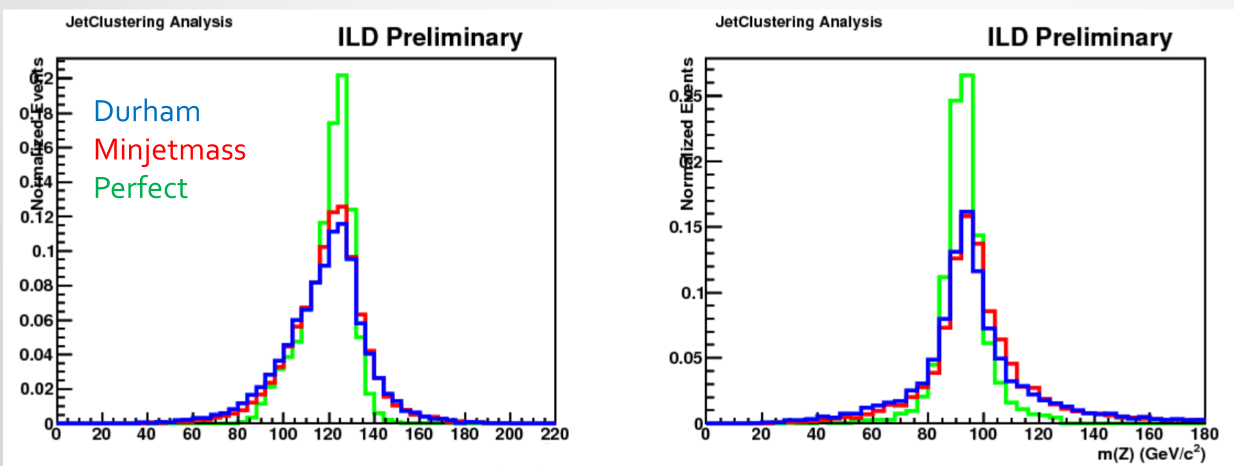
Construct
Deep Jet Clustering

Masakazu Kurata

01/20/2021

Introduction

- Jet clustering is one of the main key to obtain better physics results
  - Physics results are strongly limited by mis-clustering
  - To obtain correct jets leads to improve the mass resolution of the resonances
- Present jet clustering is far from good tool for reconstructing jets
  - e.g. Higgs self-coupling@500GeV(ZHH): ~40% improvement if perfect!

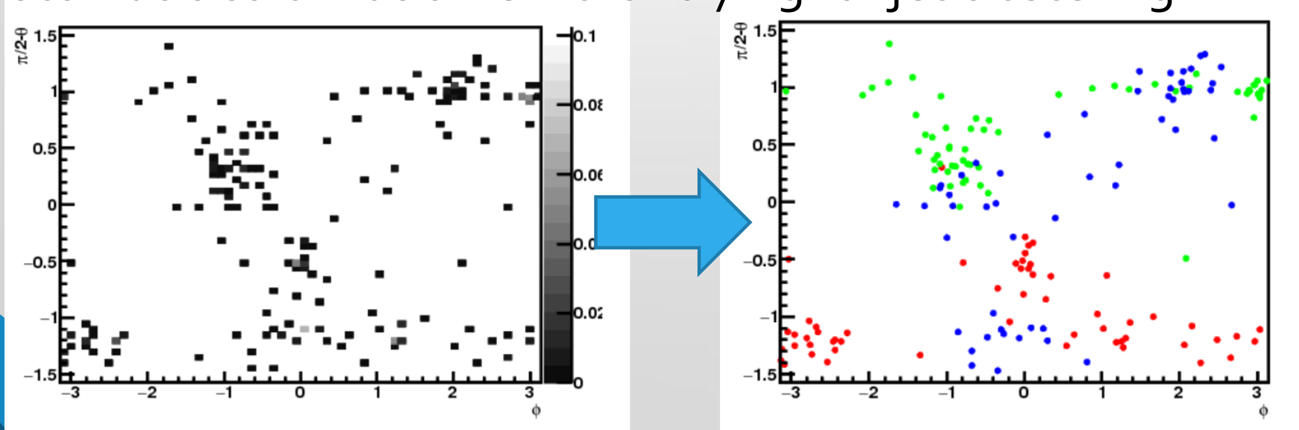


m(H)

- Even at 250GeV, clustering is very important
  - Separation of ZH/ZZ/WW in hadronic events

Use CNN for automatic colorization

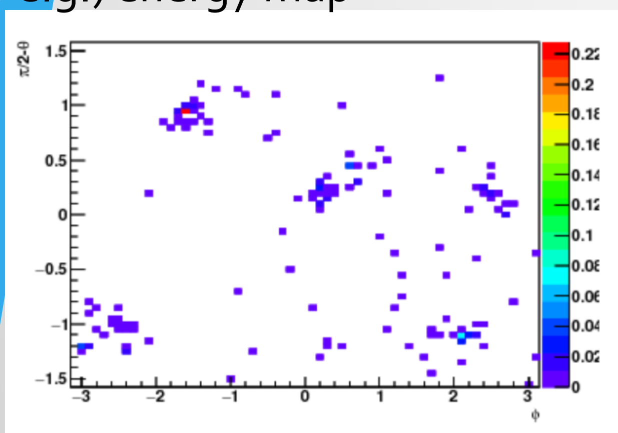
- For jet clustering, we need the global and local information for each event
  - Global: Where is the large energy located?
  - Local: Correlation between neighbors or large energy area?
- Using Convolutional Neural Network(CNN), we will extract both features
  - Encorder-Decorder type CNN is used (calls as u-network, mention later)
- Clustering is equivalent to "colorize" each particle in the same cluster
  - Grey scale ⇒ color
  - So, Automatic colorization is worth trying for jet clustering



