

Testing the neutrino mass generation mechanism at future colliders

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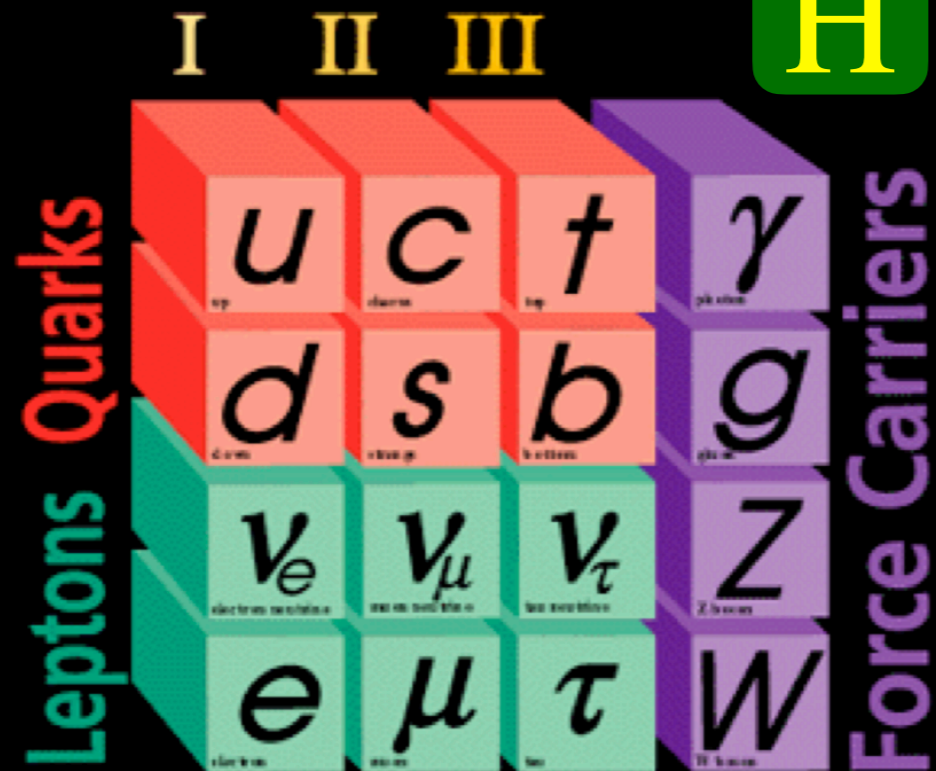
Mini – workshop on BSM at ILC

March 3, 2021

The Standard Model of Particle Interactions

Three Generations of Matter

H



Over the decades experiments have found each and every missing pieces

Verified the facts that they belong to this family

Finally at the Large Hadron collider Higgs has been observed

→ Its properties must be verified

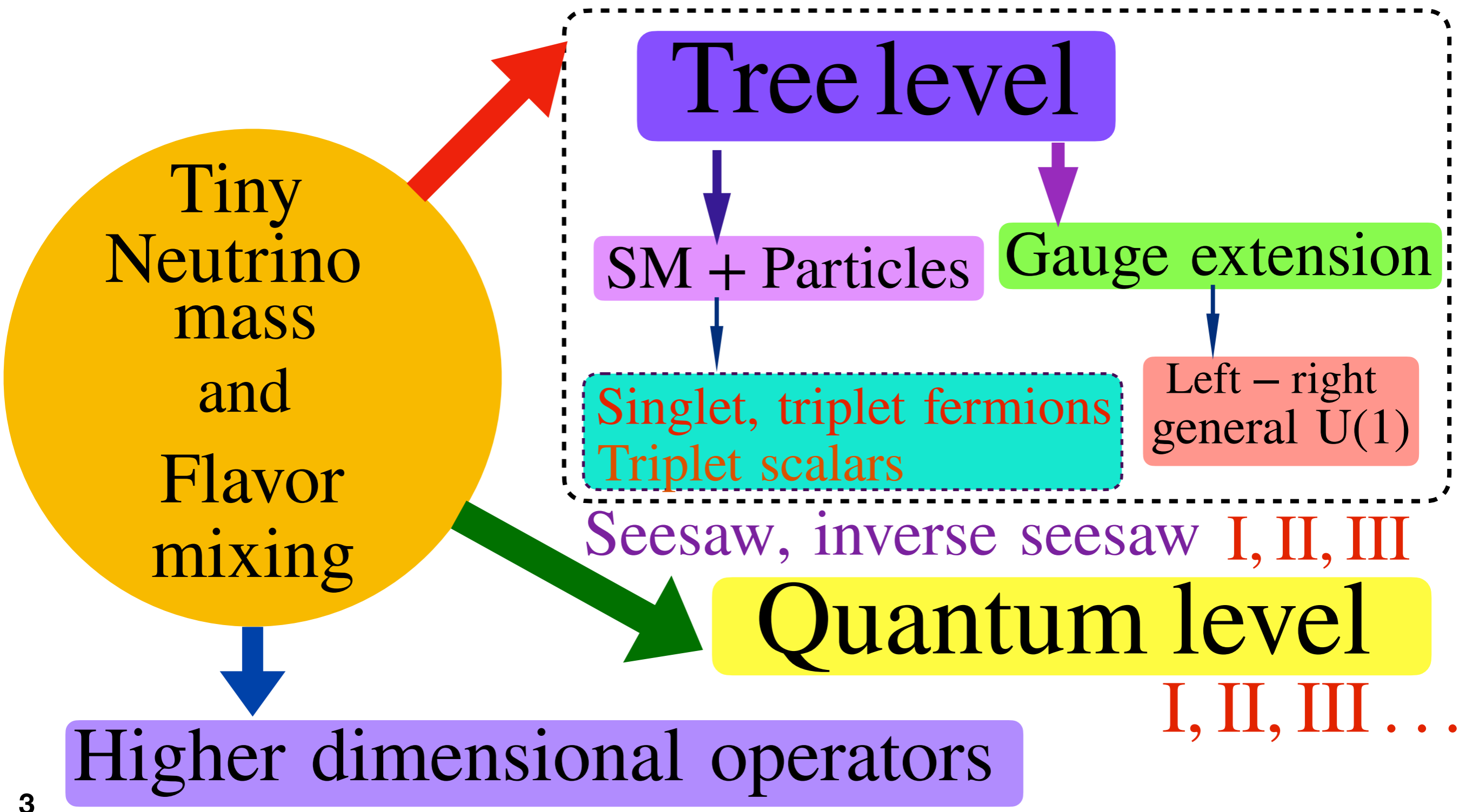
Strongly established with interesting shortcomings

Few of the very interesting anomalies :

Tiny neutrino mass and flavor mixings
Relic abundance of dark matter...

SM can not explain them

Different aspects of neutrino mass generation mechanism



Particle content

	SU(3) _c	SU(2) _L	U(1) _Y		U(1) _X
q_L^i	3	2	+1/6	x_q	$= \frac{1}{6}x_H + \frac{1}{3}x_\Phi$
u_R^i	3	1	+2/3	x_u	$= \frac{2}{3}x_H + \frac{1}{3}x_\Phi$
d_R^i	3	1	-1/3	x_d	$= -\frac{1}{3}x_H + \frac{1}{3}x_\Phi$
ℓ_L^i	1	2	-1/2	x_ℓ	$= -\frac{1}{2}x_H - x_\Phi$
e_R^i	1	1	-1	x_e	$= -x_H - x_\Phi$
H	1	2	+1/2	x'_H	$= \frac{1}{2}x_H$
N_R^i	1	1	0	x_ν	$= -x_\Phi$
Φ	1	1	0	x'_Φ	$= 2x_\Phi$

$$m_{Z'} = 2 g_X v_\Phi$$

x_H, x_Φ will appear the coupling with Z'

B - L case
 $x_H = 0, x_\Phi = 1$

3 generations of SM singlet right handed neutrinos (anomaly free)

Charges **before** the anomaly cancellations

Charges **after** imposing the anomaly cancellations

$U(1)_X$ breaking

$$\mathcal{L}_Y \supset - \sum_{i,j=1}^3 Y_D^{ij} \bar{\ell}_L^i H N_R^j - \frac{1}{2} \sum_{i=k}^3 Y_N^k \Phi \overline{N_R^k} N_R^k + \text{h.c.},$$

$$m_D^{ij} = \frac{Y_D^{ij}}{\sqrt{2}} v_h$$

$$m_{N^i} = \frac{Y_N^i}{\sqrt{2}} v_\Phi$$

$$m_\nu = \begin{pmatrix} 0 & M_D \\ M_D^T & M_N \end{pmatrix} \quad m_\nu \simeq -M_D M_N^{-1} M_D^T$$

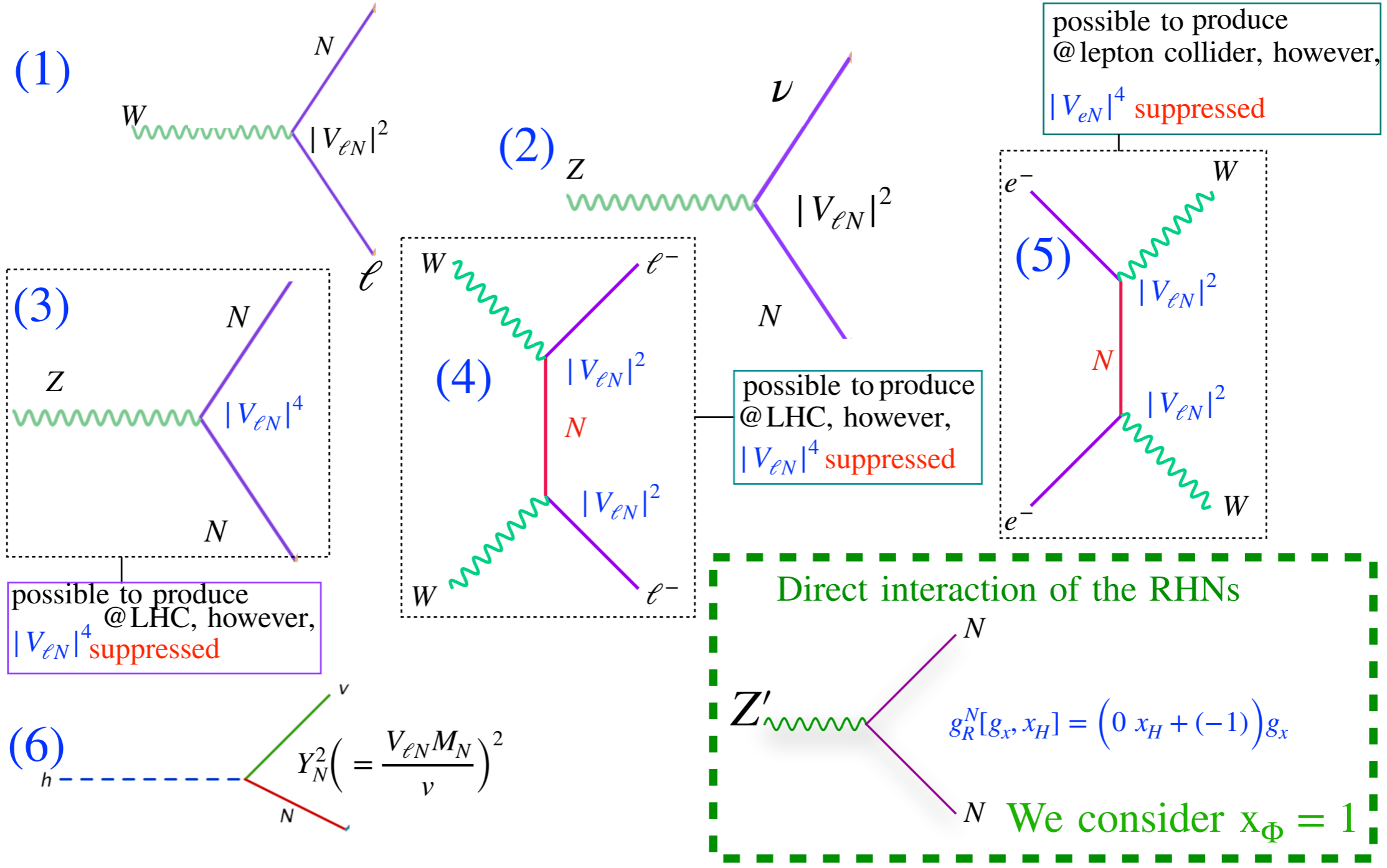
Seesaw mechanism

Production modes of the RHNs at the colliders : pp, e^-e^+, e^-p

Flavor eigenstate can be expressed in terms of the mass eigenstate

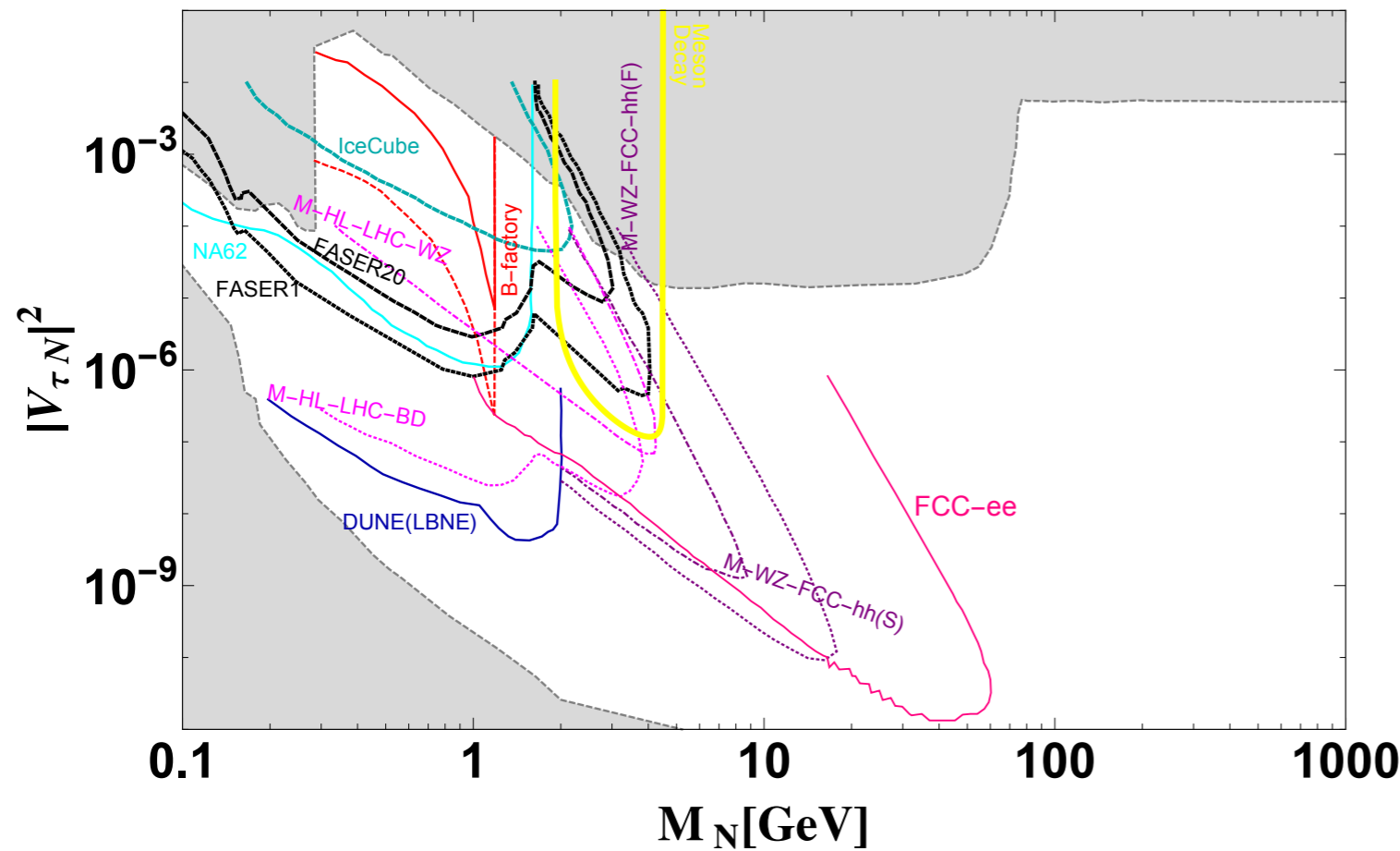
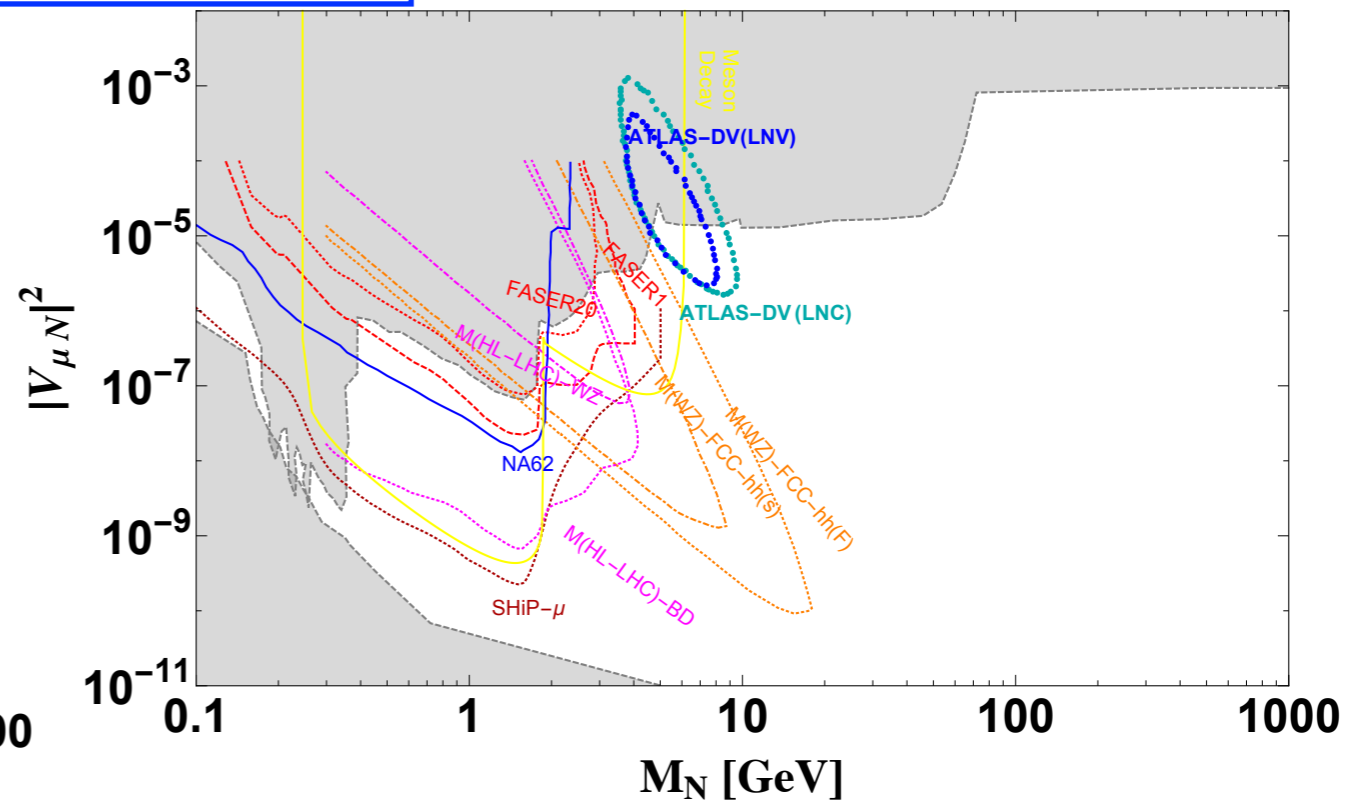
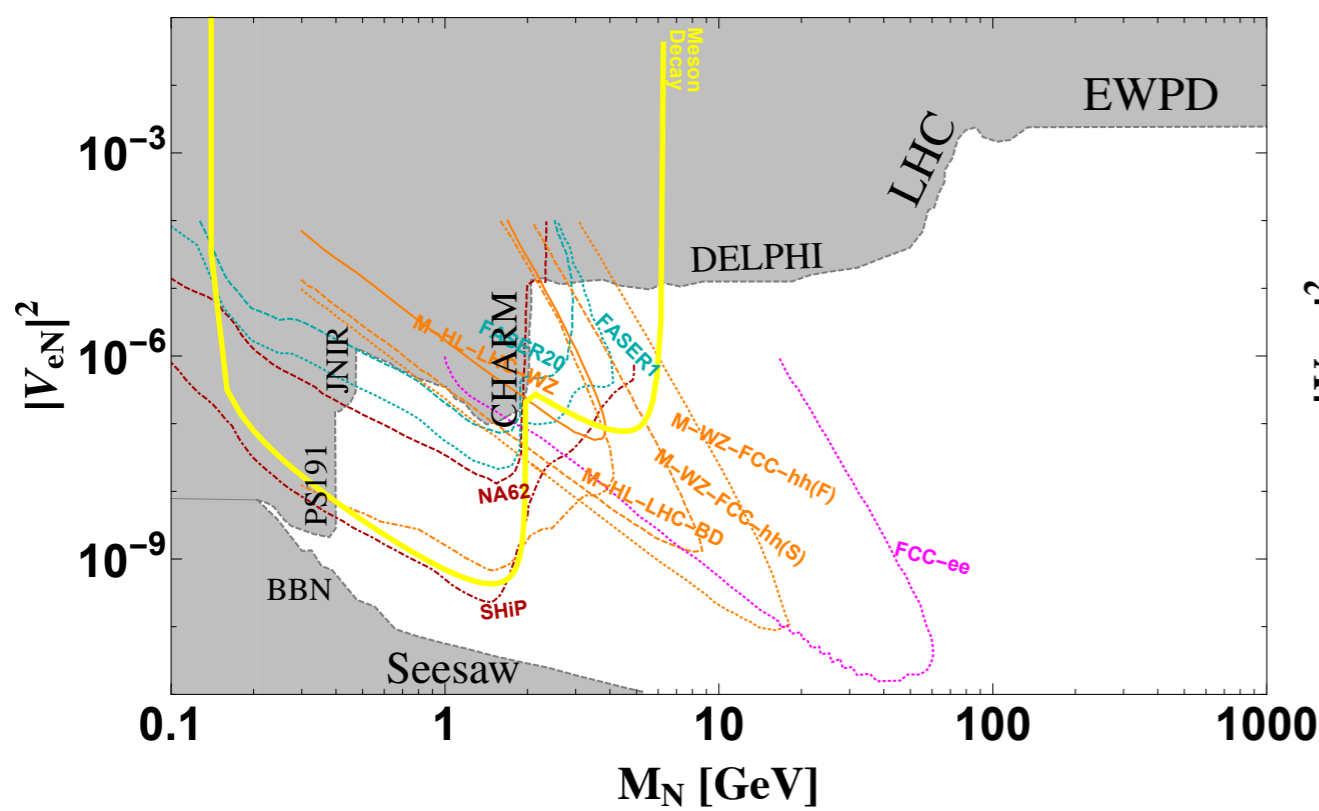
$$\nu_\ell \simeq U_{\ell m} \nu_m + V_{\ell n} N_n$$

