

Benchmark Analysis for $e^+e^- \rightarrow \text{gamma Z}$ process

SOKENDAI

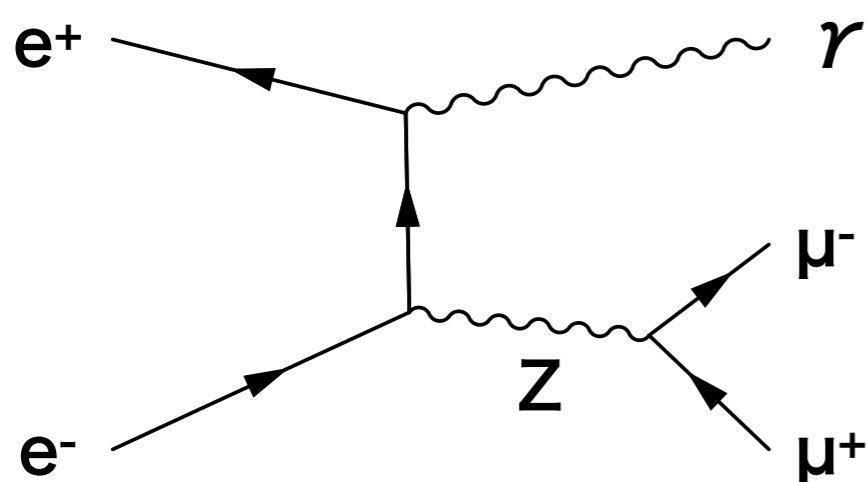
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Status report on

$e^+e^- \rightarrow \text{gamma } Z$ analysis

- Using **direction angles of μ^- , μ^+ and γ ,** photon energy calibration is being conducted.
- I checked whether constructed energy matched with the MCtrue energy, then photon energy resolution is estimated.
- Plots are very preliminary and rough today.

Determine the energy of photon and muons based on measured direction angle



Direction Angle
 θ : azimuthal angle
 ϕ : polar angle

4-momentum conservation is considered.
 The mass of muon is neglected.

Condition 1:

Using $(\theta_{\mu^-}, \theta_{\mu^+}, \theta_{\gamma}, \phi_{\mu^-}, \phi_{\mu^+}, \phi_{\gamma})$
 -> Determine $(E_{\mu^-}, E_{\mu^+}, E_{\gamma})$

Condition 2: Add **Beamstrahlung**

Using $(\theta_{\mu^-}, \theta_{\mu^+}, \theta_{\gamma}, \phi_{\mu^-}, \phi_{\mu^+}, \phi_{\gamma})$
 -> Determine $(E_{\mu^-}, E_{\mu^+}, E_{\gamma}, E_{ISR})$

Condition 3: Add the effect of **Crossing Angle**

Using $(\theta_{\mu^-}, \theta_{\mu^+}, \theta_{\gamma}, \phi_{\mu^-}, \phi_{\mu^+}, \phi_{\gamma})$
 -> Determine $(E_{\mu^-}, E_{\mu^+}, E_{\gamma}, E_{ISR})$

• Condition 1

$$\begin{cases} E_M + E_{M'} + E_R = 500 \\ E_M \sin \theta_M \cos \varphi_M + E_{M'} \sin \theta_{M'} \cos \varphi_{M'} + E_R \sin \theta_R \cos \varphi_R = 0 \\ E_M \sin \theta_M \sin \varphi_M + E_{M'} \sin \theta_{M'} \sin \varphi_{M'} + E_R \sin \theta_R \sin \varphi_R = 0 \\ E_M \cos \theta_M + E_{M'} \cos \theta_{M'} + E_R \cos \theta_R = 0 \end{cases}$$

• Condition 2

$$\begin{cases} E_M + E_{M'} + E_R + |P_{ISR}| = 500 \\ E_M \sin \theta_M \cos \varphi_M + E_{M'} \sin \theta_{M'} \cos \varphi_{M'} + E_R \sin \theta_R \cos \varphi_R = 0 \\ E_M \sin \theta_M \sin \varphi_M + E_{M'} \sin \theta_{M'} \sin \varphi_{M'} + E_R \sin \theta_R \sin \varphi_R = 0 \\ E_M \cos \theta_M + E_{M'} \cos \theta_{M'} + E_R \cos \theta_R + P_{ISR} = 0 \end{cases}$$