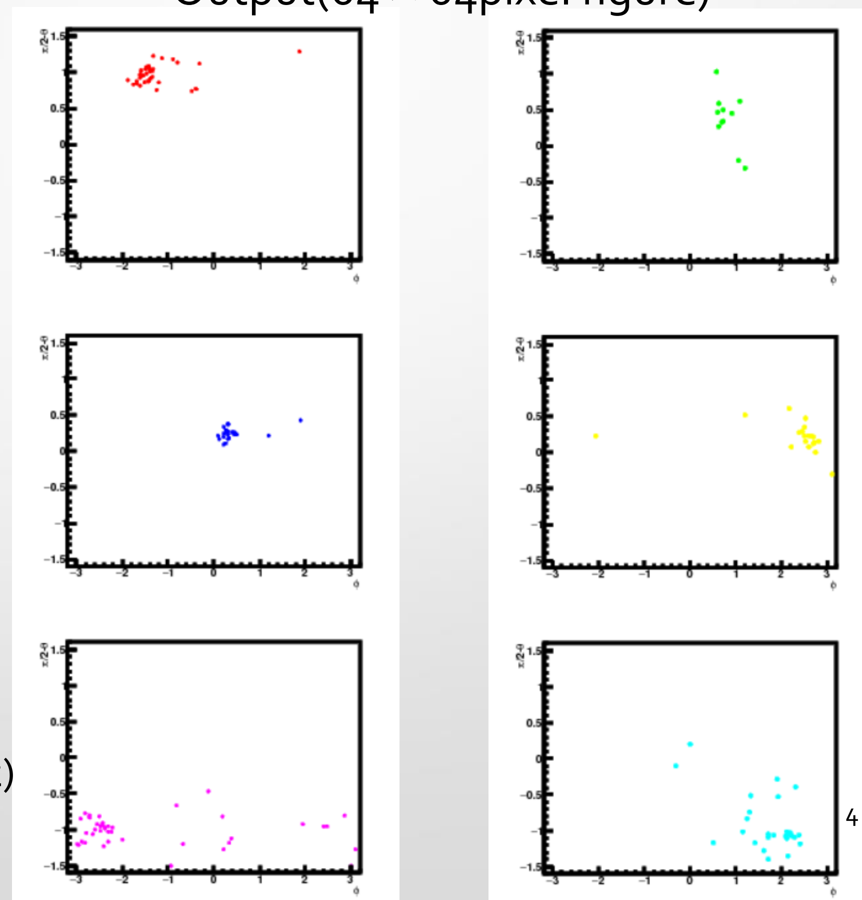
Trial

- Use Keras & tensorflow backend
- Using a certain map(s) of each event, estimate color of each track
  - Do not consider color-singlet state

Input(64×64pixel figure)
e.g.) energy map



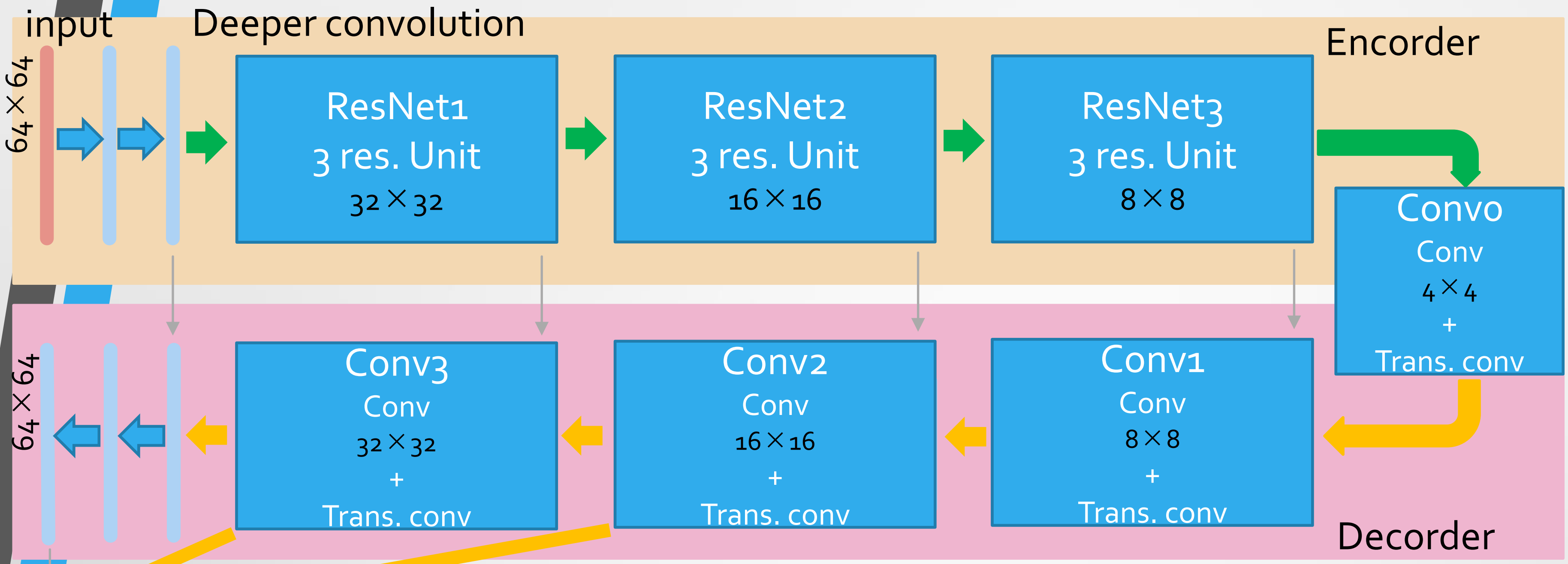
Output(64×64pixel figure)

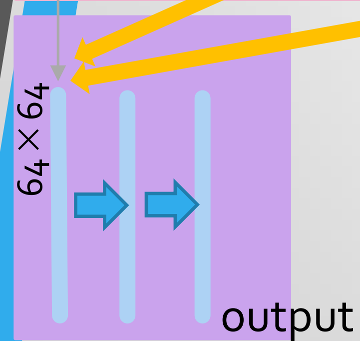


9 input images
Energy map
Charge map
Dosig map + direction vector(x, y, z)
Zosig map
Ecal map
Hcal map

