

E-Driven Positron Source capture simulation

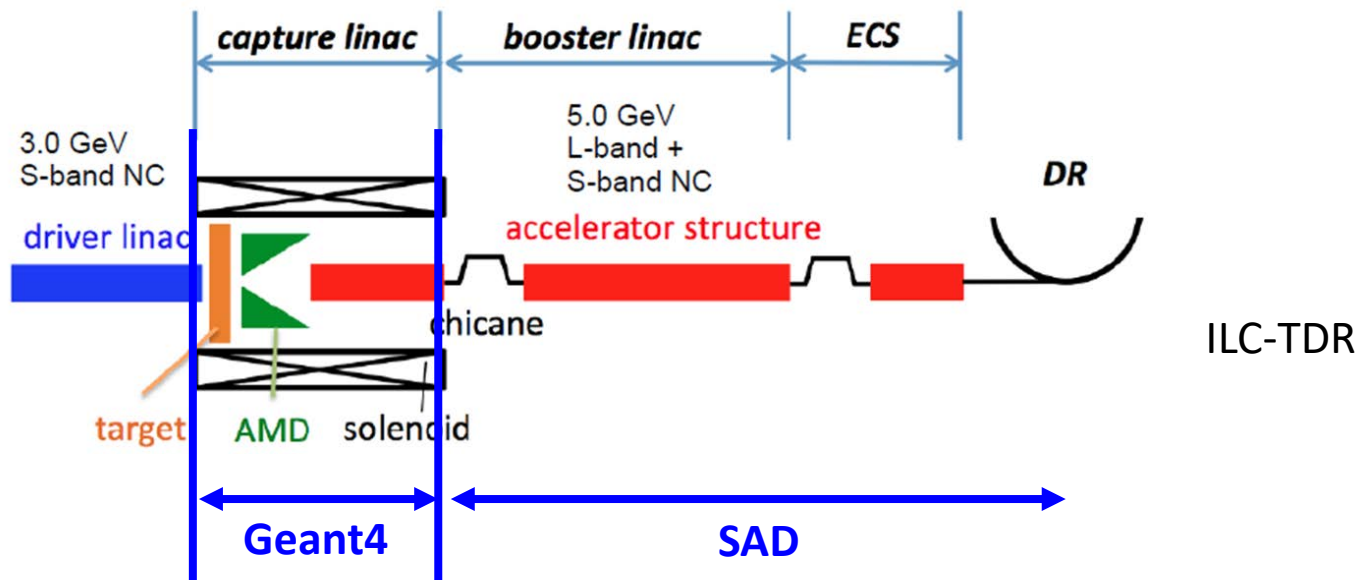
KEK M. Fukuda

Contents

- Tracking Simulation by using Geant4 and SAD
- Comparison of Nagoshi's result and Fukuda's result
- Yield calculation with divided solenoid coils
- Yield calculation when the distance of target and FC is changed

Simulation of ILC positron source for E-driven scheme

The tracking of positrons up to the exit of ECS can be simulated now.



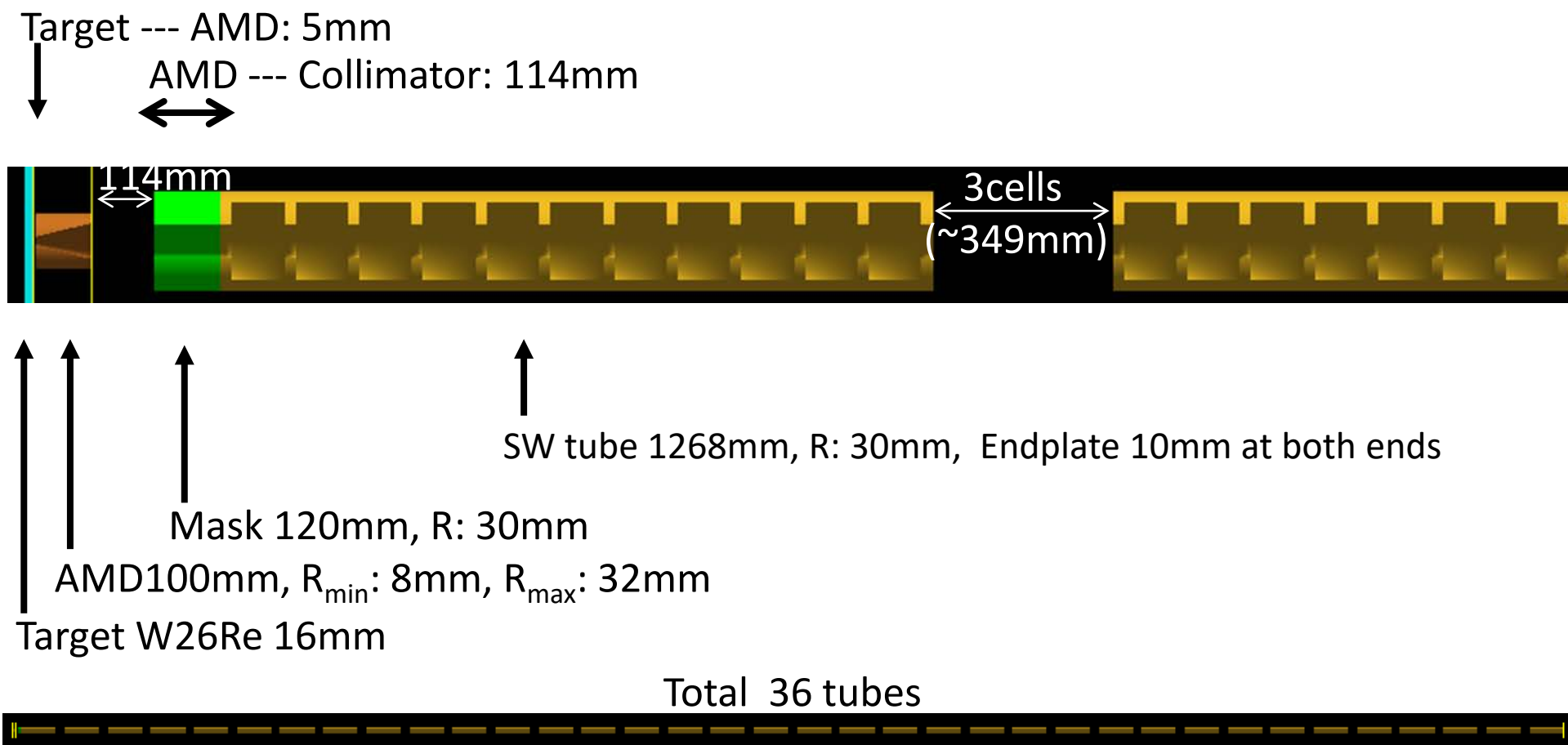
I can calculate the positron yield at DR by using the tracking code which has been succeeded from Kuriki-san and Nagoshi-san.

Positron generation at a target: Geant4

Tracking : Target --- Capture section end(250MeV): Geant4

Tracking: Capture section end --- ECS end: Strategic Accelerator Design (SAD)

Placement of each components for E-driven scheme



Positron generation

Primary e- beam

Energy: 3GeV

Number of electron: 1×10^4

Beam size on the target: 2mm (1σ)

Bunch length: 1mm (1σ)

Target: W26Re, thickness 16mm

Number of generated positrons: 7.17×10^4

W26Re 16mm

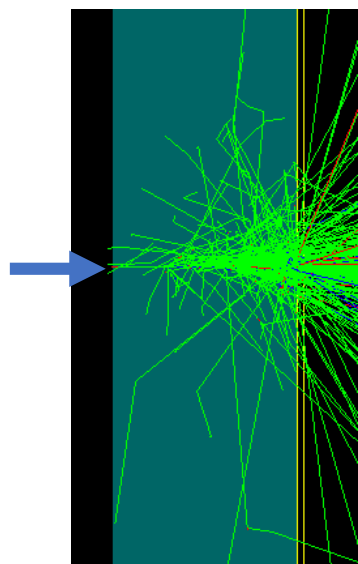
Electron beam

3GeV

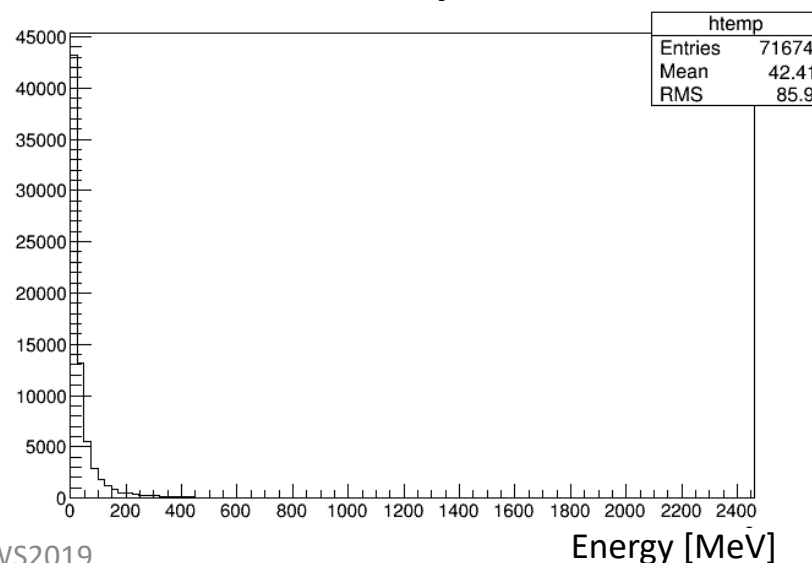
Ne-: 1×10^4

$\sigma_{x,y} = 2\text{mm}$

$\sigma_z = 1\text{mm}$

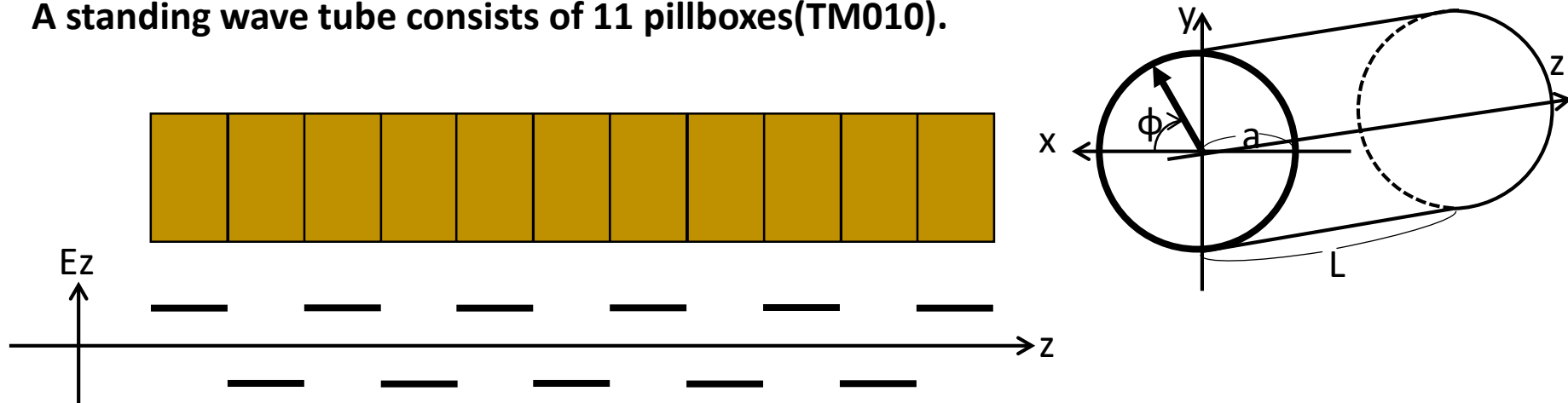


Generated positrons



Accelerating electric field of standing wave tube

A standing wave tube consists of 11 pillboxes(TM010).



