



Precision Electroweak Measurements with ILC250

Emphasis on Experimental Measurement Aspects Including \sqrt{s} , Polarization

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ILC is a unique and timely opportunity for understanding the electroweak scale

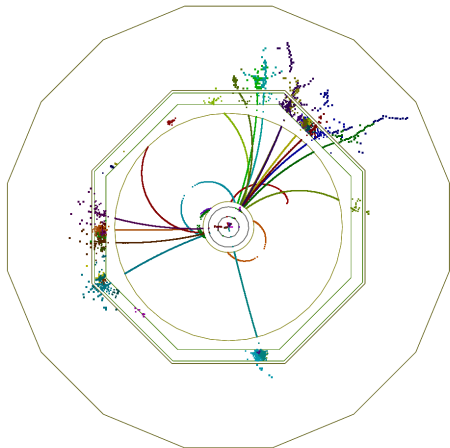
Many (physics, detector, and accelerator) opportunities to make it better!

More information on EWPO estimates - see [arXiv:1908.11299](https://arxiv.org/abs/1908.11299)

Study opportunities - see [arXiv:2007.03650](https://arxiv.org/abs/2007.03650)

Talk focus: Selected EW measurements with initial $\sqrt{s} \leq 250$ GeV stage

- 1 Physics Motivation & Remarks
- 2 ILC Accelerator and Detectors
- 3 Experimental Issues
- 4 W Mass
- 5 A_{LR}
- 6 Higher Energy
- 7 Experimental Systematics
- 8 Summary
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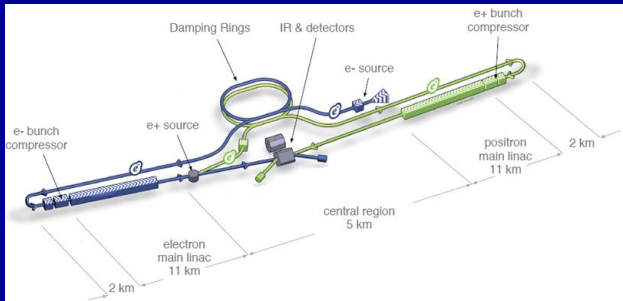


- Direct discovery of new physics would be wonderful. Many of us remain optimistic and work on such searches with LHC. e^+e^- colliders also have potential.
- Before the direct discoveries of the top quark and the Higgs boson, precision measurements of the then observable SM parameters pointed the way.
- Newer physics may continue to evade direct collider detection. Ultra-precise measurements of the fundamental SM parameters including the Higgs sector are especially compelling and can probe potentially much higher energy scales and associated new physics.
- How best to do this? The program needs to be flexible, timely, broad and probing of the underlying dynamics. Precision measurements at high energy, with full reconstruction of processes such as W^+W^- and $f\bar{f}$. But also high precision measurements of other parameters at suitable \sqrt{s} including top-threshold and Z-pole and potentially WW threshold with controlled systematics.
Polarized beams (ILC strength - 4 colliders-in-1) give essential insight.
- The physics case for a future e^+e^- collider is very well established. Let's seize this opportunity and explore the physics (preferably in our lifetime).

Linear colliders are the only practical way with e^+e^- to go significantly above the top pair threshold (synchrotron radiation and real-world economics)

- **ILC is based on superconducting RF (mature and power efficient)**
 - Under study and development for many years
 - World-wide consensus in 2001 as the next future collider
 - Fully international project with strong participation from US, Europe and Asia
 - Technology deployed in many facilities: XFEL, LCLS-II
- **ILC TDR 2013 - focus on engineered design capable of $\sqrt{s} = 200 - 500$ GeV upgradable to 1 TeV and potentially beyond**
 - longitudinally polarized electron (80%) and positron (30%) beams
 - Japan is exploring hosting the ILC as a global project
 - With the Higgs discovery - can guarantee a rich physics program
- **In recent years \rightarrow a focus on getting started as soon as possible at $\sqrt{s} = 250$ GeV while retaining energy extensibility**
 - Optimized design for $\sqrt{s} = 250$ GeV with higher luminosity
 - Now also have easily achievable running with polarized beams at lower energies including $\sqrt{s} \approx M_Z$ with $L = 4.2 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$
 - New appreciation in Japan of the longer-term opportunities with higher energy

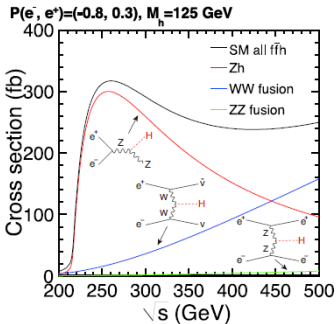
International Linear Collider Project



arXiv:1306.6327

THE INTERNATIONAL LINEAR COLLIDER

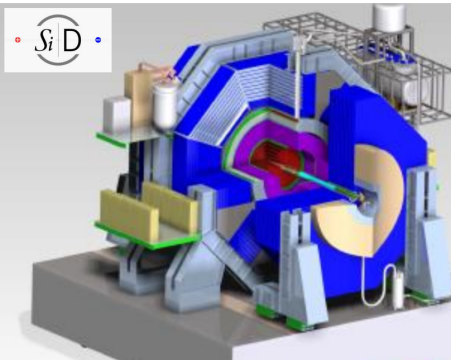
TECHNICAL DESIGN REPORT / VOLUME 1: EXECUTIVE SUMMARY



Described in arXiv:1306.6329.

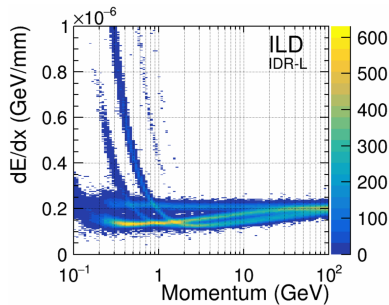
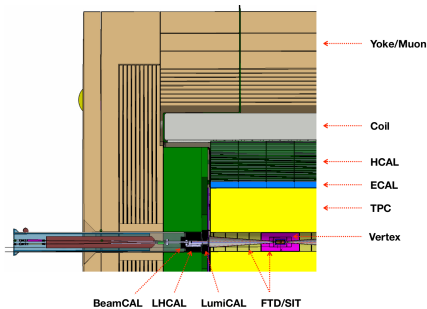
ILD = International Large Detector
(updated arXiv:2003.01116 (IDR))

SiD = Silicon Detector

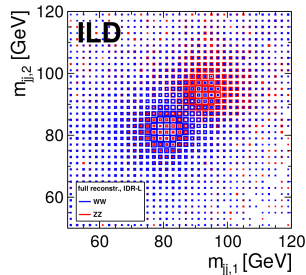
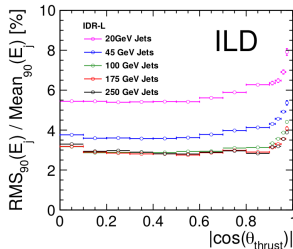
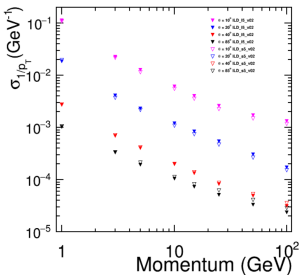


Modern detectors designed for ILC ($B=3.5-5$ T).
Particle-flow for jets. Very hermetic. Low material. Precision vertexing.
ILD centered around a TPC. SiD - all silicon tracking.

