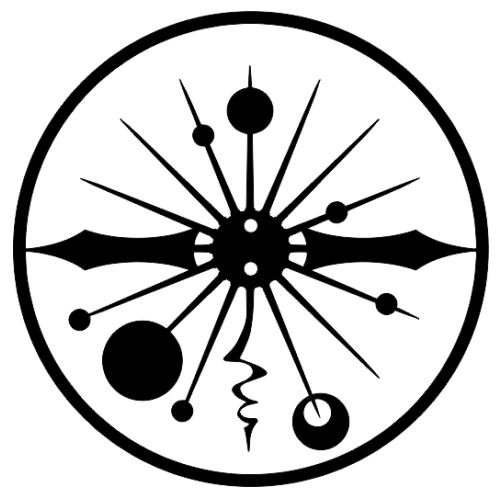
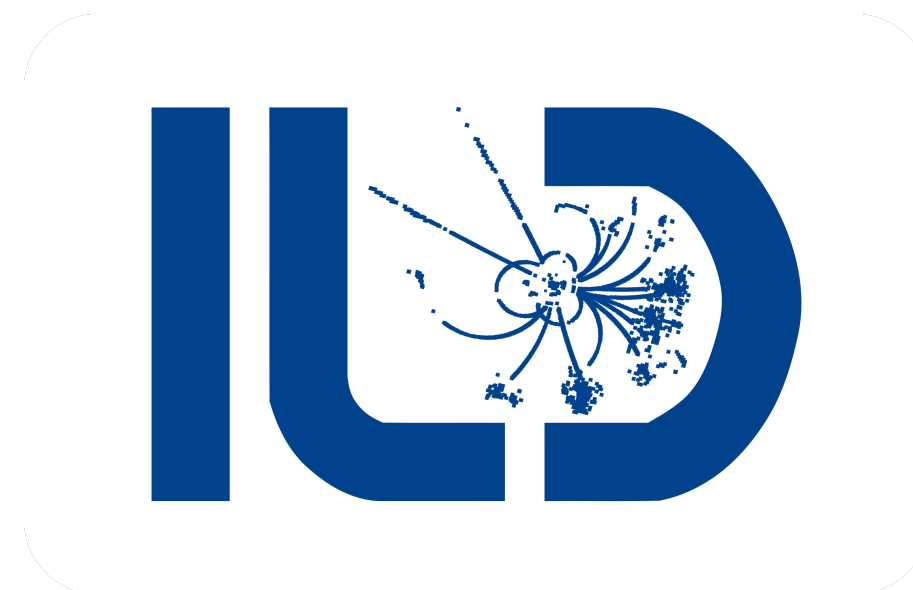


# Tau reconstruction in $e^+e^- \rightarrow \tau^+\tau^-$ at the ILC250



Keita Yumino



# Motivation 1

At the ILC, forward-backward asymmetry  $A_{FB} = \frac{3}{4} A_e \cdot A_f$  can be measured

Left- and right-handed coupling  $g_R, g_L$  to Z boson are different

⇒ Left- and right-handed polarisation asymmetry is expected.

$$A_f = \frac{g_R^2 - g_L^2}{g_R^2 + g_L^2}$$

Thanks to ILC's polarised beams,  $A_e$  can be measured

⇒  $A_f$  can be extracted from  $A_{FB}$

By measuring  $A_{FB}$  precisely and looking for deviations from SM predictions, it is possible to search for new physics, such as heavy gauge boson  $Z'$

# Motivation 2

Tau has extra information

tau is the only particle that can measure the polarisation of the final state in the ILC250

We can also directly measure  $A_\tau$  by using tau polarisation  $P(\tau)$

$$\frac{dP(\tau)}{d\cos\theta} = \frac{3}{8}A_\tau(1 + \cos^2\theta) + \frac{3}{4}A_e\cos\theta$$

The aim of this study

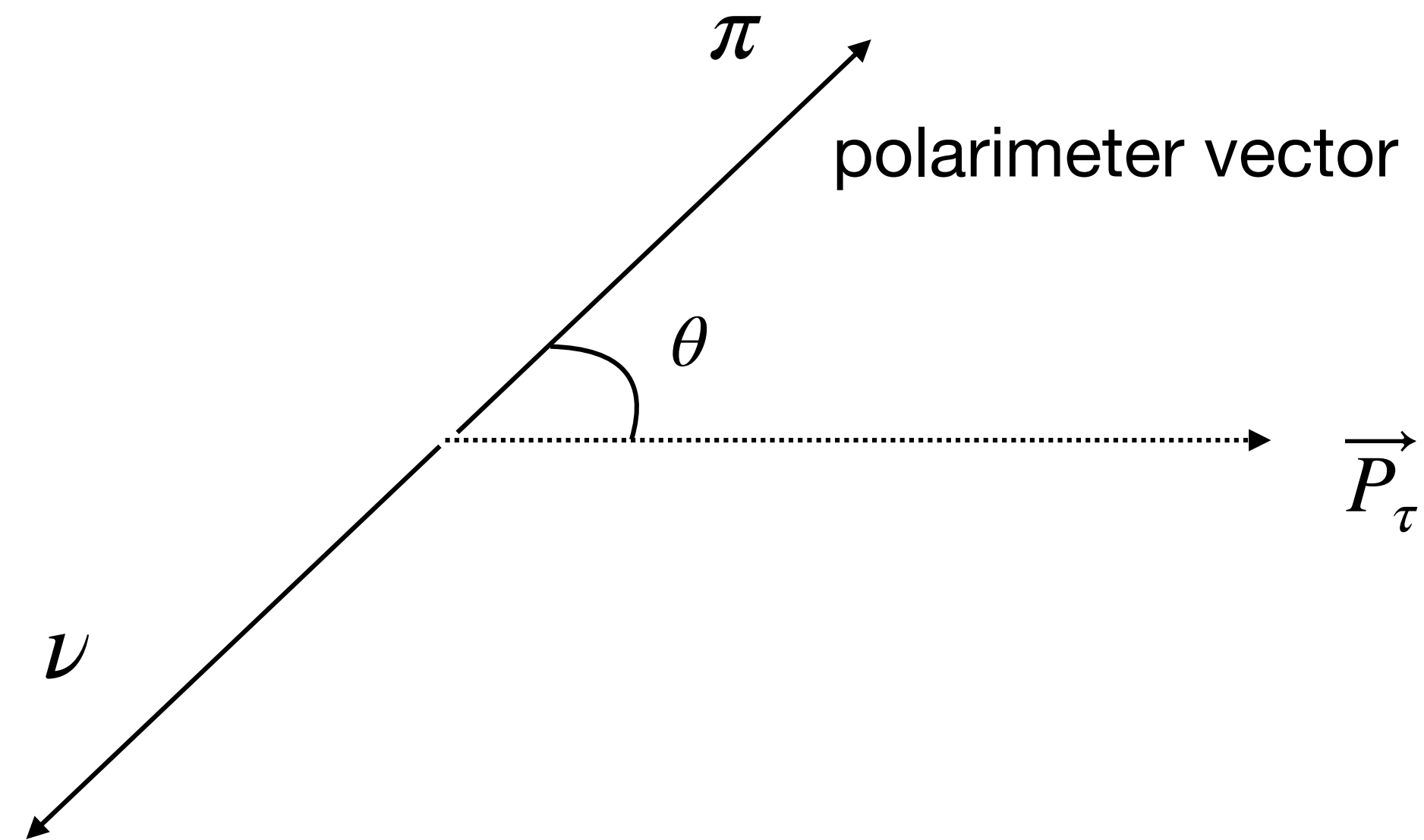
The reconstruction of tau spin orientation (“**Polarimeter**”)  
in order to measure polarisation to investigate new physics.

# Polarimeter

Reconstruction of tau polarisation  $P(\tau)$  depends on tau decay mode.