+ no particle

Network Architechture





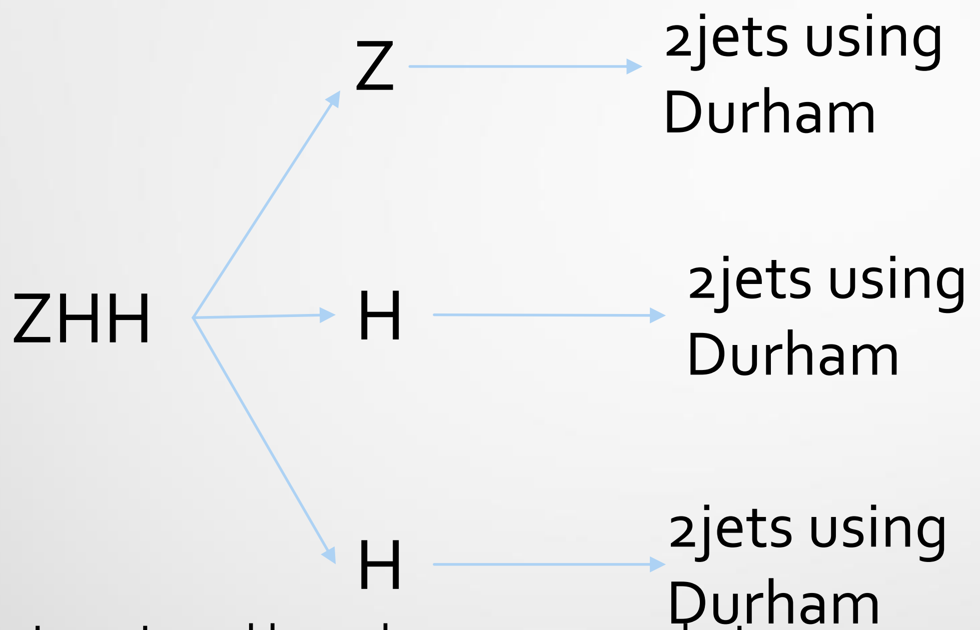
- Final convolution
  - Integrate feature at any stage(hypercolumn)
  - Output for clustering

- Encorder
  - Extract global & higher order feature
  - Downsample to make network robust for distortion & shift effect
  - Lost position information

- Decorder
  - Propagate obtained feature to local
  - Upsample to recover position information
  - Merge encoder nodes to get precise position information

Create answer

- Supervised learning - Create “answer” jets: perfect Durham jet clustering



- Number is assigned based on energy ordering
  - Highest energy jet number is 0, lowest energy jet number is 5

So far, do not consider color singlet state: number of jets is 6

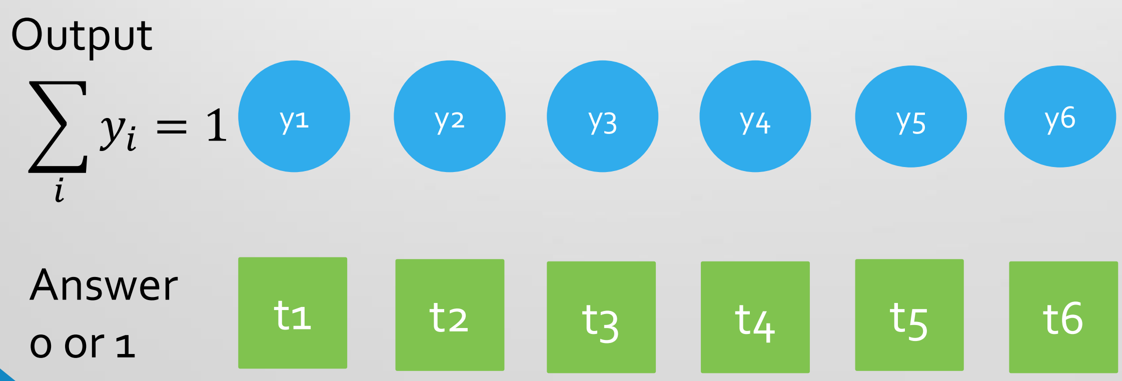
ZHH→(qq)(bb)(bb)→6jets

Basics: How to train a network

- A network is trained to minimize loss function
- If output of the network is probability, cross-entropy is a popular loss function

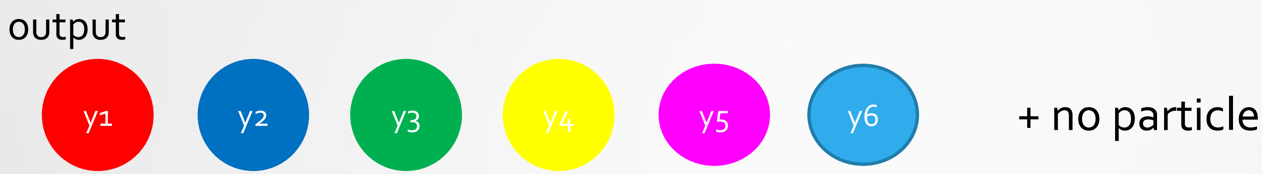
$$L = \frac{1}{n} \sum_n \sum_i t_i \log y_i$$

  - Answer is zero(data does not belong to this node) or one(data is belong to this node)
  - Only one node is 1, the other nodes are 0 (one-hot vector)
  - Smaller value of L means better performance
- Considering better loss function is one of the important points to obtain better performance

