

# Probing a minimal $U(1)_X$ model at future $e^-e^+$ collider via the fermion pair production channels

Based on : 2104.10902

In collaboration with P. S. Bhupal Dev  
Yutaka Hosotani Sanjoy Mandal



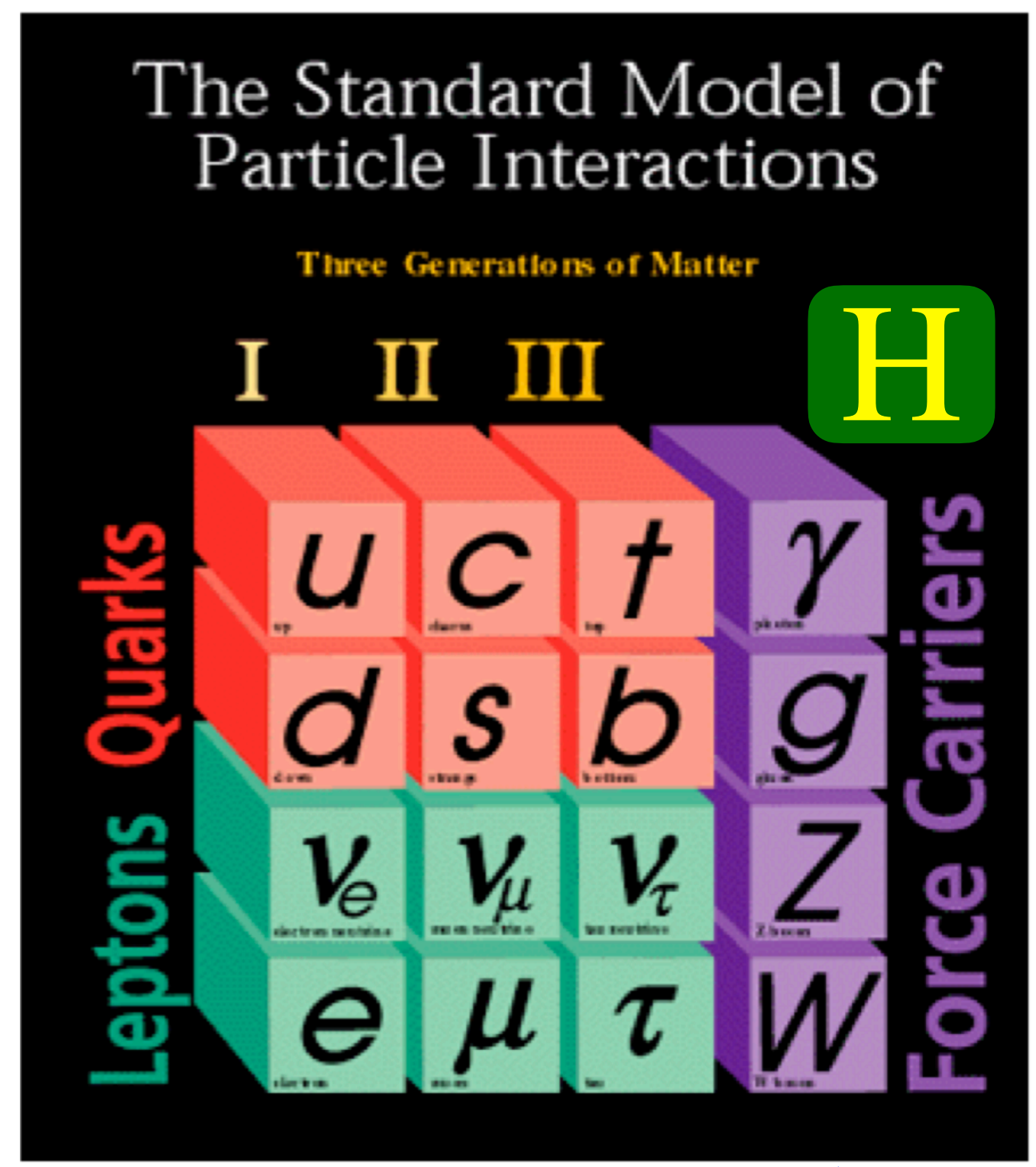
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The 72nd General Meeting of ILC Physics Subgroup

# Standard model and missing link/s



Over the decades experiments have found each and every missing pieces

Verified the facts that they belong to this family

Finally at the Large Hadron collider Higgs has been observed  
 → Its properties must be verified

Strongly established with interesting shortcomings  
 Few of the very interesting anomalies :

Tiny neutrino mass and flavor mixings  
 Relic abundance of dark matter ...

Neutrino oscillation experiment : SNO, Super - K, etc .

- Nature : Majorana/ Dirac
- Ordering : Normal/Inverted
- Nature of the mixing between the mass and the flavor eigenstates

Unknown

SM can not explain them

## Different physics frontiers

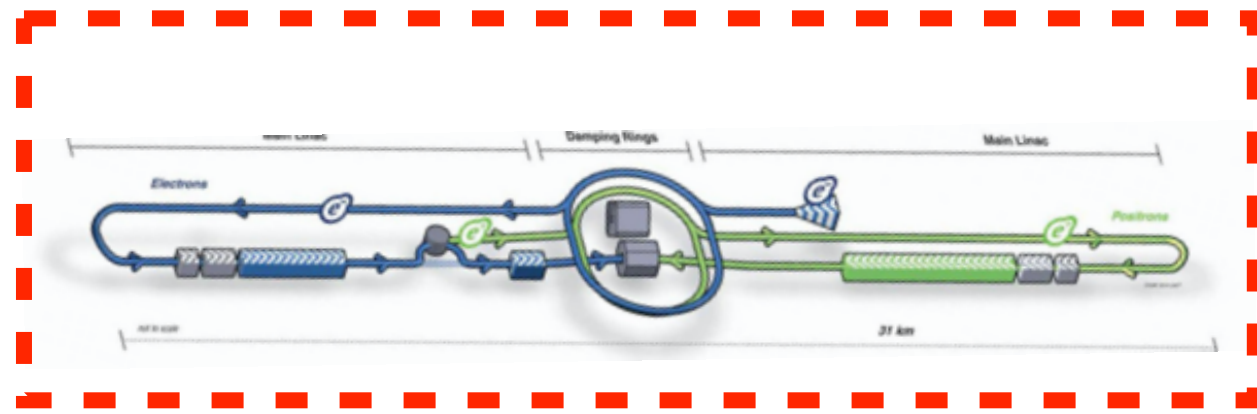
**Energy frontier** : Scientists build particle accelerators to explore high energy scale to explore new phenomena after the subatomic collisions .

**Intensity frontier** : Highly intense beams from accelerators are used to to investigate the ultra rare processes of nature .

**Cosmic frontier** : Astrophysicists use the cosmos as the laboratory to investigate the fundamental laws of physics from a complementary point of view of particle accelerator .

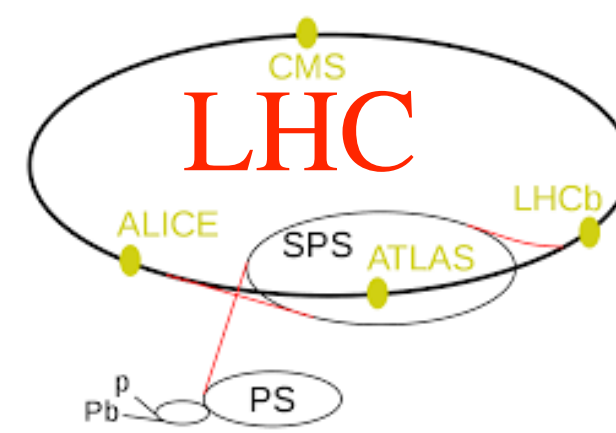
Future Circular Collider – hh/ee/eP

ILC

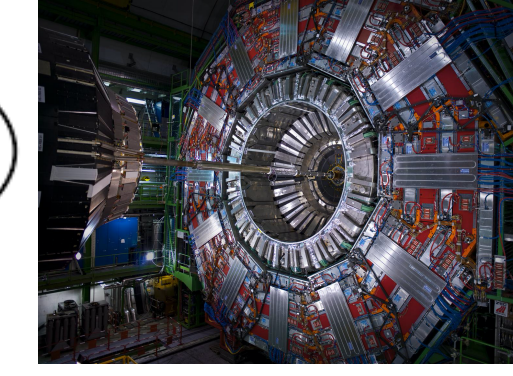


ENERGY FRONTIER

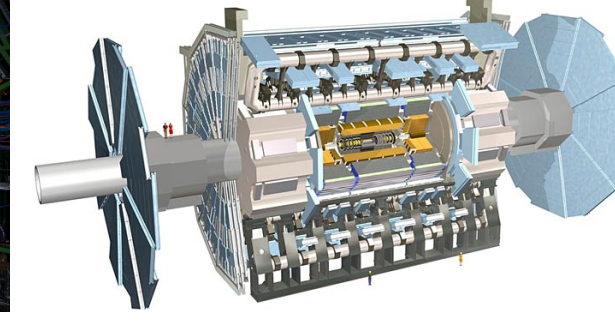
Origin of mass



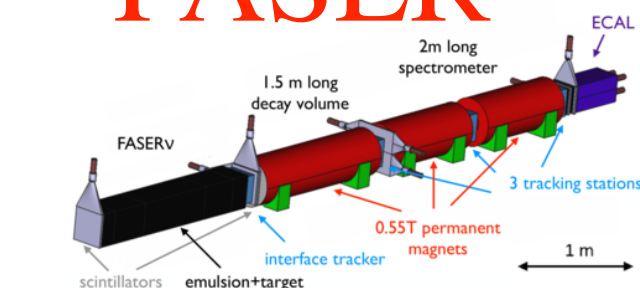
CMS



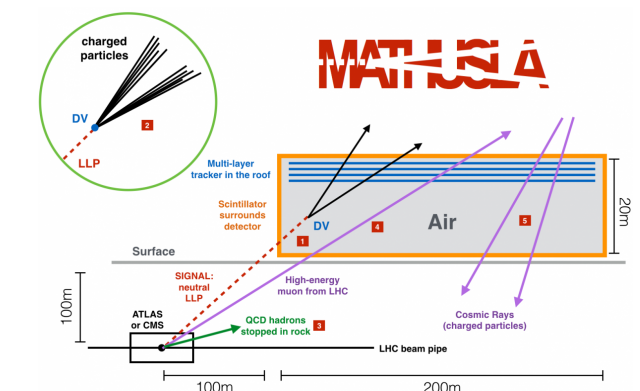
ATLAS



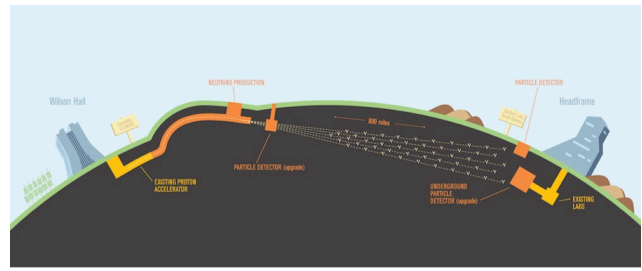
FASER



MATHUSLA



DUNE



Matter/ Antimatter Asymmetry

Dark Matter

Origin and evolution of the universe

Inflation

Unification of the forces

New physics Beyond the Standard Model

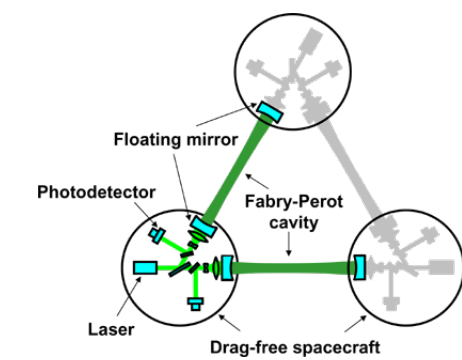
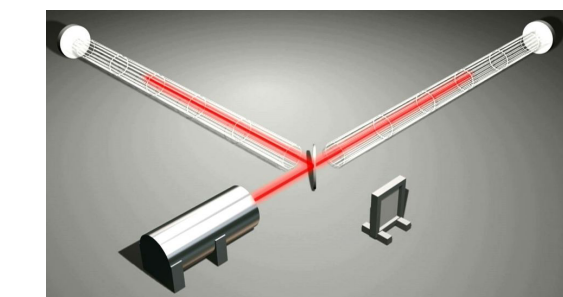
Dark Energy

Ground based telescopes

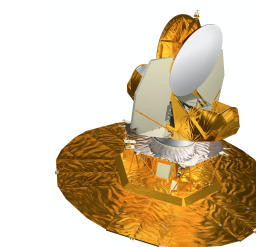


Interferometers

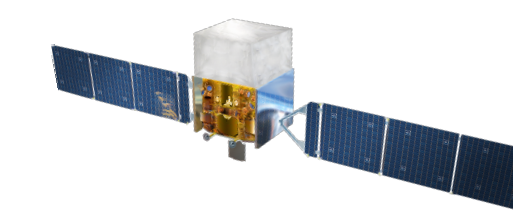
LIGO/ DECIGO



CMB/WMAP



Space Telescopes (FermiLAT)

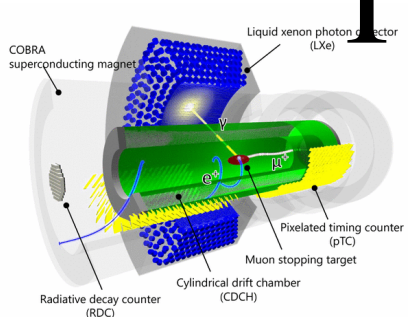


Neutrino Physics

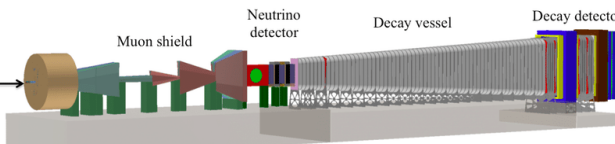
Proton Decay

Cosmic Particles

LFV(MEG, BaBar)



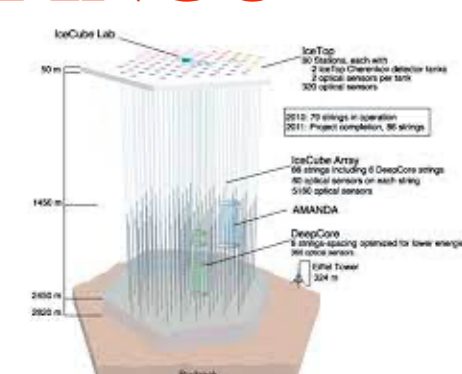
SHiP



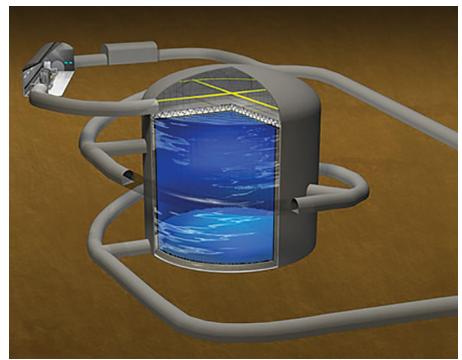
NA62



IecCube/PINGU



Hyper – K



# Proposal of a scenario

	SU(3) <sub>c</sub>	SU(2) <sub>L</sub>	U(1) <sub>Y</sub>	U(1) <sub>X</sub>	
$q_L^i$	<b>3</b>	<b>2</b>	$\frac{1}{6}$	$x'_q =$	$\frac{1}{6}x_H + \frac{1}{3}x_\Phi$
$u_R^i$	<b>3</b>	<b>1</b>	$\frac{2}{3}$	$x'_u =$	$\frac{2}{3}x_H + \frac{1}{3}x_\Phi$
$d_R^i$	<b>3</b>	<b>1</b>	$-\frac{1}{3}$	$x'_d =$	$-\frac{1}{3}x_H + \frac{1}{3}x_\Phi$
$\ell_L^i$	<b>1</b>	<b>2</b>	$-\frac{1}{2}$	$x'_\ell =$	$-\frac{1}{2}x_H - x_\Phi$
$e_R^i$	<b>1</b>	<b>1</b>	$-1$	$x'_e =$	$-x_H - x_\Phi$
$N_R^i$	<b>1</b>	<b>1</b>	$0$	$x'_\nu =$	$-x_\Phi$
$H$	<b>1</b>	<b>2</b>	$-\frac{1}{2}$	$-\frac{x_H}{2} =$	$-\frac{x_H}{2}$
$\Phi$	<b>1</b>	<b>1</b>	$0$	$2x_\Phi =$	$2x_\Phi$

Before anomaly cancellation

## Relevant part of the Yukawa sector

$$\mathcal{L}^{\text{Yukawa}} = -Y_u^{\alpha\beta} \bar{q}_L^\alpha H u_R^\beta - Y_d^{\alpha\beta} \bar{q}_L^\alpha \tilde{H} d_R^\beta - Y_e^{\alpha\beta} \bar{\ell}_L^\alpha \tilde{H} e_R^\beta - Y_\nu^{\alpha\beta} \bar{\ell}_L^\alpha H N_R^\beta - Y_N^\alpha \Phi \bar{N}_R^{\alpha c} N_R^\alpha + \text{h.c.}$$

## Anomaly cancellation conditions

$$\begin{aligned} \text{U(1)}_X \otimes [\text{SU(3)}_c]^2 & : & 2x'_q - x'_u - x'_d & = 0, \\ \text{U(1)}_X \otimes [\text{SU(2)}_L]^2 & : & 3x'_q + x'_\ell & = 0, \\ \text{U(1)}_X \otimes [\text{U(1)}_Y]^2 & : & x'_q - 8x'_u - 2x'_d + 3x'_\ell - 6x'_e & = 0, \\ [\text{U(1)}_X]^2 \otimes \text{U(1)}_Y & : & x'^2_q - 2x'^2_u + x'^2_d - x'^2_\ell + x'^2_e & = 0, \\ [\text{U(1)}_X]^3 & : & 6x'^3_q - 3x'^3_u - 3x'^3_d + 2x'^3_\ell - x'^3_\nu - x'^3_e & = 0, \\ \text{U(1)}_X \otimes [\text{grav.}]^2 & : & 6x'_q - 3x'_u - 3x'_d + 2x'_\ell - x'_\nu - x'_e & = 0. \end{aligned}$$

After anomaly cancellation

Linear combination of  $\text{U(1)}_Y$  and  $\text{U(1)}_{B-L}$

## Higgs potential

$$V = m_h^2(H^\dagger H) + \lambda(H^\dagger H)^2 + m_\Phi^2(\Phi^\dagger\Phi) + \lambda_\Phi(\Phi^\dagger\Phi)^2 + \lambda'(H^\dagger H)(\Phi^\dagger\Phi)$$

$U(1)_X$  breaking

Electroweak breaking

$$\langle\Phi\rangle = \frac{v_\Phi + \phi}{\sqrt{2}} \quad \langle H\rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} v+h \\ 0 \end{pmatrix} \quad v \simeq 246 \text{ GeV}, v_\Phi \gg v_h$$

Mass of the neutral gauge boson  $Z'$

$$M_{Z'} = g' \sqrt{4v_\Phi^2 + \frac{1}{4}x_H^2 v_h^2} \simeq 2g'v_\Phi.$$

Neutrino mass

$$\mathcal{L}^{\text{mass}} = -Y_\nu^{\alpha\beta} \bar{\ell}_L^\alpha H N_R^\beta - Y_N^\alpha \Phi \bar{N}_R^{\alpha c} N_R^\alpha + \text{h.c.} \quad U(1)_X \text{ breaking}$$

$$m_{N_\alpha} = \frac{Y_N^\alpha}{\sqrt{2}} v_\Phi, \quad m_D^{\alpha\beta} = \frac{Y_\nu^{\alpha\beta}}{\sqrt{2}} v, \quad m_\nu^{\text{mass}} = \begin{pmatrix} 0 & m_D \\ m_D^T & m_N \end{pmatrix} \quad m_\nu \simeq -m_D m_N^{-1} m_D^T$$

**Seesaw mechanism**

can explain the origin of the light neutrino mass and can be tested at the experiments

# Z' interactions

Interaction between the quarks and Z'  $\mathcal{L}^q = -g'(\bar{q}\gamma_\mu q_{x_L}^q P_L q + \bar{q}\gamma_\mu q_{x_R}^q P_R q)Z'_\mu$

Interaction between the leptons and Z'  $\mathcal{L}^\ell = -g'(\bar{\ell}\gamma_\mu \ell_{x_L}^\ell P_L \ell + \bar{\ell}\gamma_\mu \ell_{x_R}^\ell P_R \ell)Z'_\mu$

$q_{x_L}^f \neq q_{x_R}^f$  affects the phenomenology

## Partial decay width

Charged fermions  $\Gamma(Z' \rightarrow 2f) = N_c \frac{M_{Z'}}{24\pi} \left( g_L^f [g', x_H, x_\Phi]^2 + g_R^f [g', x_H, x_\Phi]^2 \right)$

light neutrinos  $\Gamma(Z' \rightarrow 2\nu) = \frac{M_{Z'}}{24\pi} g_L^\nu [g', x_H, x_\Phi]^2$

heavy neutrinos  $\Gamma(Z' \rightarrow 2N) = \frac{M_{Z'}}{24\pi} g_R^N [g', x_\Phi]^2 \left( 1 - 4 \frac{m_N^2}{M_{Z'}^2} \right)^{\frac{3}{2}}$

# Implications of the choices of $x_H$ keeping $x_\Phi = 1$

No interaction with  $e_R$

No interaction with  $d_R$

	SU(3) <sub>c</sub>	SU(2) <sub>L</sub>	U(1) <sub>Y</sub>	U(1) <sub>X</sub>	-2	-1	-0.5	0	0.5	1	2
					U(1) <sub>R</sub>						
								B-L			
$q_L^i$	<b>3</b>	<b>2</b>	$\frac{1}{6}$	$x'_q = \frac{1}{6}x_H + \frac{1}{3}x_\Phi$	0	$\frac{1}{6}$	$\frac{1}{4}$	$\frac{1}{3}$	$\frac{5}{12}$	$\frac{1}{2}$	$\frac{1}{3}$
$u_R^i$	<b>3</b>	<b>1</b>	$\frac{2}{3}$	$x'_u = \frac{2}{3}x_H + \frac{1}{3}x_\Phi$	-1	$-\frac{1}{3}$	0	$\frac{1}{3}$	$\frac{1}{2}$	1	$\frac{5}{3}$
$d_R^i$	<b>3</b>	<b>1</b>	$-\frac{1}{3}$	$x'_d = -\frac{1}{3}x_H + \frac{1}{3}x_\Phi$	1	$\frac{2}{3}$	$\frac{1}{2}$	$\frac{1}{3}$	$\frac{1}{6}$	0	$-\frac{1}{3}$
$\ell_L^i$	<b>1</b>	<b>2</b>	$-\frac{1}{2}$	$x'_\ell = -\frac{1}{2}x_H - x_\Phi$	0	$-\frac{1}{2}$	$-\frac{3}{4}$	-1	$\frac{5}{4}$	$-\frac{3}{2}$	-2
$e_R^i$	<b>1</b>	<b>1</b>	-1	$x'_e = -x_H - x_\Phi$	1	0	$-\frac{1}{2}$	-1	$-\frac{3}{2}$	-2	-3
$N_R^i$	<b>1</b>	<b>1</b>	0	$x'_\nu = -x_\Phi$	-1	-1	-1	-1	-1	-1	-1
$H$	<b>1</b>	<b>2</b>	$-\frac{1}{2}$	$-\frac{x_H}{2} = -\frac{x_H}{2}$	1	$\frac{1}{2}$	$\frac{1}{2}$	0	$\frac{1}{4}$	$\frac{1}{4}$	1
$\Phi$	<b>1</b>	<b>1</b>	0	$2x_\Phi = 2x_\Phi$	2	2	2	2	2	2	2

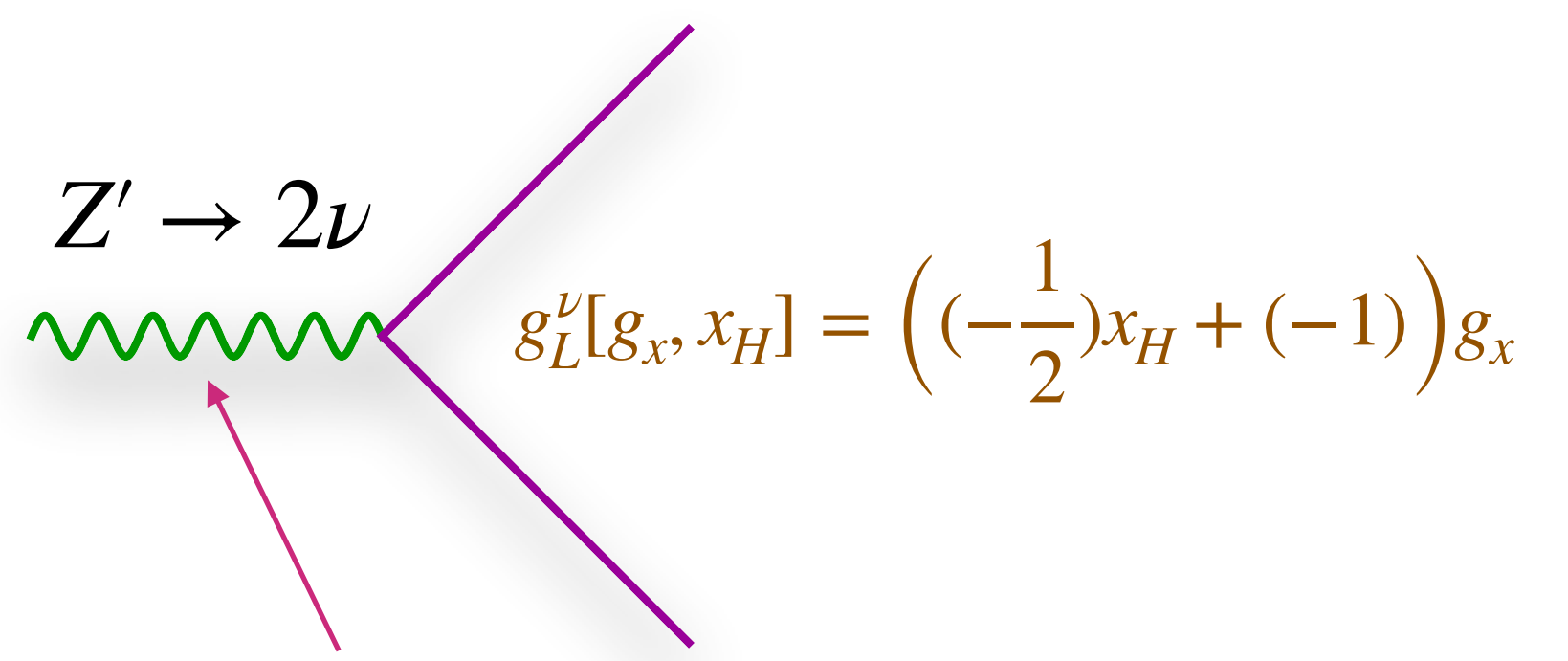
No interaction with left handed fermions