Polarimeter vectors of  $\tau \rightarrow \pi\nu$  in  $\tau$  rest frame

$$h(\tau^\pm \rightarrow \pi^\pm\nu) \propto p_{\pi^\pm}$$



Polarimeter vectors of  $\tau \rightarrow \rho\nu$  in  $\tau$  rest frame

$$h(\tau^\pm \rightarrow \pi^\pm\pi^0\nu) \propto m_\tau(E_{\pi^\pm} - E_{\pi^0})(p_{\pi^\pm} - p_{\pi^0}) + \frac{1}{2}(p_{\pi^\pm} + p_{\pi^0})^2 p_\nu$$

**“Polarimeter”**

The cosine of the angle this polarimeter vector makes to the tau flight direction

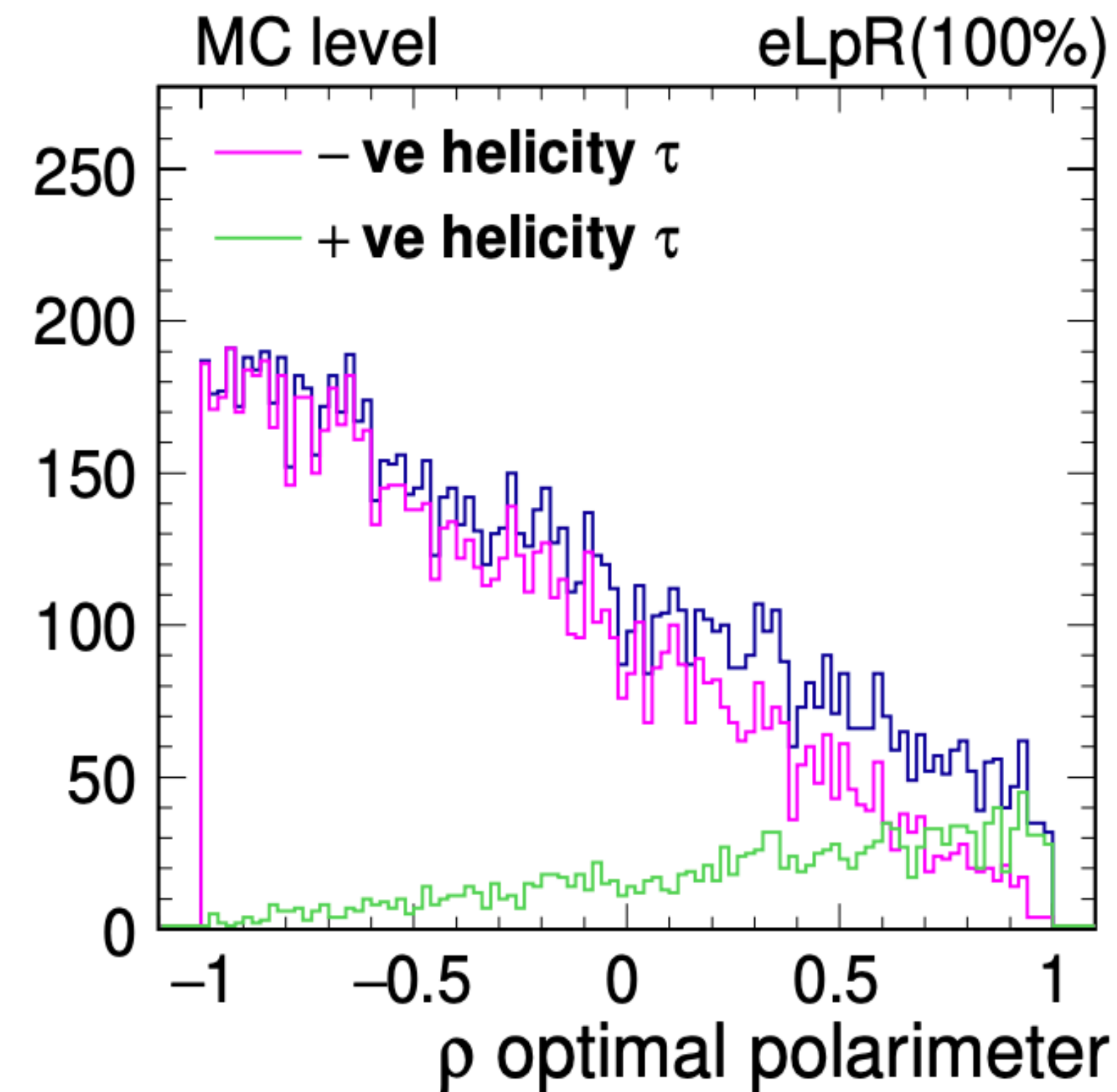
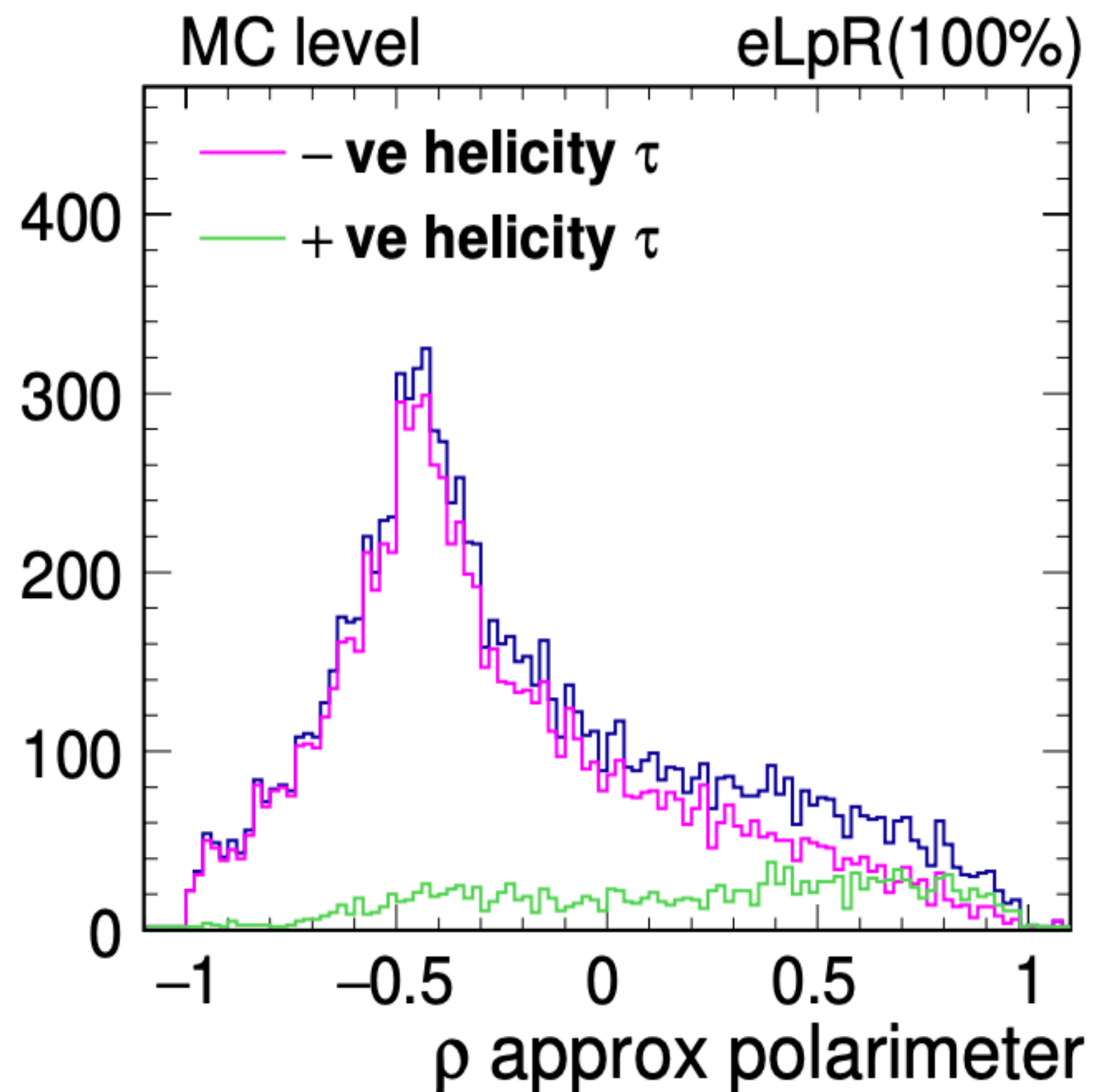
# Previous study

Extract polarimeter without using neutrino information

arXiv:1912.08403

"Approximate" polarimeters based only on the momenta of visible tau decay products

