

# Study of resolution in the time direction

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2021.7.12 seasonal ILC-JP detector meeting

# Introduction



High spatial resolution is important for tracker.

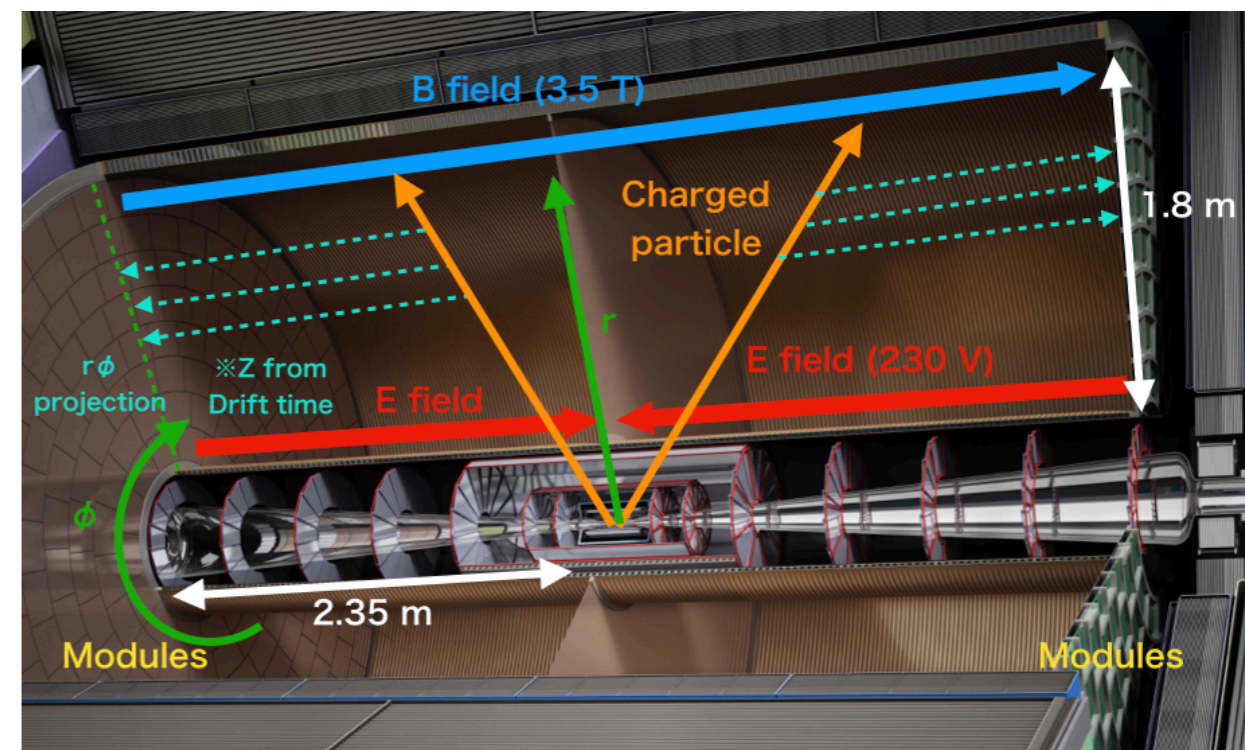
We use recoil mass to measure Higgs mass using momentum conservation law.

→ Momentum depends on spatial resolution, so high spatial resolution is necessary for Higgs precise measurement

ILD

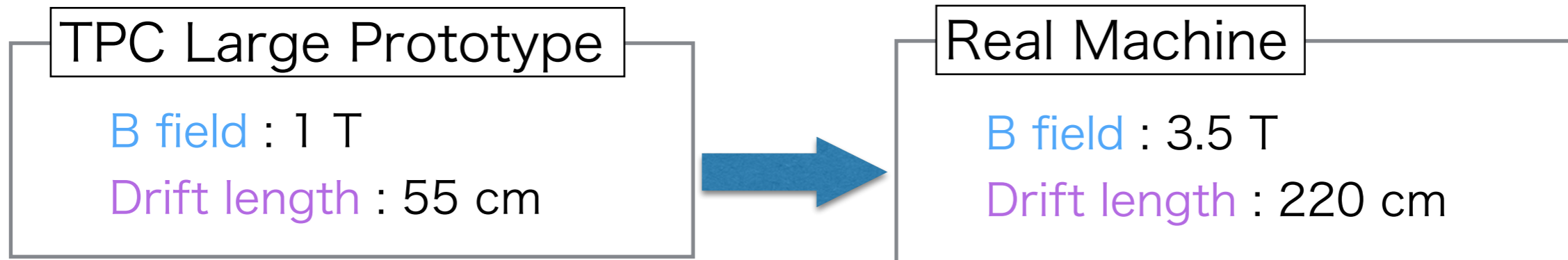
$r\phi$  resolution :  $<100\mu\text{m}$

Z (time) resolution :  $\sim 0.4 - 1.4\text{ mm}$   
(for zero – full drift)



To check if we can achieve the goal is need for ILC !

