Deep Learning Studies with the CALICE AHCAL Technological Prototype

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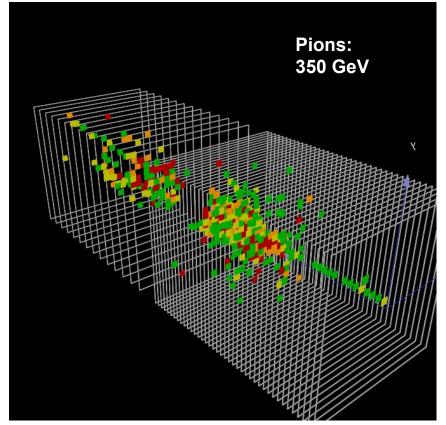








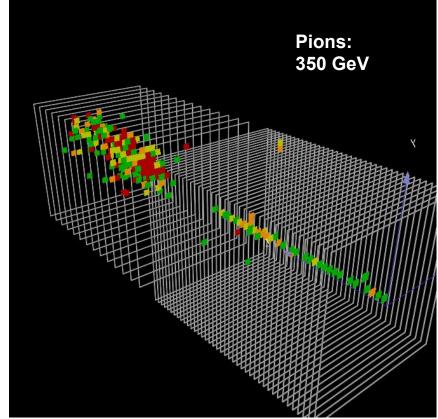








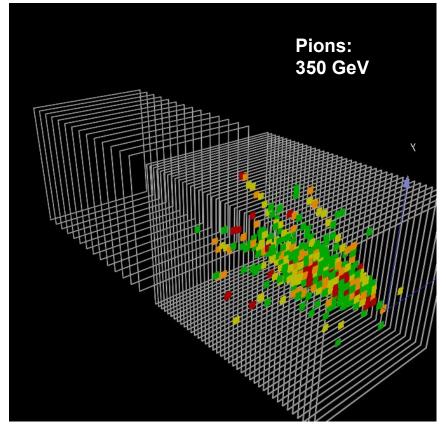












Deep Learned Calorimetry





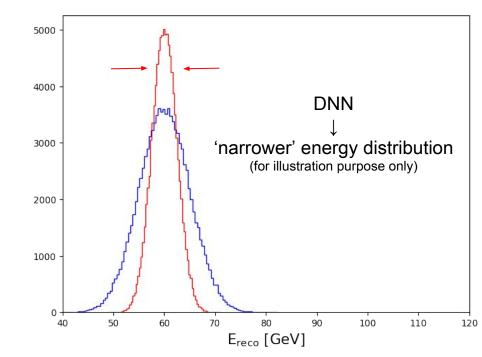
Can we analyze the "shower images" using Deep Learning?

Test beam environment:

- → labeled experimental data
- → training on data possible (instead of Monte Carlo)

Machine learning task:

- → reconstruct particle energy
- → using low level information of the highly granular calorimeter

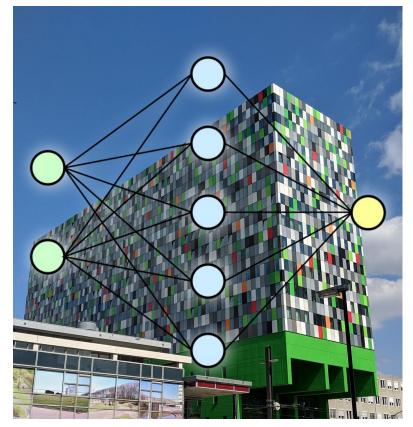


Deep Learning





- Image analysis with machine learning, i.e.
 - Classification → What particle?
 - Regression → What energy?
- Deep Neural Network (DNN) based on connection of different layers of "neurons"
- Deep Learning with data set of <u>low-level variables</u>
- Different types of layers in use
 - → Network "architecture"
- Training of connections as iterative process on labeled data set



