

# The virtual $\gamma$ saga

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ILD SW&ANA phone meeting

**CLUSTER OF EXCELLENCE**  
QUANTUM UNIVERSE



# The virtual $\gamma$ saga: Intro

- The process  $e^+e^- \rightarrow e^+e^- + f\bar{f}$  is **difficult to generate**: If the 4-momentum transfer between incoming and outgoing  $e^{+(-)}$  ( $= q \approx$  the scattering angle) becomes small, the process is dominated by scattering of virtual  $\gamma$ :s radiated off the  $e^{+(-)}$
- It becomes very hard to evaluate the phase-space integral from the full M.E. treatment, and event-generation becomes **very slow**.
- At some lowest  $q$ , we **switch** from the **M.E.** treatment to the *equivalent photon approximation* (**EPA**), where the flux of **virtual** (or better “**quasi-real**”) photons is evaluated, and the process becomes  $\gamma\gamma \rightarrow f\bar{f}$ , i.e. a  $2 \rightarrow 2$  process.
- NB: In both cases, there is a **minimum**  $M_{f\bar{f}}$  (4 GeV for  $\mu$ :s and  $e$ :s,  $2 \times M_\tau$  for  $\tau$ :s, 10 GeV for quarks)

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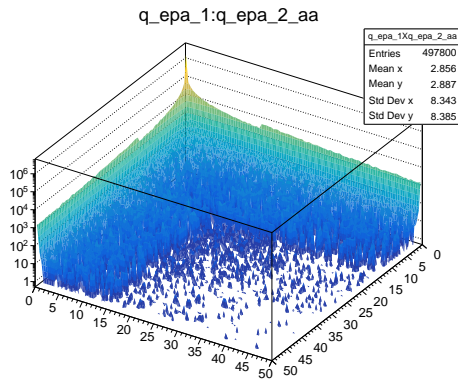
## HOWEVER ....

- The regions don't match !
- A jump  $\sim$  factor 1/2 for each  $e^{+(-)}$  replaced by an EPA...
- Also the shapes at the junction are different...

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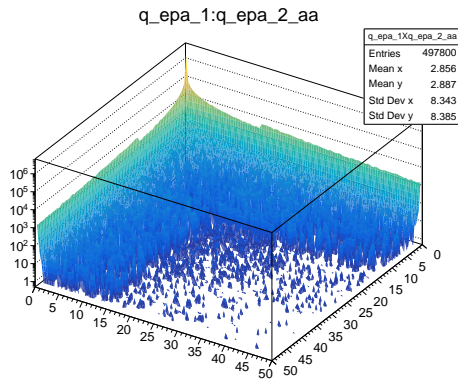




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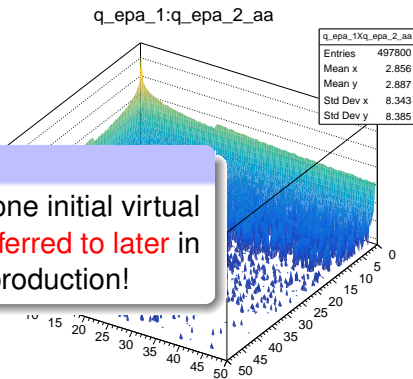
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So:

All channels with at least one initial virtual  $\gamma$  have up to now been **deferred to later** in the 250 GeV mass-production!



# The virtual $\gamma$ saga: Problem solved!

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  - There *is* indeed a factor  $\equiv 2$  missing per virtual photon if beam-polarisation is on !
- It is clear that the default cut in  $Q^2$  between the M.E. and the EPA methods of generating  $e^+e^- \rightarrow e^+e^- + X$  is *too high* wrt the cut on  $m_X$ .
- This I've studied, and found that  $\sqrt{|Q^2|} = 0.2$  is a good separation, even for a cut  $m_X$  at 4. The cut in  $\sqrt{|Q^2|}$  in the existing M.E. samples is at 4, so there is a missing part for  $\sqrt{|Q^2|} \in [0.2, 4]$
- Tip from Filip:
  - There *is* a way to emulate an OR in the cuts-definition in the sindarin ( $a \vee b \Leftrightarrow \neg(\neg a \wedge \neg b)$  ...)  $\Rightarrow$  The "L-shaped" missing phase-space in the M.E. part of  $e^+e^- \rightarrow e^+e^- + X$  can be generated in a single step.