The phase is shifted by π for each cell.

$$E_z = E_0 * J_0(p_{01} * r/a) * \sin(\omega t + \text{cavPhase});$$

$$B_\phi = E_0 * J_1(p_{01} * r/a) * \cos(\omega t + \text{cavPhase}) / c_{\text{light}};$$

$$(B_x = B_\phi * (-1.0 * y/r), B_y = B_\phi * (x/r), r = \sqrt{x^2 + y^2})$$

Wave length: $\lambda = 230.60958 \text{ mm}$ (L-band: 1.3GHz)

Radius of cylindrical cavity: $a = p_{01} * \lambda / 2\pi = 88.263 \text{ mm}$

$p_{01} = 2.404825557695772$ (when $J_0(x) = 0$, $x = p_{01}$)

$\omega_{\text{space}} = 2\pi/\lambda$, $\omega_{\text{time}} = 2\pi c/\lambda$

$$E_0 = \pi/2 * E_{\text{acc}}$$

Magnetic field of FC and Solenoid

OMD

FC: the field designed by Pavel Martyshkin by using CST studio.

DC Solenoid in a capture section

One long solenoid coil: 0.5T (Bz const)

Divided solenoid coils (*)

Divided solenoid coil with changed shape (*)

*** No coil at a space between accelerating tubes**

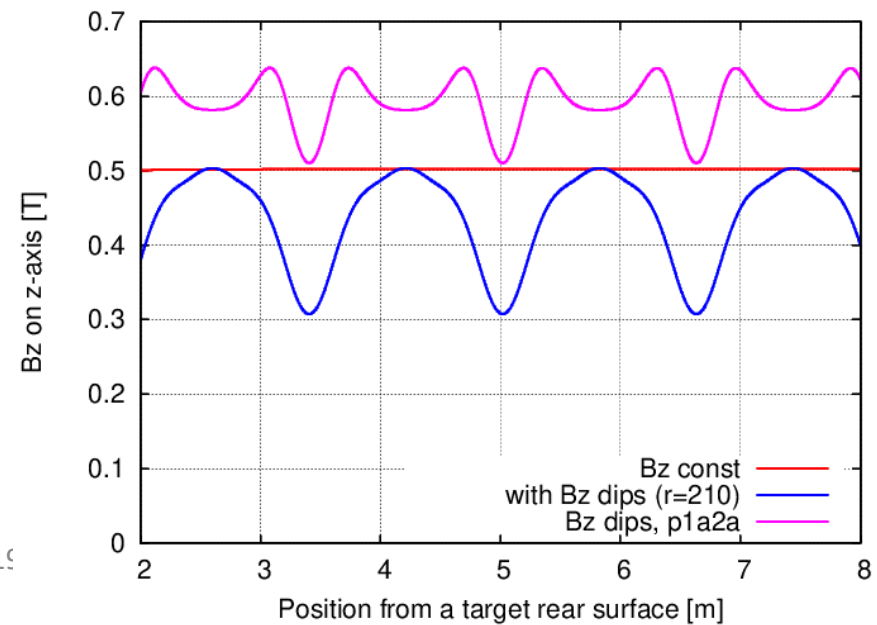
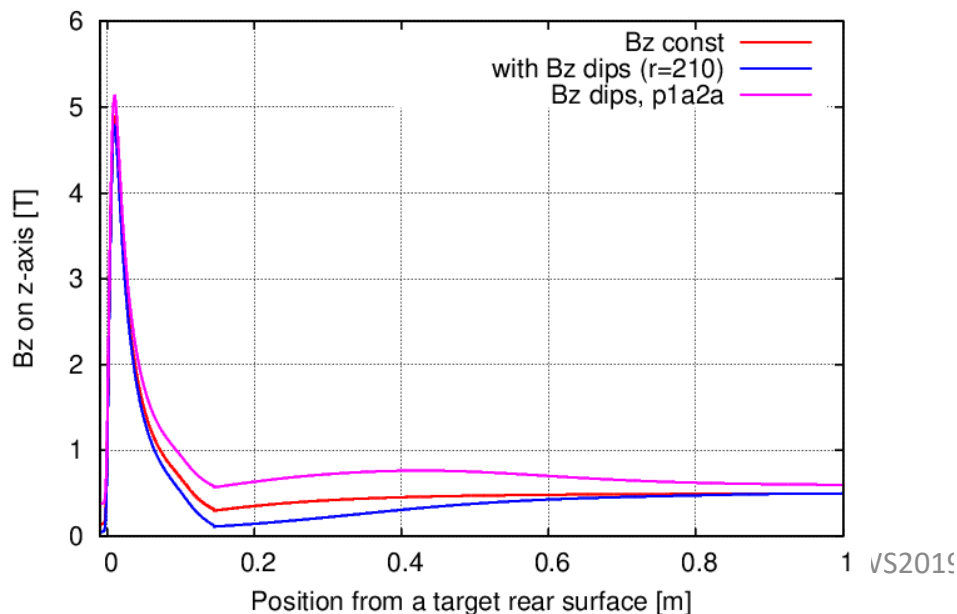
$$B_r^a(r, z) = \sum_{\nu=1}^{\infty} \frac{(-1)^{\nu}}{\nu!(\nu-1)!} B_{z0}^{(2\nu-1)}(z) \left(\frac{r}{2}\right)^{2\nu-1}$$

$$= -\frac{B'_{z0}(z)}{2}r + \frac{B_{z0}^{(3)}(z)}{16}r^3 - \frac{B_{z0}^{(5)}(z)}{384}r^5 + \frac{B_{z0}^{(7)}(z)}{18432}r^7 - \frac{B_{z0}^{(9)}(z)}{1474560}r^9 + \dots$$

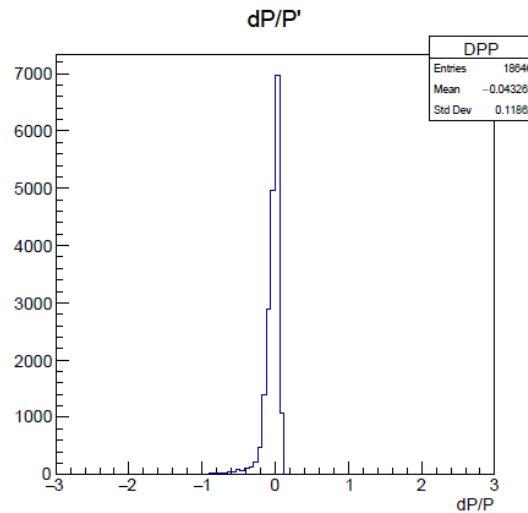
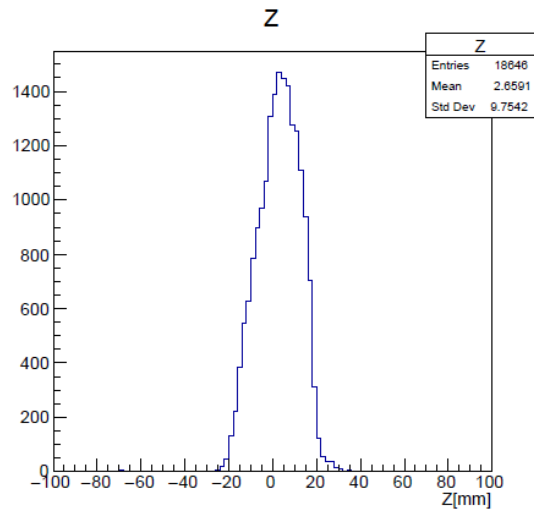
$$B_z^a(r, z) = \sum_{\nu=0}^{\infty} \frac{(-1)^{\nu}}{(\nu!)^2} B_{z0}^{(2\nu)}(z) \left(\frac{r}{2}\right)^{2\nu}$$

$$= B_{z0}(z) - \frac{B''_{z0}(z)}{4}r^2 + \frac{B_{z0}^{(4)}(z)}{64}r^4 - \frac{B_{z0}^{(6)}(z)}{2304}r^6 + \frac{B_{z0}^{(8)}(z)}{147456}r^8 + \dots$$

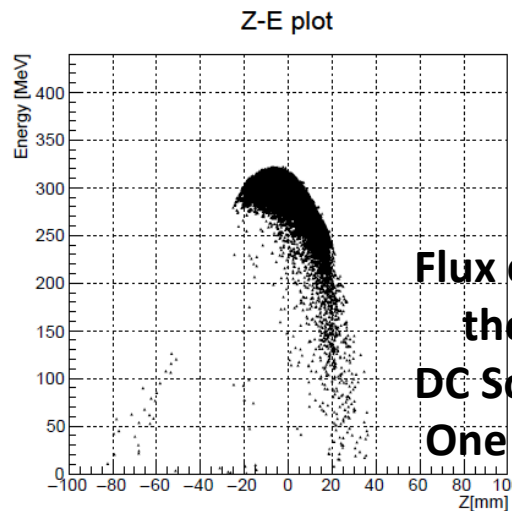
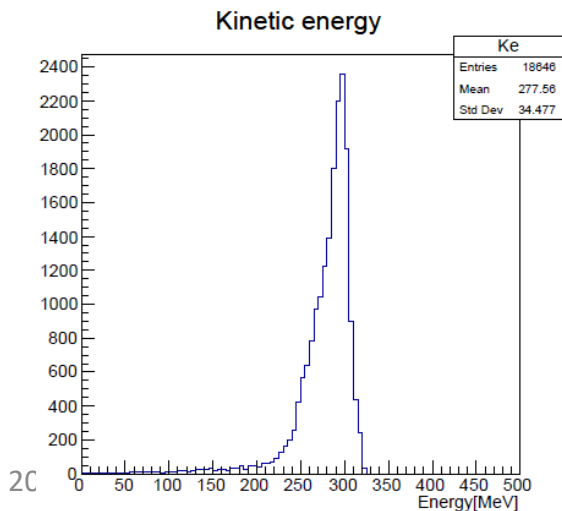
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Positron distribution at Capture end



