

# Higgs boson self-coupling as a probe of the sphaleron property

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S. Kanemura, M Tanaka: PLB 809 135711 (2020)

ILC camp 2020/9/23 (Online)

# Introduction

Standard model(SM) consistent with the collider experiments

## The problem in Higgs sector

- The structure of the Higgs potential
- The dynamics of the spontaneous electroweak symmetry breaking

## Phenomena beyond the SM(BSM)

- Baryon Asymmetry of the Universe
- Dark Matter
- Tiny mass of neutrino

The extension of the Higgs sector  $\leftrightarrow$  New Physics

# Baryon asymmetry of the Universe

[PDG 2019]

$$\frac{n_b - n_{\bar{b}}}{n_\gamma} = (5.8 - 6.6) \times 10^{-10}$$

Sakharov's conditions:

[Sakharov 1967]

- ① Baryon violation
- ② C, CP violation
- ③ Departure from thermal equilibrium

Electroweak baryogenesis,  
Leptogenesis,  
GUT baryogenesis,  
etc...

We focus on the scenario of the electroweak baryogenesis

Electroweak baryogenesis:

[Kuzmin, et al. : PLB155 (1985)]

- ① Sphaleron process
- ② The effects on the new physics ← Electric dipole moment
- ③ 1st Order Phase Transition(1stOPT) ← hhh coupling, GW spectrum

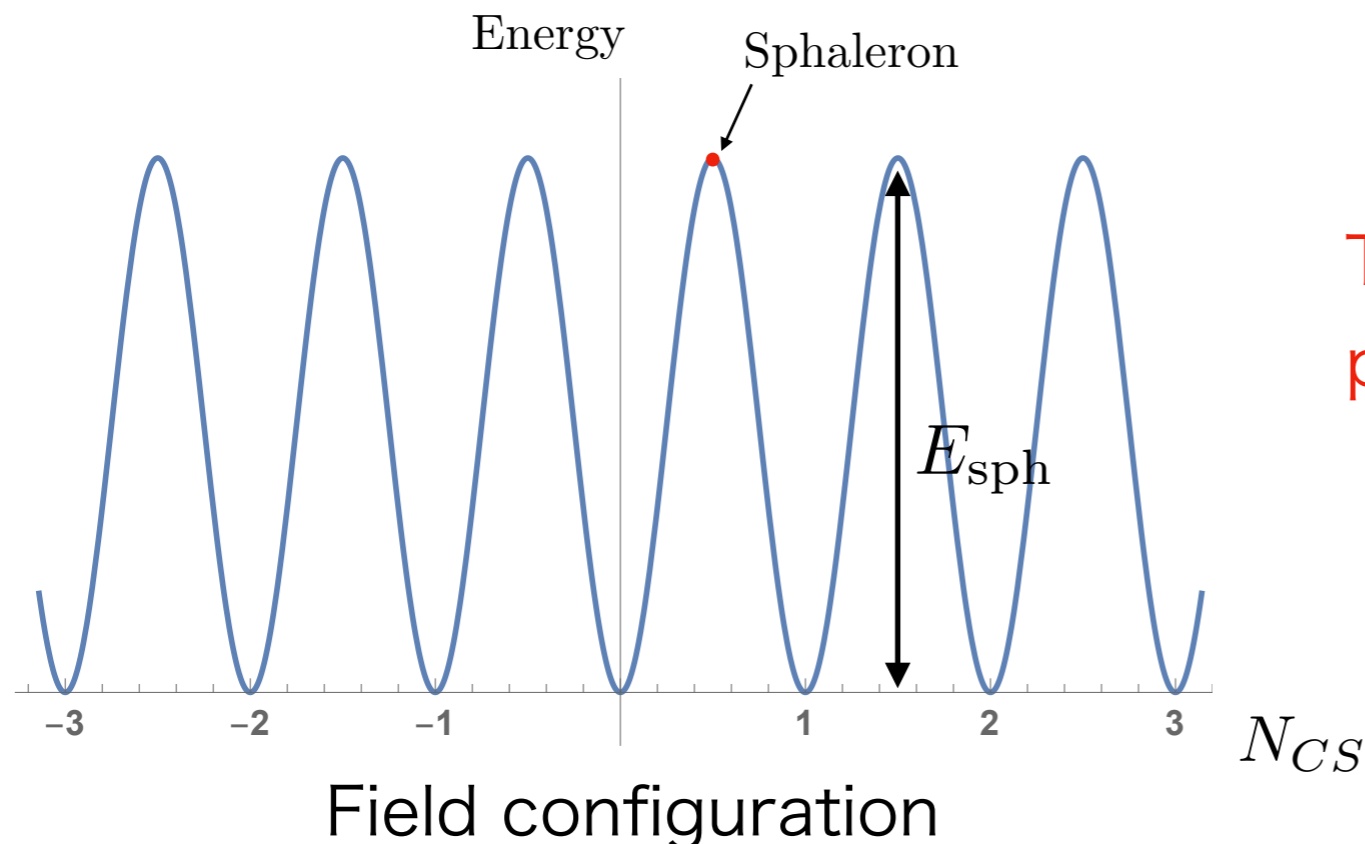
Can we determine the sphaleron property by experiments ?

