

擬南部-ゴールドストーン暗黒物質 とゲージ化された $U(1)_{B-L}$ 対称性

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Based on JHEP05(2020)057[arXiv:2001.03954 [hep-ph]]

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Pseudo-Nambu-Goldstone dark matter from *gauged* $U(1)_{B-L}$ symmetry

**Yoshihiko Abe
(Kyoto Univ.)**

Collaboration with

**Takashi Toma (Kanazawa Univ.)
Koji Tsumura (Kyushu Univ.)**

Based on JHEP05(2020)057[arXiv:2001.03954 [hep-ph]]

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Pseudo-Nambu-Goldstone dark matter

②

**and, from
gauged $U(1)_{B-L}$ symmetry**

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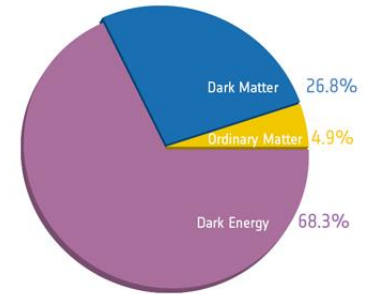
Koji Tsumura (Kyushu Univ.)

Based on JHEP05(2020)057[arXiv:2001.03954 [hep-ph]]

WIMP dark matter

- Dark matter

- The existence of dark matter is inferred from various observations.
- The nature of dark matter is still unknown.
- Identification of dark matter \Rightarrow BSM

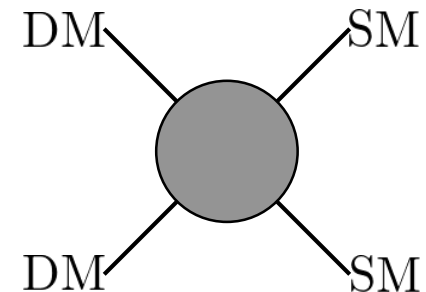
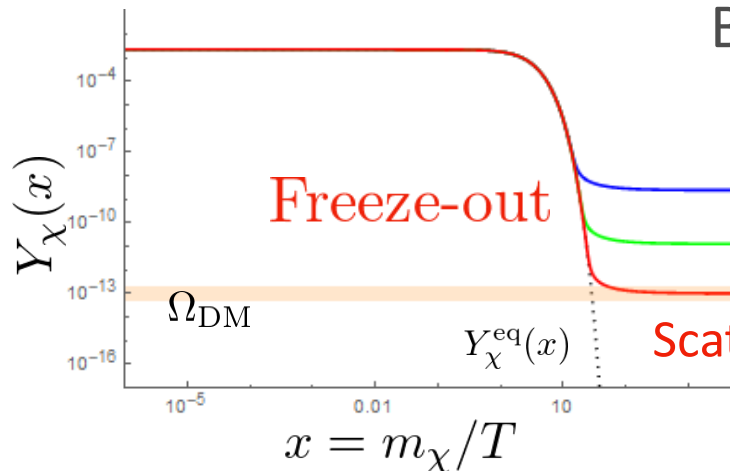


- WIMP dark matter

- Dark matter relic abundance is realized as the thermal relic

Boltzmann equation for WIMP

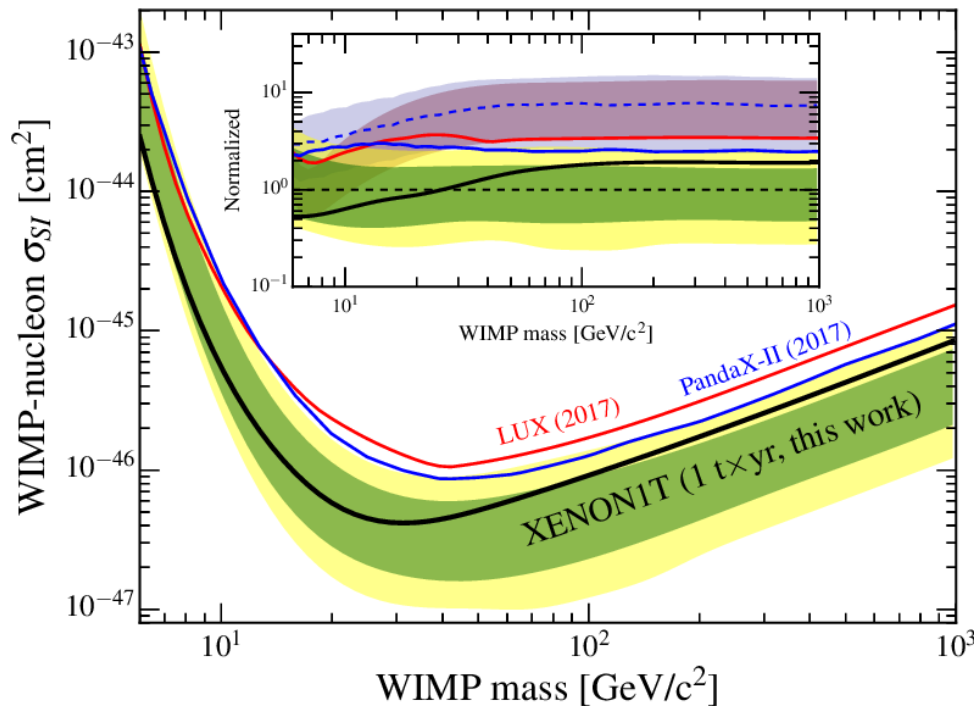
$$\frac{dY_\chi(x)}{dx} = \frac{\langle\sigma v\rangle s}{xH} \left(Y_\chi(x)^2 - Y_\chi^{\text{eq}}(x)^2 \right)$$



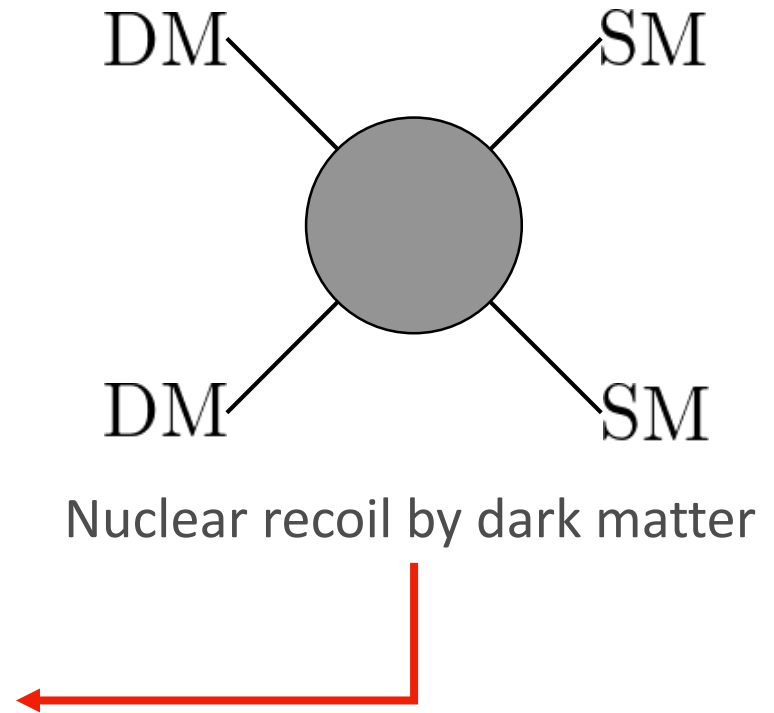
Direct detection experiments

- Direct detection experiments
LUX, PandaX-II, XENON

⇒ **Severe constraints** on the WIMP-nucleon cross section



XENON collaboration (2018)



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Pseudo-Nambu-Goldstone Dark Matter

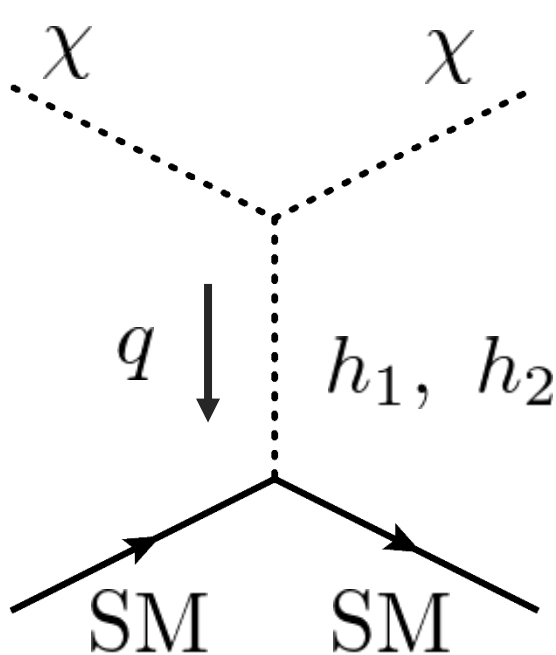
[Gross-Lebedev-Toma (2017),...]

- SM + singlet scalar S

$$V(H, S) = -\frac{\mu_H^2}{2}|H|^2 - \frac{\mu_S^2}{2}|S|^2 + \frac{\lambda_H}{2}|H|^4 + \frac{\lambda_S}{2}|S|^4 + \lambda_{HS}|H|^2|S|^2 - \frac{m^2}{4}(S^2 + S^{*2})$$

Soft breaking term \Rightarrow creating DM mass

$DM: \chi = \sqrt{2} \text{Im}(S)$



$$\kappa_{h_1\chi\chi} = -\frac{m_{h_1}^2 \sin \theta}{v_s}, \quad \kappa_{h_2\chi\chi} = +\frac{m_{h_2}^2 \cos \theta}{v_s}$$

Scattering amplitude

$$i\mathcal{M} \sim -\frac{\sin \theta \cos \theta (m_{h_1}^2 - m_{h_2}^2)}{v_s m_{h_1}^2 m_{h_2}^2} q^2 \xrightarrow{q^2 \rightarrow 0} 0$$

Cf. soft pion theorem

Our motivation

- What is the origin for the soft breaking term?

$$V_{\text{soft}}(H, S) = -\frac{m^2}{4}(S^2 + S^{*2}) \quad U(1)_S \rightarrow \mathbb{Z}_2$$

Other term? Renormalizability? Symmetry?

