
ILC Racetrack Crab Design

Prof Graeme Burt, Lancaster University / Cockcroft Institute

Thanks to Nik Templeton and James Bourne, STFC

ILC Crab Cavity Collaboration Team (c. 2008)

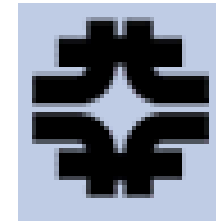
- Cockcroft Institute:

- Graeme Burt (Lancaster University)
- Richard Carter (Lancaster University)
- Amos Dexter (Lancaster University)
- Philippe Goudket (ASTeC)
- Roger Jones (Manchester University)
- Alex Kalinin (ASTeC)
- Lili Ma (ASTeC)
- Peter McIntosh (ASTeC)
- Imran Tahir (Lancaster University)



- FNAL:

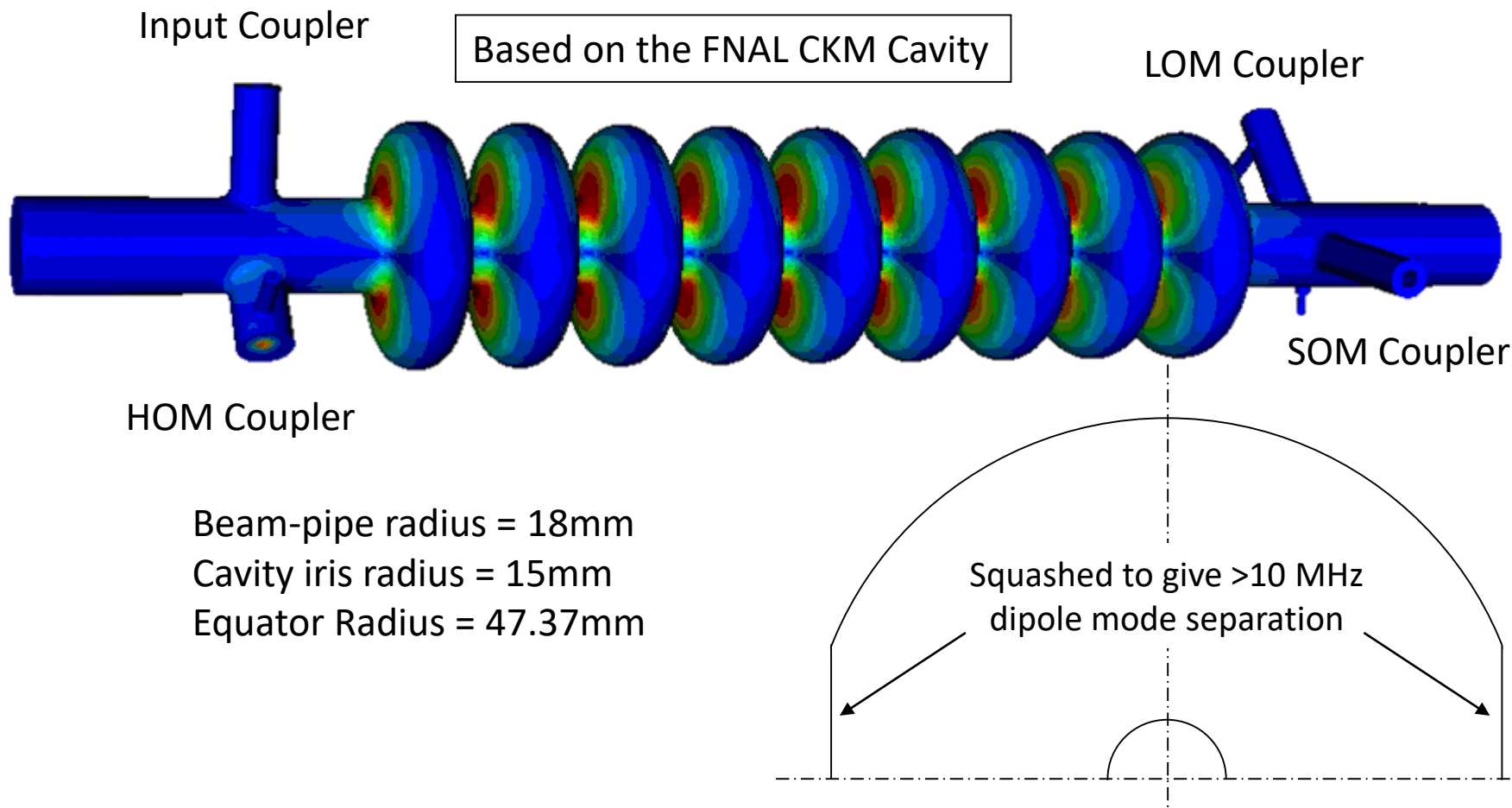
- Leo Bellantoni
- Mike Church
- Tim Koeth
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- Sergei Nagaitsev
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- SLAC:

- Chris Adolphson
- Kwok Ko
- Zenghai Li
- Cho Ng
- Andrei Seryi
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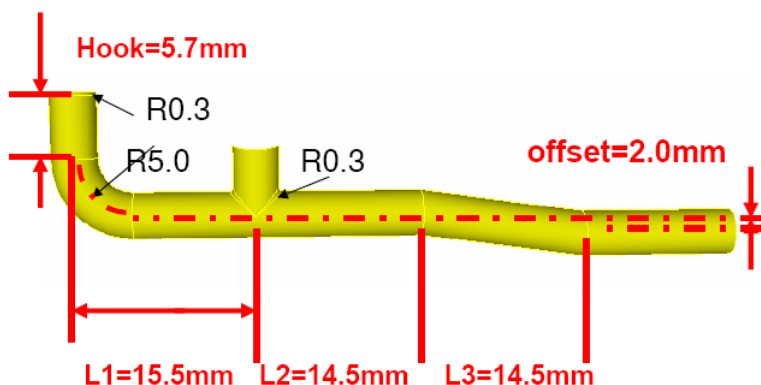
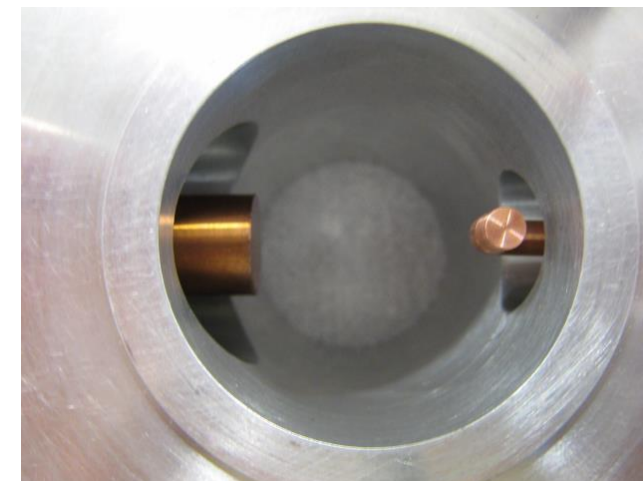
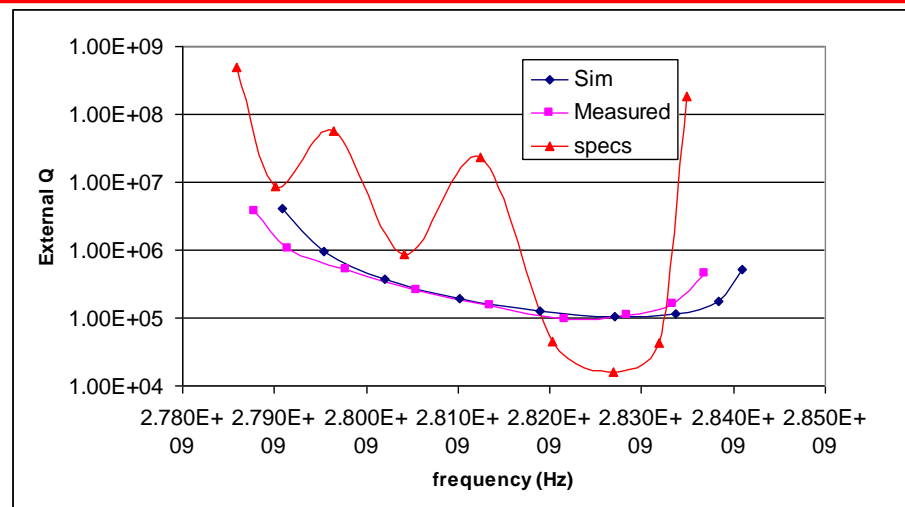




At 5MV/m P _L :	
B_{MAX}	73 mT
E_{MAX}	16.6 MV/m
U	0.25 J
Q (Nb, room temp)	4780
$\left(\frac{R}{Q}\right)' = \frac{1}{2} \frac{ V_L(r) ^2}{\omega U} \left(\frac{c}{\omega r}\right)^2$	235 Ω
$G = Q \times R_{SURF}$	225 Ω
R_{BCS} (best measurement) @ 1.8K	30n Ω
R_0 (best measurement)	40n Ω
Q @ 70n Ω , 1.8K	3.2×10^9
Surface power @ 70n Ω	1.9 W

In hindsight it may have been better to develop a racetrack solution with a larger polarisation separation. It would be prudent to revisit this.

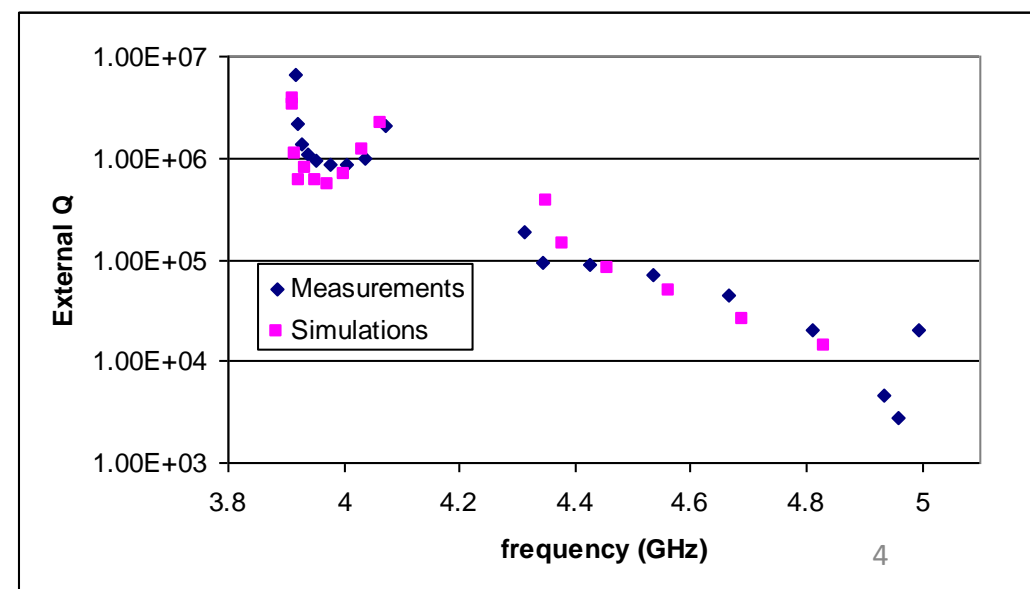
Lower Order Mode Coupler



Hook type LOM coupler designed by FNAL/Lancaster and improved by SLAC

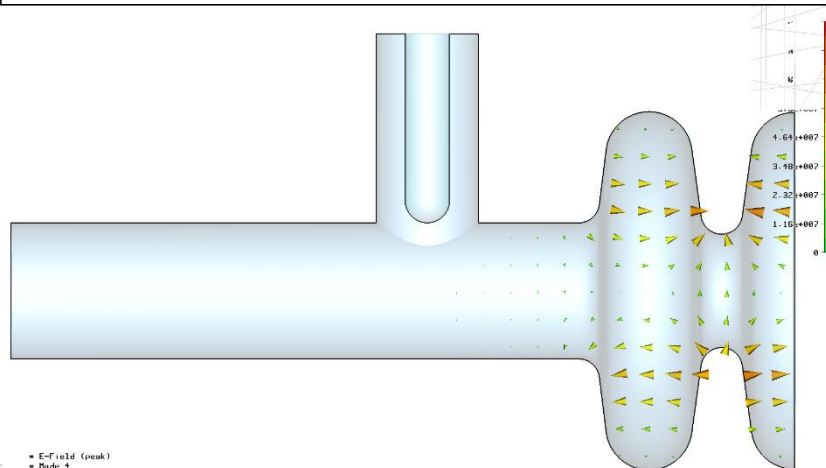
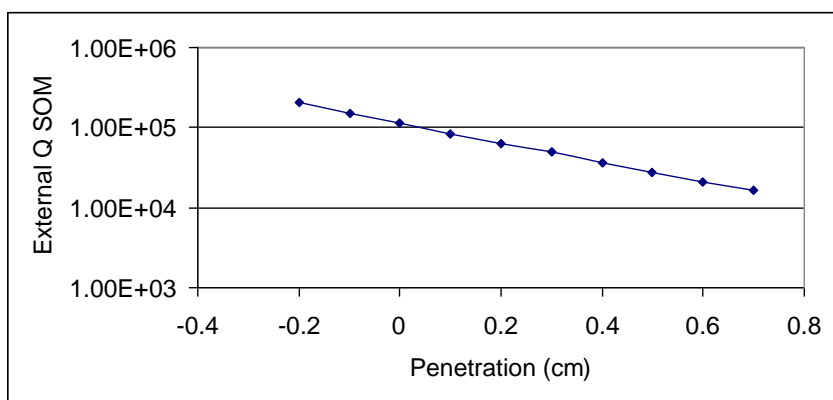
No filter, uses polarisation to avoid coupling to the crabbing mode

The LOM coupler prototype was found to give good agreement with both MWS and Omega3P simulations.



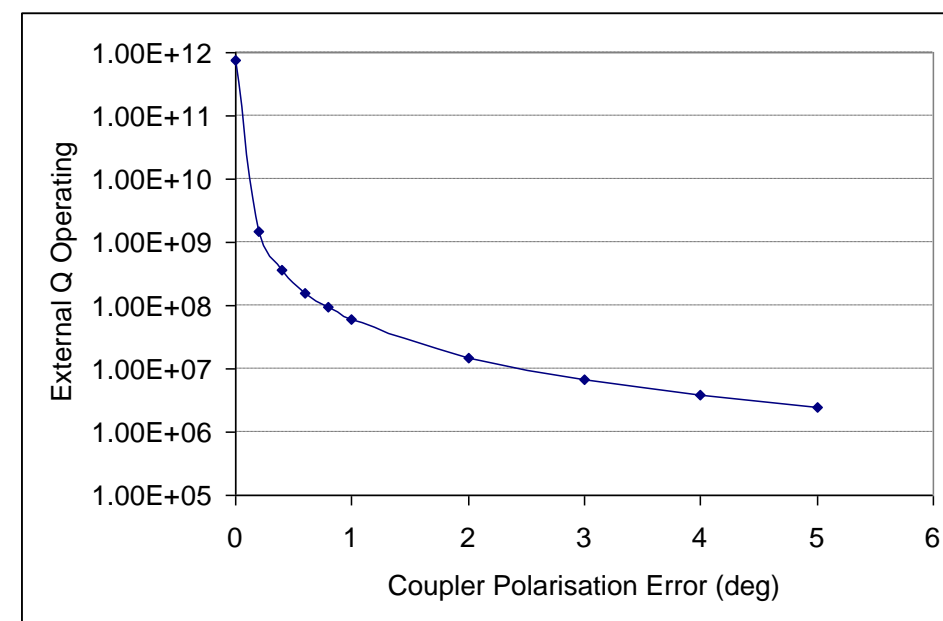
Cockcroft SOM Coupler design

The SOM coupler is currently a simple coaxial structure.



Type = E-Field (peak)
 Monitor = Mode 1
 Plane at x = 0
 Frequency = 3.87894
 Phase = 0 degrees
 Maximum=Zd = 9.28215e+07 V/m at 0 / -1.0 / -12.8953

The problem is that as we decrease the SOM external Q we make the coupler susceptible to damping the operating mode.



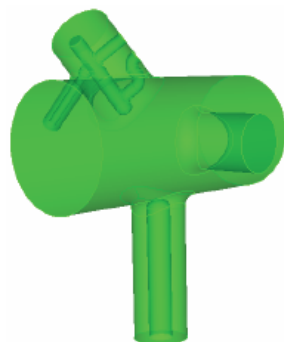
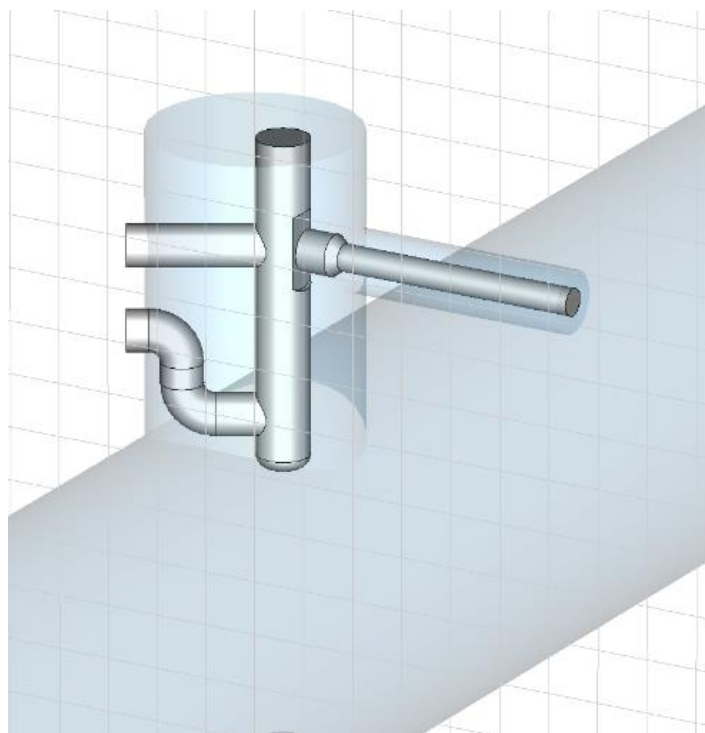
Assuming 10 Watts mean power flow in the coupler, and we meet the SOM damping spec then we need to align the coupler to within 1.4 degrees.

May be better to use a racetrack cell shape to separate the vertical and horizontal mode in frequency and use a filter

HOM Coupler

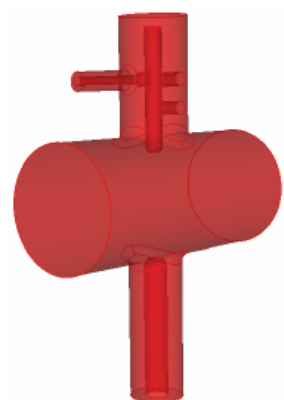
The original HOM coupler was based on the EU-XFEL 3rd harmonic HOM coupler that's slightly modified.

SLAC redesigned the coupler but did not check all modes just the first two passbands.

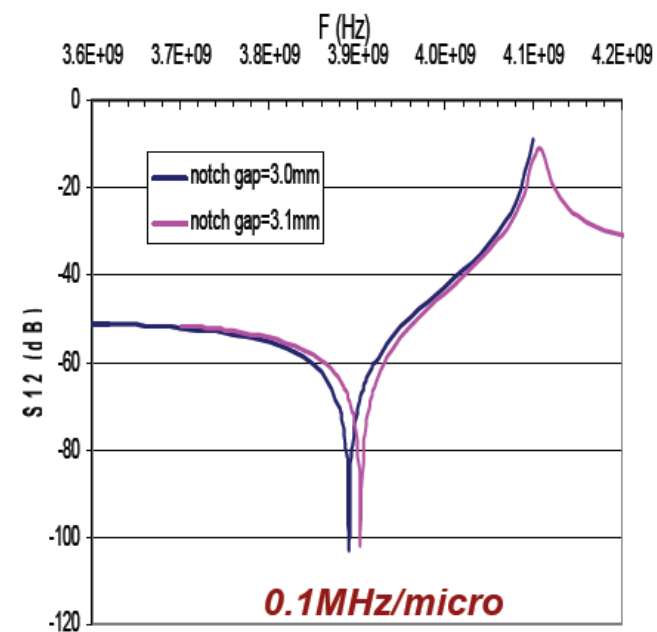


FNAL DESIGN
loop coupling:

Reduce Notch Gap Sensitivity



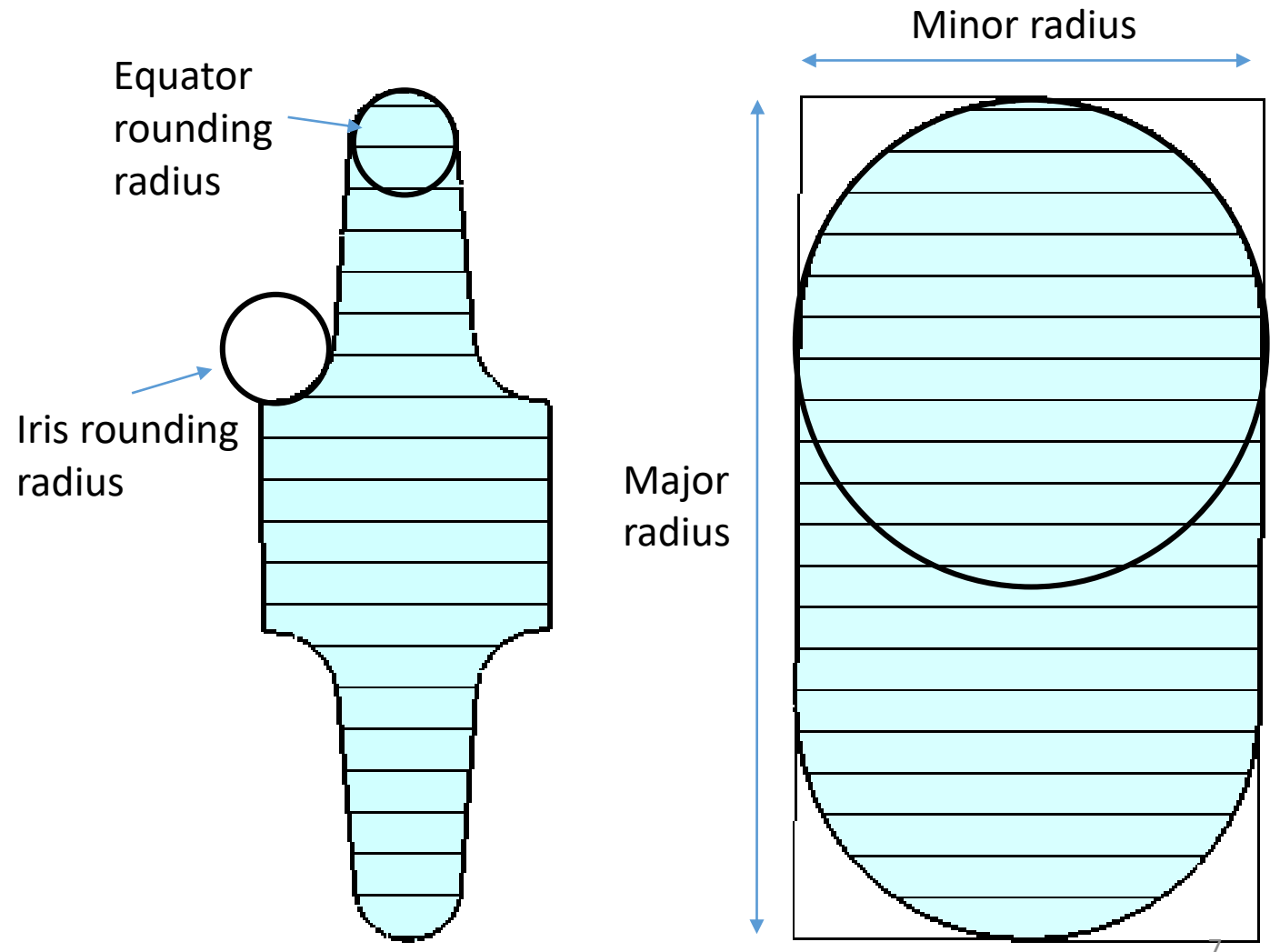
SLAC DESIGN
probe coupling



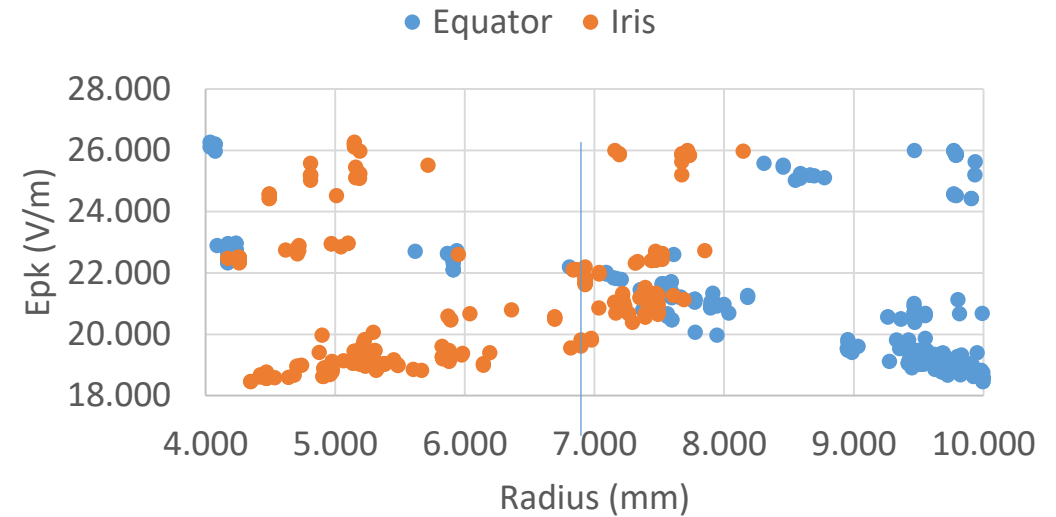
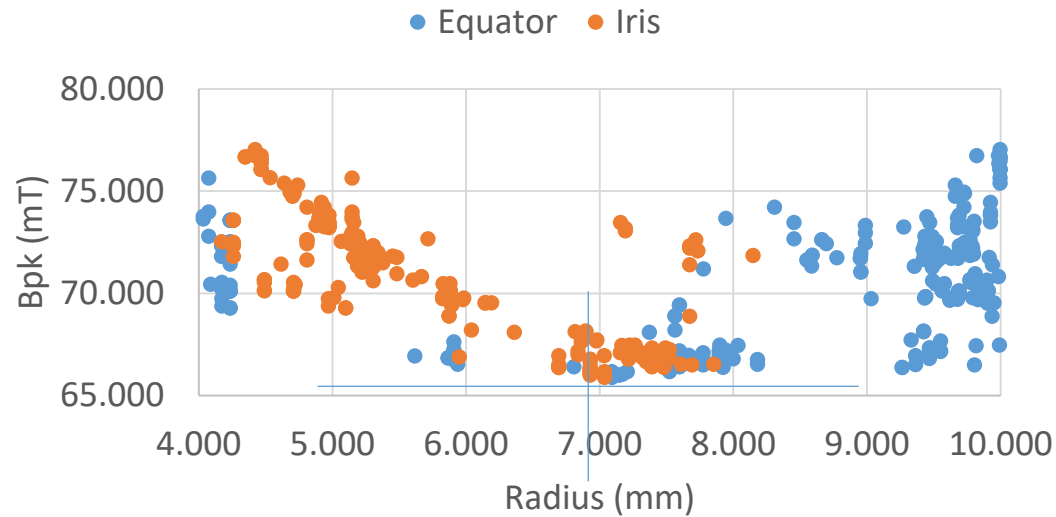
~TESLA(0.13MHz/micro)

Re-optimizing the ILC crab

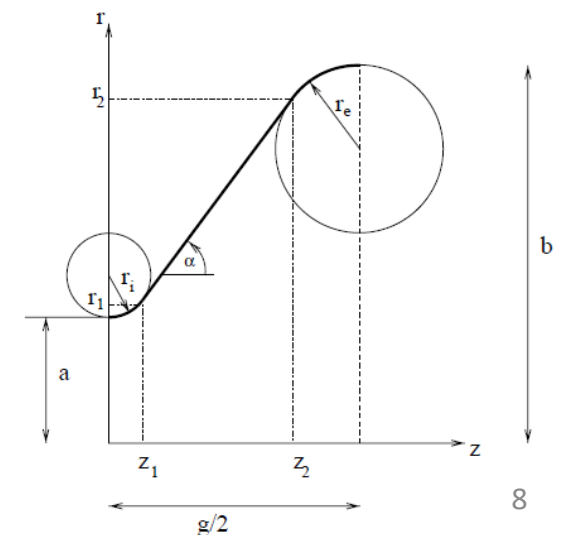
- In the original design the SOM separation is only 10 MHz which caused issues it would be good to separate them more.
- 250 GeV ILC requires a 3-cell cavity @ 5.3 MV/m, or 2x2-cells at @4.2 MV/m



Cell Optimisation (curvature radii)



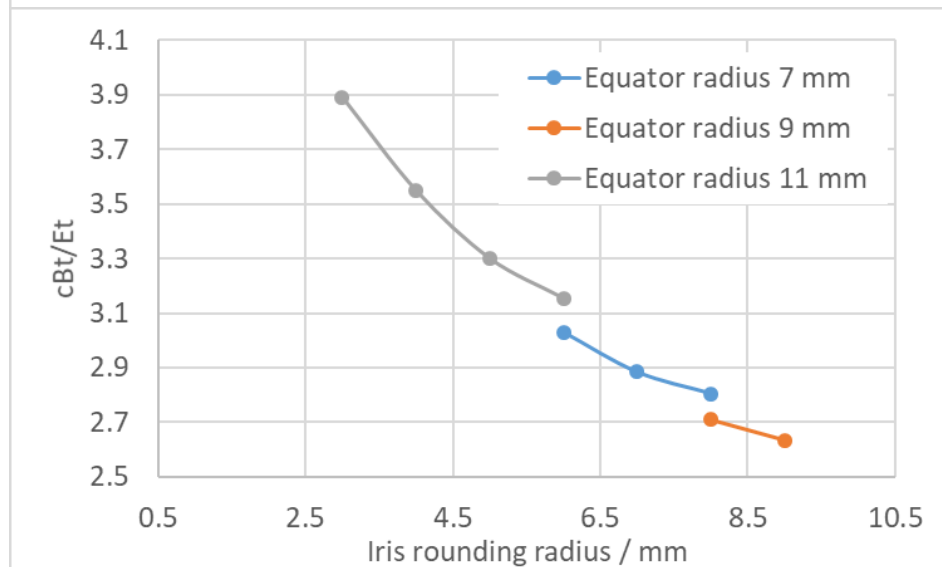
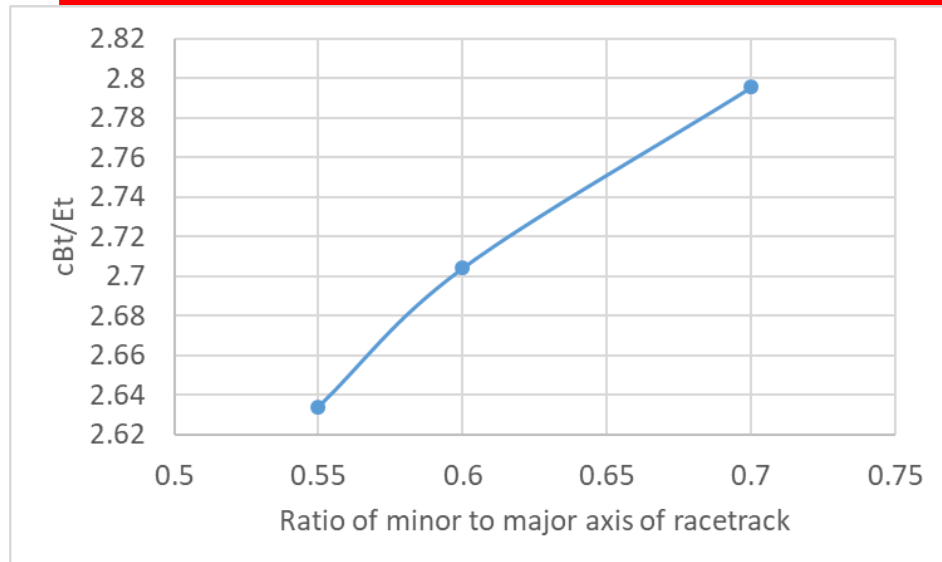
- Epk is minimised for a large rounding radius on the equator and small iris
- Bpk is minimised for iris rounding around 7 mm
- We have aimed for minimising Bpk as Epk is fairly conservative
- Note that having such a large iris rounding and hence thickness implies a smaller equator and hence cell length



Improved geometry

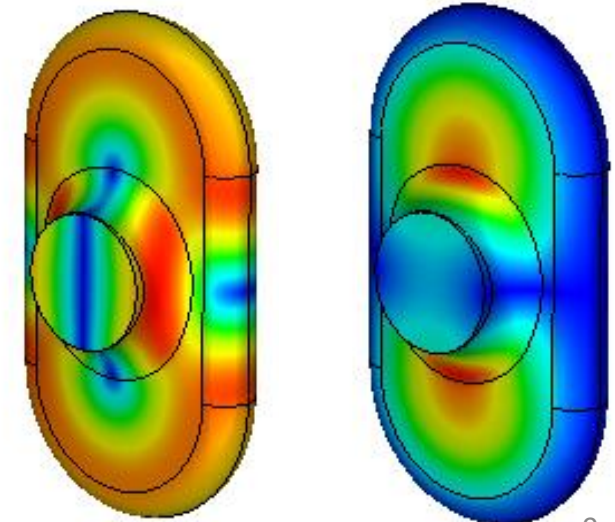
- The surface magnetic field decreases as the ratio of minor to major axis decreases (below 0.5 its starts to increase but with our aperture this is not an allowed geometry anyway)
- The surface electric field is too low to worry about

- It appears we want a small equator radius and a large equator radius (ie short cavity with a thick iris)



Magnetic

Electric



Varying the ellipticity to tune the LOM/SOM

- Making the cavity elliptical pushes the other polarization of the dipole mode to higher frequencies
- One issue with making the cavity highly elliptical is the lower order mode moves closer to the crabbing mode
- Ideally LOM and SOM spacing equal
- Making more elliptical also drops Bpk until it gets close to the aperture hence **0.55 chosen as optimum**

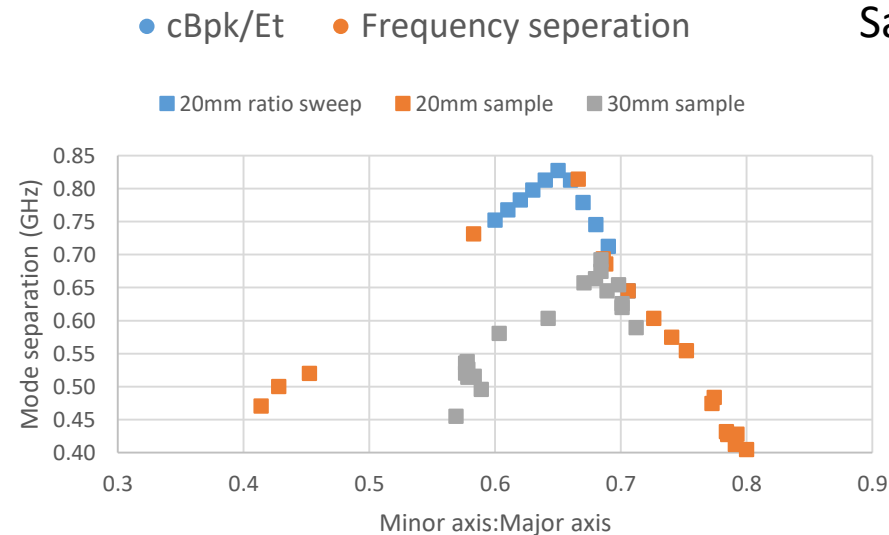
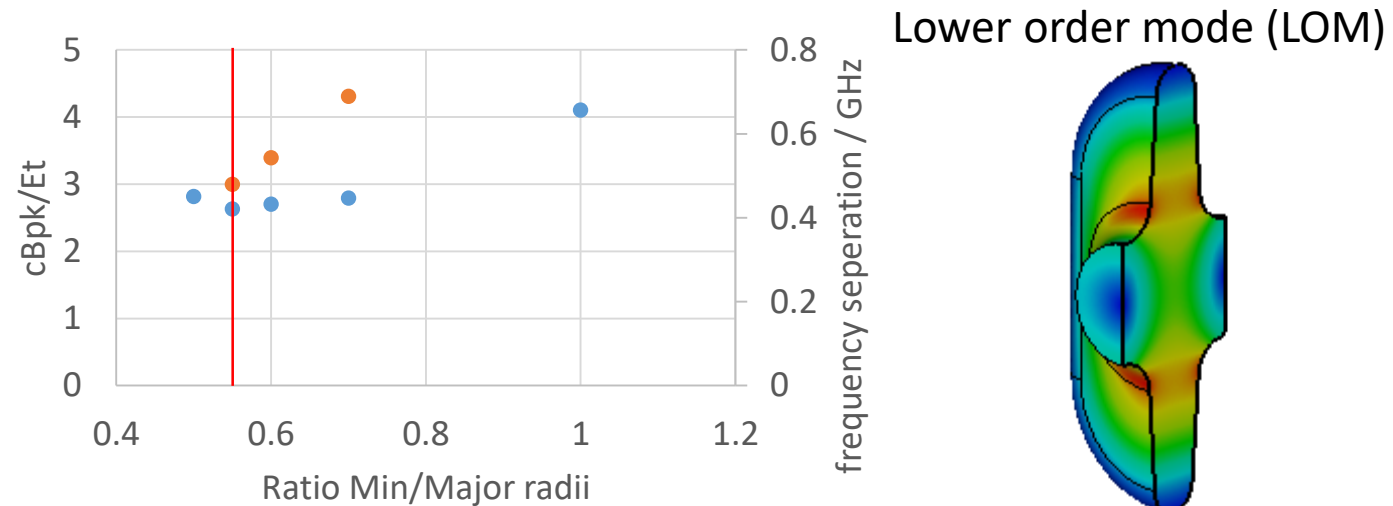
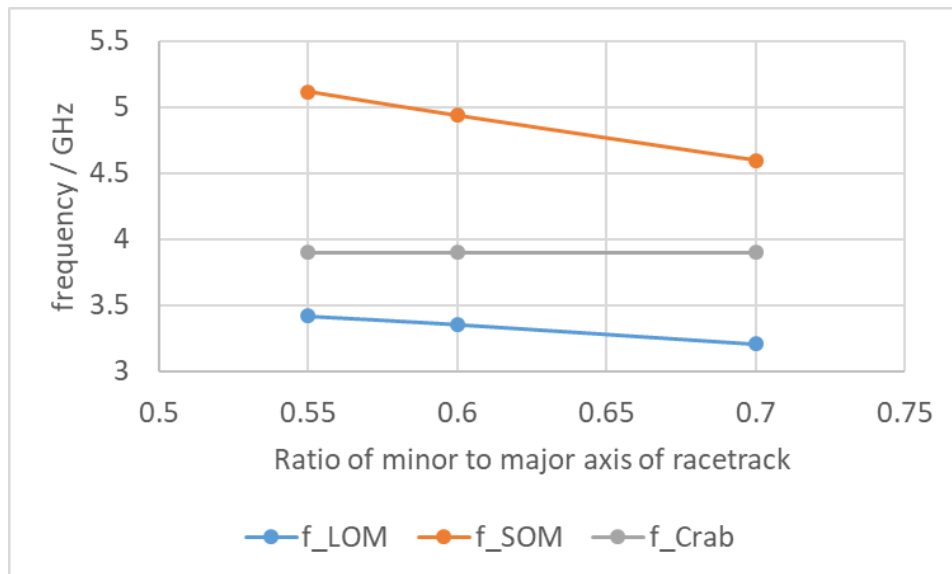


Figure 8 & Elliptical Cavity

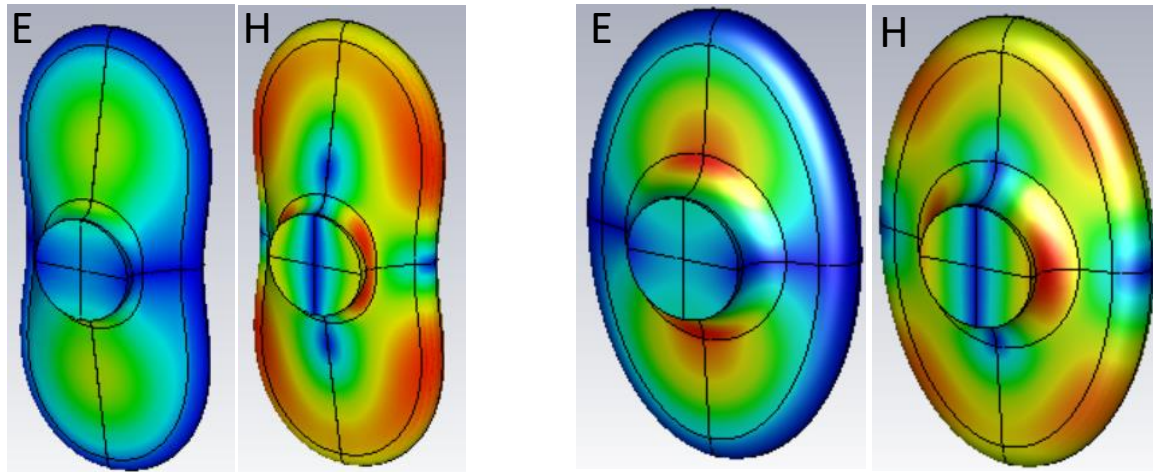
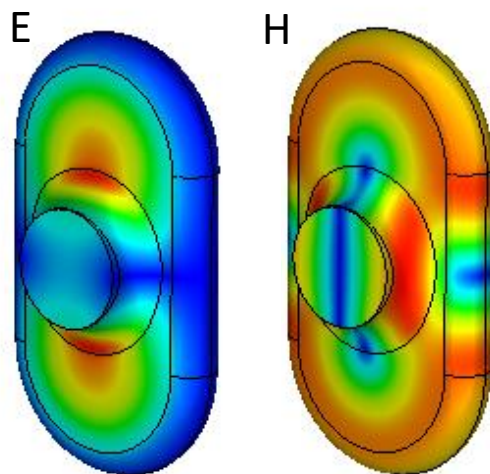


Figure 8

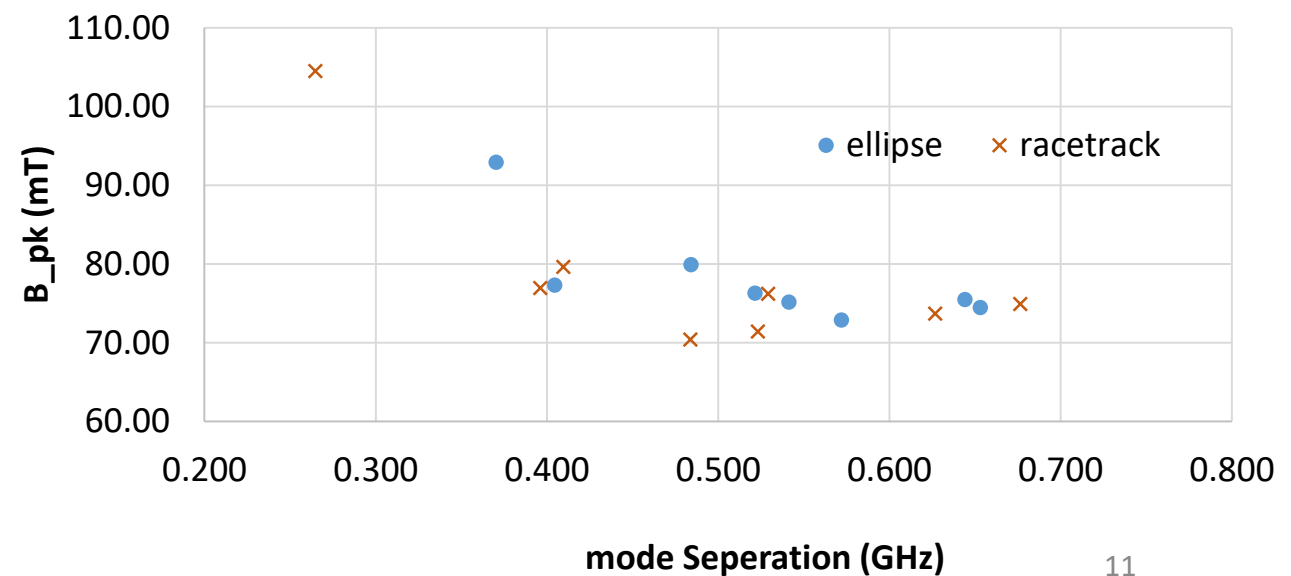
Elliptical



Racetrack

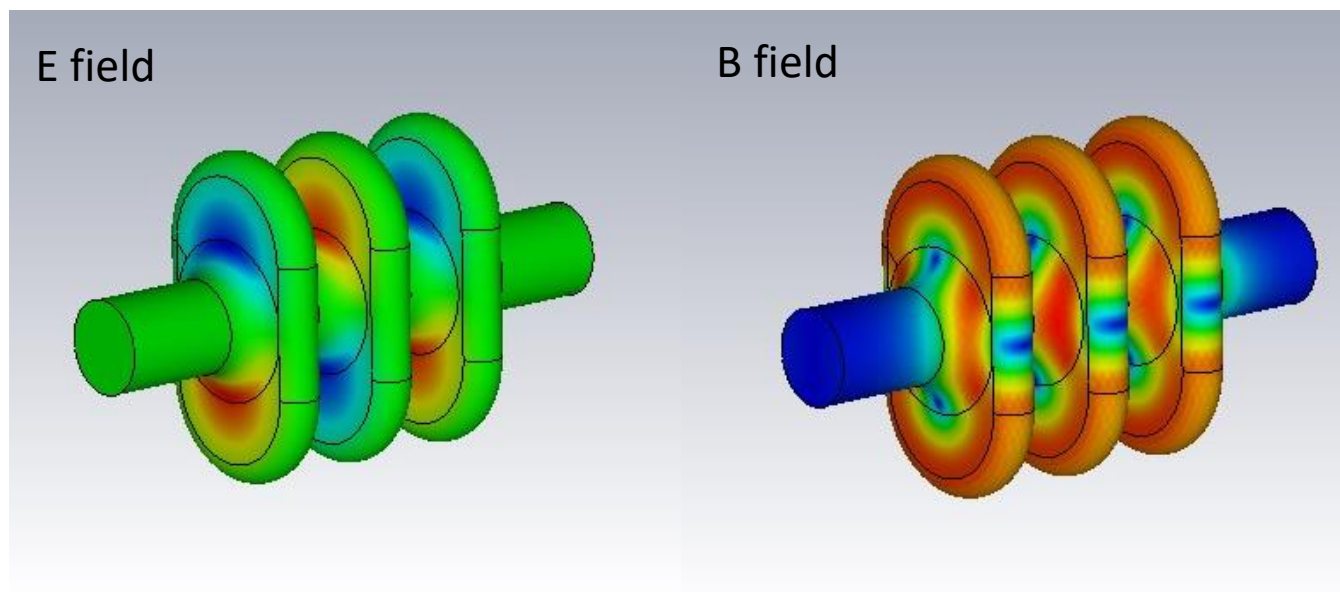
Other geometries were investigated but didn't prove to be as effective as a racetrack cavity.

