

Improving the jet energy reconstruction for Higgs precision measurement at the ILC

The Univ. of Tokyo, Dept. of Phys., The Univ. of Tokyo, ICEPP^A
Shogo Kajiwara, Kazuki Fujii, Yu Kato,
Tomohiko Tanabe^A, Satoru Yamashita^A

Overview

Aim

- To improve b jet energy reconstruction at the ILC

Analyzing process

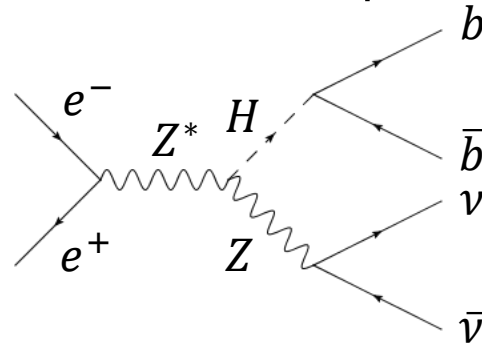
$$ee \rightarrow ZH \rightarrow \nu b \bar{b}$$

Background

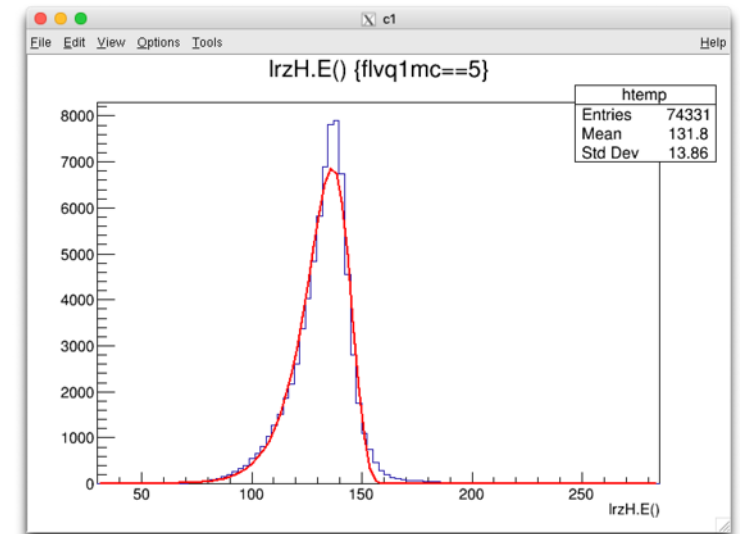
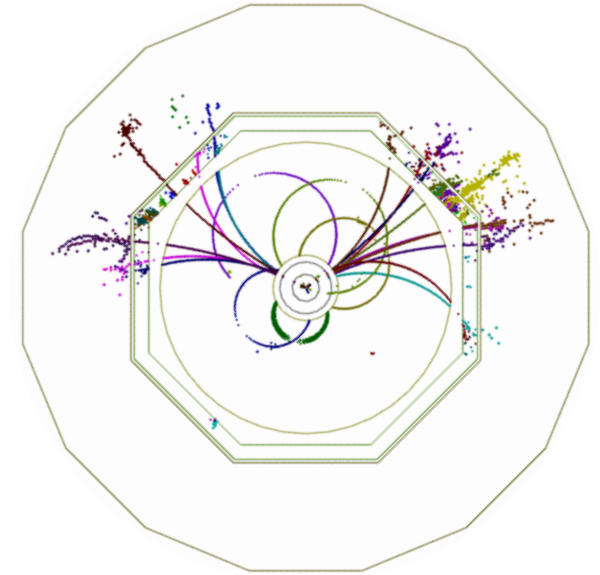
- Higgs boson decays mainly into a pair of b quarks.
- B quark jet often emits neutrinos, which makes the resolution worse.