- What is the UV physics of the pNGB dark matter model?

Our assumptions

- Renormalizable field theoretic description
- The *symmetry* of the UV physics maybe *gauge symmetry*
(discrete symmetry should be gauged)

No global symmetry, landscape, swampland [Banks-Seiberg (2010)]

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Gauged $U(1)_{B-L}$ model

[YA-Toma-Tsumura (2020), Okada-Raut-Shafi (2020)]

- Gauged $U(1)_{B-L}$ model

	Q_L	u_R^c	d_R^c	L	e_R^c	H	ν_R^c	S	Φ
$SU(3)_c$	3	$\bar{3}$	$\bar{3}$	1	1	1	1	1	1
$SU(2)_L$	2	1	1	2	1	2	1	1	1
$U(1)_Y$	+1/6	-2/3	+1/3	-1/2	+1	+1/2	0	0	0
$U(1)_{B-L}$	+1/3	-1/3	-1/3	-1	+1	0	+1	+1	+2

Our gauged $U(1)_{B-L}$ model

Ordinary $U(1)_{B-L}$ model

SM

Giving Majorana masses
⇒ type-I see-saw

+ RHv's ν_R + New gauge boson X_μ + Singlet scalar Φ

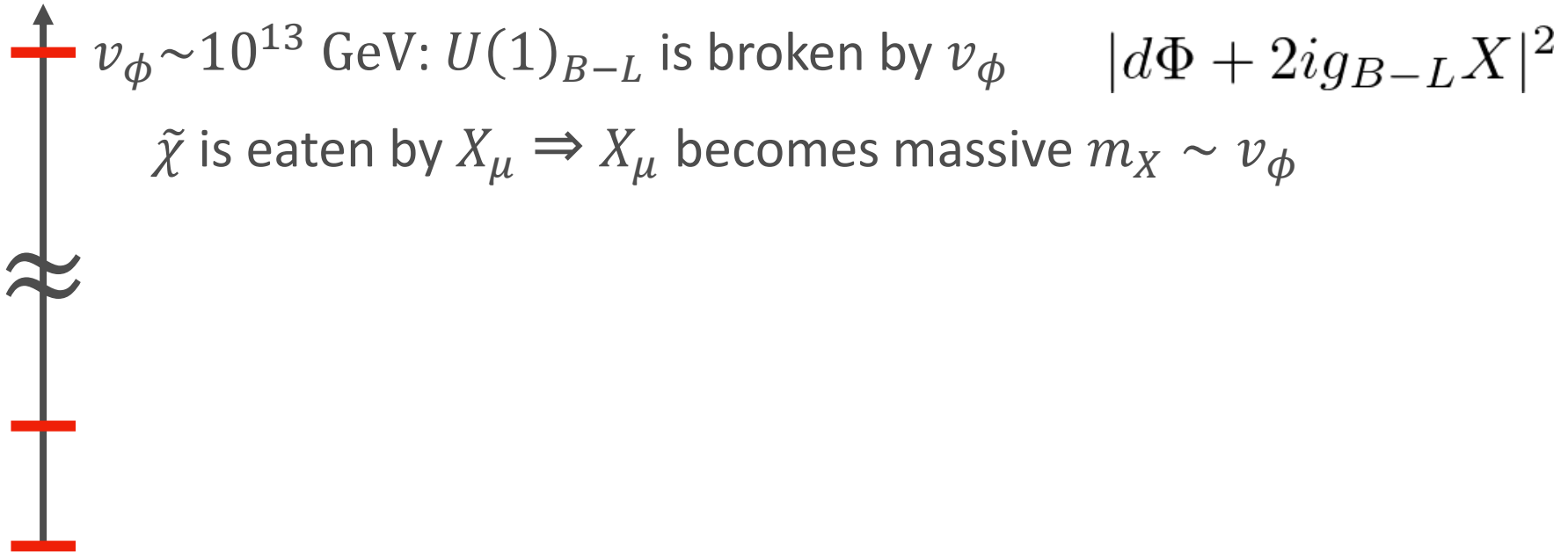
+ Singlet scalar S ← New !!

pNGB dark matter from gauged $U(1)_{B-L}$ model

- Intuitive story of our gauged $U(1)_{B-L}$ model

$$V(H, S, \Phi) = -\frac{\mu_H^2}{2}|H|^2 - \frac{\mu_S^2}{2}|S|^2 - \frac{\mu_\Phi^2}{2}|\Phi|^2 + \frac{\lambda_H}{2}|H|^4 + \frac{\lambda_S}{2}|S|^4 + \frac{\lambda_\Phi}{2}|\Phi|^4 \\ + \lambda_{HS}|H|^2|S|^2 + \lambda_{H\Phi}|H|^2|\Phi|^2 + \lambda_{S\Phi}|S|^2|\Phi|^2 - \left(\frac{\mu_c}{\sqrt{2}}\Phi^* S^2 + \text{c.c.} \right)$$

Energy scale



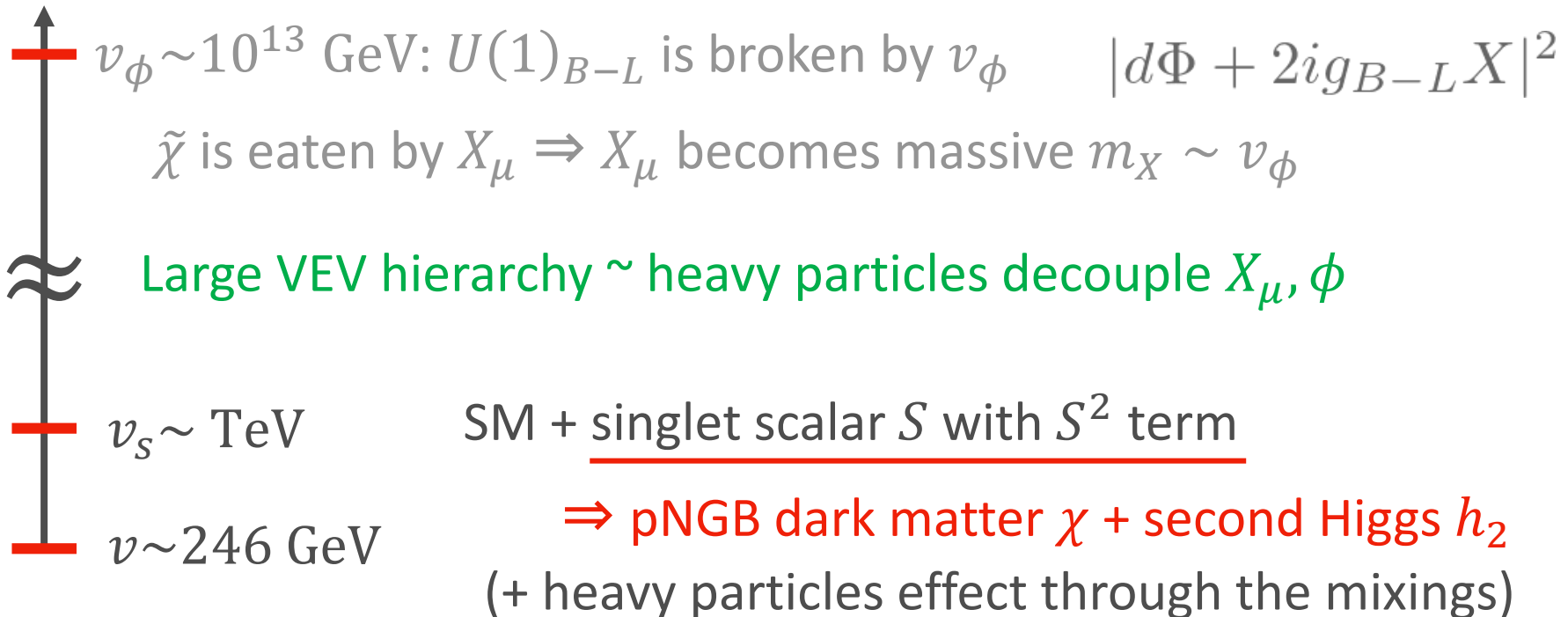
pNGB dark matter from gauged $U(1)_{B-L}$ model

- Intuitive story of our gauged $U(1)_{B-L}$ model

$$V(H, S, \langle \Phi \rangle) = -\frac{\mu_H^2}{2}|H|^2 + \frac{\lambda_{H\Phi} v_\phi^2}{2}|H|^2 - \frac{\mu_S^2}{2}|S|^2 + \frac{\lambda_{S\Phi} v_\phi^2}{2}|S|^2 + \frac{\lambda_H}{2}|H|^4 + \frac{\lambda_S}{2}|S|^4$$

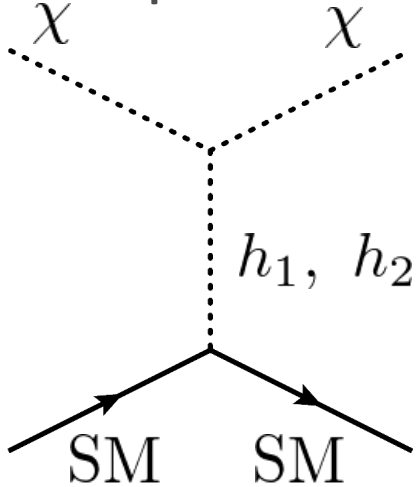
$$+ \lambda_{HS}|H|^2|S|^2 - \left(\frac{\mu_c v_\phi}{2} S^2 + \frac{\mu_c v_\phi}{2} S^{*2} \right)$$

Energy scale



pNGB dark matter from gauged $U(1)_{B-L}$ model

- Amplitude for DM + SM \rightarrow DM + SM



$$\kappa_{\chi\chi h_1} \approx -\frac{m_{h_1}^2 \sin \theta}{v_s}, \quad \kappa_{\chi\chi h_2} \approx +\frac{m_{h_2}^2 \cos \theta}{v_s},$$