ILD Detector (See IDR and T. Tanabe talk)



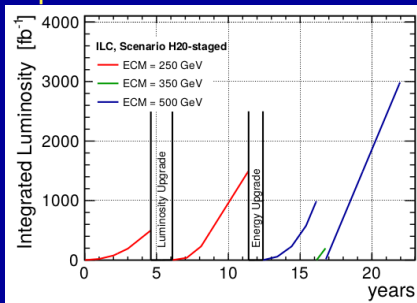
Momentum Resolution



ILC Parameters / Running Scenarios

J. Brau et al., arXiv: 1506.07830

Updated in 1903.01629



- Baseline scenario for study
- Run plan flexible - will evolve informed by future developments
- Future upgrade to 1 TeV and potentially beyond
- Options for dedicated running with polarized beams at Z-pole (100 fb^{-1}) and WW threshold (500 fb^{-1}).

\sqrt{s}	integrated luminosity with $\text{sgn}(P(e^-), P(e^+)) =$			
	(-,+)	(+,-)	(-,-)	(+,+)
	[fb^{-1}]	[fb^{-1}]	[fb^{-1}]	[fb^{-1}]
250 GeV	1350	450	100	100
350 GeV	135	45	10	10
500 GeV	1600	1600	400	400

6200 fb^{-1} total

200 fb^{-1} at $\sqrt{s} \approx 350 \text{ GeV}$

ILC Physics

- Physics studies at future e^+e^- colliders.
- Seeds were planted in the mid-80's.
- Now a vast literature.
- 3 recent publications.
 - K. Fujii et al
 - [arXiv:1506.05992](https://arxiv.org/abs/1506.05992)
 - G. Moortgat-Pick et al.,
 - [arXiv:1504.01726](https://arxiv.org/abs/1504.01726)
 - H. Baer et al,
 - [arXiv:1306.6352](https://arxiv.org/abs/1306.6352)

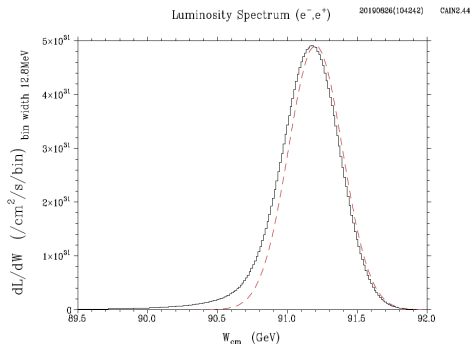
See references slide 28 containing more recent documents with consistent assumptions

Topic	Parameter	Initial Phase	Full Data Set	units
Higgs	m_h	25	15	MeV
	$g(hZZ)$	0.58	0.31	%
	$g(hWW)$	0.81	0.42	%
	$g(hb\bar{b})$	1.5	0.7	%
	$g(hgg)$	2.3	1.0	%
	$g(h\gamma\gamma)$	7.8	3.4	%
		1.2	1.0	%, w. LHC results
	$g(h\tau\tau)$	1.9	0.9	%
	$g(hc\bar{c})$	2.7	1.2	%
	$g(h\bar{t}t)$	18	6.3	%, direct
		20	20	%, $t\bar{t}$ threshold
	$g(h\mu\mu)$	20	9.2	%
	$g(hhh)$	77	27	%
	Γ_{tot}	3.8	1.8	%
	Γ_{invis}	0.54	0.29	%, 95% conf. limit
Top	m_t	50	50	MeV ($m_t(1S)$)
	Γ_t	60	60	MeV
	g_L^t	0.8	0.6	%
	g_R^t	0.8	0.6	%
	g_V^t	1.0	0.6	%
	g_A^t	2.5	1.0	%
	F_3^t	0.001	0.001	absolute
	F_2^t	0.002	0.002	absolute
W	m_W	2.8	2.4	MeV
	g_V^W	8.5×10^{-4}	6×10^{-4}	absolute
	κ_γ	9.2×10^{-4}	7×10^{-4}	absolute
	λ_γ	7×10^{-4}	2.5×10^{-4}	absolute
Dark Matter	EFT A: D5	2.3	3.0	TeV, 90% conf. limit
	EFT A: D8	2.2	2.8	TeV, 90% conf. limit

ILC running below $\sqrt{s} = 250$ GeV ?

Always foreseen as an “option” that should be justifiable by the physics du jour

- ILC TDR design focused on $\sqrt{s} > 200$ GeV
- Luminosity naturally scales with γ at a linear collider
- Now have a design that leads to $L = 4.2 \times 10^{33} \text{cm}^{-2}\text{s}^{-1}$ at $\sqrt{s} = 91$ GeV with polarized beams (see arXiv:1908.08212 by Yokoya, Kubo and Okugi [3])
- Enables a broader program of electroweak measurements
- High statistics Z samples for detector calibration and alignment, and hadronization modeling



How well can this be used?

Control systematics?

100 fb^{-1} polarized corresponds to 4.2×10^9 hadronic events and 2.0×10^8 dimuons. FWHM is about 500 MeV (beam momentum spread + beamstrahlung). Lots of fun questions to explore.

$\mu^+\mu^-/Z$ ubiquity (in \sqrt{s} scale discussion)

“ $\mu^+\mu^-$ ” or “Z” appears in many places - for varied, but related purposes.

- 1 Full energy $\mu^+\mu^-$: $e^+e^- \rightarrow \mu^+\mu^-$ with little ISR ($s' \approx s \gg M_Z^2$)
- 2 Radiative return $\mu^+\mu^-$: $e^+e^- \rightarrow \mu^+\mu^-\gamma(\gamma)$ with lots of ISR ($s \gg s' \approx M_Z^2$).
The photon(s) may or may not be detected.
- 3 Z-pole $\mu^+\mu^-$: $e^+e^- \rightarrow \mu^+\mu^-$ with \sqrt{s} near M_Z
- 4 $J/\psi \rightarrow \mu^+\mu^-$: A common source of J/ψ is from $Z \rightarrow b\bar{b}$.

Why?

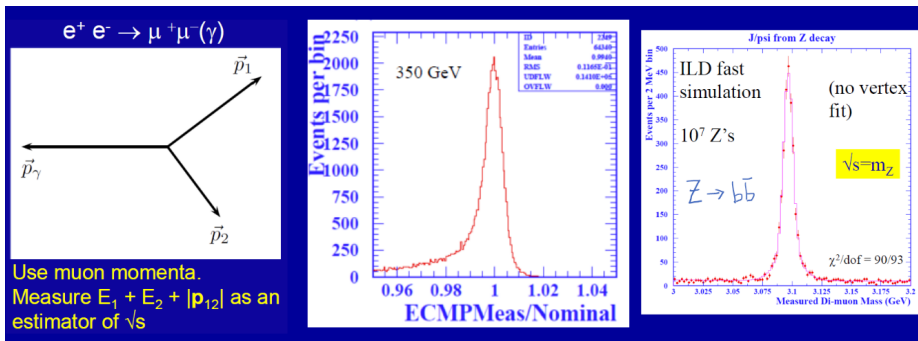
- The old method of choice for \sqrt{s} estimation at ILC was to use radiative return $\mu^+\mu^-$ and angle-based reconstruction. Robust - but suffers statistically due to Γ_Z/M_Z and relies on M_Z (23 ppm)
- New method for \sqrt{s} estimation uses all $\mu^+\mu^-$ (both full energy, intermediate energy, radiative return) to form a muon-momentum based estimator, \sqrt{s}_P .
- In turn \sqrt{s}_P needs the tracker momentum-scale to be calibrated to high precision. Principally use $J/\psi \rightarrow \mu^+\mu^-$ for this. Z running is very helpful.
- Given the 0.15% tracker momentum resolution, Z-pole $\mu^+\mu^-$, can also be used to measure \sqrt{s} for Z-pole runs (limited by 1.9 ppm $m_{J/\psi}$ knowledge).

Center-of-Mass Energy Measurement

Critical input for M_t , M_W , M_H , M_Z , M_X measurements

- 1 Standard precision of $\mathcal{O}(10^{-4})$ in \sqrt{s} for M_t straightforward
- 2 Targeting precision of $\mathcal{O}(10^{-5})$ in \sqrt{s} for M_W given likely systematics
- 3 For M_Z - helps to do even better

Use muon momenta method. Tie p to the J/ψ mass scale (1.9 ppm uncertainty).



