

BSM Triple Higgs Couplings at the LHC

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based on [arXiv: 2212.11242](https://arxiv.org/abs/2212.11242) with Francisco Arco, Sven Heinemeyer and Margarete Mühlleitner

IDT-WG3-Phys Open Meeting

09.02.2023



The 2HDM model

[Santos, Barroso: [arXiv: 9701257](https://arxiv.org/abs/9701257)]

- **CP conserving** 2HDM with two complex doublets: $\Phi_1 = \begin{pmatrix} \phi_1^+ \\ \frac{v_1 + \rho_1 + i\eta_1}{\sqrt{2}} \end{pmatrix}, \Phi_2 = \begin{pmatrix} \phi_2^+ \\ \frac{v_2 + \rho_2 + i\eta_2}{\sqrt{2}} \end{pmatrix}$
- **Softly broken \mathbb{Z}_2 symmetry** ($\Phi_1 \rightarrow \Phi_1; \Phi_2 \rightarrow -\Phi_2$) entails 4 Yukawa types (Types I and II were analyzed)

h ($m_h = 125$ GeV), **H** - CP even, **A** - CP odd, **H^+, H^-**

- Potential:
$$V_{2\text{HDM}} = m_{11}^2 (\Phi_1^\dagger \Phi_1) + m_{22}^2 (\Phi_2^\dagger \Phi_2) - m_{12}^2 (\Phi_1^\dagger \Phi_2 + \Phi_2^\dagger \Phi_1) + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \frac{\lambda_5}{2} ((\Phi_1^\dagger \Phi_2)^2 + (\Phi_2^\dagger \Phi_1)^2)$$

- Free parameters: $m_h, m_A, m_H, m_{H^\pm}, m_{12}^2, v, \cos(\beta - \alpha), \tan\beta$

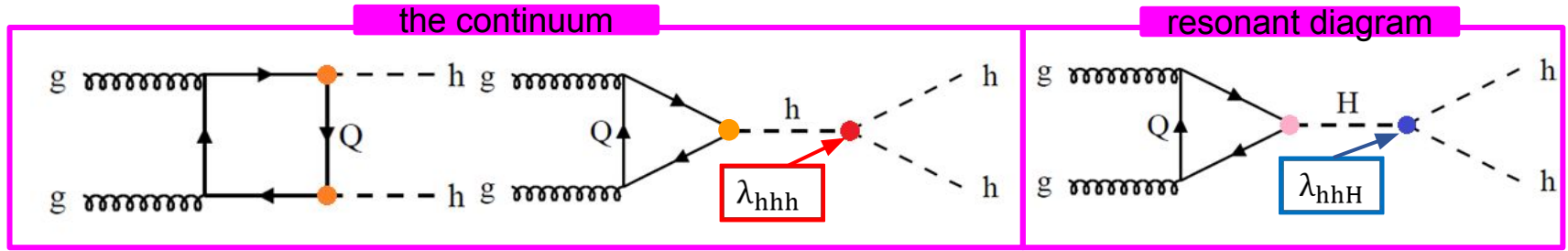
$$\tan\beta = v_2/v_1 \\ v^2 = v_1^2 + v_2^2 \sim (246 \text{ GeV})^2$$

- **Phenomenological implications** can originate from:
 - deviations in **couplings** to fermions and gauge bosons
 - contributions of the **heavy scalars** in the loops

Di-Higgs production ($gg \rightarrow hh$)

[Plehn, Spira, Zerwas : [arXiv: 9603205](#)]

- Triple Higgs couplings can be accessed through **Higgs pair production**
- The dominant process at a hadron collider is **gluon fusion** involving a quark loop



Diagrams that exist in the SM:
They have a negative interference

$$\sigma_{\text{SM}} \sim 38 \text{ fb at NLO}$$

Diagrams that are sensitive
to triple Higgs couplings

- We will study the **invariant mass distribution** of two 125 GeV in the final state
- All calculations were done using a modified version of the code **HPAIR**

[Abouabid, Arhrib, Azevedo, El Falaki, Ferreira, Mühlleitner, Santos: [arXiv: 2112.12515](#)]

Triple Higgs Couplings

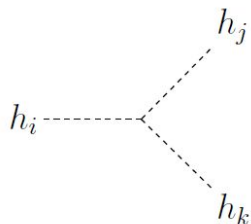
[ATLAS-CONF-2022- 050]

- Can have **large deviations** from SM predictions in BSM:

$$\kappa_\lambda = \lambda_{hhh} / \lambda_{hhh}^{SM} \quad [-0.4 < \kappa_\lambda < 6.3] \text{ (95\% CL at LHC Run II)}$$

$$\lambda_{hhh}^{SM} = \frac{m_h^2}{2v^2} \cong 0.129$$

- Higher luminosity needed → what can be expected from HL-LHC?

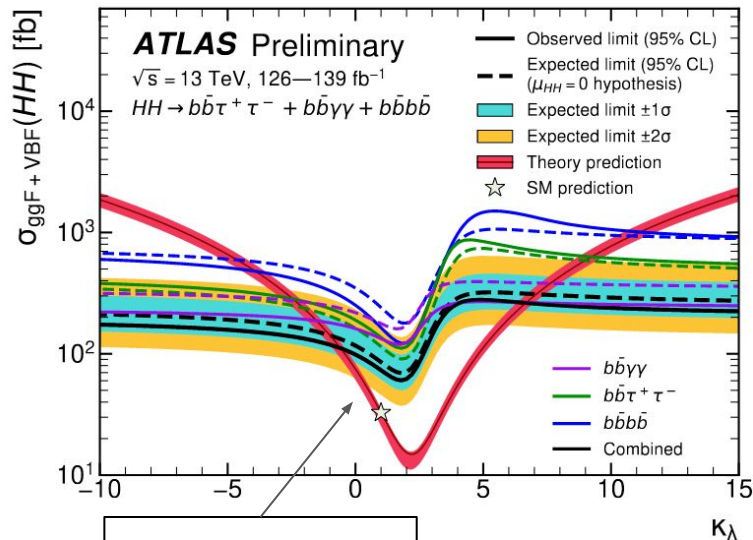


$$= -i v n! \lambda_{h_i h_j h_k}$$

n = number of identical Higgses
All couplings are at tree level

- Notation:

Large λ 's were found: far from the alignment limit and/or for large scalar masses



