

Leptonic new force for Muon $(g-2)$ and B-anomalies

S.C.Park

Based on arXiv: [1904.13053](https://arxiv.org/abs/1904.13053), [2001.06572](https://arxiv.org/abs/2001.06572), [2006.13910](https://arxiv.org/abs/2006.13910), [2012.04190](https://arxiv.org/abs/2012.04190), [2104.06656](https://arxiv.org/abs/2104.06656), ...

Collaboration with

Kayoung Ban, **Yongsoo Jho**, **Youngjoon Kwon** (Yonsei+KEK), **Yeji Park**, **Seokhee Park** (KEK)

Po-Yan Tseng (Yonsei -> Tsing Hua)

* **students @ Yonsei**
* **experiment**

Mini-workshop on BSM-related aspects at ILC and other proposed e+e- colliders

March 2 JST, 2022 <https://agenda.linearcollider.org/event/9575/>

It's like making a good Tacoyaki!



Motivation

- The LHC is an excellent probe to discover new physics
 - ✓ if it couples with hadron
 - ✓ relatively heavy (>10 GeV) depending on channels
 - ✓ nothing beyond the SM is seen yet
- There are other types of new physics
 - ✓ couples to leptons (and possibly dark sector)
 - ✓ relatively light (<10 GeV) but feebly interacting
 - ✓ BELLE-II, XENONnT, COSINE ...can cover this territory

Complementary

LHC is good here
heavy

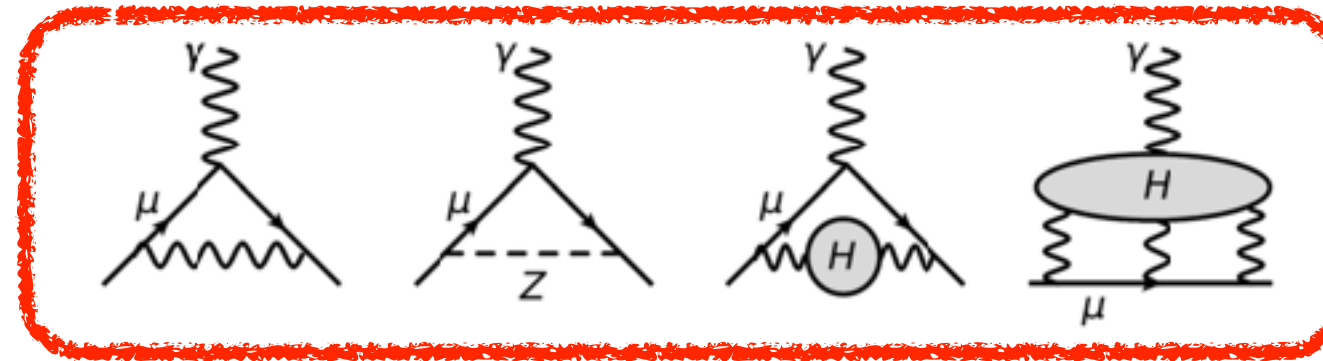
light
BELLE-II, Xenon1t etc
are good here

Motivation

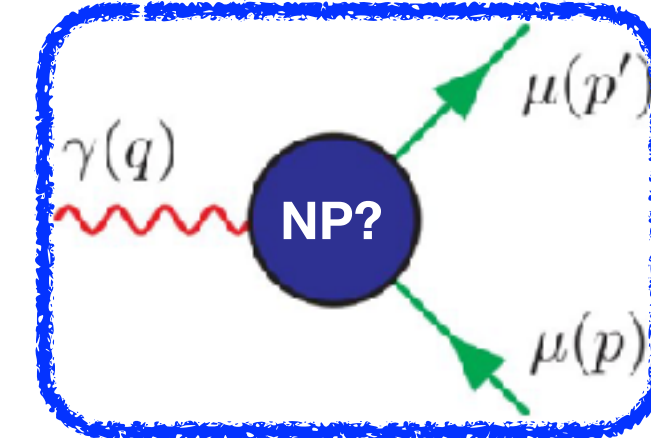
- Indeed, there have been long standing problems...
 - $(g-2)$ of muon remains anomalous for many years
 - Recent observation suggests violation of lepton universality
 - ➡ New physics BSM may have contact (exclusively) with leptonic sector
 - ➡ We want to focus on this direction today

Muon g-2 and New Physics

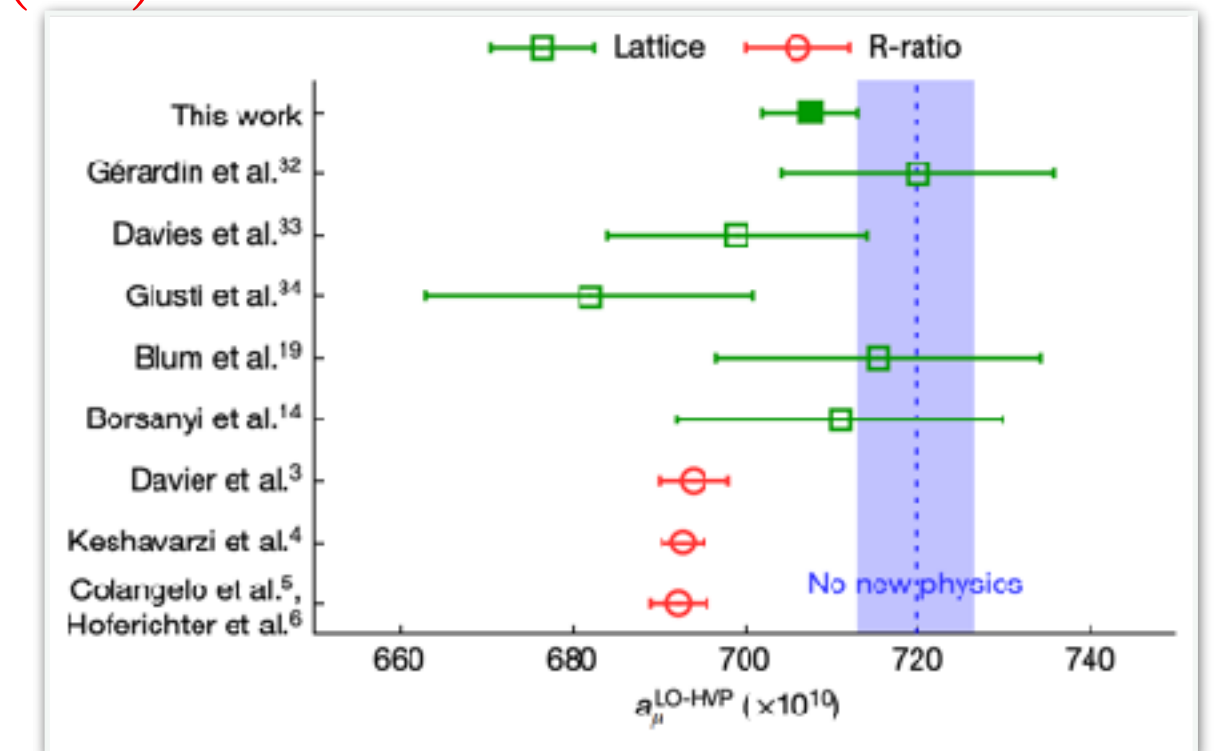
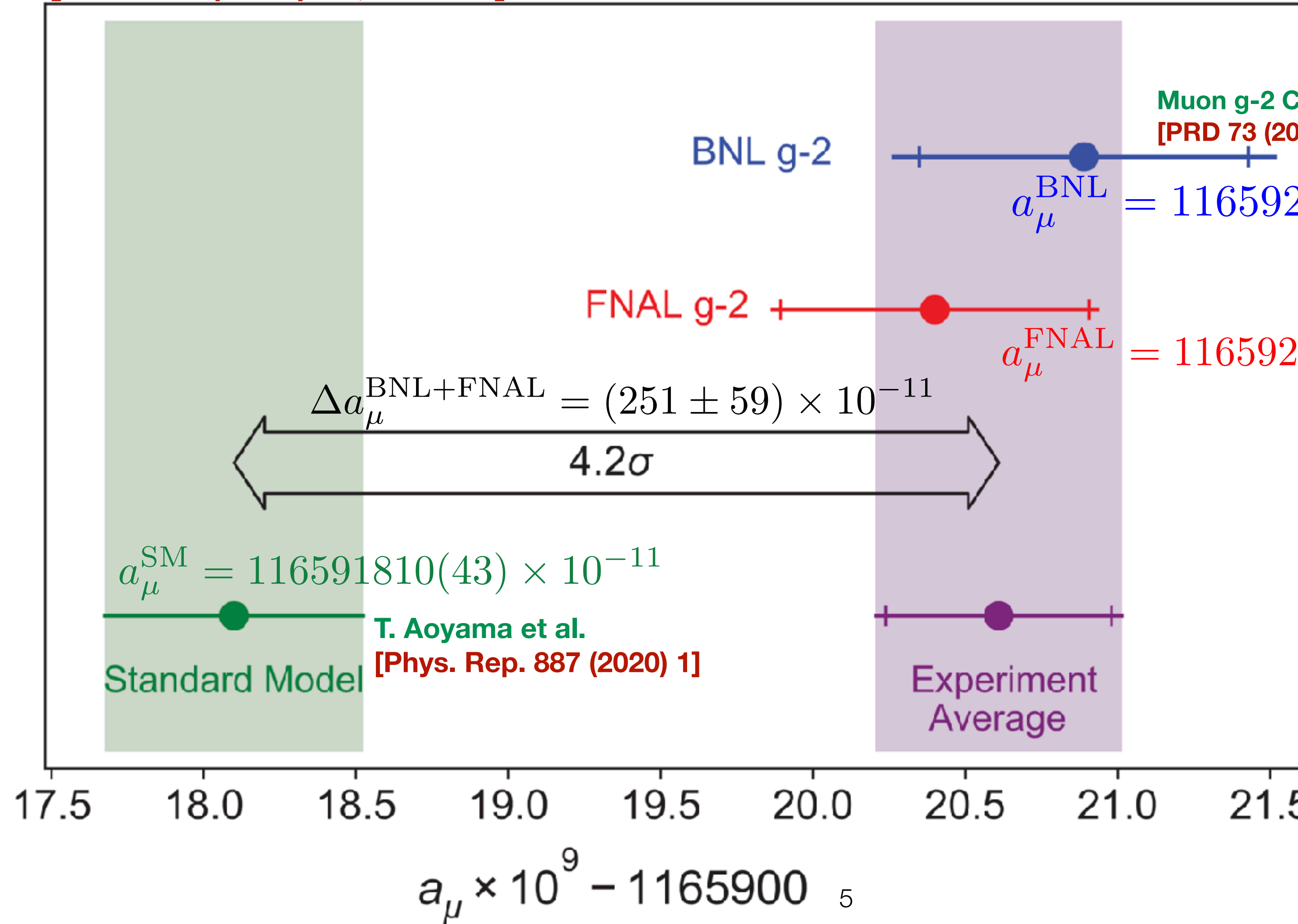
Muon g-2 Collaboration
 [PRL 126 (2021) 14, 141801]



SM



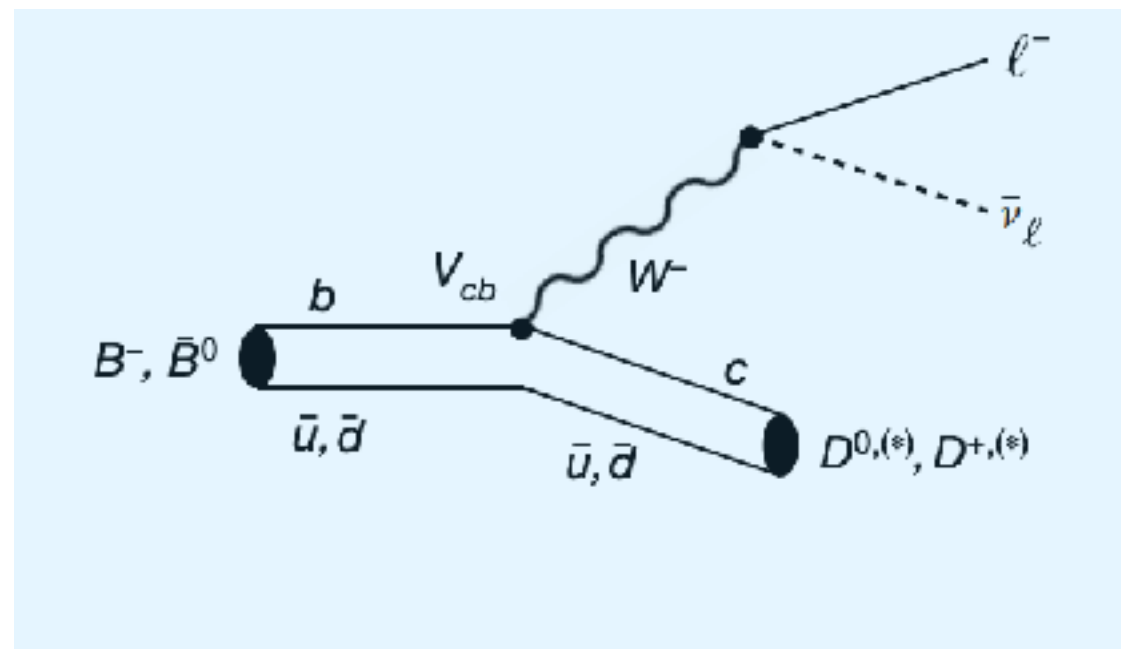
NP?