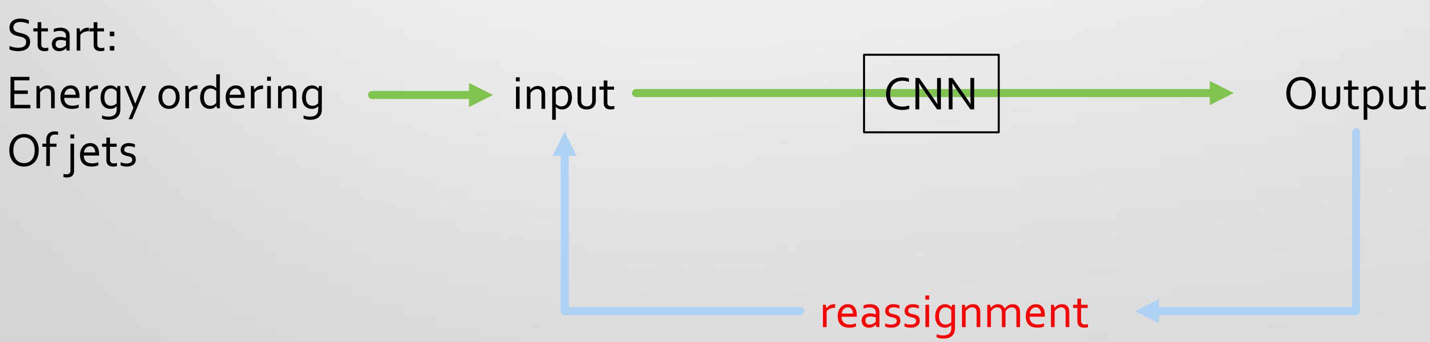


Pseudo-labelling

- Output: inference of the probability of the color to be assigned
  - $\sum y_i = 1.0$

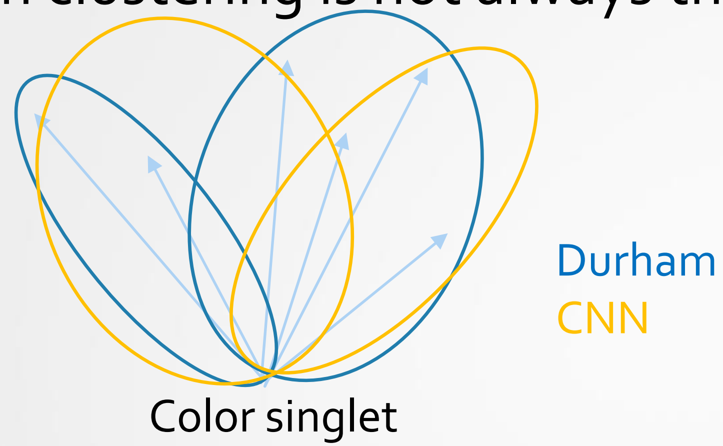


- The combination of color assignments is arbitrary, so assign them so that the loss function is minimized.
  - Using preliminary results after a training, re-assign the color combination
  - Minimize cross entropy $L = \frac{1}{n} \sum t_i \log y_j$

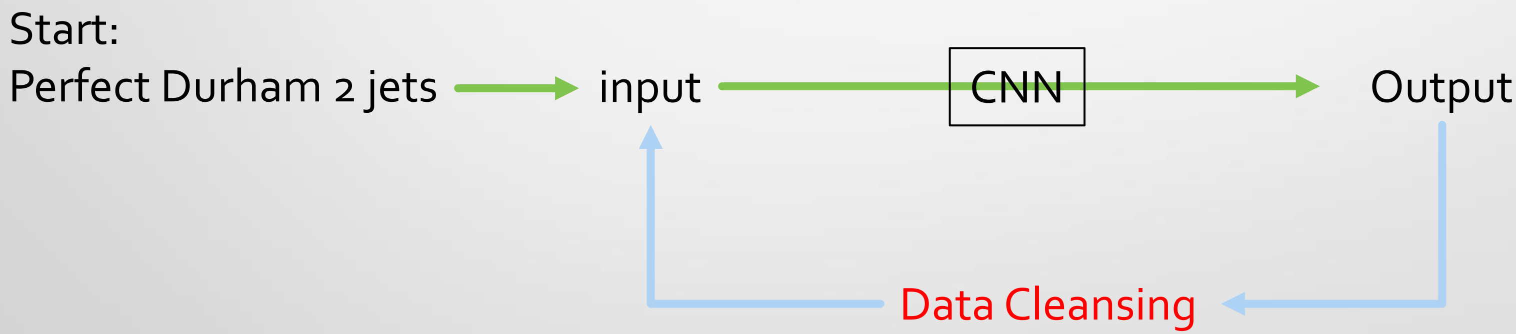


Data Cleansing

- Perfect Durham clustering is not always the best clustering into 2 jets for CNN



- By using the preliminary training weights, clustering into 2 jets is performed



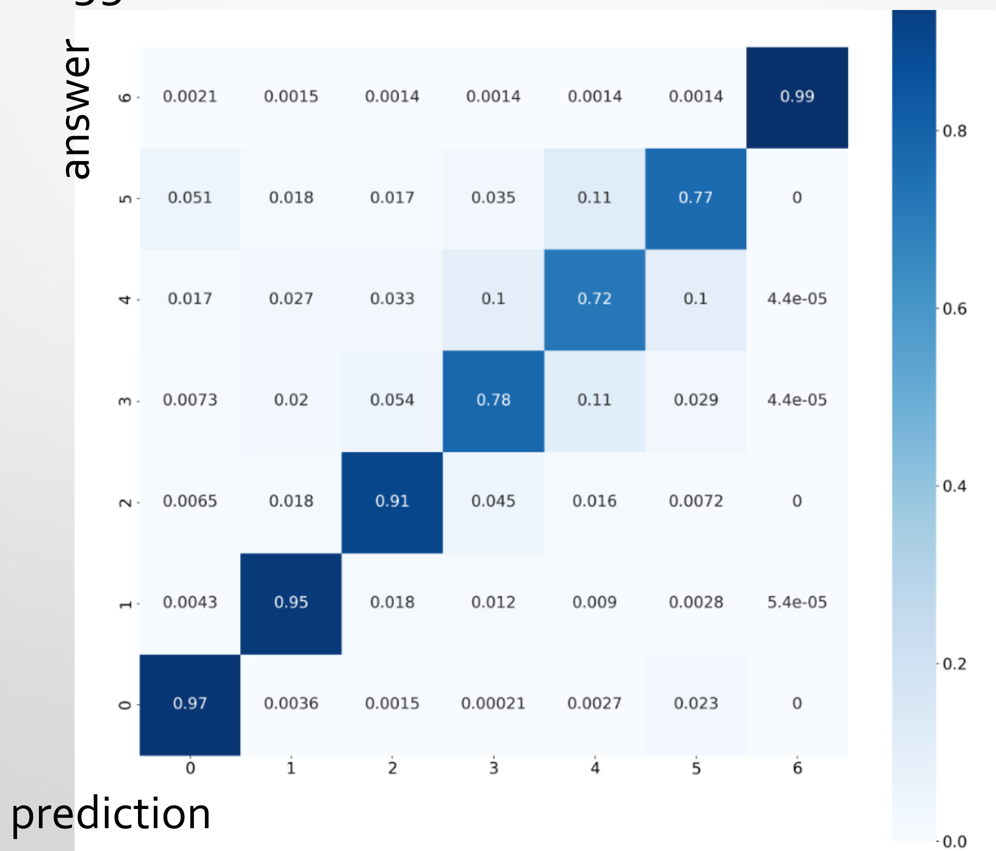
- Clustering particles to make loss function minimum