No interaction with  $u_R$

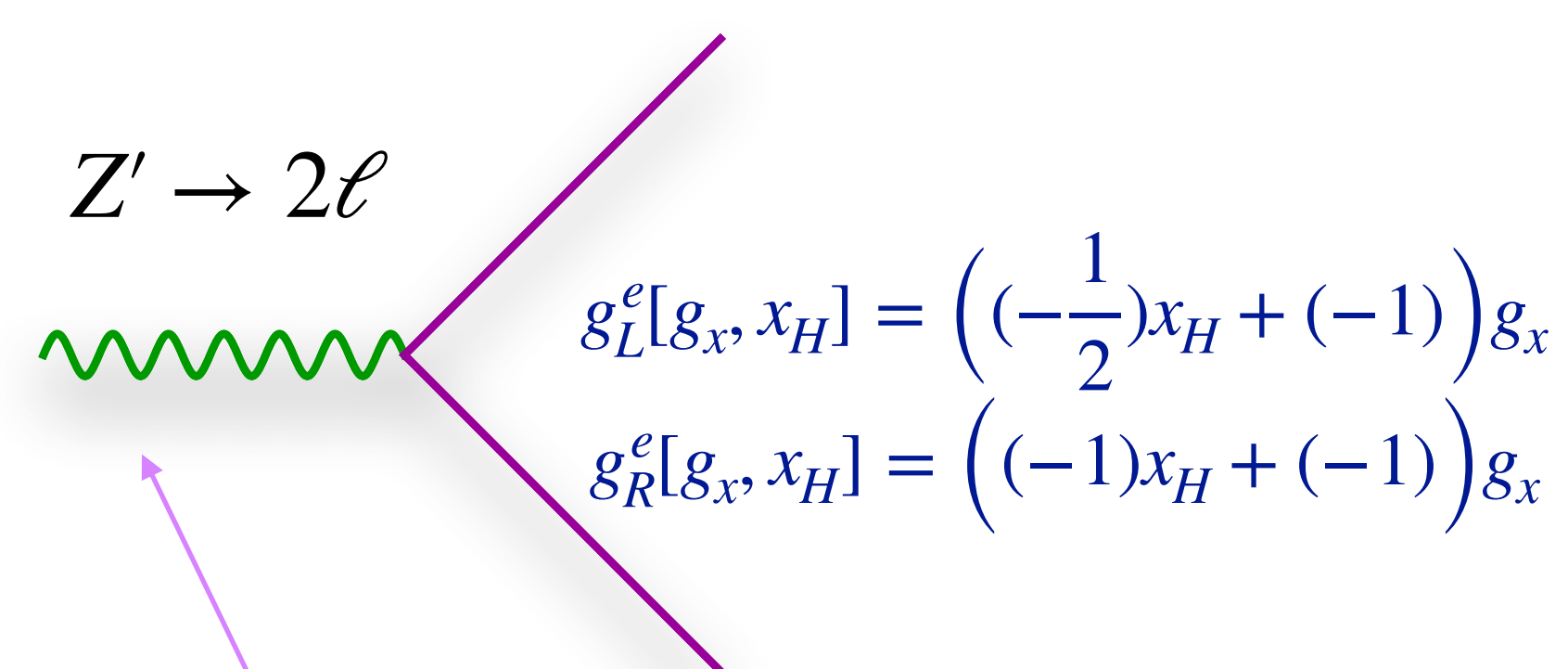


# Partial decay widths of $Z'$

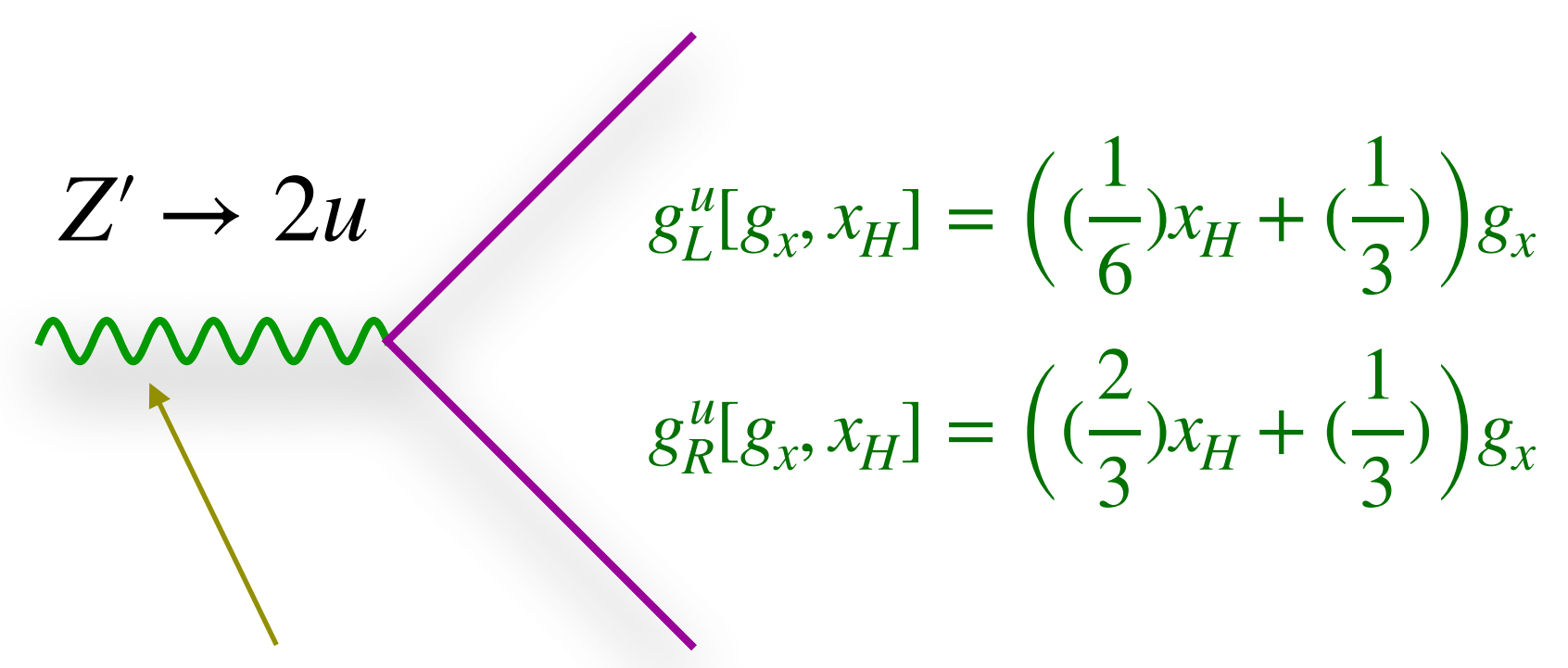
$$x_\Phi = 1$$



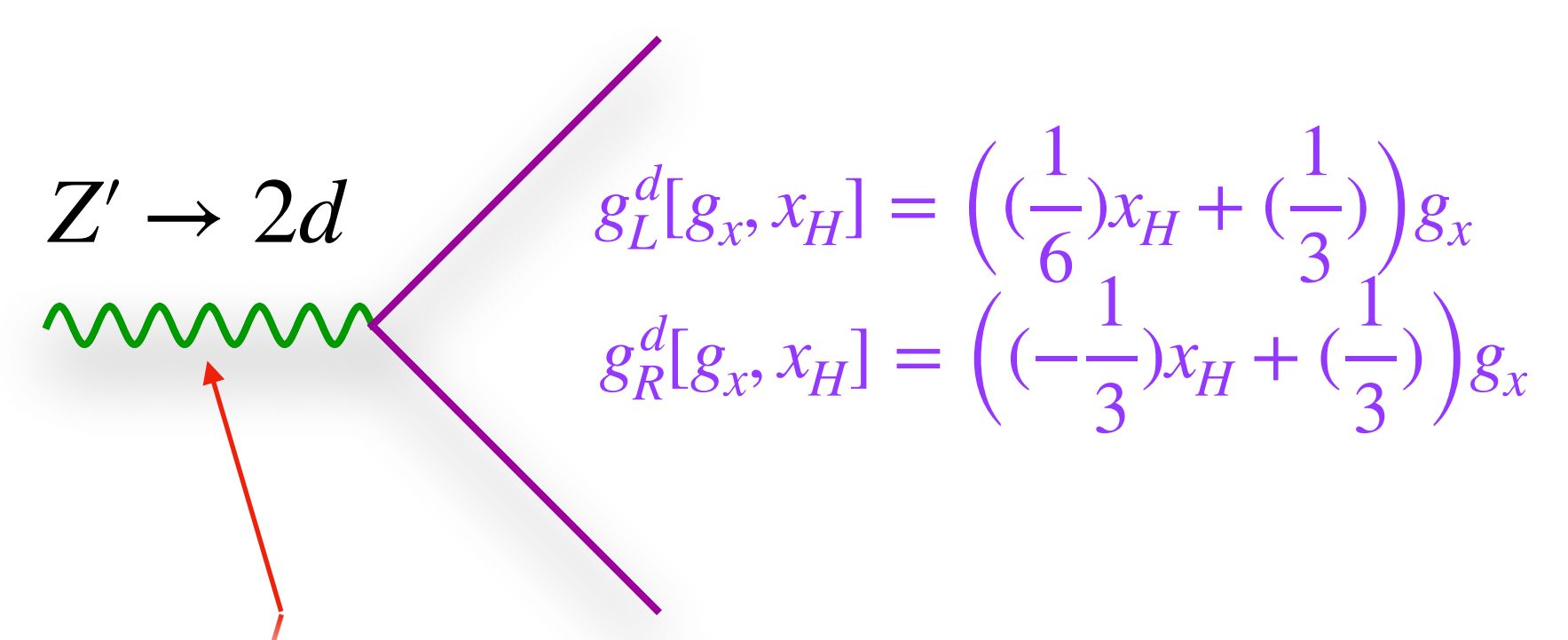
$$\Gamma[Z' \rightarrow 2\nu] = \frac{M_{Z'}}{24\pi} g_L^\nu[g_x, x_H]^2$$



$$\Gamma[Z' \rightarrow 2\ell] = \frac{M_{Z'}}{24\pi} (g_L^e[g_x, x_H]^2 + g_R^e[g_x, x_H]^2)$$



$$\Gamma[Z' \rightarrow 2u] = \frac{M_{Z'}}{24\pi} (g_L^u[g_x, x_H]^2 + g_R^u[g_x, x_H]^2)$$



$$\Gamma[Z' \rightarrow 2d] = \frac{M_{Z'}}{24\pi} (g_L^d[g_x, x_H]^2 + g_R^d[g_x, x_H]^2)$$

# Properties of the model and phenomenology

## New particles

$Z'$  boson

Heavy Majorana Neutrino

$U(1)_X$  Higgs boson

## Phenomenology

$Z'$  boson production and decay

$Z'$  boson mediated processes

Jurina Nakajima's talk

**Heavy neutrino production**

$U(1)_X$  Higgs phenomenology : Vacuum Stability

Dark Matter

collider

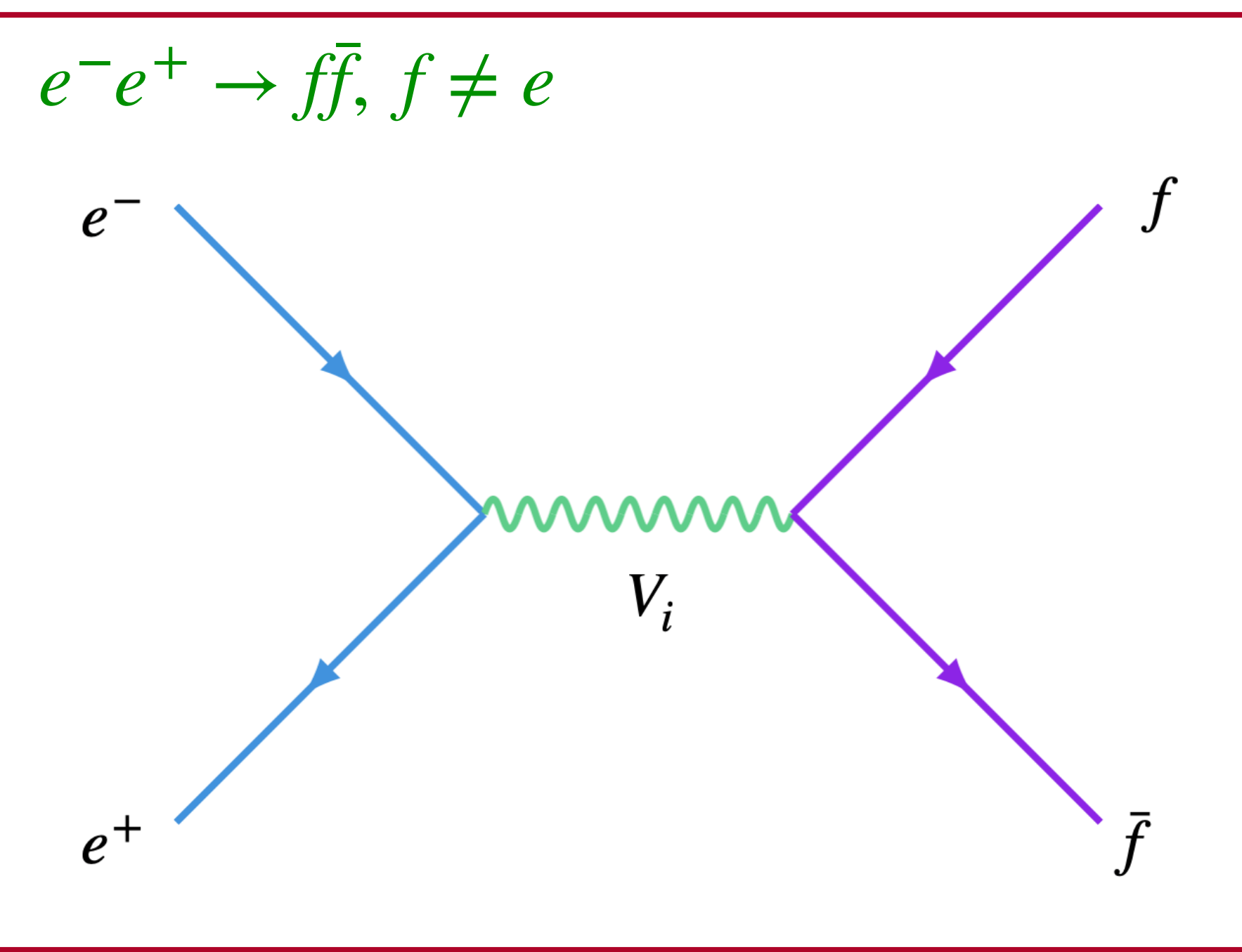
Leptogenesis and many more

Fermionic pair production from the  $Z'$

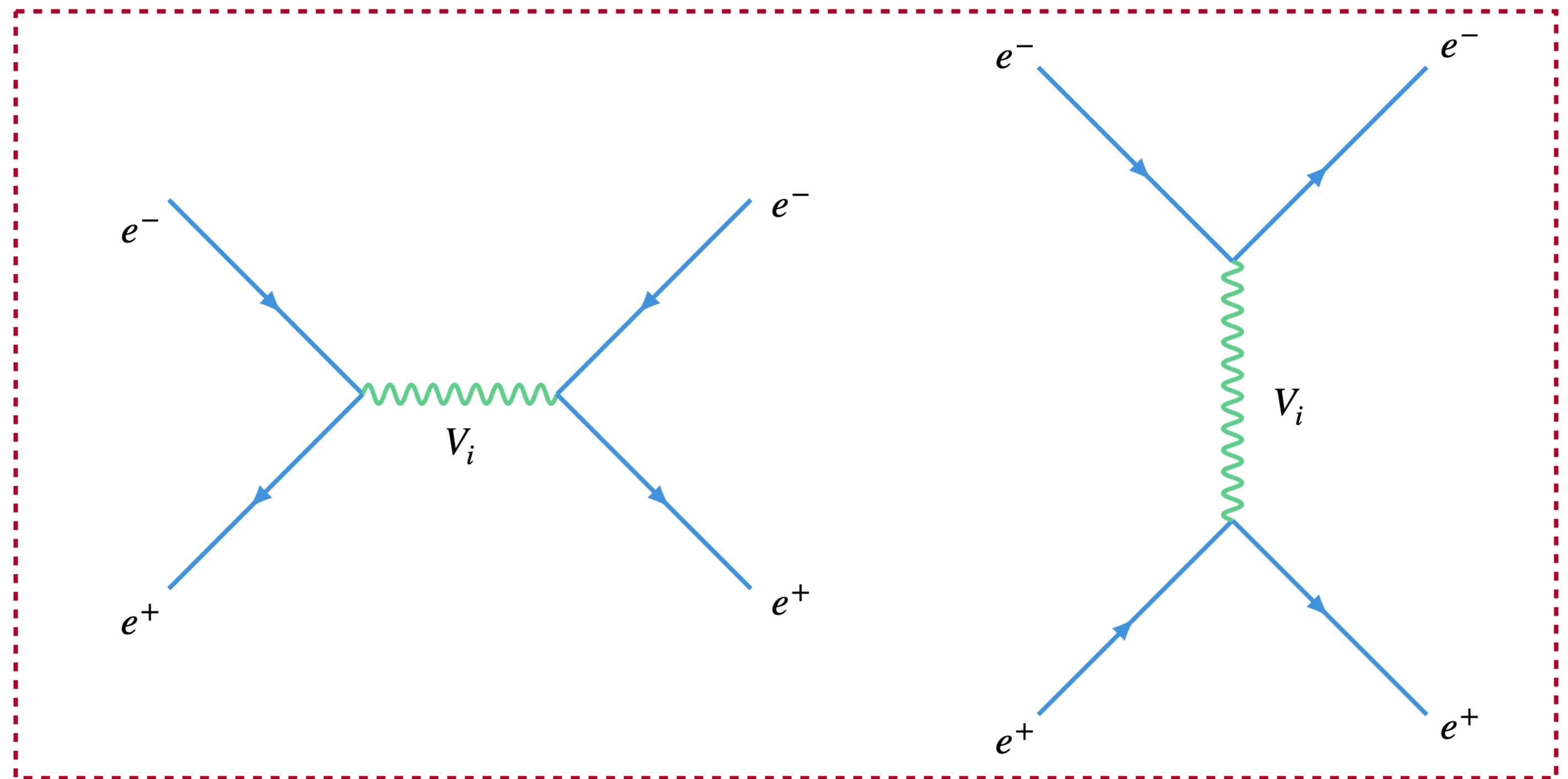
# Fermionic pair production from the $Z'$

New particles  $Z'$  boson Heavy Majorana Neutrino  $U(1)_X$  Higgs boson  
 Phenomenology  $Z'$  boson production and decay Heavy neutrino production  
 Dark Matter collider  $U(1)_X$  Higgs phenomenology : Vacuum Stability  
 Leptogenesis and many more

## Bhabha scattering



$V_i = \{\gamma, Z, Z'\}$



# Limits on the model parameters

Considering the limit  $M_{Z'} \gg \sqrt{s}$  and applying effective theory we find the limits on  $\frac{M_{Z'}}{g'}$  using **LEP – II (1302.3415)** and **(prospective) ILC (1908.11299)** :

$$\frac{\pm 4\pi}{(1 + \delta_{ef})(\Lambda_{AB}^{f\pm})^2} (\bar{e}\gamma_\mu P_A e) (\bar{f}\gamma_\mu P_B f)$$

$Z'$  exchange matrix element for our process

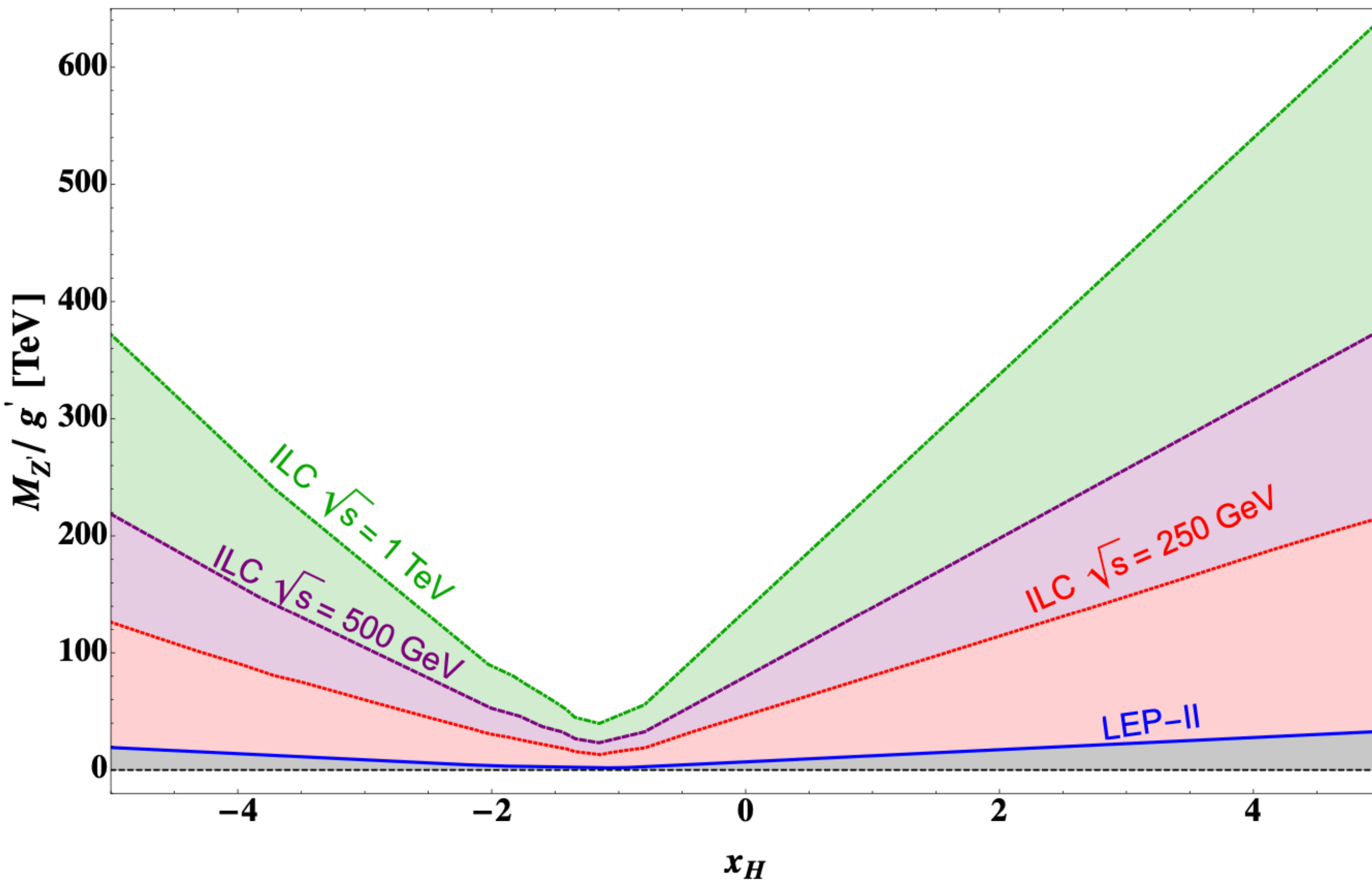
$$\frac{(g')^2}{M_{Z'}^2 - s} [\bar{e}\gamma_\mu (x_{l'} P_L + x_{e'} P_R) e] [\bar{f}\gamma_\mu (x_{fL} P_L + x_{fR} P_R) f]$$

Matching the above equations we obtain

$$M_{Z'}^2 - s \geq \frac{g'^2}{4\pi} |x_{e_A} x_{f_B}| (\Lambda_{AB}^{f\pm})^2$$

Indicates a large VEV scale can be probed from LEP – II to ILC1000 via ILC250 and ILC500

Shows limits on  $M_{Z'}$  vs  $g'$  for **LEP – II, ILC250, ILC500 and ILC1000**

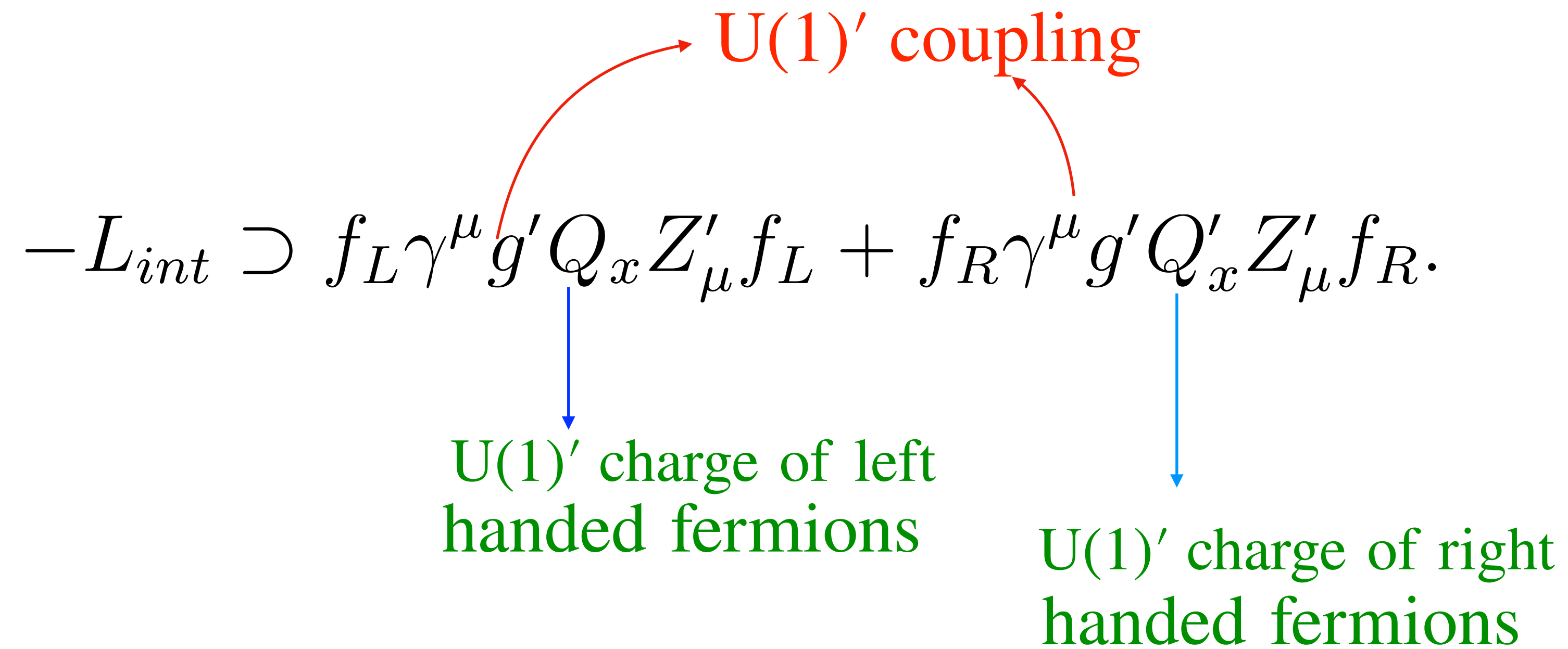


Limits on  $M_{Z'}$  and  $g'$  can also be obtained from dilepton and dijet searches at the LHC

$$g' = \sqrt{g_{\text{Model}}^2 \left( \frac{\sigma_{\text{ATLAS}}^{\text{Obs.}}}{\sigma_{\text{Model}}} \right)}$$

# Interaction between fermions and $Z'$

$$-L_{int} \supset f_L \gamma^\mu g' Q_x Z'_\mu f_L + f_R \gamma^\mu g' Q'_x Z'_\mu f_R.$$



$U(1)'$  coupling

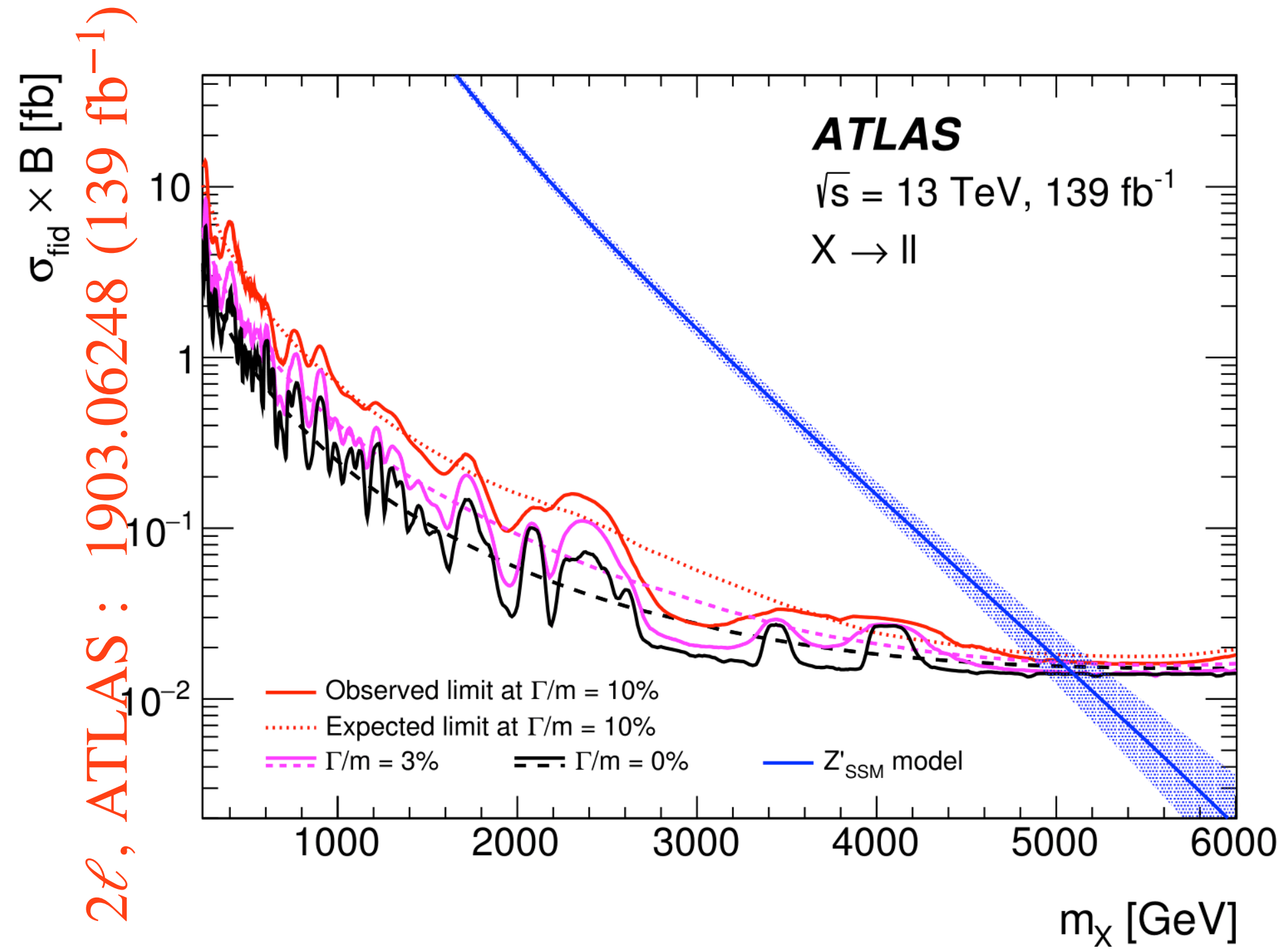
$U(1)'$  charge of left handed fermions

$U(1)'$  charge of right handed fermions

We compare dilepton production cross section with the dilepton production at the ATLAS

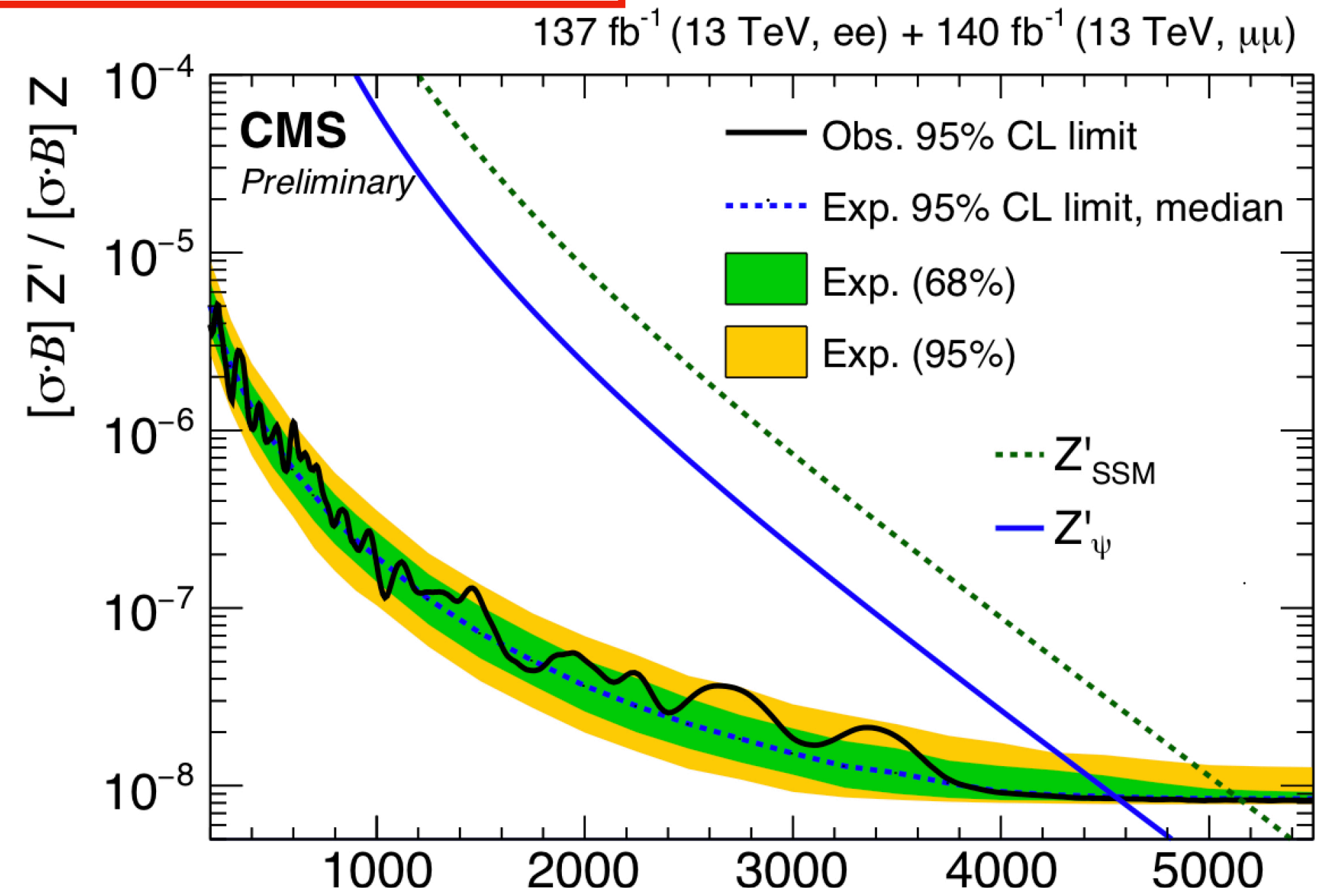
$$g' = \sqrt{\frac{\sigma_{\text{ATLAS}}^{\text{Observed}}}{\left(\frac{\sigma_{\text{Model}}}{g_{\text{Model}}^2}\right)}}$$