Condition 3

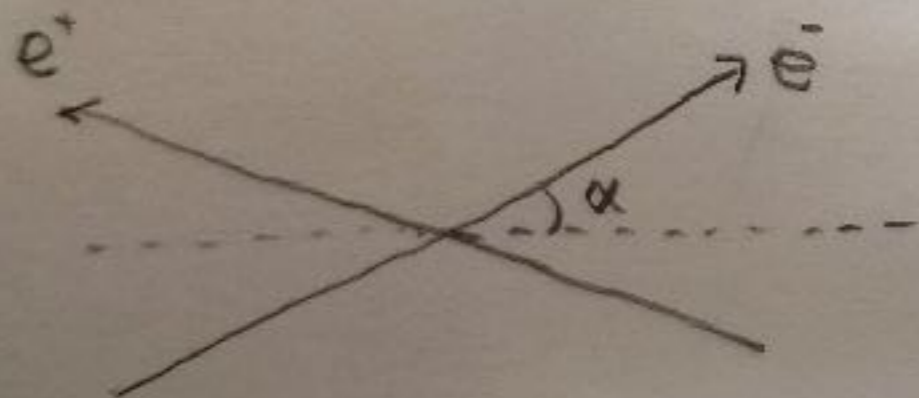
$$E_{\mu} + E_{\mu'} + E_{\gamma} + |P_{\text{ISR}}| = 500$$

$$E_{\mu} \sin \theta_{\mu} \cos \varphi_{\mu} + E_{\mu'} \sin \theta_{\mu'} \cos \varphi_{\mu'} + E_{\gamma} \sin \theta_{\gamma} \cos \varphi_{\gamma} + P_{\text{ISR}} \sin \alpha = 500 \sin \alpha$$

$$E_{\mu} \sin \theta_{\mu} \sin \varphi_{\mu} + E_{\mu'} \sin \theta_{\mu'} \sin \varphi_{\mu'} + E_{\gamma} \sin \theta_{\gamma} \sin \varphi_{\gamma} = 0$$

$$E_{\mu} \cos \theta_{\mu} + E_{\mu'} \cos \theta_{\mu'} + E_{\gamma} \cos \theta_{\gamma} + P_{\text{ISR}} \cos \alpha = 0$$

Crossing angle ($\equiv 2\alpha$)



Condition 1:

Using $(\theta_{\mu^-}, \theta_{\mu^+}, \theta_r, \phi_{\mu^-}, \phi_{\mu^+}, \phi_r)$

-> Determine $(E_{\mu^-}, E_{\mu^+}, E_r)$

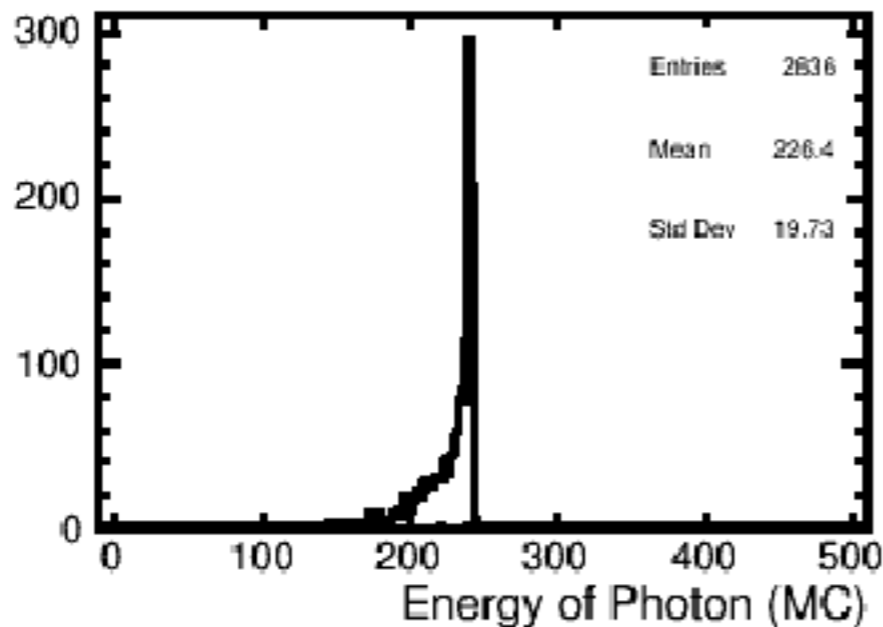
Samples:

$|\cos(\mu)| < 0.75$

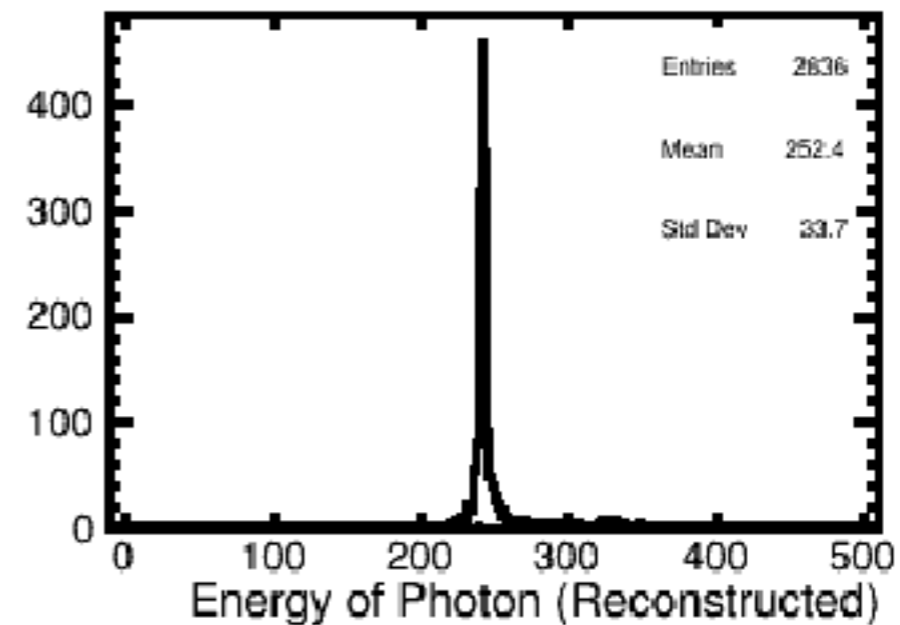
$|M(\mu^+\mu^-) - 91.2| < 10 \text{ GeV}$

Large ILD model

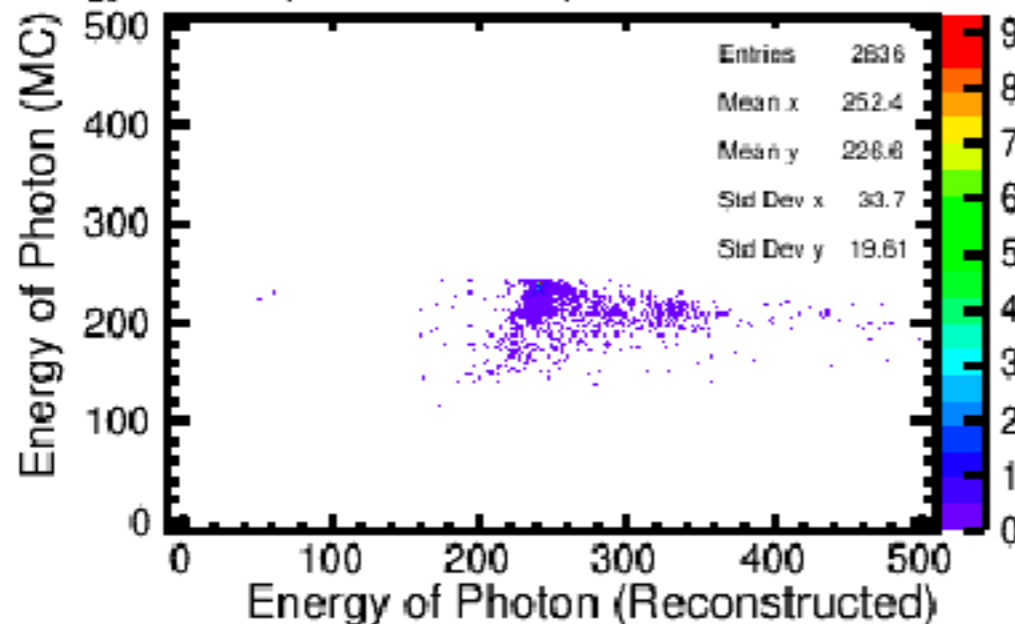
Energy of Photon (MC)