See however
 Sz. Borsanyi et al. *Nature* 593, 51–55 (2021)

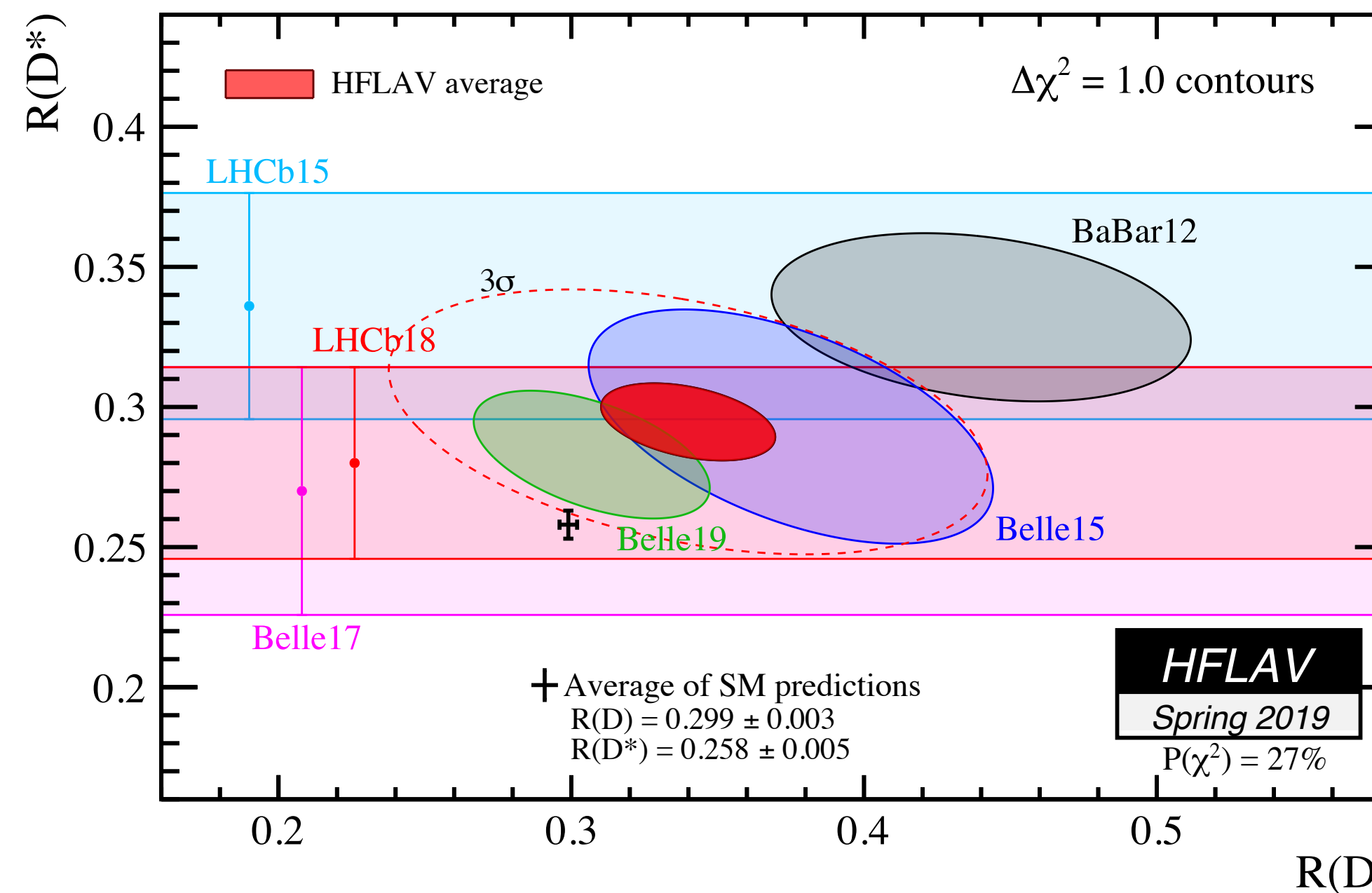
**+4.2 σ larger $(g - 2)_{\mu}$
 than the SM expectation!**

Lepton universality tests in B-meson decays (II)



$$R_D \equiv \frac{B(\bar{B} \rightarrow D\tau^-\bar{\nu}_\tau)}{B(\bar{B} \rightarrow De^-\bar{\nu}_e)} = \begin{cases} 0.299 \pm 0.003 & \text{SM} \\ 0.340 \pm 0.027 \pm 0.013 & \text{exp} \end{cases} \quad +1.4\sigma$$

$$R_{D^*} \equiv \frac{B(\bar{B} \rightarrow D^*\tau^-\bar{\nu}_\tau)}{B(\bar{B} \rightarrow D^*e^-\bar{\nu}_e)} = \begin{cases} 0.258 \pm 0.005 & \text{SM} \\ 0.295 \pm 0.011 \pm 0.008 & \text{exp} \end{cases} \quad +2.5\sigma$$

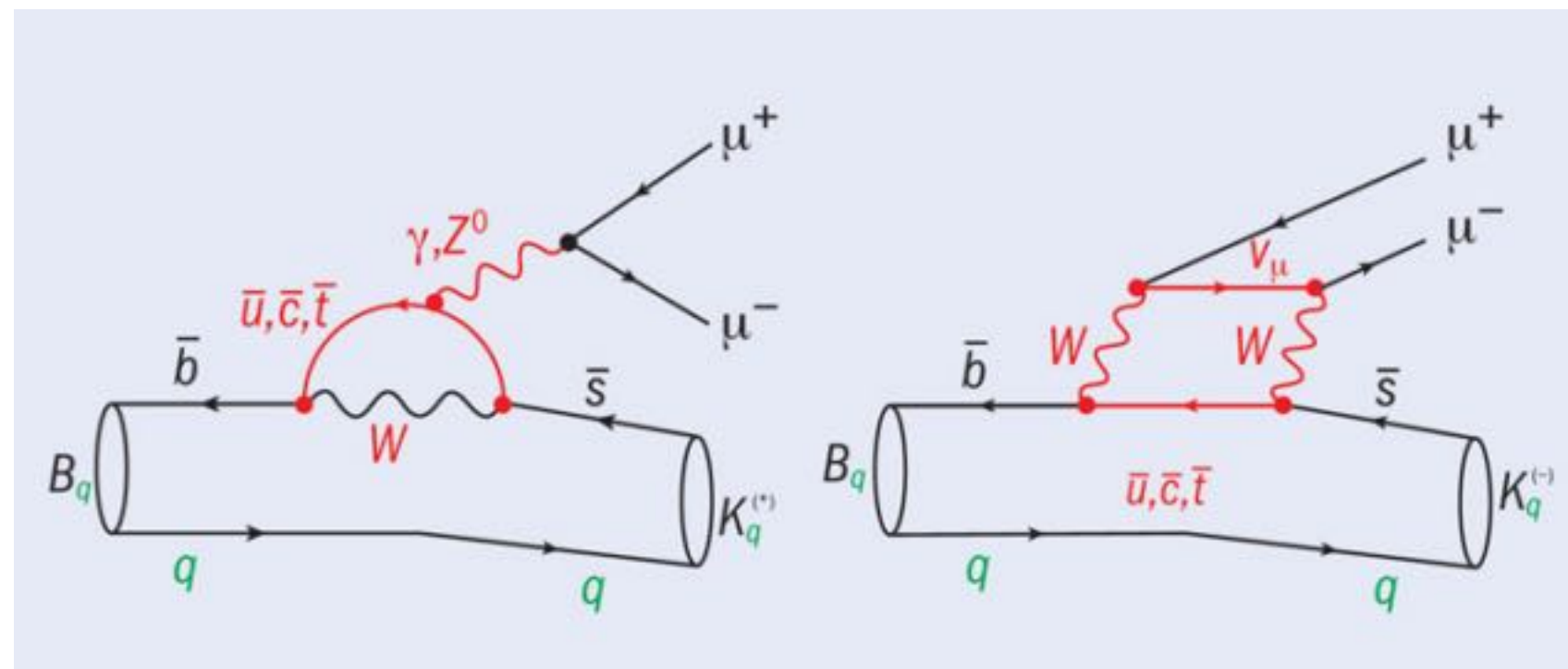


HFLAV Group
[EPJC 77 (2017) 895] [1612.07233 (hep-ph)]

HFLAV average : <https://hflav-eos.web.cern.ch/hflav-eos/semi/spring19/html/RDsDsstar/RDRDs.html>

+3.1σ (combined) larger R_D, R_{D^*} than the SM expectation!

Lepton universality tests in B-meson decays (2)



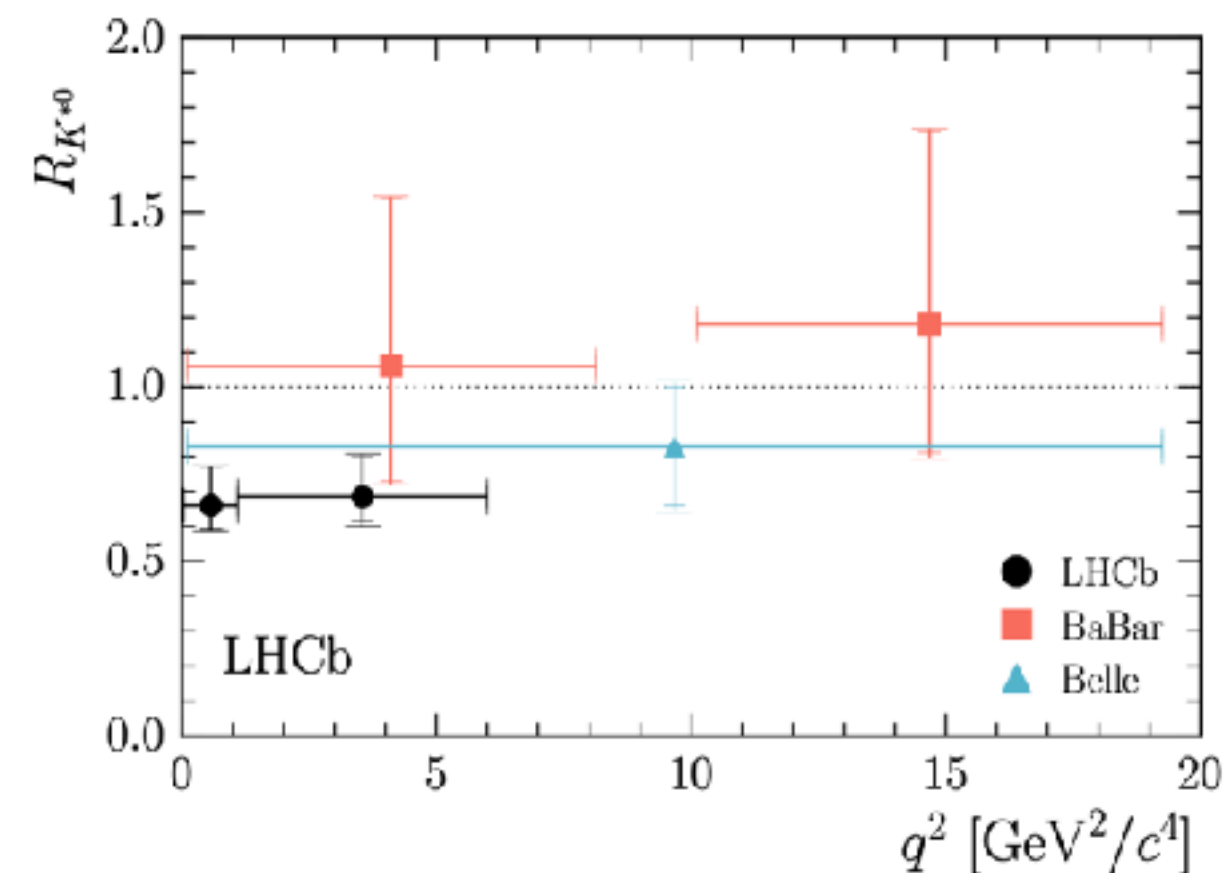
$$R_{K^{(*)}} \equiv \frac{\text{Br}(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\text{Br}(B \rightarrow K^{(*)} e^+ e^-)} \approx 1.0 \text{ SM}$$

R_{K^*}
LHCb Collaboration
 [JHEP 08 (2017) 055]

R_K
BaBar Collaboration
 [PRD 86 (2012) 032012]

Belle Collaboration
 [JHEP 03 (2021) 105]

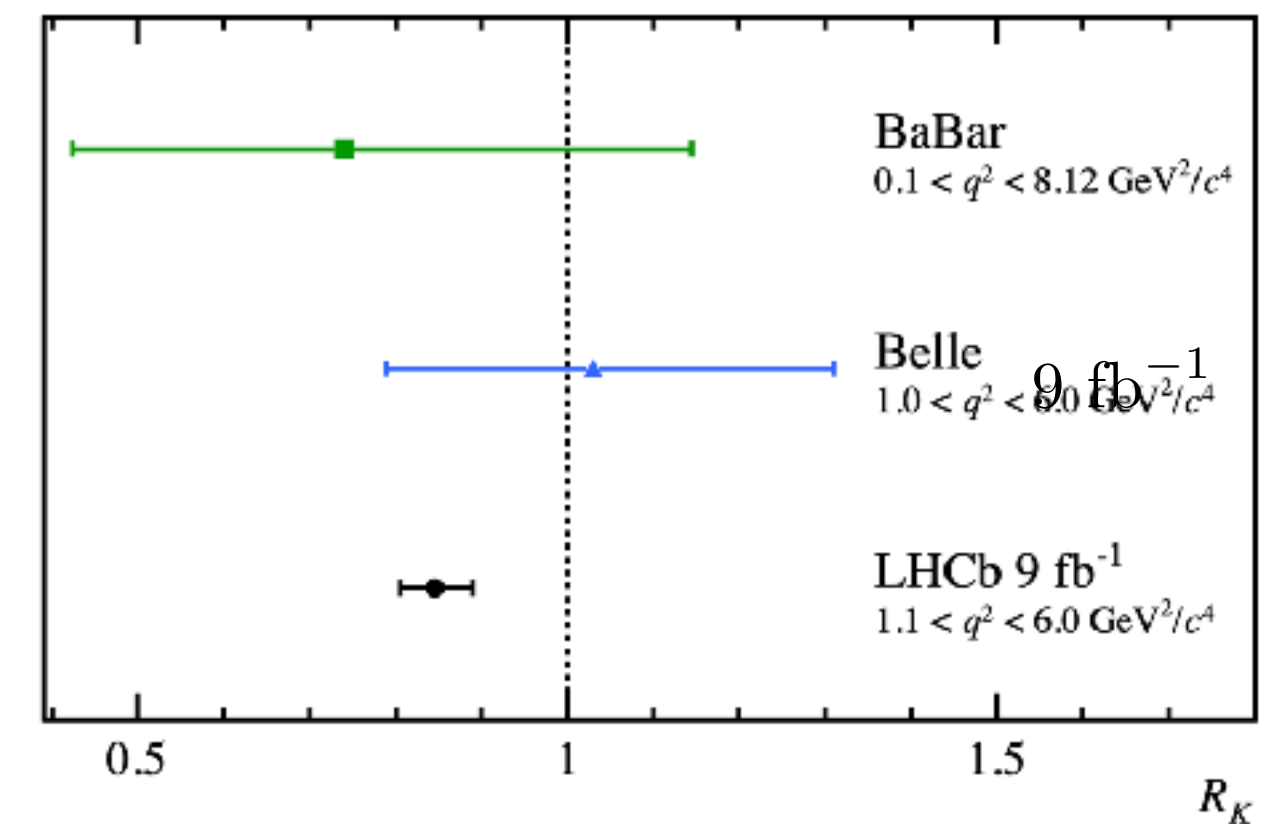
LHCb Collaboration
 [2103.11769 (hep-ex)]