status

- Use ZHH→(qq)(bb)(bb): 6jets clustering
  - q: uds + c + b   ratio: 9:9:5   need to consider the effect of flavor ratio
    - If a network can really feel flavor
- Use 230000 events for training(207000 train, 23000 validation)
  - Very weak or no over fitting can be seen between train vs. validation
- Don’t consider color singlet state for network training
- Input: 6 + 3 images   output: 6 + 1 images

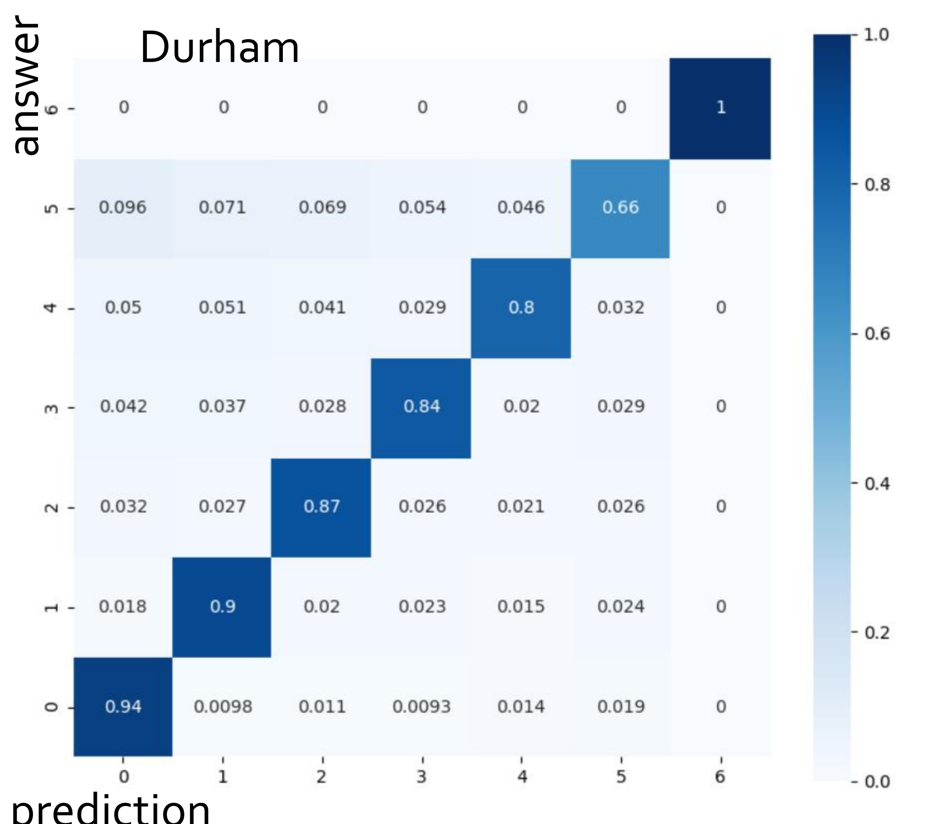
Preliminary results

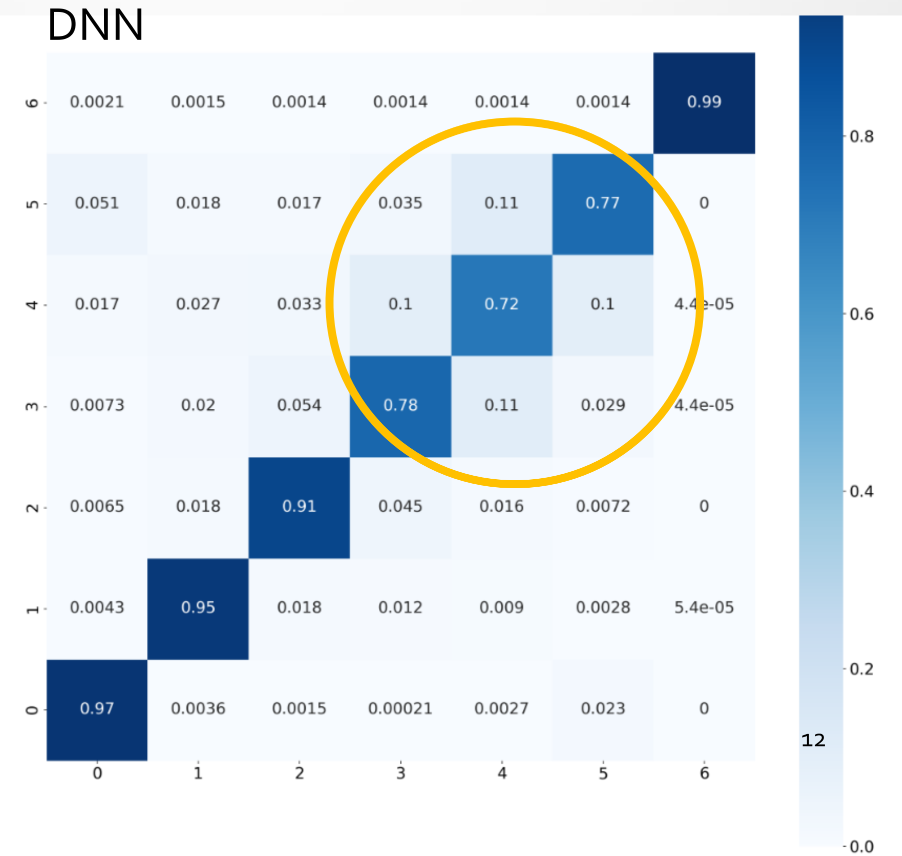
- Confusion matrix
  - 1000 events
  - Num. 0-5: jet number 6: no particle
  - Off-diagonal means mis-assignment
  - Some particles locate at adjacent jets of their answer jet: should be reduce this correlation
  - Now under investigation
- Need to check resolution of Higgs mass
  - Need to improve