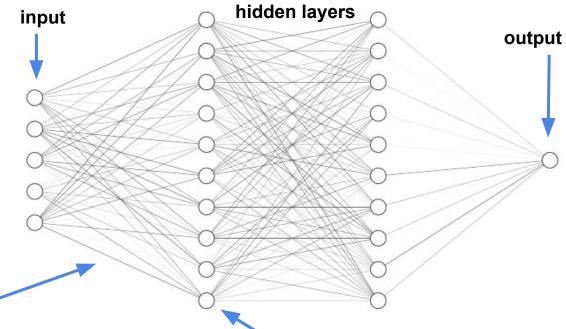
Fully Connected Layer







- Row of neurons = 1 "layer"
- During training connections are strengthened or weakened



trainable weights

Activation function, i.e.: ReLU $\max(0, x)$

Convolutional Layer



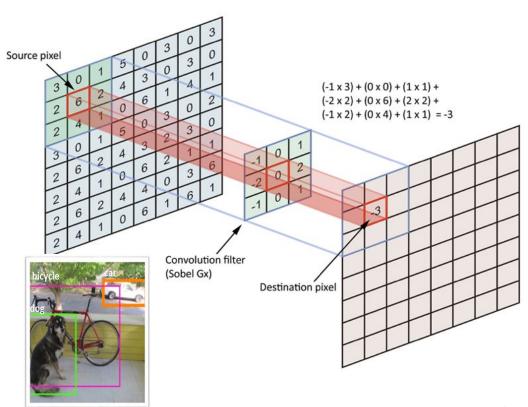


 Output value of convolutional kernel:

$$O_{conv} = (w_1 E_1 + w_2 E_2 + w_3 E_3 + \dots) + b$$

Shared weights

- Multiple filters used to learn different features of the image
- Same filter (here 3 x 3) is used at every position
 - → 9 trainable weights



Locally Connected Layer



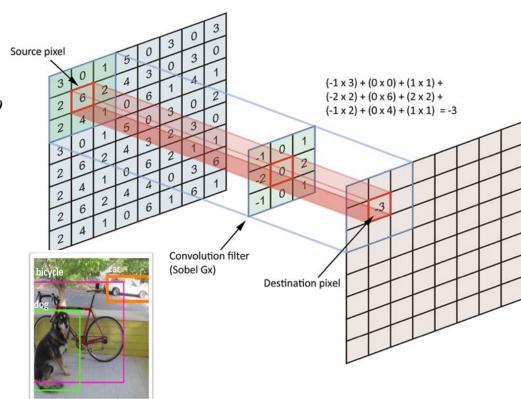


 Output value of convolutional kernel:

$$O_{conv} = (w_1 E_1 + w_2 E_2 + w_3 E_3 + \dots) + b$$

Unshared weights

- Multiple filters used to learn different features of the image
- New filter (here 3 x 3) is used at every position
 - → Localized filters
 - \rightarrow 36 x 9 = 324 trainable weights

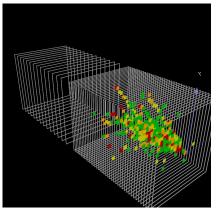


Input & Preprocessing





- Pion data from May 2018 testbeam @ SPS
 - Reconstruction performed with CALICE software
- "Shower images" as (24,24,38) arrays
 - With hit energies at (I,J,K) coordinates
- Ground truth values: known beam energies
- N_{hits} cuts for "Gaussian" distribution in event energy
 - o nHits in first & last 2 layers < 10 & energy dependent total nHits cut
- Applied rough MIP to TeV conversion factor = 2.9E-5
- Sample of 50,000 events per energy
 - 60 % for training, 20 % for validation & testing
 - Beam energies: 10, 15, 20, 30, 40, 50, 60, 80, 100, 120 & 160 GeV
 - Training sample with only every second beam energy (!)
- Two test samples ("trained on" & "NOT trained on")
 - Can network reconstruct energies it was NOT trained on?





Input & Preprocessing

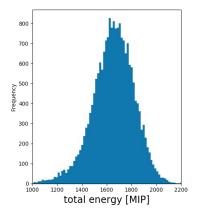
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DER FORSCHUNG | DER BILDUNG



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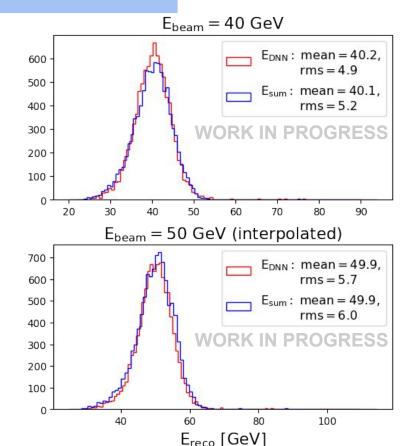
3D Conv. Filter Size = (24,24,38)