LHCb 2017, 7+8 TeV data set 3 fb^{-1}

$$R_{K^*}^{[0.045, 1.1]} = 0.66_{-0.07-0.03}^{+0.11+0.03} \quad (2.1-2.3)\sigma$$

$$R_{K^*}^{[1.1, 6.0]} = 0.69_{-0.07-0.05}^{+0.11+0.05} \quad (2.4-2.5)\sigma$$

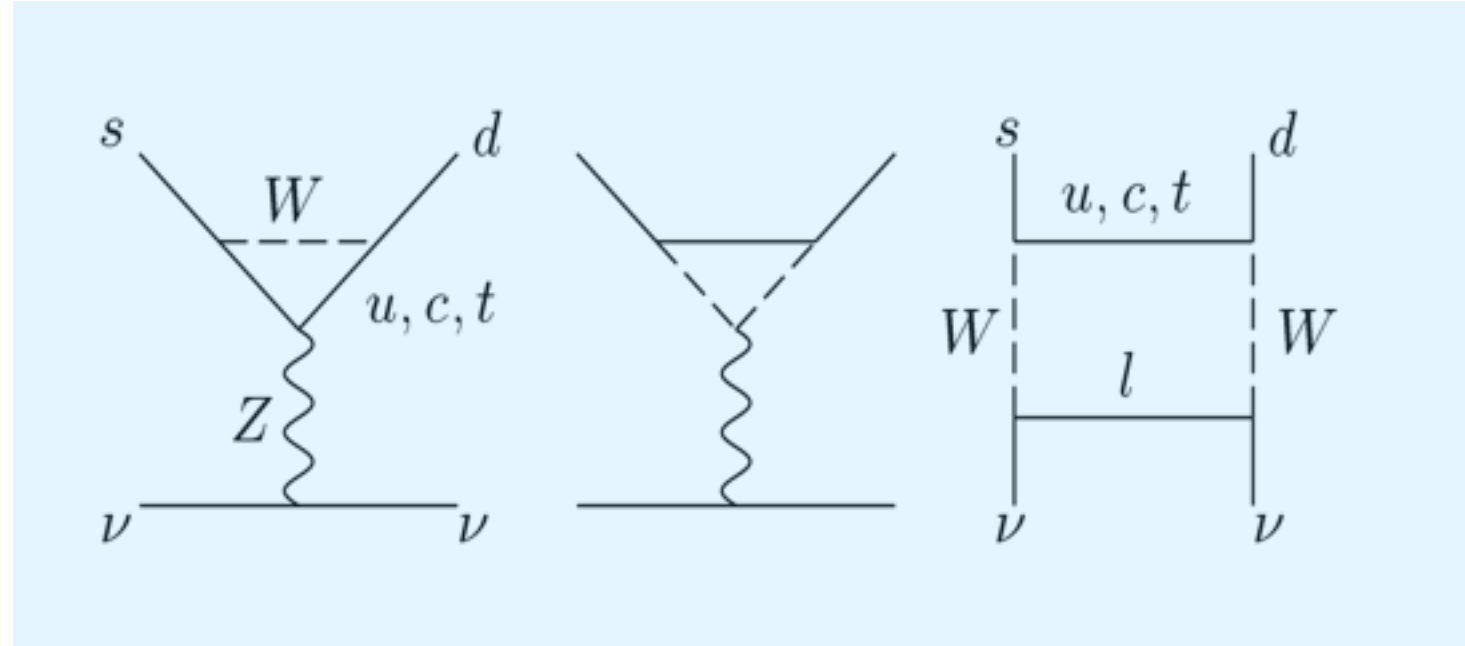


LHCb 2021, Run 1+2 full data set

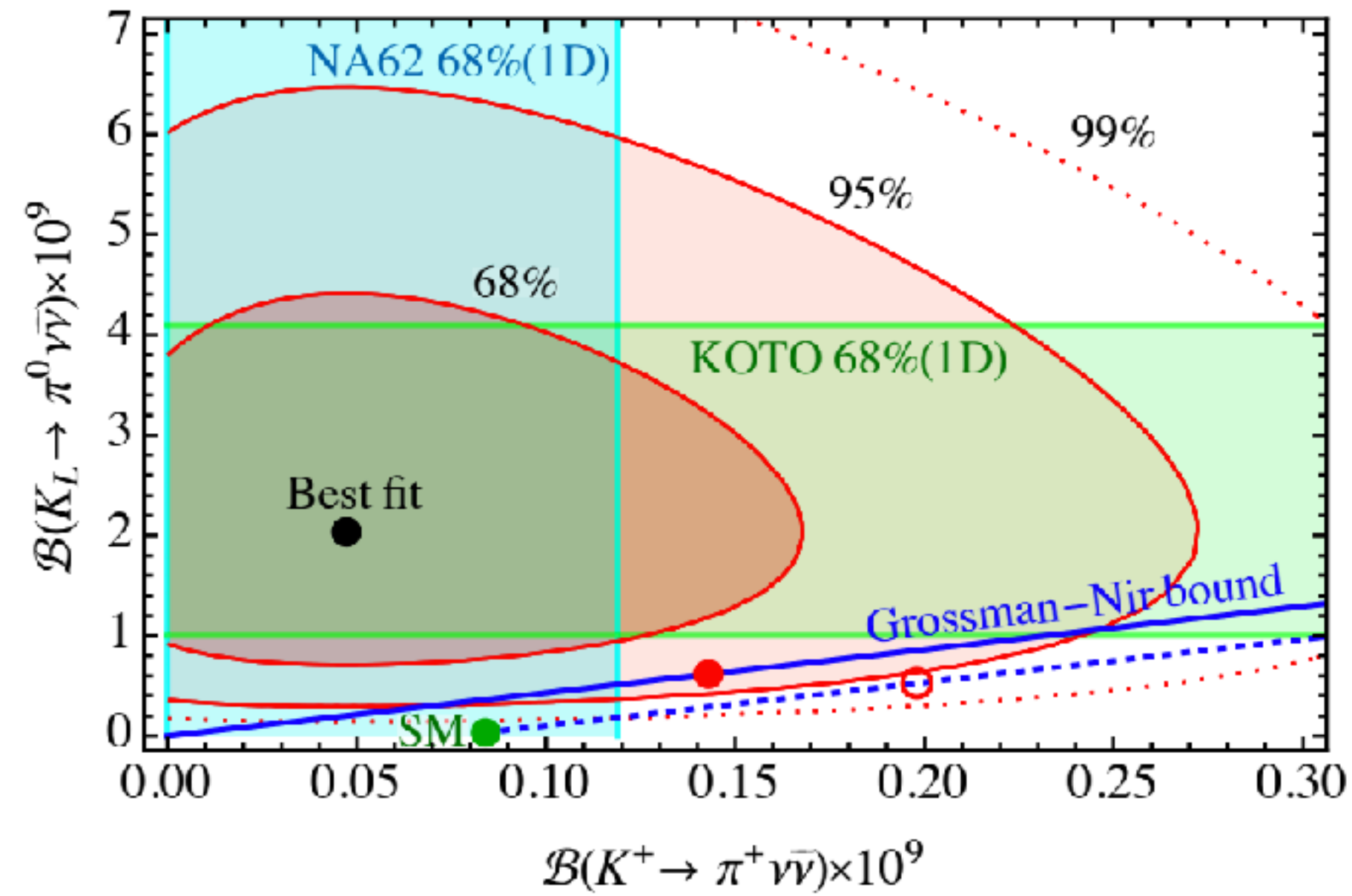
$$R_K^{[1.1, 6.0]} = 0.846_{-0.039-0.012}^{+0.042+0.013}$$

**-3.1σ smaller R_K, R_{K^*}
 than the SM expectation!**

J-PARC KOTO anomaly



$$B(K_L \rightarrow \pi^0 \nu \bar{\nu}) = \begin{cases} (2.1_{-1.1}^{+2.0}) \times 10^{-9} & \text{SM} \\ (3.0 \pm 0.3) \times 10^{-11} & \text{KOTO} \end{cases}$$



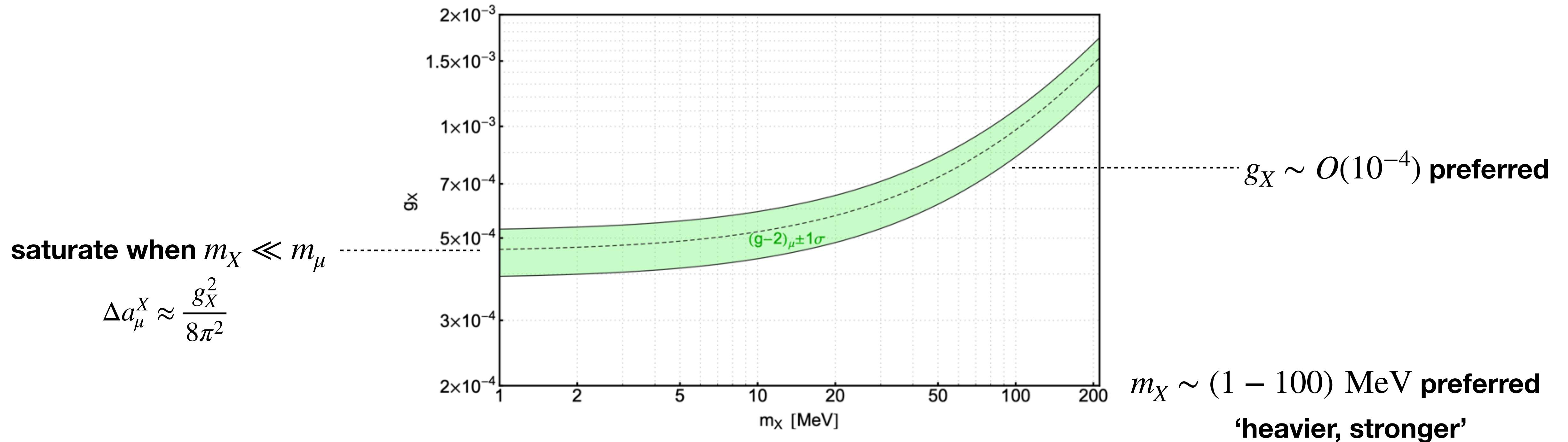
T. Kitahara et. al. 1909.11111

**$\times 10^{-2}$ smaller
than the SM expectation!**

Muonic new force for (g-2) of muon:

$$\mathcal{L}_{\text{eff}} \ni -g_X X_\alpha (\bar{\mu} \gamma^\alpha \mu) - \frac{1}{2} m_X^2 X_\mu X^\mu$$

$$\Delta a_\mu^X = \frac{g_X^2}{8\pi^2} \int_0^1 dz \frac{2z(1-z)^2}{(1-z)^2 + (m_X/m_\mu)^2 z} \quad \text{@ 1-loop}$$



Leptonic new force

- Anomaly free extension of the SM

- ▶ $L_i - L_j$

- ▶ $B_i - L_j$

- ▶ $a(B - L)_i - b(L_j - L_k)$

- ▶ Vector LQ

⊕ Kinetic mixing of $U(1)_Y \times U(1)_X$

$$\Delta\mathcal{L} = \epsilon B_{\mu\nu} X^{\mu\nu}$$

Typically, free parameters include

$$m_X, q_X, \epsilon, (a/b)$$

Effective Lagrangian for $U(1)_{\text{lepton}}$

$$\mathcal{L}_{\text{eff}} \ni -X_\mu \left(g_e J_e^\mu + g_\nu J_\nu^\mu + g_\chi J_\chi^\mu \right) + \dots$$

$$J_e^\mu = \bar{e} \gamma^\mu e$$

$$J_\nu^\mu = \bar{\nu}_L \gamma^\mu \nu_L$$

$$J_\chi^\mu = \bar{\chi} \gamma^\mu \chi$$

Controllable parameters : $g_e, g_\nu, m_X, g_\chi, m_\chi$

LQ models

$$LQ \rightarrow q + \ell$$

1. Boson (s=0, 1) s=2: not impossible

2. Quantum numbers e.g.

$$Y = Y_q + Y_\ell = \left(\frac{1}{6}, \frac{2}{3}, -\frac{1}{3}\right) \oplus \left(-\frac{1}{2}, -1\right)$$

All possible LQs couples to quark + lepton

W. Buchmüller, R. Rückl, and D. Wyler [PLB 191, 442 (1987)]

Spin	$3B + L$	$SU(3)_c$	$SU(2)_W$	$U(1)_Y$	Allowed coupling
0	-2	$\bar{3}$	1	1/3	$\bar{q}_L^c \ell_L$ or $\bar{u}_R^c e_R$
0	-2	$\bar{3}$	1	4/3	$\bar{d}_R^c e_R$
0	-2	$\bar{3}$	3	1/3	$\bar{q}_L^c \ell_L$
1	-2	$\bar{3}$	2	5/6	$\bar{q}_L^c \gamma^\mu e_R$ or $\bar{d}_R^c \gamma^\mu \ell_L$
1	-2	$\bar{3}$	2	-1/6	$\bar{u}_R^c \gamma^\mu \ell_L$
0	0	3	2	7/6	$\bar{q}_L e_R$ or $\bar{u}_R \ell_L$
0	0	3	2	1/6	$\bar{d}_R \ell_L$
1	0	3	1	2/3	$\bar{q}_L \gamma^\mu \ell_L$ or $\bar{d}_R \gamma^\mu e_R$
1	0	3	1	5/3	$\bar{u}_R \gamma^\mu e_R$
1	0	3	3	2/3	$\bar{q}_L \gamma^\mu \ell_L$

[From PDG LQ review]

LQ for $R_{D^{(*)}}, R_{K^{(*)}}$

All possible LQs couples to quark + lepton

W. Buchmüller, R. Rückl, and D. Wyler [PLB 191, 442 (1987)]

$$R_{D^{(*)}}^{\text{SM+LQ}} > R_{D^{(*)}}^{\text{SM}}$$

$$R_{K^{(*)}}^{\text{SM+LQ}} < R_{K^{(*)}}^{\text{SM}}$$

U_1 : isospin singlet
vector leptoquark

A. Angelescu et al.
[JHEP 10 (2018) 183]

Spin	$3B + L$	$SU(3)_c$	$SU(2)_W$	$U(1)_Y$	Allowed coupling
0	-2	$\bar{3}$	1	1/3	$\bar{q}_L^c \ell_L$ or $\bar{u}_R^c e_R$
0	-2	$\bar{3}$	1	4/3	$\bar{d}_R^c e_R$
0	-2	$\bar{3}$	3	1/3	$\bar{q}_L^c \ell_L$
1	-2	$\bar{3}$	2	5/6	$\bar{q}_L^c \gamma^\mu e_R$ or $\bar{d}_R^c \gamma^\mu \ell_L$
1	-2	$\bar{3}$	2	-	large μ - t -LQ coupling
0	0	3	2	7/6	$\bar{q}_L e_R$ or $\bar{u}_R \ell_L$
0	0	3	2	1/6	$\bar{d}_R \ell_L$
1	0	3	1	2/3	$\bar{u}_L \gamma^\mu \ell_L$ or $\bar{d}_R \gamma^\mu e_R$
1	0	3	1	5/3	$\bar{u}_R \gamma^\mu e_R$
1	0	3	3	2/3	$\bar{q}_L \gamma^\mu \ell_L$

If one does focus on a simultaneous explanation of $R_{K^{(*)}} / R_{D^{(*)}}$ anomalies only with a single LQ, other choices cannot make correct contributions for $R_{K^{(*)}} \& R_{D^{(*)}}$, or excluded by other rare decay processes, such as

$$\text{Br}(\tau \rightarrow \mu \gamma)$$

$$\text{Br}(B \rightarrow K \nu \bar{\nu}) \text{ and so on.}$$

Model	$R_{K^{(*)}}$	$R_{D^{(*)}}$	$R_{K^{(*)}} \& R_{D^{(*)}}$
S_1	\times^*	\checkmark	\times^*
R_2	\times^*	\checkmark	\times
\widetilde{R}_2	\times	\times	\times
S_3	\checkmark	\times	\times
U_1	\checkmark	\checkmark	\checkmark
U_3	\checkmark	\times	\times

