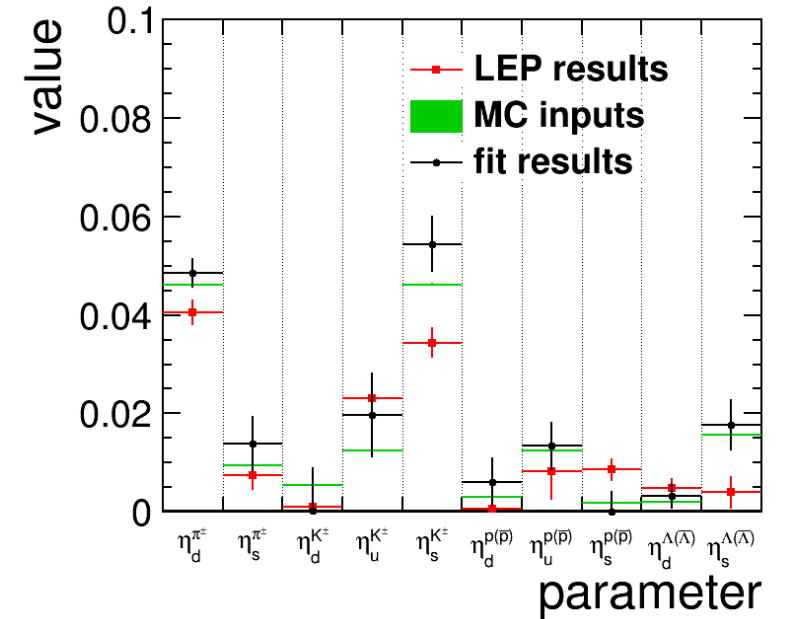
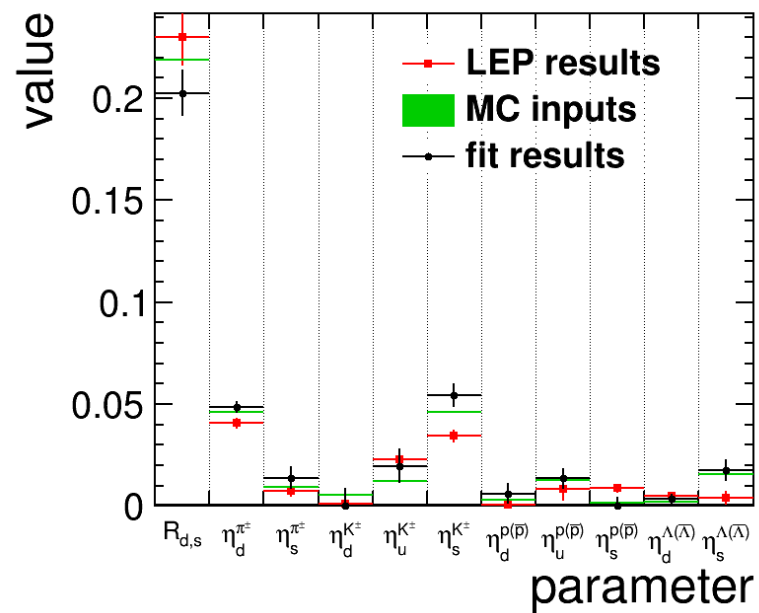


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Summary

- Measurement of light quark branching fractions was implemented.
- Statistical errors significantly improved over corresponding OPAL analysis.
 - Factor ~ 3 -4 for $R_{d,s}$.
- Major difficulties to be expected at ILC over LEP:
 - Reconstruction of ISR / effective center of mass.
 - dE/dx PID of high momentum leading particles.