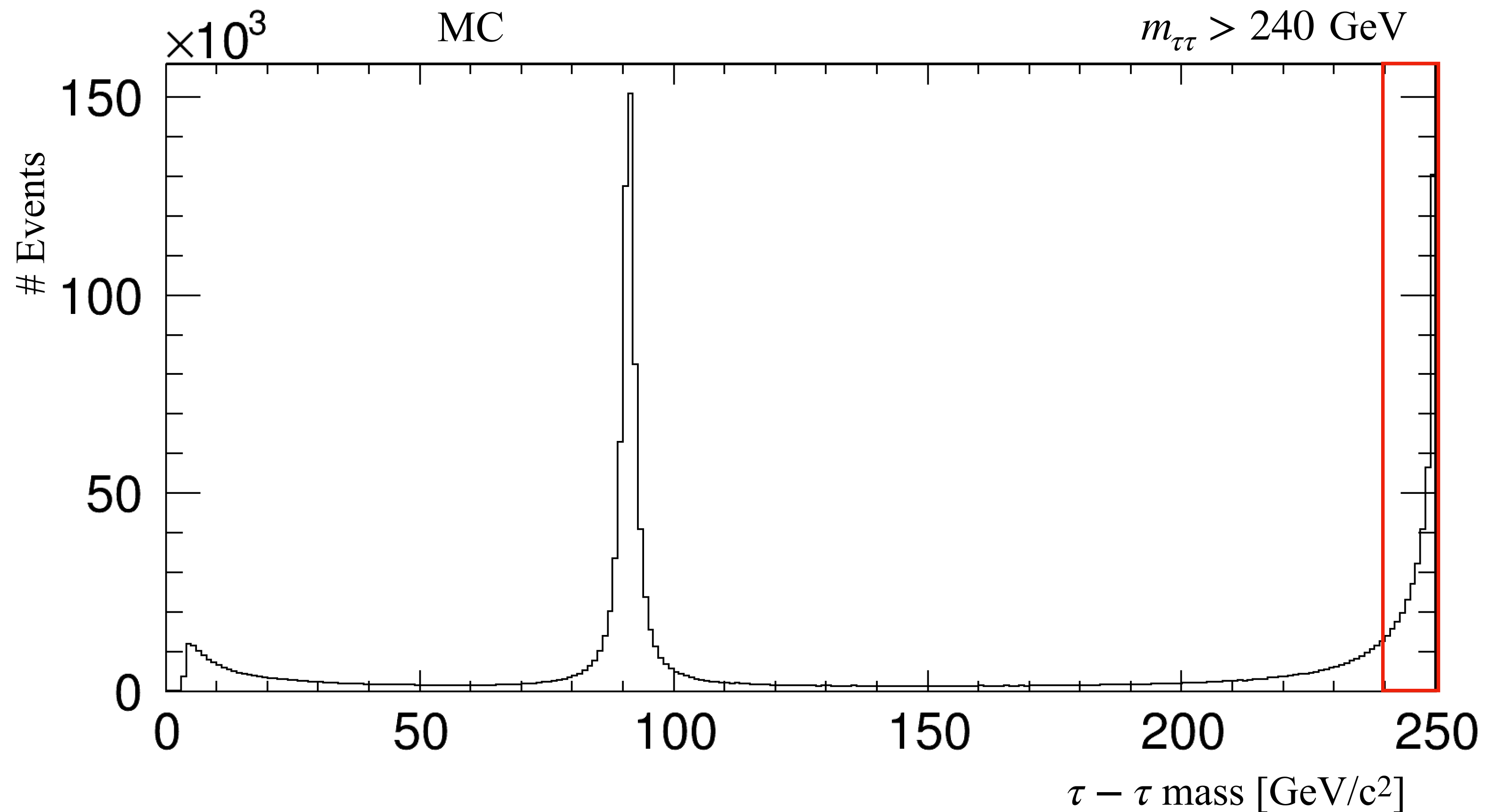
"Optimal" polarimeters including the neutrino component



We explicitly extract the neutrino momentum and reconstruct polarimeters

# Simulation setup

- Signal event sample with 100 %  $e_L^- e_R^+$  beam polarisations were generated using WHIZARD ver 2.8.5.
- The decay of the polarised tau was done using TAUOLA.
- MC truth information was used.



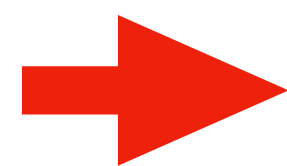
- only look at
  - $\tau \rightarrow \pi\nu$  (BR  $\sim 10\%$ )
  - $\tau \rightarrow \rho\nu$  (BR  $\sim 26\%$ )
  - $m_{\tau\tau} > 240 \text{ GeV}$



# $\tau$ reconstruction method

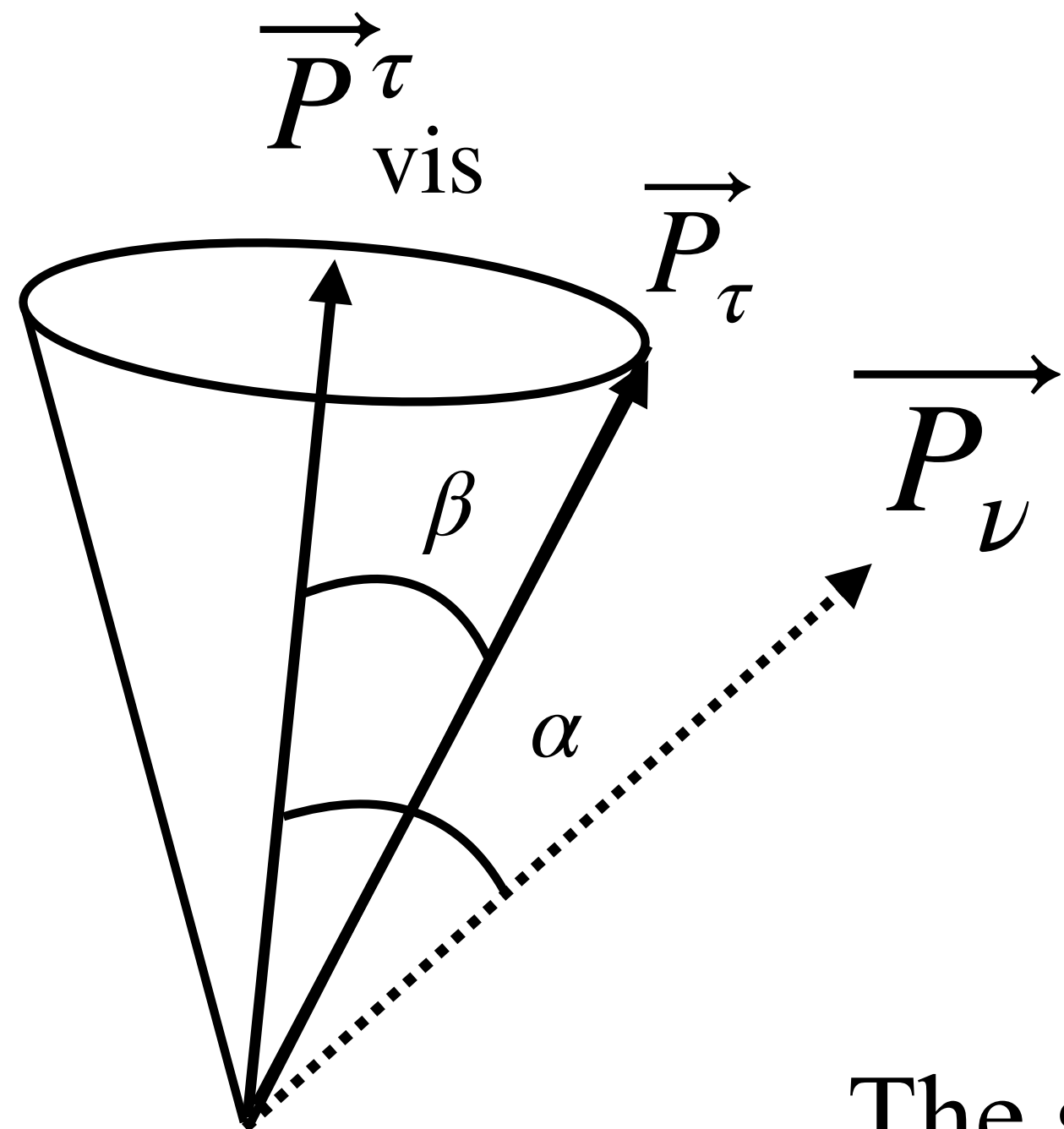
Assume

- 1 neutrino per tau
- $m_\tau = 1.776 \text{ GeV}$
- $E_\tau = \frac{E_{cm}}{2}$



from these assumptions,  $\tau$  direction must make an angle  $\beta$  to the visible  $\tau$  momentum