- One trainable Convolutional Layer with size of detector
- Output: Weighted sum of all channels
- Better performance than energy sum
- No systematic difference between "trained on" and "NOT trained on" energies

$$E_{DNN} = \sum_{i} E_{i} w_{i} \cdot f_{MIP2GeV}$$
 ~ 22,000 weights



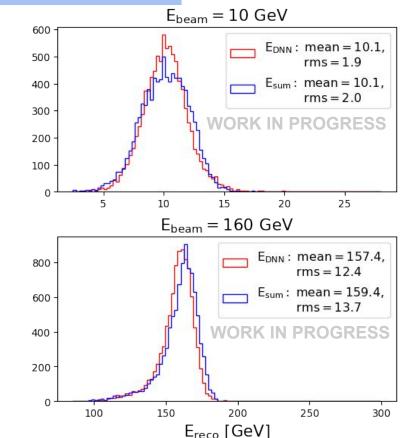
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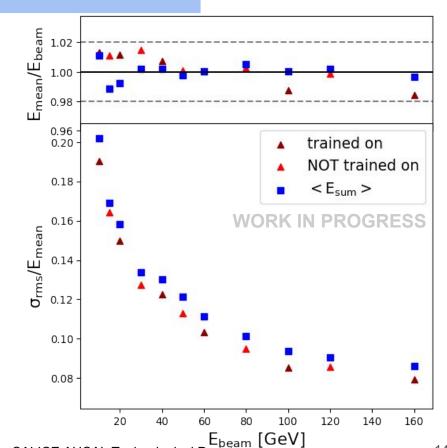
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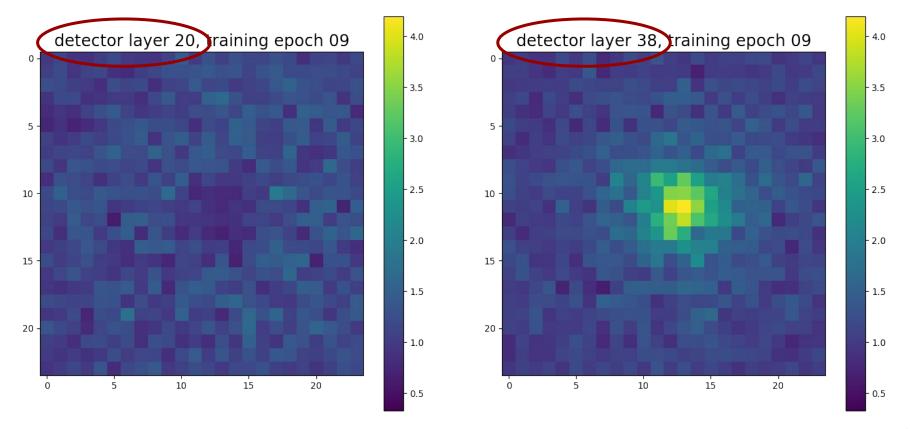
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 ~ 22,000 weights



Learned Weights





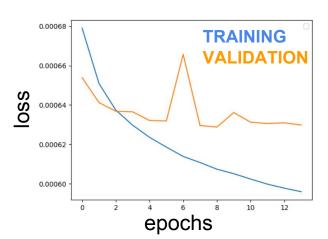


Comparison of Loss Functions





→ The <u>loss function</u> is **minimized during training** and used to adjust the weights after each training interval.



Options compared:

1) mean squared error (MSE):

$$L(E_{i,true}, E_{i,pred}) = \frac{1}{N} \sum_{i} (E_{i,pred} - E_{i,true})^{2}$$

2) mean squared relative error (MSRE):

$$L(E_{i,true}, E_{i,pred}) = \frac{1}{N} \sum_{i} \left(\frac{E_{i,pred} - E_{i,true}}{E_{i,true}} \right)^{2}$$

3) mean relative squared error (MRSE):

$$L(E_{i,true}, E_{i,pred}) = \frac{1}{N} \sum_{i} \left(\frac{E_{i,true} - E_{i,pred}}{\sqrt{E_{i,true}}} \right)^{2}$$

