

EWPOs using radiative return

- motivation
- A_{LR} (electron)
- A_f ($f=b/c/\mu/\tau$)
- R_f
- g_L & g_R

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The 62nd General Meeting of ILC Physics Subgroup, KEK

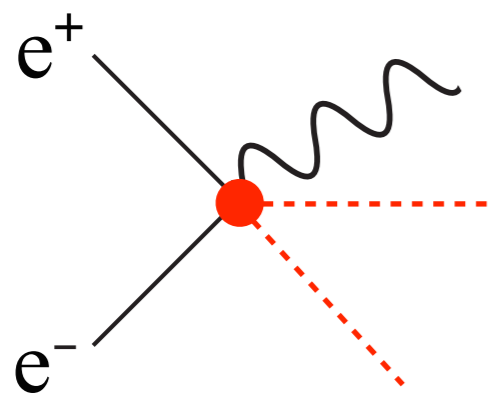
task force: K.Fujii, D.Jeans, M.Kurata, T.Suehara, J.Tian, H.Yamamoto

recap 1: Higgs couplings are related to EW couplings (EWPOs)

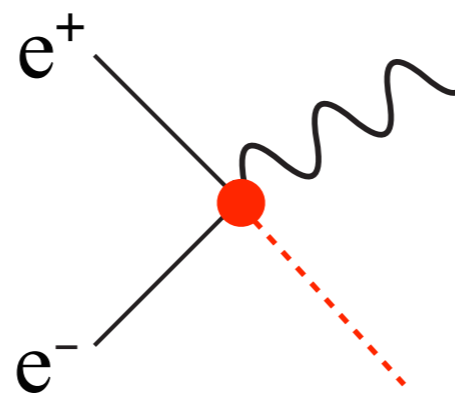
$$i \frac{C_{HL}}{v^2} (\Phi^\dagger \overleftrightarrow{D}^\mu \Phi) (\bar{L} \gamma_\mu L)$$

$$4i \frac{C'_{HL}}{v^2} (\Phi^\dagger t^a \overleftrightarrow{D}^\mu \Phi) (\bar{L} \gamma_\mu t^a L)$$

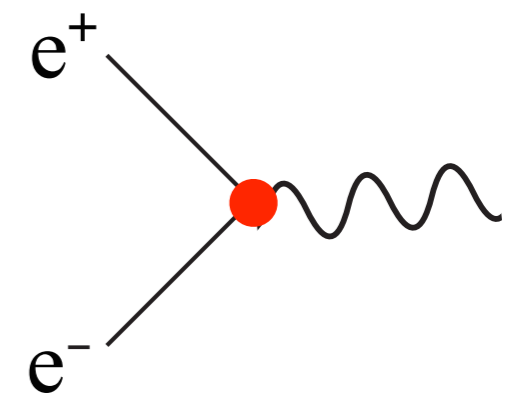
$$i \frac{C_{HE}}{v^2} (\Phi^\dagger \overleftrightarrow{D}^\mu \Phi) (\bar{e} \gamma_\mu e)$$