$$\cos \beta = f(\vec{P}_{\text{vis}}^\tau, m_\tau, E_\tau)$$



$\vec{P}_{\text{vis}}^\tau$  : tau visible daughter momentum

$\vec{P}_\nu$  : neutrino momentum

$\vec{P}_\tau$  : tau momentum

The same for the other tau

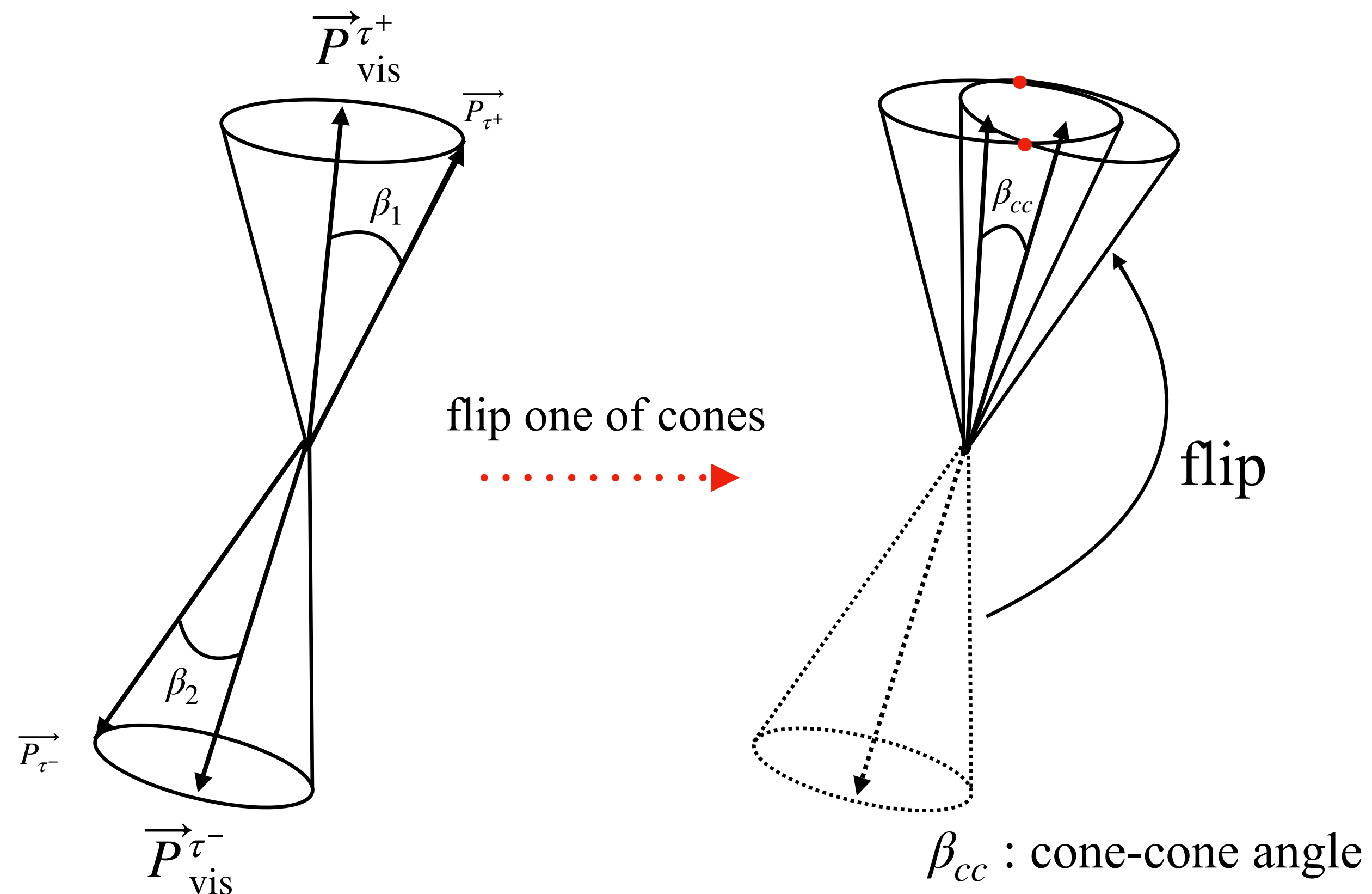
# $\tau$ reconstruction method

We further assume

- two taus are back-to-back

To reconstruct tau momentum, flip one of the cones and find the **intersections**.

The intersection of the cones are the candidate  $\tau$  momentum directions.

