

# The search for Leptophilic DM and muon $g-2$ at future lepton colliders

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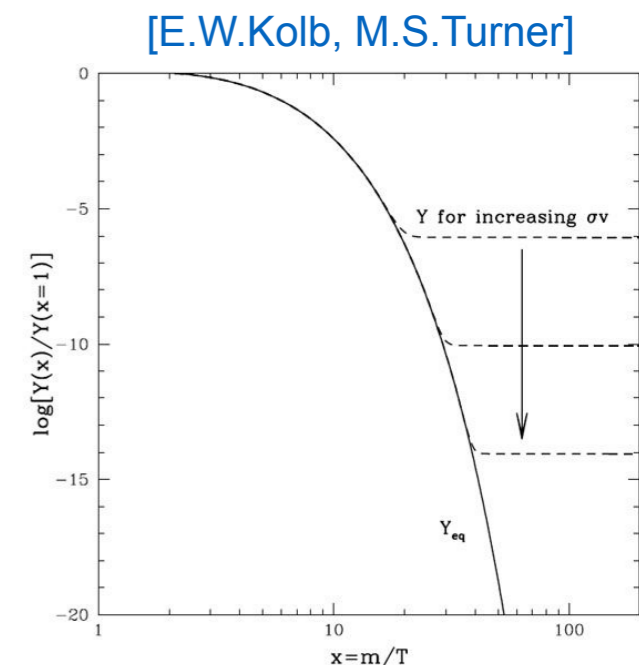
# Contents

- Introduction of WIMP
- Our model and motivation
- Current constraints on the model
- Future prospect for the model
- Contribution to muon  $g-2$
- Summary

# WIMP

- Weakly Interacting Massive Particle (WIMP)
- Well motivated DM candidate  
(by many BSM models like SUSY)
- Thermally created in the early universe
- The abundance is determined by freeze-out mechanism
- Number density follows Boltzmann-eq

$$\frac{dn}{dt} + 3Hn = \langle \sigma v \rangle (n_{\text{eq}}^2 - n^2)$$



# WIMP model

- Classifying WIMP by the representation of SM gauge group

Lorentz	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$
scalar		<b>1</b>	0
or		<b>2</b>	$-1/2, +1/2$
fermion	<b>1</b>	<b>3</b>	$-1, 0, +1$
or		<b>4</b>	$-3/2, -1/2, +1/2, +3/2$
vector		<b>5</b>	$-2, -1, 0, +1, +2$
		$\vdots$	$\vdots$

- $U(1)$  is quantized because WIMP must be electrically neutral

# WIMP model

- Classifying WIMP by the representation of gauge group

Lorentz	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$
scalar		1	0
or fermion	1	2	$-1/2, +1/2$
or vector		3	$-1, 0, +1$
		4	$-3/2, -1/2, +1/2, +3/2$
		5	$-2, -1, 0, +1, +2$
		$\vdots$	$\vdots$