\swarrow PMNS matrix \searrow $M_D M_N^{-1}$



Existing and prospective bounds on the mixings

1502.06541 1805.00070 1908.09562



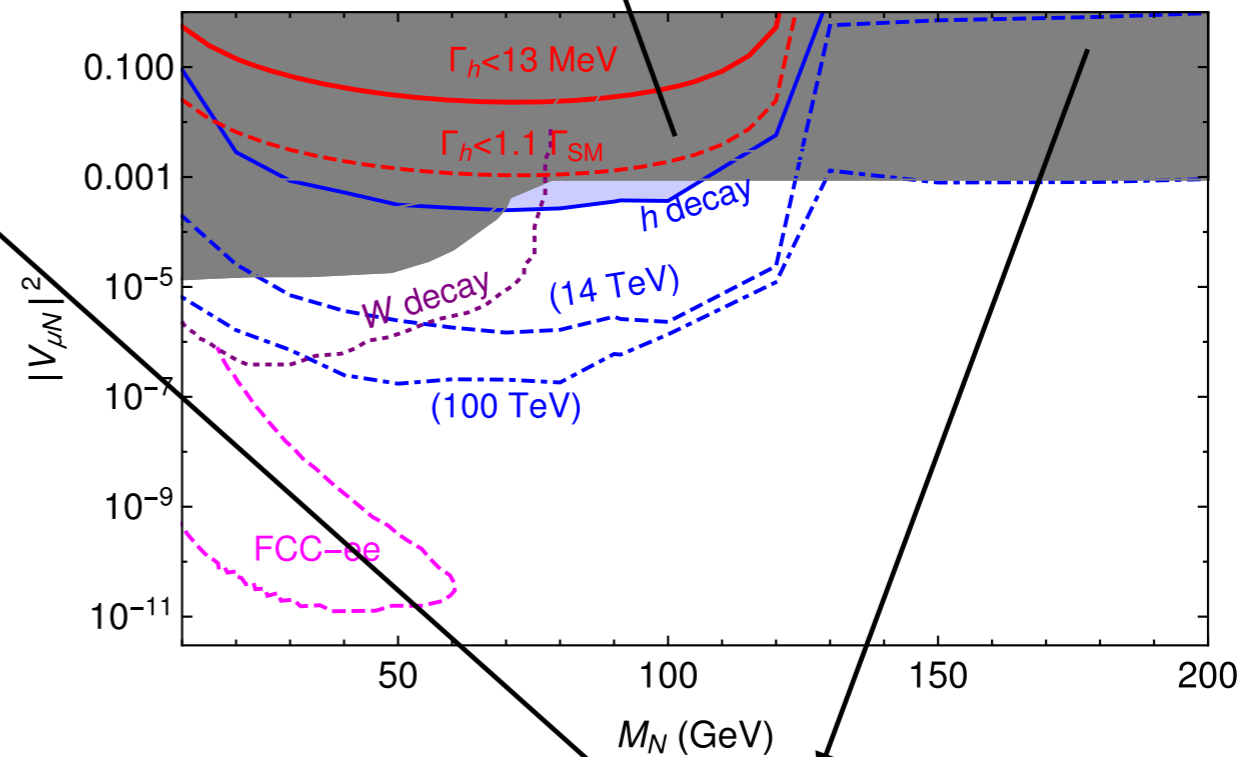
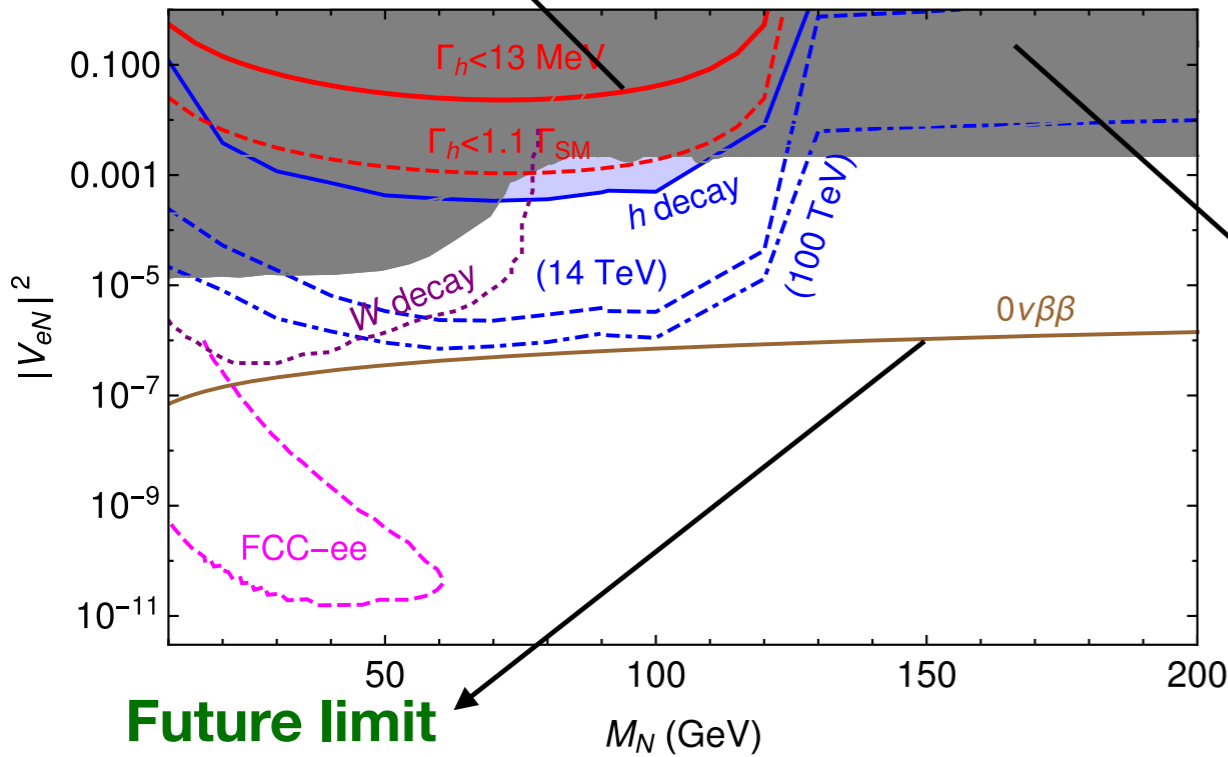
CMS $\ell^\pm \ell^\pm + \text{jets}$
 1806.10905 13 TeV, 35.9 fb⁻¹
 CMS $3\ell + \text{MET}$
 1802.02965 13 TeV, 35.9 fb⁻¹
 ATLAS $3\ell + \text{MET}$
 1905.09787, 36.1 fb⁻¹

General Yukawa structure : 1702.04668

$2\ell + p_T^{\text{miss}}$: bounds from the Higgs decay ($h \rightarrow N\nu, N \rightarrow 2\ell\nu$)

CMS, JHEP 09 (2016) 051: 7&8 TeV combined $H \rightarrow W W^*$, upper limit on Yukawa as well as mixing

Future sensitivity can go down to 1704.00880
 10% precise result at pp collider: 1704.00881
 arXiv:1606.09408

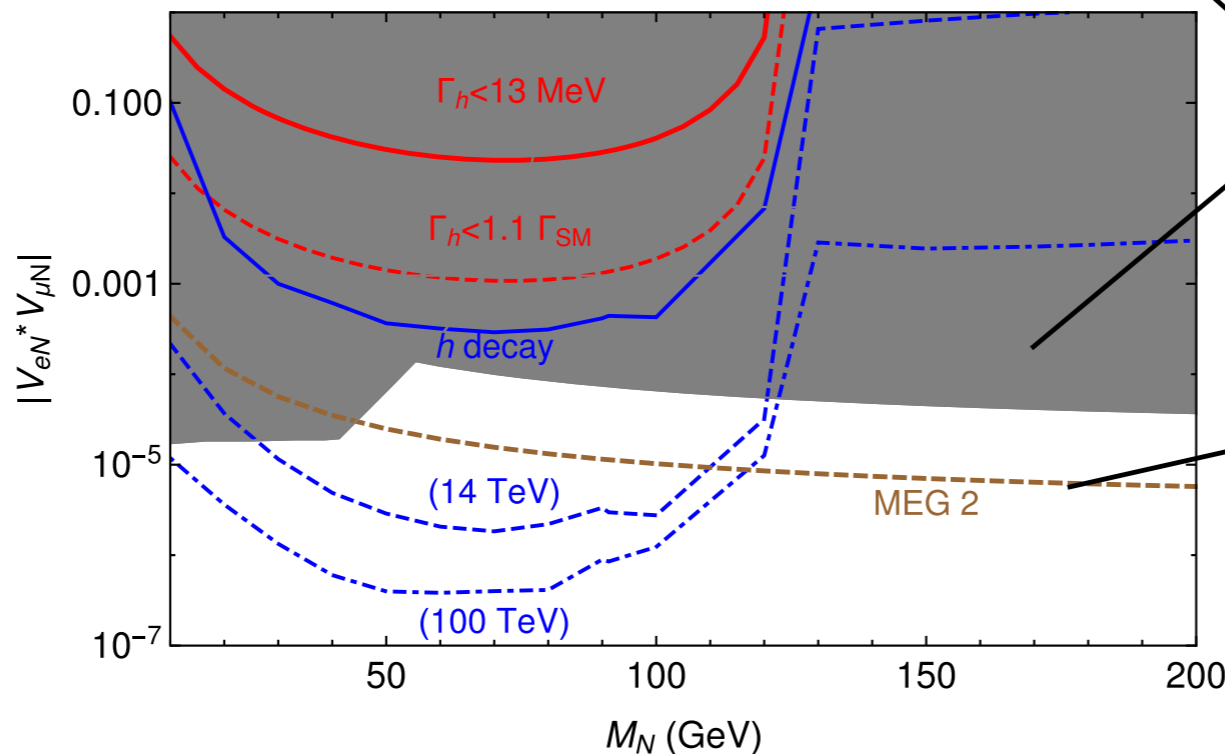


Future limit considering Majorana heavy neutrinos only

Excluded by LEP, LHC, EWPD, LFV limits from CMS is also included in the lower panel

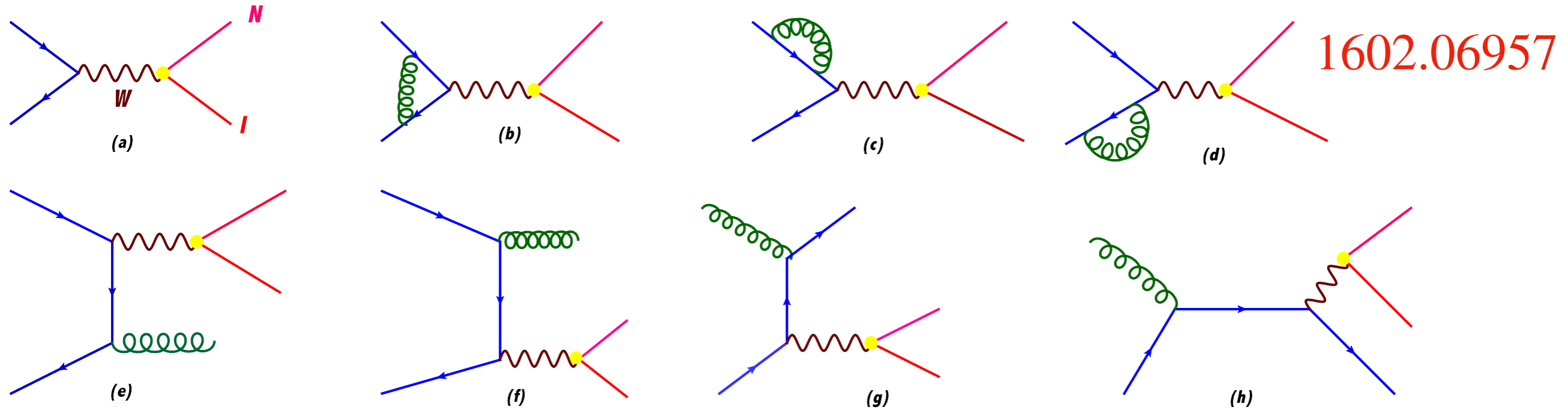
FCC-ee : Limits from Z decay
 W-decay @LHC

Future limits

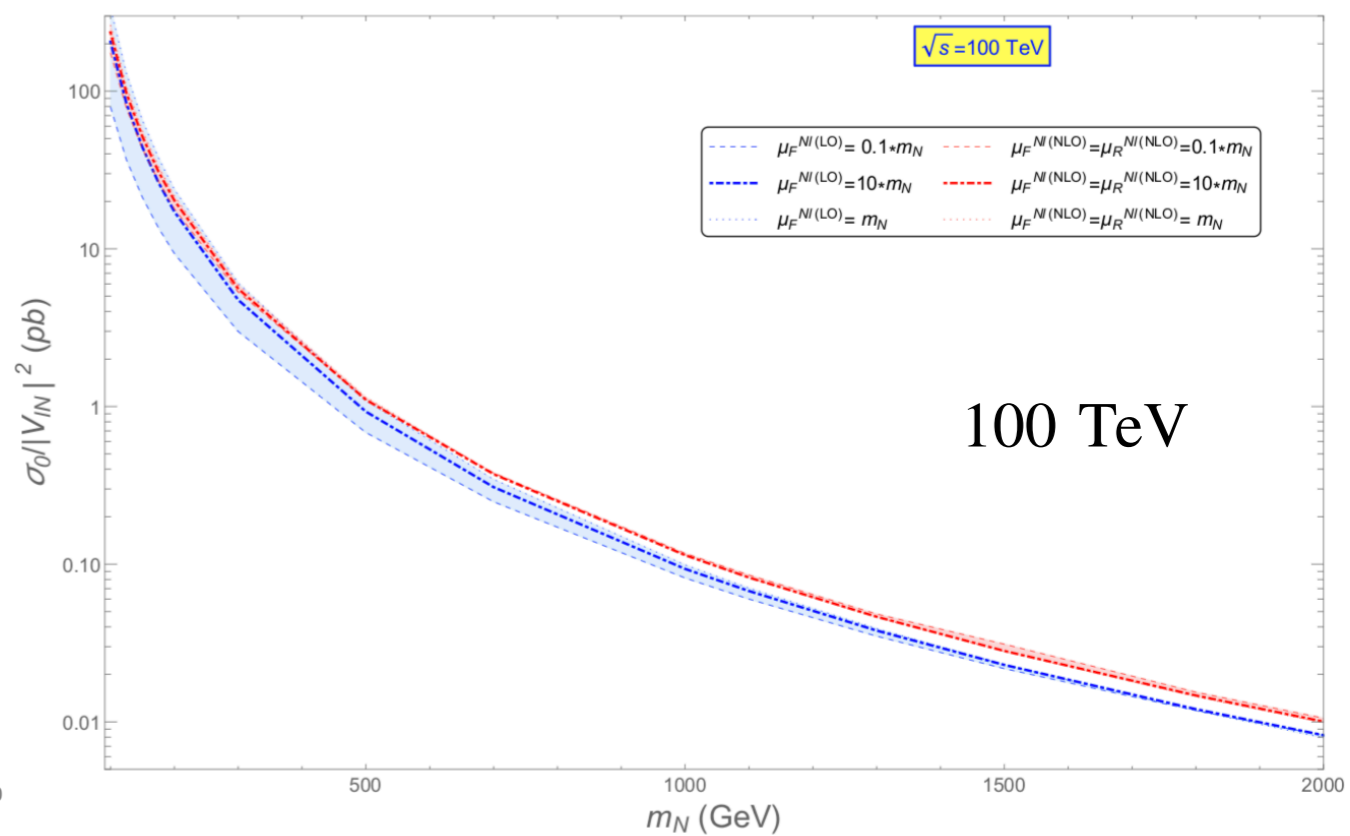
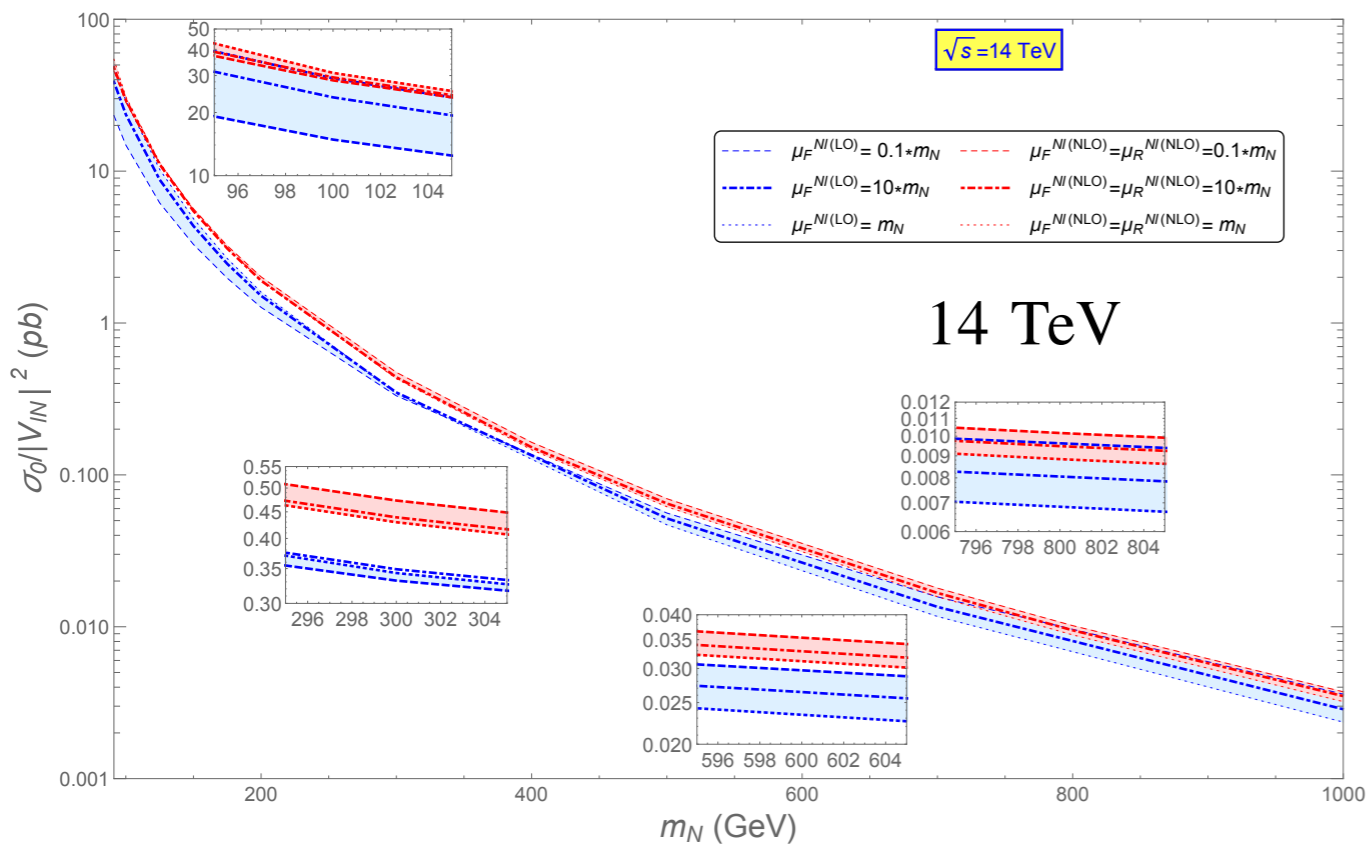


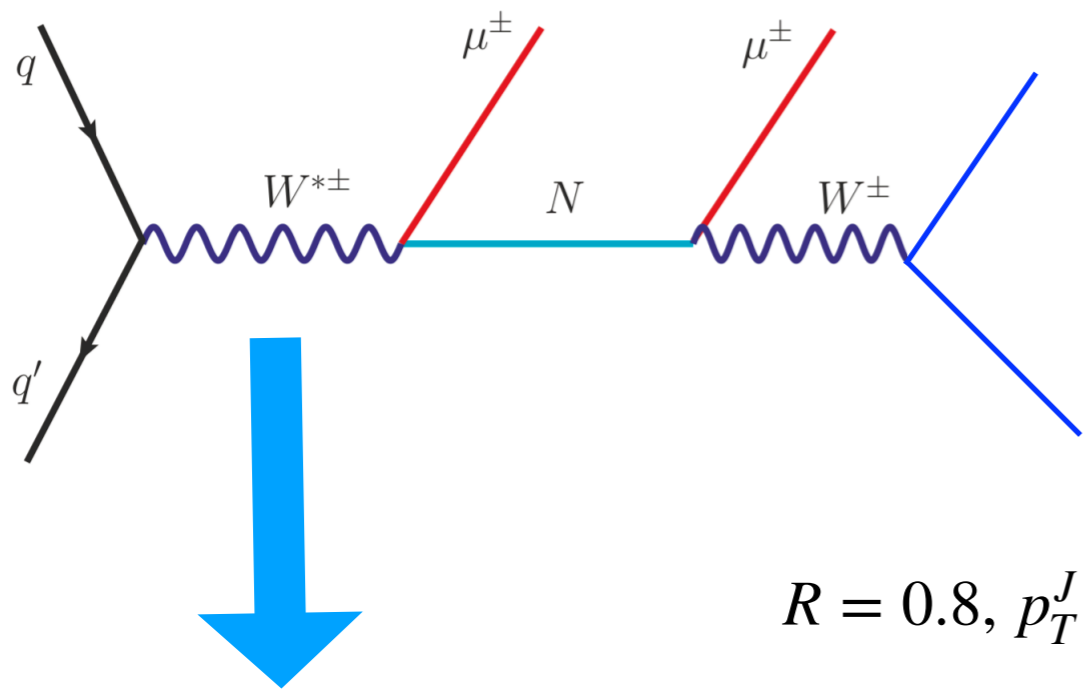
$\mu \rightarrow e\gamma$
 ~ future branching ratio $O(10^{-15})$

NLO – QCD production of the heavy neutrinos @ pp colliders



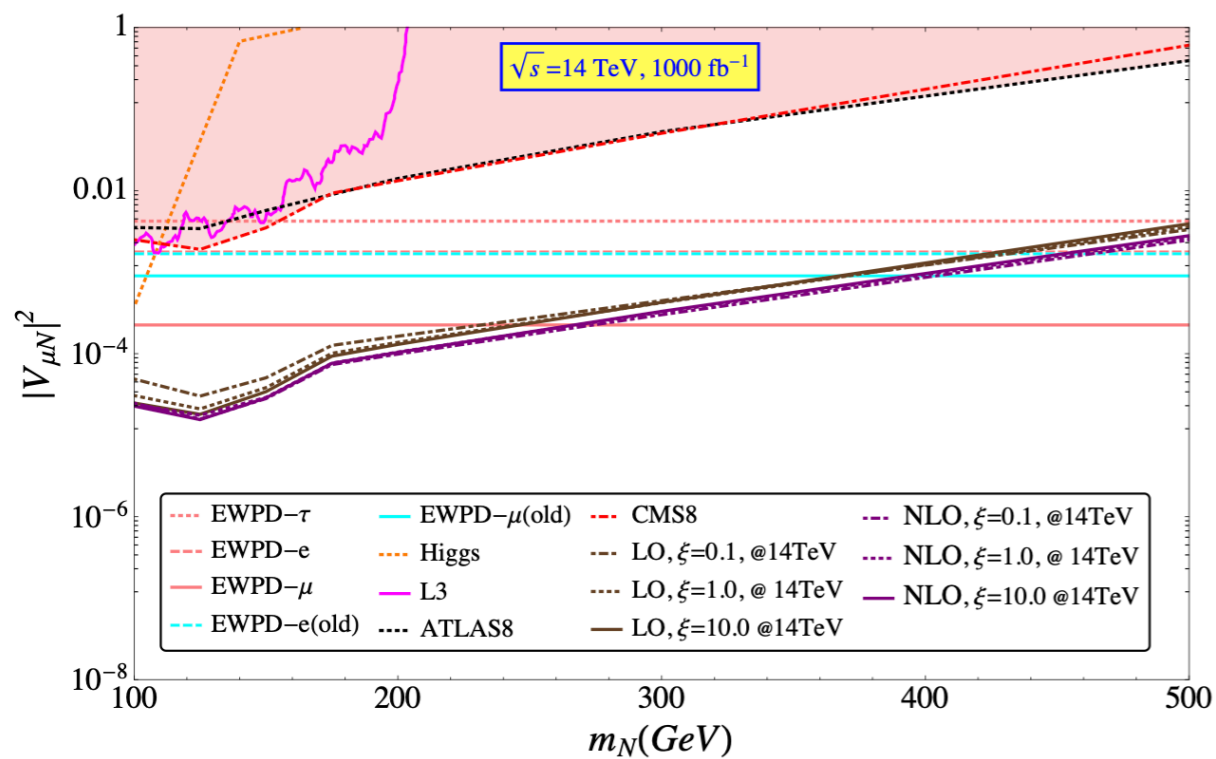
$$\mu_F^{\text{NLO}} = \mu_R^{\text{NLO}} = \xi * m_N \quad \mu_F^{\text{NLO}} = m_N, \mu_R^{\text{NLO}} = \xi * m_N \quad \mu_F^{\text{NLO}} = \xi * m_N, \mu_R^{\text{NLO}} = \xi * m_N \quad 0.1 \leq \xi \leq 10$$