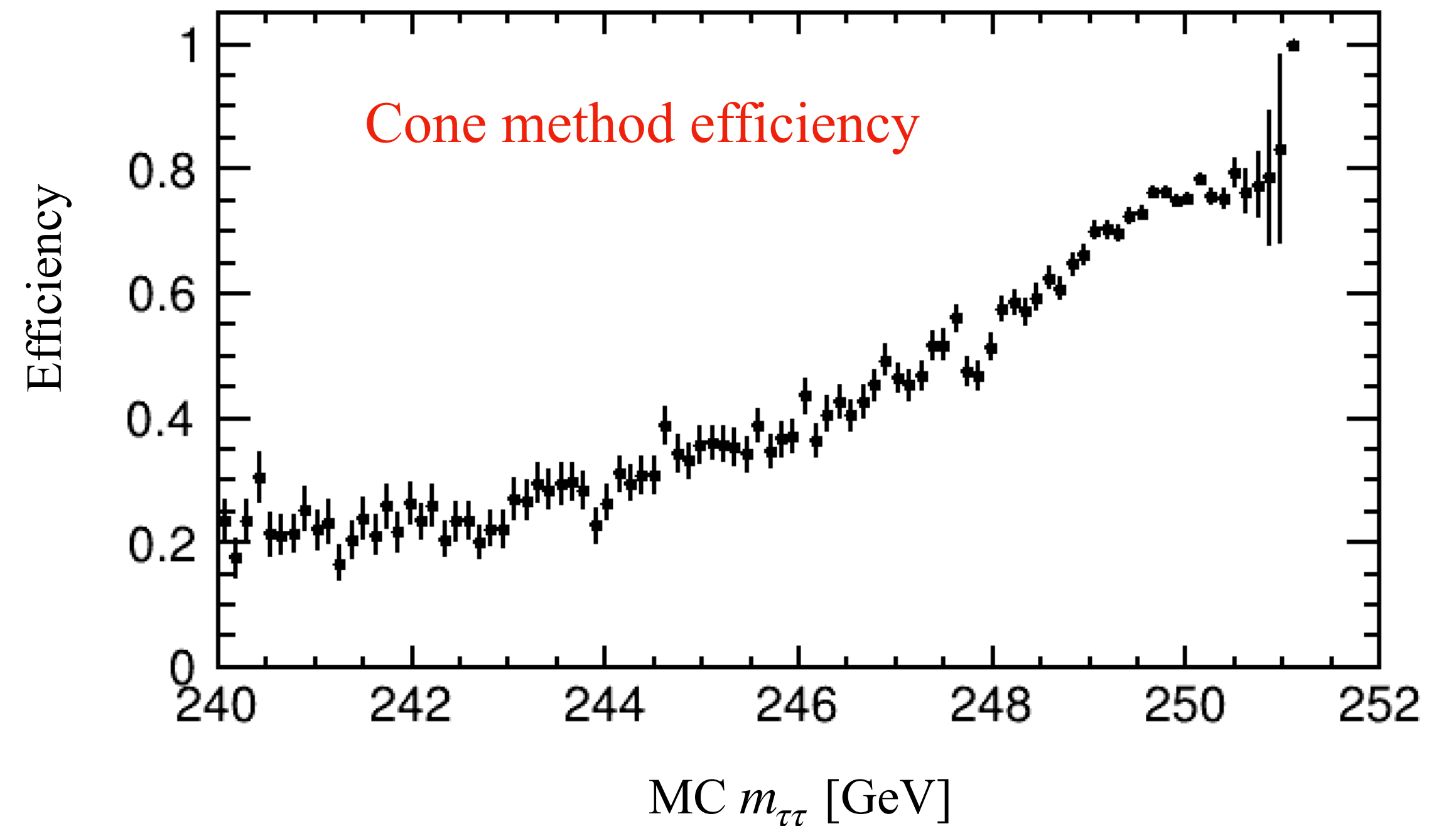
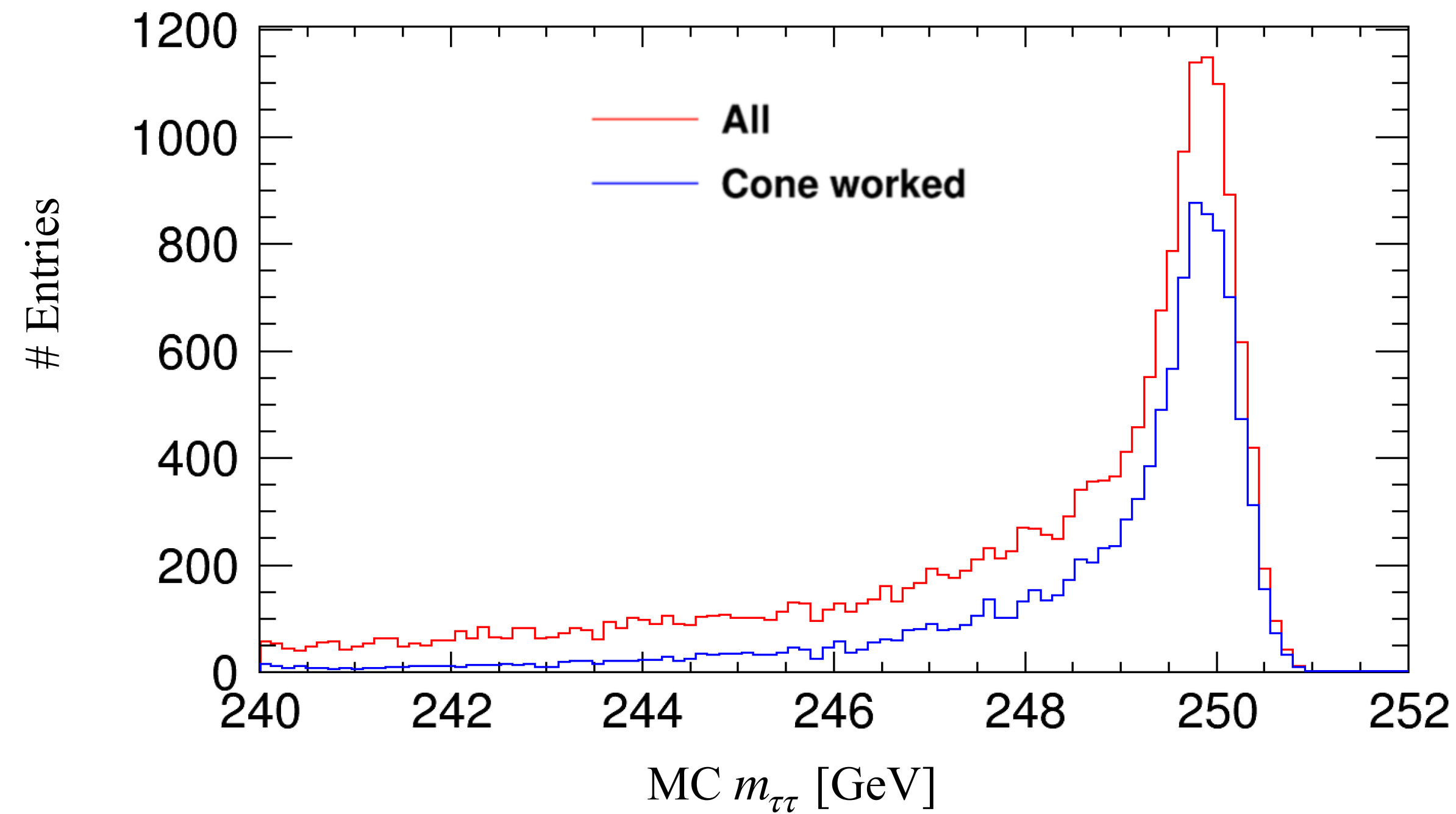
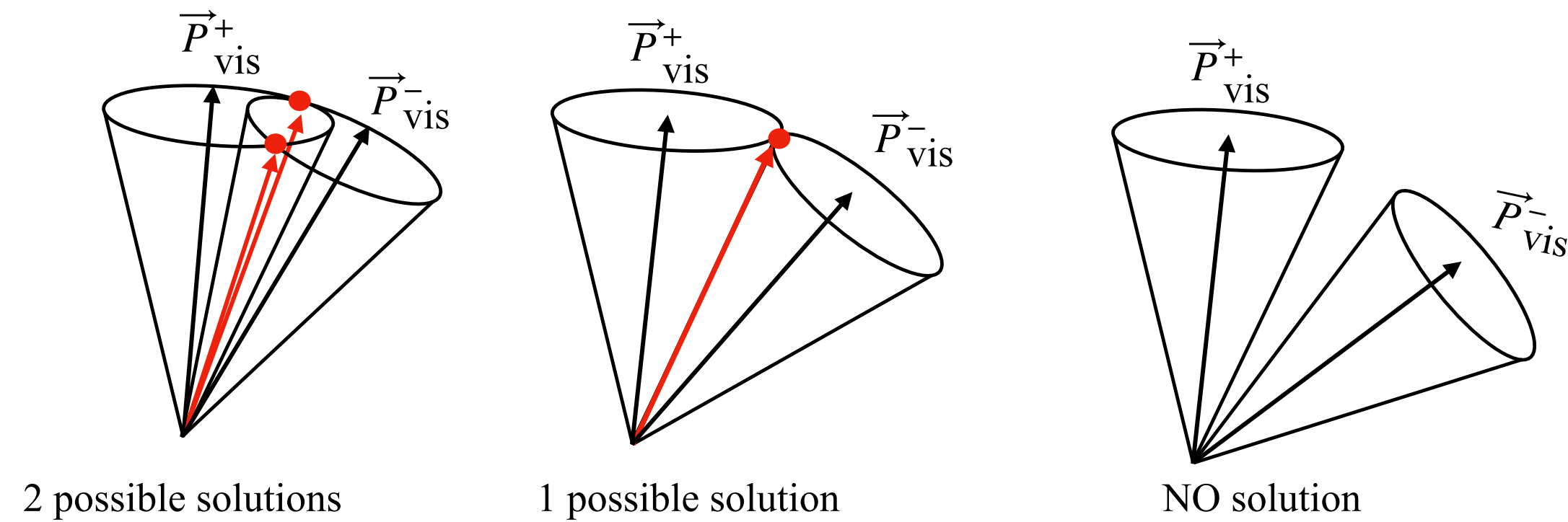


We call this “Cone method”



# Find solutions

If at least one intersection point was found, there is a solution.