Idea

1. recover missing neutrinos 4-momentum in b jet
2. apply **kinematic fit** to correct parameters

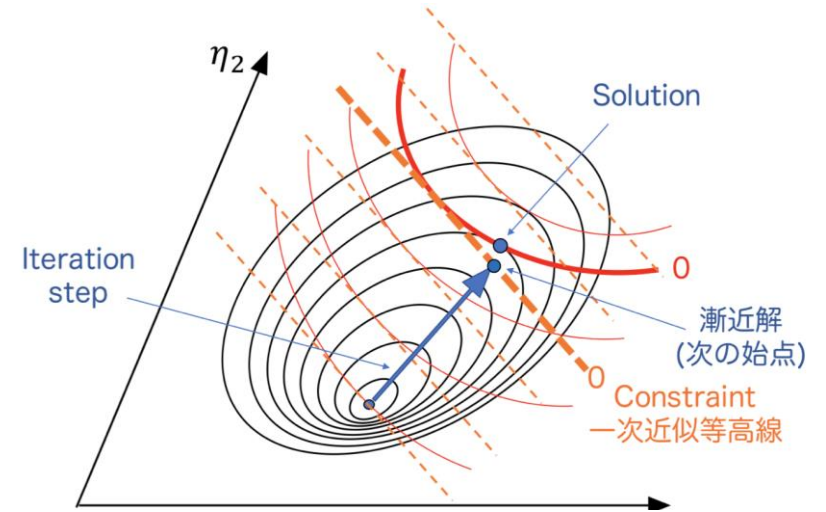


250 GeV
 $ee \rightarrow ZH \rightarrow \nu b \bar{b}$



Kinematic Fit

- a means of improving resolution
- impose kinematic constraint and detector resolution by Lagrange multiplier



\vec{y} :measured values, $\vec{\eta}$:parameters , V :covariance matrix, $\vec{\xi}$:constants

$$\chi^2 = (\vec{y} - \vec{\eta})^T V^{-1} (\vec{y} - \vec{\eta}) + 2 \sum_{k=1}^K \lambda_k g_k(\vec{\eta}, \vec{\xi}) + \sum_{l=1}^L \left(\frac{h_l(\vec{\eta}, \vec{\xi})}{\sigma_{h_l}} \right)^2$$



