



# Wakefield effects in the CLIC BDS

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# Motivation



- ▶ Understand the limitations of beam pipe apertures in the CLIC Beam Delivery System
- ▶ Ensure the beam stability and luminosity performance
- ▶ Propose an aperture model for CLIC BDS for further use, e.g. in synchrotron radiation reflections study

# Beam pipe aperture limits

- ▶ Resistive wall wake fields have been calculated assuming round beam pipes made of copper with conductivity of  $5.96 \cdot 10^7$  S/m, or steel with  $1.45 \cdot 10^6$  S/m
- ▶ Assumed maximal magnetic field at a pole of normal-conducting quadrupoles:  $\sim 1.5$  T
- ▶ Collimation depth for 380 GeV machine assumed to be the same as for 500 GeV and 3 TeV designs:  $15\sigma_x$  and  $55\sigma_y$ <sup>1</sup>
- ▶ Inner aperture calculation follows the formula:

$$R_{\text{inner}} = \max\{r_{\text{wake}}, 0.1 + \max\{15\sigma_x, 55\sigma_y\}\}, \quad (1)$$

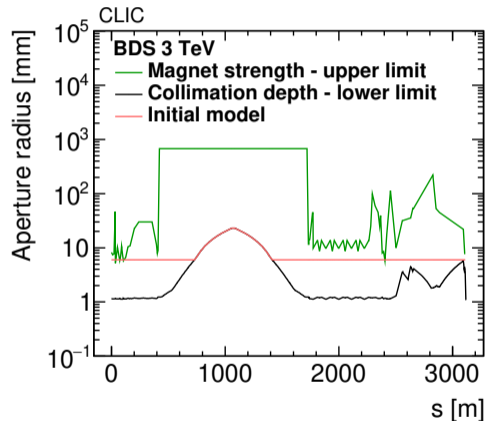
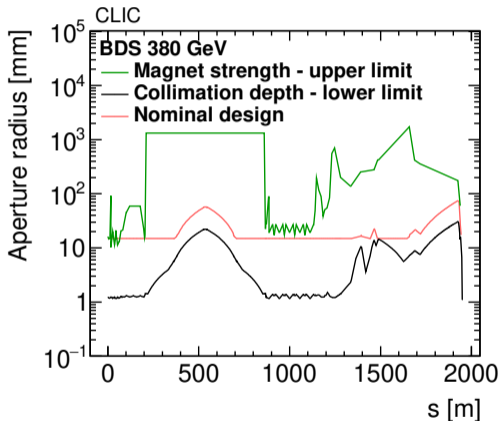
where:  $r_{\text{wake}}$  based on the previous resistive wall wakefield study<sup>2</sup>: 15 mm at 380 GeV (scaled from 500 GeV), and 6 mm at 3 TeV, and beam sizes with  $\beta$  functions coming from MAD-X:

$$\sigma_{x,y} = \sqrt{\varepsilon_{x,y}\beta_{x,y} + (D_{x,y}\delta_E)^2}, \quad (2)$$

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<sup>1</sup>From Optimization of CLIC Baseline Collimation System

<sup>2</sup>From Multi-bunch effect of resistive wall in the BDS of the CLIC



- ▶ Apertures significantly larger at 380 GeV
- ▶ A few problematic points, can be addressed by extending the magnet lengths

- ▶ Resistive wall effect is a result of finite vacuum chamber conductivity
- ▶ The surface current is delayed with respect to the source and the electric field can interact with the charged particles on the short- and long range

Classical formula of the resistive wall wake:

$$W(z) = -L \frac{c}{\pi b^3} \sqrt{\frac{Z_0}{\pi z \sigma}}, \quad (3)$$

where:  $Z_0$  - impedance of the vacuum,  $z$  - longitudinal distance between the source and the impacted particle,  $b$  - aperture radius,  $\sigma$  - conductivity of the wall,  $L$  - length of the accelerator element