# Recent bounds on the heavy $Z'$ from dilepton channel

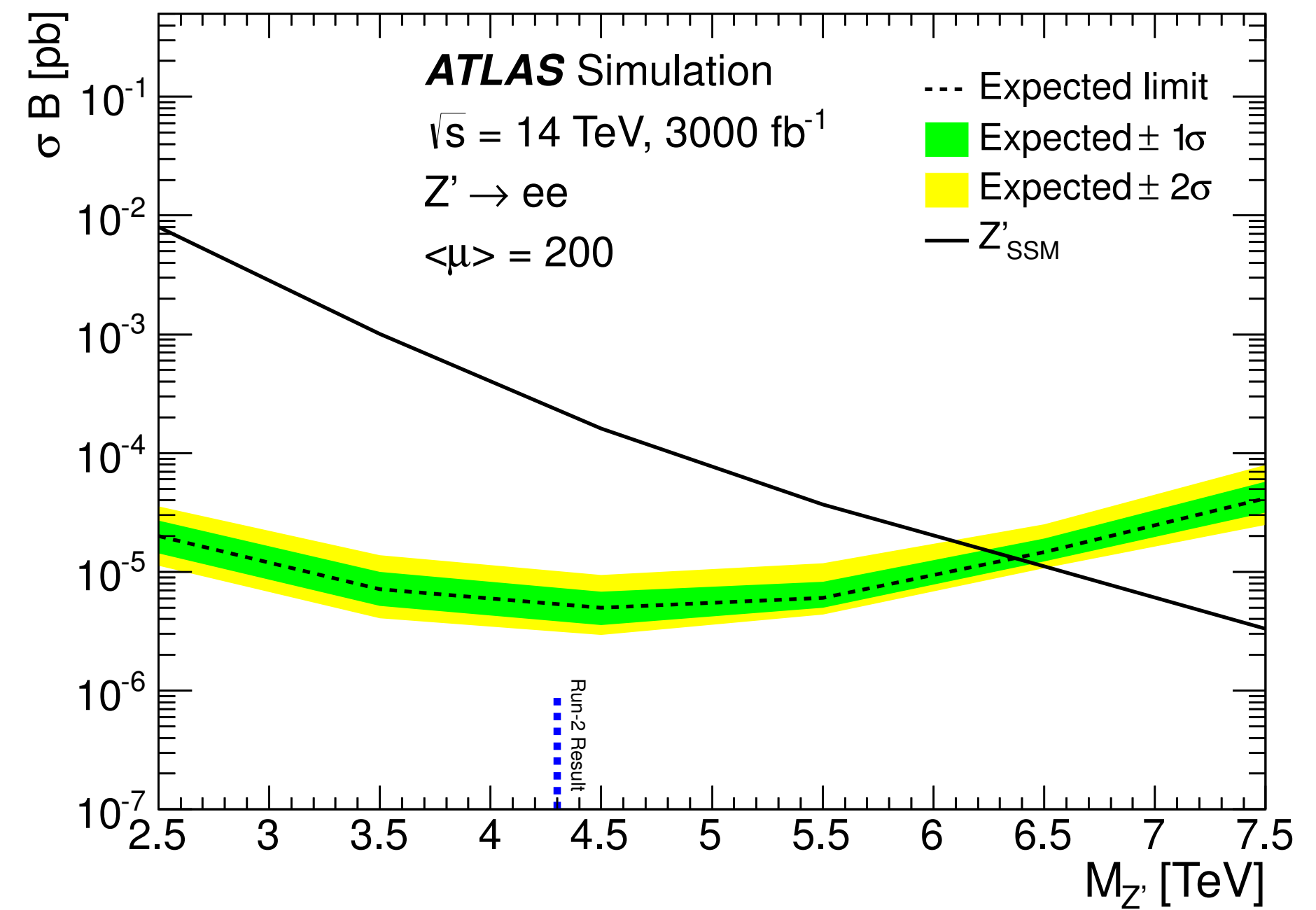


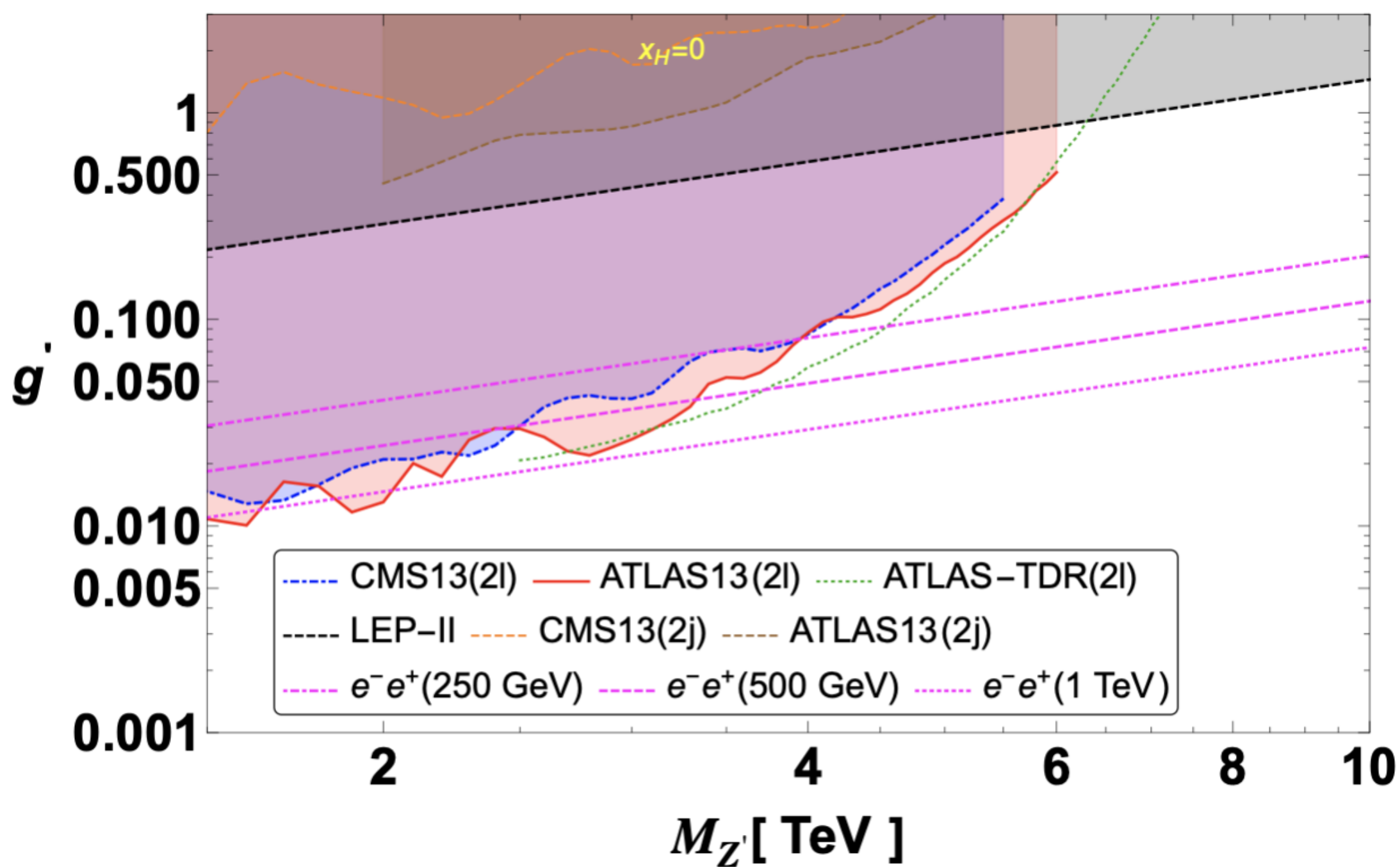
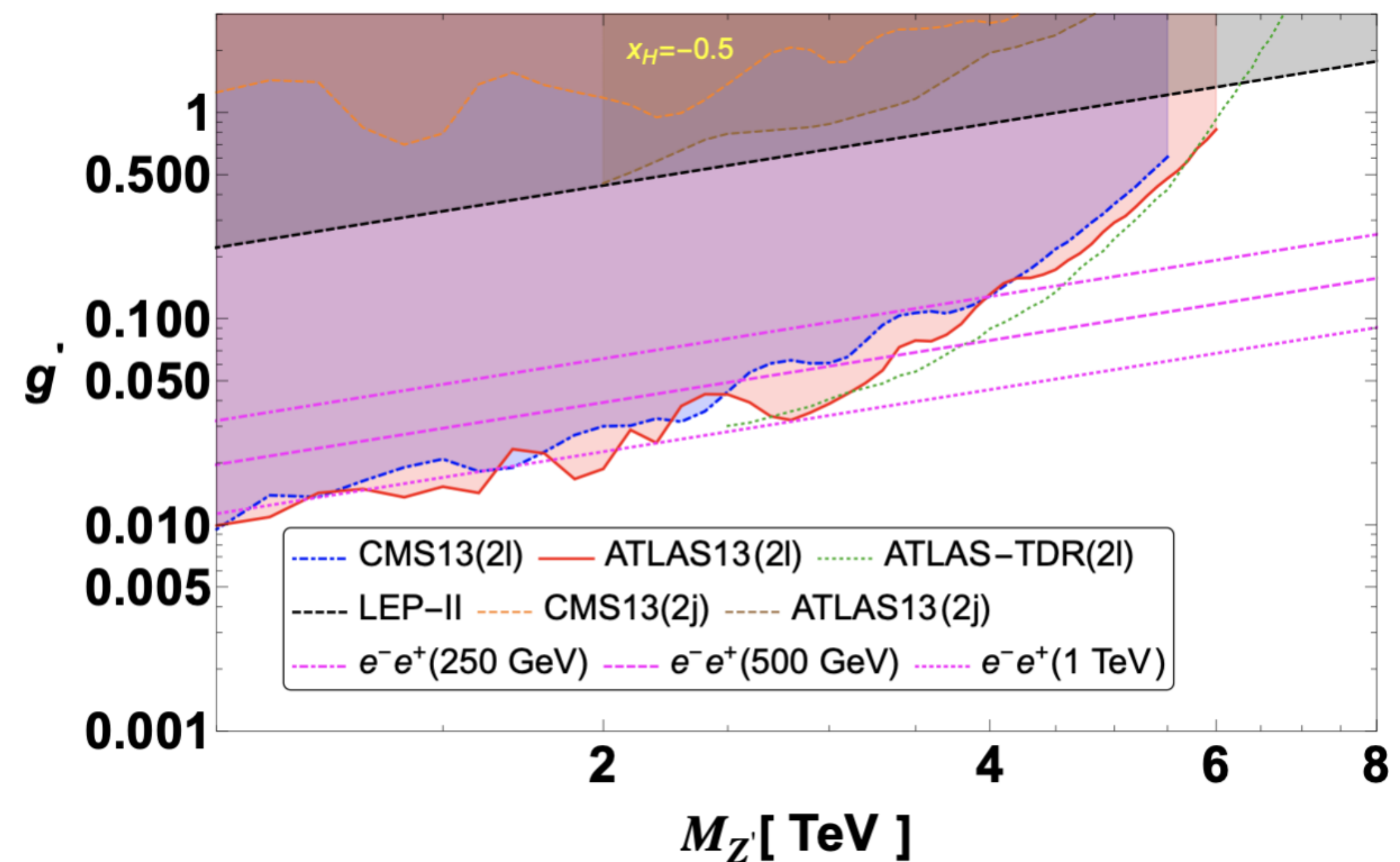
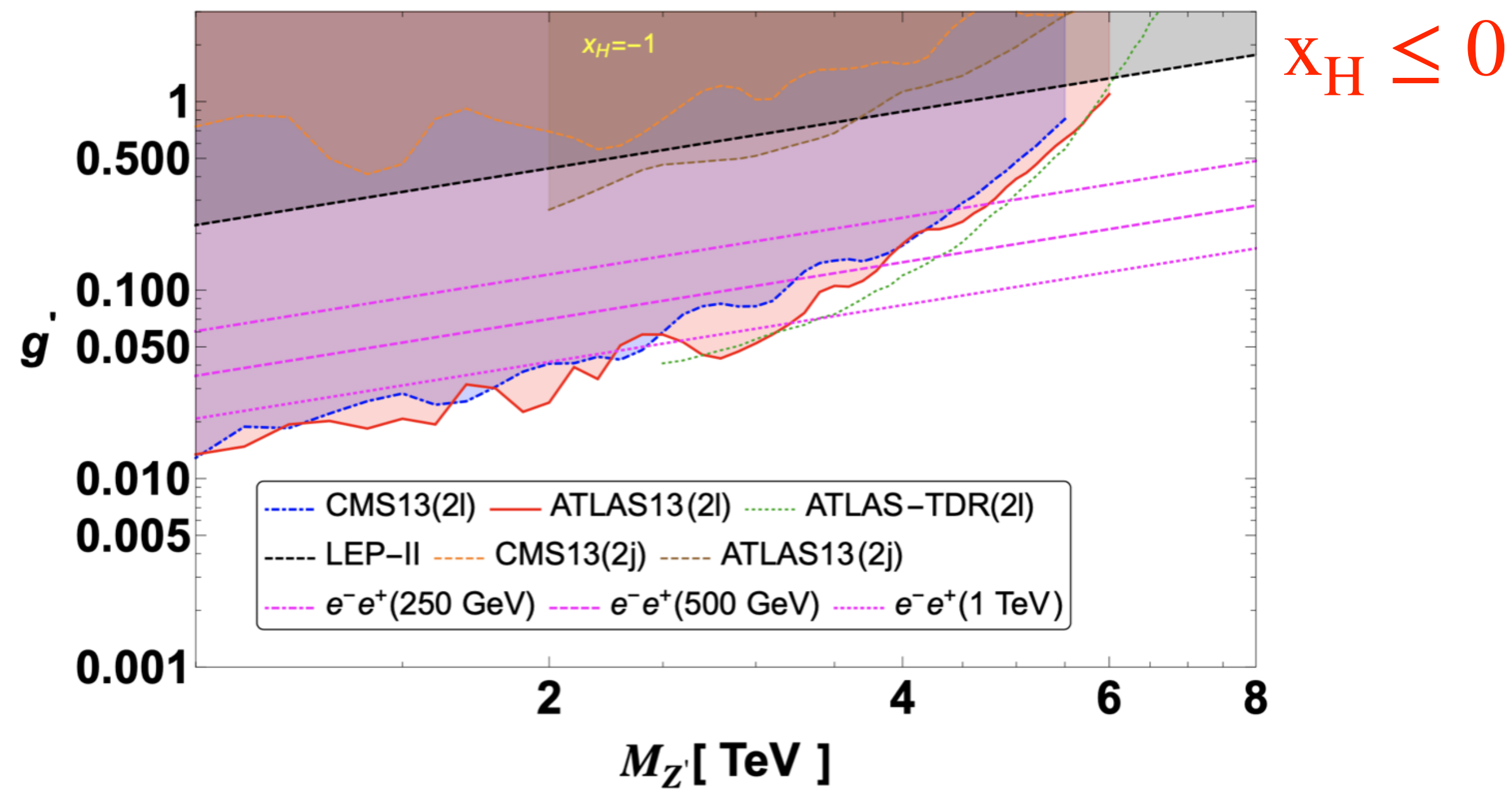
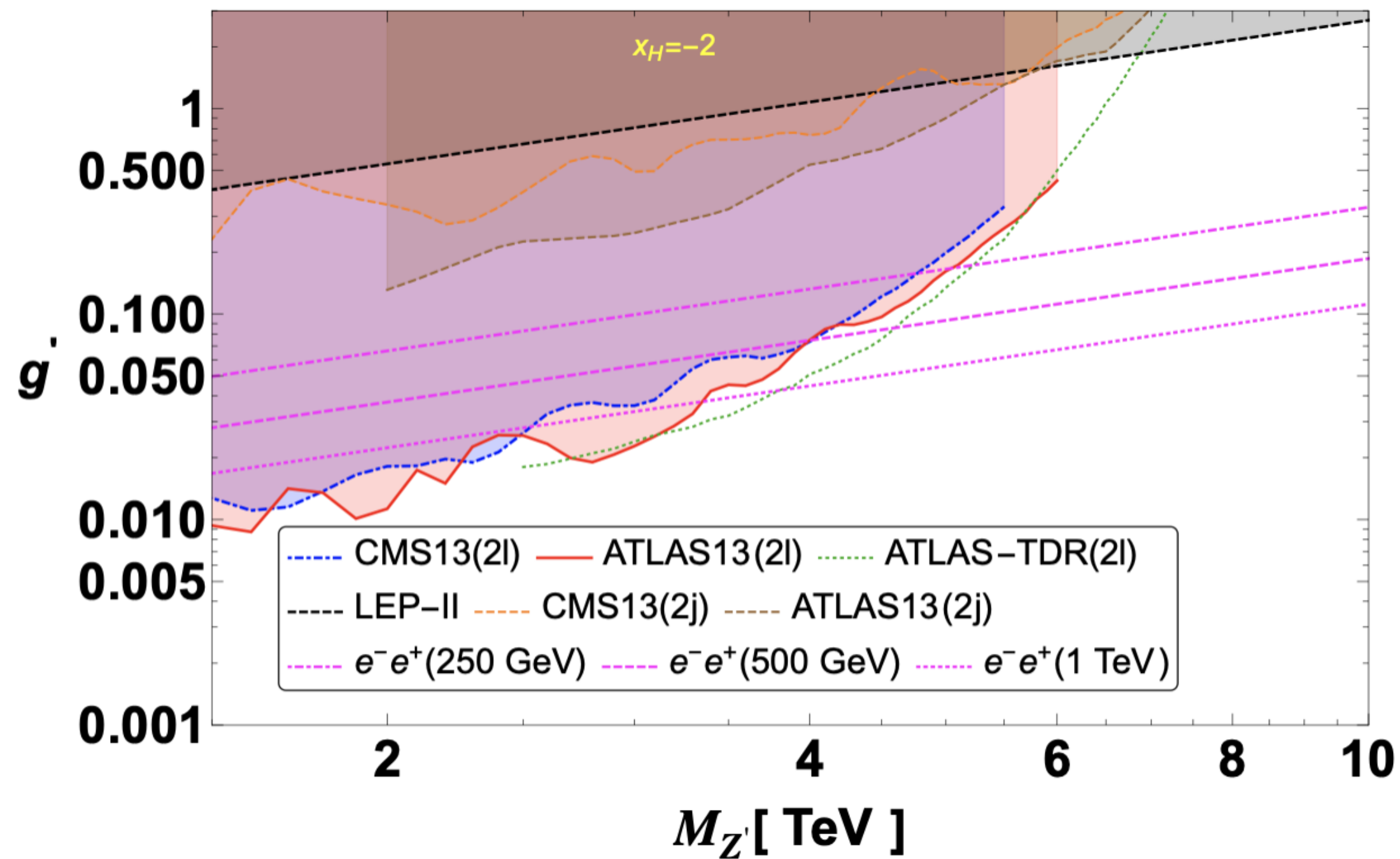
2 $\ell$ , ATLAS: 1903.06248 (139 fb<sup>-1</sup>)

ATLAS TDR -- 027  
 ee (Prospective)



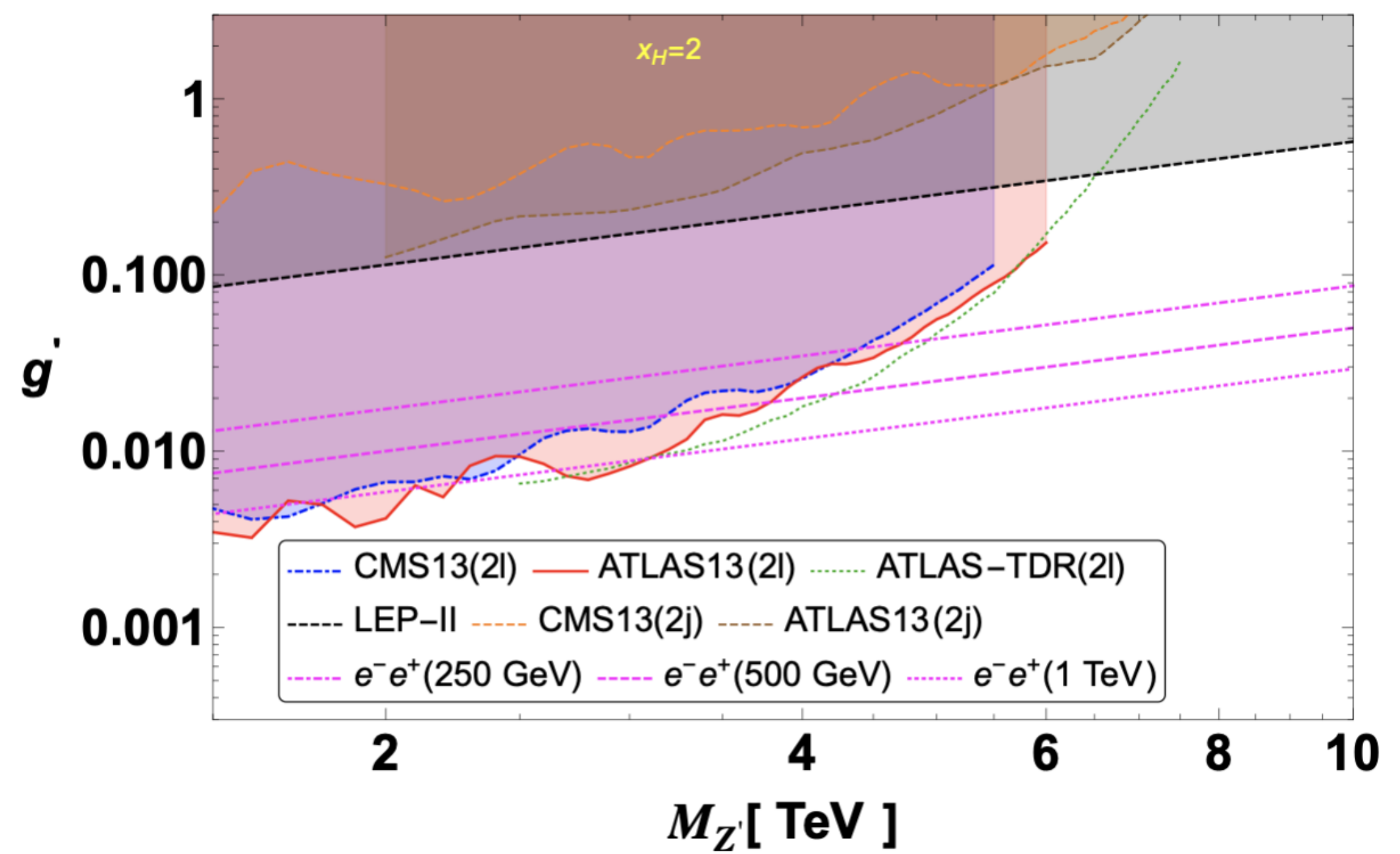
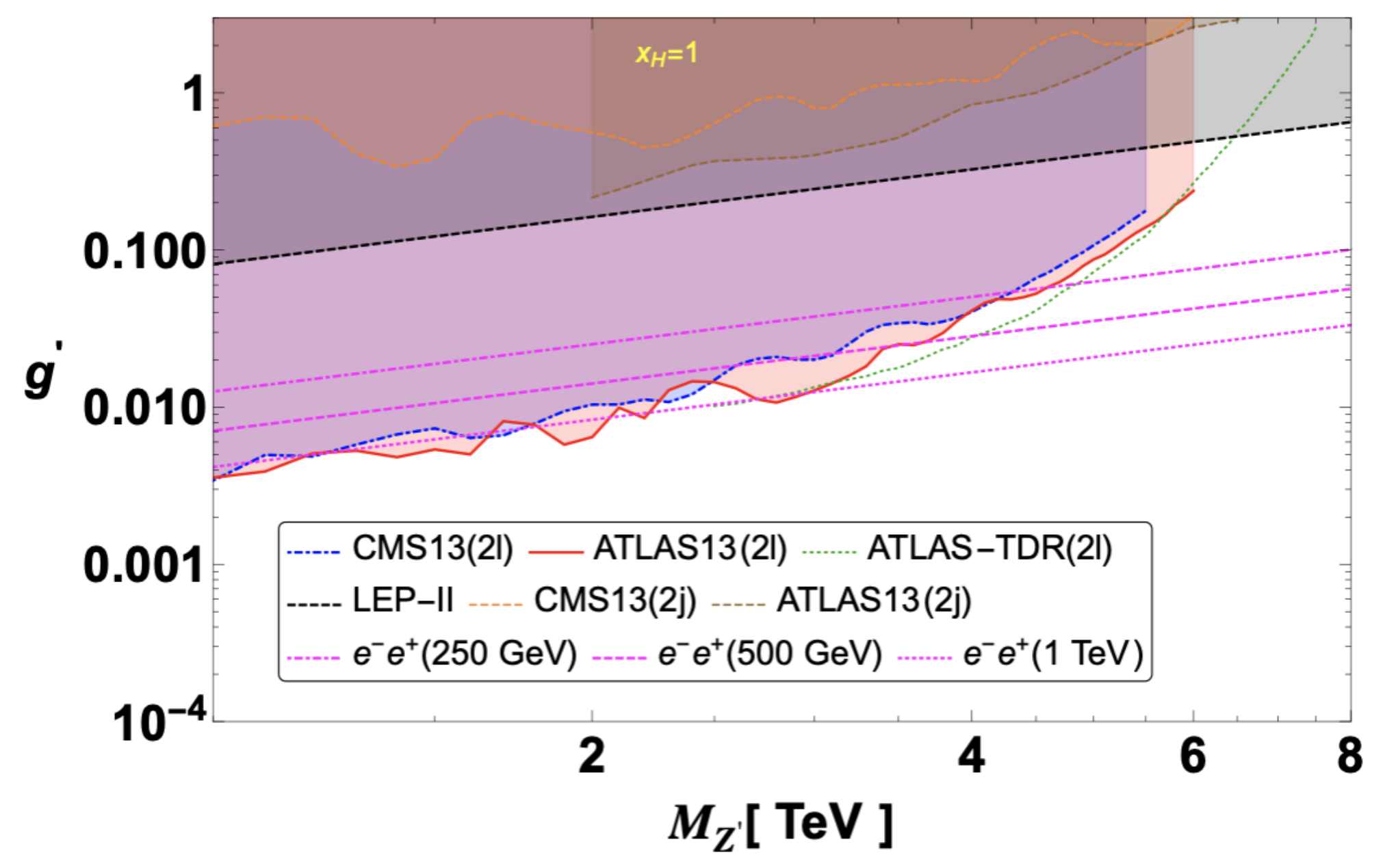
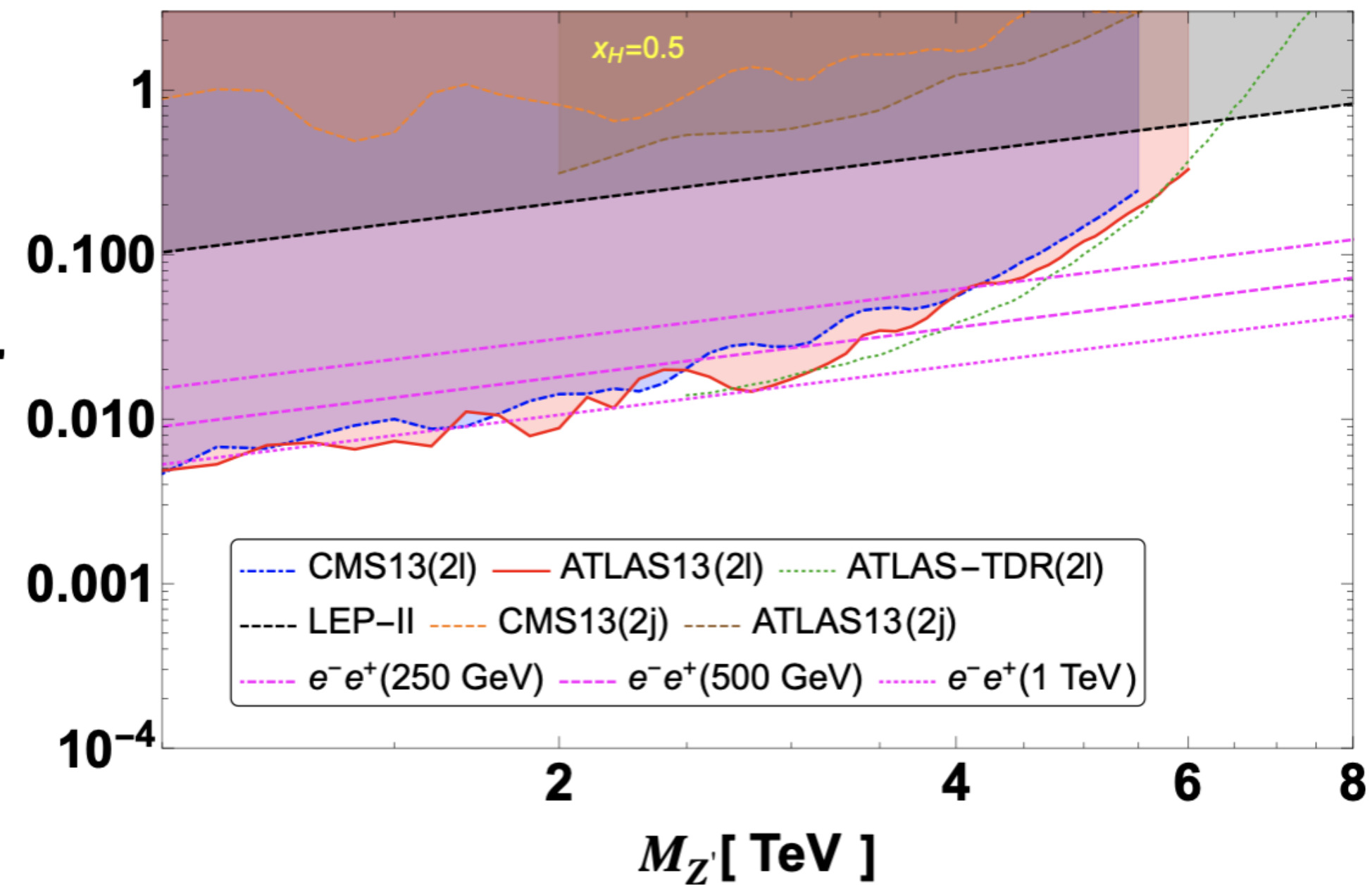
CMS PAS EXO -- 19 -- 019  
 ee(137 fb<sup>-1</sup>) +  $\mu\mu$ (140 fb<sup>-1</sup>)





For heavier  $Z'$ , the limits from  $e^-e^+$  colliders are stronger than the current LHC results

