


A relation between **track length**
and **deposited energy** in
homogeneous calorimeter by
GEANT4 simulation at high energy



Tohru Takeshita - Shinshu
CHEF2019@Fukuoka

bbjes from Higgs factory

- $E_{bjet} \sim 50-100 \text{ GeV}$ at HF

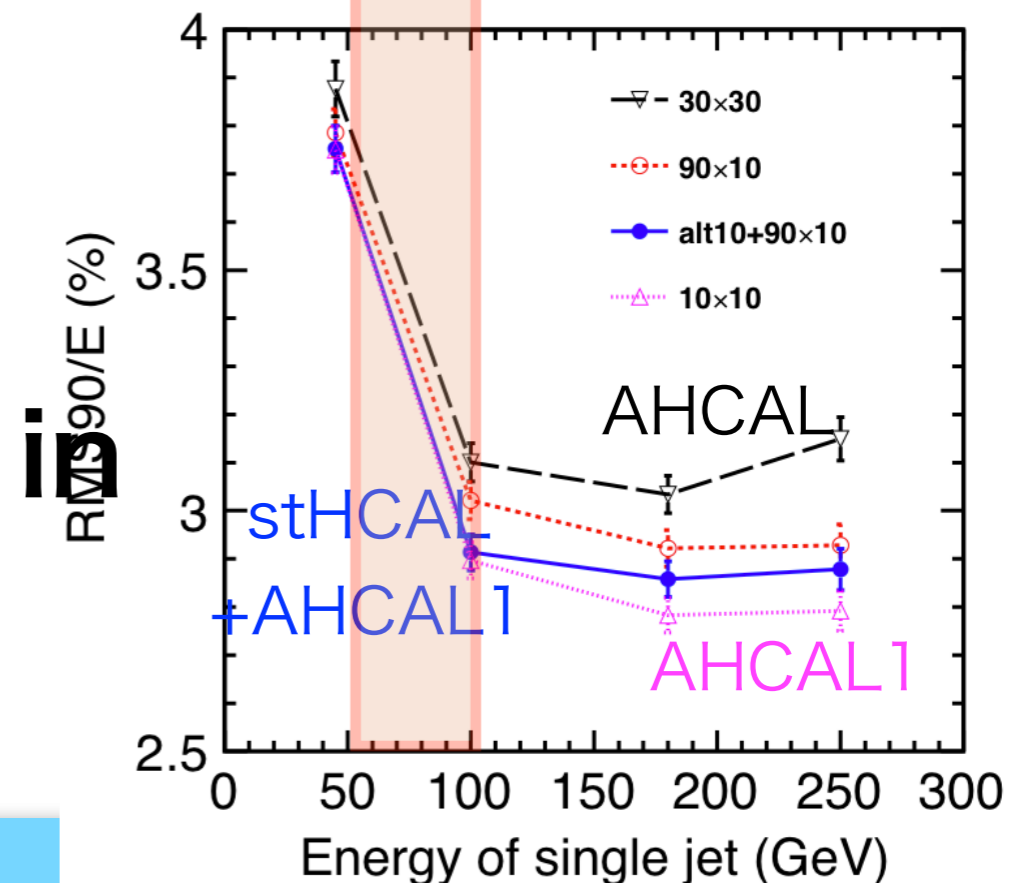
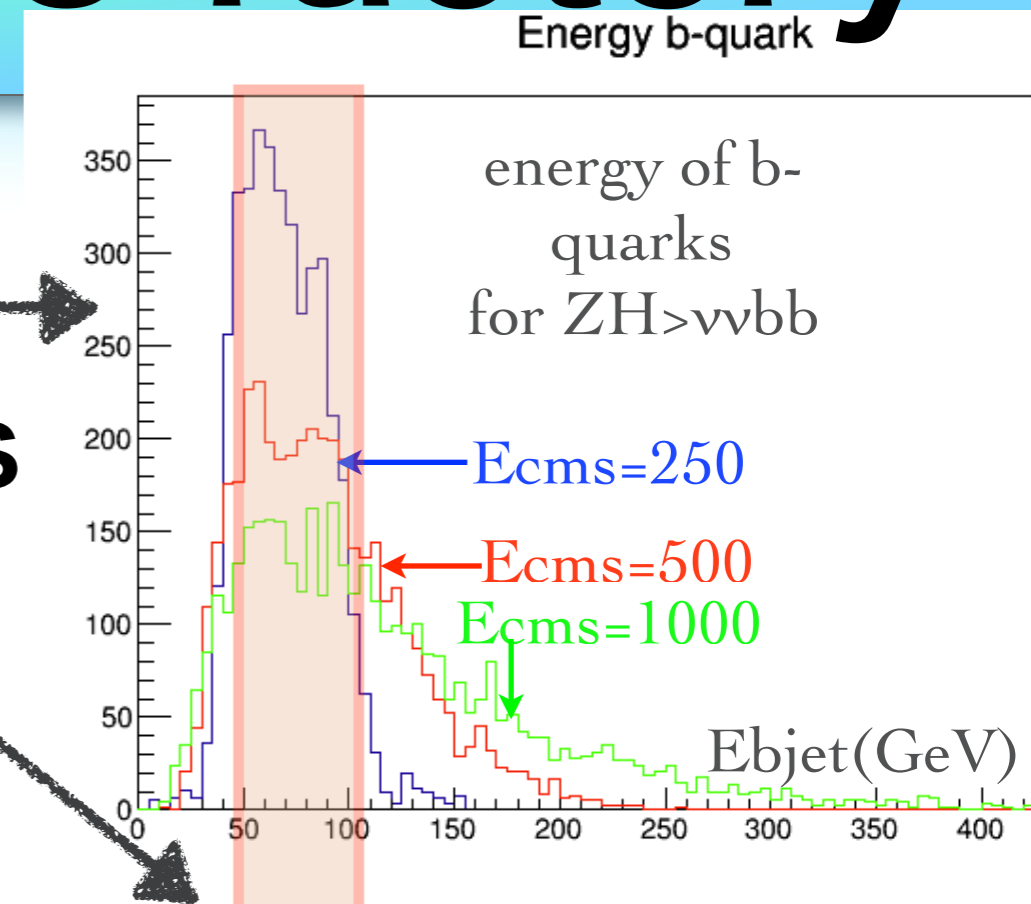
- Energy Resolution of Jets (JER) PFA is degraded

- due to HCAL E-resolution intrinsic

- PFA does work well at higher energies

- to improve Jet EReso. 50-100 GeV region

$E_{particle} < 10 \text{ GeV}$



Particle Flow Algorithm

- PFA requires 3D calorimeter

- **with fine segmented cells**

- to separate each particles

- JetER is dominated by HCAL
R at lower energies

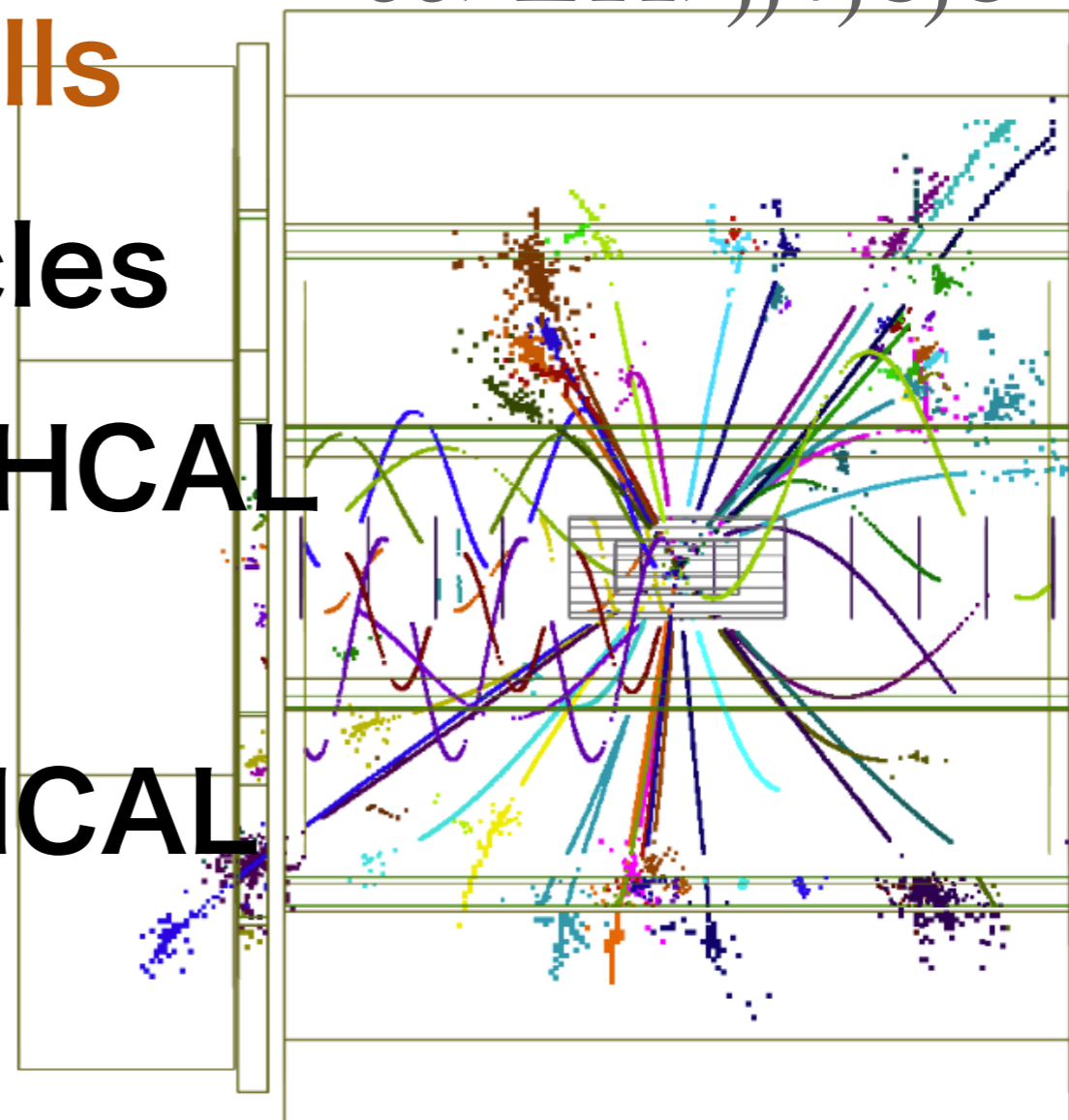
- intrinsic resolution of HCAL

- **measure total hadrons**

best case


- hoping fine segmentation

$ee \rightarrow ZH \rightarrow jj + jbjb$

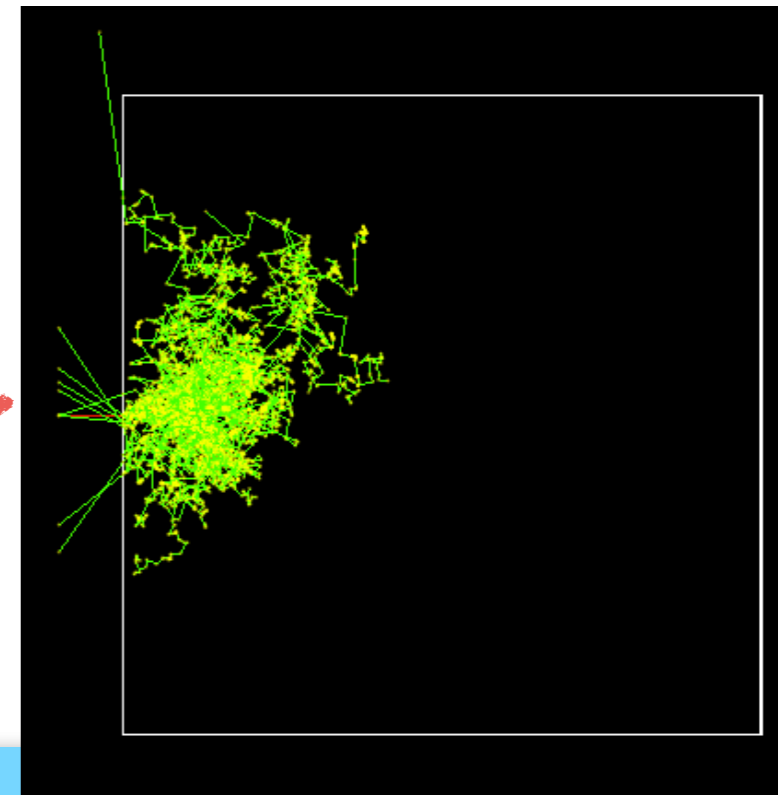


ILD at 250GeV

total measurements

- **GEANT4 simulation $2\text{m} \times 2\text{m} \times 2\text{m}$**
 - time cut $< 100\text{ns}$
 - Hadron model = FTFP-BERT
- **homogeneous CAL. for exam.:** absorber : PbWO4
- **two measures from the calorimeter**
- **TL : Track length \propto Cherenkov** PbWO4
- **ED : $dE/dx \propto$ scintillation**
- **how much ER at best ?** $3\text{ GeV } \pi^-$ 

green lines
are neutrons



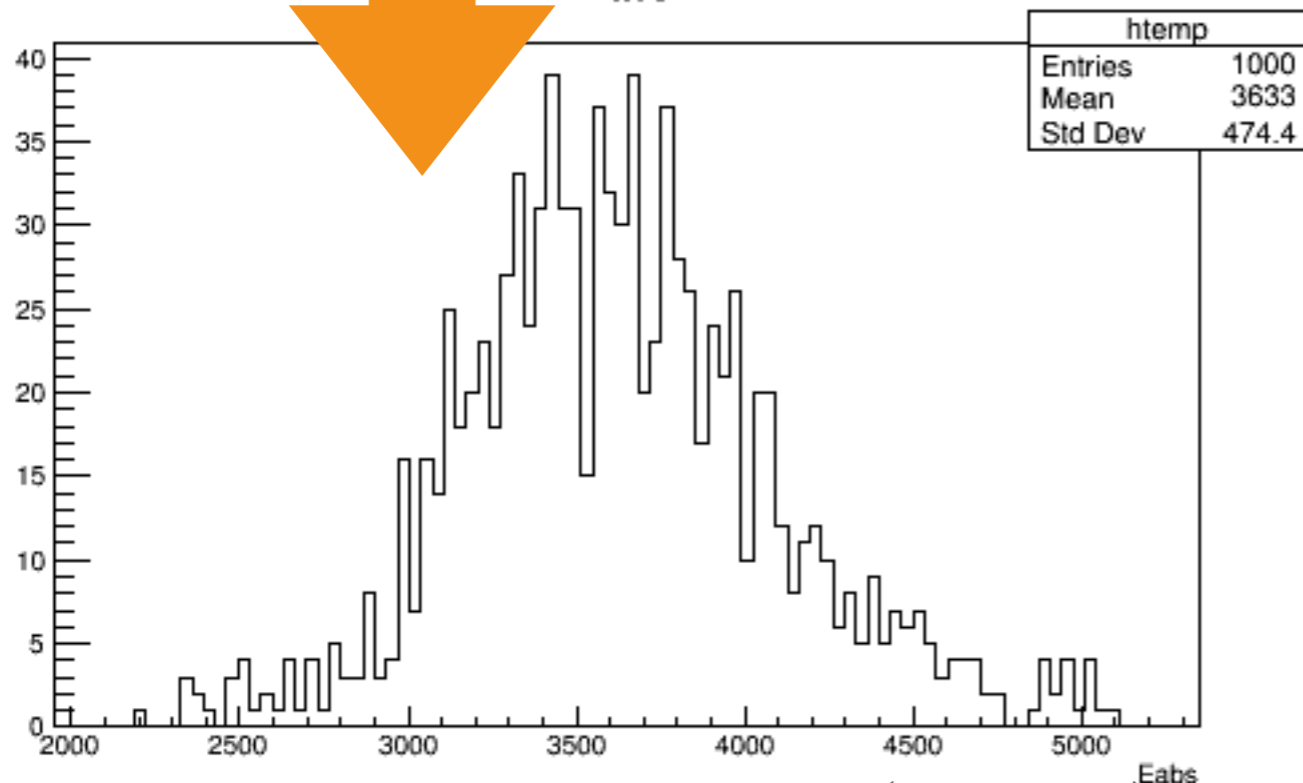
ED and TL

for 5 GeV pi-

energy sum



Eabs



ED (MeV)