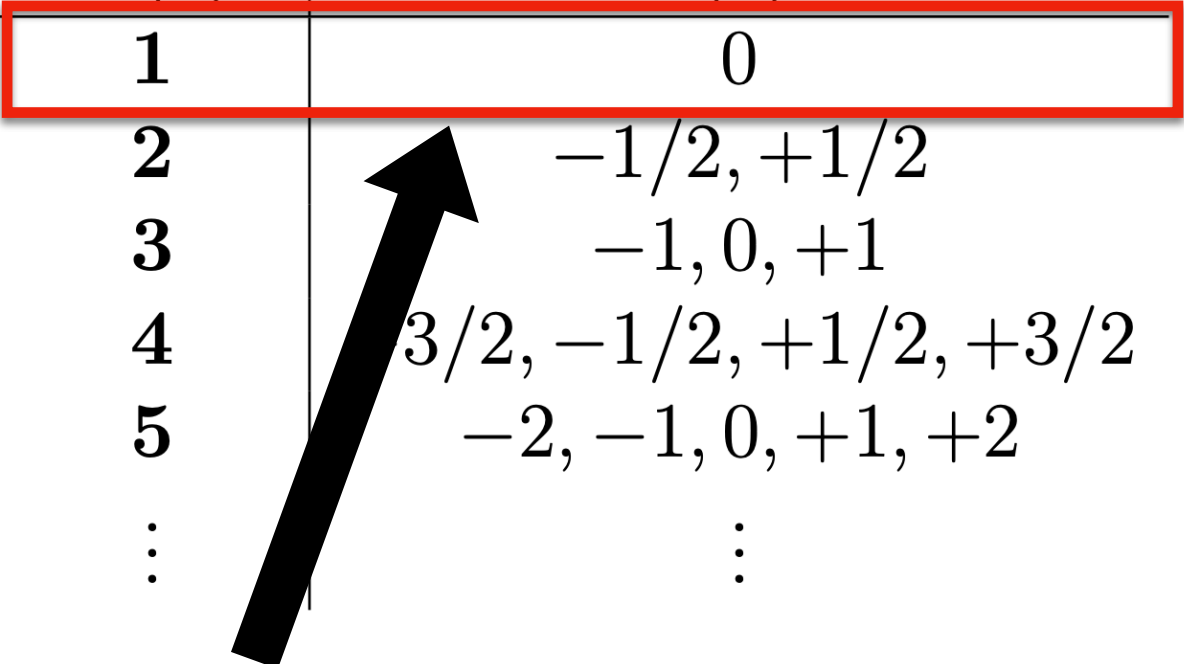


Interaction is determined by the SM gauge theory

# WIMP model

- Classifying WIMP by the representation of gauge group

Lorentz	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$
scalar		1	0
or fermion	1	2	$-1/2, +1/2$
or vector		3	$-1, 0, +1$
		4	$3/2, -1/2, +1/2, +3/2$
		5	$-2, -1, 0, +1, +2$
		$\vdots$	$\vdots$



How about here?


WIMP does not have gauge interaction

We have to study each model case-by-case

# WIMP model

- Classifying WIMP by the representation of gauge group

Lorentz	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$
scalar		1	0
or		2	$-1/2, +1/2$
fermion	1	3	$-1, 0, +1$
or		4	$3/2, -1/2, +1/2, +3/2$
vector		5	$-2, -1, 0, +1, +2$
		$\vdots$	$\vdots$



How about here?

We focus on fermionic gauge singlet WIMP

# Fermionic singlet WIMP

- We impose  $Z_2$  symmetry to make WIMP stable

$\chi$  : odd    SM particles : even

- Fermionic gauge singlet WIMP cannot have renormalizable interaction with SM particles.

Mass dimension	Operator
4	None
5	$\bar{\chi}\chi H ^2$ $\bar{\chi}i\gamma_5\chi H ^2$
6	$\bar{\chi}\gamma_\mu\gamma_5\chi\bar{Q}\gamma^\mu Q$ $\bar{\chi}\gamma_\mu\gamma_5\chi\partial_\nu F^{\mu\nu}$ etc.

- For UV completion, we need mediator particles which connect DM and SM particles
- There are many choices of mediator particles



# Our model

- We consider  $Z_2$ -odd scalar leptophilic mediator
- Correspond to **bin**o (WIMP) and **slepton** (mediator) in SUSY
- Possibility to explain **muon  $g-2$  anomaly**
- Direct detection experiment does not work effectively
- The search at collider experiments become more important
- Two scenarios for the mediator choice  
(left-handed slepton, right-handed slepton)

# Lagrangian (left-handed slepton)

$$\mathcal{L}_L = \mathcal{L}_{\text{SM}} + \frac{1}{2} \bar{\chi} (i\not{\partial} - m_\chi) \chi + (D_L^\mu \tilde{L}_i)^\dagger (D_{L\mu} \tilde{L}_i) + \mathcal{L}_{\text{DML}} - V_L(H, \tilde{L}_i),$$

$$\mathcal{L}_{\text{DML}} = -y_L \bar{L}_i \tilde{L}_i \chi + h.c., \quad \text{interaction term}$$

$$V_L = m_{\tilde{L}}^2 |\tilde{L}_i|^2 + \frac{\lambda_L}{4} |\tilde{L}_i|^4 + \lambda_{LH} |\tilde{L}_i|^2 |H|^2 + \lambda'_{LH} (\tilde{L}_i^\dagger \tau^a \tilde{L}_i) (H^\dagger \tau^a H) + \left[ \frac{\lambda''_{LH}}{4} (\tilde{L}_i^\dagger H^c)^2 + h.c. \right].$$

scalar potential term

- Most important parameters are  $m_\chi, m_{\tilde{L}}, y_L$
- Assuming flavor blindness for the analysis  
(slepton mass and interactions are universal for each flavor)