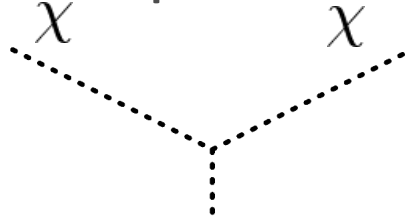
$$\kappa_{\chi\chi h_3} \approx +\frac{m_{h_3}^2}{v_s} \frac{\lambda_{S\Phi} v_s}{\lambda_{\Phi} v_{\phi}}$$

$$i\mathcal{M} \propto \frac{\sin \theta \cos \theta}{v_s} \left(-\frac{m_{h_1}^2}{q^2 - m_{h_1}^2} + \frac{m_{h_2}^2}{q^2 - m_{h_2}^2} \right) + \mathcal{O}(1/v_{\phi})$$

The scattering amplitudes are suppressed in the same way as pNGB model in order $\mathcal{O}(1/v_{\phi})$.

pNGB dark matter from gauged $U(1)_{B-L}$ model

- Amplitude for DM + SM \rightarrow DM + SM



$$\kappa_{\chi\chi h_1} \approx -\frac{m_{h_1}^2 \sin \theta}{v_s}, \quad \kappa_{\chi\chi h_2} \approx +\frac{m_{h_2}^2 \cos \theta}{v_s},$$

**Pseudo-Nambu-Goldstone dark matter
from gauged $U(1)_{B-L}$ symmetry**

$$v_s \quad \left(\quad q^2 - m_{h_1}^2 \quad q^2 - m_{h_2}^2 \right)$$

The scattering amplitudes are suppressed in the same way as pNGB model in order $\mathcal{O}(1/v_\phi)$.

Long-lived Dark Matter

- Our DM χ is **not stabilized** due to the new interactions and scalar mixings.
- Constraints of our model from a conservative limit of the DM life-time
[Baring-Ghosh-Queiroz-Sinha (2015)]

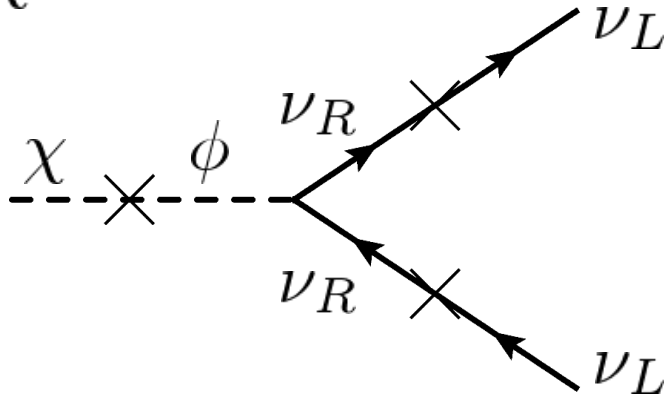
$$\tau_{\text{DM}} \gtrsim 10^{27} \text{ s} \quad \Leftrightarrow \quad \Gamma_{\text{DM}} \lesssim 6.6 \times 10^{-52} \text{ GeV}$$

- We have to check the decay channels of this pNGB DM and calculate the decay widths.

