

Status Report: Muon $g-2$ anomaly + SUSY at the ILC

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Muon $g-2$ + SUSY: status report

- Produces SUSY MC samples at ILC500 with WHIZARD2.8.5
 - Details in backup
- Run detector simulation: this time DELPHES used
 - PID performance depends on DELPHES PFA
 - Will improve (or be more realistic) when we use ILD full simulation in future
- Analysis just started

| | BLR1 | BLR2 | BLR3 | BLR4 |
|--|-----------|---------|-----------|---------|
| M_1 | 100 | 100 | 150 | 150 |
| $m_L = m_R$ | 150 | 150 | 200 | 200 |
| $\tan \beta$ | 5 | 10 | 5 | 10 |
| μ | 1323 | 678 | 1922 | 973 |
| $m_{\tilde{\mu}_1}$ | 154 | 154 | 202 | 202 |
| $m_{\tilde{\mu}_2}$ | 159 | 159 | 207 | 208 |
| $m_{\tilde{\tau}_1}$ | 113 | 113 | 159 | 158 |
| $m_{\tilde{\tau}_2}$ | 190 | 191 | 242 | 243 |
| $m_{\tilde{\nu}_{\mu,\tau}}$ | 137 | 136 | 190 | 190 |
| $m_{\tilde{\chi}_1^0}$ | 99 | 99 | 150 | 149 |
| $m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_3^0}, m_{\tilde{\chi}_1^\pm}$ | 1323–1324 | 678–680 | 1922–1923 | 973–975 |
| $a_\mu^{\text{SUSY}} \times 10^{10}$ | 27 | 27 | 17 | 17 |
| $\Omega_{\text{DM}} h^2$ | 0.120 | 0.120 | 0.120 | 0.120 |
| $\sigma_p^{\text{SI}} \times 10^{47} [\text{cm}^2]$ | 1.7 | 3.7 | 0.8 | 1.9 |
| $\mu_{\gamma\gamma}$ | 1.01 | 1.01 | 1.01 | 1.01 |

Units in GeV

So far, I am only working with BLR1 parametrization.

Produced events (1)

| Process $e^+e^- \rightarrow$ | Pol (e-, e+) (%) | Xsec (fb) | N = L*Xsec (Assume L = 4 ab ⁻¹) | N = L*Xsec (Assume L = 1.6 ab ⁻¹) | N_generated | process ID |
|-----------------------------------|---------------------|------------------------|--|--|-------------|---------------|
| $\tilde{e}_L^+ \tilde{e}_L^-$ | -80/+30 | 28.7091 +- 0.0012 | 114836 | 45935 | 500K | 1 |
| $\tilde{e}_L^+ \tilde{e}_L^-$ | +80/-30 | 22.30497 +- 0.00071 | 89220 | 35688 | 500K | 2 |
| $\tilde{e}_R^+ \tilde{e}_R^-$ | -80/+30 | 53.5626 +- 0.0019 | 214250 | 85700 | 1M | 3 |
| $\tilde{e}_R^+ \tilde{e}_R^-$ | +80/-30 | 54.6909 +- 0.022 | 218764 | 87505 | 1M | 4 |
| $\tilde{\mu}_L^+ \tilde{\mu}_L^-$ | -80/+30 | 99.1388 +- 0.0079 | 396555 | 158622 | 1.5M | 5 |
| $\tilde{\mu}_L^+ \tilde{\mu}_L^-$ | +80/-30 | 25.9426 +- 0.0021 | 103770 | 41508 | 500K | 6 |
| $\tilde{\mu}_R^+ \tilde{\mu}_R^-$ | -80/+30 | 26.9622 +- 0.0021 | 107849 | 43140 | 500K | 7 |
| $\tilde{\mu}_R^+ \tilde{\mu}_R^-$ | +80/-30 | 92.4999 +- 0.0072 | 370000 | 148000 | 1.5M | 8 |

1.6 ab⁻¹ is the integrated luminosity of ILC500 with -80/+30 and +80/-30

Produced events (2)

| Process $e^+e^- \rightarrow$ | Pol (e-, e+) (%) | Xsec (fb) | N = L*Xsec (Assume L = 4 ab ⁻¹) | N = L*Xsec (Assume L = 1.6 ab ⁻¹) | N_generated | process ID |
|-------------------------------------|---------------------|-----------------------|--|--|-------------|---------------|
| $\tilde{\tau}_1^+ \tilde{\tau}_1^-$ | -80/+30 | 92.9890 +- 0.0063 | 371956 | 148782 | 1.5M | 9 |
| $\tilde{\tau}_1^+ \tilde{\tau}_1^-$ | +80/-30 | 86.6444 +- 0.0059 | 346578 | 138631 | 1.5M | 10 |
| $\tilde{\tau}_2^+ \tilde{\tau}_2^-$ | -80/+30 | 29.0410 +- 0.0033 | 116164 | 46466 | 500K | 11 |
| $\tilde{\tau}_2^+ \tilde{\tau}_2^-$ | +80/-30 | 26.3214 +- 0.0029 | 105286 | 42114 | 500K | 12 |
| $\tilde{\tau}_1^+ \tilde{\tau}_2^-$ | -80/+30 | 8.18989 +- 0.00062 | 32760 | 13104 | 200K | 13 |
| $\tilde{\tau}_1^+ \tilde{\tau}_2^-$ | +80/-30 | 6.48573 +- 0.00050 | 25943 | 10377 | 200K | 14 |
| $\tilde{\tau}_2^+ \tilde{\tau}_1^-$ | -80/+30 | 8.19128 +- 0.00062 | 32765 | 13106 | 200K | 15 |
| $\tilde{\tau}_2^+ \tilde{\tau}_1^-$ | +80/-30 | 6.48553 +- 0.00050 | 25942 | 10377 | 200K | 16 |

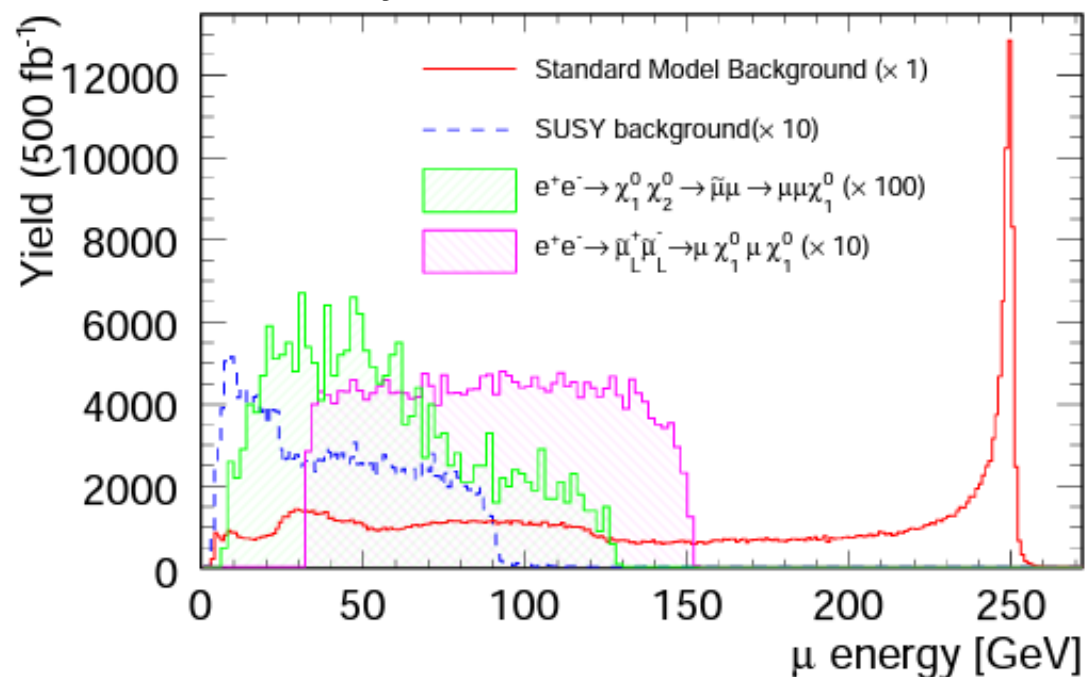
1.6 ab⁻¹ is the integrated luminosity of ILC500 with -80/+30 and +80/-30

Potential problem

- The spin information is not stored in stau events
 - This might affect to the decay products of tau
 - It is OK for SM world (e.g.: Keita's study)

Energy plot

- Since selectron/smuon decay is two-body decay, the energy distribution of visible decay products have “edges”.
- Stau is technically two-body decay as well, but the produced tau also decays and makes everything complicated.



“edges” at ~30 GeV and ~150 GeV
in smuon events (magenta)

Two-body decay kinematics (1)

- In the end, we have

- $$E^+ = \frac{\sqrt{s}}{4} \left[1 - \left(\frac{m_\chi}{m_{\text{SUSY}}} \right)^2 \right] \left[1 + \sqrt{1 - 4 \left(\frac{m_{\text{SUSY}}}{\sqrt{s}} \right)^2} \right]$$

- $$E^- = \frac{\sqrt{s}}{4} \left[1 - \left(\frac{m_\chi}{m_{\text{SUSY}}} \right)^2 \right] \left[1 - \sqrt{1 - 4 \left(\frac{m_{\text{SUSY}}}{\sqrt{s}} \right)^2} \right]$$

- where E^+/E^- is the maximum/minimum energy of lepton (electron/positron/muon/tau), m_{SUSY} is the mass of SUSY particle (selectron/smuon/stau), $\sqrt{s} = 500$ GeV in this analysis, and m_χ is the neutralino mass and equals to 99 GeV on BLR1 parametrization
- Ignored lepton masses

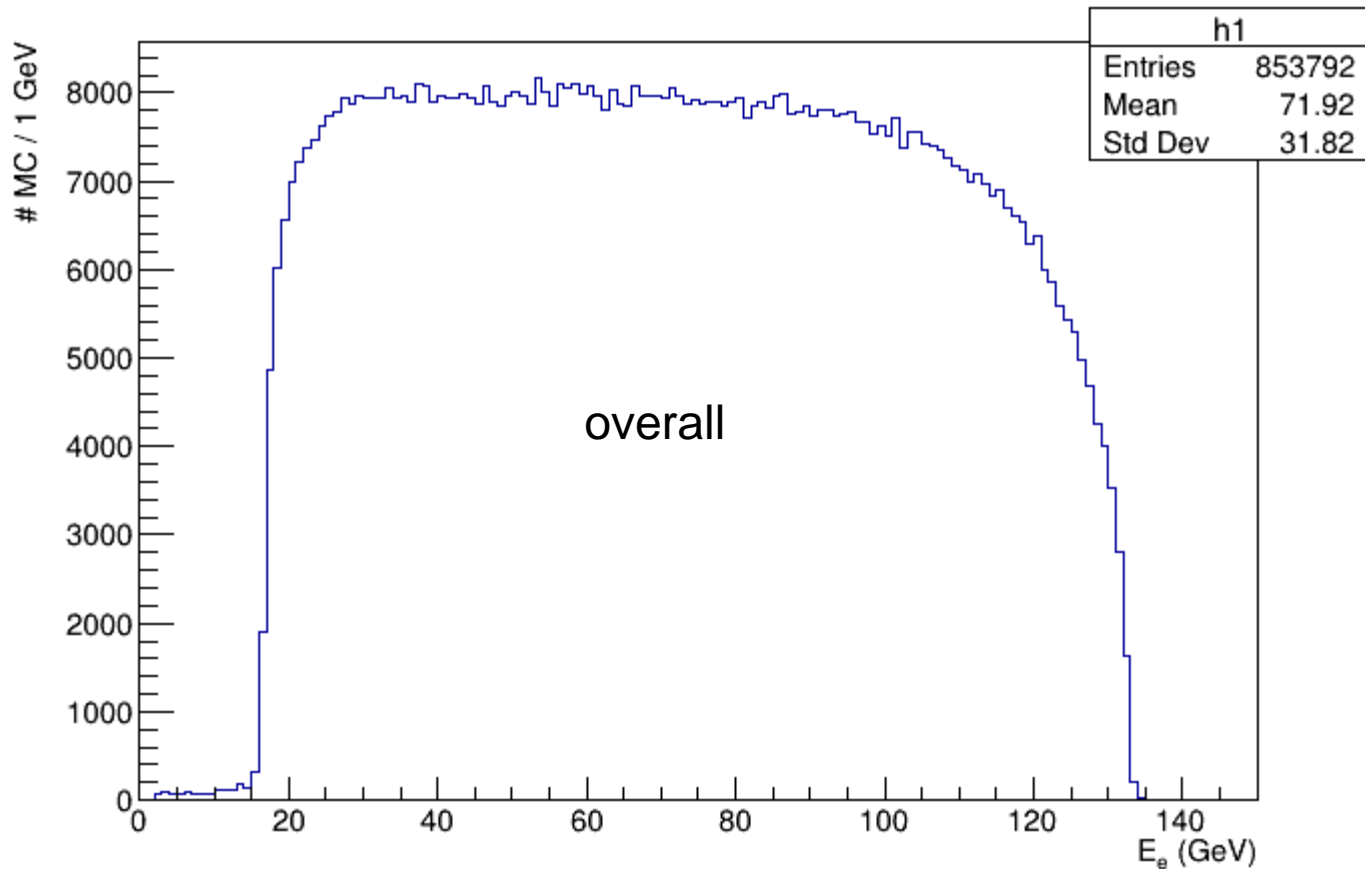
Two-body decay kinematics (2)