Comparison with Durham

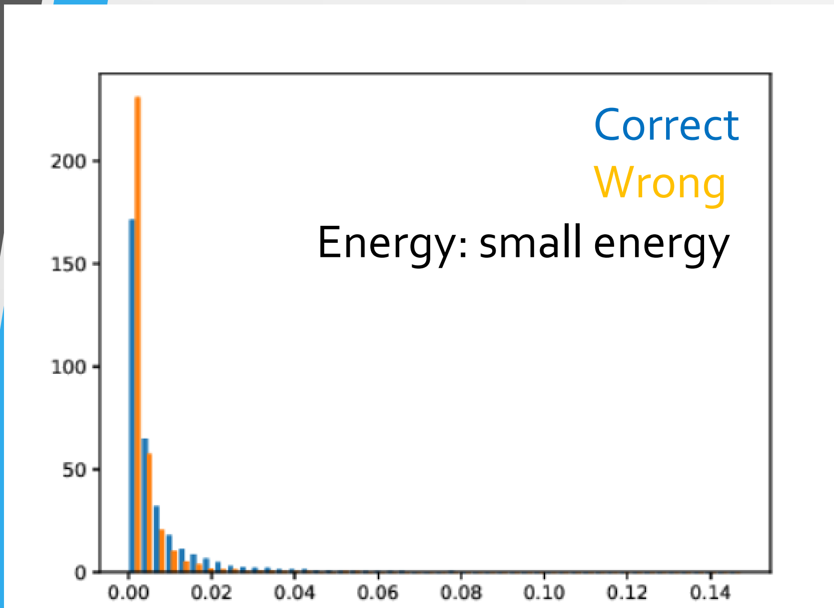
- First 3 jets: start to improve
- Last 3 jets: a bit worse
  - Worst efficiency is improved, but need to improve more
- Correlation between adjacent jets, and asymmetric
- Need to improve circle efficiency to get better performance