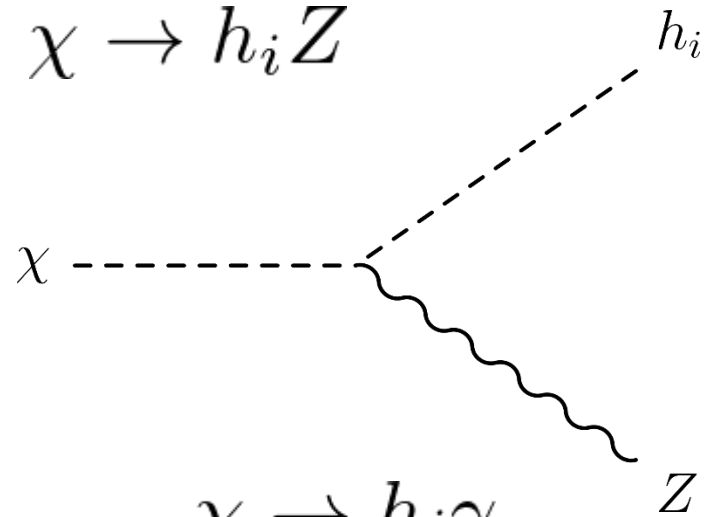
Long-lived DM

Two-body decay

$$\chi \rightarrow \nu\nu$$

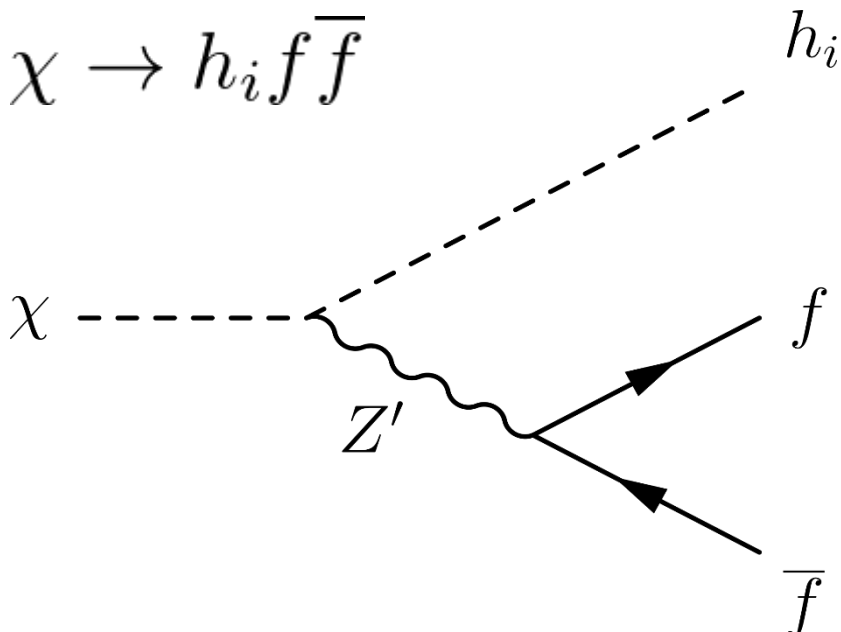


$$\chi \rightarrow h_i Z$$

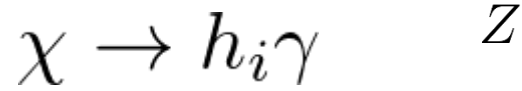


Three-body decay

$$\chi \rightarrow h_i f \bar{f}$$



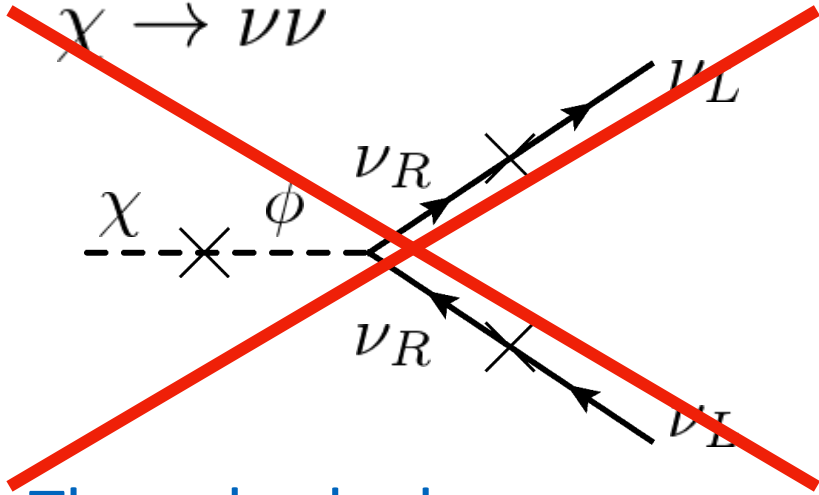
$$\chi \rightarrow h_i \gamma$$



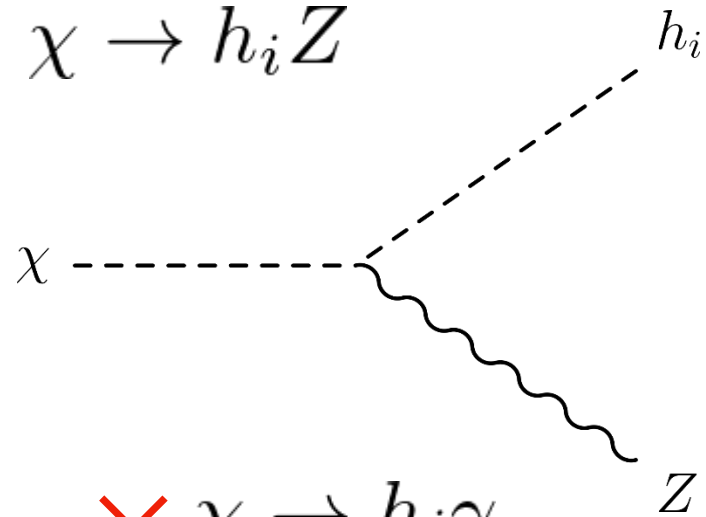
Long-lived DM

Two-body decay

$$\chi \rightarrow \nu\nu$$



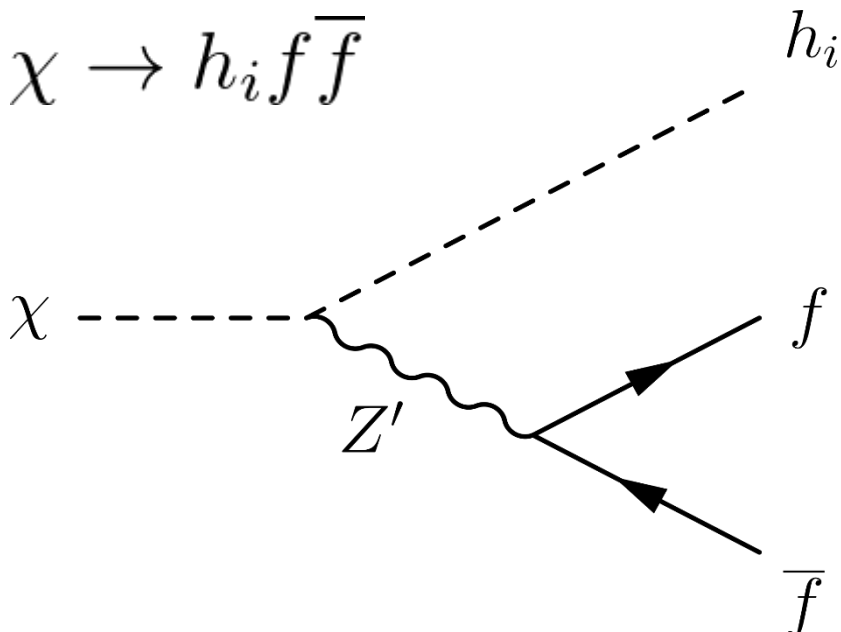
$$\chi \rightarrow h_i Z$$



$$\times \chi \rightarrow h_i \gamma$$

Three-body decay

$$\chi \rightarrow h_i f \bar{f}$$



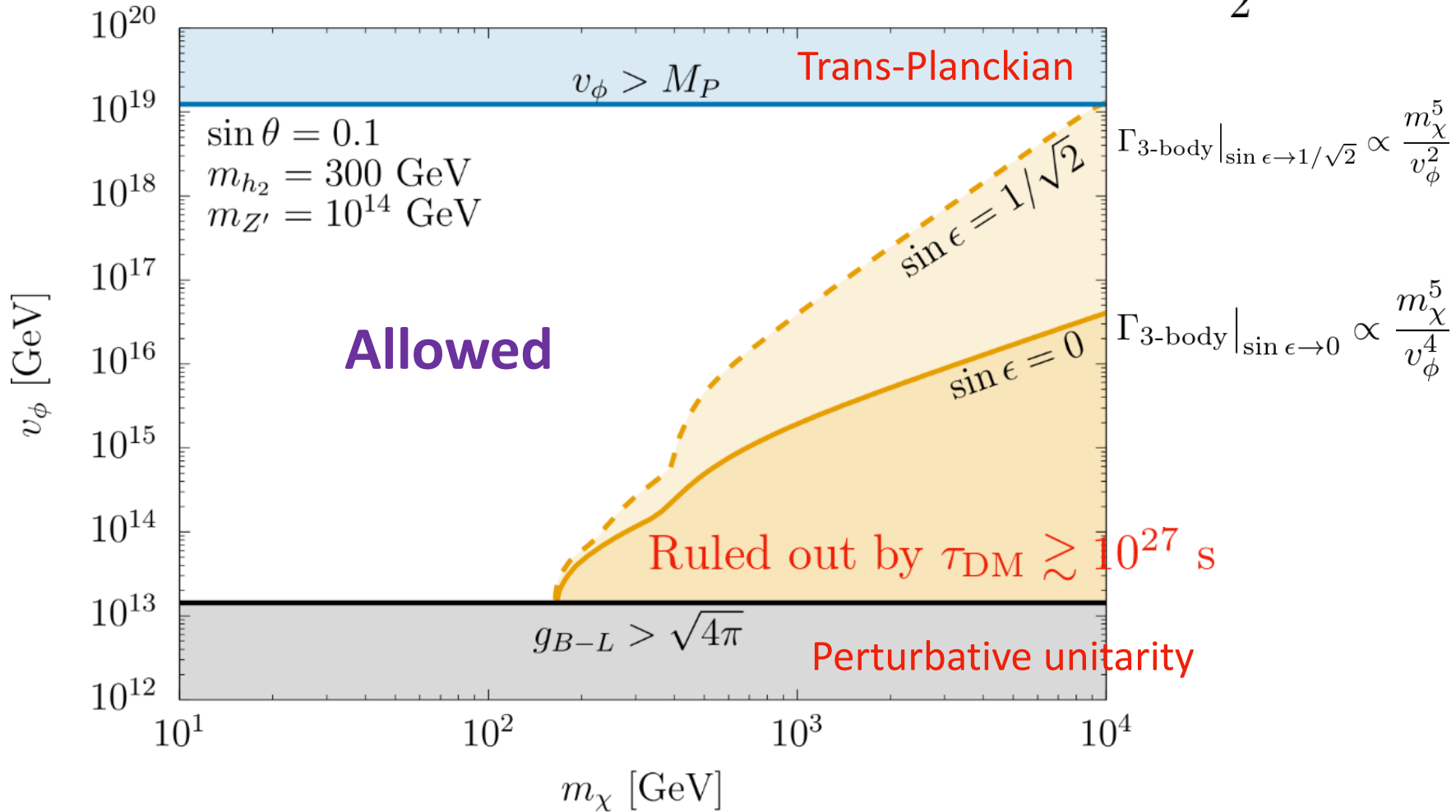
☺ helicity conservation

$$\Gamma_{2\text{-body}} \propto m_\chi^3$$

$$\Gamma_{3\text{-body}} \propto m_\chi^5$$

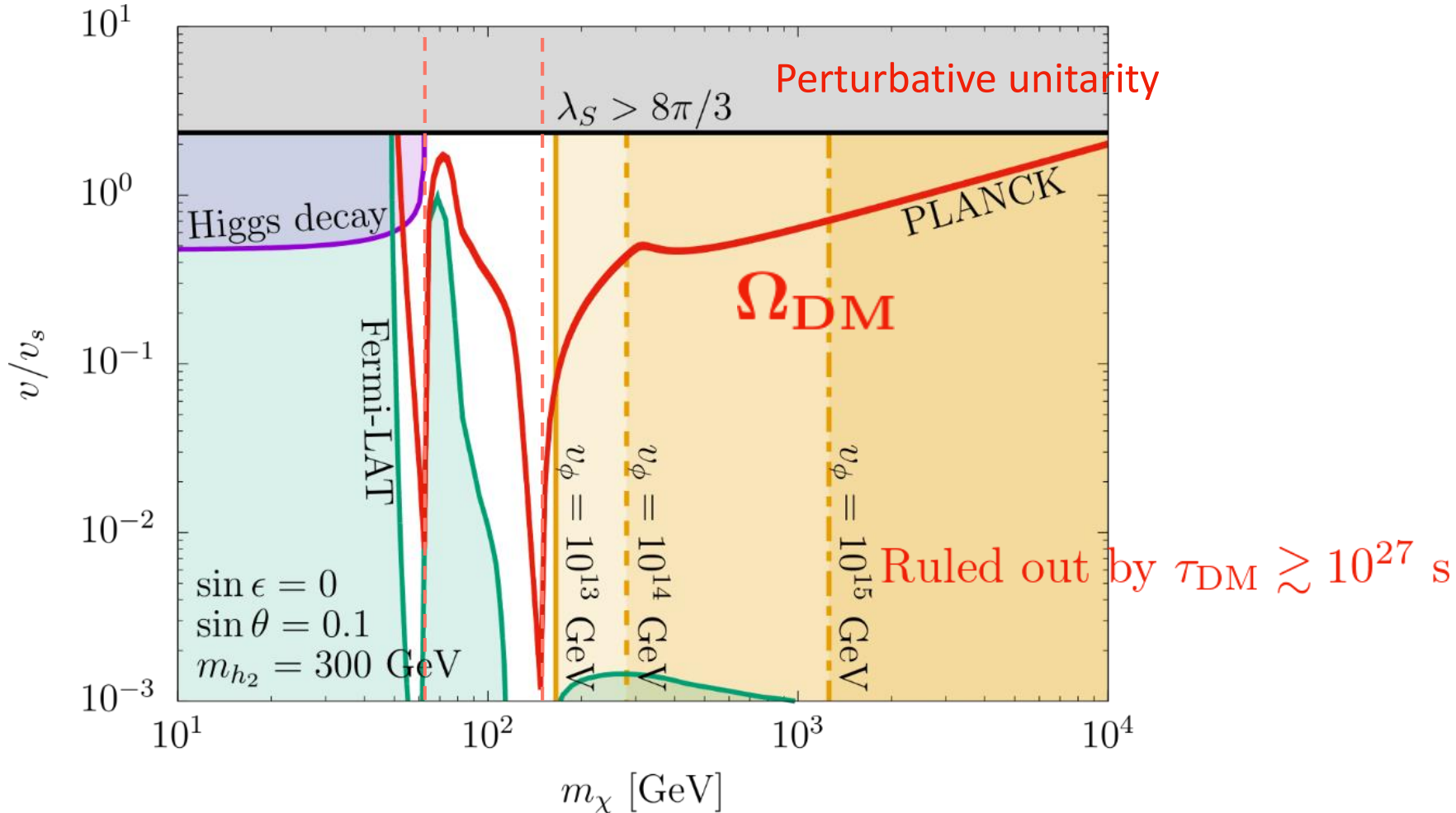
Allowed region in the (m_χ, v_ϕ) plane

$$m_{h_2} = 300 \text{ GeV}, \quad m_{Z'} = 10^{14} \text{ GeV} \quad -\frac{\sin \epsilon}{2} B_{\mu\nu} X^{\mu\nu}$$