# Can we achieve the high resolution?

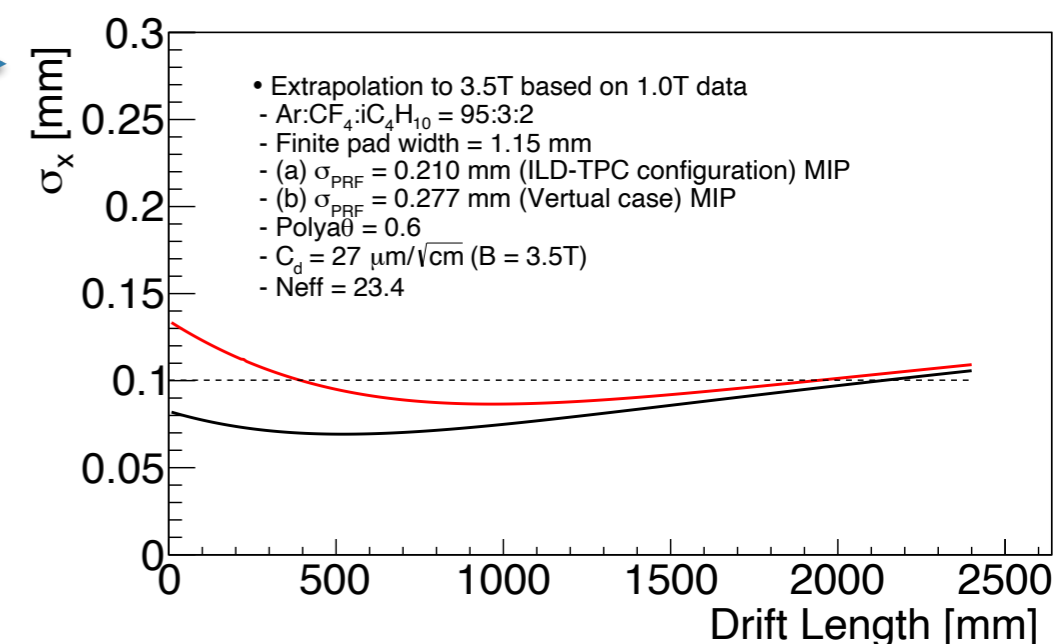
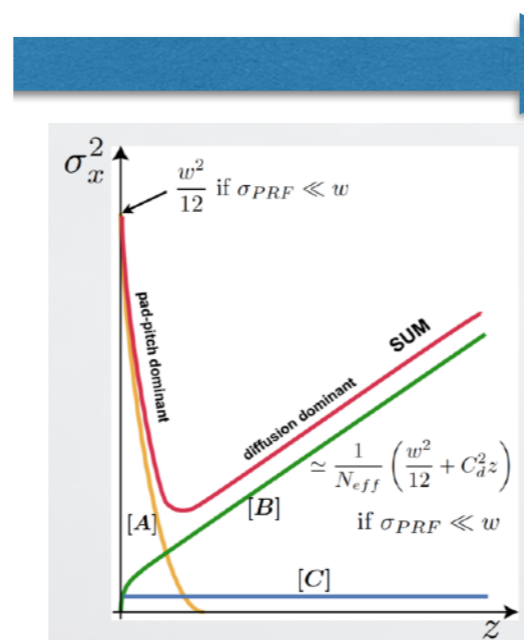
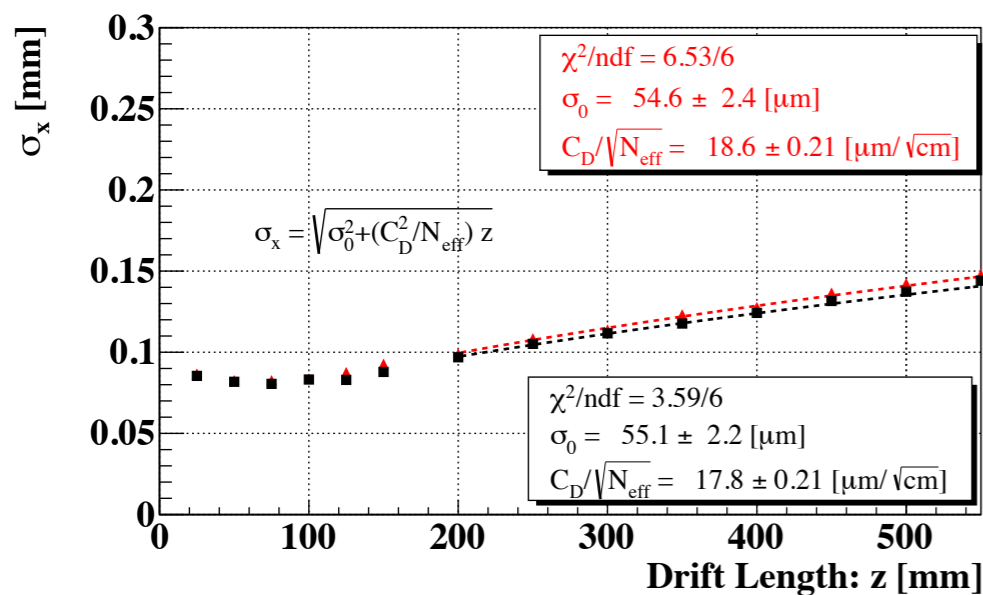


$r\phi$  resolution

$$\sigma_{r\phi}(Z)^2 = \underbrace{\sigma_0(w)^2}_{\text{hodoscope effect}} + \frac{1}{N_{eff}} \underbrace{C_d(B)^2}_{\text{Transverse diffusion constant}} \cdot Z$$

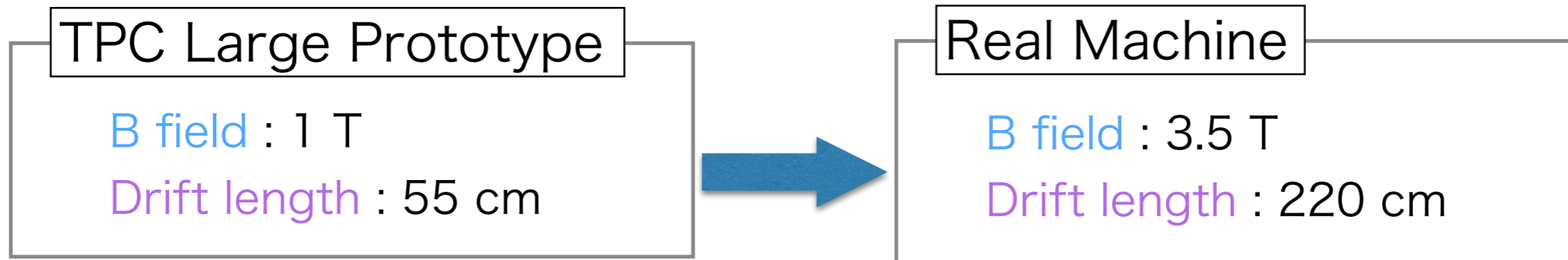
w: pad pitch

YONAMINE, Ryo. "Measuring the top Yukawa coupling at the ILC at  $\sqrt{s} = 500$  GeV and R&D for the ILD-TPC." (2012).



However we didn't know resolution formula for time direction

# Can we achieve the high resolution?



Time resolution

$$\sigma_Z(Z)^2 \stackrel{?}{=} \underbrace{\sigma_{0L}(w_t)^2}_{\text{hodoscope effect}} + \frac{1}{N_{eff}} \underbrace{C_{dL}}_{\text{Longitudinal diffusion constant}} \cdot Z$$

hodoscope effect w<sub>L</sub>: time bin

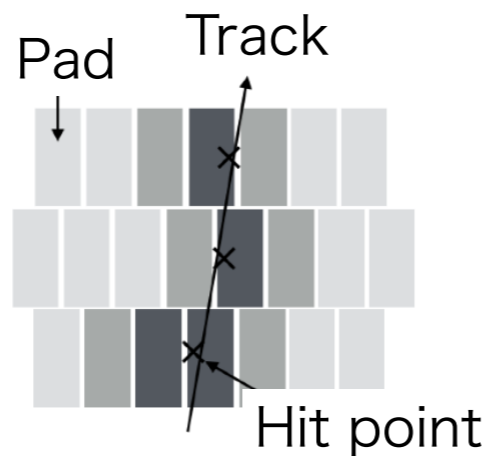
Longitudinal diffusion constant

r φ direction

time direction

Measure charge of pads

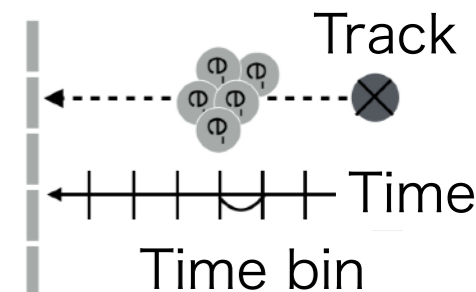
Magnetic field effect



Measure charge of time bin

Assumption

Magnetic field doesn't affect the time resolution



Can we achieve the resolution goal in time direction?