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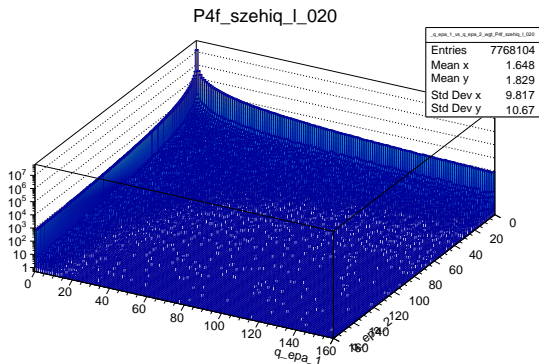
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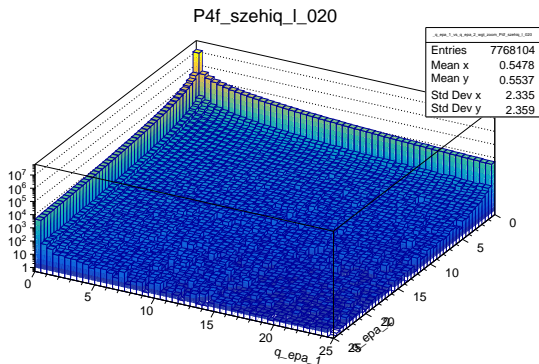
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- Full range ( $\gamma\gamma$ ,  $e^+e^-\gamma$  and M.E. high and low  $Q^2$ )
- Transition M.E. high and low  $Q^2$
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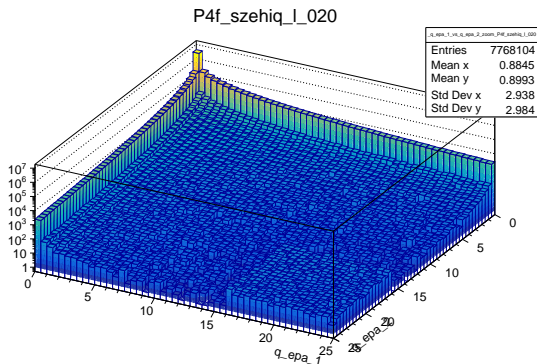
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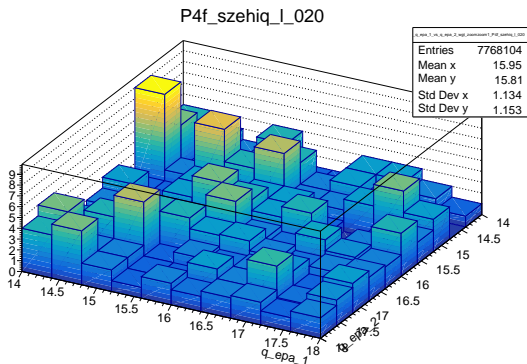
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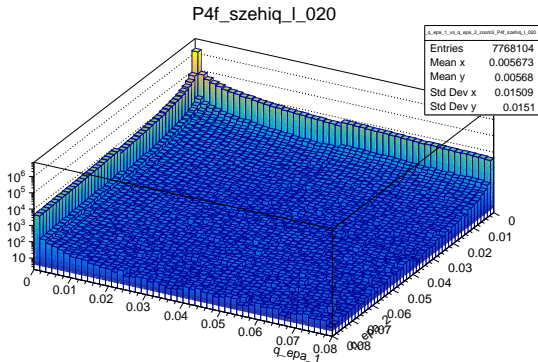
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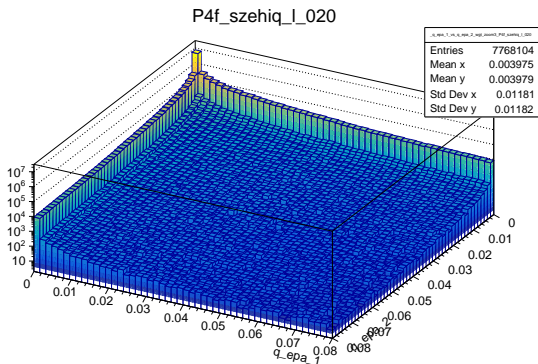
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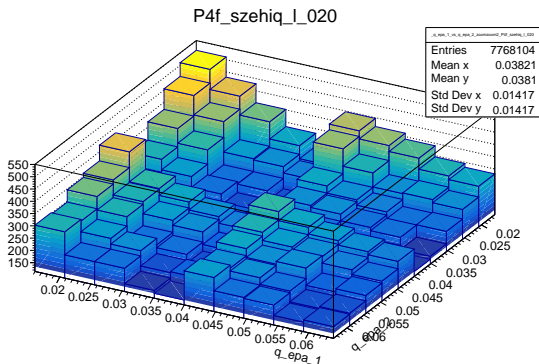
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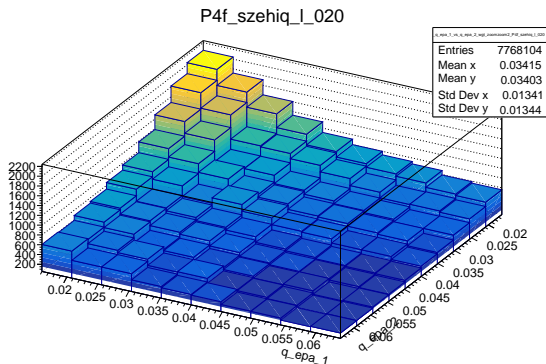
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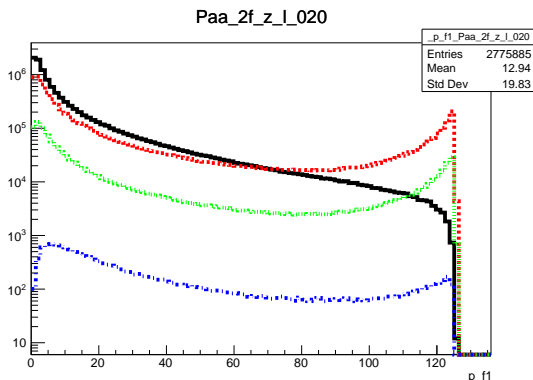
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# Properties of new events (for $\int \mathcal{L} = 5 \text{ fb}^{-1}$ )

