

Measurement of $\sigma(e^+ e^- \rightarrow HZ) \times \text{Br}(H \rightarrow ZZ^*)$ at the 250 GeV ILC

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ILC Workshop on Potential Experiments, October 28, 2021

Content

- Introduction
- Studied processes
- Event preselection procedure
- Analysis results for all channels
- Combined signal significance estimate
- Conclusions

Introduction

The width of the Higgs boson *is difficult to measure at LHC in a model-independent approach* (the uncertainty *~20% after luminosity upgrade*)

We propose to use the process $e^+e^- \rightarrow HZ$ with the subsequent decay $H \rightarrow ZZ^*$ to measure:

$$\sigma(e^+e^- \rightarrow HZ) \times Br(H \rightarrow ZZ^*) = C \cdot g_Z^4 / \Gamma_H$$

Constant,
Error < 1%
expected

Higgs boson
width

Coupling HZZ
Error < 0.5% expected

One of Z bosons is reconstructed in jets.

$Z \rightarrow jj$ or ll , $Z^* \rightarrow ll$ or jj

Studied processes

The following processes are studied:

Channel 1: $e^+e^- \rightarrow Z_1(j_1j_2)H, \quad H \rightarrow Z(j_3j_4)Z^*(l_1l_2)$

Channel 2: $e^+e^- \rightarrow Z_1(j_1j_2)H, \quad H \rightarrow Z(l_1l_2)Z^*(j_3j_4)$

Channel 3: $e^+e^- \rightarrow Z_1(v\bar{v})H, \quad H \rightarrow Z(j_1j_2)Z^*(l_1l_2)$

Channel 4: $e^+e^- \rightarrow Z_1(v\bar{v})H, \quad H \rightarrow Z(l_1l_2)Z^*(j_1j_2)$

Event preselection

Preselection tools:

1. Only specific processes and decay chains are selected on *MCParticle* level.
2. Two isolated lepton candidates are identifying with *IsolatedLeptonTagging*
3. ISR identification and removing procedure
4. Jet reconstruction using *FastJet* clustering tools
5. Applying weight factors to each event to get expected number of signal or background events

$$W = \left[\frac{1 \pm 0.8}{2} \cdot \frac{1 \pm 0.3}{2} \right] \cdot \frac{2 \text{ ab}^{-1}}{\mathcal{L}_{\text{nom}}}$$

\mathcal{L}_{nom} - The sample nominal integrated luminosity

Channels	$\mathcal{P}_{e^-e^+}$	MC events	Lepton tagging, events	Weight factors	Weighted number of events
$Z_1(jj),$	eLpR	23989	16088	$2.1 \cdot 10^{-2}$	338
$Z(jj),$	eRpL	23845	16027	$1.3 \cdot 10^{-3}$	21
$Z^*(ll)$					
$Z_1(jj),$	eLpR	23261	20879	$2.1 \cdot 10^{-2}$	439
$Z(ll),$	eRpL	23132	20664	$1.3 \cdot 10^{-3}$	27
$Z^*(jj)$					
$Z_1(\nu_e\bar{\nu}_e),$	eLpR	24044	17429	$3.7 \cdot 10^{-3}$	65
$Z(jj),$	eRpL	23910	17259	$7.9 \cdot 10^{-5}$	1.4
$Z^*(ll)$					
$Z_1(\nu_e\bar{\nu}_e),$	eLpR	23059	21108	$3.7 \cdot 10^{-3}$	79
$Z(ll),$	eRpL	23096	21149	$7.9 \cdot 10^{-5}$	1.7
$Z^*(jj)$					
$Z_1(\nu_{\mu,\tau}\bar{\nu}_{\mu,\tau}),$	eLpR	23840	17103	$4.1 \cdot 10^{-3}$	71
$Z(jj),$	eRpL	23862	17168	$1.6 \cdot 10^{-4}$	2.7
$Z^*(ll)$					
$Z_1(\nu_{\mu,\tau}\bar{\nu}_{\mu,\tau}),$	eLpR	23189	21168	$4.1 \cdot 10^{-3}$	88
$Z(ll),$	eRpL	23225	21246	$1.6 \cdot 10^{-4}$	3.3
$Z^*(jj)$					

Isolated lepton identification

We use the *IsolatedLeptonTagging* processor with default set of parameters and weights to identify leptons.