Fit Object



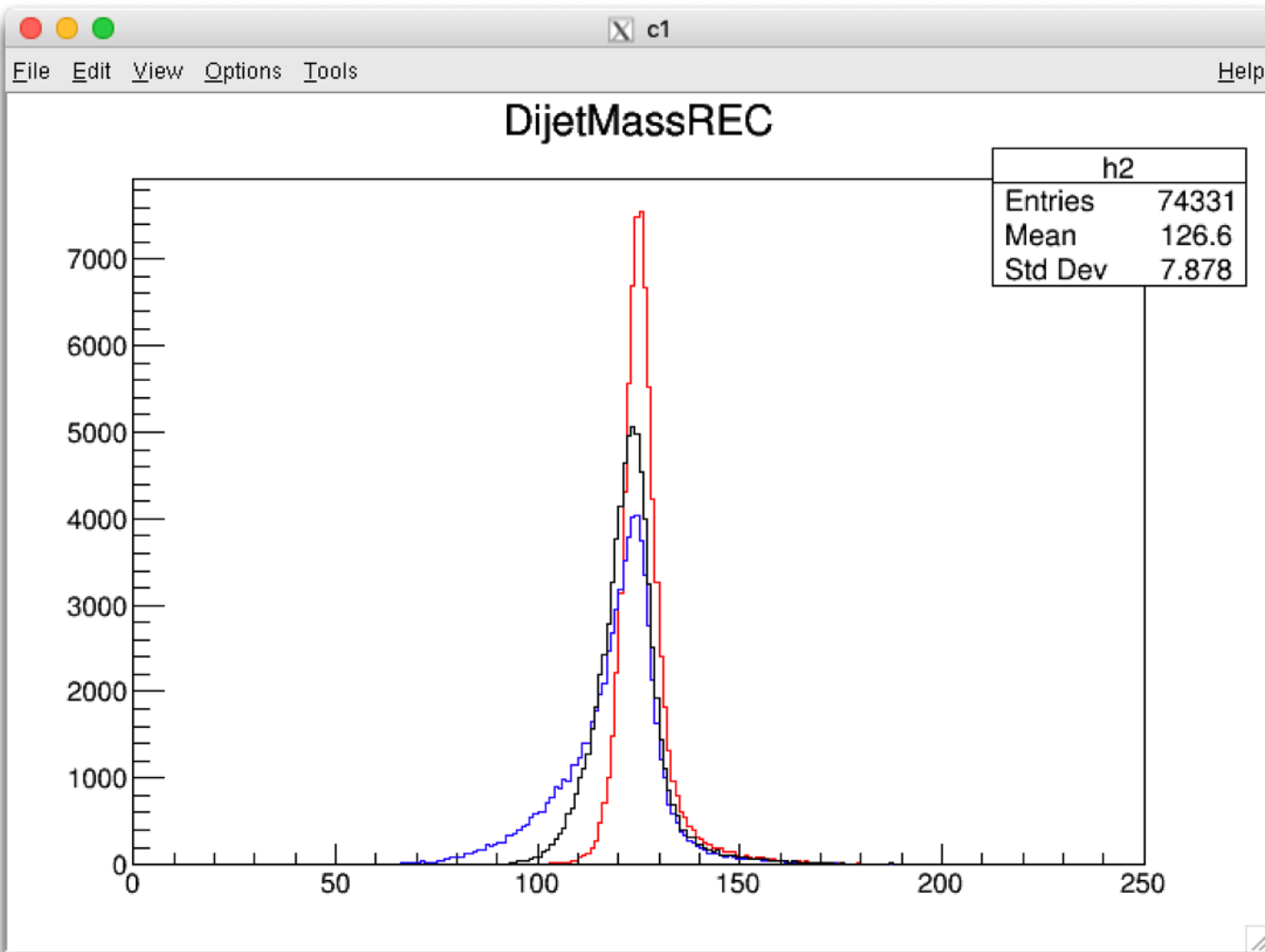
Hard Constraint



Soft Constraint

recover neutrinos for di-jet mass with MC

only $H \rightarrow b\bar{b}$

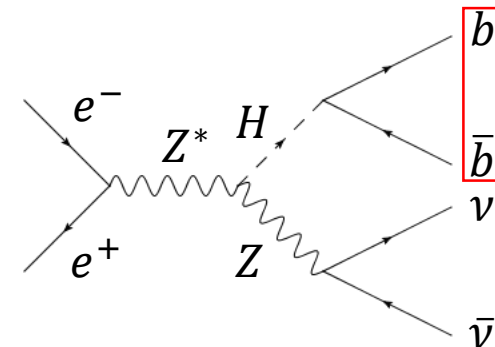


- di- b jet mass plot
- A b quark jet often emits neutrinos, which makes the resolution worse.
- recover 4-momentum of neutrinos using MC information