- Figure 8 had enhanced B field
- Elliptical had poor mode separation



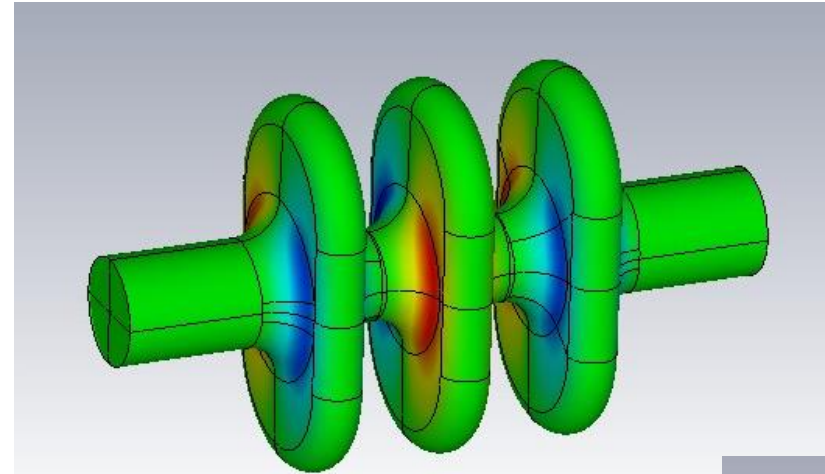
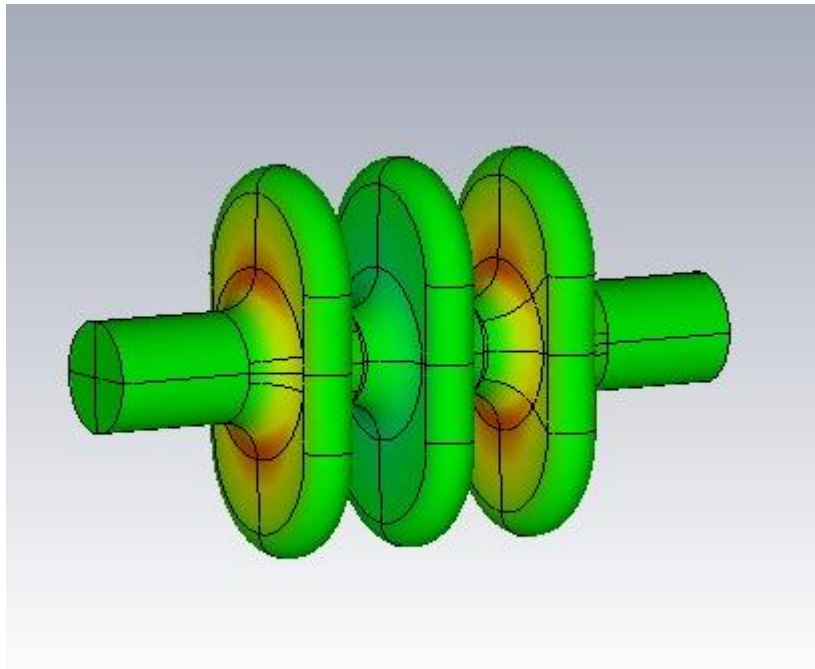
Initial 3 cell cavity design

- End cells initially had lower peak magnetic field
- Larger beampipes were used on the end cells to aid damping
- Iris was increased until the peak magnetic field was the same on all iris (iris radii 18 mm and 12.5 mm)

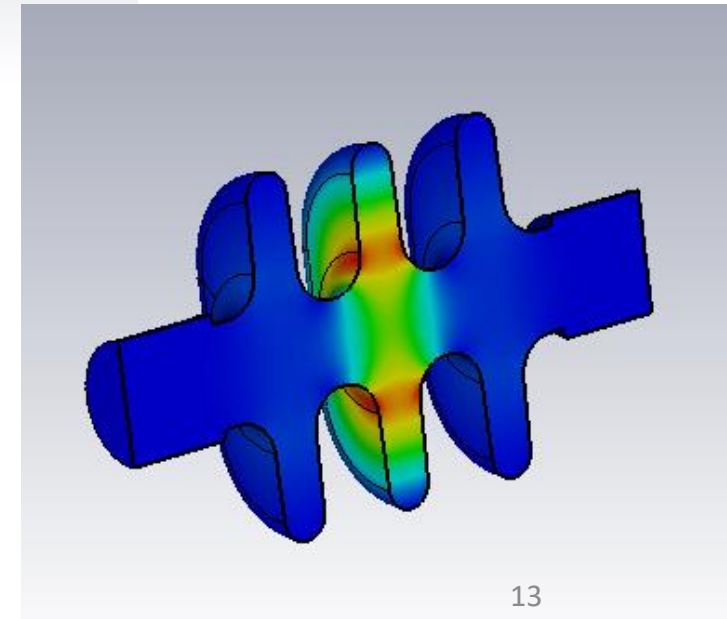


Same order and lower order modes

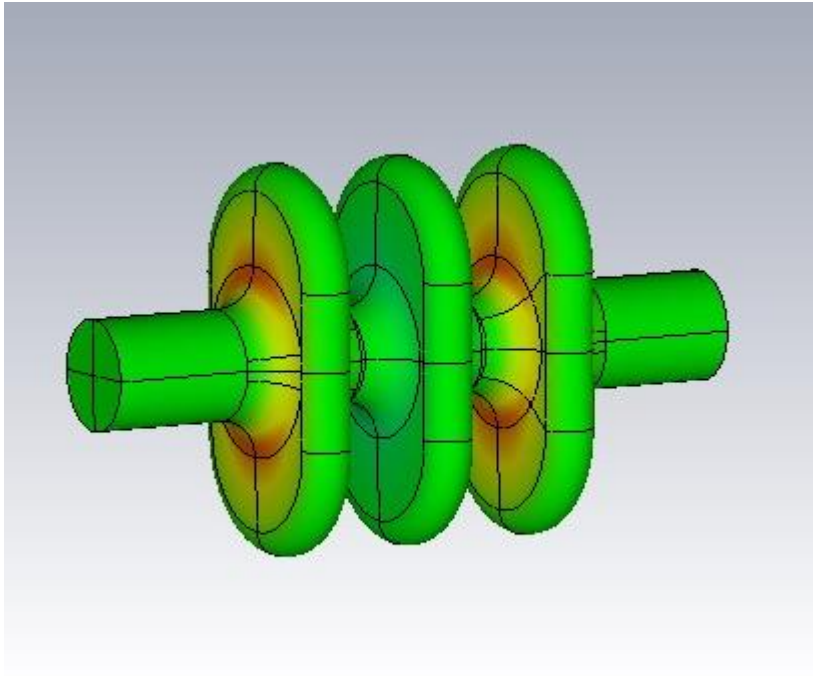
- Highest impedance SOM is the pi mode at 5.07 GHz, R_t/Q is only 50 Ohms/m due to frequency not being synchronous.



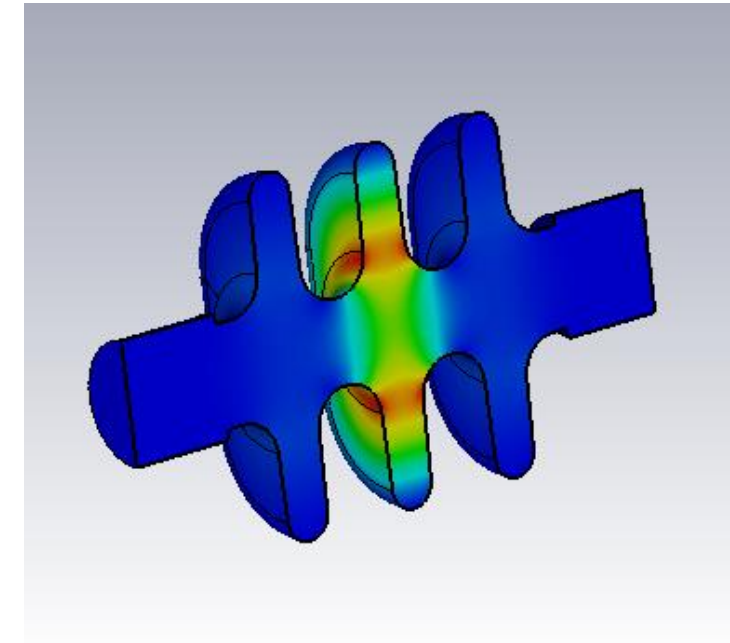
- Highest impedance LOM is the pi/2 mode at 3.32 GHz, R/Q is only 134 Ohms



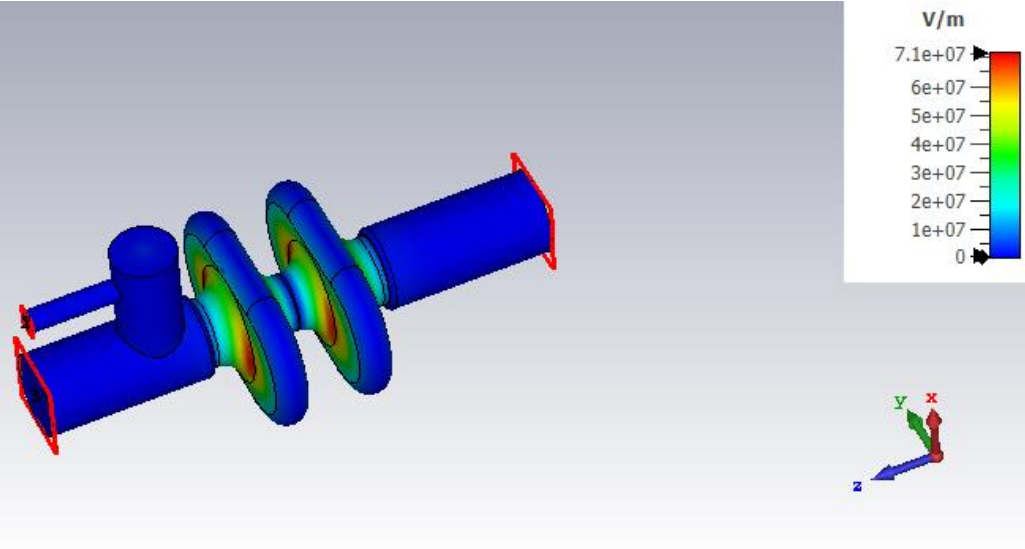
Trapped lower order modes



- Trapped mode in the centre cell may be difficult to damp so may be a larger issue
- Its caused by the racetrack geometry, as can be seen the fields are away from the iris reducing the cell-to-cell coupling
- Solutions:
 - Less elliptical design
 - Larger aperture
 - Elliptical aperture
 - On-cell damping
 - 2 cell design

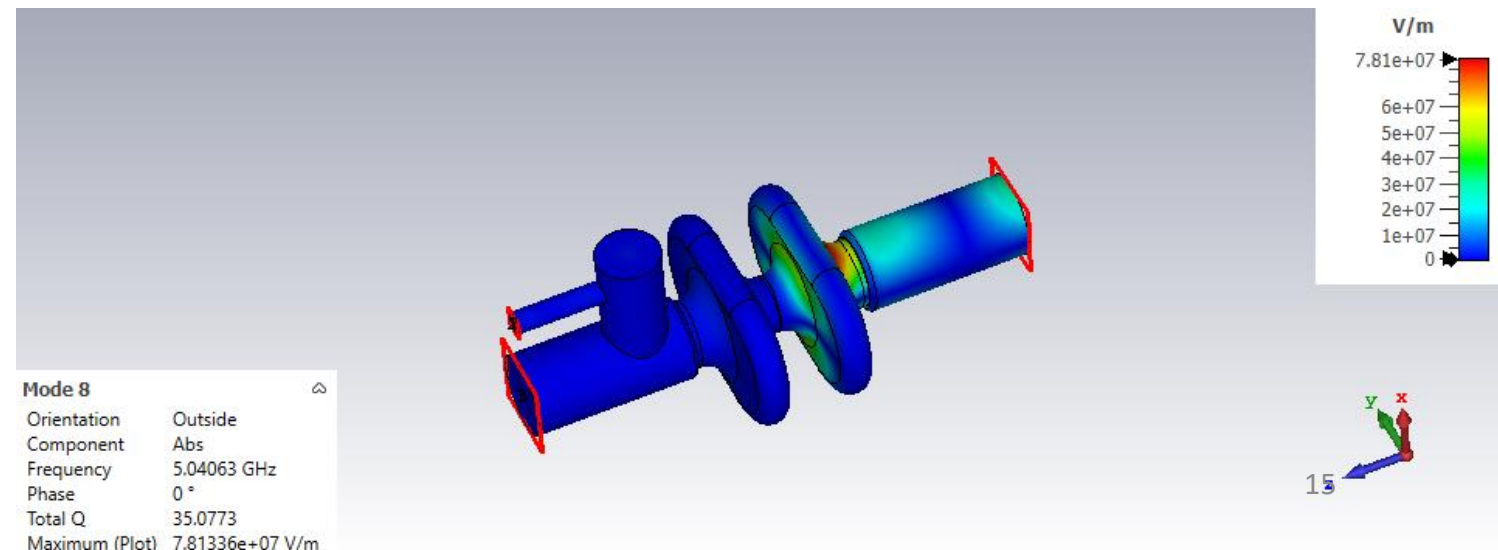


Option 1: 2 cell cavity



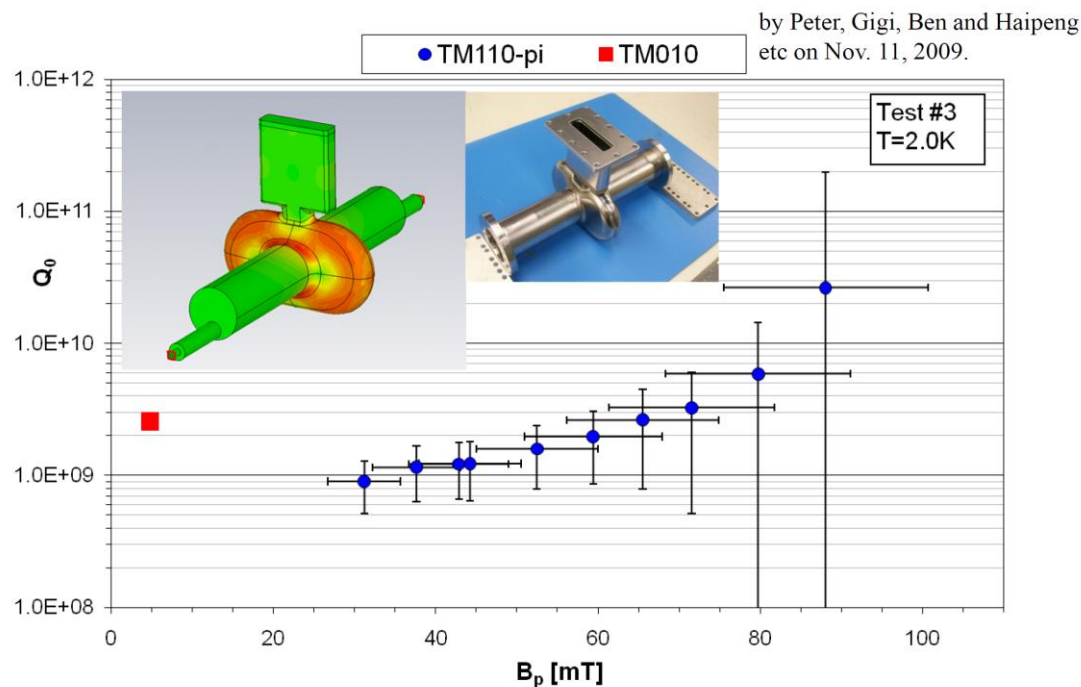
- A 2 cell cavity has no trapped mode
- However the gradient required is much higher unless we use two cavities

- LOM Q factor goes to 500,000
- SOM Q is 35-100 so not an issue.



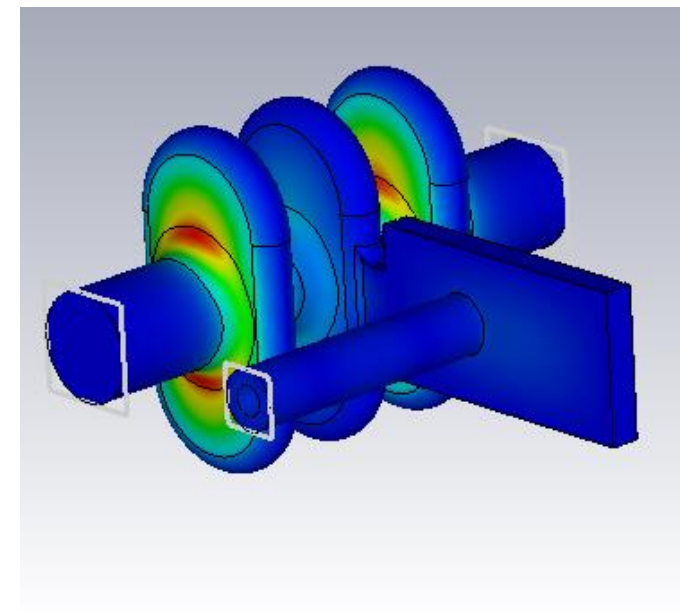
Option 2: Waveguide damping

Jlab developed an on-cell waveguide for SPX, provides better LOM damping



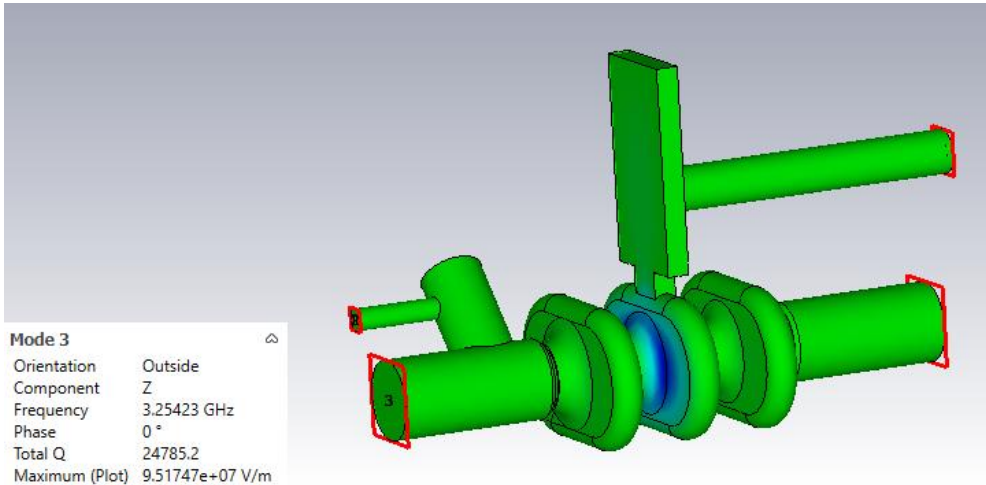
Considering a waveguide section with a coax coupled to it to minimize size and heat leak. Coax can be positioned to prevent coupling to the crabbing mode.

Good damping overall except one mode, unfortunately the highest impedance mode.

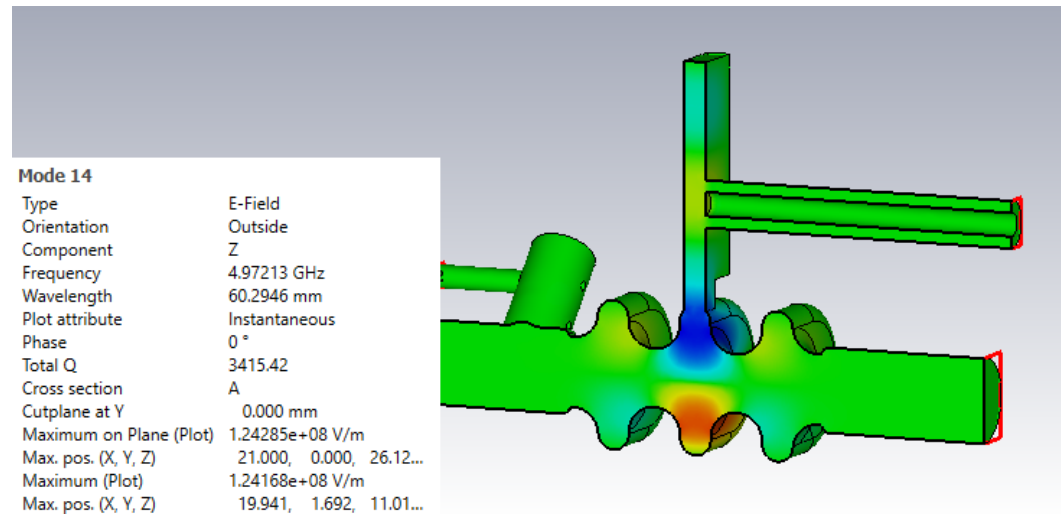
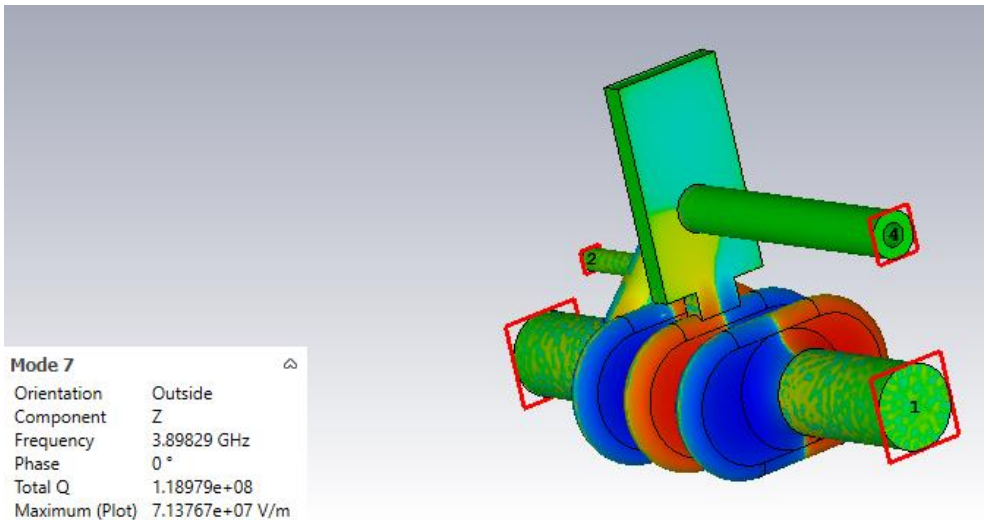


- Waveguide damper does damp the pi and 0 modes well but doesn't damp the pi/2 modes but these will be damped strongly by a coax damper in the beampipes.