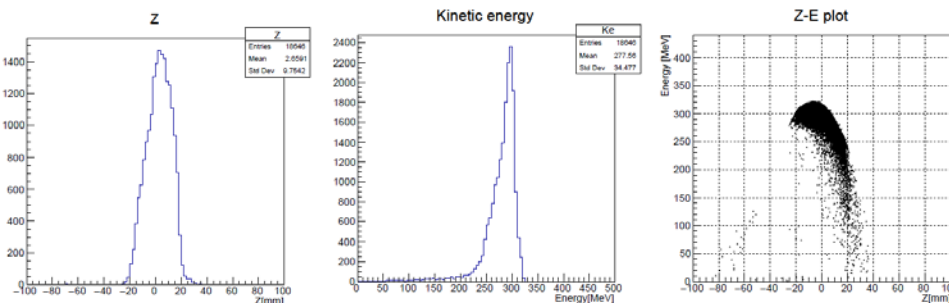
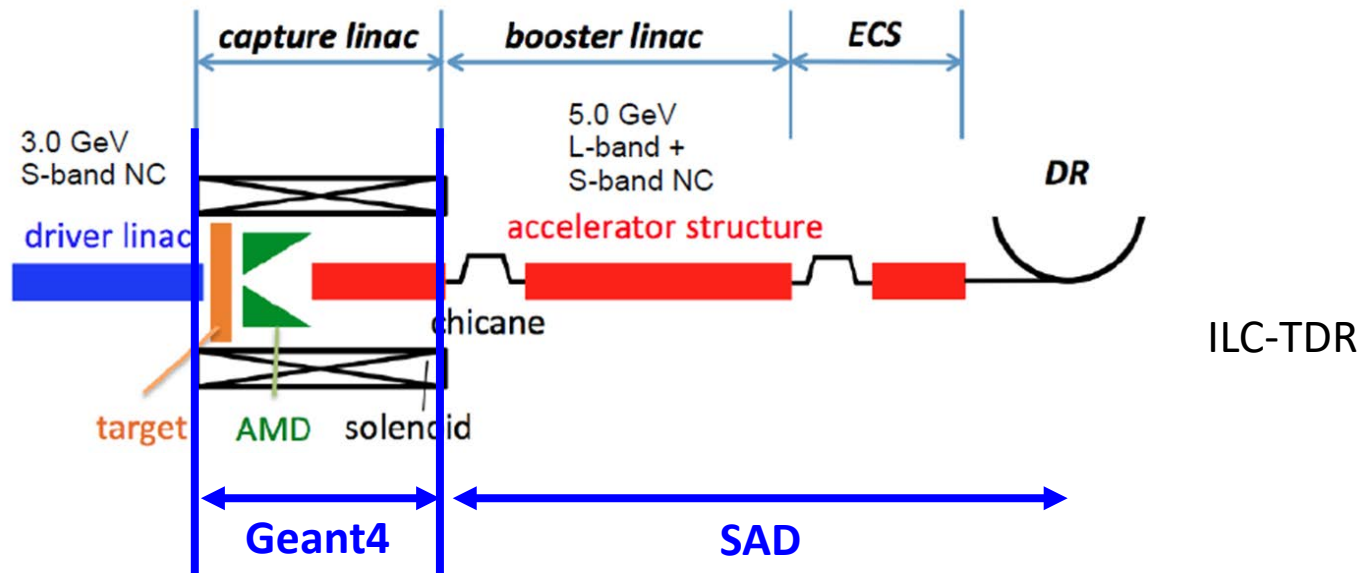
The data input to SAD code
to track positrons to ECS end.



Flux concentrator:
the field designed by P. Martyshkin
DC Solenoid in a capture section
One long solenoid coil: 0.5T (Bz const)

Tracking positrons after capture section

To track positrons after capture section, I use the tracking code which was made by Nagoshi-san.



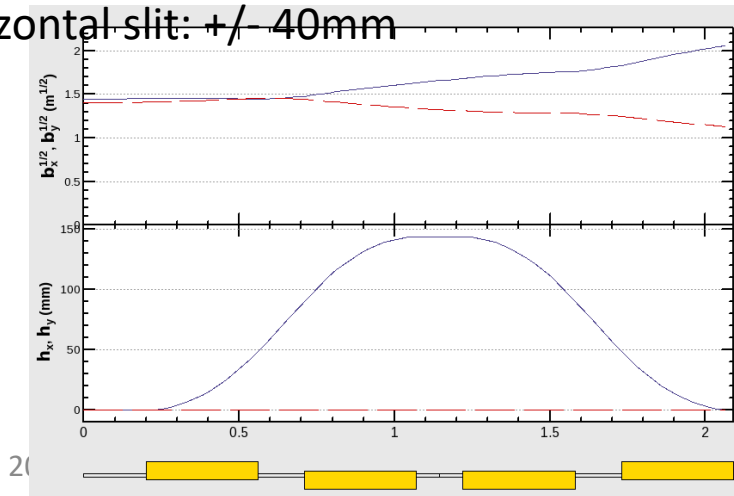
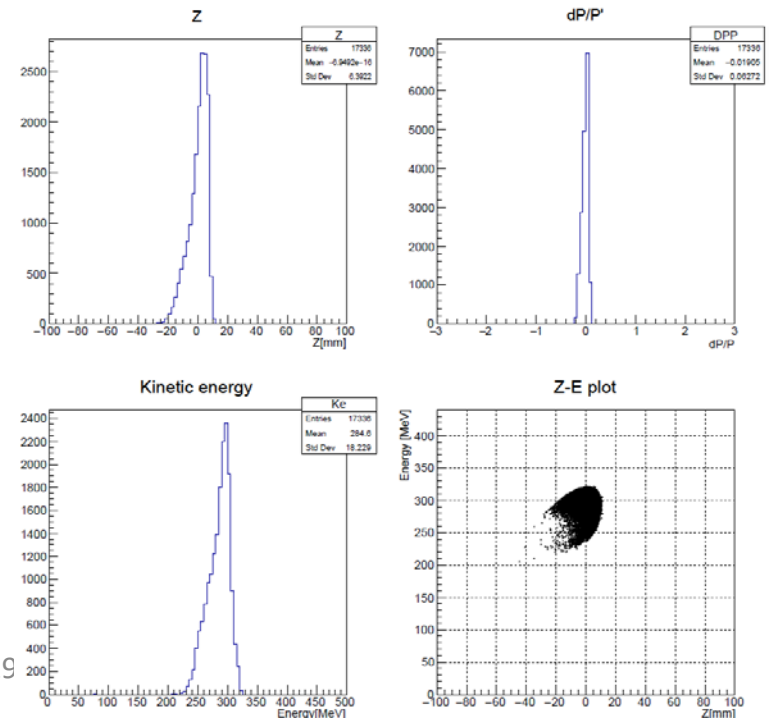
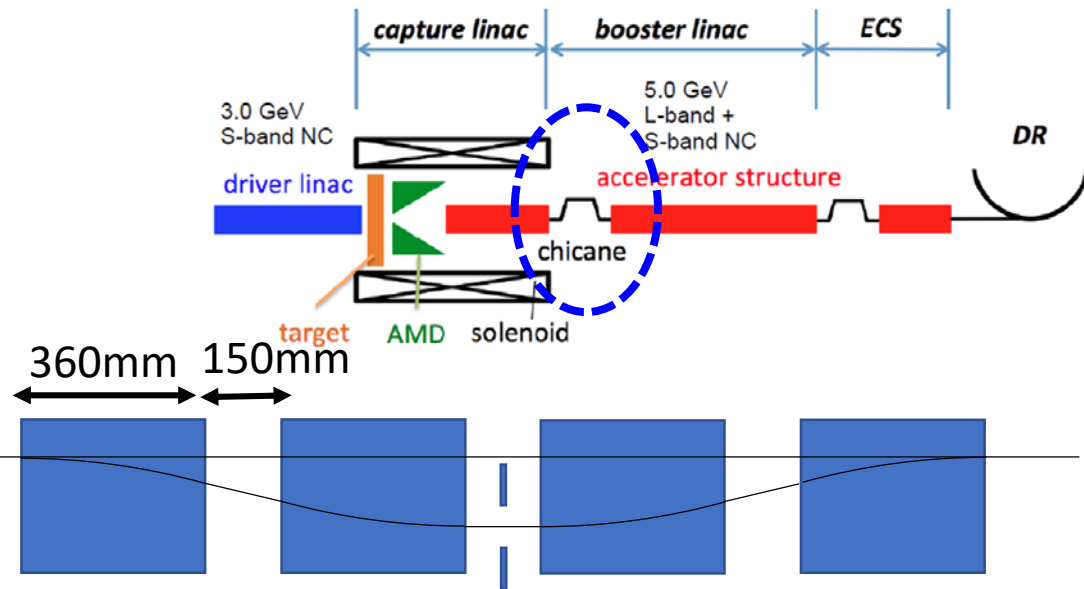
Positrons data calculated by Geant4 input to the tracking code using SAD to get yield at DR.

Chicane

Cut energy tail
Bunch compression

Bending angle : 0.27rad (15.5deg)
It is finally determined
by parameter scanning.

Radius ρ : 1.35m
B : 0.64[T] @ 260GeV/c
Offset: 138mm
Horizontal slit: +/- 40mm



Booster linac

Positrons are accelerated to 5GeV.

4Q+1L 14sets (01 --14)
 4Q+2L 29sets (15 -- 43)
 4Q+4L 18 sets (44 -- 61)
 4Q+4S 23 sets (62 -- 84)

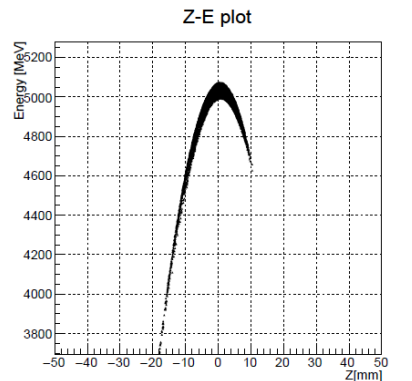
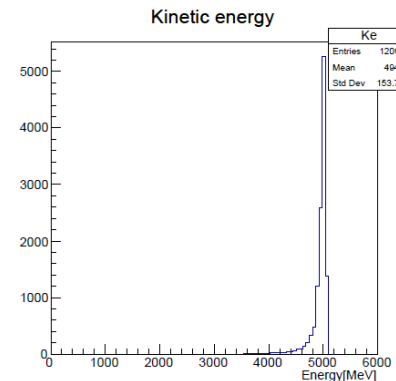
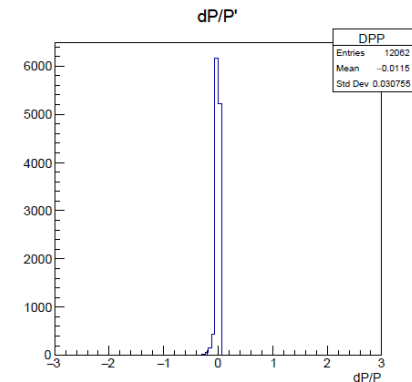
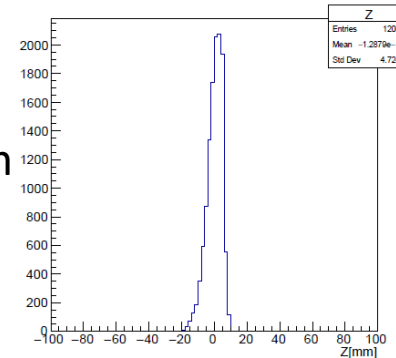
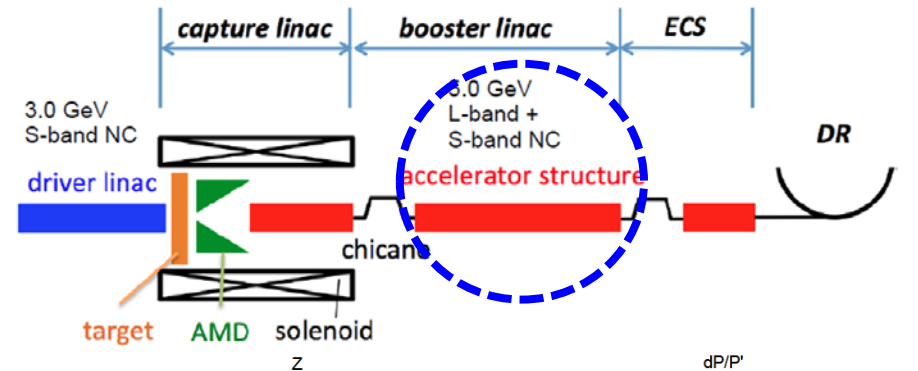
L-band ACC: 1.3GHz, 2.0m, $r=17\text{mm}$, 8.69MV/m
 S-band ACC: 2.6GHz, 1.959m, $r=10\text{mm}$, 13.02MV/m

Phase: basically on crest.
 The phase is finally determined
 by parameter scanning.