Type I

$$\kappa_\lambda = [-0.5, 1.3]$$

$$\lambda_{hhh} = [-1.7, 1.6]$$

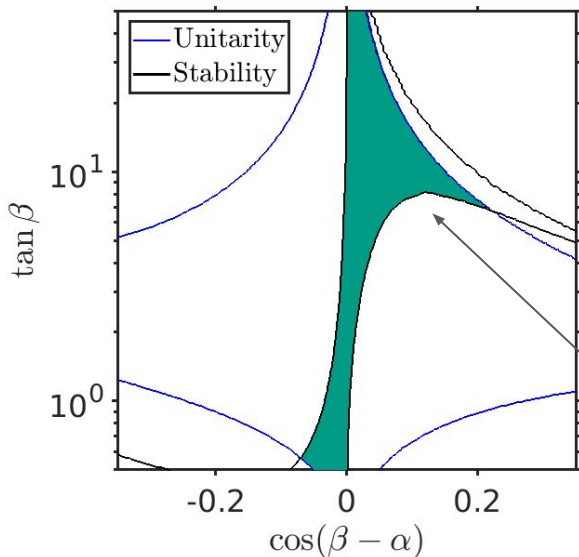
[Arco, Heinemeyer, Herrero: [arXiv: 2003.12684](https://arxiv.org/abs/2003.12684)]

Benchmark planes

[Arco, Heinemeyer, Herrero: [arXiv: 2005.10576](https://arxiv.org/abs/2005.10576)]

We scan the 2HDM parameter space fixing all but two parameters and look for large deviations in the trilinear Higgs couplings from the SM in the resulting benchmark planes

$$\text{Type I, } m_H = m_A = m_{H^\pm} = 1000 \text{ GeV, } m_{12}^2 = m_H^2 \cos^2 \alpha / \tan \beta$$



- **EWPO** → impose a condition on the Higgs boson masses:
 $(m_{H^\pm} - m_H) \sim 0$ and/or $(m_{H^\pm} - m_A) \sim 0$

- Theoretical:

Unitarity: from the $2 \rightarrow 2$ processes scattering amplitude

Stability: boundedness from below of the potential

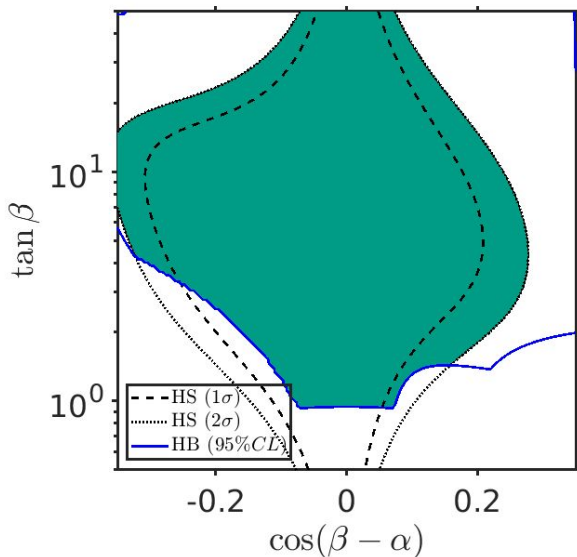
Colored area is allowed!

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- Collider searches and measurements:

Higgs Bounds: experimental limits from direct searches

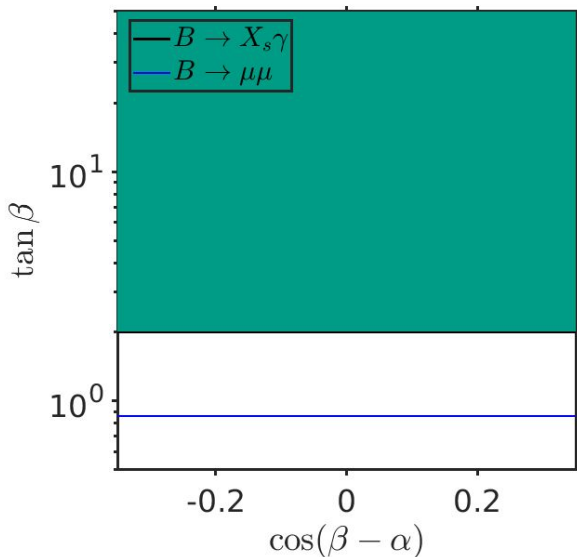
Higgs Signals: consistency with the signal strengths of the 125 GeV Higgs

Benchmark planes

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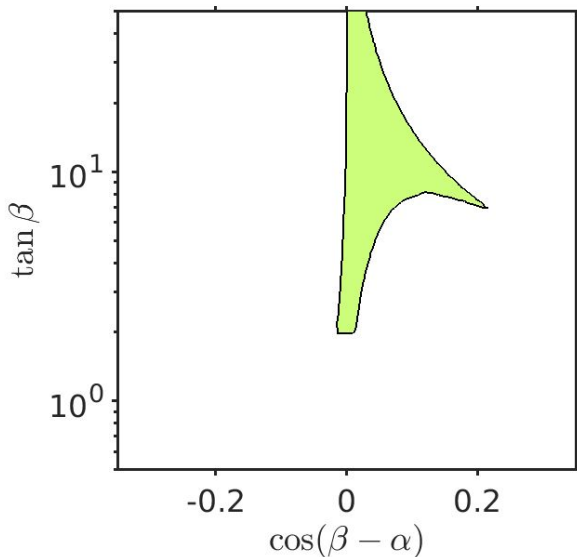
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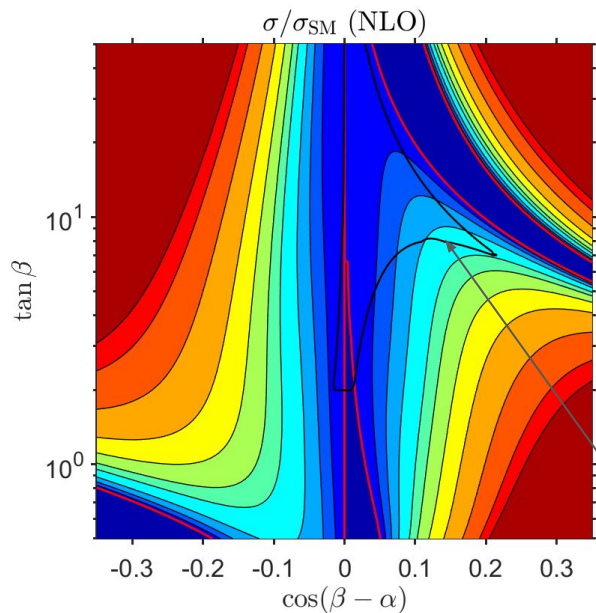