# Sphaleron

Sphaleron “ready to fall”

[Klinkhamer, Manton: PRD.30 (1984)]

- Non-perturbative solution in field equations (static and unstable)
- Saddle point field configuration
- B+L violation process: sphaleron process



$$\Delta(B + L) = 6\Delta N_{CS}$$

The process is important to produce the baryon asymmetry.

# Sphaleron in the SM

- Energy functional ( $g' = 0$ )

[Manton: PRD28 (1983)]

$$E[W_i^a, \Phi] = \int d^3x \left[ \frac{1}{4g^2} W_{ij}^a W_{ij}^a + (D_i \Phi)^\dagger D_i \Phi + V(\Phi) \right] \quad V^{\text{SM}}(\Phi) = \frac{m_h^2}{2v^2} \left( \Phi^\dagger \Phi - \frac{v^2}{2} \right)^2$$

[Akiba et al. : PRD38 (1988)]

[Spanowsky, Tamarit : PRD95 (2017)]

- Ansatz

$$W_i^a(\vec{r}) = m_W \left[ \epsilon_{aij} n_j \frac{1 - R(r) \cos \theta(r)}{r} + (\delta_{ai} - n_a n_i) \frac{R(r) \sin \theta(r)}{r} \right], \quad n_a = x^a / r$$

$$\Phi(\vec{r}) = \frac{v}{\sqrt{2}} S(r) e^{i n_a \sigma^a \phi(r)} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

[Kanemura, Tanaka: PLB 809 (2020)]

From a symmetry,

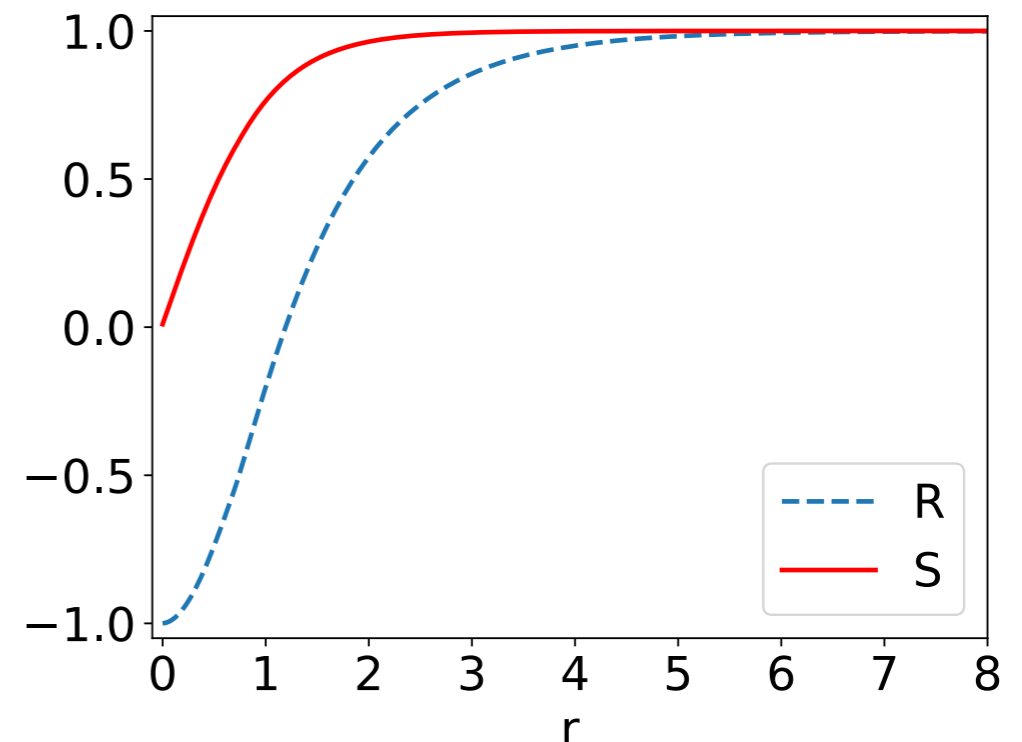
$$\theta = \pi, \quad \phi = \frac{\pi}{2}$$