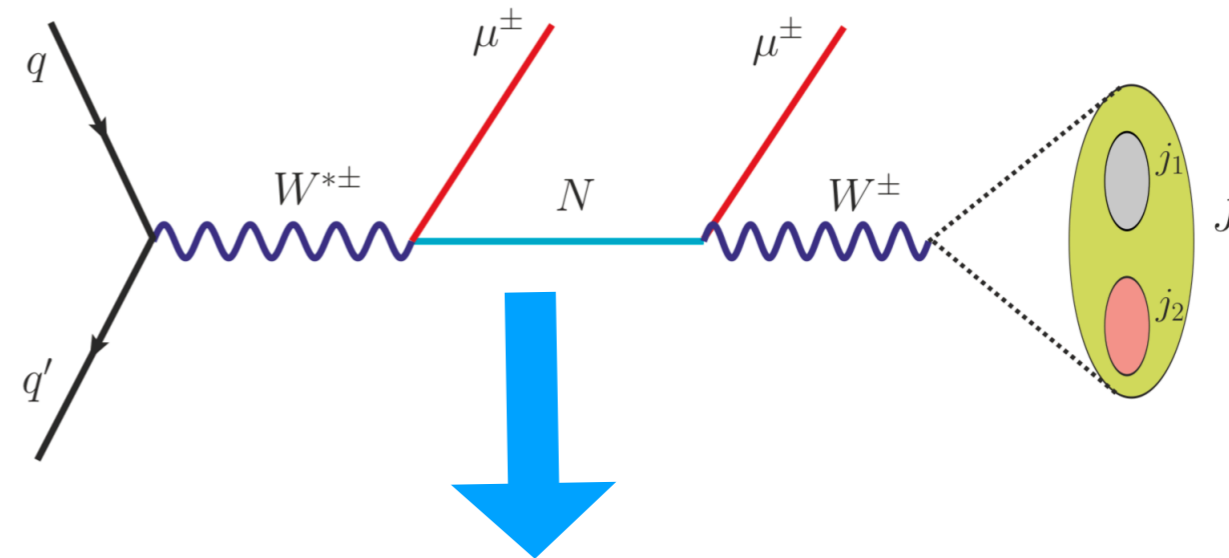


$$R = 0.8, p_T^J > 150 \text{ GeV}, \tau_{21}^J < 0.5, E_T^{\text{miss}} < 35 \text{ GeV}, M^J > 50 \text{ GeV}$$

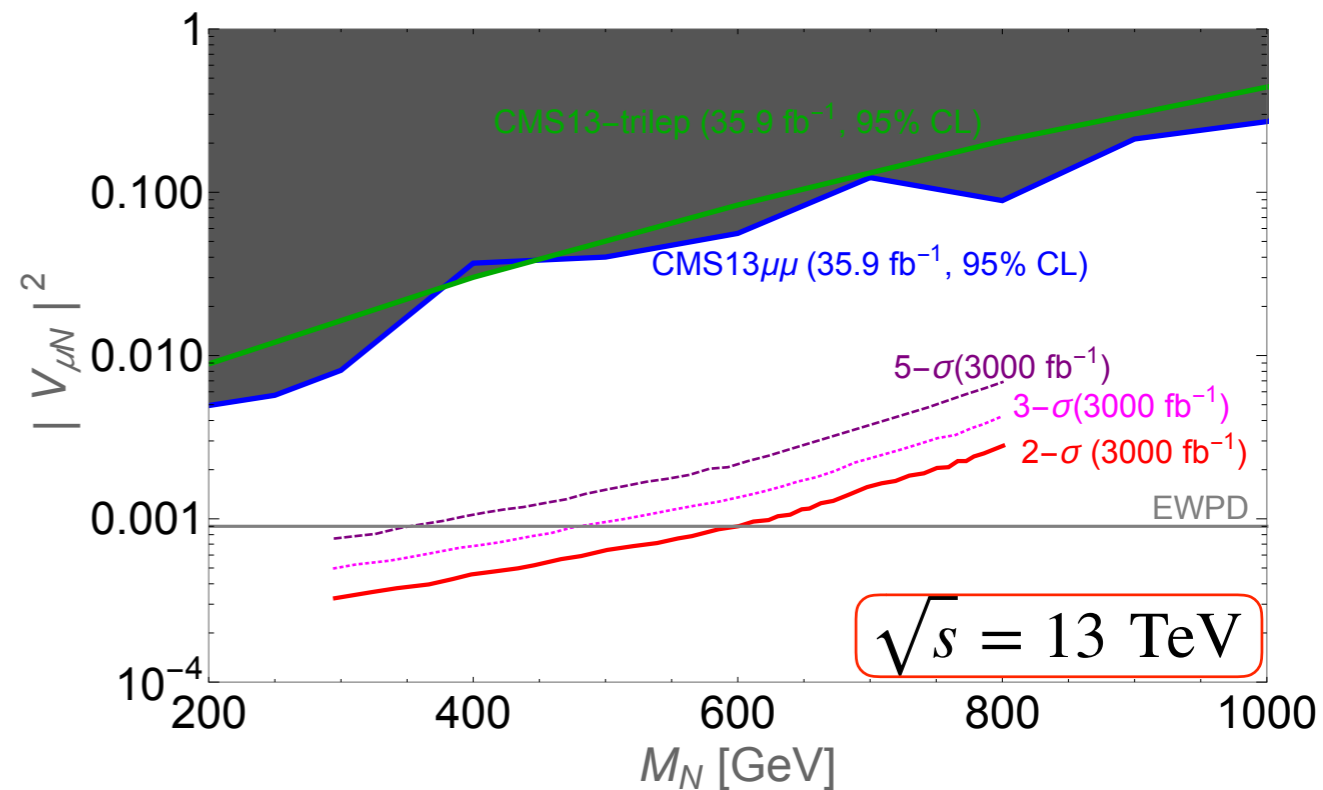
SSDDL + 2 - jet



14 TeV, 1000 fb⁻¹



SSDDL + 1 - Fat jet

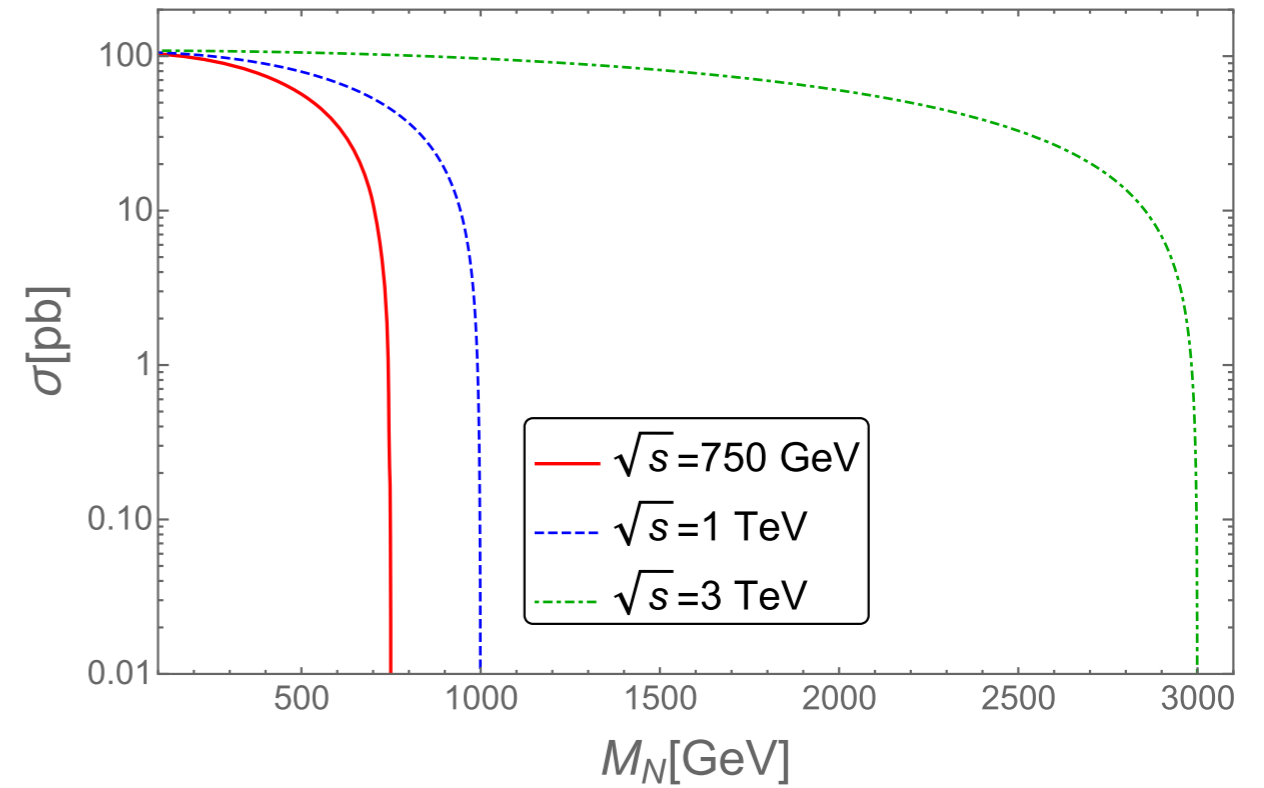
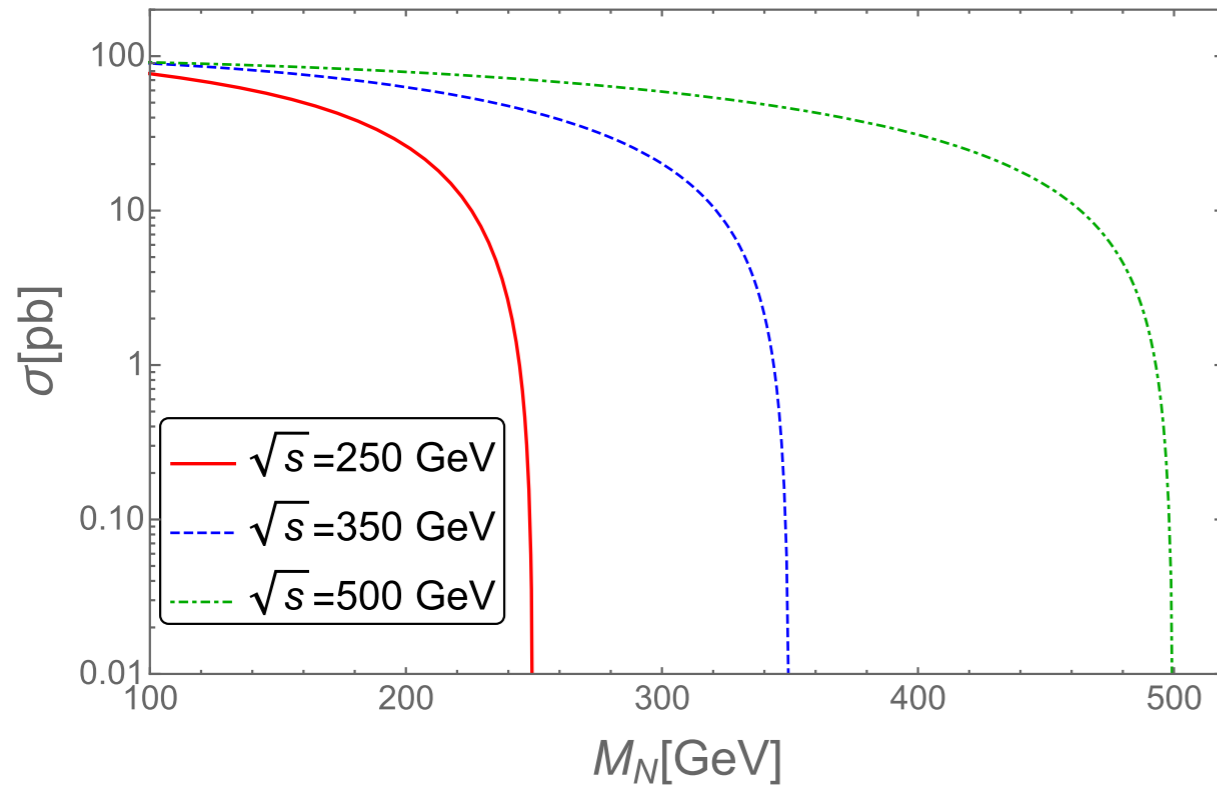


Production of the heavy neutrinos at the Linear Collider using fat-jet

1207.3734, 1811.04291
1502.05915, 1503.05491

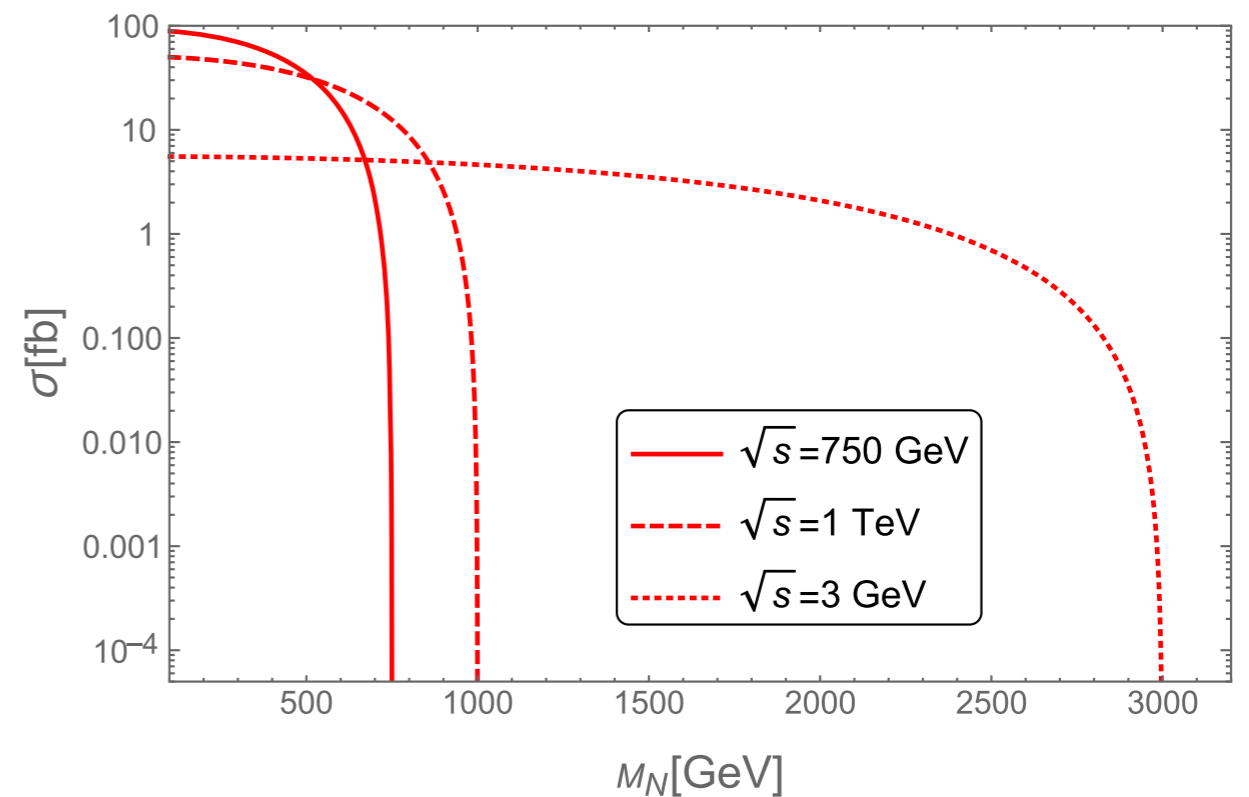
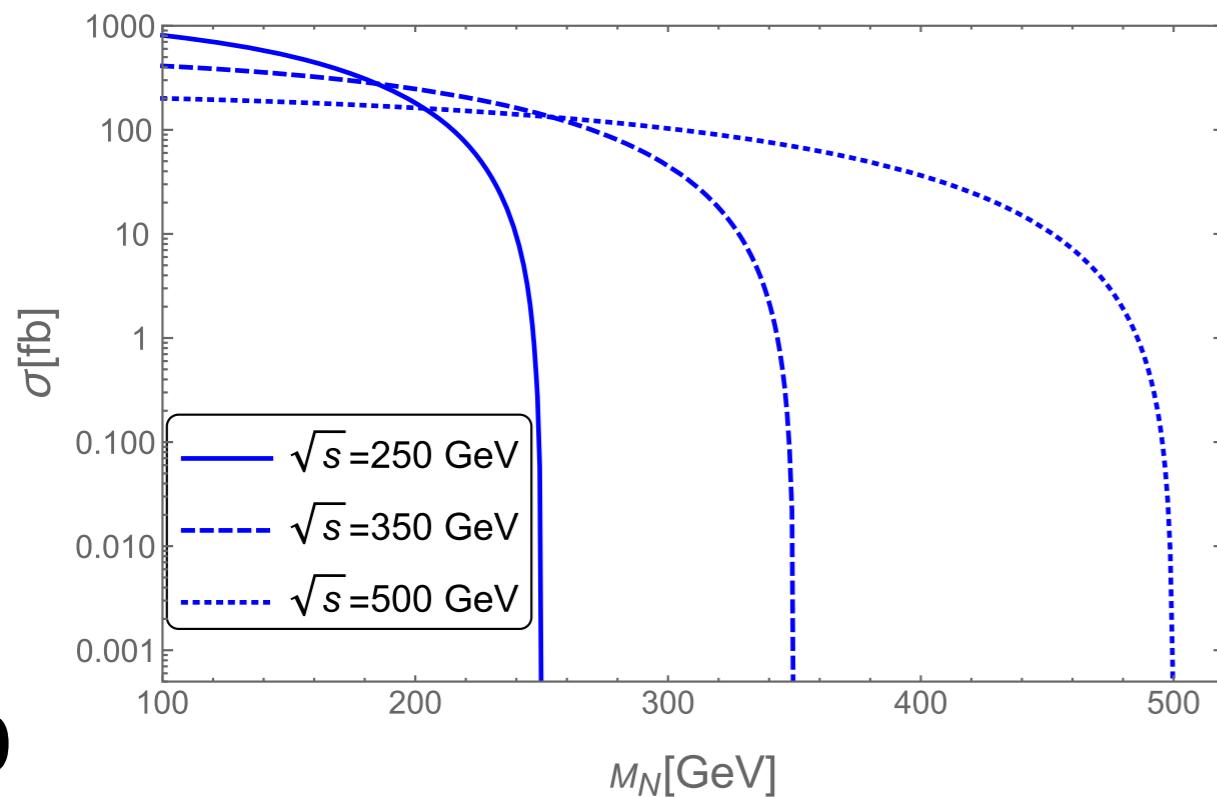
$$e^+e^- \rightarrow \nu_1 N_1$$

Includes s – channel and t – channel processes

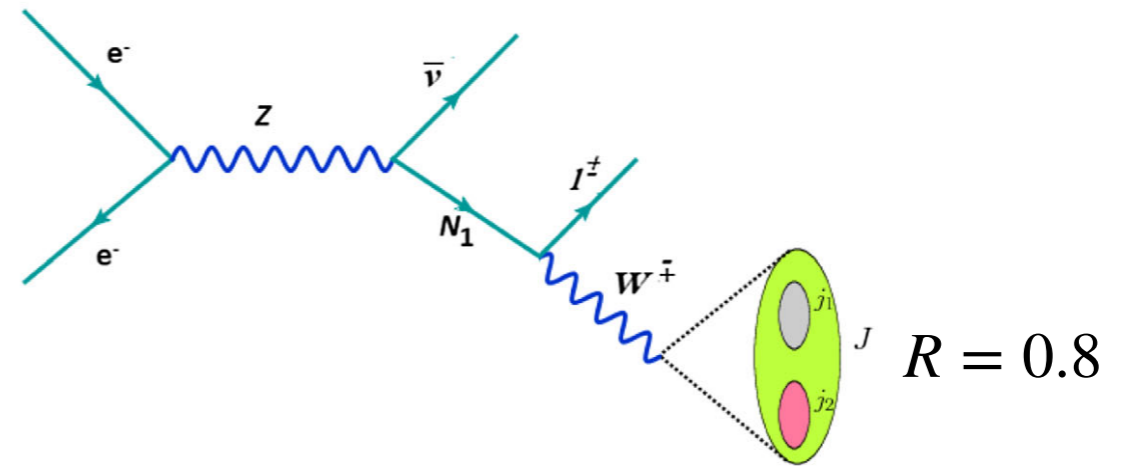
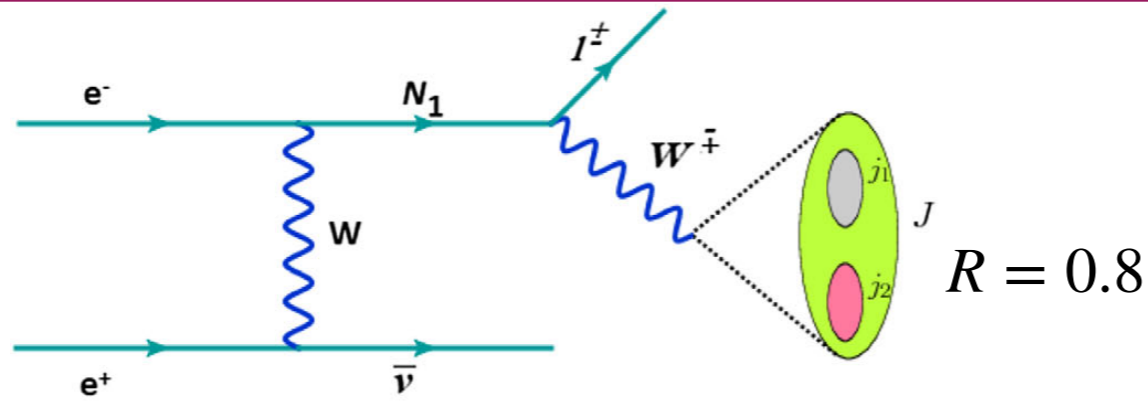


$$e^+e^- \rightarrow \nu_2 N_2 / \nu_3 N_3$$

Includes s – channel process, t – channel suppressed by off – diagonal Yukawa, away from the Z pole



$e + J + p_T^{\text{miss}}$ final states at the linear colliders.