The detectors instrumented in the magnet yoke surrounding the muon chamber are **not used** in the algorithm, it results in a **small decrease in efficiency**.

The Z^* and Z reconstruction efficiencies in the leptonic modes in the channel with four jets (two jets) are $\sim 67\%$ ($\sim 72\%$) and $\sim 90\%$ ($\sim 91\%$), respectively.

The only events with two identified isolated leptons are kept for the following analysis. These leptons are excluded from the following jet reconstruction procedure.

Jet reconstruction procedure

Valencia algorithm is used to force the remaining particles into 2 or 4 jets.

It contains 3 parameters: R - generalized jet radius, γ and β - special capture parameters in beam distance

We use $\beta = 1$ and tune R and γ with this method from [arXiv:1607.05039](#).

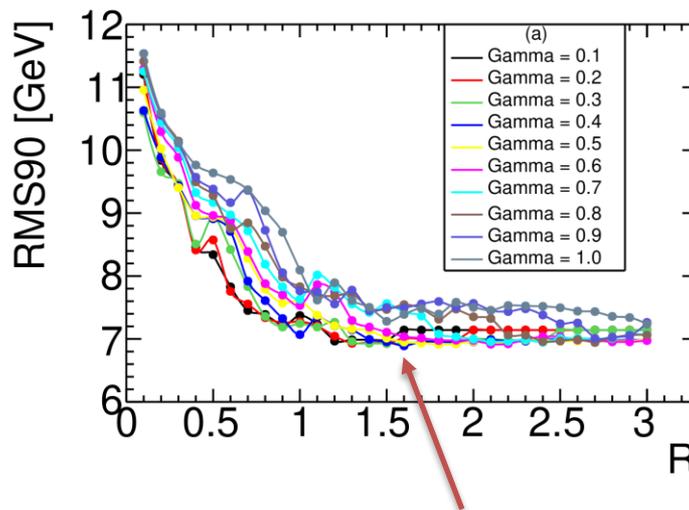
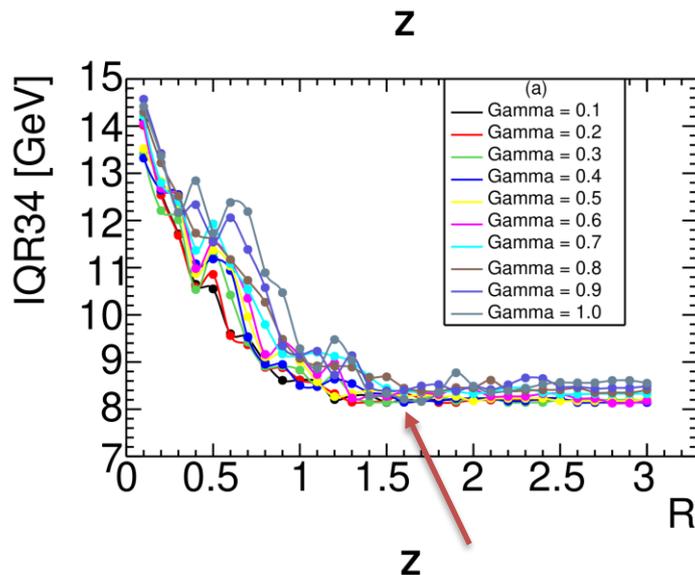
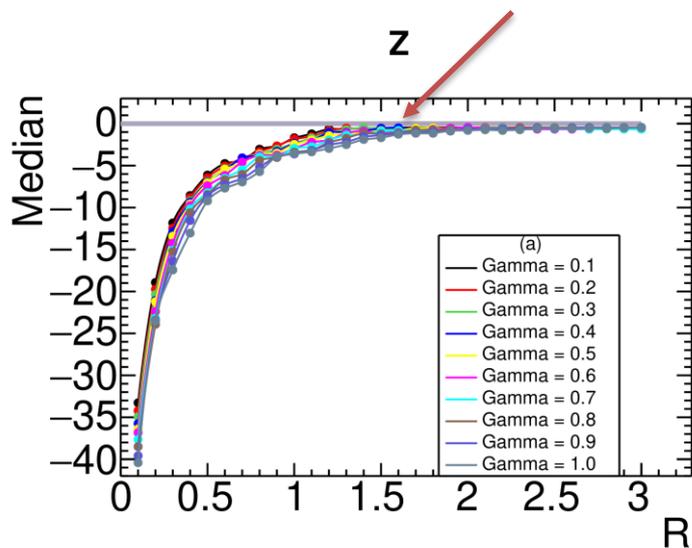
The best Valencia algorithm parameters chosen for the jet reconstruction in different channels:

Valencia parameters	$Z_1(jj), Z(jj), Z^*(\ell\ell)$	$Z_1(jj), Z(\ell\ell), Z^*(jj)$	$Z_1(\nu\bar{\nu}), Z(jj), Z^*(\ell\ell)$	$Z_1(\nu\bar{\nu}), Z(\ell\ell), Z^*(jj)$
β	1.0	1.0	1.0	1.0
γ	0.4	0.4	0.6	0.3
R	1.6	0.7	1.4	1.4

Jet reconstruction procedure

Example of jet parameters
choosing procedure for $Z(jj)$

$R[0.1, 3.0]$ and $\gamma[0.1, 1.0]$ ranges



The best R and γ parameters
are chosen.

Channel 1: $Z_1 \rightarrow jj$, $Z \rightarrow jj$, $Z^* \rightarrow ll$

The final state of the first studied channel includes *two leptons and four jets*. To form the Z_1 and Z bosons from these four jets we calculate χ^2 for six possible two-jet combinations:

$$\chi^2 = \frac{(M(Z_1) - M(Z_{nom}))^2}{\sigma^2_{M_{Z_1}}} + \frac{(M(Z) - M(Z_{nom}))^2}{\sigma^2_{M_Z}} + \frac{(P(Z_1) - \bar{P}(Z_1))^2}{\sigma^2_{P_{Z_1}}} + \frac{(P(Z + Z^*) - \bar{P}(Z_1))^2}{\sigma^2_{P_{Z+Z^*}}}$$

$\bar{P}(Z_1) = 60.0 \text{ GeV}/c$ is the mean Z_1 momentum

$M(Z_{nom}) = 91.2 \text{ GeV}$

All σ parameters are the **mean widths** of corresponding mass or momentum distributions on the reconstruction level.

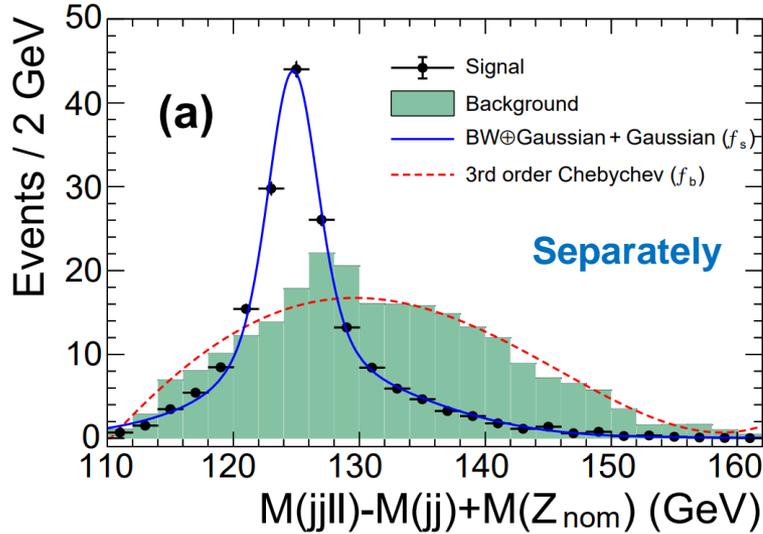
Mass difference is used to get a better mass resolution:

$$M_{\Delta} = M(jj\ell\ell) - M(jj) + M(Z_{nom})$$

Channel 1: $Z_1 \rightarrow jj, Z \rightarrow jj, Z^* \rightarrow ll$

$$M_{\Delta} = M(jj\ell\ell) - M(jj) + M(Z_{nom})$$

Background contributions:

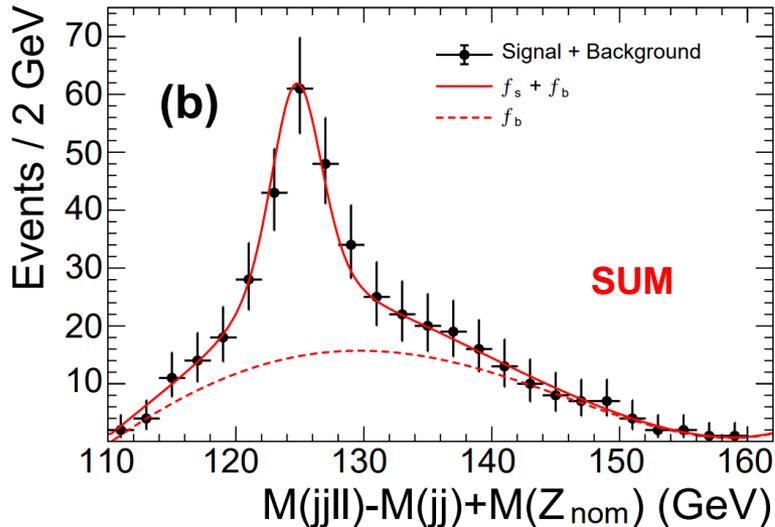
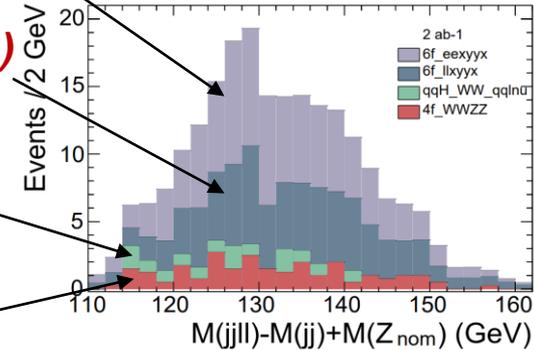


$$e^+e^- \rightarrow W^+W^- / ZZ\gamma^*(e^+e^-)$$

$$e^+e^- \rightarrow W^+W^- / ZZ\gamma^*(\mu^+\mu^-)$$

$$e^+e^- \rightarrow Z(jj)H, H \rightarrow W^+(jj)W^-(lv)$$

$$e^+e^- \rightarrow W^+(jj)W^-(jj) \text{ and } e^+e^- \rightarrow Z(jj)Z(jj)$$



Additional wide Gaussian in fit function described residual Z^*Z^* events and a few events due to a wrong jet matching in the χ^2 selection.

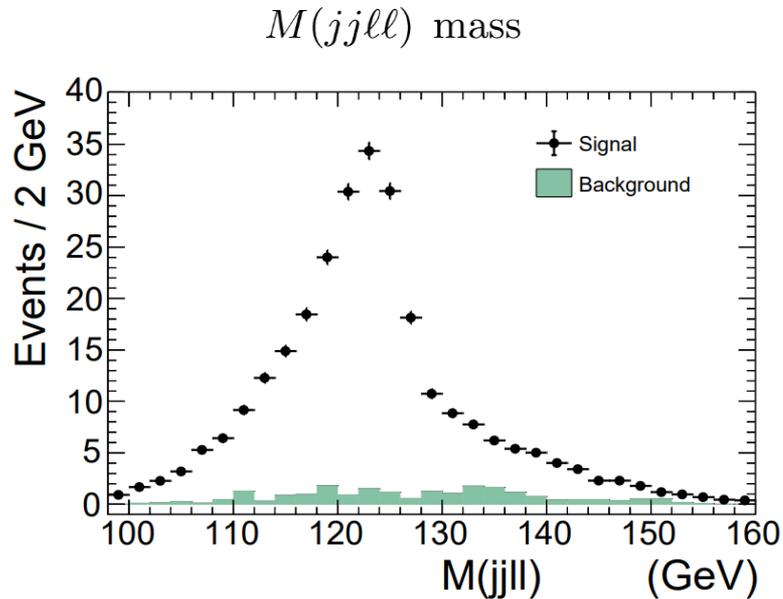
The fit yields 193.4 ± 24.5 signal events