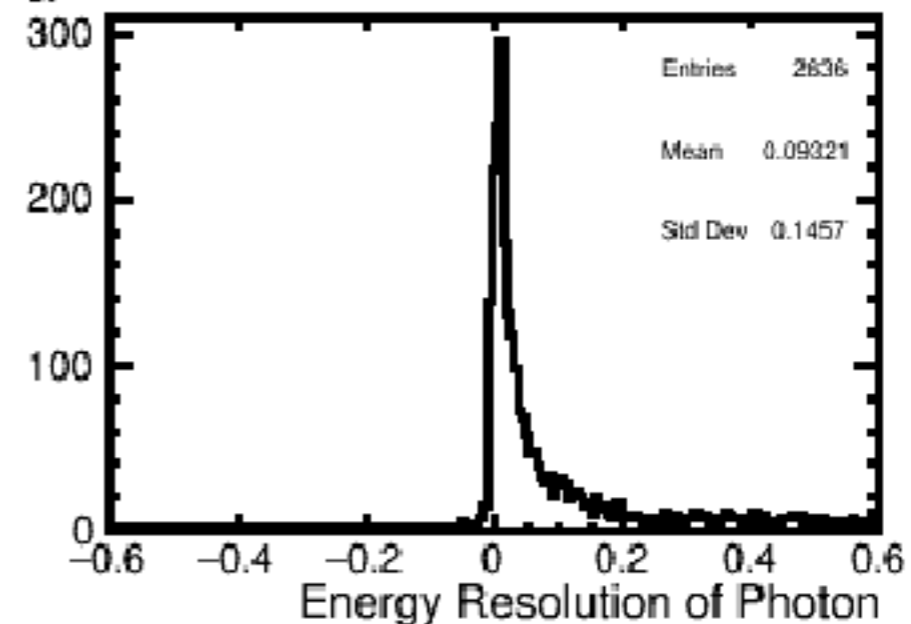
Energy of Photon (Reconstructed)



Energy of Photon (MC:Reconstructed)



Energy Resolution of Photon



Condition 2: Add **Beamstrahlung**

Using $(\theta_{\mu^-}, \theta_{\mu^+}, \theta_{\gamma}, \phi_{\mu^-}, \phi_{\mu^+}, \phi_{\gamma})$

-> Determine $(E_{\mu^-}, E_{\mu^+}, E_{\gamma}, E_{ISR})$

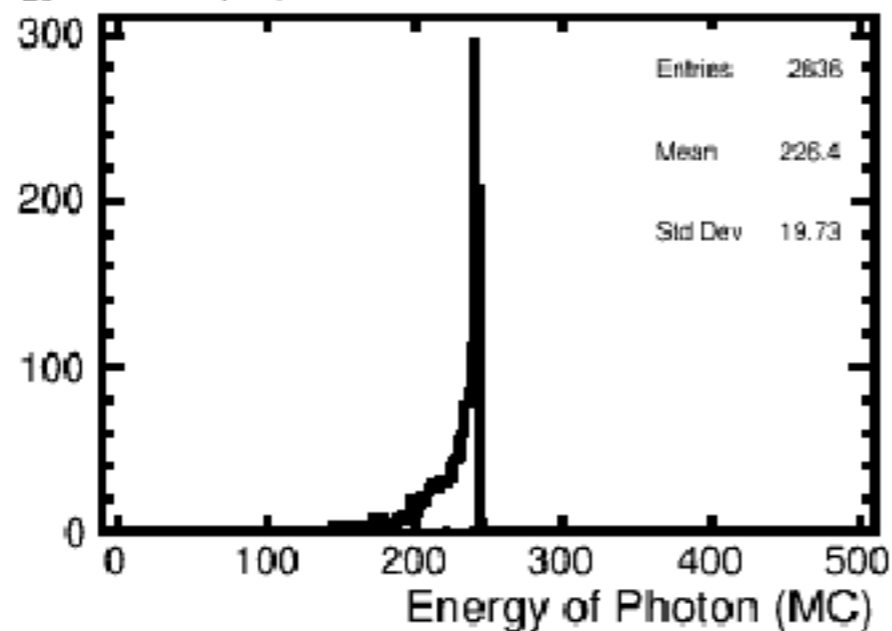
Samples:

$|\cos(\mu)| < 0.75$

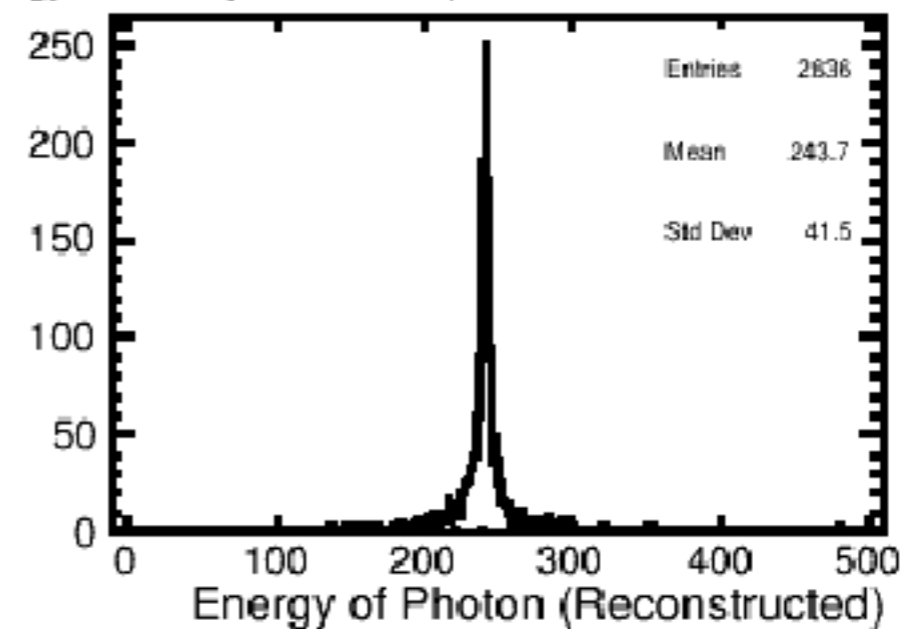
$|M(\mu^+\mu^-) - 91.2| < 10 \text{ GeV}$

Large ILD model

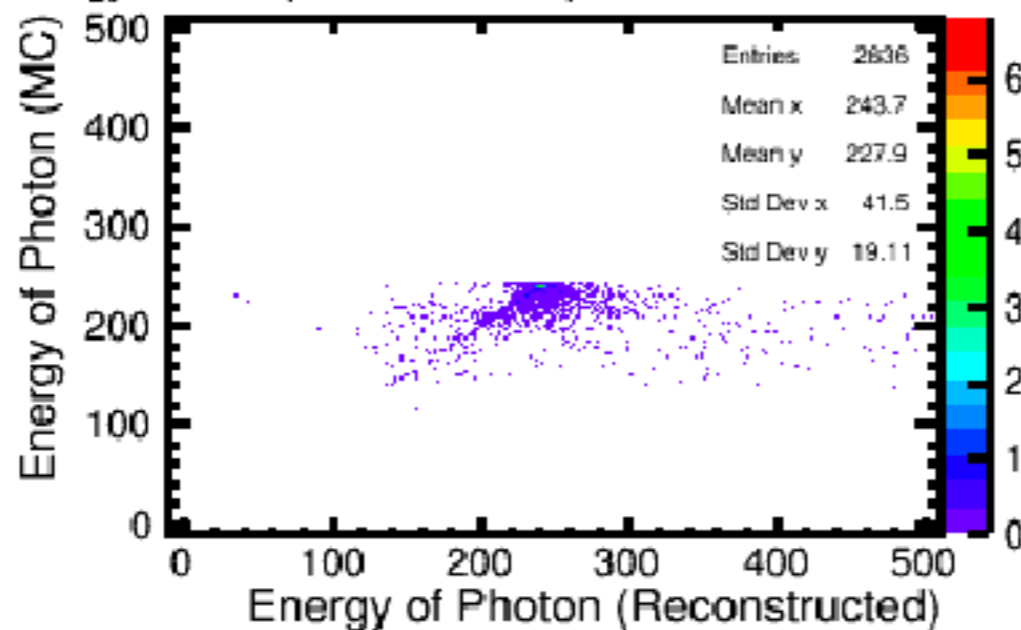
Energy of Photon (MC)