In all plots: black = aa, red = ae, green = M.E., low  $Q^2$ , and blue = M.E., high  $Q^2$ .

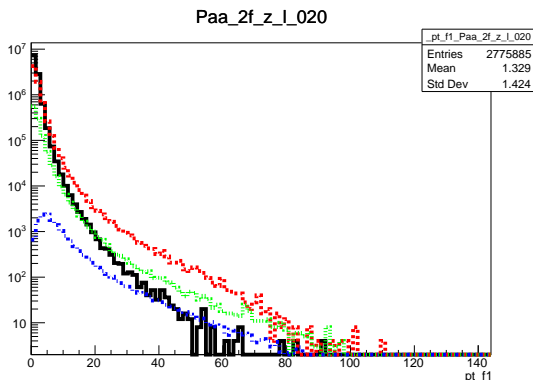
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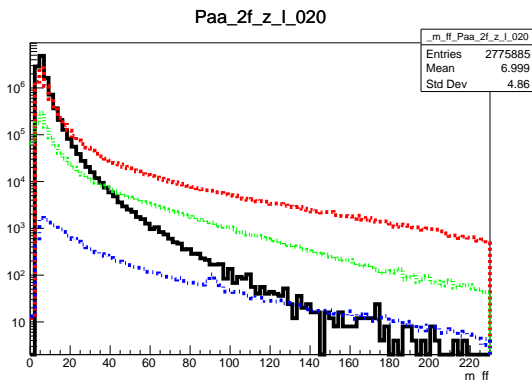
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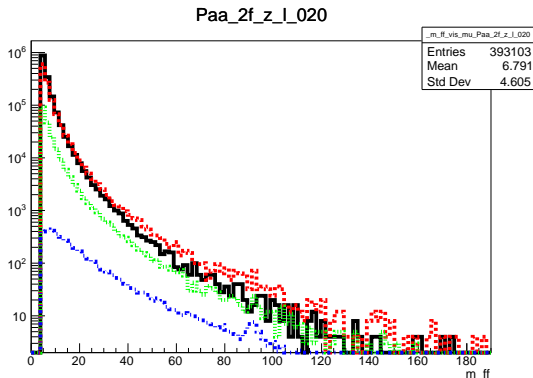




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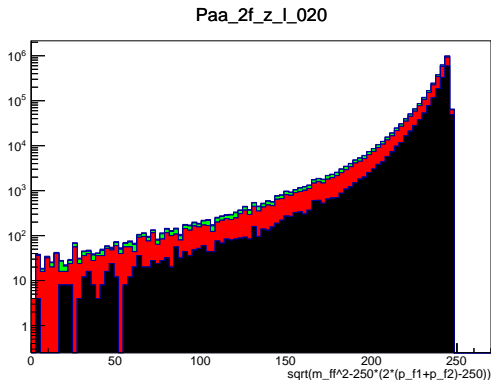
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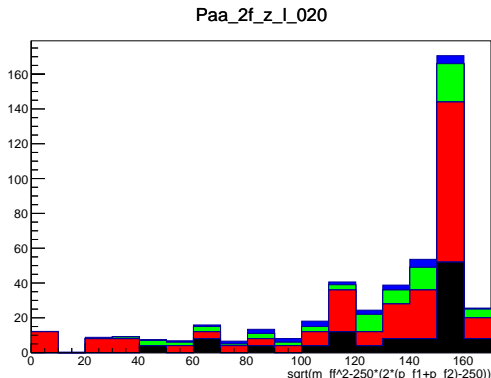
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# Cross-sections of new samples

sample	leptonic pb	hadronic pb	# Mevents	suggestion ( $\sim 1$ year)
aa_2f	2220	122	2342	426
ae_3f	1490	139	3258	296
ea_3f	1486	140	3252	296
4f_szeloq (LL and RR)	442	68.5	27	27
4f_szeloq (LR and RL)	448	69.1	138	138
Total			9017	1183