The toy MC yields 192.4 ± 24.9 signal events

Statistical uncertainty is **12.9%**

We used toy MC to obtain final results

Channel 2: $Z_1 \rightarrow jj, Z \rightarrow ll, Z^* \rightarrow jj$



χ^2 for six possible two-jet combinations:

$$\chi^2 = \frac{(M(Z_1) - M(Z_{nom}))^2}{\sigma^2_{M_{Z_1}}} + \frac{(E(Z_1) - \bar{E}(Z_1))^2}{\sigma^2_{E_{Z_1}}} + \frac{(P(Z_1) - \bar{P}(Z_1))^2}{\sigma^2_{P_{Z_1}}} + \frac{(P(Z + Z^*) - \bar{P}(Z_1))^2}{\sigma^2_{P_{Z+Z^*}}}$$

$\bar{E}(Z_1) = 110.0$ GeV is the mean Z_1 energy

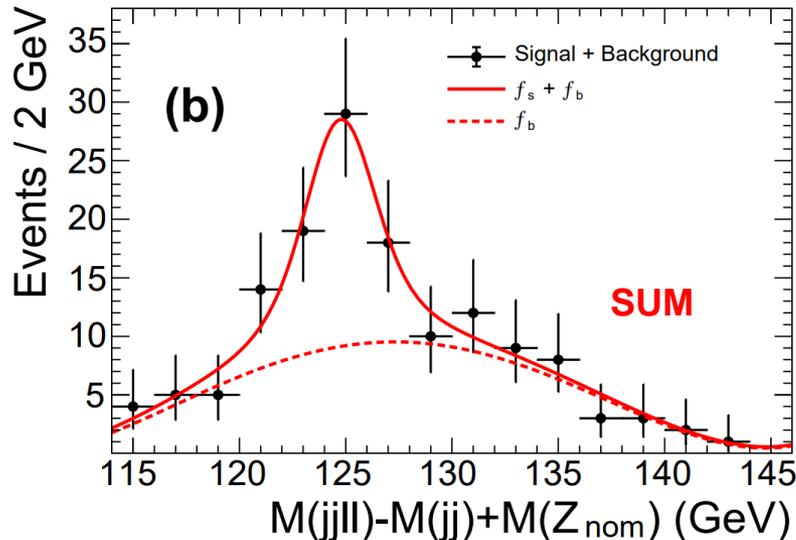
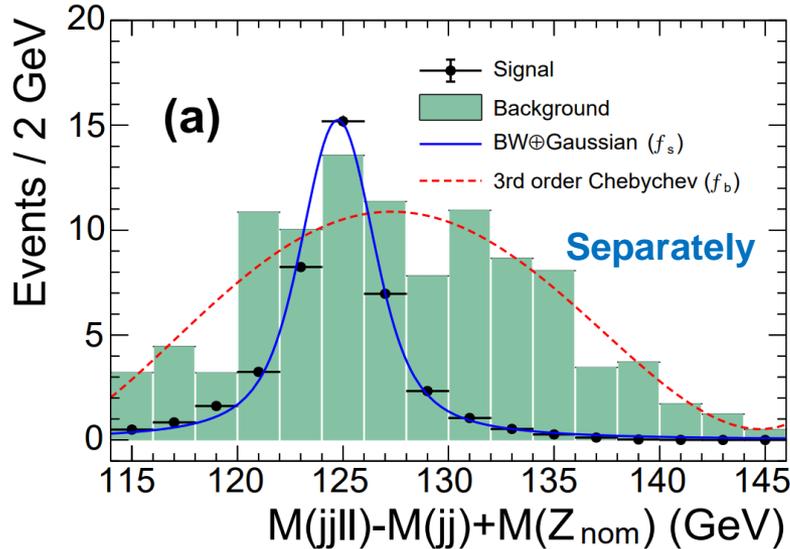
The background is **very small**, the integral over all bins is **18.3 events**