resolution~13% @ 5GeV

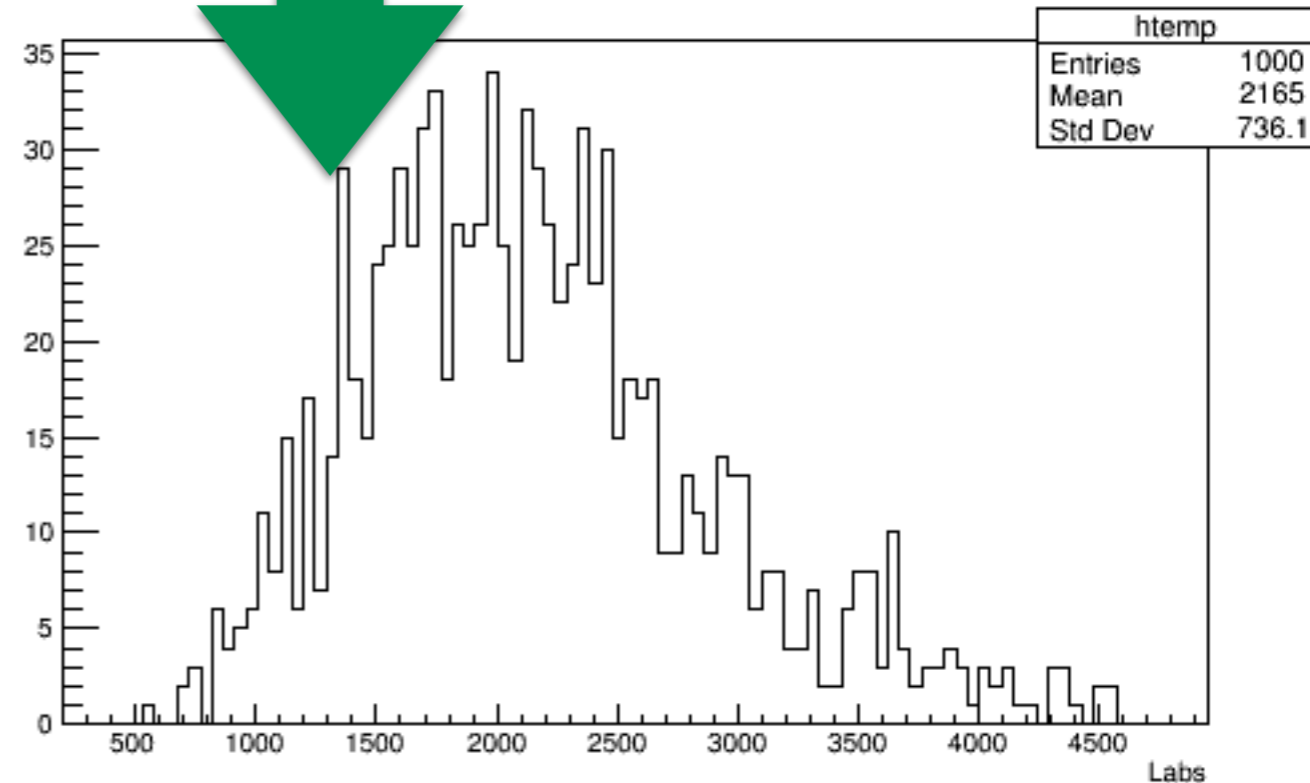
ED=sum of energy deposit

~ sum of scintillation lights in PbWO4

Cherenkov sum



Labs



TL (mm)

resolution~30% @ 5GeV

TL= sum of track length

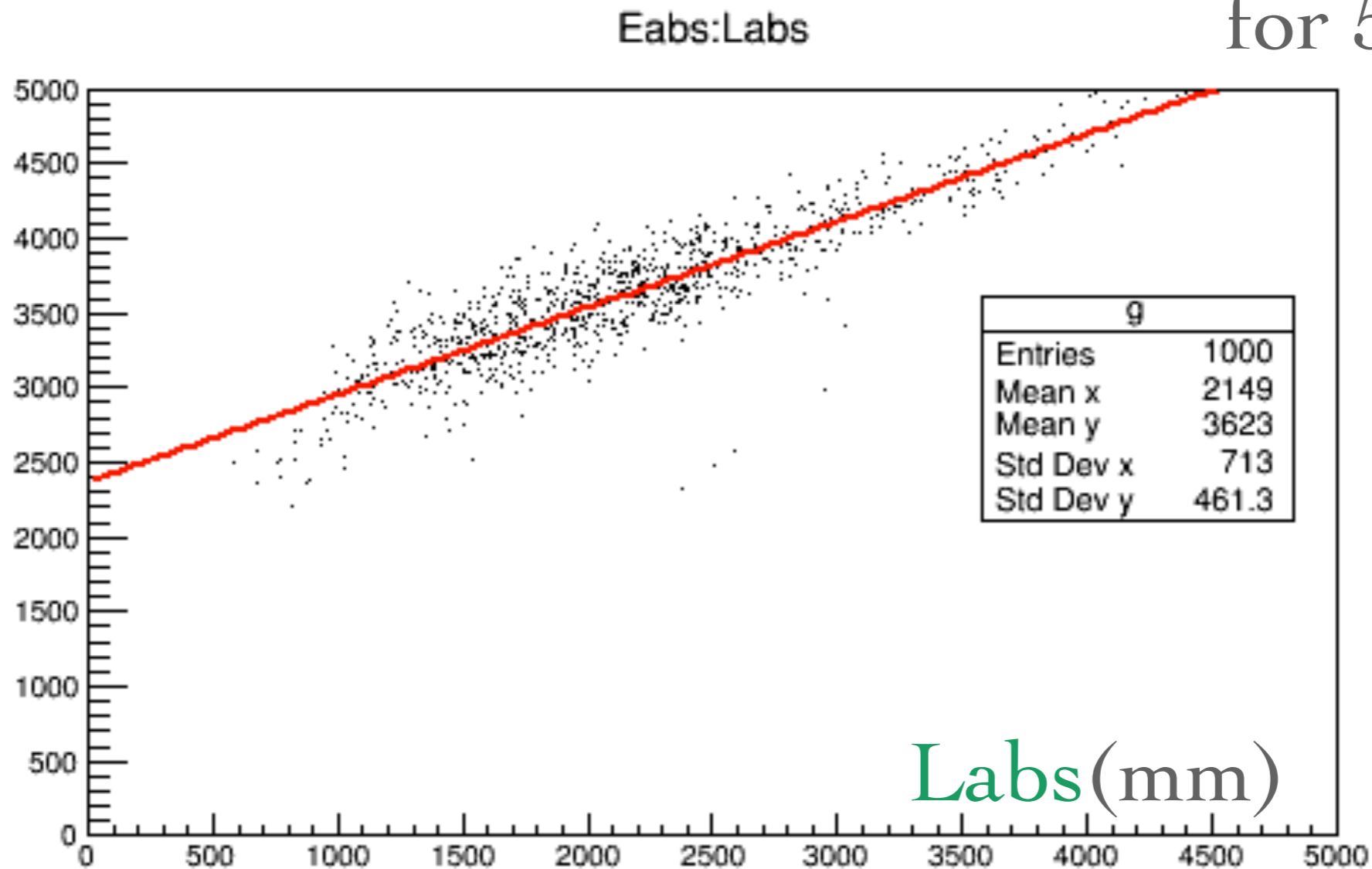
~ sum of Cherenkov lights in PbWO4

ED vs TL

- strong correlation between ED vs TL

for 5 GeV pi-

E_{abs}
(MeV)

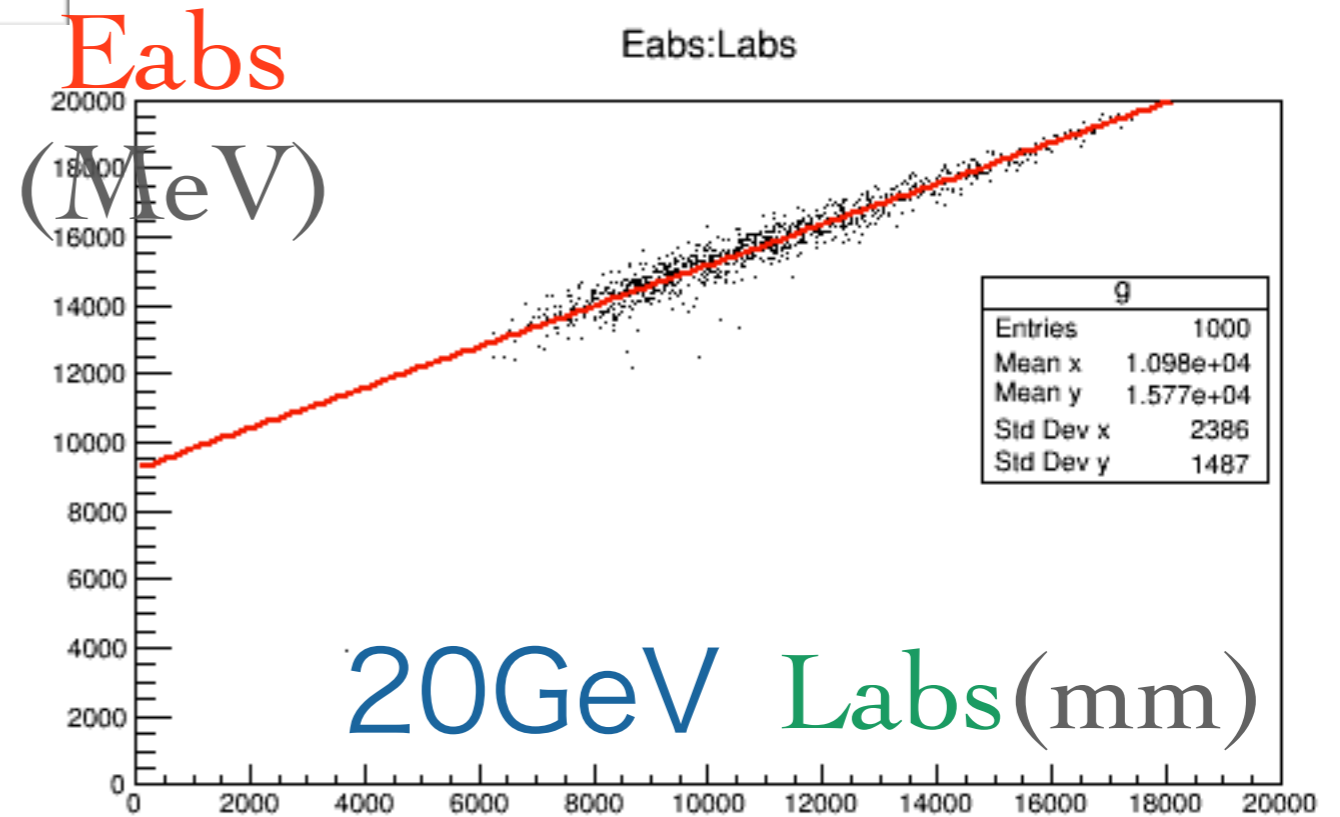
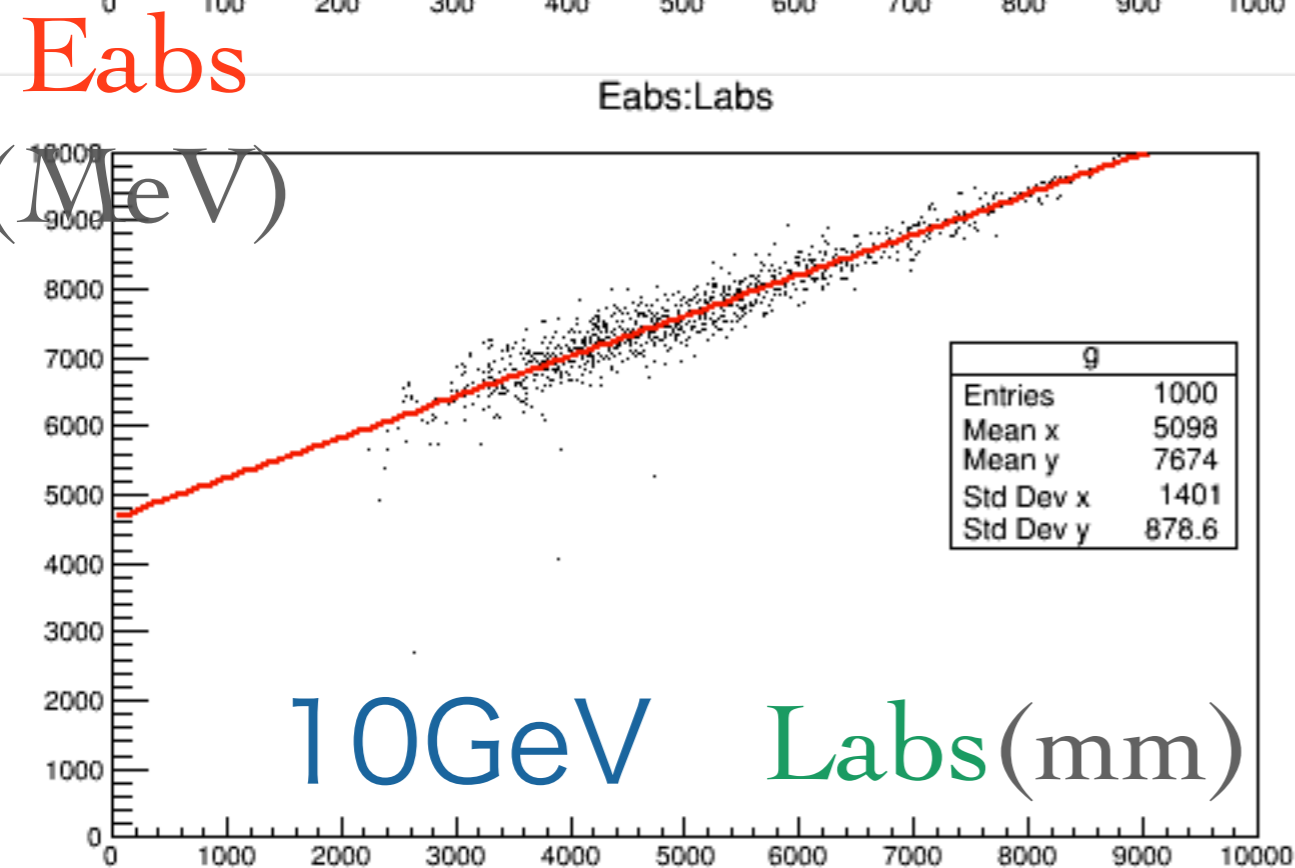
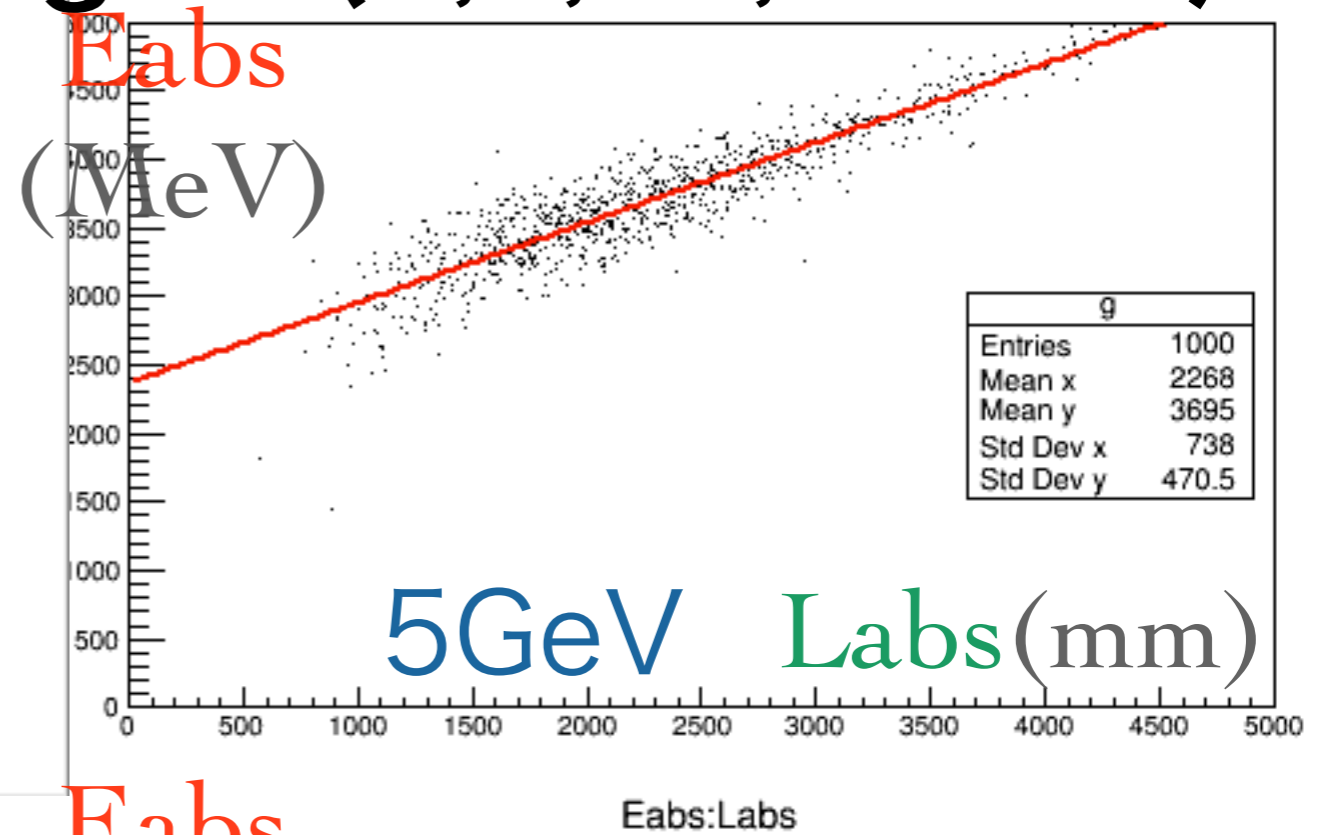
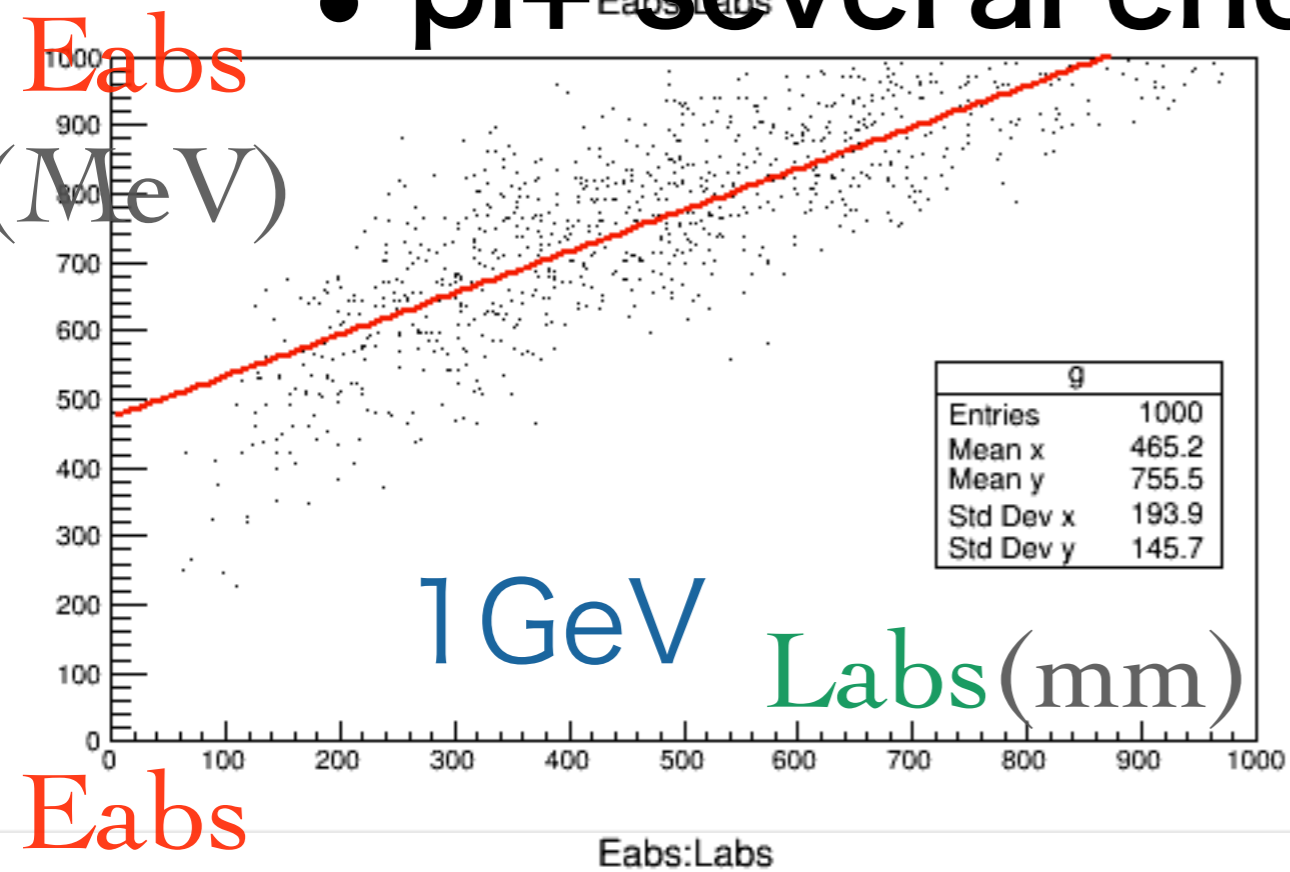