$e^+e^- \rightarrow Zhh$



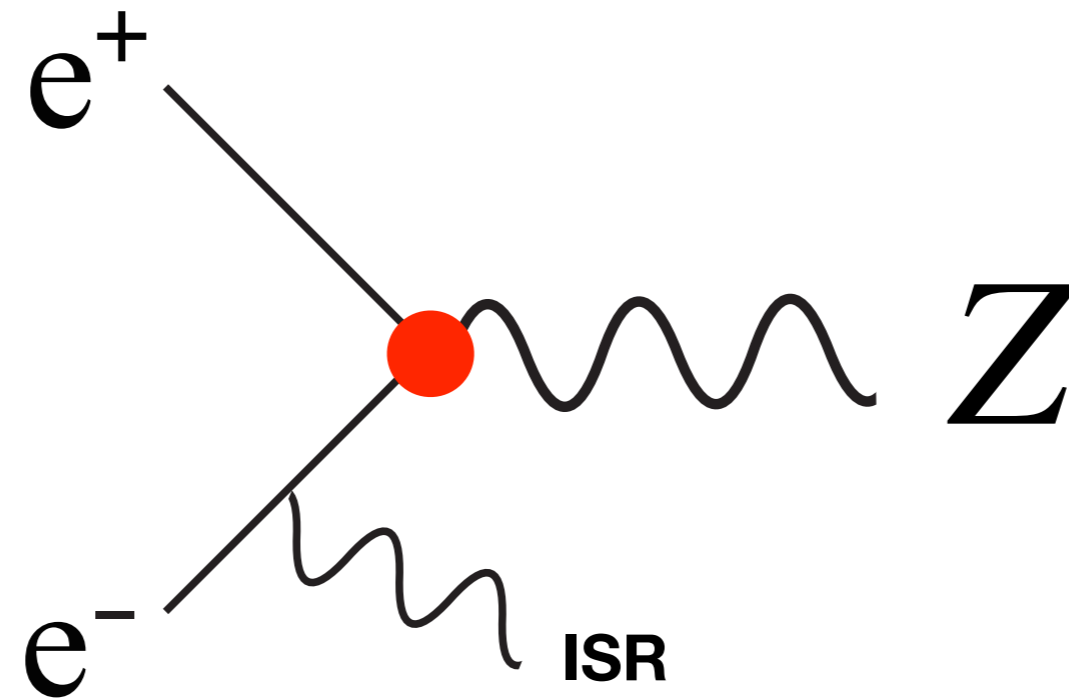
$e^+e^- \rightarrow Zh$



Z-pole

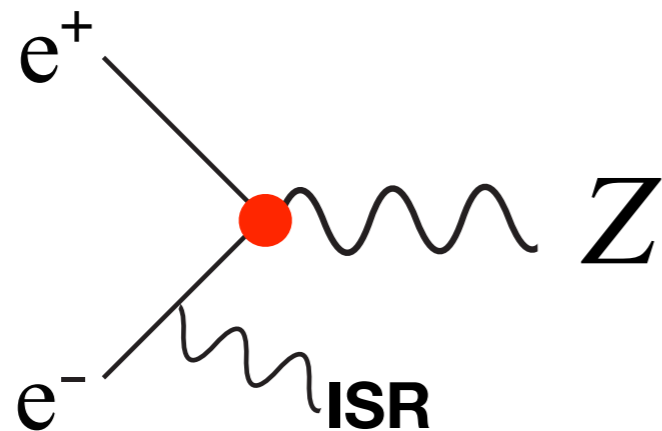
- contact interactions from $c_{HL}/c_{HL}'/c_{HE}$ in Higgs processes can be constrained by EWPOs at Z-pole: $\mathbf{A}_{LR}, \mathbf{\Gamma}_I$

a gift from ISR: radiative return @ ILC250



- ISR is mostly collinear
- asymmetric collision at Z-pole
- ISR (QED) retains initial e^-/e^+ chirality

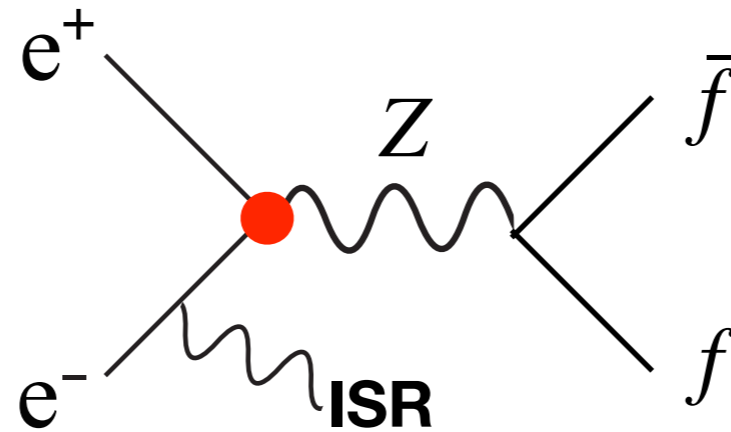
of radiative return events @ ILC250



ILC250	(-0.8,+0.3)	(+0.8,-0.3)
hadronic	46M	31M
leptonic	7.2M	4.9M
combined	54M	36M