# Lagrangian (right-handed slepton)

$$\mathcal{L}_R = \mathcal{L}_{\text{SM}} + \frac{1}{2} \bar{\chi} (i\not{\partial} - m_\chi) \chi + (D_R^\mu \tilde{R}_i)^\dagger (D_{R\mu} \tilde{R}_i) + \mathcal{L}_{\text{DMR}} - V_L(H, \tilde{R}_i),$$

$$\mathcal{L}_{\text{DMR}} = -y_R \bar{E}_i \tilde{R}_i \chi + h.c, \quad \text{interaction term}$$

$$V_R = m_{\tilde{R}}^2 |\tilde{R}_i|^2 + \frac{\lambda_R}{4} |\tilde{R}_i|^4 + \lambda_{RH} |\tilde{R}_i|^2 |H|^2, \quad \text{scalar potential term}$$

- Most important parameters are  $m_\chi, m_{\tilde{R}}, y_R$
- Assuming flavor blindness for the analysis  
(slepton mass and interaction are universal for each flavor)

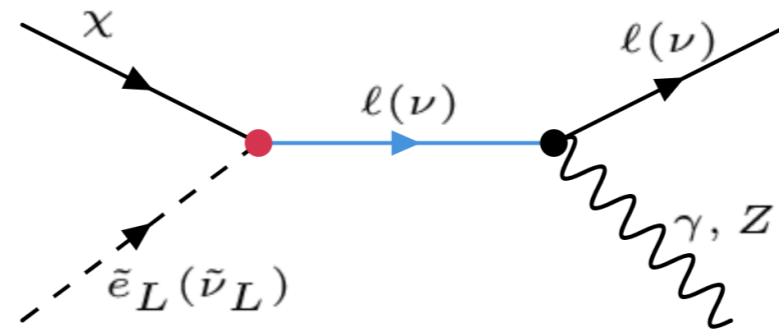
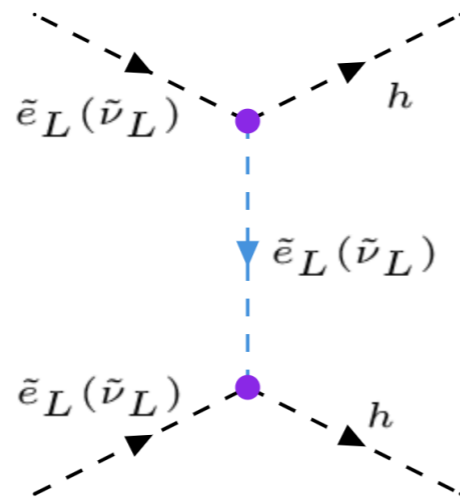
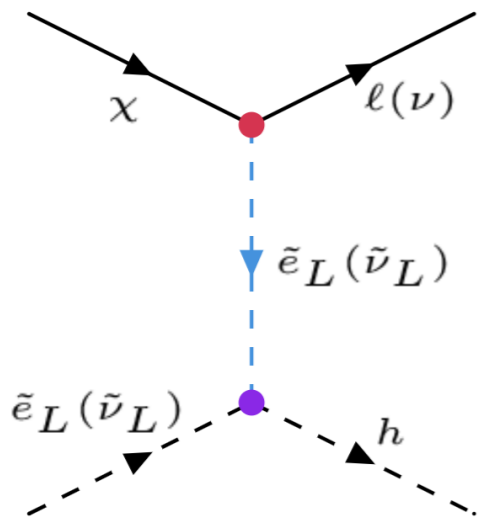
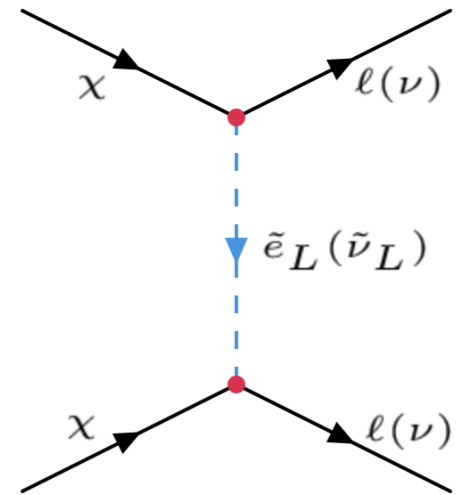
# Constraints on the model

- Vacuum stability condition
- Constraint from  $h \rightarrow \gamma\gamma$  or  $h \rightarrow \text{inv.}$  decay
- Electroweak precision measurement
- Relic abundance condition
- Direct production of mediators at colliders

# Relic abundance condition

(e.g. left-handed case)

- $\chi\chi \rightarrow \bar{l}l$  is dominant annihilation mode
- The abundance is determined by  $m_\chi, m_{\tilde{L}}, y_L$
- If WIMP mass and mediator mass are degenerate, other processes also become important (co-annihilation)