- Field equation

$$r^2 R'' - R^3 + R(1 - r^2 S^2) + r^2 S^2 = 0$$

$$S'' + \frac{2}{r} S' - \frac{1}{2r^2} S(1 - R)^2 - \frac{4}{g^2 v^4} \frac{\partial V(S)}{\partial S} = 0$$

$$E_{\text{sph}}^{\text{SM}} = 9.08 \text{ TeV}$$



Gauge field: R, Higgs field: S

# Triple Higgs coupling and sphaleron

- Triple Higgs coupling

$$\left. \frac{\partial^3 V(h)}{\partial h^3} \right|_{h=0} = \lambda_{hhh}^{\text{SM}} \left( 1 + \frac{\Delta\lambda_{hhh}^{\text{new}}}{\lambda_{hhh}^{\text{SM}}} \right) \quad \lambda_{hhh}^{\text{SM}} = \frac{3m_h^2}{v} \quad \Delta\lambda_{hhh}^{\text{new}} = \lambda_{hhh}^{\text{new}} - \lambda_{hhh}^{\text{SM}}$$

Eg) 2HDM [Kanemura et al.: PRD 70 (2004)]

$$\frac{\Delta\lambda_{hhh}^{\text{2HDM}}}{\lambda_{hhh}^{\text{SM}}} \simeq \frac{m_\Phi^4}{12\pi^2 m_h^2 v^2} \left( 1 - \frac{M^2}{m_\Phi^2} \right)^3 \xrightarrow{M \rightarrow 0} \frac{m_\Phi^4}{12\pi^2 m_h^2 v^2} \quad \text{Non-Decoupling}$$

$m_\Phi^2 \simeq M^2 + \lambda_\Phi v^2$

[Kanemura et al.: PLB606 (2005)]

The strong 1stOPT demands  $\Delta\lambda_{hhh}/\lambda_{hhh} > O(10)\%$  in 2HDM

- Sphaleron energy  $\leftrightarrow$  Higgs potential  $\leftrightarrow$  hhh coupling

$$\Rightarrow \Delta E_{\text{sph}}^{\text{new}} \simeq -A^{\text{new}} \frac{\Delta\lambda_{hhh}^{\text{new}}}{\lambda_{hhh}^{\text{SM}}}$$

$$E_{\text{sph}}^{\text{new}} = E_{\text{sph}}^{\text{SM}} + \Delta E_{\text{sph}}^{\text{new}}$$

$A^{\text{new}}$  can be determined theoretically

[Kanemura, Tanaka: PLB 809 (2020)]

Today's theme

hhh coupling  $\rightarrow$  Sphaleron energy at the early Universe

# Sphaleron at the early Universe

- SMEFT added a dim. 6 operator to Higgs potential

[Grojean et al.: PRD71 (2005)]

[Zhou et al.: PRD101 (2020)]