Measure $\langle \sqrt{s} \rangle$ and lumi. spectrum simultaneously. Expect statistical uncertainty of 1.0 ppm on p-scale per 1200k $J/\psi \rightarrow \mu^+ \mu^-$ (4×10^9 hadronic Z's).

Momentum Scale Calibration (essential for \sqrt{s})

Most obvious is to use $J/\psi \rightarrow \mu^+ \mu^-$. But event rate is limited.

Particle	n_{Zhad}	Decay	BR (%)	$n_{\text{Zhad}} \cdot \text{BR}$	Γ/M	PDG ($\Delta M/M$)
J/ψ	0.0052	$\mu^+ \mu^-$	5.93	0.00031	3.0×10^{-5}	1.9 $\times 10^{-6}$
K_S^0	1.02	$\pi^+ \pi^-$	69.2	0.71	1.5×10^{-14}	2.6×10^{-5}
Λ	0.39	$\pi^- p$	63.9	0.25	2.2×10^{-15}	5.4×10^{-6}
D^0	0.45	$K^- \pi^+$	3.88	0.0175	8.6×10^{-13}	2.7×10^{-5}
K^+	2.05	various	-	-	1.1×10^{-16}	3.2×10^{-5}
π^+	17.0	$\mu^+ \nu_\mu$	100	-	1.8×10^{-16}	2.5×10^{-6}

Candidate particles for momentum scale calibration and abundances in Z decay

Sensitivity of mass-measurement to p -scale (α) depends on daughter masses and decay

$$m_{12}^2 = m_1^2 + m_2^2 + 2p_1 p_2 [(\beta_1 \beta_2)^{-1} - \cos \psi_{12}]$$

Particle	Decay	$\langle \alpha \rangle$	max α	σ_M/M	$\Delta p/p$ (10 MZ)	$\Delta p/p$ (GZ)	PDG limit
J/ψ	$\mu^+ \mu^-$	0.99	0.995	7.4×10^{-4}	13 ppm	1.3 ppm	1.9 ppm
K_S^0	$\pi^+ \pi^-$	0.55	0.685	1.7×10^{-3}	1.2 ppm	0.12 ppm	38 ppm
Λ	$\pi^- p$	0.044	0.067	2.6×10^{-4}	3.7 ppm	0.37 ppm	80 ppm
D^0	$K^- \pi^+$	0.77	0.885	7.6×10^{-4}	2.4 ppm	0.24 ppm	30 ppm

Estimated momentum scale statistical errors ($p_X = 20$ GeV)

Use of J/ψ would decouple \sqrt{s} determination from M_Z knowledge.

Opens up improved M_Z and Γ_Z measurements. (B-field map, alignment, material etc.)

Longitudinally Polarized Beams

ILC baseline design has e^- polarized to 80%, e^+ to 30%

- $P_{e^-} = 90\%$ is not out of the question
- $P_{e^+} = 60\%$ is under study, would add significant value, and may be feasible

In contrast to circular colliders, longitudinal polarization is easier and not expected to cost luminosity.

$$\sigma(P_{e^-}, P_{e^+}) = \frac{1}{4} \{ (1 - P_{e^-})(1 + P_{e^+})\sigma_{LR} + (1 + P_{e^-})(1 - P_{e^+})\sigma_{RL} + (1 - P_{e^-})(1 - P_{e^+})\sigma_{LL} + (1 + P_{e^-})(1 + P_{e^+})\sigma_{RR} \}$$

where σ_k ($k = LR, RL, LL$ and RR) are the fully polarized cross-sections.

With both beams polarized it is **straightforward** to measure the absolute polarization of both beams *in situ* when $\sigma_{LL} = \sigma_{RR} = 0$ (such as γ/Z exchange). Using 4 cross-section measurements from the $(-, +, -, +)$ helicity combinations, solve for 4 unknowns $(\sigma_U, A_{LR}, P_{e^-}, P_{e^+})$. Assumes same $|P|$ for $+$ and $-$ helicity of same beam. Need to dedicate some \mathcal{L} to “un-interesting” $(--, ++)$ configurations.

Supplement with polarimeters to track relative polarization changes.
(Also can use W^+W^- etc at high \sqrt{s})

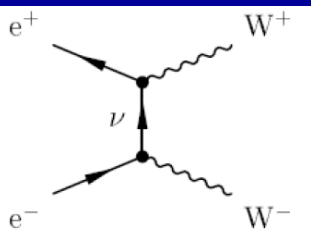
M_W is an experimental challenge. Especially so for hadron colliders.

The four most promising approaches to measure M_W at an e^+e^- collider are:

- 1 **Polarized Threshold Scan** Measurement of the W^+W^- **cross-section** near **threshold** with longitudinally **polarized** beams. Unique ILC potential.
- 2 **Constrained Reconstruction** Kinematically-constrained reconstruction of W^+W^- using constraints from **four-momentum conservation** and optionally mass-equality as was done at LEP2.
- 3 **Hadronic Mass** Direct measurement of the **hadronic mass**. This can be applied particularly to single-W events decaying hadronically or to the hadronic system in semi-leptonic W^+W^- events.
- 4 **Leptonic Observables** Use lepton **endpoints** in semi-leptonic and fully leptonic W^+W^- events with either $W \rightarrow e\nu_e$ or $W \rightarrow \mu\nu_\mu$. Use **pseudomasses** in dileptons.

Method 1 needs dedicated running near $\sqrt{s} = 161$ GeV. Methods 2, 3, and 4 can exploit the standard $\sqrt{s} \geq 250$ GeV ILC program ([deserve more study](#)). Methods 1, 2, and 4 rely on \sqrt{s} scale systematic control. Target 2 MeV uncertainty on M_W .

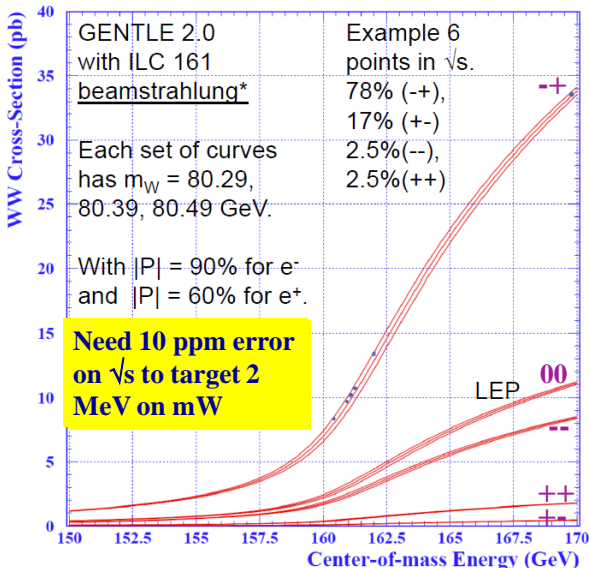
ILC Polarized Threshold Scan



Use (-+) helicity combination of e^- and e^+ to enhance WW .

Use (+-) helicity to suppress WW and measure background.