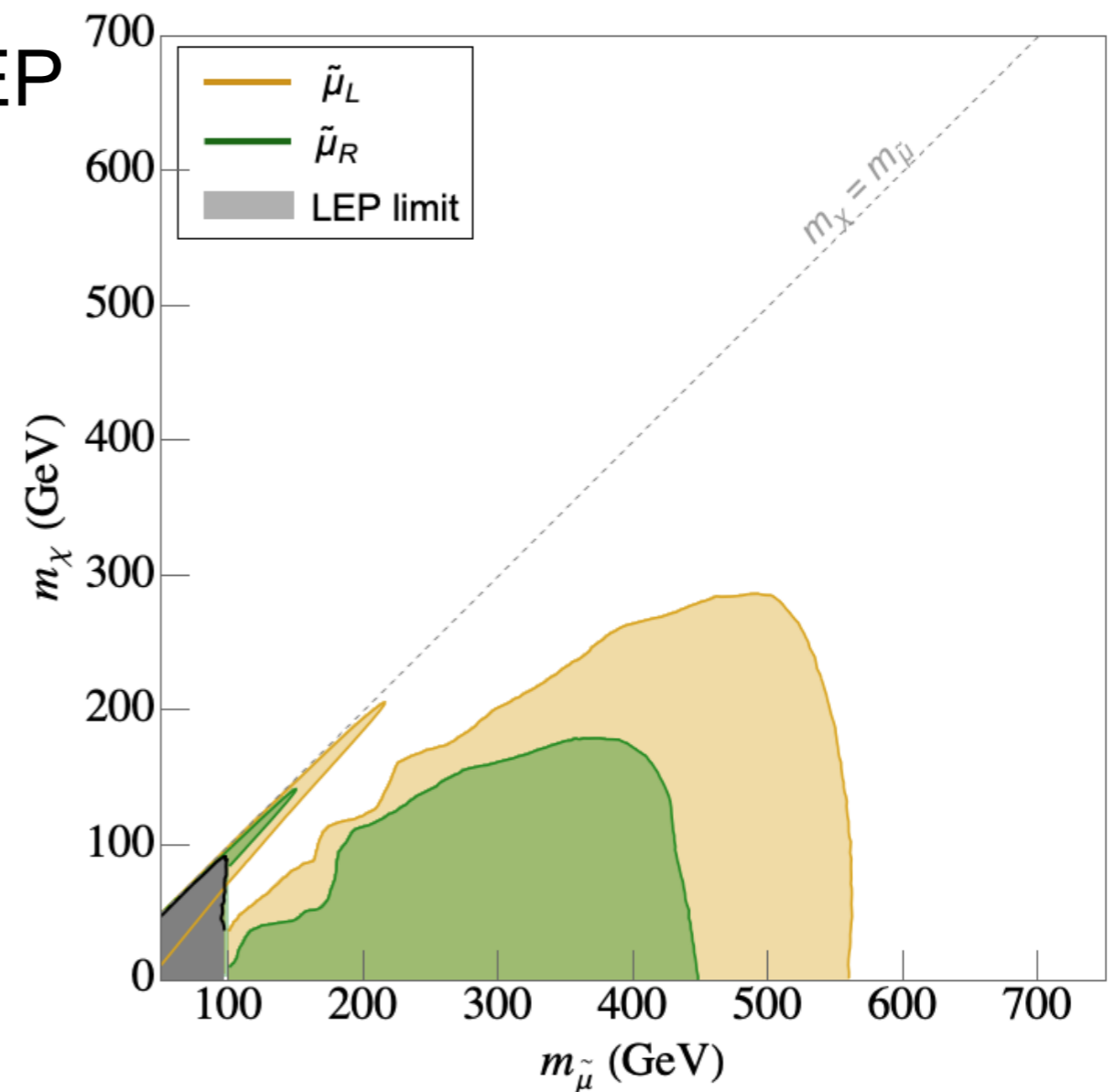


and so on

We used MadGraph5\_aMC@NLO for the calculation

# Collider constraints

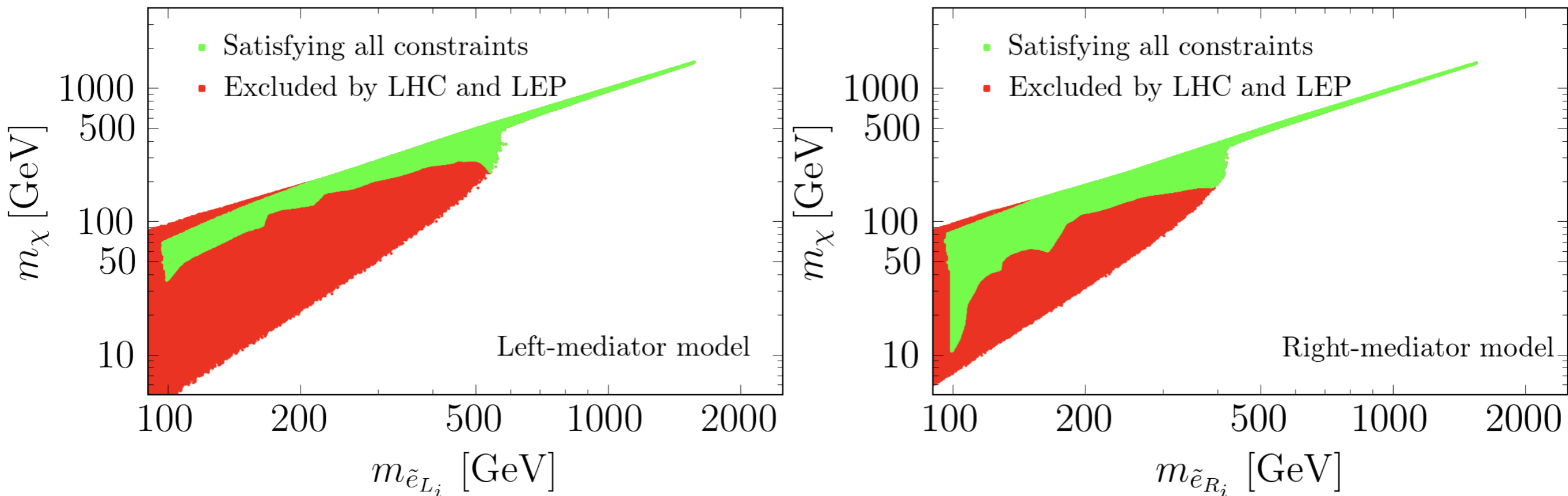
- Slepton pair can be created via Drell-Yan process at LHC or LEP
- Created slepton decays into WIMP and lepton
- Constraint on slepton mass and WIMP mass
- LEP constrain slepton below 94 GeV (under flavor blindness)



[Georges Aad et al. Phys. Rev. D, 101(5):052005,2020]