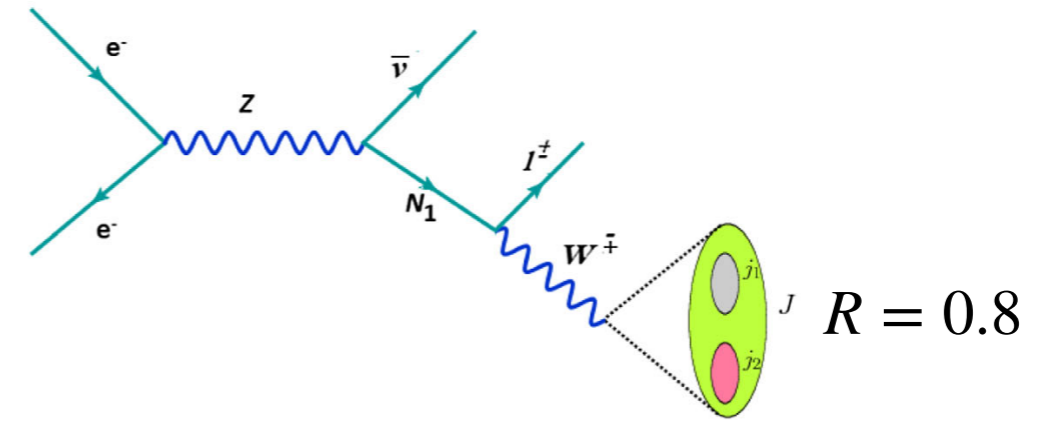
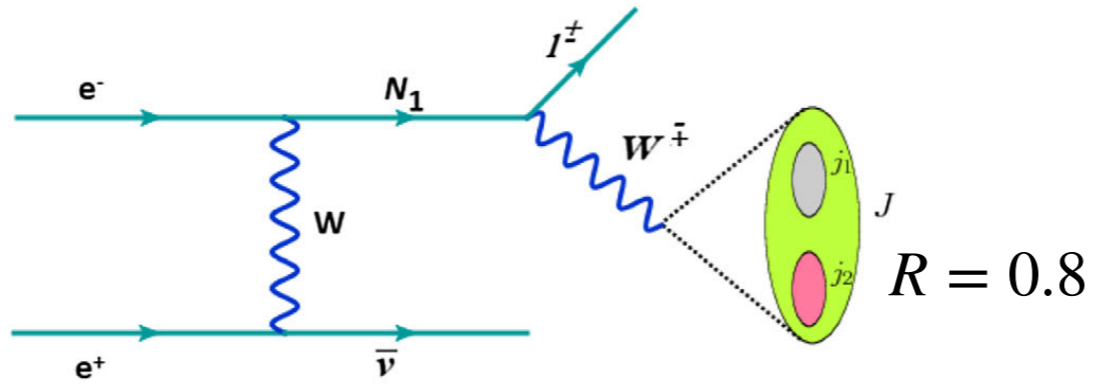
- Transverse momentum for fat-jet $p_T^J > 150$ GeV for M_N mass range 400 GeV-600 GeV and $p_T^J > 250$ GeV for M_N mass range 700 GeV-900 GeV.
- Transverse momentum for leading lepton $p_T^{e^\pm} > 100$ GeV for M_N mass range 400 GeV-600 GeV and $p_T^{e^\pm} > 200$ GeV for M_N mass range 700 GeV-900 GeV.
- Polar angle of lepton and fat-jet $|\cos \theta_e| < 0.85$, $|\cos \theta_J| < 0.85$.
- Fat-jet mass $M_J > 70$ GeV.

1 TeV e^-e^+ collider

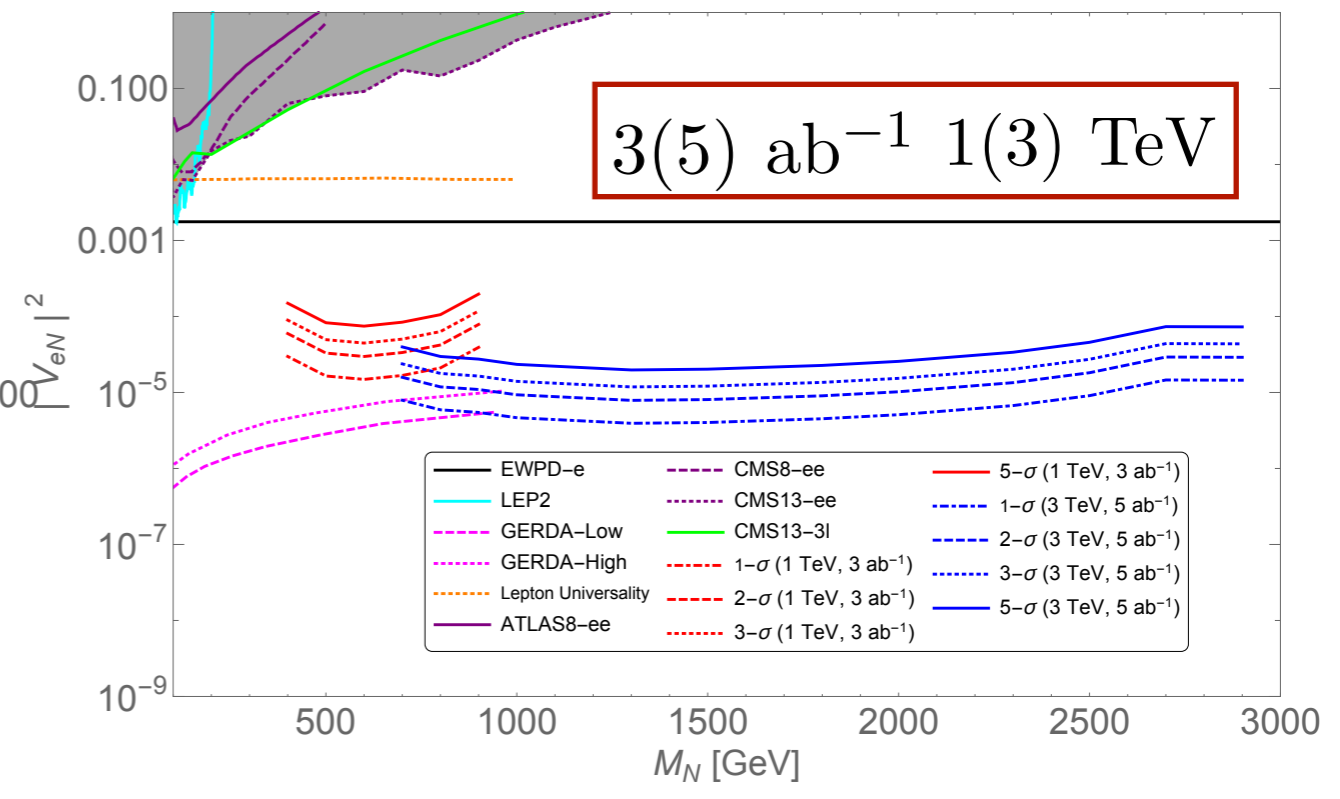
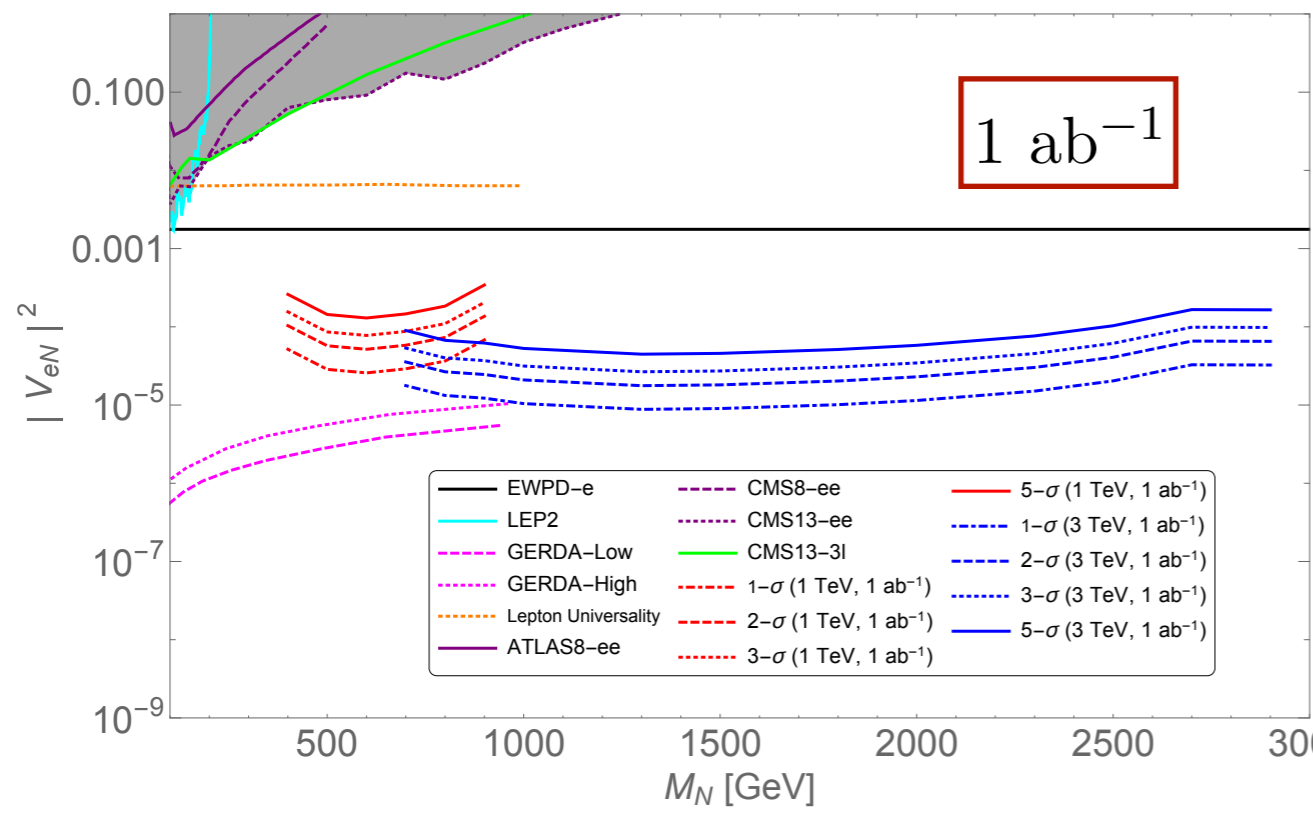
- Transverse momentum for fat-jet $p_T^J > 250$ GeV for the M_N mass range 700 GeV-900 GeV and $p_T^J > 400$ GeV for M_N mass range 1 – 2.9 TeV.
- Transverse momentum for leading lepton $p_T^{e^\pm} > 200$ GeV for M_N mass range 700 – 900 GeV and $p_T^{e^\pm} > 250$ GeV for M_N mass range 1 – 2.9 TeV.
- Polar angle of lepton and fat-jet $|\cos \theta_e| < 0.85$, $|\cos \theta_J| < 0.85$.
- Fat-jet mass $M_J > 70$ GeV.

3 TeV e^-e^+ collider

$e + J + p_T^{\text{miss}}$ final states at the linear colliders

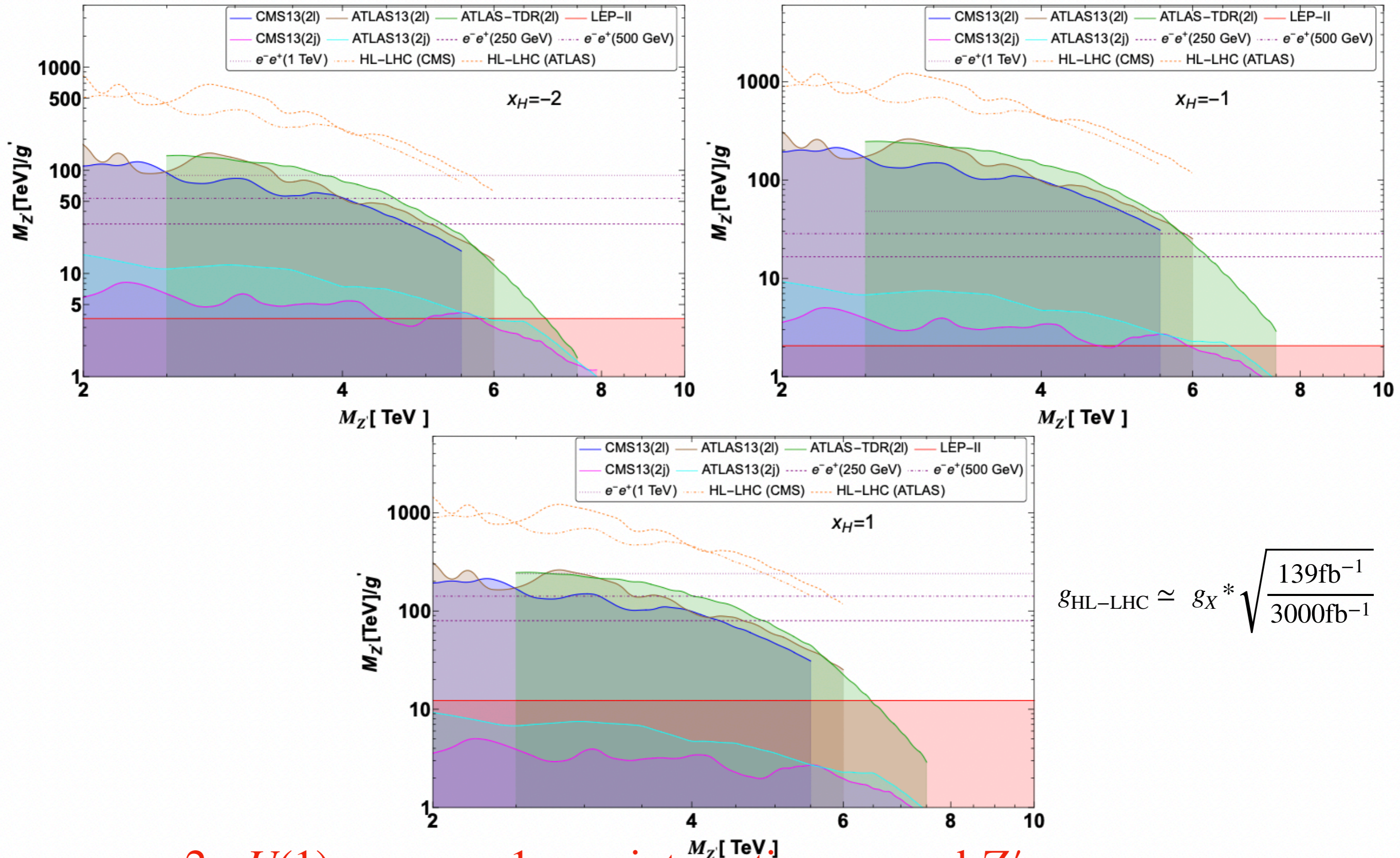


1 TeV (red band) and 3 TeV (blue band)



Limits on VEV scale of $U(1)_X$ $2\ell, 2j$ @ LHC; HL – LHC; LEP – II, ILCx

2202.13358



$$g_{\text{HL-LHC}} \simeq g_X^* \sqrt{\frac{139\text{fb}^{-1}}{3000\text{fb}^{-1}}}$$

$x_H = -2 : U(1)_R, x_H = -1 : \text{no interaction} : e_R \text{ and } Z'$

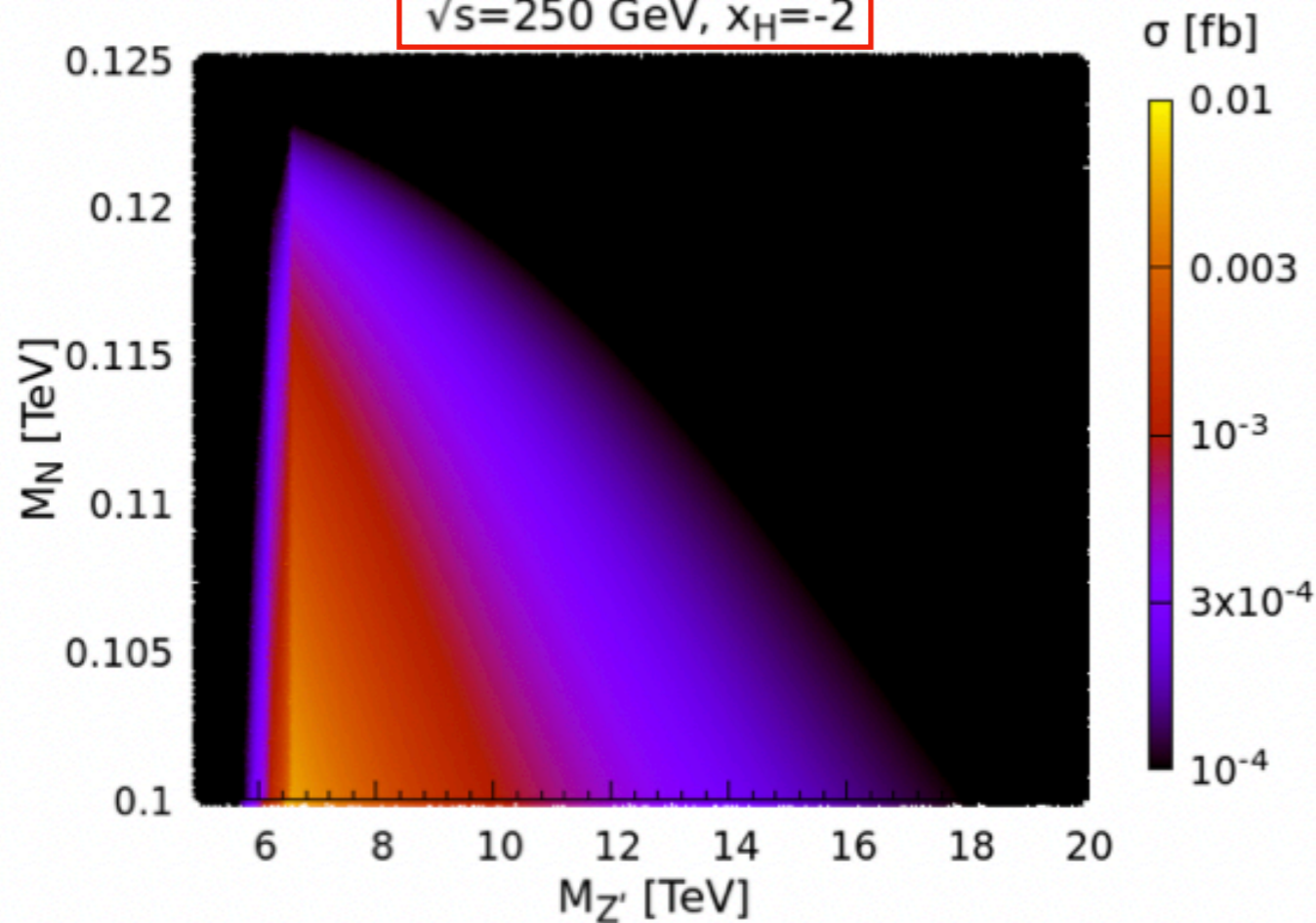
RHN pair production at the ILC from Z' : SSDL plus four jet mode

$$\sigma(e^-e^+ \rightarrow Z'^* \rightarrow N_i N_i) \simeq \left(\frac{g'^4}{M_{Z'}^4} \right) \frac{Q_N^2 s (8 + 12x_H + 5x_H^2)}{192\pi} \left(1 - 4 \frac{M_N^2}{s} \right)^{\frac{3}{2}}$$

2202.13358

SSDL production cross section

$\sqrt{s}=250 \text{ GeV}, x_H=-2$

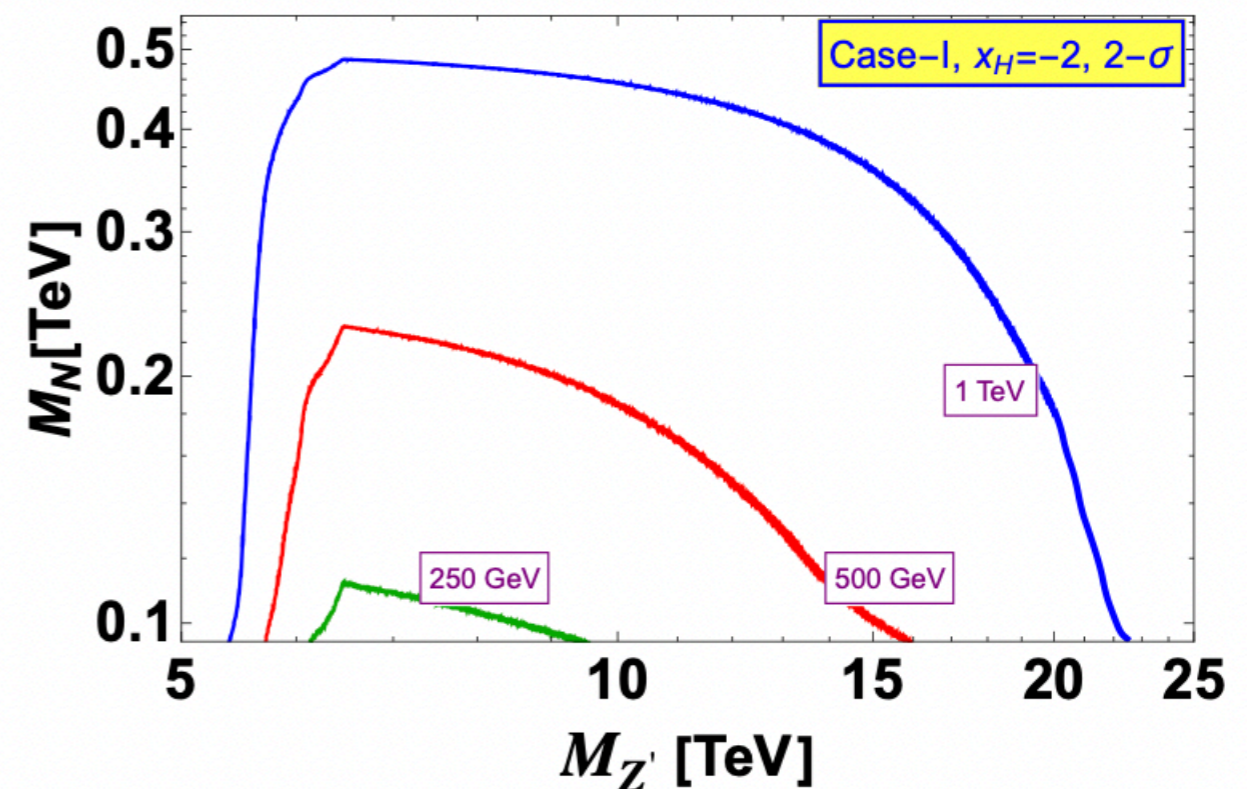


Studying signal and backgrounds

$WW, 4Z, ZZ, t\bar{t}$, etc .

Applying kinematic cuts

demanding SSDL with third lepton veto
and isolated leptons



Summary

We study the models with the heavy fermions under the simple extensions of the SM where the neutrino mass is generated by the seesaw mechanism at the tree level to reproduce the neutrino oscillation data.