- approx. in linear with constant term in ED

ED vs TL

for π^+

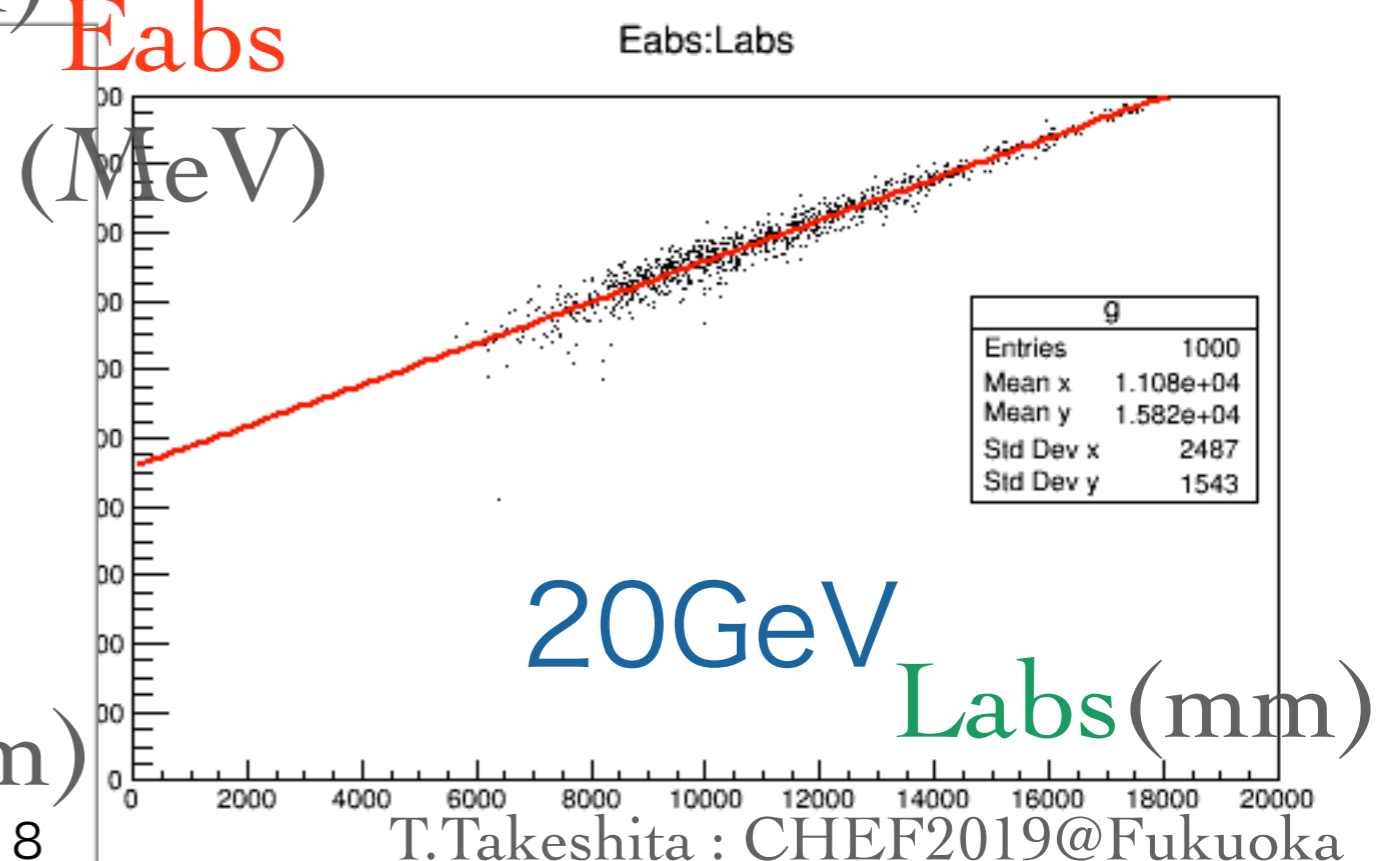
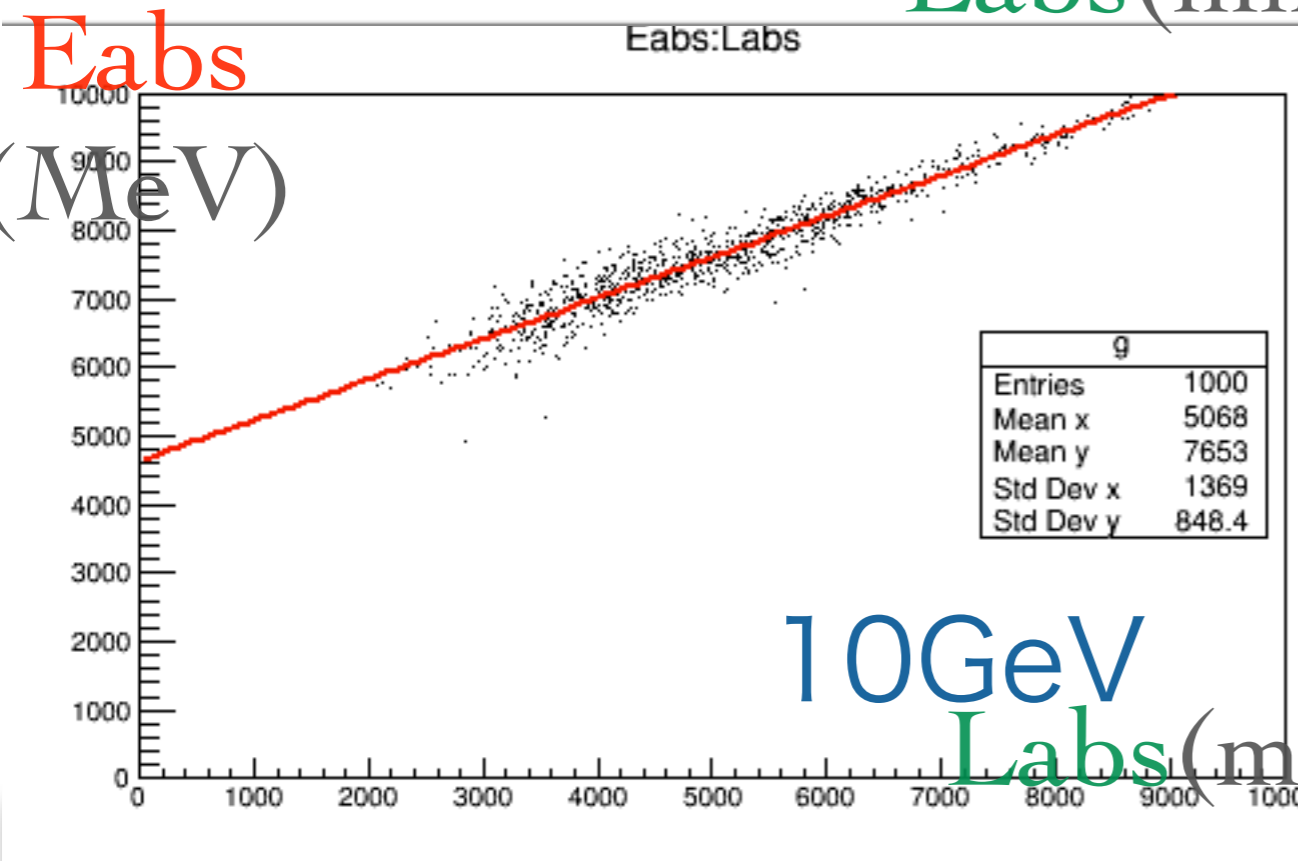
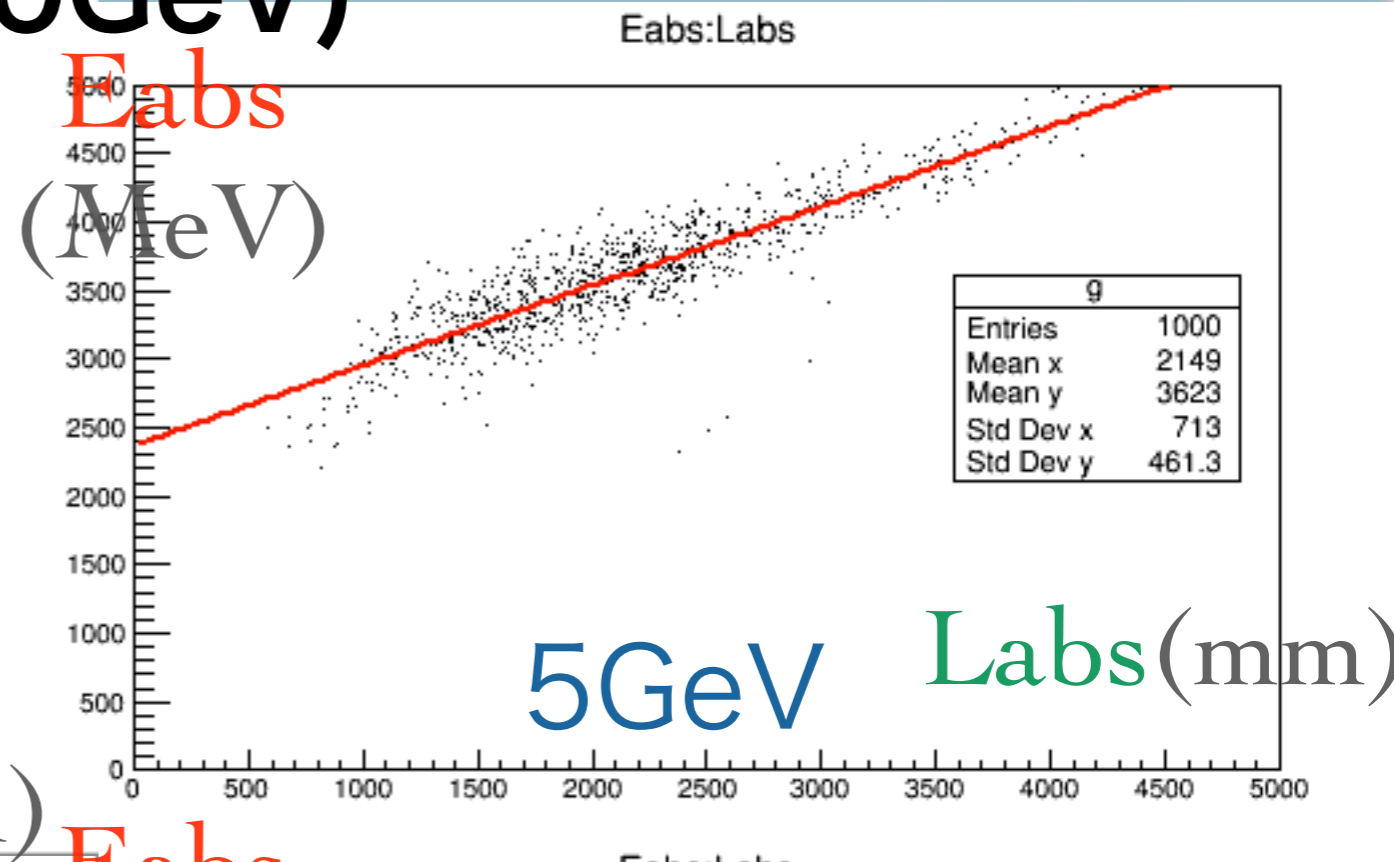
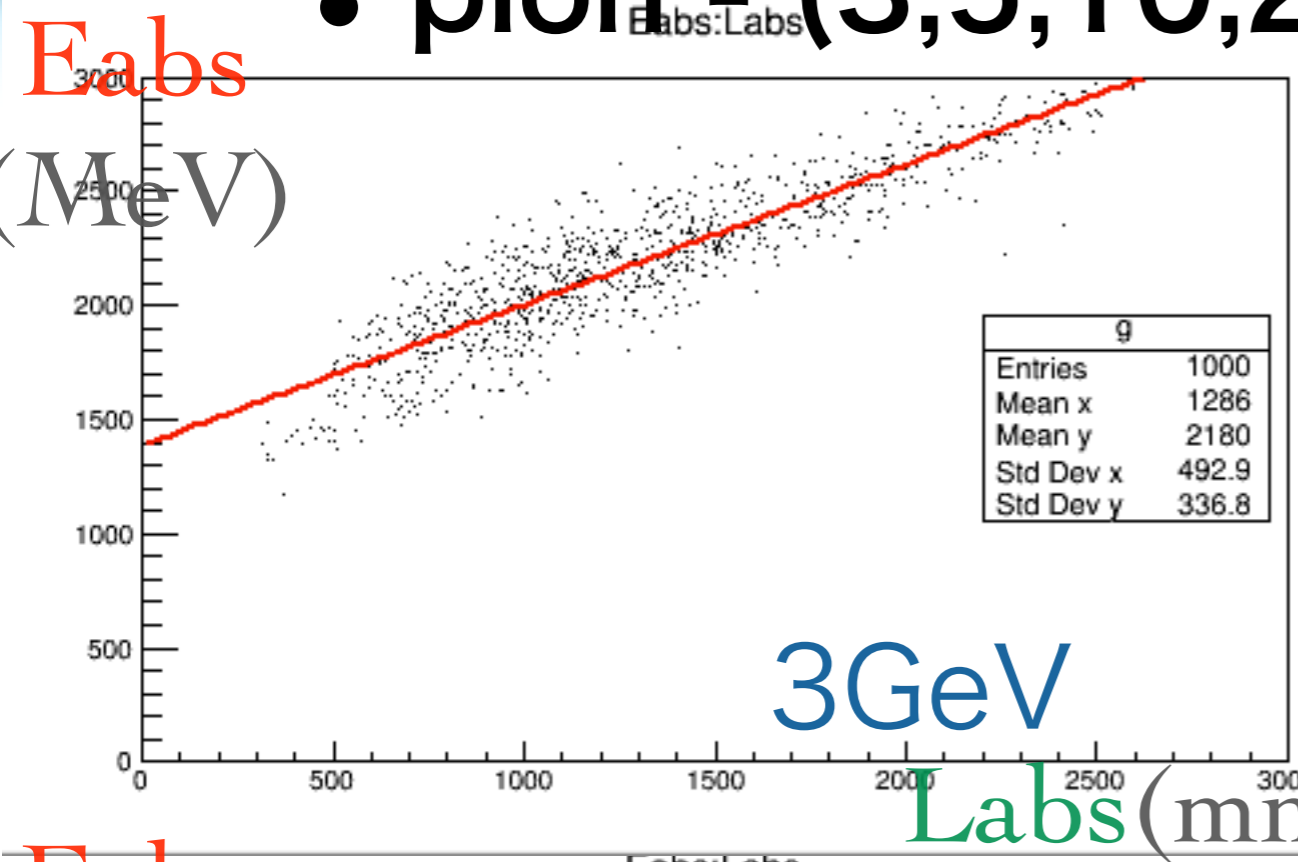
- π^+ several energies (1,5,10,20GeV)



ED vs TL

for pi-

- pion - (3,5,10,20GeV)