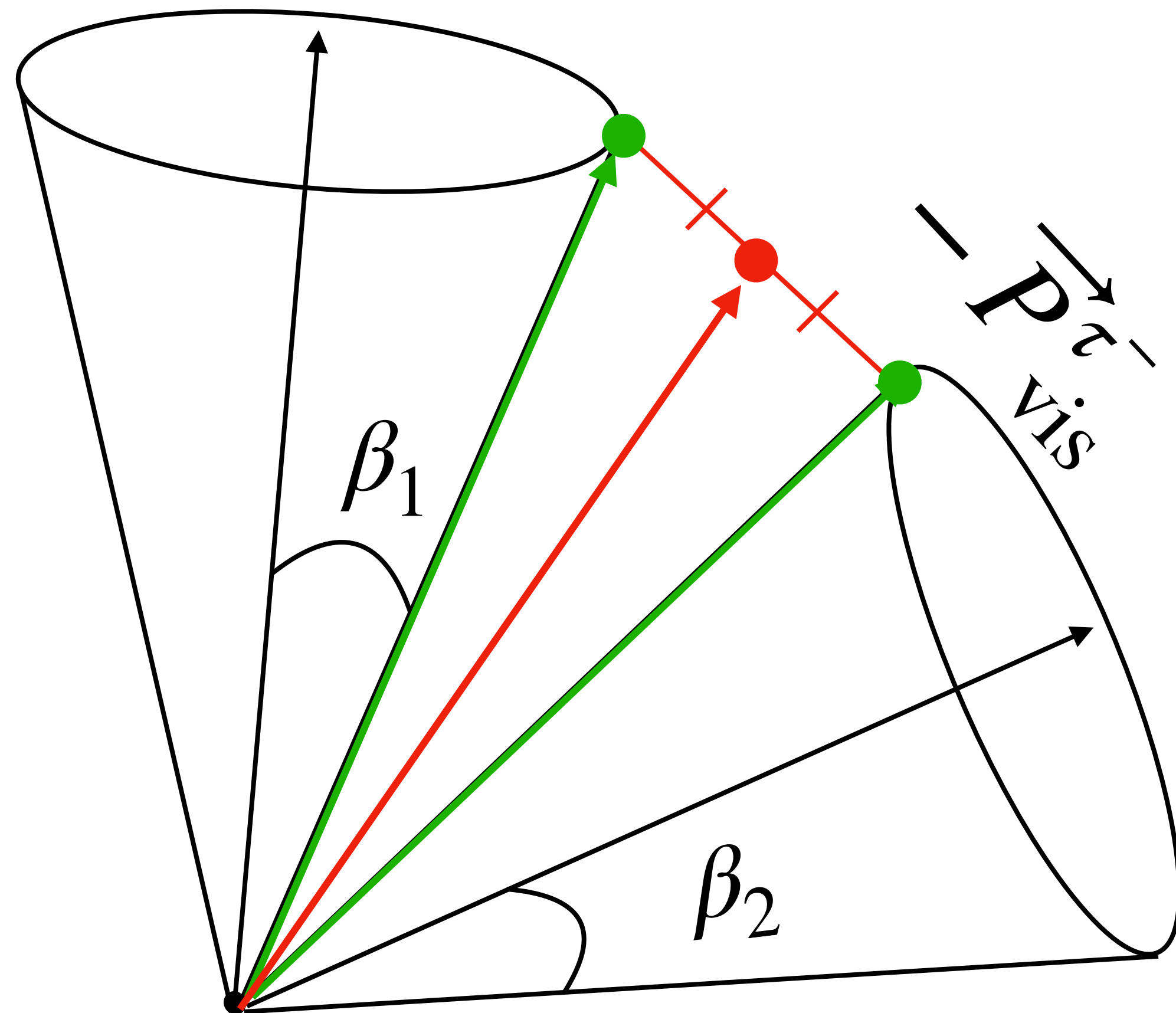


Cone method efficiency is  $\sim 80\%$  for events with  $m_{\tau\tau} \sim 250$  GeV

# Midpoint method

For events for which “Cone Method” cannot find a solution

$$\vec{P}_{vis}^{\tau^+}$$



take a midpoint of the closest approach points of the two cone edges

and use this **new vector** as a solution

We call this “Midpoint method”

# Various levels of “cheating” and methods

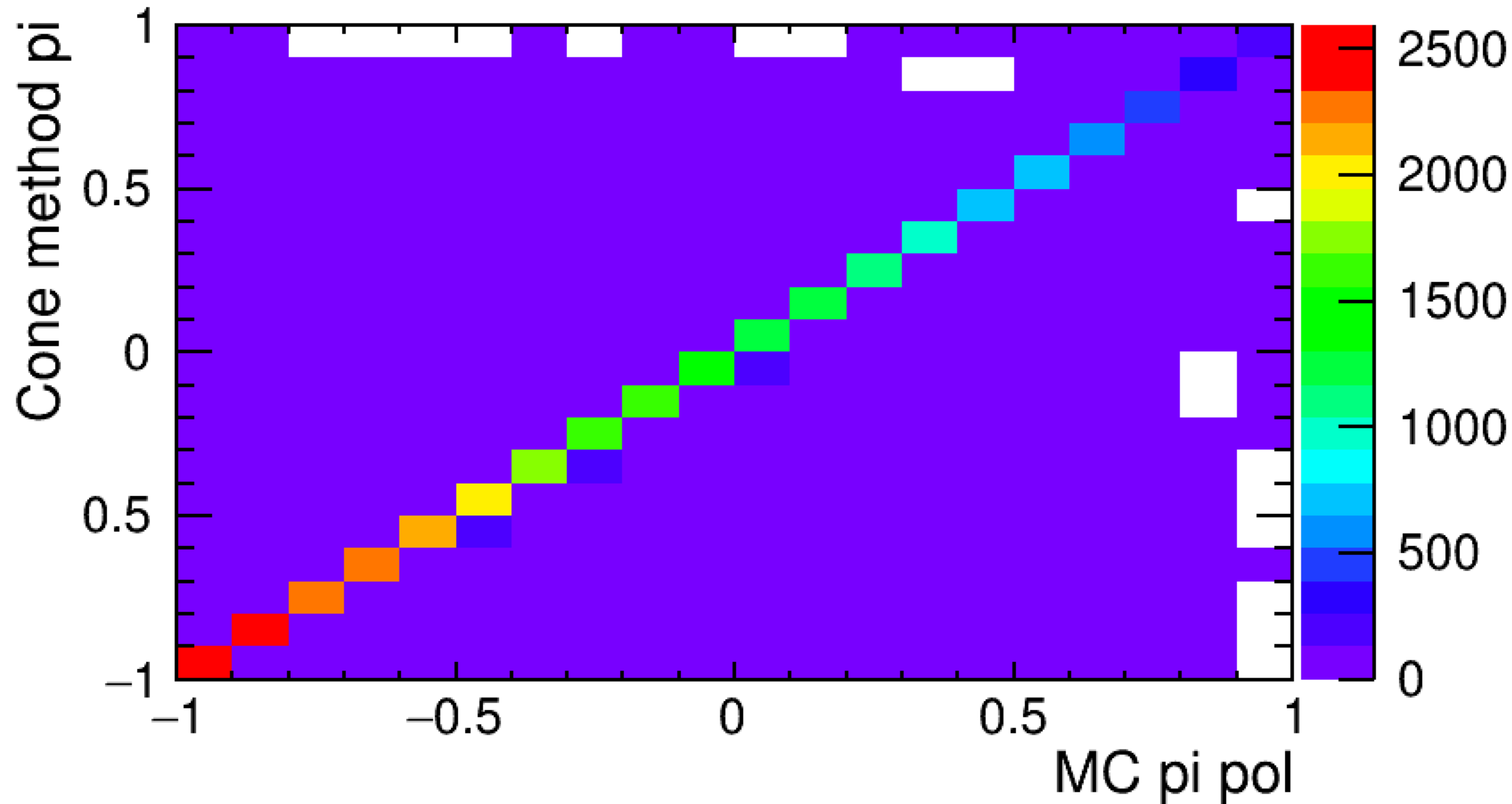
## Two levels of cheating

1. Using true neutrino momentum from MC.
2. Using true MC visible tau daughters.
  - 2.1 “Cone method” to estimate the neutrino momentum.
  - 2.2 If Cone method fails, “Midpoint method”