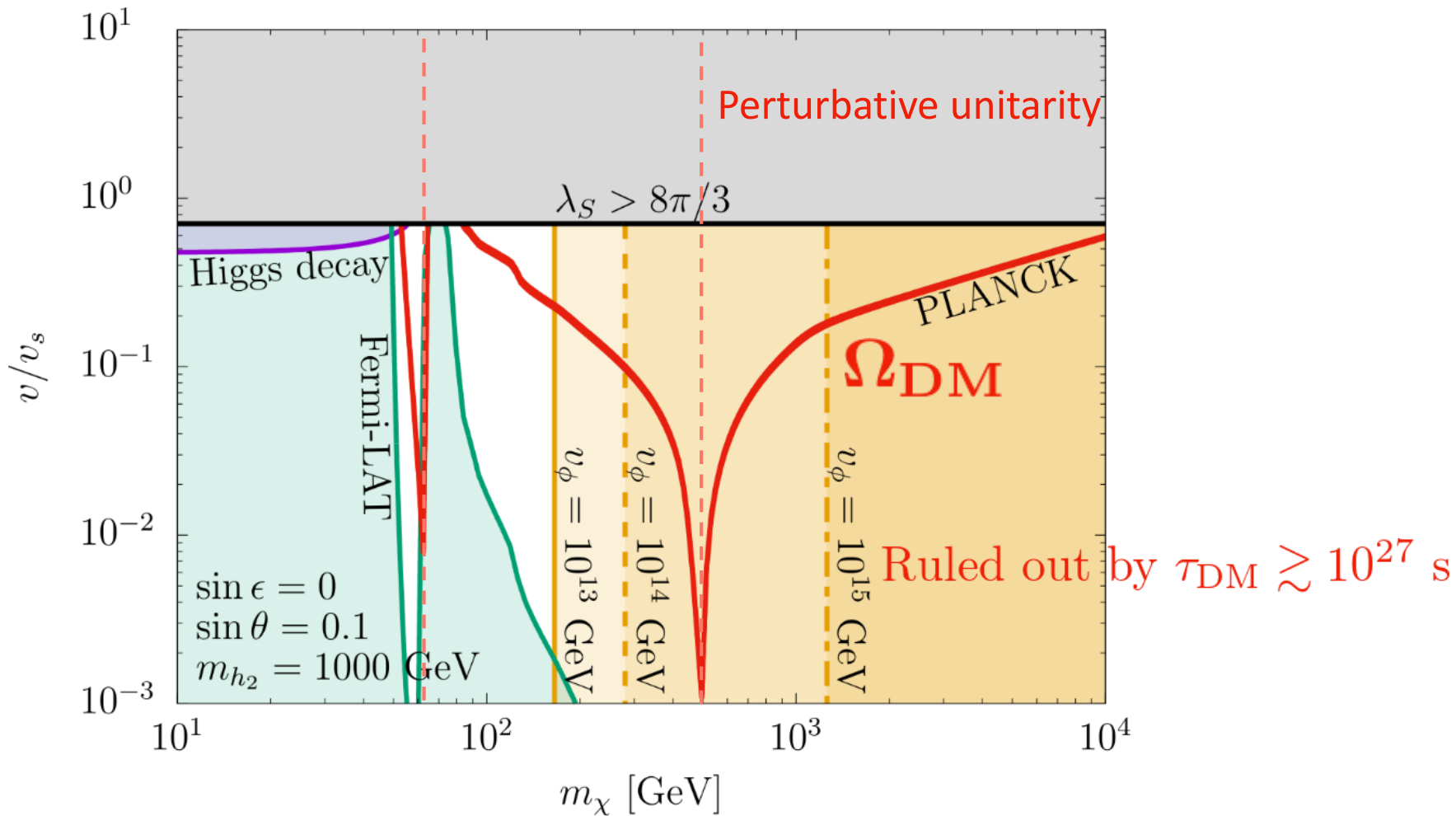
Allowed region in the $(m_\chi, v/v_s)$ plane

$$m_{h_2} = 300 \text{ GeV}, \quad \sin \epsilon = 0$$



Allowed region in the $(m_\chi, v/v_s)$ plane

$$m_{h_2} = 1000 \text{ GeV}, \quad \sin \epsilon = 0$$



Summary

- We studied the pNGB dark matter scenario derived from the *gauged* $U(1)_{B-L}$ model.
- This is the decaying dark matter then we showed the lifetime is long enough to be dark matter.
- We have found the parameter space consistent with the relevant constraints.
- This model can be explored by the planned gamma-ray observations.

e.g. CTA, LHASSO



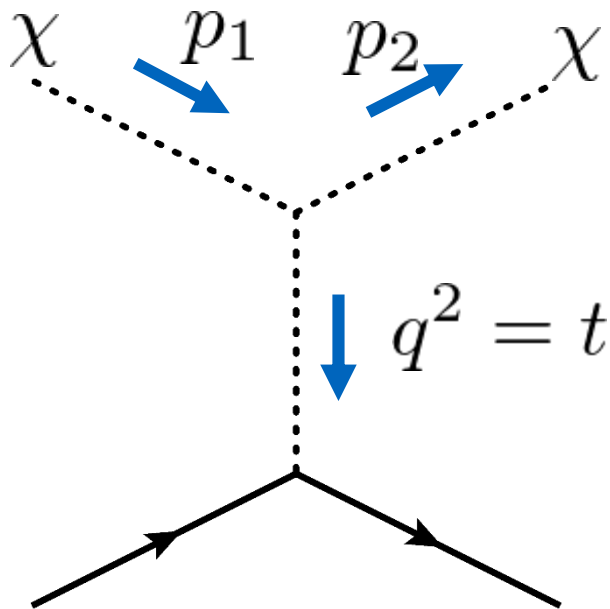
Backup

Nature of interactions of (p)NGBs

- Toy model $S = \frac{v_s + s}{\sqrt{2}} e^{i\chi/v_s}$ Non-linear rep.

$$\mathcal{L} \supset |\partial_\mu S|^2 + |\partial_\mu H|^2 - \lambda_{HS} |H|^2 |S|^2 - \frac{m^2}{4} (S^2 + S^{*2})$$

$$\sim \frac{1}{2} \left(1 + \frac{\phi}{v_s} \right)^2 \left((\partial_\mu \chi)^2 - m^2 \chi^2 \right) - \lambda_{HS} v_s s |H|^2$$



$$i\mathcal{M} \supset \lambda_{HS} \frac{((-ip_1) \cdot (ip_2) - m^2)}{t - m_s^2}$$

$$\sim \lambda_{HS} \frac{t}{t - m_s^2}$$

$$\lim_{t \rightarrow 0} \mathcal{M} = 0$$

Boltzmann equation

- Boltzmann equation for dark matter $Y_\chi(x) = n_\chi/s$, $x = m_\chi/T$

$$\frac{dY_\chi(x)}{dx} = -\frac{\langle\sigma v\rangle}{x^2} \frac{s(m_\chi)}{H(m_\chi)} (Y_\chi(x)^2 - Y_\chi^{\text{eq}}(x)^2)$$

$$s(T) = \frac{2\pi^2}{45} g_*^S T^3, \quad H(T) = \sqrt{\frac{4\pi^3}{45} g_*} \frac{T^2}{M_P}$$

$$Y_\chi^{\text{eq}} = n_\chi^{\text{eq}}/s, \quad n_\chi^{\text{eq}} = \frac{m_\chi^2 T^2}{2\pi^2} K_2(m_\chi/T)$$

$$\langle\sigma v\rangle = \frac{1}{n_\chi^{\text{eq}2}} \frac{1}{2^5 \pi^4} \left(\frac{m_\chi}{x}\right) \int_{4m_\chi^2}^{\infty} ds (s - 4m_\chi^2) \sqrt{s} K_1(x\sqrt{s}/m_\chi) \sigma(s)$$

σ : Total dark matter annihilation cross section

Gauged $U(1)_{B-L}$ model

Lagrangian

- Covariant derivative

$$D_\mu = D_\mu^{\text{SM}} + ig_{B-L} X_\mu$$

- Kinetic term of new sectors

Gauge kinetic mixing

$$\mathcal{L}_K = |D_\mu S|^2 + |D_\mu \Phi|^2 + \overline{\nu_R} i \not{D} \nu_R - \frac{1}{4} X_{\mu\nu} X^{\mu\nu} - \frac{\sin \epsilon}{2} X_{\mu\nu} B^{\mu\nu}$$

- Yukawa interactions among SM leptons, RHv's and scalars

$$\mathcal{L}_Y = -(y_\nu)_{ij} \tilde{H}^\dagger \overline{\nu_{Ri}} L_j - \frac{(y_\Phi)_{ij}}{2} \Phi \overline{\nu_{Ri}^c} \nu_{Rj} + \text{h.c.}$$

Giving Majorana masses

- Scalar potential

$$V(H, S, \Phi) = -\frac{\mu_H^2}{2} |H|^2 - \frac{\mu_S^2}{2} |S|^2 - \frac{\mu_\Phi^2}{2} |\Phi|^2 + \frac{\lambda_H}{2} |H|^4 + \frac{\lambda_S}{2} |S|^4 + \frac{\lambda_\Phi}{2} |\Phi|^4 \\ + \lambda_{HS} |H|^2 |S|^2 + \lambda_{H\Phi} |H|^2 |\Phi|^2 + \lambda_{S\Phi} |S|^2 |\Phi|^2 - \left(\frac{\mu_c}{\sqrt{2}} \Phi^* S^2 + \text{c.c.} \right)$$

Scalar sector

- Parametrization

$$H = \begin{pmatrix} 0 \\ (v + h)/\sqrt{2} \end{pmatrix}, \quad S = \frac{v_s + s + i\eta_s}{\sqrt{2}}, \quad \Phi = \frac{v_\phi + \phi + i\eta_\phi}{\sqrt{2}}$$

- Type-I see-saw mechanism identifies the scale of VEV v_ϕ .

$$v_\phi \sim 4.3 \times 10^{14} \text{ GeV} \left(\frac{y_\nu^2}{y_\Phi} \right) \gg v, v_s$$

- Masses of the heaviest CP-even scalar ϕ and massive vector boson Z'_μ

$$m_\phi, m_{Z'} \sim v_\phi$$

Mass spectrum of scalar sectors

- Mass eigenstates

$$\tan 2\theta \approx \frac{2vv_s(\lambda_{HS}\lambda_\Phi - \lambda_{H\Phi}\lambda_{S\Phi})}{v^2(\lambda_{H\Phi}^2 - \lambda_H\lambda_\Phi) - v_s^2(\lambda_{S\Phi}^2 - \lambda_S\lambda_\Phi)}$$