$\sqrt{s} = 500$ GeV, $\widetilde{\chi}_1^0 = 99$ GeV, ignored lepton masses

| SUSY particle | mass (GeV) | E^+ (GeV) | E^- (GeV) |
|----------------------|------------|-------------|-------------|
| \widetilde{e}_L | 157 | 133.9 | 16.7 |
| \widetilde{e}_R | 156 | 133.0 | 16.3 |
| $\widetilde{\mu}_L$ | 158 | 134.8 | 17.1 |
| $\widetilde{\mu}_R$ | 154 | 131.1 | 15.6 |
| $\widetilde{\tau}_1$ | 113 | 55.0 | 3.1 |
| $\widetilde{\tau}_2$ | 190 | 150.2 | 31.9 |

Selectron (\tilde{e}_L) events

pfo_electron_e {pfo_electron_e!=0&&n_electron>=1}



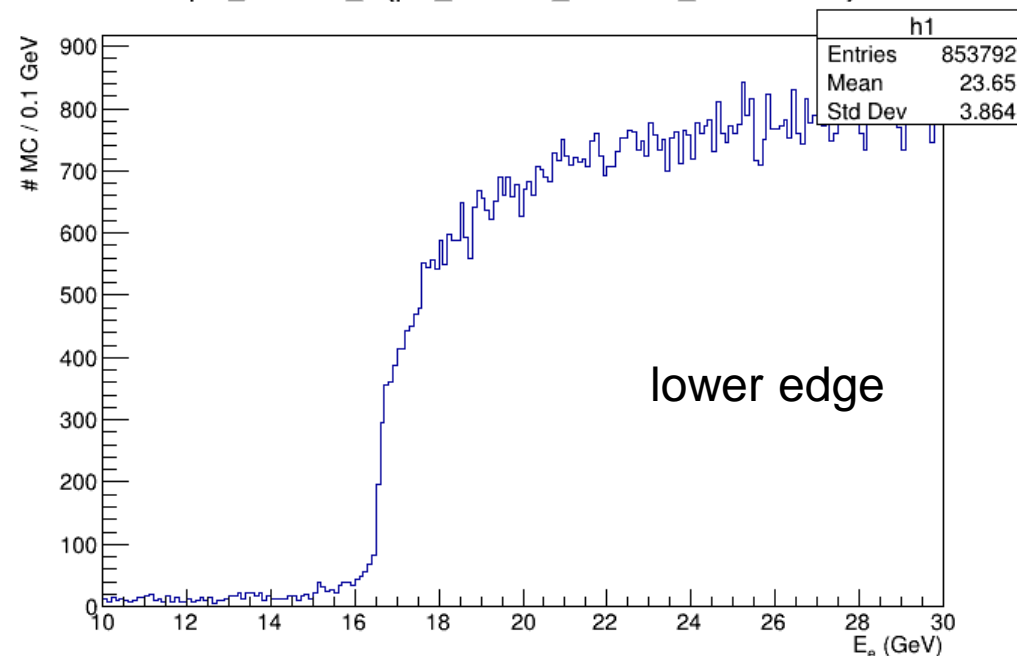
overall

se11_eLpR (mass = 157 GeV)

e >= 1, plotted energy of electron PFOs

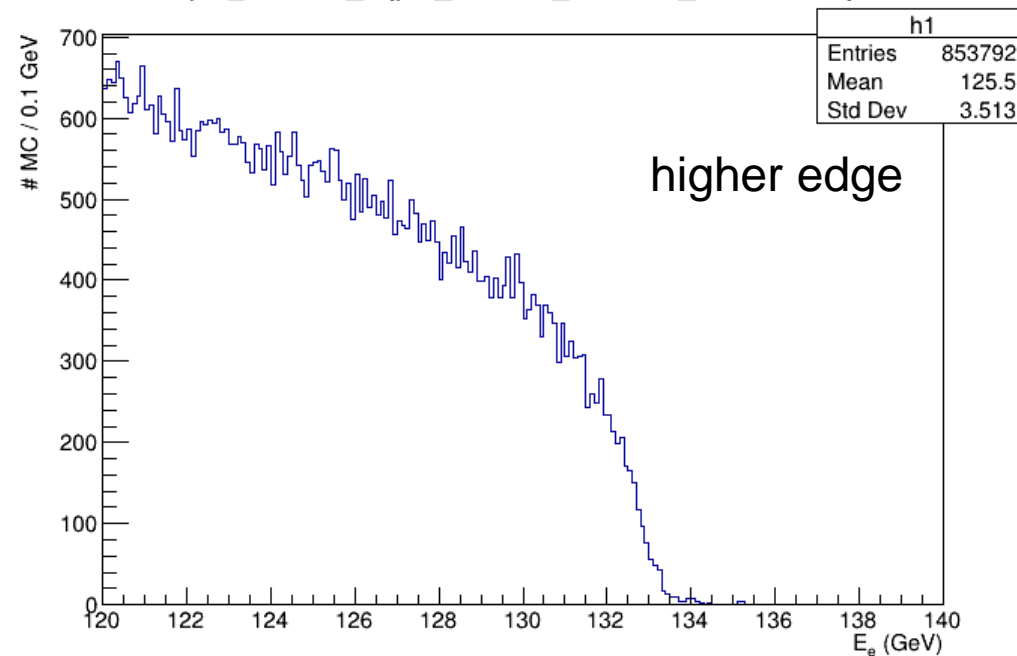
$E^+ = 133.9$ GeV and $E^- = 16.7$ GeV

pfo_electron_e {pfo_electron_e!=0&&n_electron>=1}



lower edge

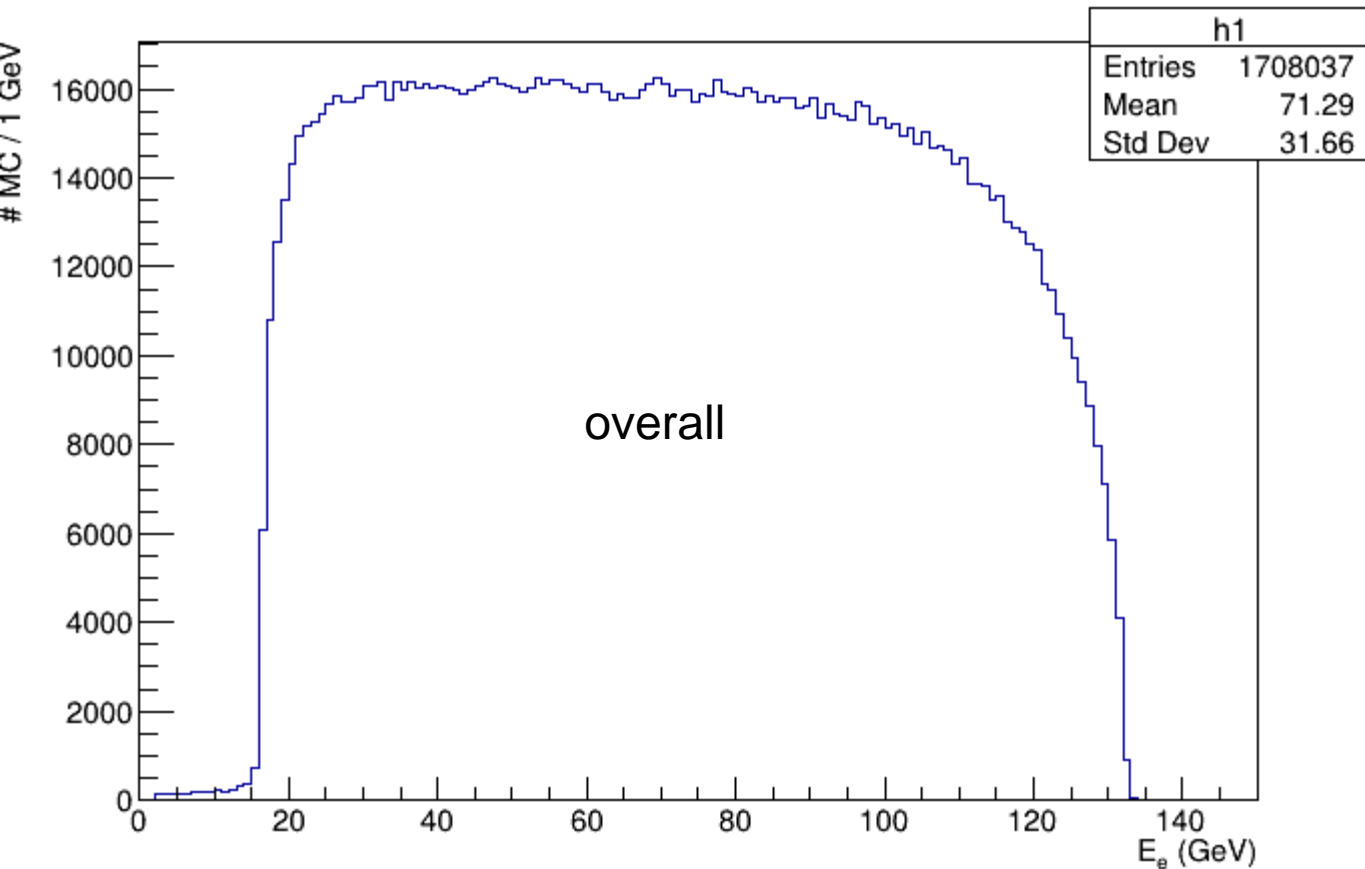
pfo_electron_e {pfo_electron_e!=0&&n_electron>=1}



higher edge

Selectron (\widetilde{e}_R) events

pfo_electron_e {pfo_electron_e!=0&&n_electron>=1}

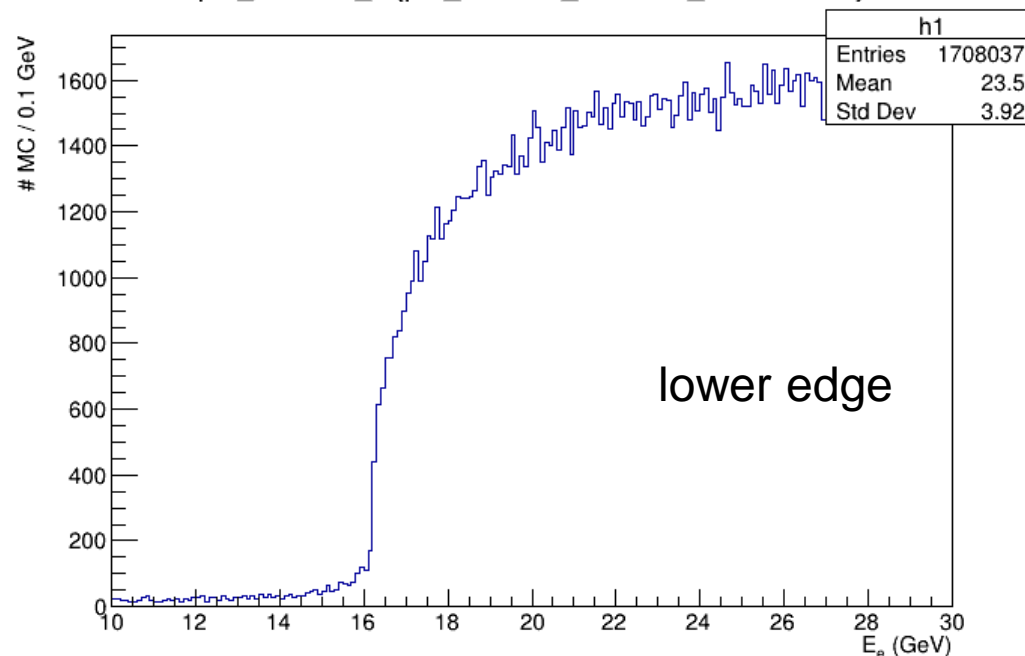


se22_eLpR (mass = 156 GeV)