- SM with additional N singlet scalars model

$$V_0(\Phi, \vec{S}) = -\mu^2 \Phi^\dagger \Phi + \lambda(\Phi^\dagger \Phi)^2 + \frac{\mu_S^2}{2} |\vec{S}|^2 + \frac{\lambda_S}{4} |\vec{S}|^4 + \lambda_{\Phi S} \Phi^\dagger \Phi |\vec{S}|^2$$

$$\vec{S} = (S_1, S_2, \dots, S_N)$$

$$\mu_S^2 > 0$$

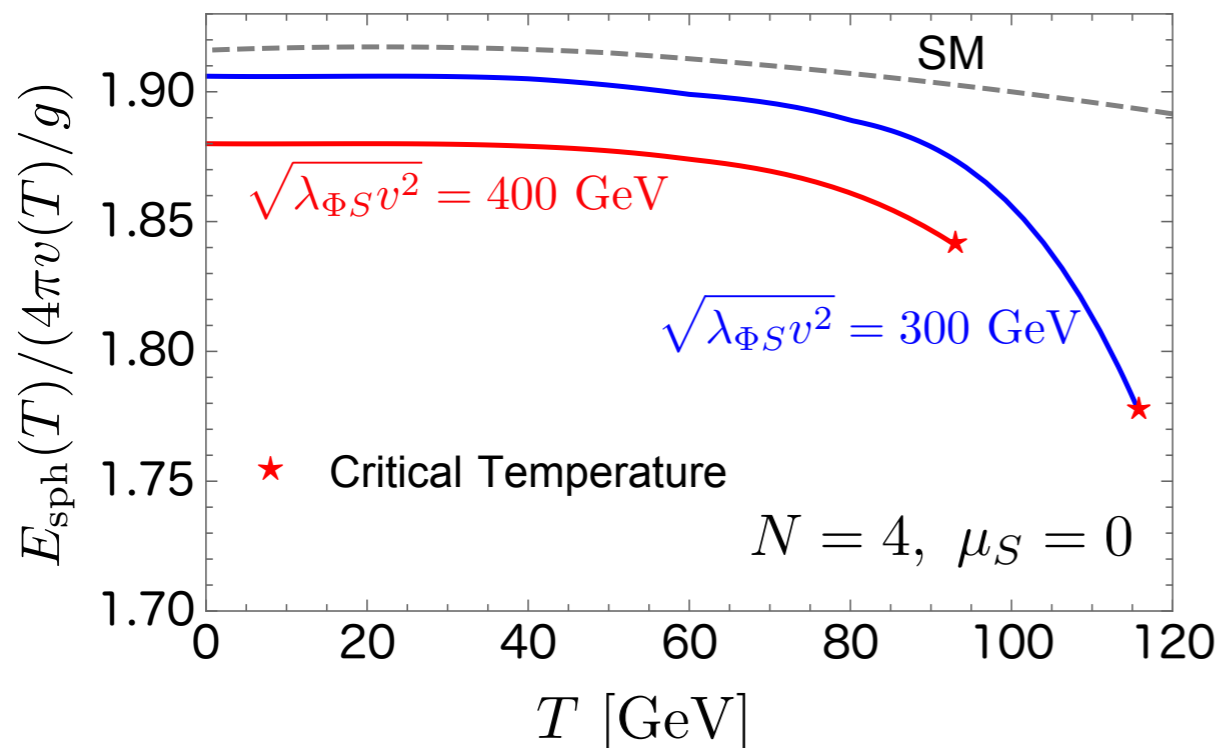
$$M_S(v)^2 = \mu_S^2 + \lambda_{\Phi S} v^2$$

The effective potential

$$V_{\text{eff}}(\Phi, T) = V_0(\Phi) + \underbrace{V_1(\Phi)}_{\text{1loop at } T=0} + \underbrace{V_T(\Phi, T)}_{\text{1loop at } T \neq 0} + \underbrace{\Delta V_T(\Phi, T)}_{\text{Daisy resummation}}$$

1loop at T=0    1loop at T≠0    Daisy resummation

[Kanemura, Tanaka: Preliminary]



$$\Delta E_{\text{sph}}^{\text{new}} \simeq -A^{\text{new}} \frac{\Delta \lambda_{hhh}^{\text{new}}}{\lambda_{hhh}^{\text{SM}}}$$

$$\Delta \lambda_{hhh}^{\text{new}} \leftrightarrow \Delta E_{\text{sph}}^{\text{new}}(T=0) \leftrightarrow \Delta E_{\text{sph}}^{\text{new}}(T=T_C)$$