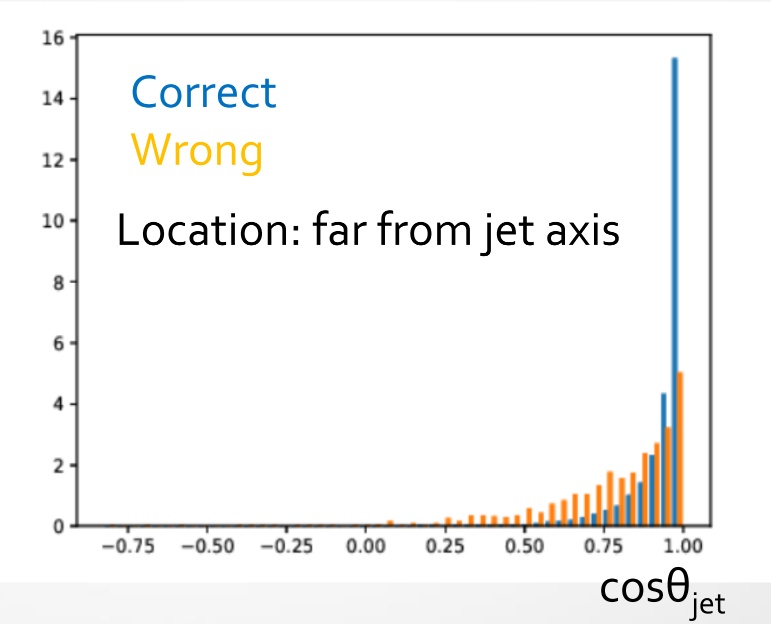




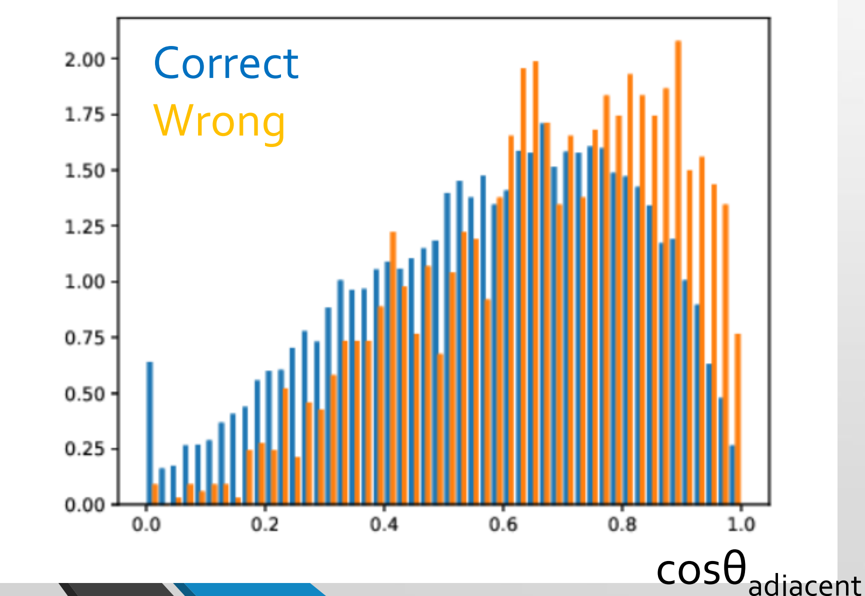
backups

Check the mis-assignment particles





Near adjacent jet axis

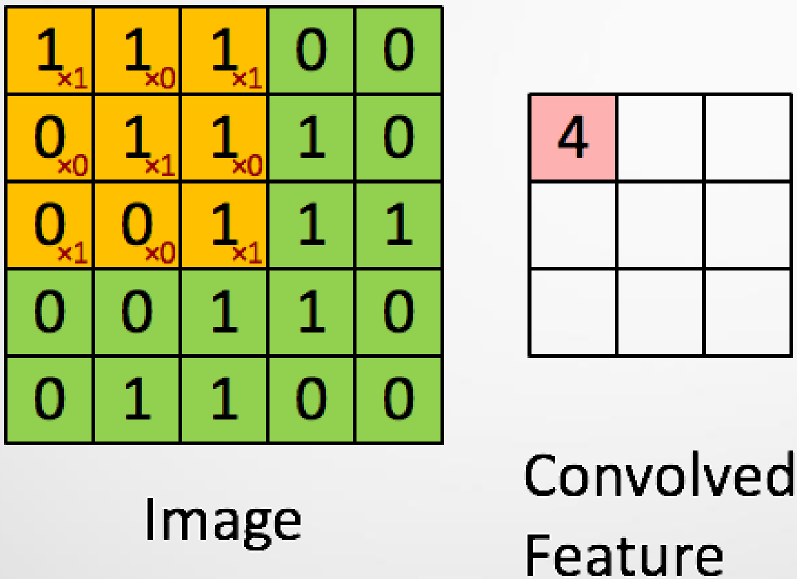


- Mis-assigned particles:
  - Small energy
  - Located at jet boundary
  - 2 jets are very close
- Now trying to solve to assign such particles correctly

Basics: convolution

- Convolution: Apply the filters to extract the feature
  - Sum of the product of each pixel and filter weights:

    $y_{kl} = \sum_{i,j} w_{ij} \cdot x_{(k+i)(l+j)} \; (+b)$
  - Slide filters over all the pixels

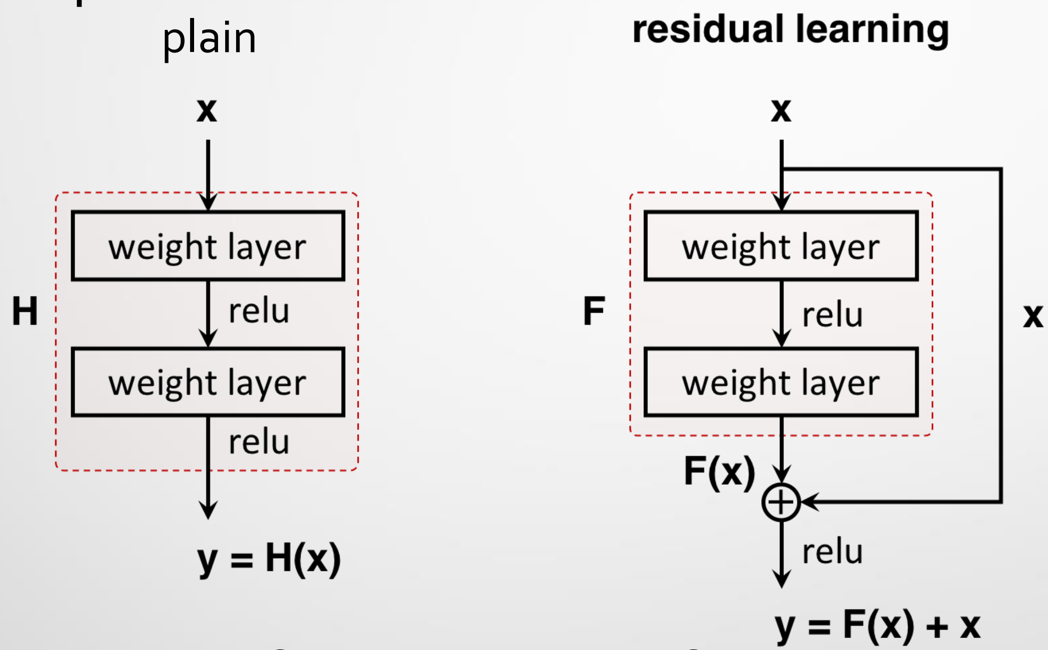


  - Filters are parameters: CNN can obtain them automatically
- After the convolutional operation, apply non-linear transform

  $z_{kl} = \sigma(y_{kl})$
  - "Non-linear" is important to get good expression
- Stack these operations