- ▶ Assumed are thick walls, ultra-relativistic particles
- ▶ Only fundamental transverse mode ( $m = 1$ ) is considered
- ▶ In simulations the wakefield effects are imposed by modifying the momenta distributions by:

$$\Delta x'_k(s) = \frac{e^2}{E_0} \sum_{j=1}^{k-1} N_j \langle x \rangle_j W(\Delta z), \quad (4)$$

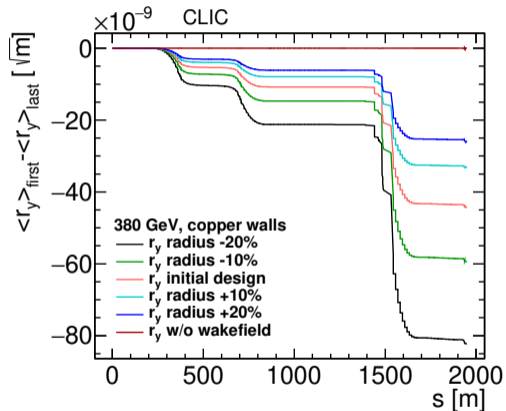
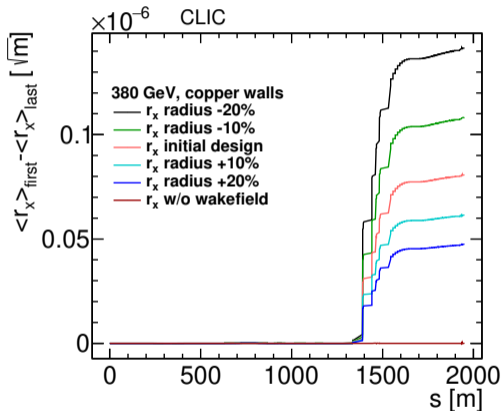
where:  $e$  - electron charge,  $E_0$  - beam energy,  $N_j$  - number of charges,  $\langle x \rangle_j$  - centre of gravity in slice  $j$ ,  $\Delta z$  - distance between slices

- ▶ Bunch trains are created at the beginning of the BDS with a uniform offset of  $+0.5 \sigma_{x,y}$  for all bunches (=worst-case scenario)
- ▶ PyHEADTAIL does linear tracking with multibunch wakefield effects up to the IP
- ▶ Impact on the beam quality checked by comparing radii of the normalised phase space between the first and last bunch, defined as:

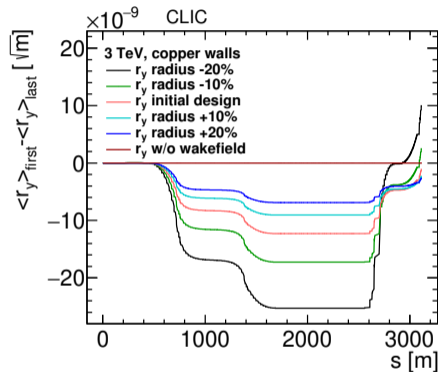
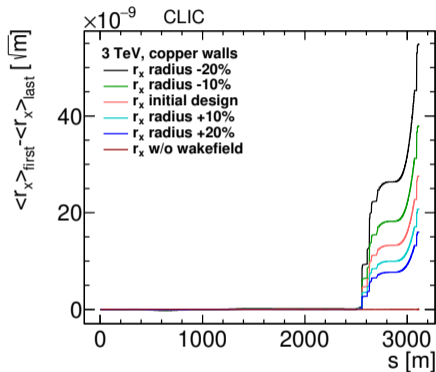
$$r_{x,y}(s)[\sqrt{m}] = \sqrt{\left(\frac{x(s)}{\sqrt{\beta_s}}\right)^2 + \left(\frac{x(s)\alpha_s + x'(s)\beta_s}{\sqrt{\beta_s}}\right)^2}, \quad (5)$$

where:  $\alpha_s, \beta_s$  - betatron functions,  $x$  - bunch centre position,  $x'$  - average bunch angle