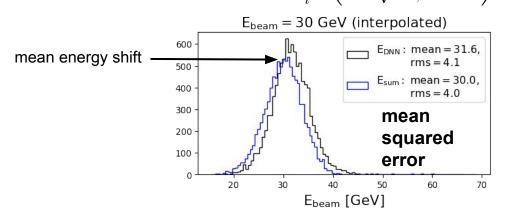
Comparison of Loss Functions



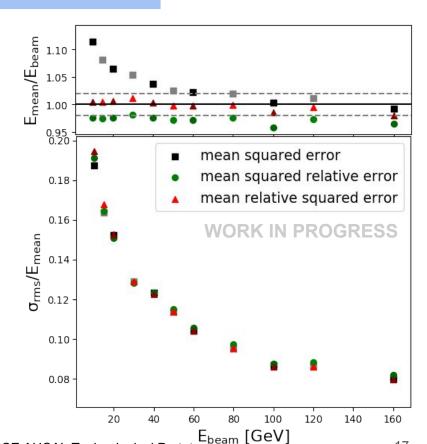


Mean energy is best reconstructed with mean relative squared error as loss:

$$L(E_{i,true}, E_{i,pred}) = \frac{1}{N} \sum_{i} \left(\frac{E_{i,true} - E_{i,pred}}{\sqrt{E_{i,true}}} \right)^{\frac{1}{2}}$$



→ Explainable with the 1/√E dependence of the calorimeter energy resolution.



Small Locally Connected Layers





- Fully Connected Network for each input channel
 - Learns per channel MIP to TeV conversion
- Implemented with Locally Connected Layer
 - Unshared weights
 - Kernel size = (1)

$$I'_{i,b} = \sum_{a} (I_{i,a} \circ W^b_{i,a}) + B^b_i$$

I': Output matrix

I: Input matrix

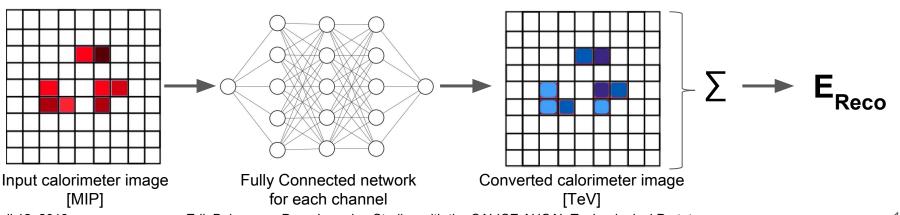
W: Weights

B: Bias

i: Input length (for 1D)

a: Input channel dimensions

b: Output channel dimensions



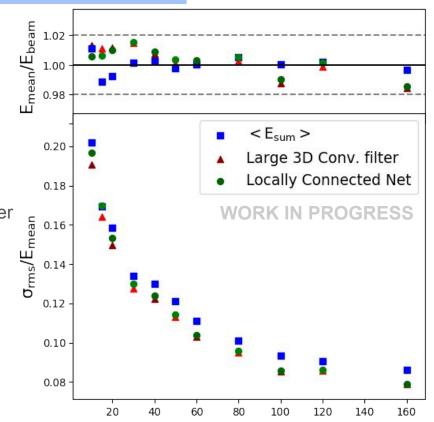
Small Locally Connected Layers





Network architecture:

- 1 layer with 32 channels
- Linear activation function & no bias
- Training procedure:
 - i. Train with shared weights (Conv. Layer)
 - ii. Transfer weights to Locally Connected Layer
 - iii. Train transferred unshared weights
- → Network performs worse for low energies & similar for high energies in comparison to implementation with large Convolutional Layer



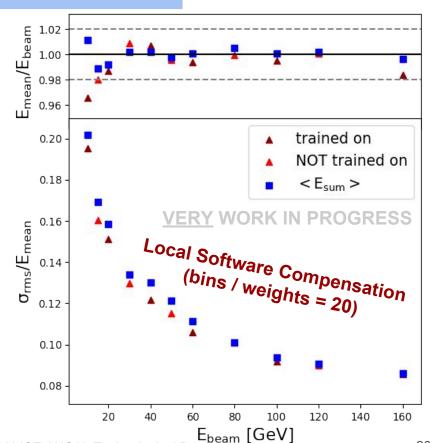
Current Studies





- More layers & training on simulation samples with 1 GeV beam energy steps
 → Currently working on event selection
- Next: Locally Connected architecture in front of Convolutional Neural Network

For comparison:
 Implementation of Local Software
 Compensation as Keras / Tensorflow
 → Non-linearity at low energies



Summary & Outlook





Summary:

- Highly granular calorimeters offer interesting applications for deep learning studies in particle physics
- Test beam data offers possibility for training on labeled experimental data
- Simple network architecture can interpolate for energies not trained on

Outlook:

- Deeper architectures for energy reconstruction; comparison to offline compensation algorithms
- Adding timing information to input
- DNN for shower separation

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Thank you!