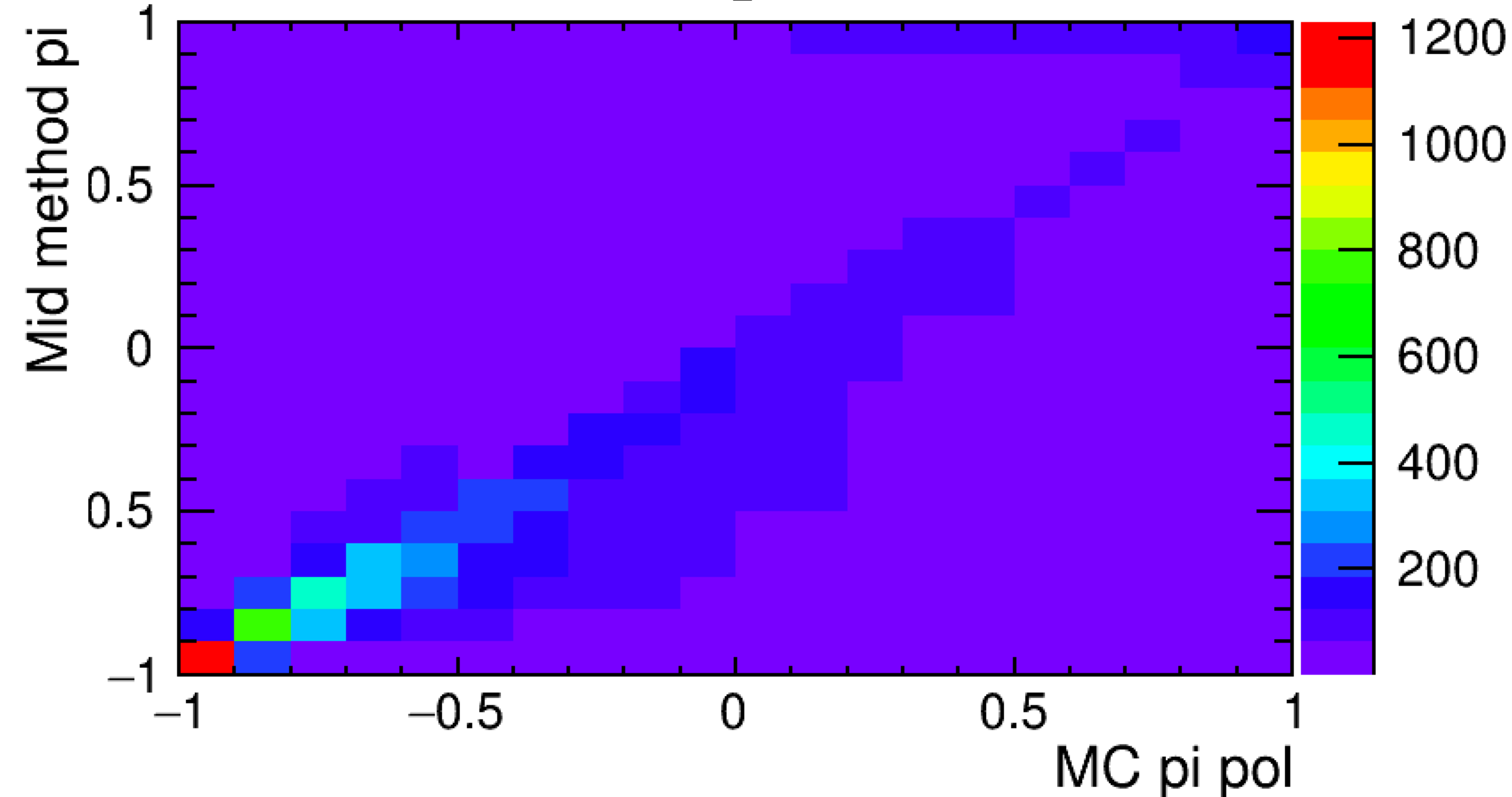
# Polarimeter: single pi decay

Polarimeter vectors of  $\tau \rightarrow \pi\nu$  in  $\tau$  rest frame  $h(\tau^\pm \rightarrow \pi^\pm\nu) \propto p_{\pi^\pm}$

true vs Cone method



true vs Midpoint method



Polarimeter using reconstructed  $\nu$  is in reasonable agreement with MC one.

Cone method works better than Midpoint method.

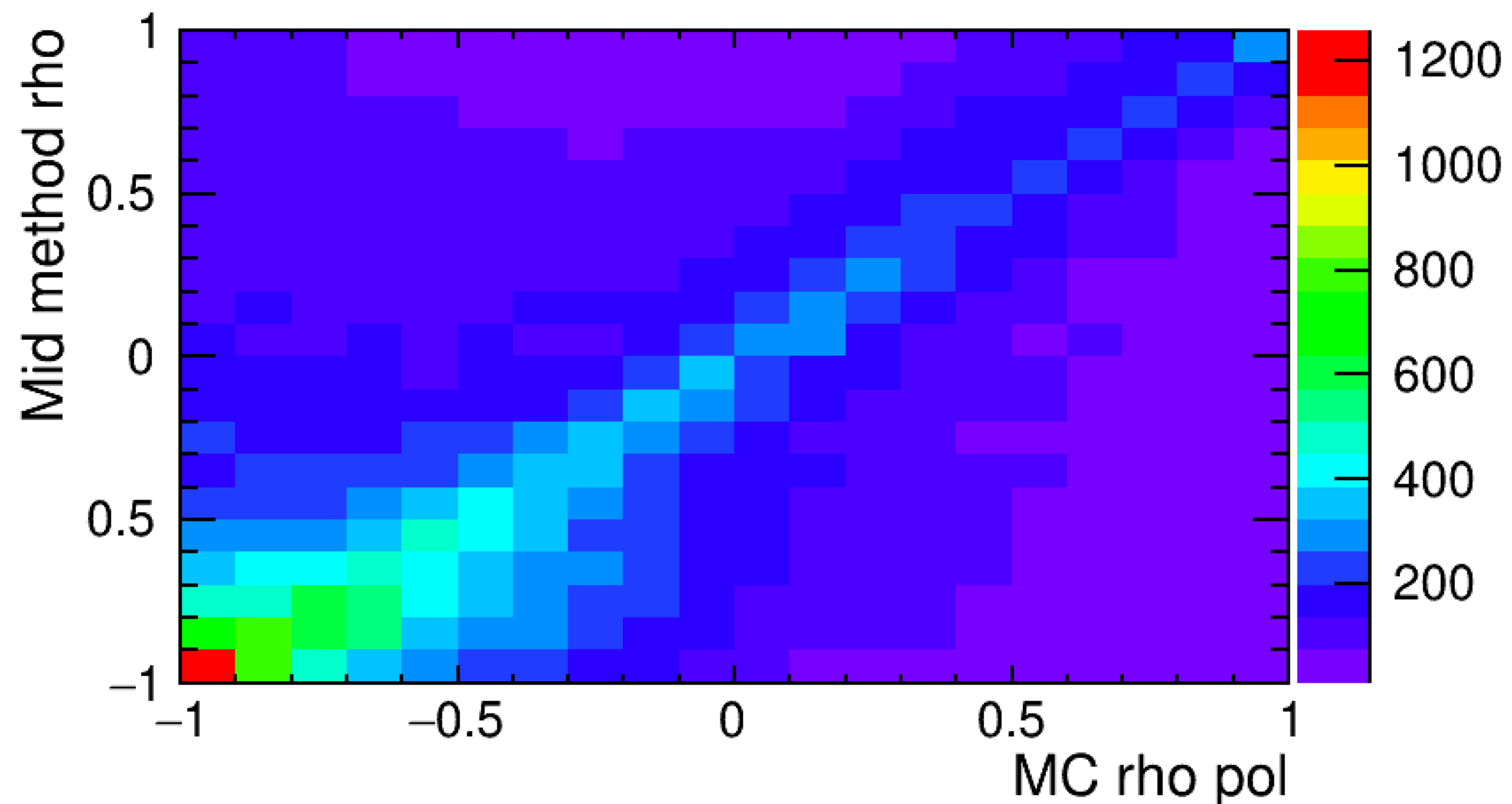
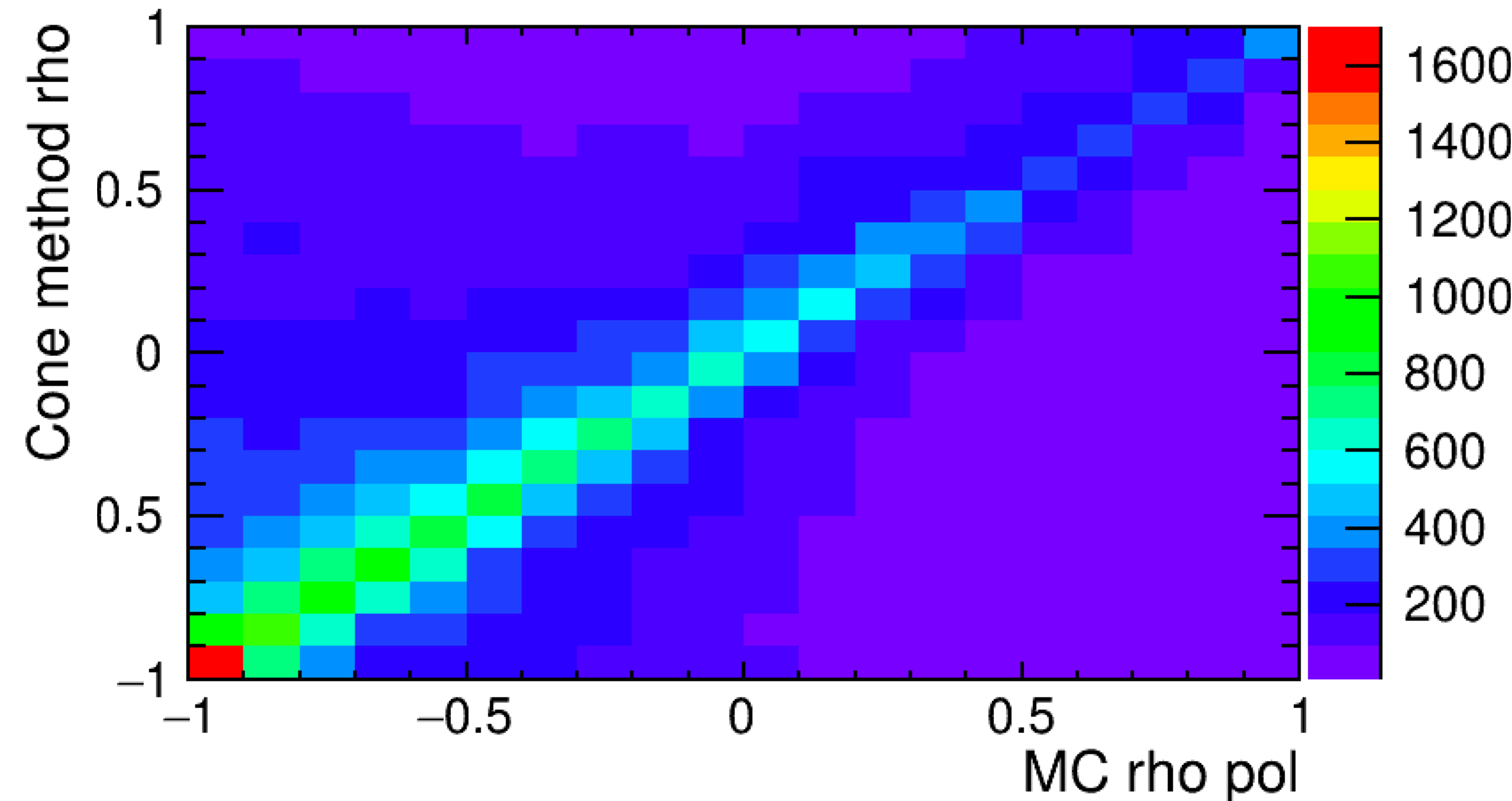
# Polarimeter: rho decay