We can determine the sphaleron energy at the early Universe via the measurements of future colliders

# Sphaleron decoupling condition

- Departure from thermal equilibrium [Kuzmin, et al. : PLB155 (1985)]

$$\Gamma_{\text{sph}}(T_C) < H(T_C) \Rightarrow \boxed{\frac{v_C}{T_C} > \zeta_{\text{sph}}(T_C) \text{ or } \frac{E_{\text{sph}}(T_C)}{T_C} > B(T_C)} \quad \Gamma_{\text{sph}}(T) = A(T)e^{-E_{\text{sph}}(T)/T}$$

- $\zeta_{\text{sph}}(T_C)$  and  $E_{\text{sph}}(T_C)/T_C$  are determined by measurements of  $\lambda_{hhh}$

$$\boxed{\Delta\lambda_{hhh}^{\text{new}} \Leftrightarrow \Delta E_{\text{sph}}^{\text{new}}(T=0) \Leftrightarrow \Delta E_{\text{sph}}^{\text{new}}(T=T_C)}$$

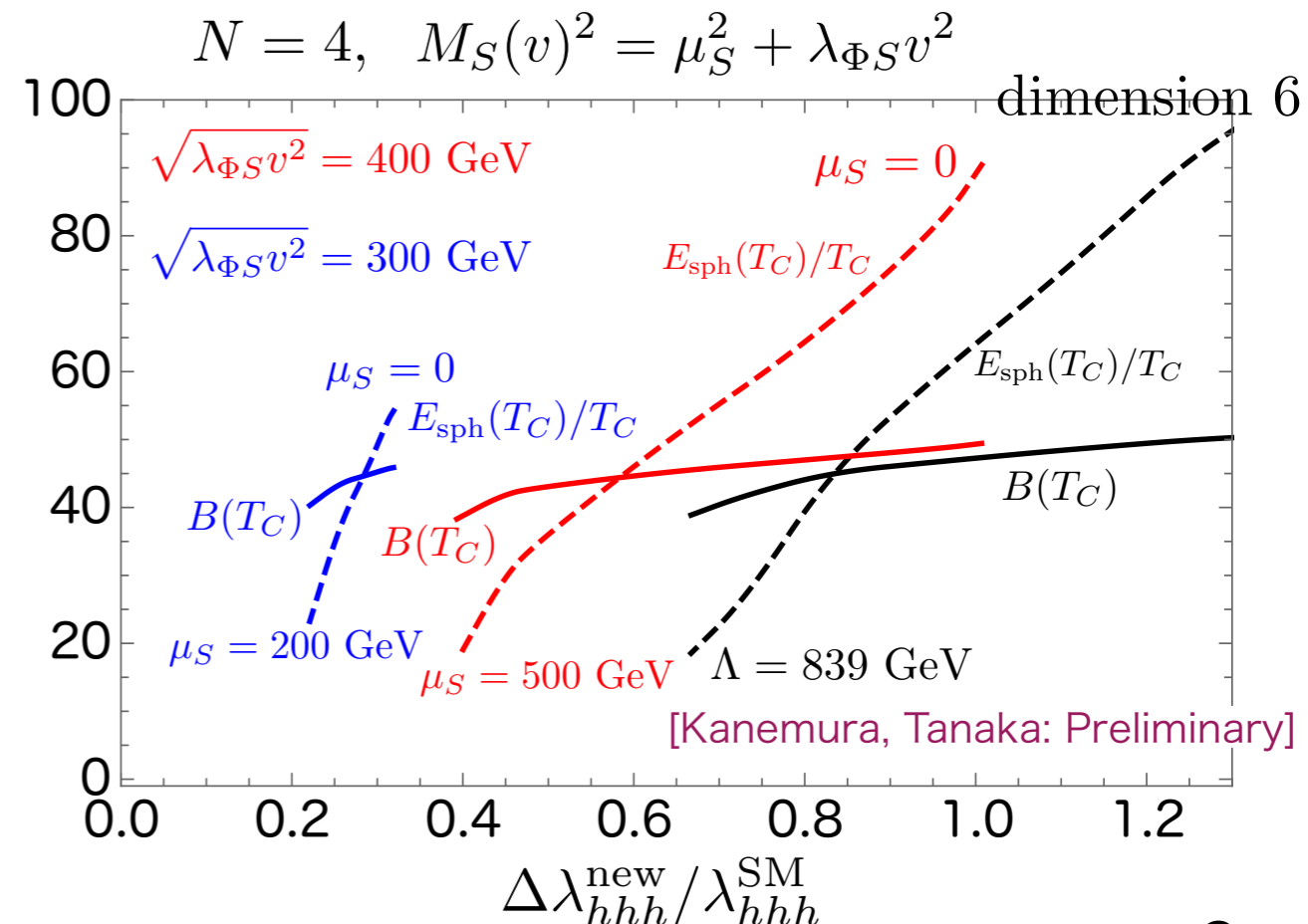
We can verify the validity of the electroweak baryogenesis at ILC