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Total di-Higgs production cross section

$$m_H = m_A = m_{H^\pm} = 1000 \text{ GeV}$$

$$m_{12}^2 = (m_H^2 \cos^2 \alpha) / \tan \beta$$

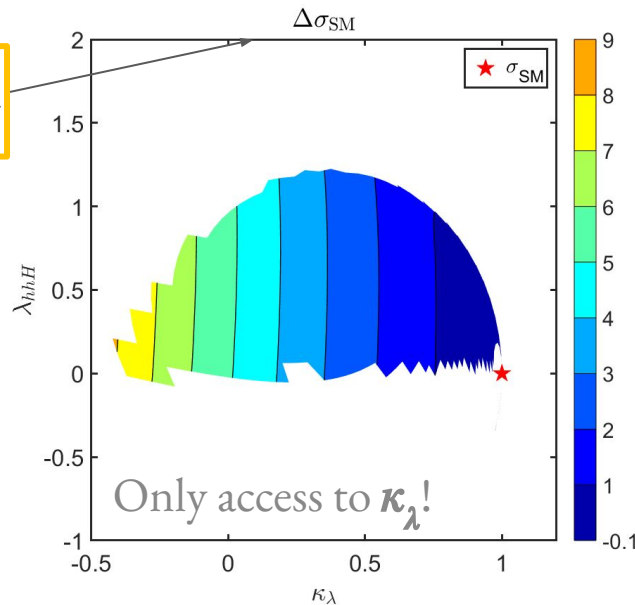


$$\Delta\sigma_{\text{SM}} \equiv \frac{\mathbf{xS}_{2\text{HDM}} - \mathbf{xS}_{\text{SM}}}{\delta\mathbf{xS}}$$

$$\delta\mathbf{xS} = \mathbf{xS}/4.5$$

Projected significance in standard deviations of the total di-Higgs production: 4.5σ

Allowed region inside the black contour!



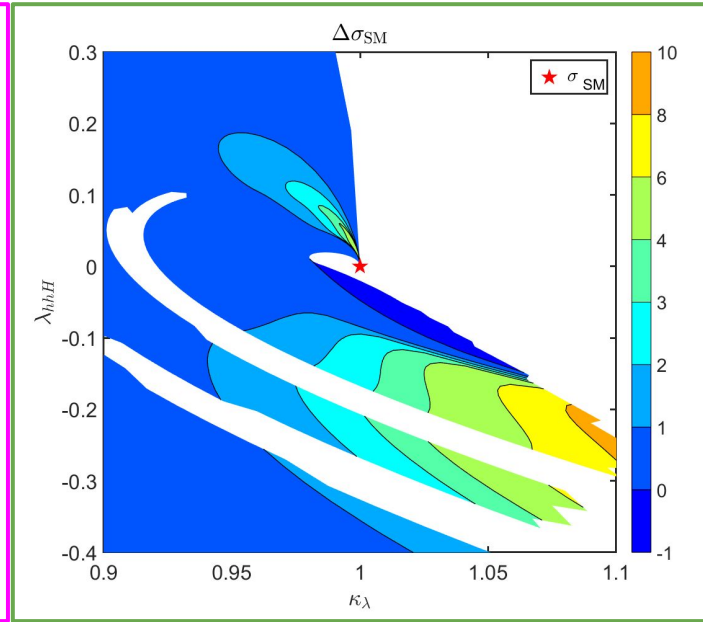
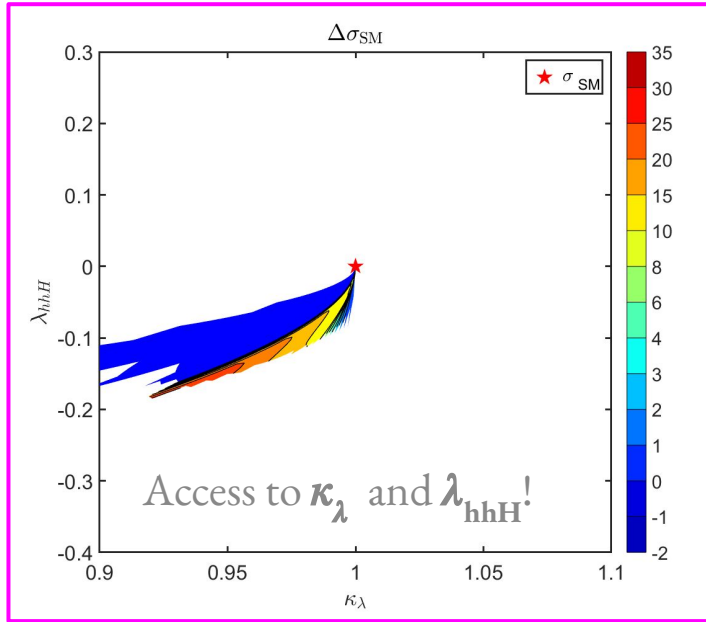
- NLO QCD corrections implemented in HPAIR (in the heavy top quark limit)
- **Largest enhancements** inside the allowed region (black contour) $\sim 3\sigma_{\text{SM}} \rightarrow$ due to deviations in κ_λ
- **Expected sensitivity** to the deviation of the \mathbf{xS} : up to 8σ away from the SM (above 2σ for $\kappa_\lambda < 0.6$)

BSM Couplings

$$m_H = m_A = m_{H^\pm}$$

$$m_{12}^2 = (m_H^2 \cos^2 \alpha) / \tan \beta$$

$$\tan(\beta) = 10$$



This scenario features a resonant enhancement of the cross section, i.e. the largest enhancement is due to the H contribution in the s-channel at $m_H \sim 350-450$ GeV

- Very large enhancements for $\cos(\beta-\alpha) < 0$ up to $8\sigma_{SM}$ that lead to deviations up to 35σ .
- Also large enhancements for $\cos(\beta-\alpha) < 0$ up to $3\sigma_{SM}$ that lead to deviations up to 10σ .

Invariant mass distribution: effects of deviations in κ_λ

BP: Type I, $\cos(\beta - \alpha) = 0.1$, $\tan \beta = 10$, $m_{12}^2 = m_H^2 \cos^2 \alpha / \tan \beta$, $m_H = m_A = m_{H^\pm}$

Prediction for SM couplings:

$$\kappa_\lambda = 1, \lambda_{hhH} = 0$$

Prediction for BSM couplings:

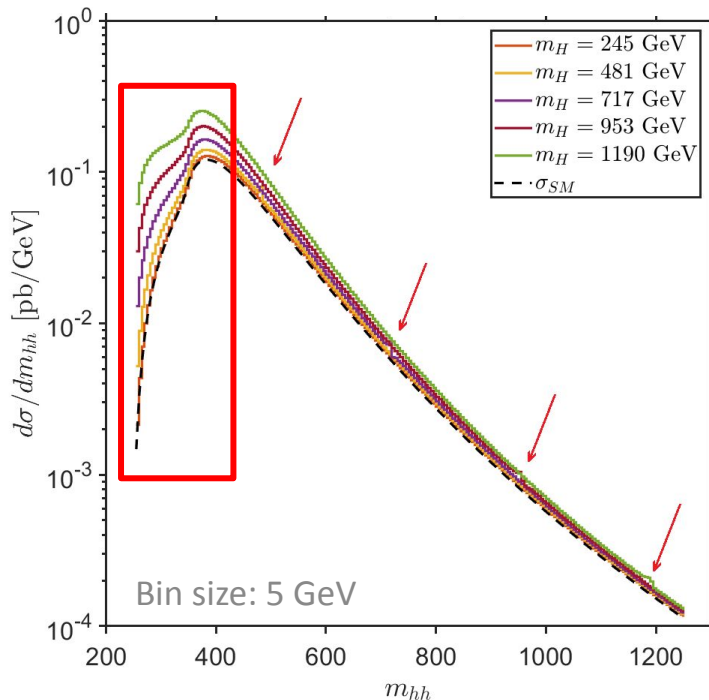
$$\kappa_\lambda = 0.97, \lambda_{hhH} = 0.05$$

$$\kappa_\lambda = 0.85, \lambda_{hhH} = 0.19$$

$$\kappa_\lambda = 0.67, \lambda_{hhH} = 0.42$$

$$\kappa_\lambda = 0.41, \lambda_{hhH} = 0.74$$

$$\kappa_\lambda = 0.08, \lambda_{hhH} = 1.15$$



- Larger sensitivity to κ_λ in the low m_{hh} region

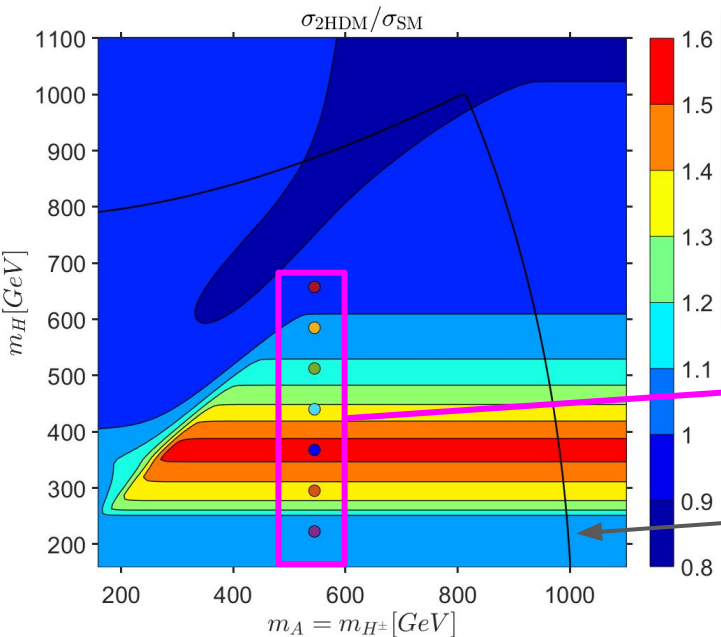
- Resonant contribution very suppressed due to very small top Yukawa $\xi_H^t \sim 10^{-4}$

$$\xi_H^t = \cos(\beta - \alpha) - \sin(\beta - \alpha) / \tan(\beta)$$

Effect of the mass of the heavy Higgs

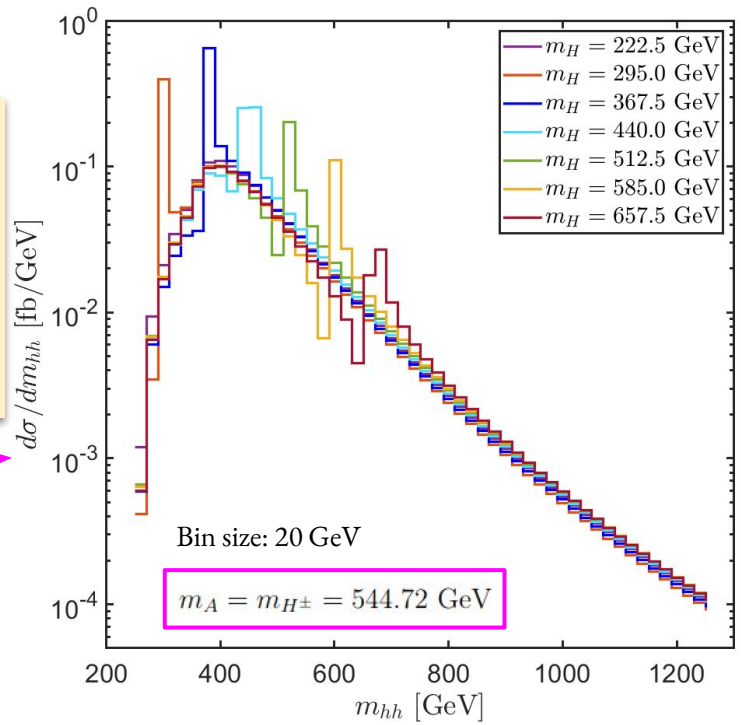
- We vary the mass of the heavy Higgs boson leaving the rest of the parameters of the model fixed.

BP: Type I, $\cos(\beta - \alpha) = 0.2$, $\tan \beta = 10$, $m_{12}^2 = m_H^2 \cos^2 \alpha / \tan \beta$



Enhancement in the total cross section is resonance dominated. **Location** of the resonance is related to the mass of **H**

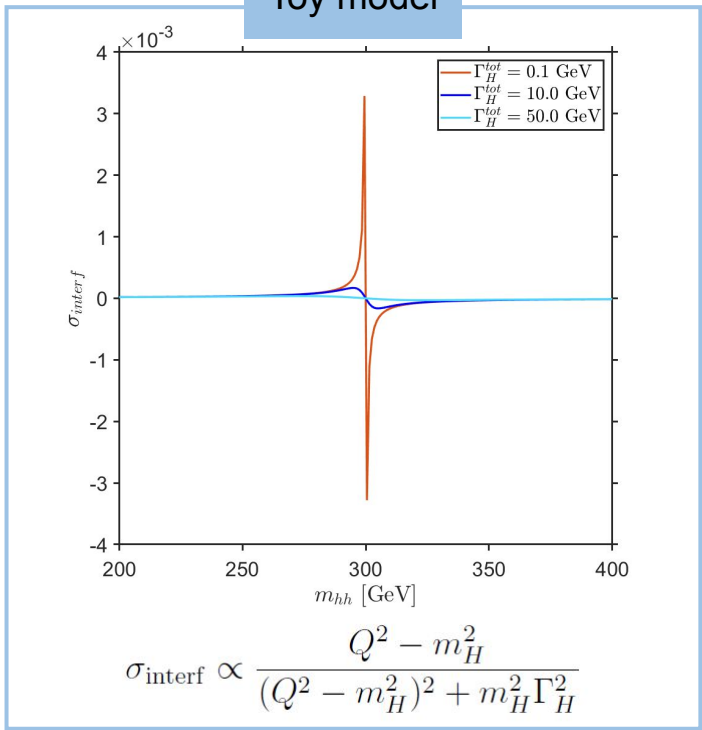
Allowed region inside the black contour.