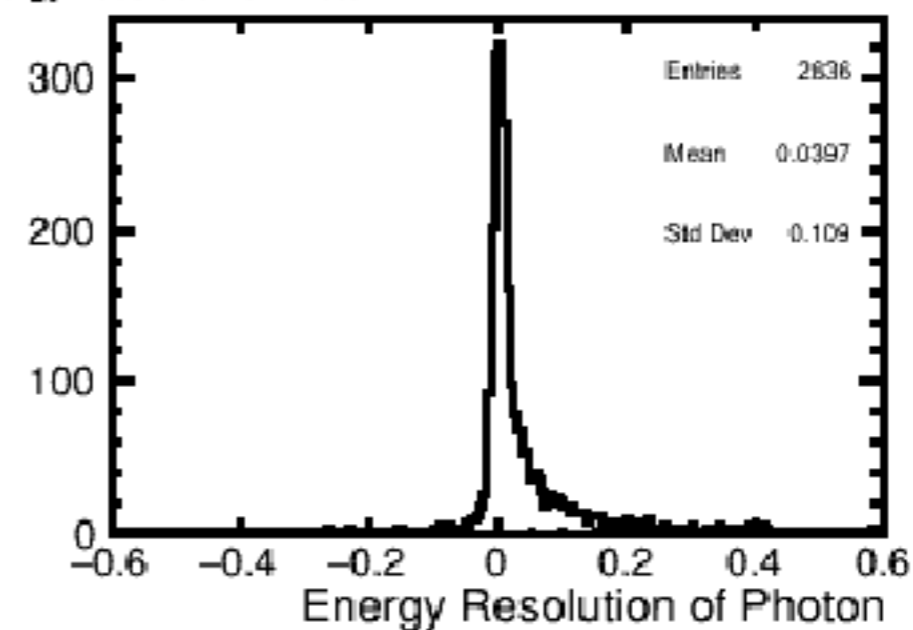
Energy of Photon (Reconstructed)



Energy of Photon (MC:Reconstructed)



Energy Resolution of Photon



Condition 3: Add the effect of **Crossing Angle**⁸

Using $(\theta_{\mu^-}, \theta_{\mu^+}, \theta_r, \phi_{\mu^-}, \phi_{\mu^+}, \phi_r)$