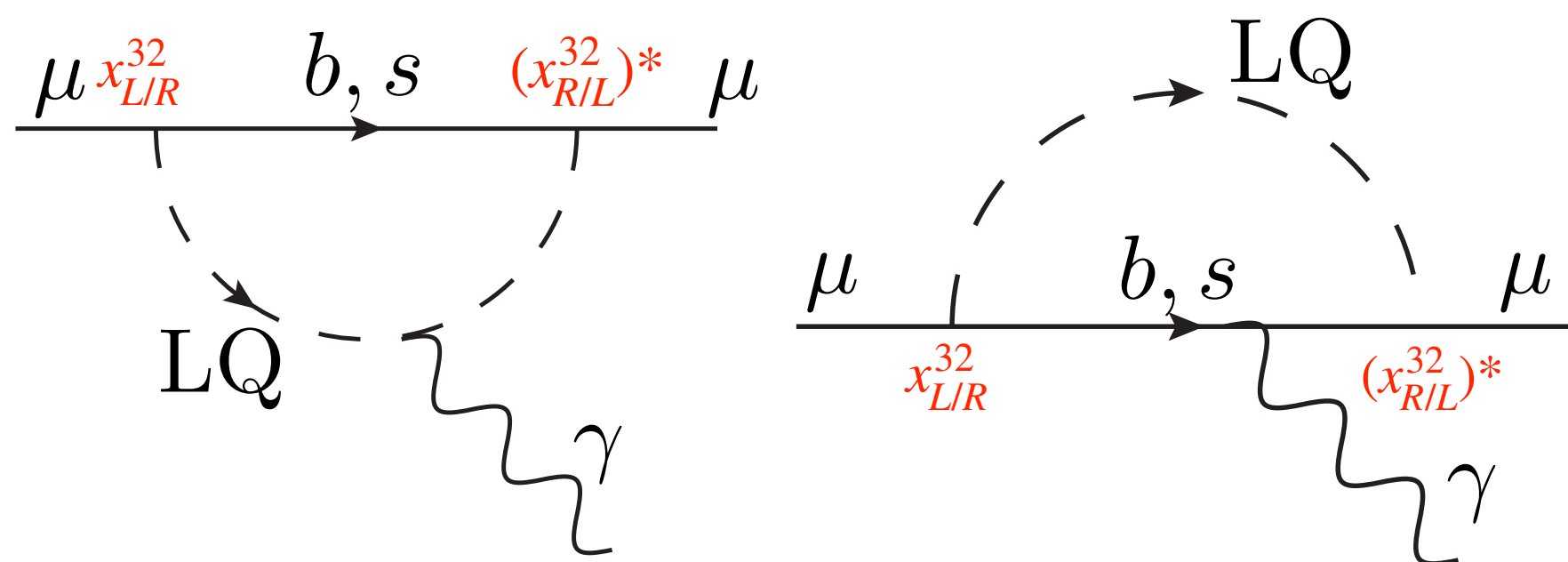
A. Angelescu et al.
[JHEP 10 (2018) 183]

$$\mathcal{L} \supset \underbrace{-\frac{1}{2} U_{1\mu\nu}^\dagger U_1^{\mu\nu}}_{\supset \text{QCD\&EM interactions}} + U_{1\mu} \sum_{i,j=1,2,3} \underbrace{\left[x_L^{ij} (\bar{d}_L^i \gamma^\mu e_L^j + (V_{\text{CKM}}^\dagger x_L U_{PMNS})_{ij} (\bar{u}_L^i \gamma^\mu \nu_L^j) + x_R^{ij} (\bar{d}_R^i \gamma^\mu e_R^j) \right]}_{\text{(effective) LQ interactions}} + \text{h.c.}$$

$$U_{1\mu\nu} = D_\mu U_{1\nu} - D_\nu U_{1\mu}$$

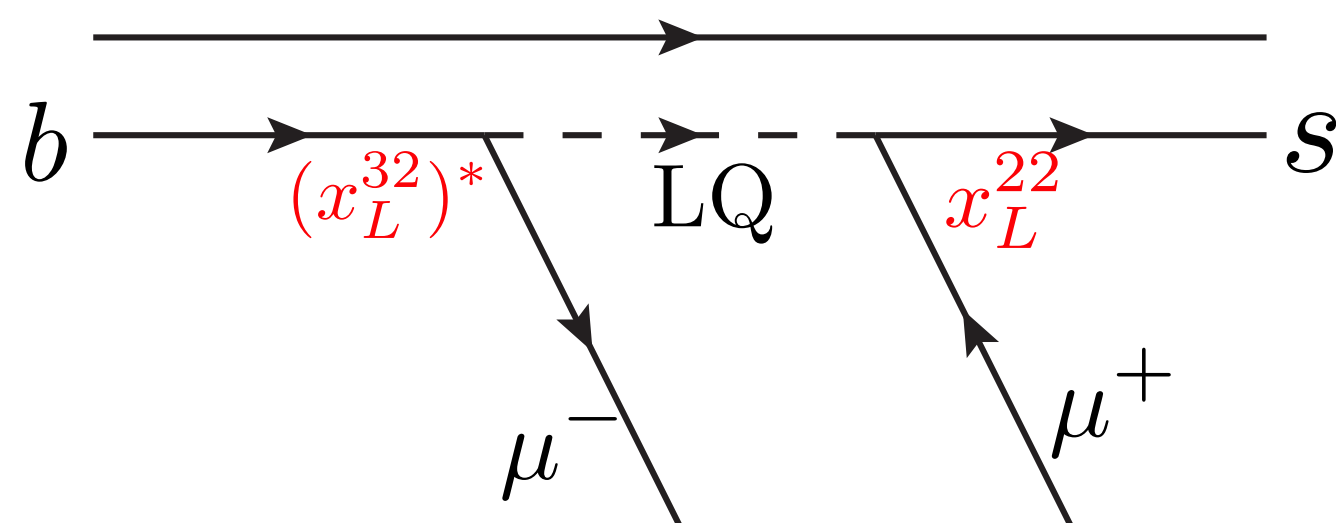
$$D_\mu \equiv \partial_\mu - i g_s G_\mu^a T_{13}^a - i \frac{2}{3} g_Y B_\mu$$

LQ contributions



$$\frac{1}{\Lambda_1} (\bar{\mu}_L \sigma^{\mu\nu} \mu_R) F_{\mu\nu} \quad (g-2)_\mu$$

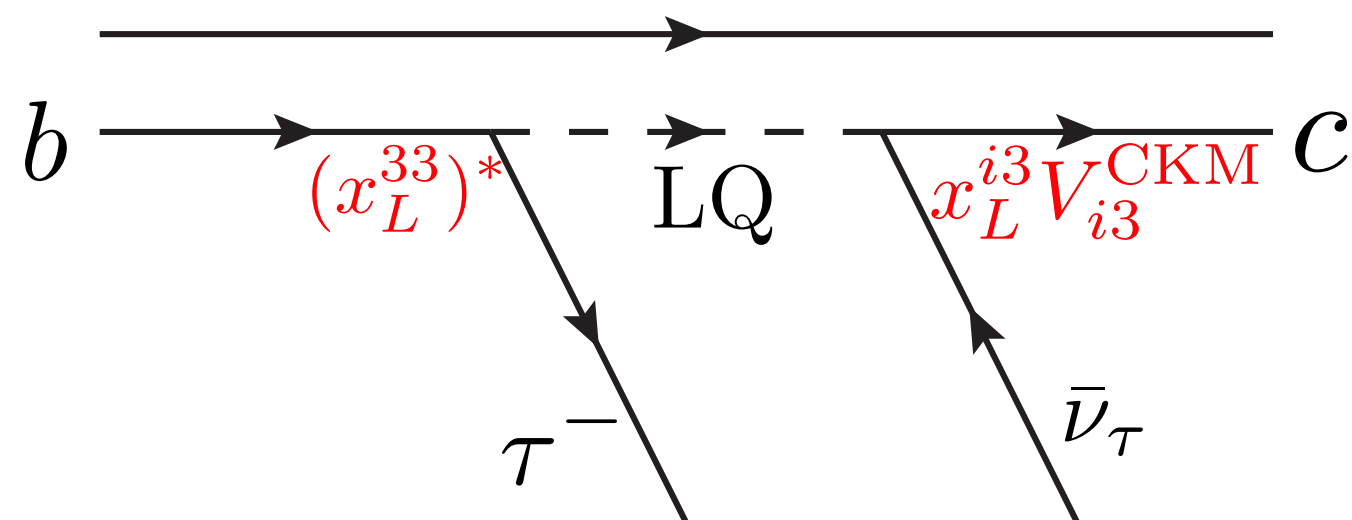
$$\Delta a_\mu \sim \frac{N_c}{16\pi^2} \cdot 4\text{Re}(x_L^{32} (x_R^{32})^*) \frac{m_b m_\mu}{m_{LQ}^2} (2Q_b - 2Q_{LQ})$$



$$\frac{1}{\Lambda_2^2} (\bar{s} \gamma_\mu P_L b) (\bar{\mu} \gamma^\mu \mu) \quad R_{K^{(*)}}$$

$$\text{Br}(B_s \rightarrow \mu\mu)$$

$$-\frac{x_L^{22} (x_L^{32})^*}{m_{LQ}^2} \subset [0.83, 1.41] \times 10^{-3} \text{ TeV}^{-2}$$

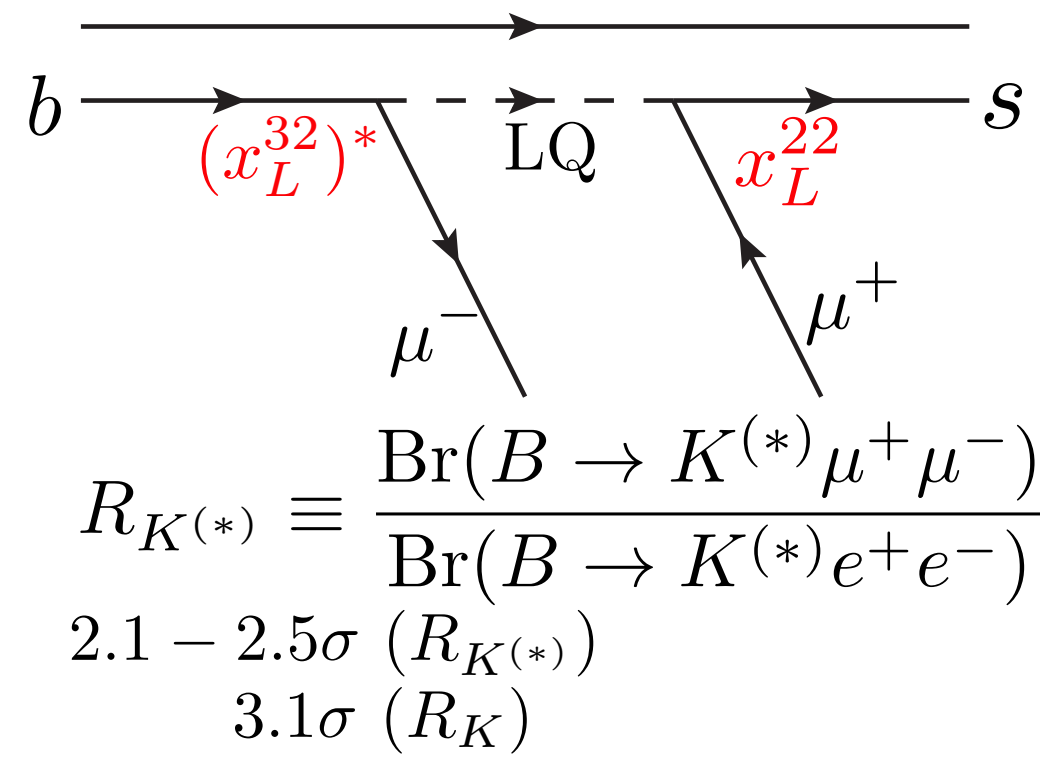


$$\frac{1}{\Lambda_3^2} (\bar{c} \gamma_\mu P_L b) (\bar{\tau} \gamma^\mu P_L \nu_\tau) \quad R_{D^{(*)}}$$