SM-like Higgs boson

- CP-even scalars

$$\begin{pmatrix} h \\ s \\ \phi \end{pmatrix} \approx \begin{pmatrix} 1 & 0 & \frac{\lambda_{H\Phi}v}{\lambda_\Phi v_\phi} \\ 0 & 1 & \frac{\lambda_{S\Phi}v_s}{\lambda_\Phi v_\phi} \\ -\frac{\lambda_{H\Phi}v}{\lambda_\Phi v_\phi} & -\frac{\lambda_{S\Phi}v_s}{\lambda_\Phi v_\phi} & 1 \end{pmatrix} \begin{pmatrix} \cos\theta & \sin\theta & 0 \\ -\sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} h_1 \\ h_2 \\ h_3 \end{pmatrix}$$

$$m_{h_1}^2 \approx \lambda_H v^2 - \frac{\lambda_{H\Phi}^2 \lambda_S - 2\lambda_{HS}\lambda_{H\Phi}\lambda_{S\Phi} + \lambda_\Phi \lambda_{HS}^2}{\lambda_{S\Phi} - \lambda_{S\Phi}^2} v^2, \quad \leftarrow 125 \text{ GeV}$$

$$m_{h_2}^2 \approx \frac{\lambda_S \lambda_\Phi - \lambda_{S\Phi}^2}{\lambda_\Phi} v_s^2 + \frac{(\lambda_\Phi \lambda_{HS} - \lambda_{H\Phi} \lambda_{S\Phi})^2}{\lambda_\Phi (\lambda_S \lambda_\Phi - \lambda_{S\Phi}^2)} v^2, \quad m_{h_3}^2 \approx \lambda_\Phi v_\phi^2$$

- CP-odd scalars

pNGB (dark matter)

$$\begin{pmatrix} \eta_s \\ \eta_\phi \end{pmatrix} = \frac{1}{(v_s^2 + 4v_\phi^2)^{1/2}} \begin{pmatrix} 2v_\phi & v_s \\ -v_s & 2v_\phi \end{pmatrix} \begin{pmatrix} \chi \\ \tilde{\chi} \end{pmatrix}$$

Eaten by X_μ

$$m_\chi^2 = \frac{\mu_c (v_s^2 + 4v_\phi^2)}{4v_\phi}$$

Gauge kinetic mixing

$SU(2)_L \times U(1)_Y \times U(1)_{B-L}$ gauge group

- Kinetic term

$$\mathcal{L}_{GK} = -\frac{1}{2} \text{tr} W_{\mu\nu} W^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} - \frac{1}{4} X_{\mu\nu} X^{\mu\nu} - \frac{\sin \epsilon}{2} B_{\mu\nu} X^{\mu\nu}$$

- Mass term

$$\mathcal{L}_M = \frac{1}{2} \begin{pmatrix} B_\mu & W_\mu^3 & X_\mu \end{pmatrix} \begin{pmatrix} \sin^2 \theta_W m_{\tilde{Z}}^2 & -\sin \theta_W \cos \theta_W m_{\tilde{Z}}^2 & 0 \\ -\sin \theta_W \cos \theta_W m_{\tilde{Z}}^2 & \cos^2 \theta_W m_{\tilde{Z}}^2 & 0 \\ 0 & 0 & m_X^2 \end{pmatrix} \begin{pmatrix} B^\mu \\ W^{3\mu} \\ X^\mu \end{pmatrix}$$

$$\sin \theta_W \equiv \frac{g_1}{\sqrt{g_1^2 + g_2^2}}, \quad \cos \theta_W \equiv \frac{g_2}{\sqrt{g_1^2 + g_2^2}},$$

$$m_{\tilde{Z}}^2 \equiv \frac{g_1^2 + g_2^2}{4} v^2, \quad m_X^2 \equiv g_{B-L}^2 (v_s^2 + 4v_\phi^2)$$

Gauge kinetic mixing

$SU(2)_L \times U(1)_Y \times U(1)_{B-L}$ gauge group

- Mixing

$$\tilde{V}_{GK} = \begin{pmatrix} 1 & 0 & -\tan \epsilon \\ 0 & 1 & 0 \\ 0 & 0 & 1/\cos \epsilon \end{pmatrix}, \quad \tan 2\zeta = \frac{-m_{\tilde{Z}}^2 \sin_W \sin 2\epsilon}{m_X^2 - m_{\tilde{Z}}^2 (\cos^2 \epsilon - \sin^2 \theta_W \sin^2 \epsilon)}$$

$$U_G = \begin{pmatrix} \cos \theta_W & -\sin \theta_W & 0 \\ \sin \theta_W & \cos \theta_W & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \zeta & -\sin \zeta \\ 0 & \sin \zeta & \cos \zeta \end{pmatrix}$$

$$\begin{pmatrix} B_\mu \\ W_\mu^3 \\ X_\mu \end{pmatrix} = \tilde{V}_{GK} U_G \begin{pmatrix} A_\mu \\ Z_\mu \\ Z'_\mu \end{pmatrix}$$

- Mass eigenvalues

$$m_Z^2 = \frac{1}{2} \left[\overline{M}^2 - \sqrt{\overline{M}^4 - \frac{4m_{\tilde{Z}}^2 m_X^2}{\cos^2 \epsilon}} \right], \quad m_{Z'}^2 = \frac{1}{2} \left[\overline{M}^2 + \sqrt{\overline{M}^4 + \frac{4m_{\tilde{Z}}^2 m_X^2}{\cos^2 \epsilon}} \right]$$

$$\overline{M}^2 \equiv m_{\tilde{Z}}^2 (1 + \sin^2 \theta_W \tan^2 \epsilon) + m_X^2 / \cos^2 \epsilon$$

Interactions

- Scalar-dark matter-massive gauge boson

$$\mathcal{L}_{Zh_i\chi} = \sum_i g_{B-L} \frac{\sin \zeta}{\cos \epsilon} \frac{U_{si}}{\sqrt{1 + v_s^2/4v_\phi^2}} Z_\mu (h_i \partial^\mu \chi - \chi \partial^\mu h_i),$$

$$\mathcal{L}_{Z'h_i\chi} = \sum_i g_{B-L} \frac{\cos \zeta}{\cos \epsilon} \frac{U_{si}}{\sqrt{1 + v_s^2/4v_\phi^2}} Z'_\mu (h_i \partial^\mu \chi - \chi \partial^\mu h_i)$$

- Massive gauge boson-fermion

$$\mathcal{L}_{Z'\bar{f}f} = -Z'_\mu \bar{f} \gamma^\mu \left[g_V^f + g_A^f \gamma^5 \right] f$$

$$g_V^f = -\frac{g_2}{2} T_3^f \sin \zeta \cos \theta_W + g_1 (Q_{\text{em}}^f - F_3^f) (\sin \zeta \sin \theta_W - \cos \zeta \tan \epsilon) \\ + g_{B-L} Q_{B-L}^f \frac{\cos \zeta}{\cos \epsilon},$$

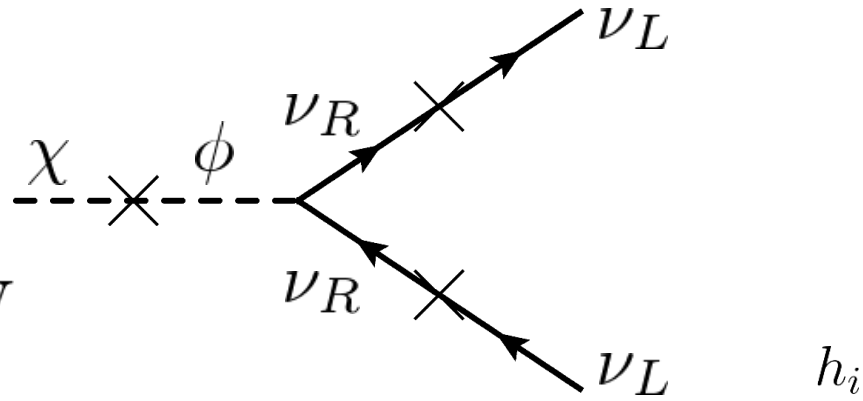
$$g_A^f = \frac{g_2}{2} T_3^f \sin \zeta \cos \theta_W$$

Long-lived dark matter

Two body decay

- $\chi \rightarrow \nu\nu$

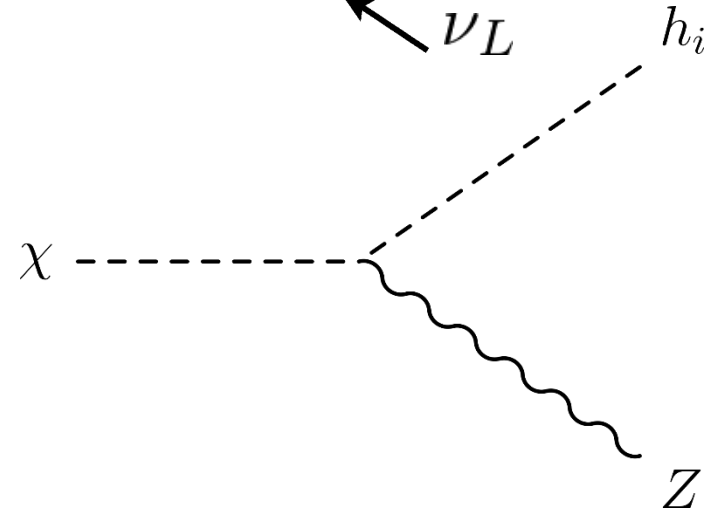
$$\Gamma_{\chi \rightarrow \nu\nu} \lesssim 10^{-67} \text{ GeV}$$



- $\chi \rightarrow h_i Z$

$$\Gamma_{2\text{-body}} \approx \frac{g_{B-L}^2}{16\pi m_{Z'}^4} m_Z^2 m_\chi^3 \sin^2 \theta_W \sin^2 \epsilon$$