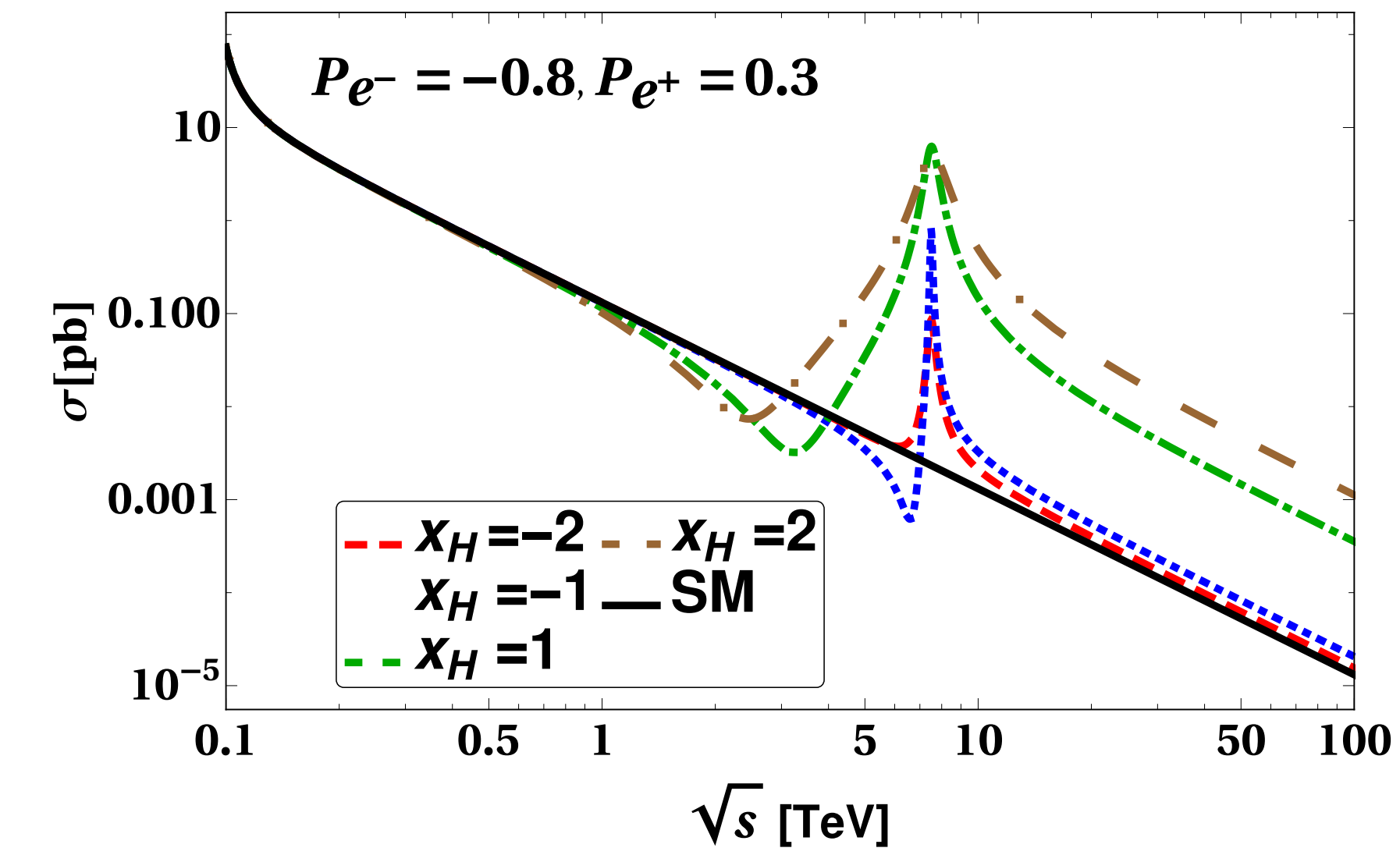
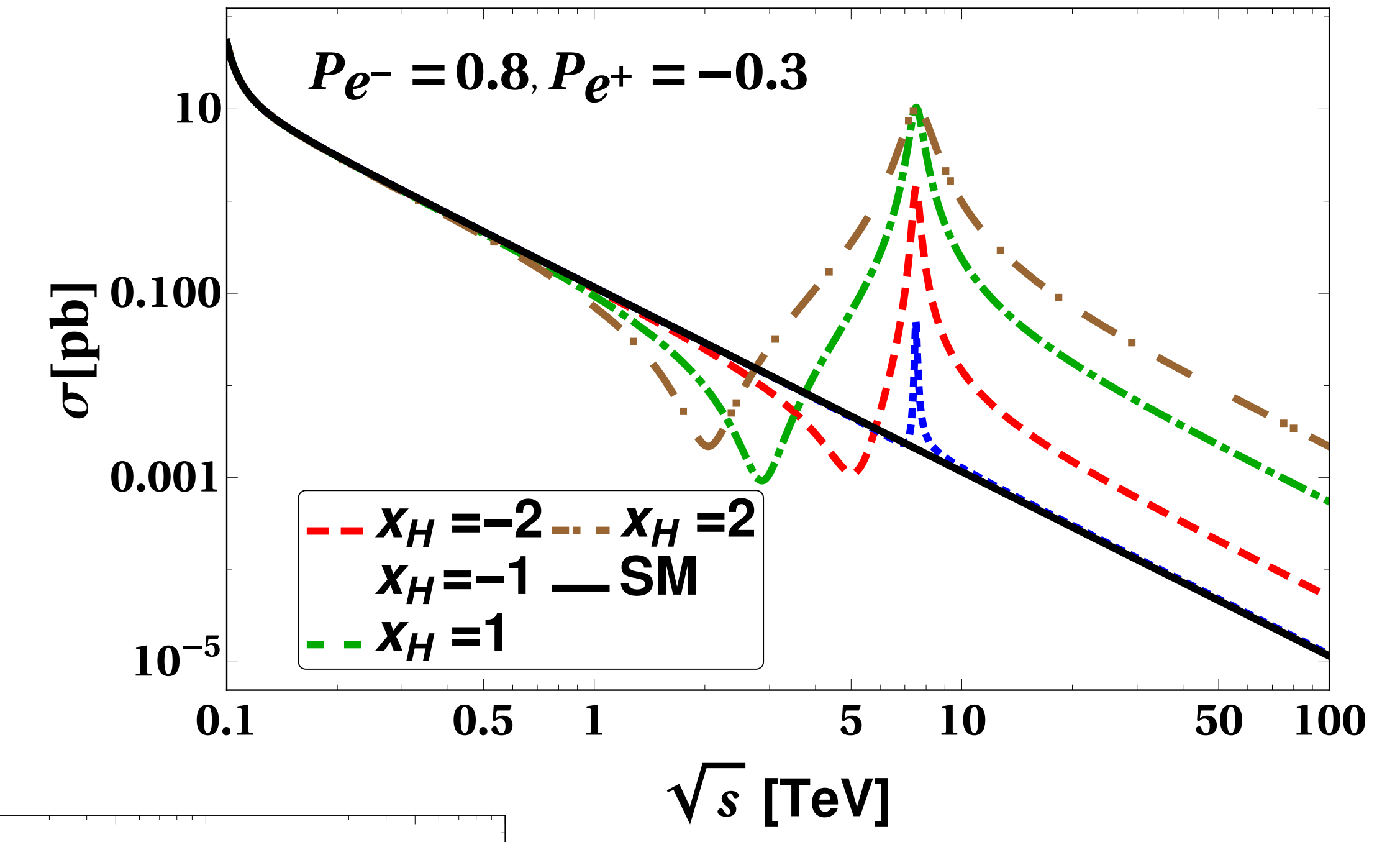
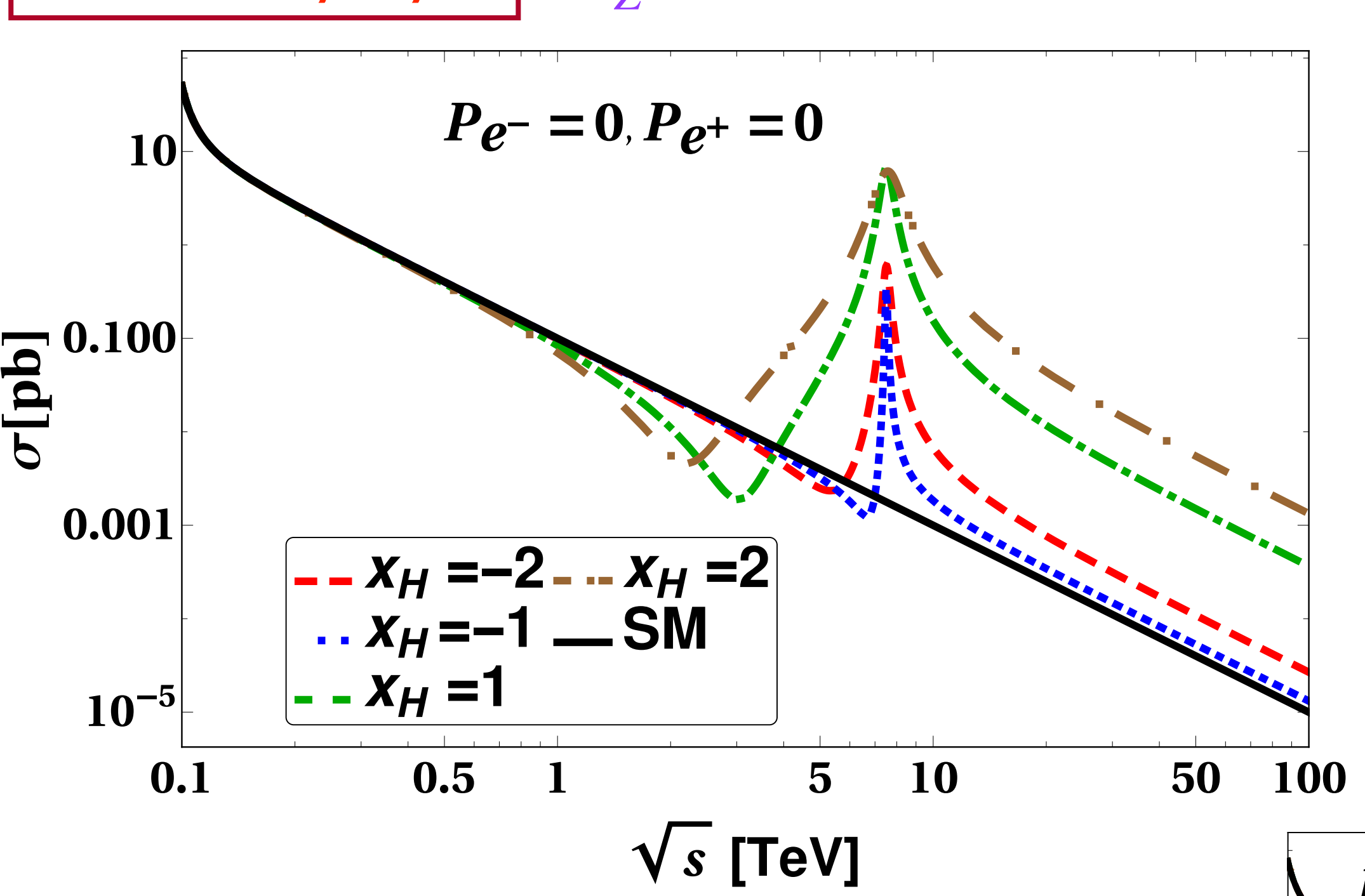
$x_H > 0$



For heavier  $Z'$ , the limits from  $e^-e^+$  colliders are stronger than the current LHC results



$e^-e^+ \rightarrow \mu^+\mu^-$   $M_{Z'} = 7.5$  TeV



Deviations in total cross sections from SM is more than 100 % for  $x_H \geq 1$  for  $\sqrt{s} = 3$  TeV. For  $\sqrt{s} < 3$  TeV the deviation is also sizable.

$$e^-e^+ \rightarrow ff$$

We define

$$q^{e_L f_L} = \sum_i \frac{g_L^{V_i e} g_L^{V_i f}}{s - m_{V_i}^2 + i m_{V_i} \Gamma_{V_i}}, \quad q^{e_L f_R} = \sum_i \frac{g_L^{V_i e} g_R^{V_i f}}{s - m_{V_i}^2 + i m_{V_i} \Gamma_{V_i}}$$

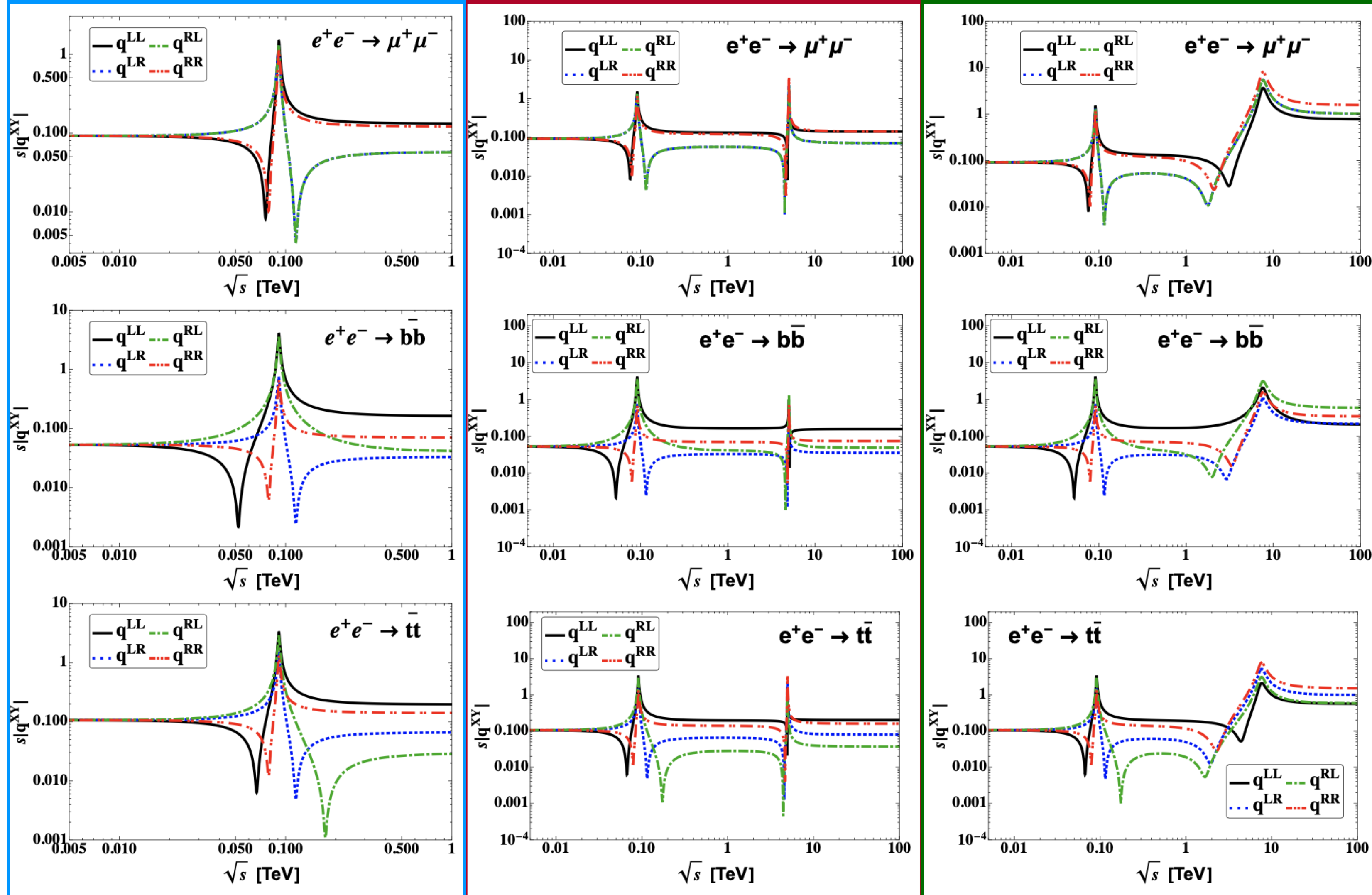
$$q^{e_R f_L} = \sum_i \frac{g_R^{V_i e} g_L^{V_i f}}{s - m_{V_i}^2 + i m_{V_i} \Gamma_{V_i}}, \quad q^{e_R f_R} = \sum_i \frac{g_R^{V_i e} g_R^{V_i f}}{s - m_{V_i}^2 + i m_{V_i} \Gamma_{V_i}}$$

$g_{L/R}^{V_i}$   $\rightarrow$  information of charges  
 $x_H, x_\Phi$

SM

$M'_Z = 5$  TeV

$M'_Z = 7.5$  TeV



$x_H = 2, x_\Phi = 1$

$$x_H = -2$$

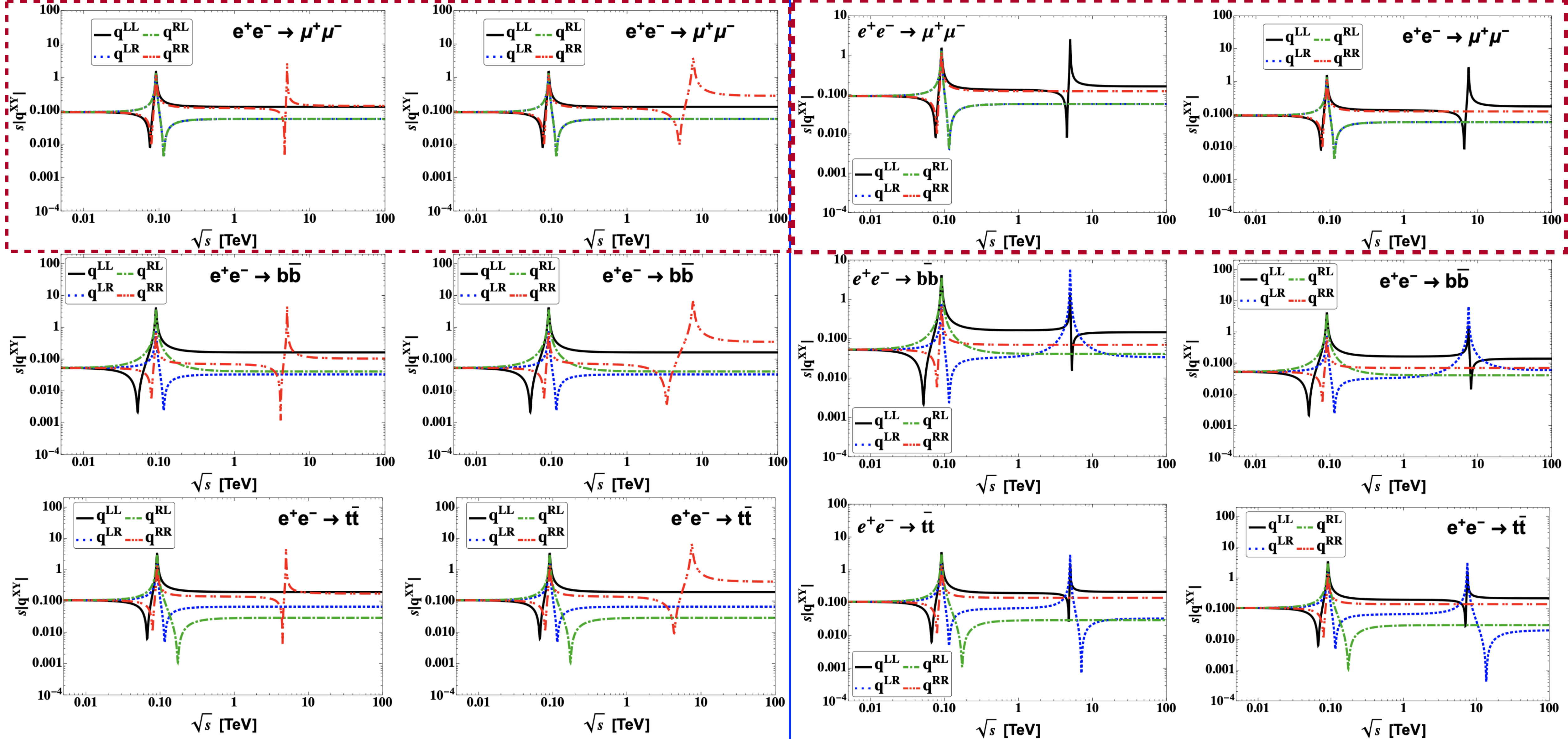
No interaction with left handed fermions

No contribution  $q_{LL}, q_{LR}, q_{RL}$  in  $\mu^+\mu^-$

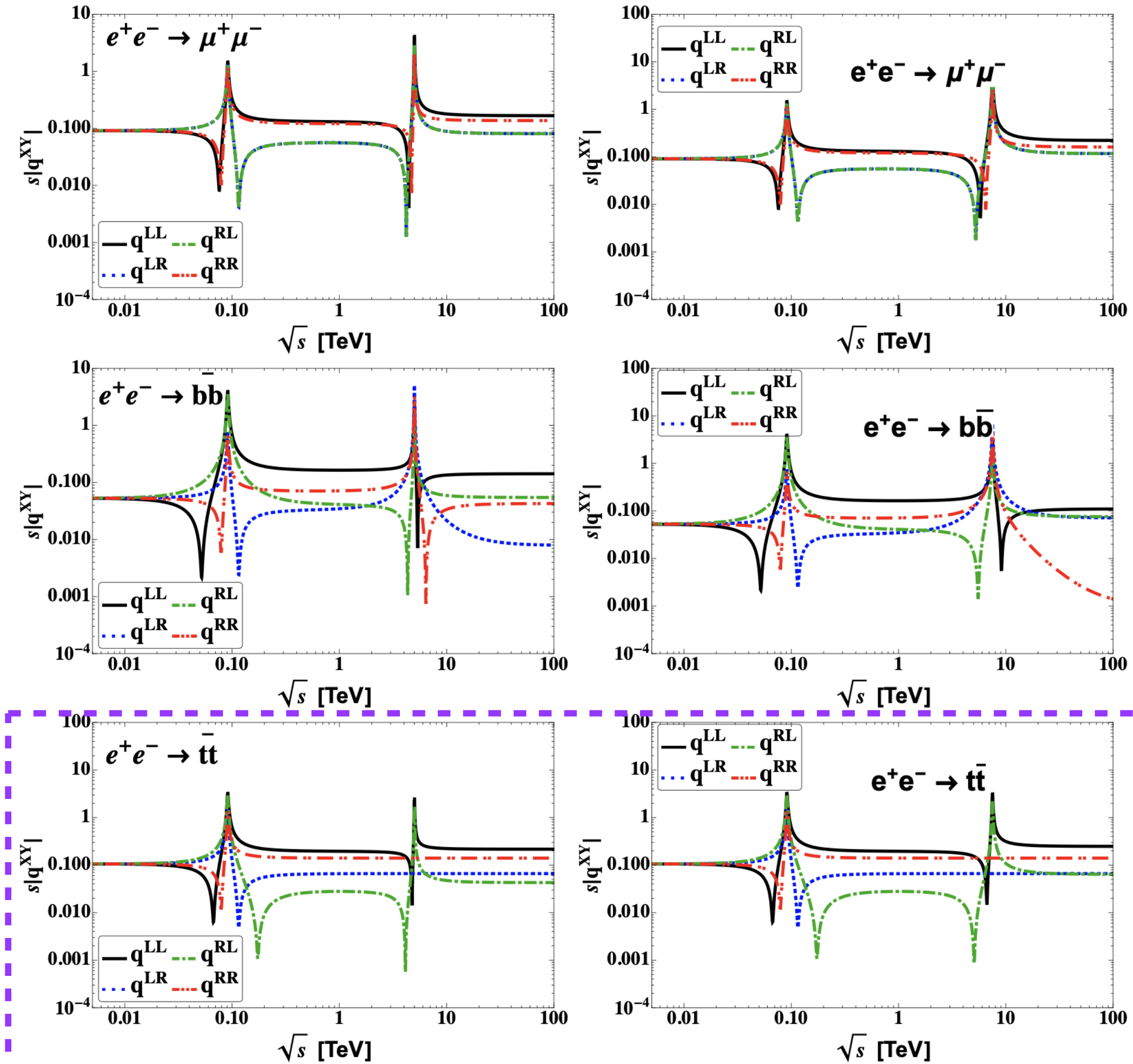
$$x_H = -1$$

No interaction with  $e_R$

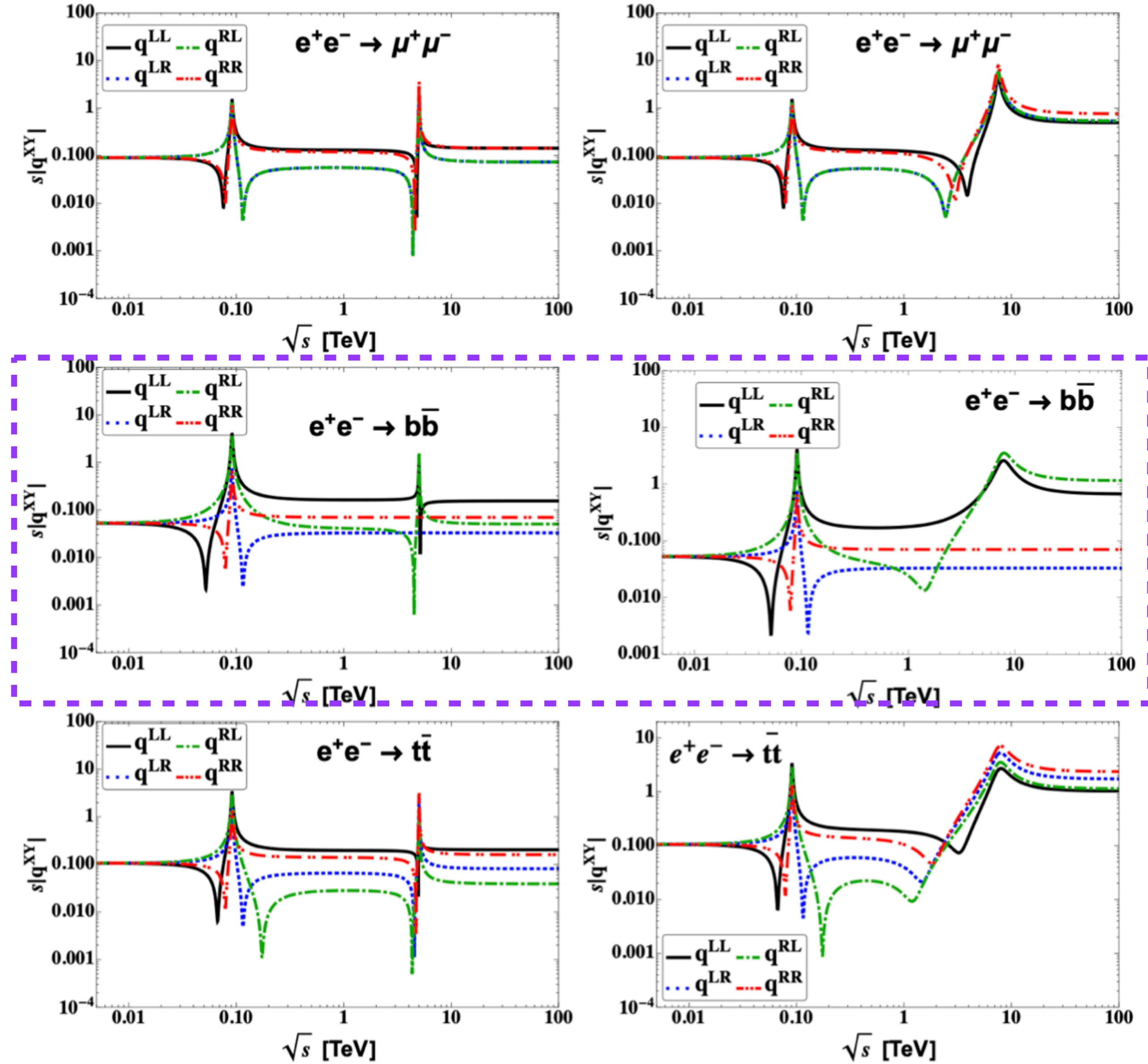
No contribution  $q_{RR}, q_{LR}, q_{RL}$  in  $\mu^+\mu^-$



$x_H = 0.5$

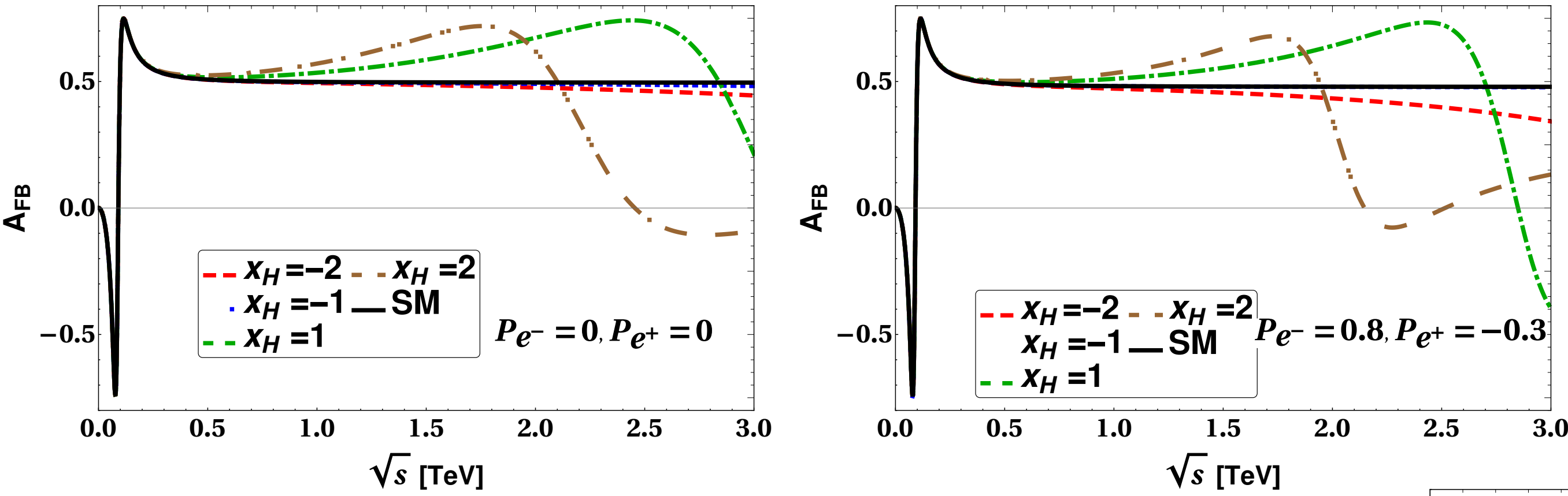
No interaction with  $u_R$ No contribution  $q_{RR}, q_{LR}$  in  $t\bar{t}$ 