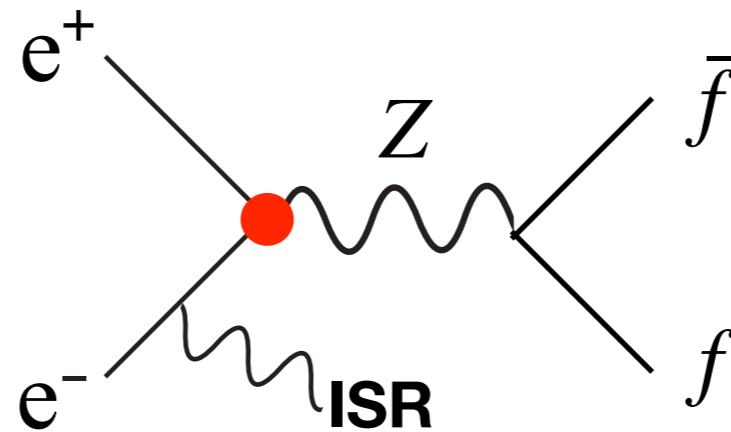
- $\sim 10^8$ events at ILC250 with 2 ab^{-1}
- > 5 (100) times than all Z at LEP (SLC)
- and now all with beam polarizations
- potentially much better A_f and R_f measurements

study of $e^+e^- \rightarrow \gamma Z$ @ ILC250



- reconstruction method from LEP 2: Z mass can be determined by only directions of two fermions
- shortly after our SMEFT studies in 2017, I proposed to use this process at ILC250 for improving A_{LR} (T.Barklow@AWLC17)
- SiD performed a fast simulation (T.Ueno@LCWS18)
- ILD full simulation ongoing (T.Mizuno)
- following are some expectations

study of $e^+e^- \rightarrow \gamma Z$ @ ILC250



method not working

$$\begin{pmatrix} p_1 \\ p_2 \end{pmatrix} = \frac{p_t}{\sin \phi} \begin{pmatrix} \frac{\sin(\phi - \phi_2)}{\sin \theta_1} \\ \frac{\sin(\phi_1 - \phi)}{\sin \theta_2} \end{pmatrix}$$

$$\phi = \phi_1 - \phi_2 \quad p_t = \sqrt{p_x^2 + p_y^2}$$

proper method

$$|\beta| = \frac{|\sin(\theta_1 + \theta_2)|}{\sin \theta_1 + \sin \theta_2}$$

for signal:

$$\beta = \frac{s - m_{12}^2}{s + m_{12}^2}$$

$$m_{12} = \sqrt{\frac{1 - \beta}{1 + \beta} s}$$

inputs and assumptions for A_f and R_f

	efficiency	systematics
Z->hadrons	73% ^[1]	0
Z-> $\mu\mu/ee$	88% ^[2]	0
Z-> $\tau\tau$ (Rf)	80% ^[3]	0.1%
Z-> $\tau\tau$ (Af)	80% ^[3]	0
Z->bb (Rf)	73% x 80% ^[4]	0.1%
Z->bb (Af)	73% x 40% ^[4]	0
Z-> cc (Rf)	73% x 30% ^[4]	0.5%
Z-> cc (Af)	73% x 10% ^[4]	0

[1] Takayuki Ueno, Master Thesis

[2] T.Suehara et al; [3] D.Jeans; [4] R.Poeschl et al

result: A_{LR} using $e+e^- \rightarrow \gamma Z (A_e)$

$$A_{LR} = \frac{\sigma_L - \sigma_R}{\sigma_L + \sigma_R} = A_e$$

$$\Delta A_e = \frac{1}{\sqrt{N}} \sqrt{K^2 - A_e^2}$$

$$K = \frac{1 + |P_{e^-} P_{e^+}|}{|P_{e^-}| + |P_{e^+}|} \quad N: \# \text{ of sig. events}$$

- to measure: cross sections for $(-0.8, +0.3)$ and $(+0.8, -0.3)$, using all hadronic and leptonic channels

ILC250	N_L	N_R	ΔA_{LR}
hadronic	46M	31M	0.00015
leptonic	7.2M	4.9M	0.00035
combined	54M	36M	0.00014

- main systematics would be uncertainty of K factor (effective polarization), which would be determined using WW data -> c.f. R.Karl's thesis, and further study would be needed

result: A_{LR} using $e^+e^- \rightarrow \gamma Z$ (A_f , $f=\mu/\tau/b/c$)

$$A_{LRFB} = \frac{\sigma_{LF} - \sigma_{LB} - \sigma_{RF} + \sigma_{RB}}{\sigma_{LF} + \sigma_{LB} + \sigma_{RF} + \sigma_{RB}} = \frac{3}{4} A_f \quad \Delta A_f = \frac{1}{\sqrt{N}} \sqrt{\frac{16}{9} K^2 - A_f^2}$$