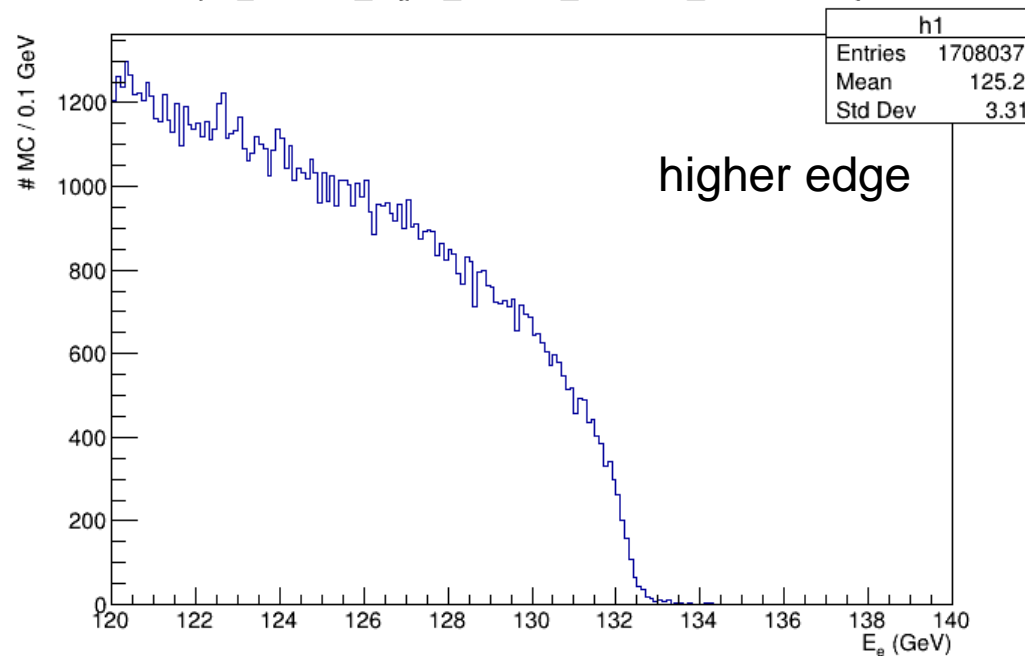
e \geq 1, plotted energy of electron PFOs

E^+ = 133.0 GeV and E^- = 16.3 GeV

pfo_electron_e {pfo_electron_e!=0&&n_electron>=1}

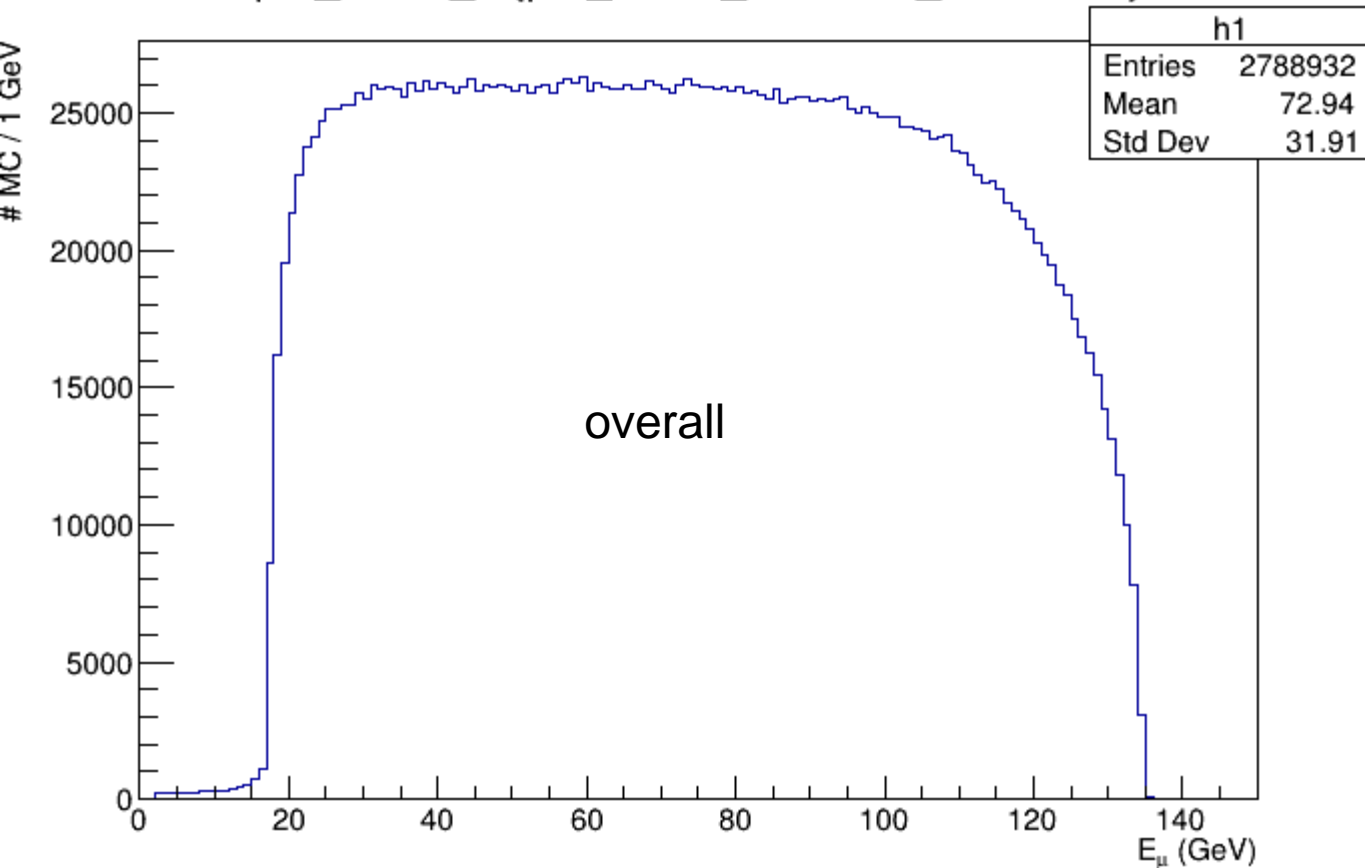


pfo_electron_e {pfo_electron_e!=0&&n_electron>=1}



Smuon ($\widetilde{\mu}_L$) events

pfo_muon_e {pfo_muon_e!=0&&n_muon>=1}

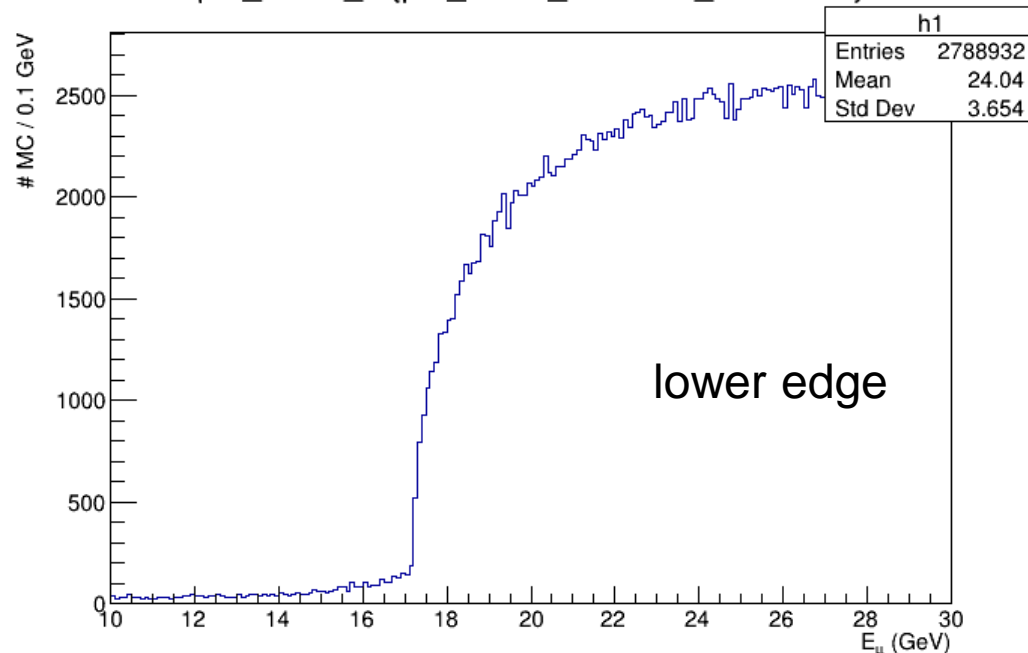


smu11_eLpR (mass = 158 GeV)