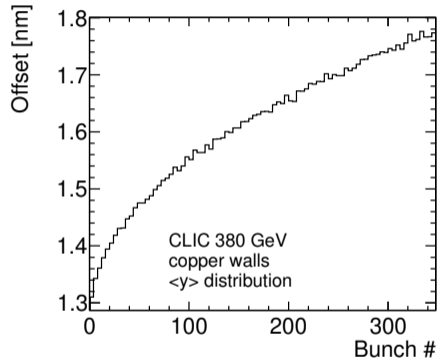
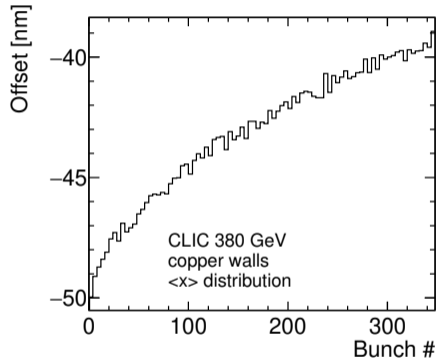
- ▶ Impact on the luminosity checked by calculating the two-beam luminosity in Guinea-Pig, where a beam transported through the BDS is duplicated and one of the duplicates is centered at (0,0) while the other is fully impacted by the resistive wall wake
- ▶ Luminosity along the bunch train is compared with a benchmark that was not impacted by wakefields; 1% loss is acceptable



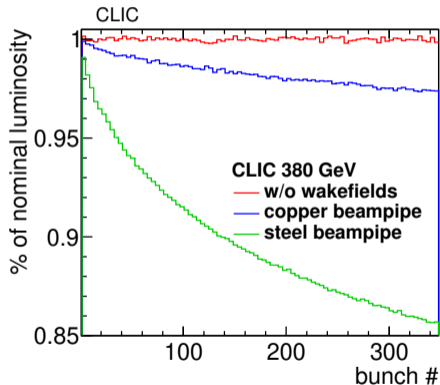
- ▶ The impact of the wakefields concentrates in the FFS ( $s > 1200$  m) in both directions
- ▶ The ordering in response to the varying apertures is as expected



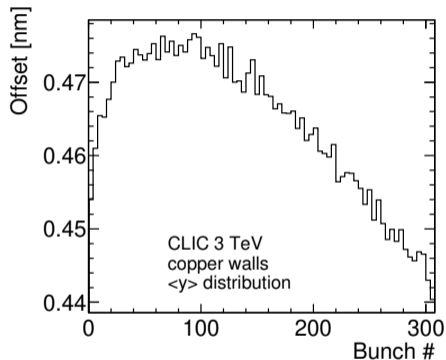
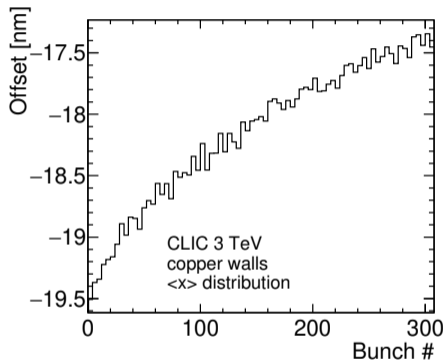
- ▶ Similar to 380 GeV, the impact concentrates in the FFS ( $s > 2300$  m) in the horizontal direction
- ▶ Reverse of the trend in the vertical direction around  $s = 2600$  m
- ▶ The ordering observed at 380 GeV not maintained in the vertical direction - non-monotonic behaviour



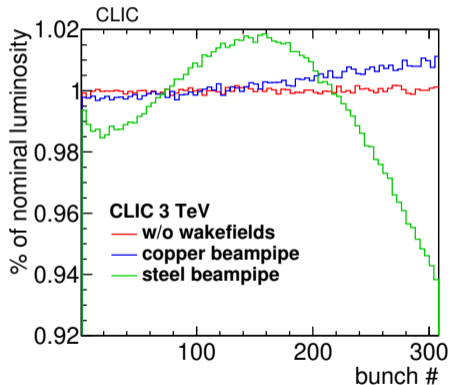
- ▶ Beams are focused in the horizontal direction and defocused in the vertical
- ▶ The vertical defocus effect dominates with 38% difference between the beginning and the end of a train (20% difference in the horizontal direction)