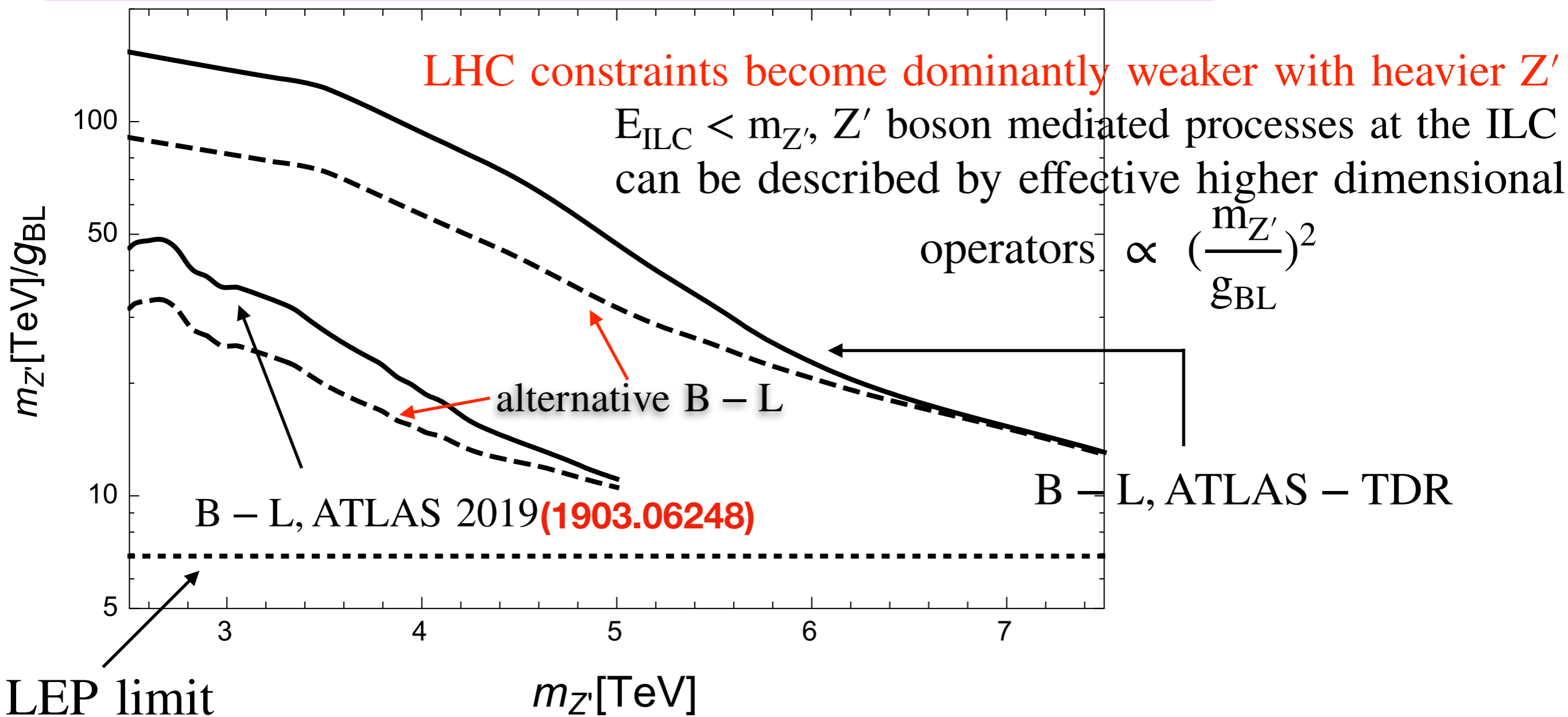
Stay tuned . . .



Thank You

We find that such heavy fermions can be tested at the underground experiments- at the proton-proton, electron-positron and electron-proton colliders in the near future. We have calculated the bounds on the light-heavy mixings for the electron-positron collider which could be probed in the near future.

Back – up slides

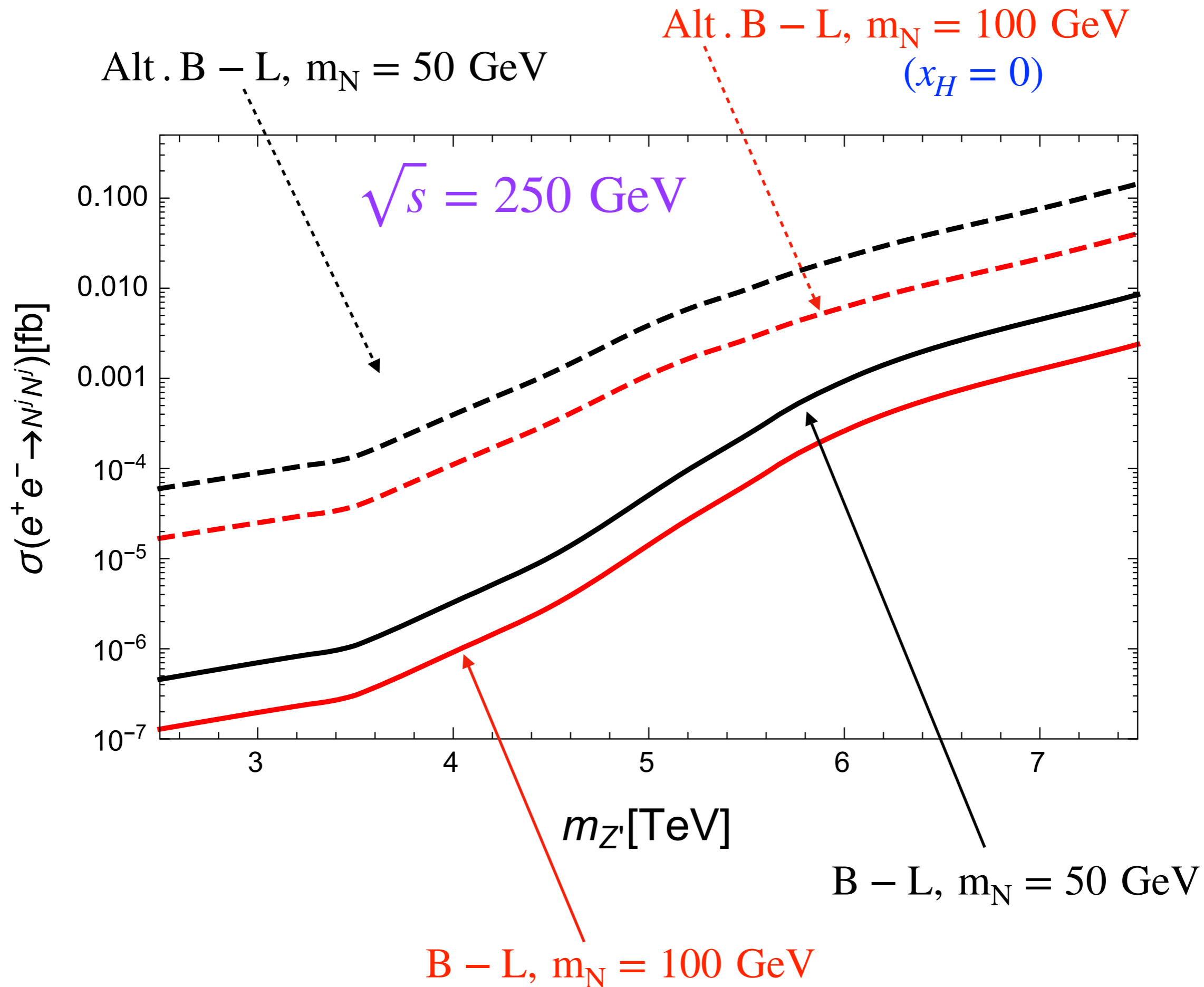


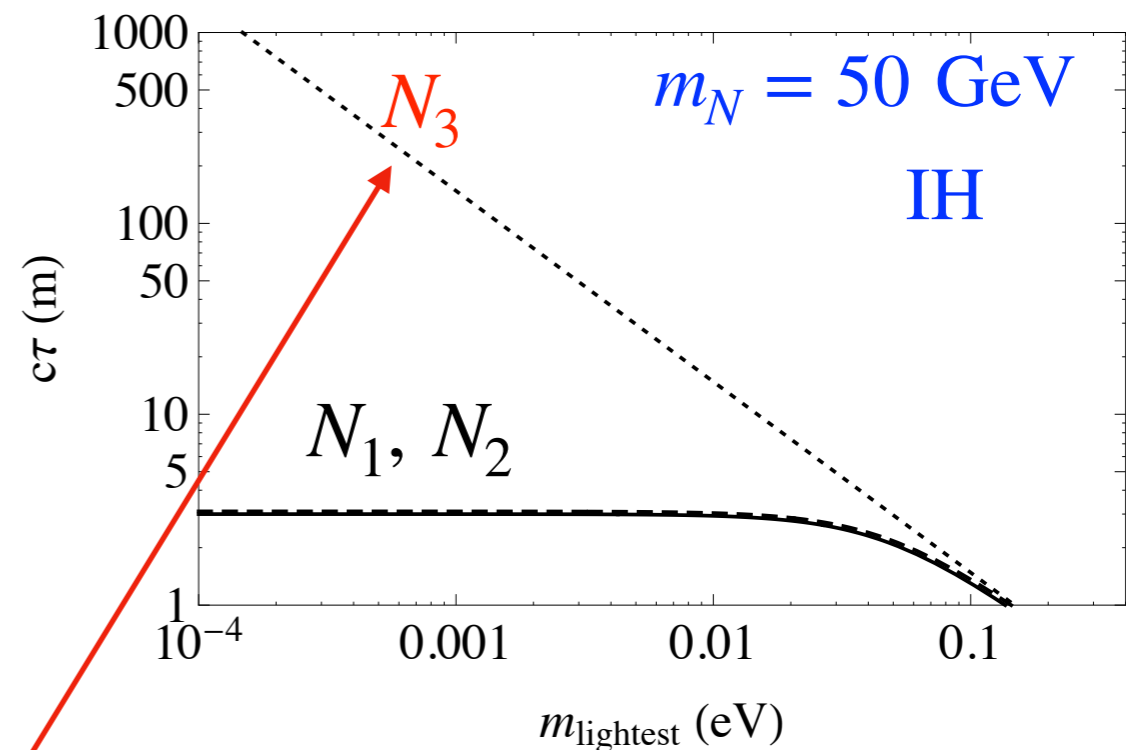
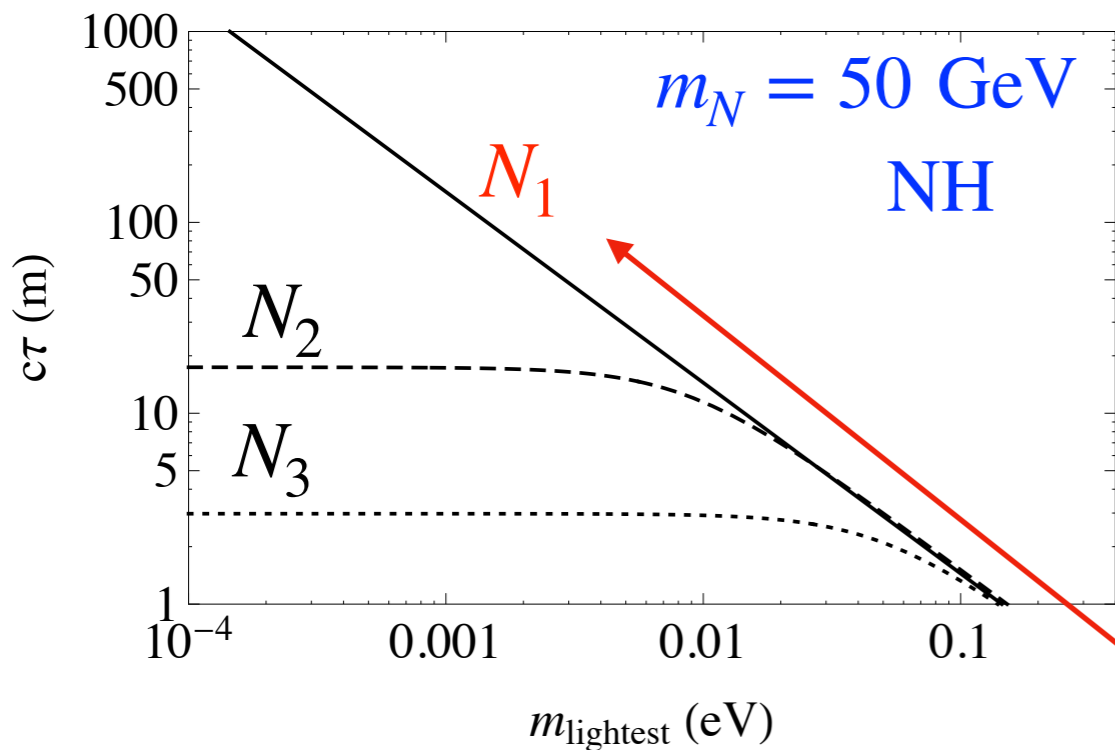
Dashed lines represent the Atl. B - L case

As a result ILC is a powerful machine to probe Z' beyond HL - LHC

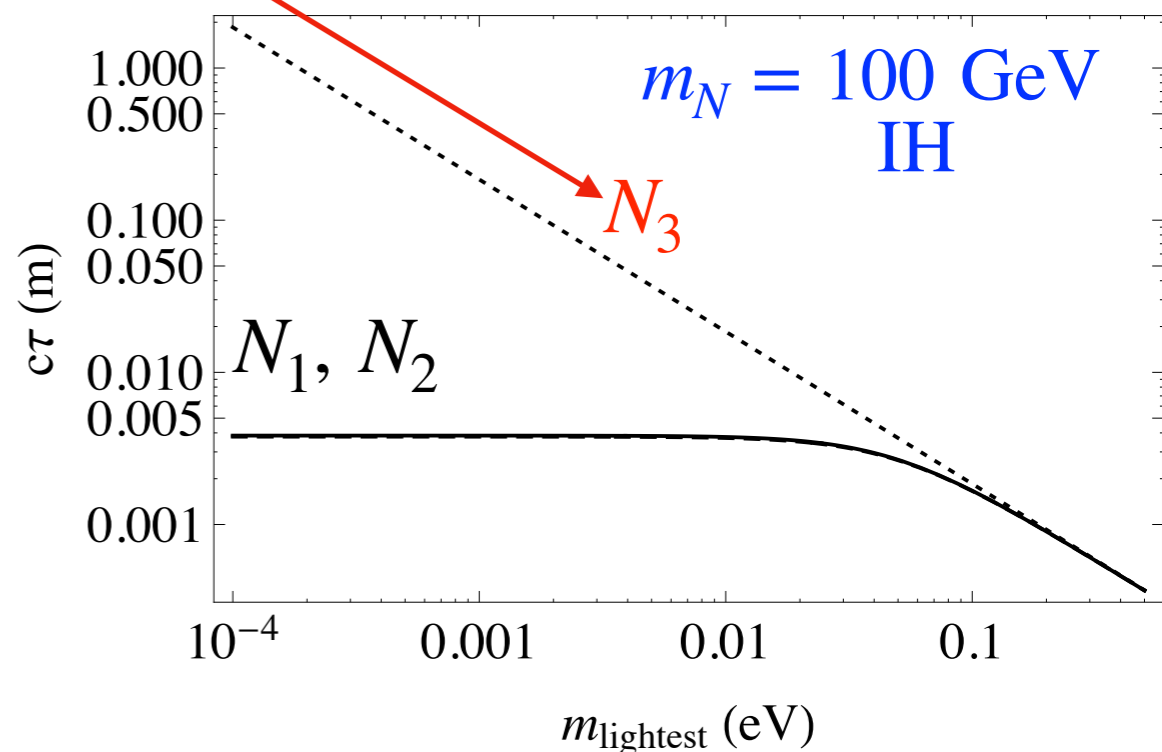
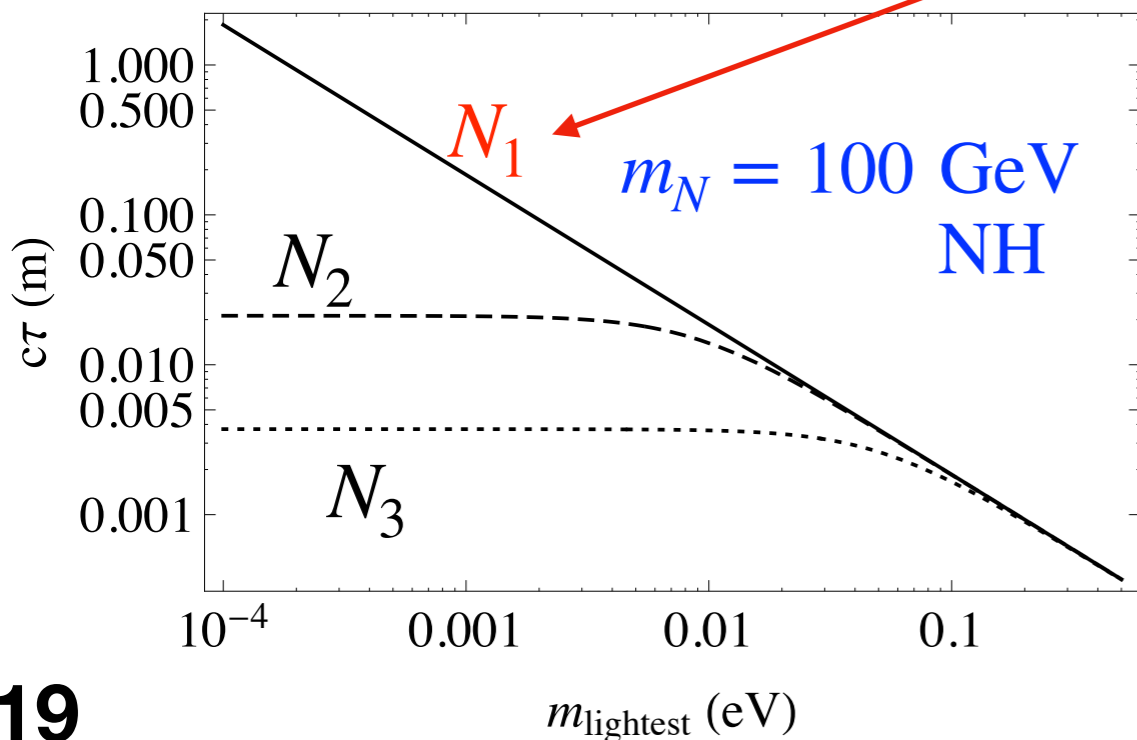
$$\sigma(e^+e^- \rightarrow Z'^* \rightarrow N^i N^i)$$

$$\simeq \frac{(Q_{Ni})^2}{24\pi} s \left(\frac{g_{BL}}{m_{Z'}}\right)^4 \left(1 - \frac{4m_{Ni}^2}{m_{Z'}^2}\right)^{\frac{3}{2}}$$





Longest lived RHN life time is inversely proportional to m_{lightest}
 $m_{\text{lightest}} \rightarrow 0$ leads to the long lived species as a potential DM candidate



Type – III seesaw

SM + SU(2)_L triplet fermion

Franceschini, Hambye, Strumia Biggio, Bonnet
 Biggio, Fernandez Martinez, Hernandez Garcia, Lopez Pavon
 AD, Mandal, Modak 2005.02267 AD, Mandal 2006.04123

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \text{Tr}(\bar{\Psi} i \gamma^\mu D_\mu \Psi) - \frac{1}{2} M \text{Tr}(\bar{\Psi} \Psi^c + \bar{\Psi}^c \Psi) - \sqrt{2}(\bar{\ell}_L Y_D^\dagger \Psi H + H^\dagger \bar{\Psi} Y_D \ell_L)$$

$$\Psi = \begin{pmatrix} \Sigma^0/\sqrt{2} & \Sigma^+ \\ \Sigma^- & -\Sigma^0/\sqrt{2} \end{pmatrix} \text{ and } \Psi^c = \begin{pmatrix} \Sigma^{0c}/\sqrt{2} & \Sigma^{-c} \\ \Sigma^{+c} & -\Sigma^{0c}/\sqrt{2} \end{pmatrix}$$

$$-\mathcal{L}_{\text{mass}} = (\bar{e}_L \ \bar{\Sigma}_L) \begin{pmatrix} m_e & Y_D^\dagger v \\ 0 & M \end{pmatrix} \begin{pmatrix} e_R \\ \Sigma_R \end{pmatrix} + \frac{1}{2} (\bar{\nu}_L^c \ \bar{\Sigma}_R^0) \begin{pmatrix} 0 & Y_D^T \frac{v}{\sqrt{2}} \\ Y_D \frac{v}{\sqrt{2}} & M \end{pmatrix} \begin{pmatrix} \nu_L \\ \Sigma_R^{0c} \end{pmatrix} + h.c. \quad \boxed{m_\nu \simeq -\frac{v^2}{2} Y_D^T M^{-1} Y_D = M_D M^{-1} M_D^T}$$

$$\Gamma(\Sigma^\pm \rightarrow \nu W) = \frac{g^2 |V_{\ell\Sigma}|^2}{32\pi} \left(\frac{M^3}{M_W^2}\right) \left(1 - \frac{M_W^2}{M^2}\right)^2 \left(1 + 2\frac{M_W^2}{M^2}\right)$$

$$\Gamma(\Sigma^\pm \rightarrow \ell Z) = \frac{g^2 |V_{\ell\Sigma}|^2}{64\pi \cos^2 \theta_W} \left(\frac{M^3}{M_Z^2}\right) \left(1 - \frac{M_Z^2}{M^2}\right)^2 \left(1 + 2\frac{M_Z^2}{M^2}\right)$$

$$\Gamma(\Sigma^\pm \rightarrow \ell h) = \frac{g^2 |V_{\ell\Sigma}|^2}{64\pi} \left(\frac{M^3}{M_W^2}\right) \left(1 - \frac{M_h^2}{M^2}\right)^2,$$

$$\Gamma(\Sigma^\pm \rightarrow \Sigma^0 \pi^\pm) = \frac{2G_F^2 V_{ud}^2 \Delta M^3 f_\pi^2}{\pi} \sqrt{1 - \frac{m_\pi^2}{\Delta M^2}}$$

$$\Gamma(\Sigma^\pm \rightarrow \Sigma^0 e \nu_e) = \frac{2G_F^2 \Delta M^5}{15\pi}$$

$$\Gamma(\Sigma^\pm \rightarrow \Sigma^0 \mu \nu_\mu) = 0.12 \Gamma(\Sigma^\pm \rightarrow \Sigma^0 e \nu_e)$$

$$\Gamma(\Sigma^0 \rightarrow \ell^+ W) = \Gamma(\Sigma^0 \rightarrow \ell^- W) = \frac{g^2 |V_{\ell\Sigma}|^2}{64\pi} \left(\frac{M^3}{M_W^2}\right) \left(1 - \frac{M_W^2}{M^2}\right)^2 \left(1 + 2\frac{M_W^2}{M^2}\right)$$

$$\Gamma(\Sigma^0 \rightarrow \nu Z) = \Gamma(\Sigma^0 \rightarrow \bar{\nu} Z) = \frac{g^2 |V_{\ell\Sigma}|^2}{128\pi \cos^2 \theta_W} \left(\frac{M^3}{M_Z^2}\right) \left(1 - \frac{M_Z^2}{M^2}\right)^2 \left(1 + 2\frac{M_Z^2}{M^2}\right)$$