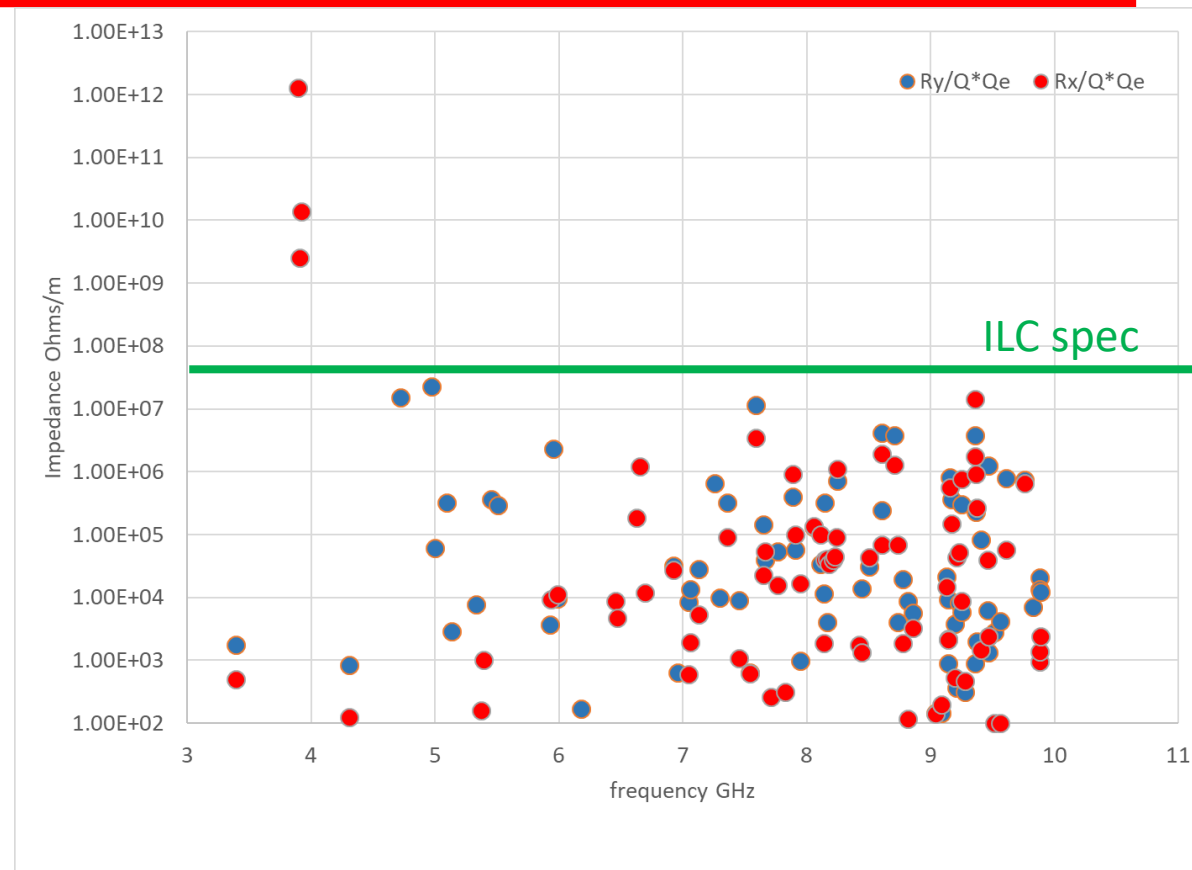
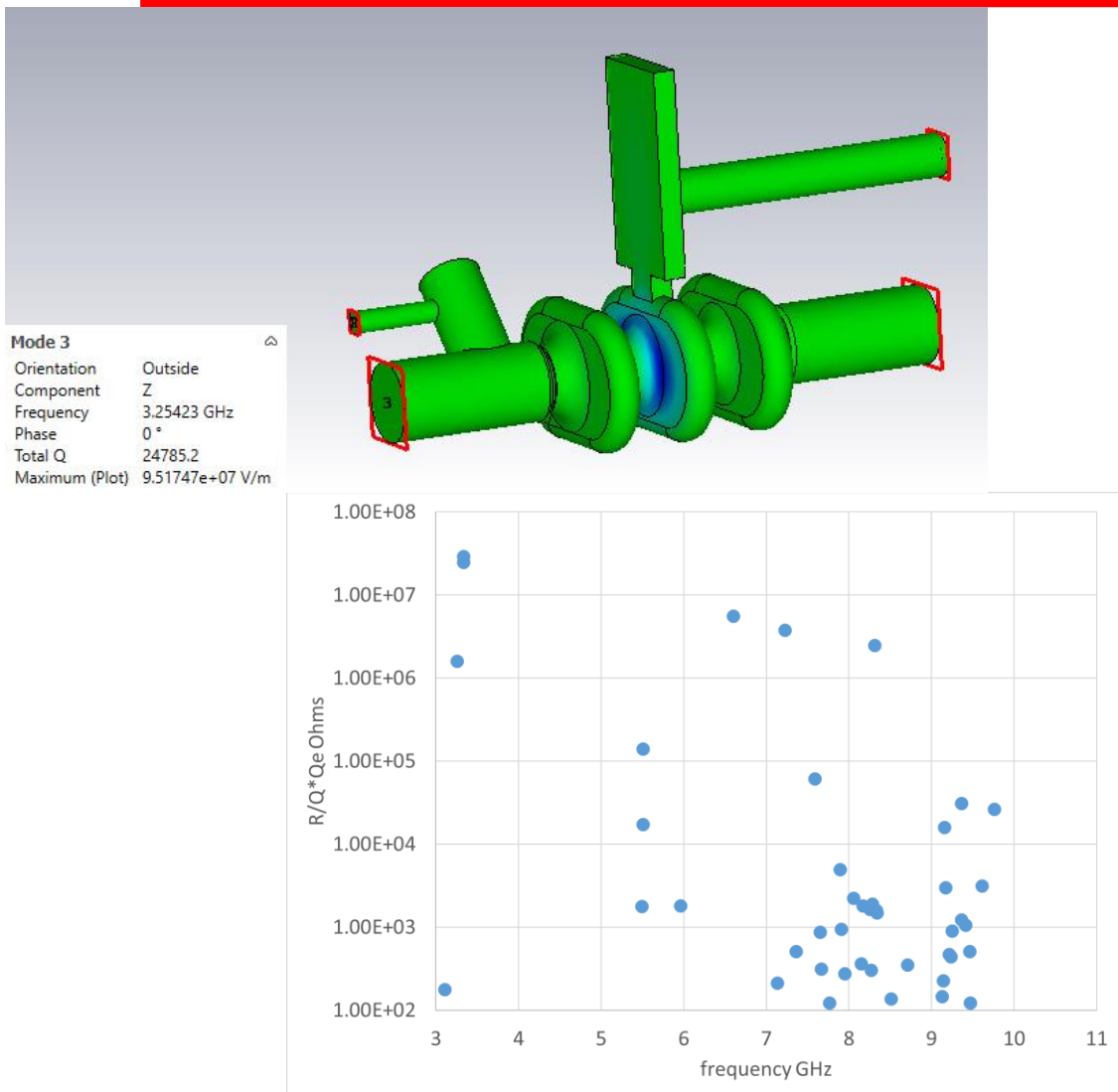
Waveguide damper with coax antenna



- Waveguide has a coax antenna positioned at the field null in the waveguide at 3.9 GHz but field maxima at 3 and 5 GHz to damp LOM and SOM
- LOM Q is 25,000 and SOM Q is 3,500

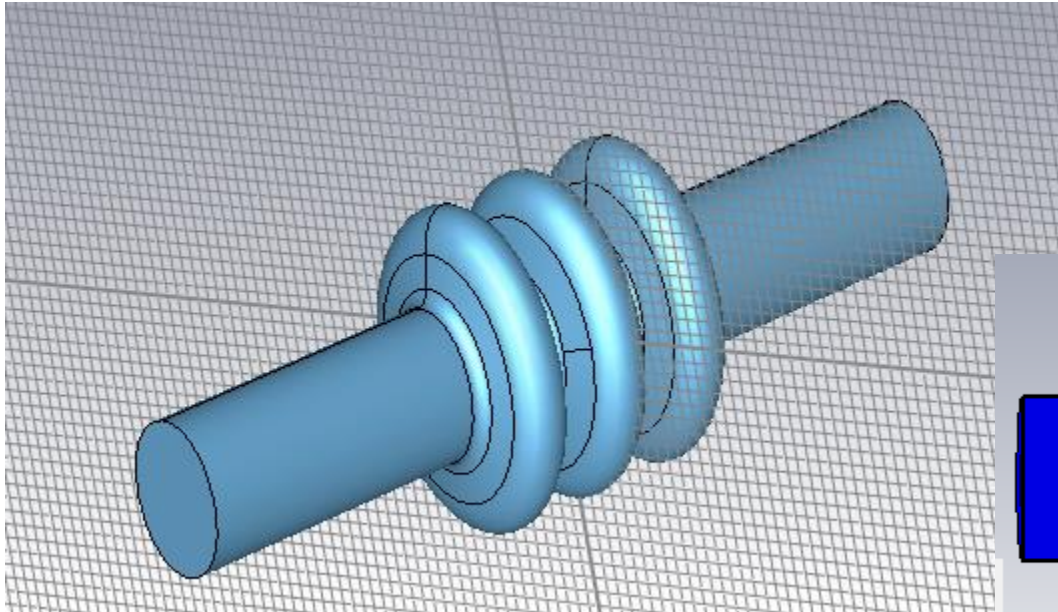


Impedance for waveguide damped 3 cell



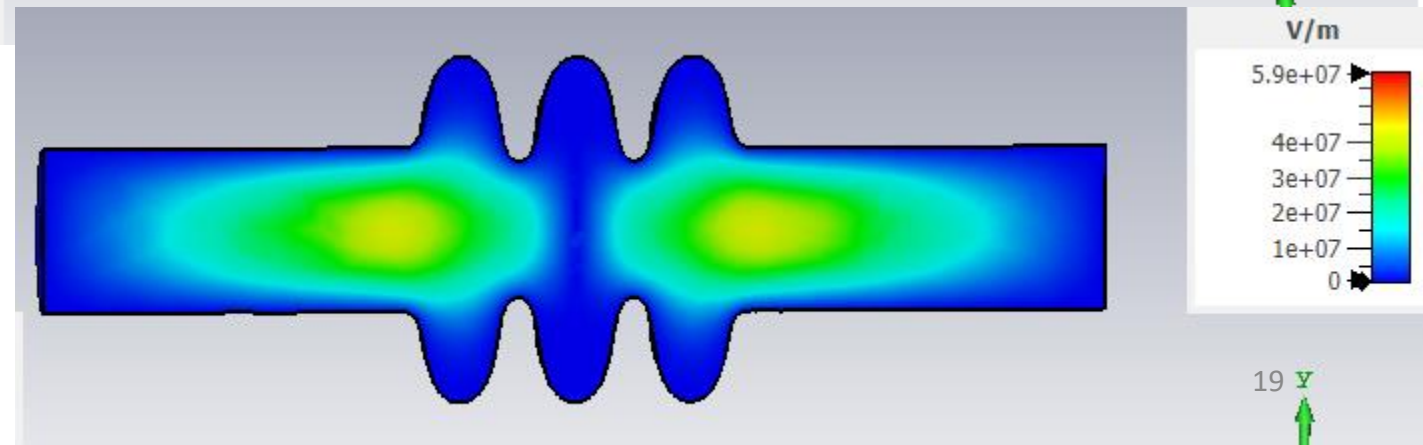
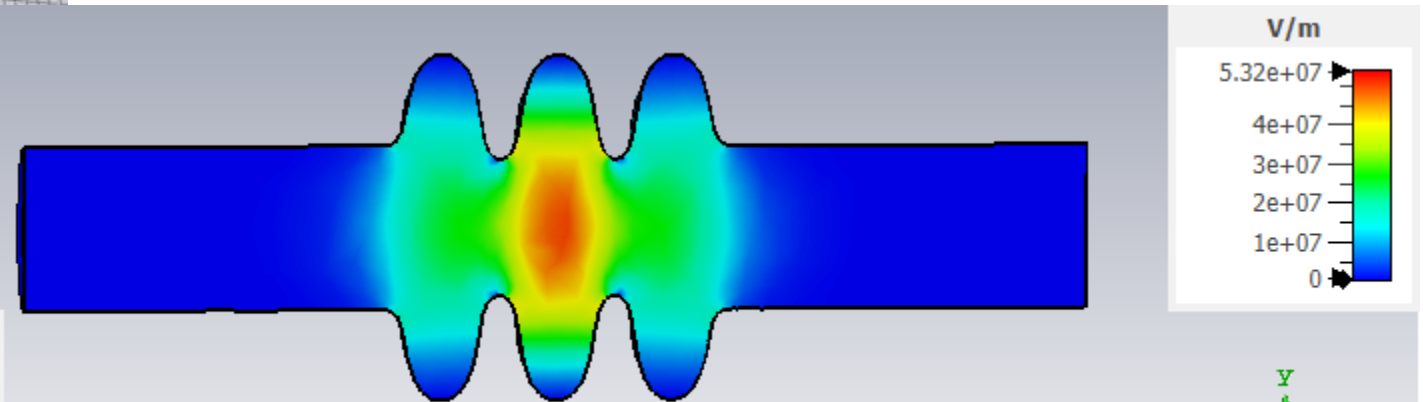
- The long. Impedance has no spec, the transverse impedance meets the spec except the other modes in the crabbing passband
- The FPC may well damp these

Option 3: Elliptical Aperture



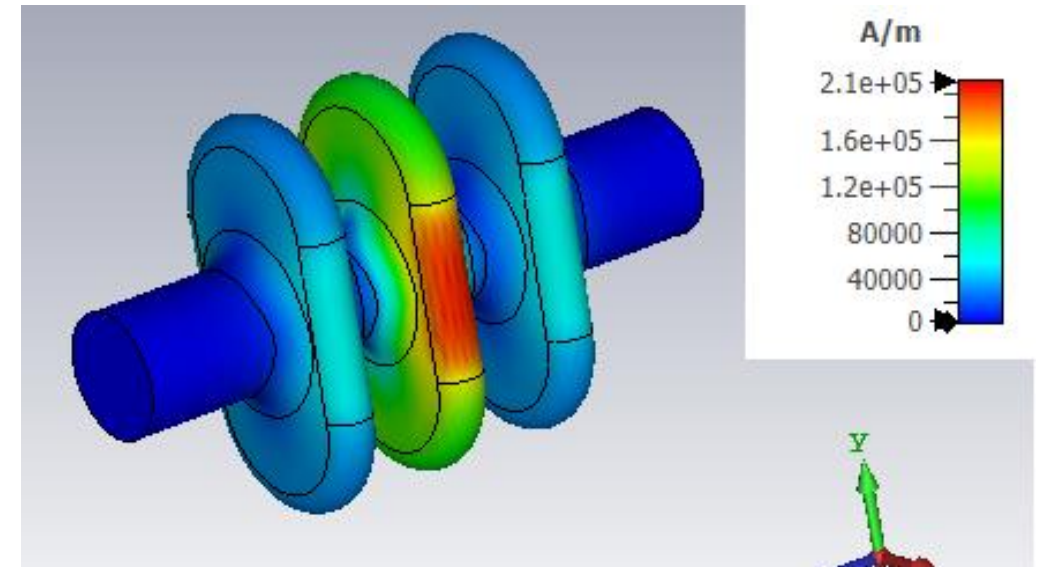
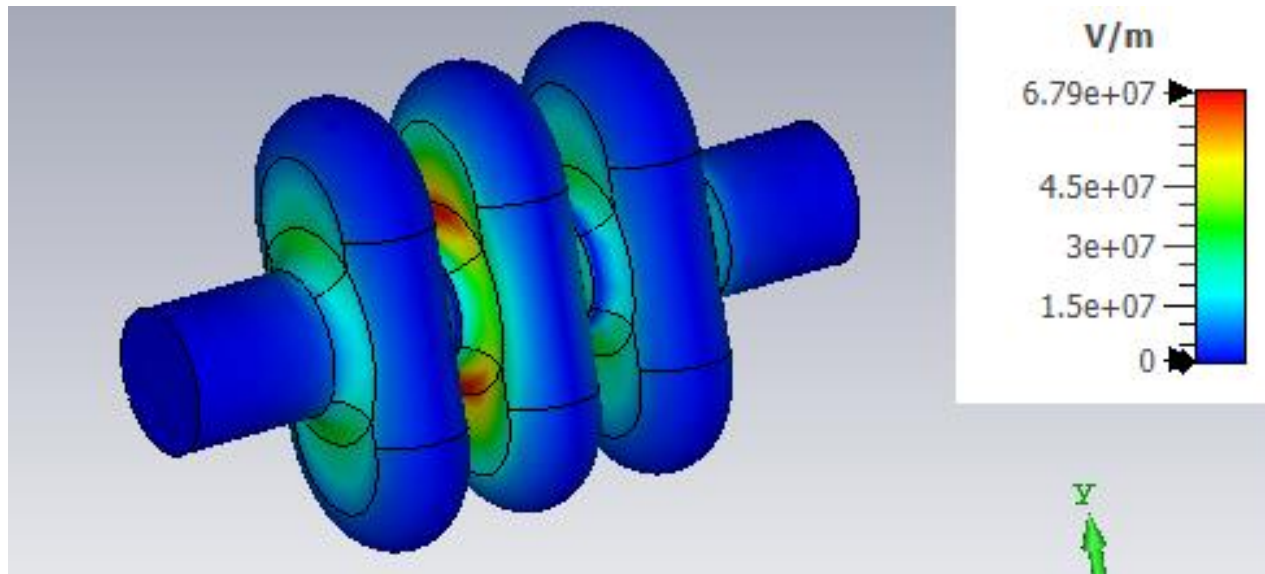
- An elliptical aperture means there is more coupling between the LOM and SOM in each cell.

- LOM is at 3 GHz and has field in all cells now
- SOM actually moves down in frequency not up to 3.3 GHz but beampipe cutoff now 3.4 GHz in vertical plane



Option 4: Larger aperture/ thinner aperture

- 30 mm aperture allows some field in the end cells, which might be OK.
- 35 mm might be better but starts to impact peak fields/ maximum ellipticity



- We had a thick iris as this gave the lowest peak fields but using a thinner iris increases cell coupling
- Peak fields were well below limits (80 mT at 7.2 MV/m)

Design evolution: Option 4 selected

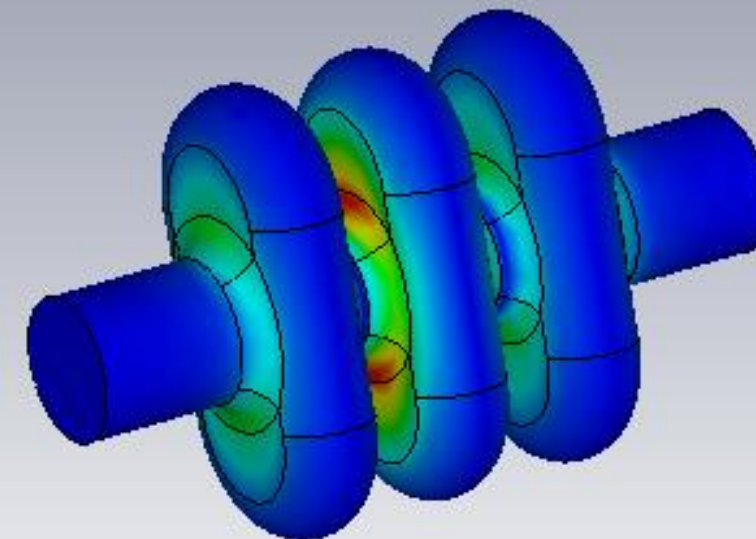
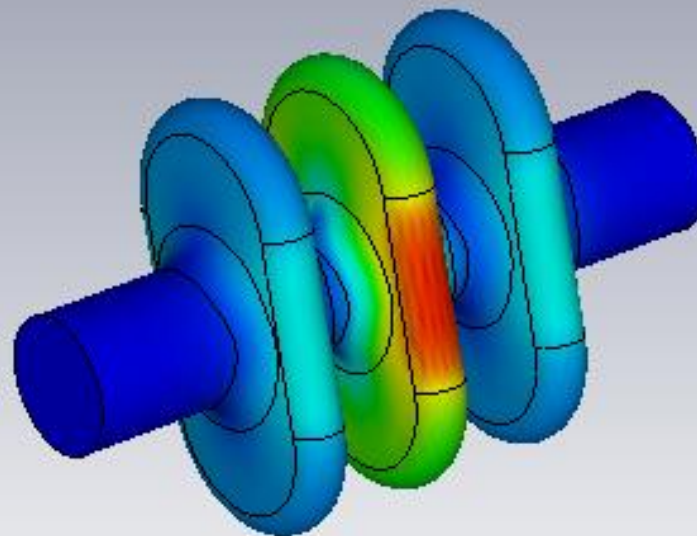
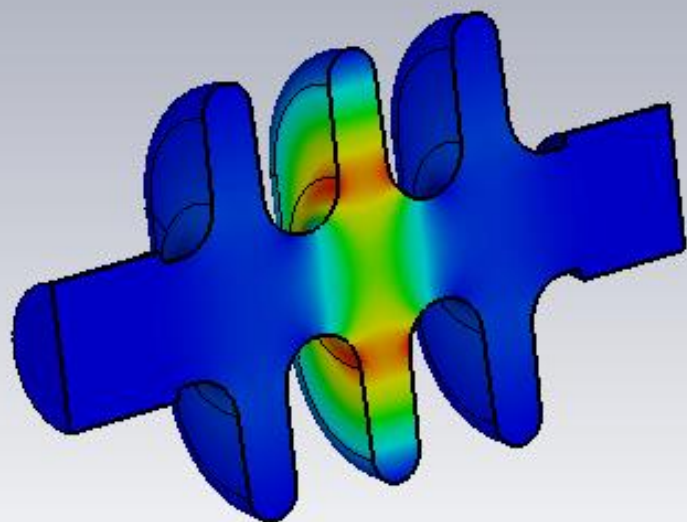
Original design
9.5 MV/m



Larger iris



Thinner iris
7.2 MV/m



Gradients shown are limit for 80 mT

Aperture size = 30 mm, increasing to 40 mm
Cavity major/min radii = 55.7 / 30.6 mm
Ration major/min axis = 0.55