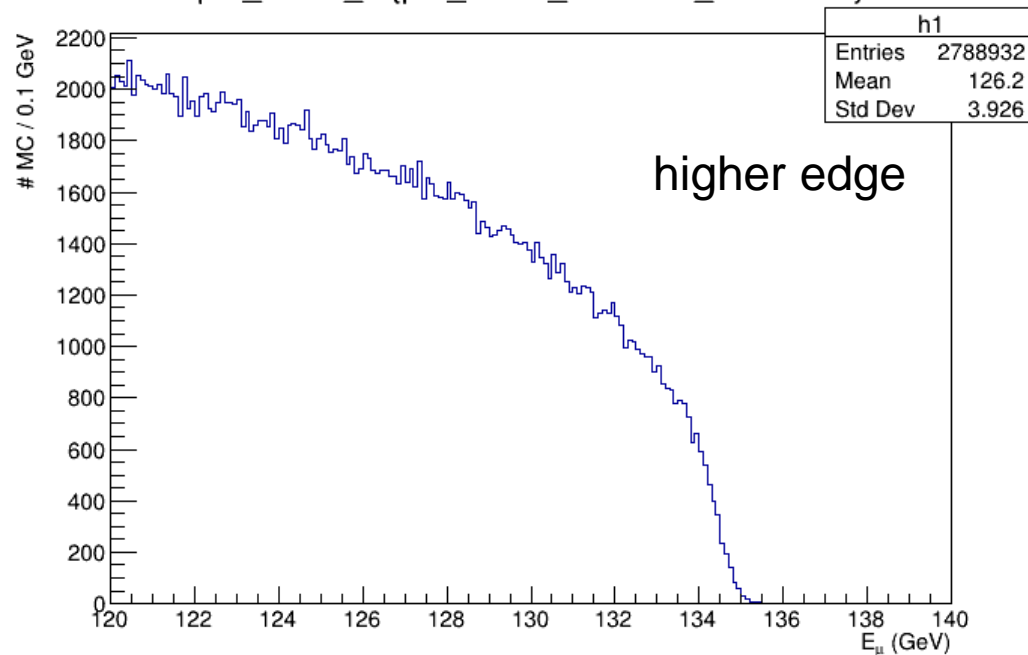
mu \geq 1, plotted energy of muon PFOs

E^+ = 134.8 GeV and E^- = 17.1 GeV

pfo_muon_e {pfo_muon_e!=0&&n_muon>=1}

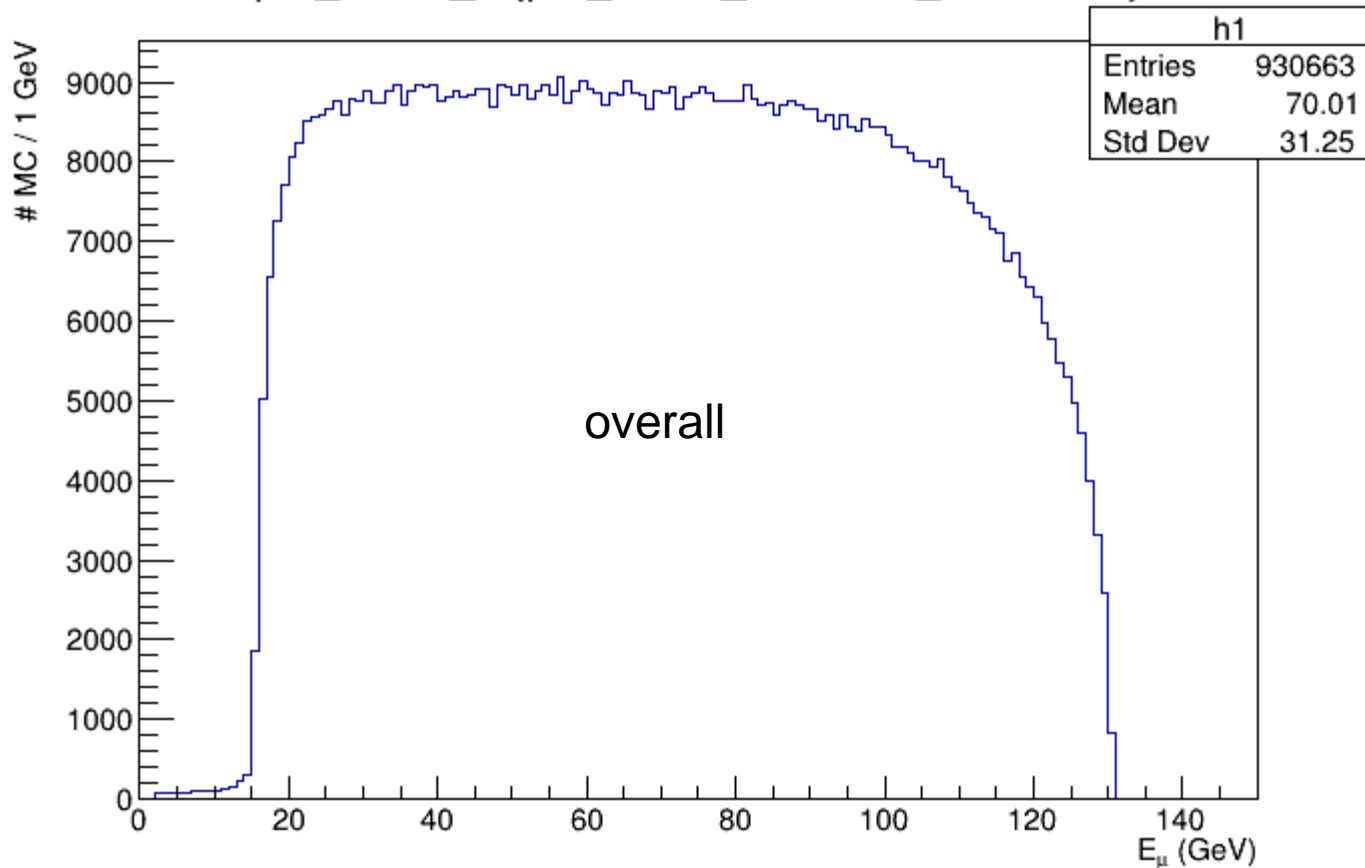


pfo_muon_e {pfo_muon_e!=0&&n_muon>=1}



Smuon ($\widetilde{\mu}_R$) events

pfo_muon_e {pfo_muon_e!=0&&n_muon>=1}

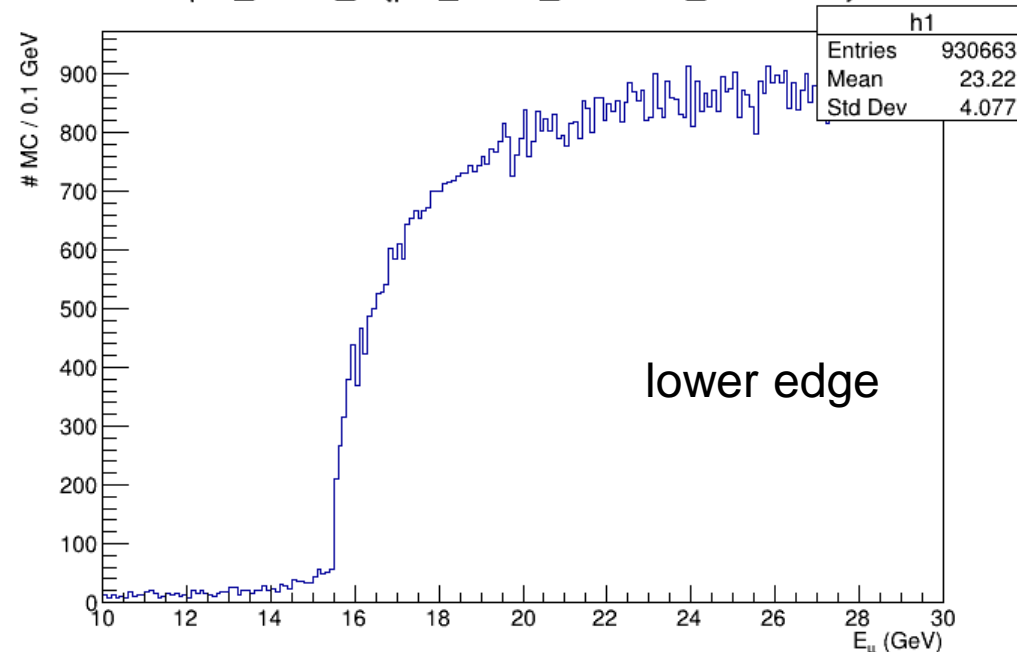


smu22_eLpR (mass = 154 GeV)

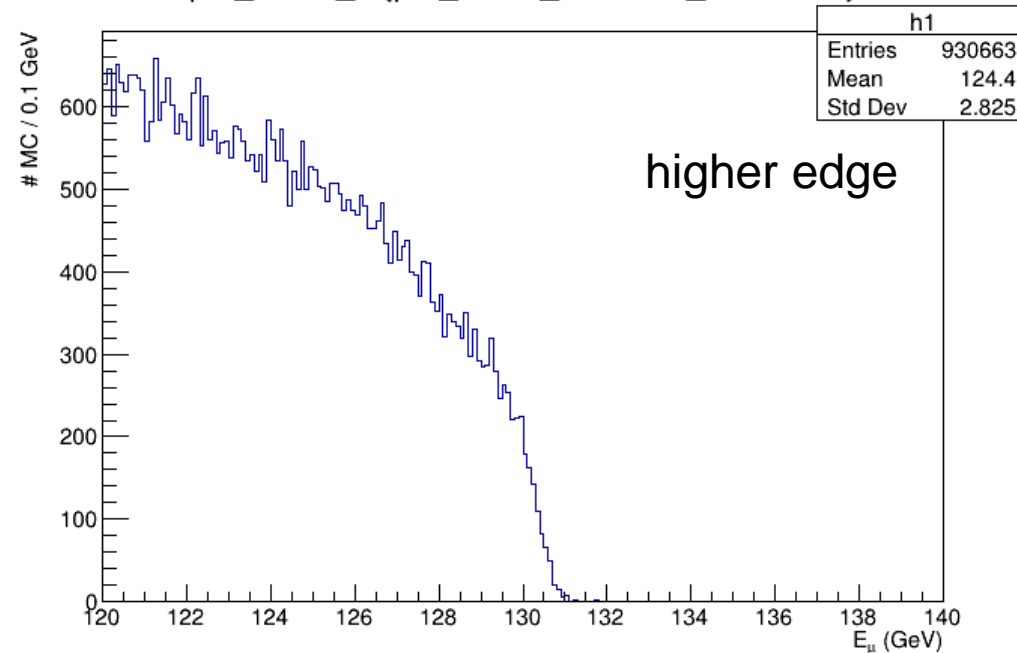
mu \geq 1, plotted energy of muon PFOs

$E^+ = 131.1$ GeV and $E^- = 15.6$ GeV

pfo_muon_e {pfo_muon_e!=0&&n_muon>=1}



pfo_muon_e {pfo_muon_e!=0&&n_muon>=1}



Energy distribution

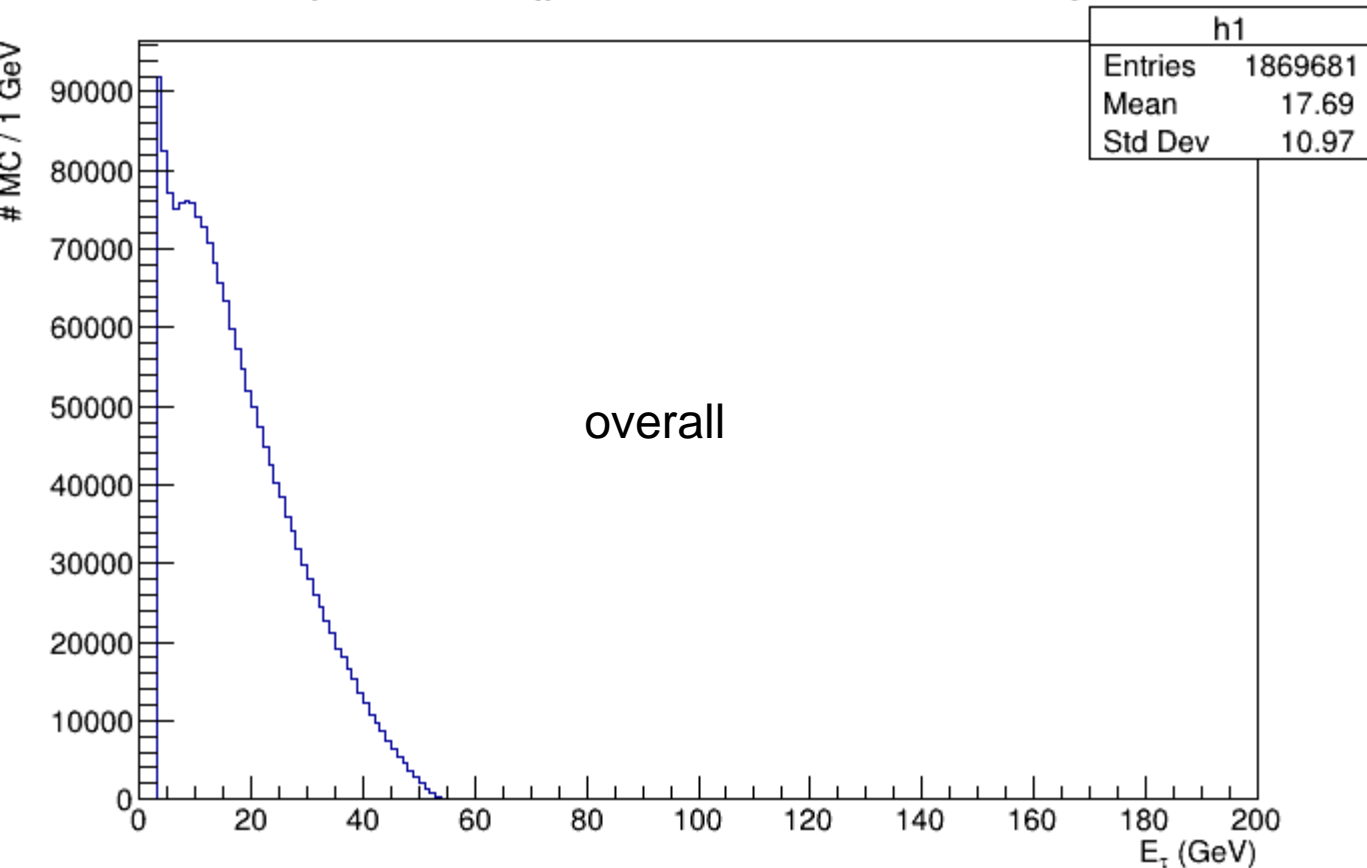
- Selectron/Smuon events have edges in both side as expected. This distribution can be used to extract the mass of neutralino/selectron/smuon.
- However, stau event is not easy: tau decays to something and make everything complicated.