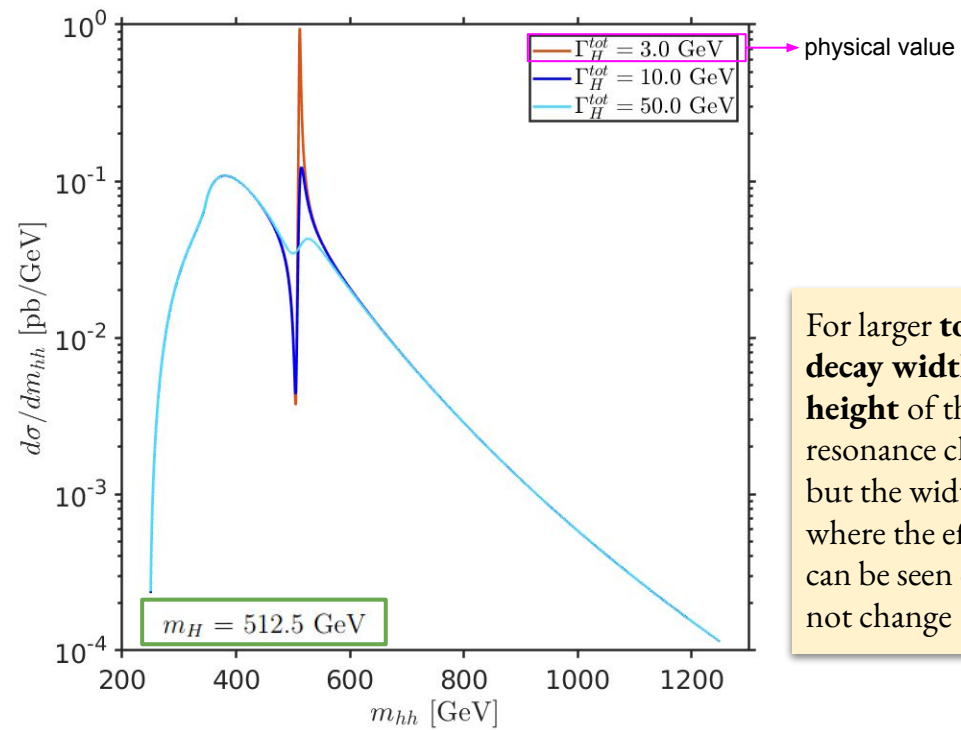
Effect of the total decay width

$$\frac{1}{Q^2 - M_{h/H}^2 + i\Gamma_{h/H}M_{h/H}}$$

Toy model



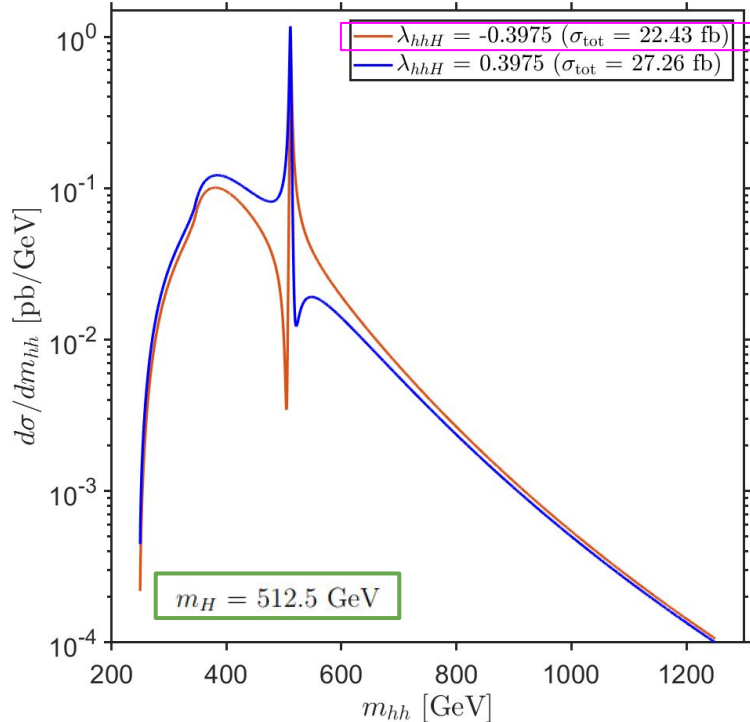
- For the green point of the previous benchmark plane we artificially change the total decay width of the heavy Higgs H:



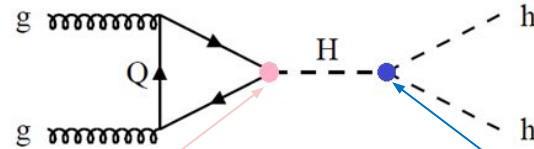
For larger **total decay widths** the **height** of the resonance changes but the width where the effect can be seen does not change

Relative sign of the couplings in the resonance

- What is the effect of the couplings involved in the resonant diagram on the invariant mass distributions?