Use (--) and (++) to control polarization (also use 150 pb Z-like events)



Experimentally very robust. Measure pol., bkg. in situ

Results from updated ILC study (arXiv:1603.06016)

Fit parameter	Value	Error
m_W (MeV)	80,388	3.77
f_l	1.0002	0.924×10^{-3}
ε (l ν l ν)	1.0004	0.969×10^{-3}
ε (qq ν)	0.99980	0.929×10^{-3}
ε (qqqq)	1.0000	0.942×10^{-3}
σ_B (l ν l ν) (fb)	10.28	0.92
σ_B (qq ν) (fb)	40.48	2.26
σ_B (qqqq) (fb)	196.37	3.62
A_{LR}^B (l ν l ν)	0.15637	0.0247
A_{LR}^B (qq ν)	0.29841	0.0119
A_{LR}^B (qqqq)	0.48012	4.72×10^{-3}
$ P(e^-) $	0.89925	1.27×10^{-3}
$ P(e^+) $	0.60077	9.41×10^{-4}
σ_Z (pb)	149.93	0.052
A_{LR}^Z	0.19062	2.89×10^{-4}

6-point (90%, 60%) scan with 100 fb^{-1}

← **Example fit**

$ P(e^-) $	$ P(e^+) $	100 fb^{-1}	500 fb^{-1}
80 %	30 %	6.02	2.88
90 %	30 %	5.24	2.60
80 %	60 %	4.05	2.21
90 %	60 %	3.77	2.12

Total M_W experimental uncertainty (MeV)

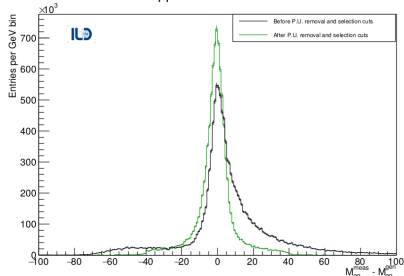
With 10 ppm assumed uncertainty on \sqrt{s} near WW threshold, additional contribution of 0.8 MeV on M_W

Fit essentially includes experimental systematics. Main one - **background** determination.

$$\Delta M_W (\text{MeV}) = 2.4 (\text{stat}) \oplus 3.1 (\text{syst}) \oplus 0.8 (\sqrt{s}) \oplus \text{theory}$$

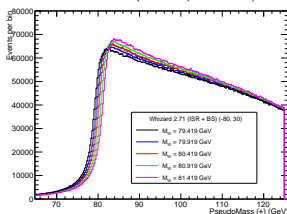
M_W , Γ_W from higher energy runs

W → qq Gen. Mass Difference

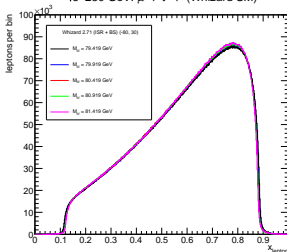


$W^+W^- \rightarrow q\bar{q}\ell\nu$ ($\ell = e, \mu, \tau$) study (J. Anguiano (KU)), using **hadronic mass**.
Statistical sensitivity of 2.4 MeV on M_W for 1.6 ab^{-1} (-80%, +30%) at $\sqrt{s} = 500 \text{ GeV}$ based on full simulation including overlay. Can be improved, but m_{had} -only measurement will likely be limited by systematics like JES. Expect improvements with **constrained fit** and $\sqrt{s} = 250 \text{ GeV}$ data set.

$\sqrt{s}=250 \text{ GeV. } \mu^+ \nu \tau^+ \nu$ (Whizard SM)



$\sqrt{s}=250 \text{ GeV. } \mu^+ \nu \tau^+ \nu$ (Whizard SM)



Di-lepton
pseudomass
 and lepton
endpoint
 distributions.
Plots to be cleaned up ...

Sensitive to M_W .

Stat. uncertainty of 4.4 MeV on M_W for 2.0 ab^{-1} (45,45,5,5) at $\sqrt{s} = 250 \text{ GeV}$. **Leptonic observables** (shape-only), x_ℓ , M_+ , M_- (GWW) Exptl. systematics should be small.

Polarization Observables

At a polarized e^+e^- collider, A_e is given by the left-right asymmetry in the total rate for Z production,

$$A_e = A_{LR} \equiv \frac{\sigma_L - \sigma_R}{(\sigma_L + \sigma_R)},$$

where σ_L and σ_R are the cross section for 100% polarized $e_L^- e_R^+$ and $e_R^- e_L^+$ initial states. For other asymmetries, beam polarization can also play a role. These quantities are measured from the left-right forward-backward asymmetry

$$A_{FB,LR}^f \equiv \frac{(\sigma_F - \sigma_B)_L - (\sigma_F - \sigma_B)_R}{(\sigma_F + \sigma_B)_L + (\sigma_F + \sigma_B)_R},$$

where, again, L and R refer to states of 100% polarization. At the tree level,

$$A_{FB,LR}^f = \frac{3}{4} A_f.$$

For unpolarized/polarized collider, the A_f values can again be obtained from quantities such as the forward-backward asymmetry using charge-identified fermion $\frac{d\sigma}{d\cos\theta}$

$$A_{FB}^f \equiv \frac{(\sigma_F - \sigma_B)}{(\sigma_F + \sigma_B)} = \frac{[(\sigma_F)_L + (\sigma_F)_R] - [(\sigma_B)_L + (\sigma_B)_R]}{[(\sigma_F)_L + (\sigma_F)_R] + [(\sigma_B)_L + (\sigma_B)_R]} = \frac{3}{4} A_e A_f,$$

Studied initially by K. Mönig 1999

For $Z \rightarrow f\bar{f}$, general cross-section formula simplifies to

$$\sigma = \sigma_u[1 - P^+P^- + A_{LR}(P^+ - P^-)]$$

With four combinations of helicities, 4 equations in 4 unknowns. Can solve for A_{LR} in terms of the four measured cross-sections (assumes helicity reversal for each beam maintains identical absolute polarization).

$$\begin{aligned}\sigma_{++} &= \sigma_u[1 - P^+P^- + A_{LR}(P^+ - P^-)] \\ \sigma_{-+} &= \sigma_u[1 + P^+P^- + A_{LR}(-P^+ - P^-)] \\ \sigma_{+-} &= \sigma_u[1 + P^+P^- + A_{LR}(P^+ + P^-)] \\ \sigma_{--} &= \sigma_u[1 - P^+P^- + A_{LR}(-P^+ + P^-)]\end{aligned}$$

For $P^- = 0.8$, $P^+ = 0.6$, $f_{SS} = 0.08$, $\sigma_U^{vis} = 33$ nb:

$$\Delta A_{LR}(\text{stat}) = 1.7 \times 10^{-5} / \sqrt{L(100 \text{ fb}^{-1})}$$

Statistical Systematics

Source		Multiplicative Factor
Bhabha Statistics	relative L ($\sigma_{\text{Bhabha}} = 250 \text{ nb}$)	1.09
Compton Statistics	relative P of opposite helicity	1.34

Center-of-mass Energy

$dA_{LR}/d\sqrt{s} = 2.0 \times 10^{-2} \text{ GeV}^{-1}$. 5 ppm (see next slide) on $\sqrt{s} \Rightarrow 0.9 \times 10^{-5}$ on A_{LR}

Beamstrahlung

Depends on machine. Previous study (TESLA) estimated a change in A_{LR} of 9×10^{-4} . Assume known to 1% $\Rightarrow 0.9 \times 10^{-5}$ on A_{LR}

$$\Delta A_{LR}(10^{-5}) = 2.4/\sqrt{L(100 \text{ fb}^{-1})} (\text{stat}) \oplus 0.9(\sqrt{s}) \oplus 0.9(\text{BS})$$

Can target experimental precision on A_{LR} of 3×10^{-5} with 100 fb^{-1} . Oft-cited 10^{-4} prospect (1.3×10^{-5} on $\sin^2 \theta_{\text{eff}}^\ell$) with 30 fb^{-1} well within reach (it was conservative). Note that $\sin^2 \theta_{\text{eff}}^\ell$ interpretation depends amongst others on improved knowledge of $\Delta\alpha_{\text{had}}$.

Polarized Observables with Radiative Return Events

See 1908.11299 for details. Use jet polar angles to infer longitudinal boost, β .