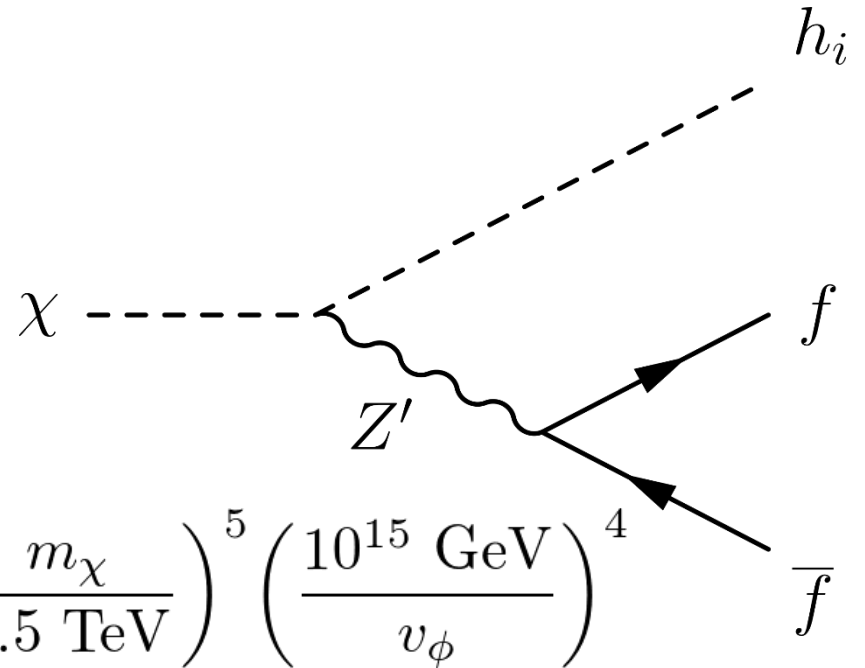
$$= \boxed{5.8 \times 10^{-52} \text{ GeV}} \left(\frac{m_\chi}{0.5 \text{ TeV}} \right)^3 \left(\frac{10^{15} \text{ GeV}}{m_{Z'}} \right)^2 \left(\frac{10^{15} \text{ GeV}}{v_\phi} \right)^2 \left(\frac{\sin \epsilon}{1/\sqrt{2}} \right)^2$$



Long-lived dark matter

Three body decay

- $\chi \rightarrow h_i f \bar{f}$



$$\Gamma_{3\text{-body}} \Big|_{\sin \epsilon \rightarrow 0} \approx \frac{13}{16} \frac{g_{B-L}^4}{1536\pi^3} \frac{m_\chi^5}{m_{Z'}^4}$$

$$\approx \boxed{5.3 \times 10^{-52} \text{ GeV}} \left(\frac{m_\chi}{0.5 \text{ TeV}} \right)^5 \left(\frac{10^{15} \text{ GeV}}{v_\phi} \right)^4$$

$$\Gamma_{3\text{-body}} \Big|_{\sin \epsilon \rightarrow 1/\sqrt{2}} \approx \frac{g_{B-L}^2}{768\pi^3} \frac{m_\chi^5}{m_{Z'}^4} (10g_1^2 - 8\sqrt{2}g_1g_{B-L} + 26g_{B-L}^2)$$

$$\approx \boxed{4.1 \times 10^{-52} \text{ GeV}} \left(\frac{m_\chi}{0.5 \text{ TeV}} \right)^5 \left(\frac{10^{15} \text{ GeV}}{m_{Z'}} \right)^2 \left(\frac{10^{15} \text{ GeV}}{v_\phi} \right)^2$$

$$\times \left[1 - \frac{2\sqrt{2}}{5} \frac{m_{Z'}}{g_1 v_\phi} + \frac{13}{20} \frac{m_{Z'}^2}{g_1^2 v_\phi^2} \right]$$

Numerical Analysis

Numerical Analysis

- Parameter sets

$$m_{h_2} = 300 \text{ or } 1000 \text{ GeV}, \quad m_{h_3} = 10^{13} \text{ GeV},$$

$$\sin \theta = 0.1, \quad \lambda_{H\Phi} = \lambda_{S\Phi} = 10^{-6}$$

$$m_{Z'} = 10^{14} \text{ or } 10^{15} \text{ GeV},$$

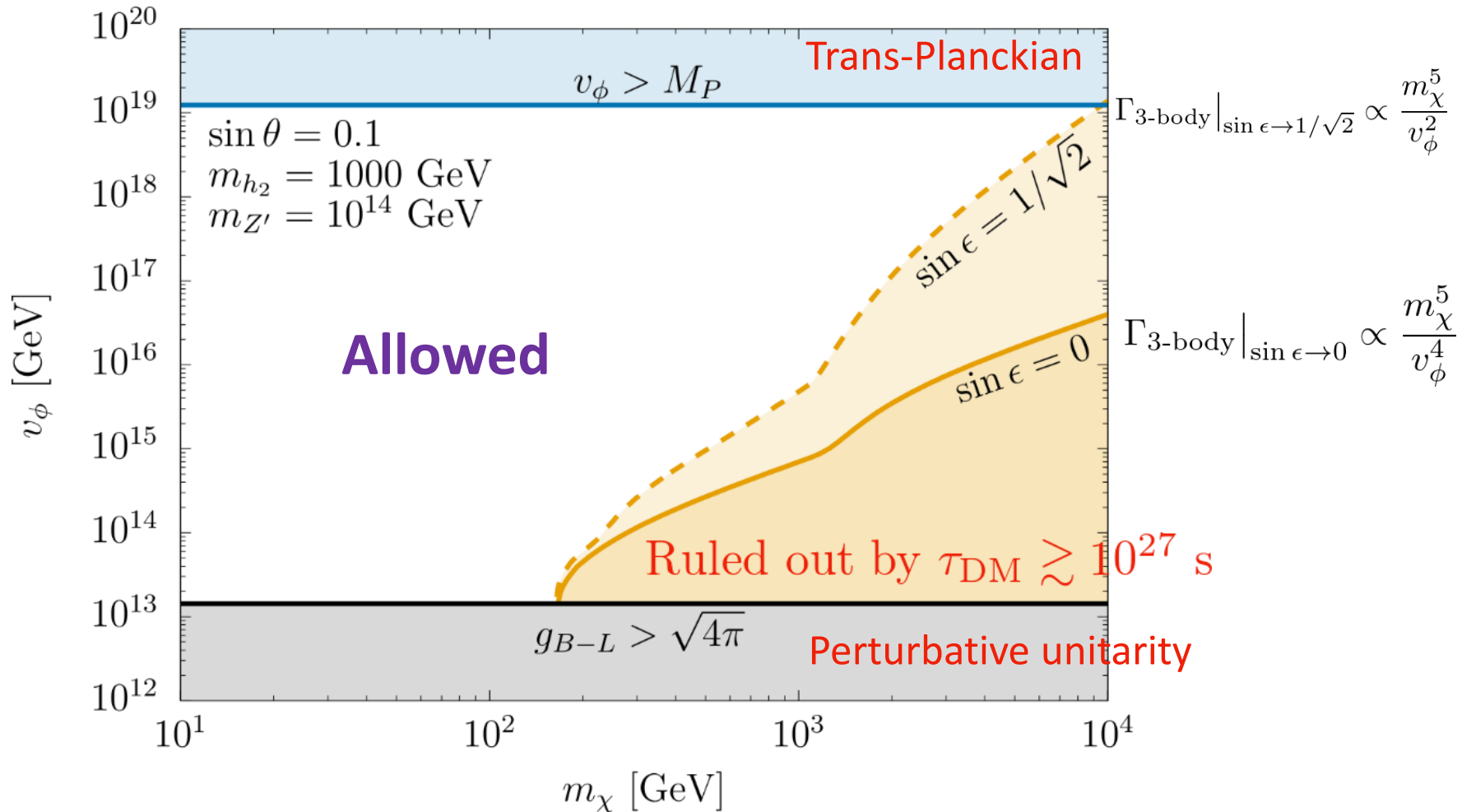
$$\sin \epsilon = 0 \text{ or } \frac{1}{\sqrt{2}}$$

B-L gauge coupling and quartic coupling are fixed by

$$g_{B-L}^2 \approx \frac{m_{Z'}^2}{4v_\phi^2}, \quad \lambda_\Phi \approx \frac{m_{h_3}^2}{v_\phi^2}$$