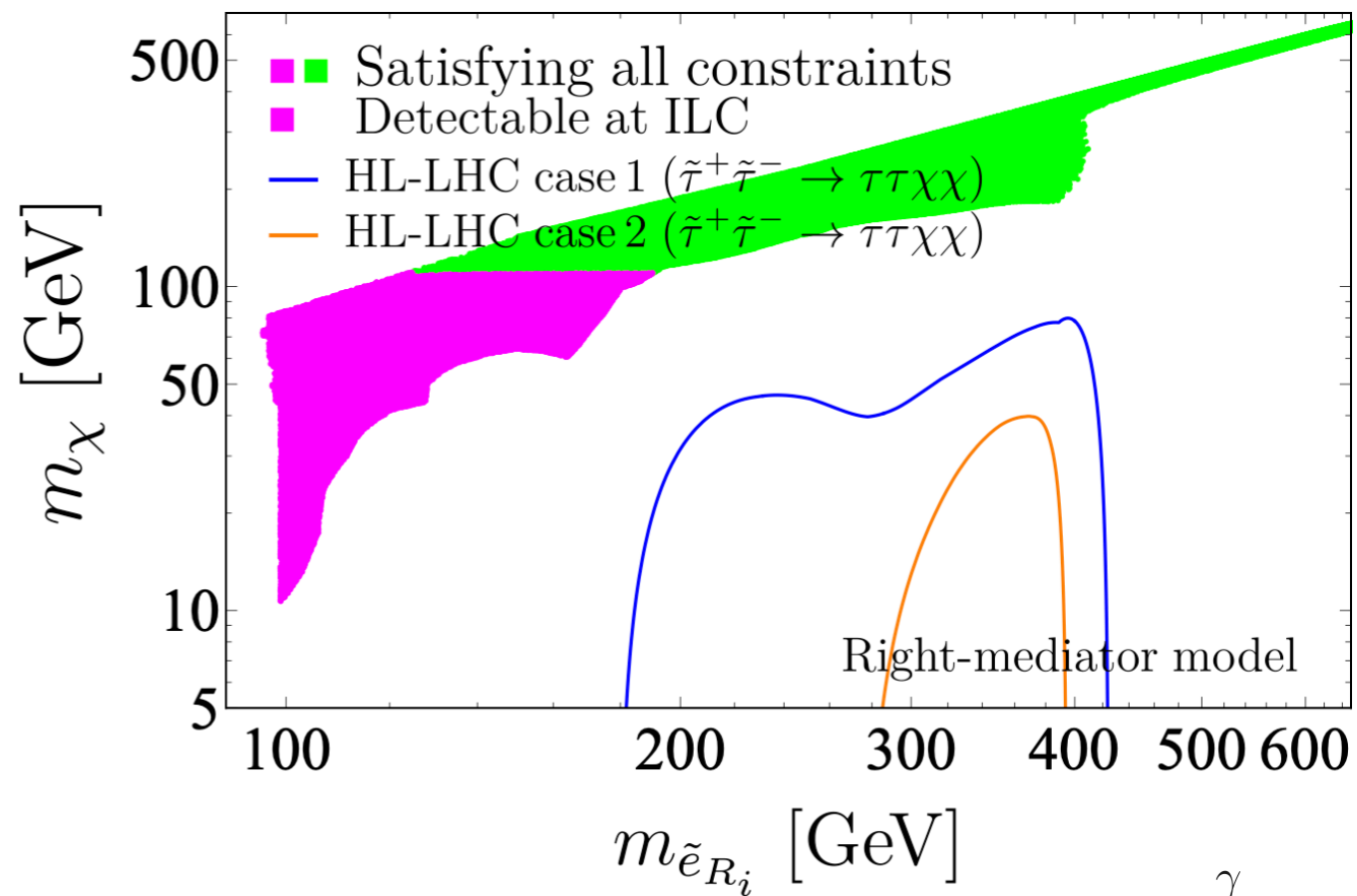
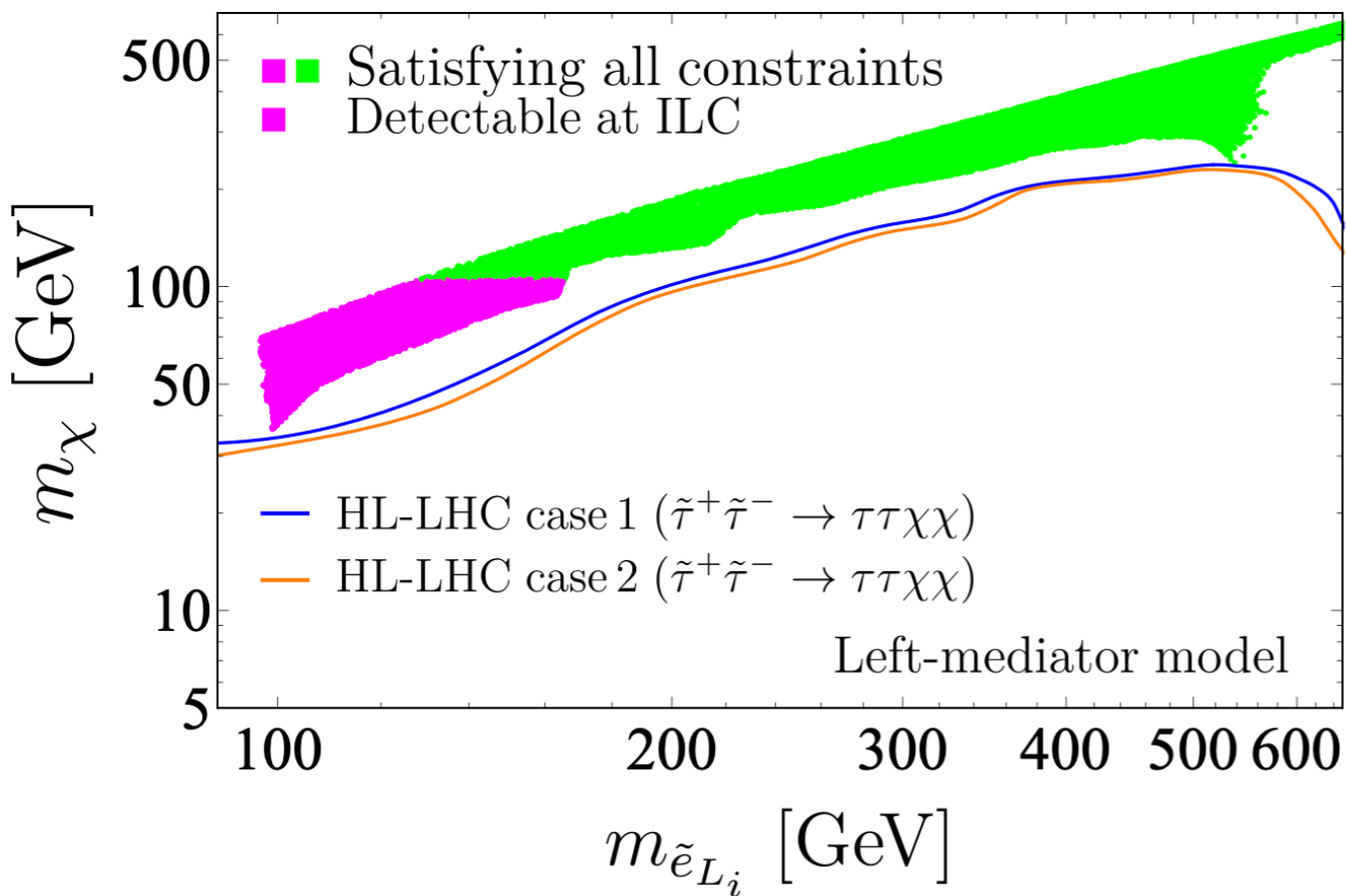
[Georges Aad et al. Phys. J. C, 80(2):123,2020]