# Motivation of this study



## Construction of time resolution formula

$$\sigma_Z(Z)^2 \stackrel{?}{=} \underbrace{\sigma_{0L}(w_t)^2}_{\substack{\text{hodoscope effect} \\ w_L: \text{time bin} \\ \frac{w_L^2}{12}}} + \frac{1}{N_{eff}} \underbrace{C_{dL}}_{\text{Longitudinal diffusion constant}} \cancel{(B)^2} \cdot Z$$

## First, I take notice of $C_{dL}$

We assume that magnetic field doesn't affect the time resolution

### Simple assumption

- There is no diffusion in amplification region
- No B effect

I'm making TPC simulator for this study

## Parameter

- Position, angle of track
- # of primary ionization
- Diffusion constant

## Create the readout structure

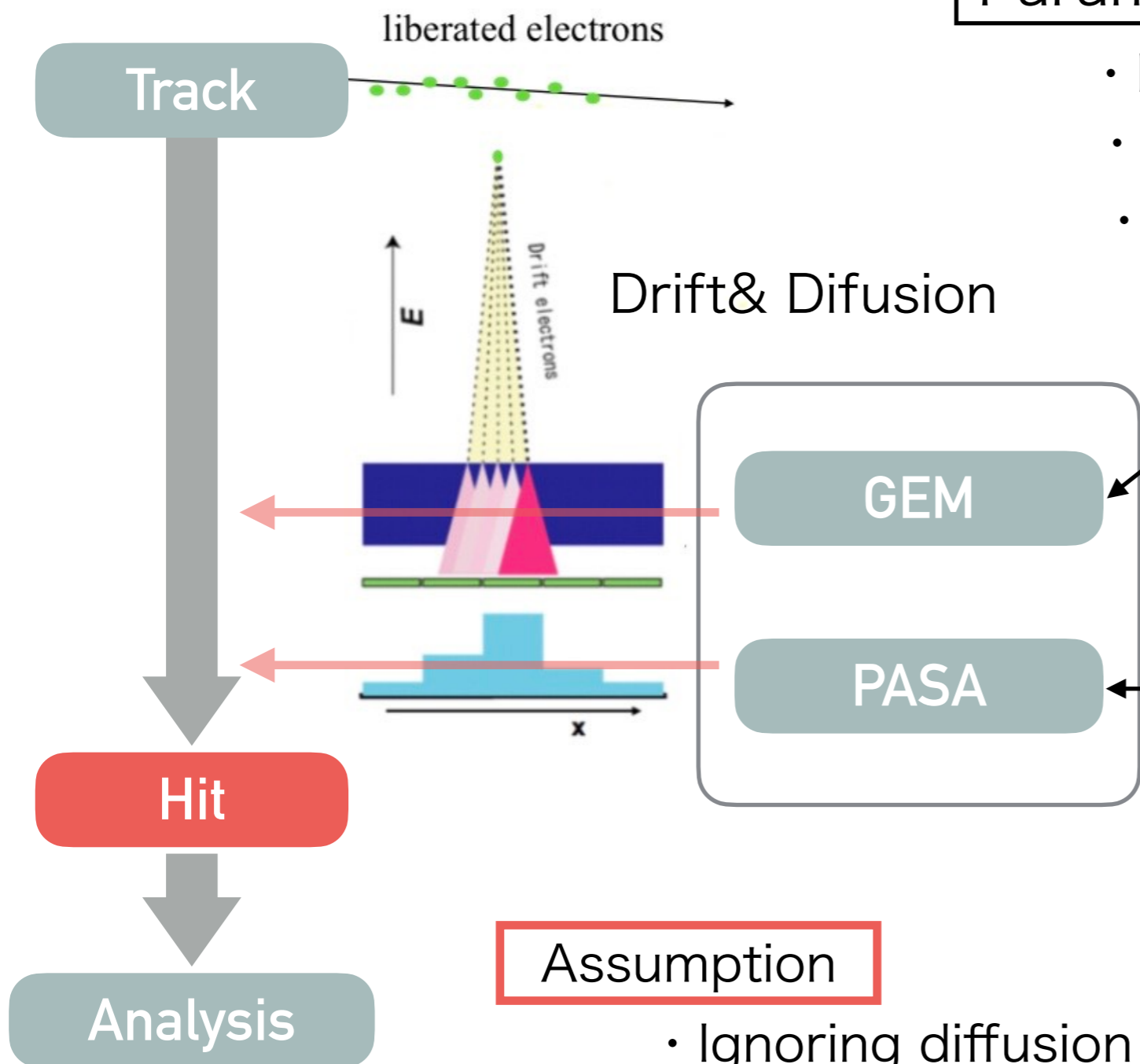
- Pad size
- Drift velocity
- Average gas gain

## Define how to treat electrons

- Peaking time
- Shaper order
- time bin width

## Assumption

- Ignoring diffusion in amplification region
- ✂ I use a pad having largest charge in the row



# How to calculate $C_{dL}$

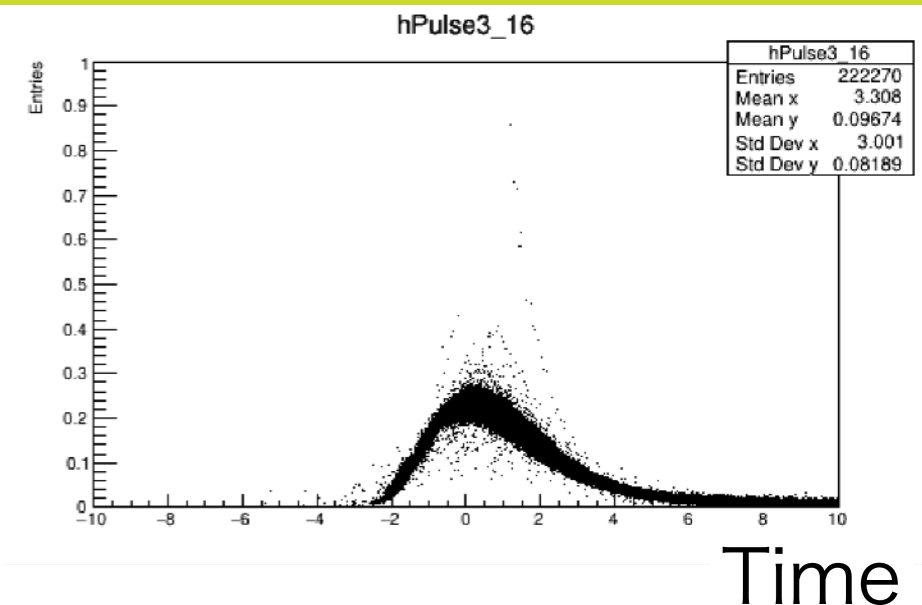


Electrons make pulse in time direction

Pulse shape is defined by structure  
of readout electronics

For accurate pulse fit, I use convolution fit.

$$f(t) = \frac{1}{n!(t_{pk}/n)} \left( \frac{t}{t_{pk}/n} \right)^n e^{-\left( \frac{t}{t_{pk}/n} \right)}$$