Summary:

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Outlook:

- Deeper architectures for energy reconstruction; comparison to offline compensation algorithms
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Bonus Slides





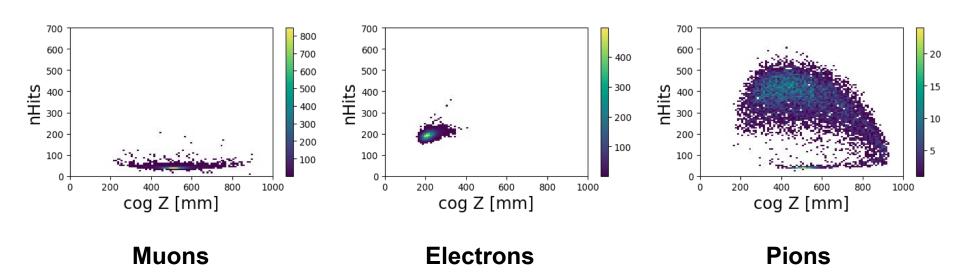


2.) Classification: Particle ID





Task: Classification of 50 GeV events into muons, electrons or pions



2.) Classification: Particle ID

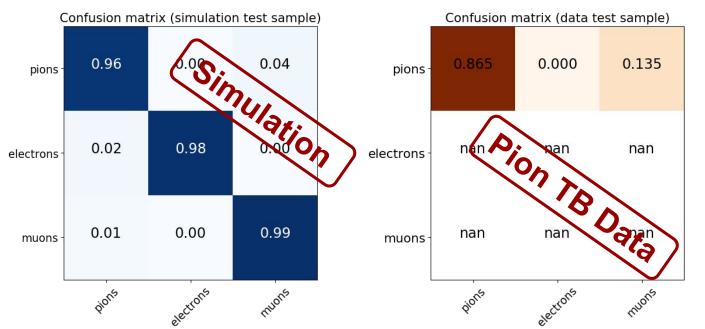




Classification: Identify particle as Pion, Electron or Muon

VGG-16 inspired network was used (CNN, filter size = (3,3,3,X))

Trained on simulation → Tested on simulation & data

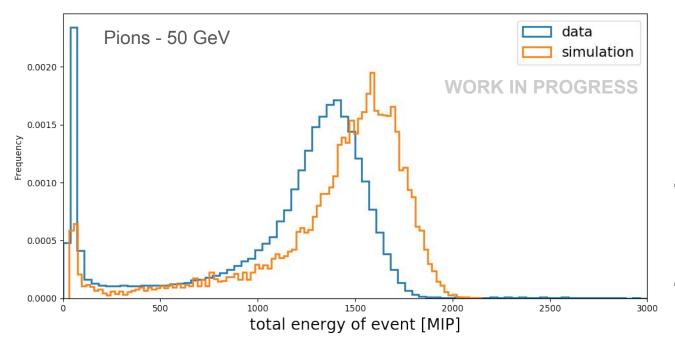


- CNN classifies simulated particles well
- → Simulation needs to improve to apply CNN classifier to data

2.) Classification: Particle ID







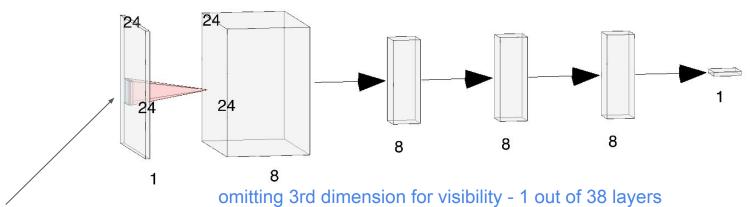
- Difference in total energy between simulation and data
- Need to improve simulation for trustworthy training

Studies with Deep Neural Networks





- Deep Neural Networks (DNN) can learn complex functions
- Convolutional layer + fully connected network
- Many trainable parameters (here: 1.4 M)
- Learns "trained on" energies, does not work well for "NOT trained on" ones