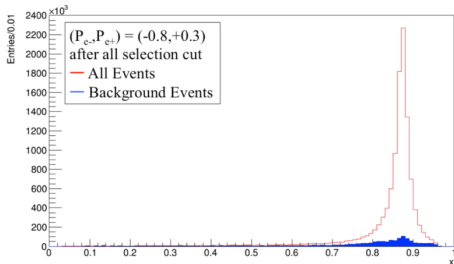


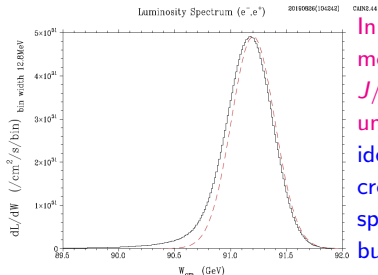
Figure 2: Reconstructed distribution of $x \equiv \frac{2|\beta|}{1+|\beta|}$ for the signal $e^+e^- \rightarrow \gamma Z, Z \rightarrow q\bar{q}$ and from background events that mimic this signal, at $\sqrt{s} = 250$ GeV with an integrated luminosity of 250 fb^{-1} .

Study indicates statistical uncertainty on A_e of 14×10^{-5} with full 2 ab^{-1} of ILC250 running.

Very different systematics to Z-pole based A_{LR} measurement and accessible with data collected synergistically with Higgs production. Nevertheless, Z-pole running precision expected to be superior.

Center-of-mass Energy Calibration around the Z-Pole

Expected lumi. spectrum at the Z, has a FWHM of about 500 MeV ($\sigma \approx 215$ MeV). Tracker momentum resolution per muon is 0.15% (88 MeV on \sqrt{s}). Leads to an average stat. uncertainty per di-muon event of ≈ 230 MeV. So one can measure the average \sqrt{s} with a stat. uncertainty of 0.18 ppm with the $100 \text{ fb}^{-1} A_{LR}$ optimized run at M_Z ($2 \times 10^8 e^+e^- \rightarrow Z \rightarrow \mu^+\mu^-$).

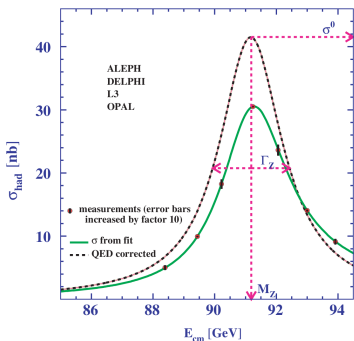


In the same data taking, one can measure the tracker momentum scale with 1.0 ppm stat. uncertainty using $J/\psi \rightarrow \mu^+\mu^-$, more than saturating the 1.9 ppm syst. uncertainty from the known J/ψ mass. Note that the idea is to collect Z events and use these to measure cross sections & asymmetries, C-o-M energy/lumi spectrum and p -scale simultaneously. Potentially even bunch-by-bunch under the exact same conditions.

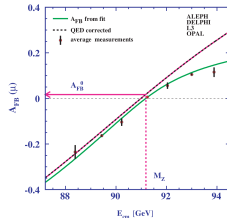
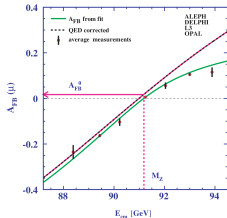
With an overall momentum scale uncertainty target at the 2.5 ppm level (earlier assumption of 10 ppm was sufficient for the M_W target) potentially within reach, one should seek to improve on the current 23 ppm uncertainty on M_Z . Uncertainties on M_Z as low as 230 keV are presumably thinkable (2.5 ppm).

Polarized Beams Z Scan for Z LineShape and Asymmetries

Essentially, redo LEP-style measurements in all channels but also with \sqrt{s} dependence of the polarized asymmetries, A_{LR} and $A_{FB,LR}^f$, in addition to A_{FB} .



LEP: $\Delta M_Z = 2.1$ MeV, $\Delta \Gamma_Z = 2.3$ MeV



With unoptimized, 100 fb^{-1} polarized 5-point scan, $(0, \pm 1, \pm 2)$ GeV around M_Z , **statistical** uncertainties on M_Z of 40 keV and Γ_Z of 90 keV from LEP-style fit to $(M_Z, \Gamma_Z, \sigma_{\text{had}}^0, R_e^0, R_\mu^0, R_\tau^0)$ using ZFITTER 6.42 for QED convolution.

Exploiting this needs in-depth study of \sqrt{s} calibration systematics + maybe improved energy-spread. **ILC \mathcal{L} is sufficient for M_Z .** Γ_Z systematic uncertainty depends on $(\sqrt{s}_+ - \sqrt{s}_-)$ uncertainty rather than absolute \sqrt{s} scale, so expect $\Delta \Gamma_Z < \Delta M_Z$.

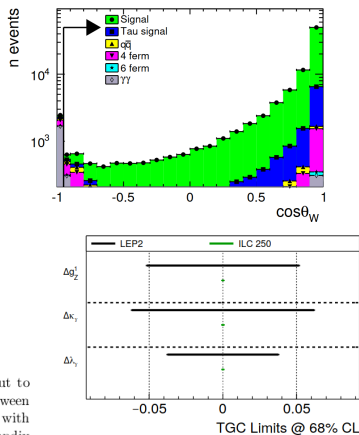
Higher Energy: Triple Gauge Couplings ($WW\gamma$, WWZ)

Many 4f processes besides W^+W^- . “Single- W ” processes, $e^+e^- \rightarrow W e \nu_e$, very important. Can disentangle the beam polarizations, P_{e^-} and P_{e^+} , and constrain residual imperfect spin-flip, using such processes where σ_{LL} or $\sigma_{RR} \neq 0$.

	250 GeV W^+W^-	350 GeV W^+W^-	500 GeV W^+W^-	1000 GeV W^+W^-
g_{1Z}	0.062	0.033	0.025	0.0088
κ_A	0.096	0.049	0.034	0.011
λ_A	0.077	0.047	0.037	0.0090
$\rho(g_{1Z}, \kappa_A)$	63.4	63.4	63.4	63.4
$\rho(g_{1Z}, \lambda_A)$	47.7	47.7	47.7	47.7
$\rho(\kappa_A, \lambda_A)$	35.4	35.4	35.4	35.4

Table 13: Projected statistical errors, in %, for $e^+e^- \rightarrow W^+W^-$ measurements input to our fits. The errors are quoted for luminosity samples of 500 fb^{-1} divided equally between beams with -80% electron polarisation and +30% positron polarisation and beams with +80% electron polarisation and -30% positron polarisation. Please see the text of Appendix B for further explanation of this table.

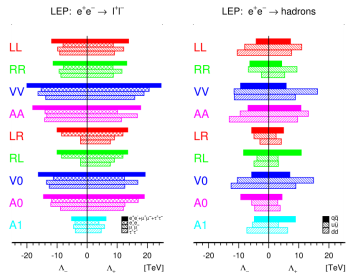
3-parameter fits based on full simulation studies and their extrapolation with ILD. **Clearly higher energy is better especially given the γ scaling of luminosity.** Already with ILC250 (2 ab^{-1}), expect 0.05% precision, compared to 5% precision for a LEP2 experiment. No comparable hadron collider results available. See thesis by Robert Karl (DESY) with work on a multi-channel global fit including correlations.