Gaussian

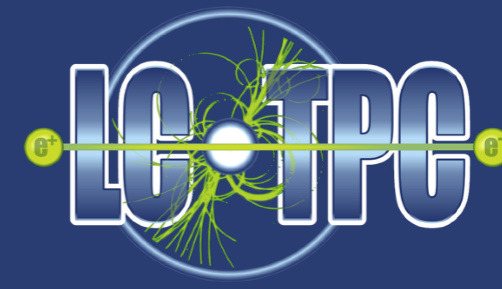
Effect of diffusion

$n$  : shaper parameter ,  $t_{pk}$  : peaking time

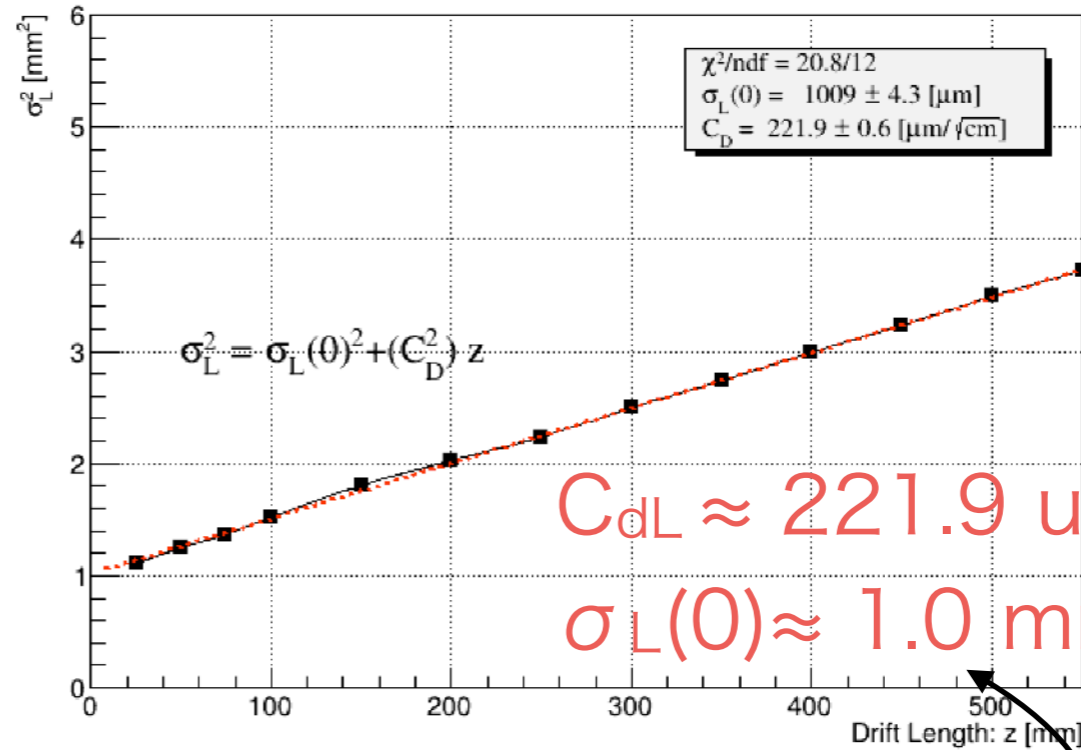
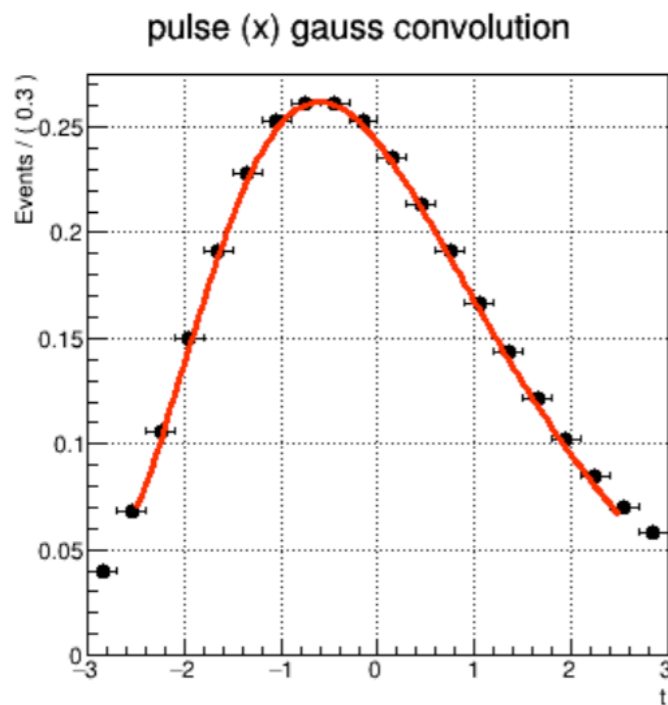
$n$  and  $t_{pk}$  is decided by electronics.

(Beam test setup :  $n=3$ ,  $t_{pk}=120\text{ns}$ ) → Former term is fixed

→ We can calculate longitudinal diffusion by  $\sigma$  of Gaussian



Simulation input :  $n=3$ ,  $tpk = 120ns$ ,  $C_{dL} = 220 \text{ } \mu\text{m}/\sqrt{\text{cm}}$



$C_{dL} \approx 221.9 \text{ } \mu\text{m}/\sqrt{\text{cm}}$   
 $\sigma_L(0) \approx 1.0 \text{ mm}$

An square root of intercept means expanse hit ← Effect of time bin width

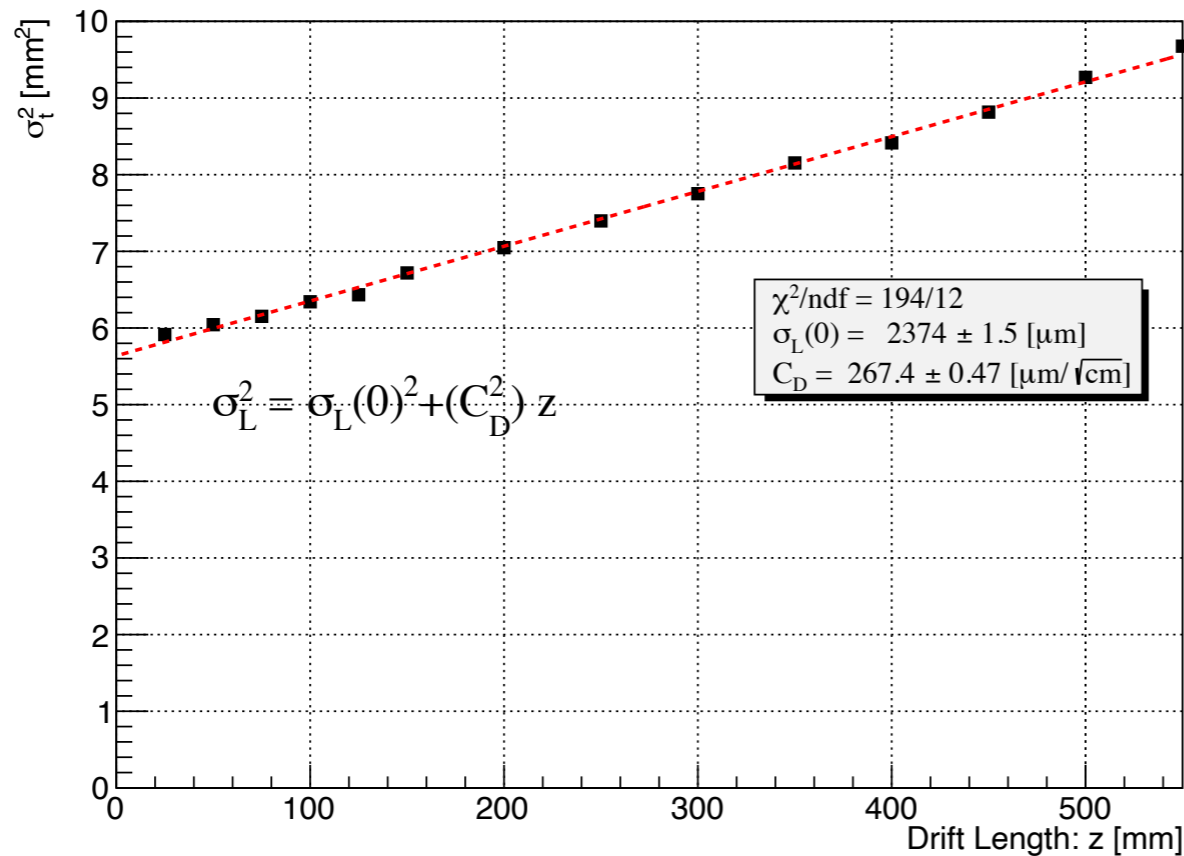
Theory 
$$\frac{\text{Drift velocity} \times \text{time bin}}{\sqrt{12}} = \frac{75 \mu\text{m}/ns \times 50ns}{\sqrt{12}} = 1.082 \text{ mm}$$

Under the assumption that the only smearing effect is diffusion in the drift region, this estimation method of  $C_{dL}$  is reasonable.