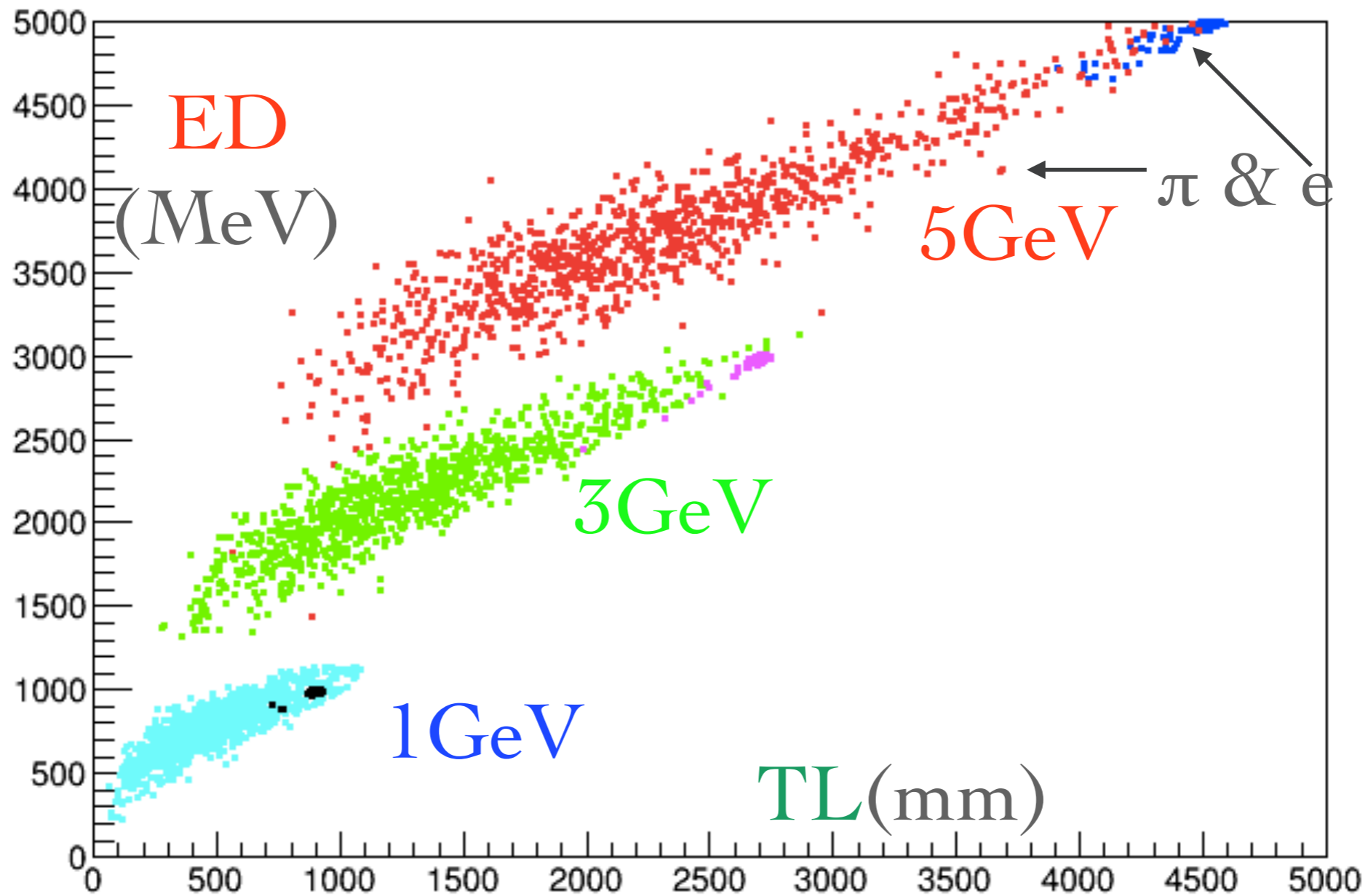
ED vs TL

constant slop for pi+ and e-

Eabs:Labs

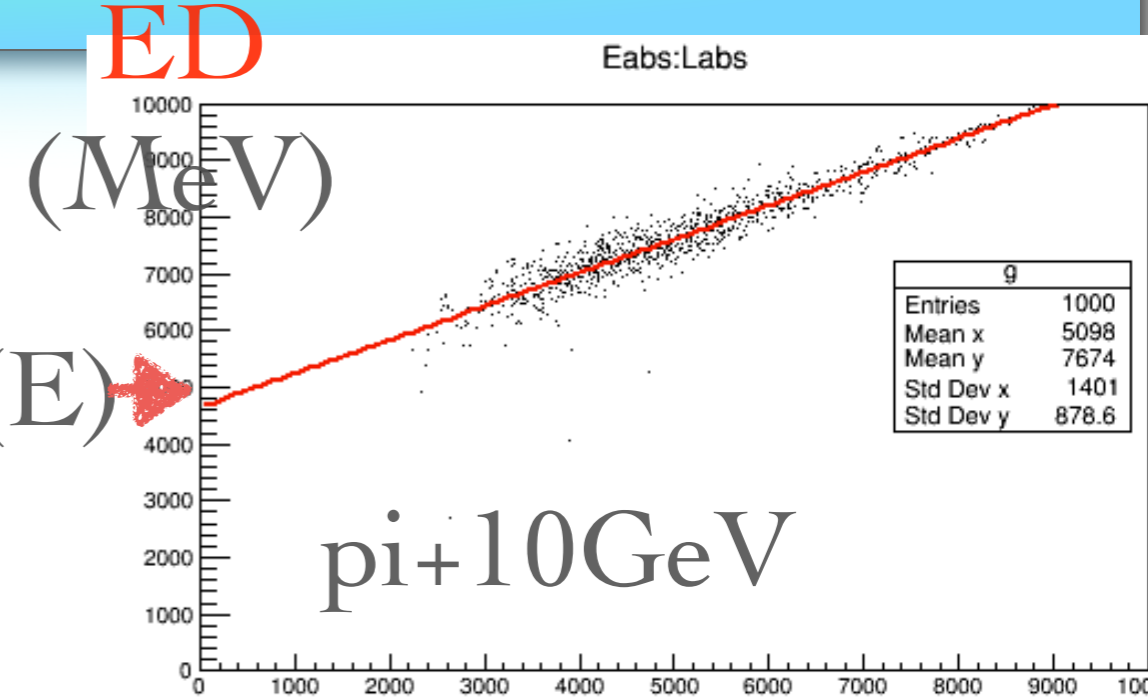
$$E_{abs} = A(E) + B * L_{abs}$$

MeV mm

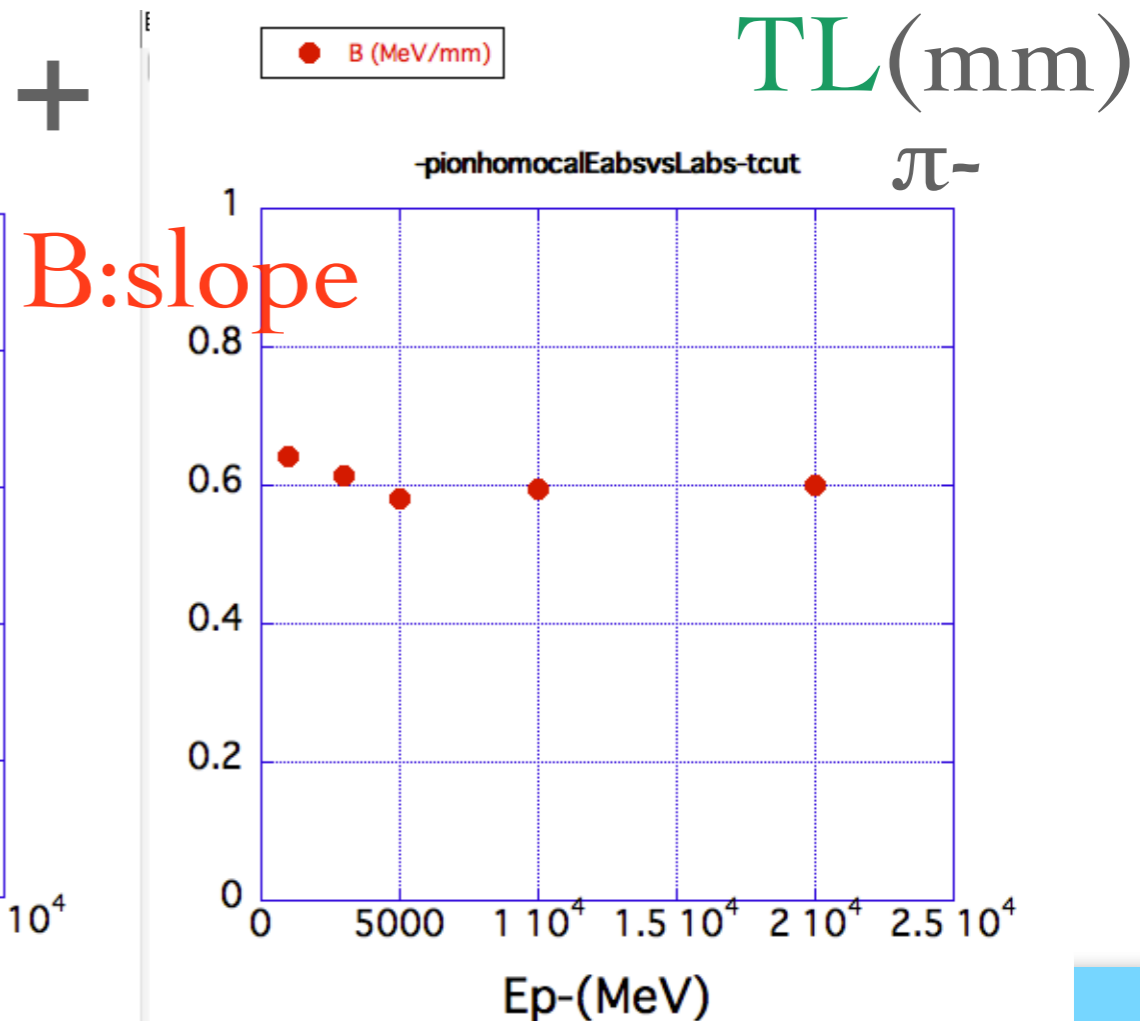
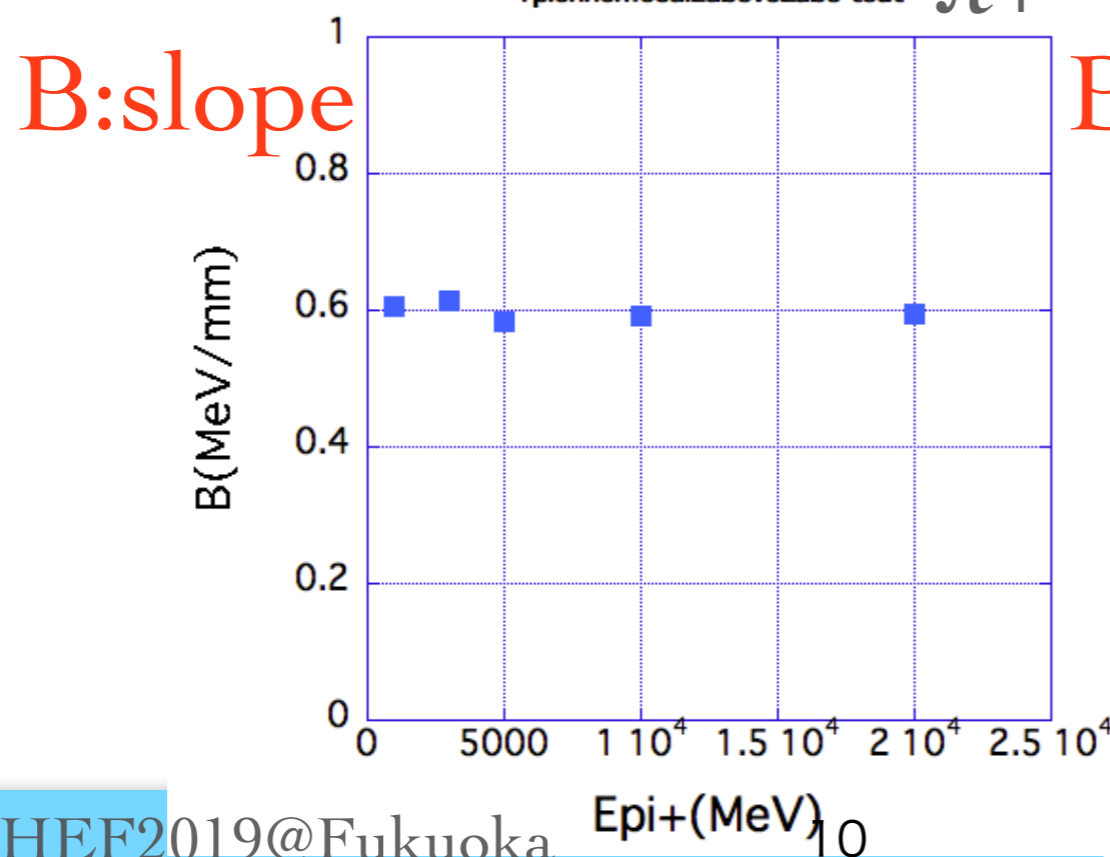


slop of ED and TL

- when fitted with linear $ED = A(E) + B * TL$
- slope = B is constant for all energies $E > 1 \text{ GeV}$