Stau event reconstruction

- Used TaJetClustering with default values
 - Choose energetic charged PFO as a seed and combine neutral PFO near to the seed to reconstruct a tau candidate
 - Apply some selection cuts

Stau ($\tilde{\tau}_1$) events

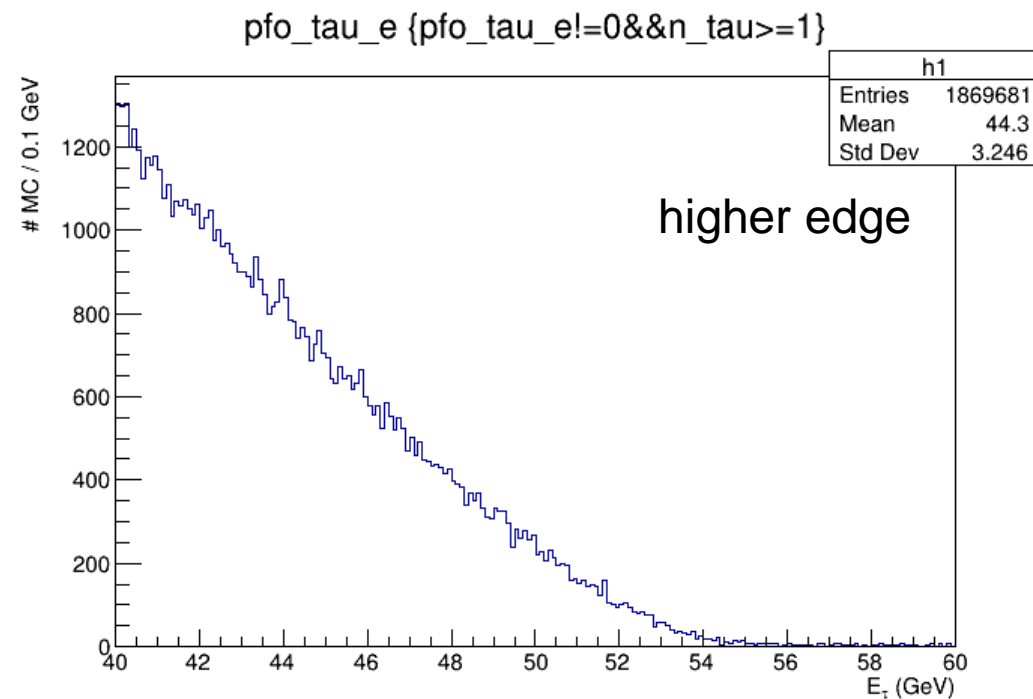
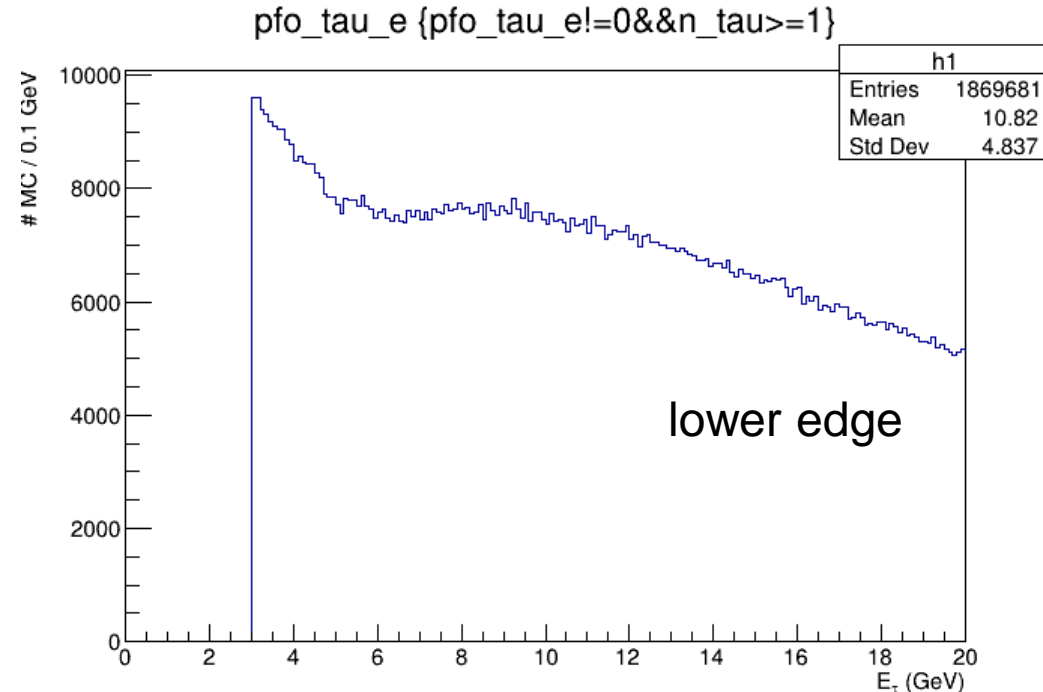
pfo_tau_e {pfo_tau_e!=0&&n_tau>=1}



stau11_eLpR (mass = 113 GeV)

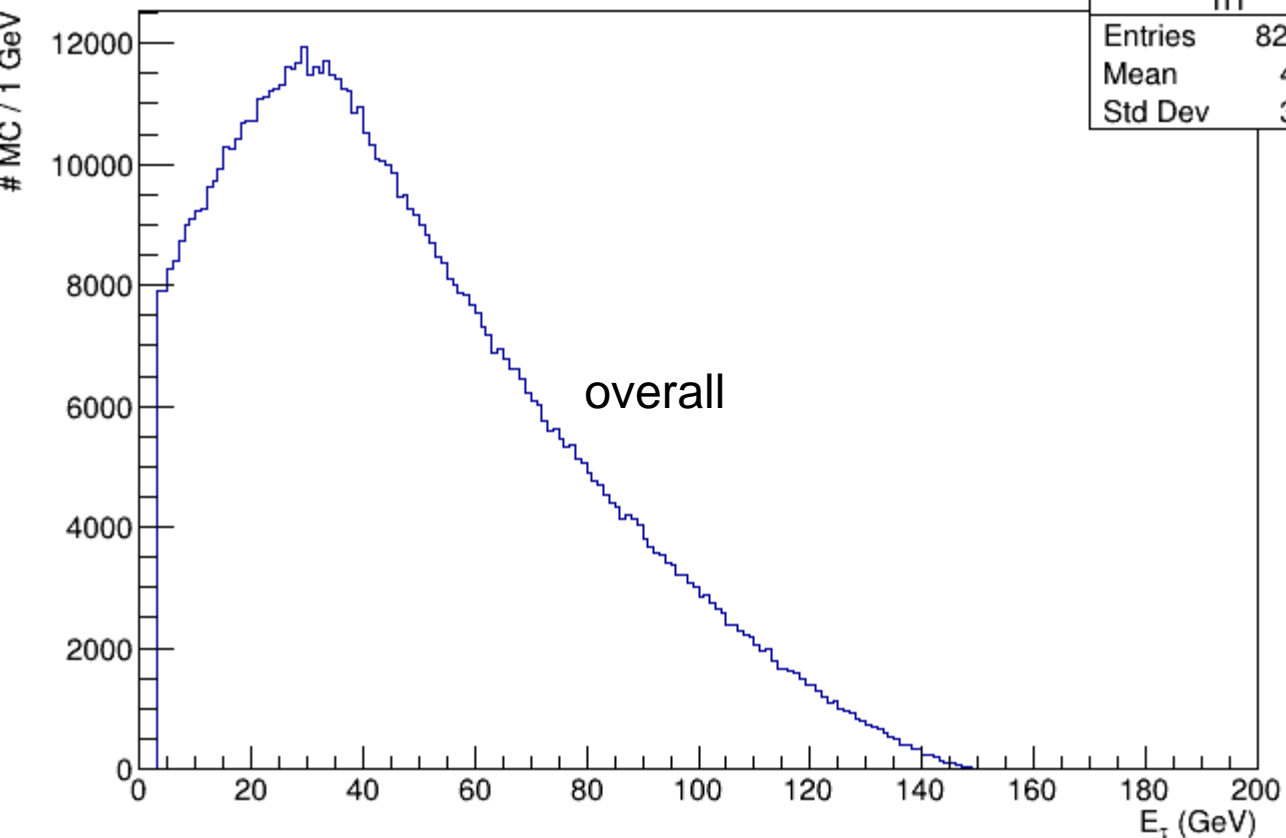
tau \geq 1, plotted energy of reconstructed taus

$E^+ = 55.0$ GeV and $E^- = 3.1$ GeV



Stau ($\tilde{\tau}_2$) events

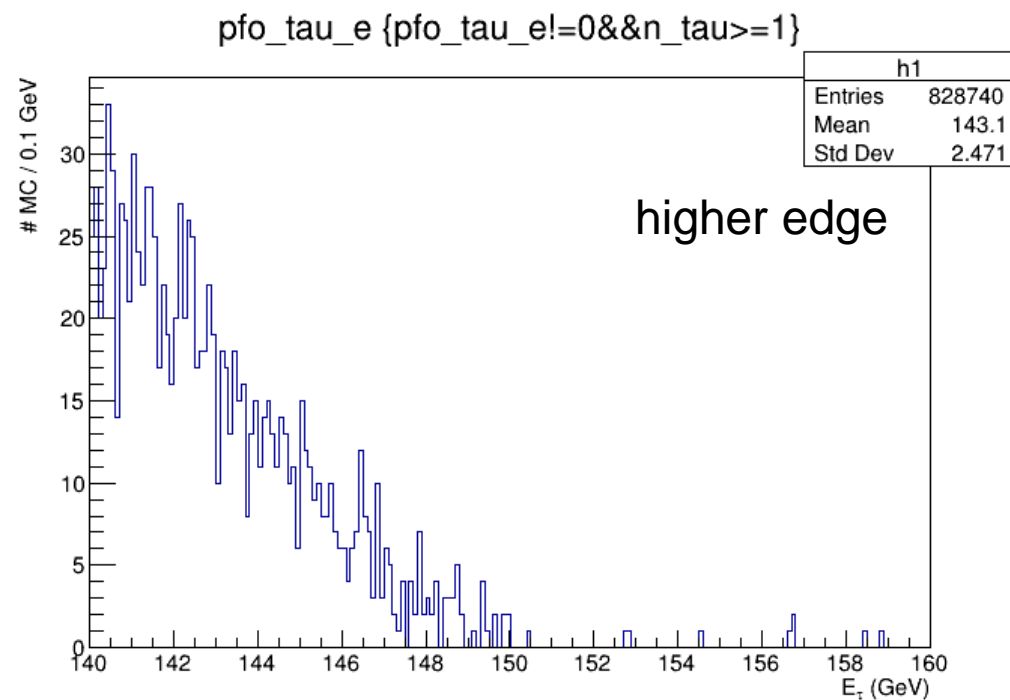
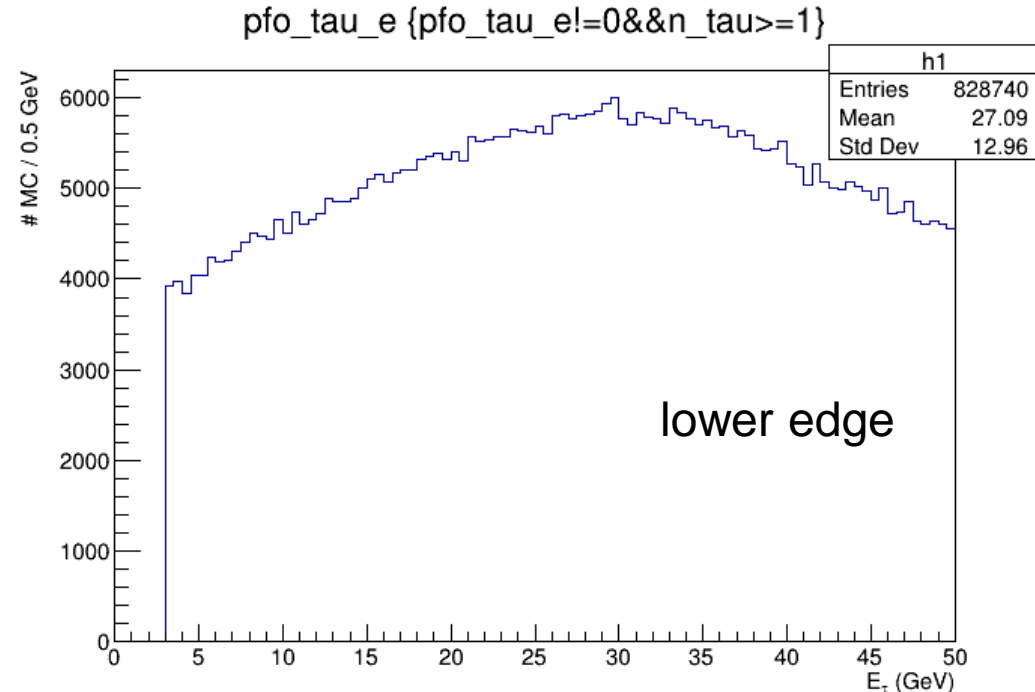
pfo_tau_e {pfo_tau_e!=0&&n_tau>=1}