Aperture:

$R=17\text{mm}$ (L-band),
 $R=10\text{mm}$ (S-band)

There are apertures at both ends
 of each accelerating tube.



ECS

Energy compression

The slit cut the low energy part

Bending angle : 0.22rad (12.6deg)

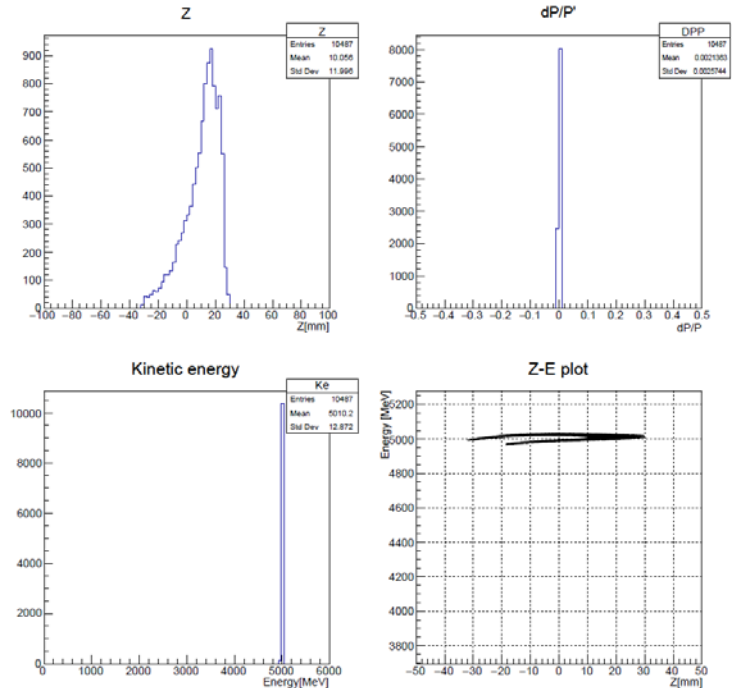
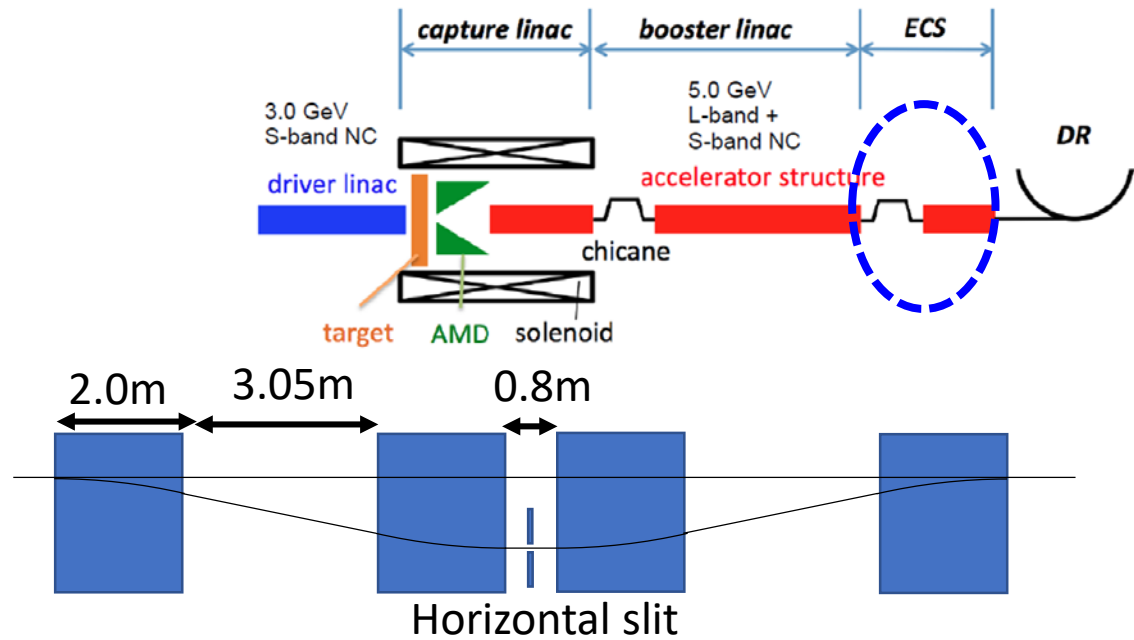
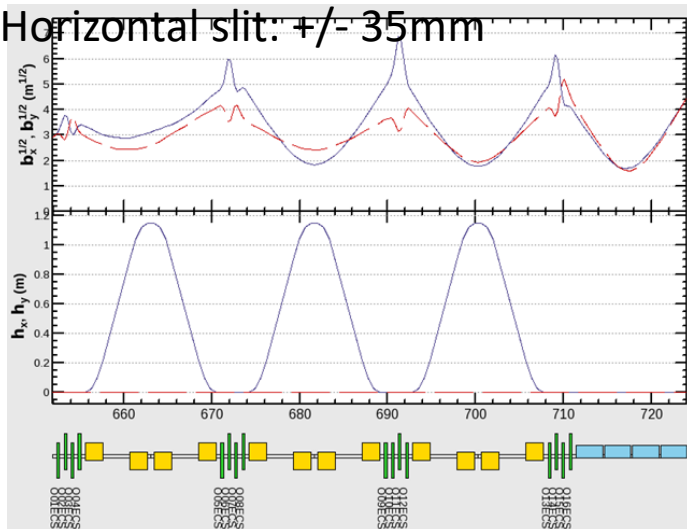
It is finally determined
by parameter scanning.

Radius ρ : 9.06m

B : 1.82[T] @ 5GeV/c

Offset: 1.11m

Horizontal slit: +/- 35mm



Cut condition of DR aperture

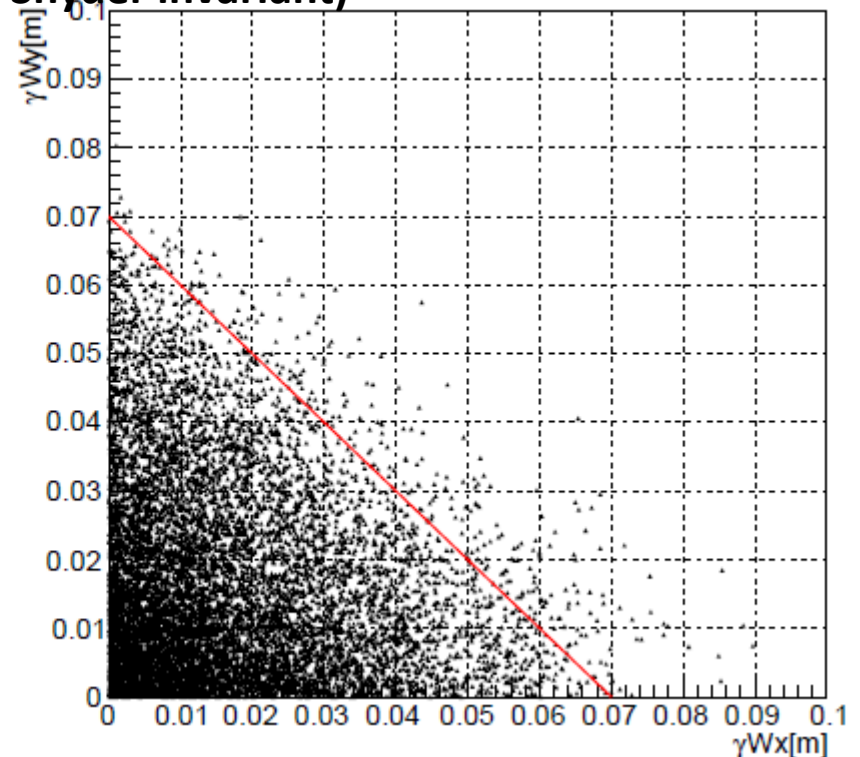
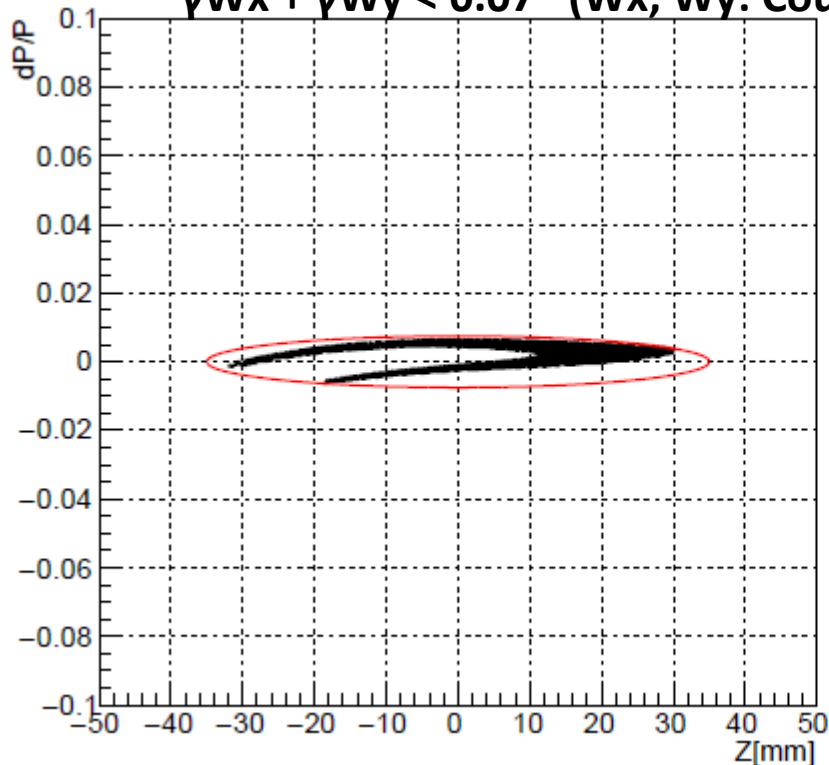
* DR acceptance of Energy and bunch length

$$(\Delta E/BW)**2 + (dz/zi)**2 < 1$$

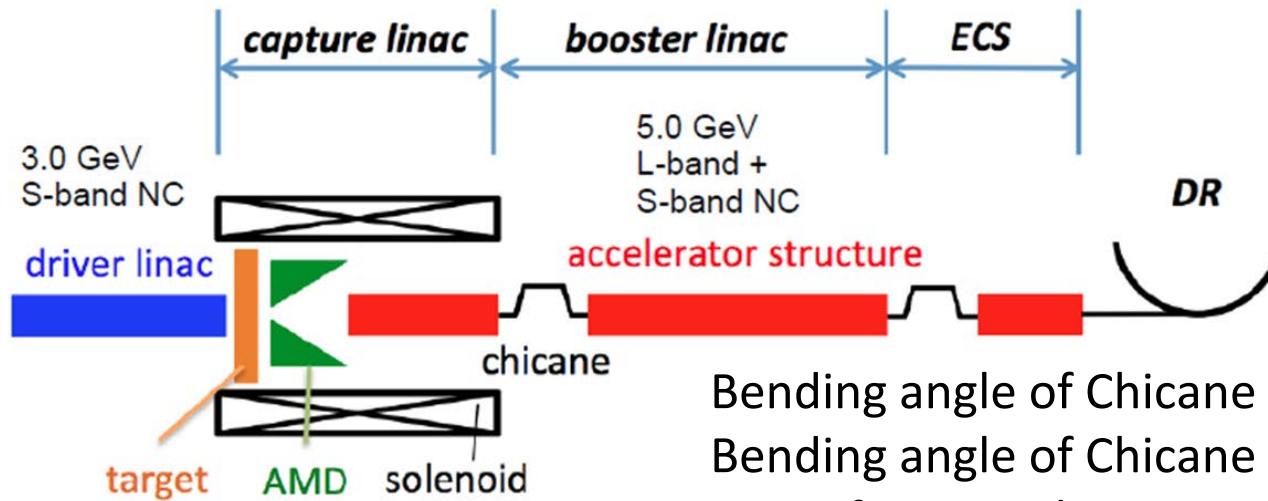
$$BW=0.0075*5=0.0375\text{GeV}, \quad zi=0.035\text{m}$$