LOM freq= 3.3 GHz
SOM freq= 5.0 GHz

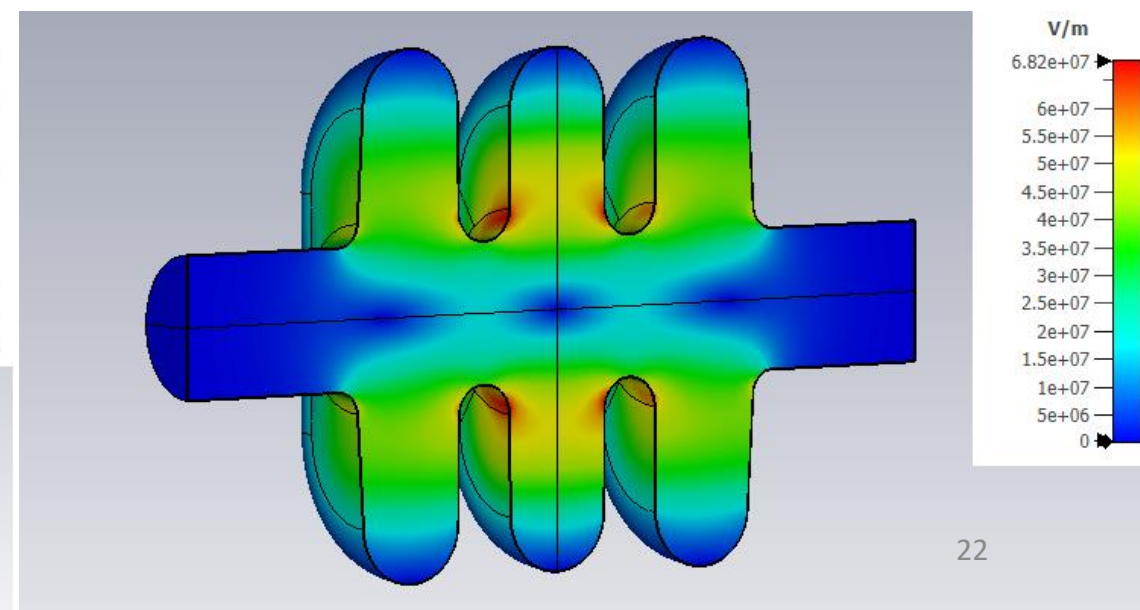
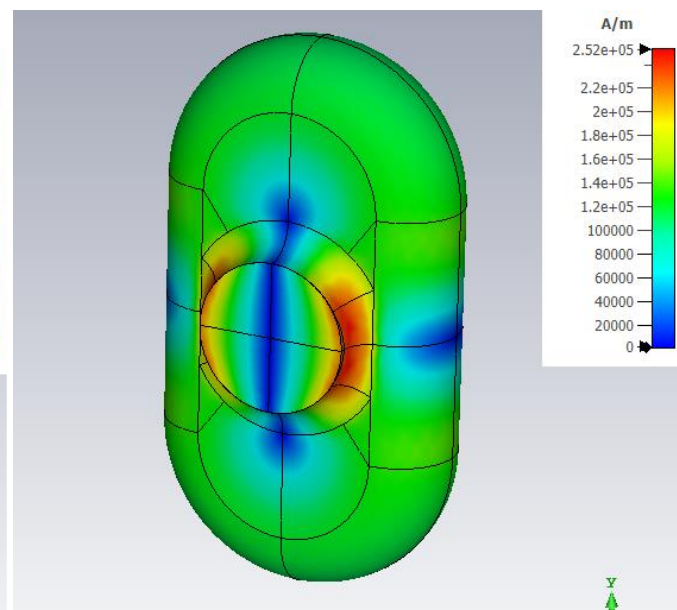
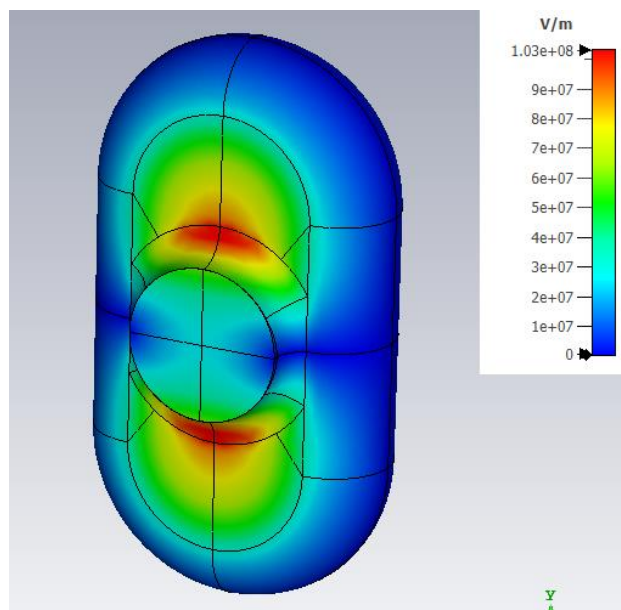
Final mid-cell and 3 cell

Mid-cell

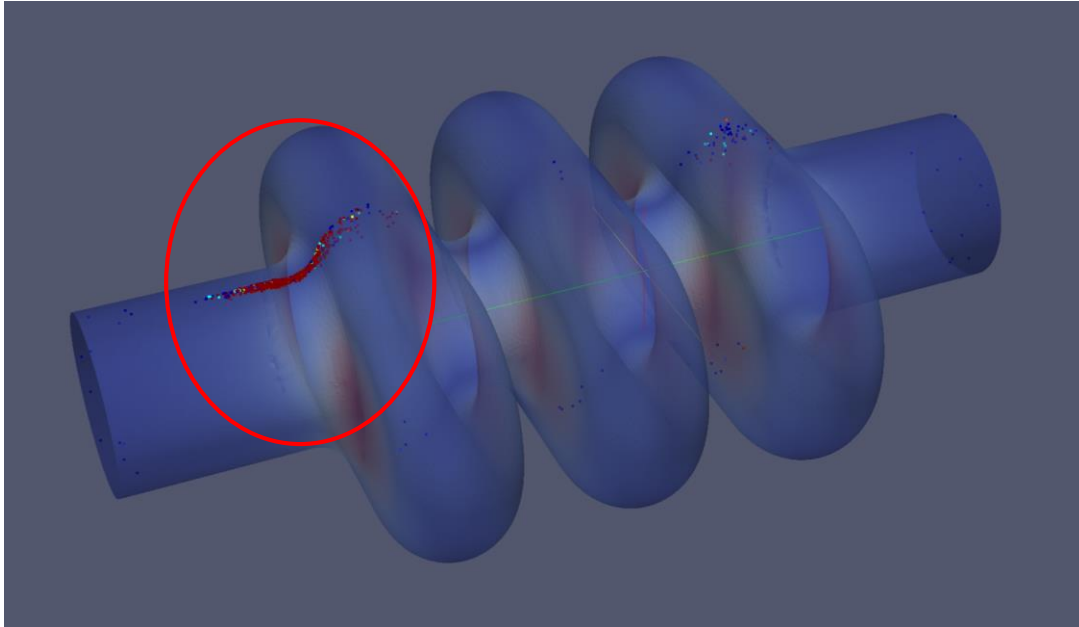
Required E_t^*	5.00	MV/m
E_{pk} operational	18.20	MV/m
B_{pk} operational	56.10	mT
B_{pk}/E_{pk}	3.08	
R_t/Q	48.00	Ohms
G	202.00	

3 cell

Required E_t^*	5.3	MV/m
E_{pk} operational	22.5	MV/m
B_{pk} operational	66.6	mT
B_{pk}/E_{pk}	2.96	
R_t/Q	140.00	Ohms
G	207.00	

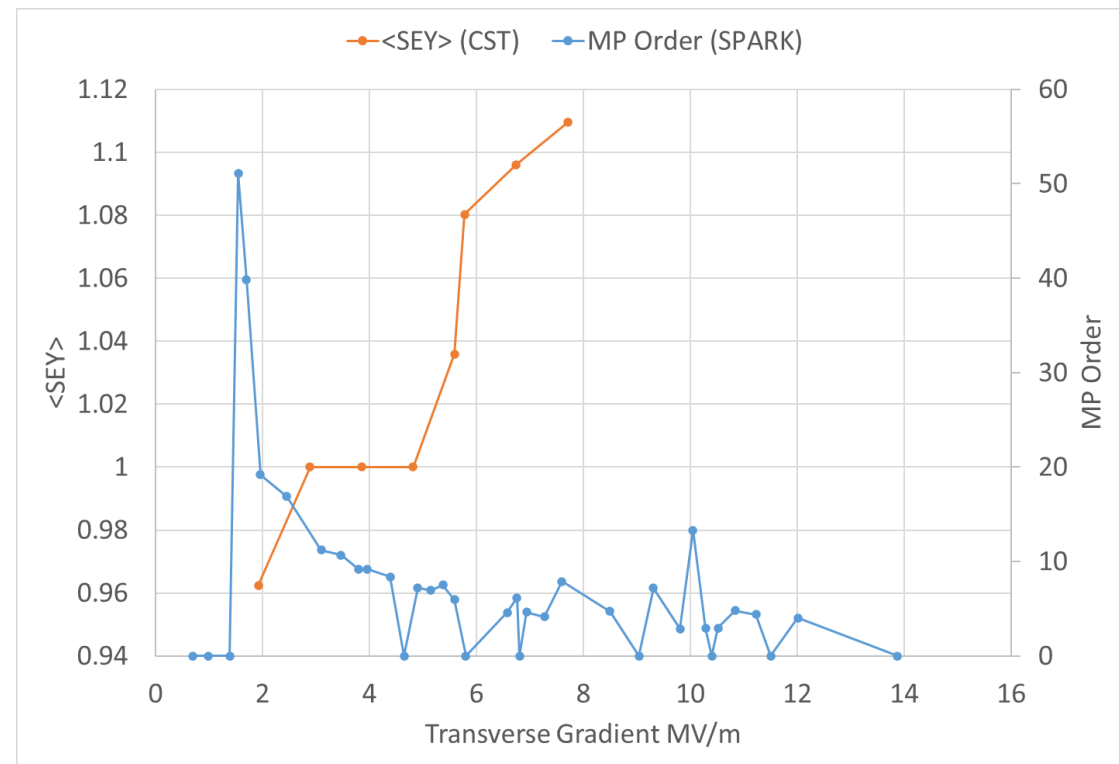


Multipactor

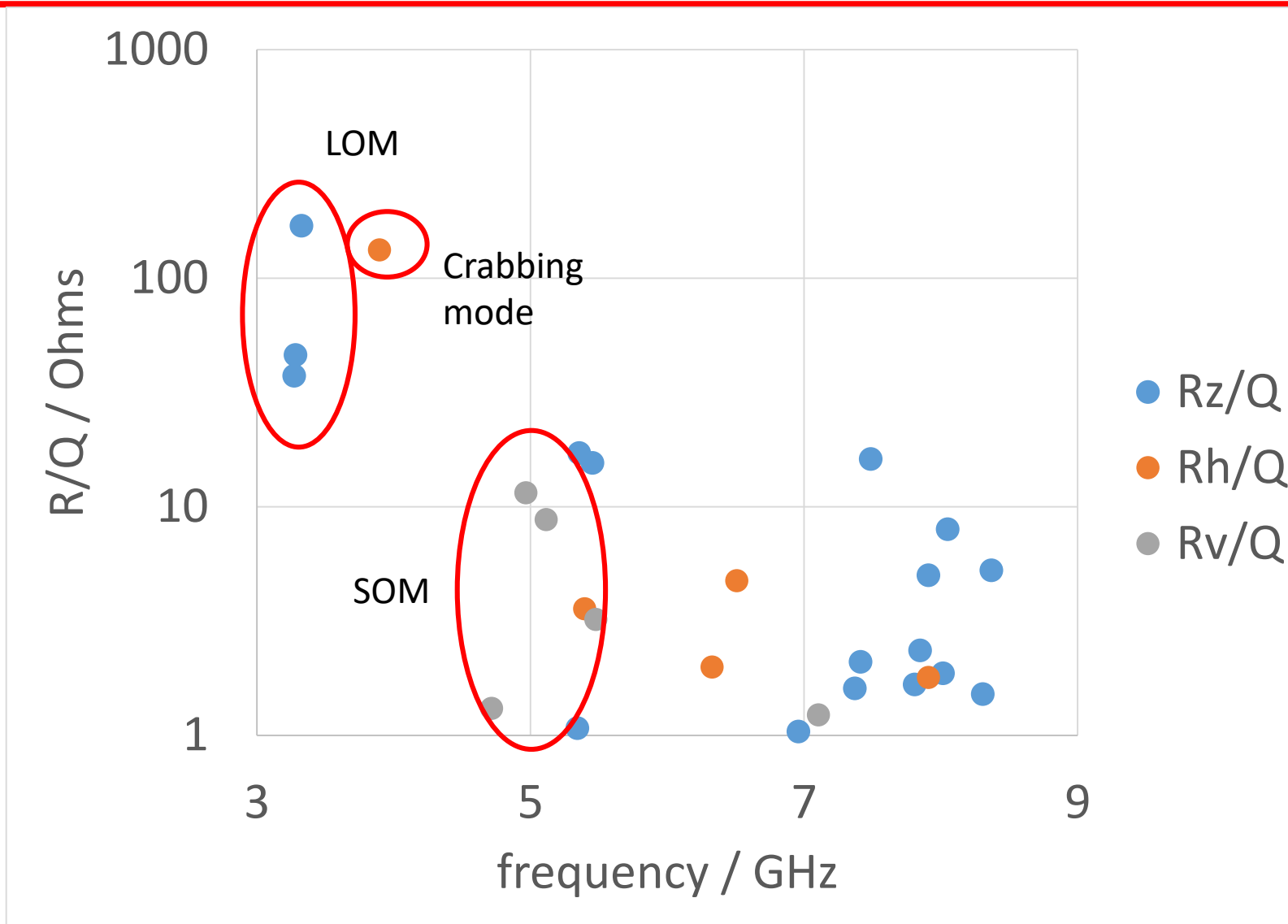


- Higher order (4th – 6th), slow-growing multipactor band found at 5.6 MV/m on minor axis iris of the end cell
- No growth below 5.6 MV/m in CST
- Multipactor is only on the end cell iris not the middle iris.

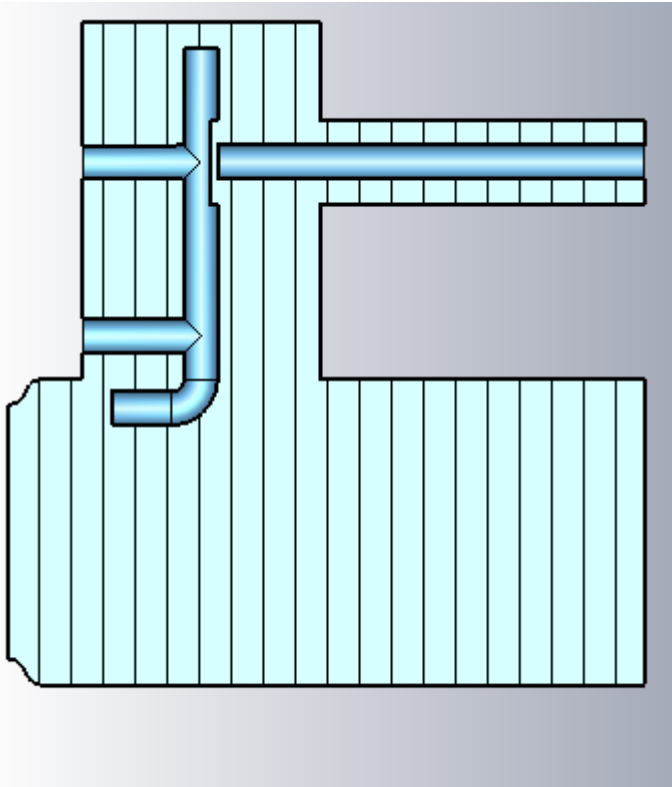
- Mid cell multipactor is up at 8 MV/m nothing seen below this
- Original elliptical design and smaller aperture design had no multipactor so clearly scope to move this
- The end cell has very low peak fields so design can prioritise multipactor suppression



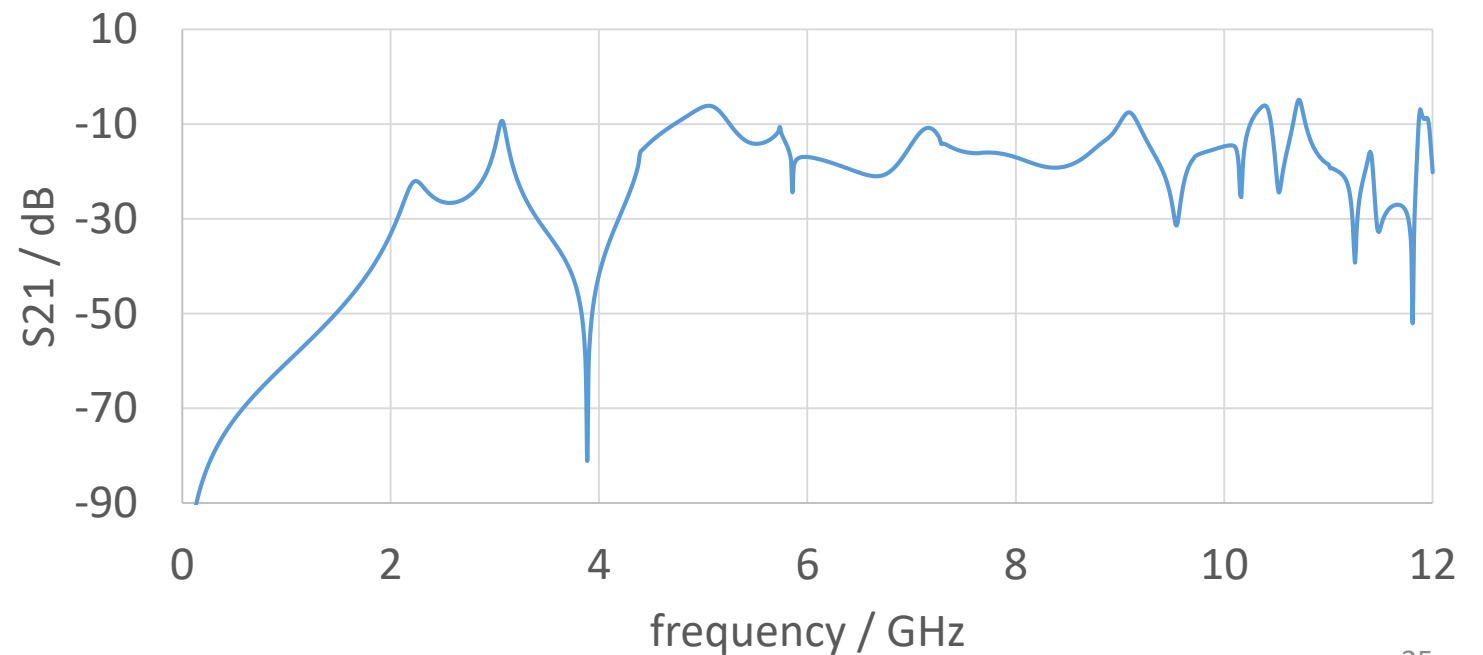
Mode spectrum



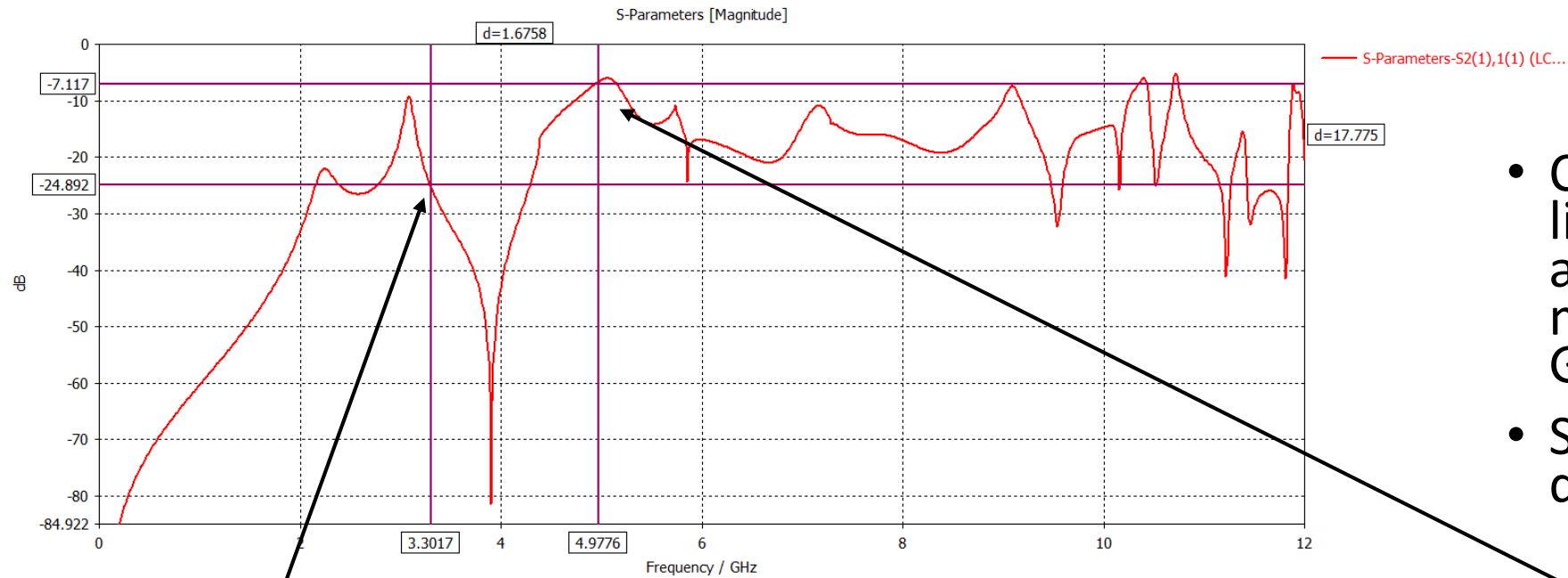
HOM coupler design



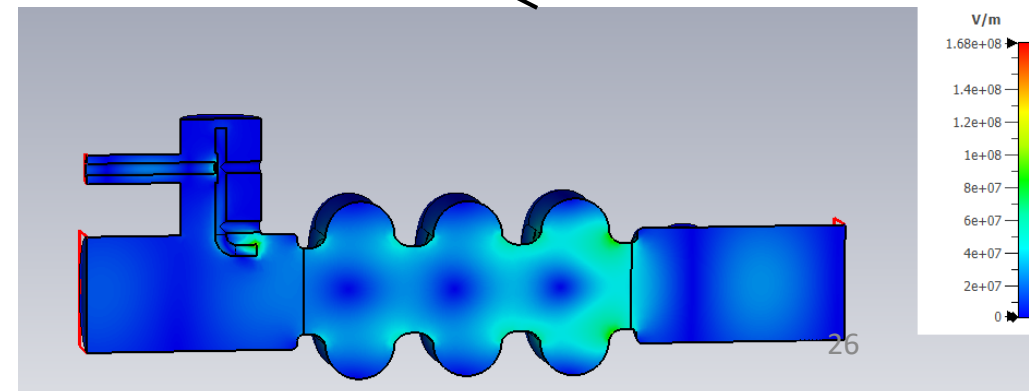
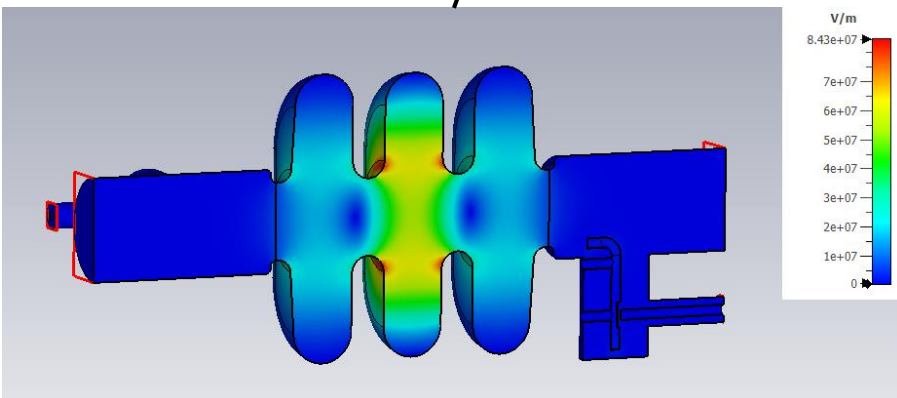
- Modified version of old ILC HOM coupler, similar to ILC main linac coupler
- Designed to have larger transmission at the LOM and SOM frequencies while filtering 3.9 GHz