The signal mean value and uncertainty is **275.3 ± 17.2**

Statistical uncertainty is **6.3%**

Channel 3: $Z_1 \rightarrow \nu\bar{\nu}$, $Z \rightarrow jj$, $Z^* \rightarrow ll$

$$M_{\Delta} = M(jj\ell\ell) - M(jj) + M(Z_{nom})$$



There are many background sources with large cross sections, which can contribute to this channel

Significant backgrounds:

$e^+e^- \rightarrow Z(jj)Z(\tau^+\tau^-)$ with following leptonic decays

$e^+e^- \rightarrow W^+(jj)W^-(lv)$

$e^+e^- \rightarrow b\bar{b}, e^+e^- \rightarrow ZH(b\bar{b})$

$H \rightarrow Z^*Z^*$

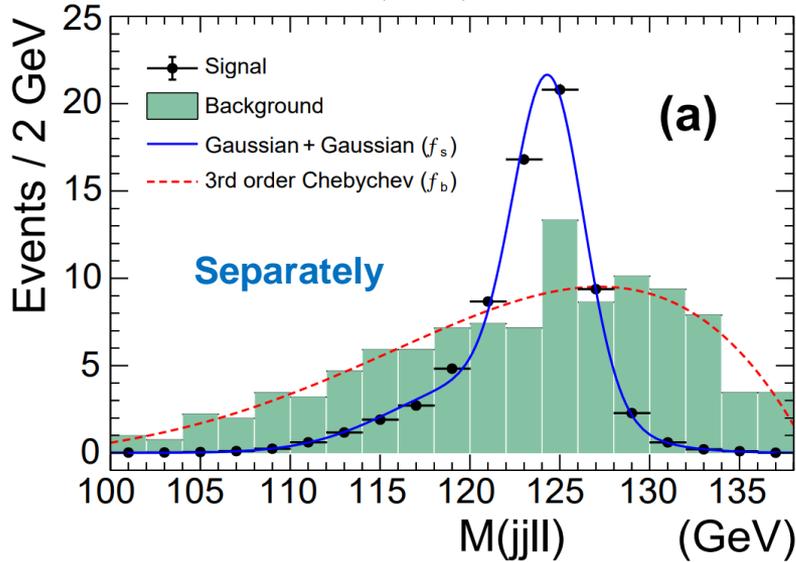
The fit yields 52.0 ± 12.7 signal events

The toy MC yields 51.9 ± 13.0 signal events

Statistical uncertainty is 25.1%

Channel 4: $Z_1 \rightarrow \nu\bar{\nu}$, $Z \rightarrow ll$, $Z^* \rightarrow jj$

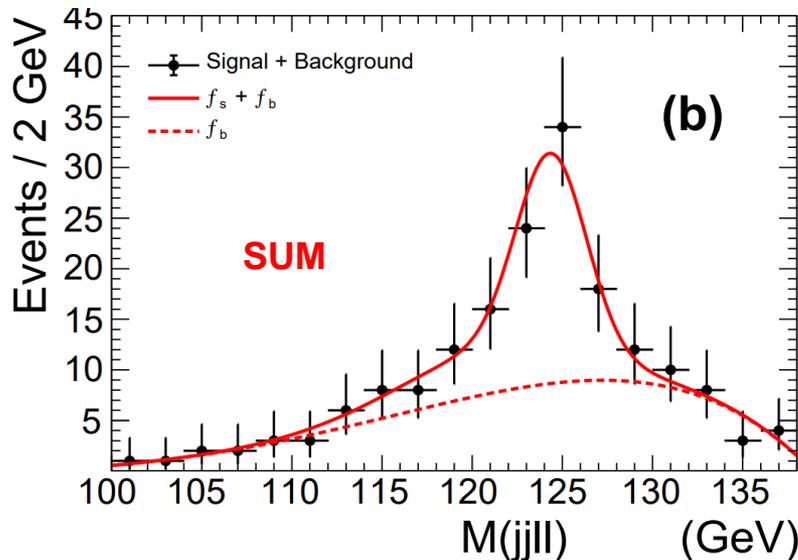
$M(jj\ell\ell)$ mass



The dangerous background sources are similar to the previous channel, except the $b\bar{b}$ background