- SM with additional N singlet scalars

$$\Delta\lambda_{hhh}^{\text{Nscalar}} / \lambda_{hhh}^{\text{SM}} > 22\% \text{ (N=4) is needed}$$

← Update of previous work

[Kanemura et al.: PLB606 (2005)]





# Summary

- ① Although the sphaleron is important in explaining the baryon asymmetry, the property of the sphaleron has not been determined by experiments.
- ② Sphaleron and triple Higgs coupling are both associated with Higgs potentials  
→ Sphaleron energy is determined via the measurement of  $\lambda_{hhh}$  at future colliders

$$\Delta E_{\text{sph}}^{\text{new}} \simeq -A^{\text{new}} \frac{\Delta \lambda_{hhh}^{\text{new}}}{\lambda_{hhh}^{\text{SM}}}$$

- ③ Sphaleron energy at the early Universe is determined the measurement of  $\lambda_{hhh}$   
→  $\zeta_{\text{sph}}(T_C)$  and  $E_{\text{sph}}(T_C)/T_C$  are also determined

$$\frac{v_C}{T_C} > \zeta_{\text{sph}}(T_C) \quad \text{or} \quad \frac{E_{\text{sph}}(T_C)}{T_C} > B(T_C)$$

→ We can verify the scenario of the electroweak baryogenesis

- ④ In order to realize the strong 1stOPT,  $\lambda_{hhh}$  should satisfy  $\Delta \lambda_{hhh}^{\text{Nscalar}} / \lambda_{hhh}^{\text{SM}} > 22\%$   
in the model with additional four scalar singlets(i.e. 2HDM)

**Back Up**

# 次元6演算子を加えた有効場の理論

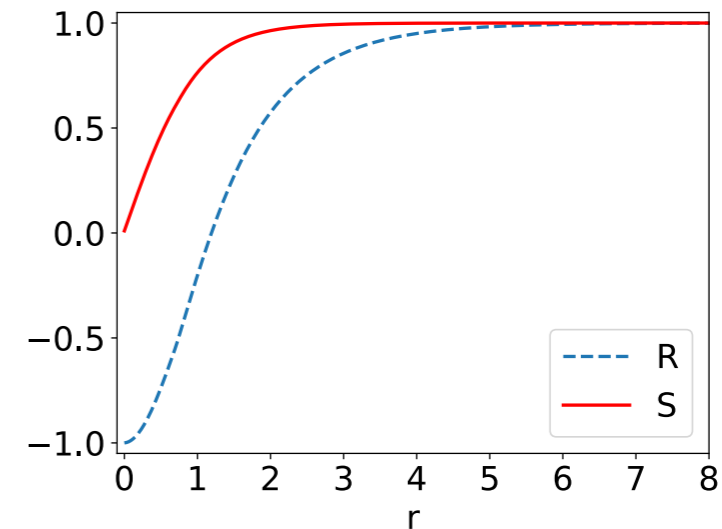
[Grojean et al.: PRD71 (2005)] [Gan et al.: PRD96 (2017)]

- ヒッグスポテンシャル:  $V(\Phi) = \frac{m_h^2}{2v^2} \left( \Phi^\dagger \Phi - \frac{v^2}{2} \right)^2 + \frac{1}{\Lambda^2} \left( \Phi^\dagger \Phi - \frac{v^2}{2} \right)^3$