Two-Fermions and Four-Fermion Contact Interactions

See LEP2 studies with cross-sections and A_{FB} / (ILC adds $A_{LR}, A_{FB,LR}^f$)

$$\mathcal{L}_{\text{eff}} = \frac{g^2}{(1 + \delta)\Lambda_{\pm}^2} \sum_{i,j=L,R} \eta_{ij} \bar{e}_i \gamma_{\mu} e_i \bar{f}_j \gamma^{\mu} f_j,$$



LEP2

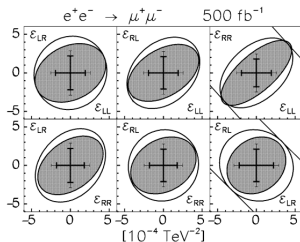


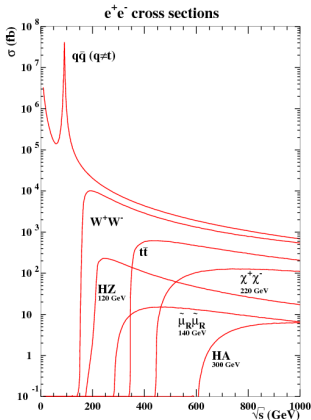
Fig. 1. Two-dimensional projections of the 95% C.L. allowed region (27) for $e^+e^- \rightarrow \mu^+\mu^-$ at $\mathcal{L}_{\text{int}} = 50 \text{ fb}^{-1}$ and $\mathcal{L}_{\text{int}} = 500 \text{ fb}^{-1}$. Note that the scales are different. $|P_e| = 0.8$, $|P_e^{\text{int}}| = 0.0$ (outer ellipse) and $|P_e^{\text{int}}| = 0.6$ (inner ellipse). The solid crosses represent the 'one-parameter' bounds under the same conditions.

At ILC, can follow a more model independent approach. Example Ref. 2. Polarization gives access to full 4-parameter space (LR,RL,LL,RR).

Current ILC projections - see arXiv:1908.11299 extend to 151 to 478 TeV for Λ in various models (driven by 8 ab^{-1} at 1 TeV).

Detector Calibration and Alignment

Clean e^+e^- environment. But particle-based calibration at high \sqrt{s} has



Challenges

- cross-sections
- duty-cycle (power-pulsing)
- “push-pull”
- seismic tolerance
- thermal issues
- unprecedented precision goals

Part of the solution

Accelerator capable of “calibration runs” at the Z with reasonable luminosity. Z running is the most statistically effective way to calibrate the detector. May be essential to fully exploiting the ILC at all \sqrt{s} . Design this capability in!

Now done!

- ILC can advance greatly our knowledge of electroweak precision physics.
- Polarized electron and **positron** beams are a unique asset.
- Can deliver much more rigorous test of the SM which explores new physics. Highlighted by top mass measurement and

$$\Delta M_W = 2 - 3 \text{ MeV}$$

$$\Delta A_{LR}(10^{-5}) = 2.4/\sqrt{L(100 \text{ fb}^{-1})} (\text{stat}) \oplus 0.9 (\sqrt{s}) \oplus 0.9(\text{BS})$$

- Scope for best M_W measurements from standard ILC running.
- Experimental strategies for controlling systematics associated with \sqrt{s} , polarization, luminosity spectrum are worked out.
- Momentum scale is a key. Enabled by precision low material tracker. Promises to also open up precision measurement advances for M_Z , Γ_Z , etc
- More study on expt./acc. systematics + tracker design work necessary.
- An accelerator is needed! On-going very encouraging developments in Japan.
- The physics discussed here benefits greatly given that the accelerator is now designed to include efficient running at lower \sqrt{s} .

- [1] K. Fujii *et al.* [LCC Physics Working Group], Tests of the Standard Model at the International Linear Collider arXiv:1908.11299 [hep-ex]
- [2] A. Babich, P. Osland, A. Pankov and N. Paver, New physics signatures at a linear collider: Model independent analysis from 'conventional' polarized observables, Phys. Lett. B **518**, 128-136 (2001)
- [3] K. Yokoya, K. Kubo and T. Okugi, Operation of ILC250 at the Z-pole [arXiv:1908.08212 [physics.acc-ph]].
- [4] K. Fujii *et al.* The role of positron polarization for the initial 250 GeV stage of the International Linear Collider, [arXiv:1801.02840 [hep-ph]].
- [5] P. Bambade *et al.* The International Linear Collider: A Global Project, [arXiv:1903.01629 [hep-ex]].
- [6] G. W. Wilson, Precision Electroweak Measurements at a Future e^+e^- Linear Collider, PoS **ICHEP2016**, 688 (2016)

Acknowledgments

Table of EWPO from arXiv:1908.11299

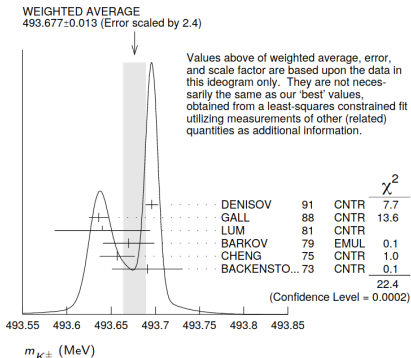
Quantity	Value	current	GigaZ		ILC250	
		$\delta[10^{-4}]$	$\delta_{stat}[10^{-4}]$	$\delta_{sys}[10^{-4}]$	$\delta_{stat}[10^{-4}]$	$\delta_{sys}[10^{-4}]$
boson properties						
m_W	80.379	1.5	-	-	-	0.3°
m_Z	91.1876	0.23	-	-	-	-
Γ_Z	2.4952	9.4	-	-	-	-
$\Gamma_Z(had)$	1.7444	11.5	-	$4.^\circ$	-	-
Z-e couplings						
$1/R_e$	0.0482	24.	2.	5^\dagger	5.5	10^+
A_e	0.1513	139.	1	$5.^\ast$	9.5	$3.^\ast$
g_L^e	-0.632	16.	1.0	3.2	2.8	7.6
g_R^e	0.551	18.	1.0	3.2	2.9	7.6
Z-ℓ couplings						
$1/R_\mu$	0.0482	16.	2.	$2.^\dagger$	5.5	10^+
$1/R_\tau$	0.0482	22.	2.	$4.^\dagger$	5.7	10^+
A_μ	0.1515	991.	2.	$5.^\ast$	54.	$3.^\ast$
A_τ	0.1515	271.	2.	$5.^\ast$	57.	$3.^\ast$
g_L^μ	-0.632	66.	1.0	2.3	4.5	7.6
g_R^μ	0.551	89.	1.0	2.3	5.5	7.6
g_L^τ	-0.632	22.	1.0	2.8	4.7	7.6
g_R^τ	0.551	27.	1.0	3.2	5.8	7.6
Z-b couplings						
R_b	0.2163	31.	0.4	$7.^\ast$	3.5	10^+
A_b	0.935	214.	1.	$5.^\ast$	5.7	$3.^\ast$
g_L^b	-0.999	54.	0.32	4.2	2.2	7.6
g_R^b	0.184	1540	7.2	36.	41.	23.
Z-c couplings						
R_c	0.1721	174.	2.	$30.^\ast$	5.8	50^+
A_c	0.668	404.	3.	$5^\ast \oplus 5^\ast$	21.	$3.^\ast$
g_L^c	0.816	119.	1.2	15.	5.1	26.
g_R^c	-0.367	416.	3.1	17.	21.	26.

Table 9: Projected precision of precision electroweak quantities expected from the ILC. Precisions are given as *relative errors* ($\delta A = \Delta A/A$) in units of 10^{-4} . Please see the text of Appendix A for further explanation of this table.

Charged Kaon Mass

A long-standing example of inconsistent precision measurements. As yet not resolved.

Citation: P.A. Zyla et al. (Particle Data Group), Prog. Theor. Exp. Phys. **2020**, 083C01 (2020)



An example of something, not so far from being fundamental with a big inconsistency. Accuracy is as important as precision. Important to measure particles with different methods if there are actually residual misunderstood systematics (examples top, W, Higgs, Z).

With ILC detectors and precision momentum-scale calibration, ILC should be able to help resolve this! This would also help lots of D, B masses etc.

Maybe worth doing a careful study of how to improve this with colliders.