— no neutrino recover

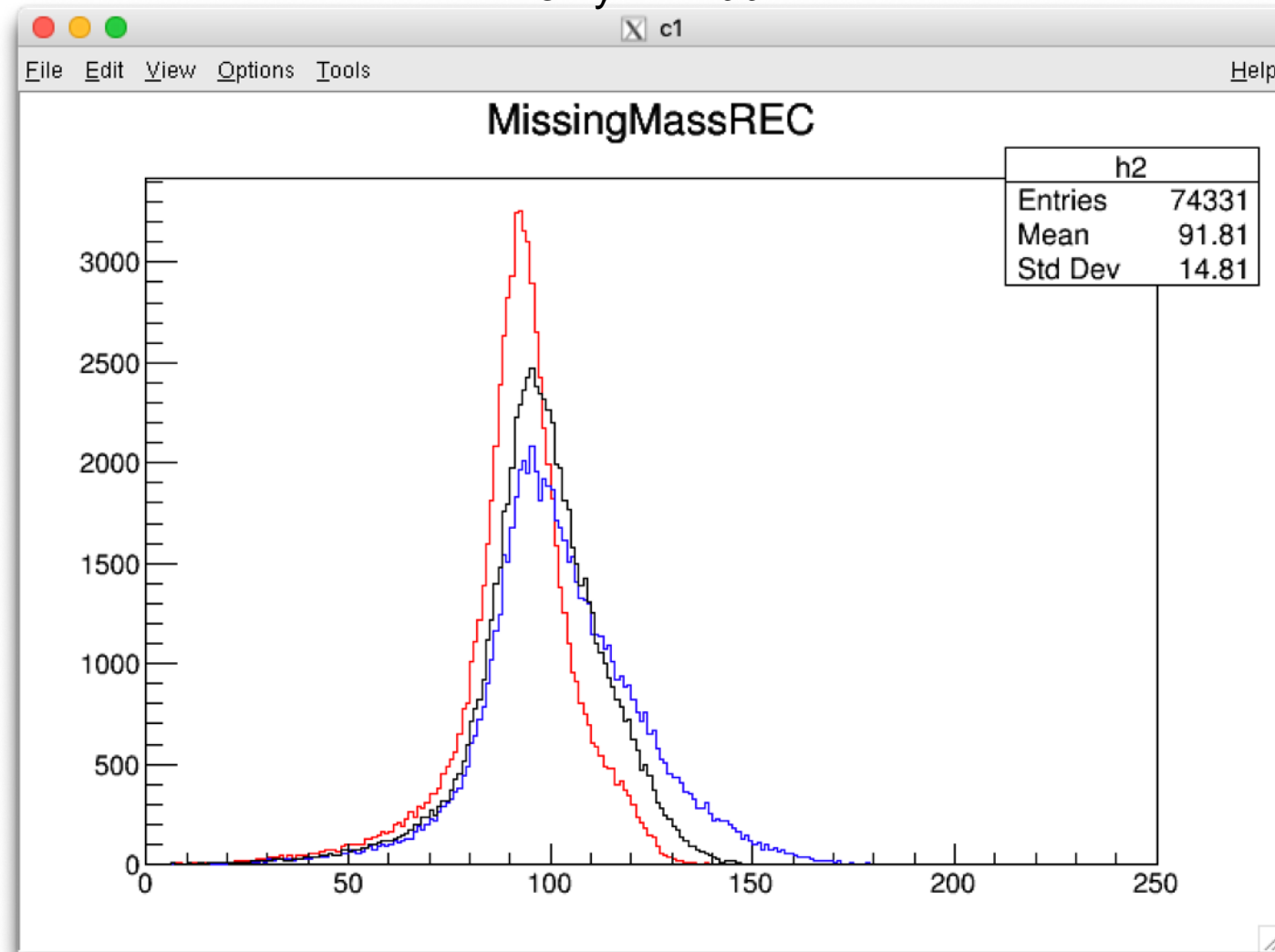
— half 4-momentum of neutrinos recovered

— full 4-momentum of neutrinos recovered



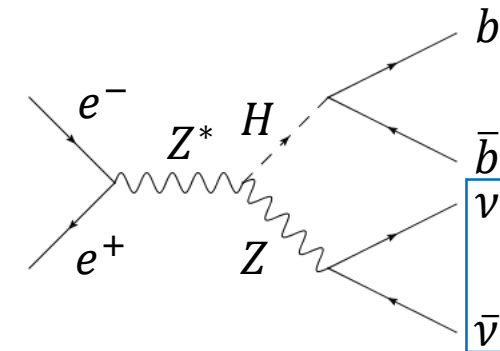
recover neutrino energy for missing mass with MC