$x_H = 1$

No interaction with  $d_R$ No contribution  $q_{RR}, q_{LR}$  in  $b\bar{b}$ 

# Integrated Forward – Backward Asymmetry ( $e^-e^+ \rightarrow \mu^-\mu^+$ ) : $\mathcal{A}_{FB}$

$M_{Z'} = 7.5 \text{ TeV}$



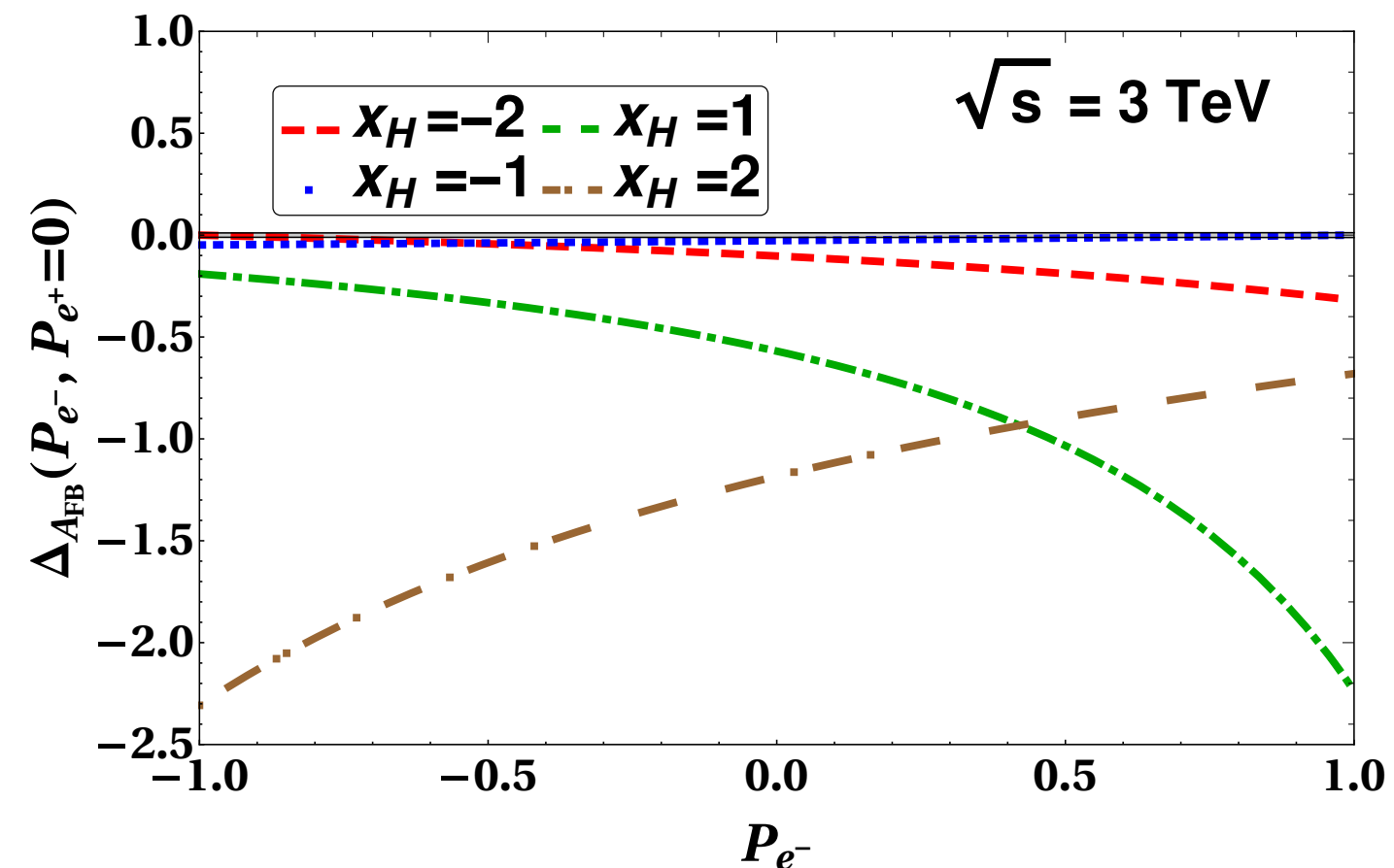
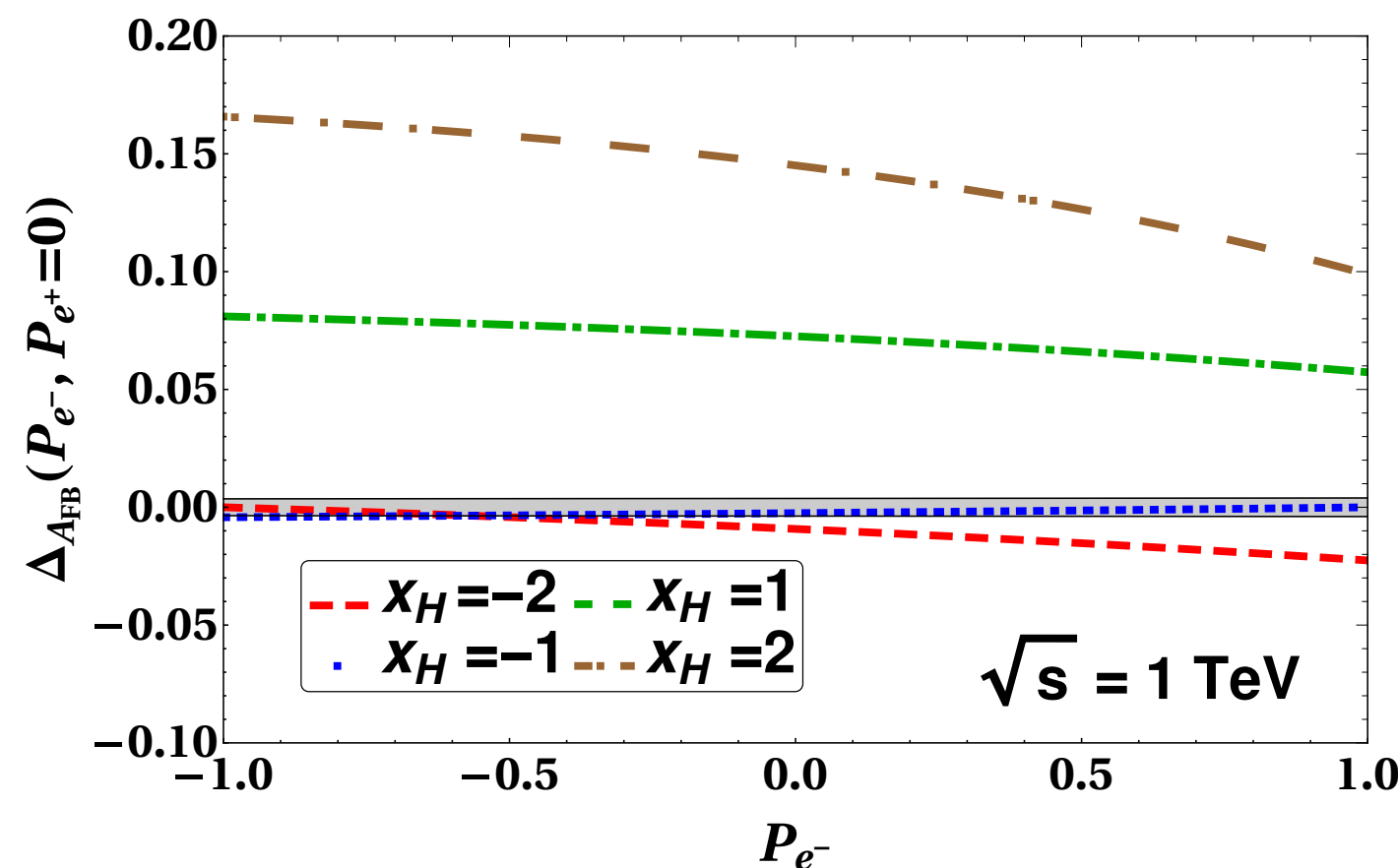
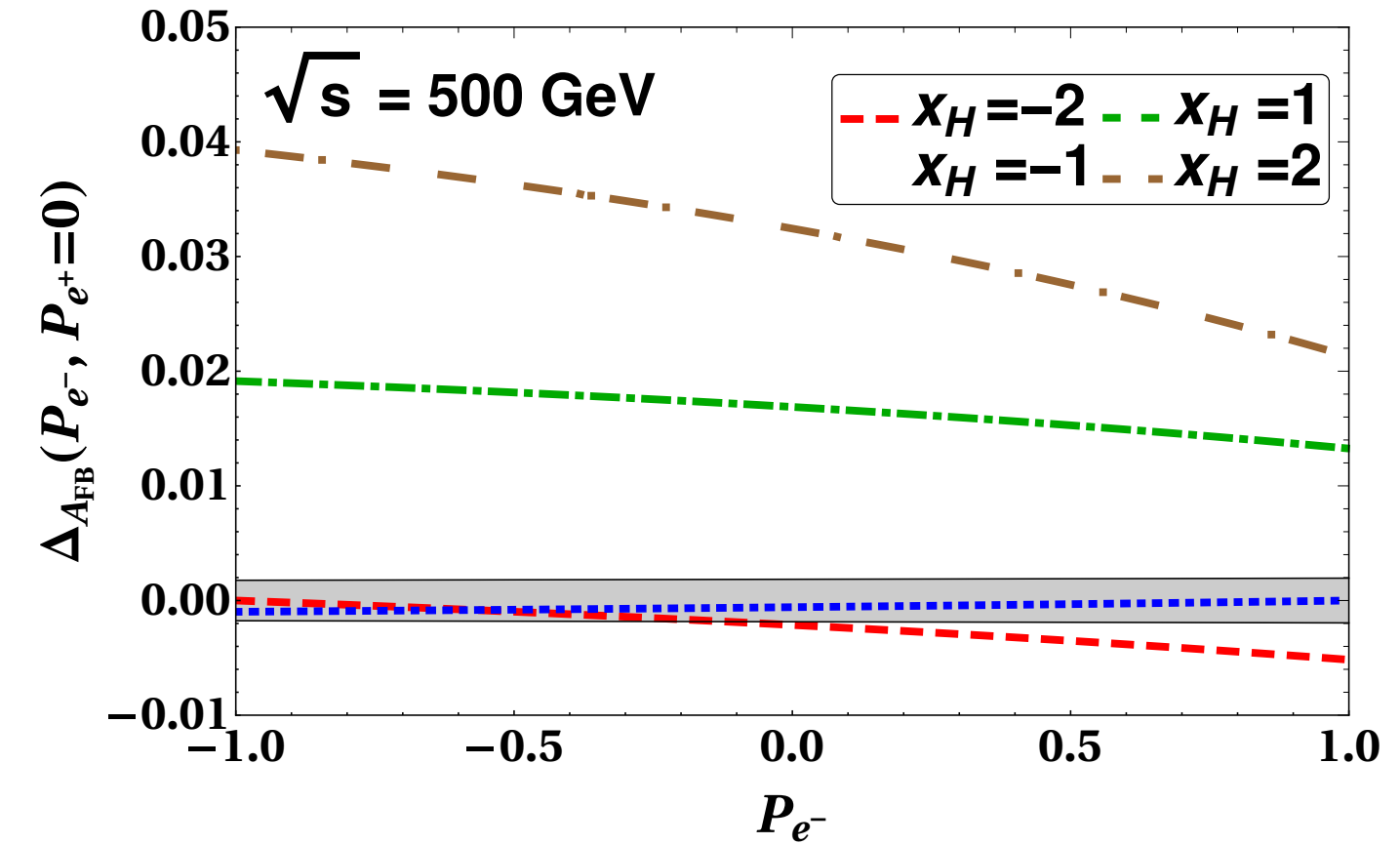
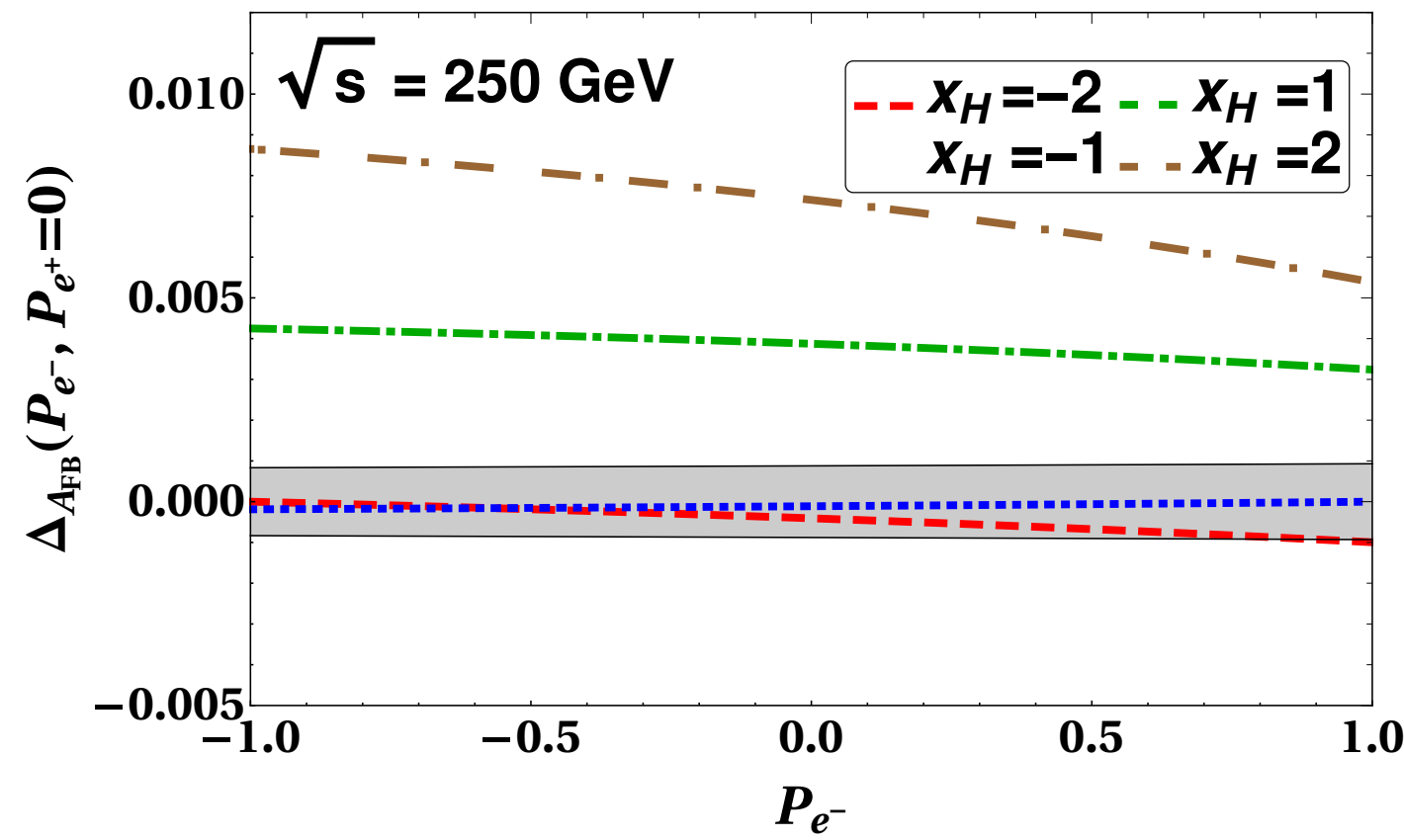
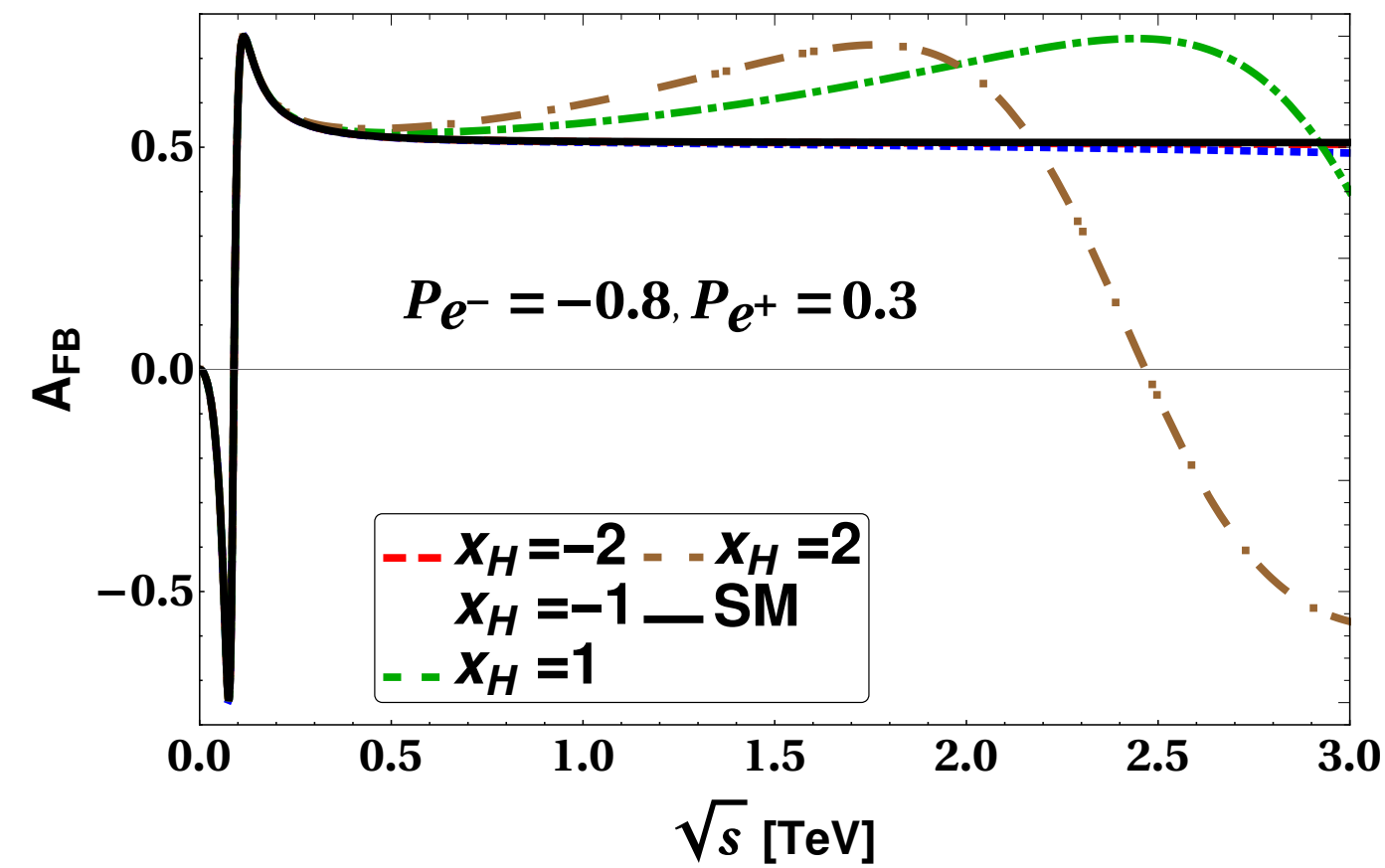
Integrated

$$\mathcal{A}_{FB}(P_{e^-}, P_{e^+}) = \frac{\sigma_F(P_{e^-}, P_{e^+}) - \sigma_B(P_{e^-}, P_{e^+})}{\sigma_F(P_{e^-}, P_{e^+}) + \sigma_B(P_{e^-}, P_{e^+})}$$

Deviation from the SM

$$\Delta_{\mathcal{A}_{FB}} = \frac{\mathcal{A}_{FB}^{U(1)_X}}{\mathcal{A}_{FB}^{SM}} - 1.$$

$x_H = 2$  : 3.8 % for  $P_{e^-} = -0.8$  at 500 GeV  
 $x_H = 1$  : 79 % for  $P_{e^-} = -0.8$  at 1 TeV  
 $x_H = -1$  : 20 % for  $P_{e^-} = 0.3$  at 3 TeV



Statistical error

$$\Delta_{\mathcal{A}_{FB}} = 2 \frac{\sqrt{n_1 n_2} (\sqrt{n_1} + \sqrt{n_2})}{(n_1 + n_2)^2} = \frac{2\sqrt{n_1 n_2}}{(n_1 + n_2) (\sqrt{n_1} - \sqrt{n_2})} \mathcal{A}_{FB}$$

$$(n_1, n_2) = (N_F, N_B) \quad N_{F(B)} = L_{\text{int}} \sigma_{F(B)}(P_{e^-}, P_{e^+})$$

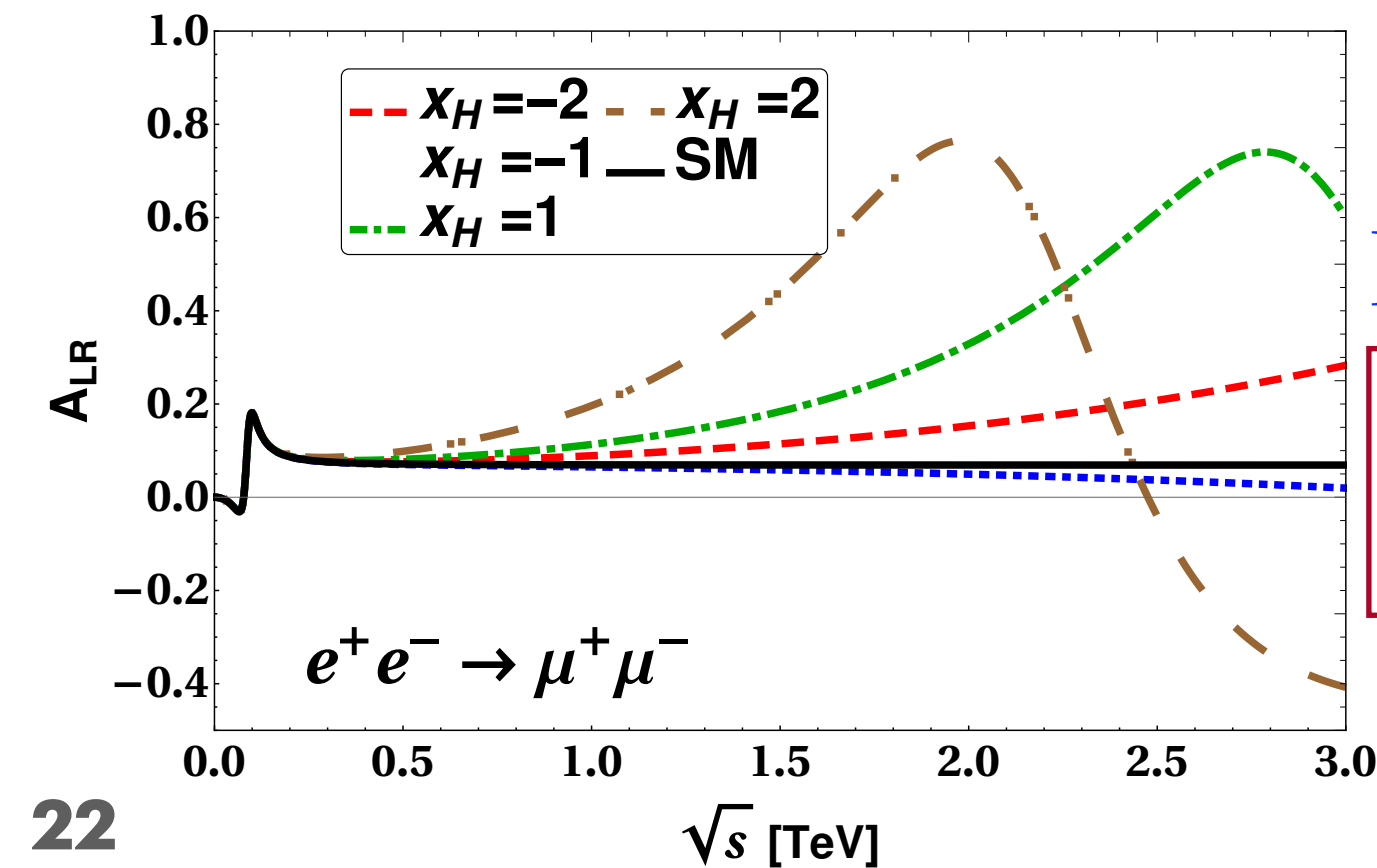
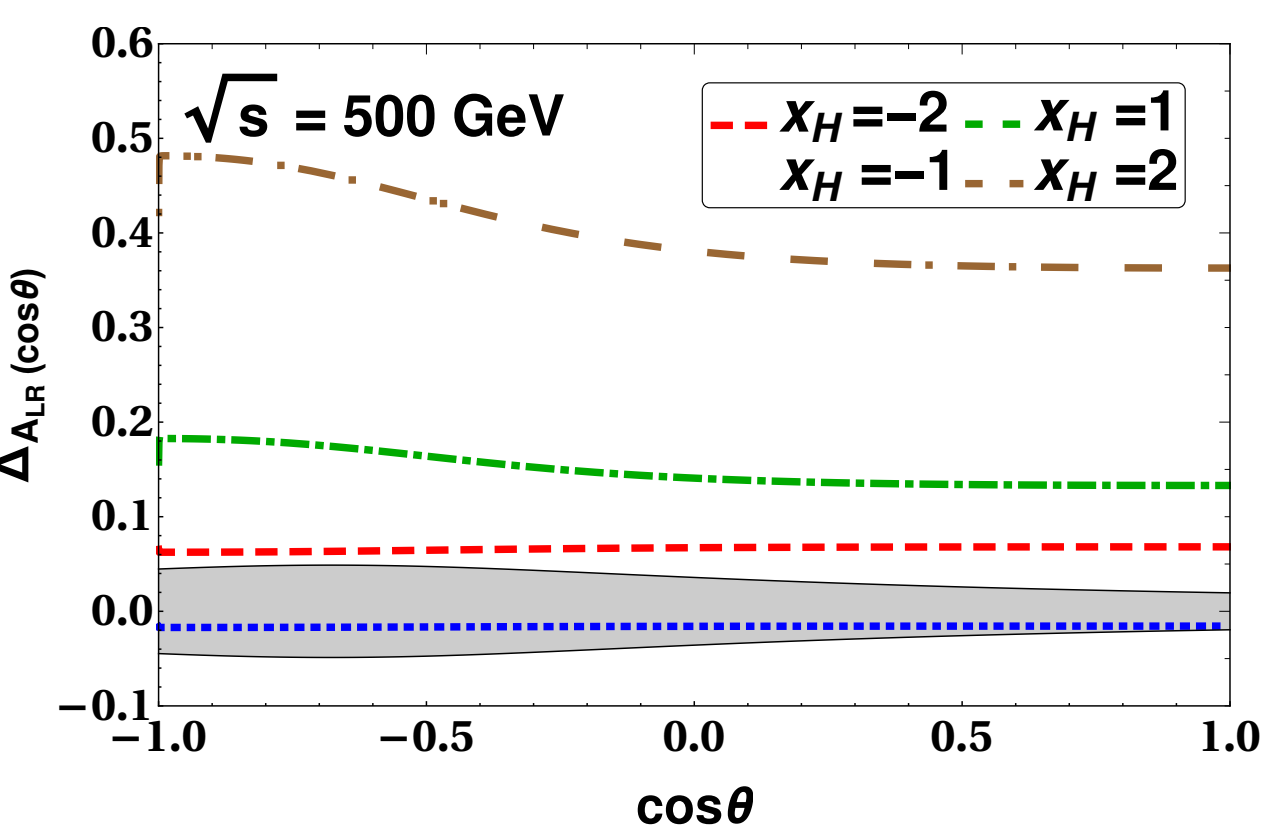
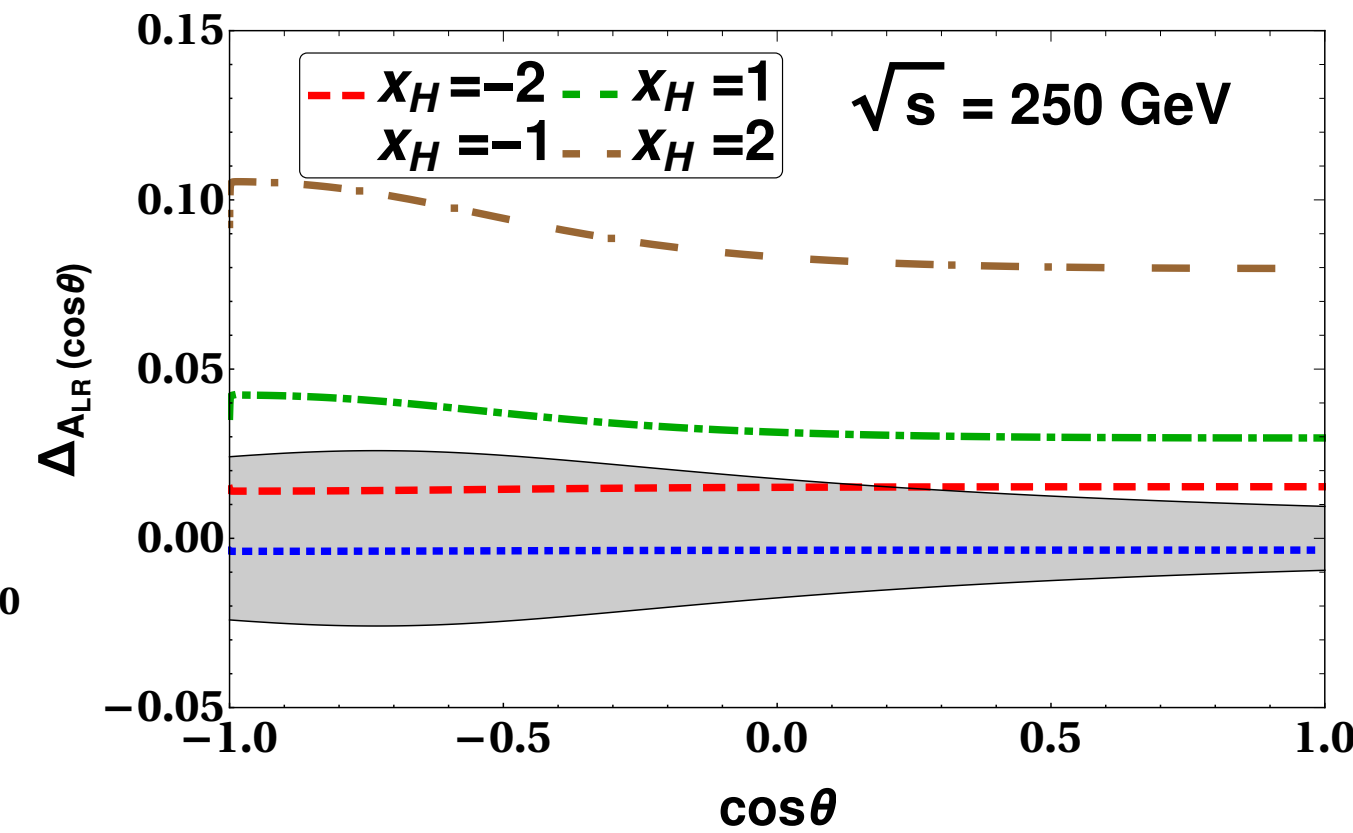
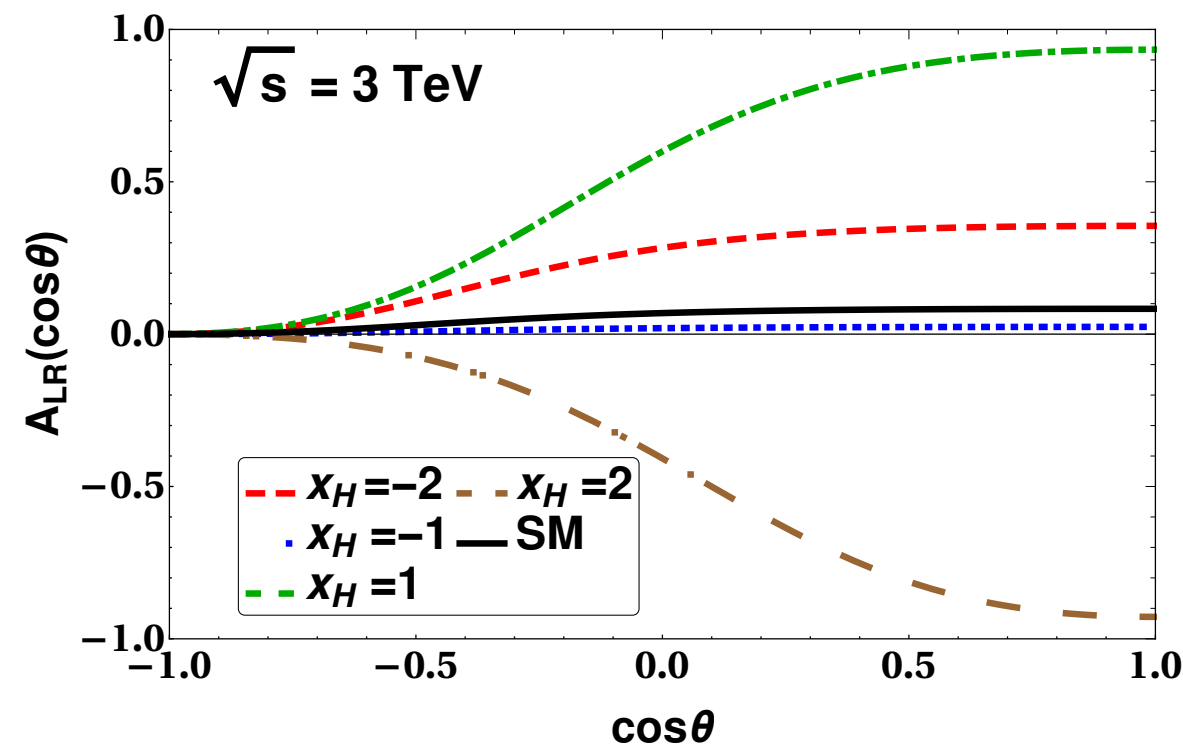
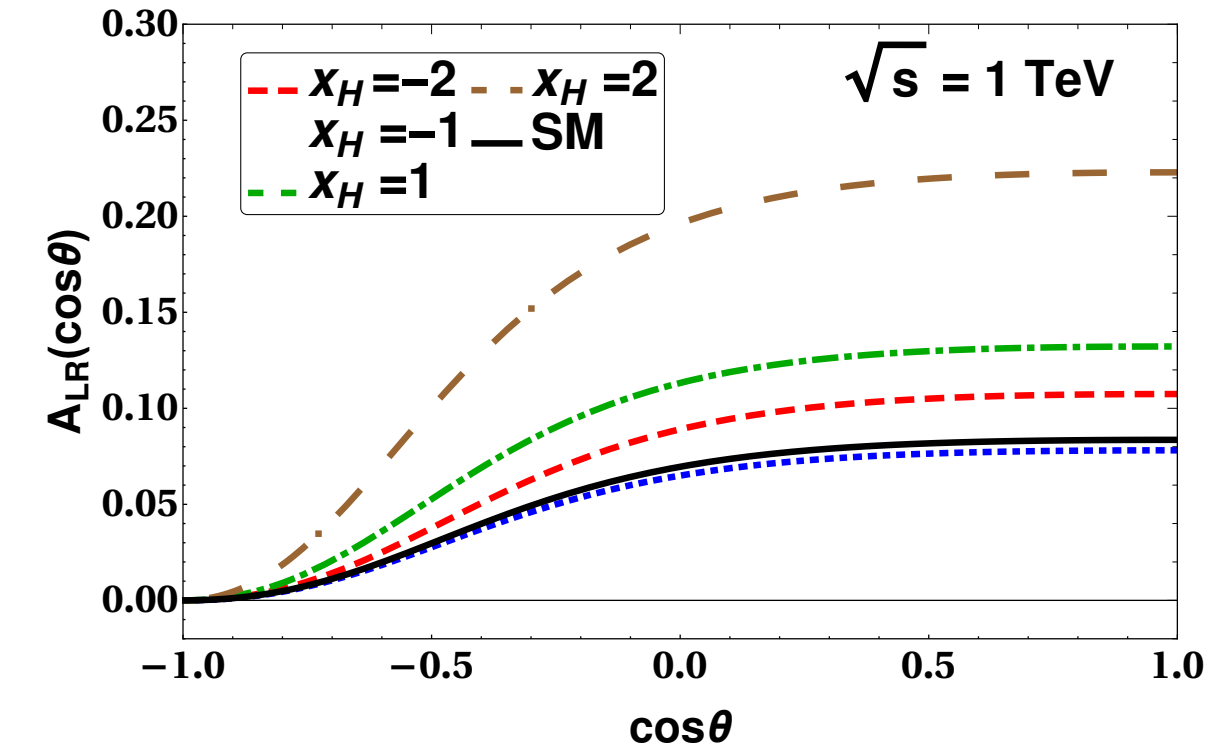
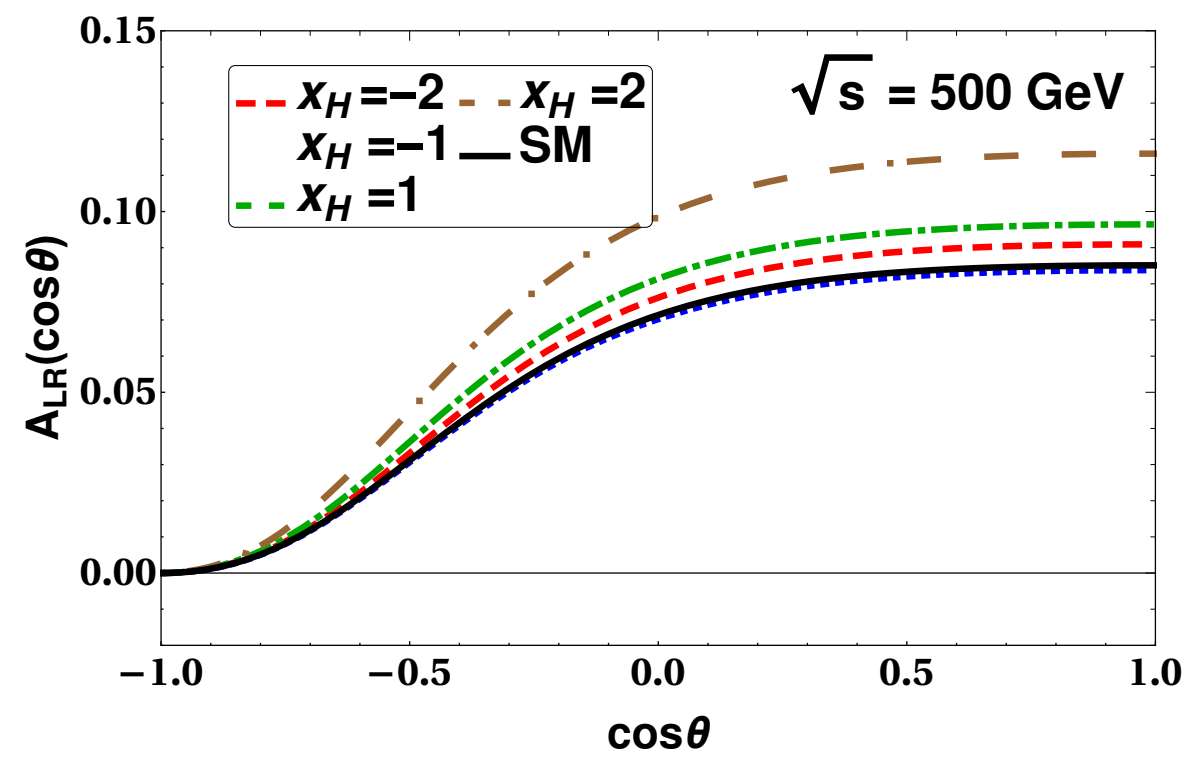
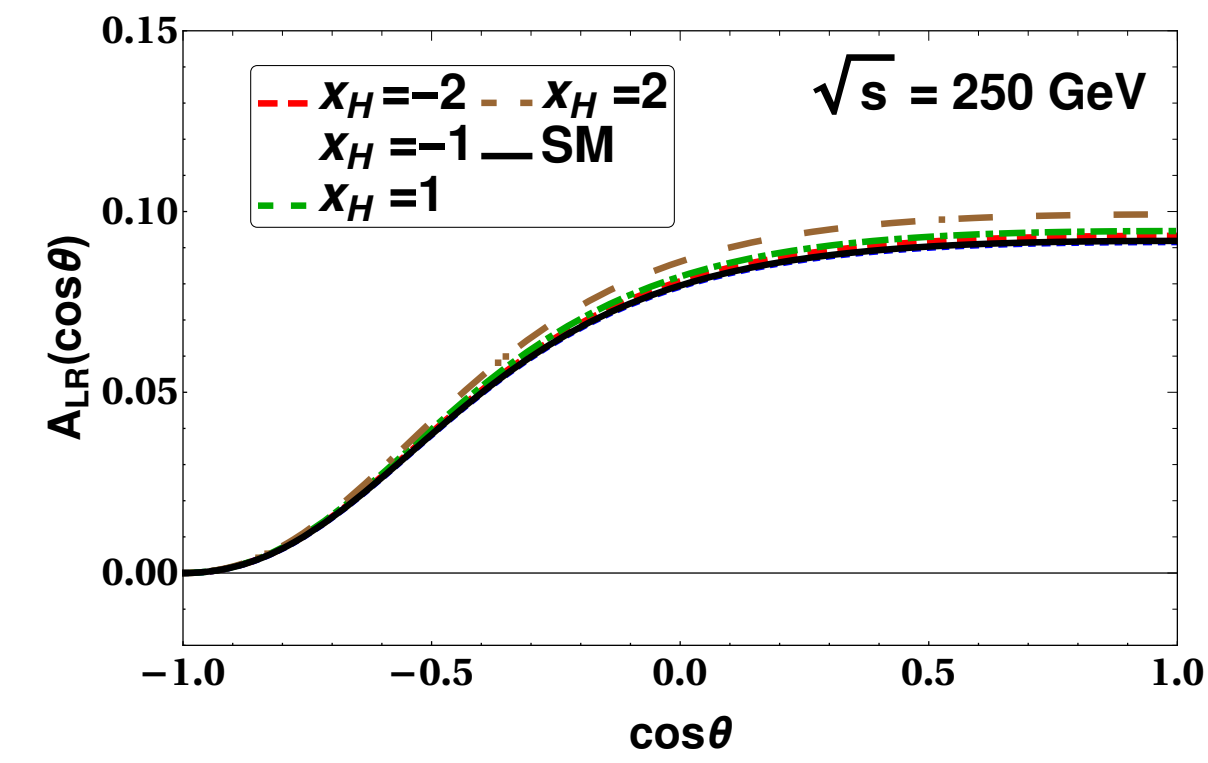
# Differential and integrated Left – Right Asymmetry ( $e^-e^+ \rightarrow \mu^-\mu^+$ ) : $\mathcal{A}_{LR}$ $M_{Z'} = 7.5$ TeV