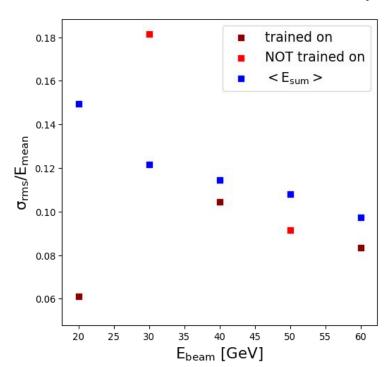
(3D conv. Kernel size = (8, 6, 6, 12))

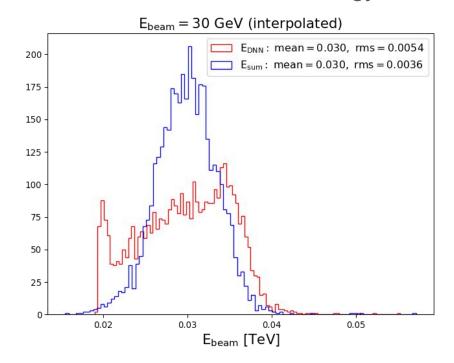
Deep Network Performance





For data set: 20 - 60 GeV → Bad performance for a "NOT trained on" energy



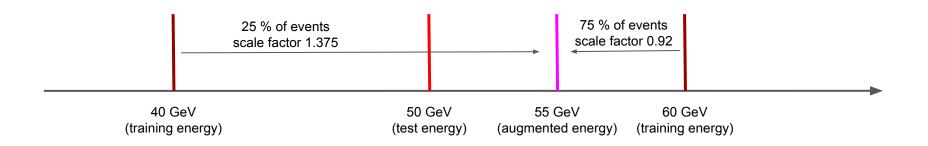


Hit Energy Augmentation





- Assuming linear scaling of hit energies with beam energy
- Filling energy regions without data by linear scaling of data
 - From 1 169 GeV in 1 GeV steps
 - Choosing energy for scaling weighted by energy gap
 - Augmented training set = 3x regular training set

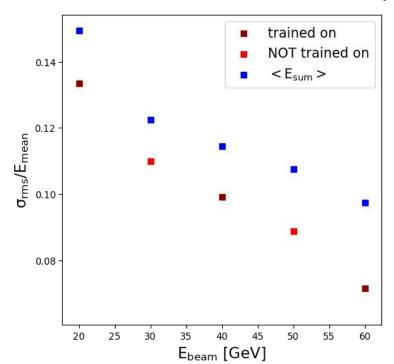


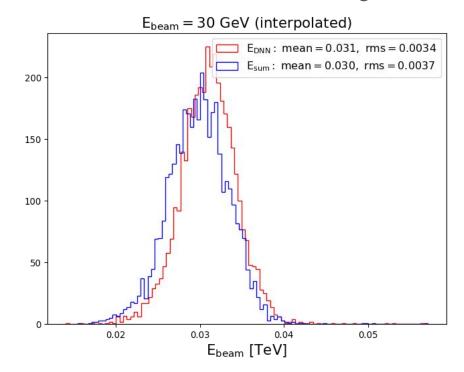
Hit Energy Augmentation





For data set: 20 - 60 GeV → Better performance for "NOT trained on" energies





Training & Testing Process





Training on sample with energies 10, 20, 40, 60, 100 & 160 GeV

Validate model with Loss evaluation validation sample (same energies, different events)

Test model on test sample 1 (same energies as training, different events)

> Predict energies & create histograms

Fit gaussian on histograms for comparison

Test model on test sample 2 (other energies, different events)

> Predict energies & create histograms

Fit gaussian on histograms for comparison

Compare:

Loss Function (performance evaluation)





Example 1) Mean Squared Error (MSE):

$$L(E_{i,true}, E_{i,pred}) = \frac{1}{N} \sum_{i} (E_{i,pred} - E_{i,true})^{2}$$

Example 2) Mean Squared Relative Error (MSRE):

$$L(E_{i,true}, E_{i,pred}) = \frac{1}{N} \sum_{i} \left(\frac{E_{i,pred} - E_{i,true}}{E_{i,true}} \right)^{2}$$

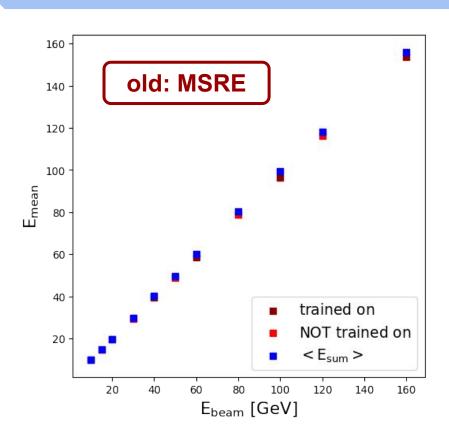
Example 3) Mean Relative Squared Error (MRSE):