Hadronization Systematics

How does a W , Z , H , t decay hadronically?

Models like PYTHIA, HERWIG etc have been tuned extensively to data. Not expected to be a complete picture.

Inclusive measurements of **identified particle rates** and **momenta spectra** are an essential ingredient to describing hadronic decays of massive particles.

ILC could provide comprehensive measurements with up to 1000 times the published LEP statistics and with a much better detector with Z running.

High statistics with W events.

Why?

Measurements based on hadronic decays, such as **hadronic mass**, **jet directions** underlie much of what we do in energy frontier experiments.

Key component of understanding jet energy scales and resolution.

Important to also understand flavor dependence: u -jets, d -jets, s -jets, c -jets, b -jets, g -jets.

Full Simulation + Kalman Filter

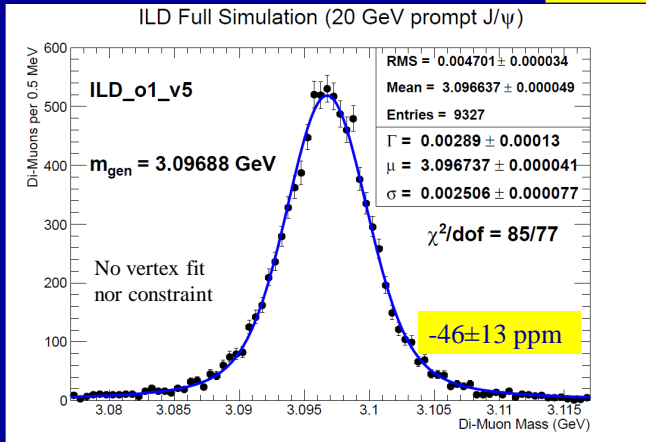
$$\sqrt{s}=m_Z$$

10k “single particle events”

Work in progress – likely need to pay attention to issues like energy loss model and FSR.

Preliminary statistical precision similar.

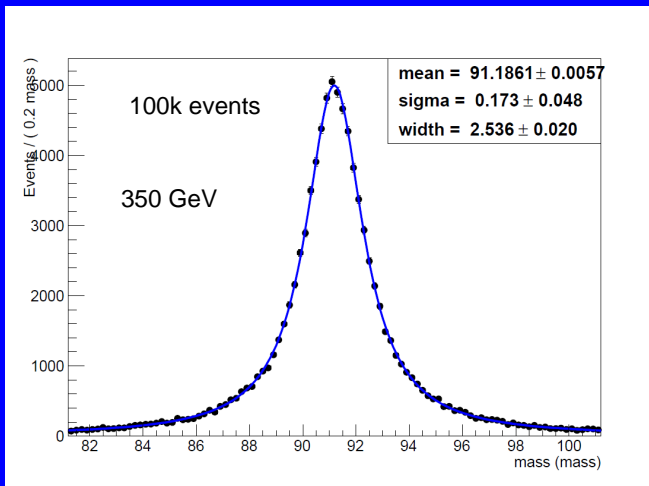
More realistic material, energy loss and multiple scattering.



Empirical Voigtian fit.

Need consistent material model in simulation AND reconstruction

Can control for p-scale using measured di-lepton mass



This is about 100 fb^{-1} at $\text{ECM}=350 \text{ GeV}$.

Statistical sensitivity if one turns this into a Z mass measurement (if p-scale is determined by other means) is

$$1.8 \text{ MeV} / \sqrt{N}$$

With N in millions.

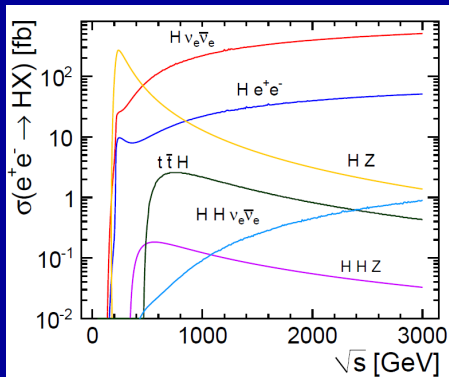
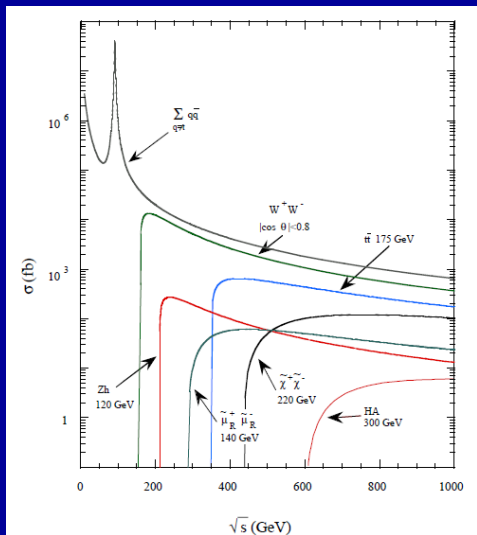
Alignment ?
B-field ?
Push-pull ?
Etc ...



Experimentation with ILC

- Physics experiments with e^+e^- colliders are **very different** from a hadron collider.
- Experiments and detectors can be **designed without the constraints** imposed by triggering, radiation damage, pileup.
- **All decay channels** can often be used (not only $H \rightarrow 4l$ etc)
- **Can adjust the initial conditions**, the beam energy, polarize the electrons and the positrons, and measure precisely the absolute integrated luminosity.
- **No trigger** needed.
- Last – but not least – **theoretical predictions** can be brought under very good control.

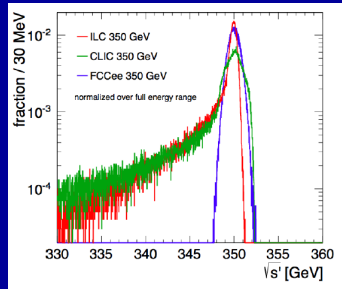
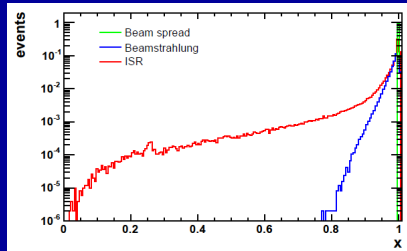
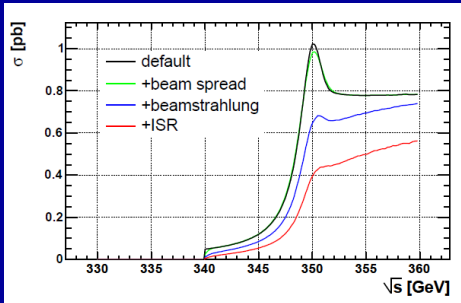
The e^+e^- Landscape



Cross-sections are typically at the pb level.

Luminosity Spectrum

- Experimentally accessible measurements are convolved with effects of ISR, beam spread and beamstrahlung



Luminosity spectrum should be controlled well at ILC (to $< 0.2\%$ differentially using Bhabhas)

m_W Prospects

1. Polarized Threshold Scan
2. Kinematic Reconstruction
3. Hadronic Mass

Method 1: Statistics limited.

Method 2: With up to 1000 the LEP statistics and much better detectors. Can target factor of 10 reduction in systematics.

Method 3: Depends on di-jet mass scale. Plenty Z's for 3 MeV.