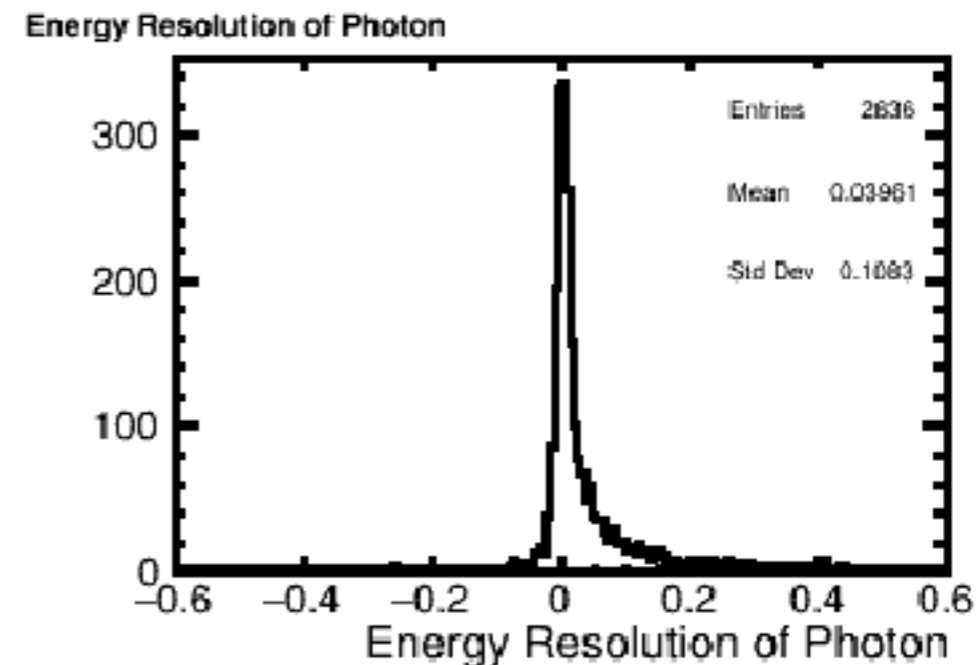
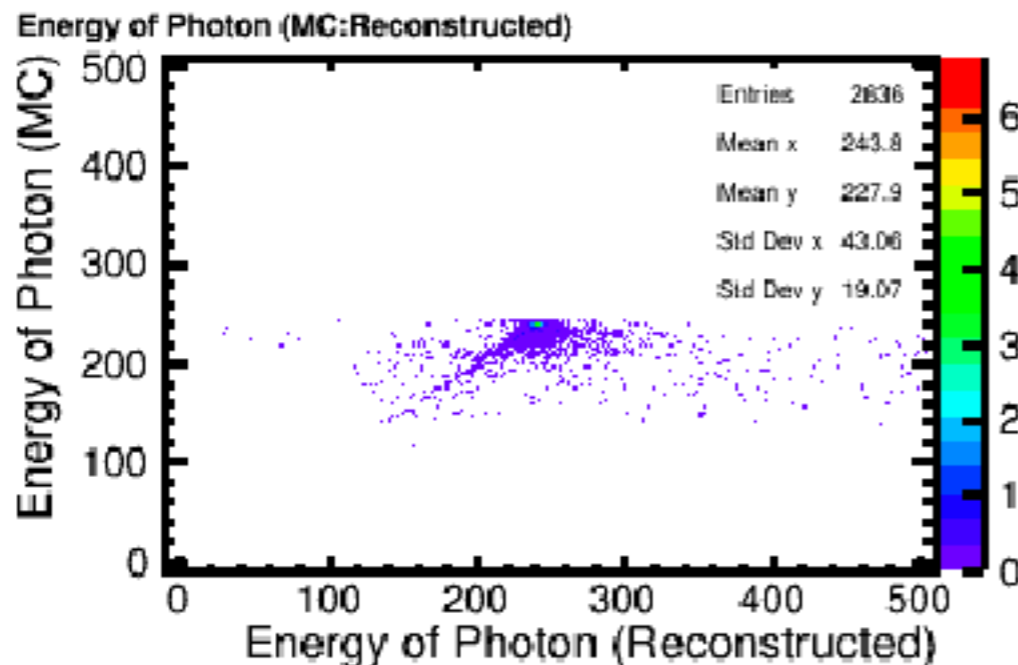
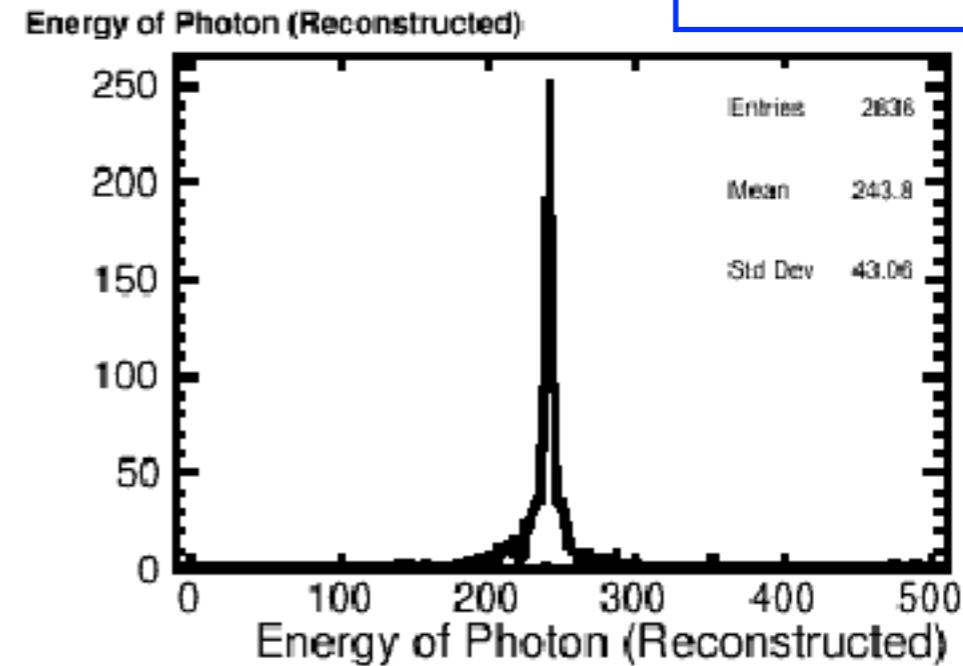
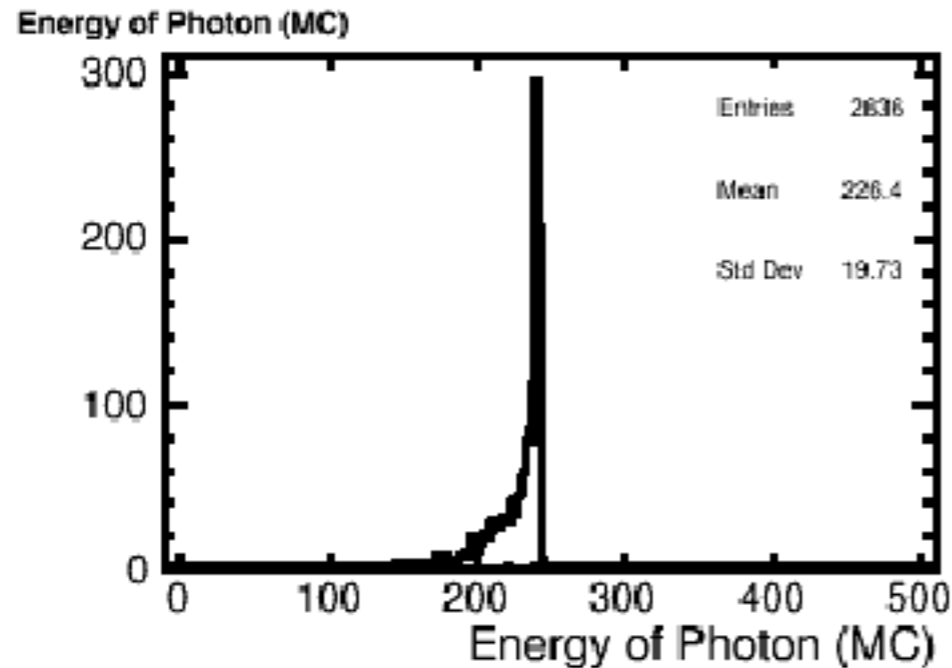
-> Determine $(E_{\mu^-}, E_{\mu^+}, E_r, E_{ISR})$

Samples:

$|\cos(\mu)| < 0.75$

$|M(\mu^+\mu^-) - 91.2| < 10$ GeV

Large ILD model



Next Step

- I will try below

Condition 4: With ISR and the effect of Crossing Angle
Using $(\theta_{\mu-}, \theta_{\mu+}, \theta_{\gamma}, \phi_{\mu-}, \phi_{\mu+}, \phi_{\gamma}, E_{\mu-}, E_{\mu+})$
-> Determine (E_{γ}, E_{ISR})

and compare the energy resolution.