- スファレロンエネルギー:  $\Delta E_{\text{sph}}^{\text{dim6}} \simeq -\frac{\pi v^2 m_h^2}{4m_W^3} \frac{2v^4}{m_h^2 \Lambda^2} \int_0^\infty dr [1 - S(r)]^3$

- ヒッグス3点結合:  $\frac{\Delta \lambda_{hhh}^{\text{dim6}}}{\lambda_{hhh}^{\text{SM}}} = \frac{2v^4}{m_h^2 \Lambda^2}$

⇒  $\Delta E_{\text{sph}}^{\text{dim6}} \simeq -A^{\text{dim6}} \frac{\Delta \lambda_{hhh}^{\text{dim6}}}{\lambda_{hhh}^{\text{SM}}}$



$$A^{\text{dim6}} = \frac{\pi v^2 m_h^2}{4m_W^3} \int_0^\infty [1 - S(r)]^3 = 0.149 \text{ TeV} \quad \leftarrow \Lambda \text{に依存しない}$$

Eg)  $\Delta \lambda_{hhh}^{\text{dim6}} / \lambda_{hhh}^{\text{SM}} = 96\%$  ( $\Lambda = 700 \text{ GeV}$ ) では  $\Delta E_{\text{sph}}^{\text{dim6}} / E_{\text{sph}}^{\text{SM}} = -1.54\%$

ヒッグス3点結合 ↔ スファレロンエネルギー

# スカラー一重項をN個追加したモデル

・ヒッグスポテンシャル(tree)  $\vec{S} = (S_1, S_2, \dots, S_N)$   $\mu_S^2 > 0$

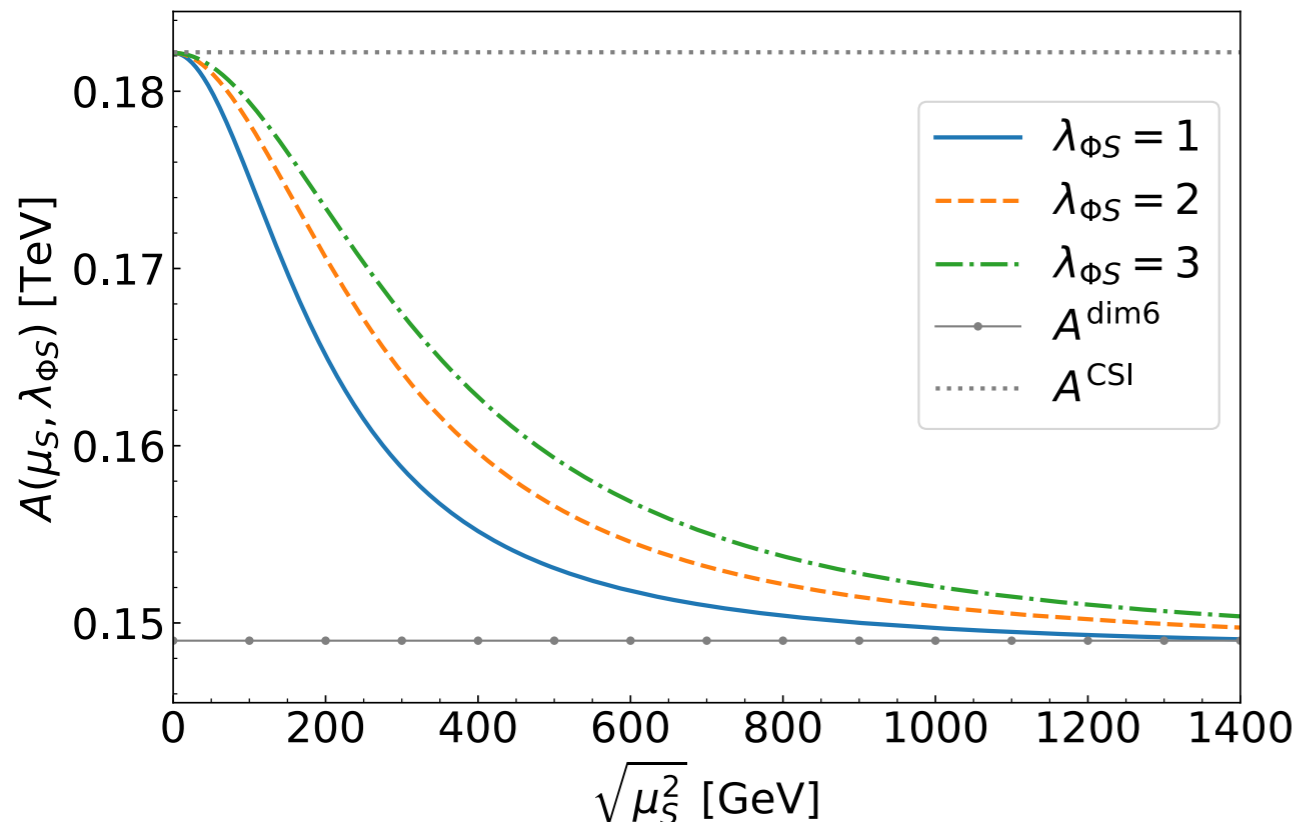
$$V_0(\Phi, \vec{S}) = -\mu^2 \Phi^\dagger \Phi + \lambda(\Phi^\dagger \Phi)^2 + \frac{\mu_S^2}{2} |\vec{S}|^2 + \frac{\lambda_S}{4} |\vec{S}|^4 + \lambda_{\Phi S} \Phi^\dagger \Phi |\vec{S}|^2 \quad M_S(v)^2 = \mu_S^2 + \lambda_{\Phi S} v^2$$