# C<sub>dL</sub> of test beam data



Input : n = 3 , t<sub>pk</sub> = 120 ns Row = 44



$$C_{dL} \approx 267.4 \text{ } \mu\text{m}/\sqrt{\text{cm}}$$
$$\sigma_L(0) \approx 2.37 \text{ mm}$$

$$\frac{\text{Drift velocity} \times \text{time bin}}{\sqrt{12}} = 1.082 \text{ mm}$$

$$\text{Difference} : \sqrt{(2.374 \text{ mm})^2 - (1.082 \text{ mm})^2} = \underline{2 \text{ mm}}$$

This result turns out that the **assumption is wrong** !

## Assumption

- There is ~~no~~ diffusion in amplification region
- ~~No~~ E×B effect (E and B field is uniform)



# What is the reason ?



Smearing effect is not only due to diffusion in the drift region

→ There is other smearing effect to expand pulse 2 mm for time direction

## Candidate list

### (A) Distortion of isochron

The drift line may be distorted by the distortion of the GEM foil, the electrode gap, etc...

In this case, a magnetic field causes the distortion of drift line due to  $E \times B$ .  
(This part depends on the magnetic field, so resolution change at 3.5 T!)

### (B) Width of arrival time due to diffusion in the GEM module

This can be estimated since the size and electric field of each region in the GEM module are known.

# Summary & Next steps



- We try to make TPC simulator for constructing time resolution formula
- We checked diffusion constant for time direction
- According to comparison between test beam data and simulation data, we realize that there is effect which we haven't evaluate to expand pulse 2 mm for time direction

## Future work

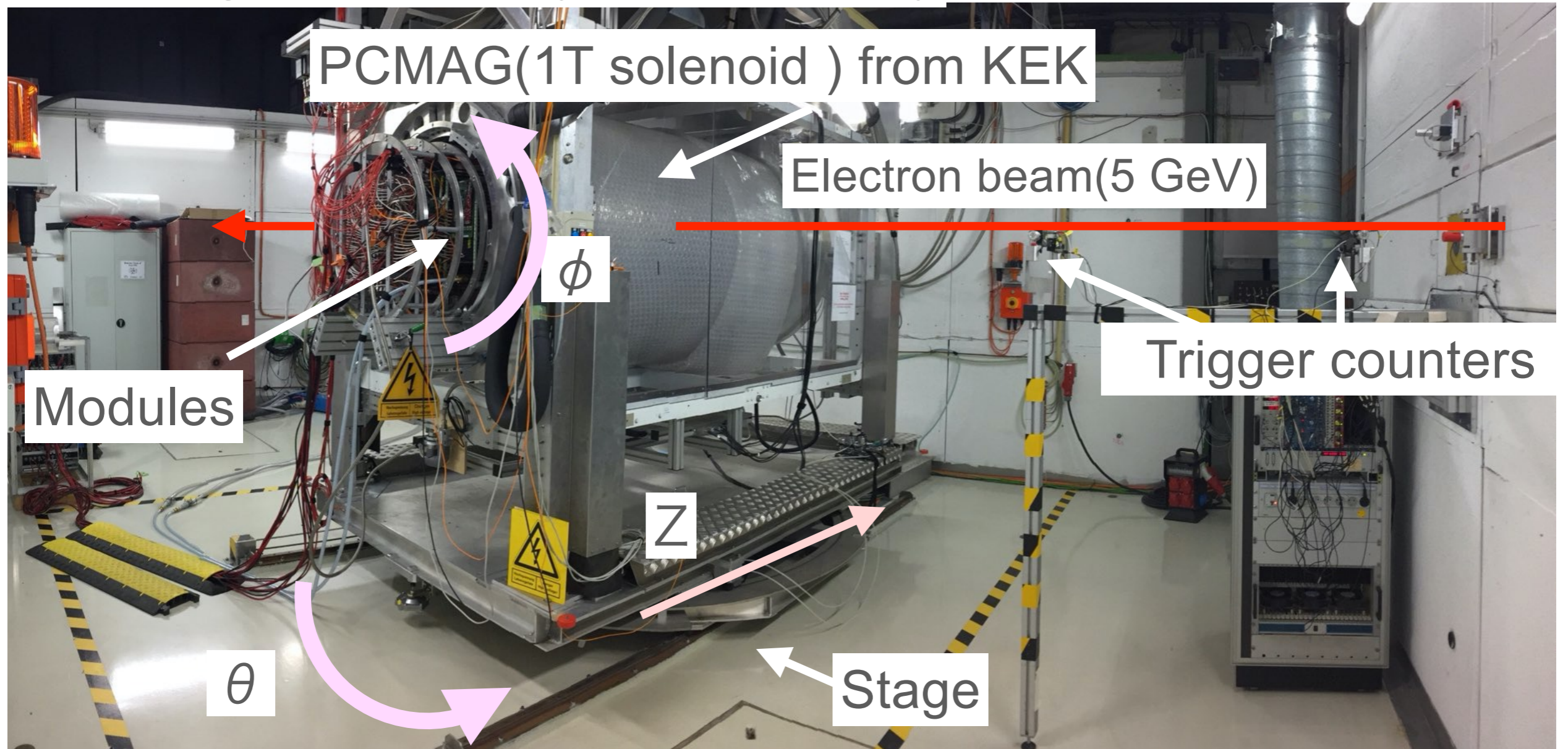
- Identify what makes hits expand
  - Check the another row data
  - Estimate diffusion in the GEM module
  - Check OT data

# Backup

# Setup



## DESY Large TPC Prototype Test Facility



PCMAG(1T solenoid ) from KEK

Electron beam(5 GeV)