# Present status

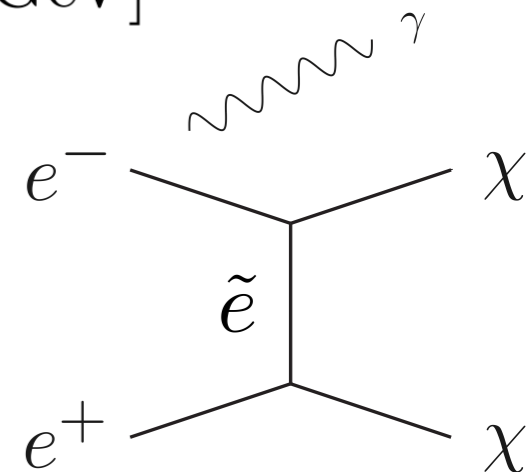


- Here we also consider other constraints (vacuum stability, electroweak precision, higgs decay)
- Green region is surviving region

# Future prospect



- We consider mono-photon search at 250 GeV ILC  
(For HL-LHC, only tau channel analysis is shown)





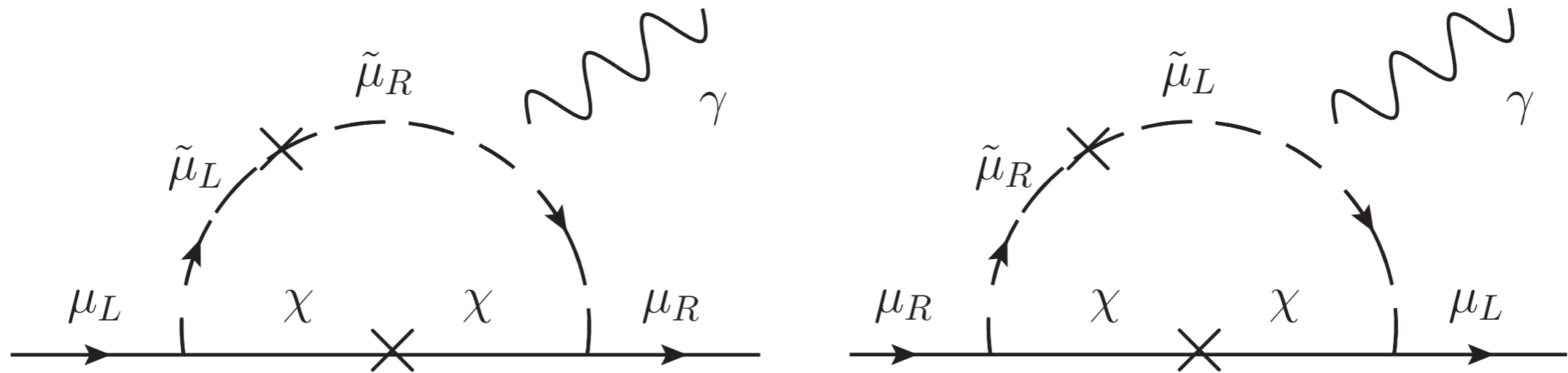
**Combined scenario of left  
and right mediators  
and muon  $g-2$**

# Muon g-2

- If we consider left and right mediators simultaneously, there emerge new scalar potential terms

$$\lambda_{LR}(\tilde{L}_i^\dagger \tilde{L}_i)(\tilde{E}_i^\dagger \tilde{E}_i) \quad Am_i \tilde{E}_i \tilde{L}_i^\dagger H + h.c.$$