Coax Coupler at key modes

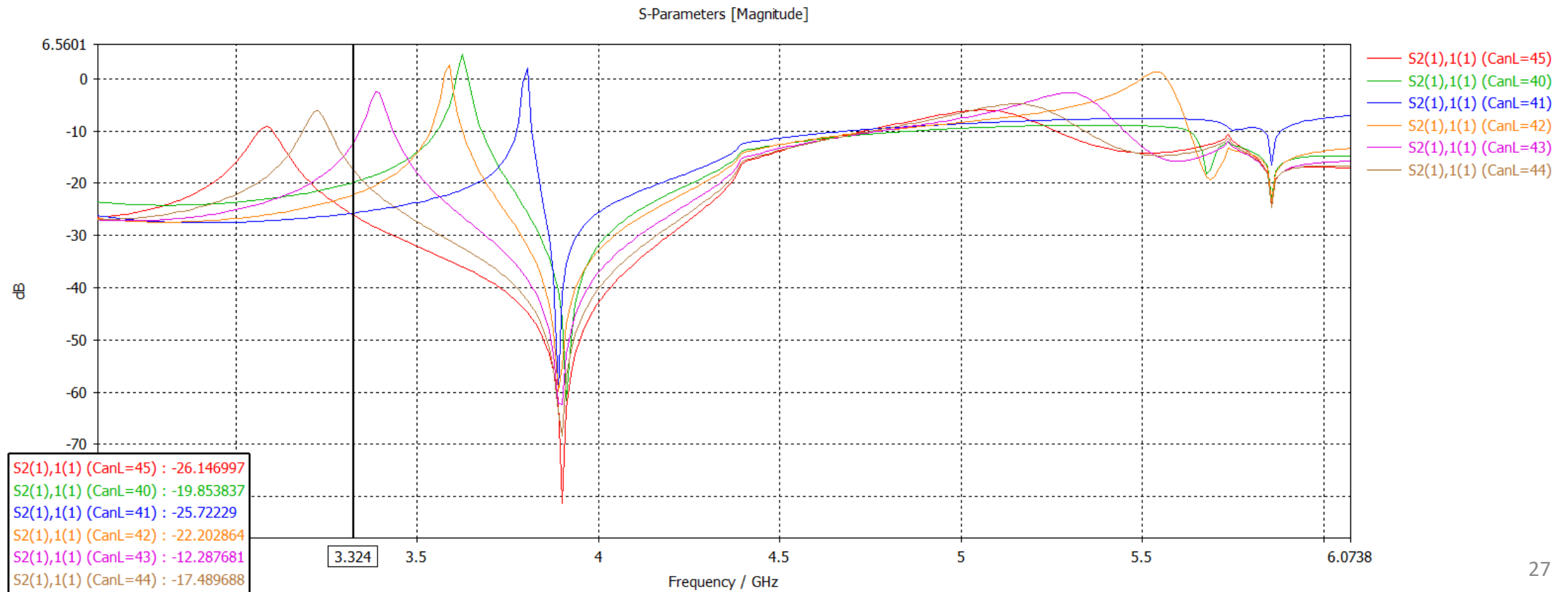


- Could do with a little optimization around the LOM to move peak to 3.3 GHz
- SOM is well damped



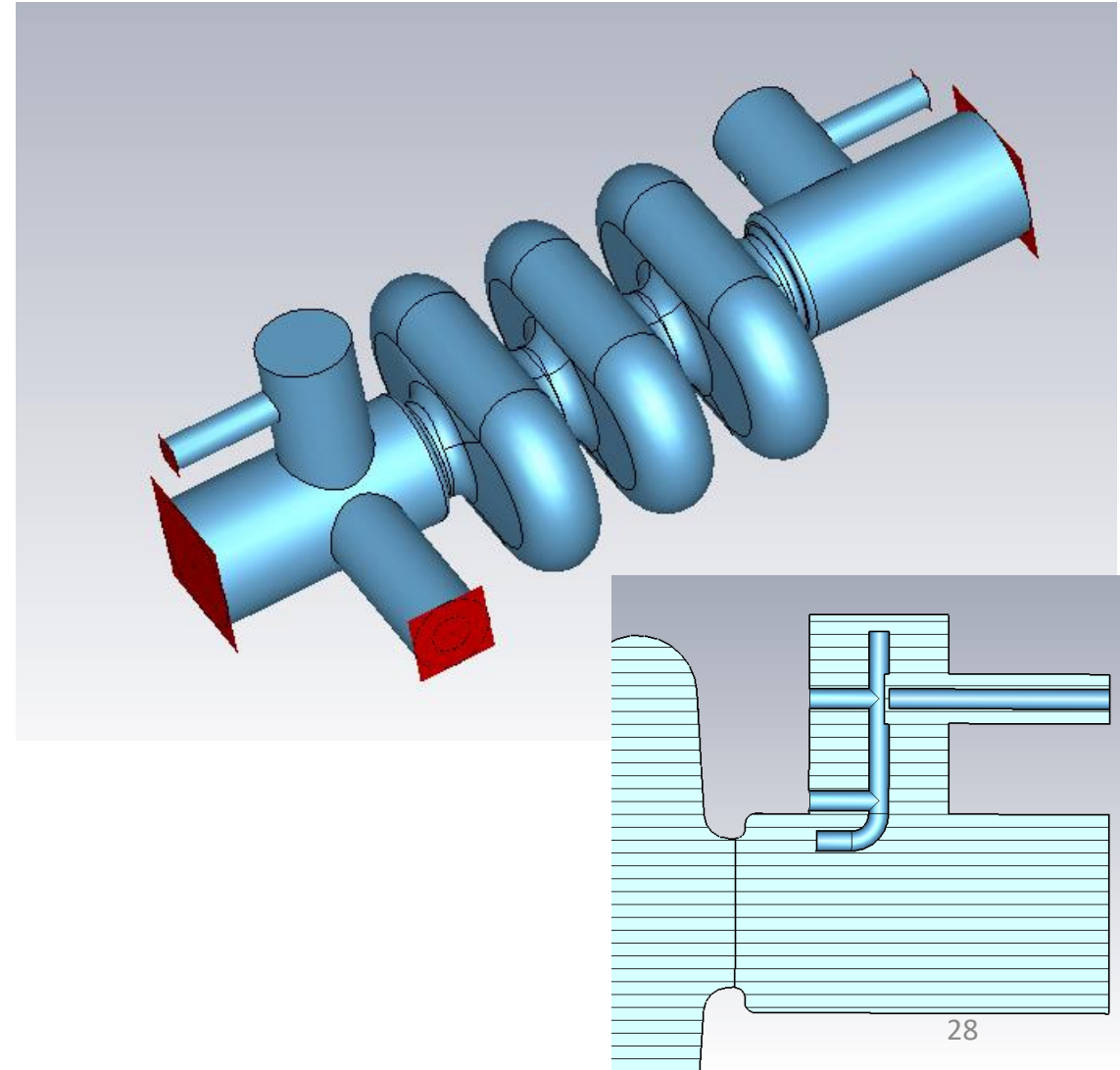
Improved HOM design

- Making the HOM can 2.5 mm shorter shows strong damping on the LOM at 3.3 GHz but impedance calculations were done with old design

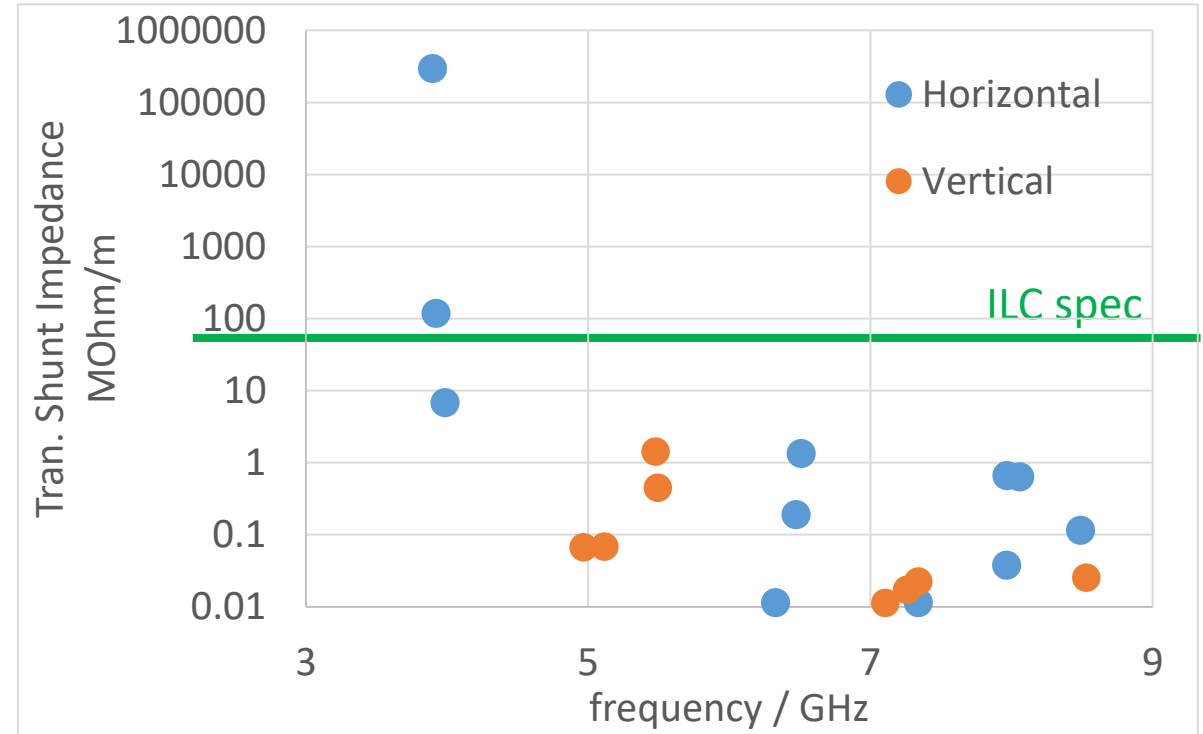
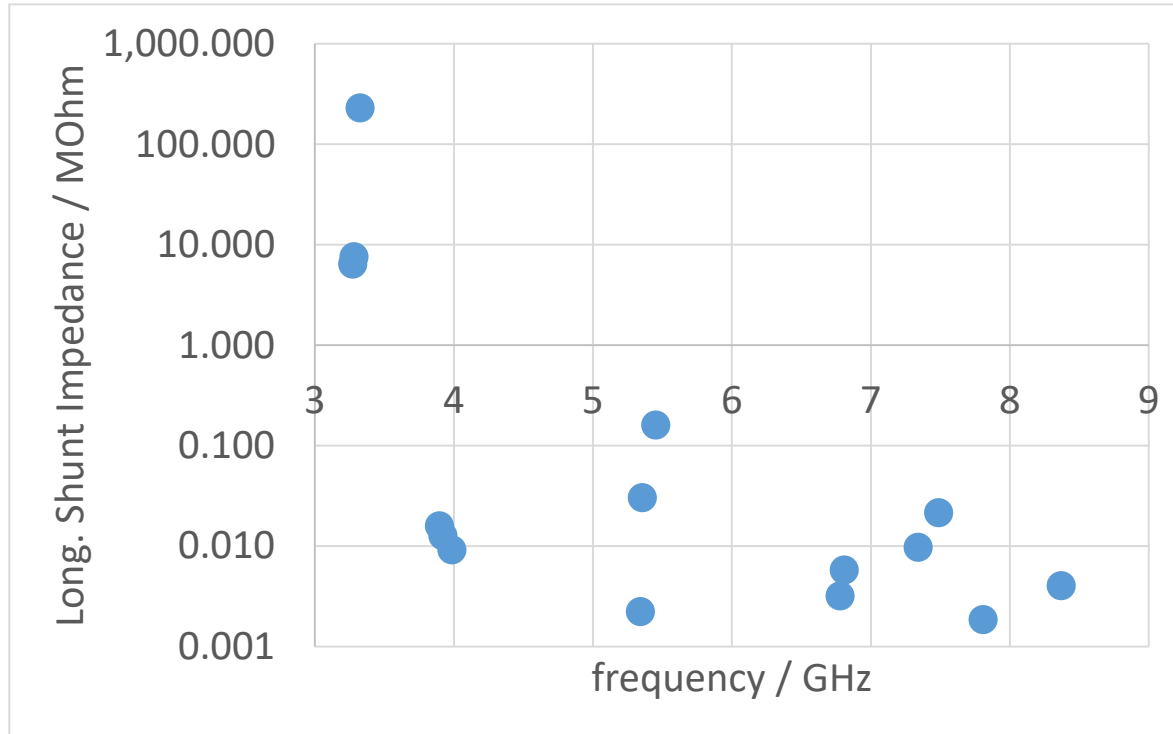


HOM coupler configuration

- The beampipe expands to 20 mm radius to push the cutoff frequency of the TM₀₁ mode down
- This has negligible effect of RF performance
- Use two identical coaxial HOM couplers
- HOM protrudes into the beampipe but still respects 25 mm clearance



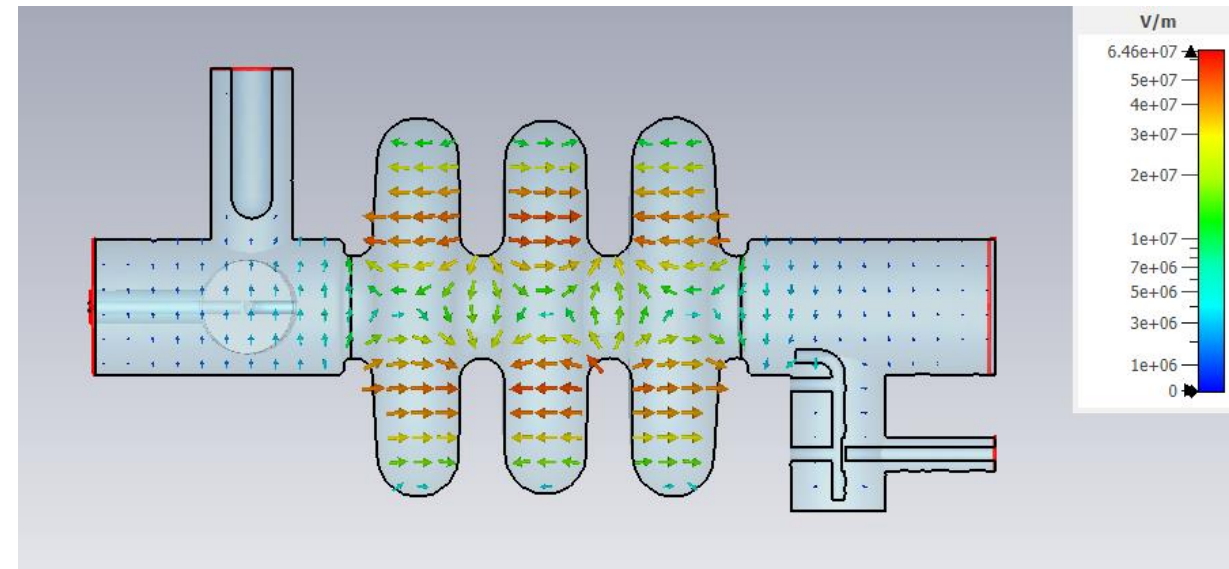
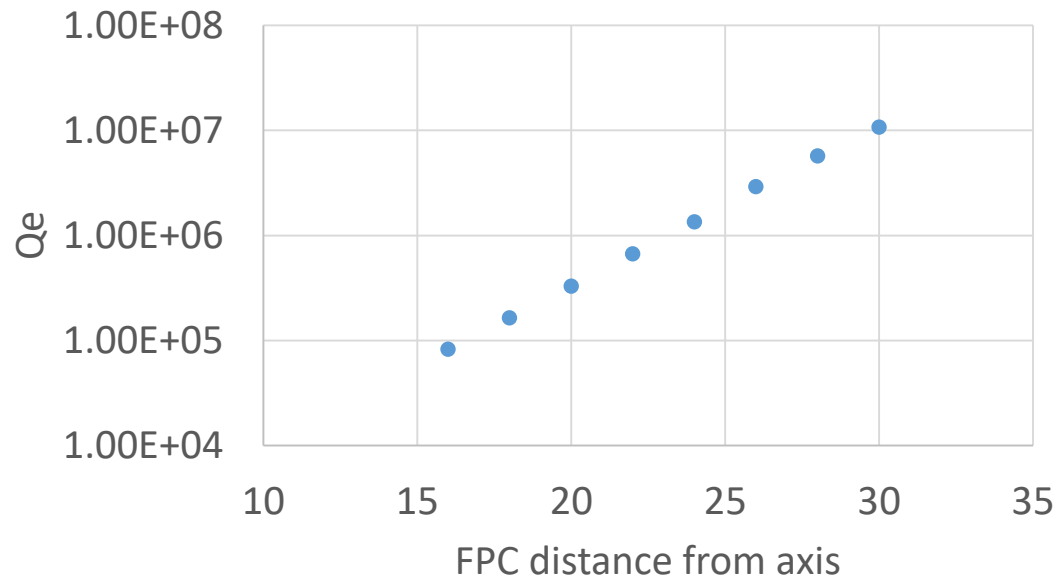
Impedance for coax damped 3 cell



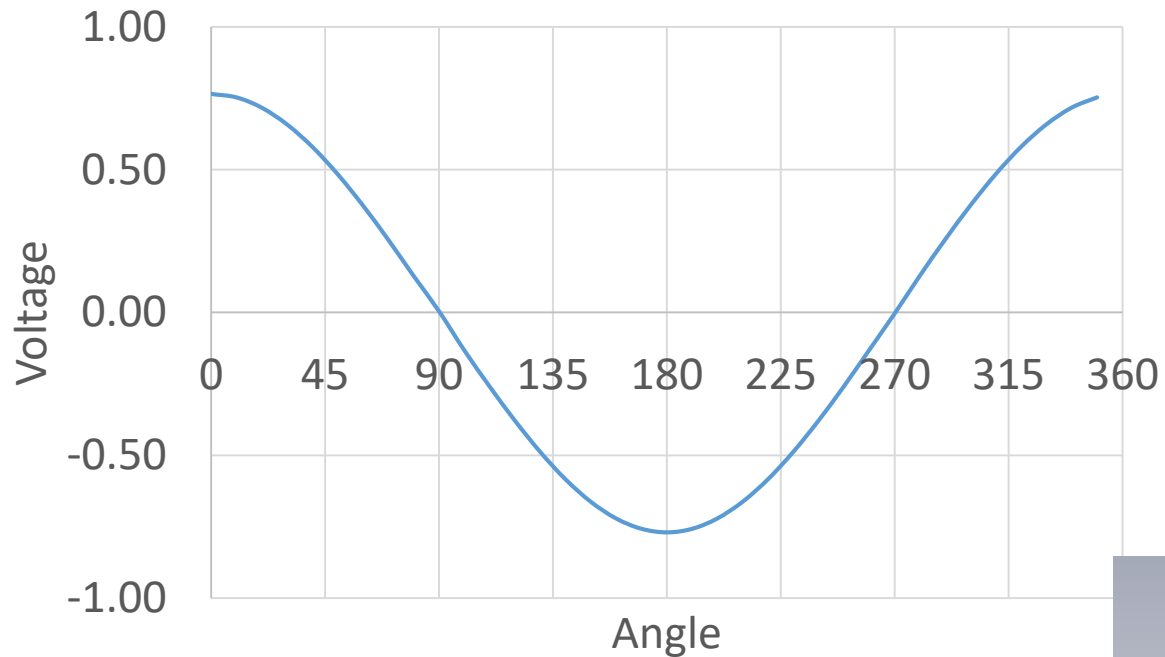
- The long. Impedance has no spec, Q achieved is around 2×10^5
- The transverse impedance meets the spec except the other modes in the crabbing passband
- The FPC will likely damp these

Fundamental power coupler

- Required QL is 10^7 as the beam power at 0.5 mm is 200 watts.
- FPC is 30 mm off axis (10 mm from the beampipe) or could shift further from the cavity

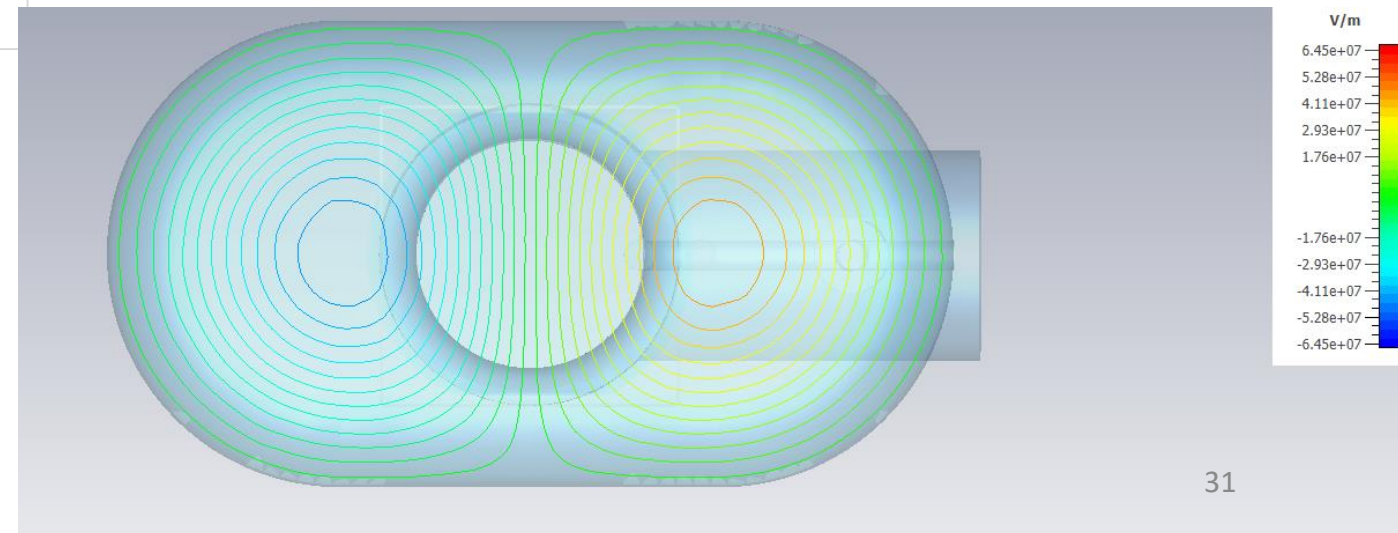


Multipole with couplers

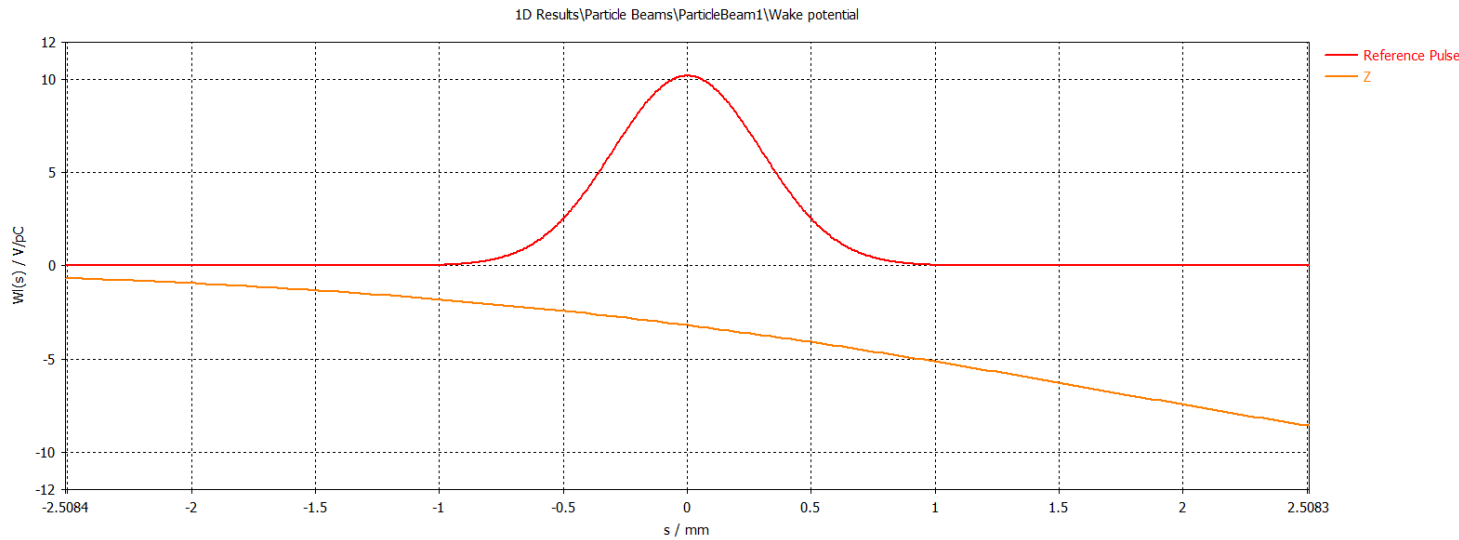


- At 5 MV/m the longitudinal voltage on axis is 570 V
- The multipoles at 5 mm normalized to b1 are shown in the table (up to b3):