* DR aperture

$$\gamma Wx + \gamma Wy < 0.07 \quad (Wx, Wy: \text{Courant-Snyder invariant})$$



Scan parameters



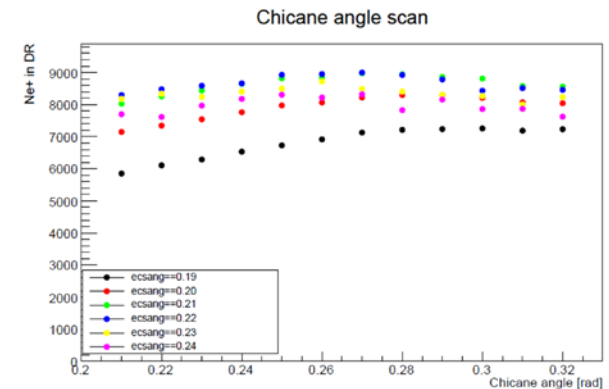
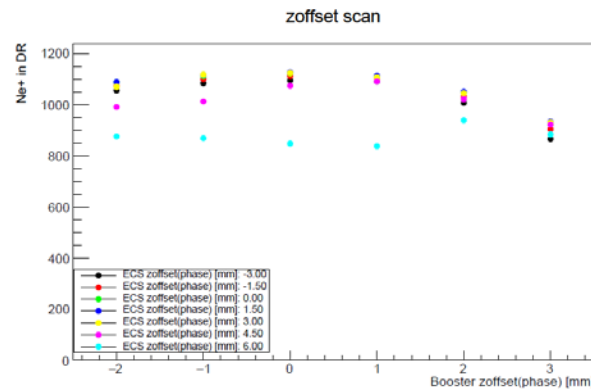
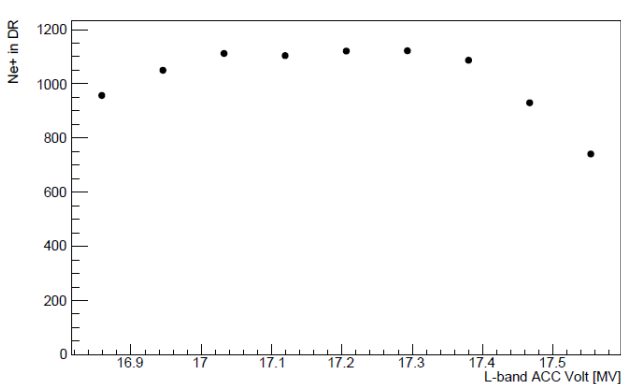
Bending angle of Chicane at capture end

Bending angle of Chicane of ECS

Eacc of Booster linac

Booster linac phase

ECS linac phase



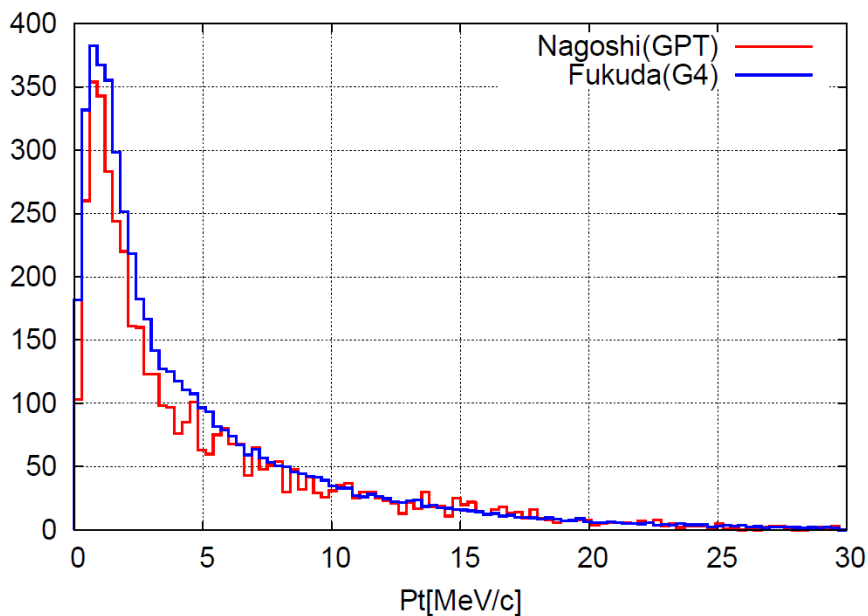
Comparison of Nagoshi's result and Fukuda's result

Exit of AMD

In comparison between my result
and Nagoshi-san's result,
The energy distributions is different.

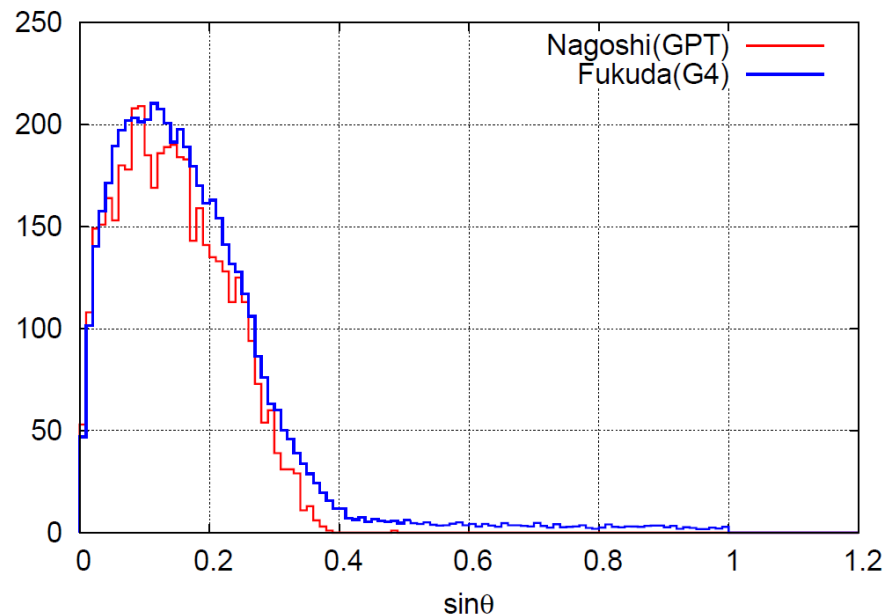
Ne+: 4475 (Nagoshi, GPT)
Ne+: 5249 (Fukuda, Geant4)

Transverse Momentum (AMD out)

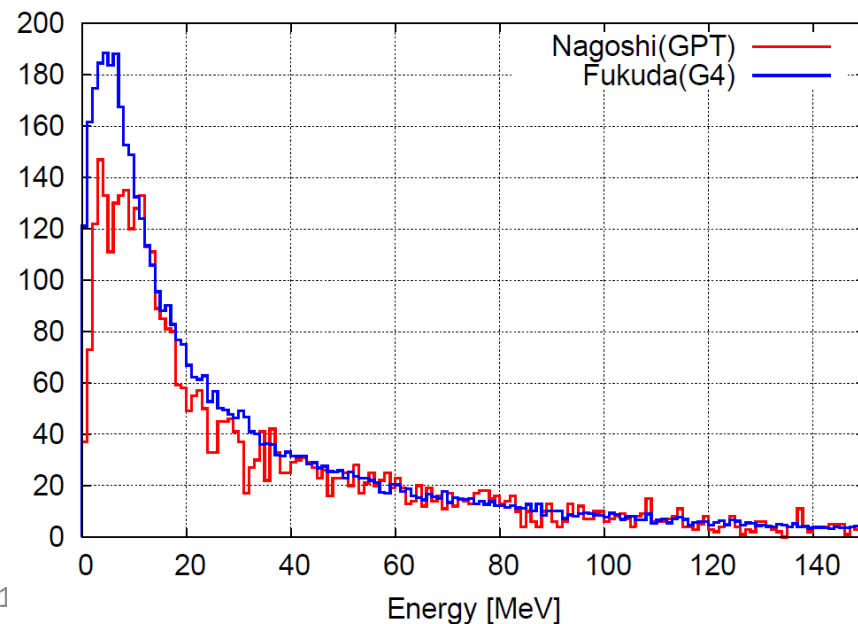


WS201

Angle (AMD out)



Energy (AMD out)



Difference of Nagoshi's simulation and Fukuda's simulation

The difference is caused by as follow effects:

- Positrons are also generated at other than a target by gamma-rays.
- Positrons are repelled at the surface of the FC. A part of that positrons is captured.

Nagoshi-san used General Particle Tracer (GPT) for tracking simulation.

The simulation by GPT does not include these effect.

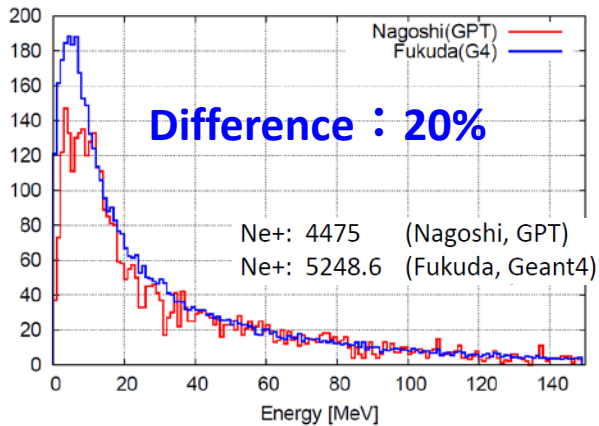
Other difference is Input data.