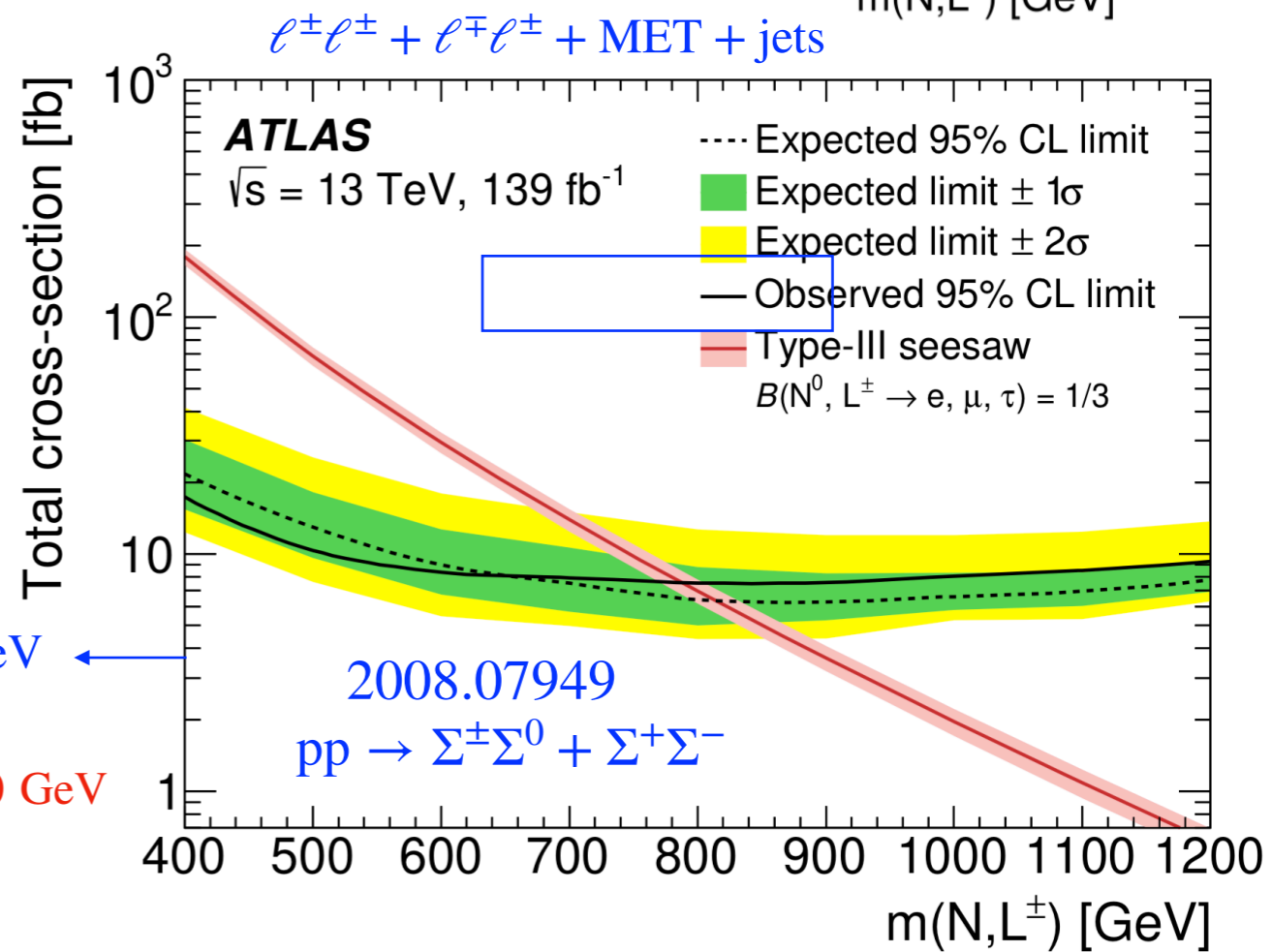
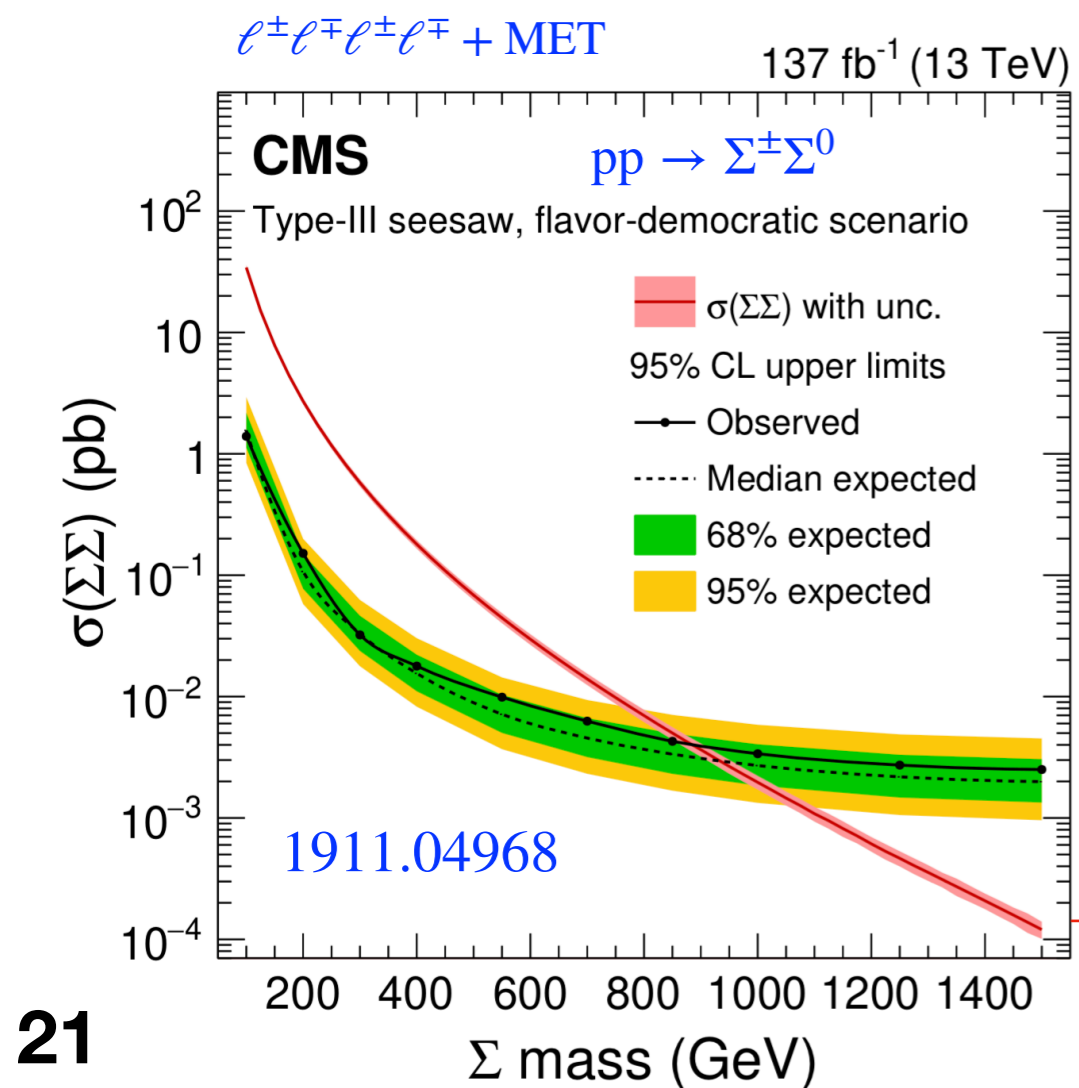
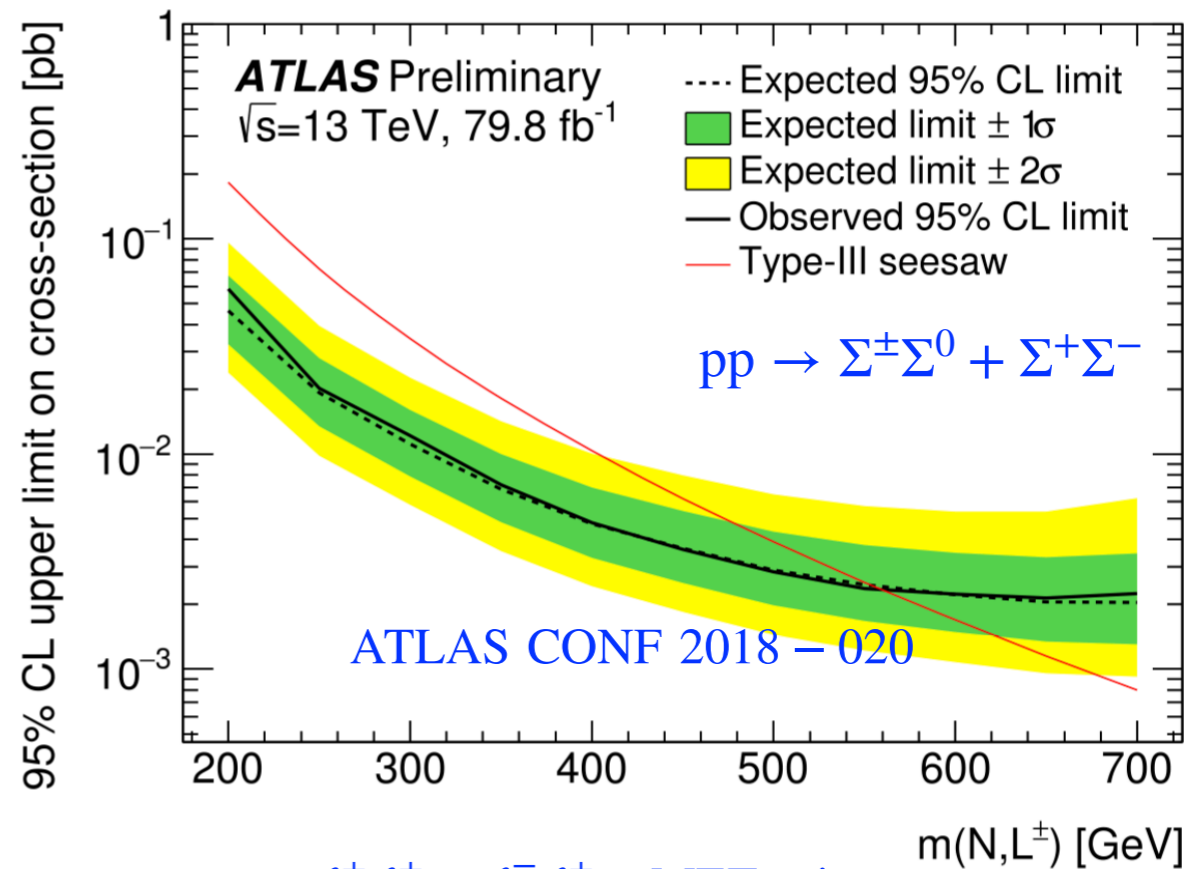
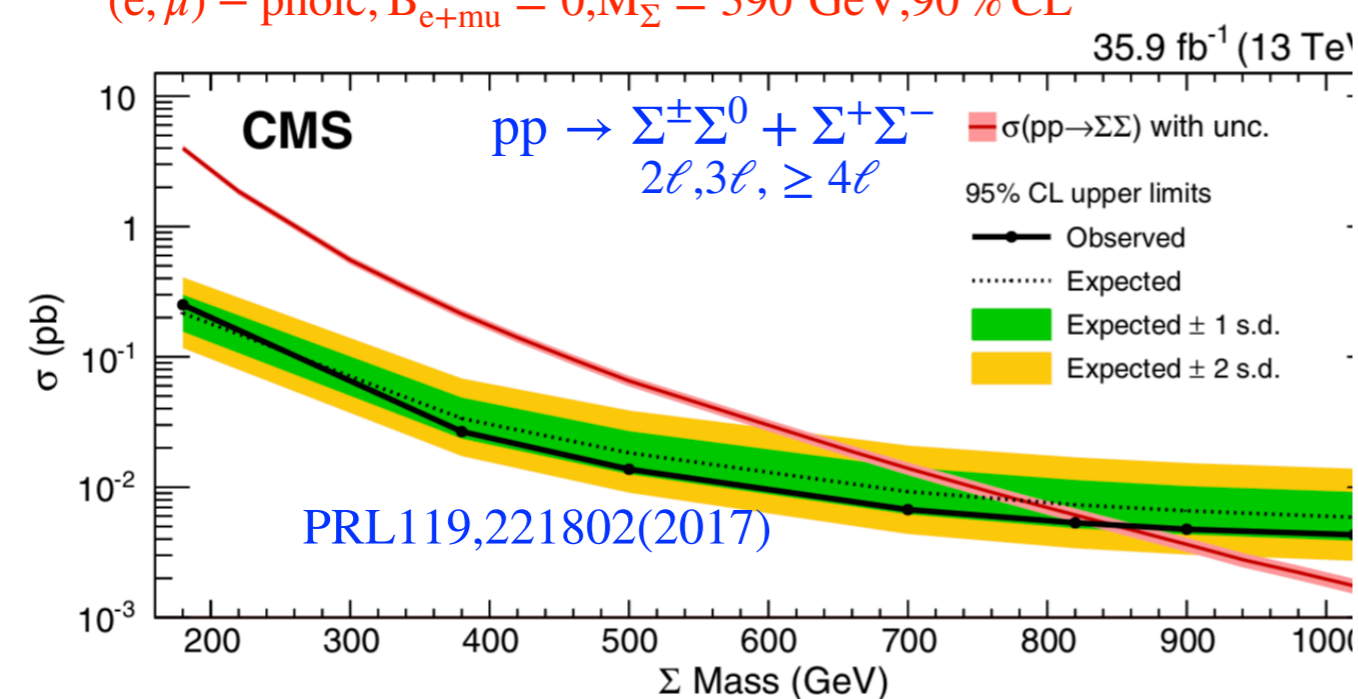
$$\Gamma(\Sigma^0 \rightarrow \nu h) = \Gamma(\Sigma^0 \rightarrow \bar{\nu} h) = \frac{g^2 |V_{\ell\Sigma}|^2}{128\pi} \left(\frac{M^3}{M_W^2}\right) \left(1 - \frac{M_h^2}{M^2}\right)^2,$$

LHC limits

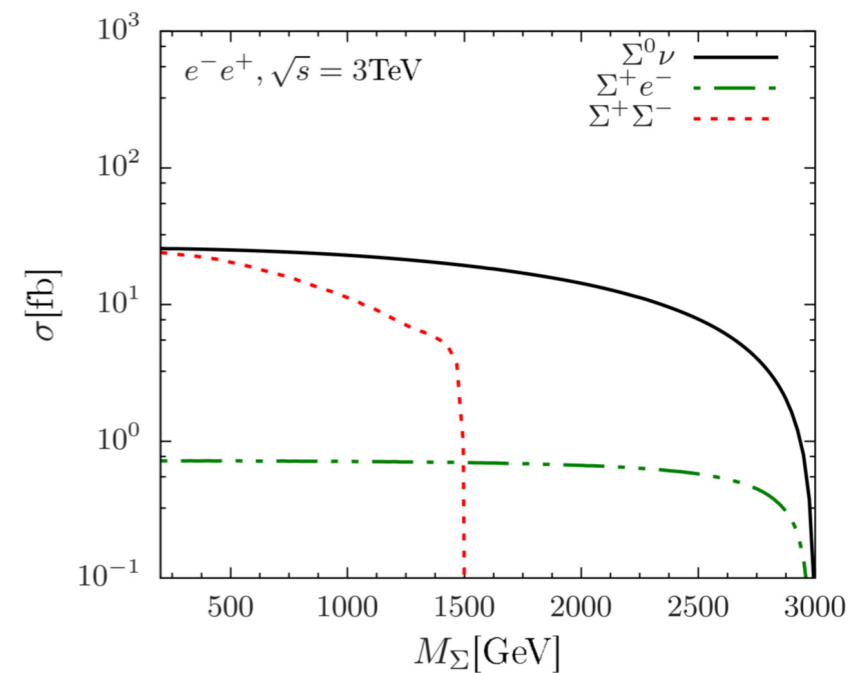
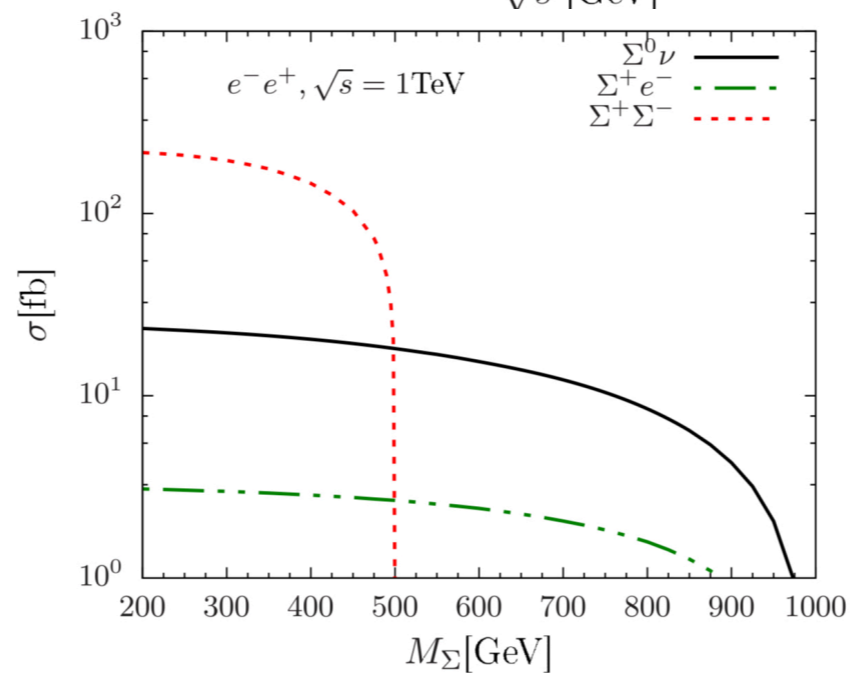
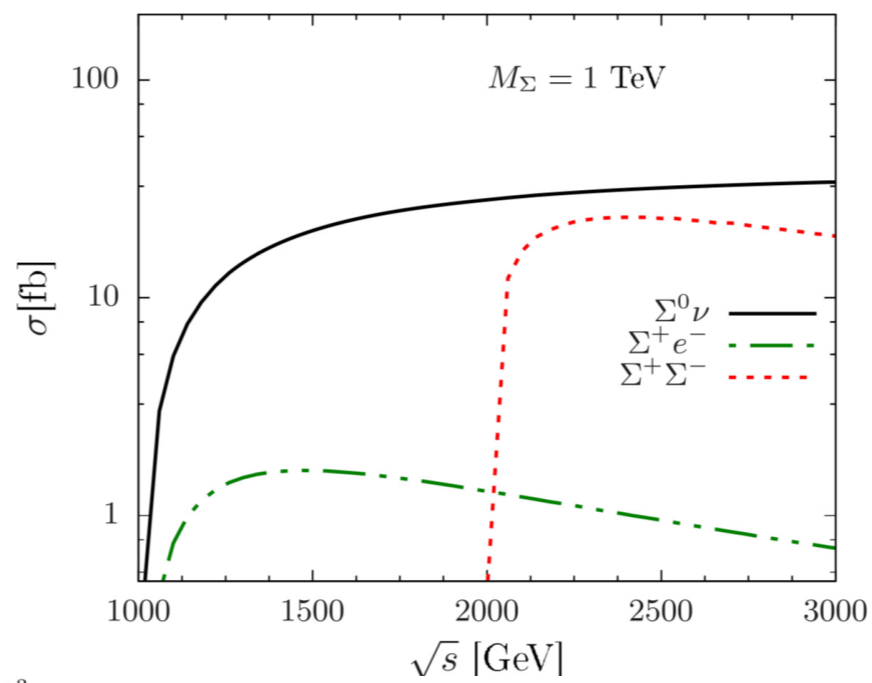
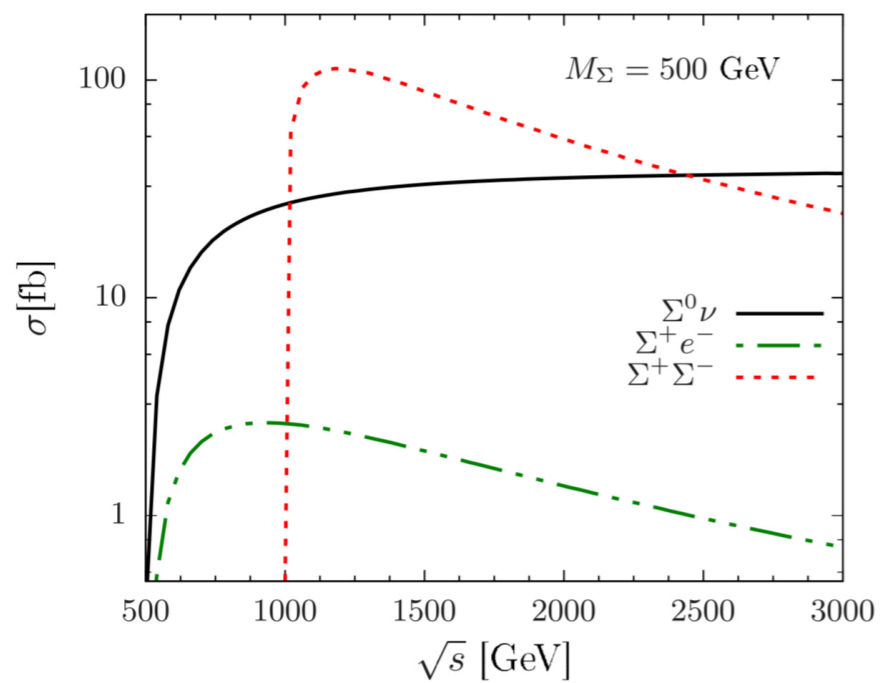
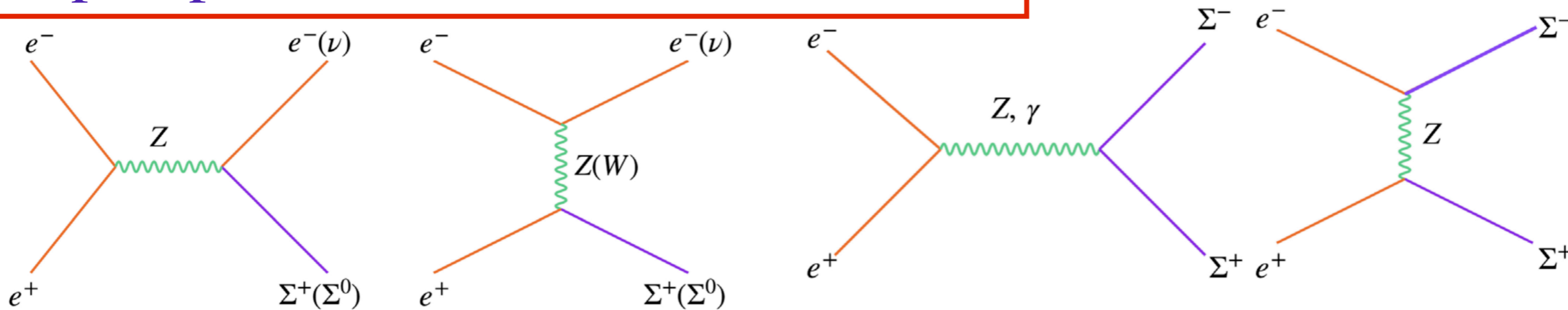
τ - phobic, $B_\tau = 0, M_\Sigma = 900$ GeV, 90% CL
 (e, μ) - phobic, $B_{e+\mu} = 0, M_\Sigma = 390$ GeV, 90% CL

$$BR = B_\ell \propto \frac{|V_\ell|^2}{|V_e|^2 + |V_\mu|^2 + |V_\tau|^2} \quad B_e = B_\mu = B_\tau$$