- to measure: + cross sections in the forward/backward regions

	ΔA_b	ΔA_c	ΔA_μ	ΔA_τ
ILC250	0.00053	0.0014	0.00080	0.00083

- systematics: + uncertainties from charge identification, momentum directions -> c.f. study by Adrain for bb/cc , need further study here due to the boost of Z (more forward jets); also need to study tau channel the about the momentum directions

result: BR(Z->ff) using e+e- -> γZ (R_f, f=μ/τ/b/c)

$$R_{b/c} = \frac{\Gamma(Z \rightarrow b\bar{b}/c\bar{c})}{\sum_q \Gamma(Z \rightarrow q\bar{q})} \quad R_{\mu/\tau} = \frac{\sum_q \Gamma(Z \rightarrow q\bar{q})}{\Gamma(Z \rightarrow \mu^+\mu^-/\tau^+\tau^-)}$$

- to measure: σxBR, relative simple

	ΔR _b	ΔR _c	ΔR _μ	ΔR _τ	ΔR _e
ILC250	0.00023	0.00087	0.011	0.024	0.024

- systematics: uncertainty on various efficiencies

result: Zff couplings (gL/gR) using e+e- -> γZ

$$\delta g_L = \frac{A_f}{2(A_f + 1)} \delta A_f \oplus \frac{1}{2} \delta R_f \oplus \frac{1}{2} \delta \Gamma_{had}$$

$$\delta g_R = \frac{A_f}{2(A_f - 1)} \delta A_f \oplus \frac{1}{2} \delta R_f \oplus \frac{1}{2} \delta \Gamma_{had}$$



note the large factor for b_R coupling

result: EWPOs from $e^+e^- \rightarrow \gamma Z$

Quantity	Value	current	GigaZ		250 GeV	
		$\delta[10^{-4}]$	$\delta_{stat}[10^{-4}]$	$\delta_{sys}[10^{-4}]$	$\delta_{stat}[10^{-4}]$	$\delta_{sys}[10^{-4}]$
boson properties						
m_W	80.379	1.5	-	-	-	0.3 °
m_Z	91.1876	0.23	-	-	-	-
Γ_Z	2.4952	9.4	-	3.2	-	-
$\Gamma_Z(had)$	1.7444	11.5	-	3.2	-	-
Z-e couplings						
$1/R_e$	0.0482	24.	2.	4 †	5.5	10 +
A_e	0.1515	139.	0.1	5 *	9.5	3 *
g_L^e	-0.632	16.	1.	2.5	2.8	7.6
g_R^e	0.551	18.	1.	2.5	2.9	7.6
Z- ℓ couplings						
$1/R_\mu$	0.0482	16.	2.	2. †	5.5	10 +
$1/R_\tau$	0.0482	22.	2.	4. †	5.7	10 +
A_μ	0.1515	991.	2.	5 *	54.	3 *
A_τ	0.1515	271.	2.	5 *	57.	3 *
g_L^μ	-0.632	66.	1.	1.8	4.5	7.6
g_R^μ	0.551	89.	1.	1.9	5.5	7.6
g_L^τ	-0.632	22.	1.	2.5	4.7	7.6
g_R^τ	0.551	27.	1.	2.5	5.8	7.6
Z-b couplings						
R_b	0.2163	31.	0.4	7. #	3.5	10 +
A_b	0.935	214.	1.	5. *	5.7	3 *
g_L^b	-0.999	54.	0.31	4.0	2.2	7.6
g_R^b	0.184	1540	7.2	36.	41.	23.
Z-c couplings						
R_c	0.1721	174.	2.	30 #,+	5.8	50 +
A_c	0.668	404.	3.	6. *	21.	3 *
g_L^c	0.816	119.	1.2	15.	5.1	26.
g_R^c	-0.367	415.	3.1	16.	21.	26.