- Positrons produced W-target are used in Nagoshi's simulation. In Fukuda's simulation, the target is W26Re.
- Statistics is different. Number of primary e-: 1000 (Nagoshi), 10000(Fukuda)

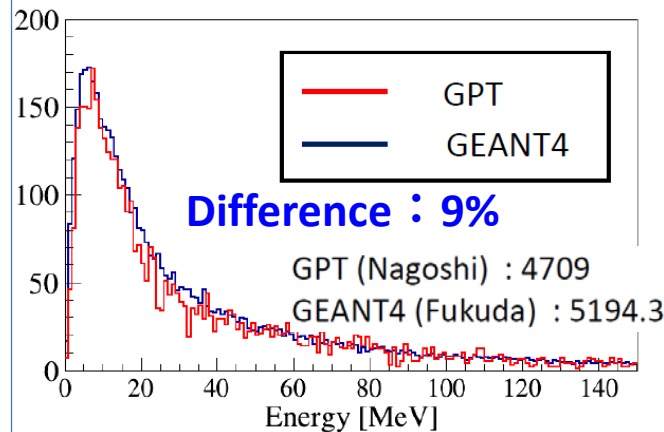
Energy distribution and Number of positrons at FC exit

With γ -ray, e-(Geant4)

Energy (AMD out)

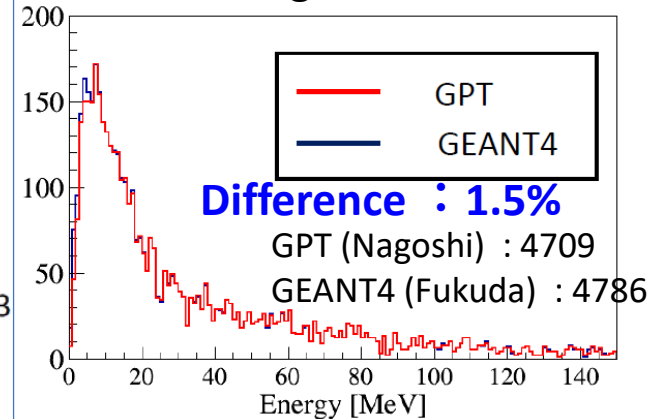


With scattering (Geant4)



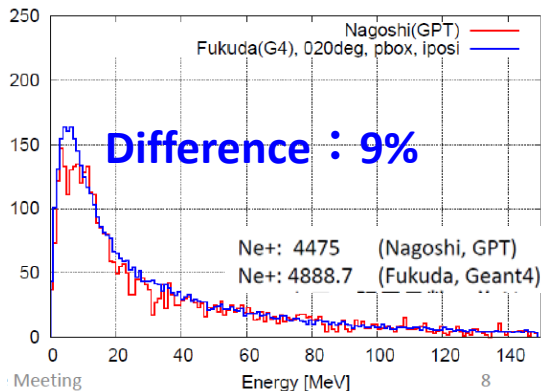
Input data

which Nagoshi-san used

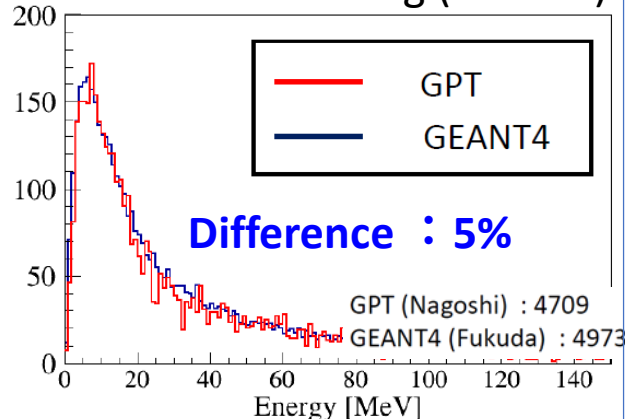


Without γ -ray, e-(Geant4)

Energy (AMD out)

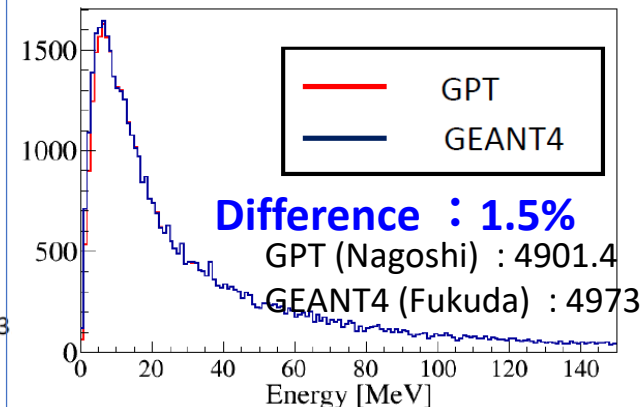


Without scattering (Geant4)



Input data

which Fukuda used



Yield calculation with divided solenoid coils

Yield calculation

The capture linac is placed in the constant magnetic field of a solenoid in simulations so far. Practically, spaces of wave guides, vacuum pumps and so on are required. Therefore, the capture linac is covered by short solenoid coils to make these spaces.

I tried to calculate the positron yield in cases of :

- Constant B_z field (a long solenoid coil)
- Magnetic field made by divided solenoid coils
- Magnetic field made by divided solenoid coil with changed shape

Input parameters

Input : 3GeV e- beam, $N_e = 1 \times 10^4$, $\sigma_{x,y} = 2\text{mm}$, $\sigma_z = 1\text{mm}$

Target : W26Re, 16mm

Target-AMD: 5mm

OMD: FC designed by Pavel Martyshkin (Peak 5.0T)

DC solenoid: One long solenoid

Divided solenoid coil

Divided solenoid coil with changed shape

Accelerating tube : SWx36

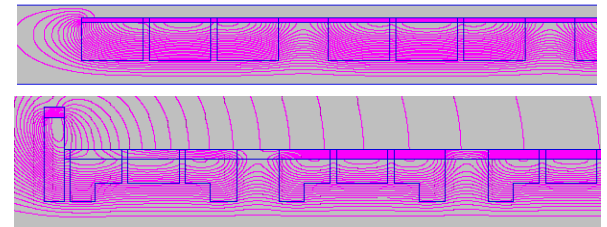
Electro-magnetic field : Pillbox (TM010)

$$E_z = E_0 \cdot J_0(p_{01} \cdot r/a) \cdot \sin(\omega t + \text{cavPhase})$$

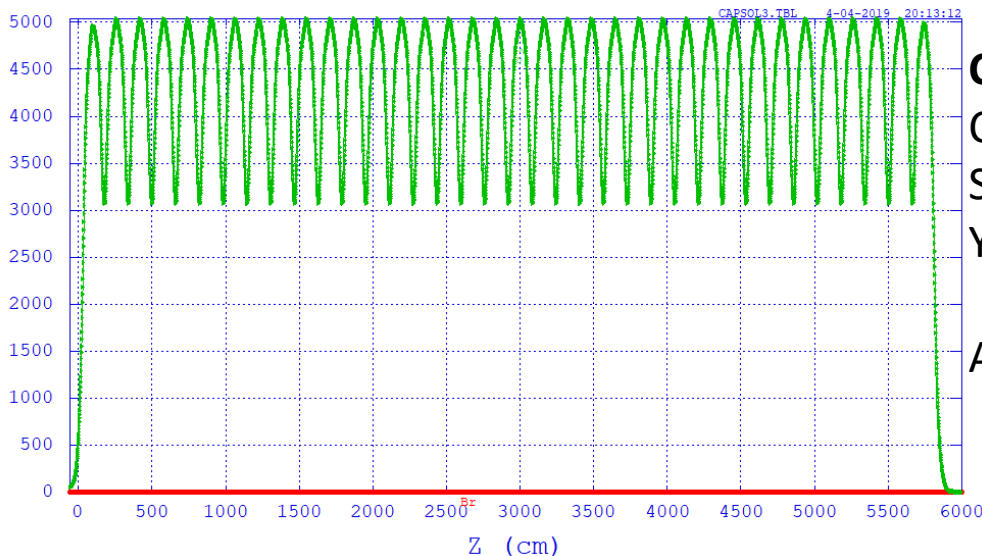
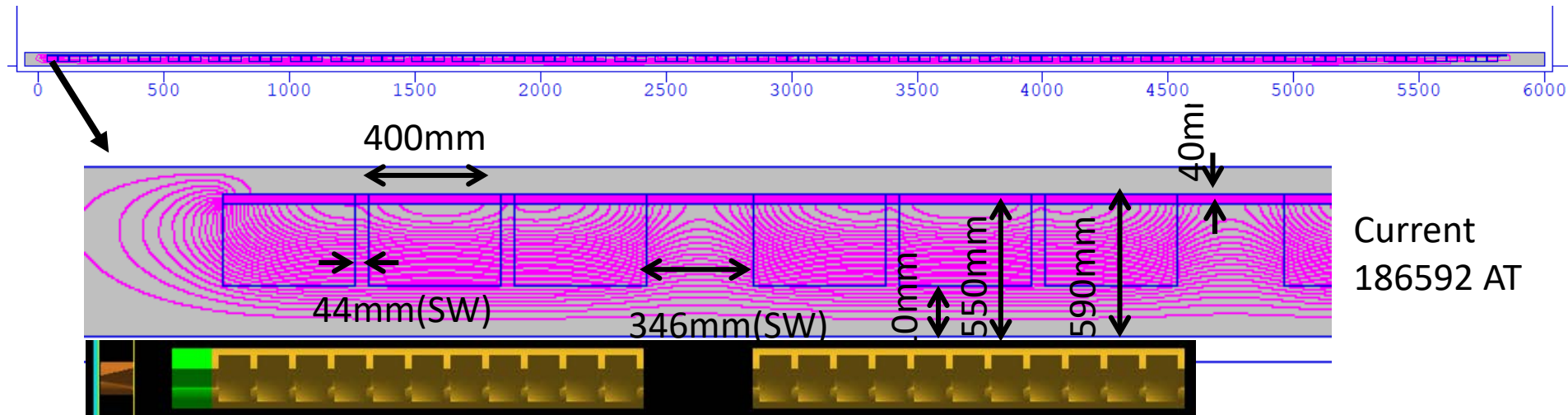
$$B_\phi = E_0 \cdot J_1(p_{01} \cdot r/a) \cdot \cos(\omega t + \text{cavPhase}) / c_{\text{light}}$$

→ Up to 250MeV.

Capture linac phase: 10deg



Divided solenoid coils



Coil current: 186592 AT

Coil length: 400mm

Space between coils: 44mm

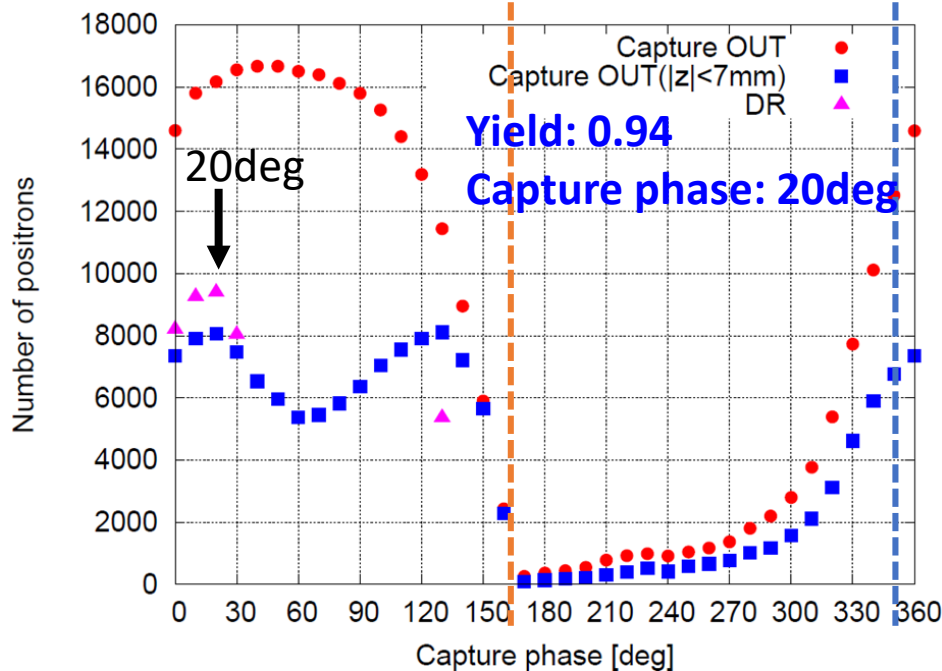
Yoke thickness: 40mm

A return yoke covers the whole capture linac.