Basics: Residual convolution

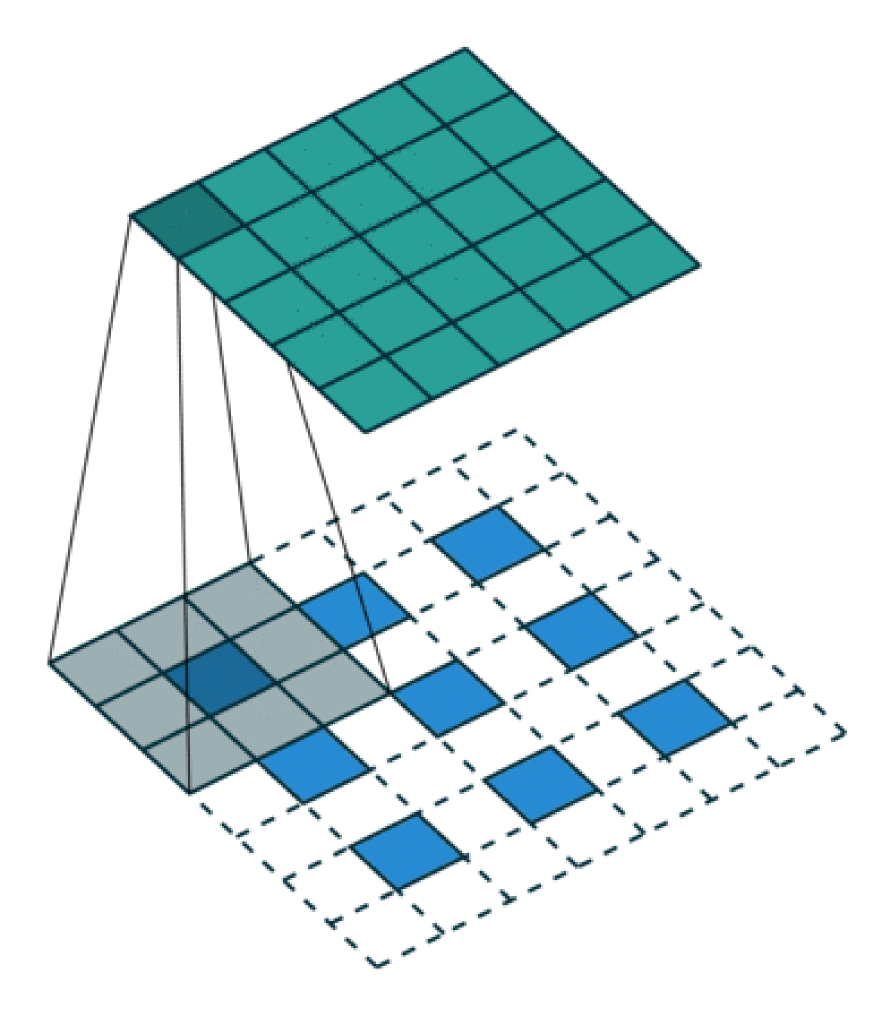
- Stream is divided into 2 paths:
  - Path with convolution
  - Path without any operation
- Sum up these 2 path in downstream



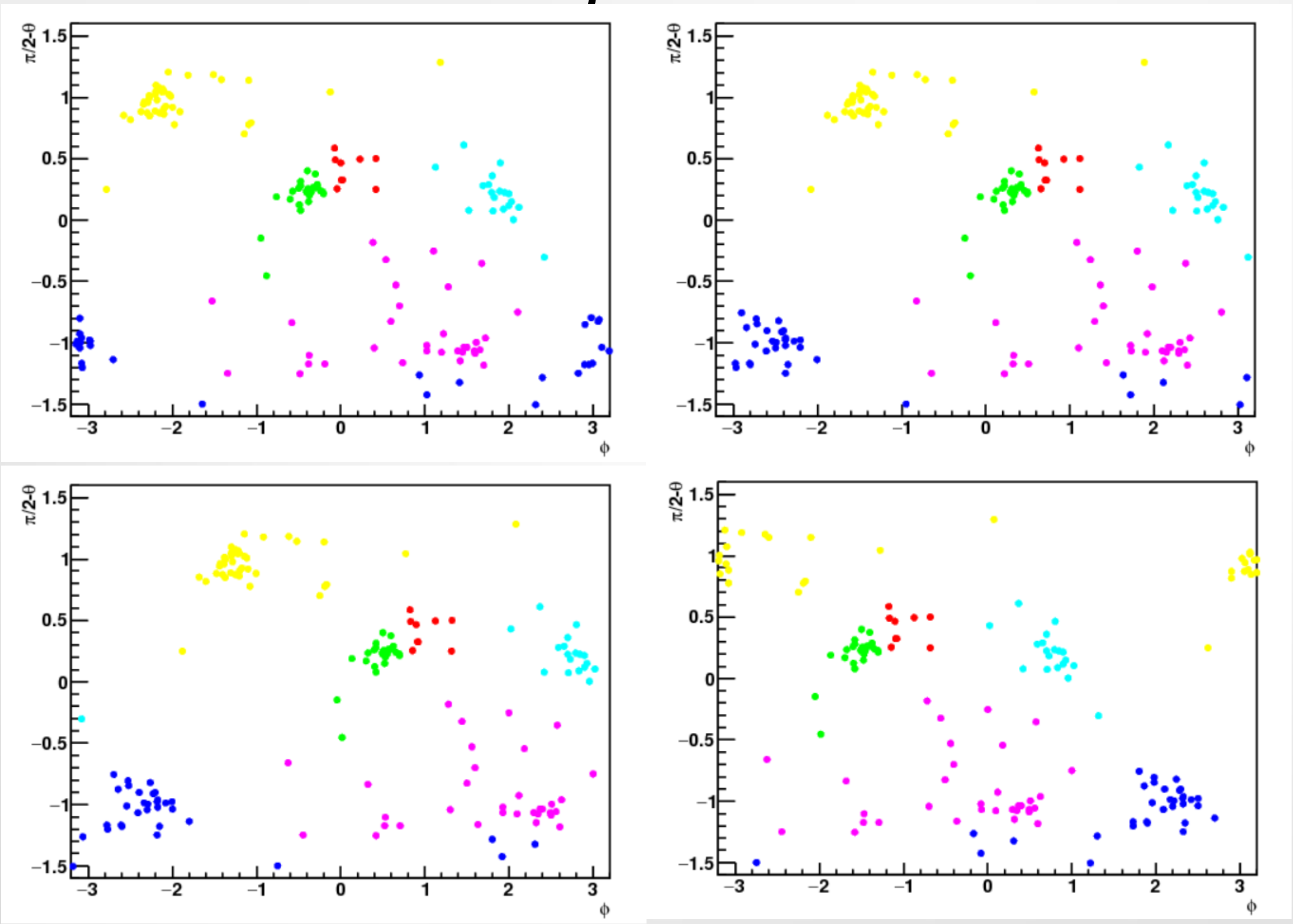
- Can learn "Residuals" of previous layer features
- Can construct very deep network
  - >100 layers can be constructed
  - Deeper will be better performance

Basics: Transposed convolution

- Reverse operation of convolution
  - After adding padding, do convolution
  - Use for upsampling



Data Augmentation



- Random shift for x axis
  - Considering periodic condition of ϕ angle (f(Φ+2π) = f(Φ))
  - To suppress over fitting
- Add random y-flip (I think not good from physics point of view, but suppress over-fitting is important)