Flavor - democratic scenario

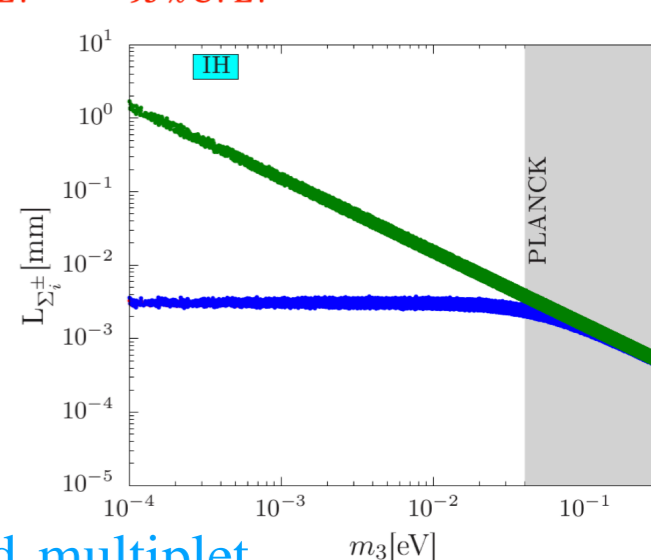
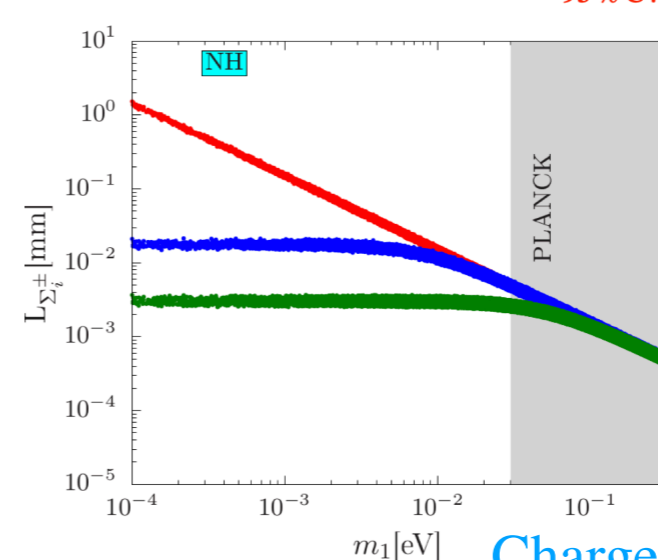
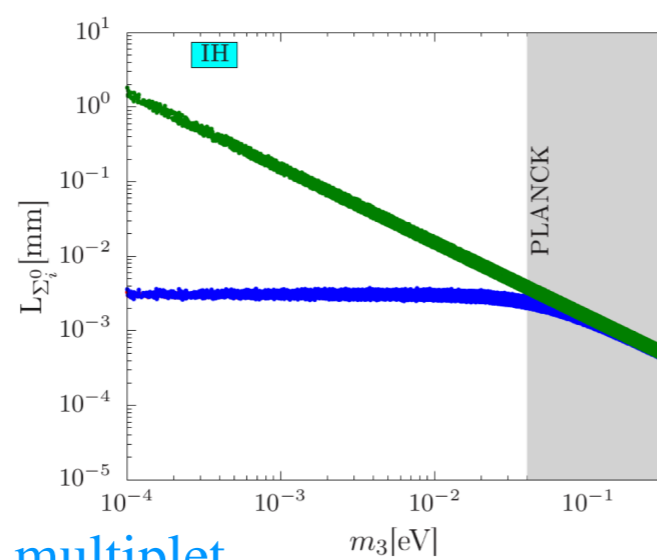
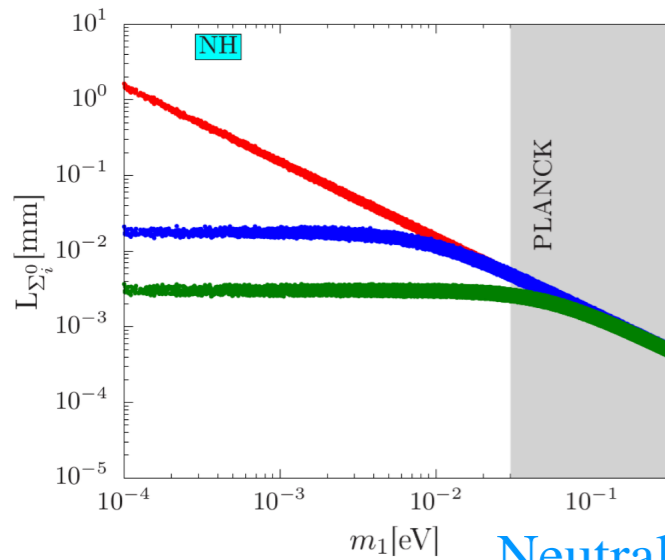
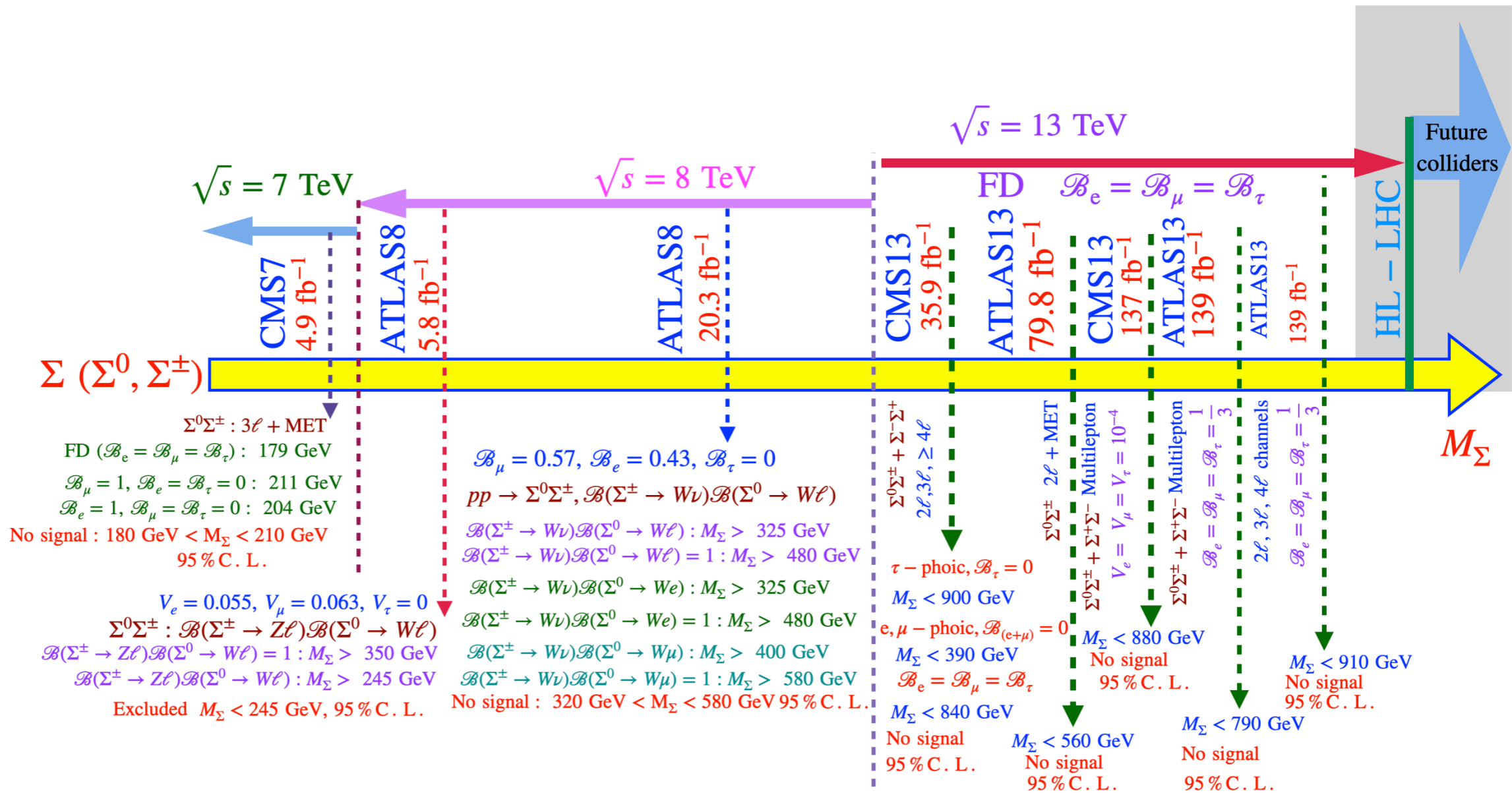


Triplet production at the e^-e^+ collider



Experimental limits from ATLAS and CMS on type – III seesaw

2006.04123

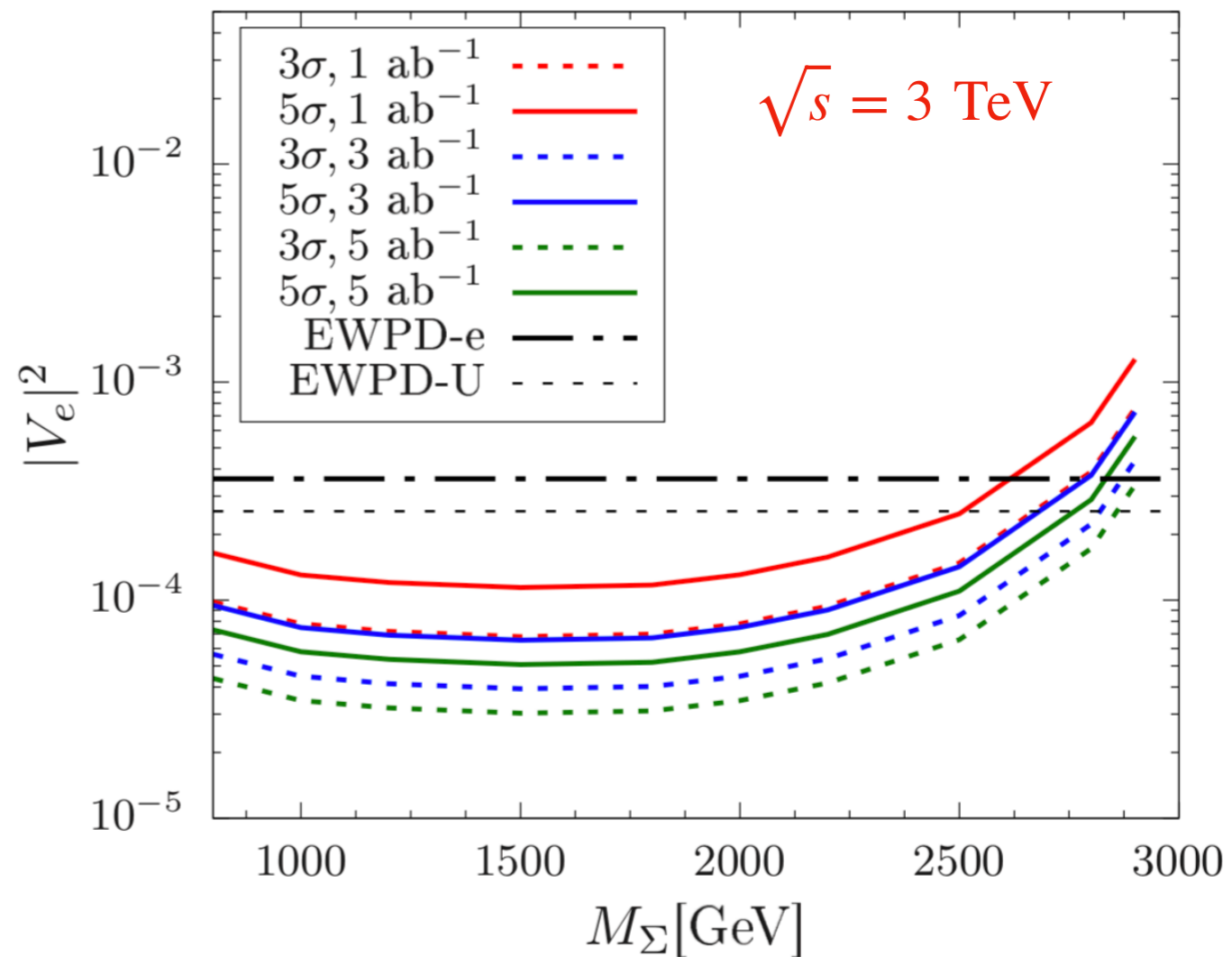
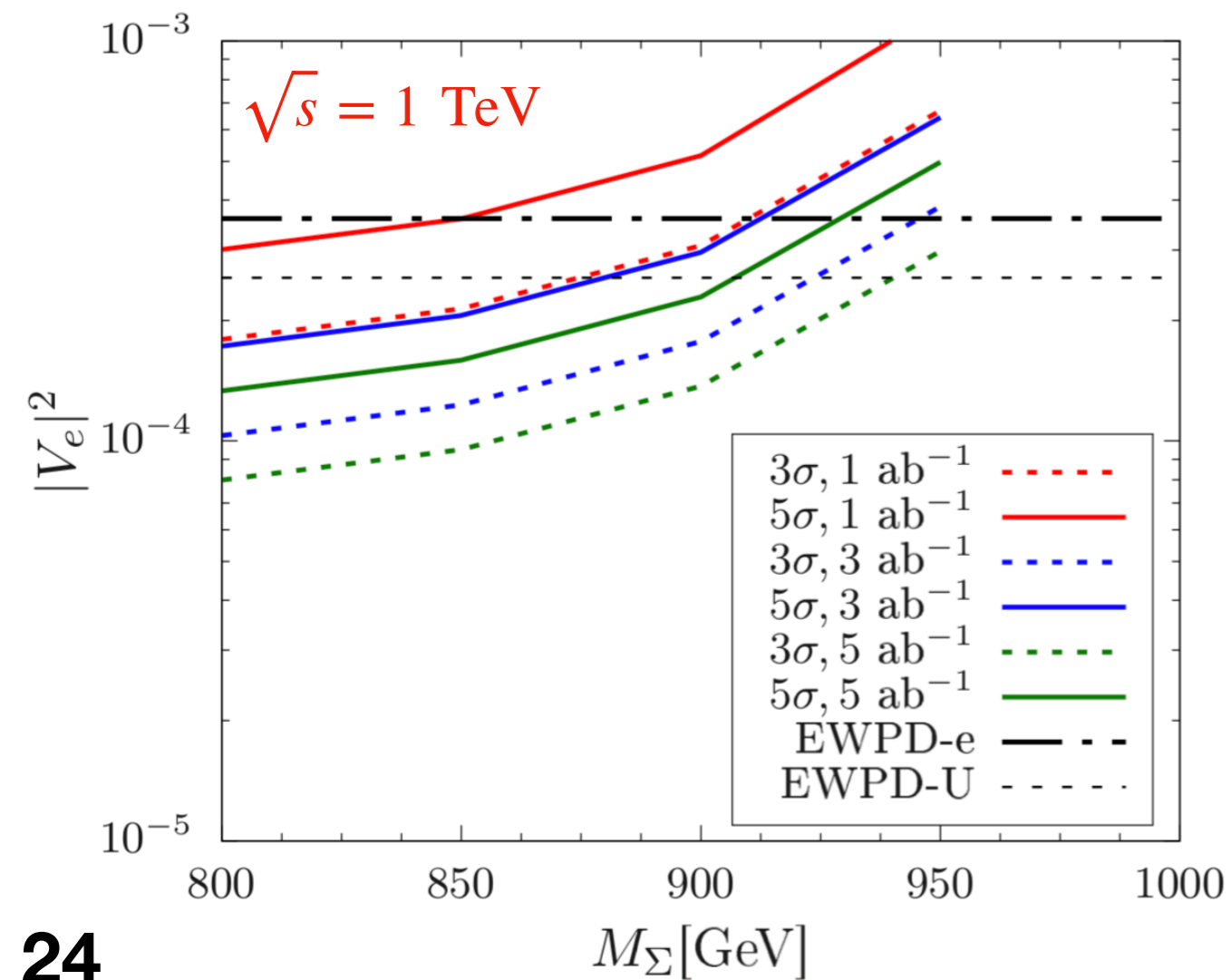
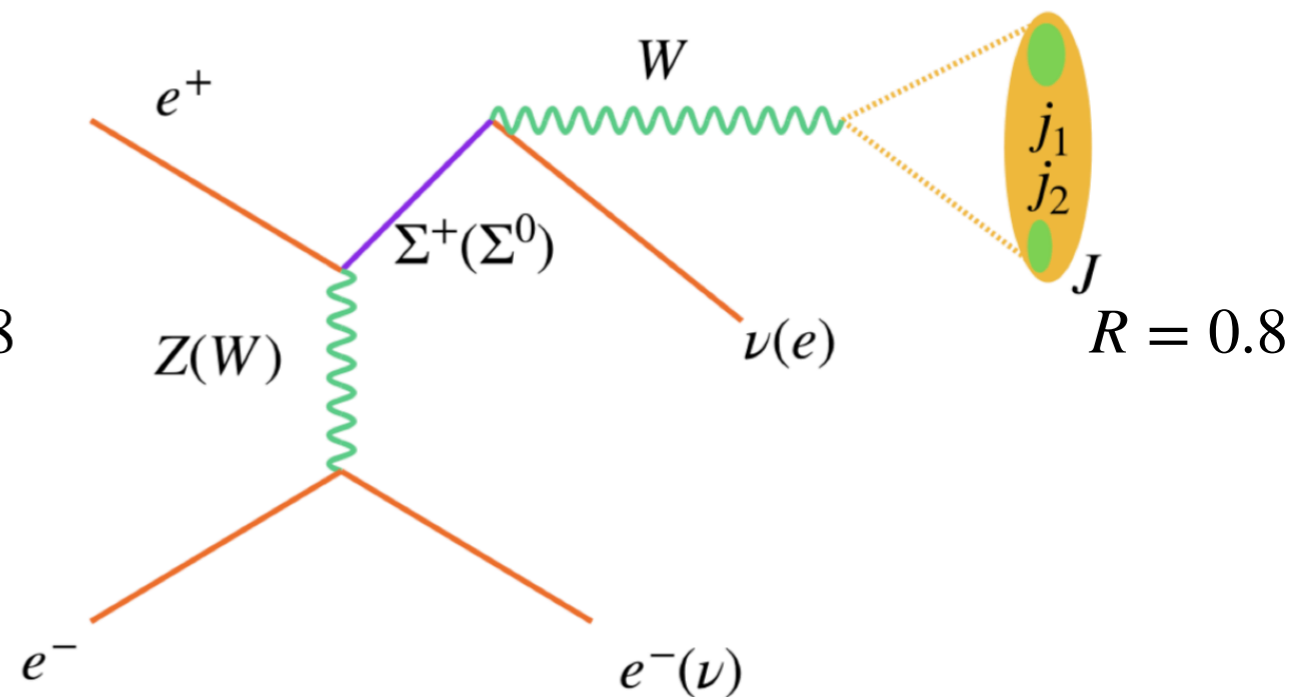
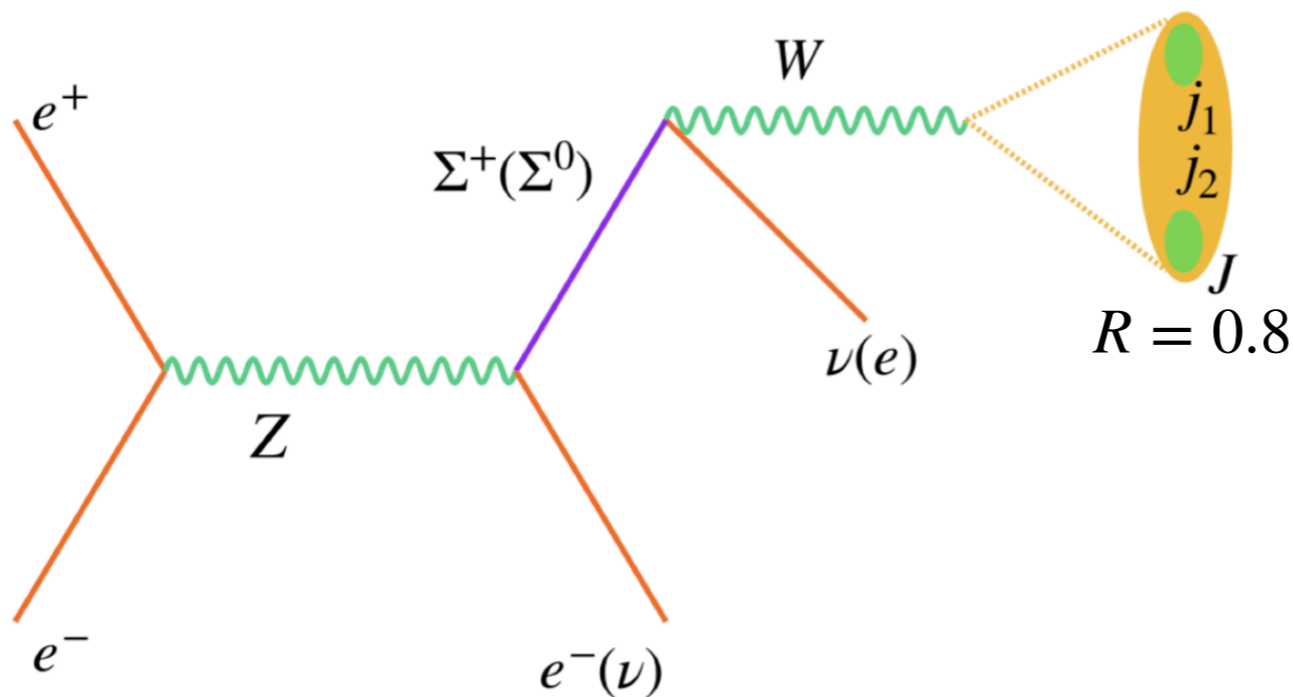


Neutral multiplet Lower in m_{lightest} increases L by (1 – 2) orders of magnitude upto a steady value.

Charged multiplet

Mass-mixing limit plots

2005.02267



Other interesting aspects at the ILC

Type – II scenario : SM + SU(2) triplet scalar : Charged scalar

1206.6278, 1811.03476, 1803.00677

Left – Right Seesaw using Beam Polarization at an e^+e^- Collider : 1701.08751 W_R

Seesaw mechanism at the 250 GeV ILC : 1812.11931 Z'

1. Test of BSM gauge mediated processes

Asymmetries

2. Pair – production of heavy neutrinos

Prompt, Displaced/ LLP study

Effect of polarization

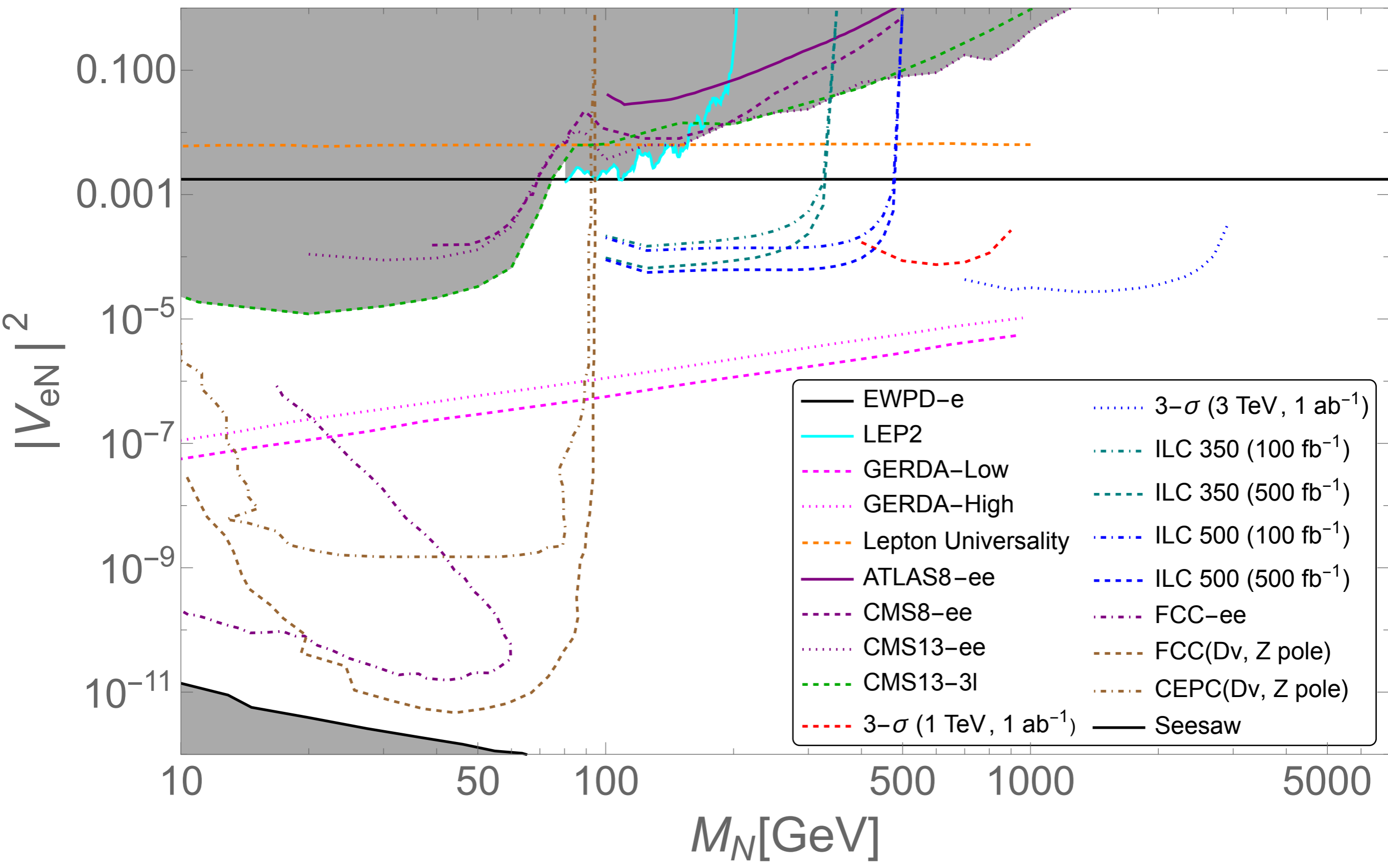
3. Beam dump, Forward Physics Facility

4. BSM scalar : Light/ Heavy, mixing with SM scalar

5. Prospect of $e - \gamma$ scattering

Existing and prospective bounds on $|V_{eN}|^2$

(Incomplete)