## Differential

$$\mathcal{A}_{LR}(\cos\theta) = \frac{\frac{d\sigma_{LR}}{d\cos\theta}(\cos\theta) - \frac{d\sigma_{RL}}{d\cos\theta}(\cos\theta)}{\frac{d\sigma_{LR}}{d\cos\theta}(\cos\theta) + \frac{d\sigma_{RL}}{d\cos\theta}(\cos\theta)}$$

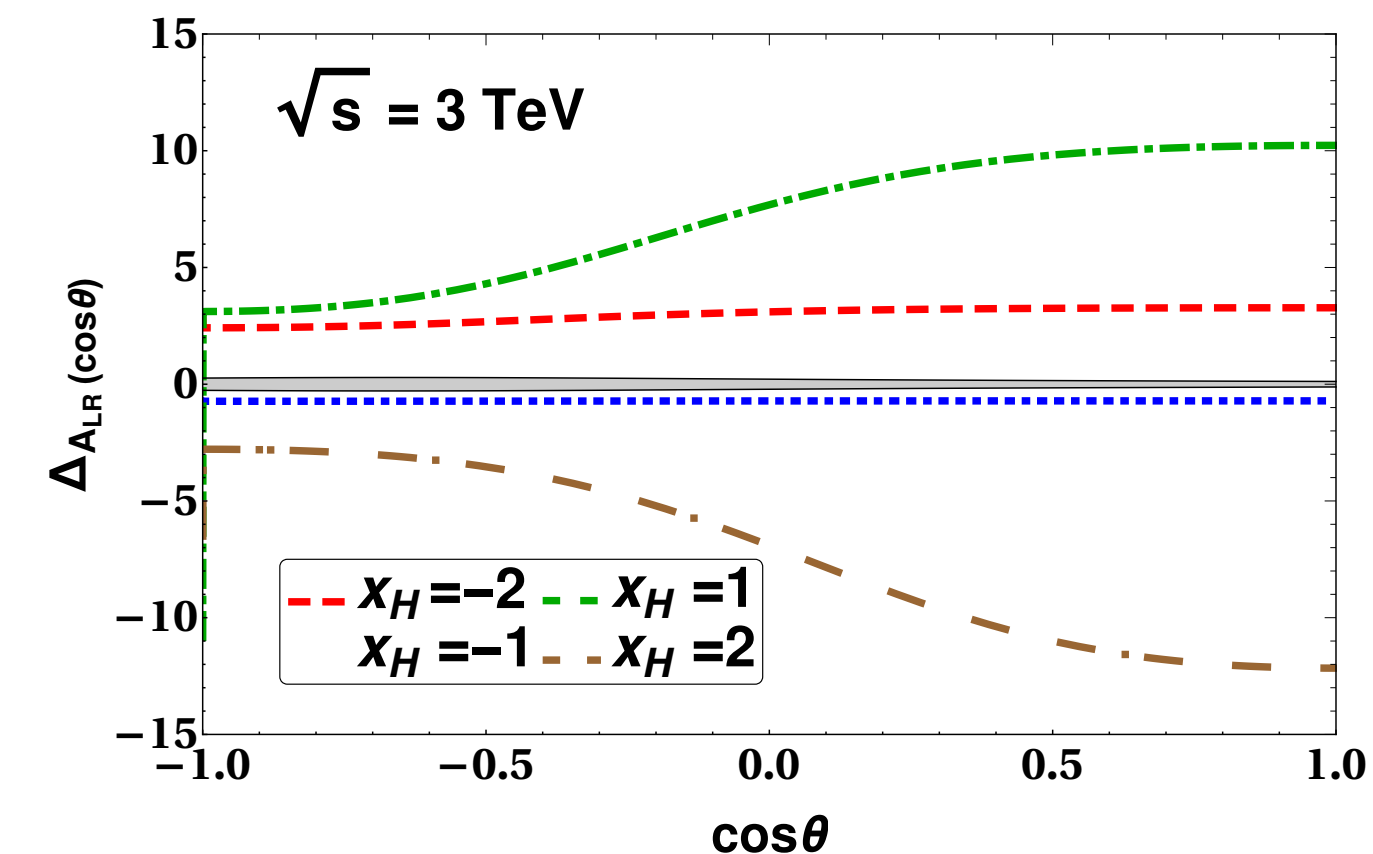
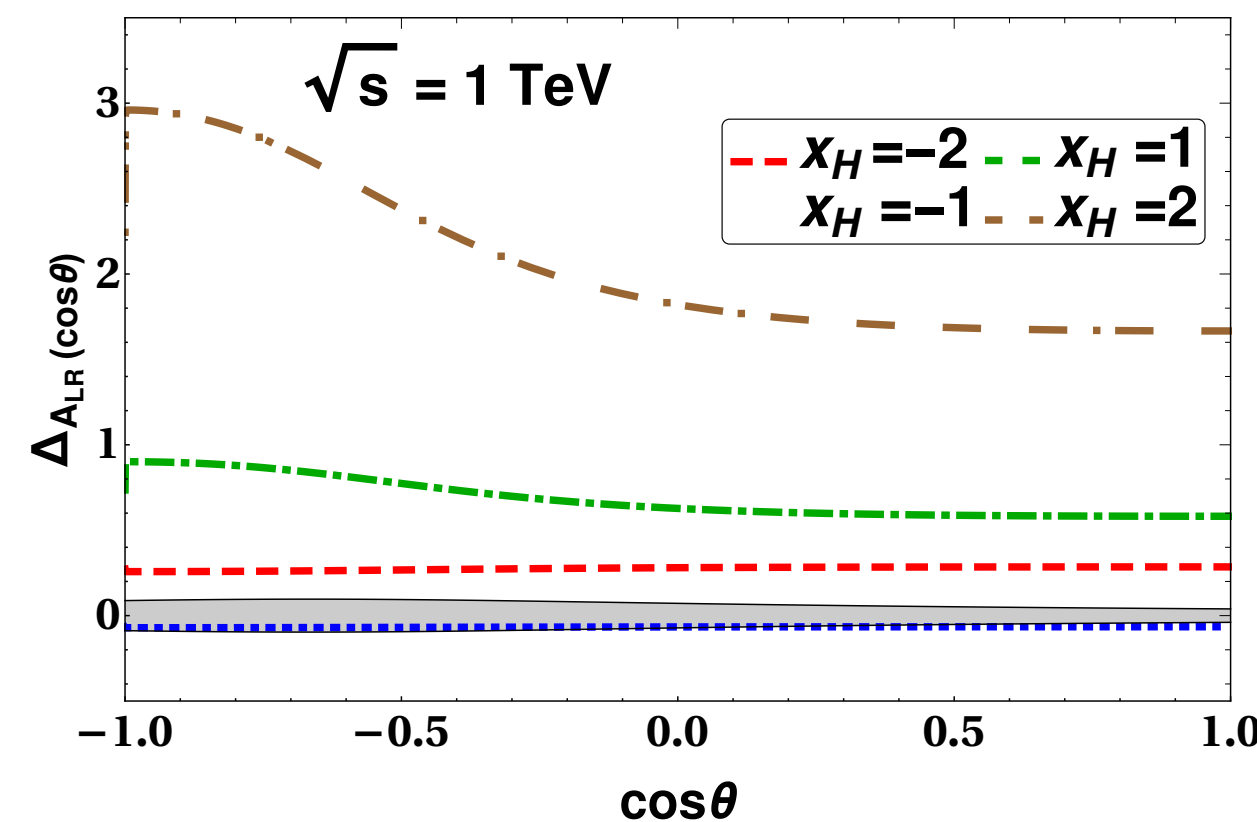
Deviation from the SM  $x_H = 2$  : 10 % for at 250 GeV  
 $x_H = 1$  : 20 % for at 500 GeV  
 $x_H = -2$  : 8 % for at 500 GeV

$$\Delta_{\mathcal{A}_{LR}}(\cos\theta) = \frac{\mathcal{A}_{LR}^{U(1)X}(\cos\theta)}{\mathcal{A}_{LR}^{SM}(\cos\theta)} - 1$$



## Integral

$$\mathcal{A}_{LR} = \frac{\sigma^{LR} - \sigma^{RL}}{\sigma^{LR} + \sigma^{RL}}$$



# Differential Left – Right, Forward – Backward Asymmetry ( $e^-e^+ \rightarrow \mu^-\mu^+$ ) : $\mathcal{A}_{LR,FB}$

$M_{Z'} = 7.5 \text{ TeV}$

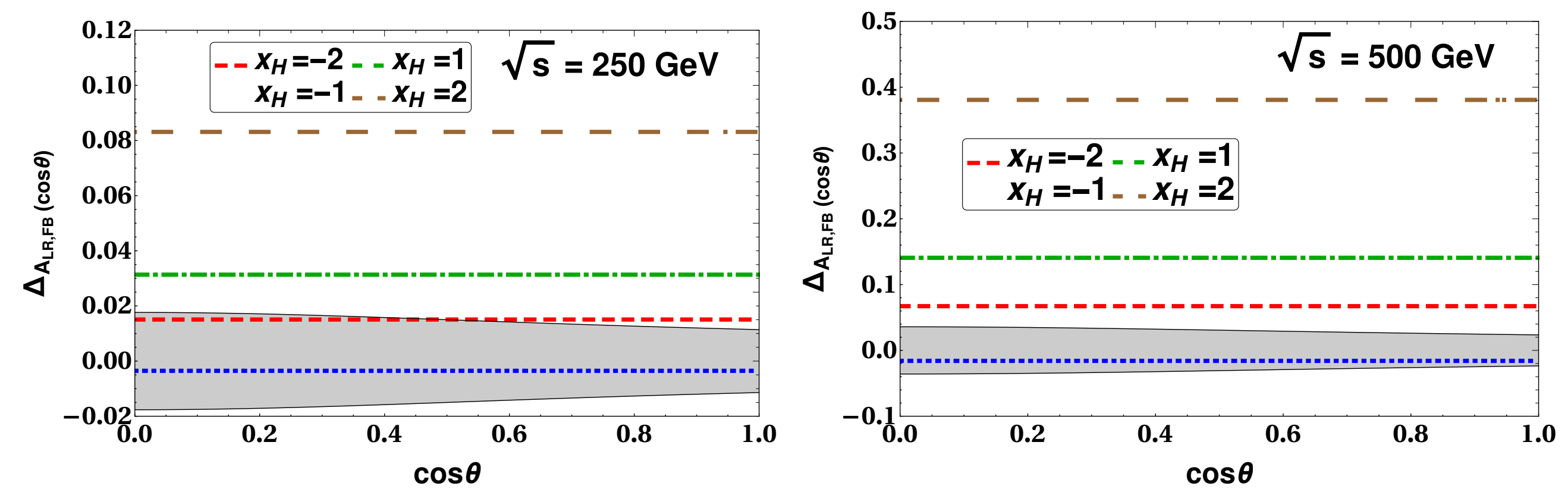
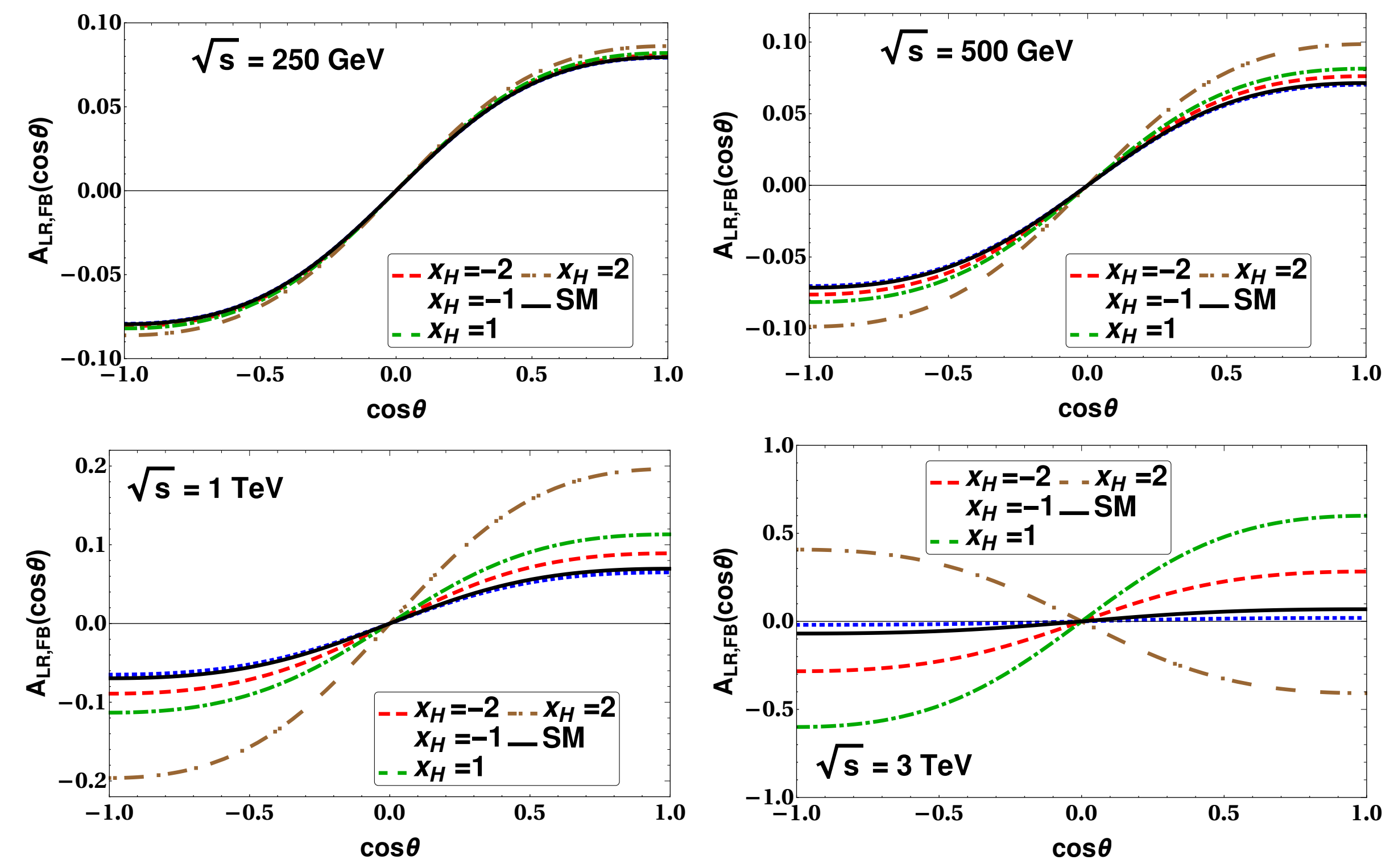
## Differential

$$\mathcal{A}_{LR,FB}(\cos\theta) = \frac{[\sigma_{LR}(\cos\theta) - \sigma_{RL}(\cos\theta)] - [\sigma_{LR}(-\cos\theta) - \sigma_{RL}(-\cos\theta)]}{[\sigma_{LR}(\cos\theta) + \sigma_{RL}(\cos\theta)] + [\sigma_{LR}(-\cos\theta) + \sigma_{RL}(-\cos\theta)]}$$

## Deviation from the SM

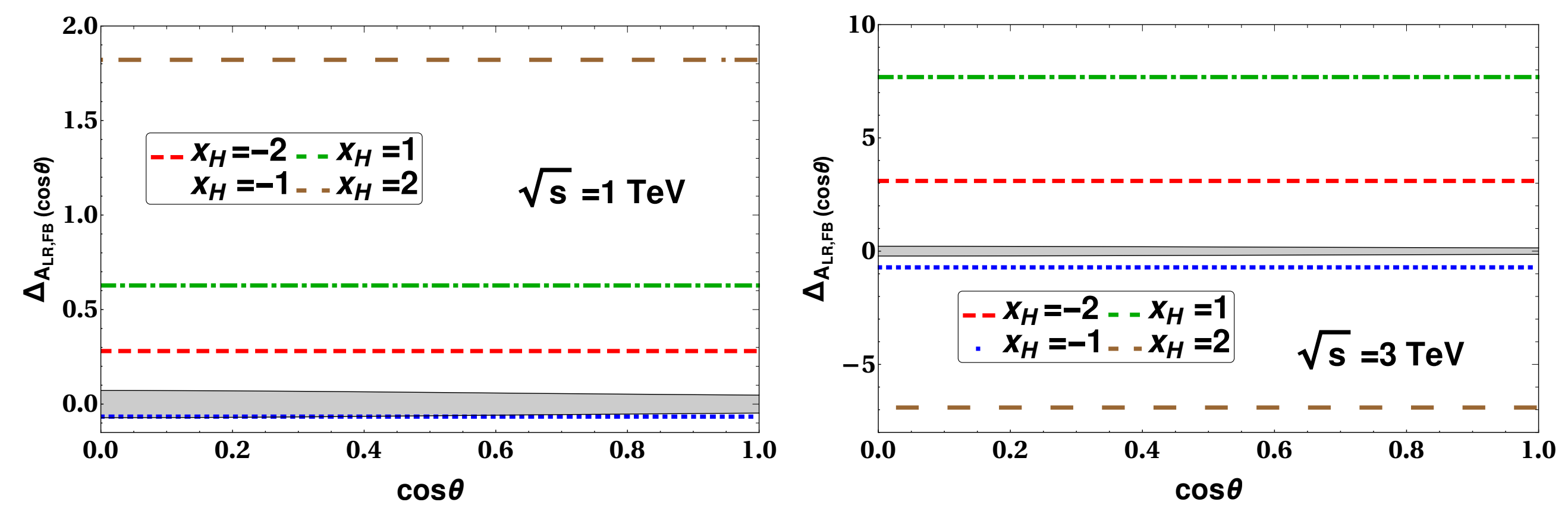
$$\Delta_{\mathcal{A}_{LR,FB}}(\cos\theta) = \frac{\mathcal{A}_{LR,FB}^{U(1)X}(\cos\theta)}{\mathcal{A}_{LR,FB}^{SM}(\cos\theta)} - 1$$

$x_H = 2 : 8.2\%$  for at 250 GeV  
 $x_H = 1 : 15\%$  for at 500 GeV  
 $x_H = -2 : 7.5\%$  for at 500 GeV