Trigger counters

Modules

$\theta$

$\phi$

Z

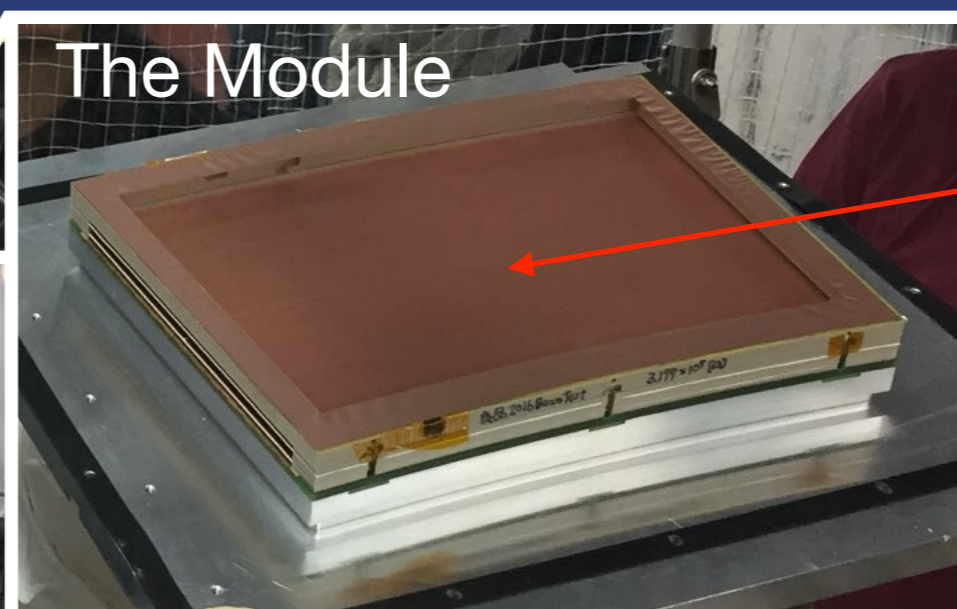
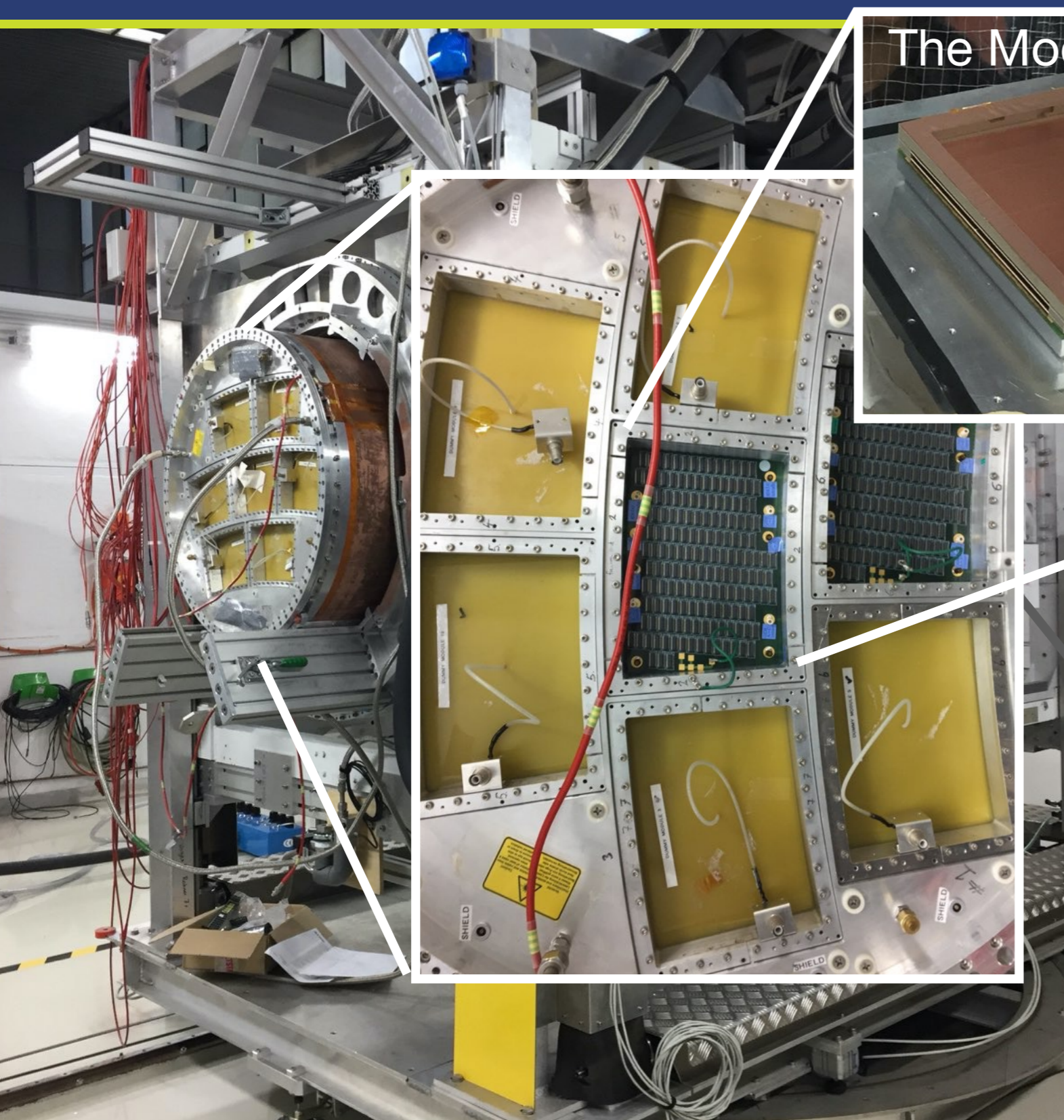
Stage

The electron beam passes two trigger counter and through the prototype.

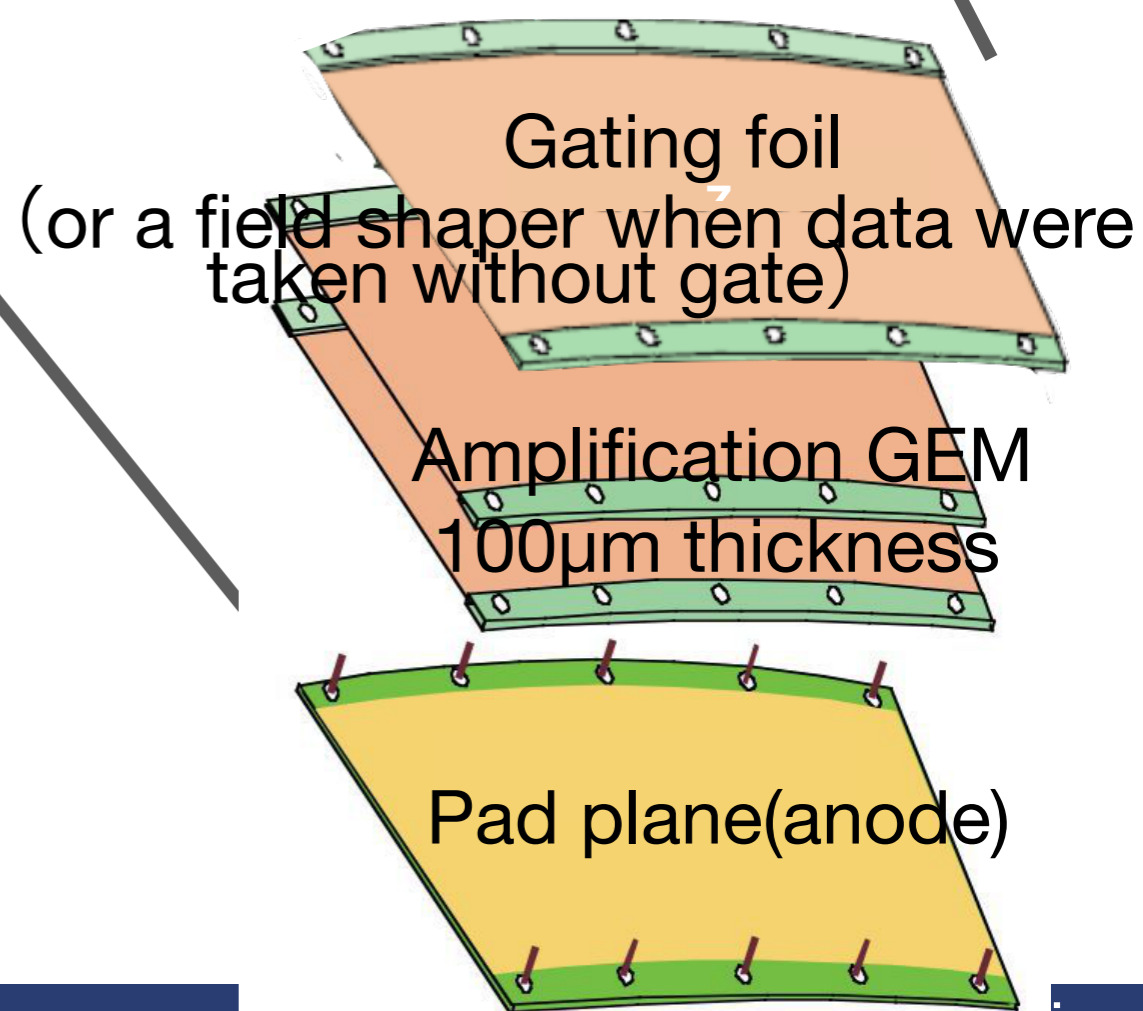
The sensitive volume of the TPC is inside a solenoid. The TPC is mounted on a movable stage so we can change drift distance(Z) and two angles,  $\theta$  and  $\phi$ .