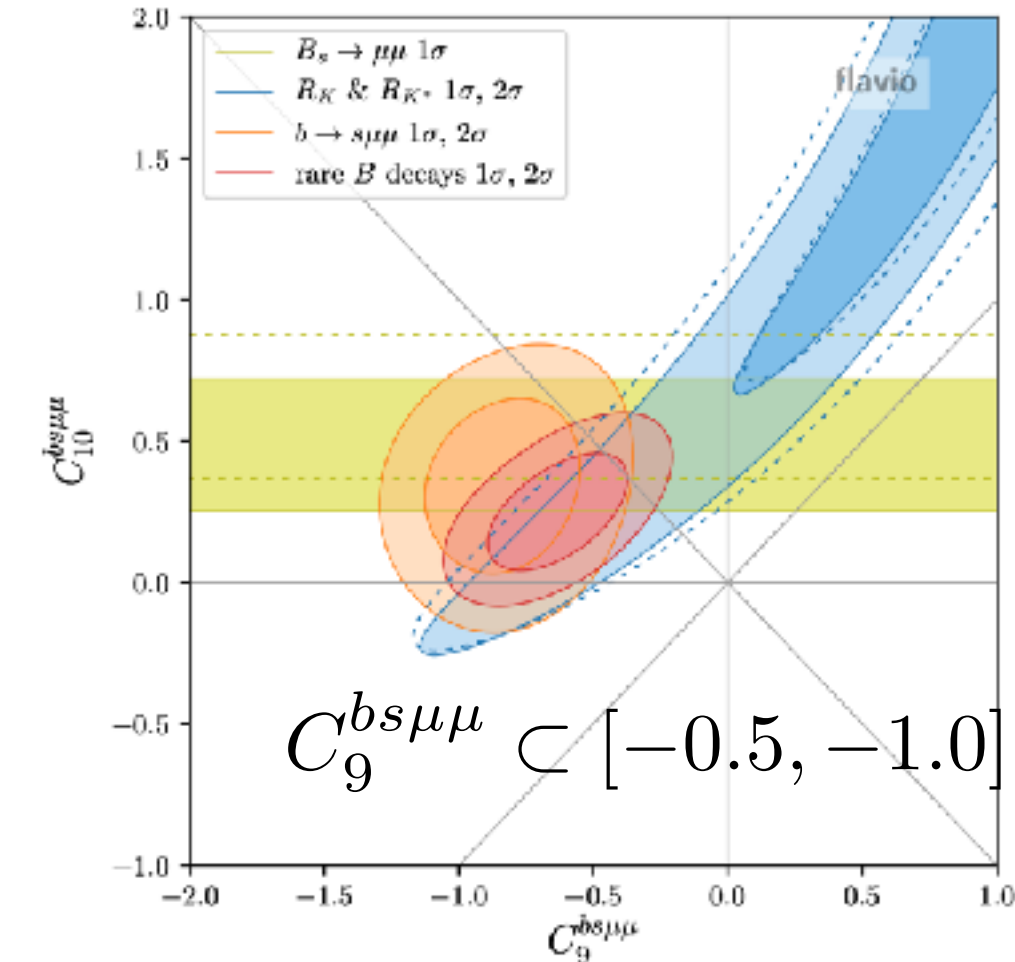
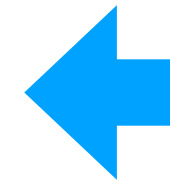
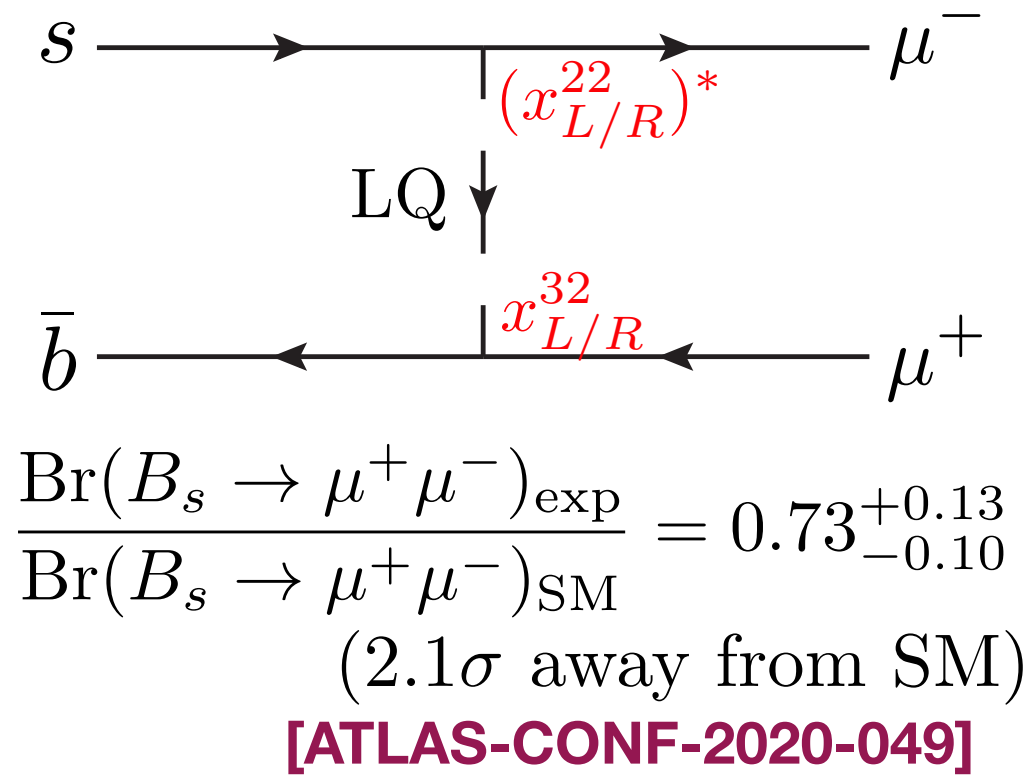
$$\frac{(V_{cs}^{\text{CKM}} x_L^{23} + V_{cb}^{\text{CKM}} x_L^{33}) (x_L^{33})^*}{m_{LQ}^2} \subset [0.12, 0.18] \text{ TeV}^{-2}$$

Ballpark & Constraints

W. Altmannshofer, P. Stangl [2103.13370]



+

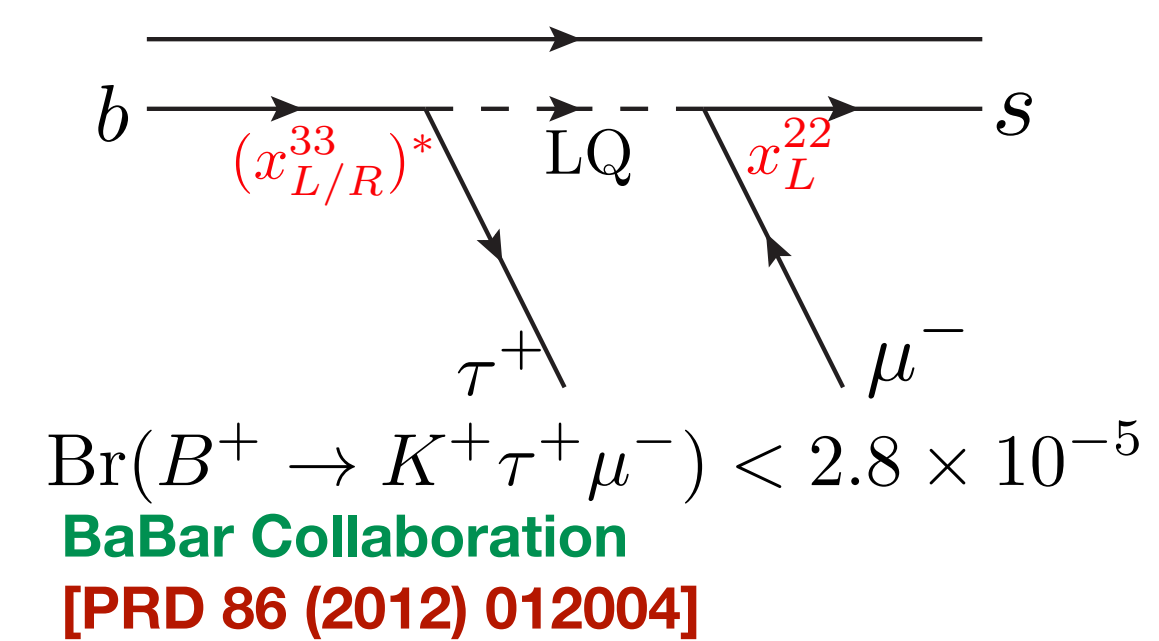
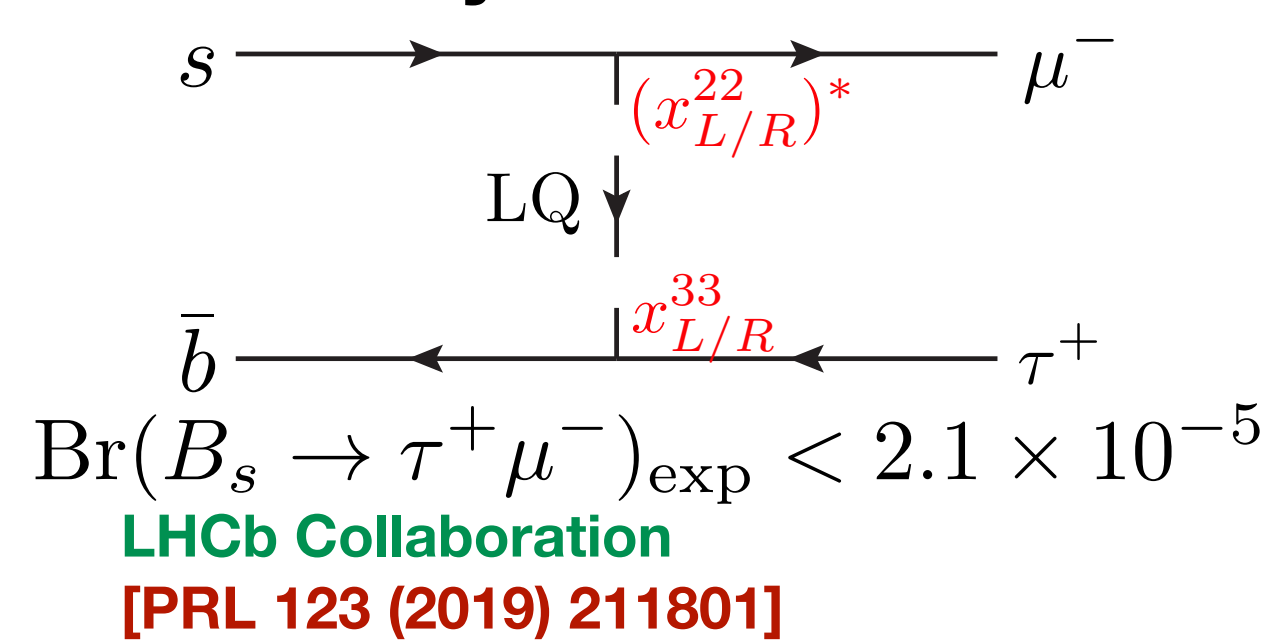
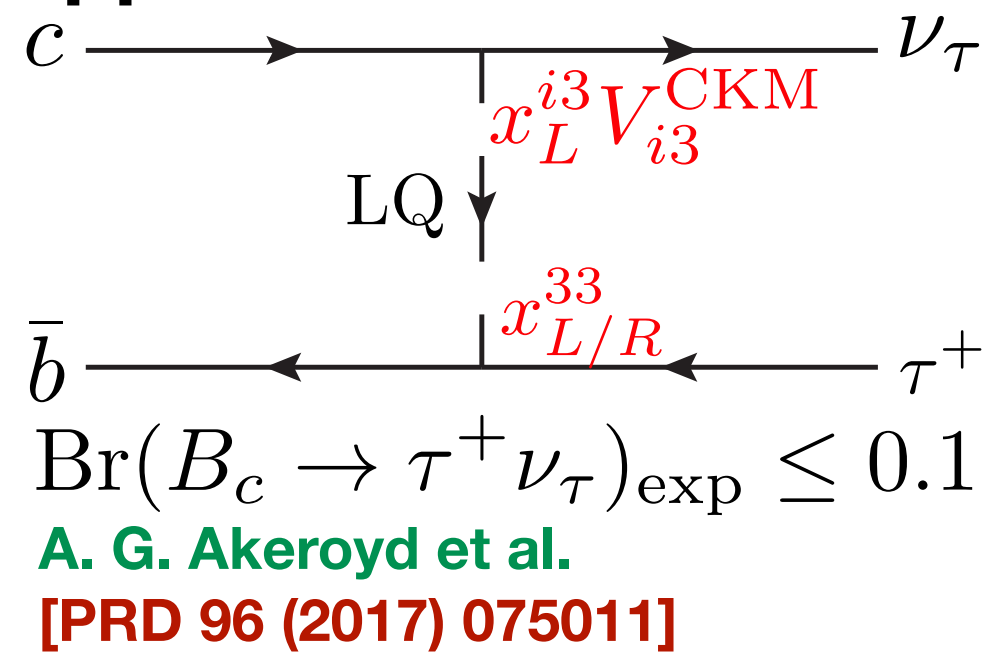


$$\mathcal{O}_9^{\ell_1 \ell_2} = \frac{e^2}{(4\pi)^2} (\bar{s} \gamma_\mu P_L b) (\bar{\ell}_1 \gamma^\mu \ell_2),$$

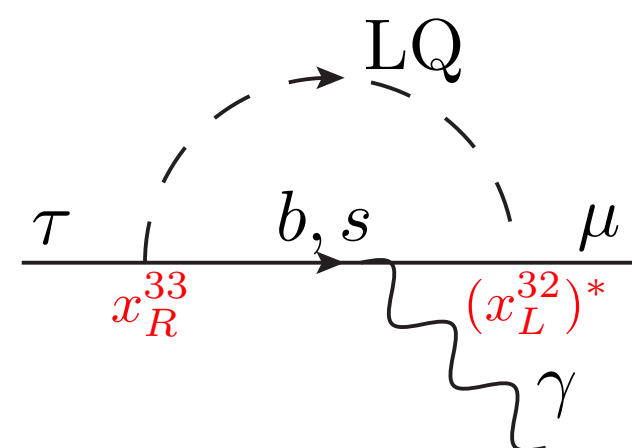
$$\mathcal{O}_{10}^{\ell_1 \ell_2} = \frac{e^2}{(4\pi)^2} (\bar{s} \gamma_\mu P_L b) (\bar{\ell}_1 \gamma^\mu \gamma^5 \ell_2),$$

(depends on scenarios / Wilson coefficients)

Upper limits from LFV in B-meson decays



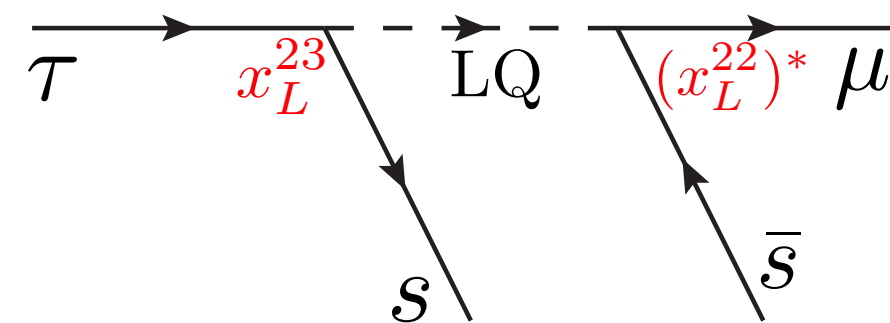
Upper limits from LFV in tau decays



$\text{Br}(\tau \rightarrow \mu \gamma) < 3 \times 10^{-8}$

Belle Collaboration
[PLB 666 (2008) 16]

BaBar Collaboration
[PRL 104 (2010) 021802]