Polarimeter vectors of  $\tau \rightarrow \rho\nu$  in  $\tau$  rest frame

$$h(\tau^\pm \rightarrow \pi^\pm \pi^0 \nu) \propto m_\tau (E_{\pi^\pm} - E_{\pi^0})(p_{\pi^\pm} - p_{\pi^0}) + \frac{1}{2}(p_{\pi^\pm} + p_{\pi^0})^2 p_\nu$$

true vs Cone method

true vs Midpoint method



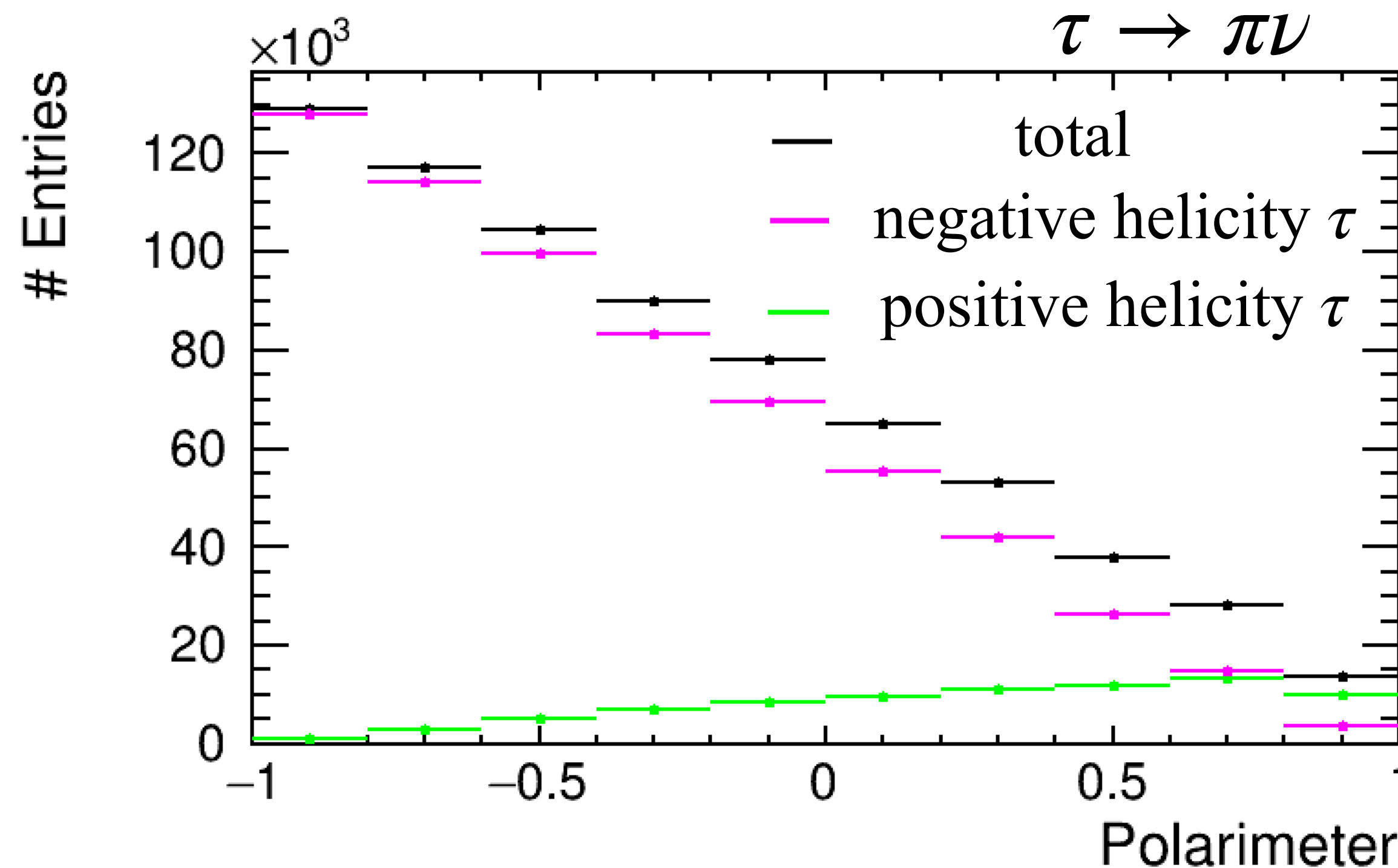
Extracted polarimeter is less precise than  $\tau \rightarrow \pi\nu$

# Tau Polarisation Accuracy

Q. How accurately can tau polarisation be measured?

Reconstructed polarimeter templates for  $\tau \rightarrow \pi\nu$  and  $\tau \rightarrow \rho\nu$  decays.

Scaled to the integrated luminosity of  $1000 \text{ fb}^{-1}$  with 100%  $e_L^- e_R^+$ .



Polarisation

$$P = \frac{N_R - N_L}{N_R + N_L}$$

Use likelihood method to analytically estimate polarisation uncertainty.



# Tau Polarisation Accuracy

Scaled to the luminosity of  $1000 \text{ fb}^{-1}$

Sample with 100 %  $e_L^- e_R^+$  beam polarisations

$N_\tau$ : the expected total number of taus,  $\sigma_P$ : the expected polarisation uncertainty

$\tau \rightarrow \pi\nu$	$N_\tau$	$\sigma_P$
MC	0.58 M	0.27 %
Cone	0.36 M	0.35 %
Mid	0.22 M	0.55 %
Combined	0.58 M	0.30 %

$\tau \rightarrow \rho\nu$	$N_\tau$	$\sigma_P$
MC	1.31 M	0.18 %
Cone	0.70 M	0.28 %
Mid	0.59 M	0.42 %
Combined	1.29 M	0.23 %

Precision on the polarisation  $\sigma_P$  of “Cone method” + “Midpoint method”

$$\tau \rightarrow \pi\nu : \sim 0.30 \% , \quad \tau \rightarrow \rho\nu : \sim 0.23 \%$$

# Summary

- The reconstruction of neutrino momentum at ILC250 was investigated.
- For events with  $m_{\tau\tau} \sim 250$  GeV, “Cone method” efficiency is  $\sim 80\%$ .
  - “Midpoint method” is used if “Cone method” fails.
- Polarimeters were reconstructed in the  $\tau \rightarrow \pi\nu$  and  $\tau \rightarrow \rho\nu$  decay modes, and used to estimate the tau polarisation.
- Reasonable agreement between MC truth polarimeter value and the one from “Cone method” for both  $\tau \rightarrow \pi\nu$  and  $\tau \rightarrow \rho\nu$  decay were found.
- The experimental sensitivity to the tau polarisation of “Cone method” and “Midpoint method” is around 0.18%, assuming  $1000 \text{ fb}^{-1}$  of 100%  $e_L^- e_R^+$  data at 250 GeV.

# Future Plan

- Investigate search for new physics by using the tau polarisation.
- Apply method to radiative return events with a visible photon.
- Add impact parameter information to improve tau and polarisation reconstruction.
- Estimate the tau polarisation precision for a realistic beam polarisation and detector resolution.