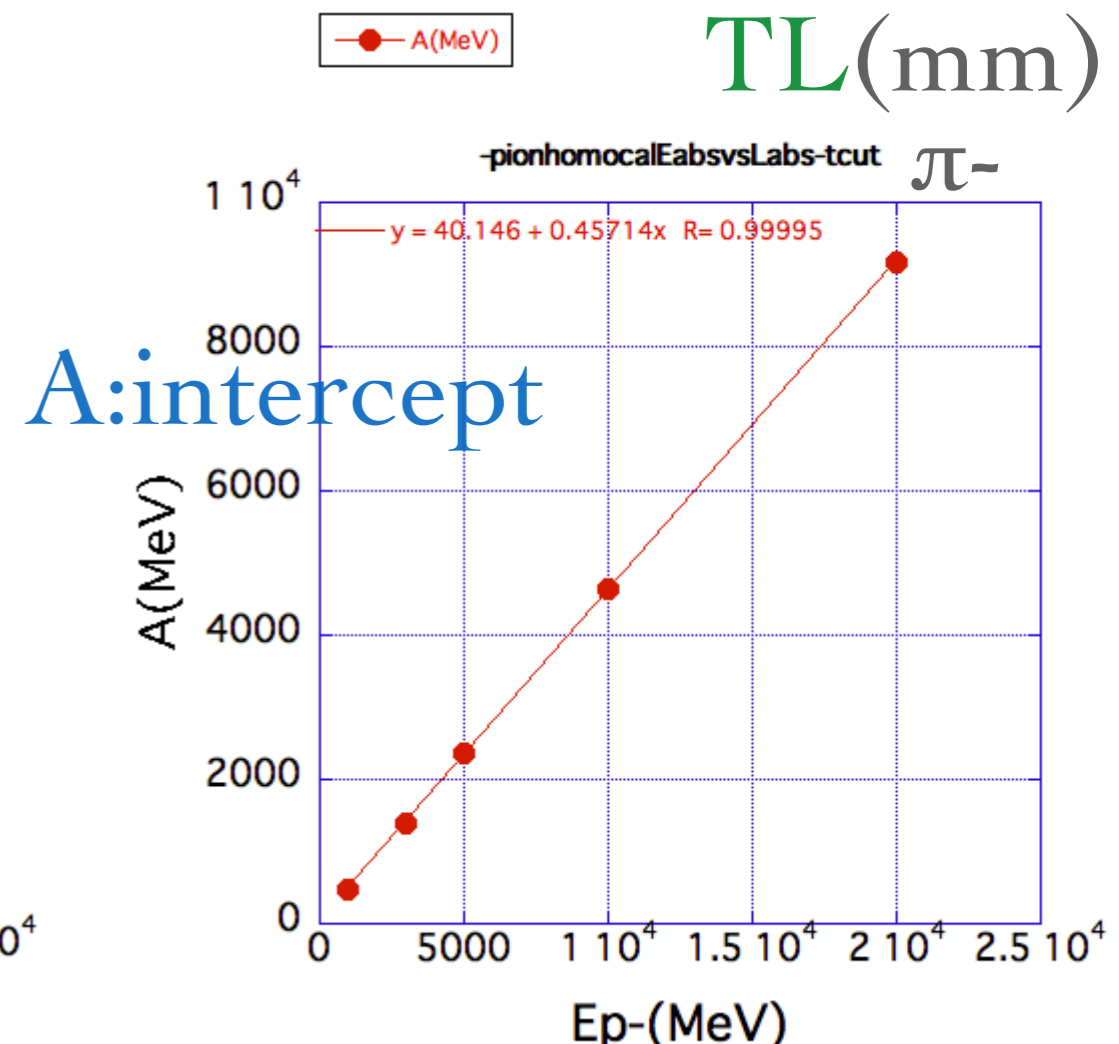
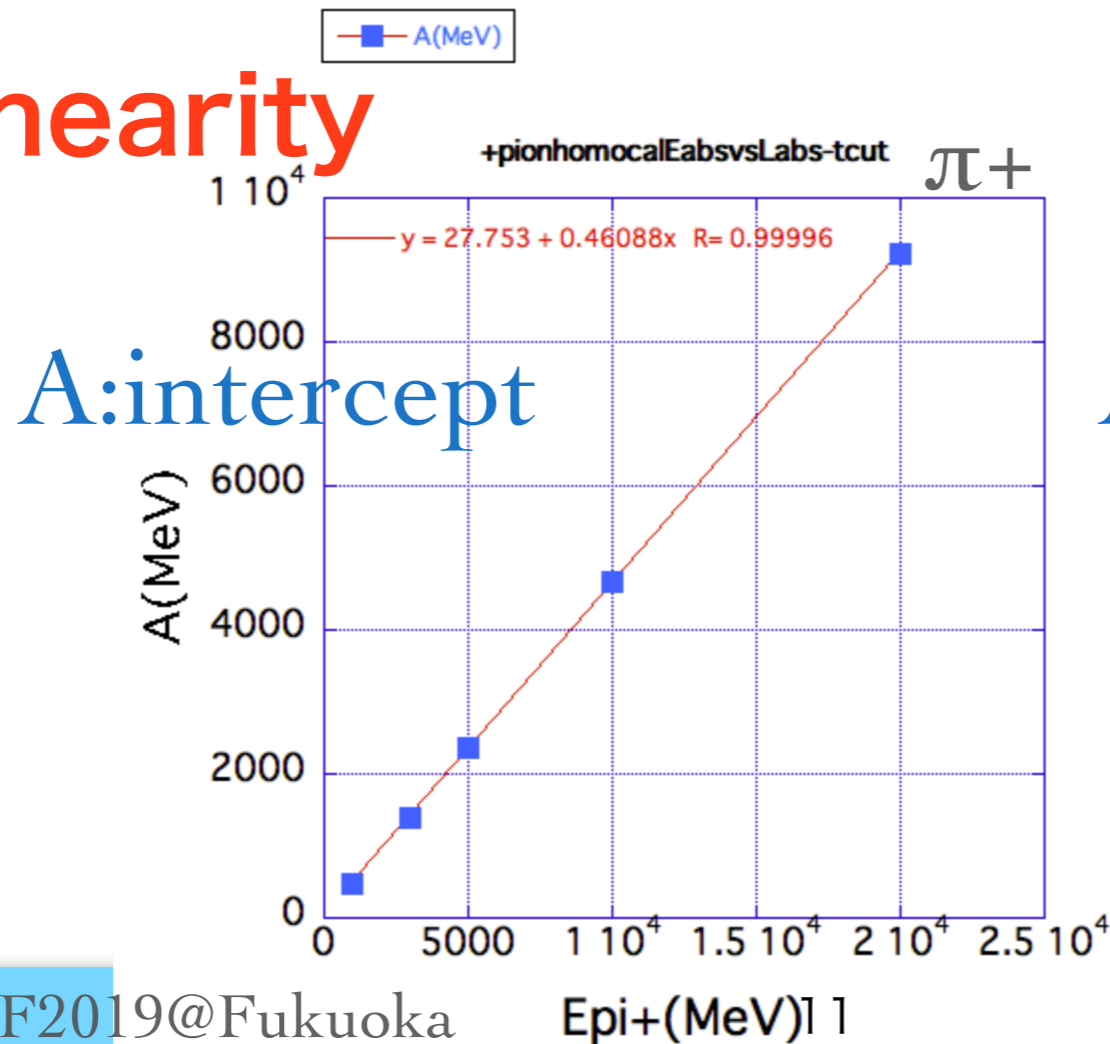
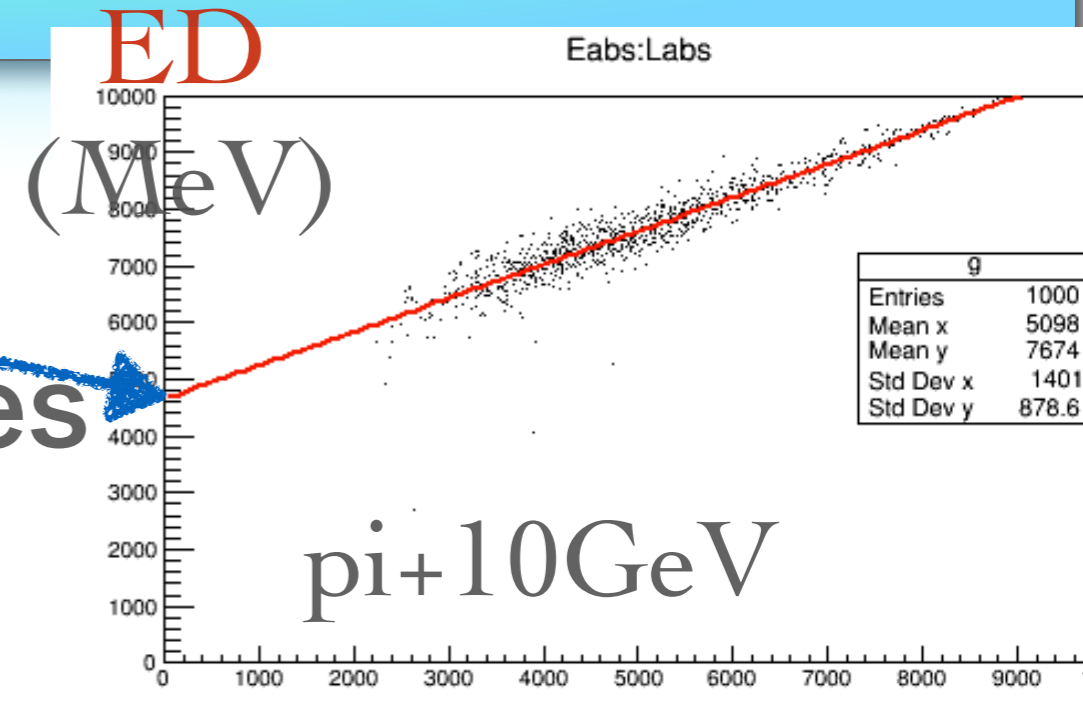
- no difference with π^- and π^+



intercept of fitted line

$$ED = A(E) + B * TL$$

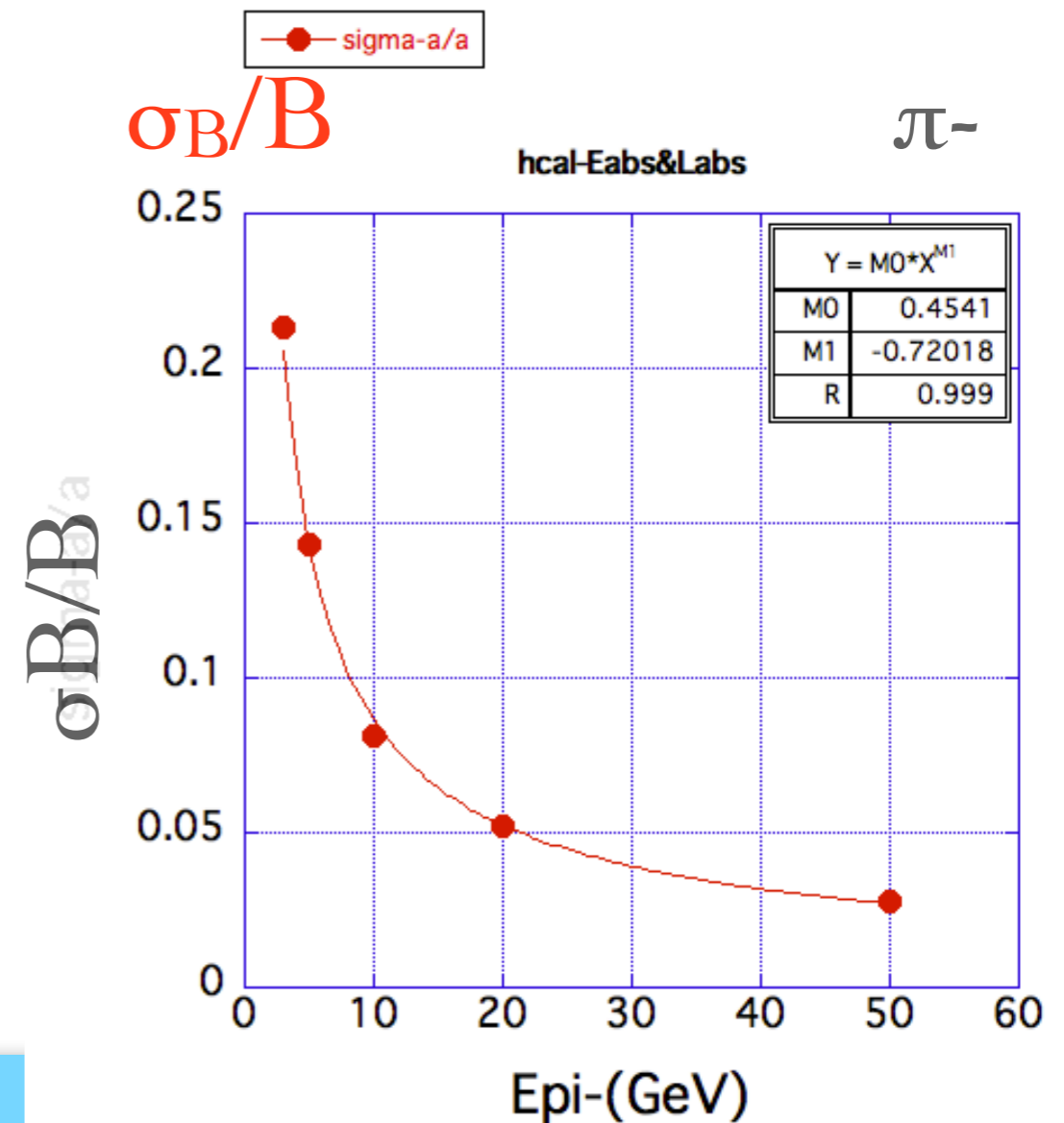
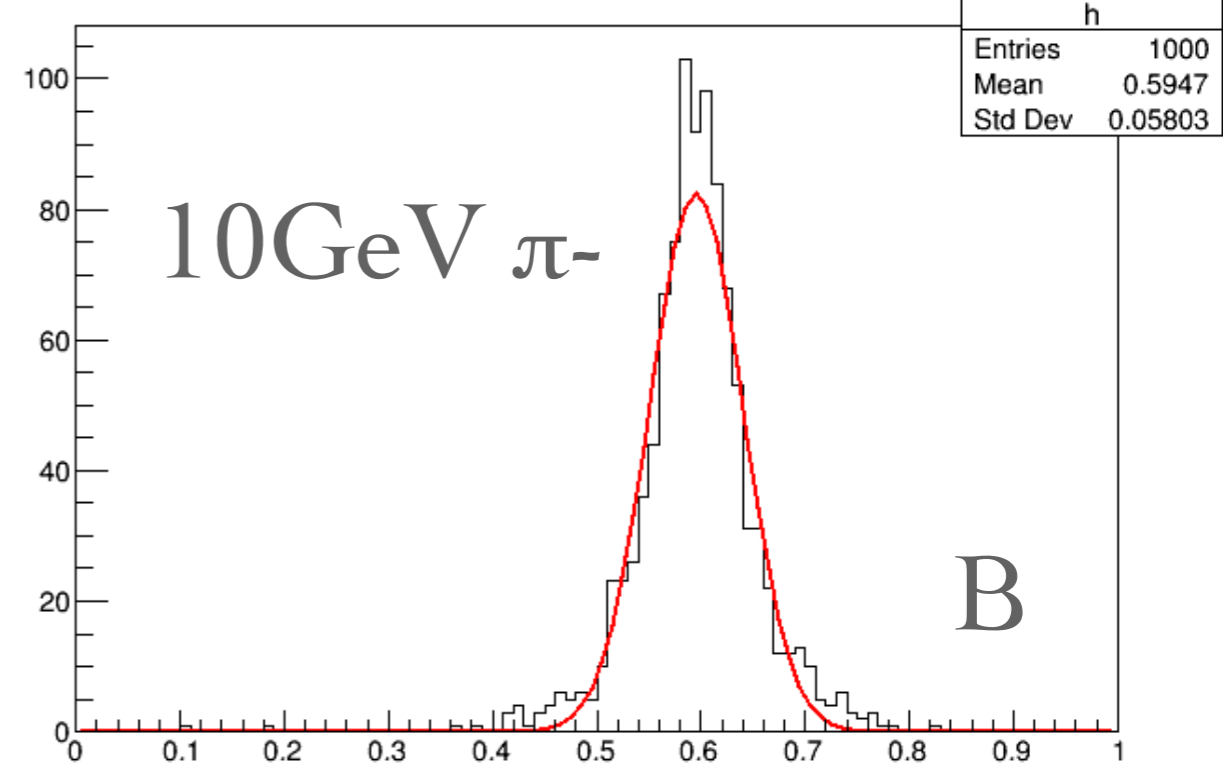
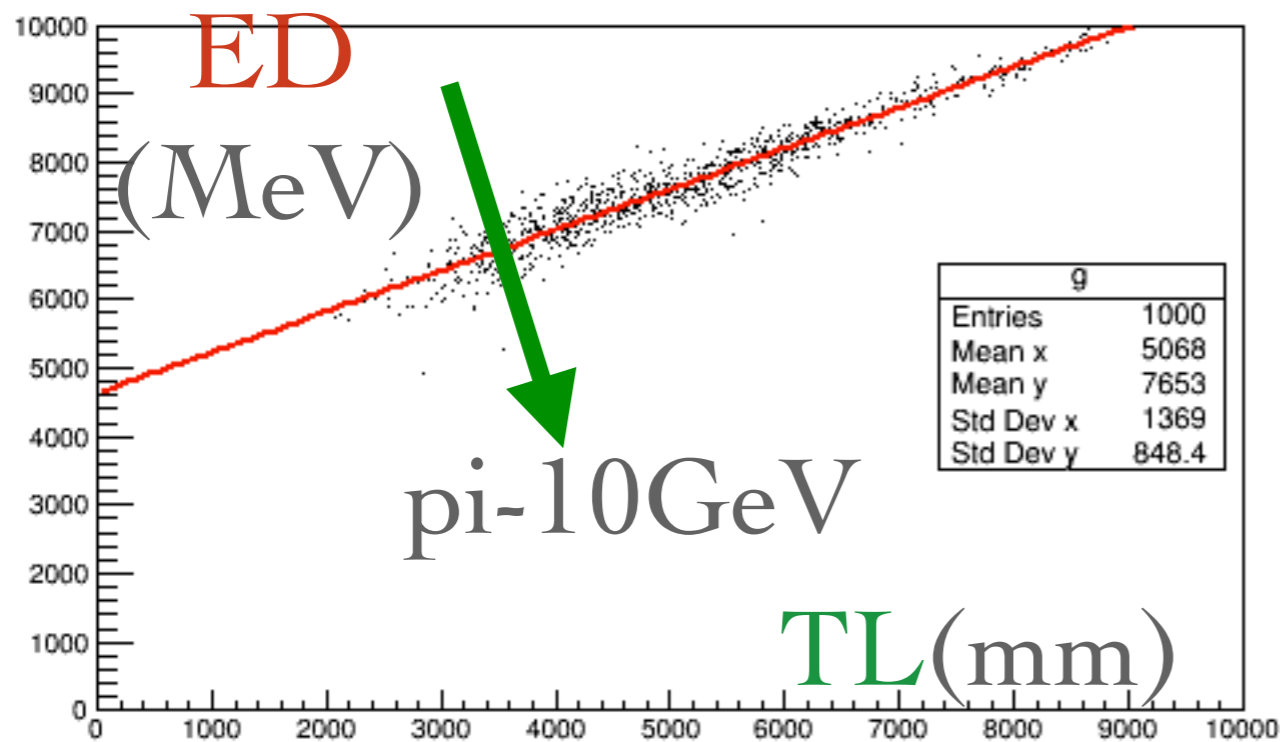
- intercept (cut) $A(E)$ is
- linear with injected energies
- same to π^- and π^+
- good **linearity**



Resolution

$$ED = A(E) + B * TL$$

- $B = (ED - A(E)) / TL$
- B is independent on E
- resolution of the calorimeter $\sim \sigma_B / B$