physical value



$$\xi_H^t = \cos(\beta - \alpha) - \sin(\beta - \alpha) / \tan(\beta) = 0.104$$

λ_{hhH}

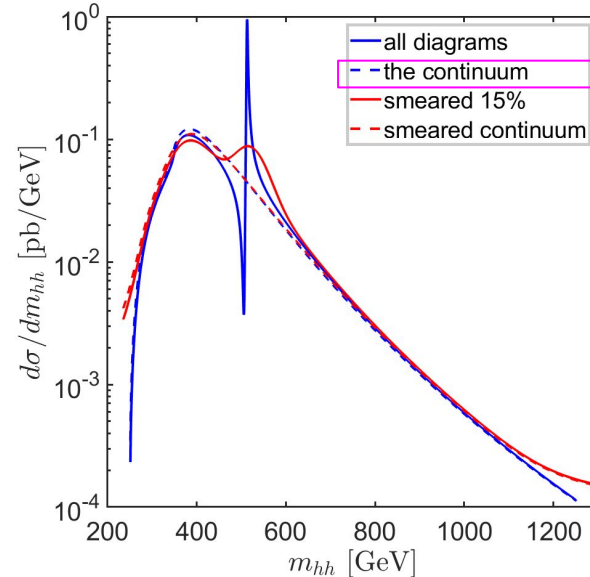
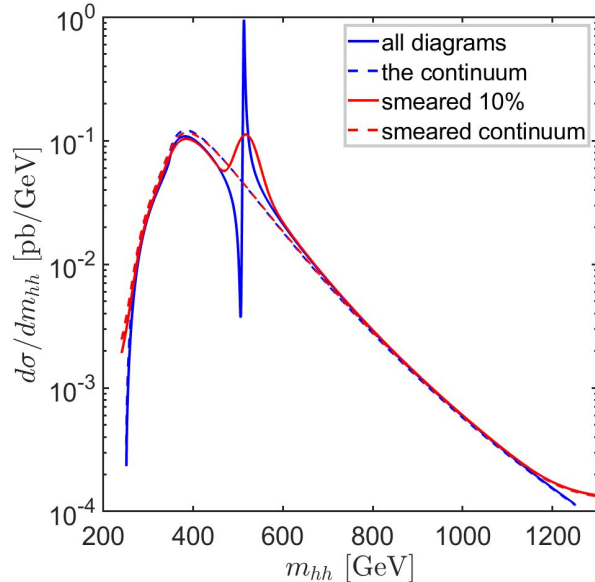
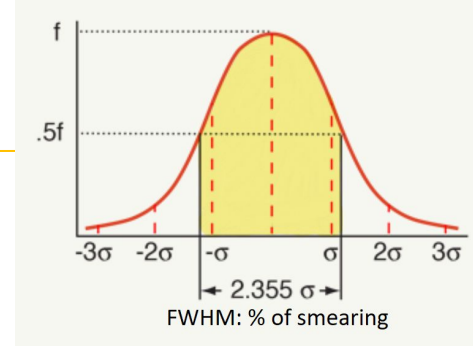
The **relative sign** of the top Yukawa and the BSM coupling to the heavy Higgs gives a **structure** to the resonance:

sign ($\lambda_{hhH} \cdot \xi_H^t$)	structure
+	peak-dip
-	dip-peak

- Will this effect remain in an experimental setup?

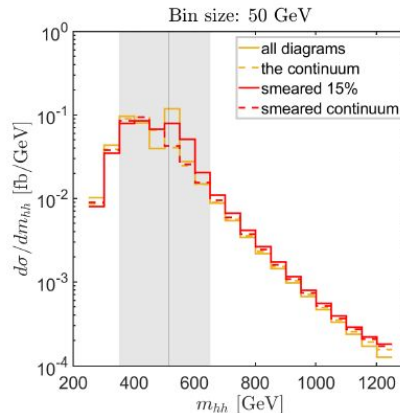
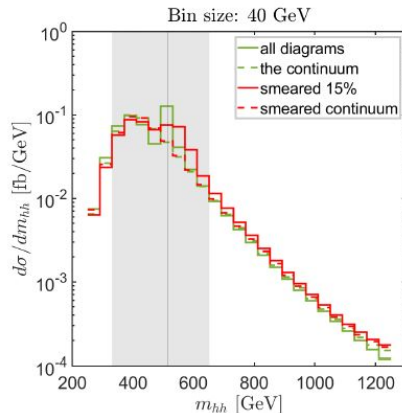
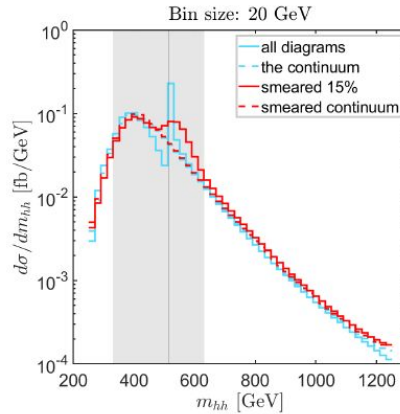
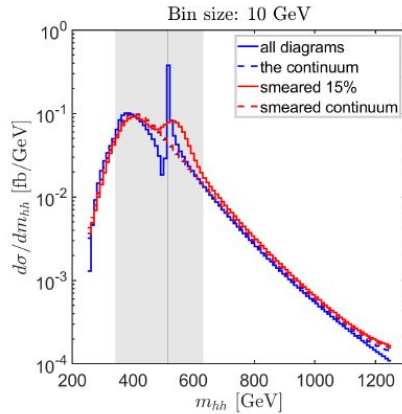
Experimental challenges: smearing

- Differential cross section measurements are affected by the finite resolution of particle detectors → observed spectrum is “**smear**ed”
- We try to mimic this effect by artificially smearing the theoretical prediction introducing **Gaussian uncertainties** in the invariant mass



→ box diagram + SM-like Higgs exchange

Experimental challenges: binning (15 % smearing)



- We define a value for the ‘significance of the signal’ according to the excess of the number of events. Assuming: $\mathcal{L} = 6000 \text{ fb}^{-1}$

events below resonant smeared contribution

events below continuum smeared contribution

$$R := \frac{\sum_i |N_i^R - N_i^C|}{\sqrt{\sum_i N_i^C}}$$

- Window definition:

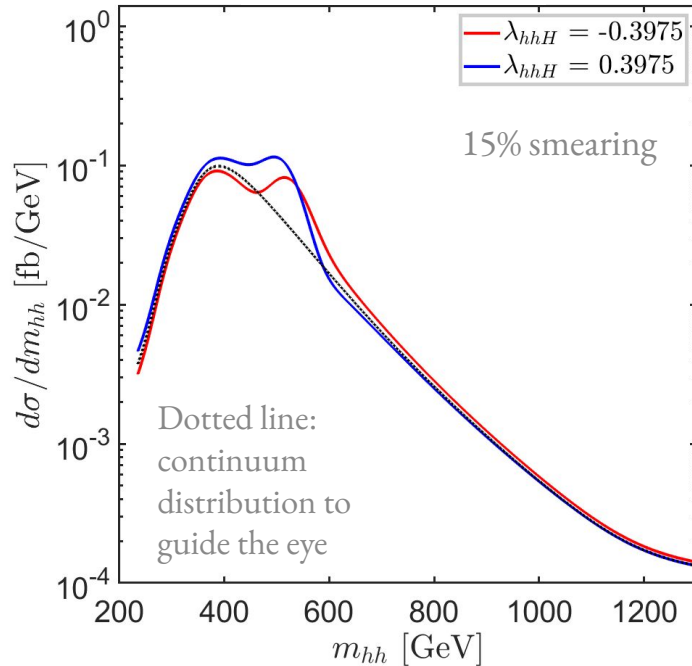
Bin size	R
10 GeV	84.9
20 GeV	86.5
40 GeV	86.8
50 GeV	87.5