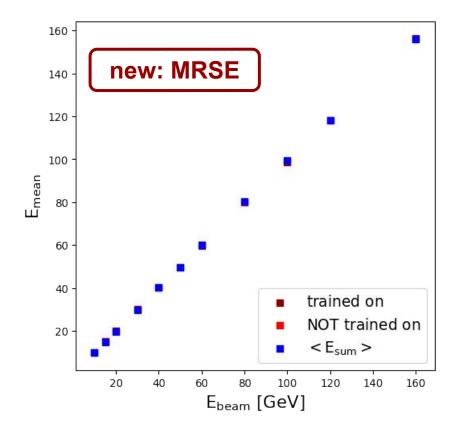
$$L(E_{i,true}, E_{i,pred}) = \frac{1}{N} \sum_{i} \left(\frac{E_{i,true} - E_{i,pred}}{\sqrt{E_{i,true}}} \right)^{2}$$

MSRE vs MRSE







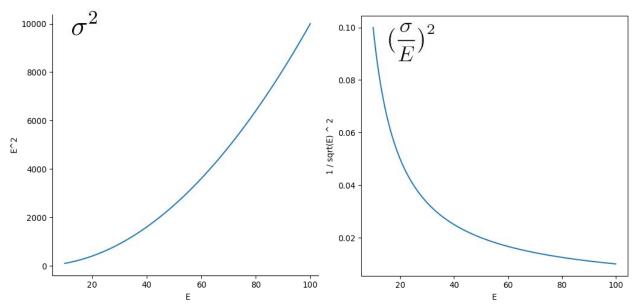


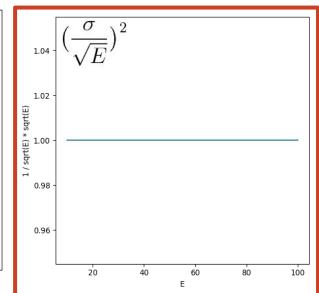
April 12, 2019

Function Comparison









LC weight heatmaps (after transfer)

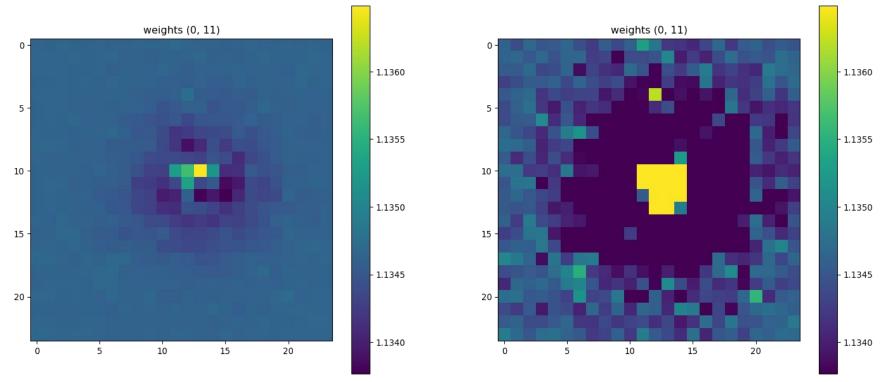




detector_layer 18, network_layer 1 epoch 001

detector layer 18, network layer 1, epoch 009



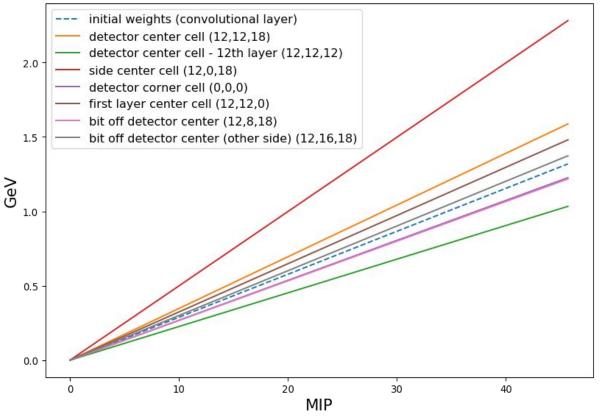


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LC calibration functions







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