Result of yield calculation

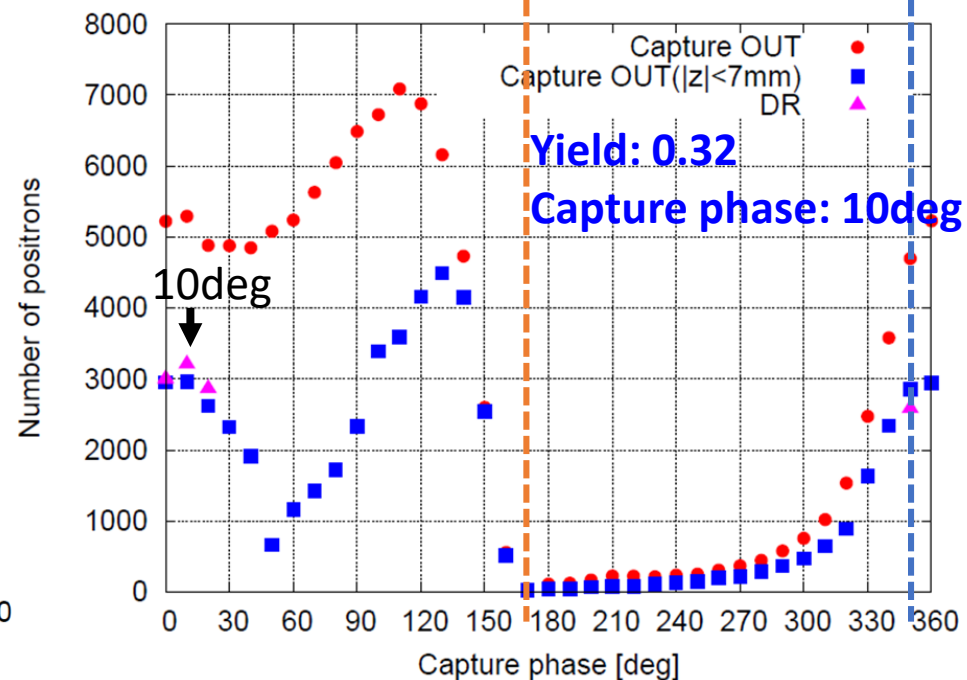
The number of positrons is reduced by 63% when the DC solenoid is changed from one long coil to divided coils

DC solenoid: One long solenoid



Accelerating Phase 172deg
Decelerating phase 352deg

Divided solenoid coils



Number of primary e⁻: 10000

Magnetic field of FC and Solenoid

OMD

FC: the field designed by Pavel Martyshkin by using CST studio.

DC Solenoid in a capture section

One long solenoid coil: 0.5T (Bz const)

Divided solenoid coils (*)

Divided solenoid coil with changed shape (*)

*** No coil at a space between accelerating tubes**

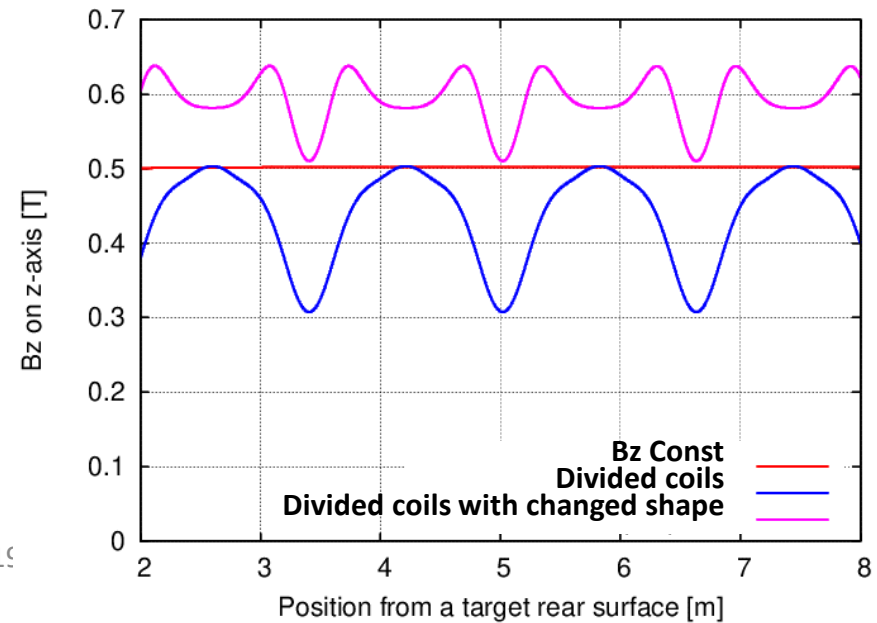
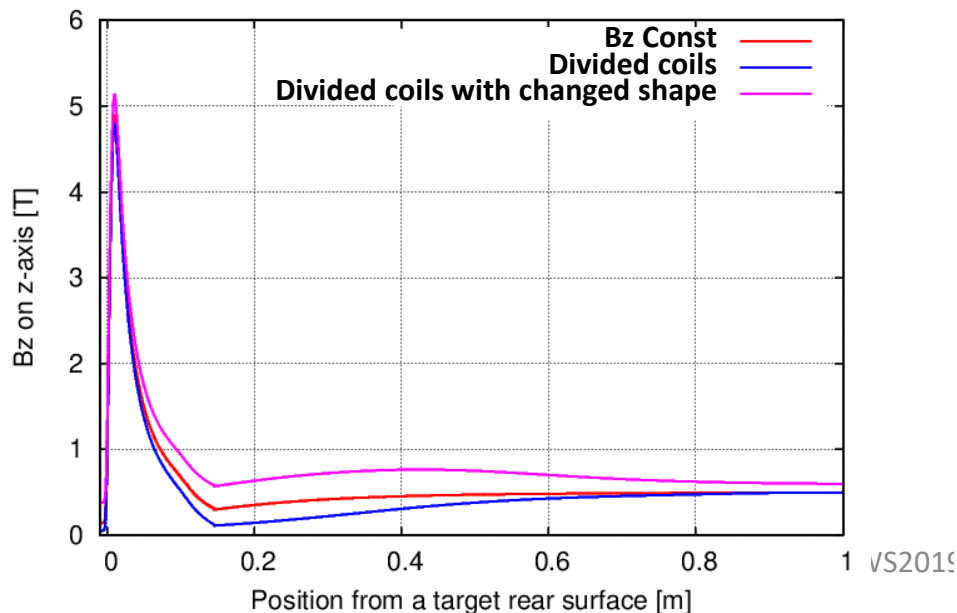
$$B_r^a(r, z) = \sum_{\nu=1}^{\infty} \frac{(-1)^{\nu}}{\nu!(\nu-1)!} B_{z0}^{(2\nu-1)}(z) \left(\frac{r}{2}\right)^{2\nu-1}$$

$$= -\frac{B'_{z0}(z)}{2} r + \frac{B_{z0}^{(3)}(z)}{16} r^3 - \frac{B_{z0}^{(5)}(z)}{384} r^5 + \frac{B_{z0}^{(7)}(z)}{18432} r^7 - \frac{B_{z0}^{(9)}(z)}{1474560} r^9 + \dots$$

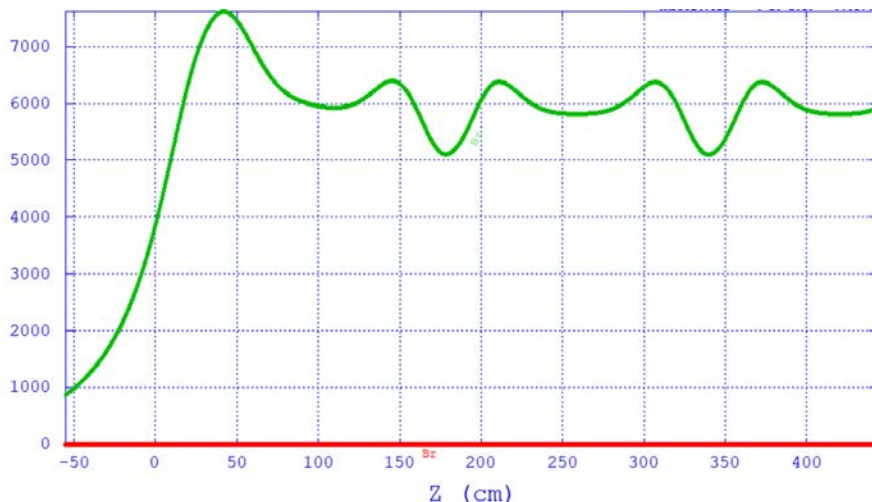
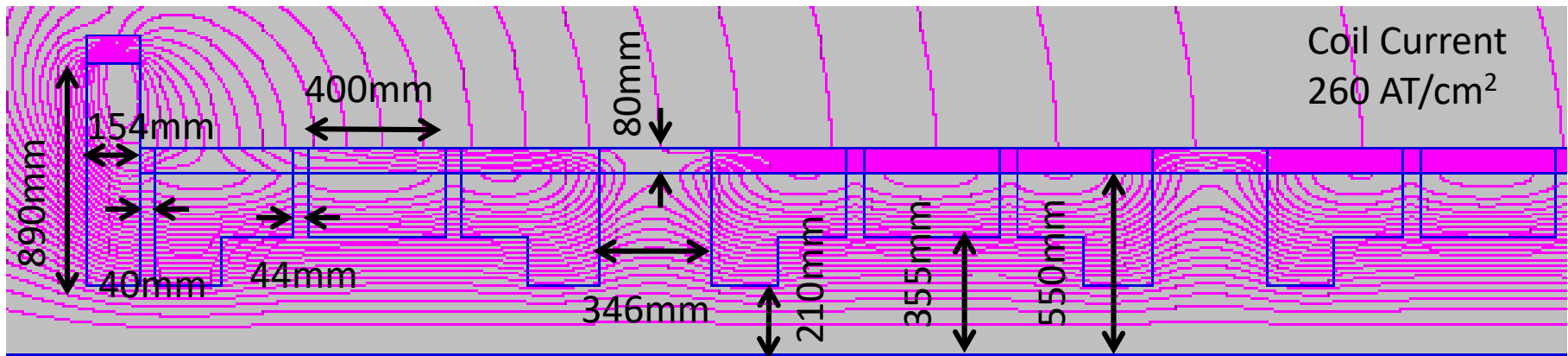
$$B_z^a(r, z) = \sum_{\nu=0}^{\infty} \frac{(-1)^{\nu}}{(\nu!)^2} B_{z0}^{(2\nu)}(z) \left(\frac{r}{2}\right)^{2\nu}$$

$$= B_{z0}(z) - \frac{B_{z0}''(z)}{4} r^2 + \frac{B_{z0}^{(4)}(z)}{64} r^4 - \frac{B_{z0}^{(6)}(z)}{2304} r^6 + \frac{B_{z0}^{(8)}(z)}{147456} r^8 + \dots$$