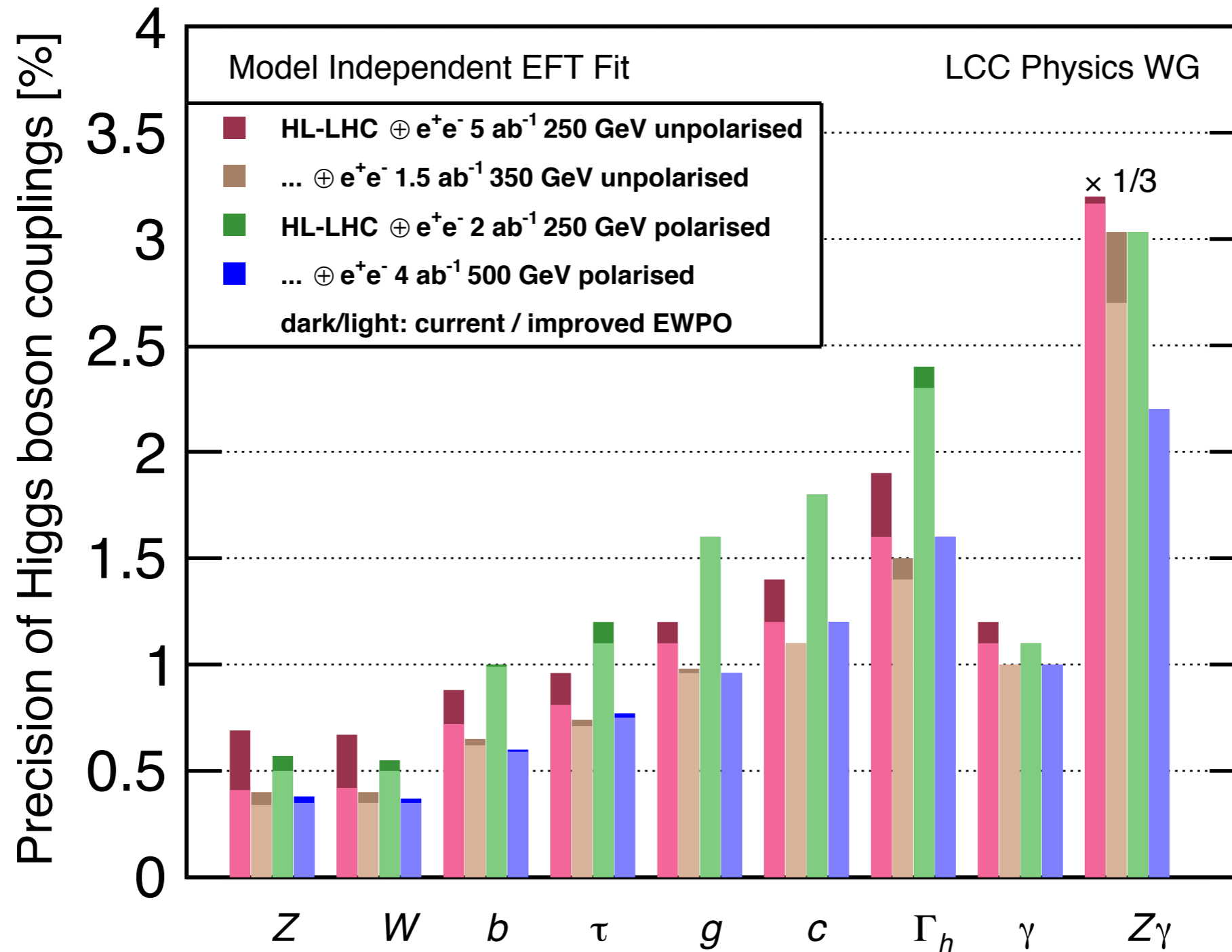
take-home message

if we work hard and be smart

$$\text{ILC250} = \text{ILC250} + 100x\text{LEP/SLC}$$

appendix

impact of EWPOs



experimental inputs and assumptions for section 1

	efficiency	systematics	$\cos\theta$	bin width
$\mu\mu$	98% ^[1]	0.1%	[-0.95,0.95]	0.1
$\tau\tau$	90% ^[2]	0.2%	[-0.95,0.95]	0.1
$b\bar{b}$	29% ^[3]	0.2%	[-0.95,0.95]	0.1
$c\bar{c}$	7% ^[3]	0.5%	[-0.95,0.95]	0.1
$e\bar{e}$	97% ^[1]	0.1%	[-0.95,0.95]	0.1

flat acceptance function within the fiducial volume

b- and c-charge identification efficiency applied

analytic differential cross section, w/o effects from beamstrahlung and ISR

[1] T.Suehara; [2] D.Jeans; [3] R.Poeschl

computation for W and Y oblique parameters

(provided by M. Peskin & M. Perelstein)