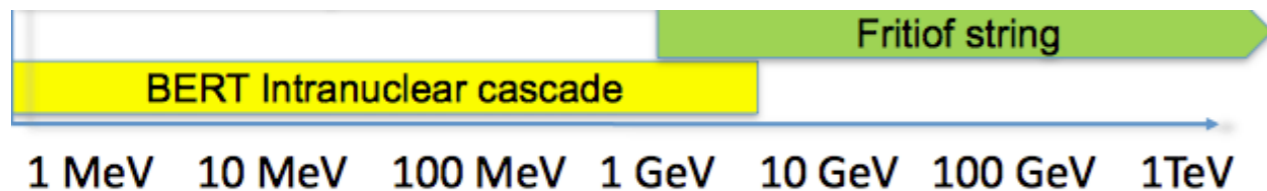
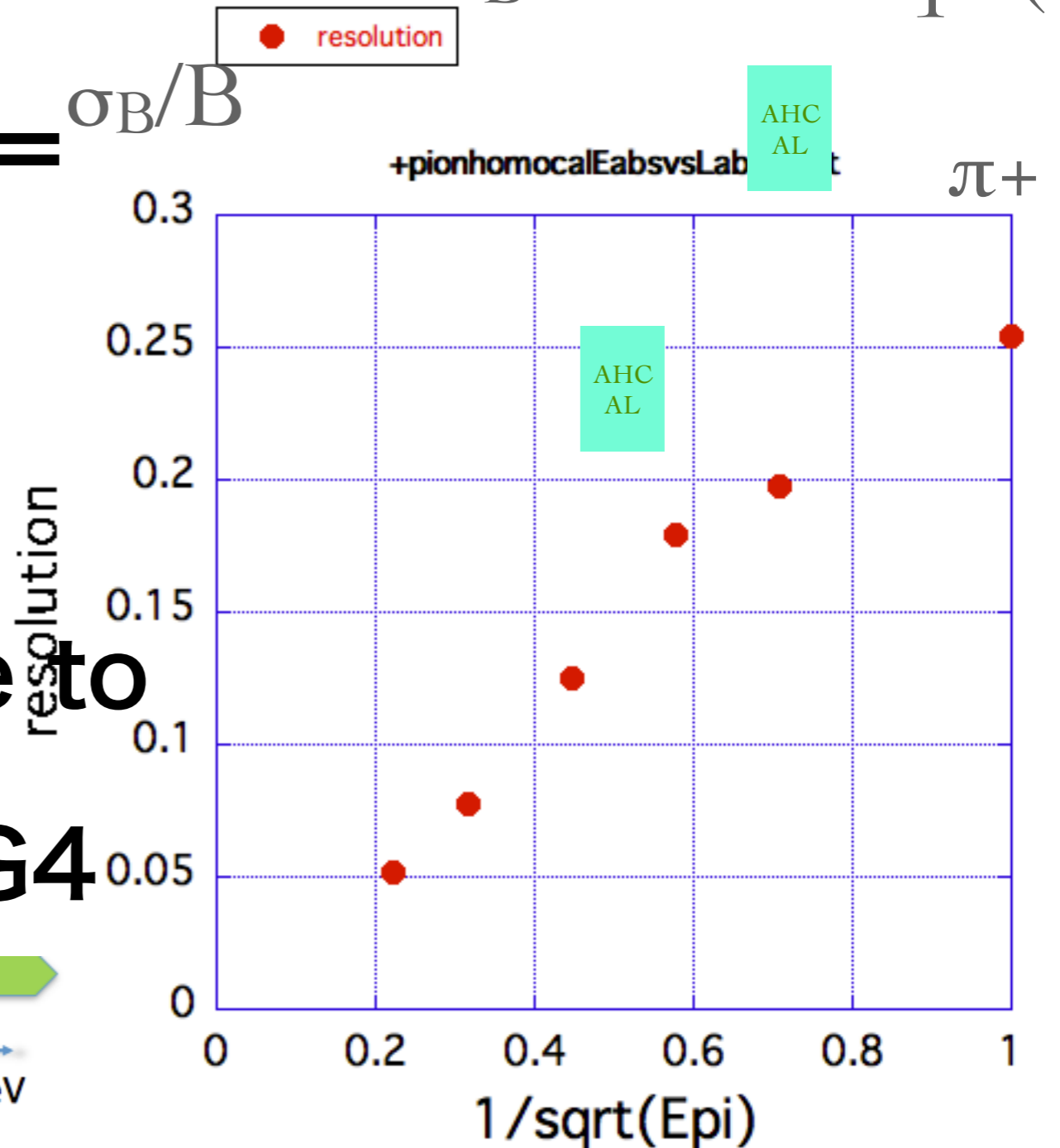
Energy resolution

AHC
AL

$$E_{abs} = A(E) + B * L_{abs}$$

$$\sigma_B/B \sim 25\% / \sqrt{E}$$

- energy resolution = σ_B/B
- “ σ_B/B ” scales in $1/\sqrt{E(\text{GeV})}$
- kink at $\sim 5\text{GeV}$ due to
- Hadron model in G4



50, 20, 10, 5, 3, 1 GeV

EM response

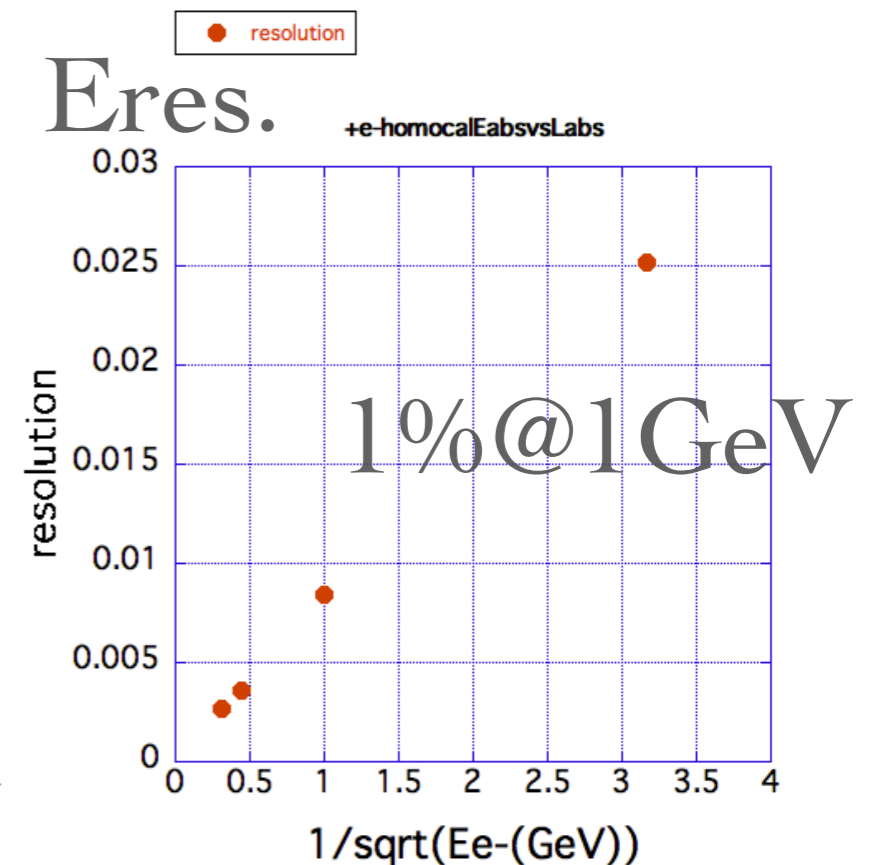
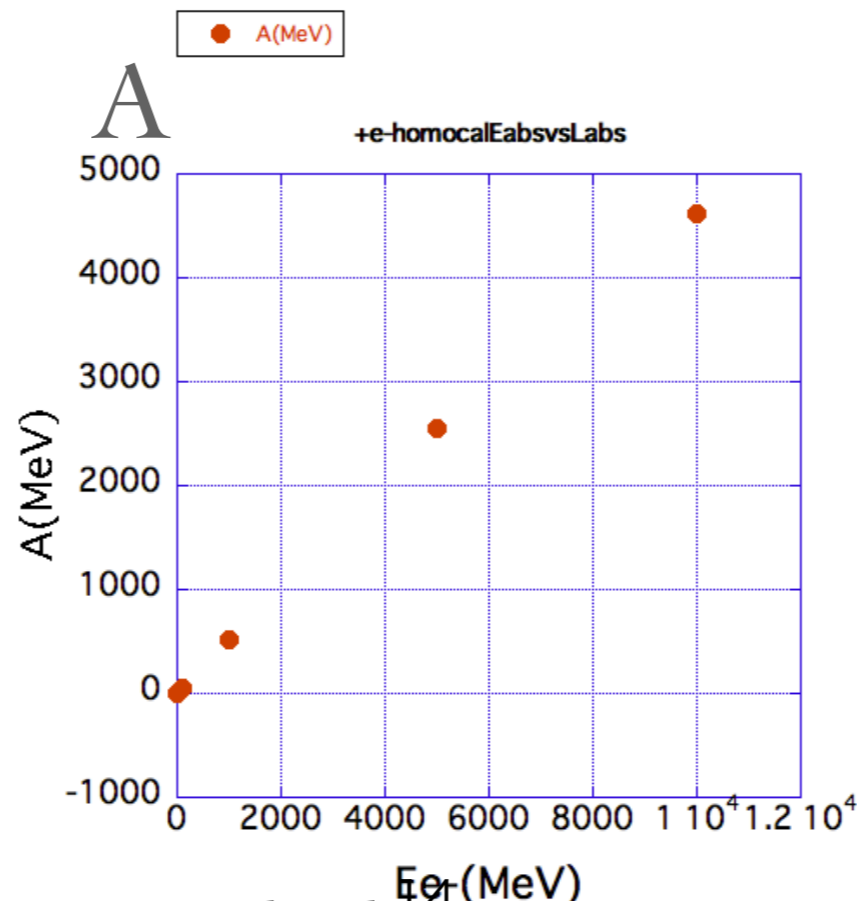
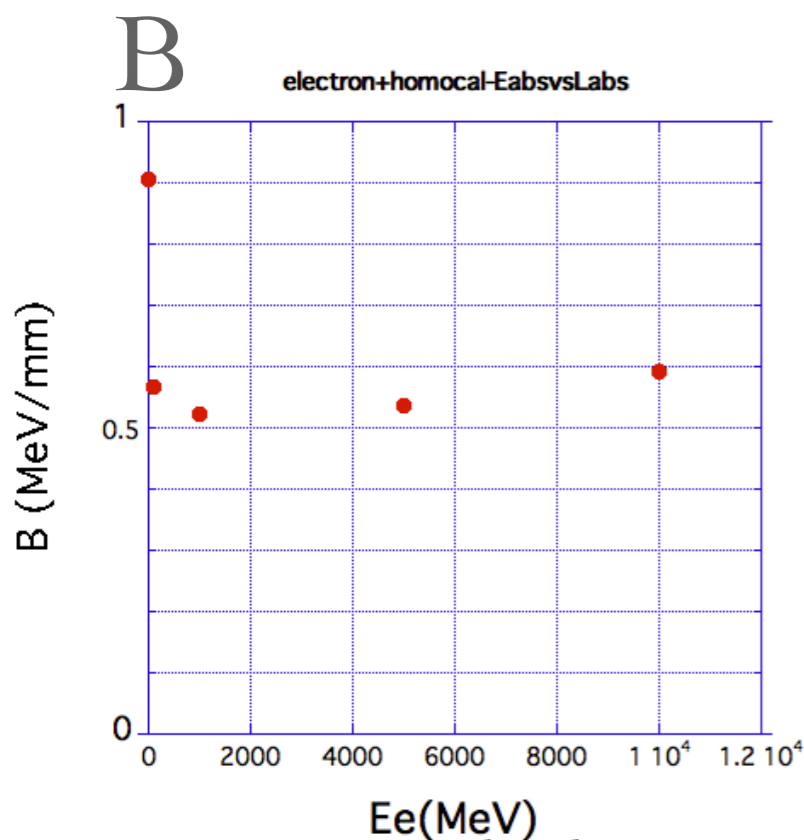
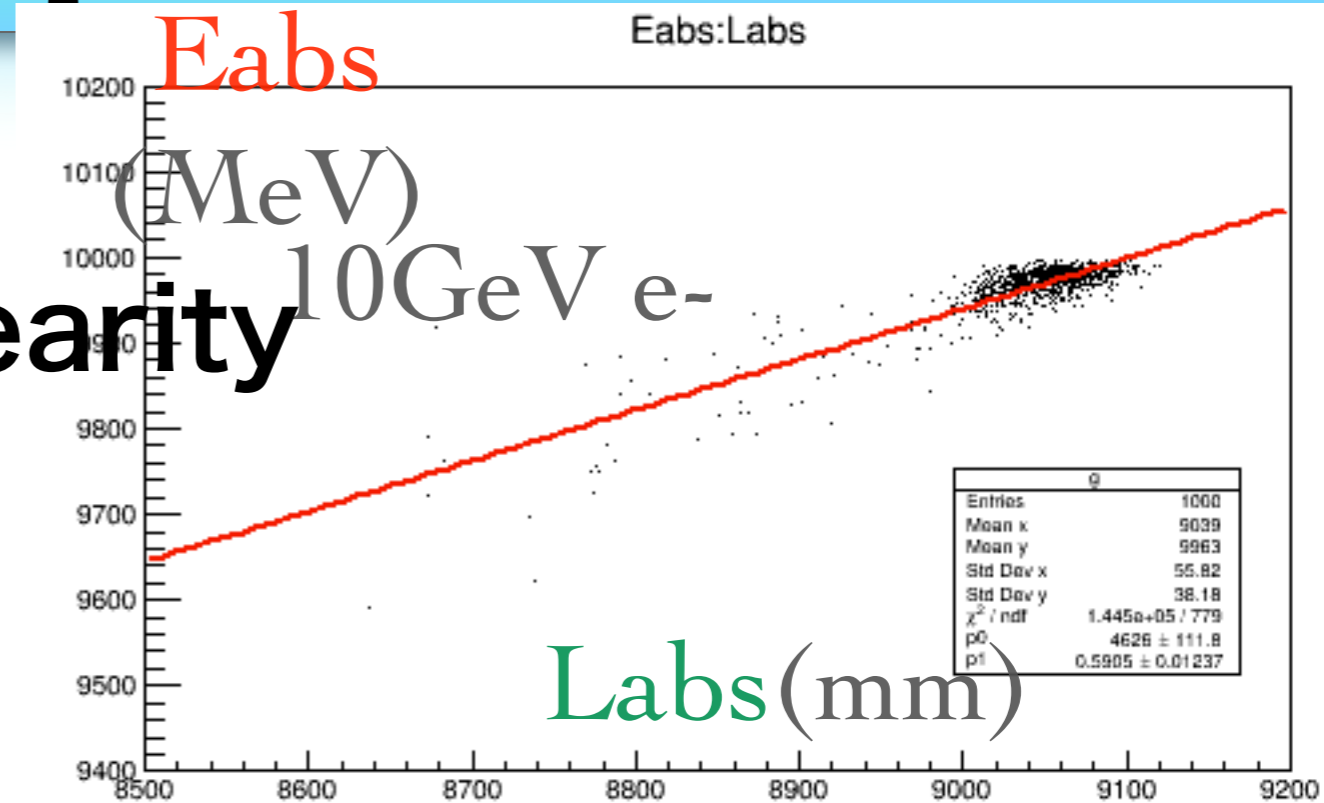
$$E_{abs} = A(E) + B \cdot L_{abs}$$

- E_{abs} vs L_{abs} :