Significant backgrounds:

$e^+e^- \rightarrow Z(jj)Z(\tau^+\tau^-)$ with following leptonic decays
 $e^+e^- \rightarrow W^+(jj)W^-(lv) H \rightarrow Z^*Z^*$



The fit yields 74.1 ± 13.9 signal events

The toy MC yields 73.3 ± 14.2 signal events

Statistical uncertainty is **19.3%**

Table of cuts for all channels

	Channel 1	Channel 2	Channel 3	Channel 4
Selection	$Z_1(jj),$ $Z(jj),$ $Z^*(\ell\ell)$	$Z_1(jj),$ $Z(\ell\ell),$ $Z^*(jj)$	$Z_1(\nu\bar{\nu}),$ $Z(jj),$ $Z^*(\ell\ell)$	$Z_1(\nu\bar{\nu}),$ $Z(\ell\ell),$ $Z^*(jj)$
$M(\ell\ell)$ (GeV/ c^2)	[13, 36]	[70, 95]	[13, 34]	[80, 95]
$M(Z \rightarrow jj)$ (GeV/ c^2)	> 70	< 50	[80, 113]	[13, 38]
$M(Z_1 \rightarrow jj)$ (GeV/ c^2)	> 70	> 70		
$E(jjjj\ell\ell)$ (GeV)	[200, 260]	[200, 260]		
$E(jj\ell\ell)$ (GeV)			< 145	< 145
$P_{\max}(\ell)$ (GeV/ c)	< 32		< 40	
$P_{\min}(\ell)$ (GeV/ c)	> 9		> 8	
$P_{\max}(j_1)$ (GeV/ c)				< 22
$P_{\max}(j_2)$ (GeV/ c)				< 42
$P(jj\ell\ell)$ (GeV/ c)			[30, 70]	[40, 70]
$ \cos \theta_{vis} $			< 0.8	< 0.9
$\Delta\phi_{ZZ^*}$ (degree)			< 120	< 140

Combined signal significance estimate

We calculate the **combined statistical uncertainty** for the four studied channels:

$$S_{\text{comb}} = 1 / \sqrt{\sum_{i=1}^4 S_i^{-2}}$$

Alternatively, we assumed two data samples with the polarizations and 0.9 ab^{-1} luminosity each.

$$\mathcal{P}_{e^-e^+} = (-0.8, +0.3)$$

$$\mathcal{P}_{e^-e^+} = (+0.8, -0.3)$$

The same analysis is repeated for this data taking scheme

Number of **signal events** and **uncertainties** obtained from **toy MC** for each channel:

	$Z_1(jj),$ $Z(jj),$ $Z^*(\ell\ell)$	$Z_1(jj),$ $Z(\ell\ell),$ $Z^*(jj)$	$Z_1(\nu\bar{\nu}),$ $Z(jj),$ $Z^*(\ell\ell)$	$Z_1(\nu\bar{\nu}),$ $Z(\ell\ell),$ $Z^*(jj)$	Sum
	2 ab⁻¹ eLpR				
Number	192.4	275.3	51.9	73.3	-
of events	± 24.9	± 17.2	± 13.0	± 14.2	-
Statistical uncertainty	12.9%	6.3%	25.1%	19.3%	5.29%
	0.9 ab⁻¹ eLpR + 0.9 ab⁻¹ eRpL				
Number	135.2	202.2	30.9	67.3	-
of events	± 20.4	± 14.7	± 10.7	± 14.3	-
Statistical uncertainty	15.1%	7.3%	34.6%	21.2%	6.15%

Conclusions

We studied the $e^+e^- \rightarrow HZ$ process with the subsequent $H \rightarrow ZZ^*$ decay.