- New 'A' term induce muon g-2



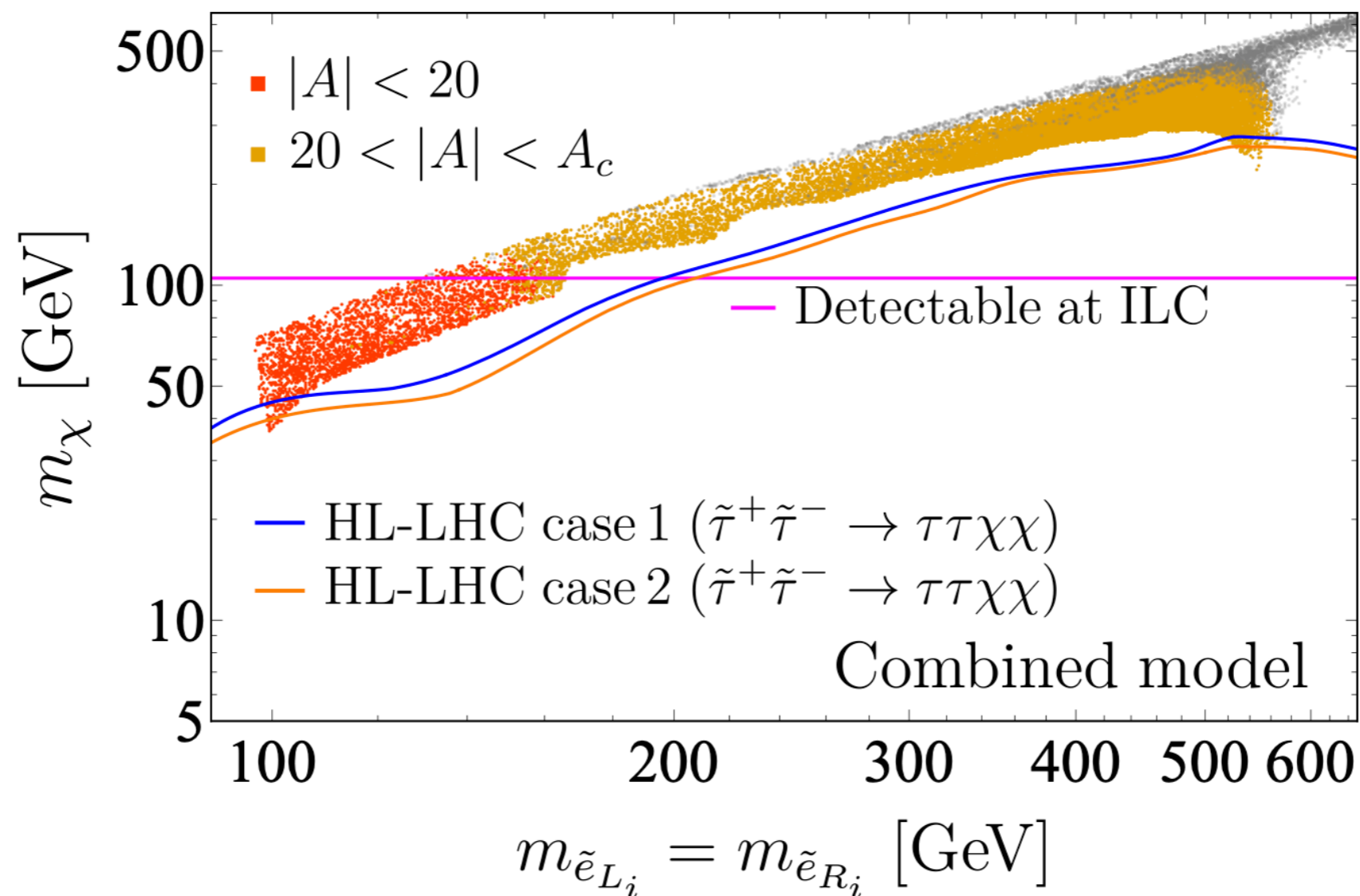
- Muon g-2 anomaly can be explained by combined model

$$\Delta a_\mu \equiv a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 251(59) \times 10^{-11} \quad [\text{Fermilab (2021)}]$$

# Muon $g-2$

- This plot shows the value of 'A' to explain muon  $g-2$  anomaly
- Yellow and red region have stable vacuum at least SUSY case

[G. H. Duan, C. Han, B. Peng, L. Wu and J. M. Yang, 2019]



# Summary

- We studied the phenomenology of **fermionic gauge singlet WIMP with leptophilic mediator**
- **ILC experiment has important role** to search such models
- Left and right combined model can be a **solution of muon g-2 anomaly**
- There are some region which can explain muon g-2 anomaly and also detectable at ILC