・1ループ効果を含む有効ポテンシャルで  $E_{\text{sph}}$  を評価 [Coleman, Weinberg.: PRD7 (1973)]

$$\Delta E_{\text{sph}}^{N \text{ scalar}} = -A(\mu_S^2, \lambda_{\Phi S}) \frac{\Delta \lambda_{hhh}^{N \text{ scalar}}}{\lambda_{hhh}^{\text{SM}}}$$

$$\frac{\Delta \lambda_{hhh}^{N \text{ scalar}}}{\lambda_{hhh}^{\text{SM}}} = \frac{N M_S^4}{12\pi^2 m_h^2 v^2} \left(1 - \frac{\mu_S^2}{M_S^2}\right)^3$$

[Kanemura, Tanaka: PLB 809 (2020)]



係数Aはモデルの間で対応関係がある

$$A(\mu_S^2, \lambda_{\Phi S}) \rightarrow \begin{cases} A^{\text{dim6}} & (\mu_S^2 \gg v^2), \\ A^{\text{ND}} & (\mu_S^2 \rightarrow 0) \end{cases}$$

Eg) Non-decouplingの場合 ( $\mu_S^2 = 0$ )

$$\frac{\Delta \lambda_{hhh}^{N \text{ scalar}}}{\lambda_{hhh}^{\text{SM}}} = \frac{3}{2} \Rightarrow \frac{\Delta E_{\text{sph}}^{N \text{ scalar}}}{E_{\text{sph}}^{\text{SM}}} = -1.2\%$$

# スファレロンの直接検証

- 加速器でB+Lの破れを引き起こす方法

[Aoyama, Goldberg, PLB 188 (1987)]

$$\Delta(B + L) = +6 \quad qq \rightarrow lllqqqqqqqqqqqq$$

[J. Ellis, K. Sakurai, JHEP 086 (2016)]

$\sqrt{s} > E_{\text{sph}} \simeq 9 \text{ TeV}$ の高エネルギー加速器実験でB+Lの破れが起きるのか？

[Tye, Wong, PRD 92 (2015)] [Funakubo, Fuyuto, Senaha, arXiv: 1612.05431]

B+Lを破る過程の散乱断面積の計算で現れる主要な問題点

- ① トンネリング因子は効くのか？
- ② Ncsを変化させるには、大量のWボソンとヒッグス粒子の生成が必要であるが、その過程は指数関数的に抑制される。この抑制を相殺するような機構は存在するのか？

[Tye, Wong, PRD 96 (2017)]

肯定的な推定では $\sqrt{s} > 25 \text{ TeV}$ ならば見える可能性が指摘されている

← QMを用いた推定で、QFTによる基礎づけは行われていない

議論が決着しておらず、B+Lの破れを加速器実験で直接観測できるかは未知