$15 \text{Br}(\tau \rightarrow \mu \phi) < 5.1 \times 10^{-8}$

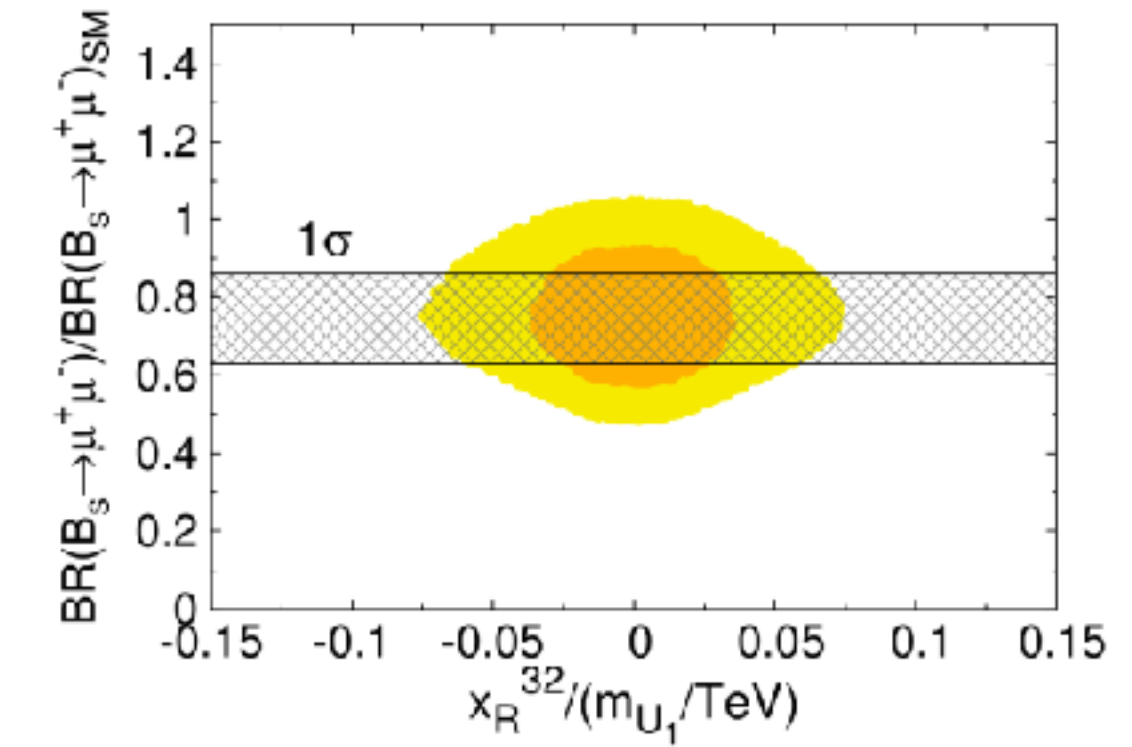
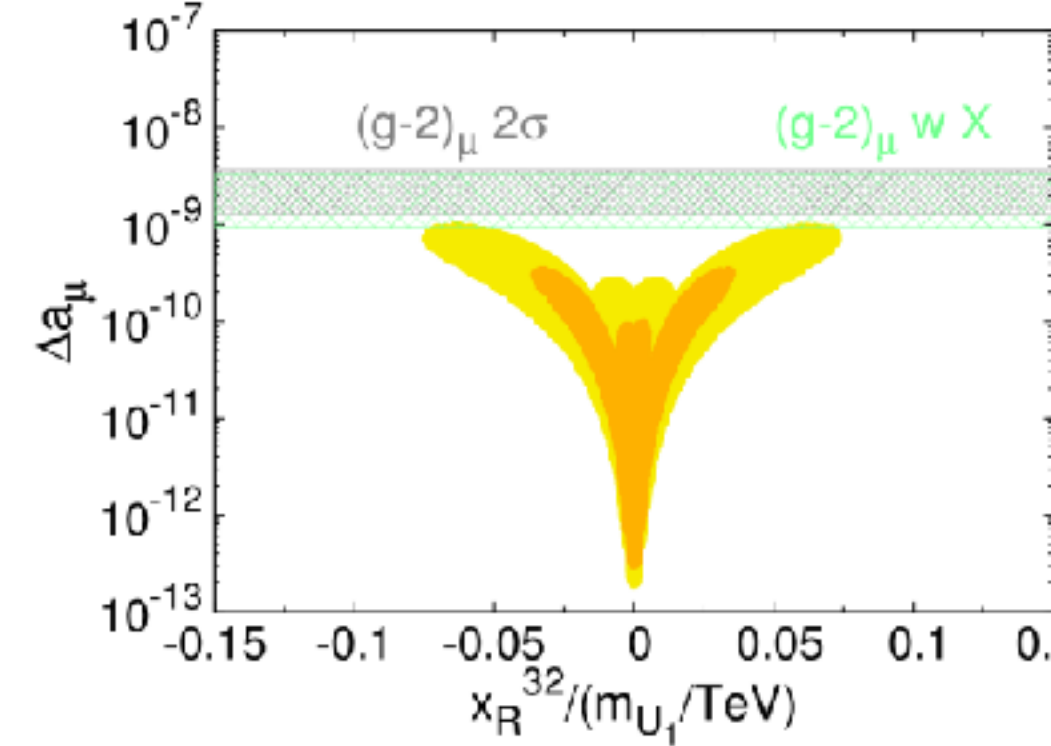
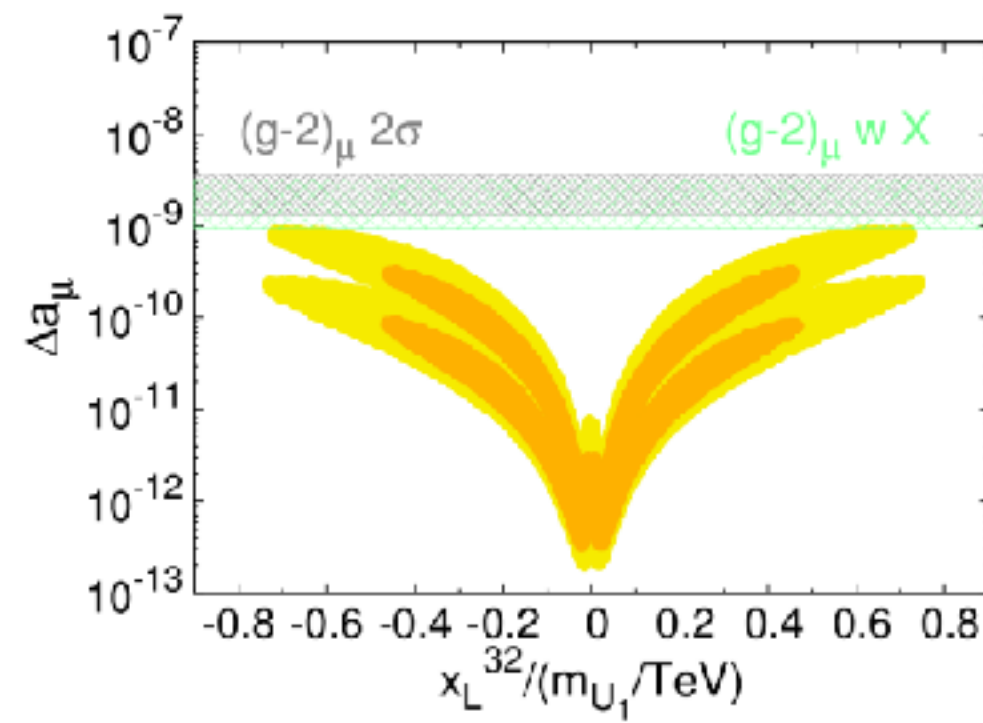
Belle Collaboration
[PLB 699 (2011) 251]

LQ + X for B-anomalies & (g-2)

for B-anomalies

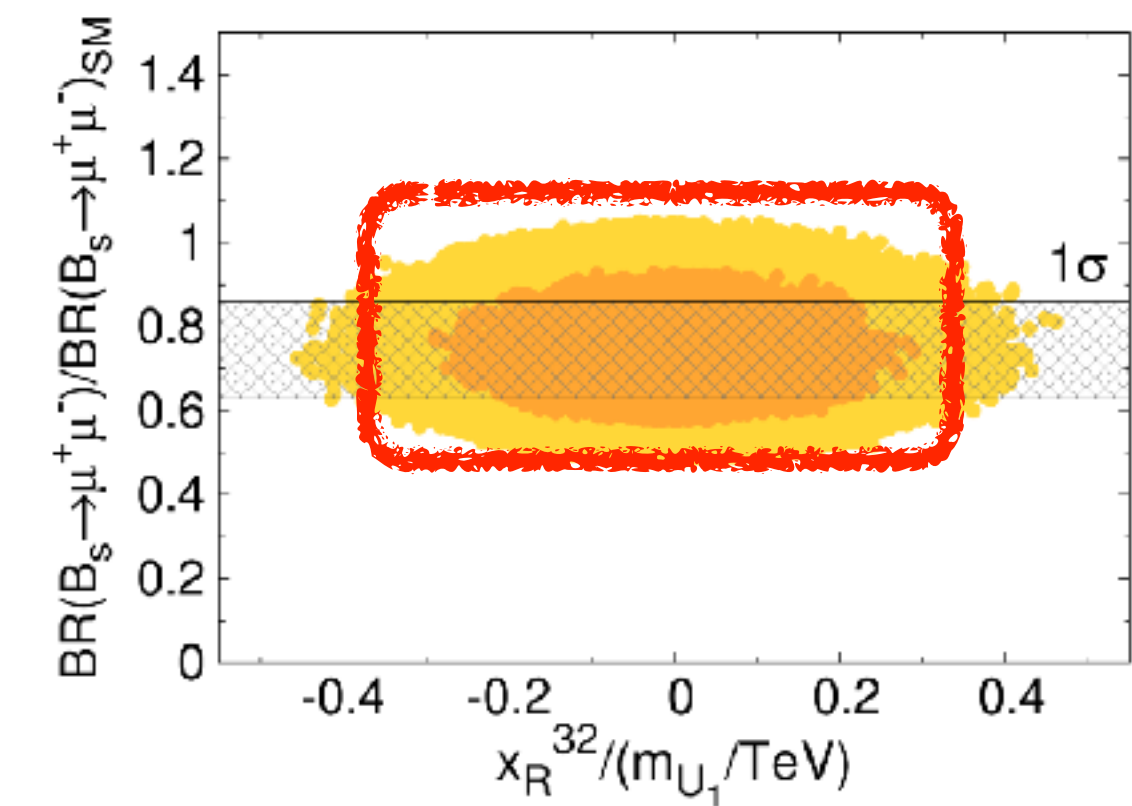
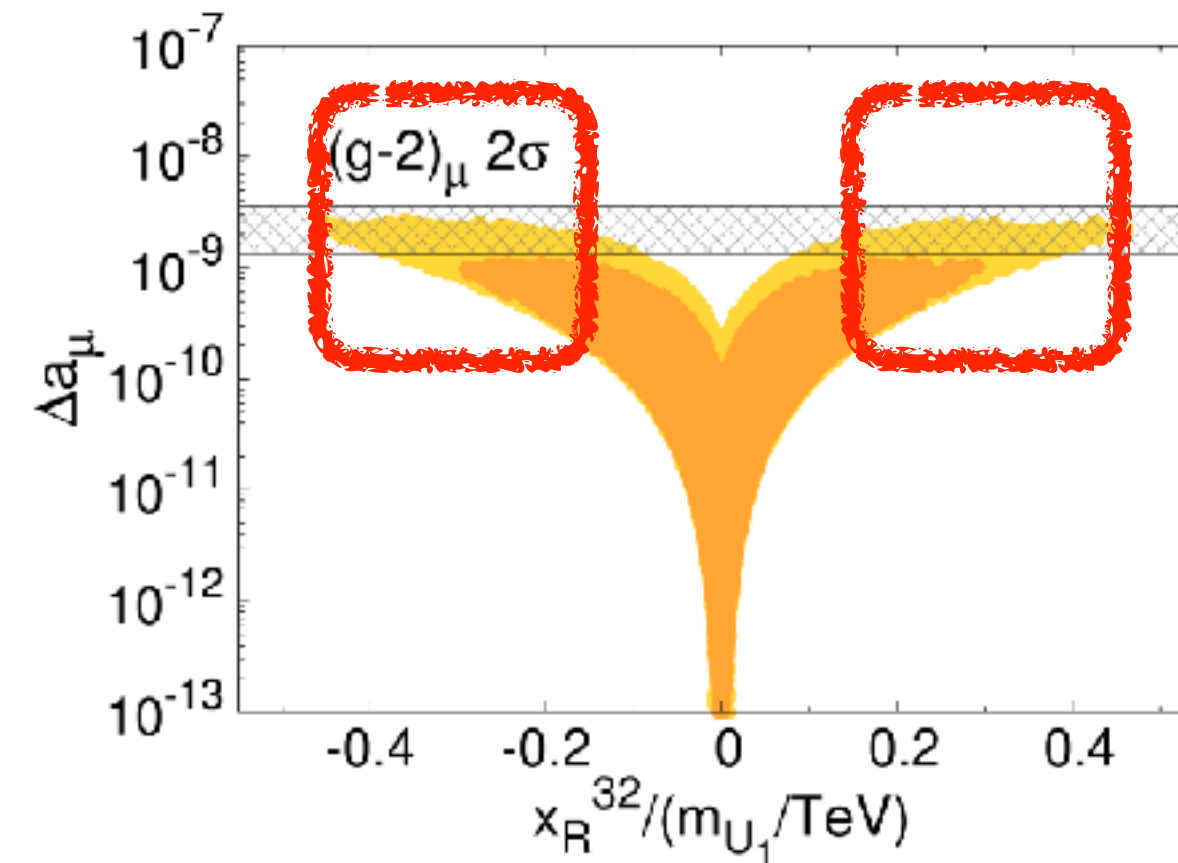
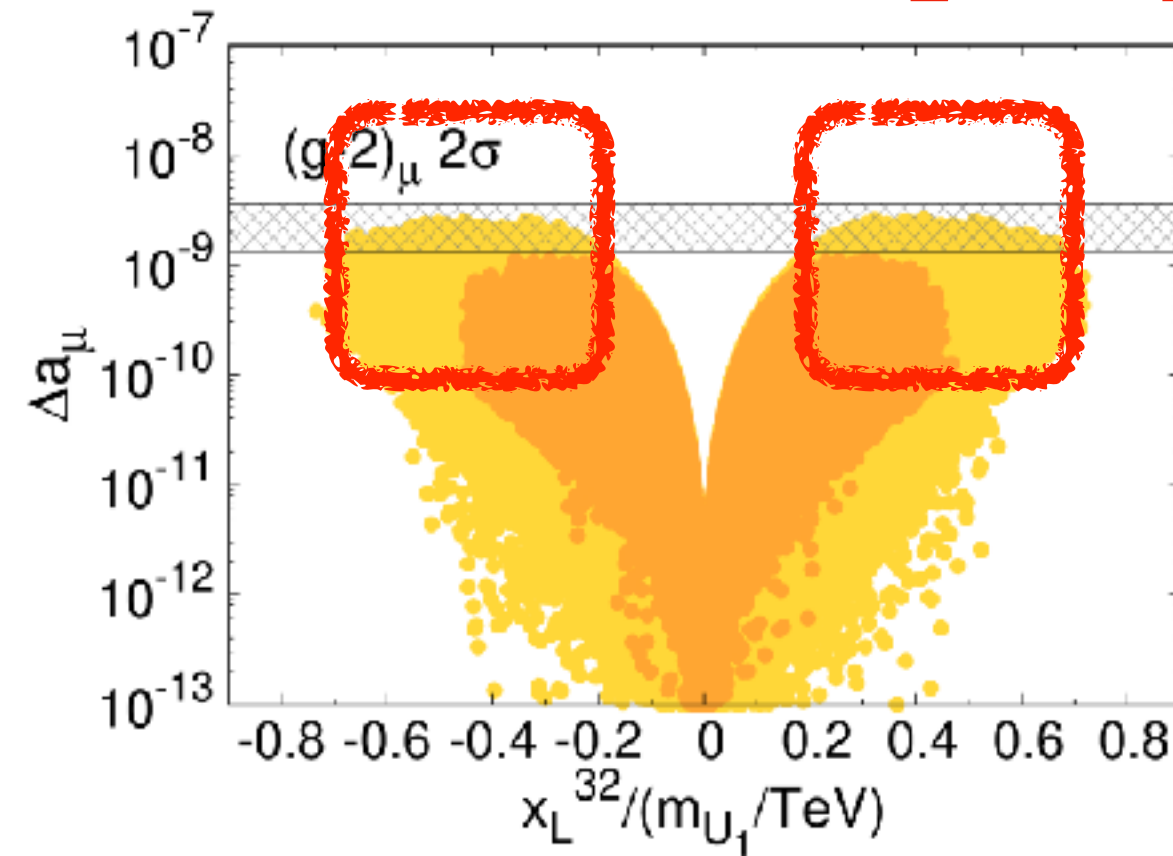
- $\Delta\chi \leq 5.99$
- $\Delta\chi \leq 2.30$

LQ only
 $m_{LQ} = 2\text{TeV}$



The couplings $x_L^{32} \sim x_R^{32} \sim 0.3$ & $U(1)_{B_3-L_2}$ X-boson provide an excellent explanation!