$$|N^R - N^C| > (\text{bin size}) \times 20$$

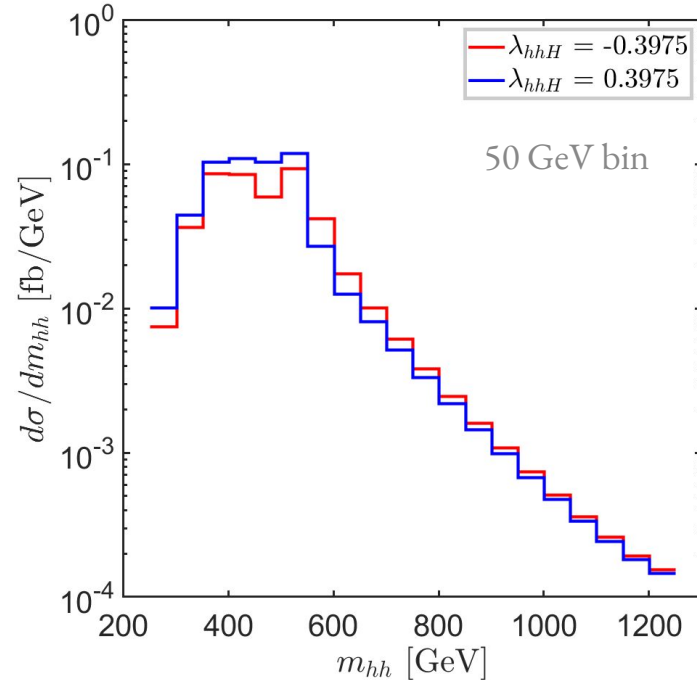
→ Smearing dilutes more the resonance than binning

Relative sign of the couplings in the resonance

Applying smearing:



Applying first smearing and then binning:



The structure of the resonance does not leave a measurable imprint once exp. uncertainties are evaluated

Conclusion

- Differences in the measured **di-Higgs production cross section** can originate from:
 1. deviations in κ_λ
 2. additional '**resonant**' contributions

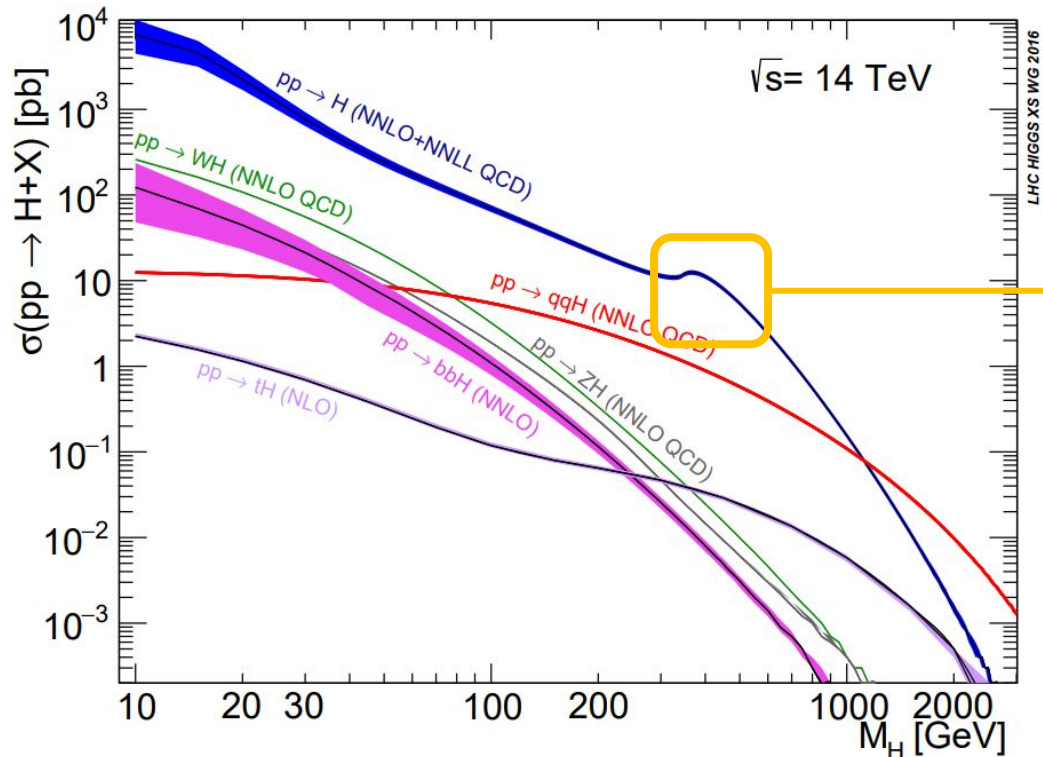
→ Cannot be disentangled from a measurement of the total cross section alone

→ High sensitivity can be reached at HL-LHC in the regions far from the alignment limit and with heavy scalar masses within 350-450 GeV
- **Invariant mass distributions** give information about **resonant production** that can be embedded in BSM models:
 1. **mass** of the intermediate Higgs boson → **position**
 2. **total decay width** → **height** of the resonance
 3. relative sign of the **couplings** → **structure** of the resonance

→ These effects may be (partially) washed out by experimental precision (**smearing and binning**)

The relative sensitivity to the coupling λ_{hhH} was analyzed by means of the variable R

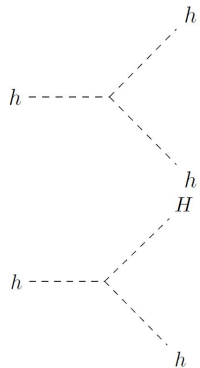
Backup: Single Higgs production



Top pair threshold \rightarrow gives a hint on the results for Higgs pair production

[LHC Higgs Working Group:
CERN Yellow Report 4]

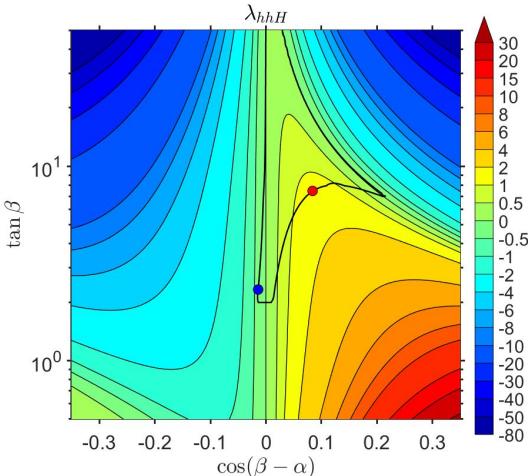
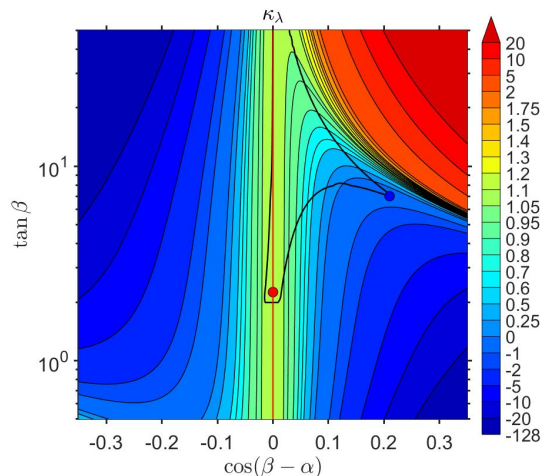
Feynman rules for 2HDM THC