- $A(E)$ shows good linearity

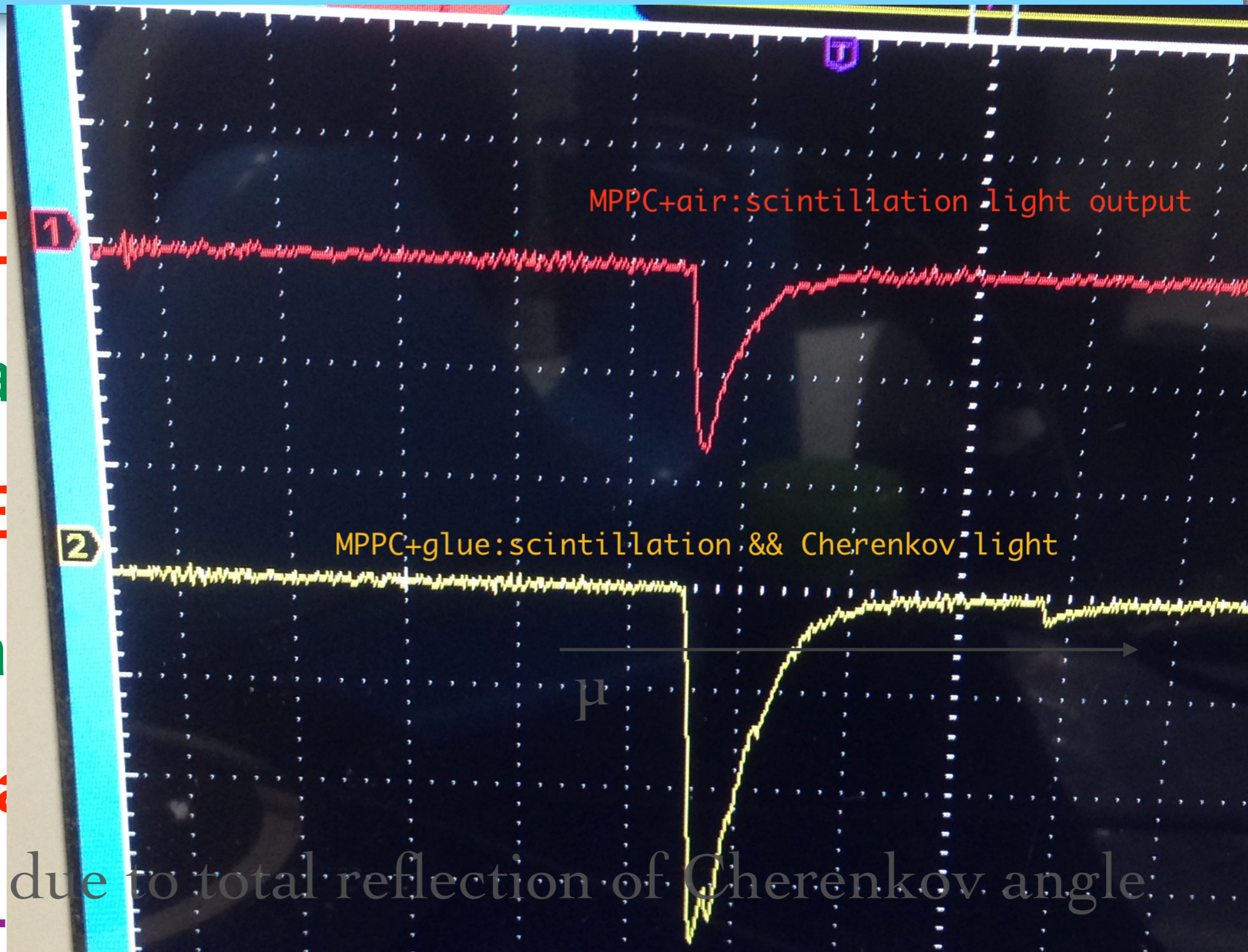
- B is const. at $E > 100 \text{ MeV}$

- B is same as $\sim \pi^+ -$



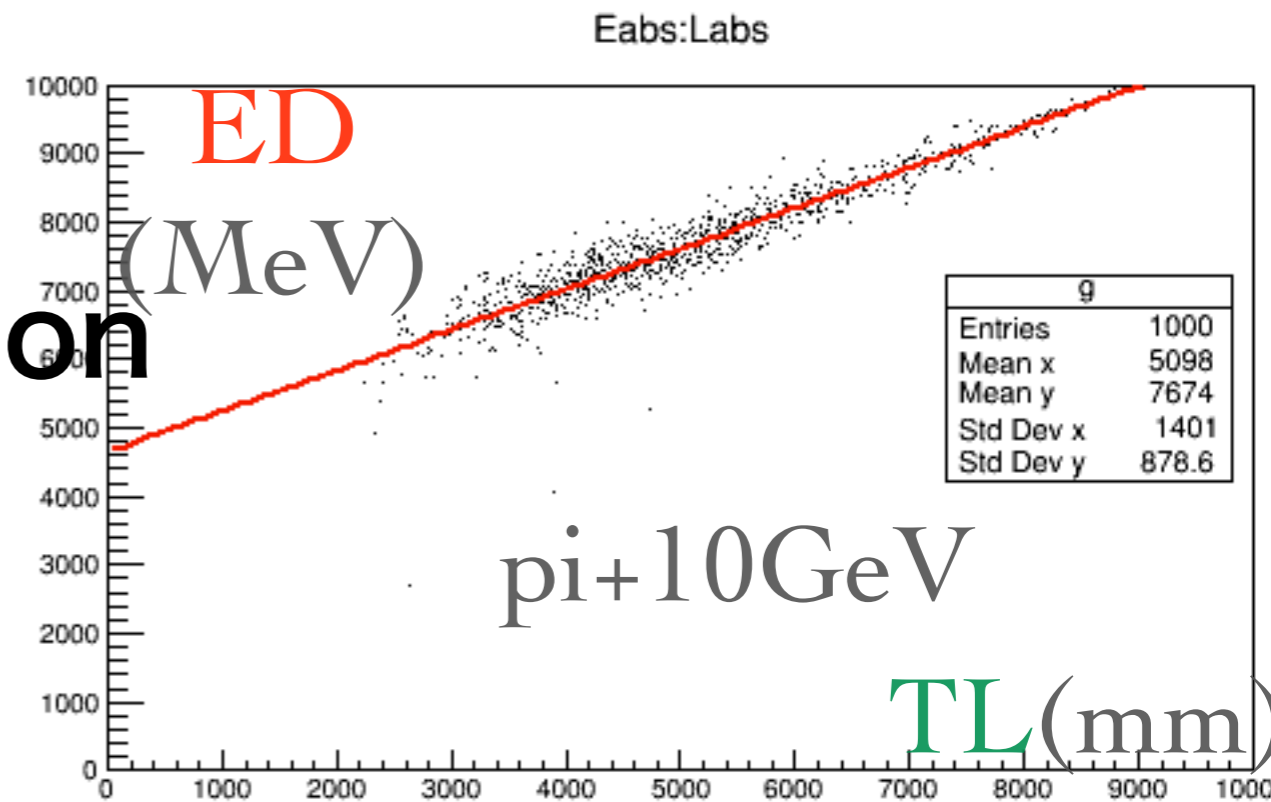
how to measure

- energy
- from ED
- use heat
- $ED \sim dE$
- $TL \sim Ch$
- MPPC+air
- MPPC+



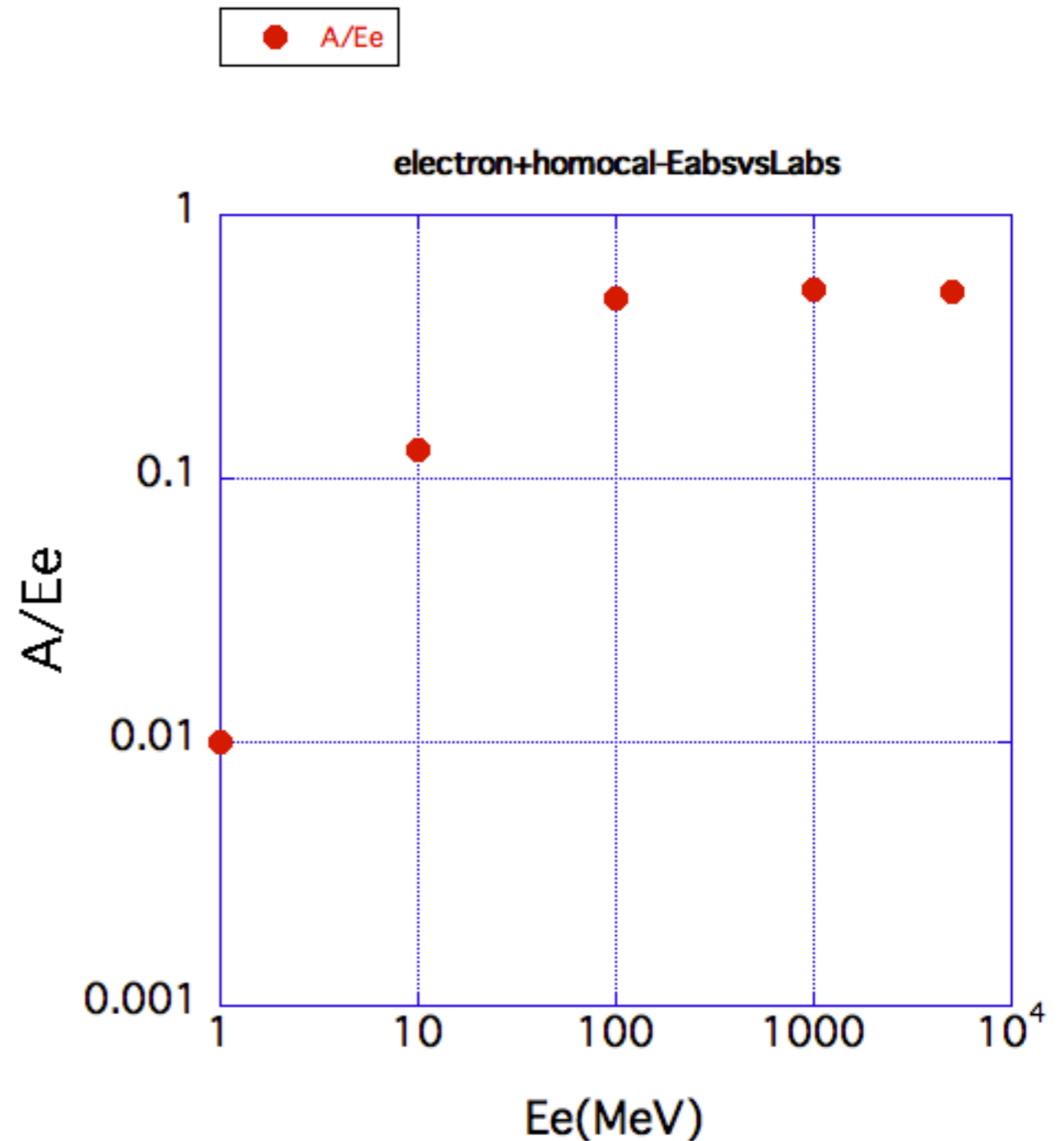
summary and outlook

- homogeneous calorimeter is simulated
- found a linear **relation between ED and TL**
- super energy resolution
- ED ~ scintillation light
- TL ~ Cherenkov light
- test calorimeter with PbWO₄



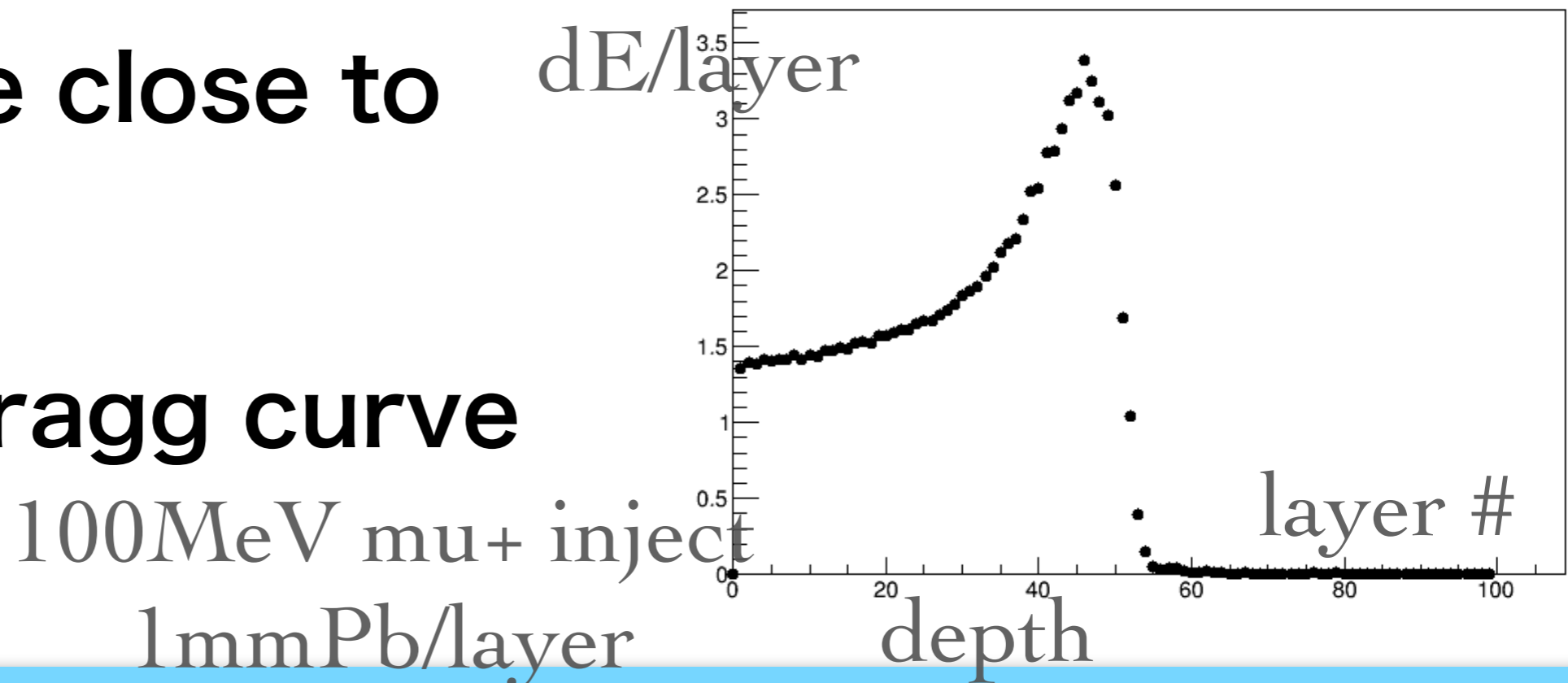
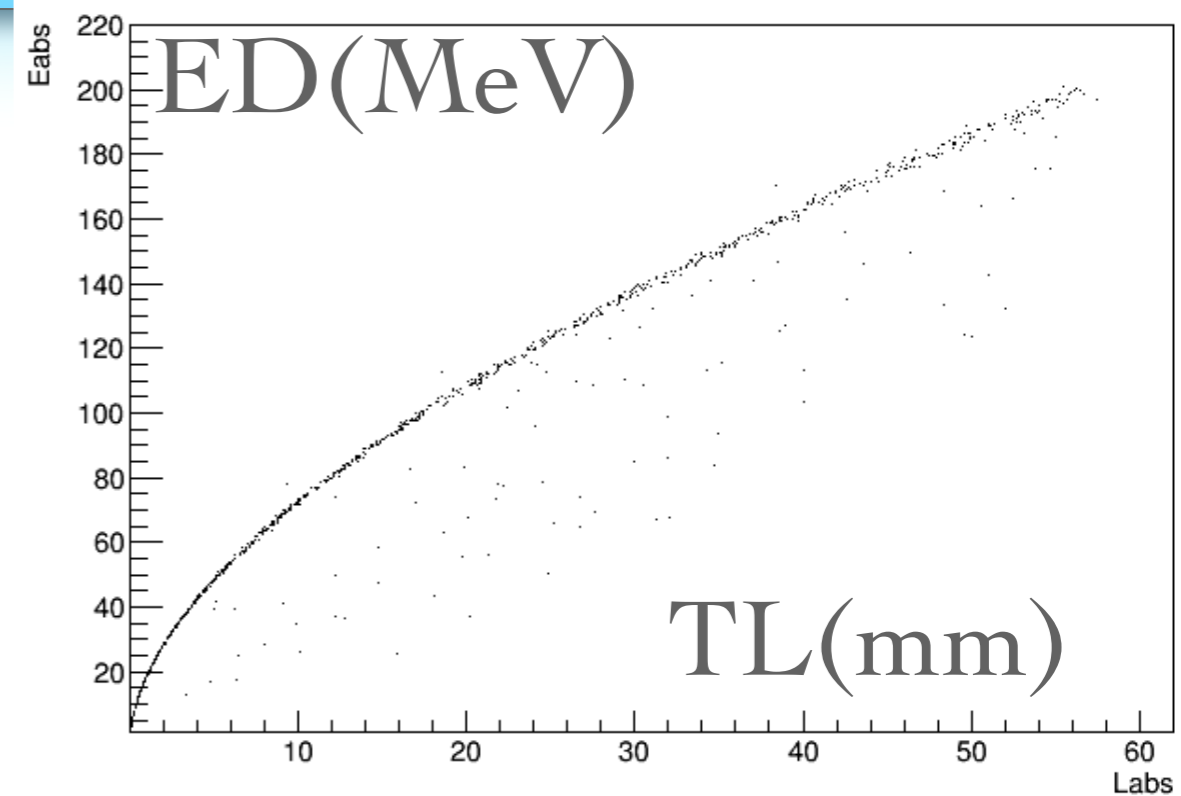
discussion

- electron cases are tested
- $A/E_e \sim \text{const.}$ at $E_e > 100 \text{ MeV}$ where EM shower dominates
- at lower E_e , close to zero