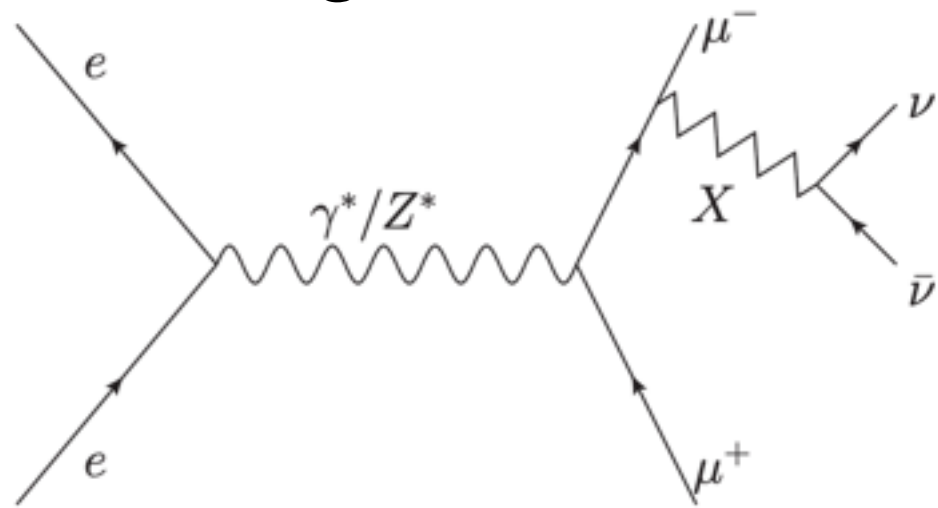
LQ + X
 $m_{LQ} = 2\text{TeV}$
 $m_X = 100\text{ GeV}$



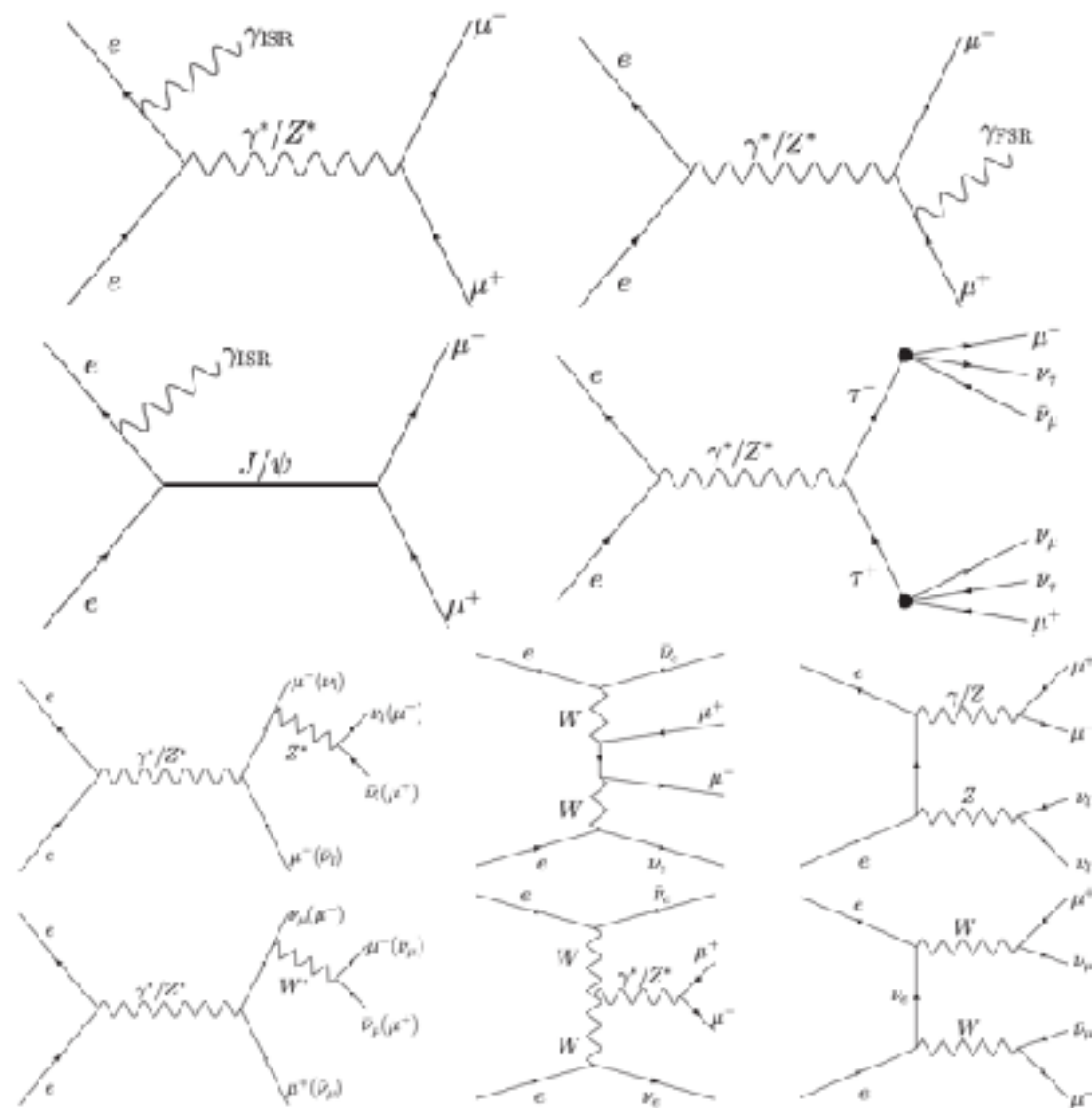
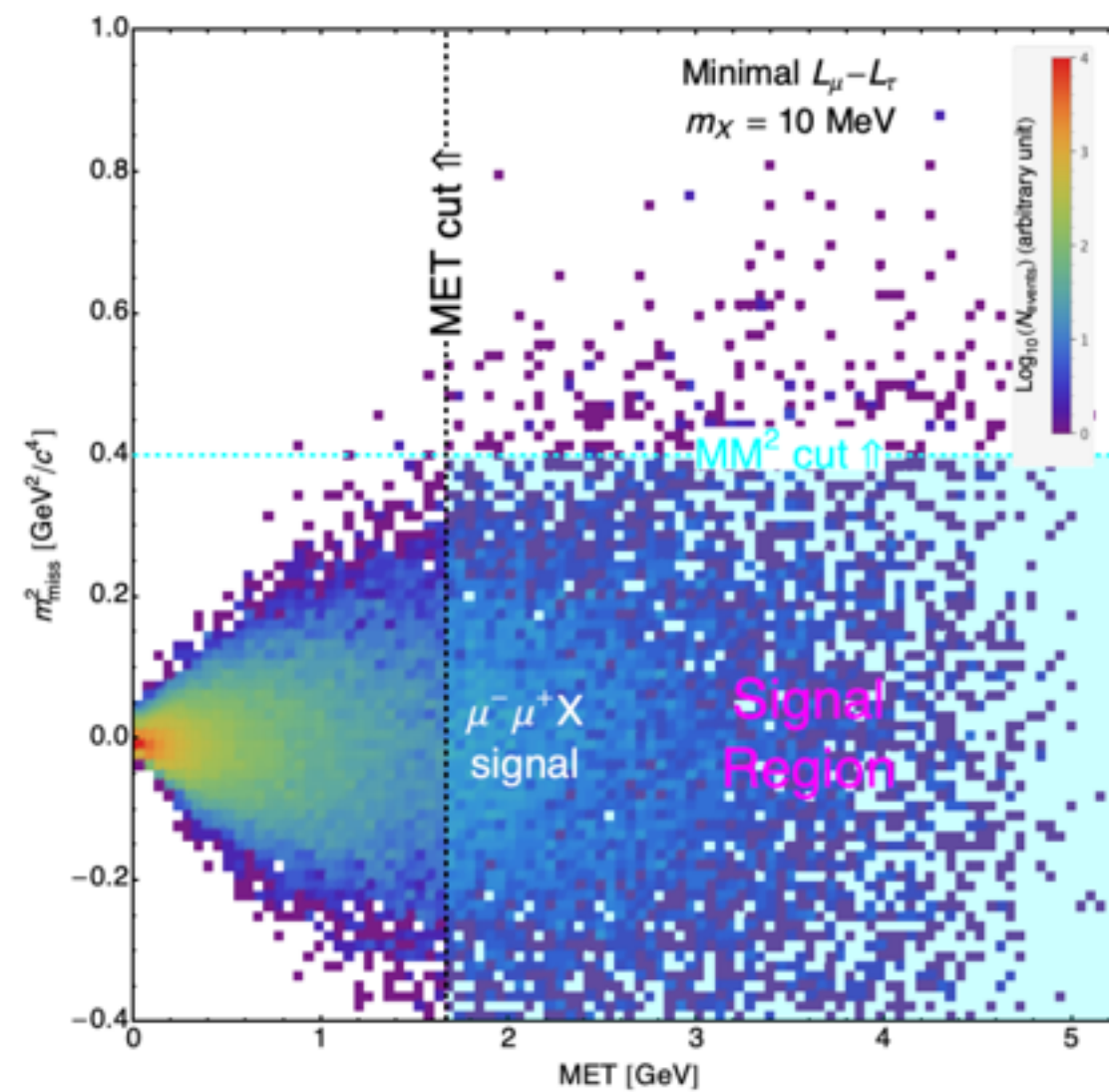
K. Ban, Y. Jho, Y. Kwon, SCP, S. Park, P.-Y. Tseng[2104.06656]

Searches of X at BELLE-II

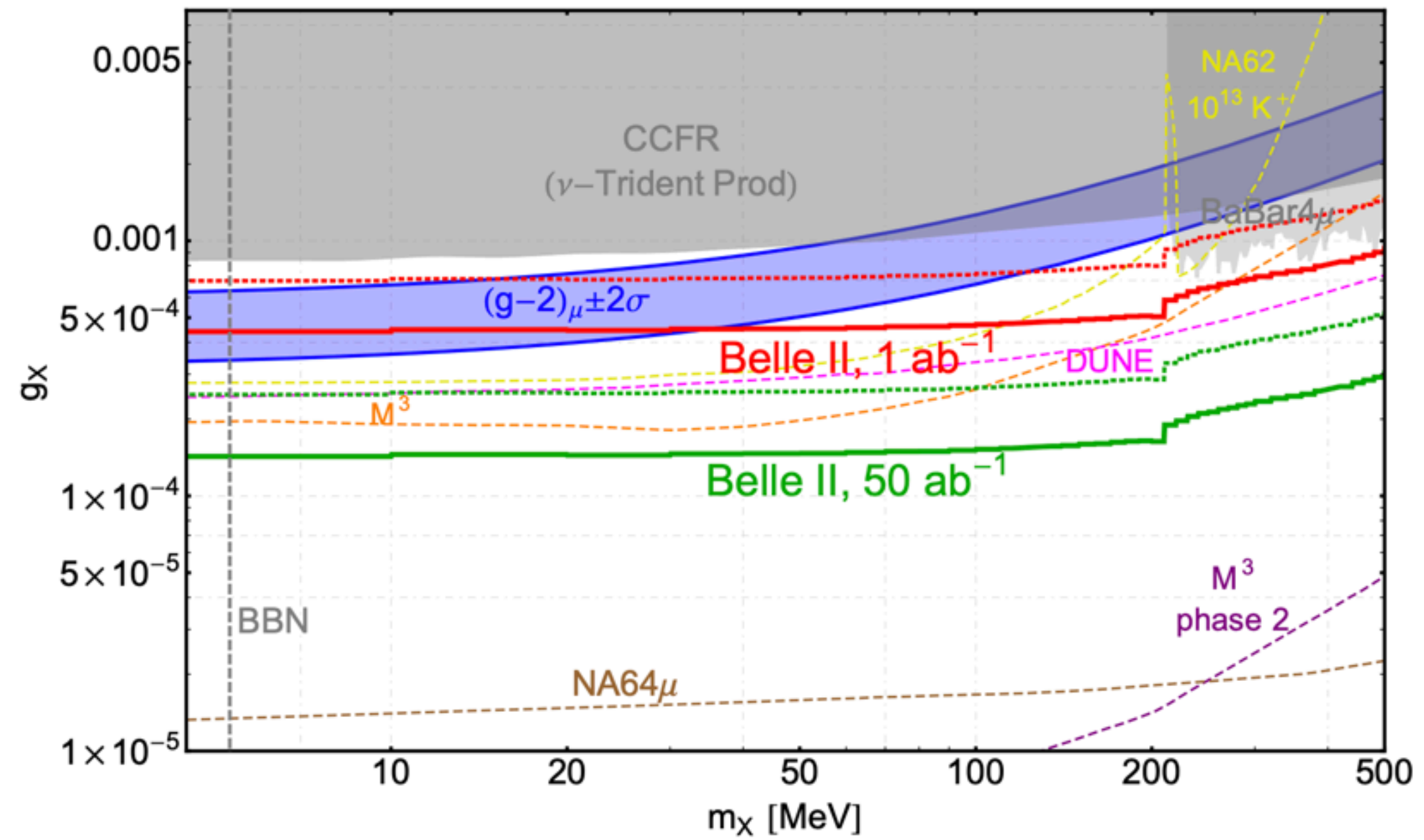
signal



background rejection
by MET, MM2, etc

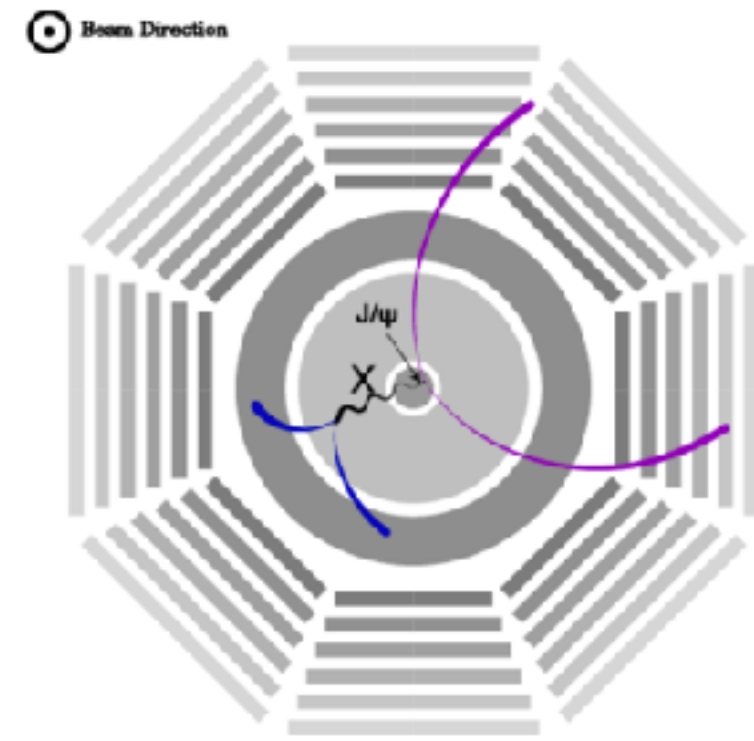
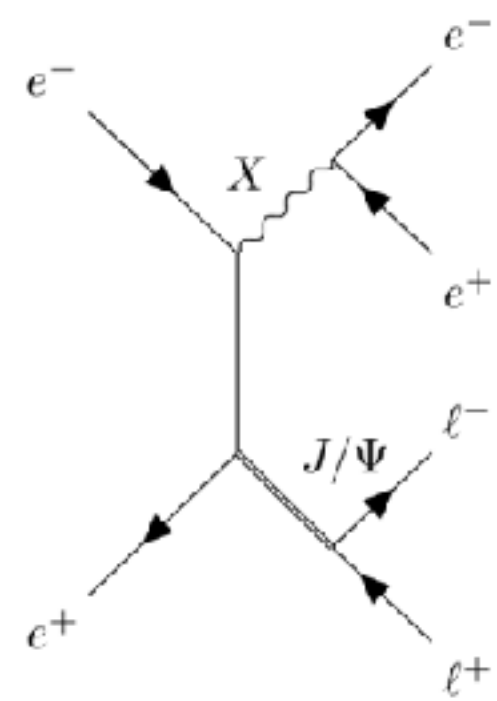