- ▶ Copper beam pipe provides predictable beam behaviour
- ▶ Luminosity loss about 2-3% below benchmark at the end of the train, more than the 1% limit
- ▶ The use of steel leads to stronger impact of the wakefields
- ▶ Luminosity loss has a steeper slope, resulting in about 15% loss at the end of the train



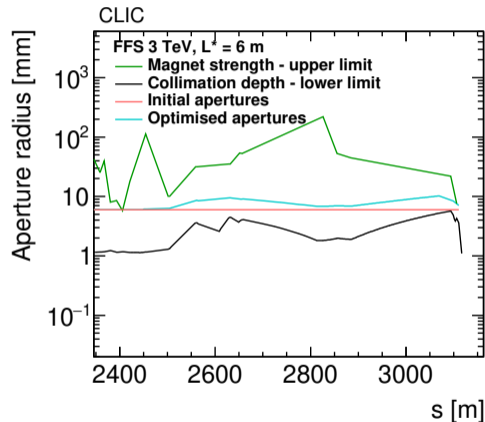
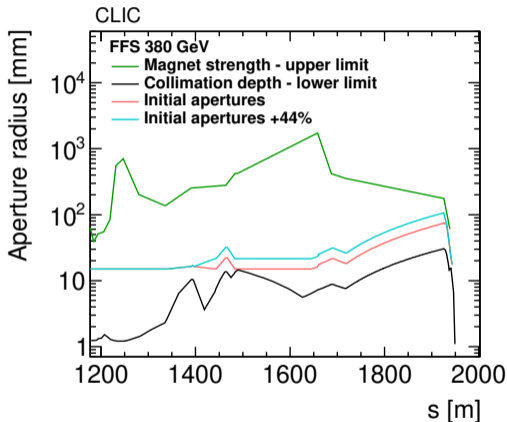
- ▶ Similar behaviour as at 380 GeV, defocusing in horizontal direction and focusing (initially) in the vertical
- ▶ In the first half of the train, the wakefield impact changes the trend of the average vertical bunch position, decreasing the offset



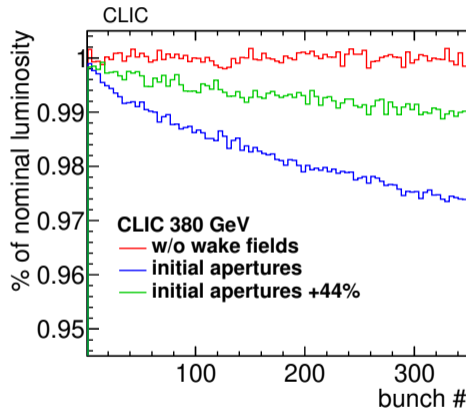
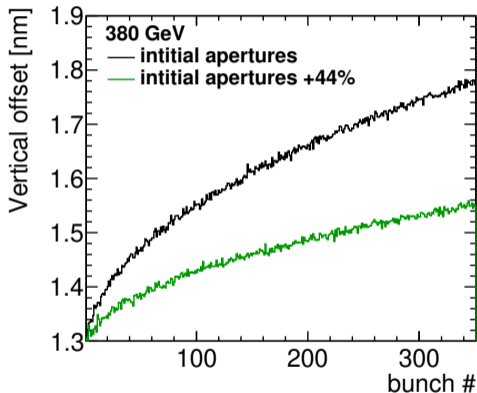
- ▶ Luminosity with copper beam pipe follows the offset distribution, strongly impacted by vertical offset
- ▶ Non-monotonic behaviour in all cases impacted by wakefields
- ▶ More challenging for the intra-train beam feedback to correct
- ▶ Steel not recommended - large total luminosity loss and unstable behaviour
- ▶ The inner radius of 6 mm does not provide the desired luminosity stability and behaviour