stau22_eLpR (mass = 190 GeV)

tau >= 1, plotted energy of reconstructed taus

$E^+ = 150.2$ GeV and $E^- = 31.9$ GeV



Mass extraction (future work with bkg)

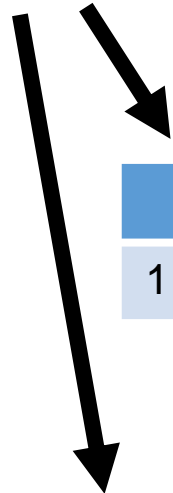
- It is possible to extract the masses of selectron/smuon/neutralino once we measure E^+ and E^- from the experiment
- In the end, we have
 - $m_{\text{SUSY}}^2 = (\sqrt{s})^2 \frac{E^+ E^-}{(E^+ + E^-)^2}$
 - $m_\chi^2 = m_{\text{SUSY}}^2 \left[1 - \frac{2(E^+ + E^-)}{\sqrt{s}} \right]$

With SM bkg: Analysis for selectron/smuon

- Made everything luminosity-weighted (and MC-weighted)
 - eLpR/eRpL for (e-, e+) = (-80%, +30%)/(+80%, -30%)
 - 1.6 ab⁻¹ for both polarization
- Added available IDR samples
 - /gpfs/group/ilc/soft/samples/mc-opt-3/ild/dst-merged/500-TDR_ws/PROCESS/ILD_I5_o1_v02/v02-00-01/~.slcio
 - processes
 - 2f: bhabha, leptonic
 - 4f: XXX_leptonic (XXX = singleW, singleZee, singleZnunu, singleZsingleWMix, WW, ZZ ZZWWMix)

Statistics (so far only eLpR)

| | $\widetilde{e}_L\widetilde{e}_L$ | $\widetilde{e}_R\widetilde{e}_R$ | $\widetilde{\mu}_L\widetilde{\mu}_L$ | $\widetilde{\mu}_R\widetilde{\mu}_R$ | $\widetilde{\tau}_1^+\widetilde{\tau}_1^-$ | $\widetilde{\tau}_2^+\widetilde{\tau}_2^-$ | $\widetilde{\tau}_1^+\widetilde{\tau}_2^-$ | $\widetilde{\tau}_2^+\widetilde{\tau}_1^-$ | all SM bkg |
|---------|----------------------------------|----------------------------------|--------------------------------------|--------------------------------------|--|--|--|--|-------------------|
| No cuts | $4.59 \cdot 10^4$ | $8.57 \cdot 10^4$ | $1.59 \cdot 10^5$ | $4.31 \cdot 10^4$ | $1.49 \cdot 10^5$ | $4.65 \cdot 10^4$ | $1.31 \cdot 10^4$ | $1.31 \cdot 10^4$ | $2.23 \cdot 10^7$ |

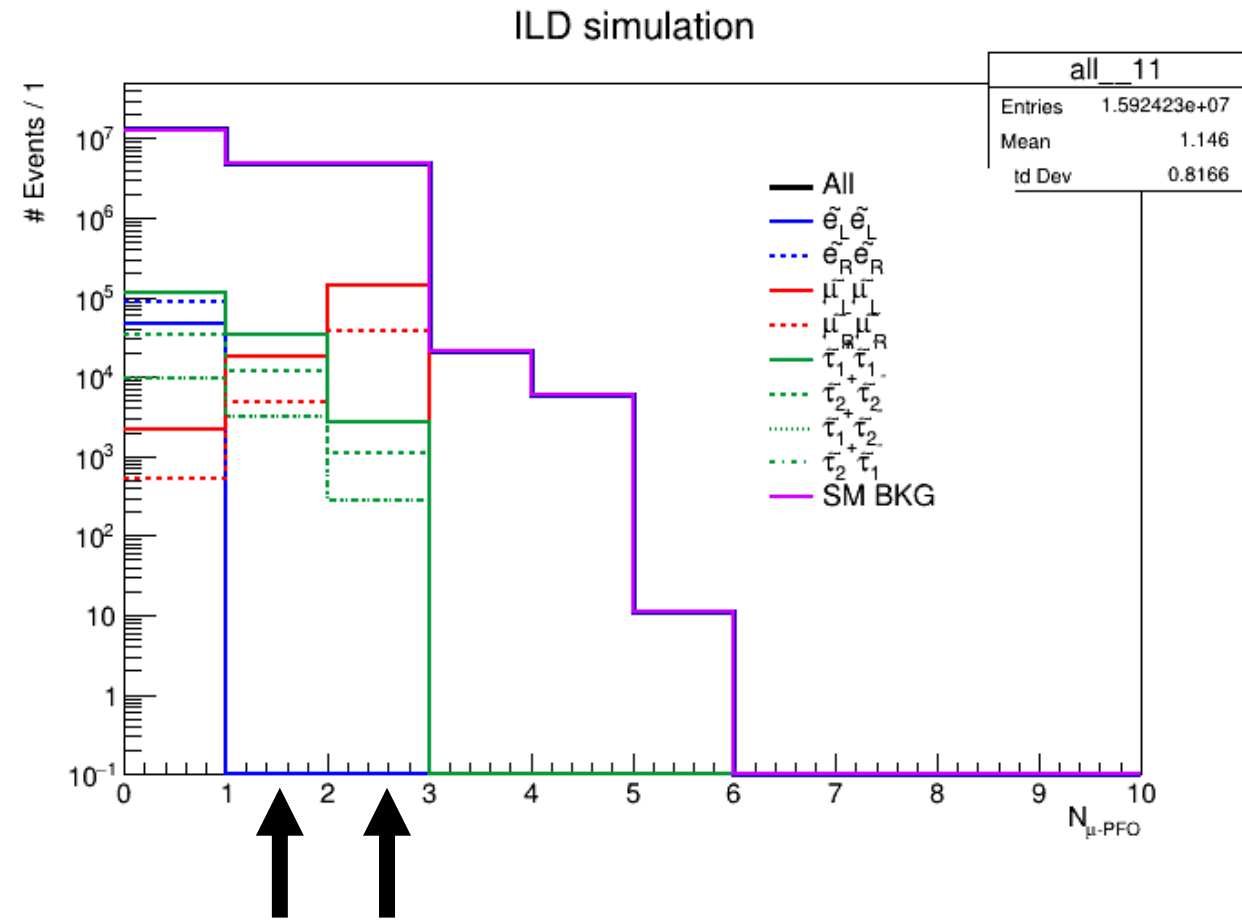
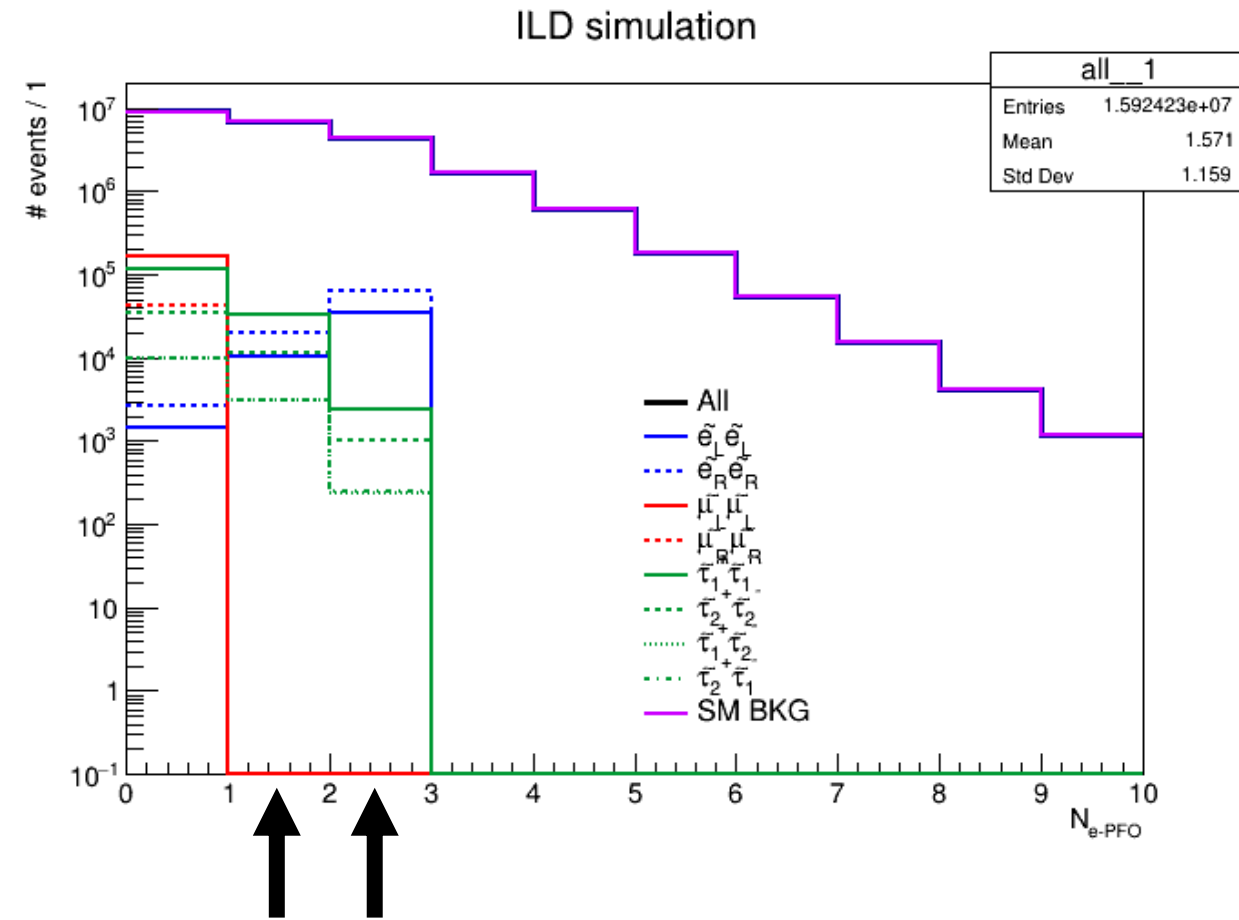