only $H \rightarrow b\bar{b}$



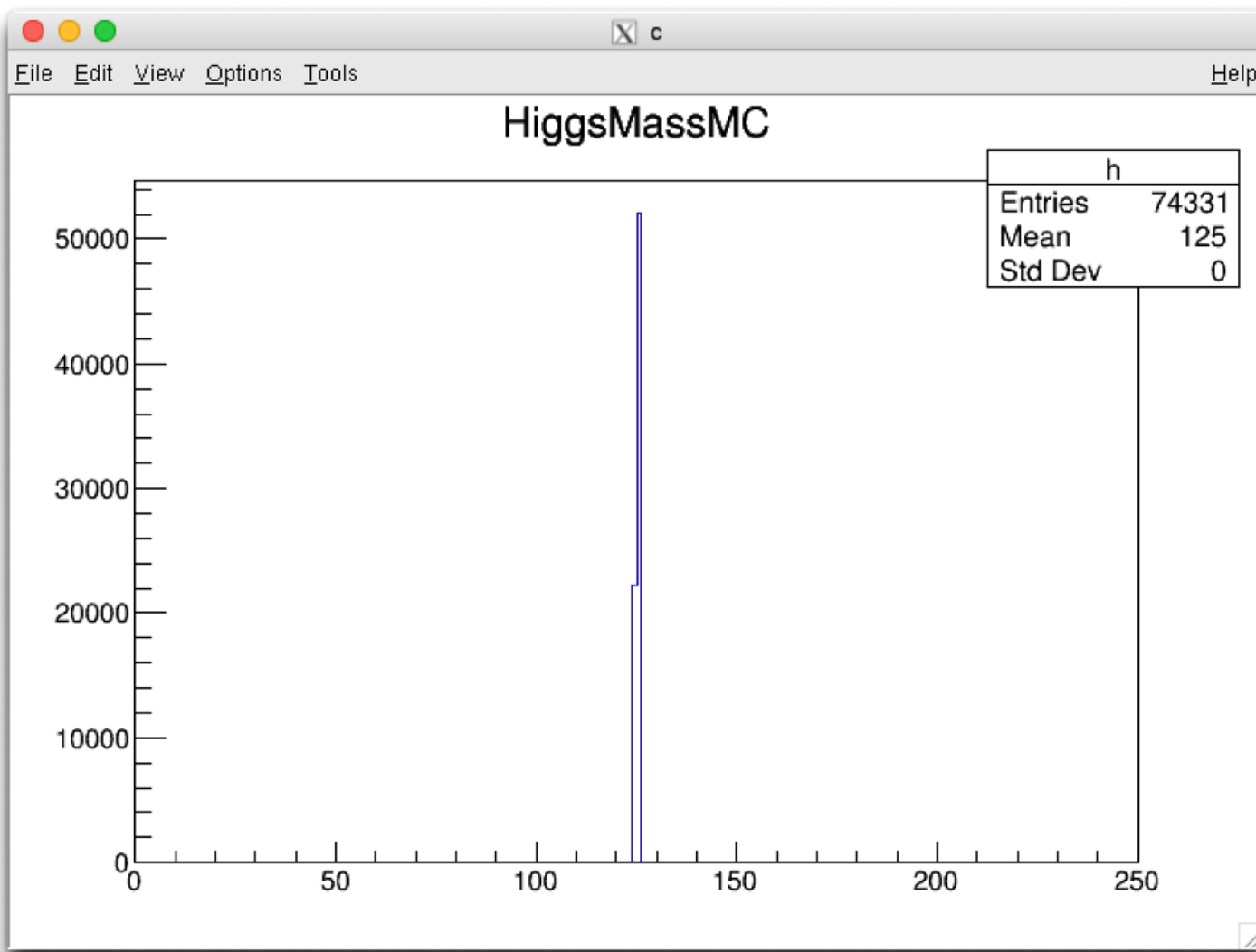
- missing mass plot
- recover 4-momentum of neutrinos using MC information

- no neutrino recovered
- half 4-momentum of neutrinos recovered
- full 4-momentum of neutrinos recovered