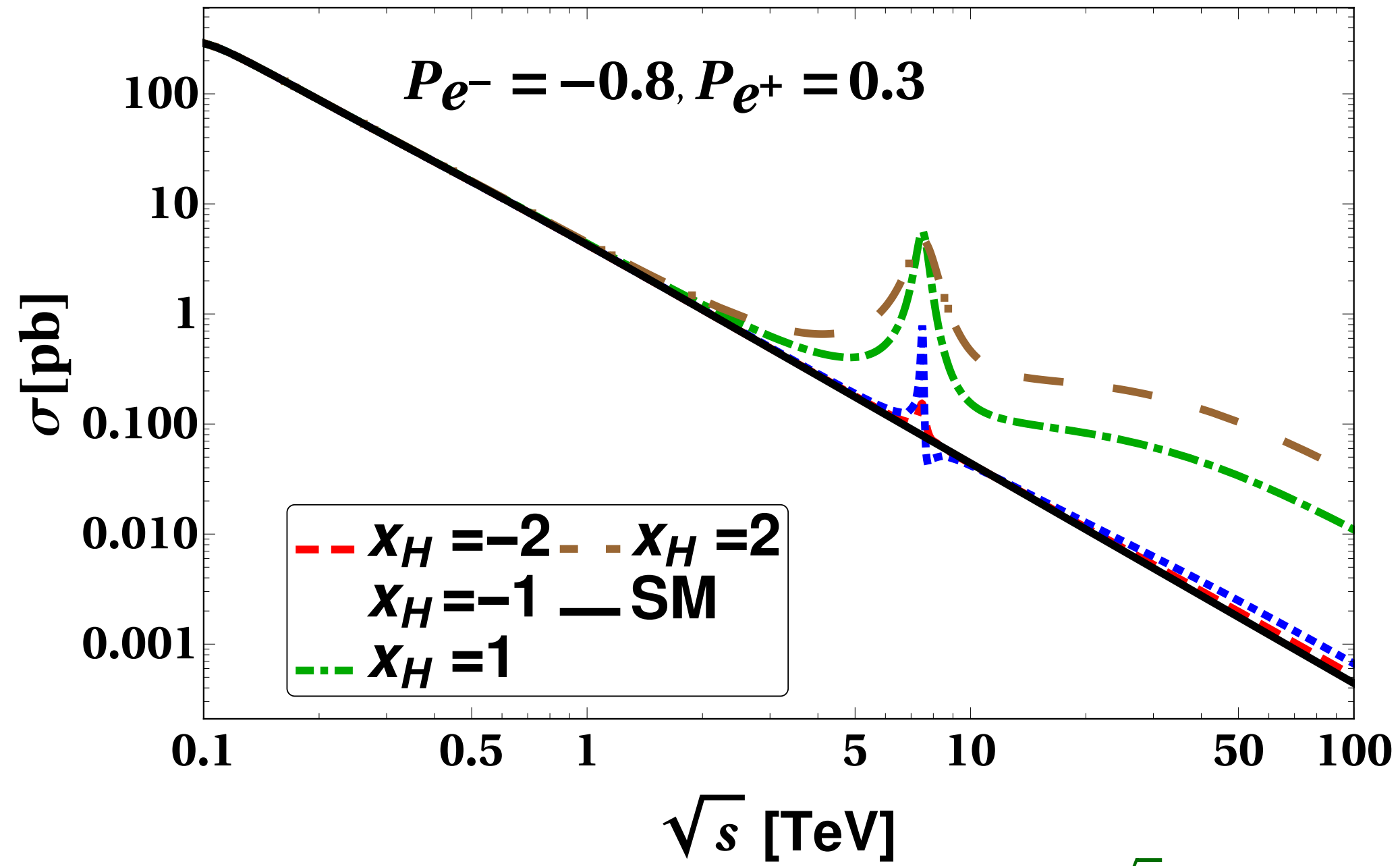
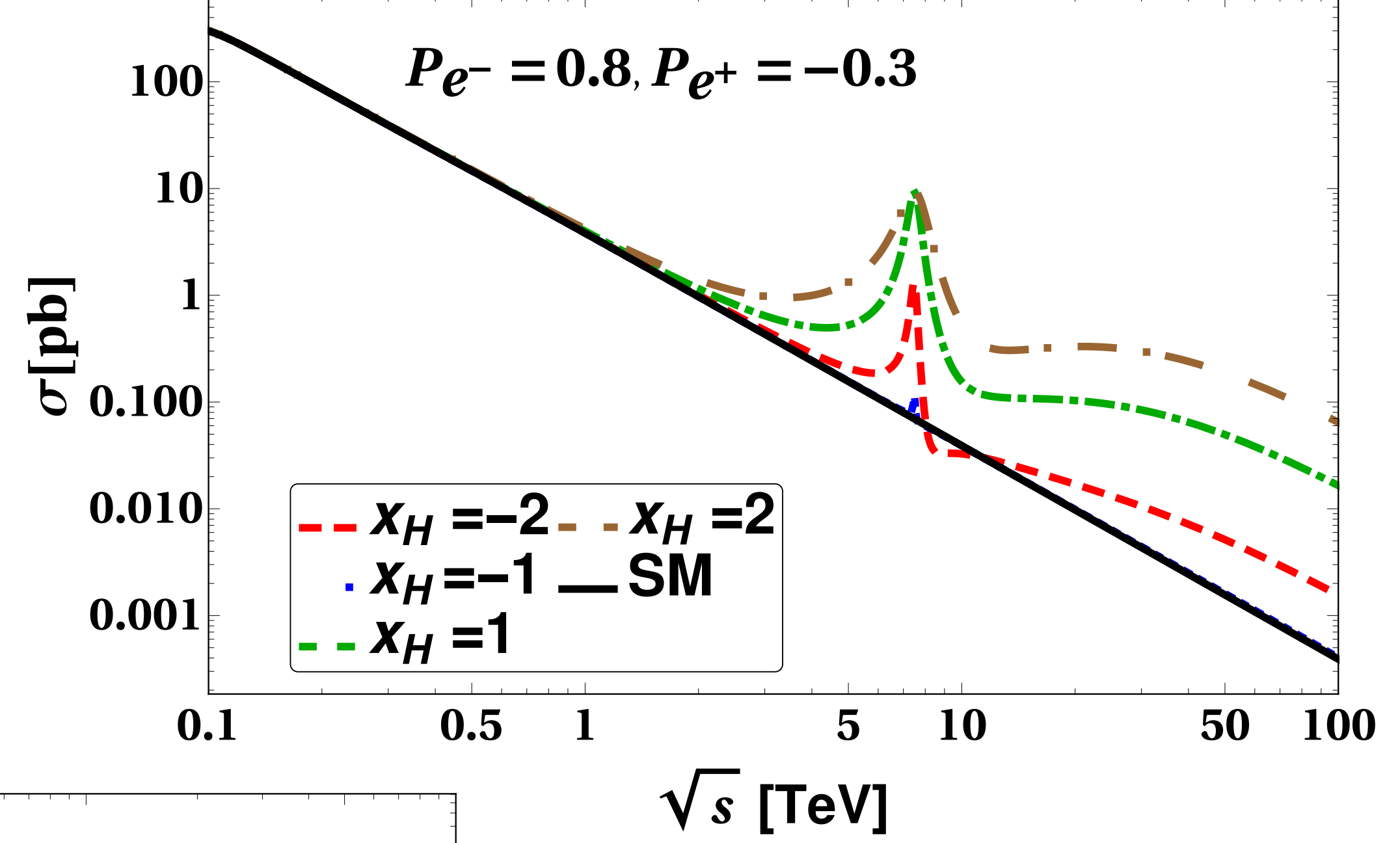
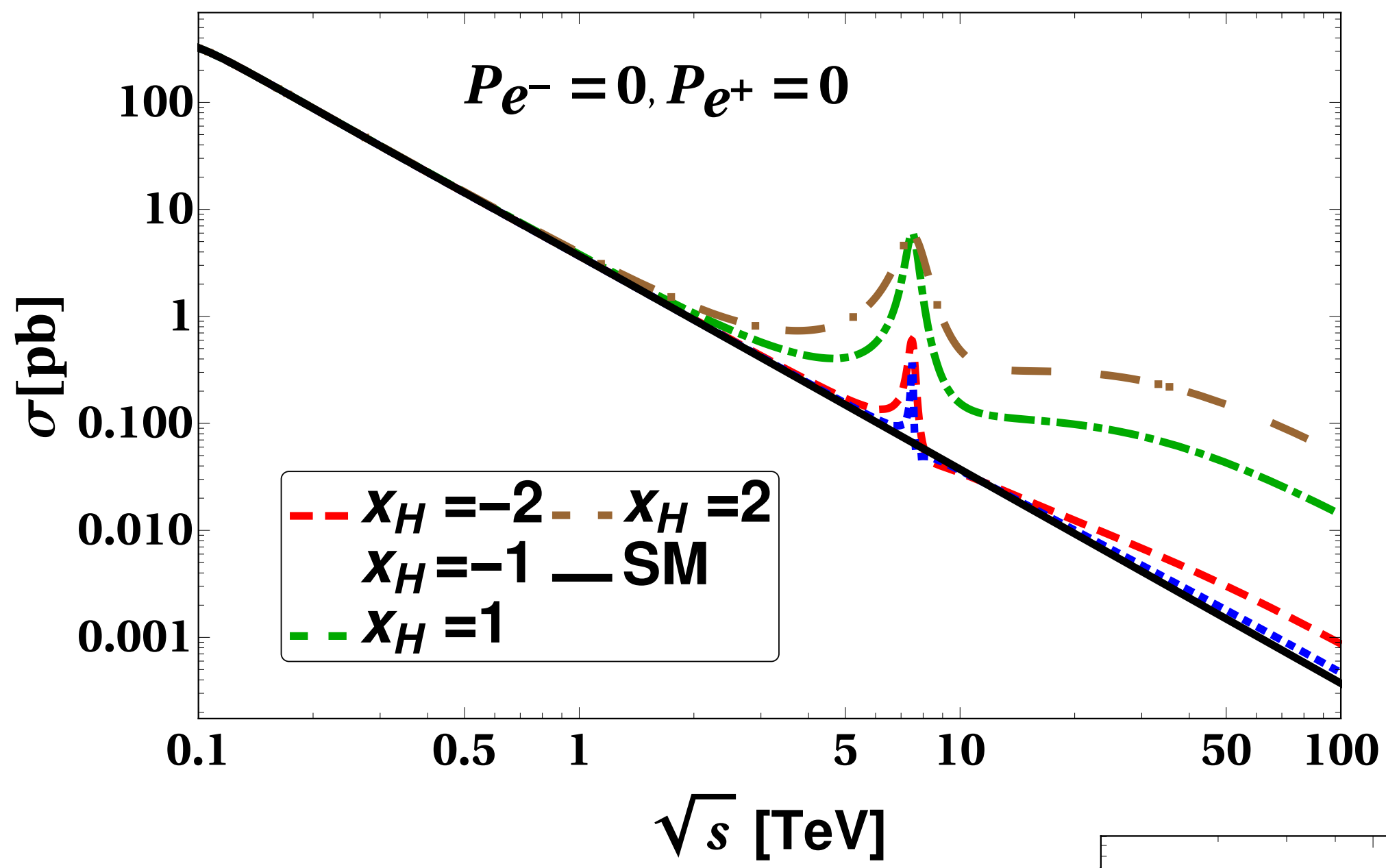
## Statistical error

$$\Delta \mathcal{A}_{LR,FB} = 2 \frac{(n_3 + n_2)(\sqrt{n_1} + \sqrt{n_4}) + (n_1 + n_4)(\sqrt{n_3} + \sqrt{n_2})}{(n_1 + n_4)^2 - (n_3 + n_2)^2} \mathcal{A}_{LR,FB}$$



# Bhabha scattering

$$e^-e^+ \rightarrow e^+e^-$$



**24** Deviations in total cross sections from SM is more than 100 % for  $x_H \geq 1$  for  $\sqrt{s} = 3$  TeV. For  $\sqrt{s} < 3$  TeV the deviation is also sizable.



# Bhabha scattering

$$q_s(s)^{\text{LL}} = \frac{e^2}{s} + \frac{g_L^2}{s - M_Z^2 + iM_Z\Gamma_Z} + \frac{g_L'^2}{s - M_{Z'}^2 + iM_{Z'}\Gamma_{Z'}}$$

$$q_s(s)^{\text{RR}} = \frac{e^2}{s} + \frac{g_R^2}{s - M_Z^2 + iM_Z\Gamma_Z} + \frac{g_R'^2}{s - M_{Z'}^2 + iM_{Z'}\Gamma_{Z'}}$$

$$q_s(s)^{\text{LR}} = q_s(s)^{\text{RL}} = \frac{e^2}{s} + \frac{g_L g_R}{s - M_Z^2 + iM_Z\Gamma_Z} + \frac{g_L' g_R'}{s - M_{Z'}^2 + iM_{Z'}\Gamma_{Z'}}$$

$s$  - channel

$$q_t(s, \theta)^{\text{LL}} = \frac{e^2}{t} + \frac{g_L^2}{t - M_Z^2 + iM_Z\Gamma_Z} + \frac{g_L'^2}{t - M_{Z'}^2 + iM_{Z'}\Gamma_{Z'}}$$

$$q_t(s, \theta)^{\text{RR}} = \frac{e^2}{t} + \frac{g_R^2}{t - M_Z^2 + iM_Z\Gamma_Z} + \frac{g_R'^2}{t - M_{Z'}^2 + iM_{Z'}\Gamma_{Z'}}$$

$$q_t(s, \theta)^{\text{LR}} = q_t(s, \theta)^{\text{RL}} = \frac{e^2}{t} + \frac{g_L g_R}{t - M_Z^2 + iM_Z\Gamma_Z} + \frac{g_L' g_R'}{t - M_{Z'}^2 + iM_{Z'}\Gamma_{Z'}}$$

$t$  - channel

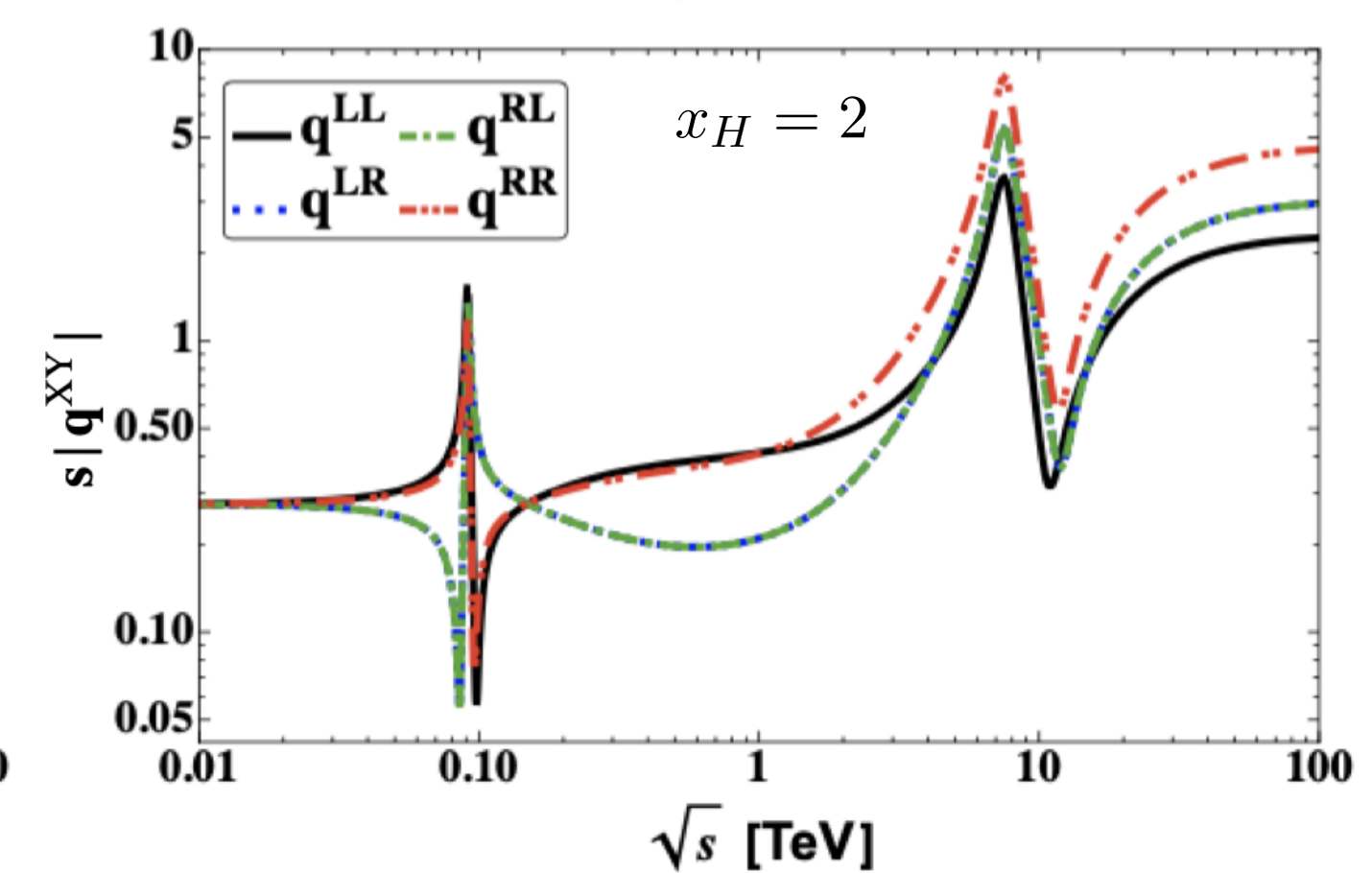
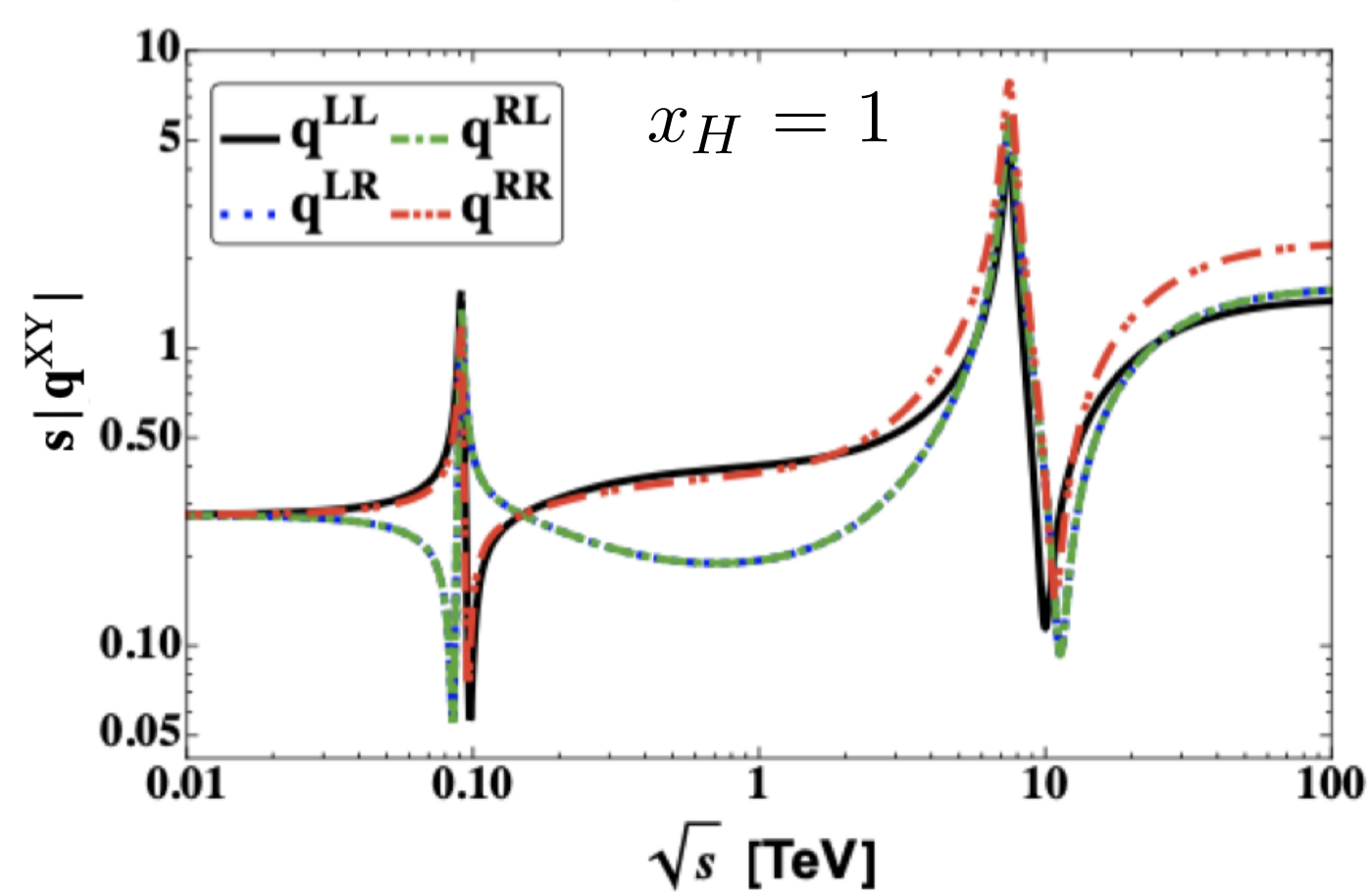
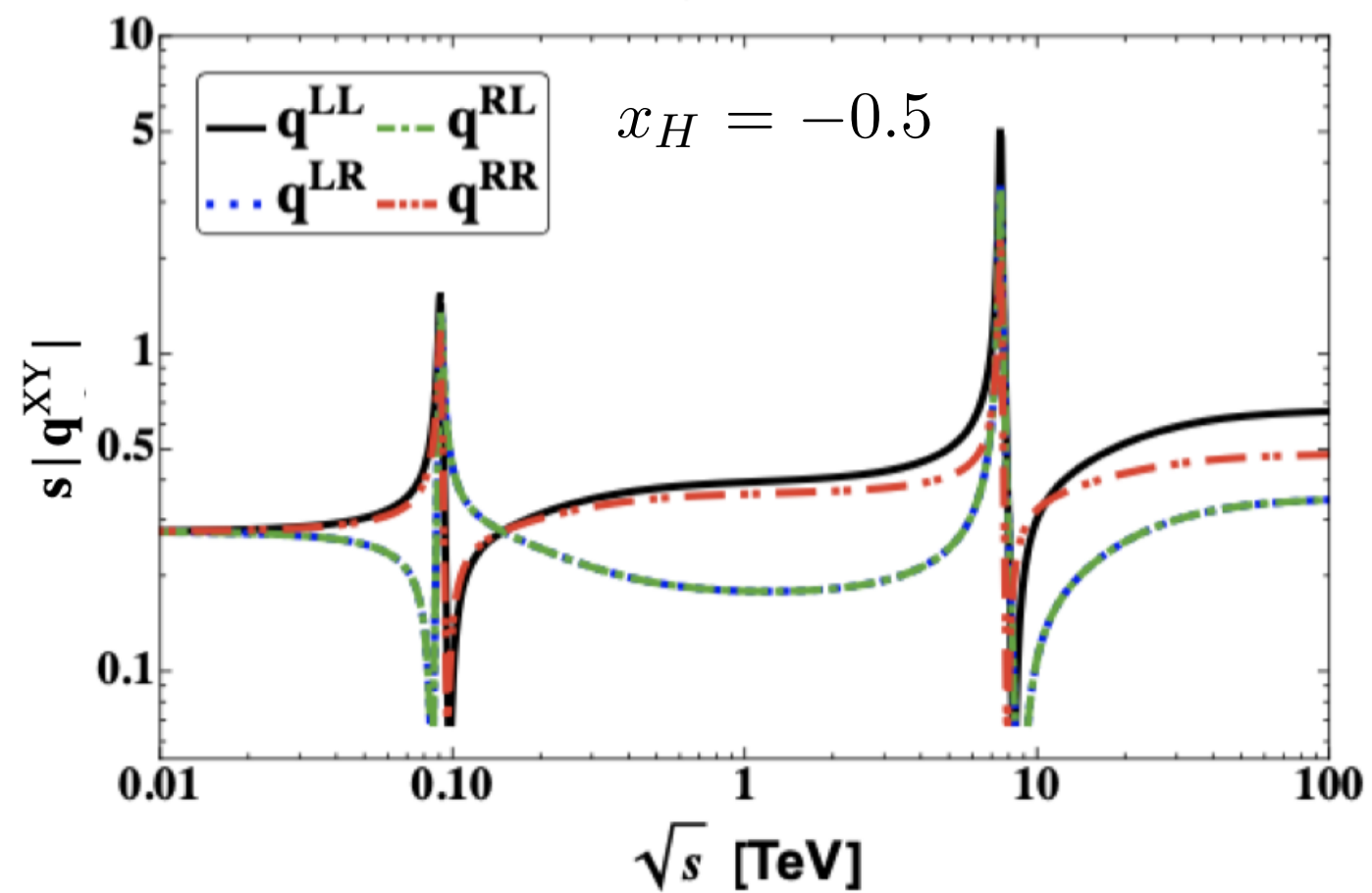
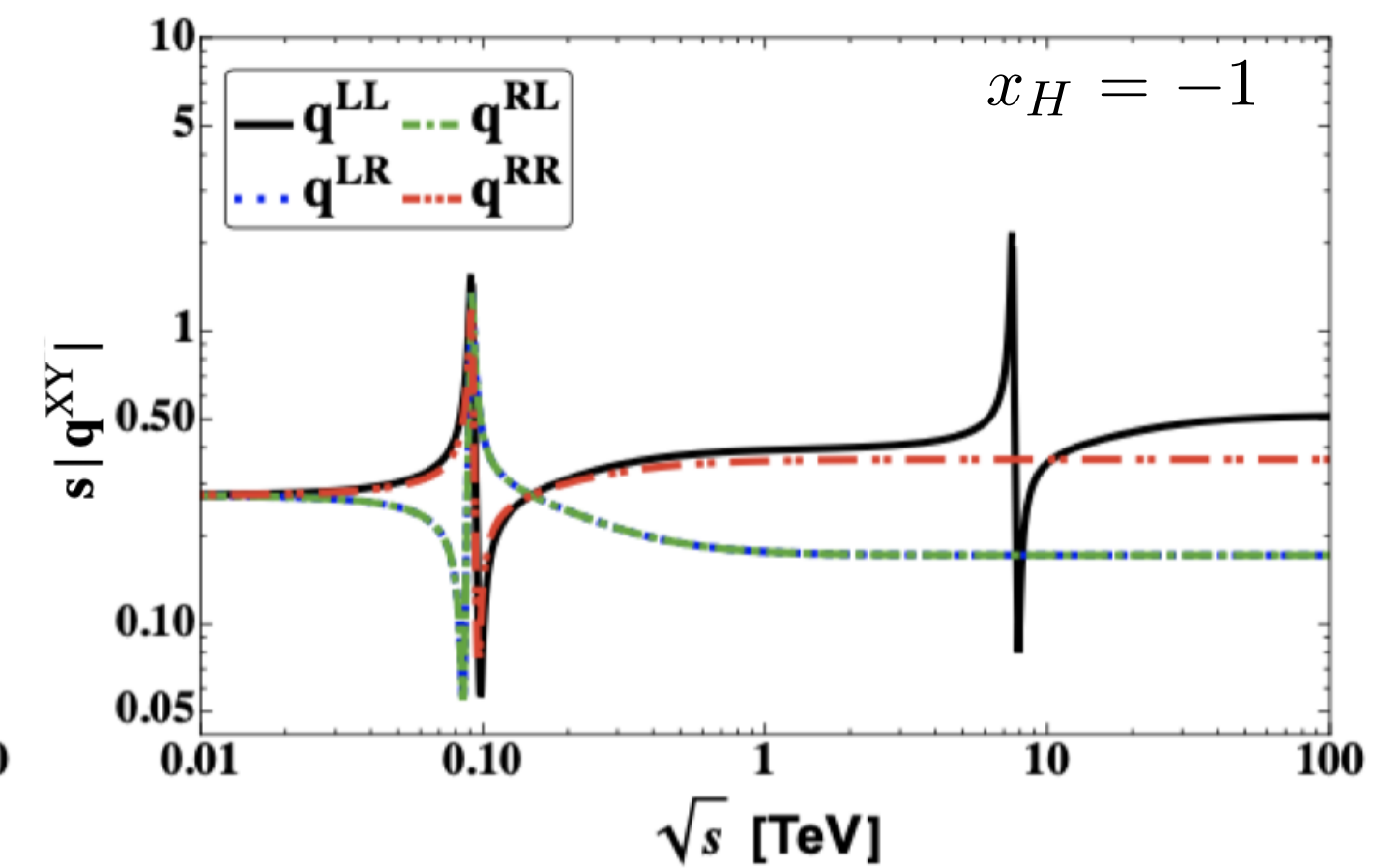
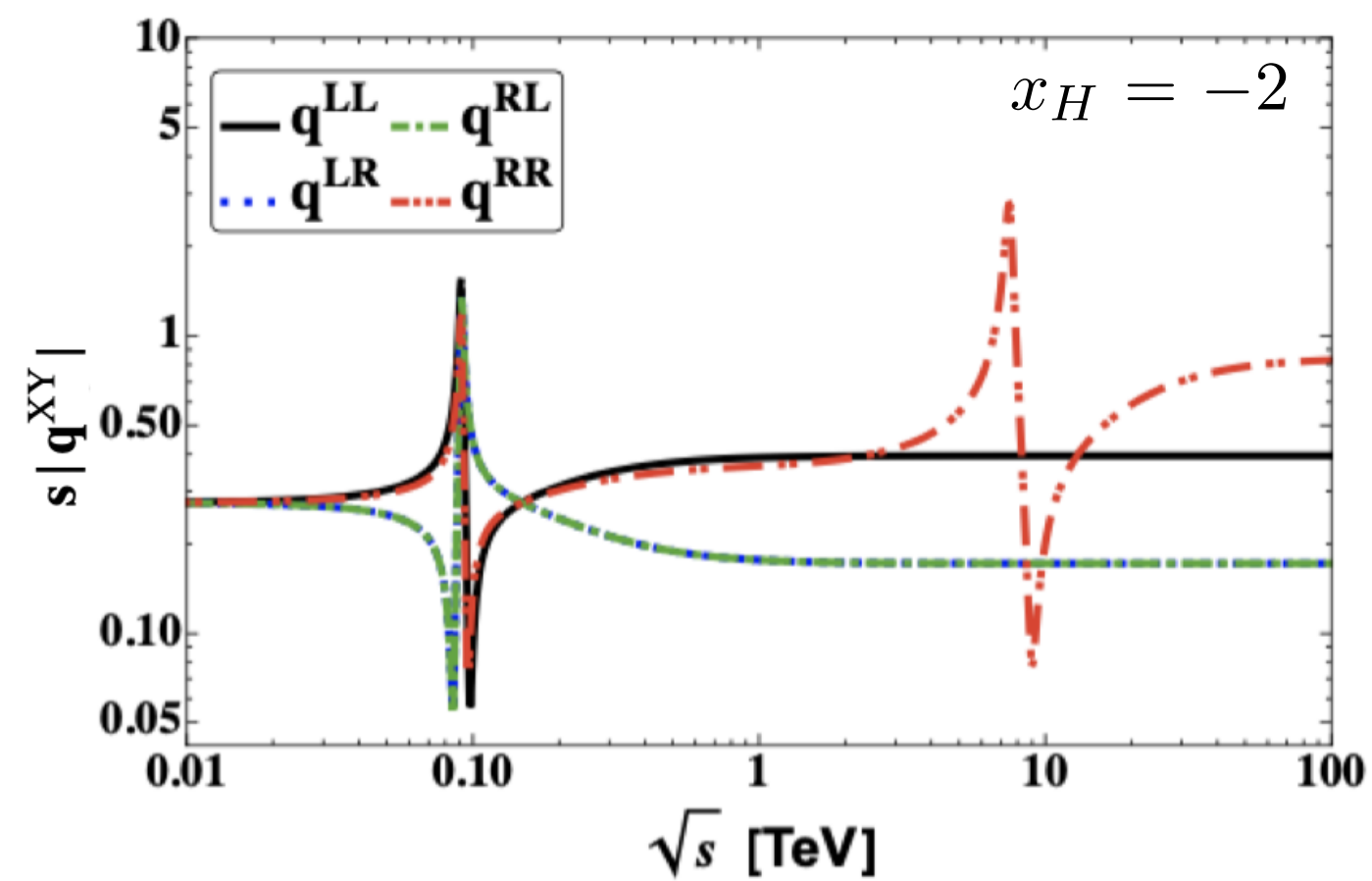
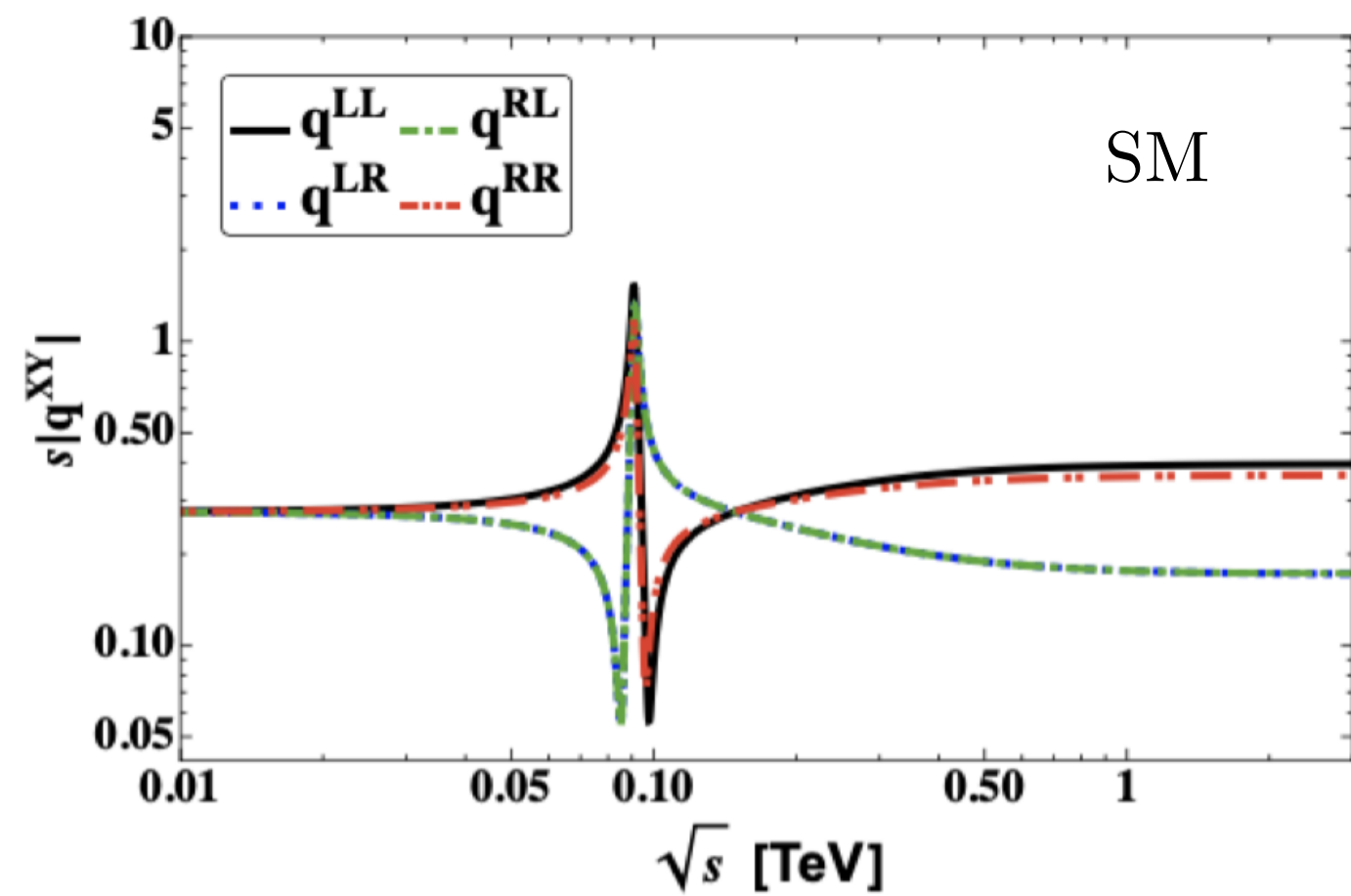
$$s|q^{\text{LL}}| = s|q_s(s)^{\text{LL}} + q_t(s, \theta)^{\text{LL}}|$$