| | $\widetilde{e}_L\widetilde{e}_L$ | $\widetilde{e}_R\widetilde{e}_R$ | $\widetilde{\mu}_L\widetilde{\mu}_L$ | $\widetilde{\mu}_R\widetilde{\mu}_R$ | $\widetilde{\tau}_1^+\widetilde{\tau}_1^-$ | $\widetilde{\tau}_2^+\widetilde{\tau}_2^-$ | $\widetilde{\tau}_1^+\widetilde{\tau}_2^-$ | $\widetilde{\tau}_2^+\widetilde{\tau}_1^-$ | all SM bkg |
|----------------------------------|----------------------------------|----------------------------------|--------------------------------------|--------------------------------------|--|--|--|--|-------------------|
| $1 \leq N_{e\text{-PFO}} \leq 2$ | $4.45 \cdot 10^4$ | $8.30 \cdot 10^4$ | 0 | 0 | $3.52 \cdot 10^4$ | $1.24 \cdot 10^4$ | $3.31 \cdot 10^3$ | $3.30 \cdot 10^3$ | $1.11 \cdot 10^7$ |

| | $\widetilde{e}_L\widetilde{e}_L$ | $\widetilde{e}_R\widetilde{e}_R$ | $\widetilde{\mu}_L\widetilde{\mu}_L$ | $\widetilde{\mu}_R\widetilde{\mu}_R$ | $\widetilde{\tau}_1^+\widetilde{\tau}_1^-$ | $\widetilde{\tau}_2^+\widetilde{\tau}_2^-$ | $\widetilde{\tau}_1^+\widetilde{\tau}_2^-$ | $\widetilde{\tau}_2^+\widetilde{\tau}_1^-$ | all SM bkg |
|------------------------------------|----------------------------------|----------------------------------|--------------------------------------|--------------------------------------|--|--|--|--|-------------------|
| $1 \leq N_{\mu\text{-PFO}} \leq 2$ | 0 | 0 | $1.56 \cdot 10^5$ | $4.26 \cdot 10^4$ | $3.74 \cdot 10^4$ | $1.32 \cdot 10^4$ | $3.51 \cdot 10^3$ | $3.49 \cdot 10^3$ | $9.65 \cdot 10^6$ |

⊗ I couldn't control legend box by hand. Why???

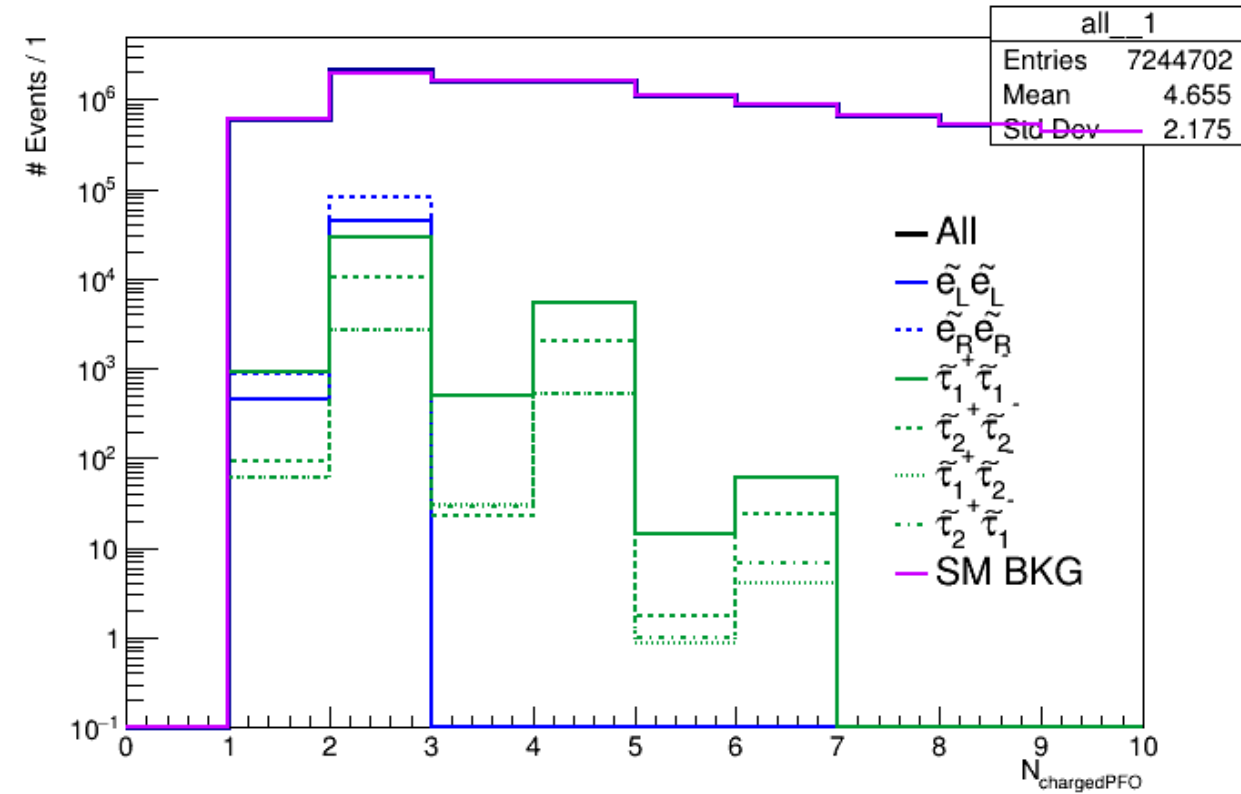
$N_{e\text{-PFO}}$ and $N_{\mu\text{-PFO}}$



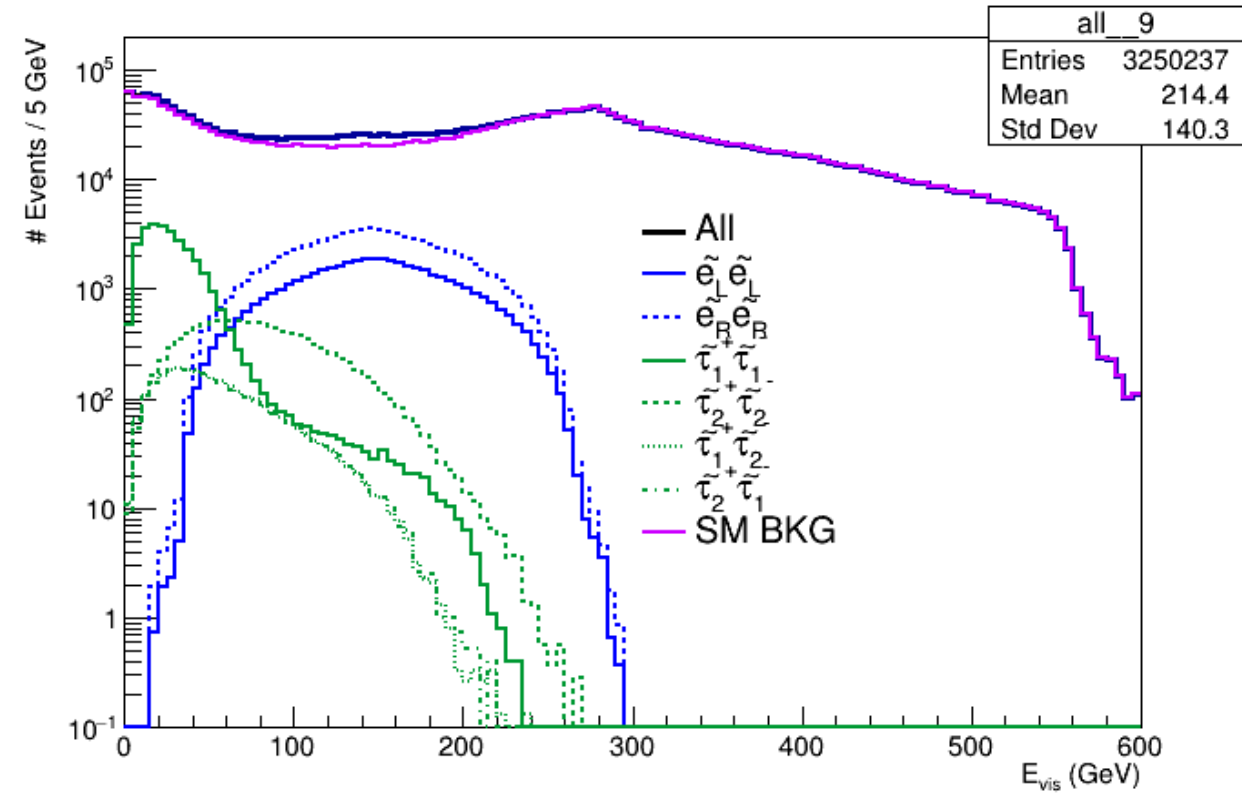
Only selected events with arrows considered so far ($N = 1$ or 2)

A few more cuts: $N_{\text{chargedPFO}}$ and E_{vis} (for \tilde{e})