# Module with Gating foil



Gating foil



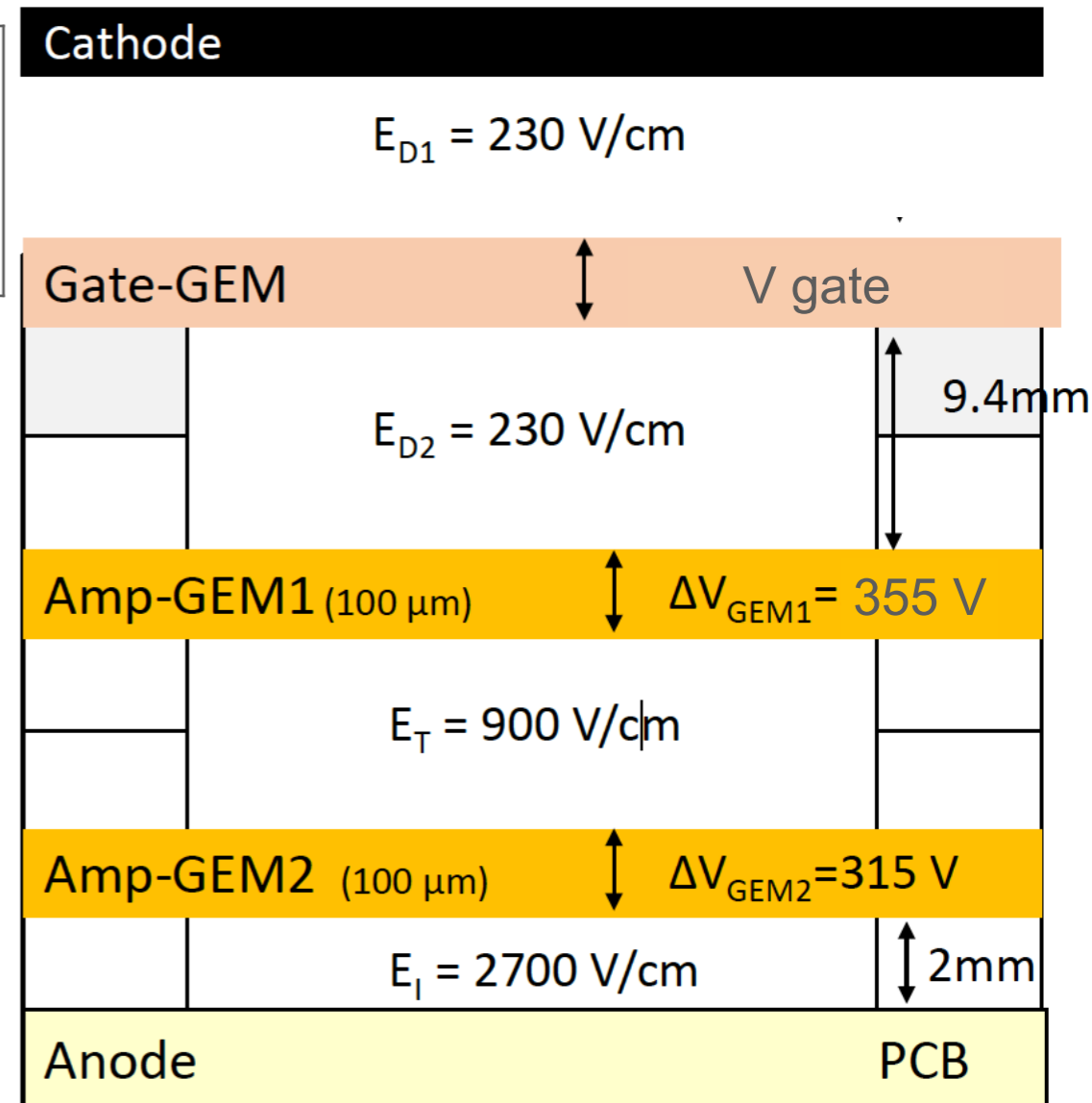


# The data I analyzed in this study



Center Module	with gatingGEM	without gatingGEM
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Z[cm] (Drift distance)	2.5,5,7.5,10,12.5,15,20 25,30,35,40,45,50,55
$\phi$ [degree]	0
$\theta$ [degree]	0
$V_{\text{gate}}$ [V]	3.5
B[T]	1