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Divided solenoid coil with changed shape



current density of coil: 260A/cm²

Coil length: 400mm

Space between coils: 44mm

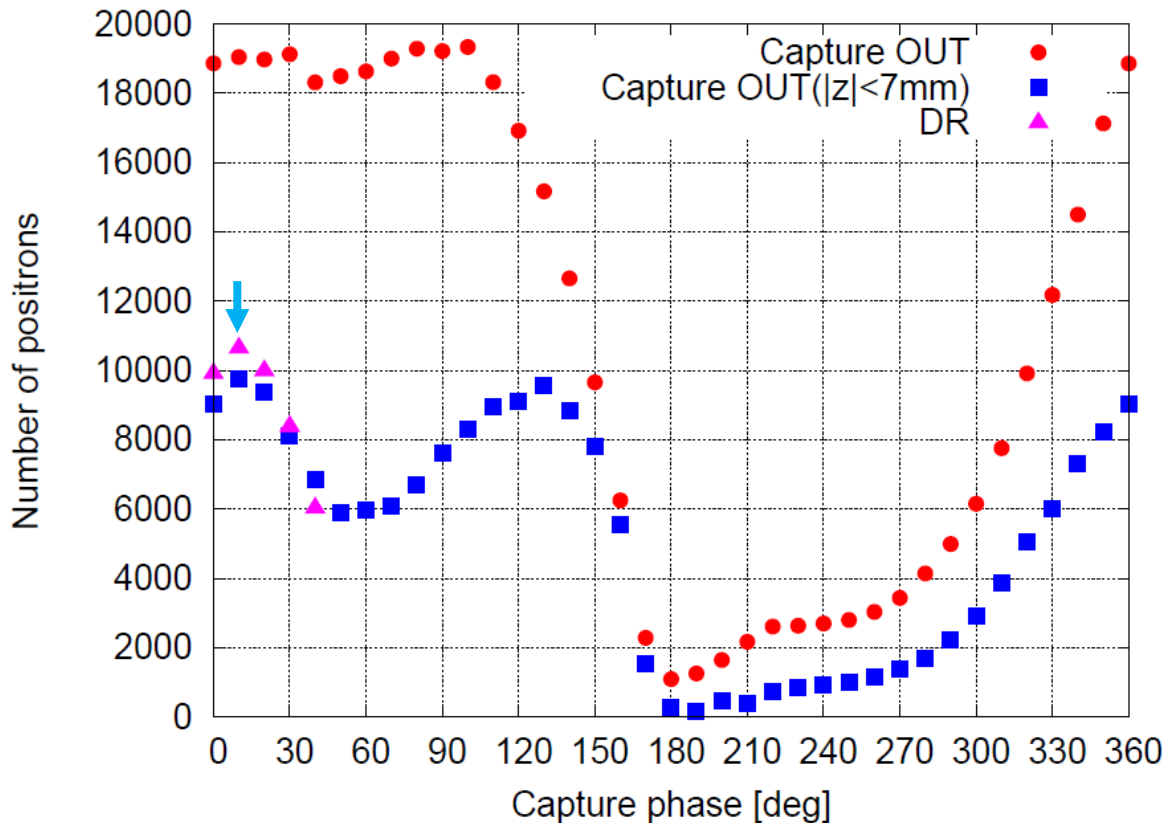
Yoke thickness: 40mm

Coil shape of both end of accelerating tubes are modified to reduce the drop of the magnetic field at intervals of tubes.

Number of positrons

Number of positrons at the capture end and the DR was calculated when the rf phase of capture linac.

Number of positrons becomes maximum at the phase of 10deg.



Ne+(DR): 10646

Yield: 1.06

Capture phase: 10deg

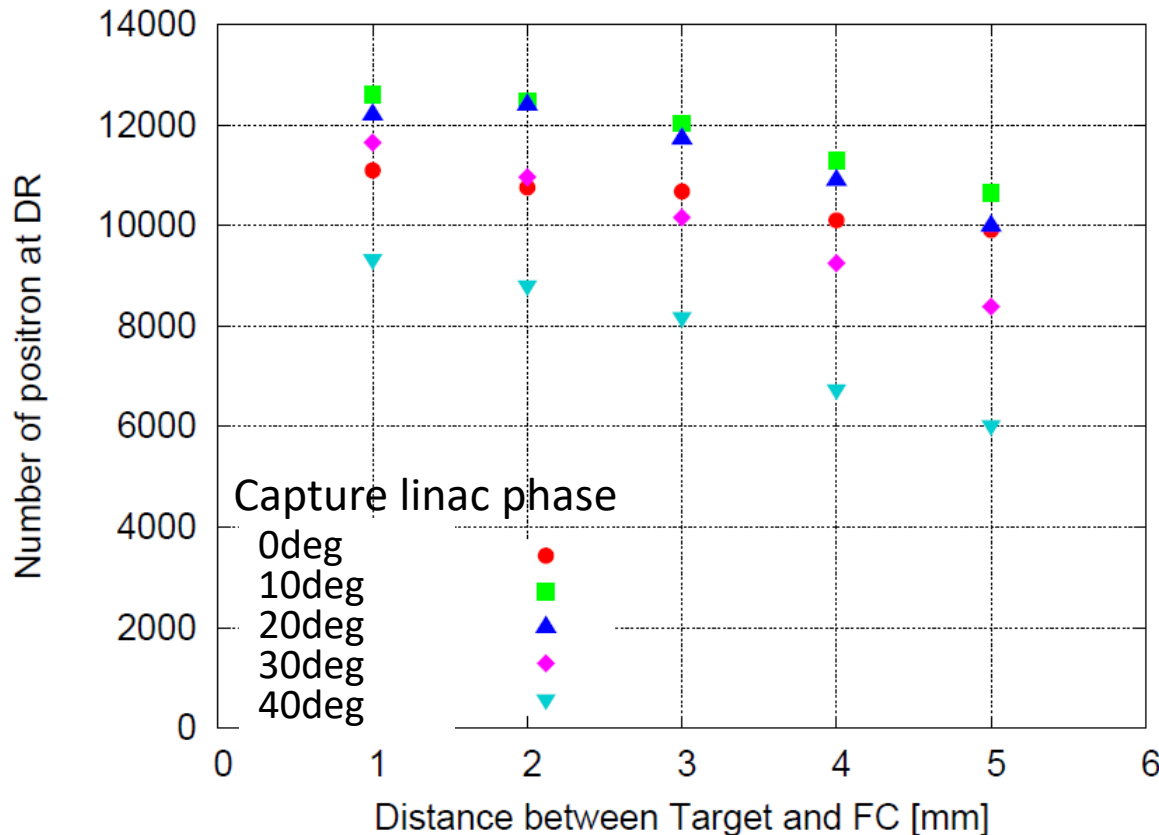
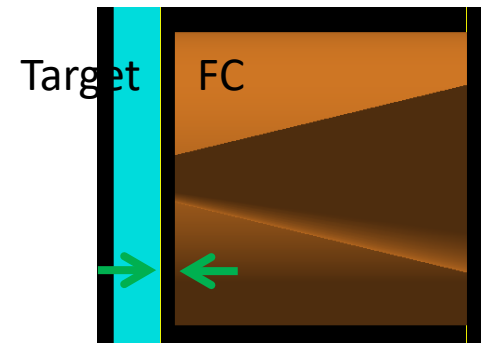
Number of primary e-: 10000

Yield calculation when the distance of target and FC is changed

Scan of distance between Target and FC

Yield increase from 1.06 to 1.26 when the distance is changed from 5mm to 1mm.

The yield saturates less than the distance of 2mm.



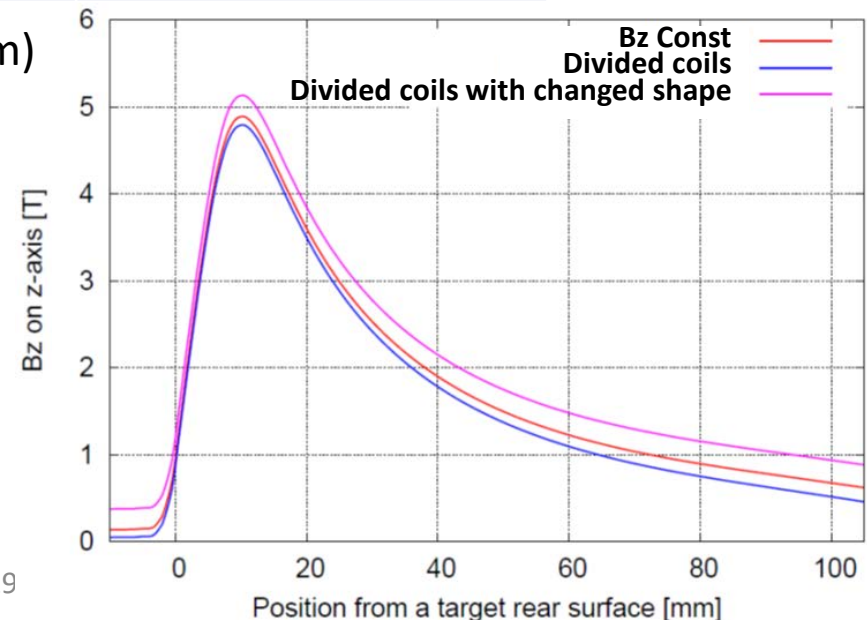
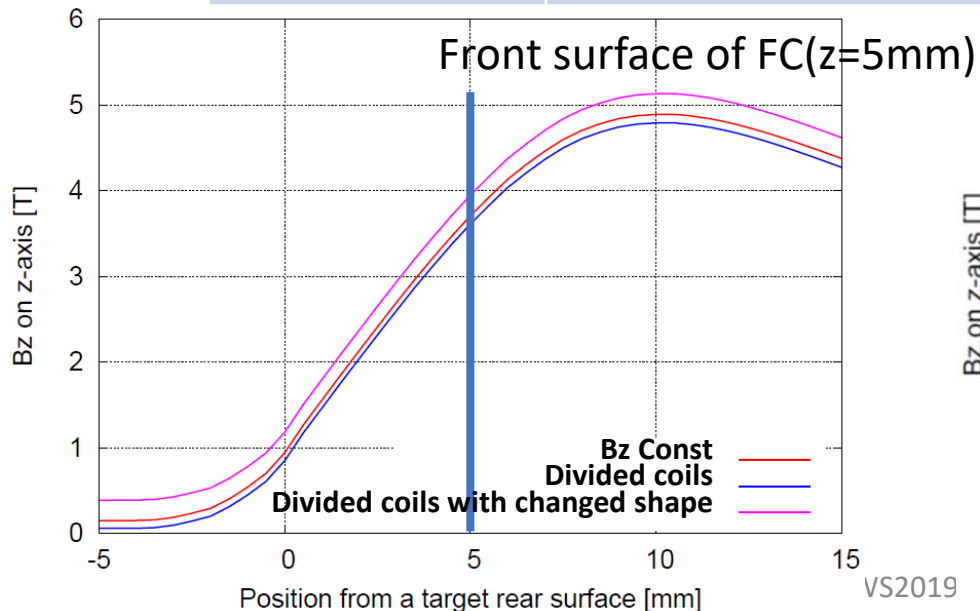
Distance between Target and FC [mm]	Ne+(DR)	Yield(DR)
1.0	12601	1.26
2.0	12472	1.25
3.0	12042	1.20
4.0	11292	1.13
5.0	10646	1.06

Primary e-: 10000

Magnetic field strength at target rear surface

Target-FC [mm]	Bz on target rear surface [T]	Heating value by eddy current [kW](*)
1.0	3.46	16
2.0	2.93	11
3.0	2.36	7
4.0	1.79	3.5
5.0	1.18	1.1

(*) estimated by T. Omori



Summary

- I could reproduce the result of Nagoshi-san's simulation.
- Now I can calculate the positron yield at DR by using the tracking code which has been succeeded from Kuriki-san and Nagoshi-san.
- Yields were calculated using a magnetic field created by divided solenoid coils in the capture linac.
 - One long solenoid(B_z const): Yield 0.94
 - Divided coils: Yield 0.32
 - Divided solenoid coil with changed shape: Yield 1.06
- Yields were also calculated when the distance between the target and the FC was changed.
 - Distance 5 → 1mm, Yield 1.06 → 1.26
 - The yield saturates less than the distance of 2mm.