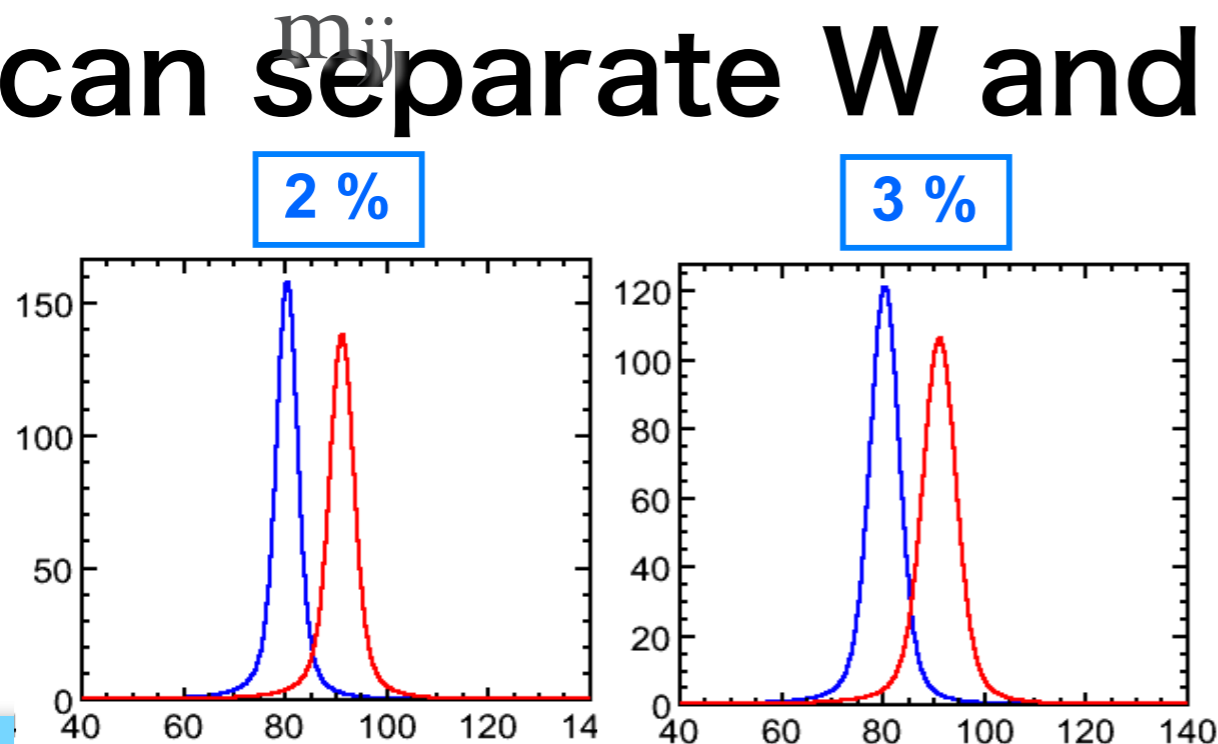
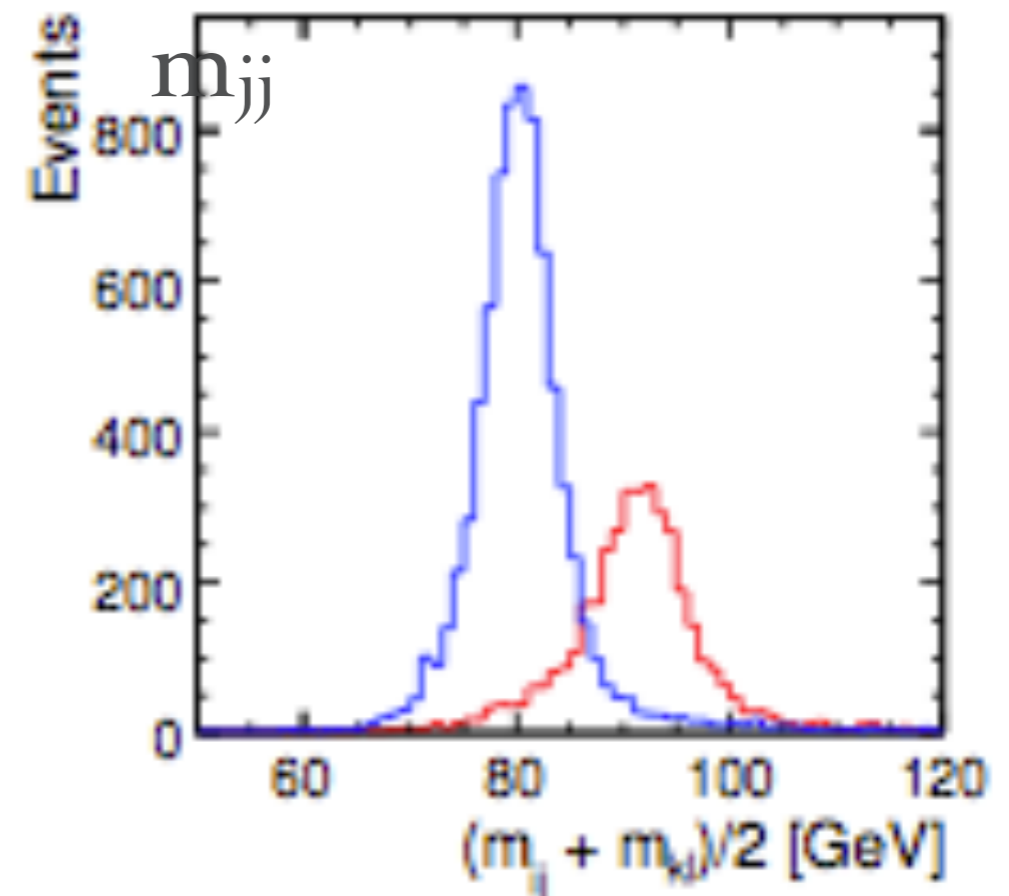
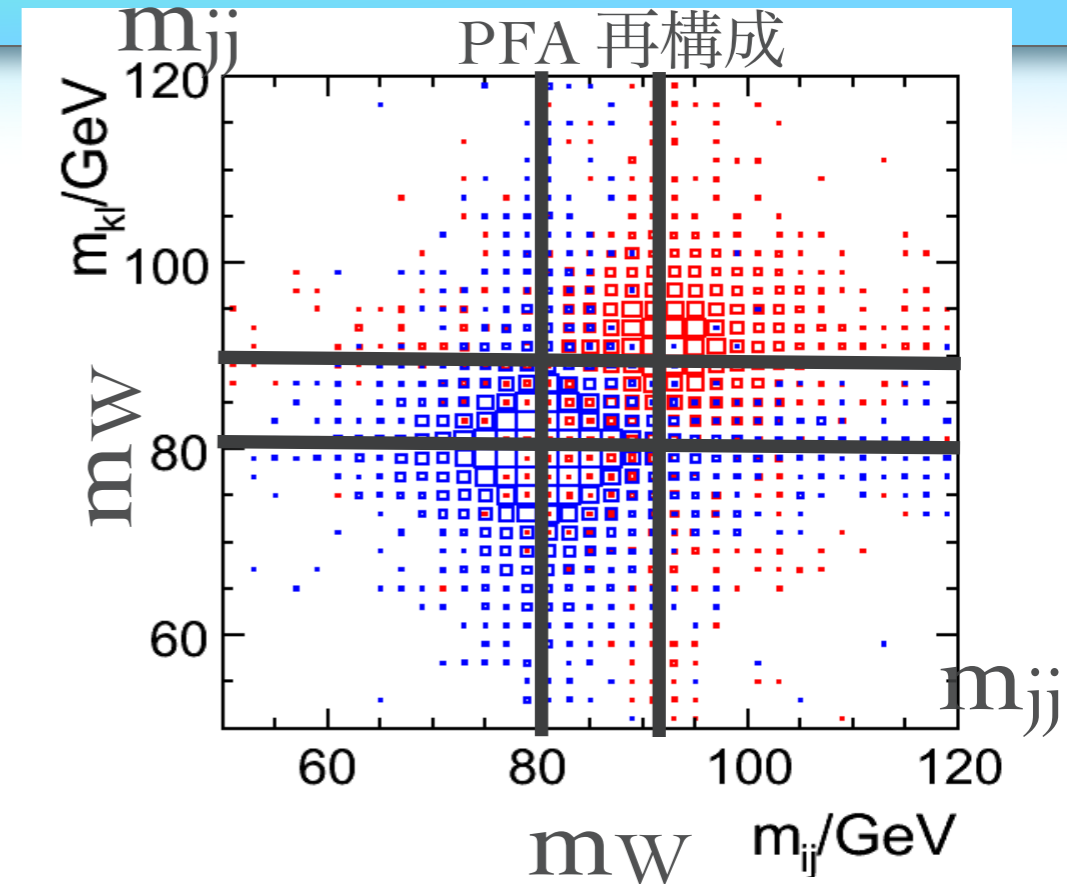
discussion

- reason of intercept
- muon+ : $< 200\text{MeV}$
uniform injection
- **non-linear**
response close to $0=ED$
- due to Bragg curve



PFA performance

- PFA utilises
- tracker for charged
- ECAL for photons
- HCAL for KoL
- can separate W and Z



track length vs

for electrons

Ncherenkov light

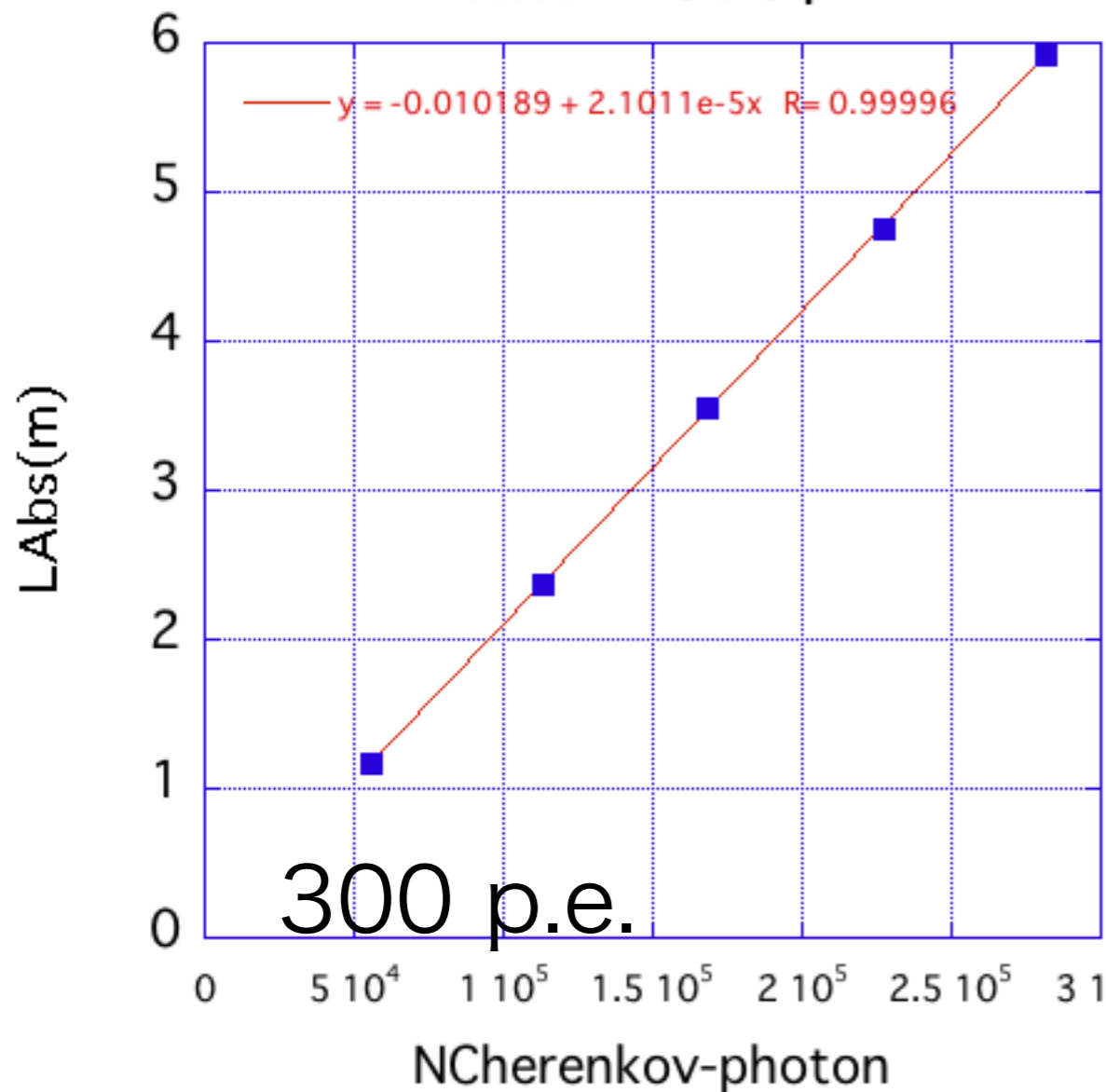
- nice correlation : we can use track length instead of number of cherenkov light which consume CPU power for simulation

—■— LAbs

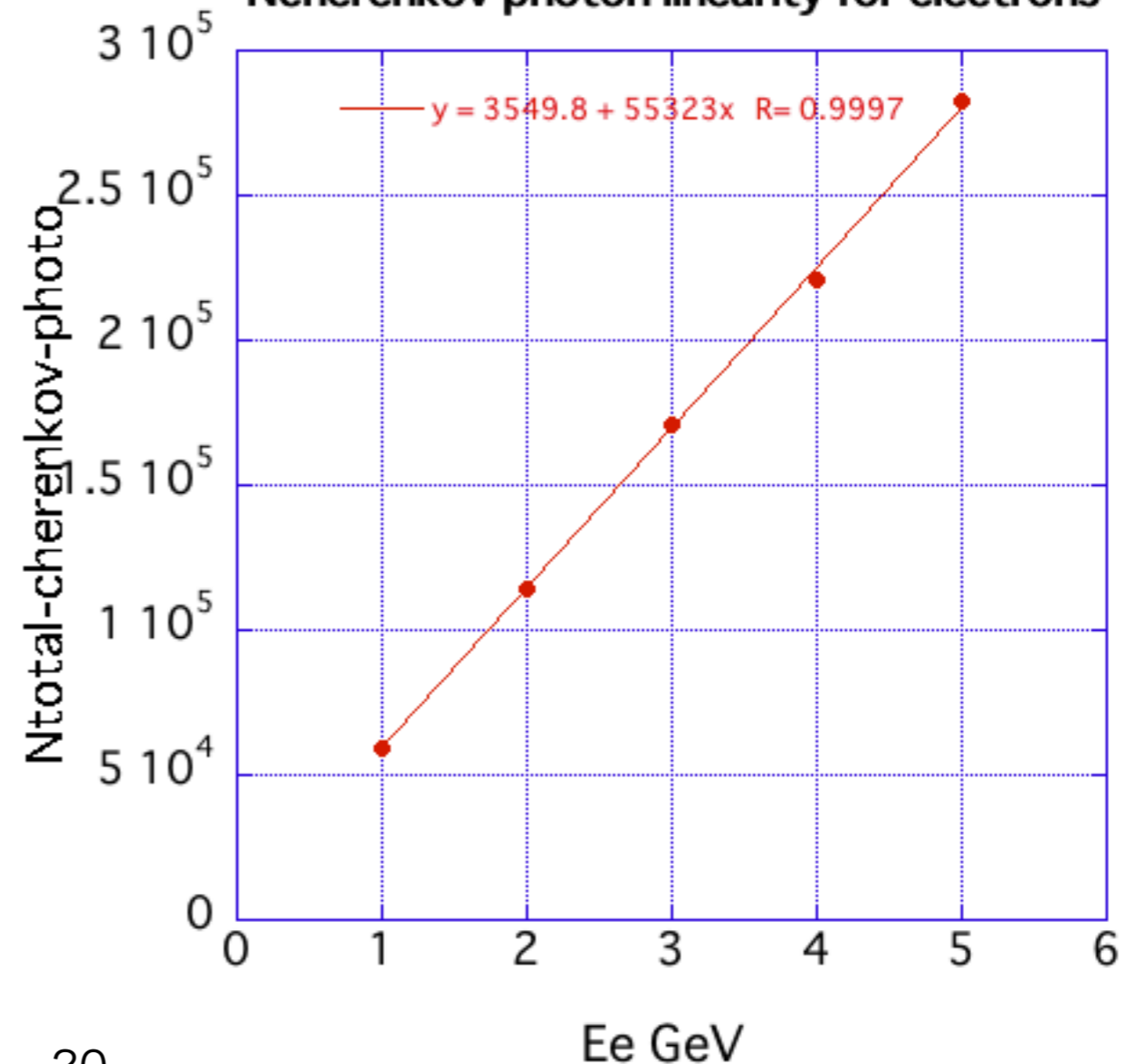
—●— Ntotal-cherenkov-photo

track length

electron-LABSvsNCHph

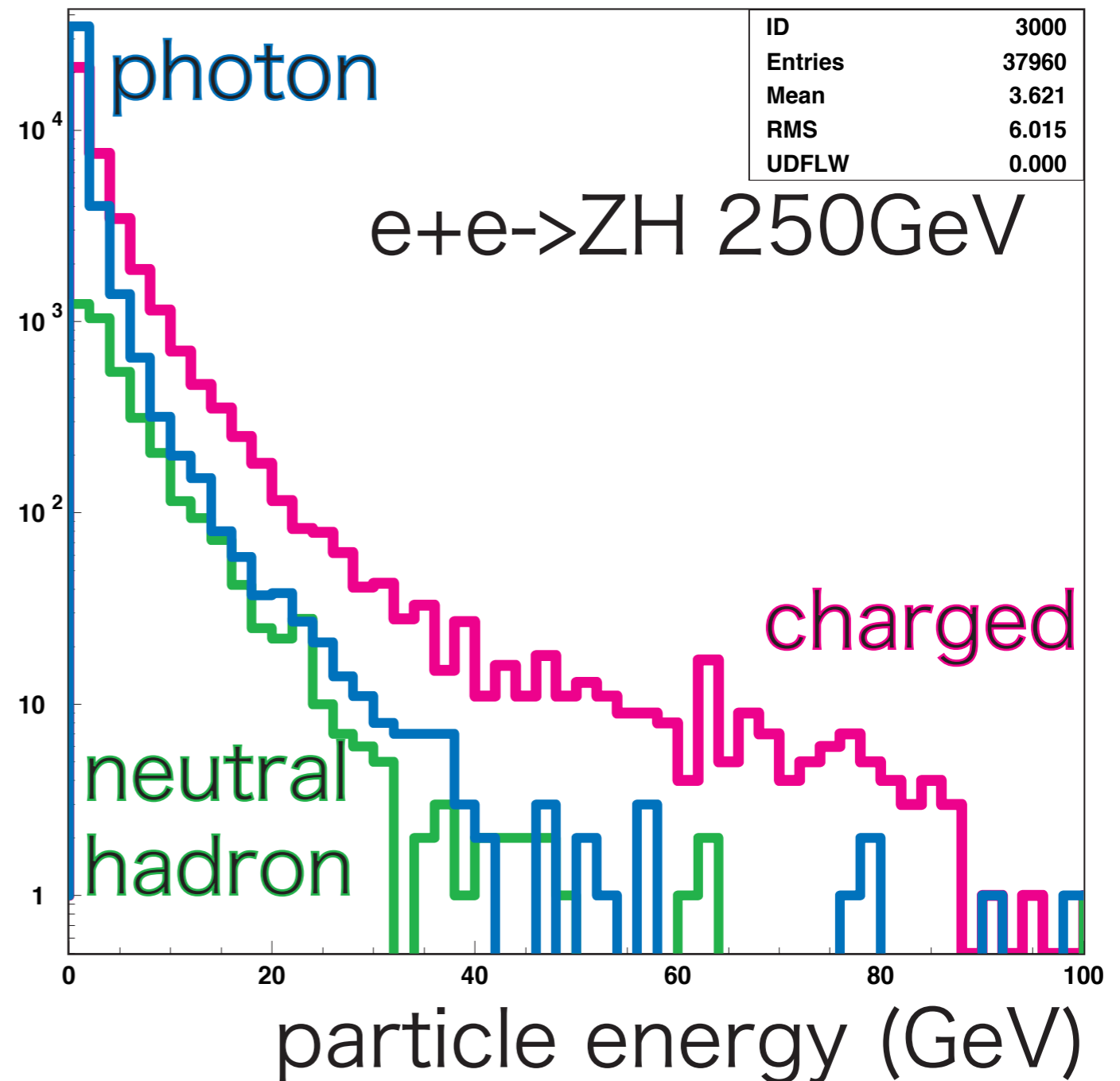


Ncherenkov photon linearity for electrons



particle energy in jet

- particle energy distribution
- $E < 10$ GeV dominating



PbWO₄



Scintillation properties of lead tungstate (PbWO₄) crystals:

Density (g.cm ⁻³)	8.28
Radiation length (cm)	0.92
Decay constant (ns)	6/30
Emission peak (nm)	440/530
Light yield (% that of NaI:TI)	0.5
Melting point (°C)	1123
Hardness (Mho)	/
refractive Index	2.16
Hygroscopicity	none
Cleavage	101