Beam: 5 GeV electron beam

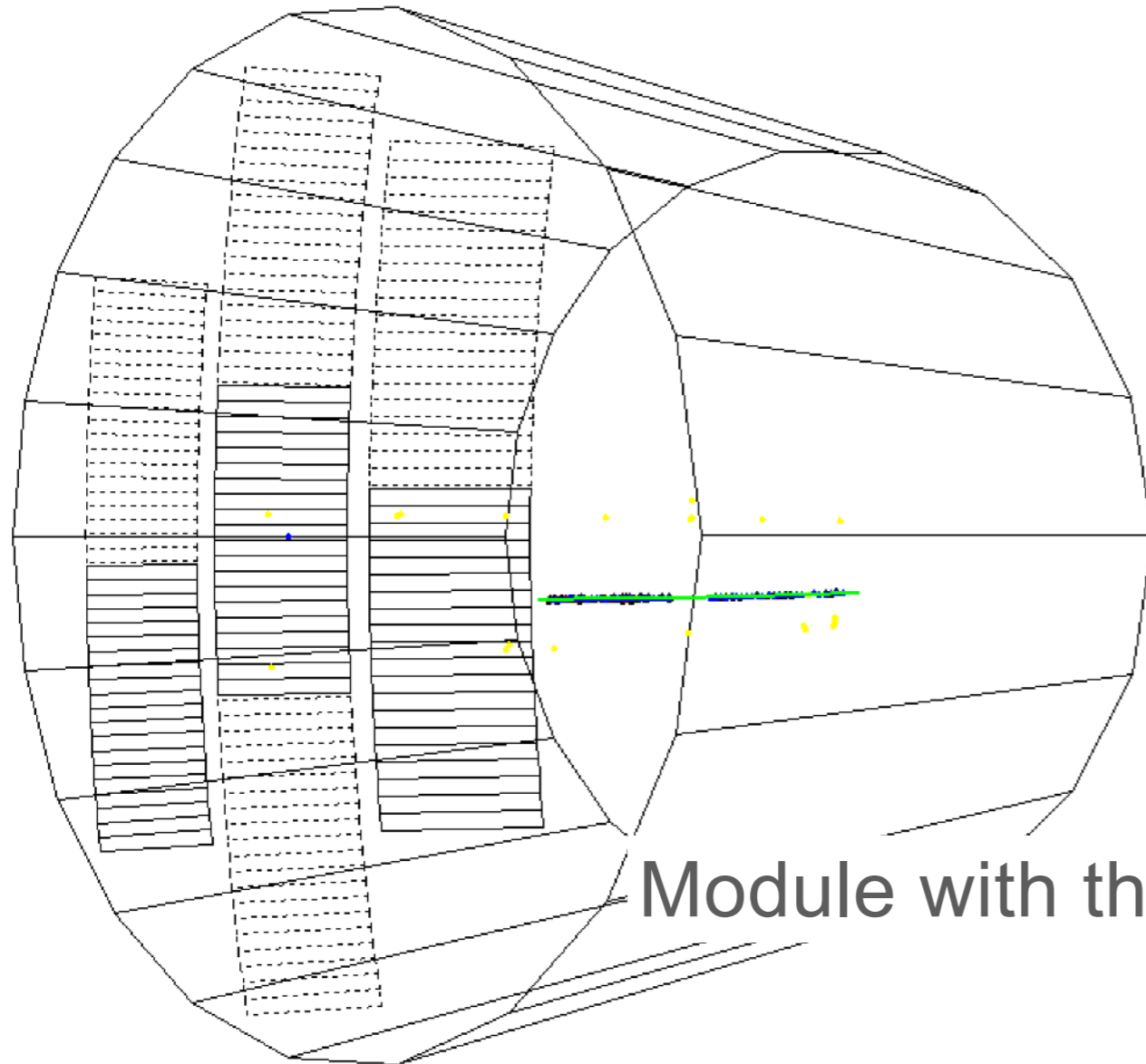
Gas:T2K gas (Ar : CF<sub>4</sub> : Iso-C<sub>4</sub>H<sub>10</sub> = 95 : 3 : 2 [%])

Flame work: yokaRowMon (20000event/1 run)

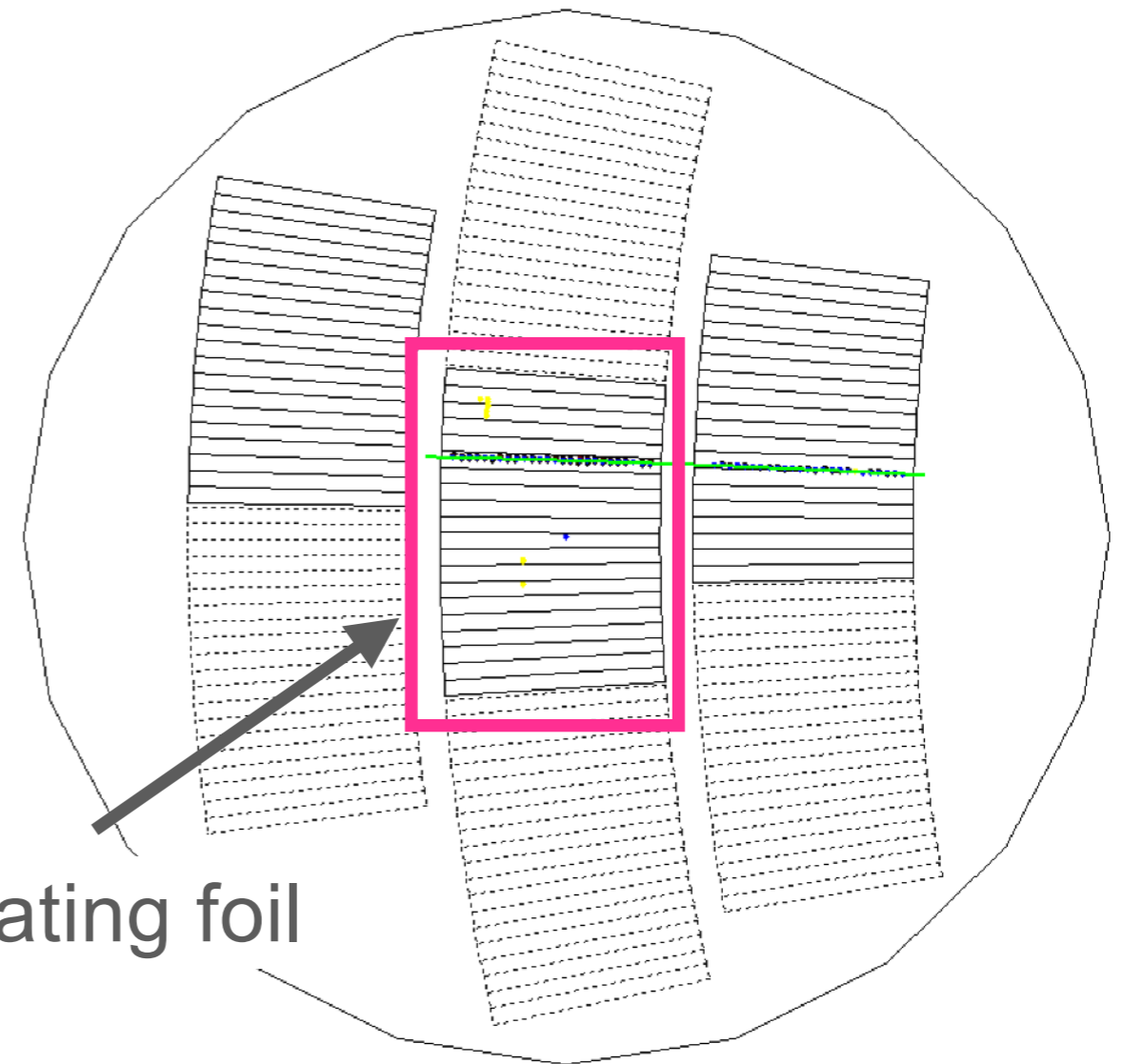
# Typical event



3D view



Projection onto the  $r\phi$  plane



The beam goes through our module with the gating foil in the region far enough from the module boundaries.

# Pad response ( $\sigma_{PR}$ )



The width of the pad response function ( $\sigma_{PR}$ ) is obtained as follows

First, we plot the charge fraction on each pad as a function of the distance of the pad center from the hit point. Then we fit this distribution to a Gaussian and get  $\sigma_{PR}$  as the standard deviation.

On the other hand,  $\sigma_{PR}$  can be expressed as follows

$$\sigma_{PR}^2 = \frac{w^2}{12} + \sigma_{PRF}^2 + C_d^2 z$$