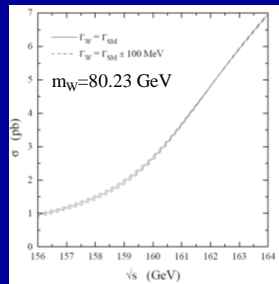
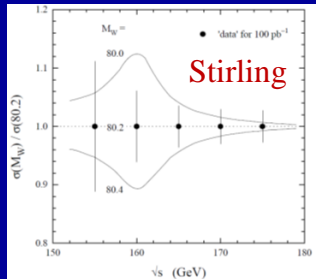
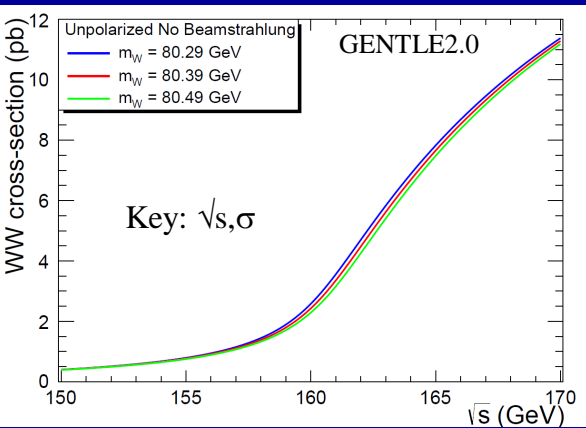
2	ΔM_W [MeV]	LEP2	ILC	ILC	ILC
	\sqrt{s} [GeV]	172-209	250	350	500
	\mathcal{L} [fb^{-1}]	3.0	500	350	1000
	$P(e^-)$ [%]	0	80	80	80
	$P(e^+)$ [%]	0	30	30	30
	beam energy	9	0.8	1.1	1.6
	luminosity spectrum	N/A	1.0	1.4	2.0
	hadronization	13	1.3	1.3	1.3
	radiative corrections	8	1.2	1.5	1.8
	detector effects	10	1.0	1.0	1.0
	other systematics	3	0.3	0.3	0.3
	total systematics	21	2.4	2.9	3.5
	statistical	30	1.5	2.1	1.8
	total	36	2.8	3.6	3.9

1	ΔM_W [MeV]	LEP2	ILC	ILC
	\sqrt{s} [GeV]	161	161	161
	\mathcal{L} [fb^{-1}]	0.040	100	480
	$P(e^-)$ [%]	0	90	90
	$P(e^+)$ [%]	0	60	60
	statistics	200	2.4	1.1
	background		2.0	0.9
	efficiency		1.2	0.9
	luminosity		1.8	1.2
	polarization		0.9	0.4
	systematics	70	3.0	1.6
	experimental total	210	3.9	1.9
	beam energy	13	0.8	0.8
	theory	-	(1.0)	(1.0)
	total	210	4.0	2.1

3	ΔM_W [MeV]	ILC	ILC	ILC	ILC
	\sqrt{s} [GeV]	250	350	500	1000
	\mathcal{L} [fb^{-1}]	500	350	1000	2000
	$P(e^-)$ [%]	80	80	80	80
	$P(e^+)$ [%]	30	30	30	30
	jet energy scale	3.0	3.0	3.0	3.0
	hadronization	1.5	1.5	1.5	1.5
	pileup	0.5	0.7	1.0	2.0
	total systematics	3.4	3.4	3.5	3.9
	statistical	1.5	1.5	1.0	0.5
	total	3.7	3.7	3.6	3.9

See Snowmass document for more details
Bottom-line: 3 different methods with prospects to measure m_W with error < 5 MeV

m_W from cross-section close to threshold



$$\sigma_t \sim \beta$$

$$\sigma_s \sim \beta^3$$

$$\Delta M_{\text{sys}}^{\text{bkgd}} = 470 \text{ MeV} \left[\frac{\Delta \sigma}{1 \text{ pb}} \right]$$

Example Polarized Threshold Scan

\sqrt{s} (GeV)	L (fb $^{-1}$)	f	$\lambda_{e^-} - \lambda_{e^+}$	N_{ll}	N_{lh}	N_{hh}	N_{RR}
160.6	4.348	0.7789	-+	2752	11279	12321	926968
		0.1704	+-	20	67	158	139932
		0.0254	++	2	19	27	6661
		0.0254	--	21	100	102	8455
161.2	21.739	0.7789	-+	16096	67610	73538	4635245
		0.1704	+-	98	354	820	697141
		0.0254	++	37	134	130	33202
		0.0254	--	145	574	622	42832
161.4	21.739	0.7789	-+	17334	72012	77991	4639495
		0.1704	+-	100	376	770	697459
		0.0254	++	28	104	133	33556
		0.0254	--	135	553	661	42979
161.6	21.739	0.7789	-+	18364	76393	82169	4636591
		0.1704	+-	81	369	803	697851
		0.0254	++	43	135	174	33271
		0.0254	--	146	618	681	42689
162.2	4.348	0.7789	-+	4159	17814	19145	927793
		0.1704	+-	16	62	173	138837
		0.0254	++	10	28	43	6633
		0.0254	--	46	135	141	8463
170.0	26.087	0.7789	-+	63621	264869	270577	5560286
		0.1704	+-	244	957	1447	838233
		0.0254	++	106	451	466	40196
		0.0254	--	508	2215	2282	50979

Illustrative example of the numbers of events in each channel for a 100 fb $^{-1}$ 6-point ILC scan with 4 helicity configurations

Kinematic Reconstruction in Fully Leptonic Events

See Appendix B of Hagiwara et al., Nucl. Phys. B. 282 (1987) 253 for full production and decay 5-angle reconstruction in fully leptonic decays as motivated by TGC analyses.

The technique applies energy and momentum conservation. One solves for the anti-neutrino 3-momentum, decomposed into its components in the dilepton plane, and out of it. Additional assumptions are:

- the energies of the two W 's are equal to E_{beam} , so $m(W^+) = m(W^-)$.
- a specified value for M_W

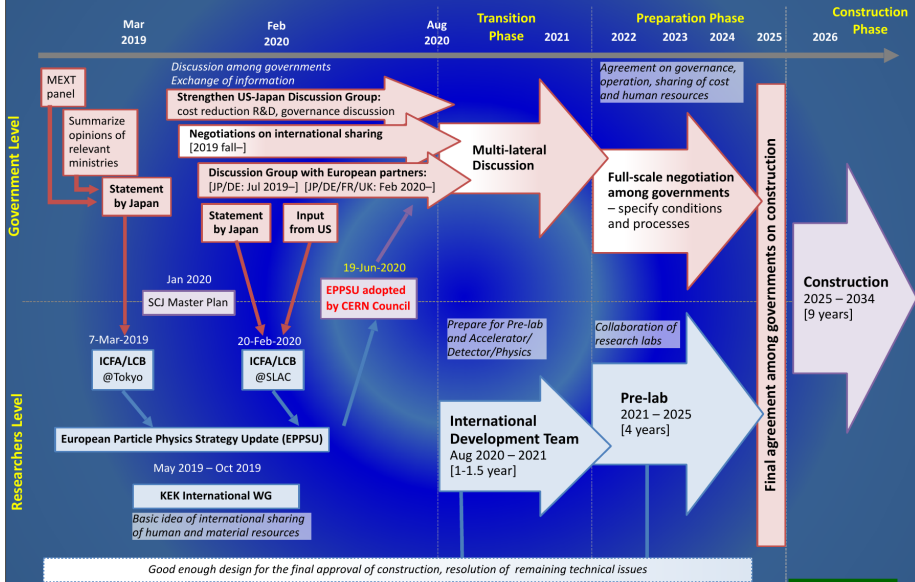
$$\vec{p}_{\bar{\nu}} = a \vec{l} + b \vec{l}' + c \vec{l} \times \vec{l}'$$

By specifying, M_W , one can find a , b and c^2 , so there are two solutions.

The alternative pseudomass technique is more appropriate for a M_W measurement. It does not assume M_W , but sets $c = 0$, similarly yielding two solutions, (a_+, b_+) and (a_-, b_-) , leading to PseudoMass(+) and PseudoMass(-) estimators per event.

ILC Project Timelines

Processes and Approximate Timelines Towards Realization of ILC



S. Yamashita