$$\frac{d\sigma}{d\cos\theta}(e_L^- e_R^+ \rightarrow f_L \bar{f}_R) = \frac{\pi\alpha^2}{2s} |F_{LL}|^2 (1 + \cos\theta)^2$$

$$\frac{d\sigma}{d\cos\theta}(e_L^- e_R^+ \rightarrow f_R \bar{f}_L) = \frac{\pi\alpha^2}{2s} |F_{LR}|^2 (1 - \cos\theta)^2$$

$$\frac{d\sigma}{d\cos\theta}(e_R^- e_L^+ \rightarrow f_L \bar{f}_R) = \frac{\pi\alpha^2}{2s} |F_{RL}|^2 (1 - \cos\theta)^2$$

$$\frac{d\sigma}{d\cos\theta}(e_R^- e_L^+ \rightarrow f_R \bar{f}_L) = \frac{\pi\alpha^2}{2s} |F_{RR}|^2 (1 + \cos\theta)^2$$

$$F_{LL}(s) = - \left[Q_f + \frac{(\frac{1}{2} - s_w^2)(I_f^3 - s_w^2 Q_f)}{s_w^2 c_w^2} \frac{s}{(s - m_Z^2)} - \frac{\frac{1}{2} I_f^3}{s_w^2} \frac{s}{m_W^2} \mathbf{W} - \frac{\frac{1}{2} Y_f}{c_w^2} \frac{s}{m_W^2} \mathbf{Y} \right]$$

$$F_{LR}(s) = - \left[Q_f + \frac{(\frac{1}{2} - s_w^2)(-s_w^2 Q_f)}{s_w^2 c_w^2} \frac{s}{(s - m_Z^2)} - \frac{\frac{1}{2} Q_f}{c_w^2} \frac{s}{m_W^2} \mathbf{Y} \right]$$

$$F_{RL}(s) = - \left[Q_f + \frac{(-s_w^2)(I_f^3 - s_w^2 Q_f)}{s_w^2 c_w^2} \frac{s}{(s - m_Z^2)} - \frac{Y_f}{c_w^2} \frac{s}{m_W^2} \mathbf{Y} \right]$$

$$F_{RR}(s) = - \left[Q_f + \frac{(-s_w^2)(-s_w^2 Q_f)}{s_w^2 c_w^2} \frac{s}{(s - m_Z^2)} - \frac{Q_f}{c_w^2} \frac{s}{m_W^2} \mathbf{Y} \right]$$

composite models

	η_{LL}	η_{RR}	η_{LR}	η_{RL}
Λ_{LL}^+	1	0	0	0
Λ_{LL}^-	-1	0	0	0
Λ_{RR}^+	0	1	0	0
Λ_{RR}^-	0	-1	0	0
Λ_{VV}^+	1	1	1	1
Λ_{VV}^-	-1	-1	-1	-1
Λ_{AA}^+	1	1	-1	-1
Λ_{AA}^-	-1	-1	1	1
$\Lambda_{(V-A)}^+$	0	0	1	1
$\Lambda_{(V-A)}^-$	0	0	-1	-1

$$\mathcal{L}_{LL} = \frac{g_{\text{contact}}^2}{2\Lambda^2} \sum_{i,j} \eta_{LL}^{ij} (\bar{\psi}_L^i \gamma_\mu \psi_L^i) (\bar{\psi}_L^j \gamma^\mu \psi_L^j),$$

$$\mathcal{L}_{RR} = \frac{g_{\text{contact}}^2}{2\Lambda^2} \sum_{i,j} \eta_{RR}^{ij} (\bar{\psi}_R^i \gamma_\mu \psi_R^i) (\bar{\psi}_R^j \gamma^\mu \psi_R^j),$$

$$\mathcal{L}_{LR} = \frac{g_{\text{contact}}^2}{2\Lambda^2} \sum_{i,j} \eta_{LR}^{ij} (\bar{\psi}_L^i \gamma_\mu \psi_L^i) (\bar{\psi}_R^j \gamma^\mu \psi_R^j),$$

$$\mathcal{L}_{RL} = \frac{g_{\text{contact}}^2}{2\Lambda^2} \sum_{i,j} \eta_{RL}^{ij} (\bar{\psi}_R^i \gamma_\mu \psi_R^i) (\bar{\psi}_L^j \gamma^\mu \psi_L^j),$$

Tanabashi, et al,
PRD 98 (2018) 030001

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