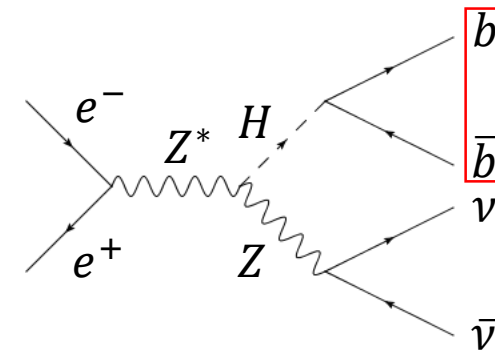
constraint for Higgs mass

only $H \rightarrow b\bar{b}$



total width of a Higgs boson < 0.013 [GeV] (PDG2019)

→ Hard Constraint



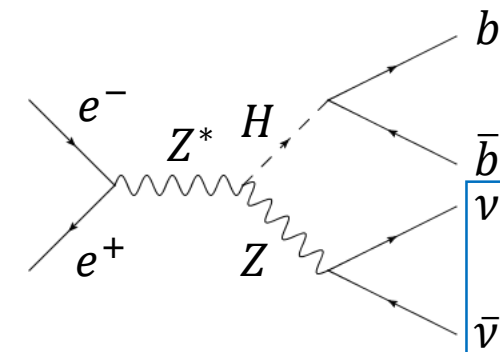
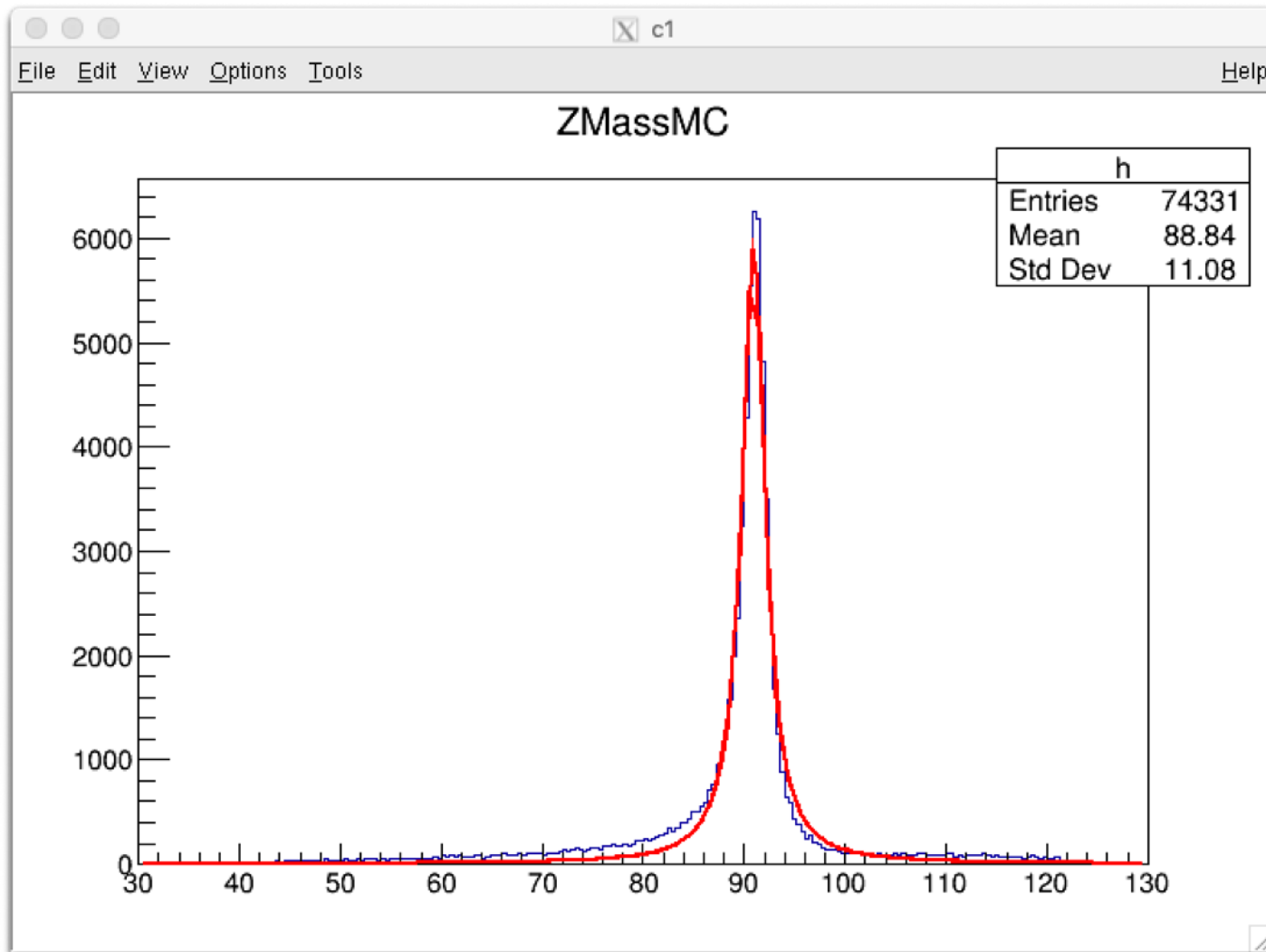
constraint for Z mass