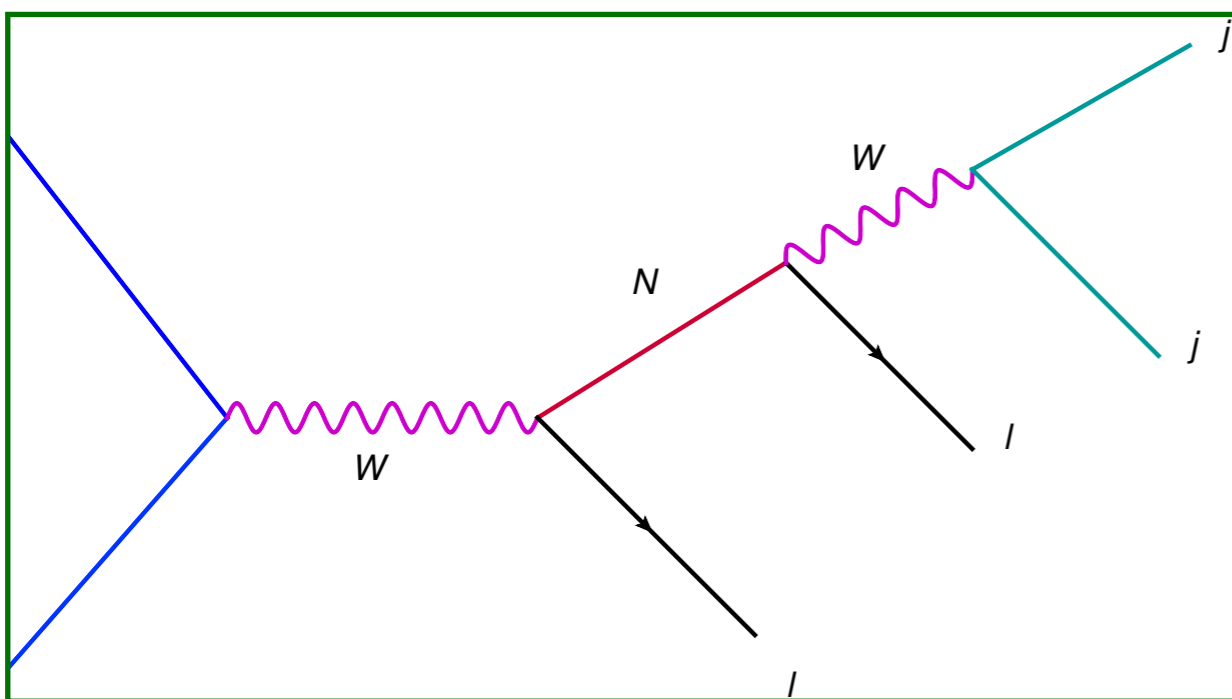
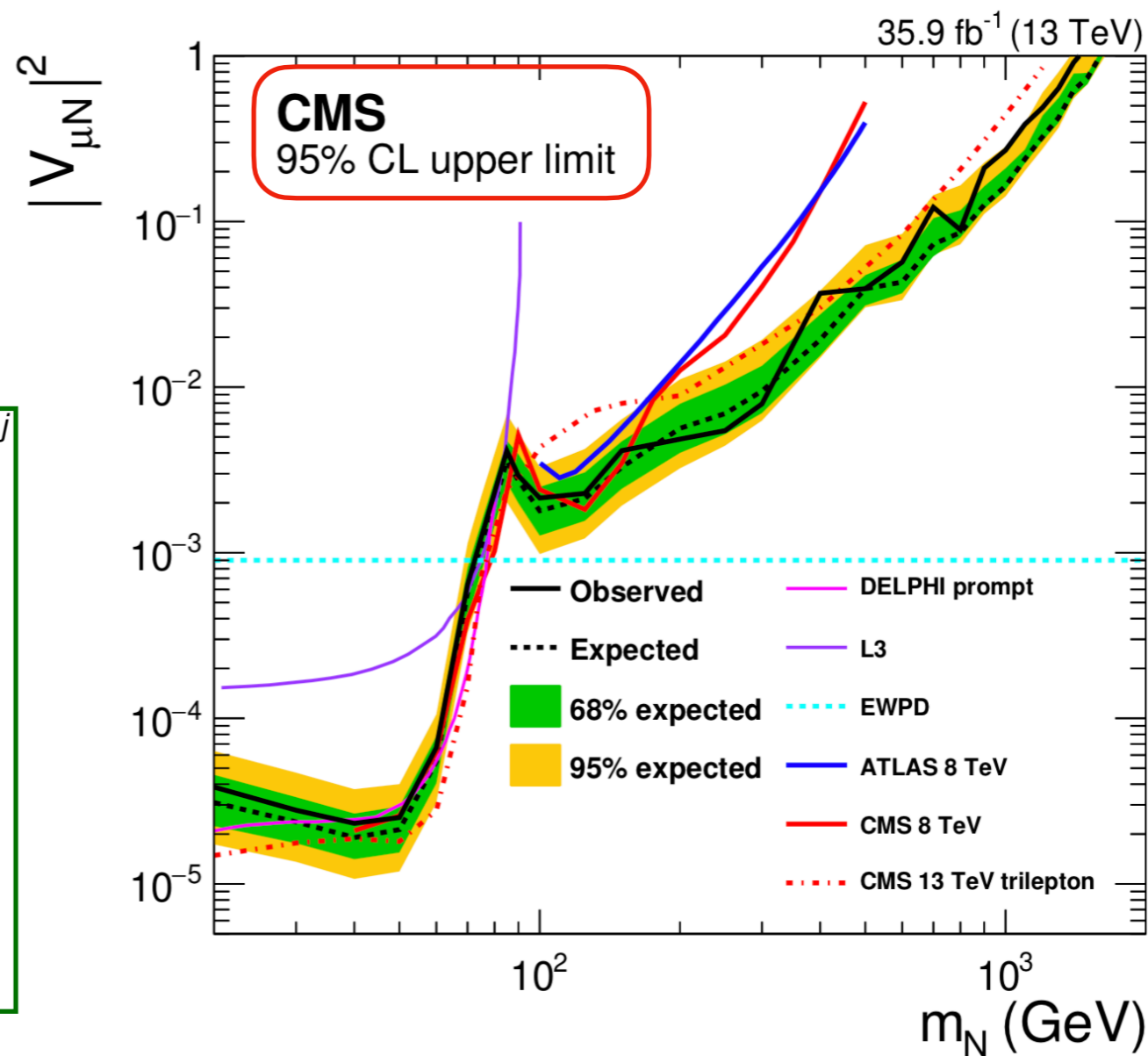
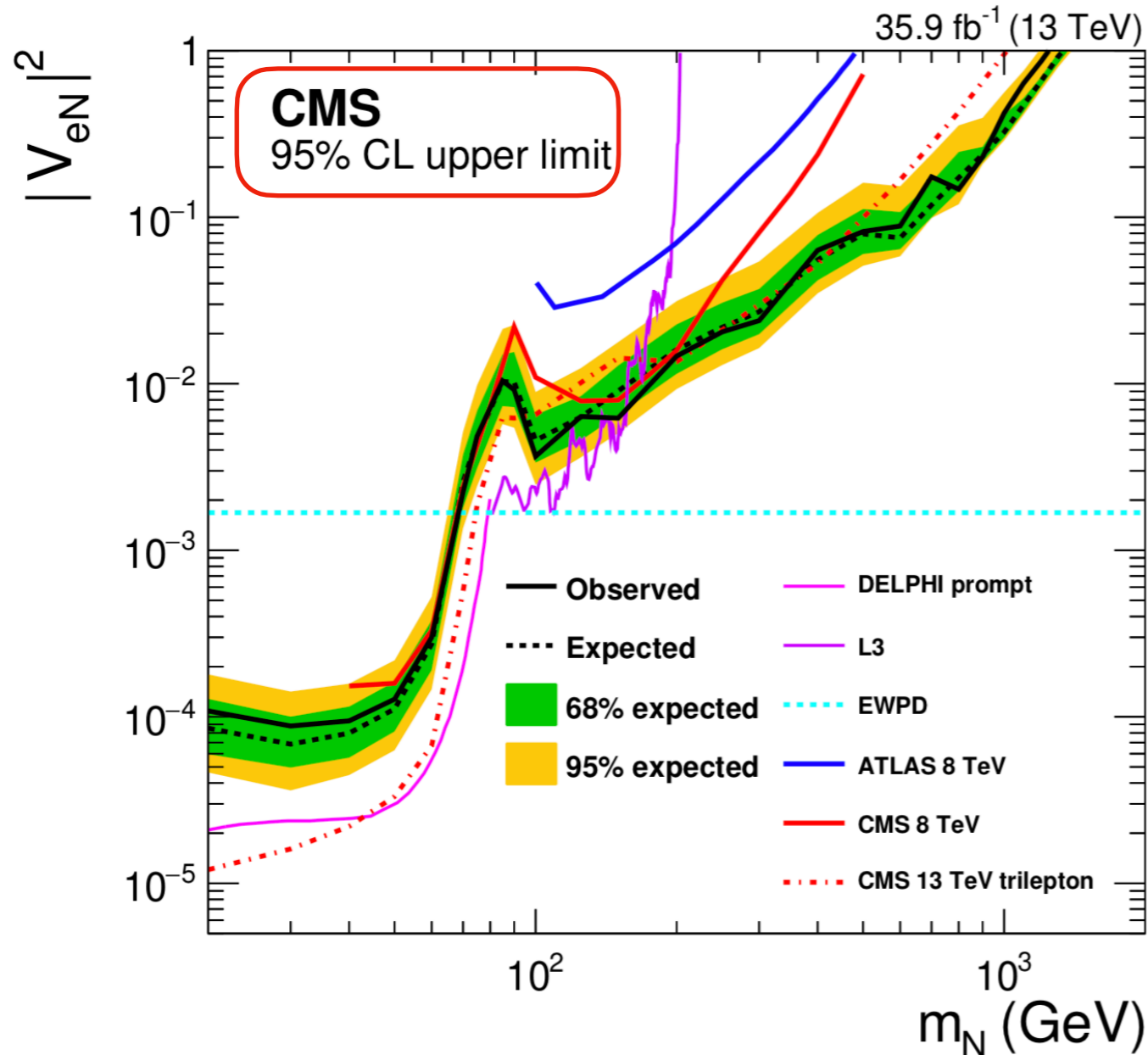
References : 1512.06035, 1604.02420, 1612.02728, 1702.04668, 1810.08970

Experimental limits

$\ell^{\pm}\ell^{\pm} + \text{jets}$

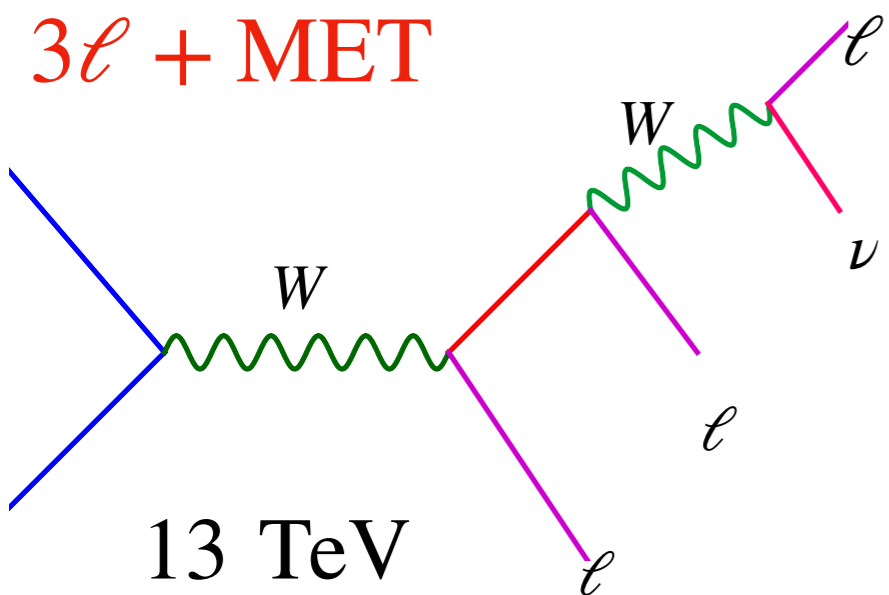
CMS

1806.10905 13 TeV, 35.9 fb⁻¹



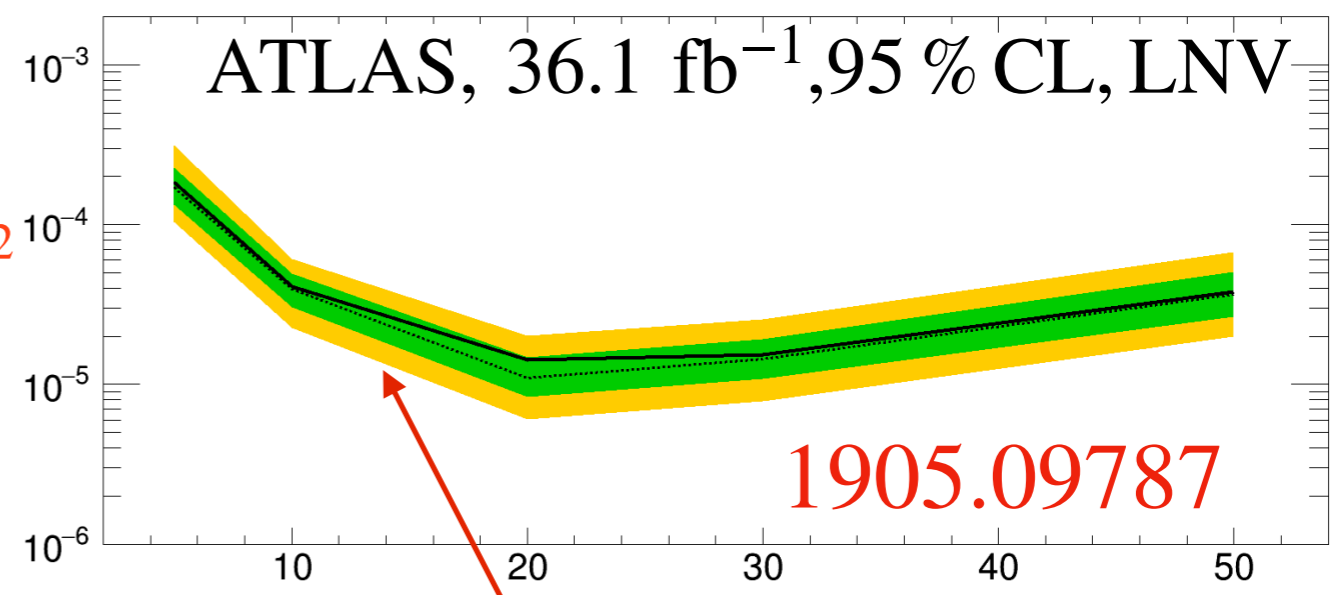
Experimental limits

$3\ell + \text{MET}$



13 TeV

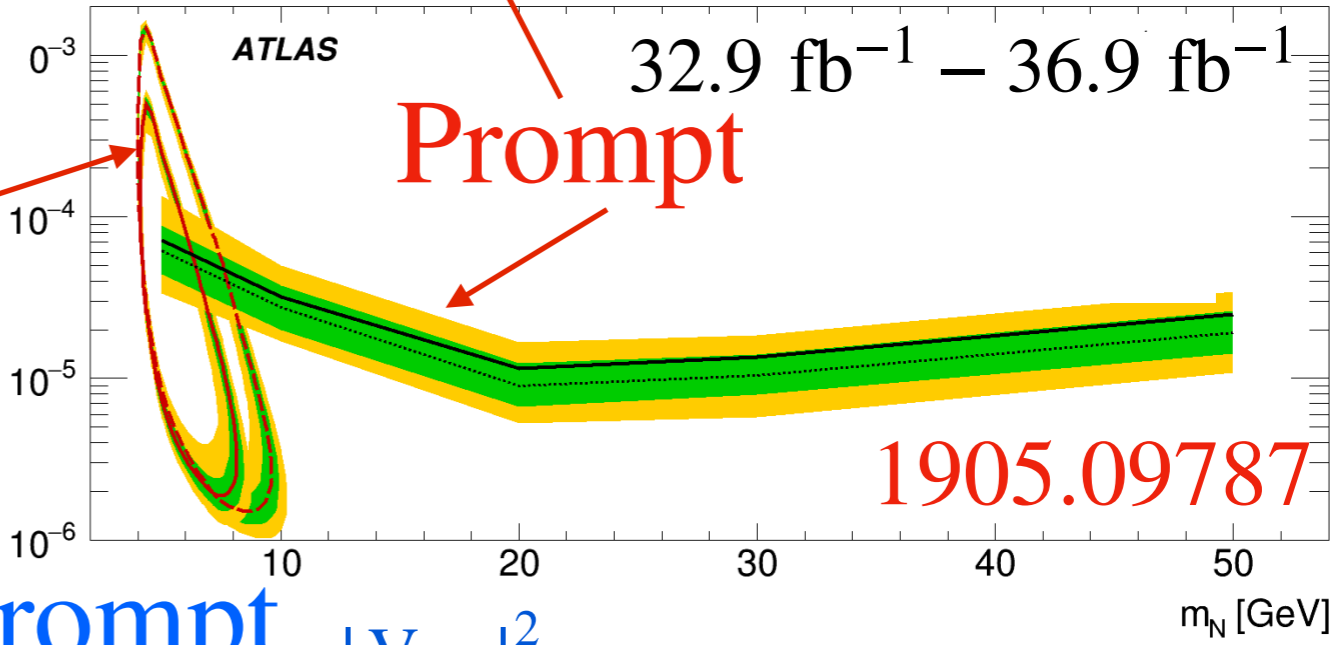
$|V_{eN}|^2$



Displaced

— LNV
- - - LNC

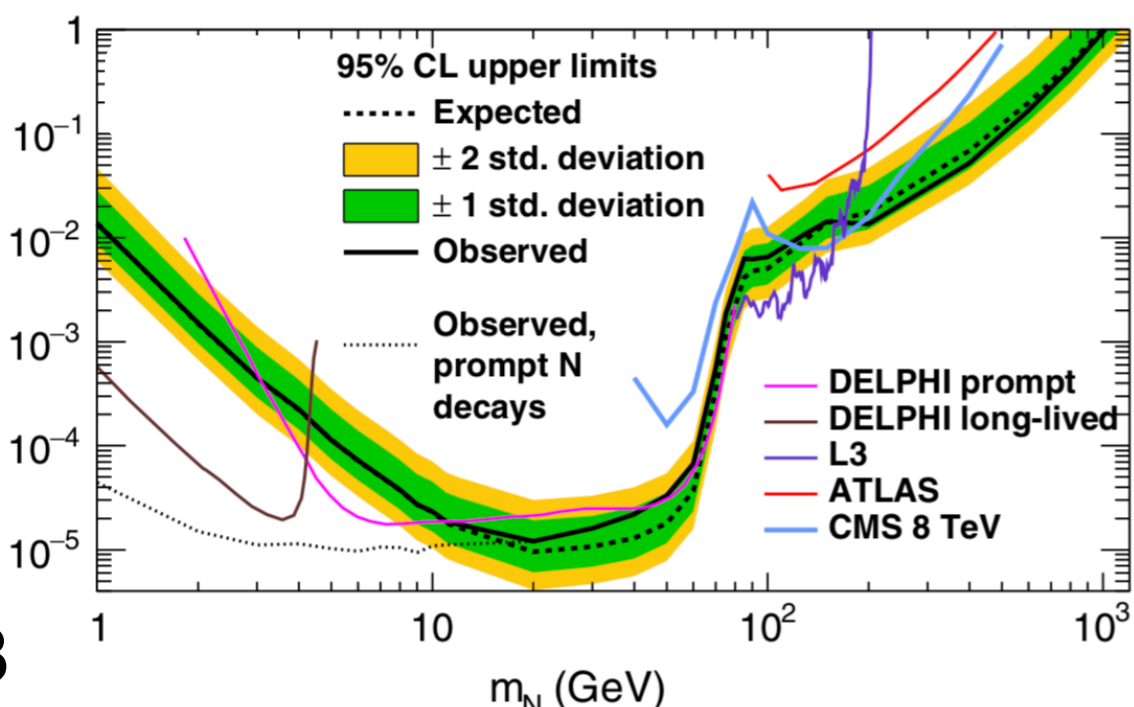
$|V_{\mu N}|^2$



$|V_{eN}|^2$

Prompt

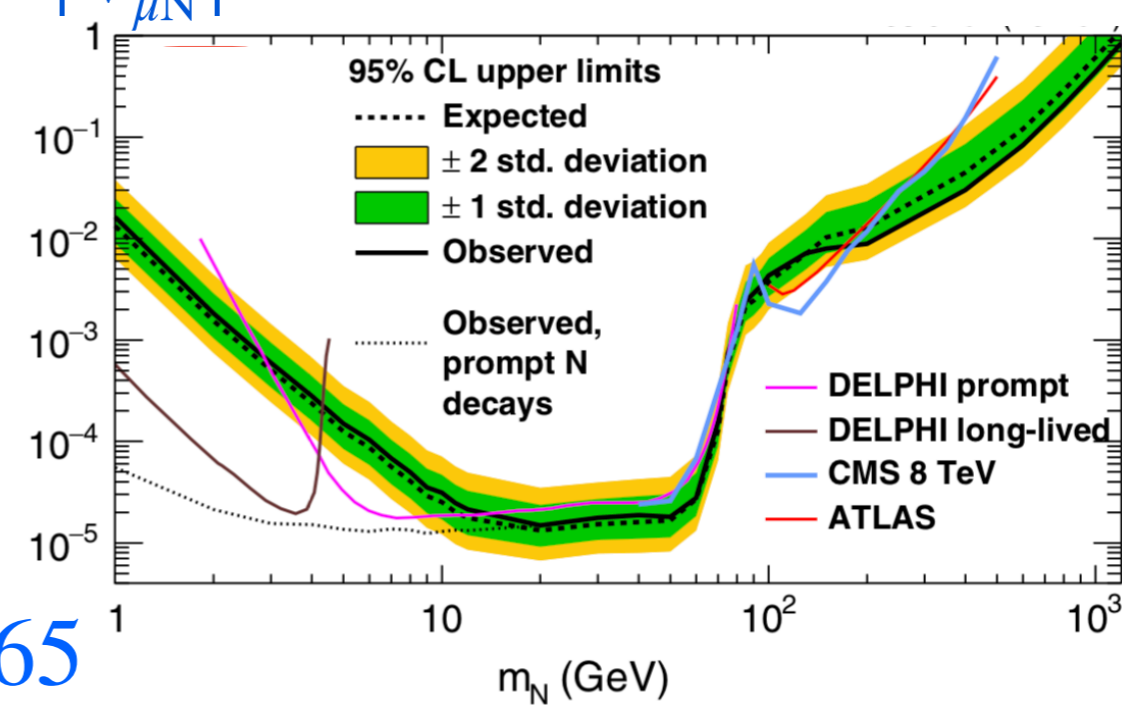
$|V_{\mu N}|^2$



CMS

35.9 fb^{-1}

1802.02965



Long – lived HNL searches at CMS

Trilpton mode : $pp \rightarrow N\ell, N \rightarrow \ell W, W \rightarrow \ell\nu$
 $pp \rightarrow N\ell, N \rightarrow \nu Z, Z \rightarrow \ell\ell$

2201.05578