ILD simulation



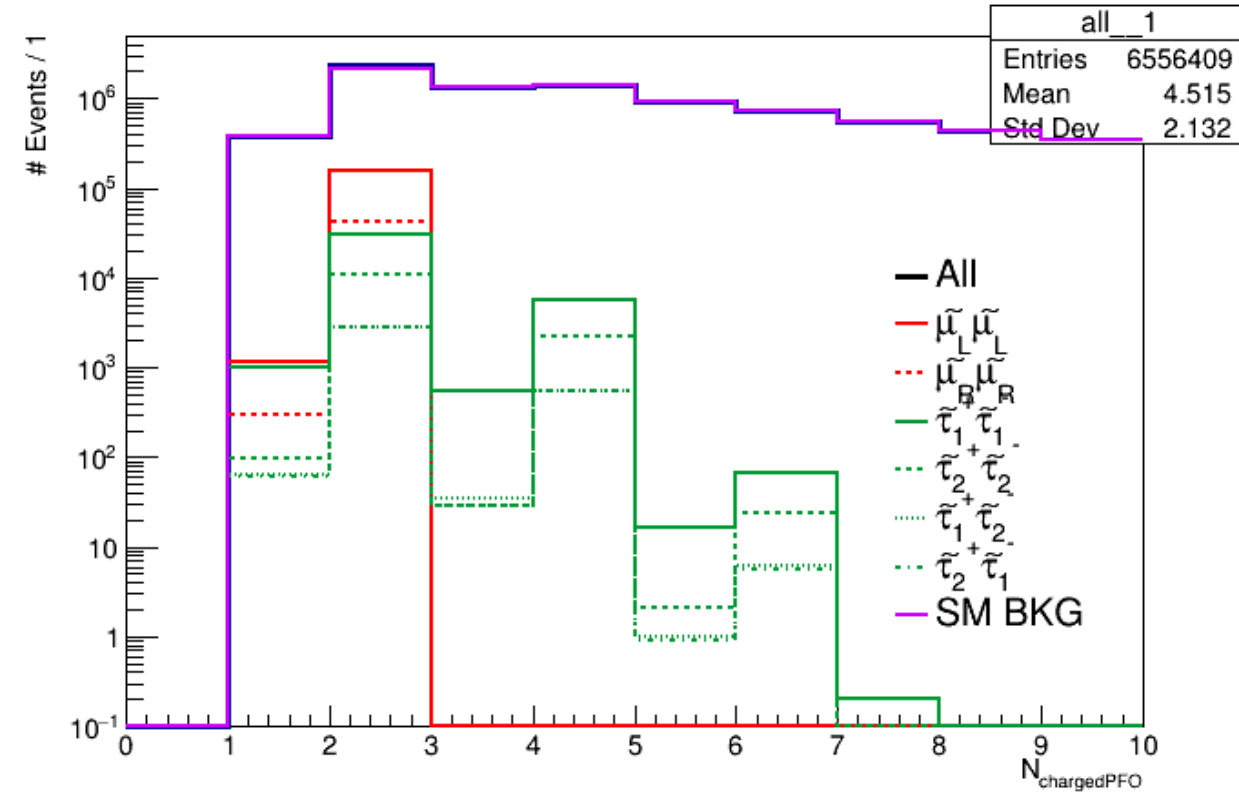
ILD simulation



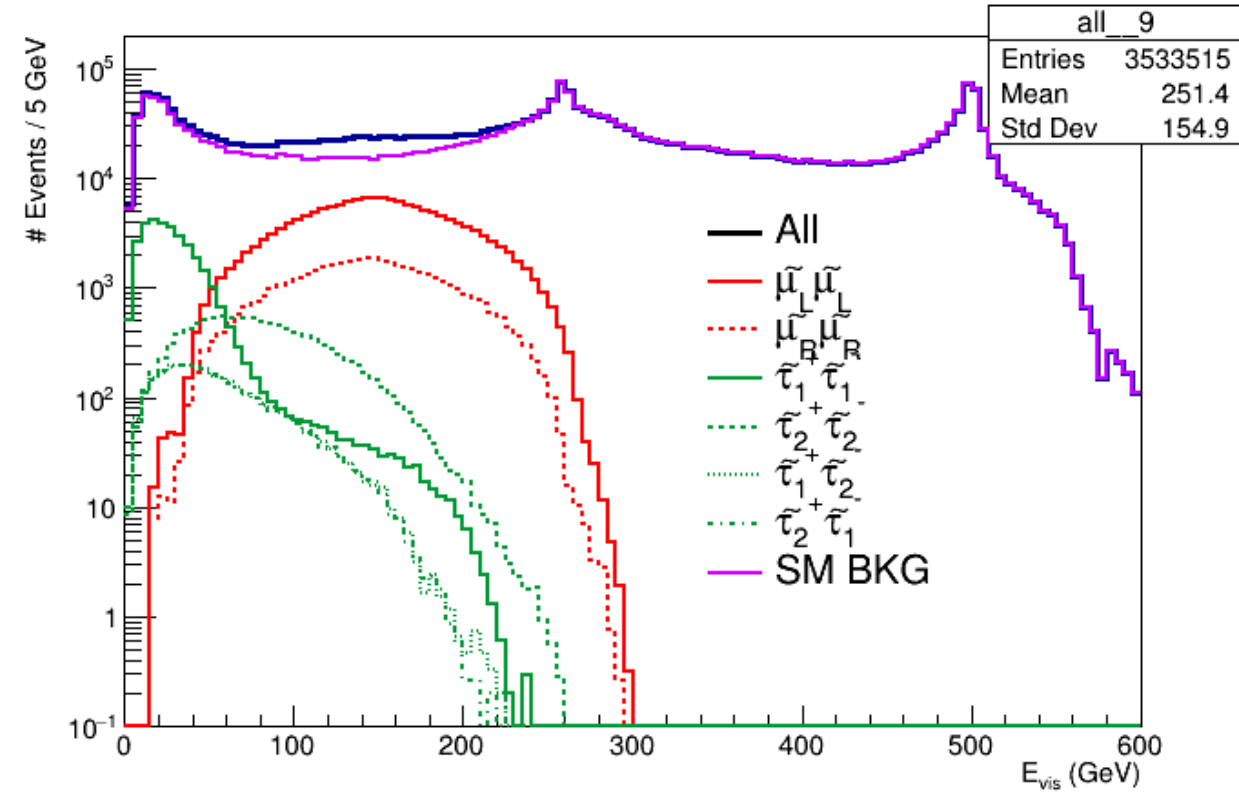
| | $\tilde{e}_L \tilde{e}_L$ | $\tilde{e}_R \tilde{e}_R$ | $\tilde{\tau}_1^+ \tilde{\tau}_1^-$ | $\tilde{\tau}_2^+ \tilde{\tau}_2^-$ | $\tilde{\tau}_1^+ \tilde{\tau}_2^-$ | $\tilde{\tau}_2^+ \tilde{\tau}_1^-$ | all SM bkg |
|------------------------------------|---------------------------|---------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------|
| $1 \leq N_{e\text{-PFO}} \leq 2$ | $4.45 \cdot 10^4$ | $8.30 \cdot 10^4$ | $3.52 \cdot 10^4$ | $1.24 \cdot 10^4$ | $3.31 \cdot 10^3$ | $3.30 \cdot 10^3$ | $1.11 \cdot 10^7$ |
| $N_{\text{chargedPFO}} \leq 2$ | $4.45 \cdot 10^4$ | $8.30 \cdot 10^4$ | $2.93 \cdot 10^4$ | $1.03 \cdot 10^4$ | $2.75 \cdot 10^3$ | $2.75 \cdot 10^3$ | $2.59 \cdot 10^6$ |
| $E_{\text{vis}} < 300 \text{ GeV}$ | $4.45 \cdot 10^4$ | $8.30 \cdot 10^4$ | $2.93 \cdot 10^4$ | $1.03 \cdot 10^4$ | $2.75 \cdot 10^3$ | $2.75 \cdot 10^3$ | $1.83 \cdot 10^6$ |

A few more cuts: $N_{\text{chargedPFO}}$ and E_{vis} (for $\tilde{\mu}$)

ILD simulation



ILD simulation



| | $\tilde{\mu}_L \tilde{\mu}_L$ | $\tilde{\mu}_R \tilde{\mu}_R$ | $\tilde{\tau}_1^+ \tilde{\tau}_1^-$ | $\tilde{\tau}_2^+ \tilde{\tau}_2^-$ | $\tilde{\tau}_1^+ \tilde{\tau}_2^-$ | $\tilde{\tau}_2^+ \tilde{\tau}_1^-$ | all SM bkg |
|------------------------------------|-------------------------------|-------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------|
| $1 \leq N_{\mu\text{-PFO}} \leq 2$ | $1.56 \cdot 10^5$ | $4.26 \cdot 10^4$ | $3.74 \cdot 10^4$ | $1.32 \cdot 10^4$ | $3.51 \cdot 10^3$ | $3.49 \cdot 10^3$ | $9.65 \cdot 10^6$ |
| $N_{\text{chargedPFO}} \leq 2$ | $1.56 \cdot 10^5$ | $4.26 \cdot 10^4$ | $3.11 \cdot 10^4$ | $1.09 \cdot 10^4$ | $2.92 \cdot 10^3$ | $2.91 \cdot 10^3$ | $2.54 \cdot 10^6$ |
| $E_{\text{vis}} < 300 \text{ GeV}$ | $1.56 \cdot 10^5$ | $4.26 \cdot 10^4$ | $3.11 \cdot 10^4$ | $1.09 \cdot 10^4$ | $2.92 \cdot 10^3$ | $2.91 \cdot 10^3$ | $1.57 \cdot 10^6$ |

Summary & Next steps

- Performed SUSY event sample generation and DELPHES simulation
- Observed clear edge structure in selectron/smuon events
- Stau events are complicated
- Analysis of background rejection started

- More cut ideas?
- Mass extraction by edge detection (How?)

BACKUP

Muon $g-2$ + SUSY: status report

- Produce SUSY MC samples at ILC500 with WHIZARD2.8.5
 - The files “blr1.slha” and SINDARIN files prepared by theorists, but beam energy spread was not included
 - Worked to include ISR / beam energy spread by implementing CIRCE2
 - Included PYTHIA6 and TAUOLA as well
 - Calculated cross-section for each SUSY process, and generated MC events
- Run detector simulation: this time DELPHES used

Problems / Questions / Next Step (1)

- When I include Pythia, it crushed.
 - Up to Xsec calculation works, but not for event generation.
- I set Tauola is on, **but it keeps PDG +-15 (no decay of tau) in the event.**
- **Solved:** These are solved when I put the sentence “\$ps_PYTHIA_PYGIVE = “MDCY(C1000022,1)=0”” in sindarlin file explicitly (written in Whizard manual).

Problems / Questions / Next Step (2)

- When running TAUOLA, I got the following message.
 - Subroutine fill_pyjets_spin_data: tau helicity information is not set, though polarized tau decay was requested. Most likely, the SINDARIN file does not include polarized for particles and/or not ?polarized_events=true
 - Still no tau decay exist in tau events. Maybe due to this message?
- **Solved:** Put the sentence “?polarized_events=true” in global.

Problems / Questions / Next Step (3)

- Found ~4[7]% events have stable tau (no daughters of tau) in $\text{stau1}+\text{stau2}-[\text{stau1}+\text{stau1}-]$ event.
- The biggest difference with Keita's study is with or without SUSY contribution.
- **Solved**: need to apply patch for PYTHIA6 (many thanks to Mikael Berggren (DESY))
 - This needs: fresh download of Whizard2.8.5, apply patch to PYTHIA6, compile and install. The Whizard2.8.5 which is already installed in KEKCC is not enough to handle stau BSM world.

Problems / Questions / Next Step (4)

- How to do detector simulation?
 - DELPHES? SGV? ILD full simulation?
 - In any case, I need to learn how to run the jobs. Started to learn DELPHES first.
 - Sometimes DELPHES does not work ---> **Solved**: some version difference (many thanks to Daniel), input file was too large.

Workflow (1)

WHIZARD 2.8.5

- used “blr1.ssha” and SINDARIN file
 - download from scratch, apply patch for PYTHIA6, compile and install
- working place:
/home/ilc/skawada/SUSYg-2/blr1_STDHEP
/home/ilc/skawada/SUSYg-2/blr1_LCIO
- procedure:
(1) source /home/ilc/skawada/SUSYg-2/SK-setup-whizard-2.8.5.sh
(2) go to working place, type “. job.sh” and “. run.sh”
(3) wait ~1-2 hours and done
- ※MC samples are stored in multiple files: 50K events / 1 file.

STDHEP file

LCIO file

can use for future ILD full simulation
stored at:

/hsm/ilc/users/skawada/SUSYg-2/blr1_sample/LCIO

Workflow (2)

STDHEP file

necessary for DELPHES simulation
(LCIO is not supported as the input for DELPHES)
stored at:
`/hsm/ilc/users/skawada/SUSYg-2/blr1_sample/STDHEP`

DELPHES + DELPHES2LCIO

- used ILC generic card for detector
- used DELPHES2LCIO for LCIO output

working place:

`/home/ilc/skawada/SUSYg-2/blr1_DEL`

procedure:

(1) `source /home/ilc/skawada/DJ-delphes-setup.sh`

(2) go to working place and type `“ . run.sh ”`

(3) type `“ . check.sh ”`, failed job must be recovered by hand

※I don't know why several jobs at KEKCC batch server fail.

The failure rate is ~10% even jobs controlled by one script.

※The EventSummary collection will be created at the end of each file.

DELPHES result (LCIO file)

Workflow (3)

DELPHES result (LCIO file)

contains DELPHES simulation result
event header information is lost
stored at:

/hsm/ilc/users/skawada/SUSYg-2/blr1_sample/DEL

MARLIN

- used to recover (or restore) event header information
- recovered cross-section, beam polarization, E_{CM} (500 GeV), process ID/name
- remove unnecessary EventSummary collection

working place:

/home/ilc/skawada/SUSYg-2/analysis/modification

procedure:

- (1) source /home/ilc/skawada/init_ilcsoft_v020202.sh
- (2) source /home/ilc/skawada/SUSYg-2/analysis/use.sh
- (3) go to working place and type “. run_modify.sh”
- (4) wait ~10 minutes and done

✂Need to assume each sample has exactly 50K + EventSummary

DELPHES result (LCIO file)
+ event header info

contains DELPHES simulation result and event header info
stored at:

/home/ilc/skawada/SUSYg-2/analysis/DEL_sample