background

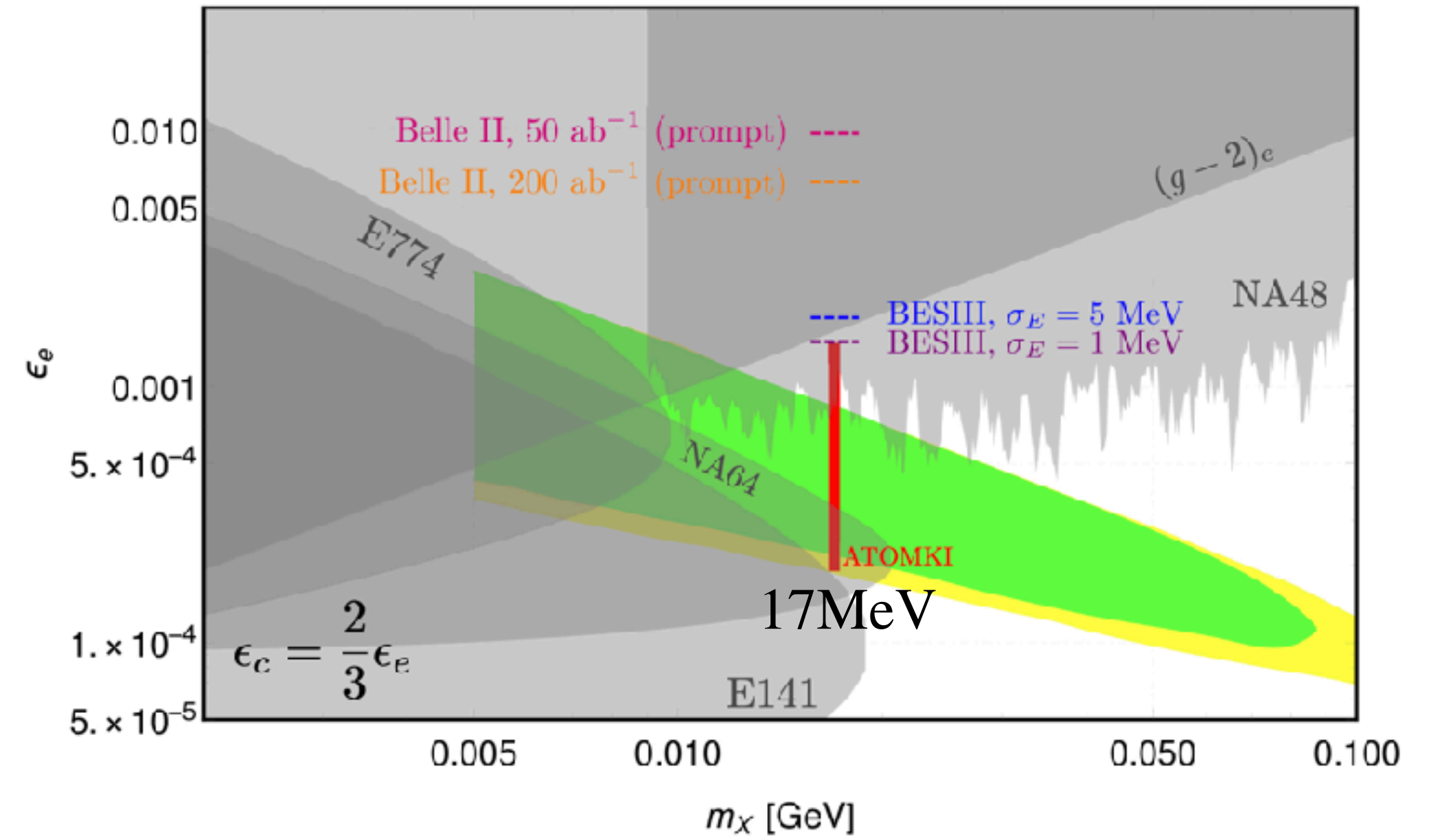


Y.S. Jho, Y.J.Kwon, SCP, P-y. Tseng, *JHEP* 10 (2019) 168 [1904.13053]

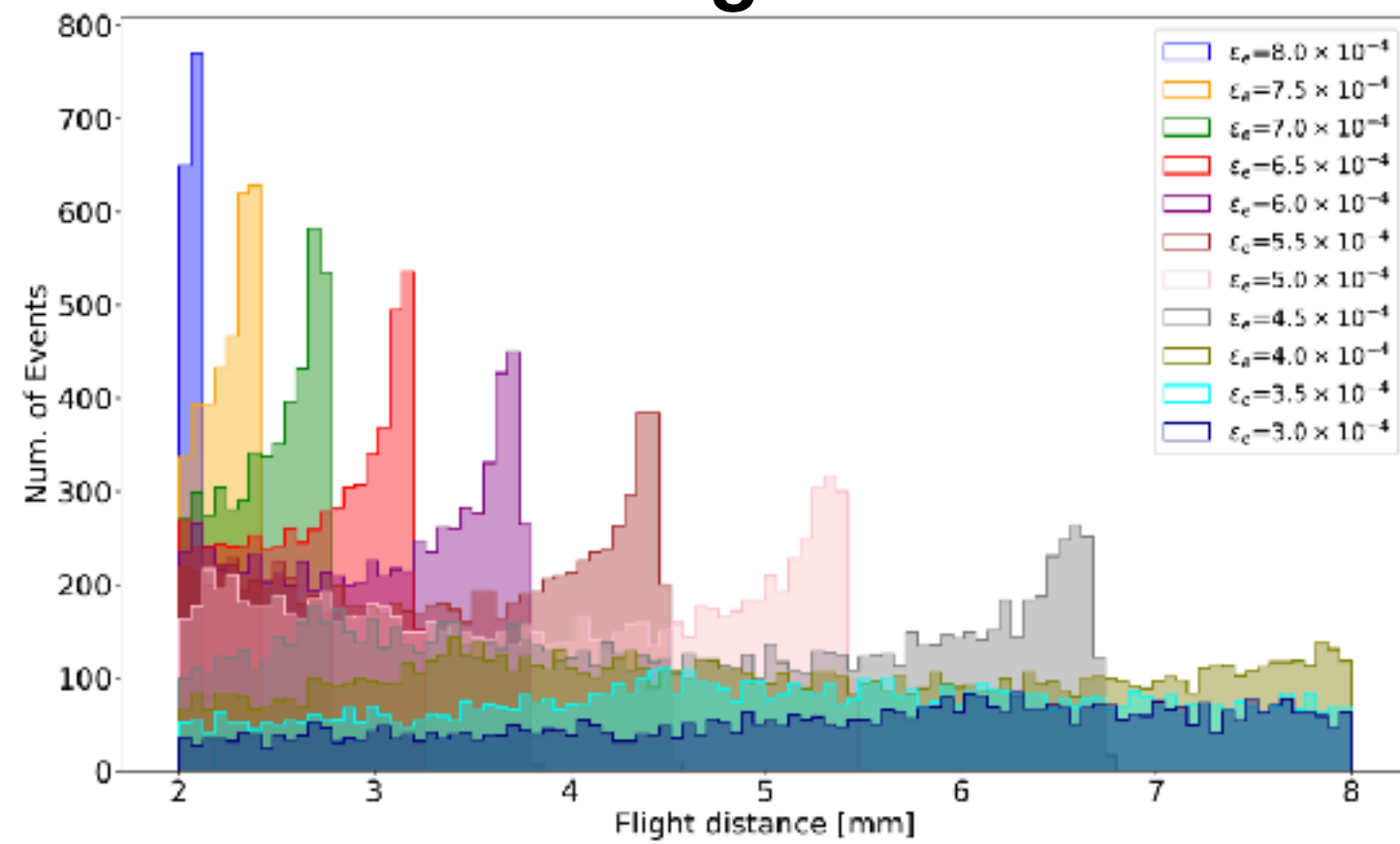
Searches of X at BELLE-II



$$g_X = e\epsilon_e$$



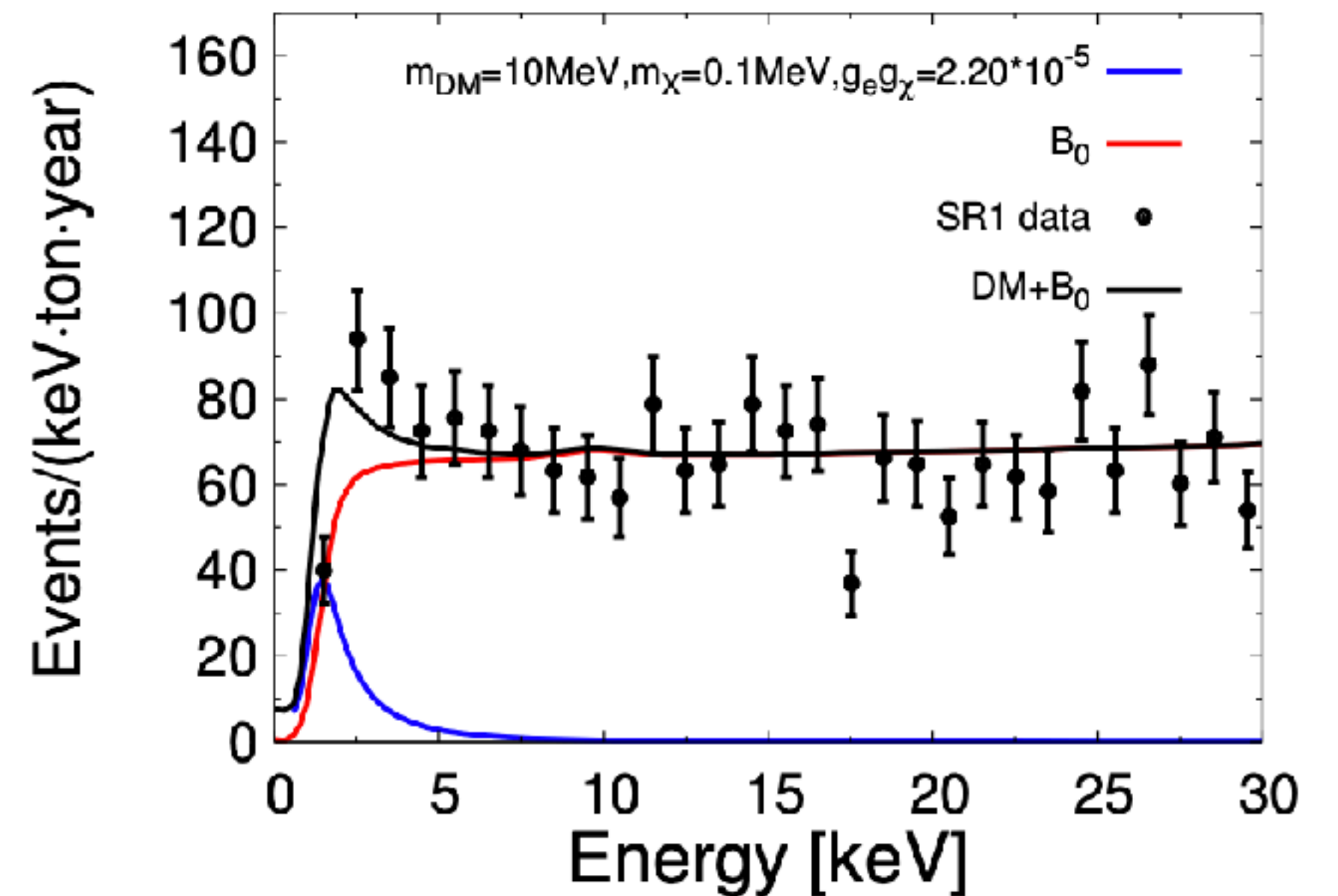
if Long lived



K. Ban, Y.S. Jho, Y.J.Kwon, SCP, S.Park *JHEP* 04 (2021) 091 [2012.04190]

New mediator for Dark sector

- The new force can be an excellent mediator for dark sector
- e.g. $\mathcal{L} \ni -X_\mu \left(g_\ell J_\ell^\mu + g_\chi J_\chi^\mu \right)$
- **NEW Boost mechanism:** CR electrons or CR neutrinos can boost DM and the boosted DM can be detected.
- e.g. Xenon1t_e O(1) keV electron recoil events with 3.5σ significance Xenon Collab. PRD 102 051702 (2020)



Y.S. Jho, J.C.Park, SCP, P-y. Tseng, PLB811 (2020) 2006.13910

Summary

- We are motivated to consider new leptonic interactions :
 $(g - 2)_\mu$, R_{D,D^*,K,K^*} , KOTO anomaly, DMe anomaly...
- Various theoretically well motivated possibilities exist :
 $L_i - L_j$, $B_i - L_j$, $(L_i - L_j) + x(B_i - L_j)$, and LQ etc...
- Using combinations of available models, we indeed can explain those anomalies (even though not necessarily by a single model)
- ‘Clean’ leptonic experiments (such as Belle-II, J-PARK, Xenon-nt, and **ILC**) are definitely helpful! Especially when MET/Missing Masses are involved and if New Physics only couples through leptons.