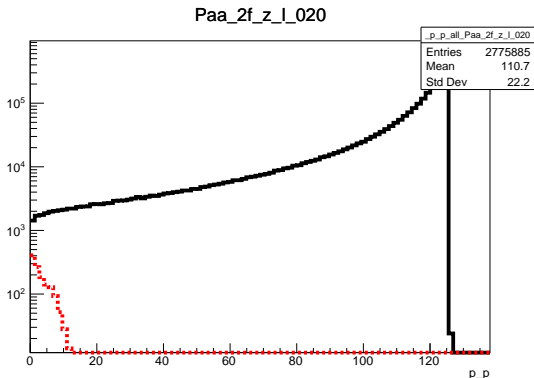
Numbers using the **standard assumptions**:  $1 \text{ ab}^{-1}$  for each of aa\_2f, ae\_3f and ea\_3f (for the latter two:  $\times 2$  polarisations),  $1 \text{ ab}^{-1}$  for each of 4f\_szeloq LR and RL, and  $0.2 \text{ ab}^{-1}$  for each of 4f\_szeloq LL and RR.

**However:** Note that the **standard assumptions** is *a lot*. The  $5/1/1/5 \text{ ab}^{-1}$  for the “normal” samples is  $\sim 10$  times the full H20 statistics, and the reduced  $1/0.2/0.2/1$  is still more than the 11 years of H20 running, except for aa\_2f, where it is about  $1/2$  of H20 .

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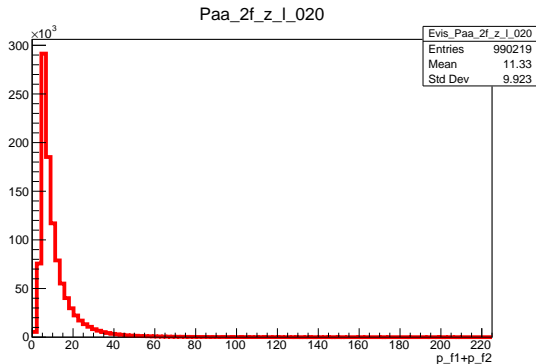
- Just 0.04 % of the events will have a beam-remnant seen in the BeamCal, and then it only deposits a few GeV.
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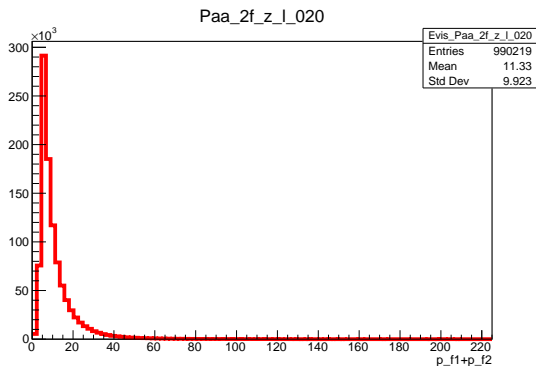
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- So, the average seen energy for the **aa\_2f** class is only 11 GeV = 4 % of 250 GeV.
- Also the **ae/ea\_3f** events are smaller than “typical” events: One beam-remnant is down the beam-pipe, but also the other, high  $Q^2$ , one is in 25 % of the events.
- The average seen energy is  $\sim 94$  GeV in this case = 37 % of 250 GeV.
- Both aa\_2f and ae/ea\_3f are mainly leptonic: 94 % and 91 %, respectively.
- All this indicates that simulation ( $\propto E_{vis}$ ), and reconstruction ( $\propto E_{vis}$  and multiplicity) should be **much faster** than for the “typical” events.
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- Need to check how much of these we can afford to generate:
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  - ... but events are **small**.
- $\Rightarrow$  Need to check simulation and reconstruction for **CPU and disk-space/event**, and then decide.
- Note that even though the big samples are only 9 channels, there are lots of **small cross-section channels** also to be done ( $e^+e^- \rightarrow e^+e^- + f\bar{f}f'\bar{f}' \dots$ ).
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