The analysis is performed assuming the integrated luminosity 2 ab^{-1} collected at the e^+e^- collisions with center-of-mass energy 250 GeV and the beam polarizations $\mathcal{P}_{e^-e^+} = (-0.8, +0.3)$. We also repeated the analysis assuming two data samples with integrated luminosities 0.9 ab^{-1} each and two beam polarizations $\mathcal{P}_{e^-e^+} = (\mp 0.8, \pm 0.3)$.

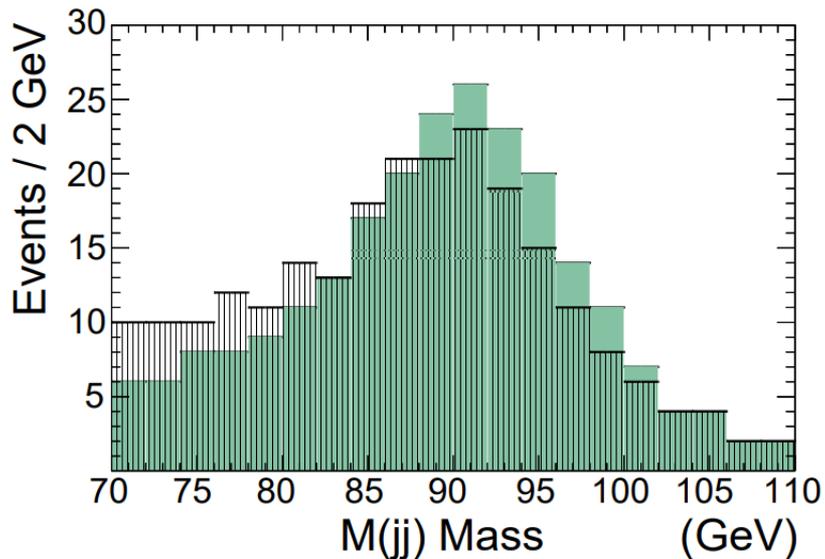
Four channels are studied and the corresponding signal and background contributions are estimated using MC simulation.

Summing results obtained in the four studied channels we obtain the combined statistical uncertainty 5.29% with 2 ab^{-1} at 250 GeV.

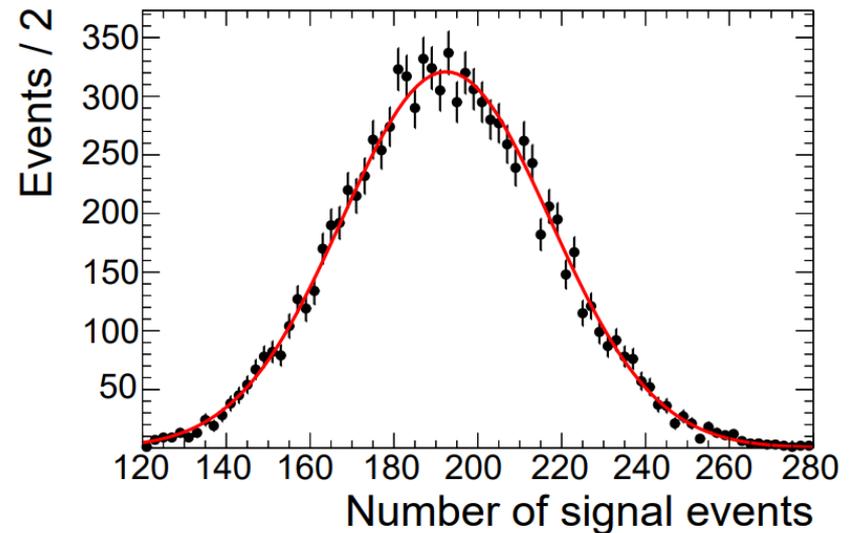
This indicates, that the Higgs width can be measured using this method with an accuracy of about (5-6)% within the model-independent approach.

Thank you for attention

Additional: Toy MC and jj masses



The $M(j_1j_2)$ (hatched histogram) and $M(j_3j_4)$ (shaded histogram) mass distributions are shown for Channel 1.



The distribution of the number of the signal events obtained from the toy MC fits (dots with errors).