b1	1
b2	0.102346
b3	251.7836



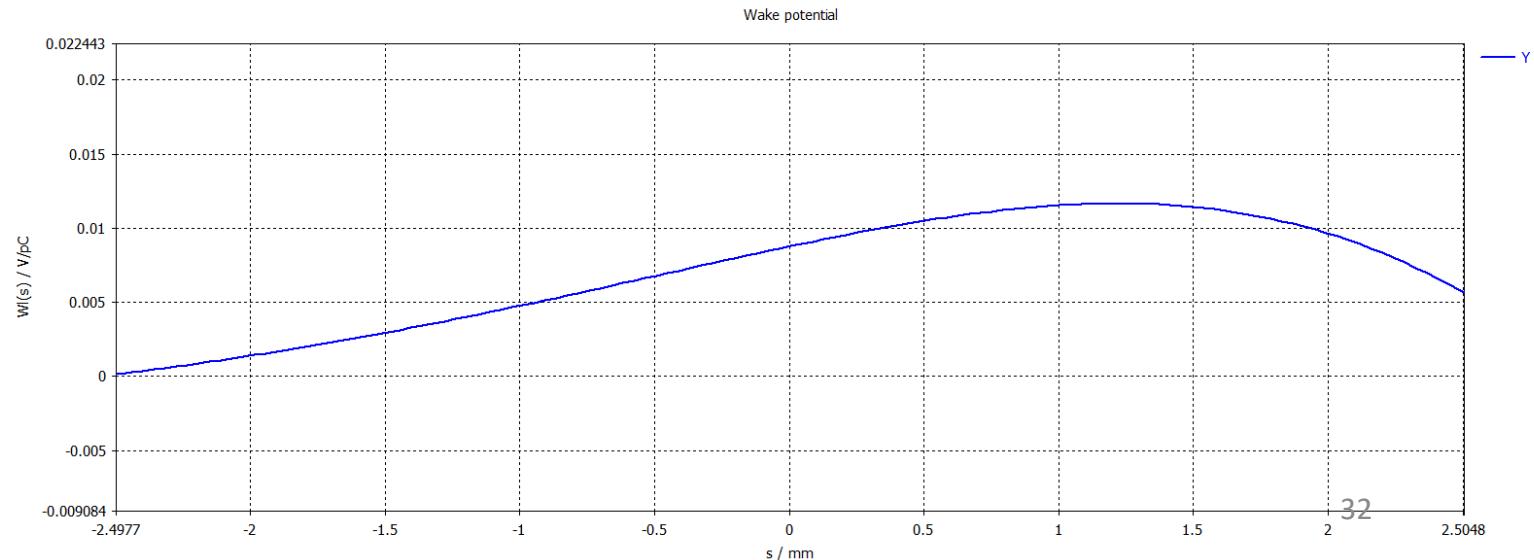
Short range Wake



- The short range wake has been calculated for a 0.3 mm long bunch.
- The transverse voltage was calculated with a 1 mm offset
- Both long. and trans. Wakes are very small

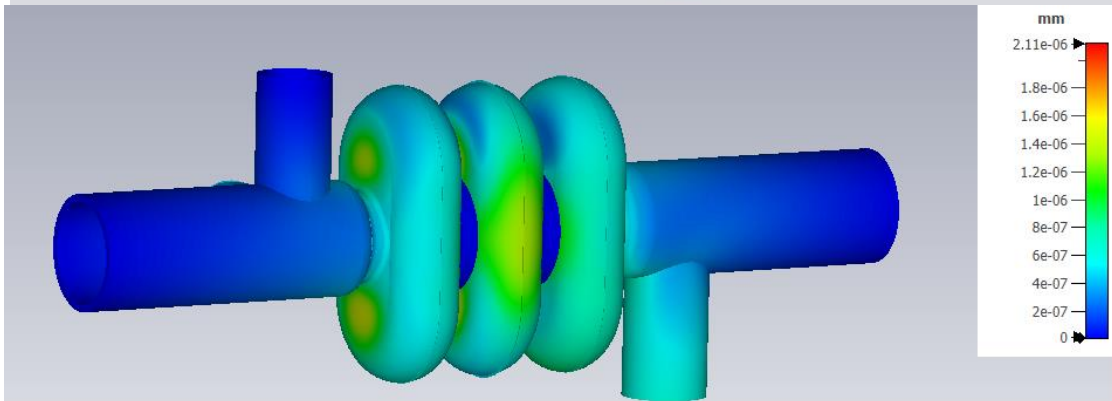
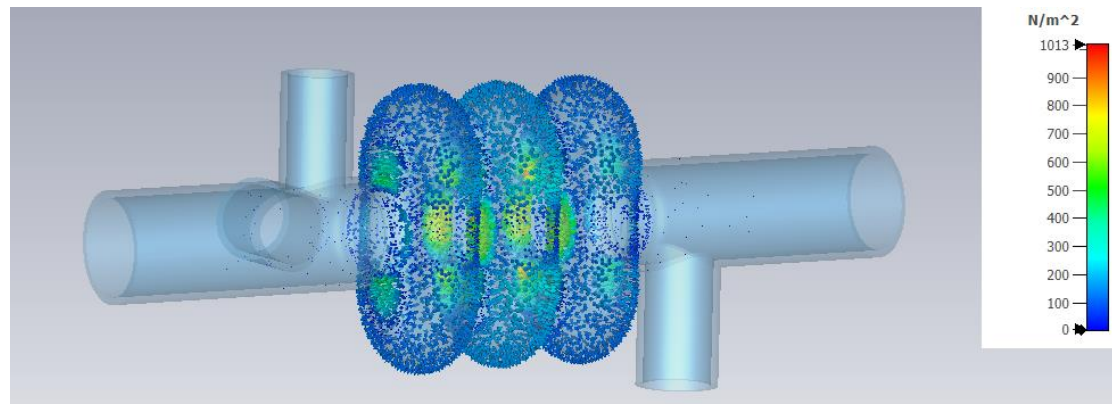
Loss factor= 3.2 V/pC

Kick factor = 16 V/pC/m

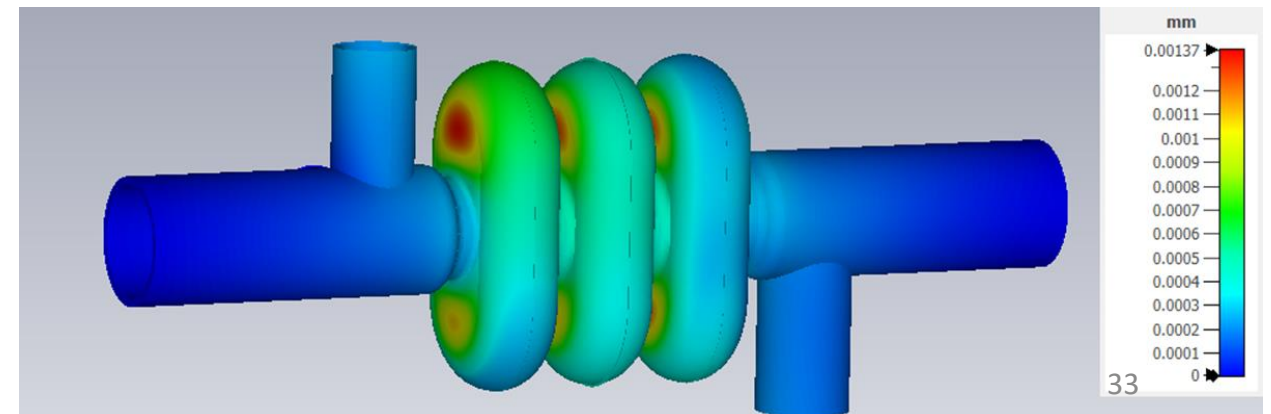


Lorentz force and pressure deformation

- Lorentz force is 1.0 kN/m^2 at 5 MV/m gradient which is fairly small
- Equivalent to a 4 nm change in the cavity length (for 3 mm thick walls) which is 120 Hz ,



- The frequency shift due to a 1 bar pressure difference is 90 kHz hence the pressure sensitivity is 90 Hz/mbar
- Max Stress is 5.4 MPa

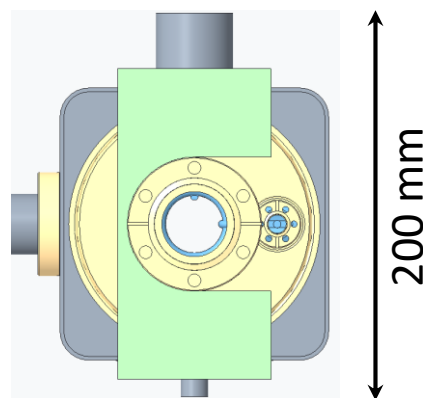
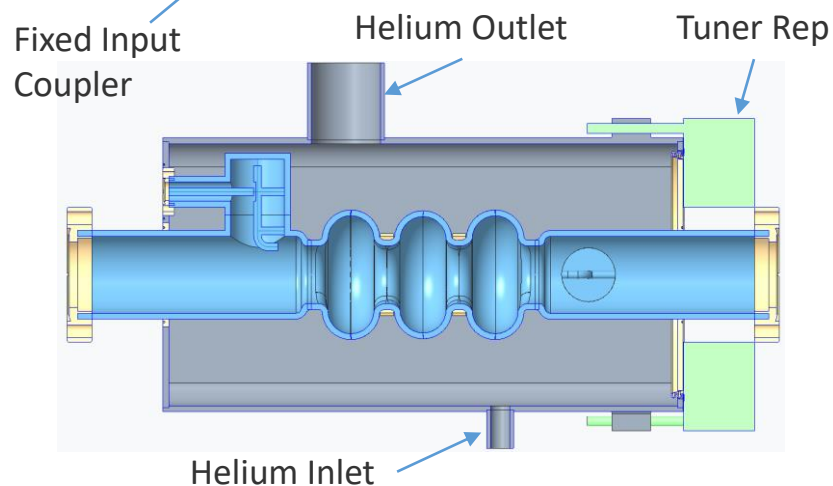
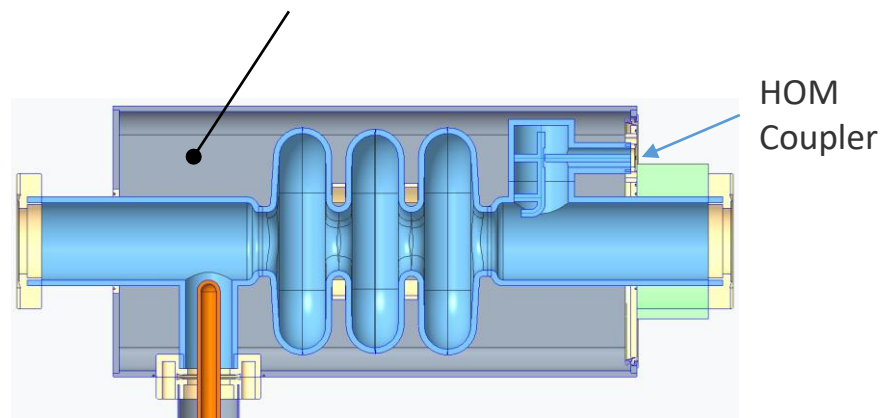


UK ILC Crab Cavity Cryo Design

James Bourne & Niklas Templeton

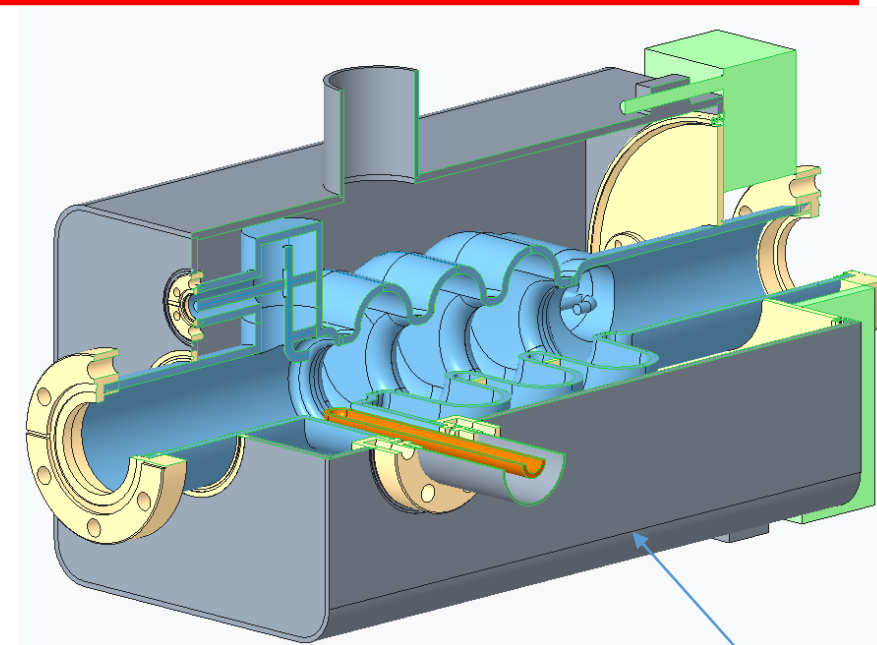
UK ILC 3.9GHz Racetrack Crab Cavity

Helium Tank Internal Volume 4.3 litres (PED Category I)



370 mm

140 mm



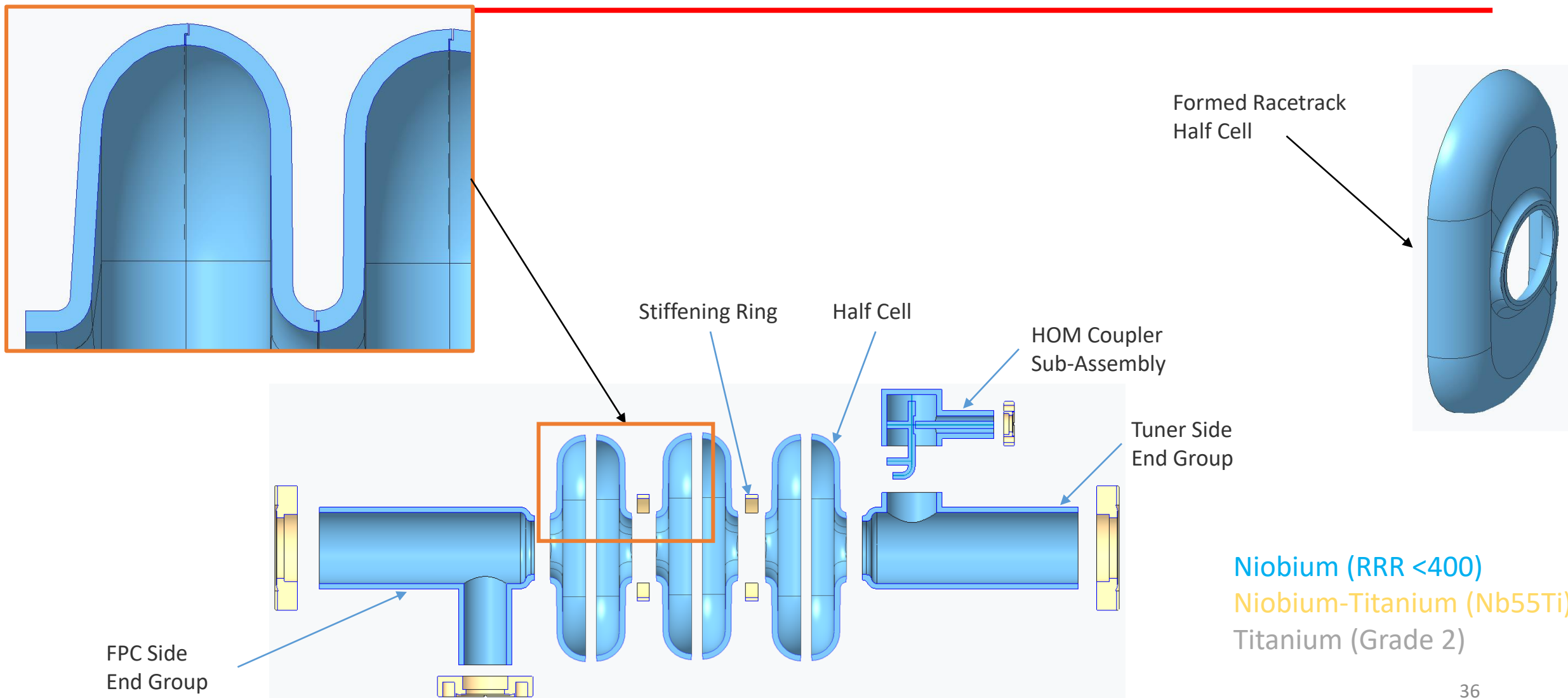
Helium Tank

Niobium (RRR <400)

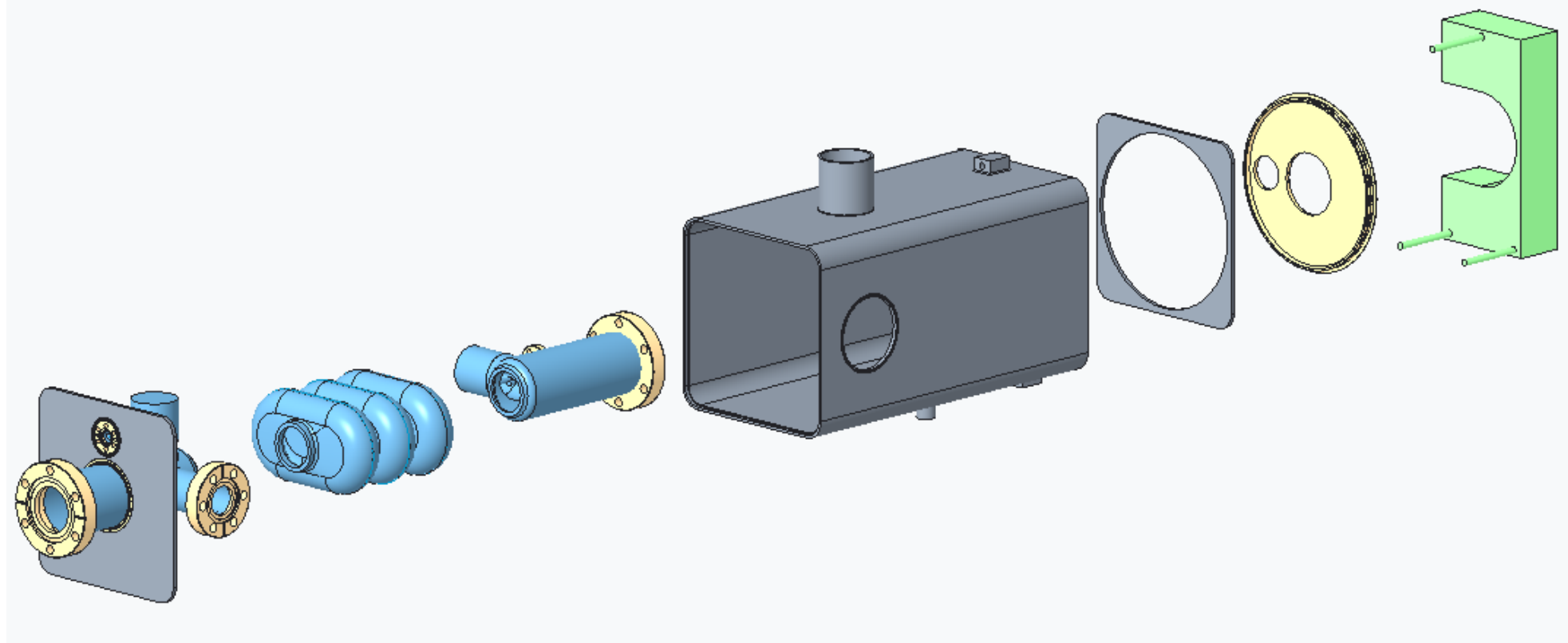
Niobium-Titanium (Nb55Ti)

Titanium (Grade 2)

UK ILC 3.9GHz Racetrack Crab Cavity – Fabrication



UK ILC 3.9GHz Racetrack Crab Cavity - Assembly



Niobium (RRR <400)

Niobium-Titanium (Nb55Ti)

Titanium (Grade 2)

1 Cavity Cryomodule Schematic

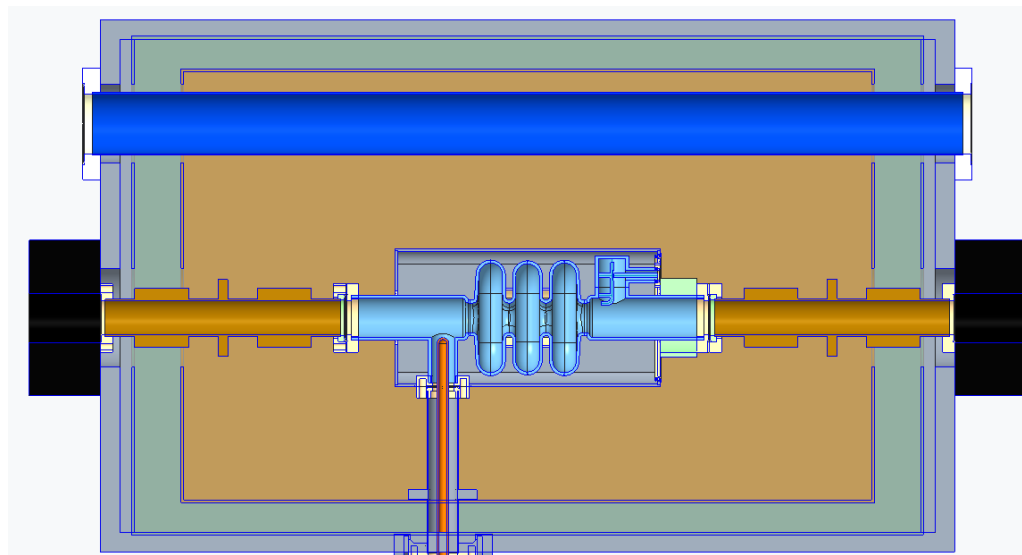
Could try to squeeze down to 950 mm to have 4 individual cryomodules in the 3.8 m installation length.