only $H \rightarrow b\bar{b}$

total width of a Z boson ~ 2.5 [GeV](PDG2019)

Breit-Wigner distribution is fit well to Z Mass plot.

→ Breit-Wigner Soft Constraint



Next Step

1. recover missing neutrinos 4-momentum in b jet
to find neutrino in b jets by detecting and correcting for semileptonic decay
2. include **kinematic fit** to correct parameters
by imposing hard constraint for di-jet mass
and soft BW constraint for missing mass

MarlinKinfIt

- a library for kinematic fitting
- uses Newton's method for chi-square minimization
- Both **hard constraint** and **soft constraint** are available.

\vec{y} :measured values, $\vec{\eta}$:parameters , V :covariance matrix, $\vec{\xi}$:constants

$$\chi^2 = (\vec{y} - \vec{\eta})^T V^{-1} (\vec{y} - \vec{\eta}) + 2 \sum_{k=1}^K \lambda_k g_k(\vec{\eta}, \vec{\xi}) + \sum_{l=1}^L \left(\frac{h_l(\vec{\eta}, \vec{\xi})}{\sigma_{h_l}} \right)^2$$



Fit Object



Hard Constraint

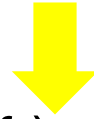


Soft Constraint

improve MarlinKinfifit

- MarlinKinfifit is developed that measured values follow a Gaussian distribution.

$$\chi^2 = (\vec{y} - \vec{\eta})^T V^{-1} (\vec{y} - \vec{\eta}) + 2 \sum_{k=1}^K \lambda_k g_k(\vec{\eta}, \vec{\xi}) + \sum_{l=1}^L \left(\frac{h_l(\vec{\eta}, \vec{\xi})}{\sigma_{h_l}} \right)^2$$



- try to redefine chi-square (f, h'_l are p.d.f.) so that it works measured values follow non Gaussian distribution as log-likelihood

$$L(\vec{\eta}) = f(\vec{y}; \vec{\eta}) \prod_{k=1}^K \delta(g_k(\vec{\eta}, \vec{\xi})) \prod_{l=1}^L h'_l(\vec{\eta}; \vec{\xi})$$

$$\chi^2 = -2 \ln f(\vec{y}; \vec{\eta}) + 2 \sum_{k=1}^K \lambda_k g_k(\vec{\eta}, \vec{\xi}) - 2 \sum_{l=1}^L \ln h'_l(\vec{\eta}; \vec{\xi})$$

forward task

- improve MarlinKinfit to assume Breit-Wigner soft constraint for Z mass
- improve MarlinKinfit to non gaussian fit object
- update $ee \rightarrow ZH \rightarrow \nu\nu b\bar{b}$ SN ratio