$$\lambda_{hhh} = \frac{1}{2v^2} \left\{ m_h^2 s_{\beta-\alpha}^3 + (3m_h^2 - 2\bar{m}^2) c_{\beta-\alpha}^2 s_{\beta-\alpha} + 2 \cot 2\beta (m_h^2 - \bar{m}^2) c_{\beta-\alpha}^3 \right\}$$

$$\lambda_{hhH} = \frac{-c_{\beta-\alpha}}{2v^2} \left\{ (2m_h^2 + m_H^2 - 4\bar{m}^2) s_{\beta-\alpha}^2 + 2 \cot 2\beta (2m_h^2 + m_H^2 - 3\bar{m}^2) s_{\beta-\alpha} c_{\beta-\alpha} - (2m_h^2 + m_H^2 - 2\bar{m}^2) c_{\beta-\alpha}^2 \right\}.$$

$$\bar{m}^2 = \frac{m_{12}^2}{\sin \beta \cos \beta}$$



$$\kappa_\lambda \in [-0.4, 1]$$

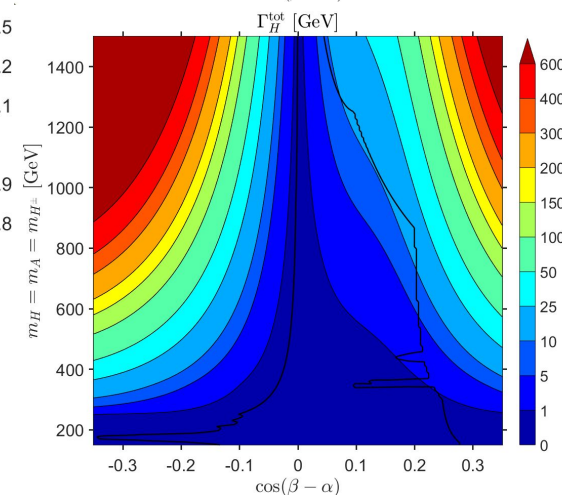
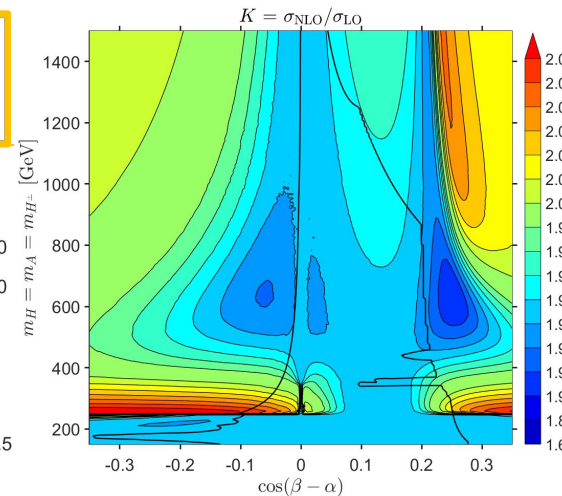
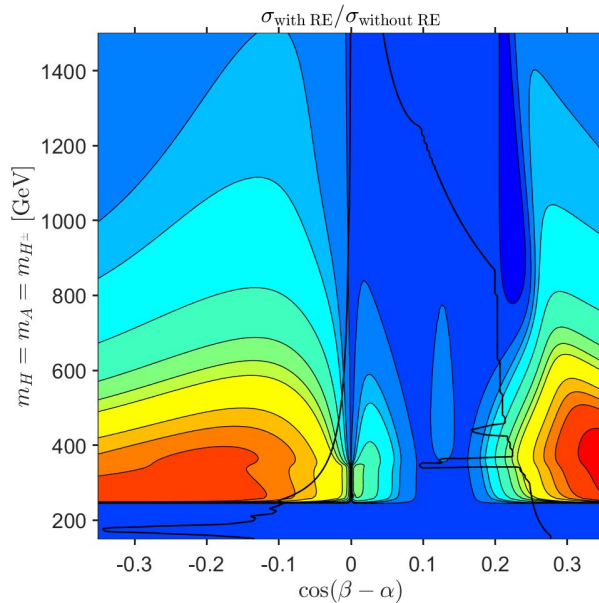
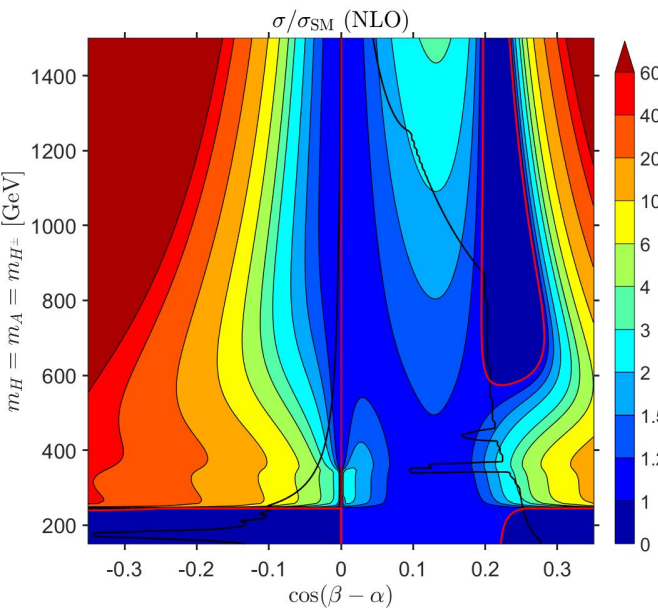
$$\lambda_{hhH} \in [-0.3, 1.2]$$

Backup: BP

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$$m_{12}^2 = (m_H^2 \cos^2 \alpha) / \tan \beta$$

$$\tan(\beta) = 10$$



NLO calculation done with HPAIR

- Large enhancements up to $8\sigma_{SM}$ for $m_H \sim 2m_{top}$.
- No enhancement below $m_H \sim 250$ GeV \rightarrow heavy Higgs is not on shell.
- Dominant contribution of the diagram involving λ_{hhH} at $m_H \sim 2m_{top}$.

Smearing applied on the invariant mass distributions

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