Outer Vacuum Chamber
Warm Magnetic Shield

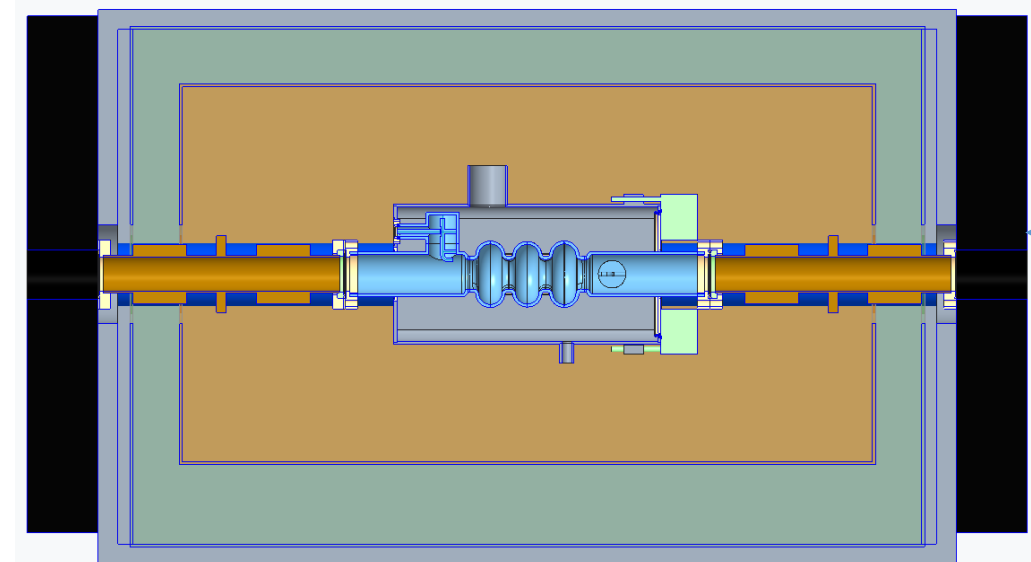
Thermal Screen

Total Length: 1014 mm

Total Length: 1014 mm



Top View



DN40 Gate Valve

Side View

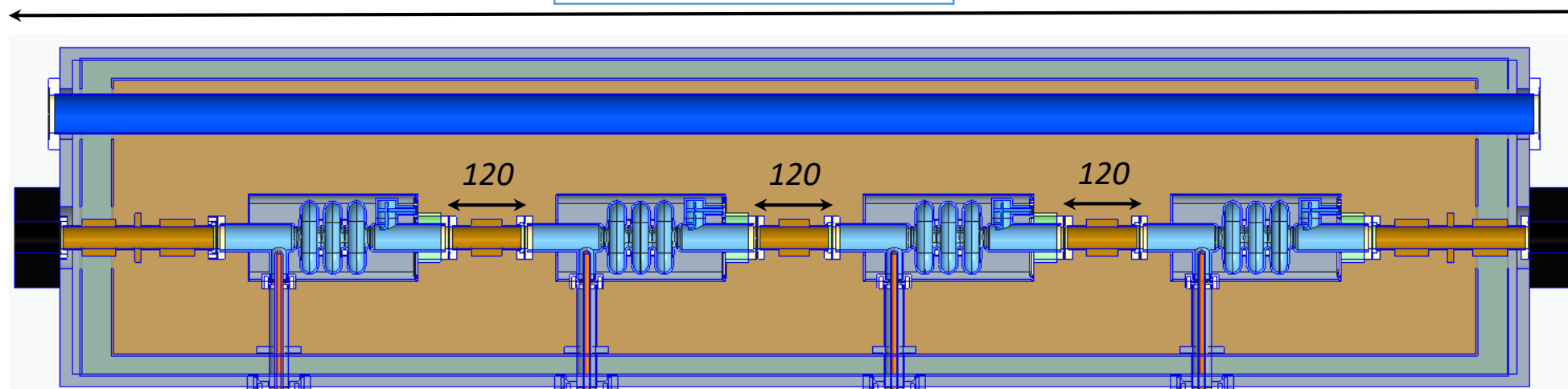
4 Cavity Cryomodule Schematic

Total Length: 2520 mm

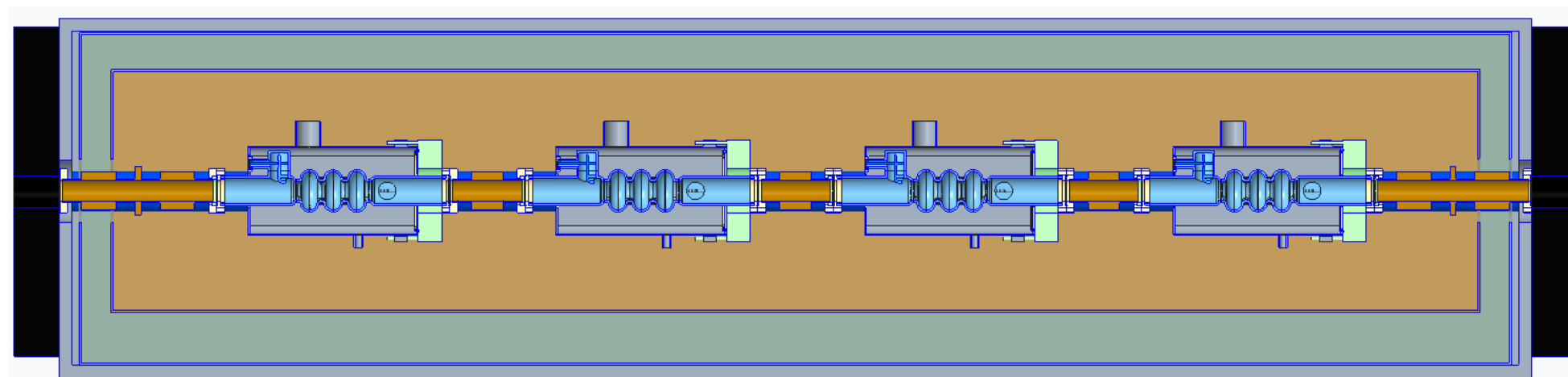
Outer Vacuum Chamber

Warm Magnetic Shield

Thermal Screen



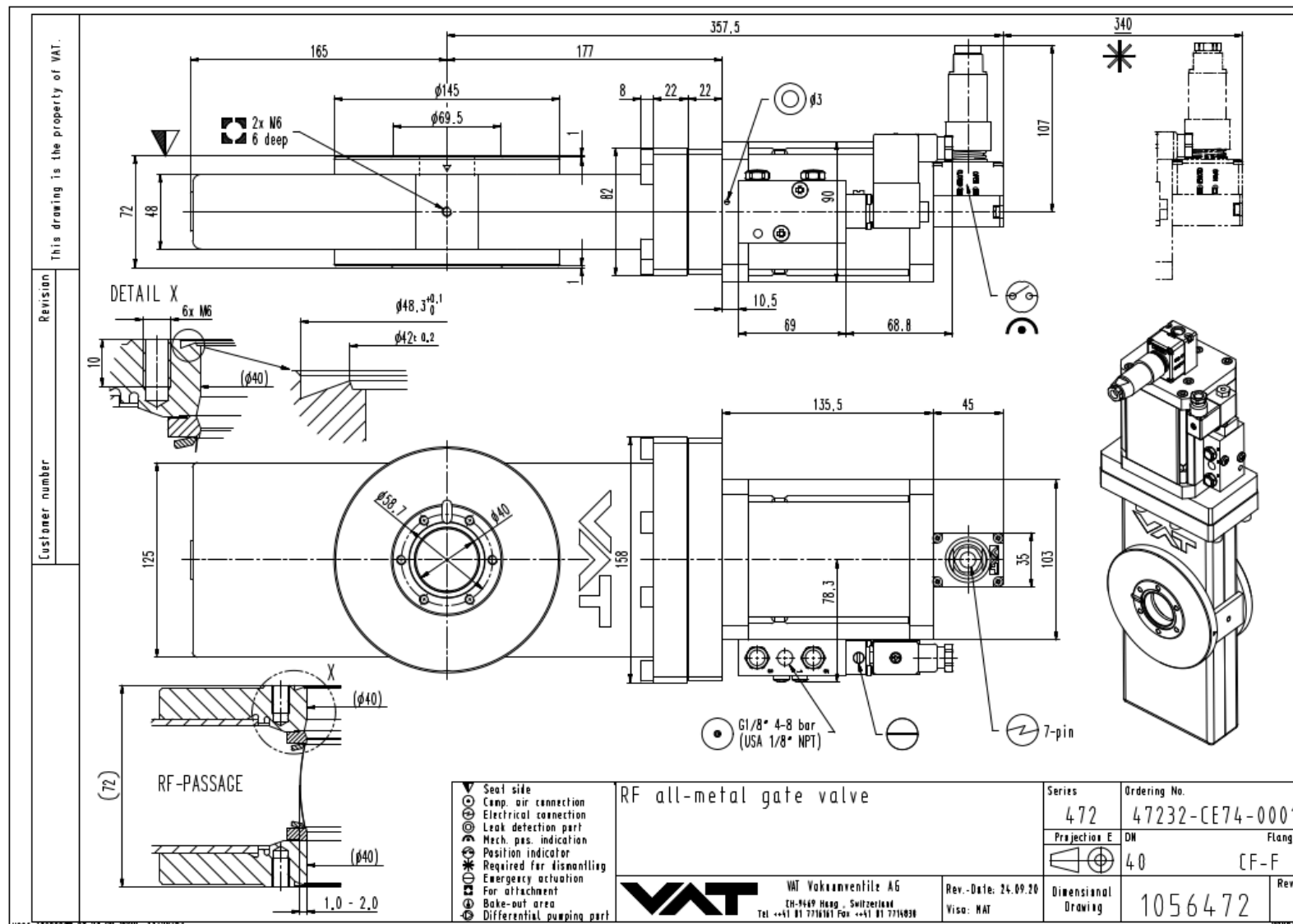
Top View



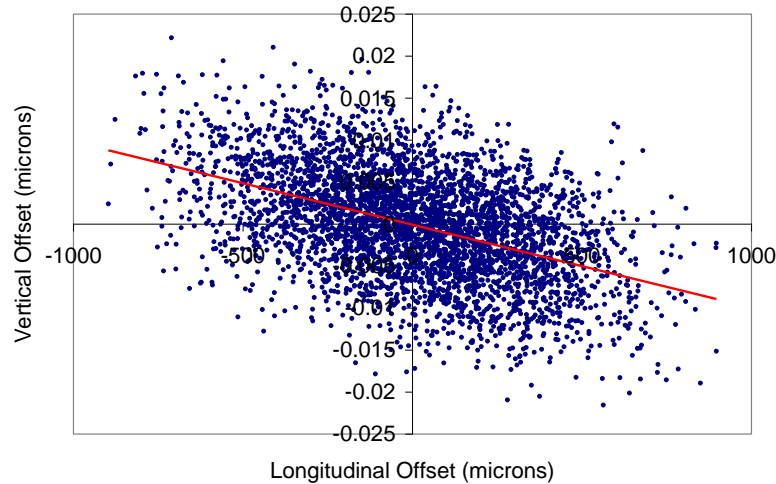
DN40 Gate Valve

Side View

DN40 Gate Valves – 523 x 125 x 72



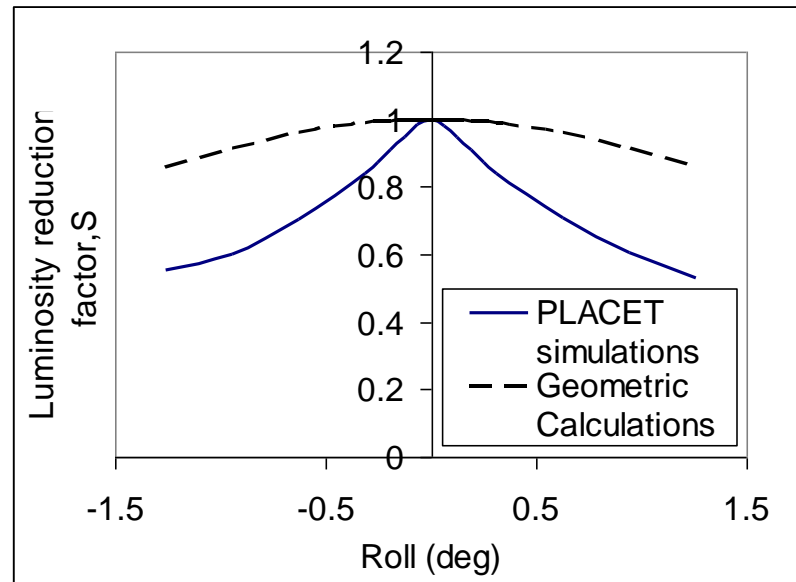
Cavity Alignment (Anti-crabbing)



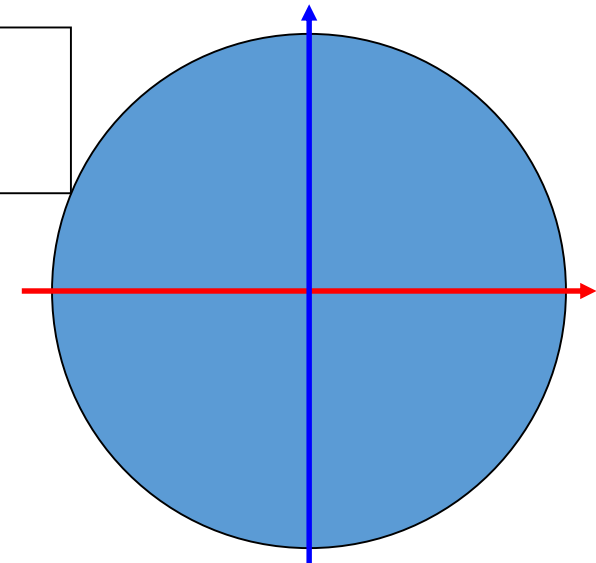
If the cavity has a roll misalignment it will cause a small crossing angle in the vertical plane.

This will significantly reduce the luminosity

Crab Cavity Effect
Anti-Crab Effect



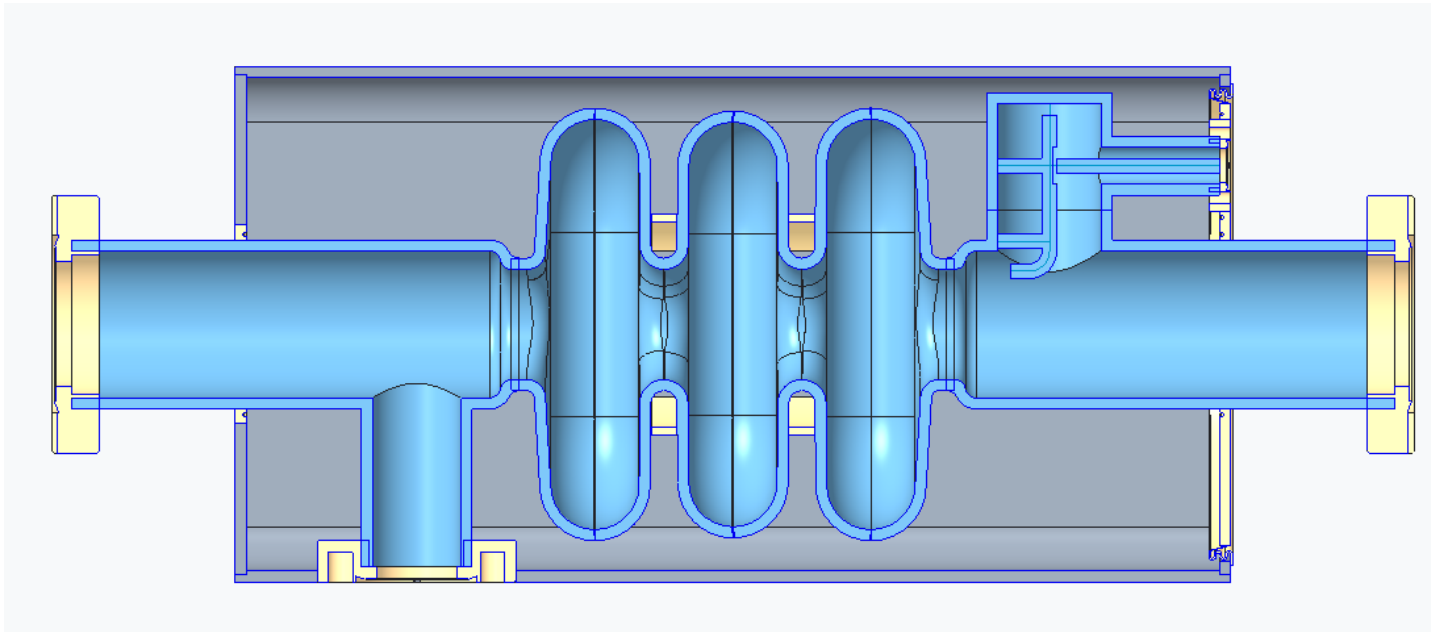
Either need active alignment or space for an extra cavity!



Adding a single cell crab cavity in the vertical (rather than horizontal) plane can correct for vertical crabbing and offsets due to cavity misalignment, wakefields or other sources of error such as x-y coupling.

Volume within Helium Tank

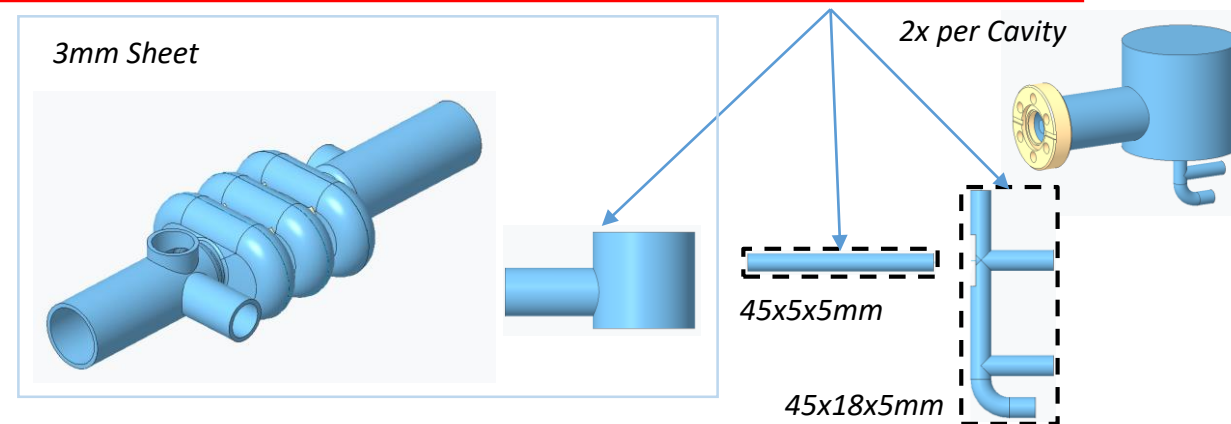
- Helium Tank: 5036080mm³
- Total Volume: $5036080 - 790119.5 = \underline{4245960.5\text{mm}^3} \rightarrow 4.25 \text{ litres}$
- PED Category I



Niobium Bill Of Materials

Bare Cavities & HOM Housing	Nb RRR 400 - Sheet				Nb RRR 400 - Billet			
	t (mm)	w (mm)	l (mm)	(kg)	t (mm)	w (mm)	l (mm)	(kg)
1	3	200	550	2.8	5	45	46	0.1
4	3	200	2200	11.2	5	45	184	0.4

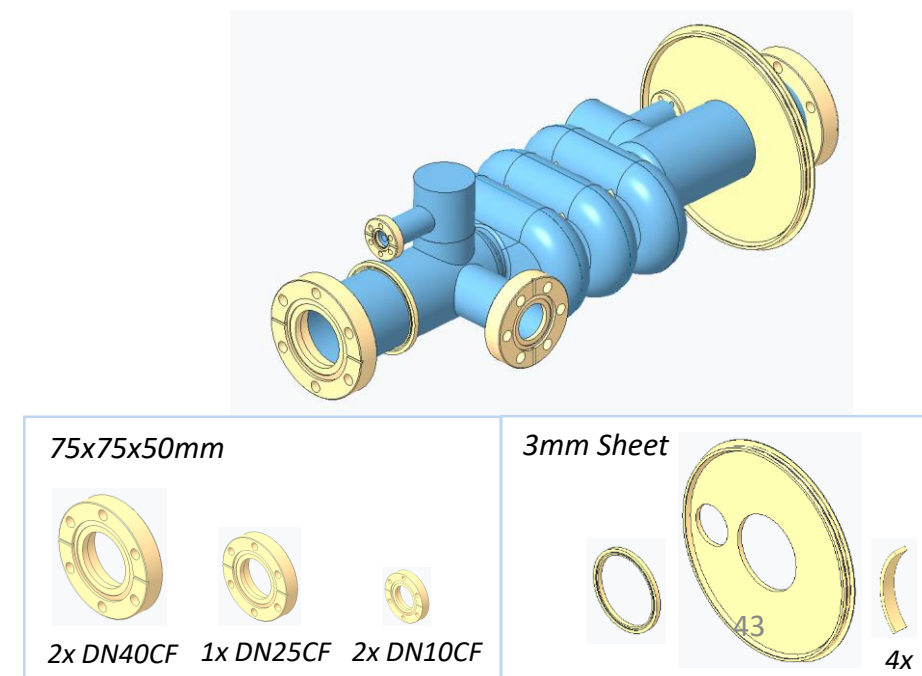
Includes ~10% waste material



NbTi Bill Of Materials

Flanges, Stiffening Rings & Bellows	Nb55Ti - Sheet				Nb55Ti - Billet			
	t (mm)	w (mm)	l (mm)	(kg)	t (mm)	w (mm)	l (mm)	(kg)
1	3	150	300	0.8	50	75	75	1.6
4	3	150	1200	3.2	50	75	300	6.4

Includes ~10% waste material



Comparison to specification

Parameter	Elliptical/Racetrack	Flange-flange Cavity Length	370
Operating frequency	3.9	Number of cells	3
SOM	5	Cavity Diameter (RF model ID largest transverse horizontal dimension closest to 2nd beam-pipe)	111.4
1 st Longitudinal HOM	3.3	Minimum Aperture	25
1 st Transverse HOM	4.7	FPC Q_L	1.0×10^7
E_p/E_t^*	4.24	Loaded Bandwidth	390
B_p/E_t^*	12.6	Cavity Input Power	0.22
B_p/E_p (including ports)	2.96	Longitudinal Loss Factor k_z	3.2
G	207	Horizontal Kick Factor k_x	16
R/Q (accelerator definition per cavity)	140	Vertical Kick Factor k_y	16
$R_t R_s$	2.9×10^4	Stored Energy W (at V_t operational)	0.1
V_t max per cavity	0.716	HOM impedance (Longitudinal)	230
V_t operational per cavity (125 GeV)	0.615	HOM impedance (Transverse) H	1.3
E_p operational	22.5	HOM impedance (Transverse) V	1.4
B_p operational	66.6	First 3 multipole parameters	1, 0.1, 250
Total No. of cavities (125 GeV beam)	1	Nb material quantity (Kg) per cavity prototype	2.9
Extendability (500 GeV beam)	Use 4 cavities	Nb material sheet/ingot	Sheet for main body, billet for HOM couplers
V_t max/ V_t operational	1.16	Maximum stresses, max pressure at RT (weakest)?	5.4

Conclusions

- Using a racetrack geometry gives improved separation to the same-order mode and minimizes the peak magnetic fields
- A 3 cell cavity with coax HOM dampers meets the ILC impedance specification
- There is a small amount of multipactor in the endcell at the operating gradient but, it appears possible to move this to higher voltages
- The cavity is small and a lower voltage is needed at 3.9 GHz making the cryomodule significantly cheaper and easier