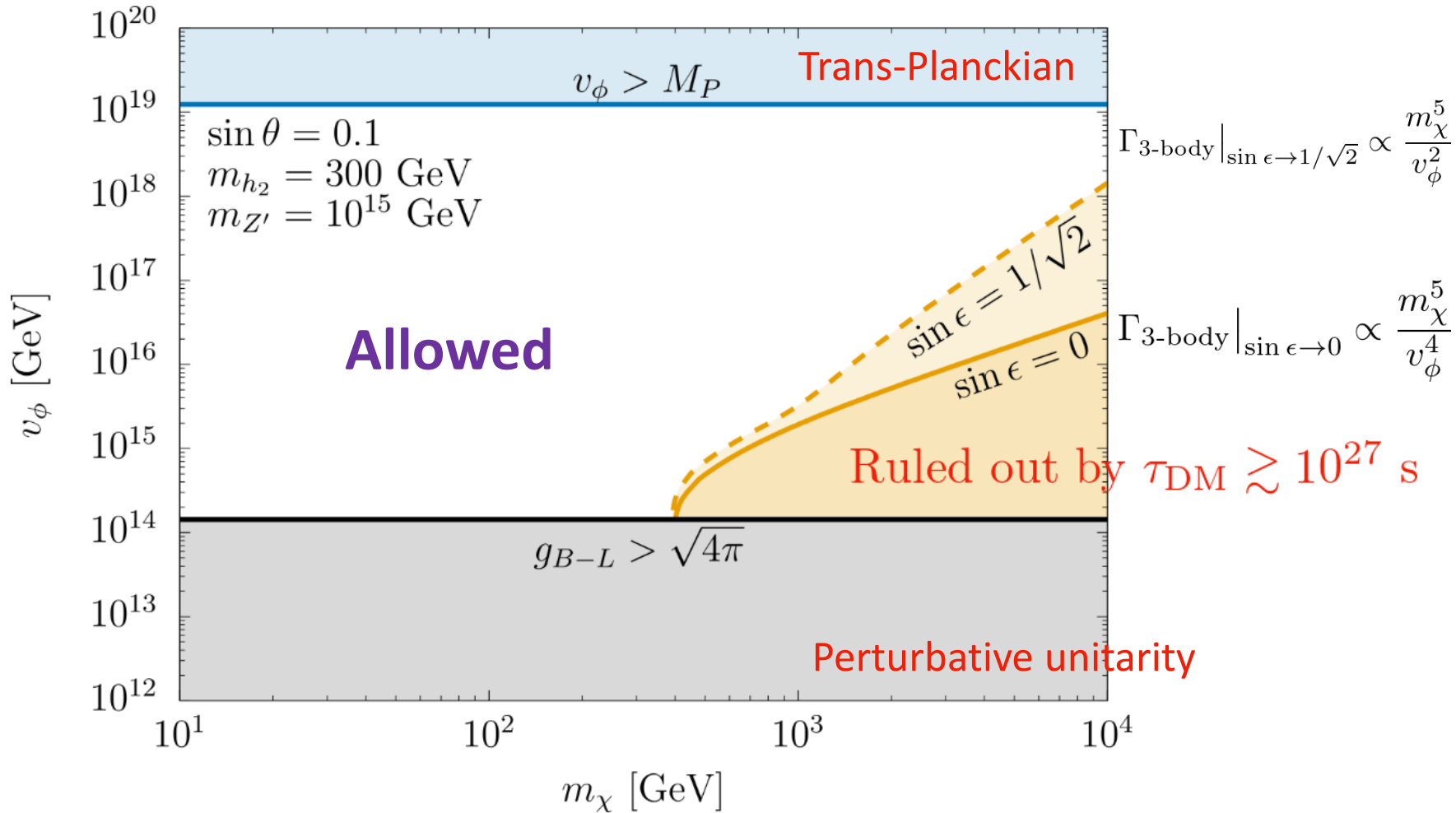
Allowed region in the (m_χ, v_ϕ) plane

$$m_{h_2} = 1000 \text{ GeV}, \quad m_{Z'} = 10^{14} \text{ GeV}$$



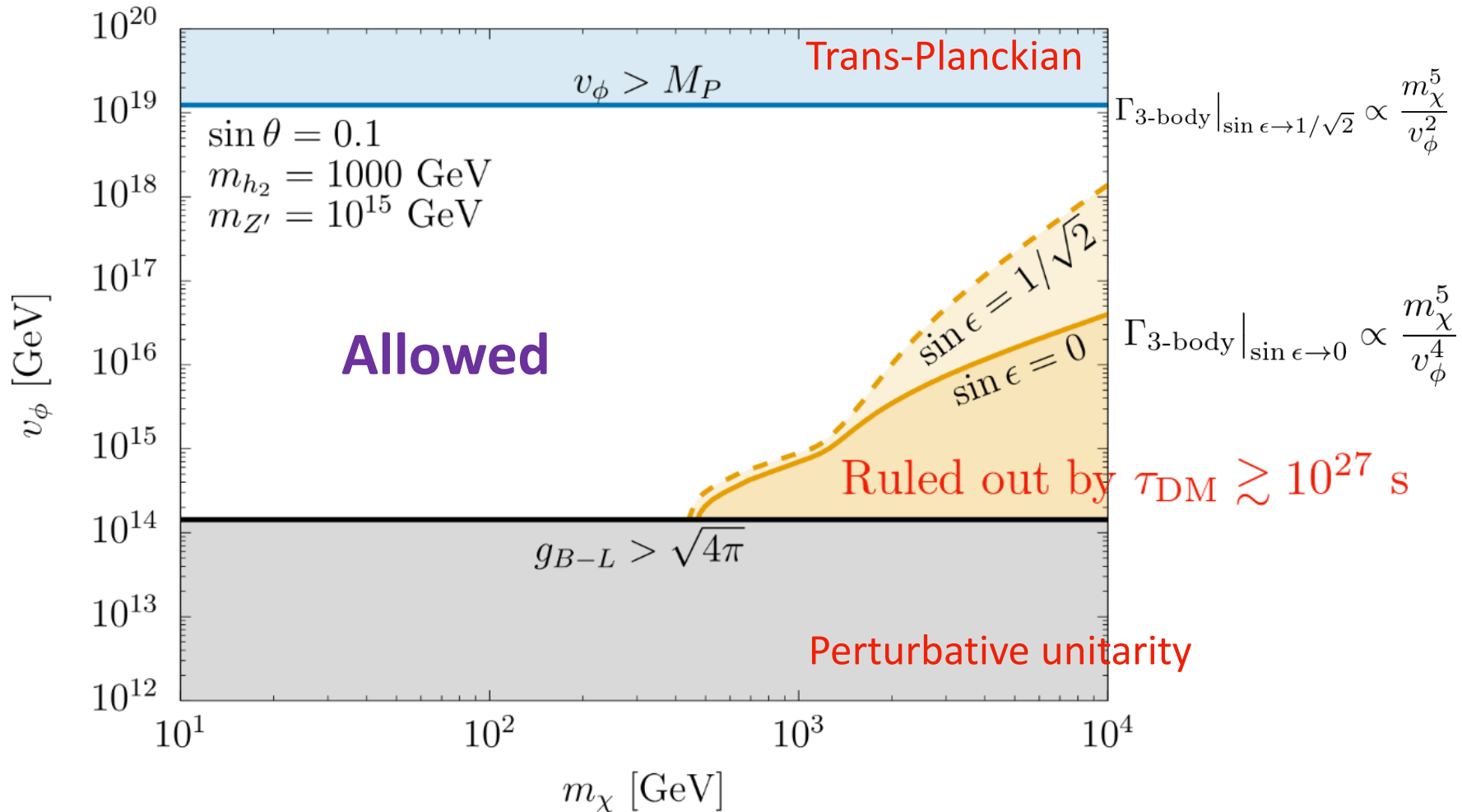
Allowed region in the (m_χ, v_ϕ) plane

$$m_{h_2} = 300 \text{ GeV}, \quad m_{Z'} = 10^{15} \text{ GeV}$$



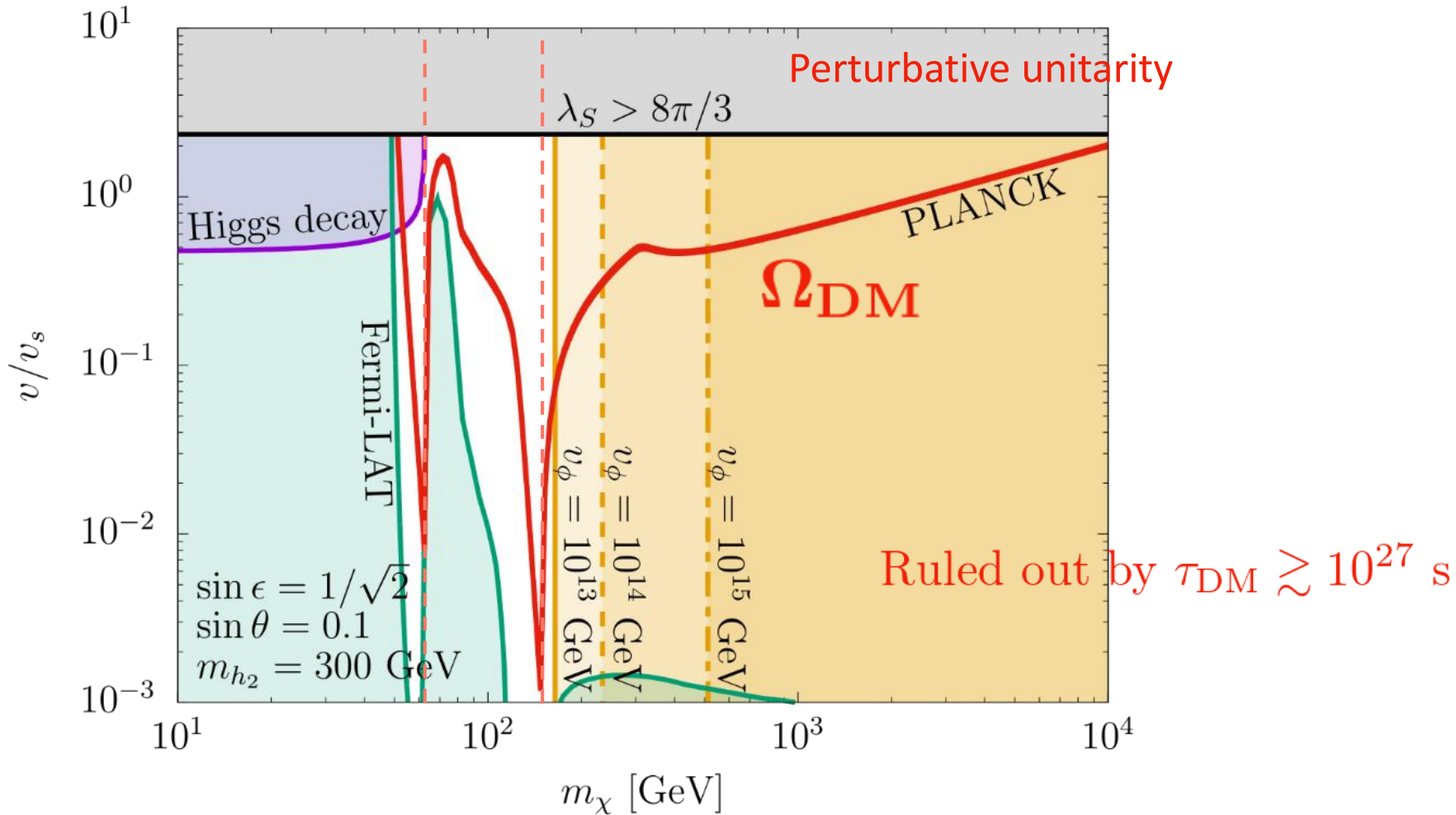
Allowed region in the (m_χ, v_ϕ) plane

$$m_{h_2} = 1000 \text{ GeV}, \quad m_{Z'} = 10^{15} \text{ GeV}$$



Allowed region in the $(m_\chi, v/v_s)$ plane

$$m_{h_2} = 300 \text{ GeV}, \quad \sin \epsilon = 1/\sqrt{2}$$



Allowed region in the $(m_\chi, v/v_s)$ plane

$$m_{h_2} = 1000 \text{ GeV}, \quad \sin \epsilon = 1/\sqrt{2}$$