$$s|q^{\text{LR}}| = s|q_s(s)^{\text{LR}} + q_t(s, \theta)^{\text{LR}}|$$

$$s|q^{\text{RL}}| = s|q_s(s)^{\text{RL}} + q_t(s, \theta)^{\text{RL}}|$$

$$s|q^{\text{RR}}| = s|q_s(s)^{\text{RR}} + q_t(s, \theta)^{\text{RR}}|$$

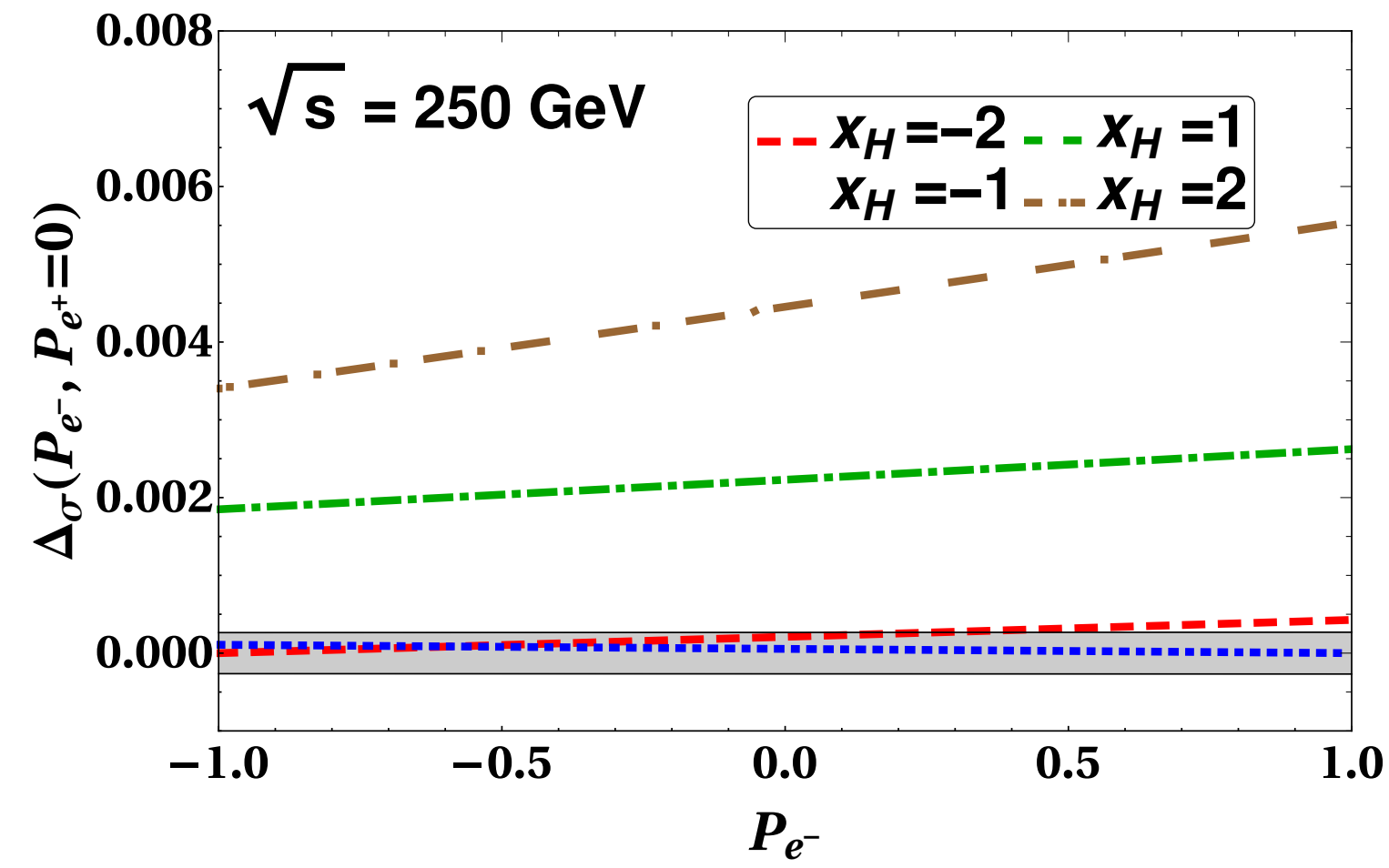
combined



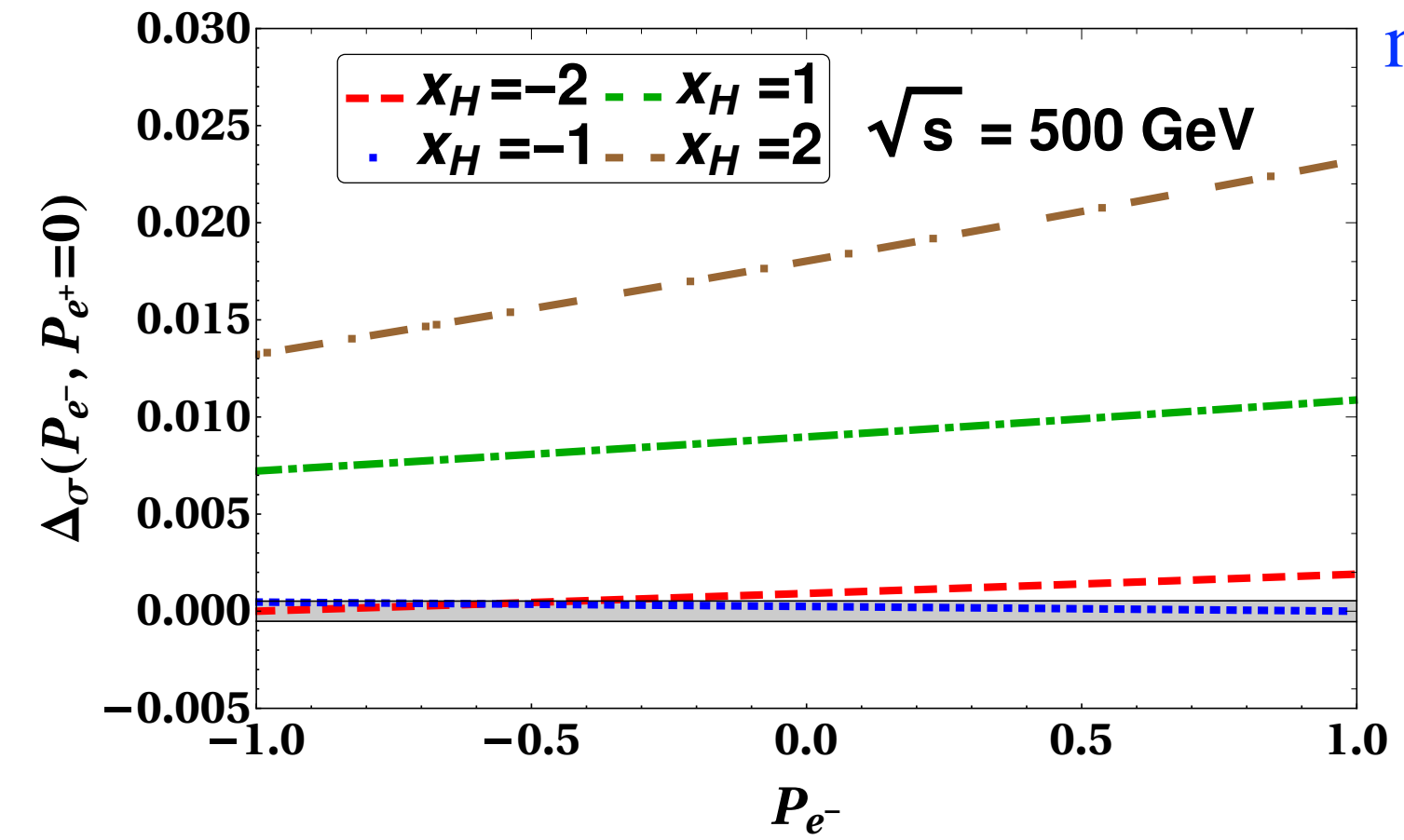
# Deviation in differential scattering cross section

$M'_Z = 7.5 \text{ TeV}$

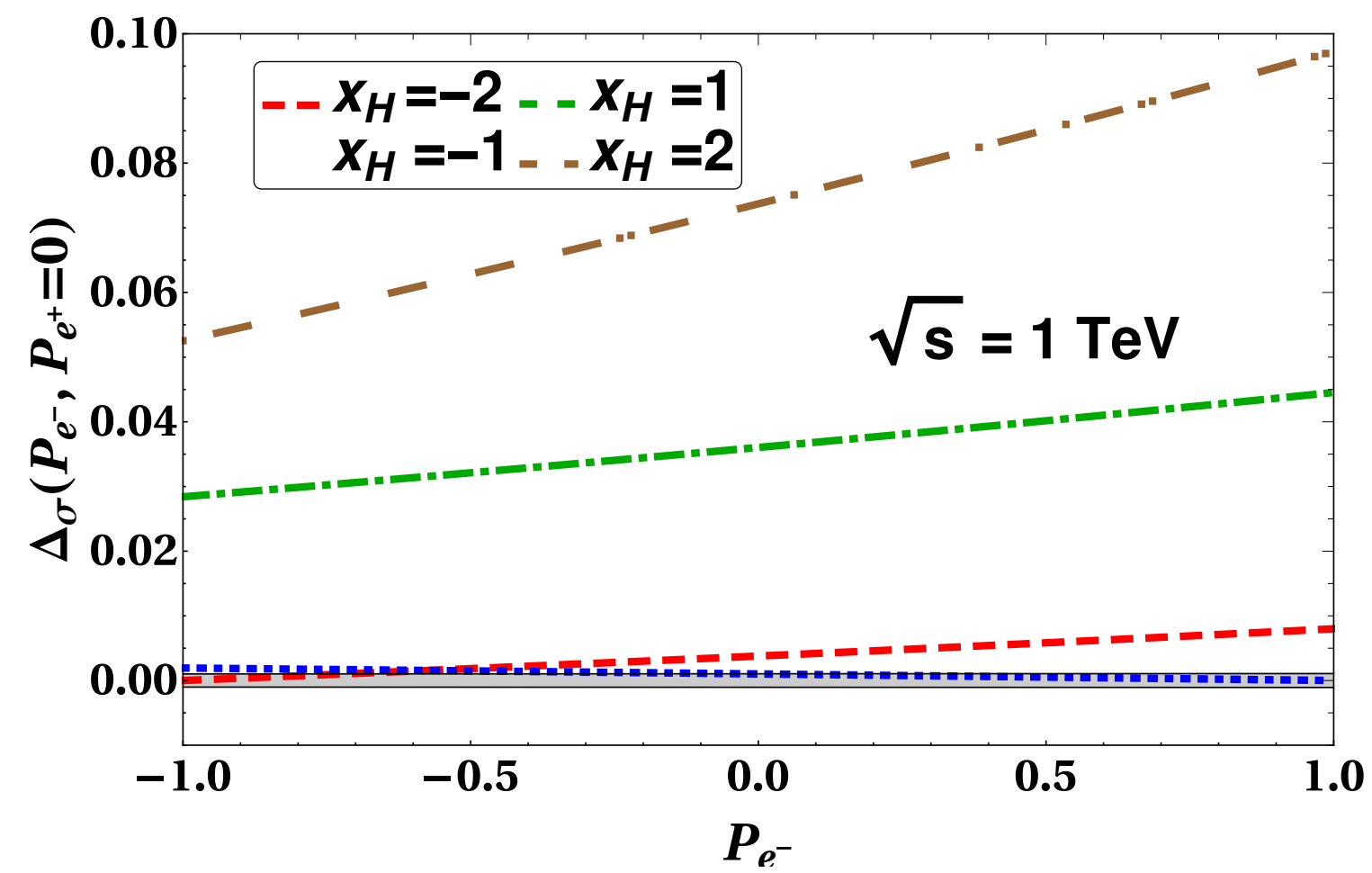
maximum deviation 0.6 %



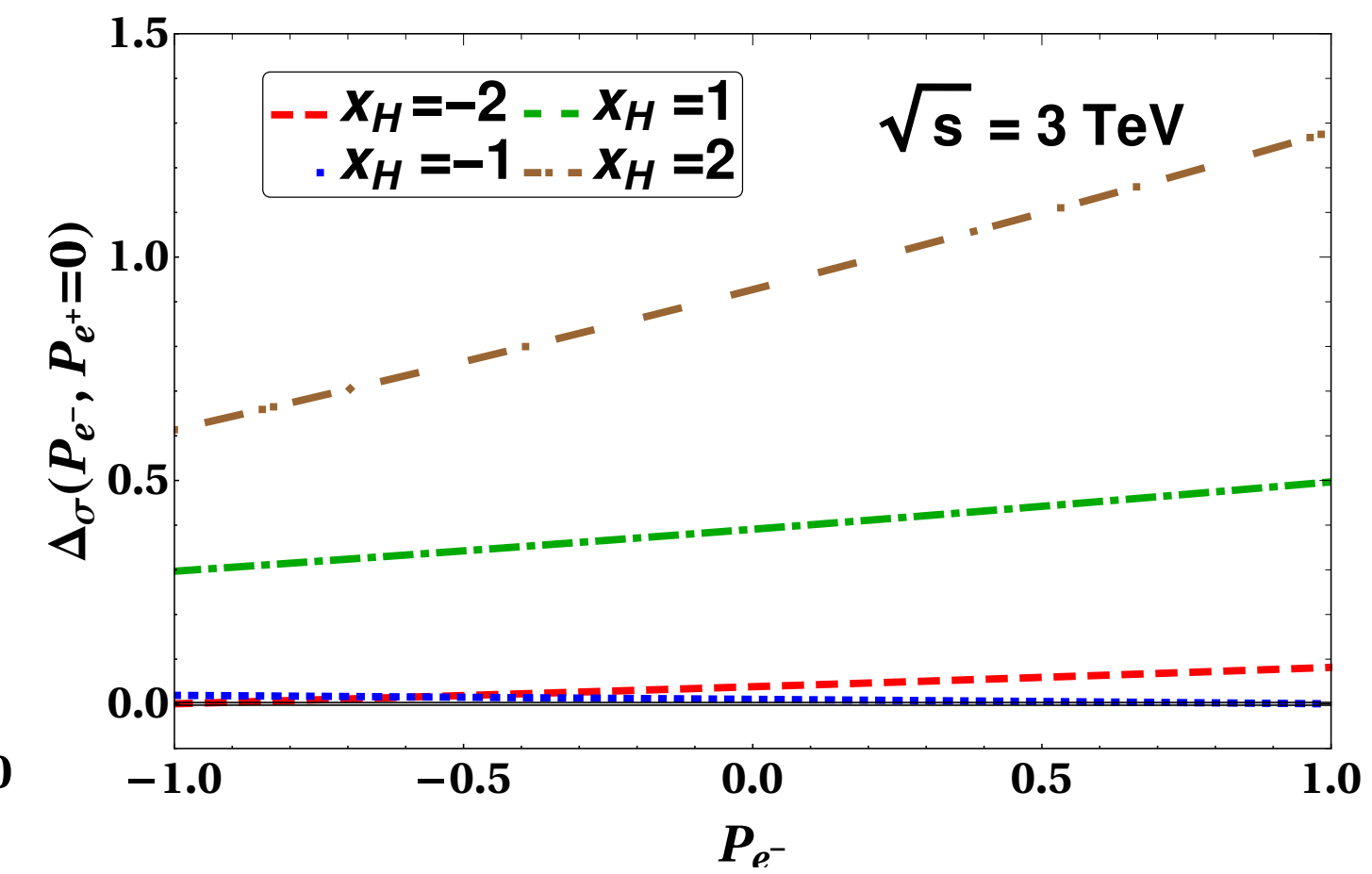
maximum deviation 2.3 %



maximum deviation 10 %



> 100 %



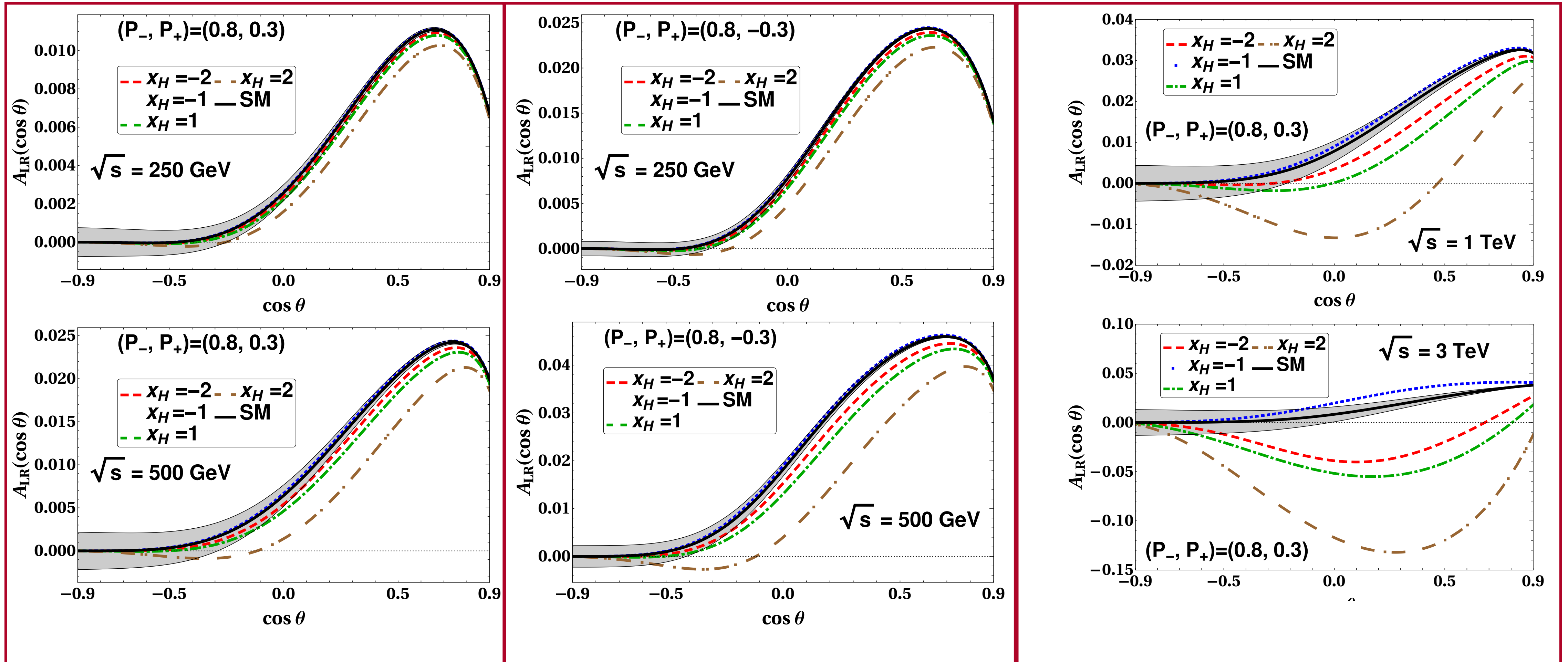
# Differential LR asymmetry

$$M'_Z = 7.5 \text{ TeV}$$

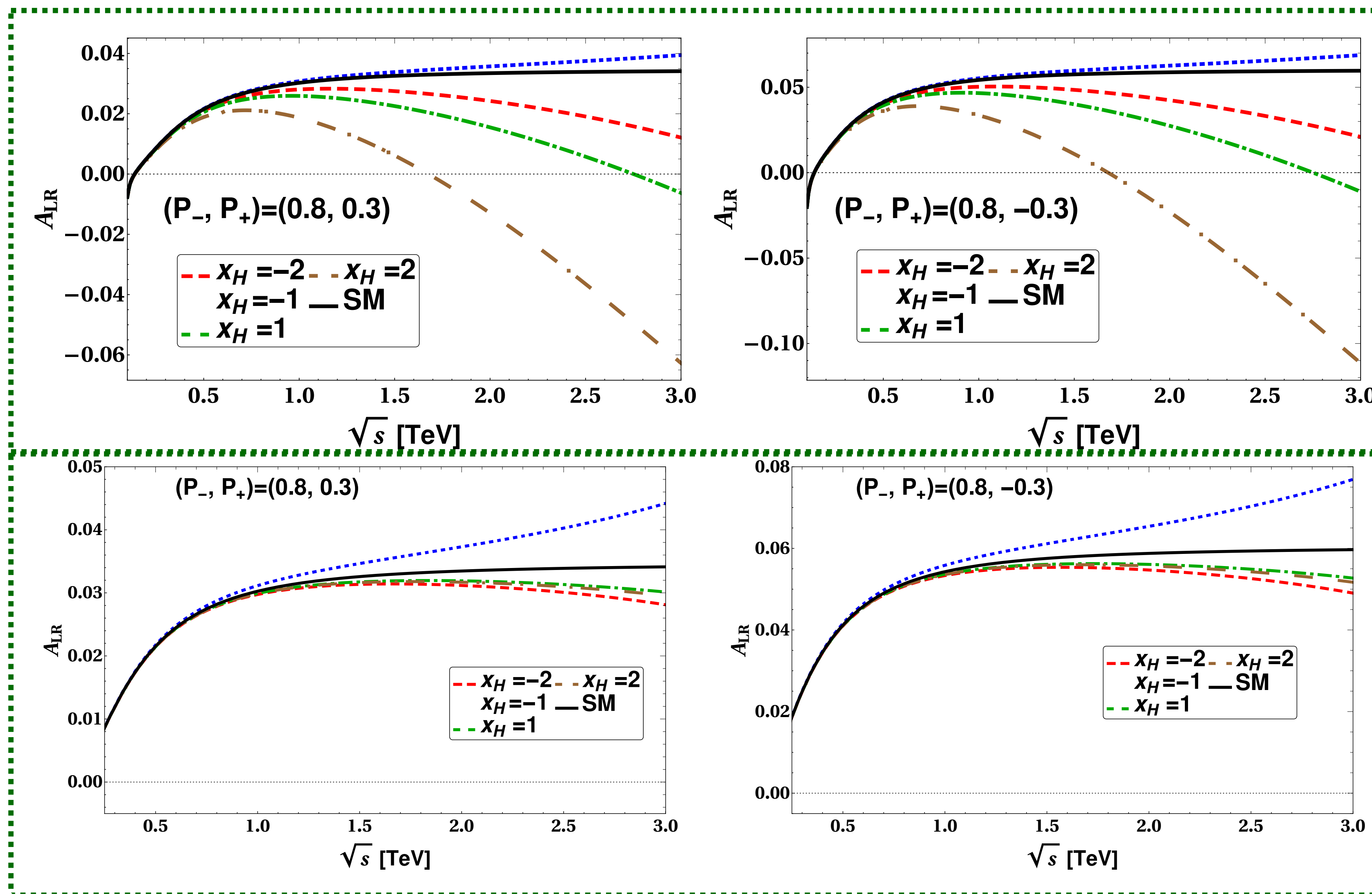
maximum deviation 1 – 2 %  
 $\sqrt{s} = 250 \text{ GeV}$

maximum deviation 2.3 – 4.3 %  
 $\sqrt{s} = 500 \text{ GeV}$

maximum deviation 12 – 13 %  
 $\sqrt{s} = 1 \text{ TeV}$



# Integrated LR asymmetry



$M_{Z'} = 7.5$  TeV

$M_{Z'} = 5$  TeV

The choices of  $x_H$  enhance the discovery potential

## Conclusions :

We are looking for a scenario where which can explain a variety of beyond the SM sceanrios .

The proposal for the generation of the tiny neutrino mass, from the seesaw mechanism, under investigation at the energy frontier .

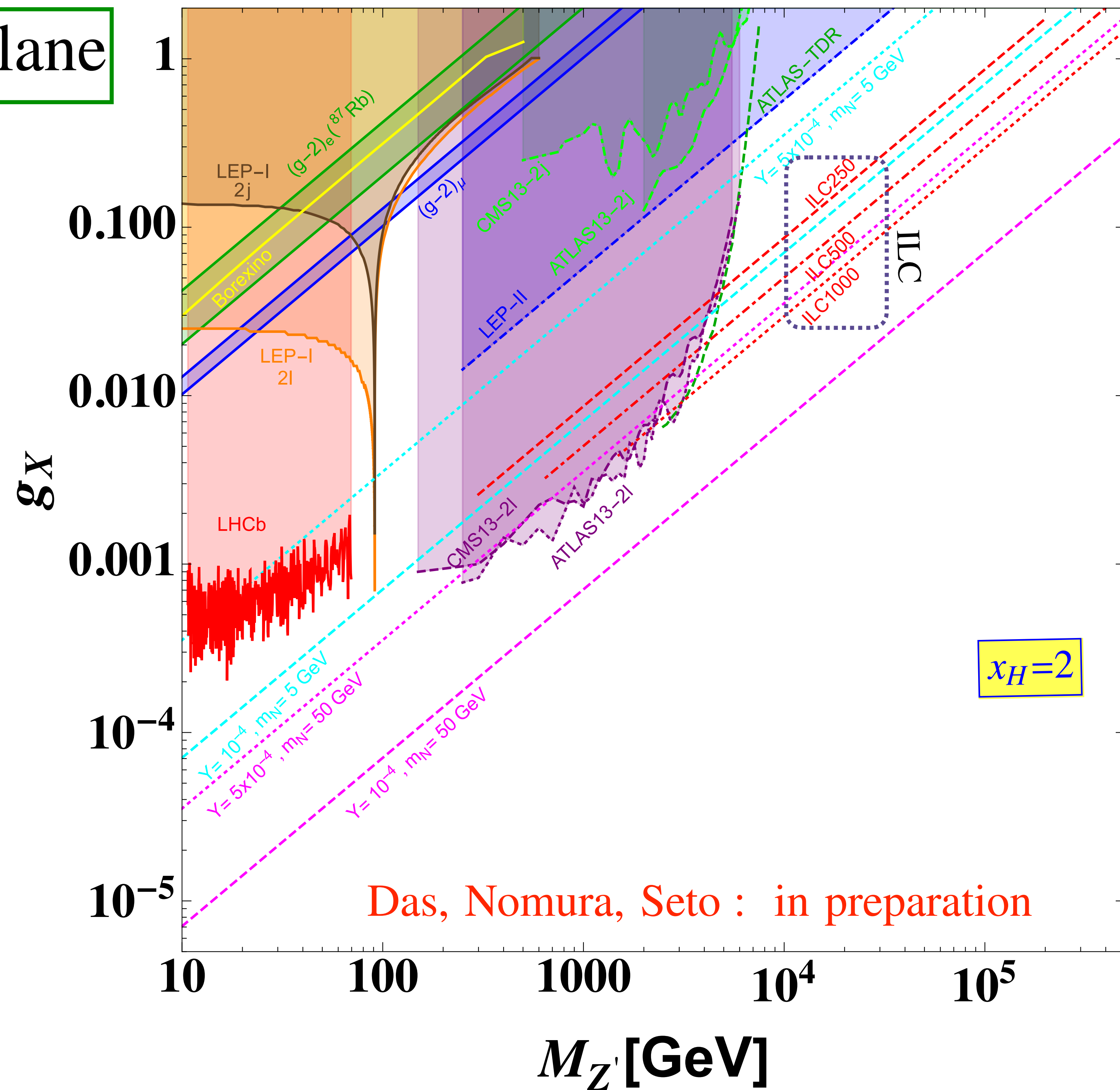
We study  $\mathcal{A}_{\text{FB}}$ ,  $\mathcal{A}_{\text{LR}}$ ,  $\mathcal{A}_{\text{LR, FB}}$  . The asymmetries are sizable at the 250 GeV and 500 GeV  $e^-e^+$  colliders or higher in the near future .

Such a model can be studied at muon colliders with high CM energy . This allows us to probe heavier  $Z'$  .

The motovation of this work is to find a new particle and/or a new force carrier as a part of the of the new physics searches including a variety of BSM aspects .

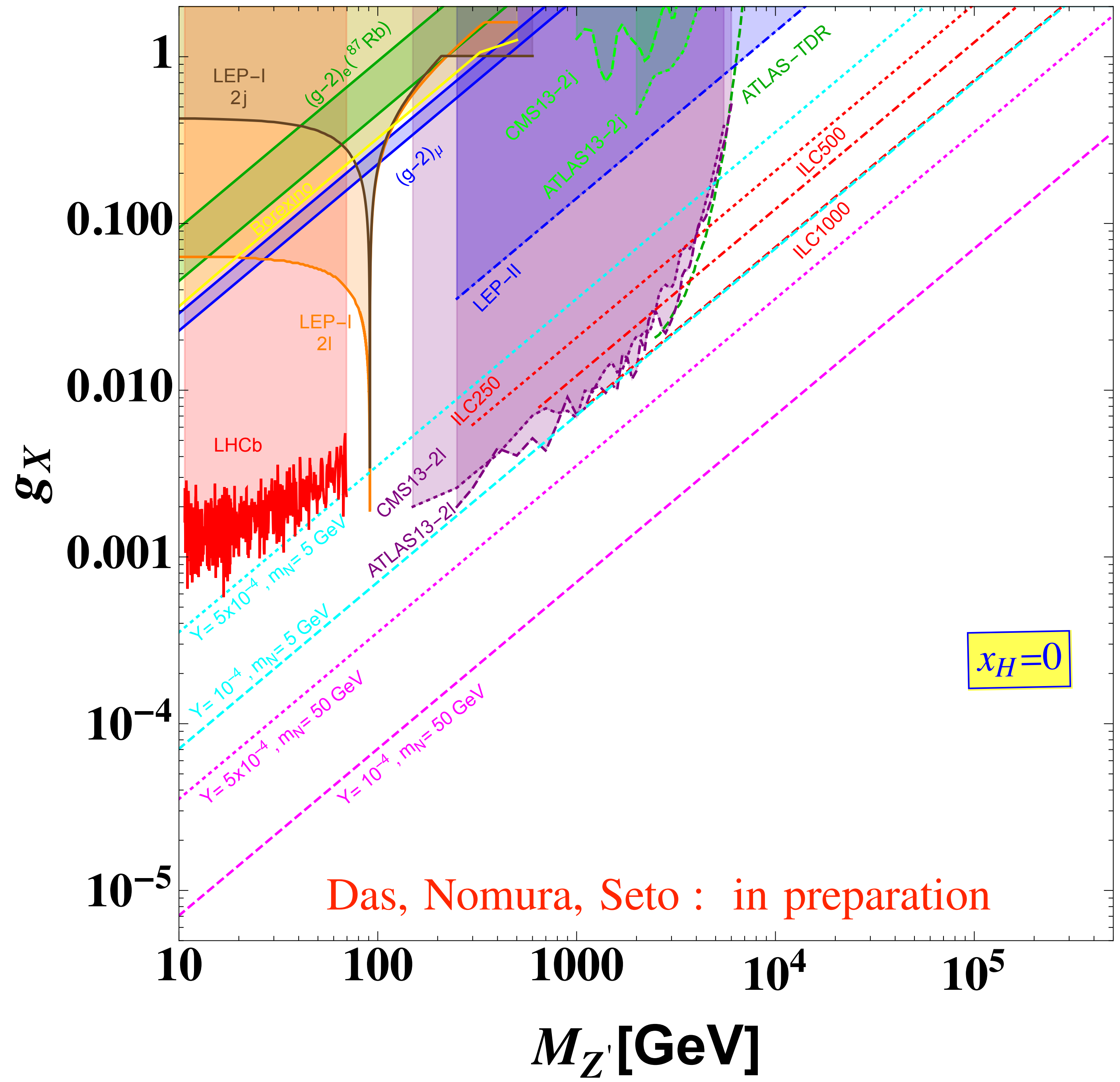
# Back-up Slides

# Limits on $g' - M_{Z'}$ plane



$x_H=2$

Das, Nomura, Seto : in preparation





Bounds on a sample B – L scenario with  $x_H = 0$ ,  $x_\Phi = 1$