- ▶ Mitigation has different goals at each energy stage: limiting luminosity loss at 380 GeV, ensuring monotonic beam behaviour at 3 TeV
- ▶ The wakefields impact concentrates in the FFS at both energy stages
- ▶ At 380 GeV, the wakefields impact and luminosity loss have to be limited by  $\frac{2}{3}$
- ▶ Achievable with a 44% extension of the apertures in the FFS
- ▶ At 3 TeV, the non-monotonic behaviour can be removed if the apertures are extended by a series of constant numbers:

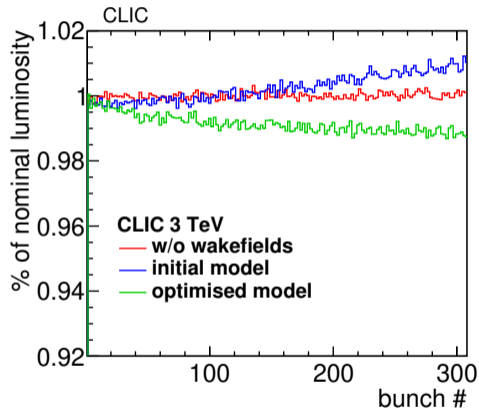
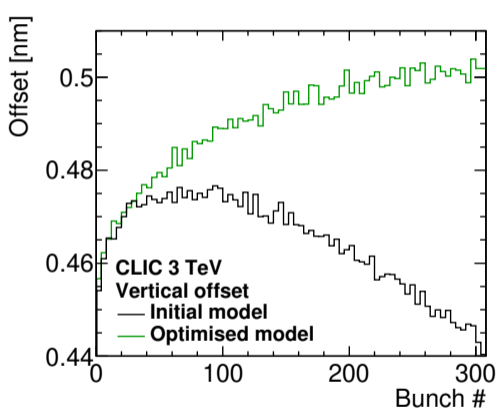
$$a(s)[\text{mm}] = \begin{cases} 3.0 & \text{if } s < 2450 \text{ m} \\ 5.0 & \text{if } 2450 \text{ m} < s < 3090 \text{ m} \\ 3.5 & \text{if } 3090 \text{ m} < s \end{cases}$$



- ▶ At both energy stages the extended apertures can be easily accommodated
- ▶ The apertures of the last magnet of the final doublet remain unchanged due to cost optimisation; this does not impact the mitigation efficiency



- ▶ Extending apertures by 44% reduces the vertical offset by 17% and luminosity loss by a factor of 3
- ▶ The final doublet magnets apertures remain unchanged



- ▶ Vertical offset and luminosity monotonic in the optimised model
- ▶ The luminosity loss at the end of the trend 1% below benchmark

- ▶ Resistive wall wakefield impact concentrates in Final Focus System
- ▶ Steel is not a safe material to use for the beam pipe in the FFS, copper coating in the order of tens of microns necessary
- ▶ Non-monotonic beam and luminosity behaviour observed at 3 TeV
- ▶ Luminosity loss at 380 GeV larger than the 1% goal
- ▶ Most of the luminosity loss from the offset, which can be alternatively cured with intra-train feedback, but the wakefield impact is non-linear thus challenging
- ▶ Extending apertures in the FFS by 44% at 380 GeV and by about 50% at 3 TeV mitigates the wakefields impact

## Outlook:

- ▶ Collimation region resistive wall and geometric wakefields simulations at 380 GeV

# Additional material

- ▶ Macroparticle simulation code library for modeling collective effects beam dynamics in **circular** accelerators
- ▶ Modular software allowing to prepare custom simulation scripts
- ▶ Special approach needed to simulate a linear machine:
  - ▶ Focus on element-by-element beam parameters instead of turn-by-turn
  - ▶ Lattice read from MAD-X Twiss table
  - ▶ Use of pre-calculated wakes
- ▶ Source code and examples available at: [PyHEADTAIL repository](#) and [PyHEADTAIL wiki](#)

